#### CS 450

# Lecture 7: The Environment Model

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#### 1 Environments

An environment is a tree of environment frames.

A frame is

- a (pasists in a proper partie and proper sociate traves (17) bir tiles, travel with
- a pointer to its parent in the tree of environment frames. This parent is called the *enclosing environment*. Of course there is one exception: the root frame, which is also called the *global environment* in the course there is one exception: the root frame, which is also called the *global environment* in the course there is one exception: the root frame, which is also called the *global environment* in the course there is one exception: the root frame, which is also called the *global environment* in the course there is one exception:

At each point during execution of a program, we have a  $\it current environment$ . This is one of the frames in the tree. Add WeChat powcoder

# 2 Evaluating a variable

The value of a variable is found by starting with the current environment and walking up the tree until the variable is found. Figure 1 shows how this works.

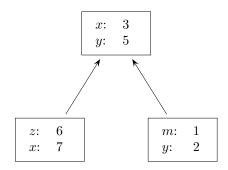


Figure 1: x may have the value 7 or 3, depending on the current environment; similarly for y.

#### 3 Evaluating a lambda expression

To evaluate a lambda expression, create a procedure object consisting of

- the text of the procedure. This in turn consists of
  - the formal parameters of the procedure, and
  - the body of the procedure.

It is important to remember that this is just copied textually—nothing in the text of the procedure is evaluated at this point.

a pointer (or more accurately, a reference) to the environment in which the lambda expression
was evaluated.

This procedure object is what the lambda expression evaluates to.

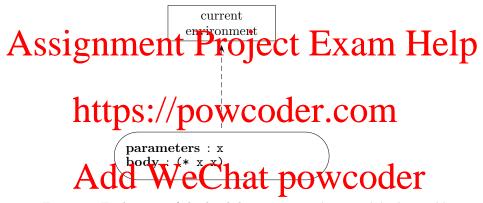


Figure 2: Evaluation of the lambda expression (lambda(x) (\* x x))

## 4 Evaluating a (user-defined) procedure call

To evaluate a procedure call (where the procedure is user-defined, and hence evaluates to a procedure object),

- 1. Evaluate the first expression in the list. This is the procedure itself, and so it evaluates to a procedure object, as above.
- 2. Evaluate the rest of the expressions of the list—these are the actual arguments to the procedure—in the current environment.
- 3. Construct a new frame containing the bindings of the formal parameters of the procedure to the corresponding values just produced in step 2.
  - The enclosing environment of this frame is the environment part of the procedure object produced in step 1.
- 4. Evaluate the body of the procedure in this new environment.

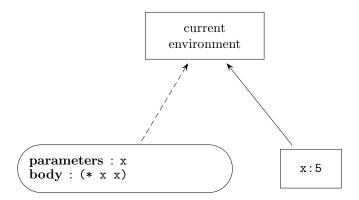


Figure 3: Applying a lambda expression: ((lambda(x) (\* x x)) 5).

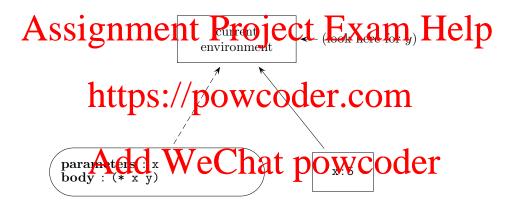


Figure 4: Applying a lambda expression (a second example): ((lambda(x) (\* x y)) 5).

Note the convention I am using for these pictures:

Frames are represented by rectangles. Frames are the *only* nodes in the environment tree.

The parent-child relation between frames is represented by a solid arrow.

**Procedure objects are represented by ovals.** This is to emphasize that procedure objects are *not* nodes in the environment tree. Each procedure object, however, does point to a node (i.e., a frame) in the environment tree. This frame is called the "environment of the procedure object". It is *not*, however, the "parent" of the procedure object, since the procedure object is not a node in the tree. For this reason,

The arrow from a procedure object to its environment frame is dotted. This is to reinforce the fact that the arrow does not represent a parent-child relation.

### 5 Evaluating define and set!

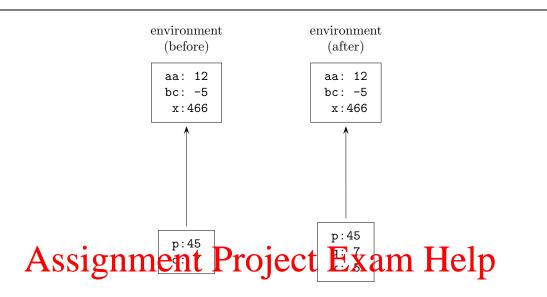


Figure 5: To evaluate (define x <exp>), evaluate <exp>, and add a binding for x to the value of <exp> to the current frame. Thus, (define x 5) adds a binding to the current frame.

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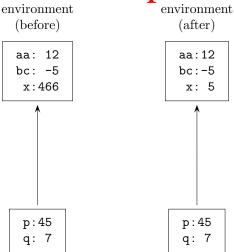


Figure 6: To evaluate (set! x < exp>), evaluate < exp>, search up in the environment for x, and change the value bound to x. Thus, (set! x 5) changes the binding of x in the first frame in which x is found.

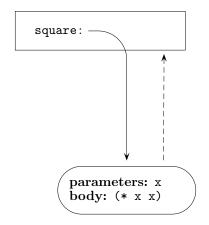


Figure 7:

(define (square x) (\* x x))

which is the same as

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#### 6 Some larger examples

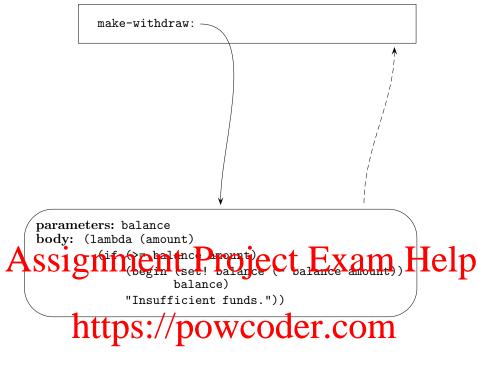


Figure 8: Definition of make-withdraw. If we then (define W1 (make-withdraw 100)), we get Figure 9.

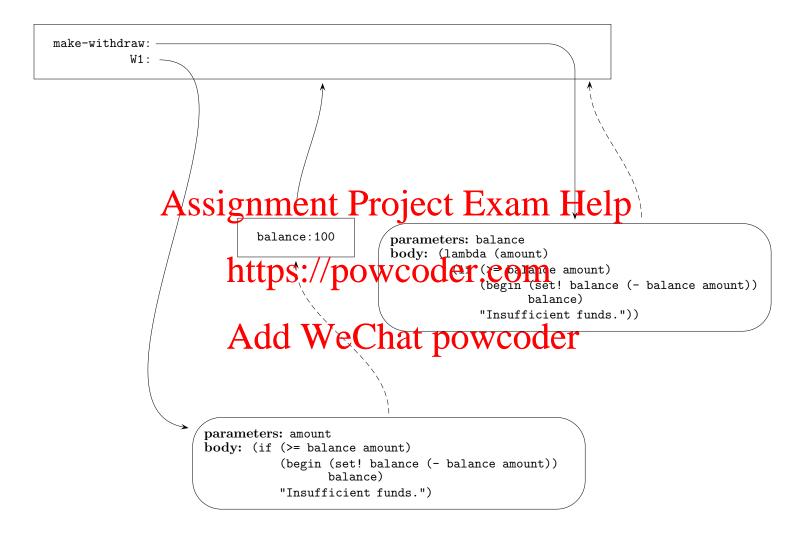
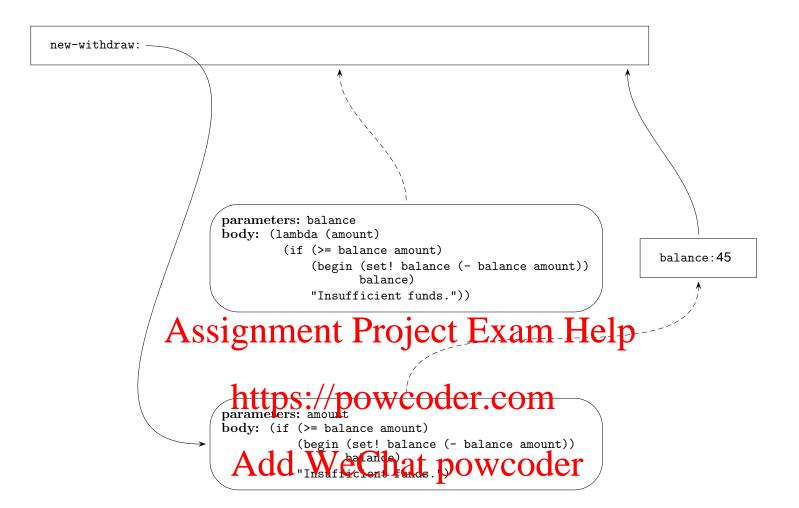


Figure 9: Evaluation of (define W1 (make-withdraw 100))



```
(define new-withdraw
  (let ((balance 100))
    (lambda (amount)
      (if (>= balance amount)
           (begin (set! balance (- balance amount))
                  balance)
          "Insufficient funds."))))
This is immediately turned internally into
(define new-withdraw
  ((lambda (balance)
     (lambda (amount)
       (if (>= balance amount)
           (begin (set! balance (- balance amount))
                   balance)
           "Insufficient funds.")))
   100)
)
```

Figure 10: new-withdraw

```
sqrt: -
parameters: x
body: (define good-enough?
         (lambda (guess)
           (< (abs (- (square guess) x)) 0.001)))</pre>
       (define improve
         (lambda (guess)
           (average guess (/ x guess))))
       (define sqrt-iter
        (lambda (guess)
           (if (good-enough? guess)
              guess
               (sqrt-iter (improve guess)))))
       (sqrt-iter 1.0)
                               x:2
                                         Project Exam Help
                       sqrt-iter: -
                                      owcoder.com
  parameters: guess
                                                                          guess:1
  body: (if (good-enough? guess)
             (sqrt-iter
                        (improve guess))
                     parameters: guess
                                                                                    guess:1
                     body: (average guess (/ x guess))))
                                                                               call to good-enough?
                                parameters: guess
                                body: (< (abs (- (square guess) x)) 0.001)))
      (define sqrt
        (lambda (x)
          (define (good-enough? guess)
            (< (abs (- (square guess) x)) 0.001))</pre>
          (define improve
            (lambda (guess)
              (average guess (/ x guess))))
          (define sqrt-iter
            (lambda (guess)
              (if (good-enough? guess)
                  (sqrt-iter (improve guess)))))
          (sqrt-iter 1.0)))
```

Figure 11: Evaluating (sqrt 2). Only the first few steps of the computation are shown.