## Assignment Project Exam Help

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#### **Functional Programming**

#### **General Concepts**

- Functional programs consist entirely of functions.
- A function can be defined in terms of other functions (previously
- seficed by the entire in the location of the primitives).
- The focus is in what is to be computed, not how it should be computed.
   Computed to the computed of t
- Modern functional languages are strongly typed (no run-time type errors) and have built-in memory management.
- Advantages: shorter programs, easier to understand, easier to design and main than in perative programs COCCT
- Disadvantage: often slower than imperative programs.

#### Reading list

- See web page for books
- www.haskell.org

#### **Examples of applications**

## Assignment Project Exam Help

- Music composition
- Theorem provers and proof assistants
   Graphical Previous POWCOGET.COM
- Expert Systems
- Telephony (Ericeson) eChat powcoder

#### Haskell

## Assignmentain example of the language in this module.

- A modern functional programming language
- Seventitip geters powers where com
- More information about Haskell, including the language report, learning resources, user manuals, etc. can be found on the web site www.dadkeweChat powcoder

#### Syntax of functional programs

The notation is inspired by the mathematical definition of functions, using equations.

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We can compute the square of a number using a function square

defined by the equation: https://powcoder.com

The role of the computer etcevaluate and display the office of the expressions that the programmer writes, using the available functions (like a sophisticated calculator).

#### **Example**

## Assignment Project Exam Help

square 6

the computer will display the result: 36

• As in mathematics, expressions may contain numbers, variables

- As in mathematics, expressions may contain numbers, variables or names of functions.
- For instance 36 square 6, x \* x are expressions Add WeChat powcoder

#### **Evaluation**

- To evaluate square 6 the computer will use the definition of square and replace this expression by 6 \* 6. Then using the predefined \* operation; it will find the result 36.
- sting an expression is a simplification process, also called reduction or evaluation.
- The goal is to obtain the value or normal form associated to the expression of a series of the community o

#### Examples

- square 6 → 6 \* 6 → 36
   36 is her are (for attack)
   ((3 + 1) + (2 + 1)) → ((3 + 1) + 3) → (4 + 3) → 7
- ②  $((3+1)+(2+1)) \rightarrow ((3+1)+3) \rightarrow (4+3) \rightarrow 7$ 7 is the value denoted by the expression ((3+1)+(2+1))

The *meaning* of an expression is its value.

#### Remark

• There may be several reduction sequences for an expression.

## And following is also a correct recognish sequence: Am Help

$$((3 + 1) + (2 + 1)) \rightarrow (4 + (2 + 1)) \rightarrow (4 + 3) \rightarrow 7$$

In both chatstp Saire is posses Coder.com

## Exercise Add WeChat powcoder

Can you draw a reduction graph of all possible reductions starting from

$$((3 + 1) + (2 + 1))$$

#### **Properties**

As significant forms: roject Exam Help In (pure) functional languages the value of an expression is uniquely determined by its components, and is independent of the order of reduction/
Advantage readabil to program.der.com

Non-termination:

Not all reduction sequences lead to a value, some reduction sequences of notice and at powcoder

#### **Example**

Let us define the constant function

```
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```

```
infinity = infinity + 1
```

- The Patition of Ind Wice Coles Commorm.
- For the expression

some equation sevue the state of normal forms).

#### **Exercise**

Can you draw a *reduction graph* of all possible reductions starting from fortytwo infinity?

#### **Strategies**

## As stingigh the normal form is an increase of exotagons ideal in parameters.

- The strategy of evaluation defines the reduction sequence that the language implements.
- language implements.

  Most pupular strategies OWCOder.com
  - Call-by-name (Normal order): reduce first the application using the definition of the function, and then the argument
  - 2 Gall-by-value (Applicative order): evaluate first the argument and therethe application using the defination of the function

#### Strategies, continued

# Remarks Softer in strategies require different number of reduction steps 1 p (efficiency).

- Call-by-name always finds the value, if there is one.
- Call by the Sin grand We make but Go Mo find a value.
- Haskell uses a strategy called *lazy evaluation*, which guarantees that in a presting the evaluation will find it. lazy evaluation = call-by-name + sharing

#### **Example: Strategies**

An example reduction graph for the expression: square (3+4)

Assignment Project Exam Help  $https://poweoder.com^{7*(3+4)}$ Add WeChat powcoder

Note: we underline each reducible expression (redex), all reductions lead to the same answer, and some reductions are longer than others.

#### **Example: Strategies**

The previous example had the shortest path for call-by-value.

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In this case, call-by-value gives the longest reduction path...

#### **Functional Values**

 Functions are also values, even though we cannot display them or print them.

type A, called the domain of the function, an element of type B, called the codomain.

• If a function f of type  $A \rightarrow B$  is applied to an argument x of type A,

- If a function f of type A → B is applied to an argument x of type A, it gives a result (f x) of type B.
- In Hackellith in thiop to associate a type to a function is:

square :: Integer  $\rightarrow$  Integer fortytwo :: Integer  $\rightarrow$  Integer

#### **Notation**

## Assumph menta Project Exam Help

- To avoid writing too many brackets there are some conventions:
  - Maying write potwistocker. Com square 3 instead of (square 3)
  - ► Application has precedence over other operations: square 3 + 1 means (square 3) + 1
  - Application associates to the test: DOWCOCET square square 3 means (square square) 3

#### **Syntax of Function Definitions**

Functions are defined in terms of equations.

Examples

## Assignment Projecty Exam Help We can also use conditional equations (aka guarded equations).

Examples

$$\begin{array}{l} \text{min } x \text{ https://powcoder.com} \\ | x > y = y \\ \text{sign } x \\ | x \text{Add = WeChat powcoder} \\ | x > 0 = 1 \end{array}$$

The latter is equivalent to, but clearer than:

if x < 0 then -1 else if x == 0 then 0 else 1

#### **Recursive Definitions**

In the definition of a function f we can use the function f:

```
fact :: Integer → Integer
fact n = if n==0 then 1 else n*(fact(n-1))
Recursive definitions are evaluated by simplification, as any other
and the simplification as any other others.
```

fact  $0 \rightarrow$ if 0 == 0 then 1 else  $0 * (fact (0 - 1)) \rightarrow$ if True then S exponentics of the conditional:

- Evaluate first the condition.
- If the result is Trivithen evaluate enly the expression in the left branch (then).
- If the result is False then evaluate only the expression in the right branch (else).

Therefore the only reduction sequence for fact 0 is the one shown above, and this program is terminating.

#### **Recursive Definitions, continued**

However, if we start with

As the reduction sequence representation of the control of the con

error is a predefined function that takes a string as argument. When evaluated it causes immediate termination of the evaluator and displays the string.

#### **Local Definitions**

## Assignment of Exam Help

or equivalently,

```
f x = let a = x/2 in a + 1
```

The words let in Swhere in the local little in

```
We can write several local definitions:
f x = aquaci (successor x) a the power of the square z = z * z ; successor x = x + 1
```

#### **Arithmetic Functions**

Arithmetic operations are also functions (primitives), used in infix notation: e.g.  $3\ +\ 4$ 

In Haskell we can use them in prefix notation if we enclose them in

## Arskeis genment Project Exam Help

- ullet + :: (Integer, Integer) ightarrow Integer
- $^{\bullet}\text{ ''}https:'/powcoder.com$

#### Examples

- 3 1 2 should be read as (3 1) 2 • (+) As the duccessor function at powcoder
- (\*) 2 is the function that doubles its argument
- Application has priority:

```
square 1 + 4 * 2 should be read as (square 1) + (4 * 2)
```

#### **Functional Composition**

## As Eulections are the building blocks of functional languages. Help one way of combining functions is composition.

Composition is itself a function (predefineds).

We can only compose functions whose types match.

square square square powcoder

#### **Types: General Concepts**

Values are divided in classes, called *types*.

Each type is associated with a set of operations. Response to the set of operations are the set of operations. The set of operations are the set of operations are the set of operations.

- Basic data types: Booleans, Characters, Numbers. In Haskell: Bool, Char, Int, Integer, Float ...
- Structured types. Tupes, Strings (biets er con In Haskell [Integer] is the type of lists of integers.
- Function types: Integer → Integer, Integer → Float input and returns an integer.
  - Convention: arrows associate to the right!

#### **User-defined types**

The programmer can also define new types.

School Air President Inustrial Carly be Expression that can be typed are considered erroneous and are rejected by the compiler without evaluation (static typing).

#### Advantada tilatically troo tangenerier.com

- Types help detecting errors at an early stage.
- Types help in the design of software since they are a simple form of specification. We Chat powcoder
   A program that passes the type controls and guaranteed to be

A program that passes the type controls is not guaranteed to be correct, but it is free of type errors at runtime.

#### **Polymorphism**

Type systems can be Assignameent expression at metatra, Help • polymorphic: some expressions have more than one type.

Example https://powcoder.com

where  $a_{t}$  by c are type variables. The c is c and c by c and c where  $a_{t}$  by c are c and c is c and c are c are c and c are c are c and c are c and c are c and c are c are c are c and c are c are c are c and c are c are c are c are c and c are c ar

Type variables can be instantiated to different types in different contexts.

Therefore (.) is a polymorphic function.

#### **Examples**

```
quad = square . square

Asequare interpretation  

quad :: Integer → Int

using: ... // 1
```

```
\underset{(\text{$n$ttps://powcoder,com$} \to \text{$Int)}}{\text{using:}}
```

```
But we can also define \texttt{sqrt}:: Integer \to Float and compose \texttt{fight} where \texttt{Right} powcoder
```

```
(.) :: (Int \rightarrow Float) \rightarrow (Int \rightarrow Int) \rightarrow (Int \rightarrow Float)
```

#### **Examples, continued**

# As steen frequency of the string of a control of the string of the strin

#### **Polymorphism and Overloading**

- Formally the language prolymorphic types is defined as I set of terms built out of type-variables (a, b, c), and type constructors which are either atomic (Integer, Float, ...) or take arguments (e.g.,  $T_1 \rightarrow T_2$ , [T]),
  - A partition stype representative of its of the obtained by substituting type variables by types.
  - Overloading is a related notion (also called ad-hoc polymorphism)
     where several functions with different types, share the came
     name.

#### **Example (Overloading)**

Arithmetic operations (such as addition) can be used both with integers or reals. But a polymorphic type such as

Assignment Project Exam Help is too geogran: It allows addition to be used with characters.

There are several solutions to this problem:

- Userdifferent symbols for addition on integers and on reals.
   E.g. Hard D. Sh. Can DOW COGET. COM
- Enrich the language of types:

E.g. + :: (Integer -> Integer -> Integer) \( \Lambda \)

Add WeChatFpoweoderFloat)

- Define a notion of type class.
  - E.g. in Haskell: (+) :: Num  $a \Rightarrow a \rightarrow a \rightarrow a$
  - (+) has type  $a \rightarrow a \rightarrow a$  where a is in the class Num.

#### **Type Inference**

Most modern functional languages do not require that the programmer provides the type for the expressions used. The compiler is able to provide the project Exam Help Intuitively:

- The expression is decomposed into smaller sub-expressions, and whe nattasic atomic expression is found, the information available is used (if it is a precefined constant) or otherwise it is assigned the most general type possible.
- The way that the different components are put together to form the
  expression indicates the constraints that the type variables must
  satisfy.

The type of an expression can be deduced from its components only.

#### Type Inference, continued

#### Axis ignment Project Exam Help square x = x \* x

```
the expression<sup>1</sup>
https://poweoder.com
```

square :: Integer  $\rightarrow$  Integer

## and therefore its argument cannot be a function. Add WeCnat powcoder

<sup>&</sup>lt;sup>1</sup>This expression is equivalent to (square square) 3 because application associates to the left.

#### **Disjoint Sums**

We can define several constructors in a type.

#### **Example:**

Assahesh Help Care Nation of the Care The Company of the Care The polymorphic, but we could define a type with polymorphic constructors.

## data Saltps://powcoder.com

The constructors are Empty and Cons (polymorphic).

Constructors are used to build terms. What distinguishes a constructor from a function is that VeChat powcoder

• There is no definition associated to constructor.

- Constructors can be used in patterns.

#### Example:

```
isempty Empty = True
isempty (Cons x y) = False
```

#### **Built-in Data Types**

- Integer
- Double
- Assignment Project Exam Help
  You can find the type of an expression using :type

(or just:t), for example:

Prehttps:True :: Bool

Prelude> :t 5

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Prelude> :t it
it :: Integer
Prelude> :t 'c'
'c' :: Char

#### Constructing data types: Pairs (x, y)

- Components do not need to have same type: (2, True)
- Built-in functions: fst, snd project the first and second Second Project Exam Help Project it ('a', Teue)

https://powcoder.com

• *n*-tuples: (2,3,5), (True,'c',42,(3,4)), etc.

Note that you can build also *n*-tuples from pairs: e.g.,

((Tracd), We Chat powcoder

Exercises. Write functions to:

- extract 'c' from ((True, 'c'), 42) using only fst and snd.
- extract 'c' from (True, 'c', 42, (3, 4))

#### Lists

• A collection of things of the same type: **Examples**: [1,2,3,7,9], [True, False, True],

Strings in Haskellare just to ject Exam Help

```
:, [], head, tail, null, length, ...
```

1: https://powcoder.com

```
head :: [a] -> a
tail :: [a] -> [a]
```

• We can generate lists in a number of different ways:

```
1:2:3:4:[]
[1, 2, 3, 4]
[1..4]
```

#### Lists: generation

Cons and append. Try these:

```
6: [7,8]
[1,2,3] ++ [4,5]
```

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What is the type of (++) ?

• Try these://powcoder.com
[10..1]
[5..11]
[3.Add WeChat powcoder

• List comprehension. Try these:

```
[x*x \mid x \leftarrow [1,2,3]]

[x*x \mid x \leftarrow [1..10], \text{ even } x]

[(x,y) \mid x\leftarrow[1..10], y\leftarrow[1..5]]
```

#### **Lists: writing functions**

We can write the built-in functions ourselves:

```
Aesignment Project Exam Help

hd [] error "list is empty"

hd (h:t) = h

tl [] error "list is empty"

tl (h:hups://powcoder.com

app [] x = x

app (h:t) x = h: (app t x)
```

- Here we dred using pattern matching possible order functions matter? What if we miss some cases?
- Exercise: can you think of a way of writing these functions without pattern matching?

#### Worked example

Write a function to sum all the elements of a list.

```
Example: sum [1..10] = 55
```

First try:

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#### Using guarded equations:

```
sum x https://powcoder.com
| null x = 0
| otherwise = head x + sum (tail x)
```

### Using parter draching eChat powcoder

```
sum [] = 0
sum (h:t) = h+sum t
```

Which way is better? Are there other ways?

#### Algebraic data types

We can define our own data types:

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data Suit = Club | Diamond | Heart | Spade

data List a = nil | Cons a (List a)

And we can write functions over these types using pattern matering: PS.//POWCOUCI.COIII

```
not True = False not False WeChat powcoder head Nil = error "list is empty" head (Cons x y) = x
```

## Assignment Project Exam Help

```
toList (Leaf a) = [a]
toList (Branch 1/r) = (toList 1) ++ (toList r)
Example: powcoder.com
```

```
[1,2] Add WeChat powcoder
```

Exercise: List to Tree? Insert in order?

#### **Summary**

- We have given a summary of many aspects of functional A Softwarming annual syntactic description of the topics in the
  - In the following lectures we will look at many of the topics in these notes again in more detail, and discuss foundations, implementations and applications of functional programming.
  - Try out examples, and also exercises, by experimenting with Haskell in the labs.
  - Test functions, find out about built-in functions, and know how to find out better withest functions
     DOWCOGET
  - Next: foundations of functional programming