Let n be a natural variable. Add time according to the recursive measure, and find a finite upper bound on the execution time of

$$P \leftarrow \text{if } n \ge 2 \text{ then } n := n-2. P. n := n+1. P. n := n+1 \text{ else } ok \text{ fi}$$

To ensure that every loop includes a time increment, it is sufficient to put t:=t+1 just before the first call. (But the question isn't any harder, and the time bound isn't significantly different, if we put t:=t+1 before both calls.) Because of the two calls, each at approximately the original value of n, I guess the time might be exponential. Actually, it looks just like Fibonacci: the first call is at n-2, the second is at n-1. Let's try

$$P = t' \le t + 2^n$$

The proof of the refinement will be by cases. First case:

$$n \ge 2 \land (n := n-2. \ t := t+1. \ P. \ n := n+1. \ P. \ n := n+1)$$

 $n \ge 2 \land (t' \le t+1+2^{n-2}. \ t' \le t+2^{n+1}. \ n' = n+1 \land t' = t)$
 $n \ge 2 \land \exists n'', t'', n''', t''' \cdot t'' \le t+1+2^{n-2} \land t''' \le t'' +2^{n''+1} \land n' = n'''+1 \land t' = t'''$
 $n \ge 2$

Oops. The final time seems to be completely arbitrary. The problem is that the first call of P allows n to change arbitrarily, so the last call of P allows t to change arbitrarily. Let's try again.

$$P = n' = n \wedge t' \leq t + 2^n$$

The proof of the refinement will be by cases. First case:

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- $= n + \frac{1}{2} + \frac{1}{2} + \frac{1}{4} + \frac{1}{4}$
- ⇒ $n \ge 2 \land n' = n \land t' \le t + 2^{n-2} + 3 \times 2^{n-2}$

when $n \ge 2$, $1 \le 2^{n-2}$ specialize and simplify

⇒ n'=n https://powcoder.com

Last case:

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- *n*<2 ∧ *ok*
- $\stackrel{=}{\Rightarrow} n^{<2} \wedge n^{\prime} = n \wedge n^{\prime} = n^{\prime} = n \wedge n^{\prime} = n^{\prime} = n^{\prime} = n^{\prime} = n^{\prime} \wedge n^{\prime} = n^{\prime} \wedge$

and $0 \le 2^n$