

A Mathematical formulas

$$\text{Q-function : } Q(x) = \frac{1}{\sqrt{2\pi}} \int_x^\infty e^{-\frac{t^2}{2}} dt \quad (1)$$

$$Q(x) = 1 - Q(-x) \quad (2)$$

$$\text{Error function : } \operatorname{erf}(x) = \frac{2}{\sqrt{\pi}} \int_0^x e^{-t^2} dt \quad (3)$$

$$\operatorname{erfc}(x) = 1 - \operatorname{erf}(x) \quad (4)$$

$$Q(x) = \frac{1}{2} \operatorname{erfc}\left(\frac{x}{\sqrt{2}}\right) \quad (5)$$

$$\text{PDF of } \mathcal{N}(\mu, \sigma^2) : f_X(x) = \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{(x-\mu)^2}{2\sigma^2}} \quad (6)$$

$$\text{CDF of } \mathcal{N}(\mu, \sigma^2) : F_X(x) = 1 - Q\left(\frac{x-\mu}{\sigma}\right) \quad (7)$$

$$\int_{-\infty}^{a_1} \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{(x-\mu)^2}{2\sigma^2}} dx = Q\left(\frac{\mu - a_1}{\sigma}\right) \quad (8)$$

$$\int_{a_2}^{\infty} \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{(x-\mu)^2}{2\sigma^2}} dx = Q\left(\frac{a_2 - \mu}{\sigma}\right) \quad (9)$$

$$\int_0^\infty Q(\sqrt{ax}) e^{-x} dx = \frac{1}{2} \left(1 - \sqrt{\frac{a}{2+a}}\right); a > 0 \quad (10)$$

$$\sqrt{\frac{x}{1+x}} \approx 1 - \frac{1}{2x} \text{ for large } x \quad (11)$$

$$e^x = \sum_{k=0}^{\infty} \frac{x^k}{k!} \quad (12)$$

$$\int_0^\infty e^{-ax} dx = \frac{1}{a}; a > 0 \quad (13)$$

$$\int_0^t e^{-ax} dx = \frac{1 - e^{-at}}{a}; a > 0 \quad (14)$$