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Examples of Optimisation Problems

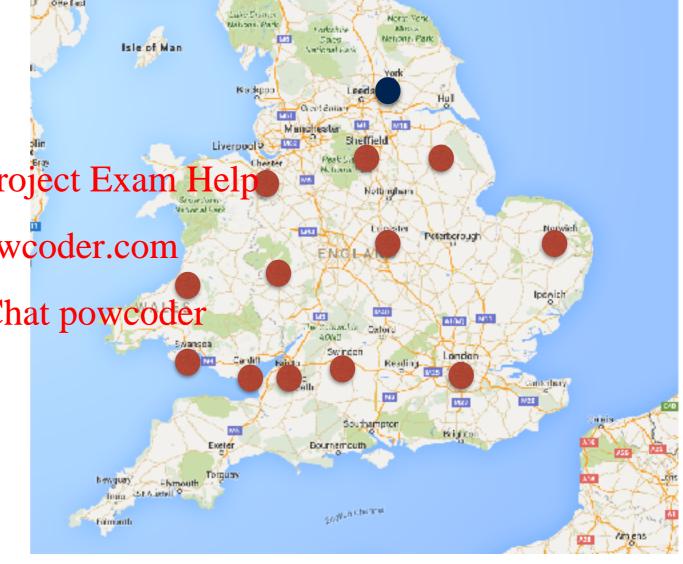
Traveling Salesman
 Problem:

A salesman must travel
 passing throughs Wegitiest Project Exam Hel

• Each city must be visited once and only once.

 He/she must finish where Chat powcoder he/she was at first.

 The path between each pair of cities has a distance (or cost).



Problem: find a sequence of cities that minimises traveling distance (or cost), where each city appears once and only once.

- Design variables represent a candidate solution.
 - Sequence x of N cities to be visited, where cities are in C.
 - C is a set containing the N cities to be visited.
 - The search space is all possible sequences of cities.
- Objective function definest the post of a solution.

$$\overline{x_1}$$
 $\overline{x_2}$ $\overline{x_3}$ $\overline{x_4}$ $\overline{x_5}$

- Total_distance(x) = Add WeChat powcoder.
 sum of distances between consecutive cities in x + distance from last city to the origin.
- To be minimised.
- [Optional] Solutions must satisfy certain constraints.
 - Each city must appear once and only once in x (explicit constraint).
 - Salesman must return to the city of origin (implicit constraint).
 - Only cities in C must appear in **x** (implicit constraint).

- Design variables represent a candidate solution.
 - The design variable is a sequence **x** of *N* cities, where $x_i \in \{1, \dots, N\}$, $\forall i \in \{1, \dots, N\}$.
 - The *N* cities to be visited are represented by values {1,...,*N*}.
 - The search space is all ignified from the search space is a sear
- https://powcoder.com

 Objective function defines the cost of a solution.

minimise totalDistance(
$$\mathbf{x}$$
) = $\left(\sum_{i=1}^{Avdd} \mathbf{WeChat powcoder} \atop D_{x_i,x_{i+1}}\right) + D_{x_N,x_1}$

$$\frac{1}{x_1} \frac{3}{x_2} \frac{2}{x_3} \frac{4}{x_4} \frac{5}{x_5}$$

where $D_{i,k}$ is the distance of the path between cities j and k.

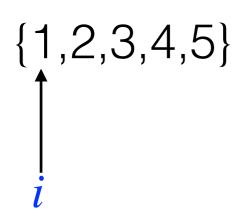
- [Optional] Solutions must satisfy certain constraints.
 - Each city must appear once and only once in x (explicit constraint).

"For each city i in
$$\{1,...,N\}$$
", $\left(\sum_{j=1}^{N} 1(x_j = i)\right) = 1$ $1(x_j = i) = \begin{cases} 1, & \text{if } x_j = i \\ 0, & \text{if } x_j \neq i \end{cases}$

$$\forall i \in \{1, \dots, N\}, \left(\sum_{j=1}^{N} 1(x_j = i)\right) = 1 \qquad 1(x_j = i) = \begin{cases} 1, & \text{if } x_j = i \\ 0, & \text{if } x_j \neq i \end{cases}$$

$$1(x_j = i) = \begin{cases} 1, & \text{if } x_j = i \\ 0, & \text{if } x_j \neq i \end{cases}$$

$$\forall i \in \{1, \dots, N\}, h_i(\mathbf{x}) = \begin{pmatrix} \text{https://powcoder.com} \\ \sum_{i=1}^{N} \mathbf{1}(\mathbf{w} = \mathbf{0}) \\ \mathbf{v} = \mathbf{0} \end{pmatrix}$$



$$\frac{4}{x_1} \frac{2}{x_2} \frac{1}{x_3} \frac{3}{x_4} \frac{3}{x_5}$$

Sum₁:
$$0 + 0 + 1 + 0 + 0 = 1$$

Sum₂:
$$0 + 1 + 0 + 0 + 0 = 1$$

Sum₃:
$$0 + 0 + 0 + 1 + 1 = 2$$

- Design variables represent a candidate solution.
 - The design variable is a sequence **x** of *N* cities, where $x_i \in \{1, \dots, N\}$, $\forall i \in \{1, \dots, N\}.$

 - The N cities to be visited are represented by values {1,...,N}.
 The search space is all possible sequences of N cities, where cities are in $\{1,...,N\}.$ https://powcoder.com
- Objective function defines the water

$$\text{minimise totalDistance}(\mathbf{x}) = \left(\sum_{i=1}^{N-1} D_{x_i,x_{i+1}}\right) + D_{x_N,x_1}$$

where $D_{i,k}$ is the distance of the path between cities j and k.

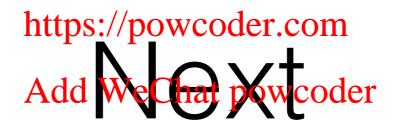
[Optional] Solutions must satisfy certain constraints.

For each city i, $h_i(\mathbf{x}) = 0$

Summary

Traveling salesman problem formulation, including constraints.

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How to deal with constraints?