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Polymorphic Higher-Order Programming

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CSI 3120

Amy Felty

University of Ottawa

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Author David Walker, updated by Amy Felty

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<https://powcoder.com> Some Design & Coding Rules

- *Laziness* can be a really good force in design.
- Never write the same code twice
 - factor out the common bits into a reusable procedure.
 - better, use someone else's (well-tested, well-documented, and well-maintained) procedure.
- Why is this a good idea?
 - why don't we just cut-and-paste snippets of code using the editor instead of creating new functions?

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- Why is this a good idea?
 - why don't we just cut-and-paste snippets of code using the editor instead of creating new functions?
 - find and fix a bug in one copy, have to fix in all of them.
 - decide to change the functionality, have to track down all of the places where it gets used.

<https://powcoder.com> Factoring Code in OCaml

Consider these definitions: [Assignment Project Exam Help](#)

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```
let rec inc_all (xs:int list) : int list =  
  match xs with  
  | [] -> []  
  | hd::tl -> (hd+1)::(inc_all tl)
```

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```
let rec square_all (xs:int list) : int list =  
  match xs with  
  | [] -> []  
  | hd::tl -> (hd*hd)::(square_all tl)
```

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let rec inc_all (xs:int list) : int list =  
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```
let rec square_all (xs:int list) : int list =  
  match xs with  
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  | hd::tl -> (hd*hd)::(square_all tl)
```

The code is almost identical – factor it out!

<https://powcoder.com> Factoring Code in OCaml

[Assignment Project Exam Help](#)
A *higher-order* function captures the recursion pattern:

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```
let rec map (f:int->int) (xs:int list) : int list =  
  match xs with  
  | [] -> []  
  | hd::tl -> f hd :: map f tl
```

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Uses of the function:

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```
let inc x = x+1  
let inc_all xs = map inc xs
```

<https://powcoder.com> Factoring Code in OCaml

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Uses of the function:

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```
let inc x = x+1  
let inc_all xs = map inc xs  
  
let square y = y*y  
let square_all xs = map square xs
```

Writing little
functions like inc
just so we can call
map is a pain.

<https://powcoder.com> Factoring Code in OCaml

A *higher-order* function captures the recursion pattern:

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  match xs with  
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```

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Uses of the function:

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```
let inc_all xs = map (fun x -> x + 1) xs  
  
let square_all xs = map (fun y -> y * y) xs
```

We can use an
anonymous
function
instead.

Originally,
Church wrote
this function
using λ instead
of **fun**:
($\lambda x. x+1$) or
($\lambda y. y*y$)

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Here's an annoying thing

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```
let rec map (f:int->int) (xs:int list) : int list =  
  match xs with  
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```

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What if I want to increment a list of floats?

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Alas, I can't just call this map. It works on ints!

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```
let rec mapfloat (f:float->float) (xs:float list) :  
  float list =  
  match xs with  
  | [] -> []  
  | hd::tl -> (f hd)::(mapfloat f tl);;
```

<https://powcoder.com> Turns out

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```
let rec map f xs =  
  match xs with  
  | [] -> []  
  | hd::tl -> (f hd)::(map f tl)  
  
let ints = map (fun x -> x + 1) [1; 2; 3; 4]  
  
let floats = map (fun x -> x +. 2.0) [3.1415; 2.718]  
  
let strings = map String.uppercase_ascii ["sarah"; "joe"]
```

<https://powcoder.com> Type of the undecorated map?

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```
let rec map f xs =  
  match xs with  
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  | hd::tl -> (f hd)::(map f tl)  
  
map : ('a -> 'b) -> 'a list -> 'b list
```

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map : ('a -> 'b) -> 'a list -> 'b list
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We often use greek letters like α or β to represent type variables.

Read as:

- for any types 'a and 'b,
- if you give map a function from 'a to 'b,
- it will return a function
 - which when given a list of 'a values
 - returns a list of 'b values.

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We can say this explicitly

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```
let rec map (f:'a -> 'b) (xs:'a list) : 'b list =  
  match xs with  
  | [] -> []  
  | hd::tl -> (f hd)::(map f tl)
```

map : ('a -> 'b) -> 'a list -> 'b list

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The OCaml compiler is smart enough to figure out that this is the *most general* type that you can assign to the code.

We say map is *polymorphic* in the types 'a and 'b – just a fancy way to say map can be used on any types 'a and 'b.

Java generics derived from ML-style polymorphism (but added after the fact and more complicated due to subtyping)

- Map is a *higher-order function* that captures a very common *recursion pattern*
- We can write clear, terse, reusable code by exploiting:
 - higher-order functions
 - anonymous functions
 - first-class functions
 - polymorphism