# Monash University Faculty of Information Technology $2^{nd}$ Semester 2018

# **FIT2014**

# Assignment 2

# Regular Languages, Context-Free Languages, Lexical analysis, Parsing, and Turing machines DUE: 11:55pm, Friday 5 October 2018

In these exercises, you will

- implement lexical analysers using lex (Problem 3);
- implement parsers using lex and yacc (Problems 1, 4);
- practise proof by induction (Problem 2);
- practise using the Pumping Lemma for regular languages (Problem 7);
- build a Turing machine (Problem 5);
- learn more about Turing machines (Problems 5–7).

Solution Assignment in the International Contract of Tuatara), which is available on Moodle.

# How to manage this assignment owcoder com

- You should start working on this assignment now, and spread the work over the time until it is due. Aim to do at least three questions before the mid-semester break. Do as much as possible before your week 10 prac class. There will not be time during the class itself to do the assignment from schach; there will only be time to go typically and darification.
- Don't be deterred by the length of this document! Much of it is an extended tutorial to get you started with lex and yacc (pp. 2–5) and documentation for functions, written in C, that are provided for you to use (pp. 5–7); some sample outputs also take up a fair bit of space. Although lex and yacc are new to you, the questions about them only require you to modify some existing input files for them rather than write your own input files from scratch.

# Instructions

Instructions are as for Assignment 1, except that some of the filenames have changed. The file to download is now asgn2.tar.gz, and unpacking it will create the directory asgn2 within your FIT2014 directory. You need to construct new lex files, using chain.l as a starting point, for Problems 1, 3 & 4, and you'll need to construct a new yacc file from chain.y for Problem 4. Your submission must include (as well as the appropriate PDF files for the exercises requiring written solutions):

- a lex file prob1.1 which should be obtained by modifying a copy of chain.1
- a lex file prob3.1 which should also be obtained by modifying a copy of chain.1
- a lex file prob4.1 which should be obtained by modifying a copy of prob3.1
- a yacc file prob4.y which should be obtained by modifying a copy of chain.y
- a Tuatara Turing machine file prob5.tm

PDF files for the exercises requiring written solutions, namely, prob1.pdf, prob2.pdf, prob6.pdf, and prob7.pdf.

Each of the problem directories under the asgn2 directory contains empty files with the required filenames. These much each be replaced by the files you write, as described above. Before submission, *check* that each of these empty files is, indeed, replaced by your own file.

To submit your work, simply enter the command 'make' from within the asgn2 directory, and then submit the resulting .tar.gz file to Moodle. As last time, make sure that you have tested the submission mechanism and that you understand the effect of make on your directory tree.

# INTRODUCTION: Lex, Yacc and the CHAIN language

In this part of the Assignment, you will use the lexical analyser generator lex or its variant flex, initially by itself, and then with the parser generator yacc.

Some useful references on Lex and Yacc:

- T. Niemann, Lex & Yacc Tutorial, http://epaperpress.com/lexandyacc/
- Doug Brown, John Levine, and Tony Mason, lex and yacc (2nd edn.), O'Reilly, 2012.
- the lex and yacc manpages

We will illustrate the use of these programs with a language CHAIN based on certain expressions involving strates. There you will use that are Dyson charges CRYPT of expressions based on cryptographic operation.

### **CHAIN**

The language CHAIN chiss is a sypression wife of wife type. An appression consists of a number of terms, with # between each pair of consecutive terms, where each term is either a string of lower-case letters or an application of the Reverse function to such a string. Examples of such expressions include

```
mala # y # Reverse(mark) WeChat powcoder
block # drive # cut # pull # hook # sweep # Reverse(sweep)
Reverse(side) # Reverse(direction) # Reverse(gear)
```

For lexical analysis, we wish to treat every lower-case alphabetical string as a lexeme for the token STRING, and the word Reverse as a lexeme for the token REVERSE.

### Lex

An input file to lex is, by convention, given a name ending in .1. Such a file has three parts:

- definitions,
- rules,
- C code.

These are separated by double-percent, %%. Comments begin with /\* and end with \*/. Any comments are ignored when lex is run on the file.

You will find an input file, chain.1, among the files for this Assignment. Study its structure now, identifying the three sections and noticing that various pieces of code have been commented out. Those pieces of code are not needed *yet*, but some will be needed later.

We focus mainly on the Rules section, in the middle of the file. It consists of a series of statements of the form

```
pattern { action }
```

where the *pattern* is a regular expression and the *action* consists of instructions, written in C, specifying what to do with text that matches the *pattern*.<sup>1</sup> In our file, each *pattern* represents a set of possible lexemes which we wish to identify. These are:

- a string of lower-case letters;
  - This is taken to be an instance of the token STRING (i.e., a lexeme for that token).
- the specific string Reverse;
  - Such a string is taken to be an instance of the token REVERSE.
- certain specific characters: #, (, );
- white space, being any sequence of spaces and tabs;
- the newline character.

Note that all matching is case-sensitive.

Our *action* is, in most cases, to print a message saying what token and lexeme have been found. For white space, we take no action at all. A character that cannot be matched by any pattern yields an error message.

If you run lex on the file chain.1, then lex generates the C program lex.yy.c.<sup>2</sup> This is the source code for the lexical analyser. You compile it using a C compiler such as cc.

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By default, cc put the executable program in a file called a cout <sup>3</sup>. This can be executed in the usual way, by just entering Danout at the command that if you prefer to give the executable program another name, such as chain-lex, then you can tell this to the compiler using the -o option: cc lex.yy.c -o chain-lex.

When you run the ptogram it wit initially that for you to input a line of text to analyse. Do so, pressing Return at inaction the line then the trice place in the line that it is a line of the line that it is a line of the messages is done by the printf statements from the file chain.1. Note how it skips over white space, and only reports on the lexemes and tokens.

### \$ ./a.out

```
mala # y #Reverse( mala)
Token: STRING; Lexeme: mala
Token and Lexeme: #
Token: STRING; Lexeme: y
Token and Lexeme: #
Token: REVERSE; Lexeme: Reverse
Token and Lexeme: (
Token: STRING; Lexeme: mala
Token and Lexeme: )
Token and Lexeme: <newline>
```

Try running this program with some input expressions of your own.

<sup>&</sup>lt;sup>1</sup>This may seem reminiscent of awk, but note that: the pattern is not delimited by slashes, /.../, as in awk; the action code is in C, whereas in awk the actions are specified in awk's own language, which has similarities with C but is not the same; and the action pertains only to the text that matches the pattern, whereas in awk the action pertains to the entire line in which the matching text is found.

<sup>&</sup>lt;sup>2</sup>The C program will have this same name, lex.yy.c, regardless of the name you gave to the lex input file.

<sup>&</sup>lt;sup>3</sup>a.out is short for assembler output.

### Yacc

We now turn to parsing, using yacc.

Consider the following grammar for CHAIN.

 $S \longrightarrow \varepsilon$  $E \longrightarrow E\#E$  $E \longrightarrow \mathbf{STRING}$  $E \longrightarrow \mathbf{REVERSE}(\mathbf{STRING})$ 

In this grammar, the non-terminals are S and E. Treat STRING and REVERSE as just single tokens, and hence single terminal symbols in this grammar.

We now generate a parser for this grammar, which will also evaluate the expressions, with # interpreted as concatenation and Reverse(...) interpreted as reversing a string.

To generate this parser, you need two files, prob1.1 (for lex) and chain.y (for yacc):

- Copy chain.1 to a new file prob1.1, and then modify prob1.1 as follows:
  - in the **Definitions** section, **un**comment the statement #include "y.tab.h";
  - in the **Rules** section, in each action:

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- · return TOKENNAME;
- return \*yytext;
- \* Comment but it Sprint Datwits On Cinay Still Plandy if debugging is needed, so don't delete them altogether, but the lexical analyser's main role now is to report the tokens and lexemes to the parser, not to the user.
- in the C code settion, comment out the function main(), which in this case occupies about four line of the enVf the file. Nat powcoder
- chain.y, the input file for yacc, is provided for you. You don't need to modify this yet.

An input file for yacc is, by convention, given a name ending in .y, and has three parts, very loosely analogous to the three parts of a lex file but very different in their details and functionality:

- Declarations,
- Rules,
- Programs.

These are separated by double-percent, %%. Comments begin with /\* and end with \*/.

Peruse the provided file chain.y, identify its main components, and pay particular attention to the following, since you will need to modify some of them later.

- in the Declarations section:
  - lines like

```
char *reverse(char *);
char *simpleSub(char *, char*);
```

which are declarations of functions (but they are defined later, in the Programs section);

- declarations of the tokens to be used:

```
%token <str> STRING
%token <str> REVERSE
```

 declarations of the nonterminal symbols to be used (which don't need to start with an upper-case letter):

```
%type <str> start
%type <str> expr
```

- nomination of which nonterminal is the Start symbol:

```
%start start
```

- in the Rules section, a list of grammar rules in BNF, except that the colon ":" is used instead of →, and there must be a semicolon at the end of each rule. Rules with a common left-hand-side may be written in the usual compact form, by listing their right-hand-sides separated by vertical bars, and one semicolon at the very end. The terminals may be token names, in which case they must be declared in the Declarations section and also used in the lex file, or single characters enclosed in forward-quote symbols. Each rule has an action, enclosed in braces {...}. A rule for a Start symbol may print output, but most other rules will have an action of the form \$\$ = .... The special variable \$\$ represents the value to be returned for that rule, and in effect specifies how that rule is to be interpreted for evaluating the expression. The variables \$1, \$2, ... refer to the values of the first, second, ... symbols in the right-hand side of the rule.
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After constructing the new prob P.O. W.C., O.G. and C. G. G. and C. and C.

```
$ yacc -d chain.y

$ flex prob1.1

$ cc lex.yy.c y.tab Add WeChat powcoder
```

The executable program, which is now a parser for CHAIN, is again named a.out by default, and will replace any other program of that name that happened to be sitting in the same directory.

```
$ ./a.out
mala  # y #Reverse( mala)
malayalam<sup>4</sup>
```

Run it with some input expressions of your own.

# Problem 1. [7 marks]

- (a) Construct prob1.1, as described above, so that it can be used with chain.y to build a parser for CHAIN.
- (b) Show that the grammar for CHAIN given above is ambiguous.
- (c) Find an equivalent grammar (i.e., one that generates the same language) that is not ambiguous.

<sup>&</sup>lt;sup>4</sup>Malayalam is the main language of the southern Indian state of Kerala. The word was given as an example of a palindrome by an FIT2014 student in a lecture last year.

# Cryptographic expressions

A **cryptographic calculator** performs simple operations on strings of a kind that are used in classical cryptosystems. It is also able to combine these operations in a natural way.

Suppose  $x = x_1 x_2 \cdots x_n$  and  $k = k_1 k_2 \cdots k_t$  are two strings, where  $x_i$  and  $k_i$  denote the *i*-th letters of x and k respectively.

The available operations are:

- sum: this is written x + k in our expressions, though our C function that computes it is called sum(...). The resulting string has length min $\{n, t\}$ , and its *i*-th letter is  $x_i + k_i \mod 26$ , where the letters of the English alphabet correspond to numbers via a = 0,  $b = 1, \ldots, z = 25$ . For example,
  - x = thebushwasalivewithexcitement
  - k =mrskoalahadabrandnewbabyandthenewsspreadlikewildfire
  - x + k = fywlisswhsdljmejlglaycjrezhga
- difference: this is written x k, and is computed by the C function diff(...). The resulting string has length min $\{n, t\}$ , and its *i*-th letter is  $x_i k_i \mod 26$ .
- Vigenère cypher: this is written Vigenere(x, k), where x is the plaintext and k is the key. We first concatenate k with itself as many times as necessary in order to make it at least as long as x. Then we form the sum. The result is a string whose i-th letter is

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For example, if the plaintext is

# inaholehttps://pioweioder.com

and the key is

bilbo

# then Vigenere (iAddhegWuEtCrhatahpo,Wcodethe cyphertext

jvlicmmtohimrscvvouvfzpmwwmobvpjmjh

• Simple Substitution: this is written SimpleSub(x, k). Again, x is plaintext, and k is the key, but this time k must be a permutation of the 26-letter English alphabet, represented as a string in which each letter appears exactly once (and t = 26). Every a in the plaintext is replaced by the 1st letter  $k_1$  of the key; every b in the plaintext is replaced by the 2nd letter,  $k_2$ , of the key; and so on. In general, the plaintext letter  $x_i$  is replaced by  $k_{x_i}$ .

For example, if the plaintext is

thequickbrownfoxjumpsoverthelazydog

and the key is

qwertyuiopasdfghjklzxcvbnm

 $then \verb|SimpleSub| (the \verb|quick| brown fox jumps over the lazydog, \verb|qwertyuiop| as dfghjklzxcvbnm|) \ returns the cyphertext$ 

 $\verb|zitj| xoeawkgvfygbpxdhlgctkzitsqmnrgu|$ 

• Local Transposition: this is written LocTran(x, k). The letters of the plaintext x are not replaced, as happens in the previous cyphers, but rather rearranged according to a permutation, which is represented by a string k of w digits, where w = |k|. This permutation string k has length  $\leq 10$ , and consists of the digits  $0, 1, \ldots, w-1$  arranged in some order. For example, if k has length 3 (so w = 3), then k can be any of the strings 012, 021, 102, 120, 201, 210. The plaintext x is divided into blocks of w letters each, and the letters within each block are permuted according to k. If there are extra letters at the end — too few letters to make up another full block — then these are just copied across, with no change in their positions.

For example, if the plaintext is

# thefamilyofdashwood

and the key is

201

then LocTran(thefamilyofdashwood, 201) returns the cyphertext

# ethmfayildofhasowod

These operations can be combined. Any valid expression can be given as the first argument to one of the cypher functions, or as any argument of a sum or difference, to give another valid espression. So you can form expressions like

Vigen to Loc Transtriantivent igor plone, 3201), bun tib) + muldjewin ke post CRYPT be the Enguage of cryptographic expressions of this type that can be generated by the following grammar.

# https://powcoder.com $E \longrightarrow E + E$ $Add_E \longrightarrow \text{SIMPLESUB}(E, \text{STRING})$ $E \longrightarrow \text{VIGENERE}(E, \text{STRING})$ $E \longrightarrow \text{LOCTRAN}(E, \text{DIGITS})$ $E \longrightarrow \text{STRING}$

In this grammar, the non-terminals are S and E. Treat SIMPLESUB, VIGENERE, LOCTRAN, STRING and DIGITS as just single tokens. For SIMPLESUB, VIGENERE, and LOCTRAN, we allow any nonempty prefix of the function name as well as the full name; e.g., S, Si, Sim, ..., SimpleSu, SimpleSub are all acceptable lexemes for the token SIMPLESUB.

# Problem 2. [7 marks]

For each  $n \geq 0$ , let  $V_n$  be the string

$$\underbrace{\text{VIGENERE}(\dots \text{VIGENERE}(\text{VIGENERE}(\text{STRING}, \text{STRING}), \text{STRING}) \dots, \text{STRING})}_{n \text{ times}}$$

where the Vigenère cypher is applied n times.

Prove, by induction on n, that  $V_n$  has a derivation, using the above grammar, of length n+2.

 $<sup>^{5}</sup>w$  stands for width, the traditional term for the size of a permutation used in local transposition.

# Problem 3. [7 marks]

Using the file provided for CHAIN as a starting point, construct a lex file, prob3, and use it to build a lexical analyser for CRYPT.

Sample output:

```
$ ./a.out
Loc(Sim(Vig(therewasmovementatthestation, banjo), thequickbrownfxjmpsvlazydg), 10)
Token: LOCTRAN; Lexeme: Loc
Token and Lexeme: (
Token: SIMPLESUB; Lexeme: Sim
Token and Lexeme: (
Token: VIGENERE; Lexeme: Vig
Token and Lexeme: (
Token: STRING; Lexeme: therewasmovementatthestation
Token and Lexeme: ,
Token: STRING; Lexeme: banjo
Token and Lexeme: )
Token and Lexeme: .,
Token: STRACS SIX AN IMPERITURE TO LETTER AND LOVERS OF THE PROPERTY OF THE PR
Token and Lexeme:
Token and Lexeme: ,
Token: DIGITS; Lexeme: 10
Token and Lexeme: https://powcoder.com
Control-D
$ ./a.out
V(twentysix - elevery elever) We Chat powcoder Token: VIGENERE; Lexing We Chat powcoder
Token and Lexeme: (
Token: STRING; Lexeme: twentysix
Token and Lexeme: -
Token: STRING; Lexeme: eleven
Token and Lexeme: ,
Token: STRING; Lexeme: eleven
Token and Lexeme: )
Token and Lexeme: <newline>
```

# Problem 4. [7 marks]

Make a copy of prob3.1, call it prob4.1, then modify it so that it can be used with yacc. Then construct a yacc file prob4.y from chain.y. Then use these lex and yacc files to build a parser for CRYPT.

Note that you do not have to program any of the cryptographic functions yourself. They have already been written: see the Programs section of the yacc file. The *actions* in your yacc file will need to call these functions, and you can do that by using the function call for reverse(...) in chain.y as a template.

The core of your task is to write the grammar rules in the Rules section, in yacc format, with associated actions, using the examples in chain.y as a guide. You also need to do some

modifications in the Declarations section to declare all tokens, using %token, and declare all nonterminal symbols, using "type." See page 4.

<sup>a</sup>You should still use start as your Start symbol. If you use another name instead, you will need to modify the %start line too.

Sample output:

### \$ ./a.out

Loc(Sim(Vig(therewasmovementatthestation,banjo),thequickbrownfxjmpsvlazydg),10) kltpysiteauzfglhctaesircrktx

Control-D

\$ ./a.out

V(twentysix - eleven, eleven)

twenty

# Binary local transposition of width 2

Binary local transposition of width 2 is a special case of the Local Transposition cypher described above (see p. 7), except that it works with the binary alphabet  $\{0,1\}$  and uses width w=2. Its input has the form xyk where

- x is a Anasystign function Project Exam Help  $x = x_1 x_2 \cdots x_n$ , where n is even;
- k is either 01 or 10; the character y is used imply to sparate x and character.

The cyphertext  $z = z_1 z_2 \cdots z_n$  is given by:

- if k = 01, then z A d d i Weither Power elements of the property of the

$$z_{2j-1} = x_{2j},$$
  
 $z_{2j} = x_{2j-1}.$ 

Think of the plaintext as divided into non-overlapping pairs of bits. Then, for each pair, the bits within it are swapped.

# Problem 5. [7 marks]

Build, in Tuatara, a Turing machine to compute binary local transposition of width 2.

Your Turing machine must have q1 as its Start State and q2 as its Accept State.

The output should have no y and/or key k after the cyphertext.

# The language of encoded Turing machines

In the next two questions, your Turing machines use input alphabet {a,b} and tape alphabet {a,b,#}. Tuatara is not used in these questions.

Problem 6 should help prepare for Problem 7.

# Problem 6. [7 marks]

- Write, in table form, a Turing machine that accepts the input string aaaaa and crashes for every other input string.
- (b) On a single line, write down a string over {a,b} that represents your Turing machine from part (a) in the Code Word Language (CWL). (See Lecture 15 for CWL.)
- (c) How many different strings in CWL represent this exact same Turing machine?
  - These strings must all represent identical Turing machines, not just Turing machines that are equivalent in the sense that they always give the same result.
  - You may assume that strings in CWL represent each Turing machine table row exactly once.
- (d) Explain how to construct, for each  $n \in \mathbb{N}$ , a Turing machine  $M_n$  that accepts the input string  $a^n$  and crashes for every other input string.

Recall from lectures that the language CWL is regular. But CWL contains many strings

that represent Turing machines that are officer invalid or useless.

Let CODD DA Settle language of 111 things in CVL that Green that (i) are valid, and (ii) accept at least one string. For example, if you have done part (b) correctly, the string you constructed there should belong to GOOD-TM.

Give a string if GCCD M that I stray property t the very start of the string, the resulting string is no longer in GOOD-TM.

# Add WeChat powcoder

# Problem 7. [8 marks]

Use the Pumping Lemma for Regular Languages to show that GOOD-TM is not regular.

FOR BONUS MARKS: determine, with proof, whether or not GOOD-TM is context-free.

# References

- Jane Austen, Sense and Sensibility, Thomas Egerton, London, 1811.
- C. J. Dennis, The Triantiwontigongolope, poem in his book, A Book for Kids, Angus & Robertson, Sydney, 1921.
- A. B. 'Banjo' Patterson, The Man from Snowy River, poem first published in The Bulletin on 26 April 1890.
- J. R. R. Tolkien, The Hobbit, Allen & Unwin, London, 1937.
- Dorothy Wall, Blinky Bill, Angus & Robertson, Sydney, 1933.