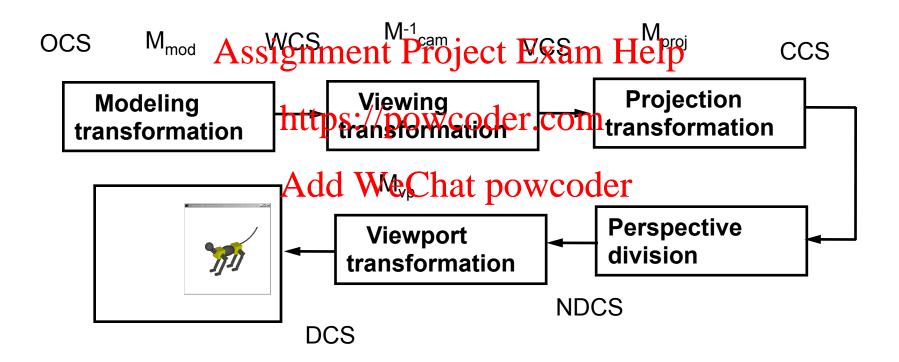
#### **All transformations**



## **Line Rendering Algorithm**

```
Compute M<sub>mod</sub>
Compute M<sup>-1</sup>cam
Compute MmodeAissign Transmin Broject Exam Help
Compute Mo
Compute M<sub>P</sub> // disregard M<sub>P</sub> here and below for orthographic-only case
Compute M_{proj} = M_{O}M_{Pdd} WeChat powcoder
Compute M<sub>VP</sub>
Compute M = M_{VP} M_{proj} M_{modelview}
for each line segment i between vertices P<sub>i</sub> and Q<sub>i</sub> do
    P = MP_i; Q = MQ_i
    drawline(P_x/h_P, P_y/h_P, Q_x/h_Q, Q_y/h_Q) // h_P,h_Q are the 4<sup>th</sup> coordinates of P,Q
end for
```

## 3D Clipping

Keep what is visible WCS VCS ocs modelling viewing projection We can clip tranformátion transformation trańsformation 1. in the WCS Assignment Project Exam Help CCS perspective division What are the six plane equations? NDCS https://powcoder.com 2. in the CCS Clipping in homogeneous coordinates 4 powcoder volume bounded by 3D planes Still simple and efficient 3. In the NDCS Singularity at  $P_z = 0$ In any case we must clip against planes

### Orthographic view volume

#### Planes in viewing coordinates

```
Normals pointing inside
```

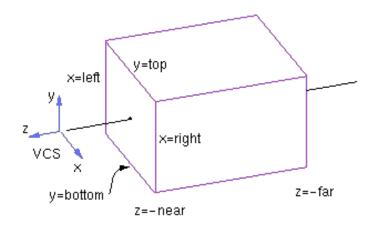
left: x - left = Assignment Project Exam Help

right: -x + right = Ohttps://powcoder.com

bottom: y - bottom = 0
Add WeChat powcoder

front: -z - near = 0

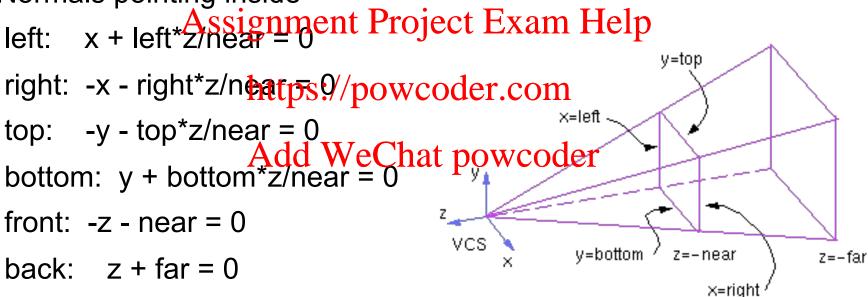
back: z + far = 0



### Perspective View volume

#### Planes in viewing coordinates

Normals pointing inside



## Clipping in NDCS (Aside)

#### Normalized view volume

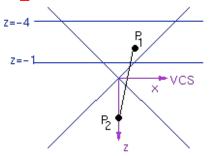
Constant planes

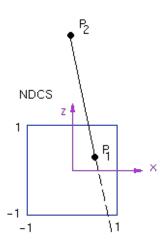
Lines in VCS lines NDCS Project Exam Help vcs (1,0,-2) (0,0,2)

#### **Problem**

https://powcoder.com/(1/2, 0, 1/3) (0, 0, -6, -2)

 Z coordinate loses its sign Add WeChat powcoder





## Clipping in CCS (Aside)

We'll define the clipping region in CCS by first looking at the clipping region in NDCS:

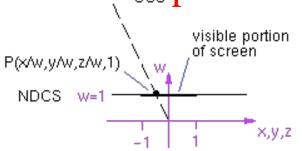
-1 <= x/w <= 1 Assignment Project Exam Help

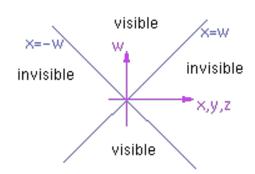
This means that in CCS, we have: https://powcoder.com

-w <= x <= w

Similarly for y,z



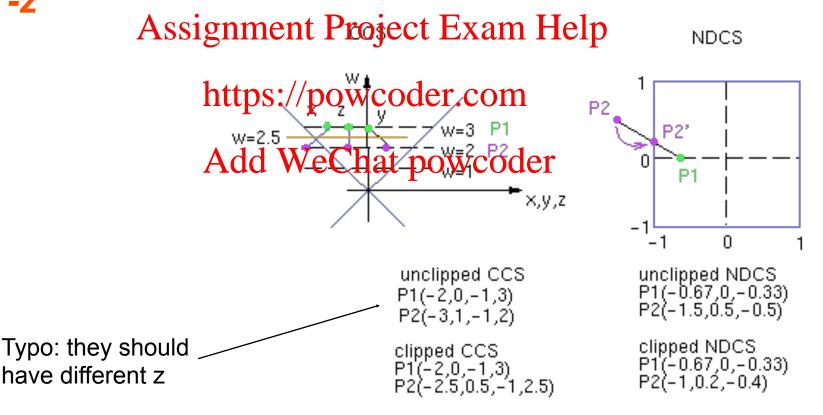




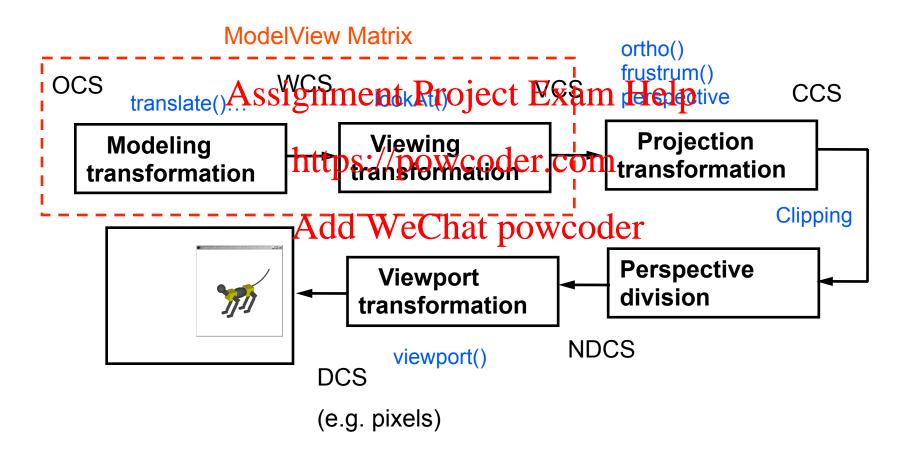
## Example (Aside)

#### The perspective transformation creates

W = -z



### So far our Pipeline



#### Rasterization

- The rasterizer outputs the location of fragments, i.e. pixel size screen elements. We can consider a fragment as pixel ment of the pare not exactly equivalents://powcoder.com
- The programmable fragment shader computes the Add WeChat powcoder colors of the fragments and now they affect the corresponding pixel

## Representations for lines and Curves

#### Line (in 2D)

- Explicit
- Implicit

Assignment Project Exam Help  $y = \frac{dy}{dx}(x - x_0) + y_0$ 

https://powcoder.com
if 
$$F(x,y) = (x-x_0)dy - (y-y_0)dx$$

$$F(x,y) = 0 \quad \text{then} \quad (x,y) \text{ is on line}$$

$$F(x,y) > 0 \quad (x,y) \text{ is below line}$$

$$F(x,y) > 0 \quad (x,y) \text{ is above line}$$

Parametric

$$x(t) = x_0 + t(x_1 - x_0)$$

$$y(t) = y_0 + t(y_1 - y_0)$$

$$t \in [0, 1]$$

$$P(t) = P_0 + t(P_1 - P_0), \text{ or }$$

$$P(t) = (1 - t)P_0 + tP_1$$

#### Circle

Explicit

### Assignment\_Project Exam Help

Implicit

https://powcoder.com

Add  $F(x, y) = x^2 + y^2 - r^2$ Add WeChat powcoder

if 
$$F(x,y) = 0$$
 then  $(x,y)$  is on circle  $F(x,y) > 0$   $(x,y)$  is outside  $F(x,y) < 0$   $(x,y)$  is inside

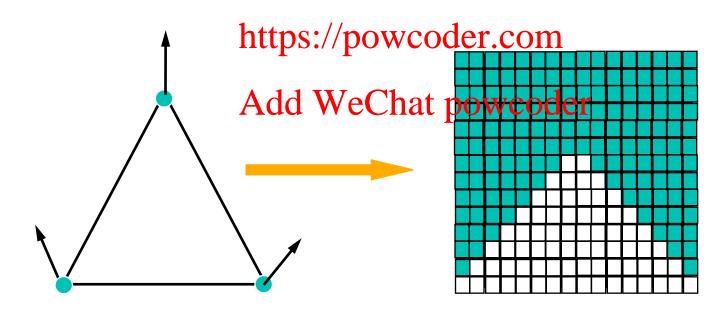
Parametric

$$x(\theta) = r \cos(\theta)$$
$$y(\theta) = r \sin(\theta)$$
$$\theta \in [0, 2\pi]$$

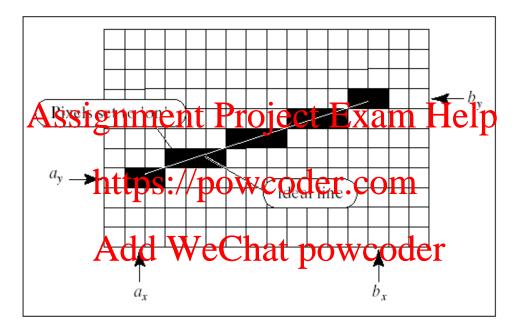
#### Rasterization

#### Primitives must be rasterized

Mathematical form --> Set of finite size pixels



#### Line rasterization



**FIGURE 10.23** Drawing a straight-line-segment.

#### Line rasterization

Desired properties

Straight

Pass through Propert Pro

**Smooth** 

Independent of end point

order

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Uniform brightness

Brightness independent of slope

**Efficient** 

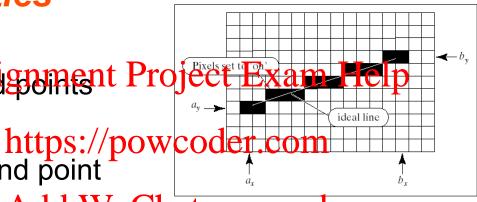
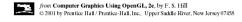


FIGURE 10.23 Drawing a straight-line-segment.



### Straightforward Implementation

#### Line between two points

$$(x_1,y_1)$$
 Assignment Project Exam Help

$$y(x) = y_1 + \frac{\text{httpst//poweoder.com}}{\text{Add WeChat powcoder}}$$

### Straightforward Implementation

```
Line between two points (slope < 45)
```

```
Round points then:
             Assignment Project Exam Help
DrawLine(int x1, int y11tiptsx2;potyx2)oder.com
     float y; Add WeChat powcoder
     int x;
     for (x=x1; x \le x2; x++) {
            y = y1 + (x-x1)*(y2-y1)/(x2-x1)
            SetPixel(x, Round(y));
```

### **Better Implementation**

#### How can we improve this algorithm?

### **Better Implementation**

```
DrawLine(int x1,int y1,int x2,int y2)
     float y,m;Assignment Project Exam Help
     int x;
     dx = x2-x1; https://powcoder.com
     dy = y2-y1;
     m = dy/ (float) Add WeChat powcoder
     for (x=x1; x \le x = x + 1)
            y = y1 + m*(x-x1);
            SetPixel(x, Round(y));
```

## Even Better Implementation: Incremental

```
DrawLine(int x1,int y1,int x2,int y2)
      float y,m; Assignment Project Exam Help
      int x;
      dx = x2-x1; https://powcoder.com
      dy = y2-y1;
      m = dy/ (float) Add WeChat powcoder
      y = y1 + 0.5;
      for (x=x1; x \le x = x + 1) {
             SetPixel(x, Floor(y));
             y = y + m;
// y(x) = mx + d --> y(x+1) = y(x) + m
```

# Midpoint algorithm (Bresenham) (ASIDE)

Line in the first quadrant ( 0<slope < 45 deg)

Implicit function:

F(x,y) = xdy - Assignment Project Exam Help dx,dy > 0 and  $dy/dx \le 10$ • Current choice P = (x,y).

• How do we chose nextlef PyeChat powcoder

P'= (x+1,y')?

 $P=(p_x,p_y)$ 

# Midpoint algorithm (Bresenham) (ASIDE)

Line in the first quadrant ( 0<slope < 45 deg)

Implicit function:

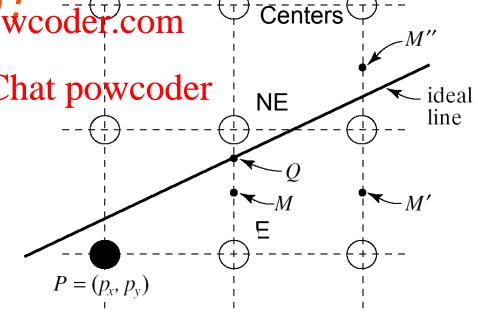
$$F(x,y) = xdy$$
 -Assignment Project Exam Help  $dx,dy > 0$  and  $dy/dx \le 1.0$ ; Pixel Center of the Context of the Power of t

Current choice P = (x,y).

How do we chose nextler WeChat powcoder

P'= 
$$(x+1,y')$$
?  
If( F(M) = F(x+1,y+0.5) < 0)  
M above line so E  
else

M below line so NE



## Midpoint algorithm (Bresenham)

```
DrawLine(int x1, float y1, int x2, float y2, int color)
        int x,y,dx,dy;
Assignment Project Exam Help
        y = Round(y1);
for (x=x1; x<=x^2, x^2) powcoder.com
       SetPixel(x, y ); Add WeChat powcoder if (F(x+1,y+0.5)>0) {
                                                                                ideal
                                                               NE
                                                                                line
                 y = y + 1;
                                           P=(p_x,p_y)
```

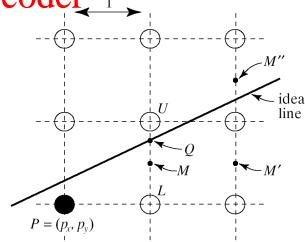
## Can we compute F in a smart way?

 We are at pixel (x,y) we evaluate F at M = (x+1,y+0.5) and E=(x+1,y) or NE=(x+1,y+1) accordingly.

(Reminder: Assignment/Project Exam Help

https://powcoder.com

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## Can we compute F in a smart way?

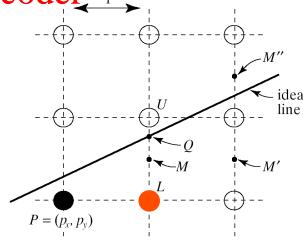
We are at pixel (x,y) we evaluate F at M = (x+1,y+0.5) and E=(x+1,y) or NE=(x+1,y+1) accordingly.

(Reminder: Assignment/Project Exam Help

If we chose E for x+1 the next criteria will be at M':

 $F(x+2,y+0.5) = [(x+1)6y/400) \times (9+6.5) \times (9+6.5)$ 

 $F(x+2,y+0.5) = F(x+1,y+0.5) + dy \rightarrow Add We Char powcoder_{1}$   $F_{F} = F + dy = F + dF_{F}$ 



## Can we compute F in a smart way?

 We are at pixel (x,y) we evaluate F at M = (x+1,y+0.5) and E=(x+1,y) or NE=(x+1,y+1) accordingly.

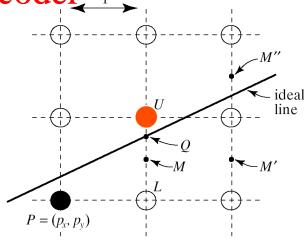
(Reminder: Assignment/Project Exam Help

• If we chose E for x+1 the next criteria will be at M': F(x+2,y+0.5) = (x + 1 + 0.5) + dy = 0.5

 $F(x+2,y+0.5) = F(x+1,y+0.5) + dy \rightarrow Add WeChat powcoder_{1}$ 

 If we chose NE then the next criteria will be at M":

$$F(x+2,y+1+0.5) =$$
  
 $F(x+1,y+0.5) + dy - dx \rightarrow$   
 $F_{NE} = F + dy - dx$ 



## Can we compute F in a smart way?

 We are at pixel (x,y) we evaluate F at M = (x+1,y+0.5) and E=(x+1,y) or NE=(x+1,y+1) accordingly.

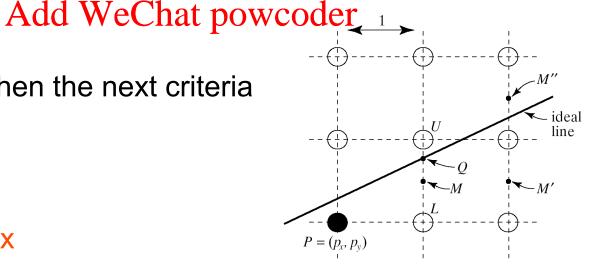
(Reminder: Assignment/Project Exam Help

 If we chose E for x+1 the next criteria will be at M': https://powcoder.com

$$F_E = F + dy$$

 If we chose NE then the next criteria will be at M":

$$F_{NE} = F + dy - dx$$



### **Criterion update**

#### **Update**

$$F_E = F + dy = F + dF_E$$

F<sub>NE</sub> = F + dy - dx<del>Assignment Project Exam Help</del>

#### Starting value?

Line equation: F(x,y) https://pewcoder.com

Assume line starts at pixel 
$$(x_0, y_0)$$

$$F_{\text{start}} = F(x_0+1, y_0+0.3) = (x_0, y_0) + (x_0,$$

= 
$$(x_0dy - y_0dx + c) + dy - 0.5dx = F(x_0,y_0) + dy - 0.5dx$$
.

 $(x_0,y_0)$  belongs on the line so:  $F(x_0,y_0) = 0$ 

#### Therefore:

$$F_{start} = dy - 0.5dx$$

## Criterion update (Integer version)

#### **Update**

$$F_{\text{start}} = \text{dy} - 0.5 \text{dx}$$
 $F_{\text{E}} = F + \text{dy} = F + \text{dF}_{\text{E}}$ 
 $F_{\text{NE}} = F + \text{dy} - \text{dx} = \text{https://powcoder.com}$ 

### Everything is integret to by speciel to be a second of the control of the control

Multiply by 2 
$$\rightarrow$$
 F<sub>start</sub> = 2dy – dx  
dF<sub>E</sub> = 2dy  
dF<sub>NE</sub> = 2(dy-dx)

### Midpoint algorithm

```
DrawLine(int x1, float y1, int x2, float y2, int color)
       int x,y,dx,dy,dE, dNE;
       dx = x2-x1;
       dy = y2-y1 ; Assignment Project Exam Help
       d = 2*dy-dx; // initialize d
       dE = 2*dy;
       dNE = 2*(dy-dx); https://powcoder.com
       y = Round(y1);
       for (x=x1; x<=x2; x+A)dd WeChat powcoder SetPixel(x, y, color);
                 if (d>0) { // chose NE
                          d = d + dNE;
                          y = y + 1;
                         // chose E
                 } else {
                          d = d + dE;
```

# Incremental algorithms for polynomials (ASIDE)

General form or a polynomial of degree *n*:

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$$F(x) = a_n x^n + \underbrace{a_{n-1} x^{n-1} \cdots + a_1 x + a_0}_{\text{https://powcoder.com}}, a_n \neq 0$$

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or

$$F(x) = a_n x^n + Q^{n-1}(x), \quad a_n \neq 0$$

# Incremental algorithms for polynomials

$$F(x) = a_{n}x^{n} + Q^{n-1}(x), a_{n} \neq 0$$

$$F(x+d) = a_{n}(x+d)^{n} + Q^{n-1}(x+d) = a_{n}(x+d)^{n} + P^{n-1}(x)$$

$$= a_{n} \sum_{k=0}^{n} \binom{n}{k!} x^{n-k} d^{k} + P^{n-1}(x)$$

$$= a_{n} \sum_{k=0}^{n} \binom{Adl We}{k!(n-k)!} \text{ where } C_{k}$$

$$= a_{n} \sum_{k=0}^{n} \binom{Adl We}{k!(n-k)!} x^{n-k} d^{k} + P^{n-1}(x)$$

$$= a_{n}x^{n} + \sum_{k=1}^{n} \binom{n}{k!(n-k)!} x^{n-k} d^{k} + P^{n-1}(x)$$

$$= a_{n}x^{n} + R^{n-1}(x) + P^{n-1}(x)$$

$$= a_{n}x^{n} + G^{n-1}(x)$$

# N-order differences (ASIDE)

Polynomial forms

$$F(x) = a_n x^n + Q^{n-1}(x), a_n \neq 0$$
  
 $F(x + a)$  Signment, Project Exam Help

First order differences

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$$\Delta F = F(x+d) - F(x+d) = a_n x^n + Q^{n-1}(x) - a_n x^n - G^{n-1}(x) = D_1^{n-1}(x)$$
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Second order differences

$$\Delta^2 F(x) = \Delta F(x+d) - \Delta F(x) = D_2^{n-2}(x)$$
:

*n*-order Differences

$$\Delta^{n} F(x) = \Delta^{n-1} F(x+d) - \Delta^{n-1} F(x) = D_{n}^{0} = c$$

### N-order difference update

Computing the polynomial incrementally from the differences

$$F(x) = a_n x^n + Q^{n-1}(x), a_n \neq 0$$

$$Assignment Project Exam Help$$

$$https://powcoder.com$$

$$F(x+d) = F(x) + \Delta^1 F(x)$$

$$\Delta F(x+d) = \mathbf{Vecaute}(x) \mathbf{vecaute}(x)$$

$$\Delta^2 F(x+d) = F(x) + \Delta F(x)$$

$$\vdots$$

$$\Delta^{n-1} F(x+d) = \Delta^{n-1} F(x) + \Delta^n F(x)$$

$$\Delta^n F(x+d) = c$$

## Example: $y = x^2$

$$y(x+d) \text{ Assign ment project } \text{Exam}(x) \text{ the properties } 2xd+d^2$$

$$\rightarrow y(x) \text{ prove other conv}(x)$$

$$where \Delta y(x) = 2xd+d^2$$

$$\Delta y(x+d) = 2(x+d)d+d^2 = \Delta y(x)+2d^2$$

$$\rightarrow \Delta y(x+d) = \Delta y(x)+\Delta^2 y(x)$$

$$where \Delta^2 y(x) = 2d^2$$

## The incremental algorithm to compute $y = x^2$ (END ASIDE)

```
computePar(int d)
    float y = Assignment Project Exam Help
    int x = 0;
DY = d^2; //at x = 0
     DDY = 2*d^Add WeChat powcoder
    for(x = 0; x < X MAX; x++) {
           printf("d, %f\", x,y);
          y = y + DY;
           DY = DY + DDY;
```

# **Polygons**

#### Collection of points connected with lines

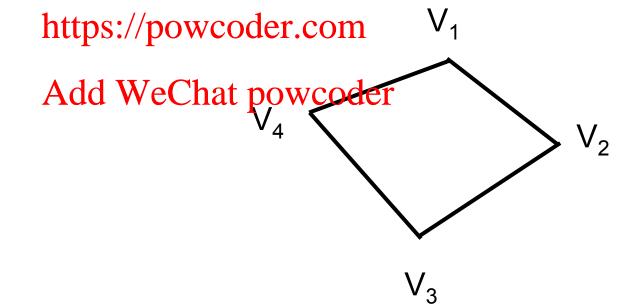
- Vertices: v1,v2,v3,v4 Assignment Project Exam Help
- Edges:

$$e_1 = v_1 v_2$$

$$e_2 = v_2 v_3$$

$$e_3 = v_3 v_4$$

$$e_4 = v_4 v_1$$



# **Polygons**

- Open / closed

Planar / non-planar
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Filled / wireframe

- Convex / concaves://powcoder.com
- Simple / non-simpleWeChat powcoder

## **Triangles**

#### The most common primitive

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Convex

https://powcoder.com

Planar

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Simple

#### Reminder

#### Plane equations

#### **Implicit**

 $F(x, y, z) = Ax + By + Szignment_P$ Project Exam Help

Points on Plane F(x, y, z) = 0https://powcoder.com

 $\overline{N}=<A,B,C>$ 

#### **Parametric**

 $Plane(s,t) = P_0 + s(P_1 - P_0) + t(P_2 - P_0)$  **Example 2** 

 $P_0, P_1, P_2$  not colinear

or

$$Plane(s,t) = (1-s-t)P_0 + sP_1 + tP_2$$

 $Plane(s,t) = P_0 + sV_1 + tV_2$  where  $V_1, V_2$  basis vectors

#### **Explicit**

$$z = -(A/C)x - (B/C)y - D/C, C \neq 0$$

#### **Point normal form**

N=<A,B,C>

#### Plane equation

Points on Plane F(x, y, z) = Ax + By + Cz + D = N Project Exam Help Points on Plane F(x, y, z) = Ax + By + Cz + D = N Project Exam Help

Observation: Let's take an arbitrary vector u that lies on the plane which can be defined by two points e.g. P1, P2 on the plane.

$$\mathbf{u} = P2 - P1$$

### Computing point normal form from 3 **Points**

$$F(x, y, z) = Ax + By + Cz + D = \mathbf{N} \cdot P + D$$

Points on Plane F(x, y, z) = 0

 $\overline{N}=<A,B,C>$ 

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First way:

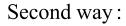
$$\mathbf{N} \bullet P0 + D = 0$$

$$\mathbf{N} \bullet P1 + D = 0$$

$$\mathbf{N} \bullet P2 + D = 0$$

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| N |= 1 (arbitrary choice) Add WeChat powcod



N is normal to F

Let's find a normal vector:

$$\mathbf{N} = (P1 - P0) \times (P2 - P0)$$

Compute *D*:

$$D = -\mathbf{N} \cdot P0$$

### Intersection of line and plane

Implicit equation for the plane:

$$F(P) = \mathbf{N} \cdot P + D$$

N=<A,B,C>

Parametric equation Arstsignmenta Project Exam Help

https://powcoder.com

Plug L(t) in F(P) and solve for  $t = t_i$ :

N Add t. We Chat powcoder

If  $N \cdot (P_a - P_b) = 0$  then zero or infinite solutions (how?). Otherwise,

$$t_i = \frac{-D - \mathbf{N} \cdot P_a}{\mathbf{N} \cdot P_b - \mathbf{N} \cdot P_a} = \frac{-F(P_a)}{F(P_b) - F(P_a)}$$

Finally, evaluate  $L(t_i)$  for the intersection point  $P_i$ :

$$P_i = P_a + \frac{-F(P_a)}{F(P_b) - F(P_a)}(P_b - P_a) = \frac{P_a F(P_b) - P_b F(P_a)}{F(P_b) - F(P_a)}$$

## Polygons in OpenGL

#### New versions ONLY TRIANGLES

Vertices have attributes (position, fromal, color, etc)

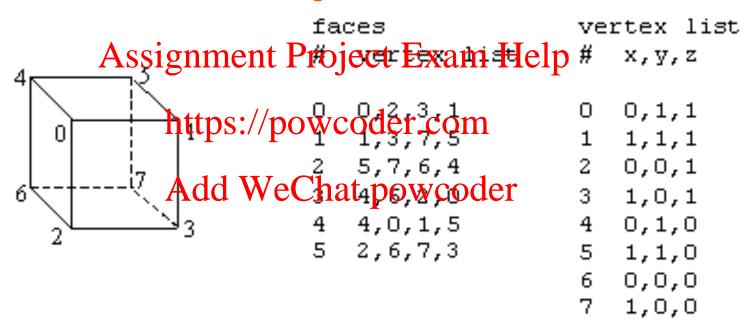
- Arrays of floats it for the stiges of the stiges of floats it for the stiges of floats it for the stiges of floats it for the stiges of the
- Indexed Arrays (Element Arrays)
   Add WeChat powcoder

#### Special functionality to store and interpret the arrays

- Vertex Buffer Objects
- Vertex Array Objects
- We will see the details later

#### **Indexed Face Sets**

#### OpenGL element arrays



- The ordering of the vertices in the faces should be consistent (clock wise or counter-clockwise)
- In OpenGL it defines the orientation (front or back) of the surface (not the normal! -- confusing, I know)

#### Vertex attributes

Generic attributes (user defined)

Commonly defined attributes Help

Position

Normal vector

Color

Texture coordinates

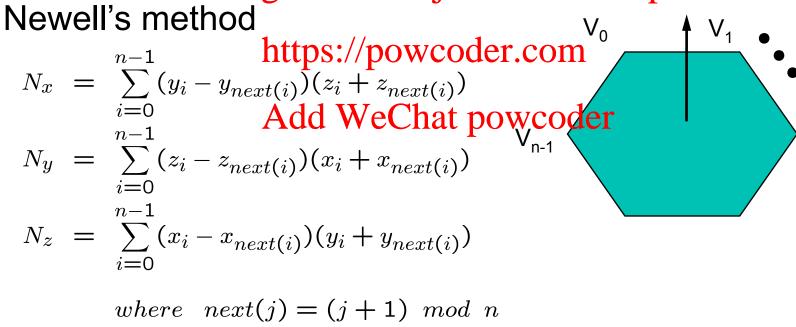
https://powcoder.com
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 Position has slightly special status, in the sense that a vertex shader must output a position

# Computing the normal of a polygon

One way:

$$N = (V_{n-1} - V_0)x(V_1 - V_0)$$
Assignment Project Exam Help



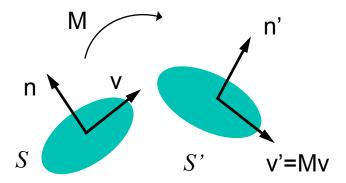
Normalize to get unit normal

#### Given an affine transformation M

• Is the new normal the M-transformed version of the Assignment Project Exam Help original normal, i.e. n' = Mn?

https://powcoder.com

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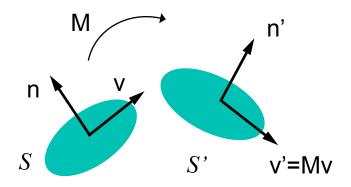


#### Given an affine transformation M

- If dot(n,v) = 0 does it mean that dot(Mn, Mv) = 0?
   Assignment Project Exam Help
- In other words is the new normal the M-transformed version of the brigginar normal the M-transformed

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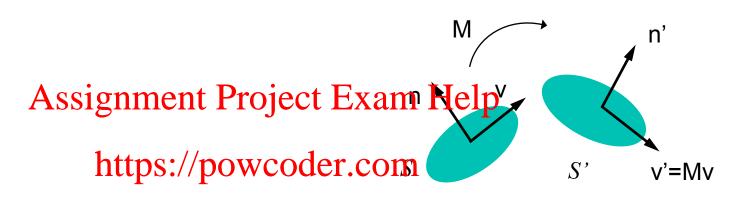
- NOT in general
  - Non uniform scale
  - Shear



$$\mathbf{n} = (n_x, n_y, n_z, 0)^T$$
 normal to  $S$ 
 $\mathbf{v} = (v_x, v_y, v_z, 0)^T$  tangent to  $S$ 
 $S' = MS$ , Assignment Project Exam Nelpy
 $\mathbf{n} \cdot \mathbf{v} = \mathbf{n}^T \mathbf{v} = 0$ 
 $\mathbf{n}^T \mathbf{v} = \mathbf{n}^T \mathbf{v} + \mathbf{v} \cdot \mathbf{v} \cdot \mathbf{v}$ 
 $\mathbf{n}^T \mathbf{v} = \mathbf{n}^T \mathbf{v} \cdot \mathbf{v} \cdot \mathbf{v}$ 
 $\mathbf{n}^T \mathbf{v} = \mathbf{n}^T \mathbf{v} \cdot \mathbf{v} \cdot \mathbf{v}$ 
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 $\mathbf{n}^T \mathbf{v} \cdot \mathbf{v} \cdot \mathbf{v} \cdot \mathbf{v}$ 

So:  $n' = M^{-T} n$ 

The inverse transpose M<sup>-T</sup> of the Modelview Matrix must be given to the shaders for transforming normals



Note: Add WeChat powcoder

- If M is pure rotation then M-T= M
- Vectors do not translate so we can and should consider only the top left 3x3 part of the matrix in this process

#### **Normalization**

Unit normals may not stay unit after transformation.
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 Transformation includes scale or shear https://powcoder.com

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# Polygon Rasterization (for OpenGL, only triangles)

We can render triangles in three different ways

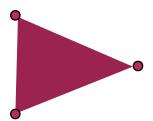
• As points: that is, only the

vertices

https://powcoder.com \*

As lines: that is only the edges

As filled in: all interior points



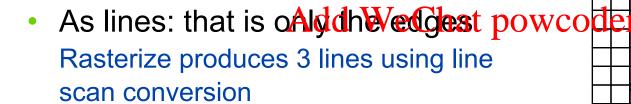
# Polygon Rasterization (for OpenGL, only triangles)

We can render triangles in three different ways

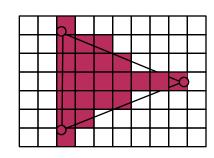
• As points: that is, only the vertices

Rasterize processing proc

https://powcoder.com



As filled in: all interior points ...coming up



# **Polygon Rasterization (for** OpenGL, only triangles)

#### Scan conversion

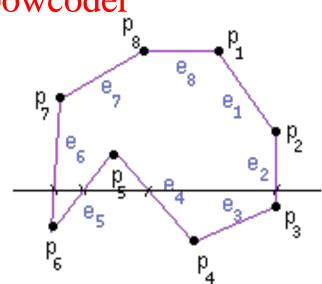
shade pixels lying within a closed polygon efficiently.
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**Algorithm** 

For each row of pixels define awcoder.com scanline through their centers

intersect each scanling with all Chat powcoder edges

- sort intersections in x
- calculate parity of intersections to determine in/out
- fill the 'in' pixels



#### **Note**

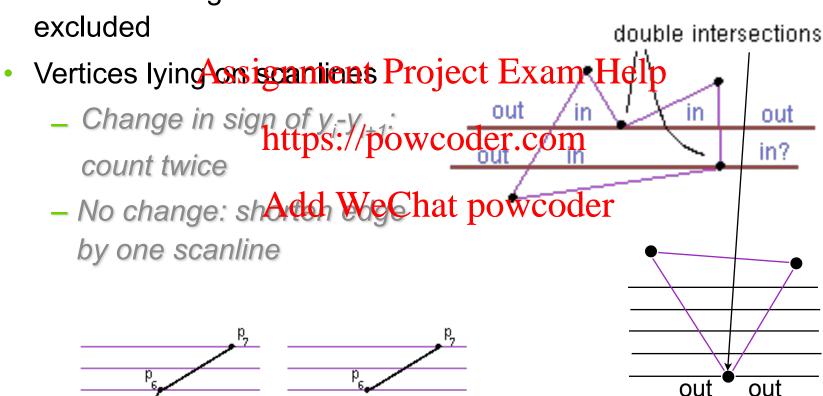
#### **During rasterization**

- Pixels centers are considered at integer values (n,k)
   Assignment Project Exam Help
- Therefore scanlines are of the of form:
   y = k, k in (1,2,\ldots,\ldots/powcoder.com
- Also, x = n, n in A(H, 2). Chat powcoder y = 3 y = 2 y = 1

$$x = 1 \ x = 2 \ x = 3$$

# Special cases (ASIDE)

Horizontal edges can be excluded



# Efficiency?

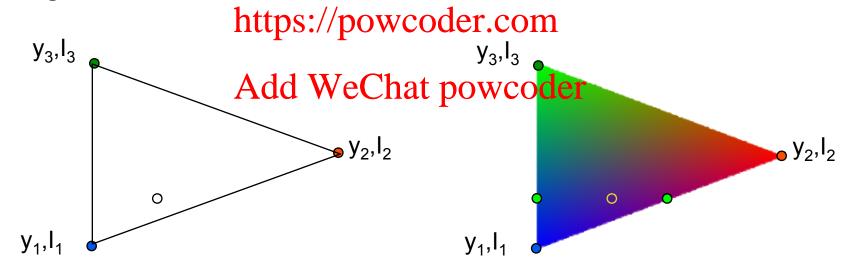
Many intersection tests can be eliminated by taking advantage of coherence between Assignment Project Exam Help adjacent scanlines.

- Edges that intersect scanline y are likely to intersect
   y+1 Add WeChat powcoder
- x changes predictably from scanline y to y+1

$$y = mx + a \rightarrow x = 1/m(y-a) \rightarrow x(y+1) = x(y) + 1/m$$

### **Attributes of Interior pixels?**

- We only have attributes for vertices
- What about the other points of the triangle Assignment Project Exam Help
- E.g. Colors:



Most common approach: interpolation

# Interpolating information along a 2D line

#### Forms and relationships

 $(x_2,y_2,I_2)$ 

Parametric from

$$x = (1 \text{ Assignment Project Exam Help} y = (1-t)y_{\text{https://powcoder.com}} y + I$$
 $I = (1-t)I_1 + tI_2.$ 

• Using ratios (for  $y_1 + d_2$ ) WeChat powcoder  $(x_1, y_1, I_1)$ 

$$\frac{I(t_a) - I(t_b)}{y(t_a) - y(t_b)} = \frac{I_1 - I_2}{y_1 - y_2}, \quad \forall t_a, t_b : t_a \neq t_b$$

• Choosing  $t_a$  and  $t_b$  we can get efficient incremental versions:

$$\frac{I_{y+1} - I_y}{(y+1) - y} = \frac{I_1 - I_2}{y_1 - y_2} \to I_{y+1} = I_y + \underbrace{I_1 - I_2}{y_1 - y_2}$$

Similarly for x

constant along line

# Bilinear Interpolation of Information during scanconversion

# Color, Normal, Texture coordinates

- Two levels of interpolation
- Along edges (green) Project Exam Help
- Along scan-line(tred) powcoder to the scanner of the scanner of
- Remember pixel centres at powcoder integer values
- First scan-line y = 0, second y = 1,...
- Pixels along scalene y:  $(x_1,y), (x_1+1,y), (x_1+2,y), ....$
- Incremental approach on both levels

# Bilinear Interpolation of Information during scanconversion

Two levels of interpolation

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 $y_2,I_2$ 

Right edge (1,2)

$$\frac{I_{r,y+1} - I_{r,y}}{(y+1) - y} = \frac{I_1 - I_2}{y_1 - y_2} \rightarrow I_r \text{https://powcoder.com} y_{1,I_{r,y+1}} y_{2,I_{r,y}} y_{2,I_{r,y}}$$
Left edge (1, 3)
$$Add \text{ WeChat powcoder} y_{1,I_1} y_{1,I_1} y_{2,I_1} y_{2,I$$

Left edge (1,3)

$$\frac{I_{l,y+1} - I_{l,y}}{(y+1) - y} = \frac{I_1 - I_3}{y_1 - y_3} \to I_{l,y+1} = I_{l,y} + \frac{I_1 - I_3}{y_1 - y_3}$$

Along a scan line

$$\frac{I_{x+1} - I_x}{(x+1) - x} = \frac{I_r - I_l}{x_r - x_l} \to I_{x+1} = I_x + \frac{I_r - I_l}{x_r - x_l}$$

# Bilinear Interpolation of Information during scanconversion

# Color, Normal, Texture coordinates

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 $y_2,I_2$ 

Right edge 
$$(1,2)$$
 https://powcoder.com  $I_x$   $I_{x+1}$   $I_{x+1}$ 

Left edge (1,3)

$$\frac{I_{l,y+1} - I_{l,y}}{(y+1) - y} = \frac{I_1 - I_2}{y_1 - y_2} \to I_{l,y+1} = I_{l,y} + \frac{I_1 - I_2}{y_1 - y_2}$$

Along a scan line

$$\frac{I_{x+1} - I_x}{(x+1) - x} = \frac{I_r - I_l}{x_r - x_l} \to I_{x+1} = I_x + \frac{I_r - I_l}{x_r - x_l}$$

# Incremental interpolation during scanconversion

#### Color, Normal, Texture coordinates

Assignment Project Exam Help

y<sub>3</sub>,l<sub>3</sub>

Right edge (1,2):

$$-\Rightarrow I \Rightarrow I \Rightarrow I + \frac{I_1 - I_2}{I_1 - I_2}$$

ght edge (1,2): 
$$\frac{I_{r,(y+1)} - I_{r,y}}{(y+1) - y} = \frac{I_1 - I_2}{y_1 - y_2} \Rightarrow I_{r,(y+1)} = I_{r,(y+1)} + I_{r$$

Left Edge (1,3):

$$\frac{I_{l,(y+1)} - I_{l,y}}{(y+1) - y} = \frac{I_1 - I_3}{y_1 - y_3} \Rightarrow I_{l,(y+1)} = I_{l,y} + \frac{I_1 - I_3}{y_1 - y_3}$$

Along scanline:

$$\frac{I_{(x+1)} - I_x}{(x+1) - x} = \frac{I_r - I_l}{x_r - x_l} \Rightarrow I_{r,(y+1)} = I_{r,y} + \frac{I_r - I_l}{x_r - x_l}$$

Constant along the line

 $y_2, l_2$ 

## How does WebGL support this?

#### Vertex shader:

varying vec4 vcolor Assignment Project Exam Help

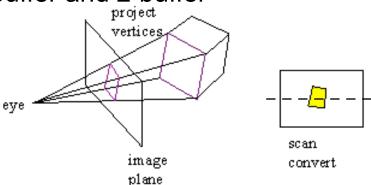
# Rasterizer knows to interpolate

vcolor

## **Z-buffer algorithm**

Although part of the positions the z-value can be viewed as a special attribute of a vertex

- for each polyganin modelnt Project Exam Help
- project vertices of polygon onto viewing plane
- for each pixel insidethesproperty of the policy of the property of the propert
- calculate pixel colour Add WeChat powcoder
- calculate pixel z-value
- compare pixel z-value to value stored for pixel in z-buffer
- if pixel is closer, draw it in frame-buffer and z-buffer
- end
- end



### **Depth Test**

- gl.enable(gl.DEPTH\_TEST);
  gl.disable(gl.DEPTH\_TEST);
  void gl.depthsignfrent Project Exam Help
- func specifies the depth companies of the specifies of
- The default value is gl.LESS: test passes if the incoming depth value is less than the stored one.
- Size of the z-buffer: canvas.height \* canvas.width floats

# **Z-fighting**

Common problem with depth test based systems

Intersections

Overlaps

Rendering
 highlights on
 top of
 geometry



## **Polygon Offset**

```
• gl.enable(gl.POLYGON_OFFSET_FILL);
gl.enable(gl.POLYGON_OFFSET_LINE);
gl.enable(gl.POLYGON_OFFSET_POINT);
Assignment Project Exam Help
```

- void gl.polygohtps: epowcoder.com tor, Glfloat units);

  Add WeChat powcoder
- Offsetting the z-values before depth comparison
- Useful for rendering hidden-line images, for applying decals to surfaces, and for rendering solids with highlighted edges
- see online manual

## Depth Value Functions (aside)

 void gl.depthRangef(gl.FLOAT nearVal, gl.FLOAT farVal);

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- After clipping and division by w, depth coordinates range from -1 to 1, corresponding to the pre-provided elipping planes. gl.depthRange specifies a linear mapping of the normalized depth coordinates in this range to window depth coordinates of the actual depth buffer implementation, window coordinate depth values are treated as though they range from 0 through 1 (like color components). Thus, the values accepted by gl.depthRange are both clamped to this range before they are accepted.
- The setting of (0,1) maps the near plane to 0 and the far plane to 1.
   With this mapping, the depth buffer range is fully utilized.

# Pixel Region filling algorithms

Scan convert boundary Fill in regions
Assignment Project Exam Help https://powcoder.com 2D paint programs Add WeChat powcoder

http://www.cs.unc.edu/~mcmillan/comp136/Lecture8/areaFills.html

# BoundaryFill

```
boundaryFill(int x, int y, int fill, int boundary) {

    if ((x < 0) || (x >= raster.width)) return;

    if ((y < 0) || (Assister height) Project Exam Help

    int current = raster.getPixel(x, y);

    if ((current != boundary) & (current != fill)) {
        raster.setPixel(fill, LXP); // POWCOder.com

    boundaryFill(x+1, y, fill,boundary);

        boundaryFill(x, Attill, Wordaryat powcoder

        boundaryFill(x-1, y, fill, boundary);

        boundaryFill(x, y-1, fill, boundary);

    }
}
```

#### Flood Fill

```
public void floodFill(int x, int y, int fill, int old)
     if ((x < 0) || (x >= raster.width)) return;
     if ((y < 0) || (y >= raster.height)) return;

if (raster.getPixel(x, y) == old) {
         raster.setPixel(fill, x, y); WeChat powcoc floodFill(x+1, y, fill, old);
         floodFill(x, y+1, fill, old);
         floodFill(x-1, y, fill, old);
         floodFill(x, y-1, fill, old);
```

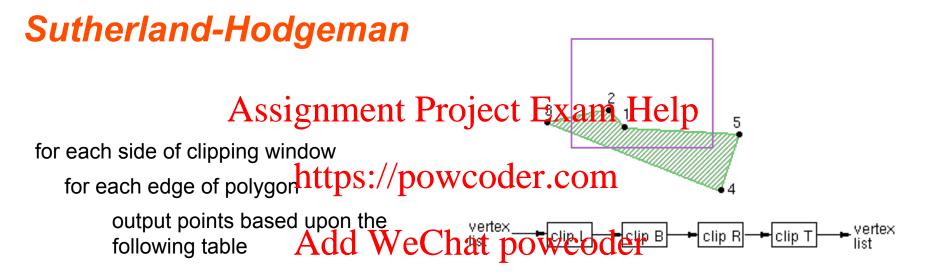
# **Adjacency**

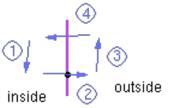
4-connected 8 connected

Assignment Project Exam Help

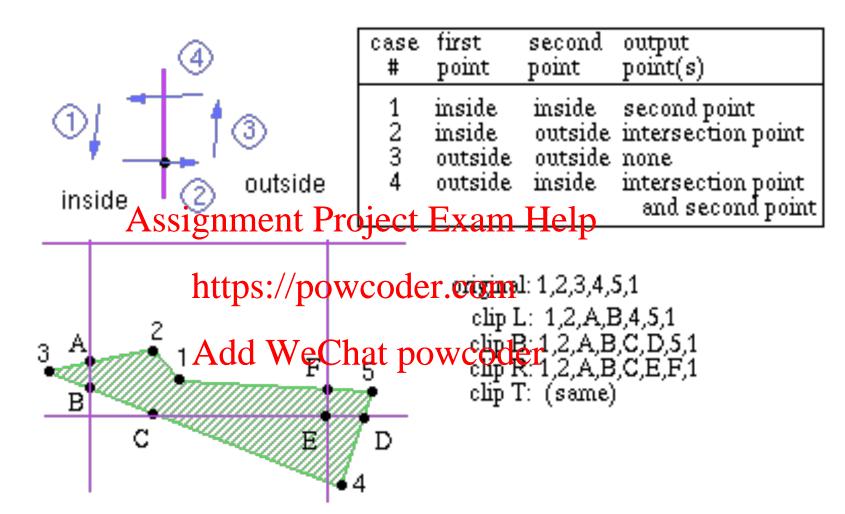
https://powcoder.com
Four-connected
neighborhood
Add WeChat powcoder
Eight-connected
neighborhood

# Polygon clipping (2D): Aside





case	first	second	output
#	point	point	point(s)
1 2 3 4	inside inside outside outside	outside outside	



## Outcodes for trivial reject/accept

[Hill 389] A vertex outcode consists of four bits: TBRL, where: T is set if y > top, Assignment Project Exam Help 1000 1010 B is set if y < bottom, https://powcoder.com R is set if x > right, and L is set if x < left. Add WeChat powcoder 0010 0000 Trivial accept: all vertices are inside (all outcodes are 0000, bitwise OR) Trivial reject: all vertices are outside 0101 0100 0110 with respect to any given side(bitwise AND is not 0000)