3D Hierarchical Modelling

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Intended Learning Outcomes

- Understand the need of hierarchical structuring for building articulated 3D objects

- Able to compute the relative coordinate transform between component parts

- Able to represent an articulated 3D object as a hierarchical structure using OpenGL

Problem:

- Given a large number of graphics models which form parts of a whole object, it is cumbersome to animate each part by individual commands

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Example : Animate a car moving at a speed of 20 miles and in direction (2, 3, 4)

```
main ()
{
    float s     = 20.0; /* speed */
    float d[3] = {2.0, 3.0, 4.0}; /* direction */

    draw_chassis (s, d);

    draw_right_front_wheel (s, d);
    draw_left_front_wheel  (s, d);
    draw_right_rear_wheel  (s, d);
    draw_left_rear_wheel   (s, d);

}
```
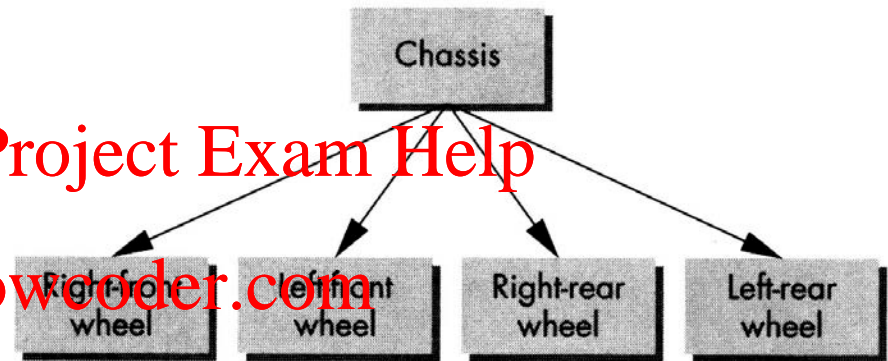

Tree with directed edge

Bad Programming - Redundancy: the 4 draw wheel functions can be replaced by one function

Introduction of hierarchical structures

- Use *relative transformation* to link the movements of different parts

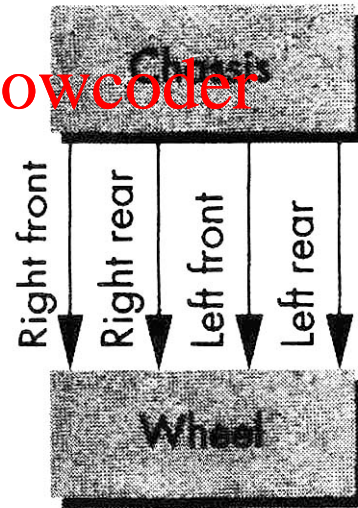- Use a single function for a unique (single) part

Directed Acyclic Graph (DAG)

- DAG is a graph with directed arc but no cycle

- It is a tree but additional allows more than one arc from one node to another node

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Revised program

```
main ()
{
    float s = 20.0;
    float d[3] ={2.0, 3.0, 4.0};
    float w = 2.0, l = 4.0;      // width and length of the car

    draw_chass (s, d);

    glTranslatef ( w/2 , l/2, 0 );   // position the right front wheel
    draw_wheel (s, d);
    glTranslatef ( -w,    0,  0 );   // position the left front wheel
    draw_wheel (s, d);
    glTranslatef (  0,    -l , 0 );   // position the left rear wheel
    draw_wheel (s, d);
    glTranslatef ( w,    0,   0  );    // position the right rear wheel
    draw_wheel (s, d);
}
```

Let the initial coordinate system be the centroid of the car

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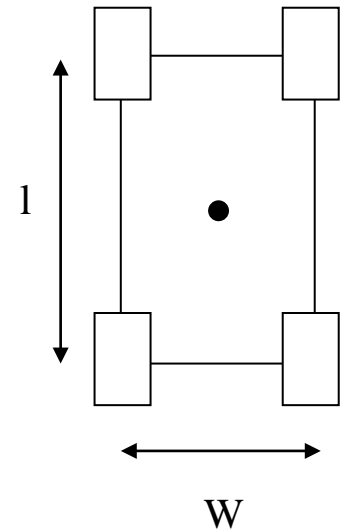
We can make it more systematic by formally introducing coordinate system change, which we do below

Moving a Robot Arm – a 3 level hierarchy

Parts : **base B** (cylinder),

lower arm La (rectangular box)

upper arm Ua (rectangular box)
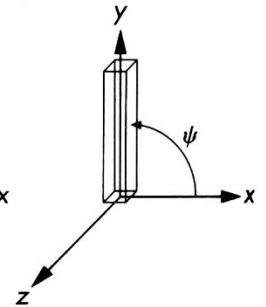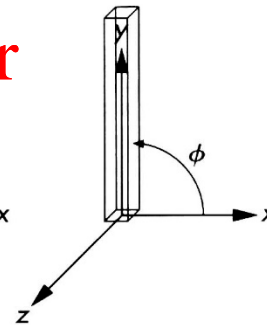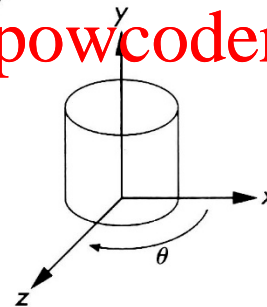
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Arm has 3 degree of freedom:

B   rotate about Y by θ

La   rotate about Z by ϕ

Ua   rotate about Z by ψ

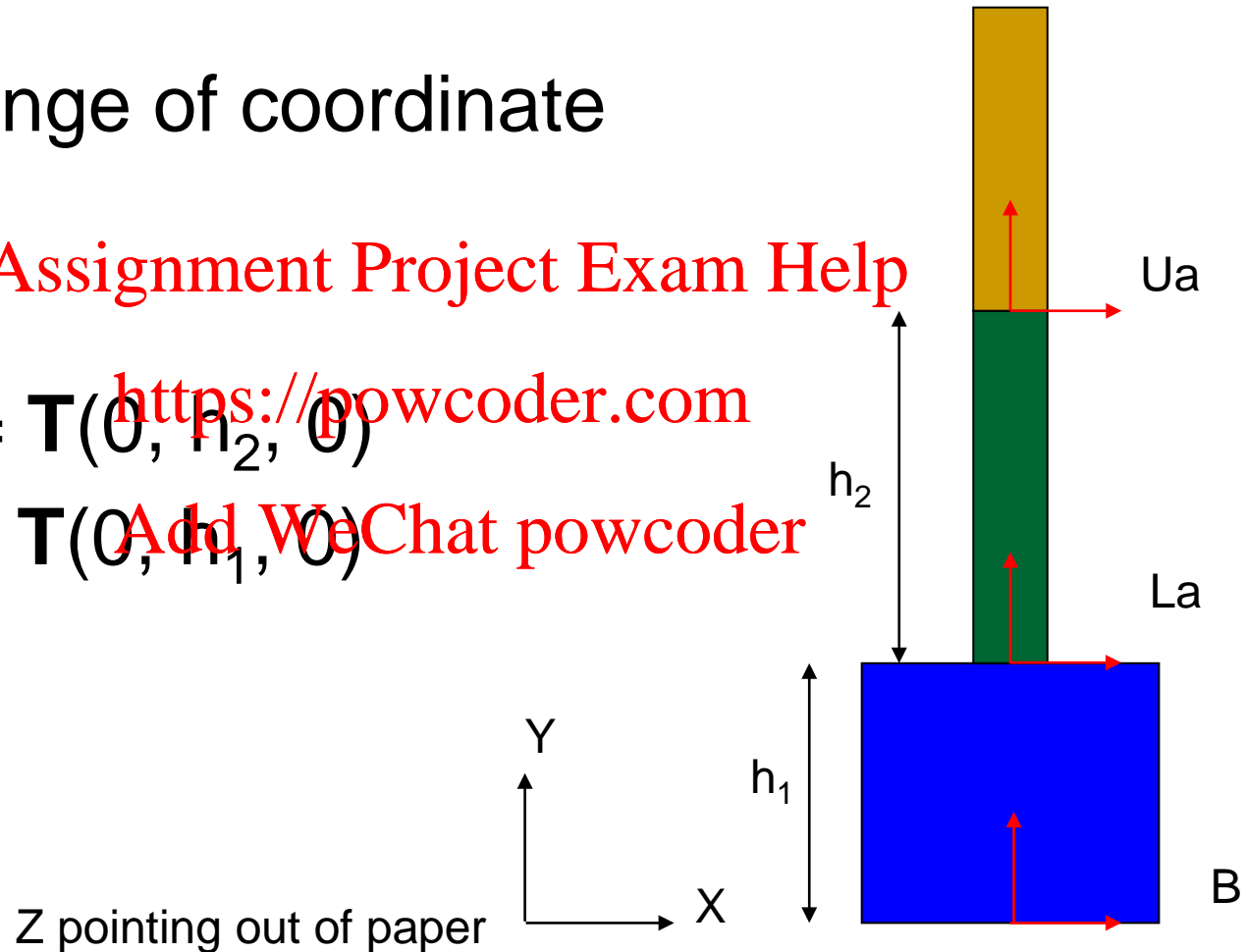https://powcoder.com

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Relative Coordinate Transformations

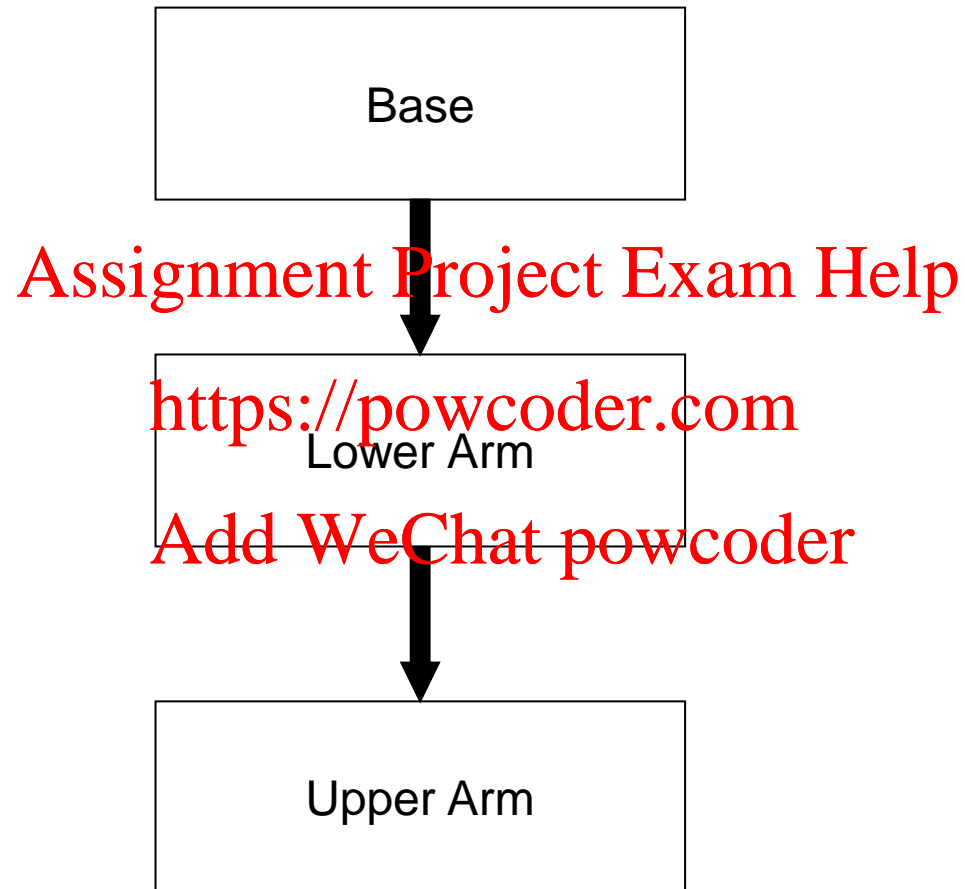- Use Change of coordinate system:

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- $\mathbf{M}_{La \leftarrow Ua} = \mathbf{T}(0, h_2, 0)$

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- $\mathbf{M}_{B \leftarrow La} = \mathbf{T}(0, h_1, 0)$

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Ua

h_2

La

Y

h_1

X

Z pointing out of paper

B

DAG

Base

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Lower Arm

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Upper Arm

Write a program to …

- Rotate the robot arm about its base by θ, then about its lower arm by ϕ, then about its upper arm by ψ

- when rotating the whole arm, everything should move; but when rotating the lower arm, only it and the upper arm should move; when rotating the upper arm, only the upper arm should move.

- Solve this using a hierarchy concept

Program

robot_arm ()
{

    glRotatef (theta, 0.0, 1.0, 0.0);   // $\mathbf{R}_y(\theta)$ *rotate the whole robot arm*

    // each point of whole robot arm will be pre-multiplied by $\mathbf{R}_y(\theta)$
    base ();

    glTranslatef (0.0, h_1, 0.0); // $\mathbf{M}_{B \leftarrow La}$ *changes lower arm coord. sy. to base coord. sy.*
    glRotatef (phi, 0.0, 0.1, 1.0); // $\mathbf{R}_z(\phi)$ *rotate the lower arm*

    // each point of lower arm will be pre-multiplied by $\mathbf{R}_y(\theta)\mathbf{T}(0,h_1,0)\mathbf{R}_z(\phi)$
    lower_arm ();

    glTranslatef (0.0, h_2, 0.0); // $\mathbf{M}_{La \leftarrow Ua}$ *changes upper arm coord. sy. to lower arm coord. sy.*
    glRotatef   (psi, 0.0, 0.0, 1.0);

    // each point of upper arm will be pre-multiplied by $\mathbf{R}_y(\theta)\mathbf{T}(0,h_1,0)\mathbf{R}_z(\phi)\mathbf{T}(0,h_2,0)\mathbf{R}_Z(\psi)$
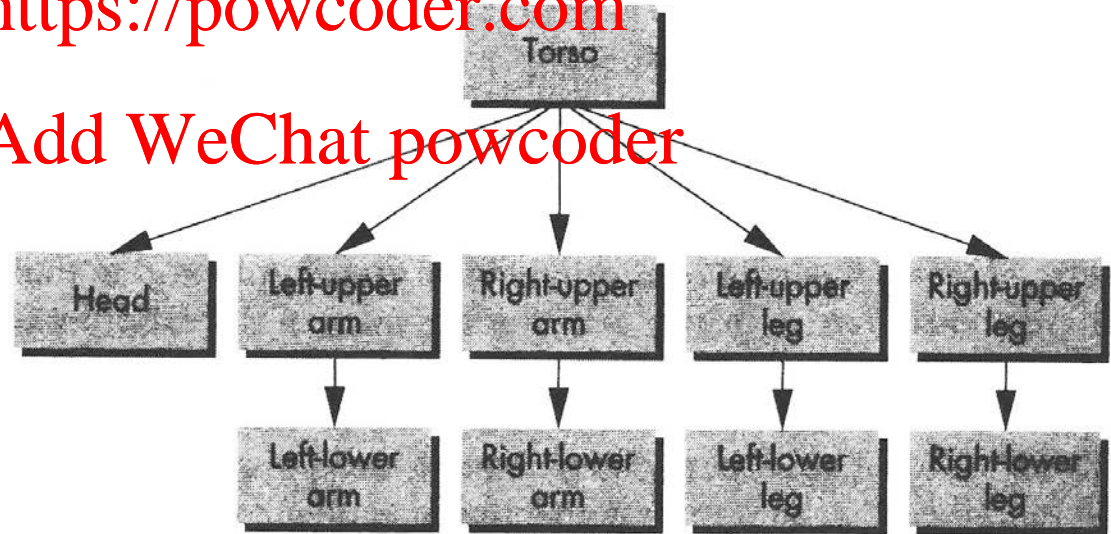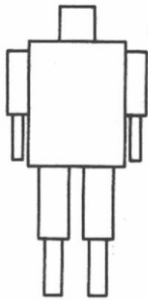   *upper_arm ();*

}

Moving a Robot

- Need to organize the hierarchy better
- Solution: use *glPushMatrix* and *glPopMatrix* to store and retrieve intermediate composite relative transformations

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Program

```
Robot ()
{
        glPushMatrix ();
        torso;

        glTranslate ...
        glRotate ...
        head ();

        glPopMatrix ();                // go back to the node of the torso
         glPushMatrix ();

        glTranslate ...                // similar technique used here as that
        glRotate ...                   // used in example 2
        left_upper_arm ();
        glTranslate ...
        glRotate ...
        left_lower_arm ();

        glPopMatrix ();                // go back to the node of the torso
         glPushMatrix ();

        glTranslate ...
        glRotate ...
        right_upper_arm ();

                ...
}
```

References

- Our exposition follows:

  E. Angel, Interactive Computer Graphics: A Top-down Approach Using OpenGL, 5th Ed. (2009), Ch. 10.1-10.4

- Ch. 11 of text provides an alterative reference.