Homework 2+

1. Pricing attributes

Consider a simple exchange economy with three commodities. A unit of each commodity contains attributes valued by consumers (protein, carbohydrates, etc. There are four attributes. The aggregate endowment in this economy is ω =(16,8,32) . The levels of each attribute are listed in the matrix $[a_{ij}]$ below.

a_{ij}	Commodity j		
Attribute <i>i</i>	Commodity 1	Commodity 2	Commodity 3
Attribute 1	1	2	1
Attribute 2	3	2	0
Attribute 3	1	2	0
Attribute 4	2	4	1

Assignment Project Exam Help

(a) What is the total endowment \bar{z}_i of each attribute?

Let z_i be consumption of attribute i. Then if a consumer furchases commodity vector x her consumption of attribute i is

Consumers purchase commodities because of their attributes. Each consumer has the same utility function $U(z) = 4 \ln z_1 + 2 \ln z_2 + 4 \ln z_3 + 6 \ln z_4$.

- (b) Explain the two different ways of solving for the equilibrium market prices.
- (c) Consider virtual markets for the four attributes. Solve for the equilibrium shadow prices of the four attributes. Choose the smallest possible integers.
- (d) Use these shadow prices to solve for the commodity prices.
- (e) Convert the problem into a standard problem with utility function u(x) and show that the prices in part (d) are indeed Walrasian Equilibrium commodity prices.

2. Walrasian Equilibrium

There are three consumers, each with a utility function of the form $U^h(x^h) = u(n^h + x^h)$ where $u(\cdot)$ is homothetic. Consumer h has an endowment of ω^h . One way to interpret this model is that consumer

h has a tradable endowment of $arphi^h$ and also a non-tradable endowment of n^h . Under this interpretation, consumer h has a total consumption of $t^h = n^h + x^h$.

(a) Explain why the budget constraint for total consumption t^h can be written as follows:

$$p \cdot t^h \leq p \cdot (\omega^h + n^h)$$
.

Hence the choice of consumer h is \overline{t}^h that solves

$$Max_{t^h > n^h} \{ u(t^h) \mid p \cdot (\omega^h + n^h) - p \cdot t^h \ge 0 \}, \ h = 1, ..., H$$
 (1.1)

Note that the lower bound for total consumption is now n^h as these are non-tradable. Except for this change, the economy looks very like the representative consumer economy.

This suggests a possible short-cut. Consider the relaxed problem (1.2) below and solve for the WE price vector.

$$Max\{u(t^h) \mid p \cdot (\omega^h + n^h) - p \cdot t^h \ge 0\}, \ h = 1, ..., H.$$
 (1.2)

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If the solution satisfies the constraints $\overline{t}^h \ge n^h$, then these are WE prices for the economy with non-

(b) Suppose that
$$U^1(x^1) = v(1+x_1^1) + v(x_2^1)$$
, $U^2(x^2) = v(3+x_1^2) + v(x_2^2)$, $U^3(x^3) = v(x_1^3) + v(x_2^3)$

where $v(t^h)$ is a strictly Angle function Chat powcoder

Endowments $\omega^1 = (4,3), \ \omega^2 = (8,13), \ \omega^3 = (0,0).$

Solve for the WE prices for the relaxed economy.

(c) Solve for the WE consumption vectors.

HINT: Each consumer purchases a fraction of the aggregate consumption bundle.

Confirm that the prices are WE prices for the model with non-tradable as well as tradable endowments.

(d) Suppose instead that

$$\omega^1 = (4,2), \ \omega^2 = (6,6), \ \omega^3 = (2,8).$$

Repeat the analysis. Hence explain whether the approach again yields the WWE prices for the economy with non-tradable as well as tradable endowments.

(e) Suppose next that $v(t) = t^{1/2}$, the non-tradable endowments are unchanged and the tradable endowments are

$$\omega^{1} = (3,40), \ \omega^{2} = (9,24), \ \omega^{3} = (0,0).$$

Repeat parts (b) and (c).

3. Firm production functions and industry production functions

There are four firms in an industry. The four production functions are as follows:

$$q_1 = z_1^{1/2}$$
 , $q_2 = 2z_2^{1/2}$, $q_3 = 2z_3^{1/2}$, $q_4 = 4z_4^{1/2}$

(a) If the total supply of inputs to the industry is \overline{z} , solve for the input vector $(\overline{z}_1, \overline{z}_2, \overline{z}_3, \overline{z}_4)$ that maximizes industry output.

HINT: From the Necessary conditions solve for each firms input as a function of λ . Then substitute back into the constraint $\sum_{i=1}^{4} z_{i} = \hat{z}$.

(b) Show that the industry production function is $q = 5z^{1/2}$.

4. Walrasian Equilibrium with production

Consider a two commonly economy. Commodity District Exam Help commodity 2. There are four firms with the production functions in question 3. The aggregate endowment vector is $\alpha = (84,0)$. Every consumer has the same utility function $U(x^h) = 4 \ln x_1^h + 6 \ln x_2^h, \ h = 1,...,H$.

$$U(x^h) = 4 \ln x_1^h + 6 \ln x_2^h, h = 1, ..., H$$

- (c) Appeal to (b) to obtain an expression for utility as a function only of the lotal input $z_{\rm l}$ used by the four firms. Then solve for the optimal input of commodity ${\bf l}$.
- (d) What is the optimal consumption vector $\overline{x} = (\overline{x}_1, \overline{x}_2)$?
- (e) At what price vector would the representative agent not wish to trade away from \bar{x} ?
- (f) What is the profit-maximizing input and maximized profit at these prices?