



# INFO20003 Database Systems

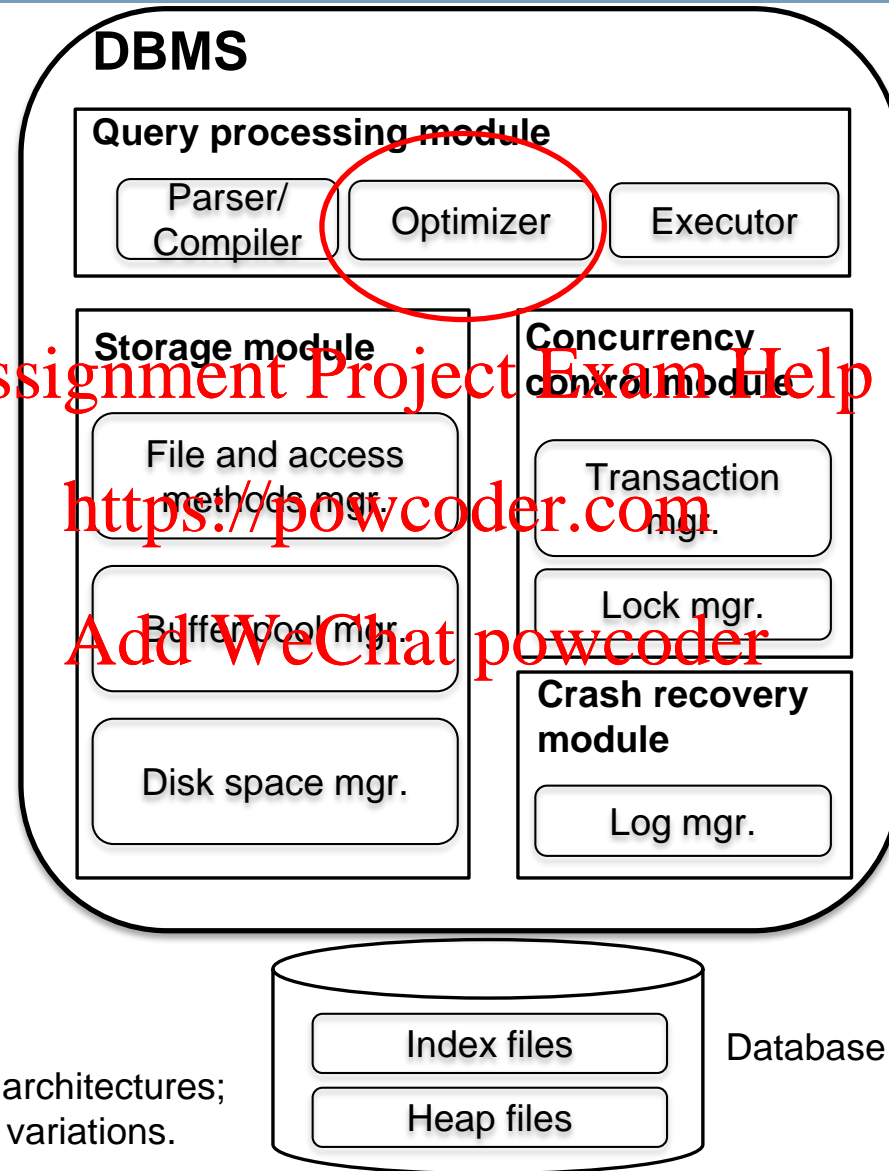
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Lecture 13  
Query Optimization Part I

# Remember this? Components of a DBMS



**TODAY &  
Next time**

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This is one of several possible architectures; each system has its own slight variations.



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- Overview
  - Query optimization
  - Cost estimation
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*Readings: Chapter 12 and 15, Ramakrishnan & Gehrke, Database Systems*



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Query

```
Select *  
From Blah B  
Where B.blah = "foo"
```

Query Parser

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Query Optimizer

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Plan  
Generator

Plan Cost  
Estimator

Catalog Manager

Schema

Statistics

Query Plan Evaluator



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- Typically there are many ways of executing a given query, all giving the same answer
- Cost of alternative methods often **varies enormously**
- Query optimization aims to find the execution strategy with the lowest cost

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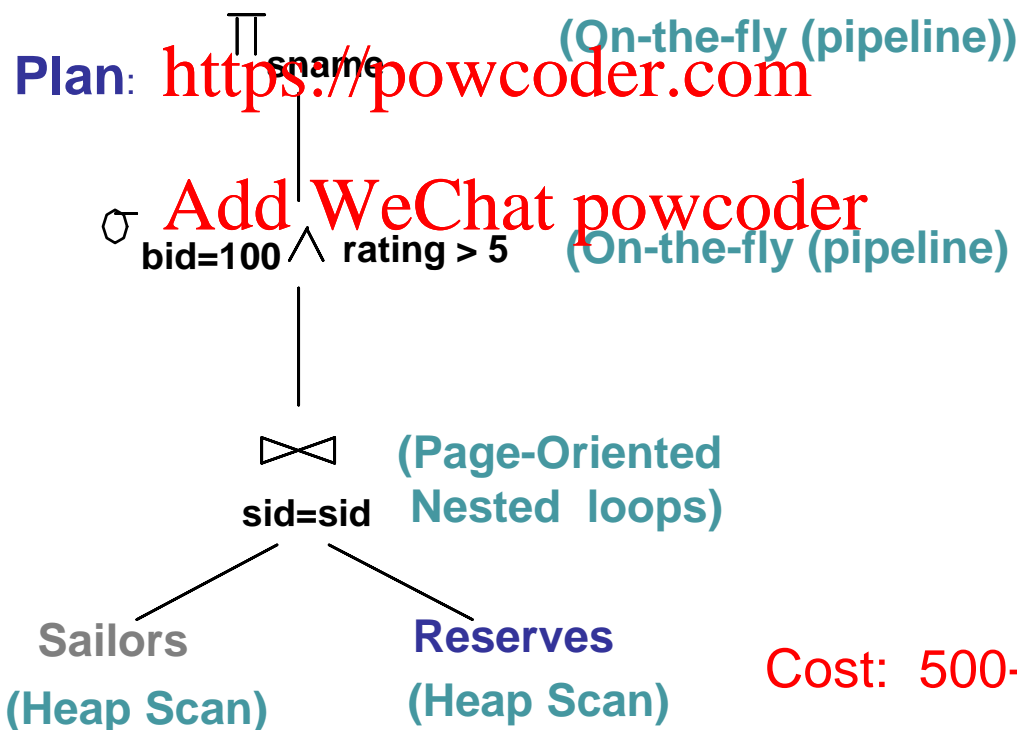
- We will cover:
  - Relational algebra equivalences
  - Cost estimation
  - Result size estimation and reduction factors
  - Enumeration of alternative plans

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- A tree, with relational algebra operators as nodes and access paths as leaves
- Each operator labeled with a choice of algorithm

SELECT sname from Sailors NATURAL JOIN Reserves  
WHERE bid = 100 and rating > 5





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*Readings: Chapter 15, Ramakrishnan & Gehrke, Database Systems*



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Sailors (*sid*: integer, *sname*: string, *rating*: integer, *age*: real)

Reserves (*sid*: integer, *bid*: integer, *day*: dates, *rname*: string)

Boats (*bid*: integer, *bname*: string, *color*: string)

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Example:

```
SELECT S.sname  
FROM Reserves R, Sailors S  
WHERE R.sid=S.sid AND  
R.bid=100 AND S.rating>5
```

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Query optimization steps: <https://powcoder.com>

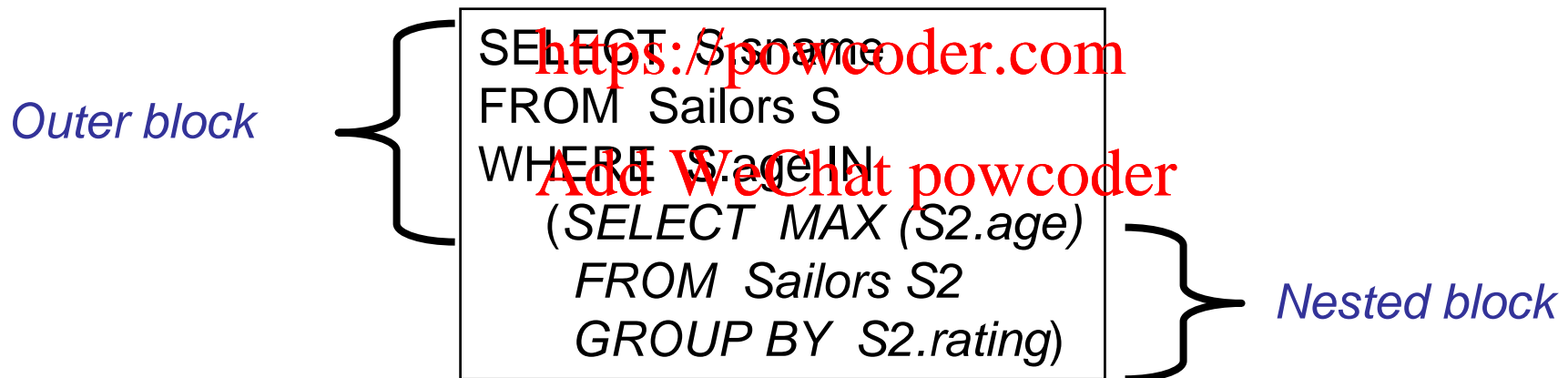
1. Query first broken into "blocks" [Add WeChat powcoder](#)
2. Each block converted to relational algebra
3. Then, for each block, several alternative query plans are considered
4. Plan with the lowest estimated cost is selected



# Step 1: Break query into query blocks

- Query block is any statement starting with select
- Query block = unit of optimization
- Typically inner most block is optimized first, then moving towards outers

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Query:

```
SELECT S.sid  
FROM Sailors S, Reserves R, Boats B  
WHERE S.sid = R.sid AND R.bid = B.bid AND B.color = "red"
```

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Relational algebra:

$$\pi_{S.sid}(\sigma_{B.color = \text{"red"}}(Sailors \bowtie Reserves \bowtie Boats))$$



- **Selections:**  $\sigma_{c_1 \wedge \dots \wedge c_n}(R) \equiv \sigma_{c_1} \left( \dots \left( \sigma_{c_n}(R) \right) \right)$  (*Cascade*)  
 $\sigma_{c_1} \left( \sigma_{c_2}(R) \right) \equiv \sigma_{c_2} \left( \sigma_{c_1}(R) \right)$  (*Commute*)
- **Projections:**  $\pi_{a_1}(R) \equiv \pi_{a_1} \left( \dots \left( \pi_{a_n}(R) \right) \right)$  (*Cascade*)  
 $a_i$  is a set of attributes of R and  $a_i \subseteq a_{i+1}$  for  $i = 1 \dots n - 1$
- These equivalences allow us to ‘push’ selections and projections ahead of joins.

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## Selection:

$$\sigma_{\text{age} < 18 \wedge \text{rating} > 5} (\text{Sailors})$$

$$\longleftrightarrow \sigma_{\text{age} < 18} (\sigma_{\text{rating} > 5} (\text{Sailors}))$$

$$\longleftrightarrow \sigma_{\text{rating} > 5} (\sigma_{\text{age} < 18} (\text{Sailors}))$$

## Projection:

~~$$\pi_{\text{age}, \text{rating}} (\text{Sailors}) \longleftrightarrow \pi_{\text{age}} (\pi_{\text{rating}} (\text{Sailors})) \quad ?$$~~

$$\pi_{\text{age}, \text{rating}} (\text{Sailors}) \longleftrightarrow \pi_{\text{age}, \text{rating}} (\pi_{\text{age}, \text{rating}, \text{sid}} (\text{Sailors}))$$



- A projection commutes with a selection that only uses attributes retained by the projection

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$\pi_{\text{age, rating, sid}} (\sigma_{\text{age} < 18 \wedge \text{rating} > 5} (\text{Sailors}))$

$\longleftrightarrow \sigma_{\text{age} < 18 \wedge \text{rating} > 5} (\pi_{\text{age, rating, sid}} (\text{Sailors}))$

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$\pi_{\text{age, sid}} (\sigma_{\text{age} < 18 \wedge \text{rating} > 5} (\text{Sailors}))$

~~$\longleftrightarrow \sigma_{\text{age} < 18 \wedge \text{rating} > 5} (\pi_{\text{age, sid}} (\text{Sailors}))$~~

?

$$R \bowtie (S \bowtie T) \equiv (R \bowtie S) \bowtie T \quad (\text{Associative})$$

$$(R \bowtie S) \equiv (S \bowtie R) \quad (\text{Commutative})$$

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- These equivalences allow us to choose **different join orders**

- Converting selection + cross-product to join

$$\sigma_{S.sid = R.sid} (\text{Sailors} \times \text{Reserves})$$

$$\leftrightarrow \text{Sailors} \bowtie_{S.sid = R.sid} \text{Reserves}$$

- Selection on just attributes of S commutes with  $R \bowtie S$

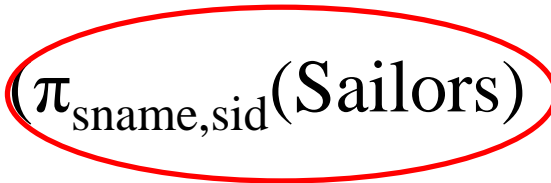
$$\sigma_{S.age < 18} (\text{Sailors} \bowtie_{S.sid = R.sid} \text{Reserves})$$

$$\leftrightarrow (\sigma_{S.age < 18} (\text{Sailors})) \bowtie_{S.sid = R.sid} \text{Reserves}$$

- We can also “push down” projection (*but be careful...*)

$$\pi_{S.sname} (\text{Sailors} \bowtie_{S.sid = R.sid} \text{Reserves})$$

$$\leftrightarrow \pi_{S.sname} (\pi_{sname, sid} (\text{Sailors})) \bowtie_{S.sid = R.sid} \pi_{sid} (\text{Reserves})$$







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- Overview
  - Query optimization
  - Cost estimation
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*Readings: Chapter 15, Ramakrishnan & Gehrke, Database Systems*



1. Query first broken into “blocks”
2. Each block converted to relational algebra
3. Then, for each block, several alternative **query plans** are considered
4. Plan with lowest **estimated cost** is selected

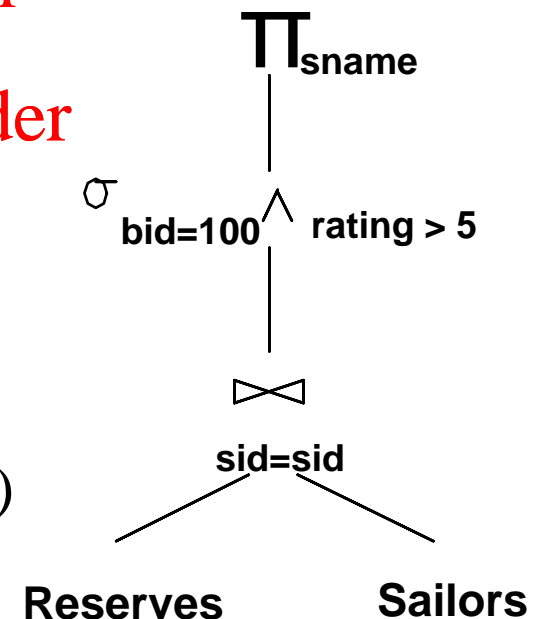
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```
SELECT S.sname
FROM Reserves R, Sailors S
WHERE R.sid=S.sid AND
      R.bid=100 AND S.rating>5
```

$\pi_{(sname)} \sigma_{(bid=100 \wedge rating > 5)} (Reserves \bowtie Sailors)$





Queries

```
Select *  
From Blah B  
Where B.blah = "foo"
```

3. What plans are considered?

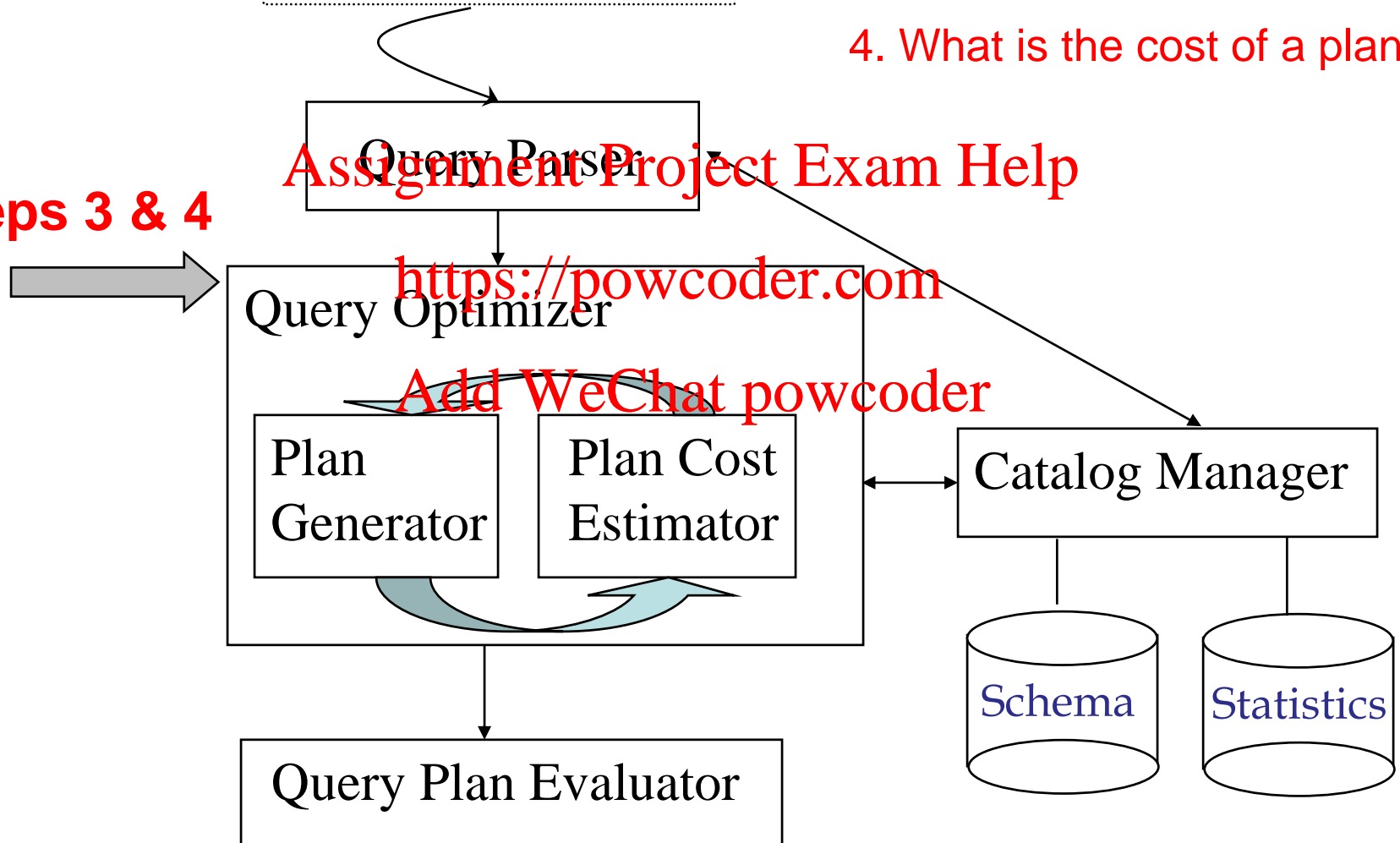
4. What is the cost of a plan?

**Steps 3 & 4**

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- For each plan considered, must estimate cost:
  - Must **estimate size of result** for each operation in tree
    - Use information about input relations (from the system catalogs), and apply rules (**discussed next**)
  - Must **estimate cost** of each operation in plan tree
    - Depends on input cardinalities
    - We've already discussed how to estimate the cost of operations (sequential scan, index scan, joins)
    - Next time we will calculate the cost of entire plans...

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- To decide on the cost, the optimizer needs information about the relations and indexes involved. This information is stored in the system **catalogs**.
- **Catalogs** typically contain at least:
  - # tuples (NTuples) and # pages (NPages) per relation
  - # distinct key values (NKeys) for each index (or relation attribute)
  - low/high key values (Low/High) for each index (or relation attribute)
  - Index height (Height(I)) for each tree index
  - # index pages (NPages(I)) for each index
- Statistics in catalogs are updated periodically

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- Consider a query block:

```
SELECT attribute list
FROM relation list
WHERE predicate1 AND ... AND predicate_k
```

- Maximum number of tuples in the result is the **product** of the cardinalities of relations in the FROM clause
- Reduction factor (RF)** associated with each predicate reflects the impact of the predicate in reducing the result size. RF is also called **selectivity**.

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- Single table selection:

$$\text{ResultSize} = NTuples(R) \prod_{i=1..n} RF_i$$

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- Joins (over k tables):

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$$\text{ResultSize} = \prod_{j=1..k} NTuples(R_j) \prod_{i=1..n} RF_i$$

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- If there are no selections (no predicates), reduction factors are simply ignored, i.e. they are ==1



- Depend on the type of the predicate:
  1. Col = value  
**RF = 1/NKeys(Col)**
  2. Col > value  
**RF = (High(Col) – value) / (High(Col) – Low(Col))**  
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  3. Col < value  
**RF = (val – Low(Col)) / (High(Col) – Low(Col))**  
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  4. Col\_A = Col\_B (for joins)  
**RF = 1/ (Max (NKeys(Col\_A), NKeys(Col\_B)))**
  5. In no information about Nkeys or interval, use a “magic number” 1/10  
**RF = 1/10**





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Sailors (S): NTuples(S) = 1000, Nkeys(rating) = 10 interval [1-10],  
age interval [0-100], Nkeys(sid)=1000

*SELECT \* FROM Sailors WHERE rating = 3 AND age > 50;*

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**Calculate result size:**

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**NTuples(S) = 1000**

**RF(rating) =  $1/10 = 0.1$**

**RF(age) =  $(100-50)/(100-0) = 0.5$**

**ResultSize = NTuples(S)\*RF(rating)\*RF(age)**

**=  $1000*0.1*0.5 = 50$  tuples**

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- What is query optimization/describe steps?
- Equivalence classes
- Result size estimation

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- Important for Assignment 3 as well

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- Query optimization Part II
  - Plan enumeration

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