

# Introduction (cont.)

- **Examples of Cryptanalysis Techniques**

**Ciphertext-only attack:** The key or plaintext is revealed exclusively by means of the ciphertext. This method is the most difficult. If too little is known of the rules of the ciphertext to be able to exploit them, only one obvious thing remains: trying every possible key. This is called **brute-force attack** (exploiting the key space). Often, however, it is sufficient to try just a few keys; but more about this later.

**Known-plaintext attack:** Part of the plaintext is known in addition to the ciphertext, and used to reveal the remaining plaintext, normally by means of the key. This is perhaps the most important cryptanalytic method, because it is much more powerful than a ciphertext-only attack and normally possible: the attacker guesses certain words in the text; the beginning of the text is fixed; known, uncritical plaintexts are encoded with the same key as confidential plaintexts, etc.

**Chosen-plaintext attack:** In this attack, the adversary has the ability to obtain the encryption of any plaintext(s) of its choice. It then attempts to determine the plaintext that was encrypted to give some other ciphertext.

**Chosen-ciphertext attack:** The final type of attack is one where the adversary is even given the capability to obtain the decryption of any ciphertext(s) of its choice. The adversary's aim, once again, is then to determine the plaintext that was encrypted to give some other ciphertext (whose decryption the adversary is unable to obtain directly).

**passive  
attacks**

hacker does  
**NOT** have access  
to crypto-system

**active  
attacks**

hacker has access  
to crypto-system

# Introduction (cont.)

## Ciphertext Only Attacks

(nothing about plaintext is known!)

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## Known Plaintext Attacks

(part of plaintext is known!)

*Hello Alice,*

0DGcvHRAfNTgTuyYe2vFPepZlBURswPGTnPP1cnw3ZBxpHB3be  
PpxFt+8X8bmdMpxwha6So6C352DeZE93dFbUpTk8aTfyYESNh+  
aYPfVEYL/6+1a2gpJ7Rdj1oCRtHy/Il6RechMjsl+wrjNHRWr+  
yP0NncBPShXrG+vEraQlgi4BaETLgA2/rtZdWcaJjBGSORyghE  
qLBuiAFAjL1iLJ8pX3SfPYRDVil4/o2LSZJVCMLVpauz5mX5Yf  
IUZCzqD2RfmPpcW/un6Nh05oLZIB/9WYAMrHVCsXwkxzw0au6s  
7IhubbU16QWAgF2lGkR1y8jz9P08L19MYFYrjxlj1M0Ytvrs5V  
wXBEGzpu6xDlOP344uR9cy0w8gY7JLG207a1lNqtrF4dLD6ZaS  
Pywo2VRcDr+kTRLv/3TKWPY1bpG3qG0l9fSB02lFPjxTPSnFET  
/ZfU3V1w6y7KMyWxcySHXzX2PwC9Wj6DluiijDfikoXjR4Lqtu  
griG+TprpPwmpCST9LwvRoe14Yh6EnYCTvYUyvZVy1foS4xd03  
CtgcYD0mZm2Vzlp+s27s9zfdGwe5YV41+ucLHCf+6o5nMnN9RV  
B/H2K0hpo2bxpgH+/Zef3d3xGqPydA

Wj6DluiijDfikoXjR4L

0DGcvHRAfNTgTuyYe2vFPepZlBURswPGTnPP1cnw3ZBxpHB3be  
PpxFt+8X8bmdMpxwha6So6C352DeZE93dFbUpTk8aTfyYESNh+  
aYPfVEYL/6+1a2gpJ7Rdj1oCRtHy/Il6RechMjsl+wrjNHRWr+  
yP0NncBPShXrG+vEraQlgi4BaETLgA2/rtZdWcaJjBGSORyghE  
qLBuiAFAjL1iLJ8pX3SfPYRDVil4/o2LSZJVCMLVpauz5mX5Yf  
IUZCzqD2RfmPpcW/un6Nh05oLZIB/9WYAMrHVCsXwkxzw0au6s  
7IhubbU16QWAgF2lGkR1y8jz9P08L19MYFYrjxlj1M0Ytvrs5V  
wXBEGzpu6xDlOP344uR9cy0w8gY7JLG207a1lNqtrF4dLD6ZaS  
Pywo2VRcDr+kTRLv/3TKWPY1bpG3qG0l9fSB02lFPjxTPSnFET  
/ZfU3V1w6y7KMyWxcySHXzX2PwC9Wj6DluiijDfikoXjR4Lqtu  
griG+TprpPwmpCST9LwvRoe14Yh6EnYCTvYUyvZVy1foS4xd03  
CtgcYD0mZm2Vzlp+s27s9zfdGwe5YV41+ucLHCf+6o5nMnN9RV

## Type of Attack

## Known to Cryptanalyst

<p>Ciphertext Only = brute force</p>	<ul style="list-style-type: none"> <li>• Encryption algorithm ← known</li> <li>• Ciphertext ← obtained</li> </ul>
<p>Known Plaintext [accelerated cryptanalysis possible]</p>	<ul style="list-style-type: none"> <li>• Encryption algorithm</li> <li>• Ciphertext</li> <li>• One or more plaintext-ciphertext pairs formed with the secret key ← can be guessed</li> </ul>
<p>Chosen Plaintext [attacker has access to the system with secret key setup (as black box) &amp; can enter chosen plaintexts]</p>	<ul style="list-style-type: none"> <li>• Encryption algorithm</li> <li>• Ciphertext</li> <li>• Plaintext message chosen by cryptanalyst, together with its corresponding ciphertext generated with the secret key</li> </ul>
<p>Chosen Ciphertext [attacker has access to the system with secret key setup (as black box) &amp; can enter chosen ciphertexts]</p>	<ul style="list-style-type: none"> <li>• Encryption algorithm</li> <li>• Ciphertext</li> <li>• Ciphertext chosen by cryptanalyst, together with its corresponding decrypted plaintext generated with the secret key</li> </ul>
<p>Chosen Text [attacker has access to the system with secret key setup (as black box) &amp; can enter both, chosen plaintexts and ciphertexts]</p>	<ul style="list-style-type: none"> <li>• Encryption algorithm</li> <li>• Ciphertext</li> <li>• Plaintext message chosen by cryptanalyst, together with its corresponding ciphertext generated with the secret key</li> <li>• Ciphertext chosen by cryptanalyst, together with its corresponding decrypted plaintext generated with the secret key</li> </ul>

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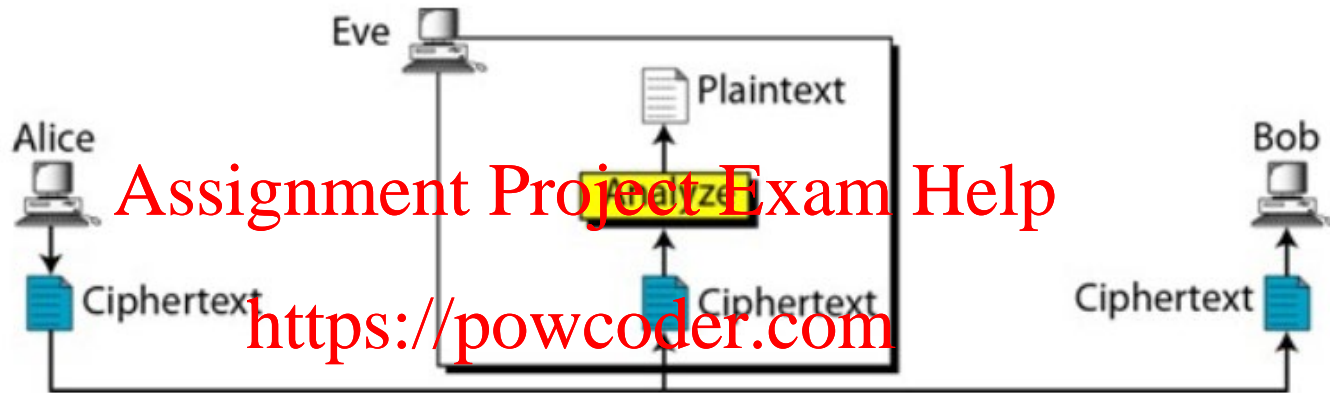
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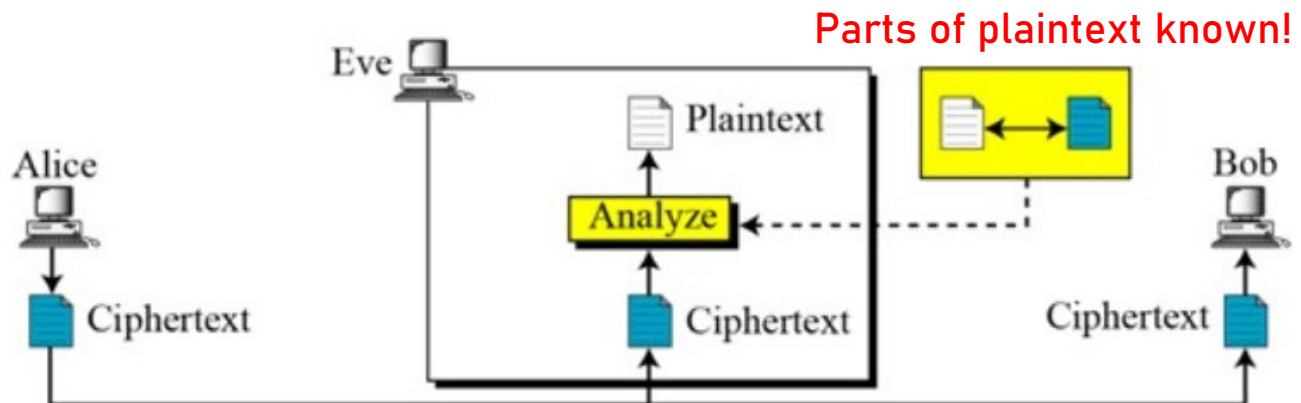
# Introduction (cont.)

**Ciphertext Only Attacks:** goal is to find the plaintext



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**Known Plaintext Attacks:** goal is to find the key

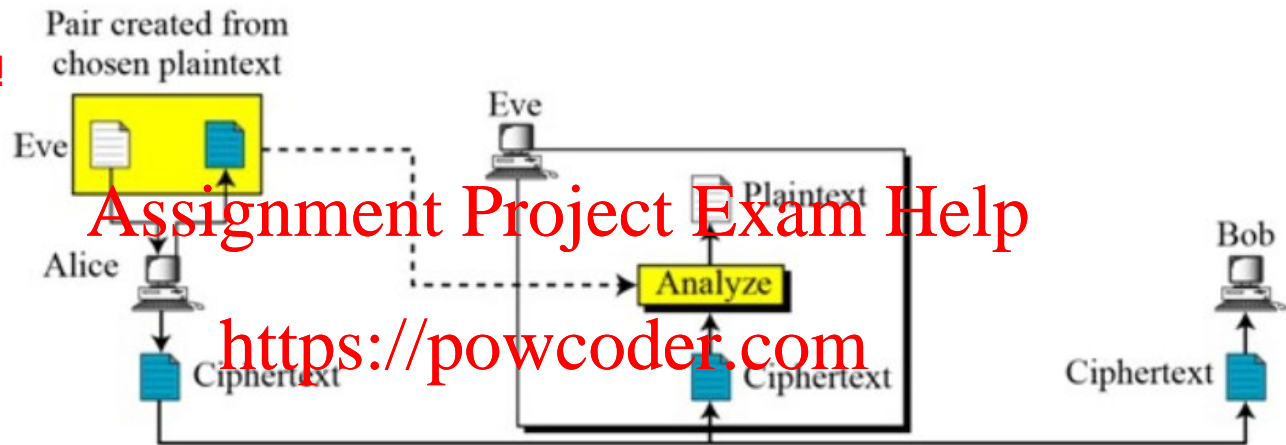


# Introduction (cont.)

lunchtime  
attacks ☺

## Chosen Plaintext Attacks: goal is to find the key

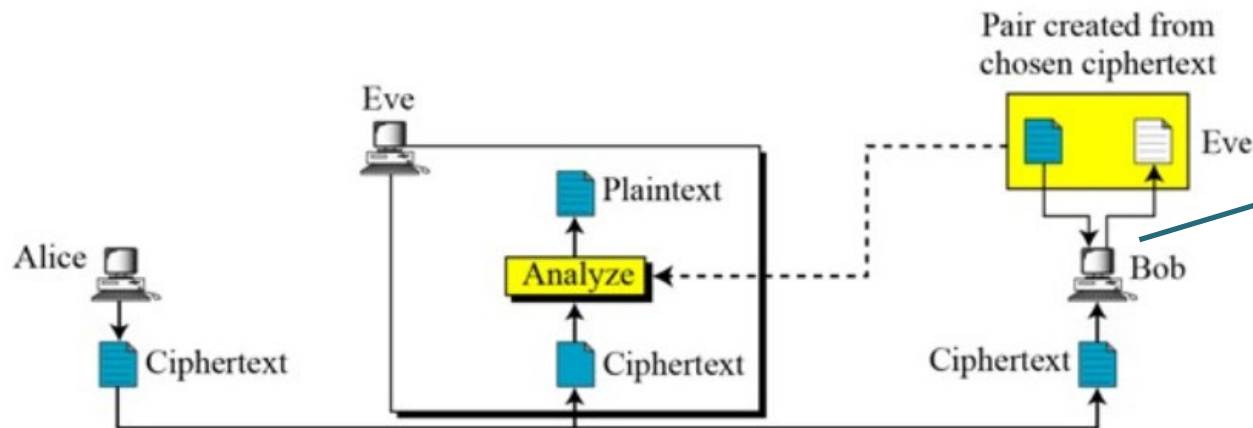
Any plaintext of  
hacker's choice!



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## Chosen Ciphertext Attacks: goal is to find the key

Any ciphertext of  
hacker's choice!



Eve gets access  
to the system  
once, manages to  
'crack' the key and  
then (re)uses this  
key to decrypt any  
subsequent  
messages ...

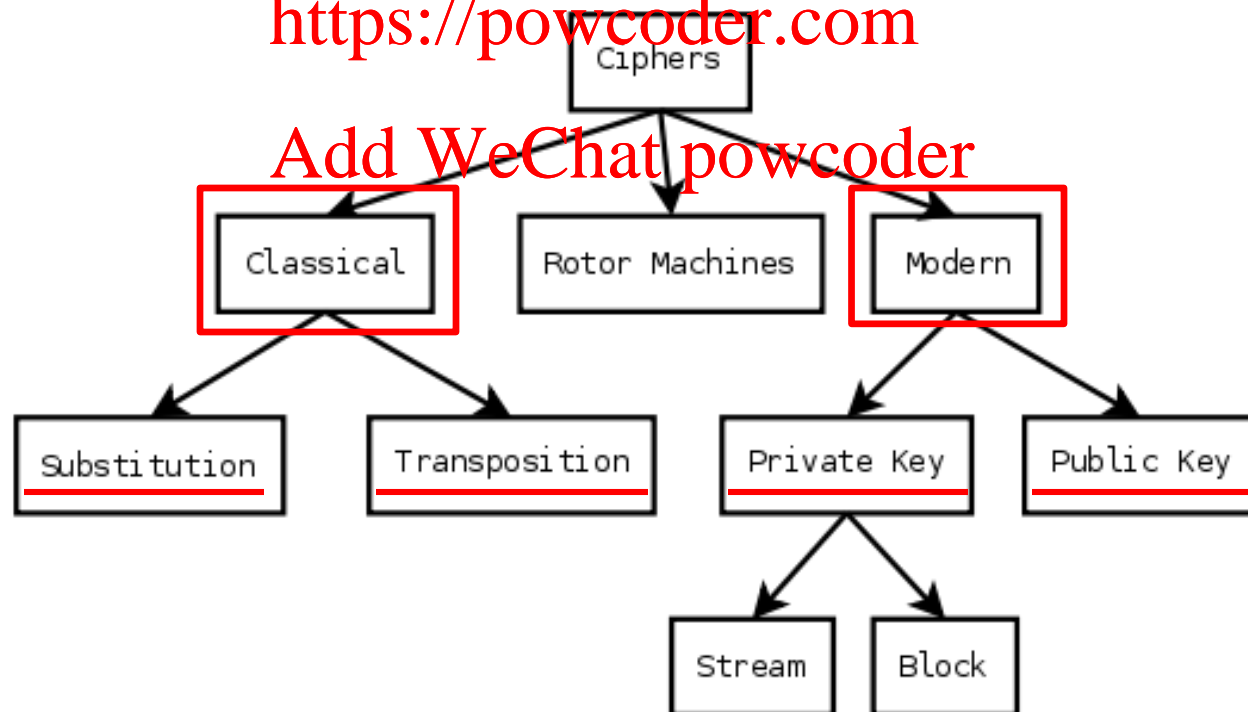
# Ciphers

- **History of Cryptography**

- ◆ humans have been using cryptographic techniques for 1000s of years – what have changed are the complexity and creativity of cryptographic techniques

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# Ciphers (cont.)

- **Classical vs. Modern Cryptography**

- ◆ **Classical cryptography** - more of an art than science

- schemes were designed in an ad-hoc manner and then evaluated based on their perceived complexity/cleverness

- true 'strength' of these schemes was in 'secrecy' of their respective protocols

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- ◆ **Modern cryptography** - based on scientific foundations

- the strength is NOT in secrecy of protocols but in **sound mathematical and computational principles**

- it is now possible to formally argue about the security protocols

- used for more than just data confidentiality - can protect data integrity, enable user authentication, etc.



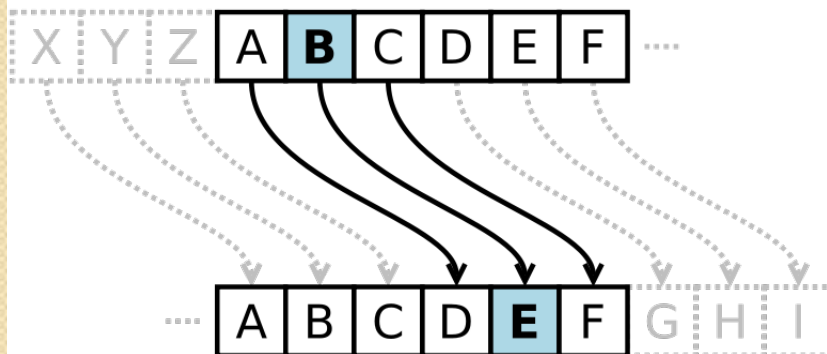
# Classical Ciphers

- ◆ **Substitution Cipher** – the units of plaintext (letters) are kept in the same original sequence, but the units themselves are altered

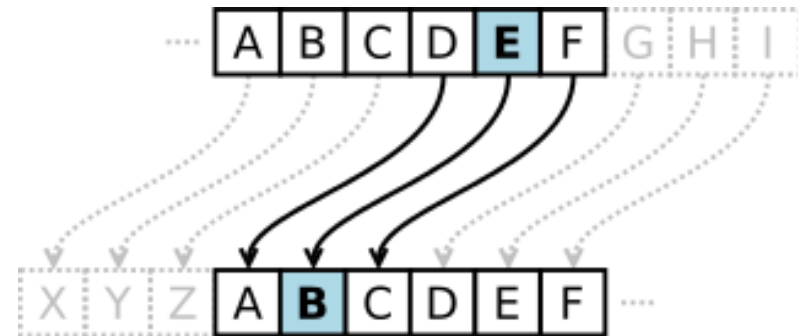
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- ◆ **Caesar Cipher** – substitution cipher in which each letter in the plaintext is replaced by a letter some fixed number of positions down the alphabet

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Example: Caesar Cipher with  $k=3$



encryption algorithm



decryption algorithm

# Classical Ciphers (cont.)

**Example: Caesar cipher encryption with  $k=3$**

Ciphertext: WKH TXLFN EURZQ IRA MXPSV RYHU WKH ODCB GRJ

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Plaintext: THE QUICK BROWN FOX JUMPS OVER THE LAZY DOG

**<https://powcoder.com>**

<https://www.cs.uri.edu/cryptography/classicalshiftdemo.htm>

[http://www.simon Singh.net/The\\_Black\\_Chamber/caesar.html](http://www.simon Singh.net/The_Black_Chamber/caesar.html)

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**Caesar cipher is easy to break.  
Keyspace = 25 different keys**

# Classical Ciphers (cont.)

Represent letters  
with numbers!

## ◆ Cesar Cipher as an Algorithm

$T_i$  -  $i$ -th character of the plain text

$C_i$  -  $i$ -th character of the cipher text

$i = 0, 1, 2, \dots, m-1$  in English

$m$  - length of the alphabet

**$k$  - shift**

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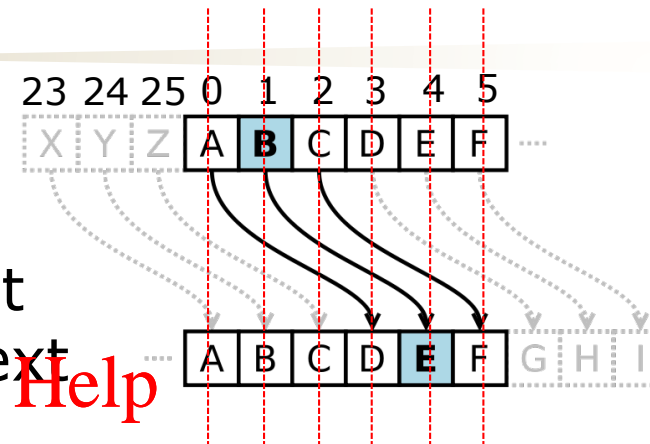
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Encryption:  $C_i = (T_i + k) \bmod m$

Decryption:  $T_i = (C_i - k) \bmod m$

NOTE:

$-b \bmod m = (-b + m) \bmod m$



# Classical Ciphers (cont.)

aka masonic or  
tic-tac-toe cipher

- ◆ **Pigpen Cipher** – substitution cipher in which each letter is replaced with a **graphical symbol**
  - alphabet is written in 4 grids shown below
  - each letter is replaced with a symbol that corresponds to the portion of the pigpen grid that contains the letter
  - used by Freemasons in the 18<sup>th</sup> century to keep their records private

A	B	C
D	E	F
G	H	I

J	K	L
M	N	O
P	Q	R

	S	
T		U
	V	

	W	
X		Y
	Z	

Example: Pigpen cipher

✓ □ L ◻ ◻ > L ◻ ◻ ◻

SECRET CODE

# Classical Ciphers (cont.)

## Example: Pigpen Cipher variants

A	C	E
G	I	K
M	O	Q

B	D	F
H	J	L
N	P	R

A	B	C
D	E	F
G	H	I

J	K	L
	M	

U	S	W
	Y	

V	T	X
	Z	

Q	R	S
T	U	V

W	X	Y
	Z	

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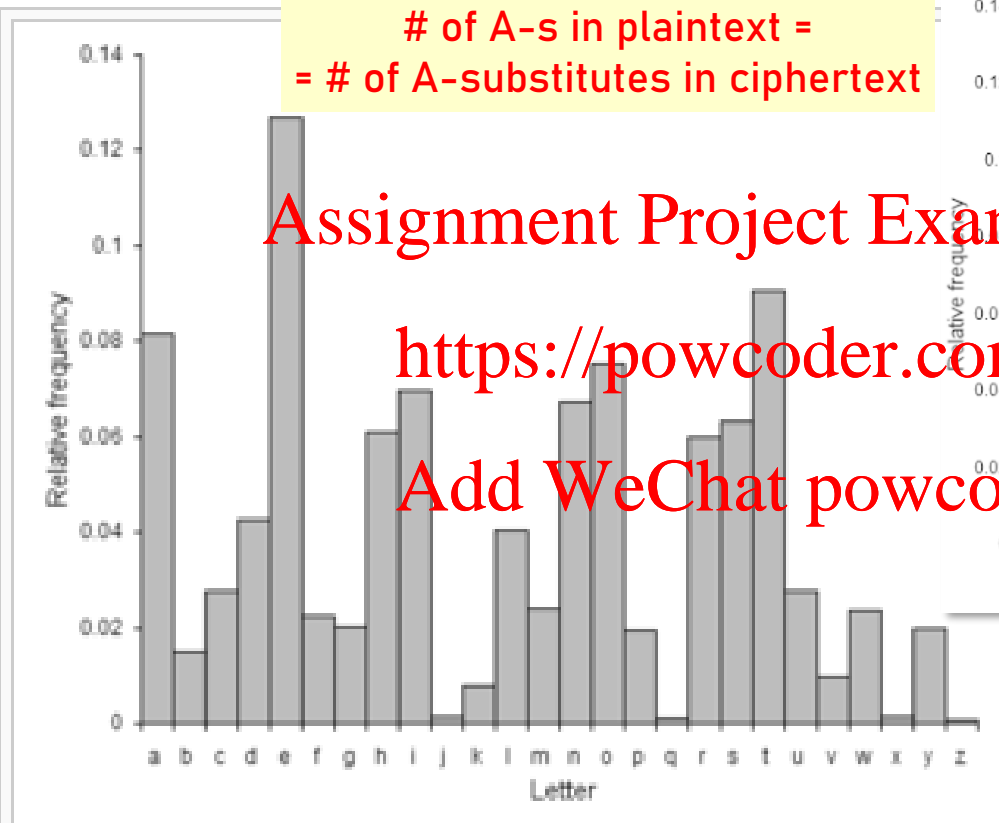
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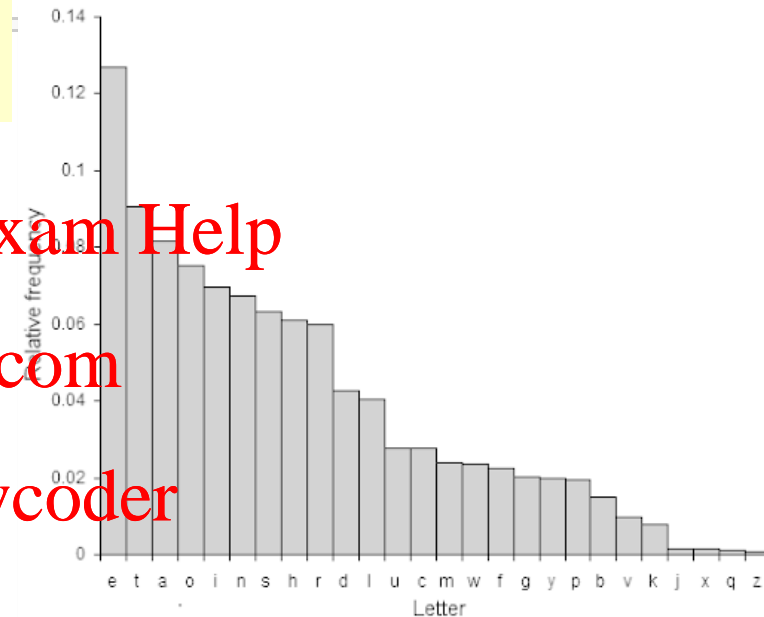
# Classical Ciphers (cont.)

**Example:** How to break a simple substitution cipher?

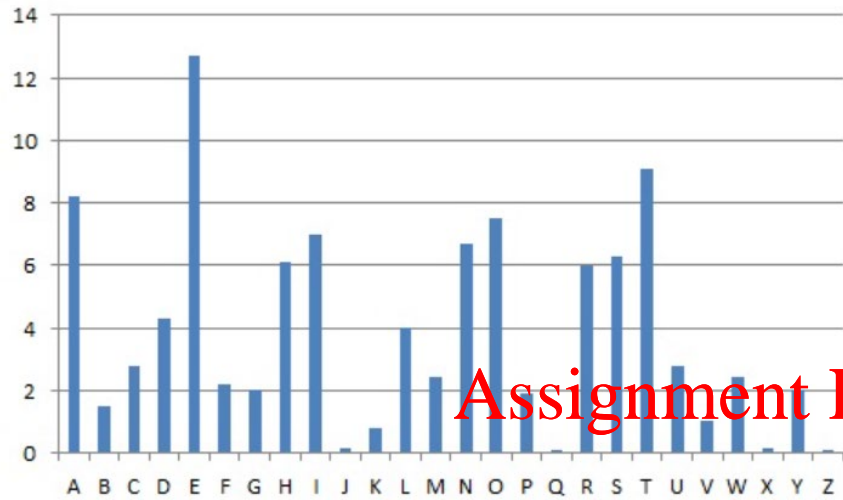
# of A-s in plaintext =  
= # of A-substitutes in ciphertext



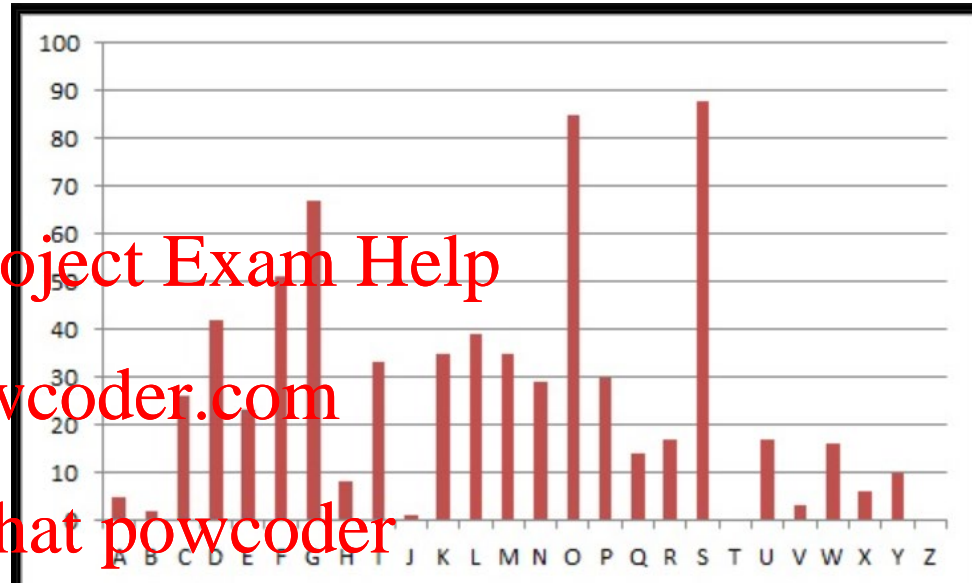
The distribution of letters in a typical sample of English language text has a distinctive and predictable shape. A Caesar shift "rotates" this distribution, and it is possible to determine the shift by examining the resultant frequency graph.



# Example: breaking a cipher using FREQUENCY analysis



The Standard English Letter Frequencies



The letter frequencies of the letters in the ciphertext.

“Now that we have all the frequencies of ciphertext letters, we can start to make some substitutions. We see that the most common ciphertext letter is "S", closely followed by "O". From the chart and table above, we can guess that these two letters represent "e" and "t" respectively, and after making these substitutions we get ... “

<https://crypto.interactive-maths.com/frequency-analysis-breaking-the-code.html>

# Classical Ciphers (cont.)

- ◆ **Polyalphabetic / Vigenere Cipher** – complex substitution cipher - instead of shifting each character by the same number, characters located at different positions are shifted by different numbers **key keeps changing!**

- key (word) must be provided

- key is aligned with plaintext – key-letter determines the value of cipher-letter

PLAINTEXT

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
A	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
B	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A
C	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B
D	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C
E	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D
F	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E
G	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F
H	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G
I	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H
J	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I
K	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J
L	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K
M	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L
N	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M
O	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N
P	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O
Q	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P
R	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q
S	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R
T	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S
U	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T
V	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U
W	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V
X	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W
Y	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X
Z	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y

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# Classical Ciphers (cont.)

Example: Vigenere Cipher - decryption using the table

Plaintext: HOW ARE YOU

Key: ABC ABC ABC

Ciphertext: HPY ASG YPW

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key

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
A	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
B	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A
C	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B
D	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C
E	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D
F	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E
G	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F
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J	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I
K	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J
L	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K
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Q	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P
R	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q
S	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R
T	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S
U	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T
V	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U
W	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V
X	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W
Y	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X
Z	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y



# Classical Ciphers (cont.)

## ◆ Vigenere Cipher as an Algorithm

$T_i$  -  $i$ -th character of the plain text

$C_i$  -  $i$ -th character of the cipher text

$K_i$  -  $i$ -th character of the key phrase

$i = 0, 1, 2, \dots, m-1$

$m$  - length of the alphabet

Encryption:  **$C_i = (T_i + K_i) \bmod m$**

Decryption:  **$T_i = (C_i - K_i) \bmod m$**



# Classical Ciphers (cont.)

**Example:** Vigenere Cipher - encryption using algorithm

Open text: ATTACK AT DAWN

Key phrase: CAT

Length of the alphabet: 26

23	0	1	2	3	4	5
X Y Z	A	B	C	D	E	F

A	+	C	=	0	+	2	=	2	=	C
T	+	A	=	19	+	0	=	19	=	T
T	+	T	=	19	+	19	=	12	=	M
A	+	C	=	0	+	2	=	2	=	C
C	+	A	=	2	+	0	=	2	=	C
K	+	T	=	10	+	19	=	3	=	D
A	+	C	=	0	+	2	=	2	=	C
T	+	A	=	19	+	0	=	19	=	T
D	+	T	=	3	+	19	=	22	=	W
A	+	C	=	0	+	2	=	2	=	C
W	+	A	=	22	+	0	=	22	=	W
N	+	T	=	13	+	19	=	6	=	G

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