### Fall 2013, MATH 407, Mid-Term Exam 2

### Wednesday, November 20, 2013

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Name:		

Circle the time of your discussion section: 8am 9am 10am

### **Instructions:**

- No books, notes, or calculators.
- You have 50 minutes to complete the exam.
- Show your work.

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	Total	50	

Problem | Possible | Actual |

**Problem 1.** A fair die is rolled until the total sum of all rolls exceeds 300. Compute approximately the probability that at least 80 rolls are necessary. Note that, for a single roll of the die, the expected value and variance of the outcome are 7/2 and 35/12, respectively. Use the continuity correction. Leave the answer in the form P(Z < r), where Z is a standard normal random variable and r is a suitable real number.

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**Problem 2.** Customers arrive at a bank according to a Poisson process. Suppose that two customers arrives during the first hour. Compute the probability that at least one arrived during the first 20 minutes. Add WeChat powcoder

**Problem 3.** Let X, Y be independent random variables, both uniform on (0, 1). Find the joint density of X + Y and X/(X + Y).

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**Problem 4.** For a randomly selected group of 100 people, compute the expected number of distinct birthdays (that is, the expected number of the days of the year that are a birthday of at least one person in the group).

**Problem 5.** The joint probability density function of two random variables X and Y

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(a) Are X and Y independent? Justify your answer.

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(b) Compute E(X|Y). Suggestion: keep your computations to a minimum. In particular, there is no need to know C.