

Lecture 10

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Examples of Bode diagrams

Outline

- Recap of Bode diagrams
- Bode via Matlab
- Examples of Bode diagrams
- Conclusions

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Bode via Matlab

- To get the magnitude in decibels, use

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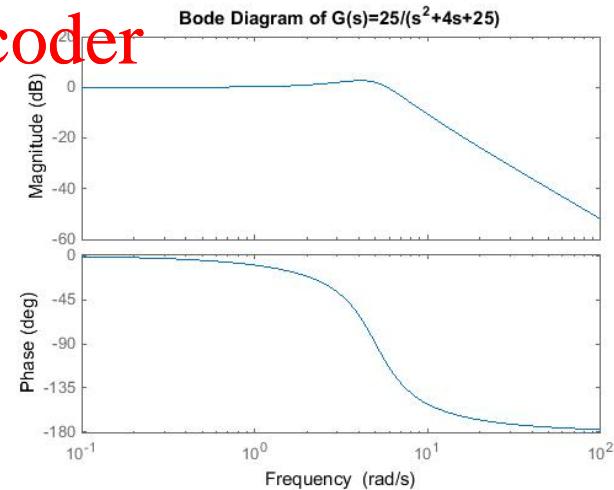
- For this transfer function:

$$G(s) = \frac{25}{s^2 + 4s + 25}$$

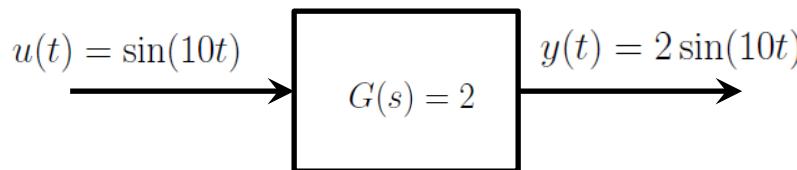
use

```
num=[0 0 25]  
den=[1 4 25]  
bode(num,den)  
title('Bode Diagram of G(s)=25/(s^2+4s+25)')
```

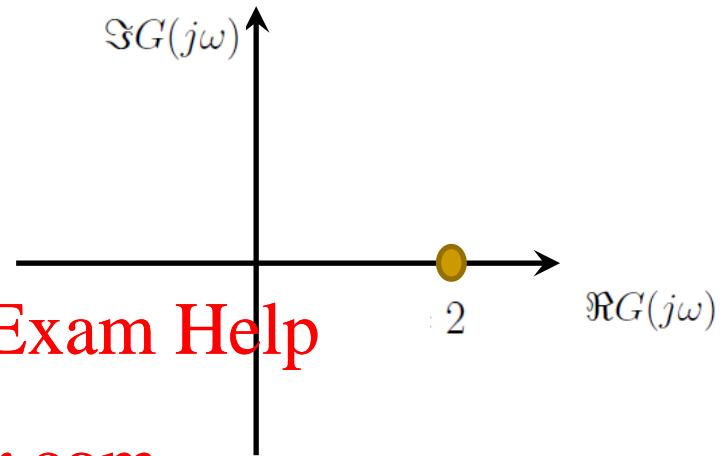
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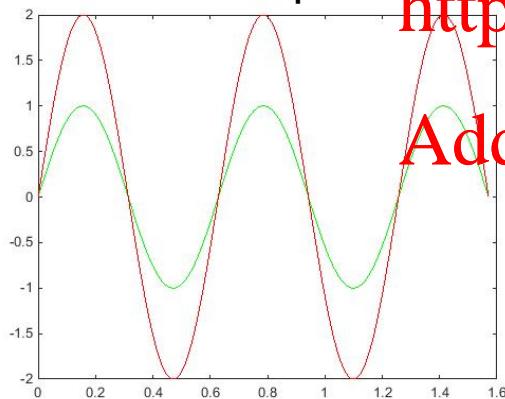
Bode diagram of a positive constant



$$G(j\omega) = 2, \forall \omega \in (-\infty, +\infty)$$

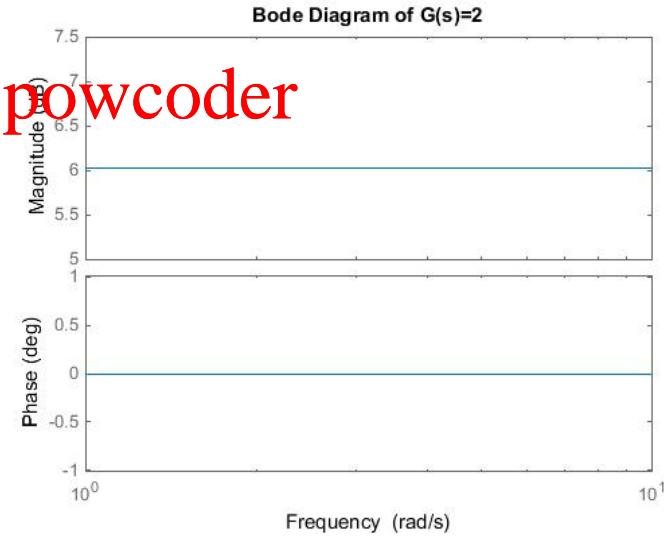


Time response



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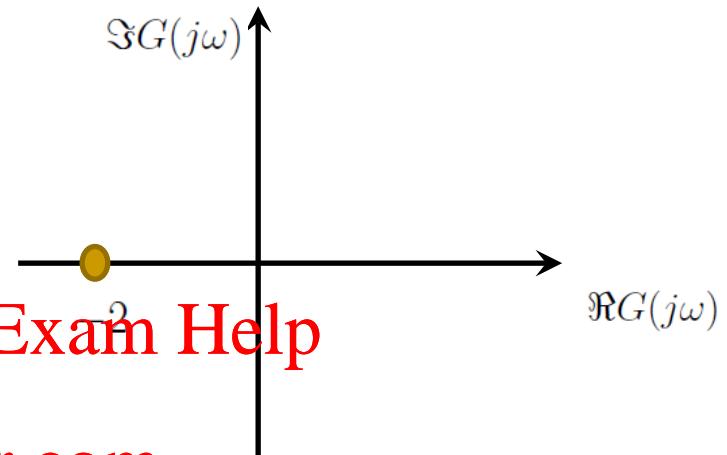
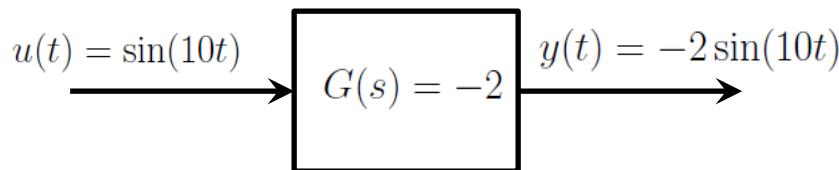
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$$20 \log |G(j\omega)| = 20 \log 2 = 6.0206$$

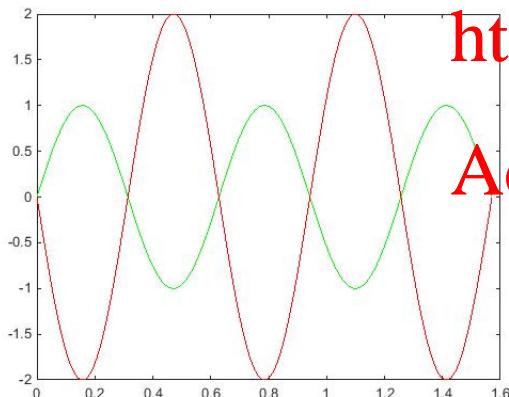
$$\angle G(j\omega) = 0$$

Bode diagram of a negative constant



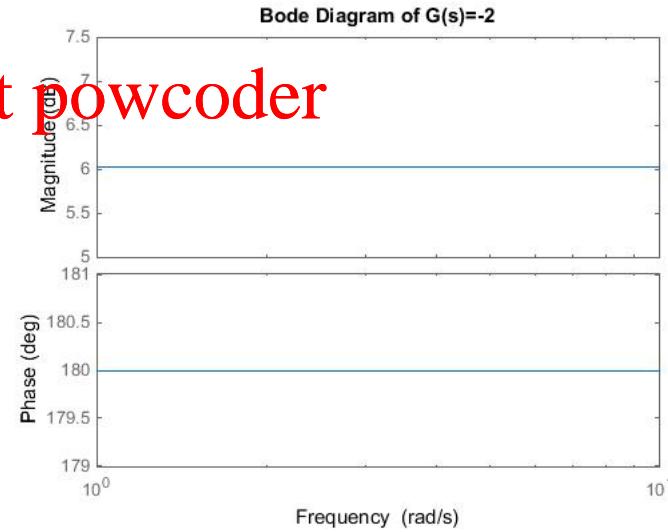
$G(j\omega) = -2$, Assignment Project Exam Help

Time response



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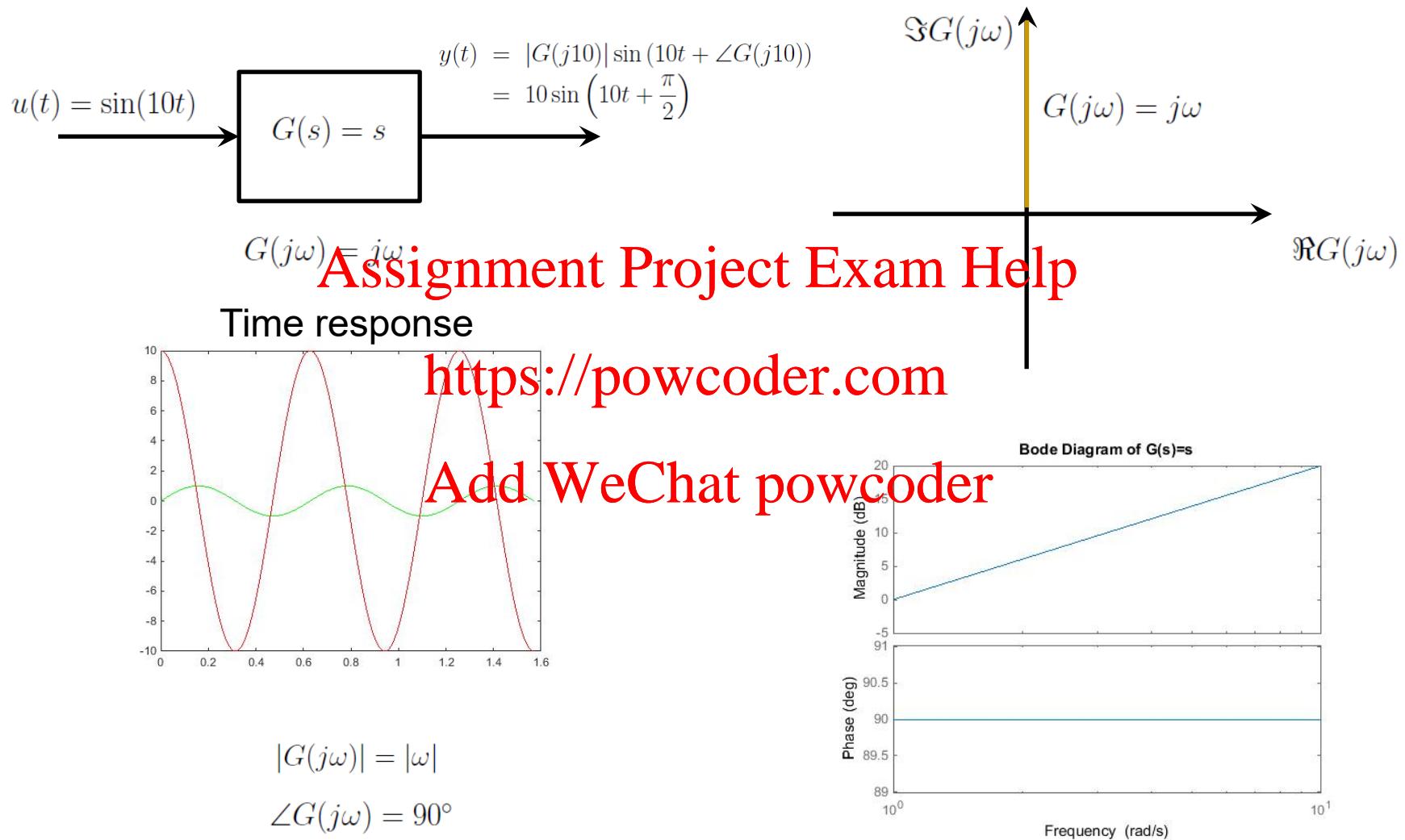
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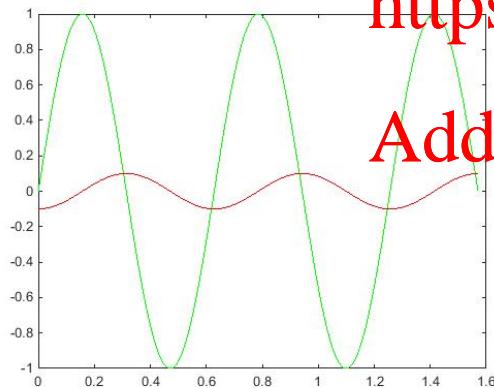
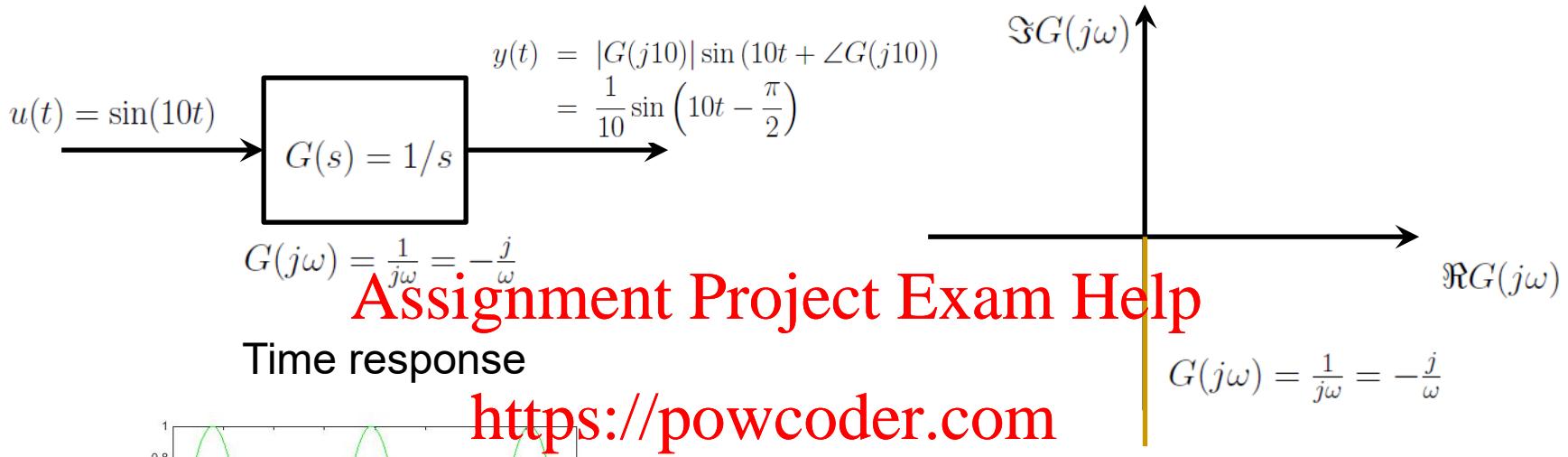
$$20 \log |G(j\omega)| = 20 \log 2 = 6.0206$$

$$\angle G(j\omega) = 180^\circ$$

Bode diagram of a differentiator

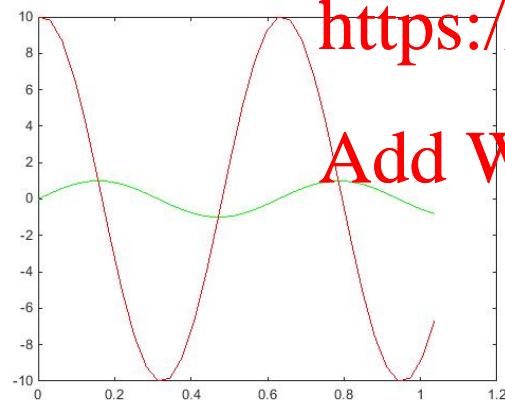
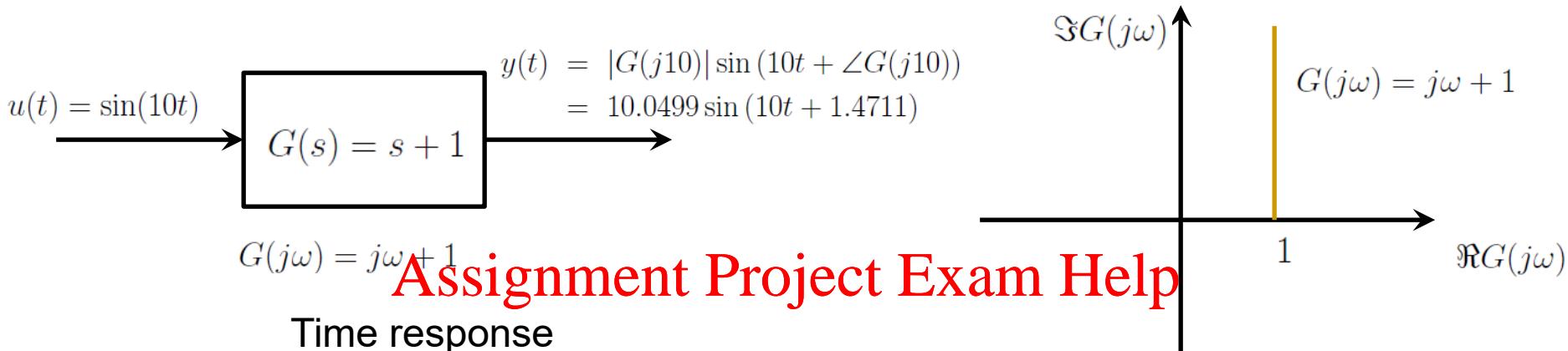


Bode diagram of an integrator



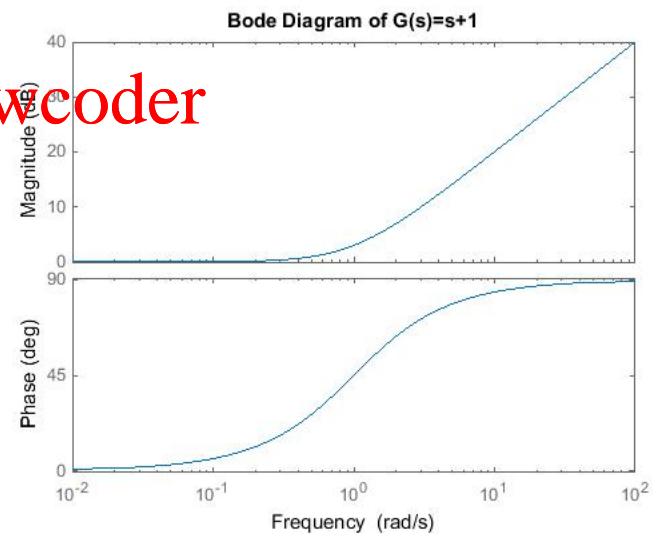
$$|G(j\omega)| = \frac{1}{|\omega|}$$
$$\angle G(j\omega) = -90^\circ$$

Bode diagram of a “real zero” term



$$|G(j\omega)| = \sqrt{1 + \omega^2}$$

$$\angle G(j\omega) = \tan^{-1} \frac{\Im G(j\omega)}{\Re G(j\omega)} = \tan^{-1} \omega$$



Asymptotic behaviour

- For small frequencies the system behaves like positive constant gain

$$\omega \ll 1 \implies |G(j\omega)| = \sqrt{1 + \omega^2} \approx 1$$

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$$\omega \ll 1 \implies \angle G(j\omega) = \tan^{-1} \omega \approx \tan^{-1} 0 = 0$$

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- For large frequencies the system behaves like a differentiator:

$$\omega \gg 1 \implies |G(j\omega)| = \sqrt{1 + \omega^2} \approx |\omega|$$

$$\omega \gg 1 \implies \angle G(j\omega) = \tan^{-1} \omega \approx \tan^{-1} \infty = 90^\circ$$

A useful relationship

- For reciprocal factors, Bode diagrams just need to “change sign”:

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$$20 \log \left| \frac{1}{G(j\omega)} \right| = -20 \log |G(j\omega)|$$

$$\angle \frac{1}{G(j\omega)} = -\angle G(j\omega)$$

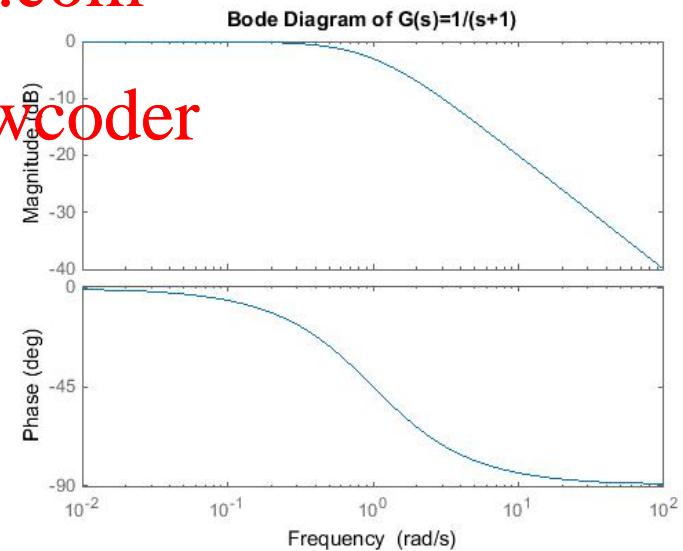
Bode diagram of a “real pole” term

- For instance, we have for $G(s) = \frac{1}{s+1}$

$$20 \log \left| \frac{1}{j\omega + 1} \right| \quad \text{Assignment Project Exam Help}$$

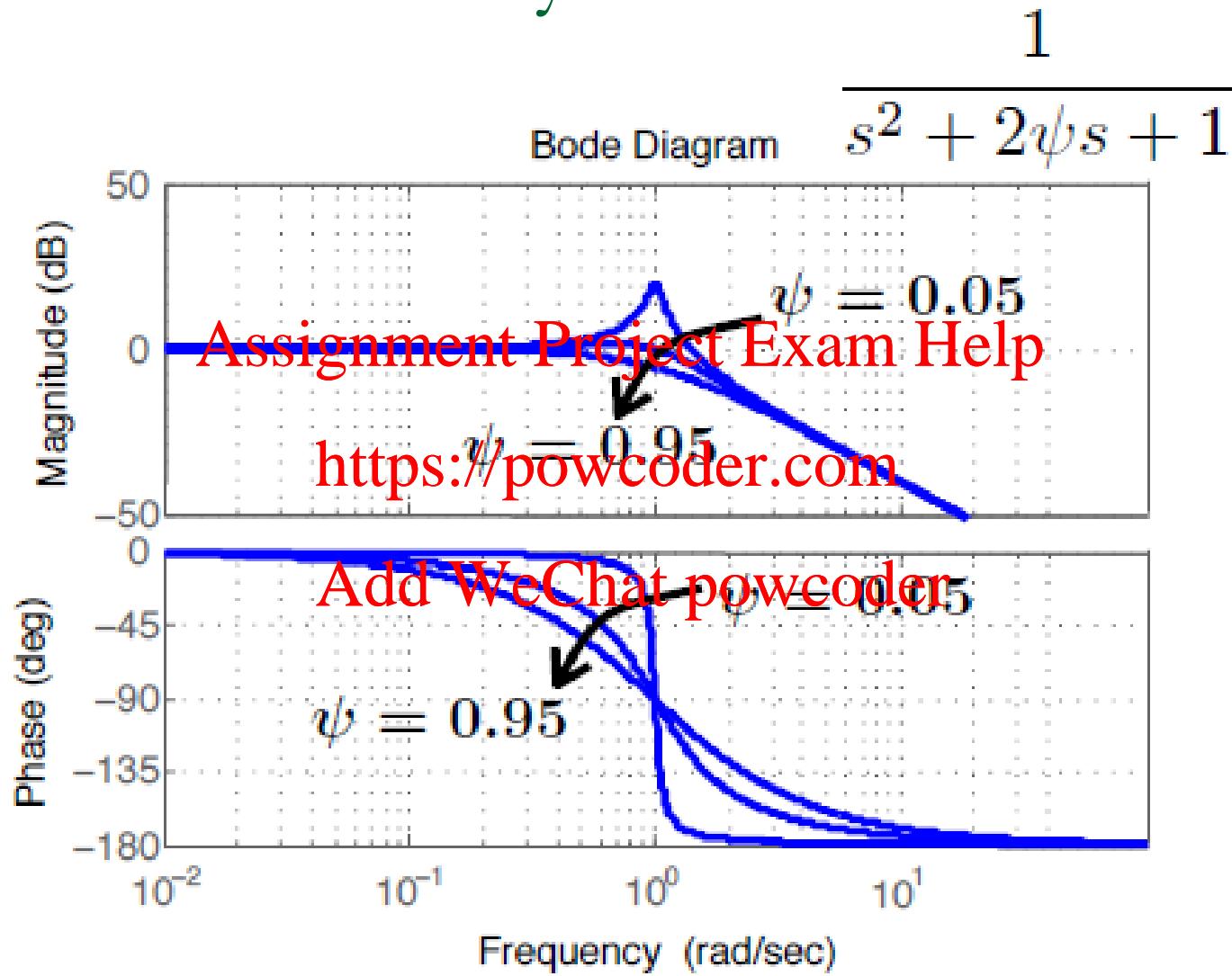
$$\angle \frac{1}{j\omega + 1} = -\angle(j\omega + 1) = -\tan^{-1}\omega$$

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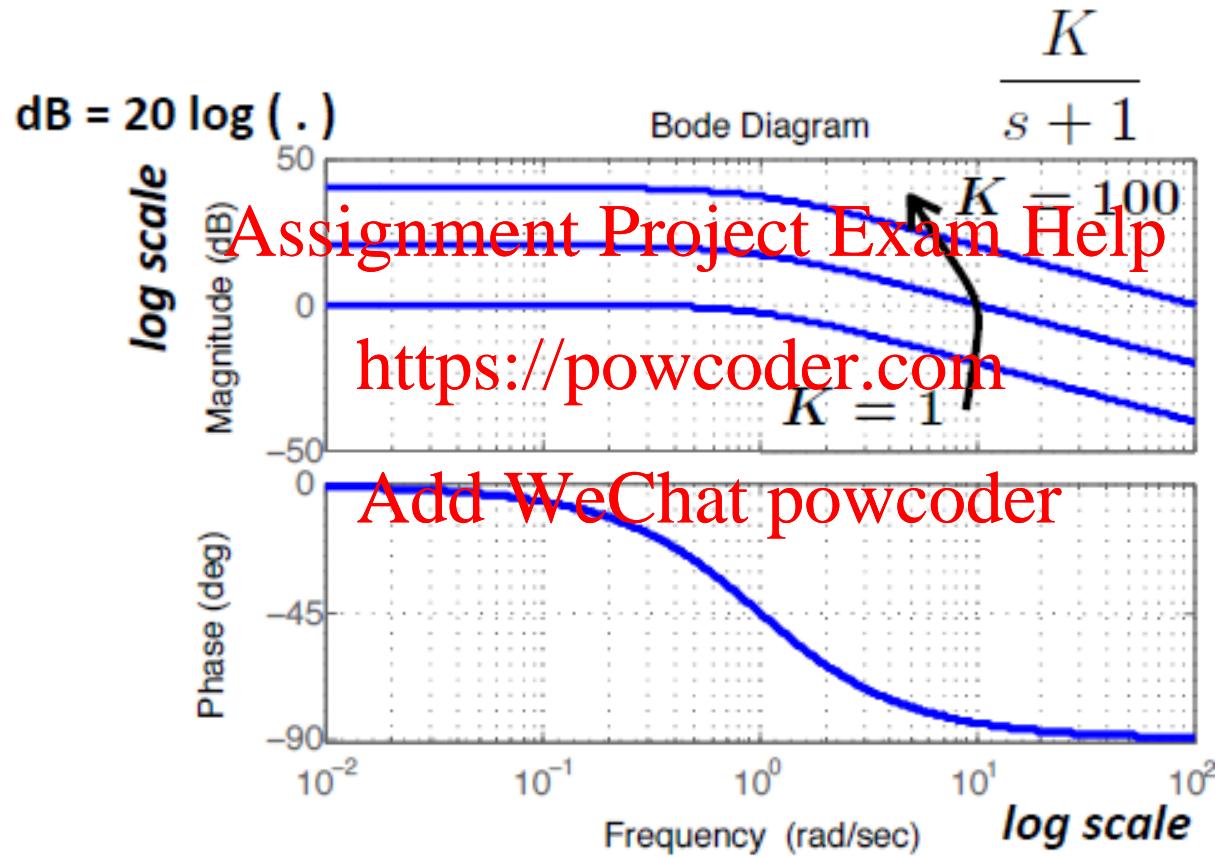


For exercise find the time response of the system as we did in previous examples.

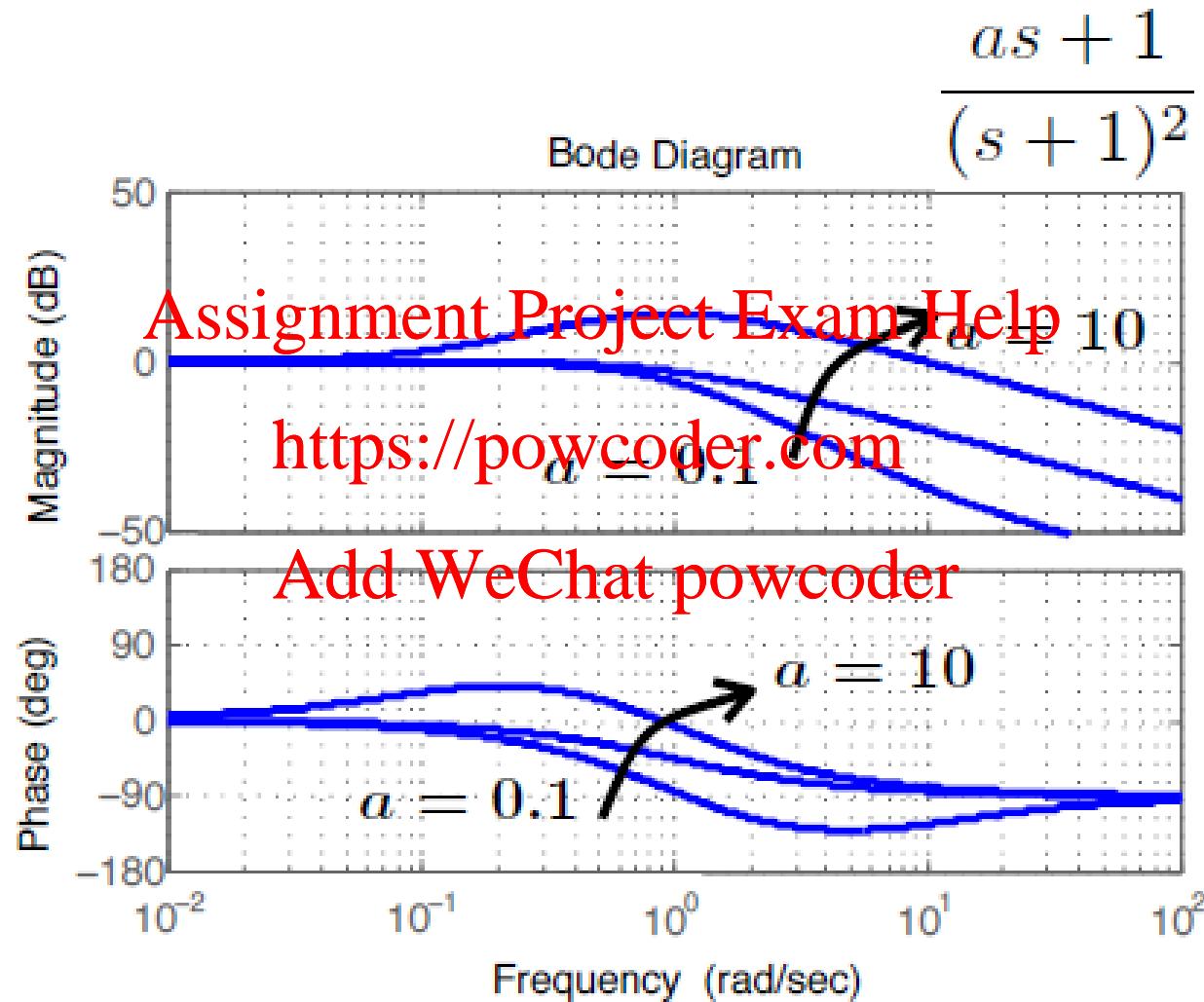
A second order system



Example

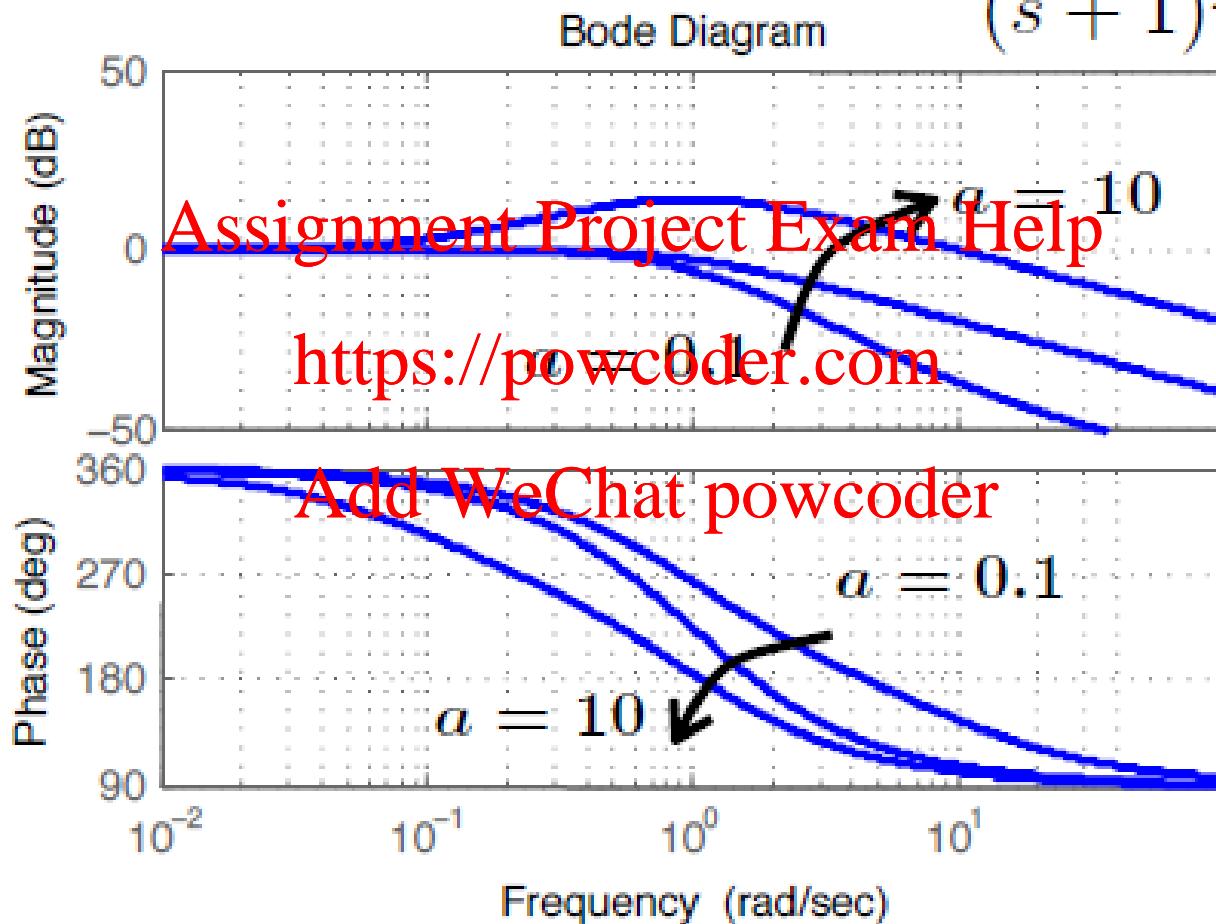


Example



Example

$$\frac{-as + 1}{(s + 1)^2}$$



Summary of common cases

System	Parameter	Step response	Bode (gain)	Bode(phase)
$\frac{K}{\tau s + 1}$	K			
	τ			
$\frac{\omega_n^2}{s^2 + 2\psi\omega_n s + \omega_n^2}$	ω_n			
	ω_n			
$\frac{as + 1}{(s + 1)^2}$	a			
$\frac{-as + 1}{(s + 1)^2}$	a			

Taken from Goodwin, Graebe and Salgado, Control system design.

Example

$$\frac{1}{s} = \lim_{k \rightarrow \infty} \frac{k}{ks + 1}$$

$$\frac{(s + 1)(s - 50)}{s(s - 0.1)(s + 10)} = \frac{50(s + 1)(0.02s - 1)}{s(10s - 1)(0.1s + 1)}$$

Bode Diagram

