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ECEN 4133

FEB 4, 2021

Shared key limitations

Suppose Alice publishes data to lots of people, and they all want to verify integrity...

Can't share an integrity key with *everybody*, or else *anybody* could forge messages

Suppose Bob wants to receive data from lots of people, confidentially...

Schemes we've discussed would require a separate key shared with each person https://powcoder.com

[What to do?]

Public-key crypto

So far, encryption key == decryption key "symmetric key crypto"

New idea: Keys are distined, saignament filtojecto Extantilelelp

Almost always used by splitting https://powcoder.com
Alice keeps one key private ("private key")
Publishes the other key ("public key")
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Invented in 1976 by Diffie and Hellman (earlier by Clifford Cocks of British intelligence, in secret)

First popular public key algorithm: RSA Rivest, Shamir, and Adleman 1978

Requirements for a public key crypto system to be secure

- Computationally easy for B to generate a key pair: PU_b, PR_b
- Computationally easy for sender A to generate the ciphertext for message M: $C=E(PU_b, M)$ Assignment Project Exam Help Computationally easy for receiver B to decrypt the ciphertext: $M=D(PR_b, C)$
- Computational infeasible to steps / powispler.com
- Computational infeasible to recover W from PU and Coder

RSA



A Method for Obtaining Digital Signatures and Public-Key Cryptosystems

R.L. Rivest, A. Shamir, and L. Adleman*

How RSA works

Key generation:

- 1. Pick large (say, 1024 bits) random primes **p** and **q**
- 2. Compute N := pq Assignment Project Exam Help (RSA uses multiplication mod N)
- 3. Pick e to be relatively primattphe://powcoder.com
- 4. Find **d** so that **ed** mod (p-1)(q-1) = 1
- 5. Finally: Public key is (eAnd WeChat powcoder Private key is (d,N)

To encrypt: $E(x) = x^e \mod N$ To decrypt: $D(x) = x^d \mod N$

Why RSA works

"It works" theorem:

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For all 0 < x < N, can show that D(E(x)) = x Assignment Project Exam Help Proof:

D(E(x)) = (x^e \mod pq)^d \mod p \frac{1}{2} \frac{1
```

Is RSA secure?

Best known way to compute **d** from **e** is factoring **N** into **p** and **q**.

Best known factoring algorith Assignment Project Exam Help General number field sieve

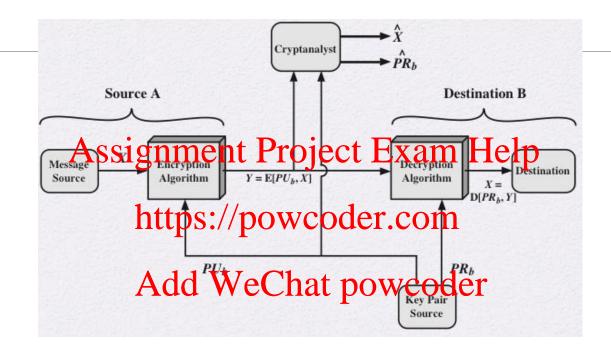
Takes more than polynomial time, but less than exponential time, to factor **n**-bit number. https://powcoder.com
(Still takes way too long if **p**,**q** are large enough and random.)

Fingers crossed...

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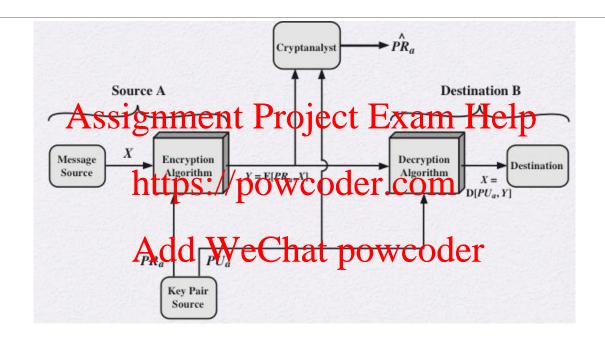
but can't rule out a breakthrough!

Signing with the public key for confidentiality or secrecy:



Does this provide integrity?

Signing with private key for integrity/authentication.



Does this provide confidentiality?

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RSA can be used for either confidentiality or integrity

RSA for confidentiality:

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Decrypt with public key

Decrypt with private key Assignment Project Exam Help

"your eyes only message"
```

RSA for integrity:

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Decrypt ("sign") with private key

Decrypt ("verify") with public keadd WeChat powcoder

called a digital signature

[What if we want both confidentiality and integrity on the same message?]

Which of these provides both confidentiality and integrity?

Alice (A) wants to send a secret message M to Bob (B) so that Bob can verify that it comes from Alice.

Which one(s) is/are sed signment Project Exam Help

- 1. $E(E(M, PR_A), PU_B)$
- 2. $E(E(M, PU_R), PR_{\Delta})$
- 3. $C=E(M, PR_A) t=E(H(C), PU_B)$
 - Send C||t
- 4. $C=E(M, PU_B) t=E(H(C), PR_A)$
 - Send C||t

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Review: Public-key Crypto

```
So far, encryption key == decryption key 
"symmetric key crypto"
```

New idea: Keys are distinct.

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RSA:
        N := pq
```

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Public key is (e,N)

https://powcoder.com **Private key** is (d,N)

To encrypt: $= x^e \mod N$

E(x)D(x)To decrypt:

= x^d mod NAdd WeChat powcoder

RSA for confidentiality:

Encrypt with public key Decrypt with private key

RSA for integrity (digital signatures):

Encrypt ("sign") with private key Decrypt ("verify") with public key

[Cautions?!]

RSA drawback: Performance

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Factor of 1000 or more slower than AES.
 Dominated by exponentiation – cost
 goes up (roughly) as cube of key size. ASSIGNMENT Project Exam Help Message must be shorter than N.
 [How big should the RSA keys be?] https://powcoder.com
Use in practice:
   ncryption: Add WeChat powcoder

Use RSA to encrypt a random \mathbf{x} < \mathbf{N}, compute \mathbf{k} := PRF(\mathbf{x}), encrypt message using a symmetric
 Encryption:
   cipher and key k
 Signing:
   Compute \mathbf{v} := PRF(\mathbf{m}), use RSA to sign a carefully padded version of \mathbf{v}
   (many gotchas!)
 Almost always should use crypto libraries to get the details right
```

True or False?

Public-key encryption is a general-purpose technique that has made symmetric encryption obsolete

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True or False?

Key distribution is trivial when using public-key encryption, compared to the cumbersome handshaking involved with key distribution centers for symmetric encryption.

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Attacks against RSA

- Brute force: trying all possible private keys
- Mathematical attacks: factoring Assignment Project Exam Help Timing attacks: using the running time of decryption
- Hardware-based fault attack: https://fapowicological.com/generate digital signatures
- Chosen plaintext attack on unpadded RSC hat powcoder

Exercise

Suppose Bob uses RSA crypto with a very large modulus **n** for which the factorization cannot be found in a reasonable amount of time.

Suppose Alice sends a measignment represent fresh letter as an integer between 0 and 25 (A->0, ..., Z->25) and then encrypting each number separately using RSA with large e and large n. https://powcoder.com

Is this method secure?

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If yes, why?

If not, how to efficiently attack this encryption method?

Solution

For a set of message block values SM = $\{0, 1, 2, ..., 25\}$. The set of corresponding ciphertext block values SC = $\{0^e \mod N, 1^e \mod N, ..., 25^e \mod N\}$, and can be computed by everybody with the knowledge of the public key of Bob ment Project Exam Help

The most efficient attack is to compute M^e mod N for all possible values of M, then create a look-up table with a ciphertext $\frac{1}{2}$ $\frac{$

Two subtle "textbook" RSA problems:

 For small e and m: m^e mod N == m^e Trivial to decrypt!

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2. If m is chosen from a small set, easy to confirm a ciphertext is a given message (anyone can encrypt!)

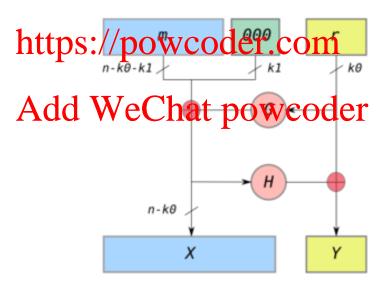
Chosen plaintext attack

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Solution: RSA Padding

Need to make sure m is as *large enough* to wrap around N (so can't take e-th root of ciphertext)

Need to randomize before encryption (so low-entropy plaintext can't be decrypted)
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Other public key cryptography systems

RSA is popular, but not the only one:

DSA – Digital Signature Algorithm

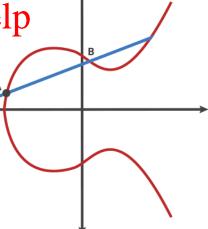
• ECDSA – Elliptic Curve Digital Signature Project Exam Help

Very small public keys: e.g. curve25519: 256-bits (32 bytes)

Post-Quantum Cryptography: https://poy

• Ring-LWE, NTRU, hash-based

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So Far:

The Security Mindset

Message Integrity Assignment Project Exam Help

Confidentiality

Key Exchange https://powcoder.com

Building a Secure Channel

Public Key Crypto

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Next Week:

Begin Web Security Unit

HTTPS: Secure channels for the web