

# Cryptography Basics – Key exchange

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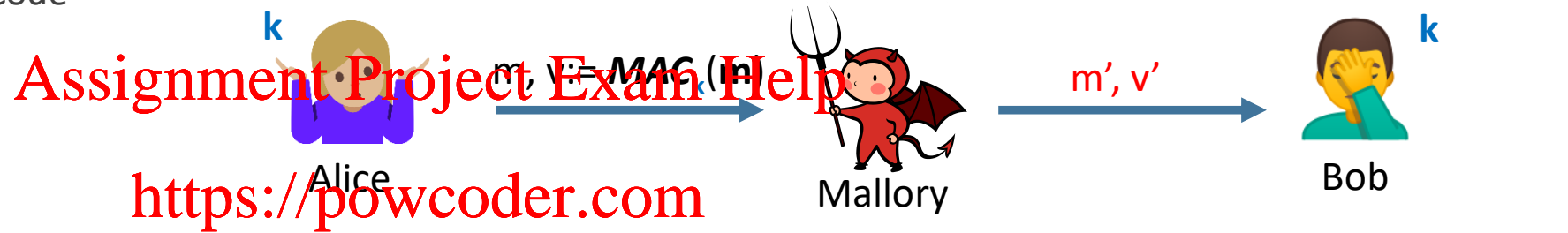
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# Review

**Integrity:** prevent Mallory from tampering

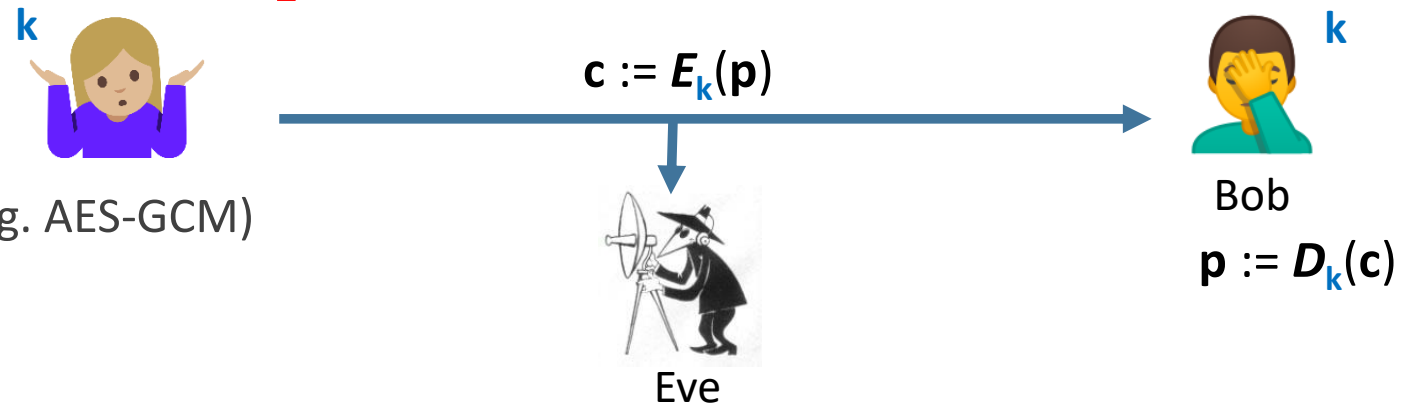
- Message Authentication Code
- Hashes -> HMAC
  - Use: SHA2, SHA3



**Confidentiality:** prevent eavesdropper (Eve) from learning the (plaintext) message

- Stream ciphers
  - AES-CTR, ChaCha20
- Block ciphers
  - AES-CBC (caution: padding oracles!)

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**Best practice:** Authenticated ciphers (e.g. AES-GCM)

- Encrypt, then MAC

# Sharing $k$

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## Amazing fact:

Alice and Bob can have a public conversation to derive a shared key!

**Diffie-Hellman (D-H) key exchange** **Assignment Project Exam Help**

1976: Whit Diffie, Marty Hellman

with ideas from Ralph Merkle

(earlier, in secret, by Malcolm Williamson of British intelligence agency)

Relies on a mathematical hardness assumption called *discrete log problem*  
(a problem believed to be hard)

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# Diffie-Hellman protocol

## D-H protocol

1. Alice and Bob agree on public parameters (maybe in standards doc\*, or pick them)  
 $p$ : a large "safe prime" s.t.  $(p-1)/2$  is also prime  
 $g$ : a square mod  $p$  (but not 1)

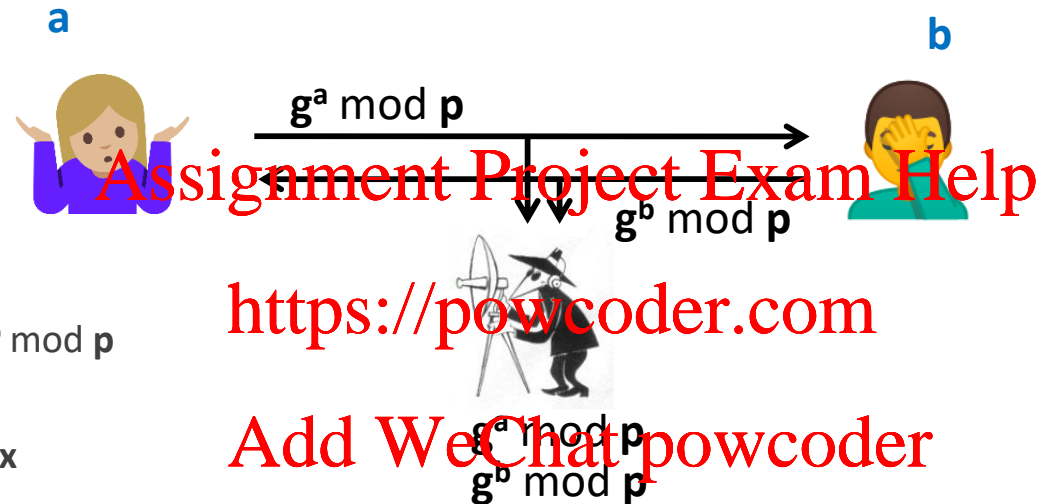
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2. **Alice** a  
Generates random secret value  $a$ .  
( $0 < a < p$ )  
  
**Bob** b  
Generates random secret value  $b$ .  
( $0 < b < p$ )  
  
Communication: Alice sends  $g^a \bmod p$  to Bob, and Bob sends  $g^b \bmod p$  to Alice.  
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3. **Alice**  
Computes  $x$   
 $= (g^b \bmod p)^a \bmod p$   
 $= g^{ba} \bmod p$   
**Bob**  
Computes  $x'$   
 $= (g^a \bmod p)^b \bmod p$   
 $= g^{ab} \bmod p$

(Notice that  $x == x'$ )  
Can use  $k := \text{HMAC}_0(x)$  as a shared key.

# DH passive eavesdropping attack



Eve wants to compute  $x = g^{ab} \bmod p$

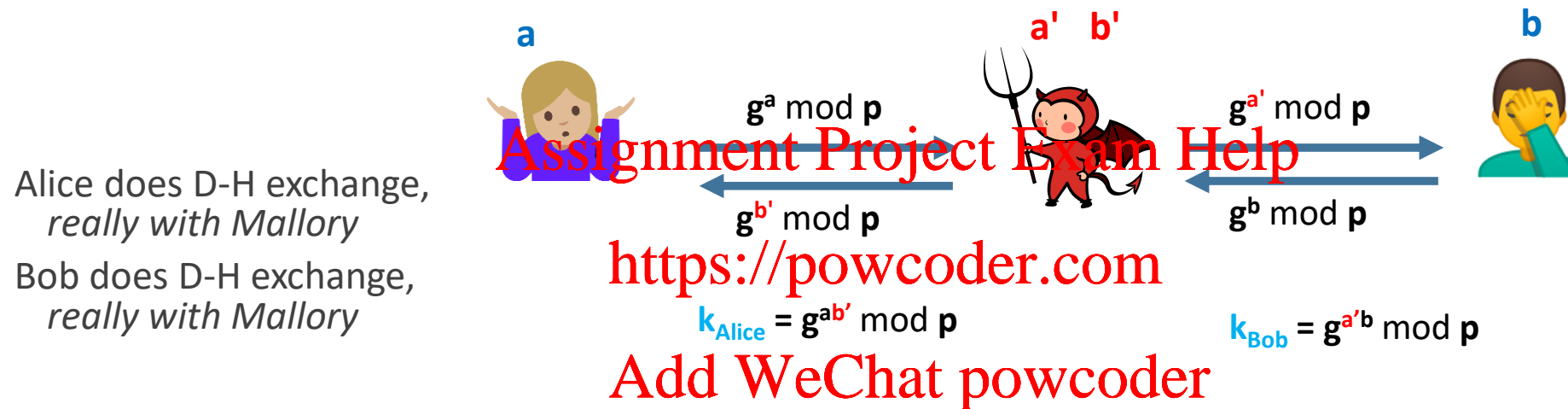
Best known approach:  
Find  $a$  or  $b$ , then compute  $x$

Finding  $y$  given  $g^y \bmod p$  is an instance of the **discrete log problem**:  
No known efficient algorithm\*

**Best practice:** Use large DH group size (e.g. 2048-bit primes)  
or a more secure group (Elliptic curve cryptography)

[Breakout exercise: what about Mallory (active attacks)?]

# Man-in-the-middle (MITM) attack



Alice and Bob each think they are talking with the other,  
but really Mallory is between them and knows both secrets

*Bottom line:*

D-H gives you secure connection, but you don't know who's on the other end!

# Defending D-H against MITM attacks

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- Cross your fingers and hope there isn't an active adversary.
- Rely on out-of-band communication between users. [Examples?]
- Rely on physical contact to make sure there's no MITM. [Examples?]
- Integrate D-H with user authentication.

If Alice is using a password to login to Bob, leverage the password:

Instead of a fixed  $g$ , derive  $g$  from the password – Mallory can't participate w/o knowing password.

- Use digital signatures. [More next week.]

# Public key encryption

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Can Alice share a “public key” ( $g^a \bmod p$ ) and have anyone encrypt a message only she can read?

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# Public key encryption

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Can Alice share a “public key” ( $g^a \bmod p$ ) and have anyone encrypt a message only she can read?

Diffie-Hellman doesn't allow this directly, but with some math:

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Alice's **public key** is  $A = g^a \bmod p$  and her **private key** is  $a$

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Bob has Alice's public key, and a message  $m$  he wants to send her:

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- Pick a random value  $r$   $[0, p-2]$
- Compute  $R = g^r \bmod p$
- Compute  $S = m * A^r \bmod p$
- Send Alice  $(R, S)$

To decrypt:

- Alice computes  $S * R^{-a} \bmod p = m * A^r * g^{r(-a)} \bmod p = m * g^{ar} g^{r(-a)} \bmod p = m * g^{ar-ar} \bmod p = m * g^0 \bmod p = m$