For a short humorous talk on languages without terms trangitions:

https://powcoder.com https://www.destroyallsoftware.com/talks/wat Add WeChat powcoder

[Broader point: No one (few people) knows what their programs do in untyped languages.]

Type Checking Basics

https://powcoder.com

Add WeChat powcoder CSI 3120

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Last Time

Functional programming history

- Church & the lambda calculus
- Scheme
- ML (OCaml)
- Modern times:sftgfiloierr Project Texaguitelp

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OCaml

- Functional language determost at optomore day analyzing old data and producing new, immutable data
- Simple, typed programming language based on the lambda calculus
- Immutable data is the default; mutable data is possible (imperative, object-oriented)

Type Checking

- Every value has a type and so does every expression
- This is a concept that is familiar from Java but it becomes more important when programming in a functional language
- The type of an expression is determined by the type of its subexpression signment Project Exam Help
- We write (e:t) to say that expression e has type t. eg: https://powcoder.com

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2 : int "hello" : string

2 + 2 : int "I say " ^ "hello" : string

- There are a set of simple rules that govern type checking
 - programs that do not follow the rules will not type check and
 OCaml will refuse to compile them for you (the nerve!)
 - at first you may find this to be a pain ...

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- But types are a great thing:
 - they help us think about now to construct our programs
 - they help us find stupid economic studies economic economic studies economic economic studies economic economic economi
 - they help us track down compatibility errors quickly when we edit and maintain our code
 - they allow us to enforce powerful invariants about our data structures

Example rules:

```
(1) 0: int (and similarly for any other integer constant n)
```

(2) "abc": string (and similarly for any other string constant "...")

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Example rules:

```
(1) 0: int (and similarly for any other integer constant n)

(2) "abc": string (and similarly for any other string constant "...")

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(3) if e1: int and e2: int (4) if e1: int and e2: int then e1 + e2: int https://powcodetheorg1 * e2: int
```

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Example rules:

then e1 ^ e2 : string

then string_of_int e : string

Example rules:

2: int and 3: int.

```
(1)
     0 : int
                       (and similarly for any other integer constant n)
(2)
    "abc": string (and similarly for any other string constant "...")
                 Assignment Project Exam Help
                            (4) if e1: int and e2: int
    if e1: int and e2: int
(3)
    then e1 + e2 : int <a href="https://powcoder.heore1">https://powcoder.heore1</a> * e2 : int
     if e1: string and exching eChalopowcoder
(5)
     then e1 ^ e2 : string
                                             then string_of_int e : string
  Using the rules:
```

(By rule 1)

Example rules:

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  Using the rules:
                       (By rule 1)
     2: int and 3: int.
```

Therefore, (2 + 3): int (By rule 3)

Example rules:

5 : int

```
(1)
     0 : int
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(2)
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  Using the rules:
                       (By rule 1)
     2: int and 3: int.
     Therefore, (2 + 3): int (By rule 3)
```

(By rule 1)

Example rules:

```
(1)
     0 : int
                      (and similarly for any other integer constant n)
(2)
    "abc": string (and similarly for
                 Assignment
                                      FYI: This is a formal proof
    if e1: int and e2: int
(3)
                                      that the expression is well-
    then e1 + e2 : int https://
                                                  typed!
     if e1: string and eActive Ch
(5)
     then e1 ^ e2 : string
                                                  ring_or_init e : string
  Using the rules:
                               (By rule 1)
     2: int and 3: int.
                            (By rule 3)
     Therefore, (2 + 3): int
                               (By rule 1)
     5 : int
     Therefore, (2 + 3) * 5 : int (By rule 4 and our previous work)
```

Example rules:

then e1 ^ e2 : string and eAcctring eChaloponneconter

then string_of_int e : string

Another perspective:

rule (4) for typing expressions says I can put any expression with type int in place of the ????

????? * ???? : int

Example rules:

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7 * ????? : int

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    (5) if e1: string and eAddingeChat6powcoder
```

Another perspective:

then e1 ^ e2 : string

```
rule (4) for typing expressions says I can put any expression with type int in place of the ????
```

7 * (add_one 17) : int

then string_of_int e : string

 You can always start up the OCaml interpreter to find out a type of a simple expression:

\$ ocaml Version 4.07.0

https://powcoder.com

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 You can always start up the OCaml interpreter to find out a type of a simple expression:

```
$ ocaml Version 4.07.0
# 3 + 1; https://powcoder.com

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```

 You can always start up the OCaml interpreter to find out a type of a simple expression:

```
$ ocaml Version 4.07.0

# 3 + 1; https://powcoder.com
- : int = 4

# Add WeChat powcoder

press
return
and you
find out
the type
and the
value
```

 You can always start up the OCaml interpreter to find out a type of a simple expression:

```
$ ocamsignment Project Exam Help
Ocaml Version 4.07.0

# 3 + 1; https://powcoder.com
- : int = 4

# "hello Add Wechat' powcoder
- : string = Wechat' powcoder
# "
```

press return and you find out the type and the value

 You can always start up the OCaml interpreter to find out a type of a simple expression:

```
$ ocame Project Exam Help
Ocame Version 4.07.0

# 3 + 1; https://powcoder.com
-: int = 4

# "hello Add Wechat' powcoder
-: string = Wechat' powcoder
# #quit;;
$
```

Example rules:

```
(1) 0: int (and similarly for any other integer constant n)

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(3) if e1: int and e2: int (4) if e1: int and e2: int then e1 + e2: int https://powcodetheore1 * e2: int

(5) if e1: string and eAdthive Chatepower then e1 ^ e2: string then string_of_int e: string
```

Violating the rules:

```
"hello" : string
1 : int
1 + "hello" : ??
(By rule 2)
(By rule 1)
(NO TYPE! Rule 3 does not apply!)
```

Violating the rules:

```
# "hello" + 1;;
Error: This expression has type string but an expression weignment Projecty Examt Help
```

https://powcoder.com

- The type error message tells you the type that was expected and the type that it inferred for your subexpression
- By the way, this was one of the nonsensical expressions that did not evaluate to a value
- It is a good thing that this expression does not type check!

"Well typed programs do not go wrong" Robin Milner, 1978

Violating the rules:

```
# "hello" + 1;;
Error: This expression has type string but an expression weignment Projecty Examt Help
```

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A possible fix:

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```
# "hello" ^ (string_of_int 1);;
- : string = "hello1"
```

 One of the keys to becoming a good ML programmer is to understand type error messages.

Example Type-checking Rules

```
if e1: booksignment Project Exam Help
and e2: t and e3: t (the same type t, for some type t)
then if e1 then e2 else e3: t (that same type t)
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```

Type errors for if statements can be confusing sometimes.
 Example: We create a string from s, concatenating it n times:

```
let rec concatn s n =
if n <= 0 then

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else

https://fowcoder.com<sup>1))</sup>
```

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https://fowcotter.com<sup>1))</sup>
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OCaml says: Add WeChat powcoder

```
Error: This expression has type int but an expression was expected of type string
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Assignment Project Exam Help
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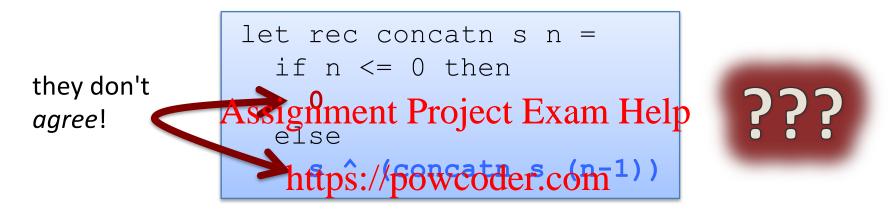
https://powcoder.com1))
```

???

OCaml says: Add WeChat powcoder

```
Error: This expression has type int but an expression was expected of type string
```

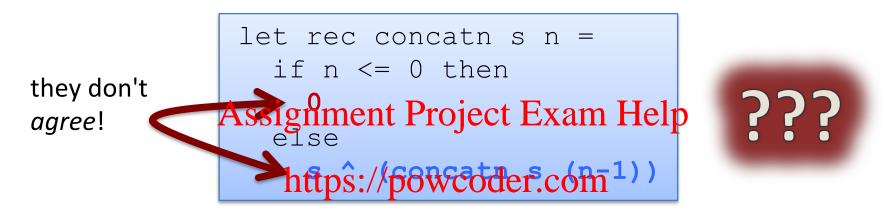
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OCaml says: Add WeChat powcoder

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Error: This expression has type int but an expression was expected of type string
```

Type errors for if statements can be confusing sometimes.
 Example. We create a string from s, concatenating it n times:



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The type checker points to the correct branch as the cause of an error because it does not AGREE with the type of an earlier branch.

Really, the error is in the earlier branch.

Moral: Sometimes you need to look in an earlier branch for the error even though the type checker points to a later branch.

The type checker doesn't know what the user wants.

A Tactic: Add Typing Annotations

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```
Error: This expression has type int but an expression was expected of type string
```

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EXCEPTIONS: DO THEY CAUSE PROGRAMS TO "GO WRONG"?

What about this expression:

```
# 3 / 0 ;;
Exception: Division_by_zero.
```

• Why doesn't the Metyperthet Rer do us the expression will raise an exception? expression will raise an exception?

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What about this expression:

```
# 3 / 0 ;;
Exception: Division_by_zero.
```

- Why doesn't the Metype the Exercication as the expression will raise an exception?
 - In general, detecting a divide-by-zero error requires we know that the divisor evaluated to W.e Chat powcoder
 - In general, deciding whether the divisor evaluates to 0 requires solving the halting problem:

```
# 3 / (if turing_machine_halts m then 0 else 1);;
```

 There are type systems that will rule out divide-by-zero errors, but they require programmers to supply proofs to the type checker

Isn't that cheating?

"Well typed programs do not go wrong" Robin Milner, 1978

(3 / 0) is well typed. Does it "go wrong?" Answer: No. Assignment Project Exam Help

"Go wrong" is a technical term meaning of have no defined semantics." Raising an exception is perfectly well defined semantics, which we ded reachable we can handle in ML with an exception handler.

So, it's not cheating.

Type Soundness

"Well typed programs do not go wrong"

Programming languages with this property have sound type systems. They are called safe languages.

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Safe languages are generally immende to buffer overrun vulnerabilities, uninitialized pointer vulnerabilities, etc. (but not immune to all bugs!) Chat powcoder

Safe languages: ML, Java, Python, ...

Unsafe languages: C, C++, Pascal

Well typed programs do not go wrong



Robin Milner

Turing Award, 1991

"For three distinct and complete achievements:

- 1. LCF, the mechanization of Scott's Logic of Computable Functions, probably the first theoretically based yet practical tool for machine assisted proof

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- 2. ML, the first language to include polymorphic type inference together with a type-safe polymorphic first language to include polymorphic type inference together with a type-safe polymorphic first language to include polymorphic type inference together with a type-safe polymorphic type inference together with
- 3. CCS, Agener Wheel topower der

In addition, he formulated and strongly advanced full abstraction, the study of the relationship between operational and denotational semantics."

"Well typed programs do not go wrong" Robin Milner, 1978 Assignment Project Exam Help

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SUMMARY

OCaml

OCaml is a *functional* programming language

- Java gets most work done by modifying data
- OCaml gets most work done by producing new, immutable data

Assignment Project Exam Help OCaml is a *typed* programming language

- the type of an expression correctly predicts the kind of value the expression will generate when it is executed
- there are systematic rules defining when any expression (or program) type checks
 - these rules actually form a formal logic ... it is not a coincidence that languages like ML are used inside theorem provers
- the type system is sound; the language is safe