Assignment Project Exam Help Public-Key-Crypto

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Review: Integrity

Problem: Sending a message over an untrusted channel without being changed

Provably-secure solution: Random function

Practical solution:



e.g. "Attack at dawn", 628369867...

Assignment Project Exam Help Pseudorandom function (PRF)

Input: hatybitrappytengdlarkcom

Output: fixed-length value

a random function, unless know k

Real-world use:

Message authentication codes (MACs)

built on cryptographic hash functions

Popular example: HMAC-SHA256_k(m)

[Cautions?!]

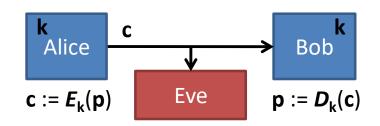
Review: Confidentiality

Problem: Sending message in the presence of an eavesdropper without revealing it

Provably-secure solution: One-time pad

Practical solution:

Pseudorandom generator (PRG)



Inputssigfixed of Patheet Exam Help

Output: arbitrary-length stream

Secure if the stice by inclusting wishable from a random stream, unless know k Add WeChat powcoder

Real-world use:

Stream ciphers (can't reuse k)

Popular example: AES-128 + CTR mode

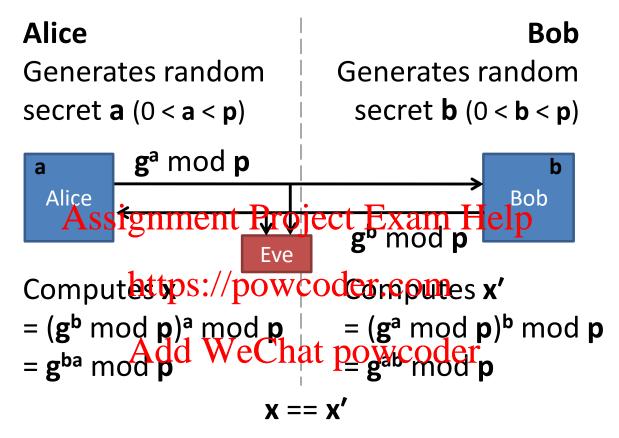
Block ciphers (need padding/IV)

Popular example: AES-128 + CBC mode

[Cautions?!]

Review: Diffie-Hellman Key Exchange

Lets Alice and Bob **agree on a shared secret** value by having a public conversation



Problem: Man-in-the-middle attacks



<u>Caution</u>: D-H gives you a shared secret, but don't know who's on the other end!

Suppose Alice publishes data to lots of people, and they all want to verify integrity...

Can't share an integrity key with *everybody*, or else *anybody* could forge messages

Suppose Bob wants to receive data from lots of perspectations. Help

https://pmascwdere.diacussed would require a separate key Addhyrechat.peychoperson

[What to do?]

Solution:

Public-key Crypto

So far, encryption key == decryption key "symmetric key crypto"

New idea: Keys are distinct, and you can't find one from the other

Almost always used by splitting key-pair

Aligher Propertive to the properties the other key ("public key")

https://powcoder.com Many applications

Invented 1976 by the God Hellman (earlier by Clifford Cocks of British intelligence, in secret)

Best known, most common public-key algorithm: RSA Rivest, Shamir, and Adleman 1978

Requirements for a public key crypto system to be secure

- 1. Computationally easy for B to generate a key pair: PU_b, PR_b
- 2. Computationally easy for sender A to generate the ciphertext for mesiage of: Reject Lyan Help
- 3. Computationally easy for received Byte Chacpy ptcther ciphertext: M=D(PR_b, C)
- 4. Computational infeasible to guess PR_b knowing PU_b.
- 5. Computational infeasible to recover M from PU_h and C.



A Method for Obtaining Digital Signatures and Public-Key Cryptosystems

R.L. Rivest, A. Shamir, and L. Adleman*

How RSA works

Key generation:

- 1. Pick large (say, 1024 bits) random primes **p** and **q**
- Compute N := pq
 (RSA uses multiplication mod N)
- 3. Pick e to be relatively prime to Assignment Project Exam Help
- 4. Final q = 1
- 5. Finally: Public key is (e,N)
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 Private key is (a,N)

To encrypt: $E(x) = x^e \mod N$

To decrypt: $D(x) = x^d \mod N$

Why RSA works

"It works" theorem:

```
For all 0 < x < N,
can show that D(E(x)) = x
```

Proof:

```
D(E(x)) = (xe mod pq)d mod pq
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= xa(p-1)(q-1)+1 mod pq for some a
https://powcoder.com
(because ed mod (p-1)(q-1) = 1)

Add(xwell-h)ax powdopqler

= (x(p-1)(q-1) mod pq)ax mod pq

= 1ax mod pq

(because of the fact that if p,q
are prime, then for all 0 < x < N,
x(p-1)(q-1) mod pq = 1)

= x
```

Is RSA secure?

Best known way to compute **d** from **e** is factoring **N** into **p** and **q**.

Best known factoring algorithm:

General number field sieve

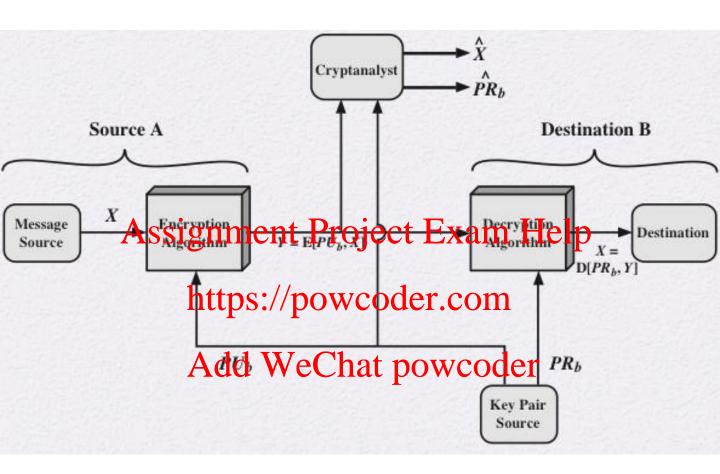
Takes more than polynomial time but less than exponential time Assignment Project Exam Help to factor **n**-bit number.

(Still taketpwa/provologierif pring are large enough and random.)

Fingers crossed...

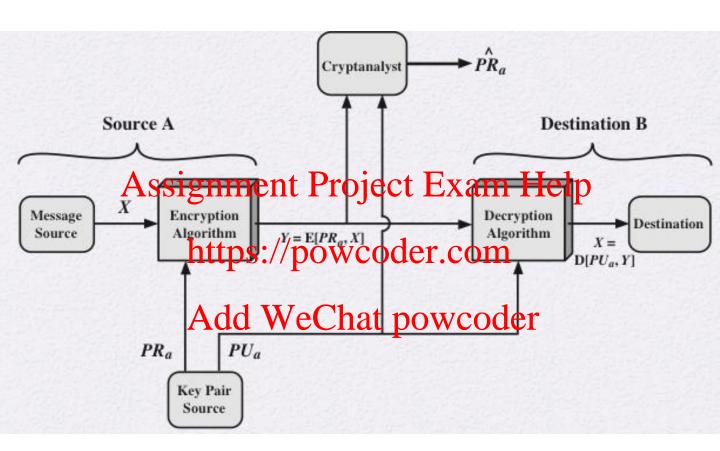
but can't rule out a breakthrough!

Signing with the public key for confidentiality or secrecy:



Does this provide integrity?

Signing with private key for integrity/authentication.



Does this provide confidentiality?

Subtle fact: RSA can be used for either confidentiality or integrity

RSA for confidentiality:

Encrypt with public key
Decrypt with private key
"your eyes only" message

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Encrypt ("sign") with private key Decrypt ("verify") with public key Adda We Chat powspderure

[What if we want both confidentiality and integrity on the same message?]

How to have both confidentiality and integrity (using RSA)?

Alice (A) wants to send a secret message M to Bob (B) so that Bob can verify that it comes from Alice.

Which specification is parte secretare? Help

- 1. E(E(NhttpR//popycoder.com
- 2. E(E(M, PU_B), PR_A)
- 3. $C=E(M, PR_A) t=E(H(C), PU_B)$
 - Send C||t
- 4. $C=E(M, PU_B)$ $t=E(H(C), PR_A)$
 - Send C||t

Review: Public-key Crypto

So far, encryption key == decryption key "symmetric key crypto"

New idea: Keys are distinct.

Public key is (e,N)

Private key is (d,N)

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To encrypt: E(x) = xe mod N

To degryptio R(x) dex.compd N

RSA for confidential: powcoder

Encrypt with public key

Decrypt with private key

RSA for integrity (digital signatures):

Encrypt ("sign") with private key
Decrypt ("verify") with public key

[Cautions?!]

RSA drawback: Performance

Factor of 1000 or more slower than AES.

Dominated by exponentiation – cost goes up (roughly) as cube of key size.

Message must be shorter than N.

[How big should the RSA keys be?]

Use in practice:

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Use RSA to encrypt a random x < N, computes k : PPRF(x), encrypt message using a symmetric cipher and key k Add WeChat powcoder Signing:

Compute **v** := PRF(**m**), use RSA to sign a carefully padded version of **v** (many gotchas!)

Almost always should use crypto libraries to get the details right

True or false:

Public-key encryption is a generalpurpose technique that has made symmetric encryption obsolete

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True or false:

Key distribution is trivial when using public-key encryption, compared to the cumbersome handshaking involved with key distribution centers for symmetric encryption.

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Attacks against RSA

- 1. Brute force: trying all possible private keys
- 2. Mathematical attacks: factoring
- 3. Timing attacks: using the running times of a stacks: using the running
- 4. Hardware posed fault attack: induce faults in hardware to generate digital signatures
- Chosen plaintext attack on unpadded RSA

Exercise

Suppose Bob uses RSA crypto with a very large modulus **n** for which the factorization cannot be found in a reasonable amount of time.

Suppose Alice sends a message to Bob by representing each appliabet letter as an integer between 0 and 25 (A->0, ..., Z->25) and then encrypting each humber separately using RSA with large e and large n.

Is this method secure?

If yes, why?

If not, how to efficiently attack this encryption method?

Solution:

For a set of message block values SM = {0, 1, 2, ..., 25}. The set of corresponding ciphertext block values SC = {0^e mod N, 1^e mod N, ..., 25^e mod N}, and can be computed by every with the knowledge of the public keyvoto below

The most efficient attack of to compute M^e mod N for all possible values of M, then create a look-up table with a ciphertext as an index, and the corresponding plaintext as a value of the appropriate location in the table.

Two subtle "textbook" RSA problems:

- 1. For small e and m:

 m^e mod N == m^e

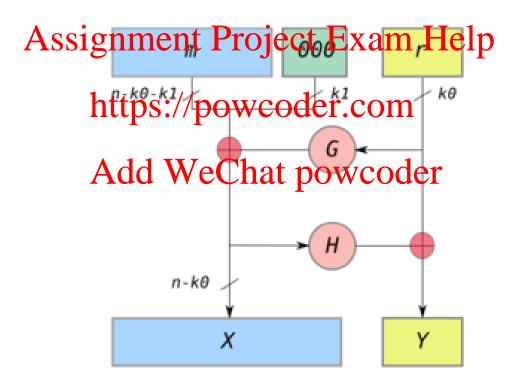
 Trivightede Trivite Exam Help
- 2. If m isteriosem for a small set, easy to go firm a pointertext is a given message (anyone can encrypt!)

 Chosen plaintext attack

Solution: RSA Padding

Need to make sure m is as large enough to wrap around N

Need to *randomize* before encryption



So Far:

The Security Mindset

Message Integrity

Confidentiality

Key Exchange

Building a Secure Channel Assignment Project Exam Help

Public Key Crypto https://powcoder.com

Next Weeki WeChat powcoder

Begin Web Security Unit

HTTPS: Secure channels for the web