

Topic 11 Assignment Project Exam Help

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More On Algorithms
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ICT167 Principles of Computer Science

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OBJECTIVES

- Be able to give a rough estimate of the running stigner (in basic Steps) of simple algorithms https://powcoder.com
- Explain the concept of recursion
 Give recursive algorithms for simple problems
- Trace the operation of recursive calls
- Be able to implement simple recursive algorithms in Java



OBJECTIVES

Be able to implement a binary search of a sorted arraignusing rejectorsion Help

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Reading:

Savitch Chapter 11 plus extra material



Example Algorithm

- Consider the common problem of finding (searching) a target value in a sorted array and returning some index at which it appears (or an indication if it does not appear at all)
- The next slide provides pseudo-code for a straight-forward solution for the case with an array of integers
 - The algorithm will return the index at which the target value first appears or -1 if the target value does not appear in the array
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Pseudo-code

```
Given an array a of integers and a target
integer value
let len = Assignment Project Exam Help
i = 0
while ((i < len) and (a[i] < target))
  i = i + 1 Add WeChat powcoder
endwhile
answer = -1
if (i < len) then
  if (a[i] == target) then
     answer = i
  endif
endif
```

Time Complexity of Algorithms

- When designing software and choosing between several ideast for algorithms it is often useful to get a rough idea of how long the algorithm will take to run Add WeChat powcoder
 Formal measures of this are called measures
- Formal measures of this are called measures of time complexity of an algorithm
- For example with our search algorithm we can say:



Time Complexity of Algorithms

- To search in 1000 items it might take about 500 iterations of the loop on average, or at worst 1000 iterationssignment Project Exam Help
- If we knew that it took 1 second to search through https://powcoder.com/1000 items then we might guess it would take about 1000/secondsh(about obliminutes) to search through 1 million items
- The time taken is roughly proportional to the size of the array to search

Time Complexity of Algorithms

- Measuring time complexity, estimating it and inventing quick algorithmais debig area of computer science research.
- We look at time complexity again later in this topic Add WeChat powcoder
 Note that there are other reasons to choose
- Note that there are other reasons to choose between one algorithm and another in specific circumstances
 - For example, space complexity measures of how much memory an algorithm needs

Recursion

- One way of inventing quick algorithms for some problems is to take a metal resident approach https://powcoder.com
- *An object is recursive if it partially consists of or is defined in terms of itself." N. Wirth
- An algorithm is a step-by-step set of rules to solve a problem; it must eventually terminate with a solution



Recursion

- A recursive algorithm uses itself to solve one or recursive algorithm uses itself to solve
- That is, in problem solving using recursion, a solution is expressed in terms of itself
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 Recursive methods implement recursive
- Recursive methods implement recursive algorithms
- A recursive method is one whose definition includes a call to itself



Recursion as a Problem Solving Tool

- Solution to task T:
 - Solve task The Whitch is and Italical in nature to task The but/smaller than T
- Example task weChat powcoder
 - Search a dictionary for a word



A Recursion Algorithm

```
If it is a one page dictionary then scan the
page for the word Project Exam Help
else
  open dictibus: /pawsodencomiddle
  determine which chalf contains the word
  if word is in first half then
     search 1st half of dictionary for word
  else
     search 2nd half of dictionary for word
  end if-else
end if-else
end algorithm
```

Recursive Definitions

- A recursive definition contains
 - A base part write Projected in the Project in the stop the recursion, and condition to stop the recursion, and
 - A recursive part, where each successive call to itself must be a "smaller version of itself" so that a base case is eventually reached



Example 1

- Definition of an integer constant (eg: 571) (decimal spigtantion) Pigject Exam Help
 - Any decimal digital recommendation of the second se
 - Any decimal digit followed by an integer constant Add WeChat powcoder
 Base: Any decimal digit (0 through 9)
- Recursive: Any decimal digit followed by an integer constant
- Recursive part reduces to the base part with repeated applications

Example 2

- The Fibonacci numbers:
 - 1, 1, Assignment Project Exam Help...
- The first nultiperpigwooder.com
- The second thumber is powcoder
- Each of the other numbers is the sum of preceding two numbers



Recursive Definition: Example 2

- fib(1): 1 // base part
- fib(2): Assignment Project Exam Help
- fib(n): fib(rhttpt)/ppwftb(lar_com

Add/WeChasiwevpaletrfor n > 2

- Eg:
- fib(3) = fib(2) + fib(1)



Recursive Methods

- Methods designed to solve problems by calling theirselve Project Exam Help
- Characteristics: of our counsing solution:
 - Calls a method to solve a smaller problem of the same type
 - Size of problem diminishes in successive calls
 - A base case is solvable directly
 - That is, a recursive method **must** have a terminating condition the recursive definition on the previous slide demonstrates this

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Recursive Fibonacci Method

```
static int fib(int n)
//pre-conditional Project Exam Help
  return Add WeChat powcoder
  else
                // recursive step
    return fib(n - 1) + fib(n - 2);
} // end fib
// a call to method fib
int x = fib(5);
// x will have the 5<sup>th</sup> Fibonacci
```

Recursive Fibonacci Method

 Invocations of method fib during calculation of the 5th Fibonacci pumber Help

```
fib(4) +Add WeChat powcader)
                       fib(2)
fib(5)
                       fib(2)
         fib(3)
                       fib(1)
```

Another Example

- A recursive function for summing array elementssignment Project Exam Help
- Task: Sumithe first melements of array A
- sum (A, n) isdd WeChat powcoder
- A[0], if n = 1 // base case
- A[n-1] + sum (A, n-1), if n > 1 // recursive step



Recursive Sum Method

```
static int sum(int[] A, int n)
//pre-conAssignment Project ExhmHelp

{
          https://powcoder.com
          if (n == 1)
                Add WeChat powcoder
                return A[0]; //base case
    return A[n-1] + sum(A, n-1);
}
```



Recursive Sum Method

RecursiveSumArray.java

```
// RecursiveSumArray.java
// Sums the elements of an array recursively Assignment Project Exam Help
public class https://poiwcoden.comay {
 public static void main(String[] args) {
    Add WeChat powcoder
   int[] anArray =
            {98,76,65,105,45,1,199,15,88,100};
 // determine sum of elements of the array
 int arraySum;
 arraySum = Sum(anArray, anArray.length);
```

RecursiveSumArray.java

```
System.out.println("The numbers are:");

for(intAssignmentProjectAtrantHelpgth; i++)

System.out.println(anArray[i]);

https://powcoder.com

System.out.println("The sum of array

Add WeChatlpowcoder " + arraySum);

System.out.println("End of program.");

} // end main
```



RecursiveSumArray.java

```
static int Sum(int[] A, int n)
//pre-cassignment Project Exam Help
{
    https://powcoder.com
    if (n == 1)
        returAddaWeChat powcodese case
    return A[n-1] + Sum(A, n-1);
    } // end Sum
}//end of class RecursiveSumArray
```



- A common strategy is:
- Given a problem broisse n, splitthe problem into two subupsoplemsder.com
 - A problem of size of which is directly solvable //the base case
 - A problem of size n 1 that involves recursion



- Example:
- A methodsignmentiplyithe integer numbers m and n https://powcoder.com
 - Assume we know our addition table but not the multiplication table!

```
// Recursive multiply method
// Performs multiplication using the + operator Assignment Project Exam Help
static int Multiply (int m, int n)
// PRE: Assignehttps://powgoder.com) && n > 0
// POST: returns m * n Chat powcoder
   if (n == 1)
      return m; // base case
  else
                    // recursive step
      return m + Multiply (m, n - 1);
```

```
Example of a call to the previous method:
Scanner i Assigtament Project Examile pstem.in);
System.out.print("Enter an integer: ");
int y = input.nextInt();
System.out.println("\nThe product of " +
  x+" and "+y+" is: " + Multiply(x, y));
// Alternatively,
int result = Multiply(x,y);
```

Exercise for Topic 11

 Give a recursive Java method for writing out any givens string time time time to be a second to the s

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Recursion: Pros and Cons

- A powerful problem solving tool elegant and conciseAssignment Project Exam Help
- Not necessarily/more efficient than nonrecursive (looping = iterative) solution
- Recursive routines can be slower and require more memory space due to overheads associated with function calls
- Can be difficult to debug and may result in infinite recursion

Recursion: Pros and Cons

- Infinite recursion is worse than infinite loop
 - It makes the composite of Fangule by using up all available memory (stack overflow)
- Note that there are general techniques for getting rid of recursion from an algorithm and making an iterative version (but the idea might have been recursive originally and it might be easier to understand the recursive version)



To Recurse or Not To Recurse? That is the Question

- Choose recursion when
 - The problem is tated recursively and the recursive solution appears less complex https://powcoder.com
 That is, when it makes the code easier to
 - That is, when it makes the code easier to understandand without reflicted to is not important
- Choose a non-recursive algorithm when
 - Both versions appear equally complex
- Methods re-written without recursion typically have loops, so they are called iterative methods
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To Recurse or Not To Recurse? That is the Question

- Iterative methods generally run faster and use less methods
- If the use aftastablevisanaption
 - Use table looking (see next slide)



Table Lookup

- Replaces a sequence of instructions with a simple array look Project Exam Help
- Out-performs both weatersive and iterative algorithms
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- Recall the common problem of finding a target value in eat sorted Farra y land returning some index at which it appears (or an indication if it does not appear at all)

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 Here is another (recursive) idea for a solution:
- - Start in the middle and (if the target value is not there) search either the first half or the second half depending on where the target would be



- Here is pseudocode:
- given array **a** of integers and target integer value
- output binsearch(a, 0, length(a)-1, target)
- binsearch(int array a, int first, int last, int target)
- if (first>last) Assignment Project Exam Help
- mid= (first+last)/2 (integer division) https://powcoder.com
- if (a[mid]==target) return mid
- if (a[mid]>target) Add WeChat powcoder
- return binsearch(a, first, mid-1, target)
- else
- return binsearch(a, mid+1, last, target)
- The idea of binsearch is to find an index in the range first to last inclusive such that the target value appears there in the array. Here is one possible Java implementation ...

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Here is pseudocode:

```
Given array a of integers and target value output binsearch(a, 0, length(a)-1, target)

Assignment Project Exam Help
binsearch(int array a, int first, int last,

https://powcoder.com int
```

```
target)
if (first>last) WeChat powcoder

mid = (first+last)/2 // integer division
if (a[mid] == target) return mid
```



```
if (a[mid] > target)
    returnsighmentProject ExamiHest, mid-
1, target)
https://powcoder.com
else
    return Add WeChat powcoder
binsearch(a, mid+1, last, target)
```



- The idea of binsearch is to find an index in the rangesignment to jeat Examples ive such that the targety alue appears there in the array
- Here is one possible Java implementation ...



```
/ * *
Class for Assignment Project Exam Help
integers.
To search the https://powcodernomtely filled array
b, use the following:
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ArraySearcher bSearcher new ArraySearcher (b);
 int index = bSearcher.find(target);
where index will be given an index of where
target is located
otherwise index will be set to -1 if target is
not in the array
* /
```

```
public class ArraySearcher {
  privateAssignment Project Exam Help
   // constructor
  https://powcoder.com
public ArraySearcher(int[] theArray)
   /** Precondi Add We Chat powsoder and is sorted
                    from lowest to highest */
     a = theArray;
     // a is now another name for theArray
   } // end constructor ArraySearch
```



```
/** Uses binary search to search for target in
   a[first] through a[last] inclusive
   Returns the index of target if target is found.
   RetuAssighment Projecti Exam Helpd. */
Add WeChat powcoder
  int result = -1;
  int mid;
  if (first > last)
     result = -1;
  else {
```

```
mid = (first + last) / 2;
         if (target == a[mid])
         result = mid;
Assignment Project Exam Help
else if (target < a mid)
            results://pobinarySearch(target,first,
                                             mid-1);
        else Add/WeChatpewsodemid])
            result = binarySearch(target, mid+1,
                                               last);
      return result;
  } // end binarySearch
} // end class ArraySearcher
```

Binary Search Demo

```
import java.util.*;
public classighment Project Exampelp
  System. Add Wechatrpowcoder 10 integers in
                       increasing order.");
    System.out.println("One per line.");
    Scanner keyboard=new Scanner (System.in);
    for (int i = 0; i < 10; i++)
       a[i] = keyboard.nextInt();
    System.out.println();
```

Binary Search Demo

```
System.out.print("a["+i+"]="+a[i]+" ");
System.out.println();
System out println() Exam Help
ArraySearcher finder = new
        https://powcoder.comraySearcher(a);
String and WeChat powcoder
do {
  System.out.println("Enter a value to
                          search for:");
  int target = keyboard.nextInt();
  int result = finder.find(target);
```

Binary Search Demo

```
if (result < 0)
           System.out.println(target + " is
                            not in the array.");
        else
          Assignment Project Exam Help
System.out.printin (target + " is at
              https://powcoder.comdex " + result);
        System.out.println("Again?(yes/no)");
        ans = Add WeChatrpoxycoder
     } while (ans.equalsIgnoreCase("yes");
     System.out.println("May you find what
                    you're searching for.\n");
  } // end main
} // end class ArraySearcherDemo
```



How Long Does It Take?

- It is a bit harder to analyze the time complexity goff bin ary search (than the simple iterative version given earlier in the topic)
- Eg: to search through 1000 items we (in a couple of operations) break the problem down into a search through 500 items, then 250 items, then 125 items, then 63, then 32, then 16, then 8, then 4, then 2, then we must have found our target (or returned –1)
 - There are about 10 such steps

How Long Does It Take?

- In general to search through N items, we take log₂(N) Assignment Project Exam Help
 - Recall 10 ppis about 2 to the tenth
- To search though 1 million items only takes twice as long!!
- The individual steps may take a little longer (i.e. consist of several basic operations) but, for large N, this is outweighed



How Long Does It Take?

Eg: made up figures ...

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search times	simple linear	binary
1 item	tps://powcoder.com	.01 sec
10 items A	d 0 10seC hat powcode	e 03 sec
1000 items	1 sec	0.1 sec
1 million items	17 minutes	0.2 sec

So binary search is a much better searching algorithm

Algorithm Efficiency

- We have seen that choosing the right algorithms fonther jobjean sometimes make enormous differences to the efficiency of programs
- Many important problems and possible algorithmic solutions have been studied for complexity and other efficiency issues

Algorithm Efficiency

- Eg: getting a really big job done faster
 - Allocates imports Pudients From Wells ity places in less than one hour instead of several days, or

 - Timetabling, or Add WeChat powcoder
 Many scientific and engineering applications, or
 - Internet searches, or
 - Searching and sorting in large databases, etc.



Algorithm Efficiency

- Eg: getting a reasonably large job done very Assignment Project Exam Help
 - Graphics introduced ity, orm

 - Games, or Add WeChat powcoder Finding words in files or emails on a PC, etc.



- Note that you will sometimes see the big-oh notation to express the order of magnitude measure on thou long an algorithm takes to solve a problem
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 Eg: saying that our simple linear search
- Eg: saying that our simple linear search algorithm is O(N) means that its running time is proportional to N where N is the size of the data



- You will see O(log₂(N)) for binary search and O(N²) for signment or tijngt algorithms, etc.
- These giventhe: implementer a rough idea of which algorithms are best for the problem
- You may also see reports that certain problems are O(N) or O(N²) or O(N³) or O(log₂N), etc.



- This means that it has been mathematically proved that this is the best time complexity possible for any algorithm to solve that problem
 - Add WeChat powcoder

 It is impossible to find a better algorithm
- Eg: to sort N items takes O(N log N) steps on average
- No algorithm (even one not yet invented) can do better than that on average

Insertion sort takes O(N²) steps on average, quicksottstakes O(N) log M) insteps on average. Quicksort is the state of the control of the con

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sorting	insertion	quicksort
1 item	.001 sec	.010 sec
1000 items	17 minutes	100 sec
1 million items	32 years	2 days



Grouping Algorithms by Efficiency

- Most algorithms execute in polynomial time, expressediament/(N) jecohstanttelp> 0
- Eg: O(N) https://pearctimecom
- O(N2) A is quadraticationer
- $O(N^3)$ is cubic time
- Algorithms whose running time is independent of problem size are known as constant time algorithms
- Big-O notation: O(1)



Grouping Algorithms by Efficiency

- Algorithms requiring time proportional to a^N
 (where assistance Staint) Exent Holy n as
 exponential algorithms.com
- Execution times for exponential algorithms increase extremely fast with problem size
- Exponential algorithms are not suitable for any values of N except very small



Growth Rates for Selected Algorithms

 Average running times of some searching and sorting algignithms Project Exam Help

Algorithm https://pow	Efficiency -average case
Sequential searchdd WeCh	appwcoder
Binary search	$O(\log_2 N)$
Bubble sort	$egin{array}{c} \mathbf{O}(N^2) \\ \mathbf{O}(N^2) \end{array}$
Selection sort	
Quick sort	$O(N \log_2 N)$



Calculating Running Time in Big-O Notation

- An algorithm without loops or recursion requires (Sign) time roject Exam Help
- An algorithm with Materations requires O(N) time
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- Eg:

```
for i = 1 to N
    statements without any more looping
endfor
```



Calculating Running Time in Big-O Notation

- An algorithm with one loop nested inside another Anaisnquad Patic efficientely O(N²)
- Eg: https://powcoder.com

```
for i = 1 Atd WeChat powcoder
  for j = 1 to N
    statements without more looping
  endfor
endfor
```



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