Sample Questions For Term Test 2 Covers Backtracking Search and Uncertainty

November 26, 2020

1. A latin square of size m is an $m \times m$ matrix containing the numbers 1-m such that no number occurs more than once in any row or column. For example

1 2 3 4

4 1 2 3

3 4 1 2

2 3 4 1

is a latin square essize 4. Specify this the problem of finding a latin square of size m as a CSP. That is, give the variables, the variable domains, and the constraints for a CSP representing this problem.

2. Consider the N-Queens problem. That is, the problem of placing N Queens on an $N \times N$ chess-board so that no two Queens can attack each other.

Find the first solution to the 5 Queens problem by using the Farward Checking algorithm using Minimum Remaining Values Heuristic (always instantiate next the variable with smallest remaining number of elements in its current domain). Also breaking ties in favour of the lowest numbered variable.

(Note, use the same CSP formulation as that used in class. That is, we have 5 variables, Q_1, \ldots, Q_5 each with domain [1, 2, 3, 4, 5]. Each variable Q_i represents the queen in the *i*-th row, and the assignment $Q_i = j$ means that the queen in the *i*-th row has been placed in the *j*-th column.

Draw the search tree explored by this algorithm. At each node indicate

- (a) The variable being instantiated, and the value it is being assigned.
- (b) A list of the variables that have had at least one of their values pruned by the new assignment, and for such variable a list of its remaining legal values. Note, you must follow the forward checking algorithm precisely: only prune values that would be pruned by the algorithm.
- (c) Mark any node where a deadend occurs because of a domain wipe out (use the symbol DWO).

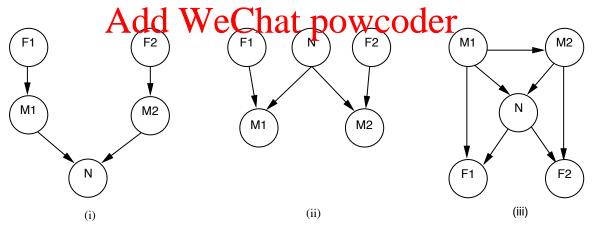
- 3. Repeat the same problem of 5-Queens but this time use GAC. This time show the initial domains after GAC Enforce is run at the root, then show the search tree as before, specifying the variable branched on and the value assigned, list of variables pruned by GAC Enforce by that decision, and the list of remaining values for the pruned variables.
- 4. Say we have 4 variables X, Y, Z, and W, with the following domains of values:
 - (a) $Dom[X] = \{1, 2, 3, 4\}$
 - (b) $Dom[Y] = \{1, 2, 3, 4\}$
 - (c) $Dom[Z] = \{1, 2, 3, 4\}$
 - (d) $Dom[W] = \{1, 2, 3, 4, 5\}$

And 3 constraints:

- (a) $C_1(X, Y, Z)$ which is satisfied only when X = Y + Z
- (b) $C_2(X, W)$ which is satisfied only when W > X
- (c) $C_3(X, Y, Z, W)$ which is satisfied only when W = X + Z + Y

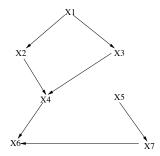
Enforce GAC on these constraints, and give the resultant GAC consistent variable domains.

5. Two ashorogers indiffered parts of the workshape measurements M and M of the number of stars N in some small region of the sky, using their telescopes. Normally, there is a small probability e or error of up to one star in each direction. Each telescope can also be badly out of focus with probability f. Let F_1 and F_2 be boolean variables with $F_i = \mathbf{true}$ being that the i-th telescope \mathbf{true} of \mathbf{foc} whice \mathbf{true} is \mathbf{true} of \mathbf{true} of \mathbf{true} and \mathbf{true} of $\mathbf{tr$

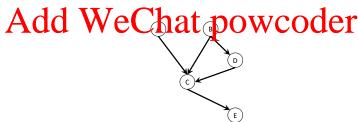


- (a) Which of these Bayesian Networks can correctly representation the preceding information? (Note that additional edges in a network do not make the network incorrect, they only make the network redundant). **Note this question was done in tutorial**
- (b) Which is the best network? Explain. Note this question was done in tutorial
- (c) Write out the CPT for $Pr(M_1|N, F_1)$ for the case where $M_1 \in \{0, 1, 2, 3, 4\}$ and $N \in \{1, 2, 3\}$. Express the entries in terms of e and f.

- (d) Use your CPT for $Pr(M_1|N, F_1)$ to compute the CPT for $Pr(M_1|N)$ (again expressed in terms of e and f). Hint, use summing out rule for conditional probabilities and knowledge of independencies in this domain.
- (e) Suppose $M_1 = 1$ and $M_2 = 3$. What are the *possible* numbers of stars.
- 6. Consider the Bayes Network given below.



- (a) What is the product decomposition specified by this network?
- (b) Say that variable X_7 has 3 possible values, X_6 has 2 possible values, and X_4 has 4 possible values. How many values will be contained in the conditional probability table for XSS1gnment Project Exam Help
- (c) Are X_1 and X_5 conditionally independent given X_2 , given X_7 , given X_6 , given X_4 ?
- (d) What are the relevant variables given the query X_3 and the evidence items X_6 , given evidence X_1 , every School X_6 , given evidence X_6 , $X_$
- 7. Consider the Bayes Net given below.

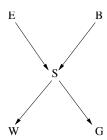


- (a) Which of the following statements are asserted by this Bayes net.
 - i. P(A, D) = P(A)P(D)
 - ii. P(E|C,D) = P(E|C,D,B)
 - iii. P(E|D,B) = P(E|D)
 - iv. P(C|A, B) = P(C|A, B, D)
- (b) Say we want to use variable elimination to compute the probability of P(E) given no evidence, what would be the elimination width of the following orderings. (The variables are to be eliminated in the order listed).
 - i. A, B, C, D, E.
 - ii. C, A, B, D, E.

iii. B, D, C, A, E.

iv. E, B, A, D, C.

- (c) List the pairs of variables that are conditionally independent in this network given.
 - i. No evidence
 - ii. Given C
 - iii. Given D.
- 8. Consider the Bayes net given below.



In this network all variables are binary with values true and false. E represents the occurrence of an Fatter are property of a large part of the control of the control of the control of the property of a large part of the control of the control

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E	e	-е	В	b	-b	S		s	-s	W	w	-w
	1/10	9/10		1/10	9/10	e∧b		9/10	1/10	s	8/10	2/10
				eΛ	-b	2/10	8/10	-s	2/10	8/10		
						-e /	\ b	8/10	2/10			
						-e ∧ -b		0	1			
					G	g -g						
					s	1/2	1/2					
					-s	0	1					

- (a) Given that Mrs. Gibbons phones you (g) what is the probability that the alarm went off (s)?
- (b) Say that there was a burglary (b) and but no earthquake (-e), what is the expression specifying the posterior probability of Dr. Watson phoning you (w) given the evidence. (You do not need to calculate a numeric answer, just give the probability expression).
- (c) What is P(G|S)? (i.e., the four probability values P(g|s), P(-g|s), P(g|-s), P(-g|-s).

- (d) What is $\mathbf{P}(G|S \wedge W)$? (i.e., the 8 probability values $\mathbf{P}(g|s \wedge w)$, $\mathbf{P}(g|s \wedge -w)$, ..., $\mathbf{P}(-g|-s \wedge -w)$).
- (e) What do these values tell us about the relationship between G, W and S?
- (f) What is $\mathbf{P}(G|W)$? (i.e., the four probability values $\mathbf{P}(g|w)$, $\mathbf{P}(-g|w)$, $\mathbf{P}(g|-w)$, and $\mathbf{P}(-g|-w)$).
- (g) What do these values tell us about the relationship between G and W, and why does this relationship differ when we know S?

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