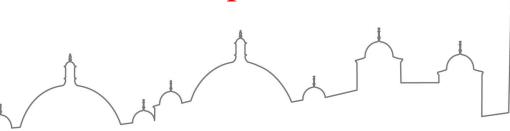


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Dr Leonardo Stella

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Aims of the Session

This session aims to help you:

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- Describe the fundamental concepts in probability theory https://powcoder.com
- Explain Bayes' Theoretical Explain Bayes' The

Apply Naïve Bayes to classification for categorical and numerical independent variables

Overview

- Fundamental concepts in Probability Theory Assignment Project Exam Help
- Bayes' Theoremhttps://powcoder.com
- Naïve Bayes for Categorical Independent Variables
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- Naïve Bayes for Numerical Independent Variables

Fundamental Concepts in Probability Theory

- Probabilistic model: a mathematical description of an uncertain situation. The two main elements of a probabilistiq model are:
 - The **sample space** Ω , which is the set of all possible outcomes
 - The **probability law typich** a spign to O(A) (called the **probability** of A)

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- Every probabilistic model involves an underlying process, called the experiment, that produces exactly one of several possible outcomes
- A subset of the sample space Ω is called an **event**

Example: Toss of a Coin

- Consider the following experiment a single toss of a fair coin
 - The sample space of nead (H) or tall (T)
 - The probability law: P(H) = 0.5 (called the probability of H), P(T) = 0.5 https://powcoder.com

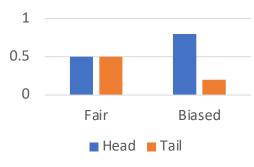
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Example: Toss of a Coin

- Consider the following experiment a single toss of a fair coin
 - The sample space at nead (H) or tall (T)
 - The **probability law**: P(H) = 0.5 (called the **probability** of H), P(T) = 0.5 https://powcoder.com
- Let us now consider the exactly 2 heads? What about exactly 1 head?

Example: Toss of a Coin

- Consider the following experiment a single toss of a fair coin
 - The sample space of the nead (H) or tail (I) Exam Help
 - The probability law: P(H) = 0.5 (called the probability of H), P(T) = 0.5 https://powcoder.com
- Let us now consider the experiment consisting of a coin tosses. What is the probability of having exactly 2 heads? What about exactly 1 head?
- Repeat with the biased coin: P(H) = 0.8



Probability Axioms

- Nonnegativity: $P(A) \ge 0$, for every event AAssignment Project Exam Help
- Additivity: If A and B are two disjoint events, then the probability of their union satisfies: P(PS; BPO) COM

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■ Normalisation: The probability of the entire sample space is equal to 1, namely $P(\Omega) = 1$

(Discrete) Random Variables

Given an experiment and the corresponding sample space, a random variable maps A particular muth per with faxland to the corresponding sample space, a random variable maps A particular muth per with faxland to the corresponding sample space, a random variable maps A particular muth per with faxland to the corresponding sample space, a random variable maps A particular muth per with faxland to the corresponding sample space.

Mathematically, a random variable x is a real-valued function of the experimental outcome.

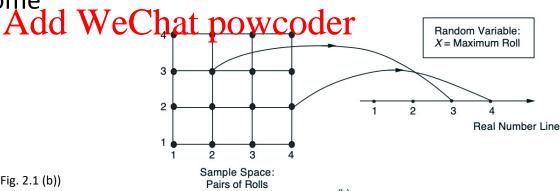


Image: taken from Introduction to Probability (Fig. 2.1 (b))

Probability Mass Function (PMF)

- The probability mass function (PMF) captures the probabilities of the values that a (discrete) randompyorjable Extake Help
- Let us consider the https://pxampleder.com

$$P(X = 1) = 1/16$$

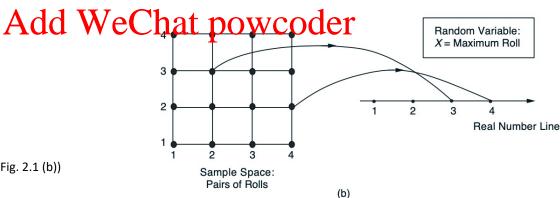


Image: taken from Introduction to Probability (Fig. 2.1 (b))

Probability Mass Function (PMF)

- The probability mass function (PMF) captures the probabilities of the values that a (discrete) random projeble Extake Help
- Let us consider the https://pxampleder.com

$$P(X = 1) = 1/16$$

$$P(X = 2) = 3/16$$

$$P(X = 3) = 5/16$$

$$P(X = 4) = 7/16$$

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Random Variable: X = Maximum RollFig. 2.2 (b))

Sample Space: Pairs of Bolls

(b)

Image: taken from Introduction to Probability (Fig. 2.2 (b))

Notation

- Random variables are usually indicated with uppercase letters, e.g., X or Temperature of infestionent Project Exam Help
- The values are indicated with plower case letters, i.e.g., $X \in \{true, false\}$ or $Infection \in \{low, moderate, high\}$

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- Vectors are usually indicated with bold letters or a small arrow above the letter, e.g., \pmb{X} or \vec{X}
- PMF is usually indicated by the symbol $p_X(x)$

Unconditional/Conditional Probability Distributions

- An unconditional (or prior) probability distribution gives us the probabilities of all possible events without knowing anything else about the problem, e.g., the maximum value of two rolls of a 4-sided die
- $P(X) = \{\frac{1}{15}, \frac{3}{15}, \frac{5}{15}\}$ https://powcoder.com
- A conditional (or posterior) probability distribution gives us the probability of all possible events with some additional knowledge, e.g., the maximum value of two rolls of a 4-sided die knowing that the first roll is 3
- $P(X \mid X_1 = 3) = \{0, 0, \frac{3}{4}, \frac{1}{4}\}$

Joint Probability Distributions

- A joint probability distribution is the probability distribution associated to all combinations gfithremature of every fragre land pm variables
- This is indicated by tommas, power of the Toothache, Cavity)

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• We can calculate the joint probability distribution by using the product rule as in the following:

$$P(X,Y) = P(X \mid Y) P(Y) = P(Y \mid X) P(X)$$

Mean, Variance and Standard Deviation

- The mean (or expected value or expectation), also indicated by μ , of a random variable X with $ANF p_X(x)$ represents the centre of gravity of the PMF: $\mathbf{E}(X) = \sum_x x p_X(x)$
- E.g., let us consider the random variable X1 i.e., the roll of a 4-sided die. The mean is calculated as: E(X) = 1 * 4 + 2 * 4 + 3 * 4 + 4 * 14 = 2.5
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 The variance of a random variable X provides a measure of the dispersion around the mean:

$$var(X) = \sum_{x} (x - E(X))^{2} p_{X}(x)$$

The standard deviation is another measure of dispersion: $\sigma_X = \sqrt{var(x)}$

Continuous Random Variables

A random variable X is called continuous if its probability law can be described in terms of a nonnegative function (PDF) and is the equivalent of the PMF for discrete random variables

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Since we are dealing with continuous variables, there are an infinite number of values that X can take

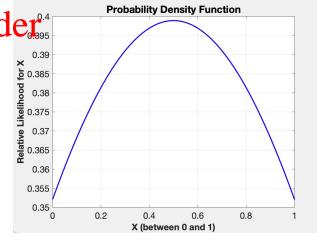
 As for the discrete case, also for continuous random variables we can have unconditional, conditional and joint probability distributions

Example: Random Number Generator

- As an example, let us consider a random number generator that returns a random value between earth of eet 12 am Help
- And let us model it https://apsiwo.org/portant/ distribution

$$P(X = a \mid \mu, \sigma^2) = \frac{\text{Add}}{\sigma\sqrt{(2\pi)}} e^{\frac{\text{WeChat powcode}}{2\sigma^2}},$$

where μ is the mean and σ^2 is the variance Also, recall that $\pi=3.14159$ and e=2.71828



Overview

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Bayes' Theorem

Recall the product rule for a joint probability distribution of independent variable(s) X and dependent variable Y:
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$$P(X,Y) = P(X | Y) P(Y) = P(Y | X) P(X)$$

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By taking the second and last term from the above equation and rearranging, we get: Add WeChat powcoder

$$P(X \mid Y) = \frac{P(Y \mid X)P(X)}{P(Y)}$$

The above equation is known as **Bayes' Theorem** (also Bayes' rule or Bayes' law)

ML: Probabilistic Inference

Our ML task consists in computing the posterior probabilities for query propositions gays isomerome Projecte Executives Intelliped is probabilistic inference

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 We use Bayes' Theorem to make predictions about an underlying process given a knowledge base bonsipply 6046 data produced by this process

Equivalent Terminology

- Input attribute, independent variable, input variable
- Output attributes signandent verificaties to the signandent verification.
- Predictive model, classifier/(questifier), contypothesis (statistical learning)
- Learning a model, traididg Wroodeab prioring a model.
- Training examples, training data
- Example, observation, data point, instance (more frequently used for test examples)
- $P(a,b) = P(a \text{ and } b) = P(a \land b)$

Consider the training set

Assignment Project Exem Helpo

yes no https://powcoder.com
Add WeChat powcoder no no

Sunny (X_1)

yes

Windy (X_2)

no

ves

Tennis (Y)

yes

yes

yes

no

Days

Day 1

Consider the **training set**

Day 1 yes no yes Assignment Project yes ves no yes no no Add WeChat powcoder ves no

Sunny (X_1)

Windy (X_2)

Tennis (Y)

Days

Let us build the **model** for <u>one</u> independent variable, e.g., Windy (X_2)

Frequency Table	Tennis = yes	Tennis = no	Total
Windy = yes			
Windy = no			
Total			

Consider the **training set**

Day 1 yes no yes Assignment Project yes ves no yes https://po no no Add WeChat powcoder ves no

Sunny (X_1)

Windy (X_2)

Tennis (Y)

Let us build the **model** for <u>one</u> independent variable, e.g., Windy (X_2)

Days

Frequency Table	Tennis = yes	Tennis = no	Total
Windy = yes	1		
Windy = no			
Total			

Consider the **training set** Assignment Project

> https://powcoder yes no Add WeChat powcoder ves

Sunny (X_1)

yes

Windy (X_2)

no

Tennis (Y)

yes

yes

ves

no

no

no

Let us build the **model** for <u>one</u> independent variable, e.g., Windy (X_2)

Frequency Table	Tennis = yes	Tennis = no	Total
Windy = yes	1		
Windy = no	2		
Total	3		

Days

Day 1

Consider the training set
 Assignment Project Expenses

Sunny (X_1)

Windy (X_2)

no

Tennis (Y)

yes

yes

ves

• Let us build the **model** for <u>one</u> independent variable, e.g., Windy (X_2)

Days

Frequency Table	Tennis = yes	Tennis = no	Total
Windy = yes	1	2	3
Windy = no	2	1	3
Total	3	3	6

Learning Probabilities (continued)

		Tennis = yes		Total
P(Windy=no Tennissignment Proje	Windy = ves	m Help	2	3
P(Windy=yes Tennis=no) = https://powce	• •		1	3
P(Windy=no Tennis=no) =	Oder.co	Ŋ	3	6

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Learning Probabilities (continued)

		Tennis = yes		Total
P(Windy=no Tennissignment Proje	Ct Example Windy = yes	m Help	2	3
P(Windy=yes Tennis=no) = 2/3 https://powce	<u> </u>		1	3
P(Windy=no Tennis=no) = 1/3	Outer.co		3	6

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Learning Probabilities (continued)

		Tennis = yes		Total
P(Windy=no TenAissiesn#12#3nt Proje	Table EX a	m Heln		
	Windy = yes	1 1 1 P	2	3
P(Windy=yes Tennis=no) = 2/3	W <mark>i</mark> ndy = no	2	1	3
P(Windy=yes Tennis=no) = $\frac{2}{3}$ P(Windy=no Tennis=no) = $\frac{2}{3}$ /POWC	oder.co	ng.	3	6

P(Windy=yes) =
$$3/6 = 1/2$$

P(Windy=no) = $3/6 = 1/2$

P(Tennis=yes) = $3/6 = 1/2$

P(Tennis=no) = $3/6 = 1/2$

Applying Bayes' Theorem

Let us consider output class c and input value(s) a. Bayes' Theorem can be rewritten assignment Project Exam Help $P(c \mid a) = \frac{P(a \mid c)P(c)}{\text{https://powcoden.com}}$

$$P(c \mid a) = \frac{P(a \mid c)P(c)}{\text{https://powcode(n)com}}$$

Now, given input value(s) a, we calculate the above for every class c: our prediction is the on Awith: We Chat powcoder

$$P(Tennis = yes \mid Windy = yes) = \frac{P(Windy = yes \mid Tennis = yes)P(Tennis = yes)}{P(Windy = yes)}$$

Applying Bayes' Theorem (continued)

$$P(Tennis = yes | Aissignment Project Exam Help $P(Windy = yes) P(Tennis = yes)$$$

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Frequency Table	Tennis = yes	Tennis = no	Total
Windy = yes	1	2	3
Windy = no	2	1	3
Total	3	3	6

Applying Bayes' Theorem (continued)

$$P(Tennis = yes | Aissignment Project Exam Help $P(Windy = yes)$$$

https://pawcoder.com

$$P(Tennis = no \mid Windy = yes)$$
 We Chat pow Force $p(Windy = yes)$

Frequency Table	Tennis = yes	Tennis = no	Total
Windy = yes	1	2	3
Windy = no	2	1	3
Total	3	3	6

$$=\frac{2/3*3/6}{3/6}=0.67$$

Applying Bayes' Theorem (continued)

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P(https://powindoder.com67

maxArdel We Chartops, w.60 pler 0.67

Frequency Table	Tennis = yes	Tennis = no	Total
Windy = yes	1	2	3
Windy = no	2	1	3
Total	3	3	6

Normalising Factor

```
P(Tennis = yes) P(Tennis = y
```

- 1/P(Windy = yes) can be seen as a normalisation constant for the distribution: we can replace it with the constant parameter $\alpha = 1/\beta$

More than 1 Independent Variable

$$P(c|a_1Assign \underbrace{P(c)}_{\sum_{c \in \mathcal{U}}(P(c)} \underbrace{\prod_{i=1}^{n} P(a_i|c)}) = Expan, Help c)P(c)$$

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 P represents the probability calculated based on the frequency tables
- c represents a classAdd WeChat powcoder
- a_i represents the value of independent variable $x_i \in \{1, ..., n\}$
- n is the number of independent variables
- α is the normalisation factor

Problems: Scaling and Missing Values

	toothache		¬toothache	
	Assignmen	t-Rroject Ex	tam Help	¬catch
cavity	0.108	0.012	0.072	0.008
¬cavity	0.016 https://	rewcoder.c	:Offn	0.576

- In this example (from the book), we have 3 Boolean variables
- For a domain described by two canatripoles, we do tild need an input table of size $O(2^n)$ and it would take $O(2^n)$ to process the table
- Also, it is reasonable to think that we will never see values for all possible combinations of the variables
- Naïve Bayes can be used to deal with these issues

Overview

- Fundamental concepts in Probability Theory Assignment Project Exam Help
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- Naïve Bayes for Numerical Independent Variables

Recall: Issues with Bayes' Theorem

			¬toothache	
	Assignmen	t-Aroject Ex	tam Help	¬catch
cavity	0.108	0.012	0.072	0.008
¬cavity	0.016 https://	rowcoder.c	o t n	0.576

For increasing numbers of weep and eptowich terms and possible combinations must be considered:

$$P(c|a_1,...,a_n) = \alpha P(c) P(a_1,...,a_n|c)$$

For a domain described by n Boolean variables, we would need an input table of size $O(2^n)$ and it would take $O(2^n)$ to process the table

Naïve Bayes: Conditional Independence

- Assumption: each input variable is conditionally independent of any other input variable.
- Independence: A is independent of B when the following equality holds (i.e., B does not alter the probability that A has occurred):

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• Conditional independence: x_1 is conditionally independent of x_2 given y when the following equality holds:

$$P(x_1|x_2, y) = P(x_1, y)$$

Naïve Bayes

• Conditional independence: x_1 is conditionally independent of x_2 given y when the following requestity Probject Exam Help $P(x_1|x_2,y) = P(x_1,y)$

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 $P(c|a_1,dd,a_n)$ eChat powcoder $_n|c)$

Naïve Bayes

• Conditional independence: x_1 is conditionally independent of x_2 given y when the following requestity Probject Exam Help $P(x_1|x_2,y)=P(x_1,y)$

https://powcoder.com

 $P(c|a_1,dd,a_n)$ eChat powcoder $_n|c)$



 $P(c|a_1,...,a_n) = \alpha P(c) P(a_1|c) P(a_2|c) ... P(a_n|c)$

Naïve Bayes

$$P(c|a_1,...,a_n) = \alpha P(c) P(a_1|c)P(a_2|c) ... P(a_n|c)$$
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 $P(c)$
 $P(c)$

where
$$\alpha = 1/\beta$$
 and $\beta = \sum_{c \in \mathcal{Y}} (P(c) \prod_{i=1}^{n} P(a_i | c))$

Example: Naïve Bayes

Consider again the training set

Sunny (X_1) Windy (X_2) Tennis (Y)**Days** Day 1 yes no yes Assignment Project t Exam Help yes yes ves https://powcoder. no yes no no Add WeChat powcoder ves no

Because of conditional independence, we have a table for each variable:

Frequency Table	Tennis = yes	Tennis = no	Total
Windy = yes	1	2	3
Windy = no	2	1	3
Total	3	3	6

Frequency Table	Tennis = yes	Tennis = no	Total
Sunny = yes	3	0	3
Sunny = no	0	3	3
Total	3	3	6

Example: Naïve Bayes (continued)

Let us determine the predicted class for the following instance:

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Frequency	Tennis = yes	Tennis = no	Total	J	Frequency	Tennis = yes	Tennis = no	Total
Table		httr	is.//box	1C	Table	m		
Windy = yes	1	2	3.//pow		Table OCCT.CO Sunny = yes	3	0	3
Windy = no	2	1 1 1	d WoCl	30	Sunny = no	0	3	3
Total	3	3 Au	y weci	Ia	Total	ger	3	6

- $P(c|a_1,...,a_n) = \alpha P(c) \prod_{i=1}^{n} P(a_i|c)$
- $P(\neg T | \neg W, \neg S) = \alpha P(\neg T) P(\neg W | \neg T) P(\neg S | \neg T) = \alpha \frac{3}{6} * \frac{1}{3} * \frac{3}{3} = \frac{1}{6} \alpha$ $P(T | \neg W, \neg S) = \alpha P(T) P(\neg W | T) P(\neg S | T) = \alpha \frac{3}{6} * \frac{2}{3} * \frac{0}{3} = 0$

Example: Naïve Bayes (continued)

- $P(\neg T | \neg W, \neg S) = \alpha P(\neg T)P(\neg W | \neg T)P(\neg S | \neg T) = \alpha \frac{3}{6} * \frac{1}{3} * \frac{3}{3} = \frac{1}{6}\alpha$ $P(T | \neg W, \neg S) = Assignment Project Exame Melp$
- $\alpha = \frac{1}{\beta} = \frac{1}{\frac{3}{6} + \frac{2}{3} + \frac{3}{6} + \frac{3}{6} + \frac{3}{2} + \frac{3}{2}} = \frac{\text{lttps://powcoder.com}}{\beta}$

Add WeChat powcoder $P(\neg T | \neg W, \neg S) = \frac{1}{6} * 6 = 1$

- $P(T|\neg W, \neg S) = 0$
- Problem: in this example, there is no data where Tennis = yes with Sunny = no, so regardless of the value of Windy, we will get inaccuracies in doing predictions

Laplace Smoothing

To avoid this problem, we can use Laplace smoothing by adding 1 to the frequency of Assignments of the problem.

Frequency	Tennis = yes	Tennis = no	Total		Frequency	Tennis = yes	Tennis = no	Total
Table		httr	os · //nov	10	Table OCCT.CO	m		
Windy = yes	1+1	2+1	3+2 POV		Sunny = yes	3+1	0+1	3+2
Windy = no	2+1	1+1	3+2	3.0	Sunny = no	0+1 Oder	3+1	3+2
Total	3+2	3+2 Au	G+4V ECI	Ia	Total	3+2 3+2	3+2	6+4

- Then we use the updated tables when calculating $P(a_i|c)$, so we do not get values with 0
- When we calculate P(c), we use the original tables

Summary

Naïve Bayes Learning Algorithm

- Create frequency tables for each independent variable and the corresponding values for the frequency of an event Significant Project Exam Help
- Count the number of training examples of each class with each independent variable
- Apply Laplace smoothing https://powcoder.com

Naïve Bayes Model

Consists of the frequency tables obtained from Bayes' Theorem under the conditional independence assumption (with or without Laplace smoothing)

Naïve Bayes prediction for an instance (X=a, Y=?)

We use Bayes' Theorem under the conditional independence assumption

Overview

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- Naïve Bayes for Numerical Independent Variables

$$P(c|a_1,...,a_n) = \alpha P(c) P(a_1|c) P(a_2|c) ... P(a_n|c)$$
Assignment Project Exam Help

 $P(c|a_1,...,a_n) = \alpha P(c) P(a_1|c) P(a_2|c) ... P(a_n|c)$

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where
$$\alpha = 1/\beta$$
 and $\beta = \sum_{c \in \mathcal{Y}} (P(c) \prod_{i=1}^{n} P(a_i|c))$

• We predict the class with $\max_{c} [P(c|a_1, ..., a_n)]$

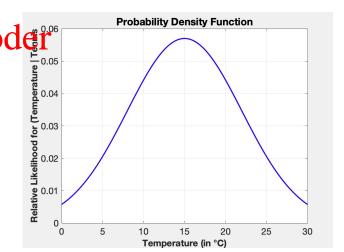
For categorical independent variables, we can compute the probability
of an event the symptometra probability material for the symptometral probability of the symptometral proba

https://powd	Frequency	Tennis = yes OM	Tennis = no	Total
	Windy = yes		2+1	3+2
Add WeCha	atipowc	øder	1+1	3+2
	Total	3+2	3+2	6+4

- Instead, we assume that examples are drawn from a probability distribution. Wessing when a figure of the distribution and the distribution are distribution as a sum of the distribution and the distribution are distribution as a sum of the distribution and the distribution are drawn from a probability distribution.
- Gaussian distribution with mean $\mu = \frac{1}{2}$ and variance $\sigma^2 = 49$

$$P(X = a \mid \mu, \sigma^2) = \frac{1}{\sigma\sqrt{(2\pi)}} e^{\frac{-(a-\mu)^2}{2\sigma^2}},$$

Also, recall that $\pi = 3.14159$ and e = 2.71828



- Let us consider the training data below. We create the PDF for Tennis = yes and for Tennis ignoment Project Exam Help
- So, for Tennis = yes, websiculate mean and variance

•
$$\mu = \frac{1}{n} \sum_{i=1}^{n} x_i = \frac{\text{Add WeCha}}{3} = 25$$

$$\sigma^2 = \frac{1}{n-1} \sum_{i=1}^{n} (x_i - \mu)^2$$

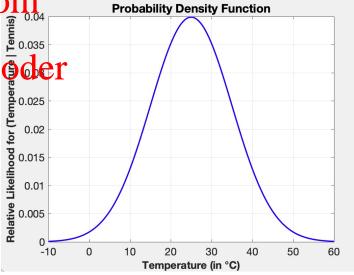
$$= \frac{1}{2} [(15 - 25)^2 + (25 - 25)^2 + (35 - 25)^2] = 100$$

a Days		Temp. (X ₂)	Tennis (Y)
atapowe Day 1	yes	15	yes
Day 2	yes	25	yes
Day 3	yes	35	yes
Day 4	no	10	no
Day 5	no	20	no
Day 6	no	5	no

• Gaussian distribution with mean $\mu = 25$ and variance $\sigma^2 = 100$ Assignment Project Exam Help

 $P(X = a \mid \mu, \sigma^2) = \frac{\text{https}}{\sigma\sqrt{(2\pi)}} \frac{e^{-(a-\mu)^2}}{\sigma\sqrt{(2\pi)}} \text{wcoder.com}$

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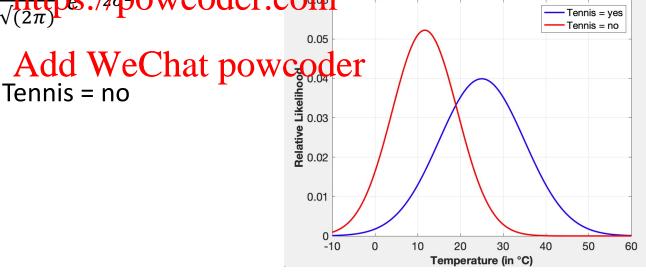


Gaussian distribution with mean $\mu=25$ and variance $\sigma^2=100$ Assignment Project Exam Help

$$P(X = a \mid \mu, \sigma^2) = \frac{https \frac{-(a-\mu)^2}{\sqrt{(2\pi)}}}{\sigma\sqrt{(2\pi)}} wcoder.com$$

Now, if we repeat for Tennis = no

- $\mu = 11.67$
- $\sigma^2 = 58.34$



Probability Density Function

Let us build the tables for

Assignment Project

Assignment Proje

Days	Sunny (X_1)	Temp. (<i>X</i> ₂)	Tennis (Y)
Day 1	yes	15	yes
Day 2	yes	25	yes
Day 3	yes	35	yes
Day 4	no TT 1	10	no
ect Exa	m Help	20	no
Day 6	no	5	no

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Frequency Table	Tennis = yes	Tennis And d	WeCha
Sunny = yes	3+1	0+1	3+2
Sunny = no	0+1	3+1	3+2
Total	3+2	3+2	6+4

Parameter The WCC	Tennis = yes	Tennis = no
μ	25	11.67
σ^2	100	58.34

Now, let us use Naïve Bayes to make a prediction based on the tables:

Frequency Table	Tennis = yes	resignm	ent Proj	CC and CX a	m _{ennis} e _{ye} p	Tennis = no
Sunny = yes	3+1	0+1 http	s ³ ¹ //powc	oder.co	177	11.67
Sunny = no	0+1	3+1	3+2	σ^2	100	58.34
Total	3+2	3+2 Add	WeCha	t nowcc	oder	

- $P(c|a_1,...,a_n) = \alpha P(c) \prod_{i=1}^n P(a_i|c)$
- We use the frequency table for the categorical independent variables
- We use the parameter table for the numerical independent variables

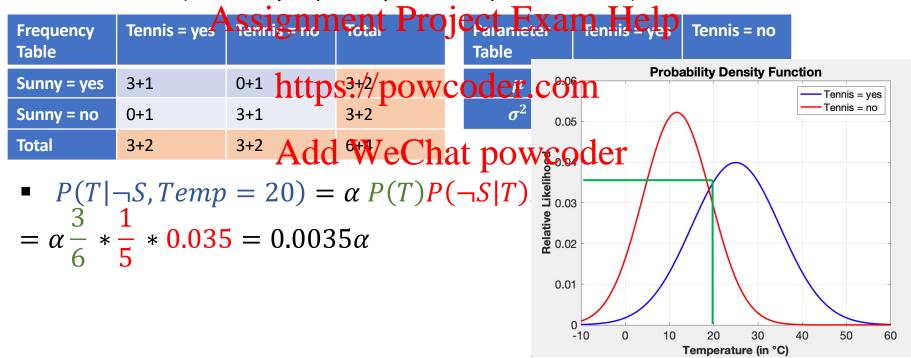
Calculate P(Tennis=yes|Sunny=no,Temperature=20):

Frequency Table	Tennis = yes	ssignm	ięgt Pro	Table	m _{ennis} e _{ye} p	Tennis = no
Sunny = yes	3+1	0+1 http:	S3+/2/DOW(coder.co	n ri	11.67
Sunny = no	0+1	3+1	3+2	σ^2	100	58.34
Total	3+2	3+2 Add	WeCh	at powed	oder	

$$P(T|\neg S, Temp = 20) = \alpha P(T)P(\neg S|T)P(Temp = 20|T)$$

$$= \alpha \frac{3}{6} * \frac{1}{5} * P(Temp = 20|T)$$

Calculate P(Tennis=yes|Sunny=no,Temperature=20):



Calculate P(Tennis=no|Sunny=no,Temperature=20):

Frequency Table	Tennis = yes	Aşşignm	ient Pro	ject _{an} eza Table	m _{entis} ejep	Tennis = no
Sunny = yes	3+1	0+1 http	S3+/2/pow	coder.co	1 71	11.67
Sunny = no	0+1	3+1	3+2	σ^2	100	58.34
Total	3+2	3+2 Add	WeCh	at powco	oder	

$$P(\neg T | \neg S, Temp = 20) = \alpha P(\neg T)P(\neg S | \neg T)P(Temp = 20 | \neg T)$$

$$= \alpha \frac{3}{6} * \frac{4}{5} * 0.029 = 0.0116\alpha$$

- Calculate P(Tennis=no|Sunny=no,Temperature=20):
- $P(T|\neg S, Temps signment(Project Texamplelp0|T)$ 3 1

$$= \alpha \frac{3}{6} * \frac{1}{5} * 0.035 = 0.0035 \alpha / powcoder.com$$

$$P(\neg T | \neg S, Temp = Add We Chat prowede(Temp = 20 | \neg T)$$

$$= \alpha \frac{3}{6} * \frac{4}{5} * 0.029 = 0.0116\alpha$$

Predicted class: Tennis = no

Summary

Naïve Bayes Learning Algorithm

- Create frequency tables for each categorical independent variable and the corresponding values for the frequency of an each categorical independent variable and the corresponding values for the frequency of an each categorical independent variable and the corresponding values for the frequency of an each categorical independent variable and the corresponding values for the frequency of an each categorical independent variable and the corresponding values for the frequency of an each categorical independent variable and the corresponding values for the frequency of an each categorical independent variable and the corresponding values for the frequency of an each categorical independent variable and the corresponding values for the frequency of an each categorical independent variable and the corresponding values for the frequency of an each categorical independent variable and the corresponding values for the frequency of an each categorical independent values and the corresponding values for the categorical independent values and the corresponding values are categorical independent values and the corresponding values and the corresponding values and the corresponding values are categorical independent values and the corresponding values are categorical values.
- Apply Laplace smoothing
- Calculate the parameters of the BDF corresponding equal to management wariable

Naïve Bayes Model

Consists of the frequency tables obtained from Bayes' Theorem under the conditional independence assumption (with or without Laplace smoothing)

Naïve Bayes prediction for an instance (X=a, Y=?)

We use Bayes' Theorem under the conditional independence assumption

Pros and Cons of Naïve Bayes

Pros

- Easy to implement ging farther tellicoge leasts from maintifie data (online learning)
- Performs well in multiplass prodiction coder.com
- Good for categorical variables in general

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Cons

- Data that are not observed require smoothing techniques to be applied
- For numerical variables, Gaussian distribution is assumed (strong assumption)
- Not good for regression problems

Aims of the Session

You should now be able to:

Assignment Project Exam Help

- Describe the fundamental concepts in probability theory https://powcoder.com
- Explain Bayes' Theoret and its Capate Pow Goder

Apply Naïve Bayes to classification for categorical and numerical independent variables