

Limits of Computation
Feedback Exercises 3
Programs-As-Data, Self-Interpreter, and hwhile
(covers Lectures 3–6)
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1. Consider the programs **p1** in Figure 1 and **add** in Figure 2.

<pre> p1 read L { R := 0; X := hd L; Y := hd tl L; while X { R := <add> [Y, R]; X := tl X; } write R </pre>	<pre> add read L { X := hd L; Y := hd tl L; while X { Y := cons nil Y; X := tl X; } write Y </pre>
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Figure 1: WHILE-program **p1**

Figure 2: WHILE-program **add**

- (a) What is $\llbracket \mathbf{p1} \rrbracket^{\text{WHILE}} (\ulcorner [2, 5, 7, 8] \urcorner)$ according to the definition of **p1** and **add** (from the last exercise sheet) according to $\llbracket _ \rrbracket^{\text{WHILE}}$?

Answer: Since **p2** is addition (on encodings of natural numbers), **p1** is multiplication, so $\llbracket \mathbf{p1} \rrbracket^{\text{WHILE}} (\ulcorner [2, 5] \urcorner) = \ulcorner 10 \urcorner$. Note that only the first two elements are used in the input list.

- (b) Translate the program **add** from above into its data representation (programs as data) using the definition of the encoding presented in Lecture 6. Encode the variables starting from number 0 in the order of appearance.

Answer:

```

[0,
 [[:=,1,[hd,[var,0]]],
  [:=,2,[hd,[tl,[var,0]]]],
  [while,[var,1],
   [[:=,2,[cons,[quote,nil],[var,2]]],
    [:=,1,[tl,[var,1]]]
  ]
 ],
 2]

```

Make sure that you have the right number of square brackets for all the blocks.

2. On our Canvas page you find the program `STEP_incomplete.while` in the *Programs* section – or also from this link

canvas.sussex.ac.uk/courses/12888/files/2022795

This program is macro-called in the self-interpreter for the WHILE-language with one variable, called `WH1LE`. One case in the second switch construct is missing (for assignment). Fill in the missing lines.

Answer:

```

val:1 arg:
DSt:= tl DSt;
CSt:= tl CSt

```

This follows directly from Lecture 6, Slide 20.

3. Run the program `p1` from Question 1 in `hwhile`. Which output flag is appropriate here?

Please consult the Canvas page:

canvas.sussex.ac.uk/courses/12888/pages/while-programs-and-hwhile

on our Limits site for more info about `hwhile`. Ask the tutor in your seminar if you have problems with installation. Note that `hwhile` is also available on the SoftwareHub on the Chichester Lab machines (which are accessible remotely).

Answer: The `-i` flag as the result is a number.