Logic and AI Programming:

Introduction to Logic Introduction to Prolog

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October – December

Course Material

Course material will be available via CATE, including signment Project Exam Help

- ✓ Notes https://powcoder.com
- ✓ Tutorial Exercises Chat powcoder
- ✓ Tutorial Exercise Solutions
- ✓ Coursework

CONTENTS

Introduction to logic

Propositional lagiroject Exam Help

- Syntax
- Semanligst freuth power oder.com
 Rules of inference (Natural Deduction)

Predicate dog We Chat powcoder

- Syntax
- Informal semantics
- Rules of inference (Natural Deduction)

Prolog programming

Time permitting: Probabilistic Prolog Abductive Reasoniong



Books

background reading on logic

- Any book on logic will have useful examples.
- Richard Spencer-Smith, Logic and Prolog, Harvester Wheatsweathat The Library has a number of copies)
- Jim Woodcock and Martin Loomes, Software Engineering Mathematics", Pitman Publishing



Books Prolog



• Ivan Bratko, "Prolog programming for Assignment Project Exam Help artificial intelligence", Addison-Wesley, Third Edition, 200 and 180.

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Assessments and Examination

- One Logic Coursework
- One Prolog Lab Assessment Help
- One Examination in May: com

Paper M1 (Paddr We Chatgrow codergic) will have:

- two questions on Logic and
- two questions on Object-Oriented Design

Relevance of this course to Spring Term Modules

- Logic-based Learning course
- Introduction to Artificial intelligence
- System Verhed Wie Chat powcoder
- Argumentation and Multi-Agent Systems

and to a lesser extent

- Databases Assignment Project Exam Help
 - Database httpsiages, e.g. relational calculus and some features of SQL Add WeChat powcoder
 Datalog: emerging e.g. in data integration,
 - Datalog: emerging e.g. in data integration, information extraction, network monitoring, security and cloud computing

Logic has many applications in computing

For example:

• Basis of as farming of projects Farming of a languages, projects Farming of Set Programming).

• Basis of verification tools to reason about C, Java and JavaScript programs, and algorithms for concurrency, e.g. using Separation Logic.

• Software engineering: Formal specifications and formal supported to be a specification of the support of the

How do you https://powcoderogram is "correct"? Add WeChat powcoder Review, again and again and

- Review the spec
- Review the design description
- Review the code

Test, again and again and

- Unit testing

 Assignment Project Exam Help
- Integratiohttestingowcoder.com
- Validation testime Chat powcoder

But that is not enough.

How many tests do you run to be sure the system is cortetne.//powcoder.com

- ✓ Logic provided Wethatopowcoderg the system correct and
- ✓ this can be automated too.



Logic is also useful more generally in life

Clear thinking

• Judging validity of arguments and justification to the composition of arguments and justification to the composition of the c

- Spotting in colds Wterholes owcoder
- Awareness and avoidance of ambiguities of natural language

Which of the following arguments are valid?



- Advertisement for a computing book: If you don't use tempenters jest Examt Heled this book. But hope are owners who uses computers. So you need this book.
- ➤ If you work hard you will succeed. So if you do not succeed you have not worked hard.

Which of the following arguments are valid?

Heard in a radio interview with a well-known polishers. Project Examples have come from thes Plow concertaing good has resulted for us from our membership of the EU.

More reasoning exercises

- 1. All the trees in the park are flowering trees.
- 2. Some of the trees in the park are dogwoods.
- 3. All dogwoods in the park are flowering trees.

Assignment Project Examine the first two statements are true, the third

statement is

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- A. true
- B. false
- C. uncertain



More reasoning exercises

- 1. All the this signment Project Exam Help
- 2. All the roses in Zoe's garden are yellow.
- 3. All the flowers https://gaptowacoder.voormar yellow

If the first two statements we can the provided is

- A. true
- B. false
- C. uncertain

More reasoning exercises

- Fact 1: All dogs like to run.
- Fact 2:
- Some dogs like to swim.
 Some dogs look like their owners.

 Project Exam Help Fact 3:

If these three statements are facts, which of the following statements must also be a lace? / powcoder.com

- I.
- All dogs who like to swim look like their owners.

 Dogs who like to swim also like to run. II.
- Dogs who like to run do not look like their owners. III.
- Α. I only
- **B**. II only
- II and III only
- D None of the statements is a known fact.

Some arguments – Are they valid?

- It has been proven that all heroin addicts smoked his signmenta Project Examille! Therefore, smoking maniful parteader tooheroin addiction. Add WeChat powcoder
- ➤ We cannot win the war on poverty without spending money. So if we do spend money we will conquer poverty.

Another argument – Is it valid?

> One of the old arguments of tobacco spokesmen against the glaim that smeking causes lying cancer: Lung cancer is more common among male smokers than the among temale smokers. If smoking were the cause of lung cancer, this would not be true. The fact that lung cancer is more common among male smokers means that it is caused by something in the male make-up. If follows that lung cancer is not caused by smoking, but something in the male make-up.

Propositional Logic

- A good place to start.
- It is the core of many logics.

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Components of a logic

- Language:
 - alphabet symbols

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 - syntax : rultepforpouting to gether the symbols to make grammatically correct sentences.
- Semantics: meaning of the symbols and the sentences.
- Inference rules

The Propositional Language: Alphabet

Propositional symbols

```
e.g. use_conjunctst, Projects Fook, Help, r, s, p1
```

• Logical cohtnectipues coder.com

```
and (conjunction) wcoder
```

: (inclusive) or (disjunction)

 \neg : not (negation)

sometimes denoted as ~

 \rightarrow : implication (if-then)

The Propositional Language: Syntax of a grammatically correct sentence

(well formed formula, wff)

- A propositional symbol is a wff.
- If W, Wasignman Projects and Help are

```
¬ (W) https://poweorderimes written as ~(W) (W1 \land W2) Add WeChat powcoder (W1 \lor W2) (W1 \rightarrow W2) (W2 \leftarrow W1) (W1 \leftrightarrow W2)
```

• There are no other wffs.

Examples

Suppose p, q, r, s, t are propositions. Then: Assignment Project Exam Help $(p \rightarrow q)$ (r \ \ \ t) https://powcoder.com $(p \rightarrow q)$ Addi Washat wowcoder $((p \rightarrow q) \lor ((p \land r) \rightarrow \neg (s)))$ is a wff $((p \rightarrow q) \lor ((p \land r) \rightarrow \neg(s)))$ Draw a parse tree.

Examples

Passing the exams and the project implies passing Arignment Project Exam Help

```
(pass_exams \ hatps:p/pojweodes.coMSc
```

You do not pass the MSc and you do not get a certificate if you do not pass the exams or you do not pass the project.

Exercise

- Formulate the first two arguments from the beginning is the beginning in the beginning is the beginning in t
- Advertisemehttpsr/apcompdtingdmok: If you don't use computers you don't need this book. But you are a person who uses computers. So you need this book.
- ➤ If you work hard you will succeed. So if you do not succeed you have not worked hard.

Some notes on simplifying syntax

• To avoid ending up with a large number of brackets signment repetite van Halpst brackets. https://powcoder.com

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Examples:

```
(p \rightarrow q) can be written as p \rightarrow q

((p \rightarrow q) \lor r) can be written as (p \rightarrow q) \lor r.
```

• "— "binds more closely than the other connectives." This Projecte Example 10 arop some brackets. https://powcoder.com

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Example

$$(\neg (p) \land q) \rightarrow t$$
 can be written as
 $(\neg p \land q) \rightarrow t$

 • A and ∨ bind more closely than → and ↔. This can be used itendropts Broje brackets. Help

Examples: https://powcoder.com
$$(\neg p \land q) \rightarrow t$$
 can be written as Add WeChat powcoder
$$\neg p \land q \rightarrow t.$$

$$(p \land q) \rightarrow (r \lor s)$$
 can be written as $p \land q \rightarrow r \lor s$.

Binding Strength of the Connectives

To avoid having to use many brackets, there is a convention of the transfer transfer the transfer transfer to the transfer tra

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Also: Add WeChat powcoder

- Order of precedence
- Binding priority

Binding Strength of the Connectives

Strongest Assignment Project Exam Help

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 \rightarrow

Weakest

 \longleftrightarrow

Binding conventions: Examples

- $p \vee q \wedge r$ is understood as $p \vee (q \wedge r)$
- ¬p ∨ q Assignment Project Exam Help (¬p) ∨ q
- $p \rightarrow q \leftrightarrow r$ is understood as $(p \rightarrow q) \leftrightarrow r$

I prefer the first and third bracketed versions. They are more clear, and having a few brackets is not much of a burden! Please don't write unreadable formulas like

$$p \lor \neg q \to \neg r \leftrightarrow \neg \neg s \land t \lor \neg u$$

Use brackets to remove ambiguity

Example:

is ambiguous. https://powcoder.com

In general Add WeChat powcoder

$$P \rightarrow (Q \rightarrow R)$$

and

$$(P \rightarrow Q) \rightarrow R$$

are not equivalent (do not have the same meaning).

Binding conventions

```
So p \rightarrow q \rightarrow r
is a problem.

It needs brackets to disambiguate it.

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But p \wedge q \wedge r and p \vee q \vee r
are fine (to be discussed later).
```

Exercise:

Which of the following are wffs?

Assume

p, q, r, sad, happy, tall, rich, work_hard, powcoder.com steal, borrow, Addd posses powcoder are propositional symbols.



- rich \rightarrow happy
- $(p \lor q) \land (r \to p)$ Project Exam Help
- $p \lor \rightarrow q$ https://powcoder.com
- sad $\rightarrow -happy$ WeChat powcoder
- \neg happy \leftarrow sad

- rich $\rightarrow \neg\neg$ happy
- rich

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 (work hard ∨ steal)
- (steal $\land \lor$ borrow) \rightarrow possess
- (steal v borned Wechatosses der
- steal ∨ borrow → possess

- $(p \land q \rightarrow r) \land (\neg p \rightarrow \neg q)$
- $p \rightarrow \neg p$ Assignment Project Exam Help
- https://powcoder.com p ∧¬p

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We will look at

- Parse trees Assignment Project Exam Help
- > Principle https://piowcoder.com
- Subformulated WeChat powcoder in the lecture.

Notes on terminology

- \neg is a **unary** operator.
- The other science raie ti Fary of the lators.
- $X \vee Y$ is hathed/theordisitenction of X and Y.
- X \ Y X and Y are disjuncts. Add Wechat powcoder
- $X \wedge Y$ is called the **conjunction of X and Y**.
- $X \wedge Y$ X and Y are conjuncts.
- $\neg X$ is called the **negation of X**.

Notes on terminology cntd.

• A → B is called an implication.

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A is called the antecedent,

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Called the consequent.

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A *Literal* is a proposition or the negation of a proposition.

Semantics

Provides

- The meaning of the simple (atomic) units
- Rules for putting together the meaning of the atomic Adits Wo Champahe aning of the complex units (sentences).

Semantics specifies under what circumstances a sentence is *true* or *false*.

```
T (truth) and
F (falsity) Assignment Project Exam Help
are known as https://powcoder.com
Add WeChat powcoder
```

Constructing Truth Tables for the connectives

Assignment Pr	oject Exam Help
Т	vcoder.com F hat powcoder
	To post of the
F	T

A	В	$\mathbf{A} \wedge \mathbf{B}$
1 1	1	Exam Help T
https	://powcode	r.com
TAdd	WeChat po	wcoder
F	T	F
F	F	F

Example

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John is not happy://put/dedsrcomfortable.

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Represent as $-h \wedge c$

Four possible cases

Example cntd. $\neg h \qquad \neg h \land c$ Assignment Project Exam Help_F Add WeChat powcoder F F

A	В	A∨B
Assignme	ent Project	Exam Help
Thttps	T://powcode	r.com
TAdd	WeChat po	wcoder
F	T	T
F	F	F

A	В	A→B
	nt Project F T //powcoder	Γ
Add V	WeChat pov	wcodEr
F	T	T
F	F	Т

Compare \land with \rightarrow

A	В	$A \wedge B$	A	В	$A \rightarrow B$
T	Assig T	nment I T	ject Exa T coder.co	1	T
T	F	F Add We	T	F	F
F	T	F	F	Т	T
F	F	F	F	F	T

A	В	A↔B
Assignmen	t Project Exan	n Help
	T powcoder.con	
T _{Add} W	eChat powcoo	der F
F	T	F
F	F	T

Note

For any wffs A and B, "A \leftrightarrow B" is true exactly where A and B riest Entershile truth values, i.e. when they ware depth true or both false.

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The truth value of a wff is uniquely determined by the truit trained by the truit to a truit the component at the component of the component o

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Example:

The truth table for the wff $(p \lor q) \land (r \rightarrow p)$ is as follows:

```
p \lor q \qquad r \to p \qquad (p \lor q) \land (r \to p)
T T T Assignment Project Exam Help
            T https://powcoder.com
   TF
   FT
            T Add We Chat powcoder
   FF
                               F
   TF
F
   FT
            F
                  F
                               F
```

Exercise:

How many rows will there be in a truth table for a wff contain/ipgwsqlerpositional symbols? Add WeChat powcoder

 2^n



Exercise:

Recall we sassignment Erreject Exam Help

 $P \rightarrow (Q \rightarrow R)$ https://powcoder.com

 $(P \rightarrow Q) \rightarrow R$ Add WeChat powcoder

in general do not have the same meaning.

Under which interpretation(s) do the truth values of the two wffs differ?

Notes

The connective "v" stands for *inclusive* or, i.e. p v q is Aistigpneted Recipert Whemelither proposition is true or both are. https://powcoder.com

Often in English when we atspower over intend exclusive or, e.g.

- I'll go shopping or I'll stay at home.
- We will meet at his house *or* at the club.

Notes cntd.

In this propositional language there is no connective for exclusive or but propen still express the concept, e.g.

```
(goshopping stayinome) \land
\neg (\textbf{goshwptihat} \cdot \textbf{potaychdene})
In general "p exor q" can be represented as:
(p \lor q) \land \neg (p \land q)
```

Exercise:

Draw the truth table of the first wff above.

A	В	A\sigma B	$\neg (A \land B)$	A exor B
	Assignn	nent Pro	ject Exam	$\text{HapB}) \land \neg (A \land B)$
T		•	codeF.com	
T	F Add	l W _P Ch	at powcod	ler T
F	T	T	Т	T
F	F	F	T	F

Notes cntd.

- Law of excluded middle:
- So propositional liver Chan powdude rlogic.
- There are other logics, including 3-valued ones.
- SQL, for example, implements 3-valued logic, where comparisons with NULL, including that of another NULL gives *UNKNOWN*.

Example NULL Values

Table T of people and their hair colours:

Name	Hat Size	Hair Colour
Helen	Assignment Proje	
John	https://powce	
Tom	Large WeCha	t powcoder

Select Name

From T

Where Hat Size=Large AND Hair Colour ≠ Brown

	A	В	$A \vee B$
	T	T	T
	T	F	T
^	F	T	T
A	ssignment F	Froject Ex	F
	https://p	owcoder.c	om T
	Andrd We	Chat powd	oderT
	F	U	U
	U	F	U
	U	U	U

• A proposition (and consequently a wff) cannot best outhern Project felsen Help

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Exercise:

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Draw the truth table for $A \land \neg A$.

A	$\neg A$	$A \wedge \neg A$
Assignme T	ent Project F	Exam Help F
https	://powcode	r.com
FAdd	WeChat po	wcoder

Notes cntd.

- The interpretation of "→" may be unintuitive sometimes.
- The semanifics of Project Exam Helple in logic. https://powcoder.com
- $A \rightarrow B$ is simply the same as $der A \lor B$.
- In English we use "if .. then" in many different ways, and sometimes quite confusingly.
- Don't read $A \rightarrow B$ as "A causes B".

Some definitions

Definition:

A wff whichseighnates Projectificatory Helperpretation of its constituent parts is called a tautology. https://powcoder.com

Example Add We Chat powcoder

 $A \rightarrow A$

The two wffs above represent the **Law of excluded** middle.

A	$\neg \mathbf{A}$	$A \lor \neg A$
Assignme	ent Project	Exam Help
	F://powcode	_
FAdd	WeChat po	wcoder

Definition

A wff which evaluates to false in every interpretation of the worktituent parts is called an inconsistency (contradiction), or is said to be inconsistent.

Example $A \land \neg A$

Definition

A wff which is neither a tautology, nor an inconsistencypis/apowneilegency, or is said to be contingental WeChat powcoder

Exercise

For each of the following determine if it is a tautology signosist proper continuency by drawing the truth table.

- a. $P \wedge (P \vee Q)$ https://powcoder.com
- b. $(P \vee Q) \wedge (Add W)$ eChat powcoder
- c. $Q \land \neg P \land (P \lor (Q \rightarrow P))$
- d. $(P \land (Q \lor P)) \leftrightarrow P$
- e. $(P \rightarrow Q) \rightarrow (\neg P \lor Q)$
- f. $((P \rightarrow Q) \land (R \rightarrow S) \land (P \lor R)) \rightarrow (Q \lor S)$

Definition: Equivalence

Two wffs are equivalent iff their truth values are the same mede Projecty Exampled ation.

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A is equivalentation as

$$A \equiv B$$
.

"≡" is the metasymbol for equivalence.

Double Negation Rule

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Implication RedeWeChat powcoder

$$A \rightarrow B \equiv \neg A \vee B$$

Commutative Rules

Associative RedreweChat powcoder

$$(A \wedge B) \wedge C \equiv A \wedge (B \wedge C)$$

$$(A \lor B) \lor C \equiv A \lor (B \lor C)$$

Idempotence

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$$A \wedge A = \frac{\text{https://powcoder.com}}{\text{max}}$$

Distributive Rules

$$A \wedge (B \wedge C) = A \wedge (B \wedge C)$$

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De Morgan's Rules

$$\neg (A \lor B) \equiv \neg A \land \neg B$$

$$\neg (A \land B) \equiv \neg A \lor \neg B$$

$$A \leftrightarrow B \equiv$$
 $(A \to B) Assignment Project Exam Help$
 $https://powcoder.com$

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$$A \wedge B \equiv B$$
 if ????

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$$A \wedge B \equiv B$$
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$$A \vee B \equiv B$$
 if ????

 $A \lor B \equiv B$ if A is an inconsistency

Exercise





```
Show
```

A →B Assignment Project Exam Help

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Example Add WeChat powcoder I get an MSc \rightarrow I get big salary \equiv \neg (I get an MSc $\land \neg$ I get big salary)

Exercises

Show

https://powcoder.com

Show

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$$A \leftrightarrow B \equiv \neg A \leftrightarrow \neg B$$

Showing $A \leftrightarrow B \equiv \neg A \leftrightarrow \neg B$

LHS
$$\equiv (A \rightarrow B) \land (B \rightarrow A)$$

RHS $\equiv (A \rightarrow B) \land (B \rightarrow A)$
 $\equiv (A \rightarrow B) \land (A \rightarrow B)$
 $\Rightarrow (A \rightarrow B) \rightarrow (A \rightarrow B)$
 $\Rightarrow (A \rightarrow B) \rightarrow$

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Compare LHS with RHS:

LHS
$$\equiv (A \rightarrow B) \land (B \rightarrow A)$$

 $| \qquad | \qquad |$
RHS $\equiv (\neg B \rightarrow \neg A) \land (\neg A \rightarrow \neg B)$

And both correspondences are an instance of one equivareignment Project Exam Help

 $X \rightarrow Y \underline{\text{httpsy/powepder.com}}$

So this equivaled we clean prograte deprove LHS = RHS.

Showing
$$X \to Y \equiv \neg Y \to \neg X$$
 $X \to Y \equiv$
Assignment Project Exam Help
$$\neg X \lor Y \equiv \begin{array}{c} \text{https://powcoder.com} \text{n rule} \\ \neg X \lor Y \equiv \end{array}$$

$$\neg X \lor Y \equiv \begin{array}{c} \text{https://powcoder.com} \text{n rule} \\ \neg X \lor \neg \neg Y \equiv \text{Add WeChat power degration} \\ \neg Y \lor \neg X \equiv \end{array}$$

$$\text{commutativity of } \lor \neg Y \to \neg X$$

$$\text{implication rule}$$

Back to Exercise

For each of the following determine if it is a tautology signosist proper continuency by drawing the truth table.

- a. $P \wedge (P \vee Q)$ https://powcoder.com
- b. $(P \vee Q) \wedge (Add)$ We Chat powcoder
- c. $Q \land \neg P \land (P \lor (Q \rightarrow P))$
- d. $(P \land (Q \lor P)) \leftrightarrow P$
- e. $(P \rightarrow Q) \rightarrow (\neg P \lor Q)$
- f. $((P \rightarrow Q) \land (R \rightarrow S) \land (P \lor R)) \rightarrow (Q \lor S)$