### Assignment Project Exam Help

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Introduction t	Add WeChat powcoder	networks and
Space	Forward	
Right, Down, Page Down	Next slide	
Left, Up, Page UpNASI	Previous slide	
P	Open presenter console	
Н	Toggle this help	

# From logic to algebra

• Boolean logic Assignment Project Exam Help

• Boolean algebra rules https://powcoder.com

bootean atgebra i	accs
Karnaugh maps	Add WeChat powcoder
Connec	Forward
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Left, Up, Page Up	Previous slide
P	Open presenter console
Н	Toggle this help

Boolean logic is probably the simplest possible (useful) logic. Basic concepts:

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TRUE, FALSE

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• AND, OR

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NOT

TRUE and FALSE are values for statements.

Note that not all statements qualify:

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- Today, the temperature is to be to be the temperature is to be the temperature is to be to be the temperature is to be
- Today, the weather is goodd WeChat powcoder
- Haggis tastes great.

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Usually, TRUE is represented by 10.

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Do not confuse binary and Boolean:

	Assignment Project Exam Help Binary https://powcoder.com	Boolean
0	Zero Add WeChat powcoder	FALSE
1	One	TRUE

A AND B can be represented as A  $\square$  B, A  $\times$  B, AB

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A OR B can be represented as https://powcoder.com
A [] B, A+B

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NOT A can be represented as  $\overline{A}$ ,  $\neg A$ 

Do not confuse binary and Boolean:

	Assignment Project Exam Help Binary https://powcoder.com	Boolean
0+0	O Add WeChat powcoder	0 OR 0 = 0
1+1	10	1 OR 1 = 1

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<a href="https://powcoder.com">https://powcoder.com</a>

Statement A AND Statement Add Wolfbat by wheler both statements are TRUE.

# Examples

Donald Duck wears a blue sailor suit AND Donald Duck does not wear

trousers.

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Is obviously TRUE

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At the moment we have 15 degrees AND at the moment we have below
 5 degrees.

Is obviously FALSE

Using 1 and 0, we can get a very compact representation as a truth table:

A	B Assignment Project Exam Help	AB
0	0 https://powcoder.com	0
0	1 Add WeChat powcoder	0
1	0	0
1	1	1

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A OR B means that either A or Asla Wis Chatanew Roller

OR different from our usualssignmentanding Exam. Help

Example: On my toast I like bacon projected on my toast I like bacon

In Boolean logic, this would mean Lalso enjoy having both, bacon and jam on my toast, which is actually not true.

## Examples

• Today it will be warm signment Project Exam. Help

https://powcoder.com Means that it can be warm and dry, cold and raining, or warm and raining. Add WeChat powcoder

• Today it is more than 15 degrees OR below 16 degrees.

This is obviously always TRUE.

#### Truth table for OR

A	Assignment Project Exam Help	A+B
0	0 https://powcoder.com	0
0	1 Add WeChat powcoder	1
1	0	1
1	1	1

#### Assignment Project Exam Help

Now, we only need to add negation and we can construct rather complex expressions.

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### NOT

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If something is TRUE, then, the negation NOT TRUE is obviously FALSE.

A Add WeCha	A
0	1
1	0

In electrical circuits, AND, ARIGNO Ena Project divided Deperators (e.g. XOR, NAND, NOR) are realised as so-called logic gates. A gate performs one (or several) logical operations on some logical input (i.e. bits) and produces a single logical output.

# Examples for gates

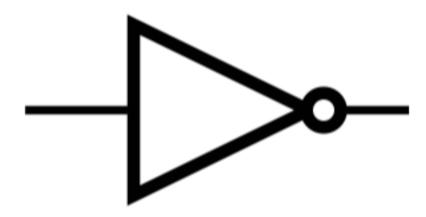
AND

OR

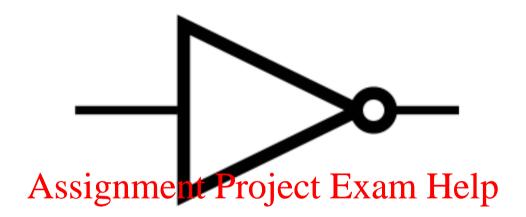
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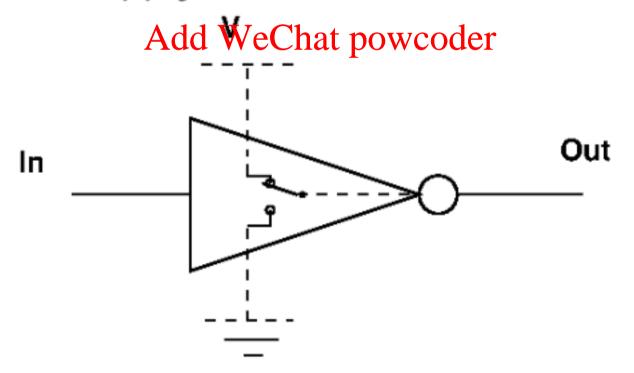
NOT



Logical circuits are not electrical circuits! Low input can result in high output:



The reason is, that power supply is now shown the schematic symbols.



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• In the lab we will use a the Weeks (Legys) of the lab we will use a the lab will use a the lab we will use a

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So far, you have mainly seen Boolean logic
The term Boolean algebra implies that we might be able to do arithmetic on symbols.

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Algebra

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(Merriam Webster)

# Laws of Boolean Algebra

- Identity Law
- Null Law (or Dominance Law)
- Idempotent Law
- Complement Law
- Commutative Law
- Associative Law
- Distributive Law
- Absorption Law
- DeMorgans Law
- Double Complement Law

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Identity Law Assignment Project Exam Help

AND Form	https://powcoder.com	
1A = A	Add WeChatpowcoder	

### Null Law (Dominance Law Assignment Project Exam Help

AND Form	https://powcoder.com	
0A = 0	Add WeChat powcoder	

Idempotent Law Assignment Project Exam Help

AND Form	https://powcoder.com
AA = A	Add WeChat powcoder

Complement Law Assignment Project Exam Help

AND Form	https://powcoder.com	
$A\overline{A} = 0$	Add WeChat powcoder	

Commutative Law Assignment Project Exam Help

AND Form	https://powcoder.com
AB = BA	Add WeChat Aport coder A

Associative Law Assignment Project Exam Help

AND Form	https://powcoder.com
(AB)C = A(BC)	Add WeChat poswooder (A+B)+C

Distributive Law Assignment Project Exam Help

AND Form	https://powcoden.com
A+(BC) = (A+B)(A+C)	Add WeChappwcpderAB+AC

Absorption Law Assignment Project Exam Help

AND Form	https://powcoder.comm
A(A+B) = A	Add WeChat powgoderA

DeMorgans Law Assignment Project Exam Help

AND Form	https://powcoder.com	
$\overline{AB} = \overline{A} + \overline{B}$	Add WeChat(powedode)	

Double Complement Law

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# Optimization of Boolean functions

When realizing a function as circuit, one would like to minimize gates. Boolean functions can be minimized with the Parite Fara Walls p

However, determining the cor**het**ts.p/pdevcolleapphying the laws is sometimes difficult.

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In addition, one would like to minimize the use of different types of gates.
Therefore, normalized forms can be useful.

One generic approach for minimizing (smaller) Boolean functions are Karnaugh maps or K-maps.

One of the most common forms of simplification in Boolean algebra is the following:

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One of the most common forms of simplification in Boolean algebra is the https://powcoder.com

 $A\overline{B} + AB = A(\overline{B} + B) = A$  Add WeChat powcoder

One of the most common forms of simplification in Boolean algebra is the following:

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 $A\overline{B} + AB = A(\overline{B} + B) = A$ 

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The same with three variables:

 $\overline{ABC} + ABC = AC$ 

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Both functions are independent from the value of B.

K-maps provide an easy graphical/way to find minimal AND terms that are then combined with OR to get the complete function.

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#### Truth table for A AND B

A	В	AB
0	0	0
0	1	0
1	Assignment Project Exam Help	0
1	1 https://powcoder.com	1

#### K-map for A AND B

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		В	
		0	1
Α	0	0	0
	1	0	1

Let's look at a K-map with 3 variables:

$$\overline{B}A\overline{C} + AB\overline{C} + ABC + \overline{A}BC + \overline{A}B\overline{C}$$

		BC			
		Assignment Pro	j <b>e01</b> Exam Help	11	10
А	0	0 https://pow	coder.com	1	1
	1	1 Add WeCh	at Powcoder	1	1

- Find groups of 1s.
- The group of four 1s represents B.

Let's look at a K-map with 3 variables:

$$\overline{B}A\overline{C} + AB\overline{C} + ABC + \overline{A}BC + \overline{A}B\overline{C}$$

		BC			
		00	01	11	10
А	0	0	ject Exam Help	1	1
	1	1 https://pow	coder.com	1	1

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- Find groups of 1s.
- The group of four 1s represents B=1.
- The wrapped group represents A=1 AND C=0.

#### Let's look at a K-map with 3 variables:

$$\overline{B}A\overline{C} + AB\overline{C} + ABC + \overline{A}BC + \overline{A}B\overline{C}$$

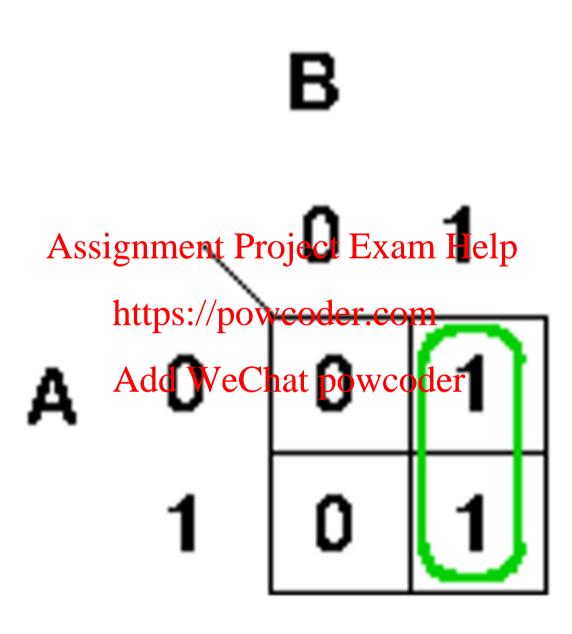
		BC			
		00	01	11	10
А	0	Assignment Pro	je <b>0</b> t Exam Help	1	1
	1	1 https://pow	coder.com	1	1

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- Find groups of 1s.
- The group of four 1s represents B=1.
- The wrapped group represents A=1 AND C=0.

Simplified version:  $B + A\overline{C}$ 

# 7 rules for https://pwicpdegconvith K-maps Add WeChat powcoder



Rule 1: No group can contain https://powcoder.com

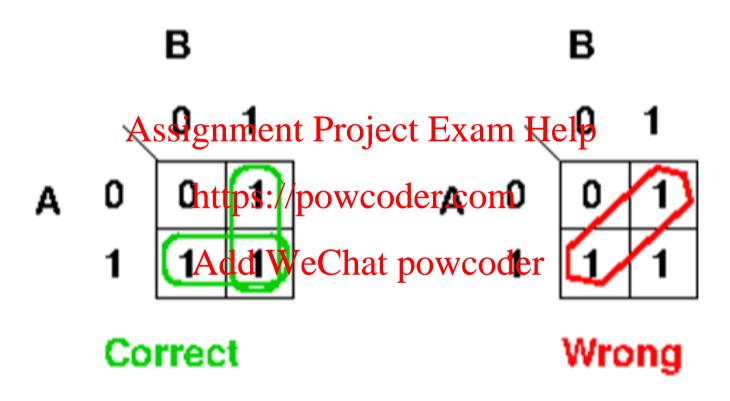
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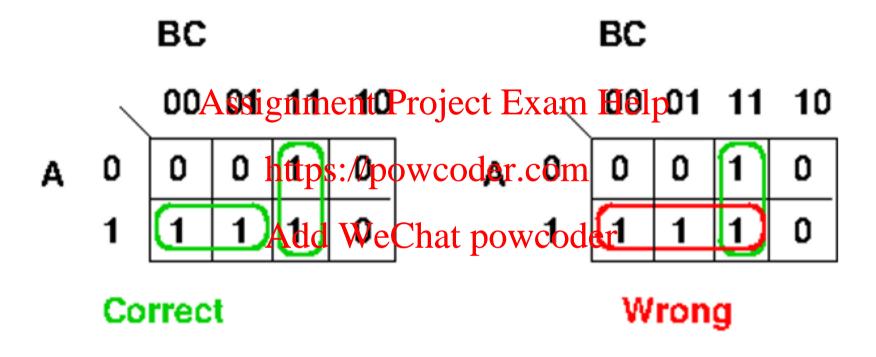
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Rule 2: Groups may be horizohttp://perveadesquare, but never diagonal.

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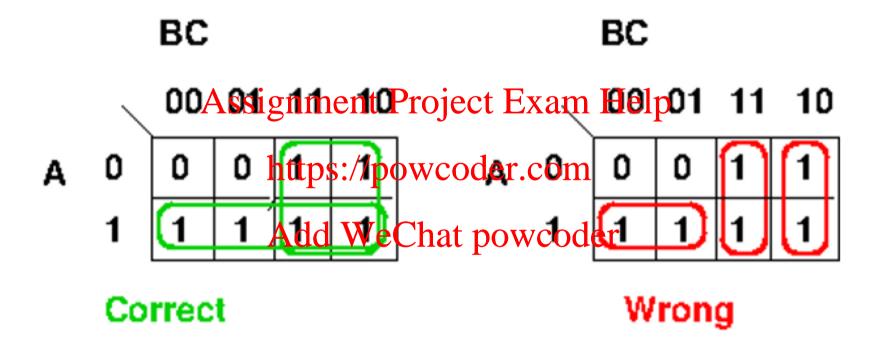




Rule 4: Each group must be as large as possible.

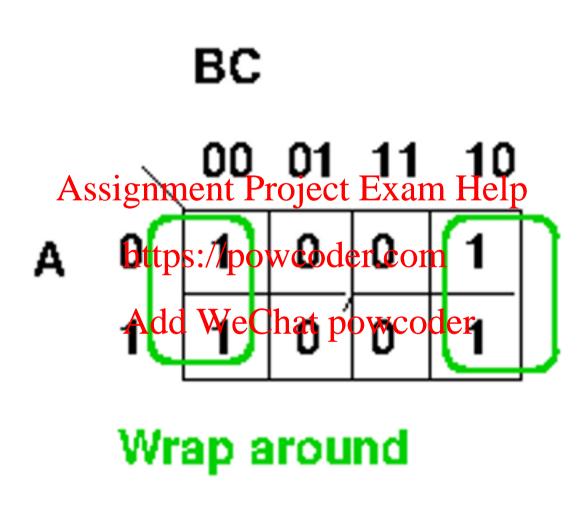
Rule 5: Groups can overlap. https://powcoder.com

Rule 6: Each 1 must be part of Add Washanpewcoder.



Rule 7: Groups may wrap around the wooder.com

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- Rule 1: No group can contain a zero.
- Rule 2: Groups may be horizontal/vertical/square, but never diagonal.

  Assignment Project Exam Help
  Rule 3: Groups must contain 1,2,4,8,16,32,... (powers of 2).
- Rule 4: Each group must be a https://powscodershotte.
- Rule 5: Groups can overlap. Add WeChat powcoder
- Rule 6: Each 1 must be part of at least one group.
- Rule 7: Groups may wrap around the map.

K-maps are useful for smaller Boolean functions.

Automated algorithms for optimization are used for bigger functions.

## Universal gates

NAND and NOR gates have special projecties am Help

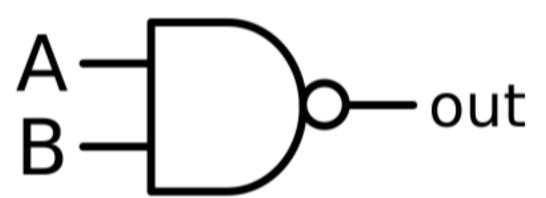
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- 1. NAND can be realised very efficiently.
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- 2. All other gates can be build only using NAND gates.

NAND is  $\overline{AB}$ 

## Truth table and symbol for NAND

A	В	AB
0	0 Assignment Project Exam Help	1
0	1 https://powcoder.com	1
1	O Add WeChat powcoder	1
1	1	0

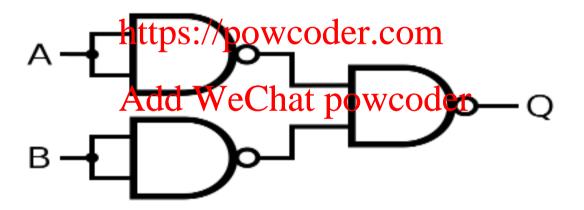


## Building NOT with NAND gates



# Building Assignment Project Example D gates https://powcoder.com A Add We Chat powcoder Q

# Building OR with NAND gates



### Summarize topics of first 2 weeks

- A little bit of history Assignment Project Exam Help
- Vacuum tubes and transistors/powcoder.com
- bit, byte, word (8bit/16bit/
- Numbering systems (base 2, base 10, base 16)
- Conversion between numbering systems

• Signed integer representations (sign/magnitude, 1's complement, 2's complement)

- Properties of 2's complement, adding 2's complement numbers https://powcoder.com
- Floating point representation Add WeChat powcoder
- Properties of floating point, precision, rounding
- Characters: ASCII and Unicode

- Error detection: Parity bits, Checksum, CRC
- Boolean Logic AND, OR, NOT, XOR, NAND, NOR Assignment Project Exam Help
- Logic gates
   https://powcoder.com
- Simple logic circuits Add WeChat powcoder
- Boolean Algebra, Laws
- Karnaugh Maps/K-maps