# Assignment Project Exam Help SUBSET-SUM https://powcoder.com

#### SUBSET-SUM

• Recall, the subset-sum problem is the following language:

$$\{\langle S,t\rangle : S=\{x_1,\dots, \text{assignment-Breject, Examp } \text{ Help},\dots,x_n\}, \sum_{i=1}^n y_i=t\}$$
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- Inputs: an integer value (taket) Wardhare polyintegers  $a_1, \dots, a_n$
- Output: YES if there is a subset that adds up to t, NO otherwise

### SUBSET-SUM is in NP

• Proof: Sipser Theorem 7.25

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### SUBSET-SUM is in NPc

• Proof: Sipser Theorem 7.56

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• We show that  $3SAT \leq_{p} SUBSET-SUM$ https://powcoder.com

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• How?

• Given a 3CNF formula  $\emptyset$ , we want (within polytime in the length of  $\emptyset$ ) to create(build) an instance of SUBSET-SUM (dependent on  $\emptyset$ ):  $\langle S_{\emptyset}, t_{\emptyset} \rangle$  such that  $\emptyset$  is satisfiable iff  $S_{\emptyset}$  has a subset that adds up to  $t_{\emptyset}$ .

# From $\emptyset$ to $\langle S_{\emptyset}, t_{\emptyset} \rangle$

• Suppose it has variables  $x_1, \dots, x_l$  and clauses  $c_1, \dots, c_k$ 

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- $t_{\emptyset} = \underbrace{11 \dots 1}_{l} \underbrace{33 \dots 3}_{k}$  (decimal number) https://powcoder.com
- Example: If l=1 and  $k_{A}$  and  $k_{A}$  then  $t_{\emptyset}$  is thirties in

If 
$$\emptyset = (x_1 \lor \neg x_2 \lor \neg x_3) \land (x_3 \lor \neg x_4 \lor x_5)$$
, then  $t_\emptyset = 1111133$ 

$$S_{\emptyset} = ??$$

(1) If  $x_i$  is a variable in the formula  $\emptyset$  and the literal  $x_i$  appears in the clauses  $c_{j_1},...,c_{j_r}$ , then include in  $S_\emptyset$  the number  $Y_i=$ :

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Where in red, the 1's are in the positions  $j_1, \dots, j_r$ Add WeChat powcoder

- (2) Do the exact same for the literal  $\neg x_i$ . Call the resulting number  $Z_i$
- (3) For each clause  $c_j$ , include  $D_i = 1 \underbrace{00 \dots 0}_{k-j}$  and  $H_i = 2 \underbrace{00 \dots 0}_{k-j}$

## This construction works

- (1) If  $\emptyset$  is satisfiable, we can find a subset T of  $S_\emptyset$  such that the sum of the elements in T equals  $t_\emptyset$ Assignment Project Exam Help
- (2) Conversely, if we can find a subset f of  $S_{\emptyset}^{m}$  such that the sum of the elements in T equals  $t_{\emptyset}$ , Atherwais  $t_{\emptyset}$  is satisfiable at

# (1)

- Suppose that  $\emptyset$  is satisfiable (by some assignment); here we build T
- If  $x_i$  is assigned TRUE, in Also Legitarine of the Project Exam Help
- If  $x_i$  is assigned FALSE, includettps://powcoder.com
- With the elements included so far, the sum of the elements in T should be something like  $\underbrace{11\dots1}_{l}\underbrace{23\dots1\dots3}_{k}$

(the last k digits are made from 1,2,3)

• If needed, include in T from  $D_i$  and  $H_i$  what brings up the sum to  $\underbrace{11...1}_{l}\underbrace{33...3}_{k}$ 

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(2)

- Suppose we can find a subset T of  $S_\emptyset$  such that the sum of the elements in T equals  $t_\emptyset$  Assignment Project Exam Help
- We build an assignment which satisfies on Add WeChat powcoder
- If T contains  $Y_i$ , then assign  $x_i$  to TRUE
- If T contains  $Z_i$ , then assign  $x_i$  to FALSE

# (2) Clarified

- Note that all we know about T here is that it is a collection of  $Y_i$  's,  $Z_j$ 's,  $D_m$ 's, and  $H_n$  's Assignment Project Exam Help
- They all add up to 11 ..https://powcoder.com

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- The 1's at the beginning imply that for each variable  $x_i$ , exactly one of  $Y_i$  or  $Z_i$  is in T
- These  $Y_i$  's (or  $Z_i$ 's) contribute at least a 1 to each 3

# Assignment Project Exam Help Related Problems https://powcoder.com

### **PARTITION**

 PARTITION = {S : S finite subset of Z that can be split into two sets which sum to equal values} Assignment Project Exam Help

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• SUBSET-SUM  $\leq_p$  PARTITAON We Chat powcoder

So, PARTITION is NP-complete

## KNAPSACK

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