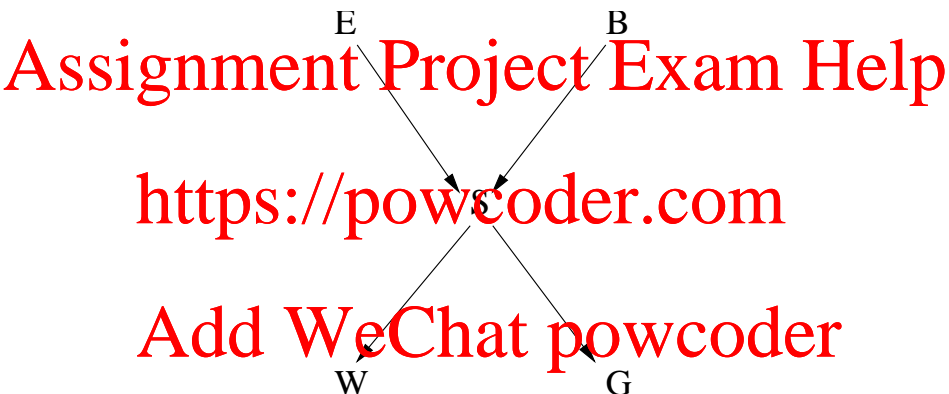


Assignment Project Exam Help

Tutorial Examples Uncertainty

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November 27, 2020
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$$P(E, S, B, W, G) = P(E)P(B)P(S|E, B)P(W|S)P(G|S)$$

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$P(E)$	e	$-e$	$P(B)$	b	$-b$
	1/10	9/10		1/10	9/10

$P(S E,B)$	s	$-s$	$P(W S)$	w	$-w$
$e \wedge b$	9/10	1/10	s	8/10	2/10
$e \wedge -b$	2/10	8/10	$-s$	2/10	8/10
$-e \wedge b$	8/10	2/10			
$-e \wedge -b$	0	1			

$P(G S)$	g	$-g$
s	1/2	1/2
$-s$	0	1

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- ▶ Given the alarm went off (s) what is the probability that Mrs. Gibbons phones you (g)?

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- ▶ Given the alarm went off (s) what is the probability that Mrs. Gibbons phones you (g)? probability that the alarm went off (s)?

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$$P(g|s) = 1/2$$

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- ▶ Given that Mrs. Gibbons phones you (g) what is the probability the alarm went off (s)?

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Given that Mr. Gibbons phones you (g) what is the probability the alarm went off (s)?

1. Bayes Rule says: $P(S|g) = P(g|S) * P(S) / P(g)$
2. $P(-s|g) = P(g|-s) * P(-s) / P(g) = 0$.
3. Therefore $P(s|g) = 1$ ($P(s|g) + P(-s|g)$ must sum to 1).

$P(s|g) = 1$ $P(-s|g) = 0$
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Alternatively: $-s \rightarrow -g$, so $g \rightarrow s$, so $P(s|g) = 1$.

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- Say that there was a burglary (b) and but no earthquake (-e), what is the expression specifying the posterior probability of Dr. Watson phoning you (w) given the evidence. (You do not need to calculate a numeric answer, just give the probability expression).

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- ▶ Say that there was a burglary (b) and but no earthquake (-e), what is the expression specifying the posterior probability of Dr. Watson phoning you (w) given the evidence. (You do not need to calculate a numeric answer, just give the probability expression).

$P(w|b, -e)$
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- ▶ What is $P(G|S)$? (i.e., the four probability values) $P(g|s)$, $P(-g|s)$, $P(g|-s)$, $P(-g|-s)$.

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Assignment Project Exam Help

- ▶ What is $P(G|S)$? (i.e., the four probability values $P(g|s)$, $P(-g|s)$, $P(g|-s)$, $P(-g|-s)$).

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$$P(g|s) = 1/2 \quad P(-g|s) = 1/2 \\ P(g|-s) = 0 \quad P(-g|-s) = 1$$

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- ▶ What is $P(G|S \wedge W)$? (i.e., the 8 probability values $P(g|s \wedge w)$, $P(g|s \wedge \neg w)$, ..., $P(\neg g|s \wedge \neg w)$).

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- ▶ What is $P(G|S \wedge W)$? (i.e., the 8 probability values $P(g|s \wedge w), P(g|s \wedge -w), \dots, P(-g| -s \wedge -w)$).

$$P(g|s, -w) = P(g|s, w) = P(g|s) = 1/2$$

$$P(-g|s, -w) = P(-g|s, w) = P(-g|s) = 1/2$$

$$P(g| -s, -w) = P(g| -s, w) = P(g| -s) = 0$$

$$P(-g| -s, -w) = P(-g| -s, w) = P(-g| -s) = 1$$

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- ▶ What do these values tell us about the relationship between G , W and S ?

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G is conditionally independent of W given S

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- ▶ What is $P(G|W)$? (i.e., the four probability values $P(g|w)$, $P(-g|w)$, $P(g|-w)$, and $P(-g|-w)$).

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- ▶ What is $P(G|W)$? (i.e., the four probability values $P(g|w)$, $P(\neg g|w)$, $P(g|\neg w)$, and $P(\neg g|\neg w)$)

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Must do variable elimination.

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- ▶ What is $P(G|W)$? (i.e., the four probability values $P(g|w)$, $P(-g|w)$, $P(g|-w)$, and $P(-g|-w)$).

- ▶ Query variable is G .
- ▶ First run of VE, evidence is $W = w$.
- ▶ Second run of VE, evidence is $W = -w$.
- ▶ Use same ordering for both runs of VE: E, B, S, G .
- ▶ With same ordering some factors can be reused between the two runs of VE.

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- ▶ What is $P(G|W)$? (i.e., the four probability values $P(g|w)$, $P(-g|w)$, $P(g|-w)$, and $P(-g|-w)$).

1. $E: P(E), P(S|E, B)$

2. $B: P(B),$

3. $S: P(w|S), P(S|G)$

4. $G:$
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Inference in Bayes Nets

- ▶ What is $P(G|W)$? (i.e., the four probability values $P(g|w)$, $P(-g|w)$, $P(g|-w)$, and $P(-g|-w)$).

1. E : $P(E)$, $P(S|E, B)$

2. B : $P(B)$

3. S : $P(w|S)$, $P(S|G)$

4. G :

$$\begin{aligned} F_1(s, B) &= \sum_{E \in \{e, -e\}} P(E) \times P(S|E, B) \\ &= P(e) \times P(S|e, B) + P(-e) \times P(S|-e, B) \end{aligned}$$

$$\begin{aligned} F_1(-s, -b) &= P(e)P(-s, e, -b) + P(-e)P(-s, -e, -b) \\ &= 0.1 \times 0.8 + 0.9 \times 1 = 0.98 \end{aligned}$$

$$\begin{aligned} F_1(-s, b) &= P(e)P(-s, e, b) + P(-e)P(-s, -e, b) \\ &= 0.1 \times 0.1 + 0.9 \times 0.2 = 0.19 \end{aligned}$$

$$\begin{aligned} F_1(s, -b) &= P(e)P(s, e, -b) + P(-e)P(s, -e, -b) \\ &= 0.1 \times 0.2 + 0.9 \times 0 = 0.02 \end{aligned}$$

$$\begin{aligned} F_1(s, b) &= P(e)P(s, e, b) + P(-e)P(s, -e, b) \\ &= 0.1 \times 0.9 + 0.9 \times 0.8 = 0.81 \end{aligned}$$

1. E : $P(E), P(S|E, B)$

2. B : $P(B), P(S|B)$

3. S : $P(w|S), P(S|G)$

4. G :

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$$\begin{aligned} F_2(S) &= \sum_B P(B) \times F_1(S, B) \\ &= P(b)F_1(S, b) + P(-b)F_1(S, -b) \end{aligned}$$

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$$\begin{aligned} F_2(-s) &= P(b)F_1(-s, b) + P(-b)F_1(-s, -b) \\ &= 0.1 \times 0.19 + 0.9 \times 0.98 = 0.901 \\ F_2(s) &= P(b)F_1(s, b) + P(-b)F_1(s, -b) \\ &= 0.1 \times 0.81 + 0.9 \times 0.02 = 0.099 \end{aligned}$$

Inference in Bayes Nets

1. $E: P(E), P(S|E, B)$

2. $B: P(B), F_1(S, B)$

3. $S: P(w|s), P(s|g), F_2(s)$

4. $G:$

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$$\begin{aligned} F_3(G) &= \sum_S P(w|S) \times P(S|G) \times F_2(S) \\ &= P(w|s)P(s|G)F_2(s) + P(w|-s)P(-s|G)F_2(-s) \end{aligned}$$

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$$\begin{aligned} F_3(-g) &= P(w|s)P(s|-g)F_2(s) + P(w|-s)P(-s|-g)F_2(-s) \\ &= 0.8 \times 0.5 \times 0.099 + 0.2 \times 1 \times 0.901 = 0.2198 \end{aligned}$$

$$\begin{aligned} F_3(g) &= P(w|s)P(s|g)F_2(s) + P(w|-s)P(-s|g)F_2(-s) \\ &= 0.8 \times 0.5 \times 0.099 + 0.2 \times 0 \times 0.901 = 0.0396 \end{aligned}$$

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1. $E: P(E), P(S|E, B)$

2. $B: P(B), F_1(S, B)$

3. $S: P(w|S), P(S|G), F_2(S)$

4. $G: F_3(G)$

Normalize $F_3(G)$:

$$\frac{P(-g|w)}{P(g|w)} = \frac{0.2198}{0.2198+0.0396} = 0.8473$$
$$\frac{0.0396}{0.2198+0.0396} = 0.1527$$

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► Now $P(G|-w)$?

1. E : $P(E), P(S|E, B)$

2. B : $P(B)$

3. S : $P(-w|S), P(S|G)$

4. G :

Already computed as $F_1(S, B)$

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1. E : $P(E), P(S|E, B)$

2. B : $P(B), F_1(S, B)$

3. S : $P(-w|S), P(S|G)$

4. G :

Already computed as $F_2(S)$

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Inference in Bayes Nets

1. $E: P(E), P(S|E, B)$

2. $B: P(B), F_1(S, B)$

3. $S: P(A|w, s), P(s|G), F_2(s)$

4. $G:$

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$$\begin{aligned} F_3(G) &= \sum_S P(-w|S) \times P(S|G) \times F_2(S) \\ &= P(-w|s)P(s|G)F_2(s) + P(-w|-s)P(-s|G)F_2(-s) \end{aligned}$$

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$$\begin{aligned} F_3(-g) &= P(-w|s)P(s|-g)F_2(s) + P(-w|-s)P(-s|-g)F_2(-s) \\ &= 0.2 \times 0.5 \times 0.099 + 0.8 \times 1 \times 0.901 = 0.7307 \end{aligned}$$

$$\begin{aligned} F_3(g) &= P(-w|s)P(s|g)F_2(s) + P(-w|-s)P(-s|g)F_2(-s) \\ &= 0.2 \times 0.5 \times 0.099 + 0.8 \times 0 \times 0.901 = 0.0099 \end{aligned}$$

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1. $E: P(E), P(S|E, B)$

2. $B: P(B), F_1(S, B)$

3. $S: P(-w|S), P(S|G), F_2(S)$

4. $G: F_3(G)$

Normalize $F_3(G)$:

$$\frac{P(-g|-w)}{P(g|-w)} = \frac{\frac{0.7307}{0.7307+0.0099}}{\frac{0.0099}{0.2198+0.00099}} = \frac{0.9866}{0.0134}$$

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- ▶ What do these values tell us about the relationship between G and W and why does this relationship differ when we know S ?

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Assignment Project Exam Help

- ▶ What do these values tell us about the relationship between G and W , and why does this relationship differ when we know S ?

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G and W are not independent of each other. But when S is known they become independent.

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