

### Constraint Handling — Objective Function

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#### Traveling Salesman Problem Formulation

- Design variables represent a candidate solution.
  - The design variable is a sequence **x** of *N* cities, where  $x_i \in \{1, \dots, N\}$ ,  $\forall i \in \{1, \dots, N\}.$

  - The N cities to be visited are represented by values {1,...,N}.

    The search space is also possible seed to be visited are in  $\{1,...,N\}.$ https://powcoder.com
- Objective function defines the wetcher solutionder

minimise totalDistance(
$$\mathbf{x}$$
) =  $\left(\sum_{i=1}^{N-1} D_{x_i, x_{i+1}}\right) + D_{x_N, x_1}$ 

where  $D_{i,k}$  is the distance of the path between cities j and k.

[Optional] Solutions must satisfy certain constraints.

$$\forall i \in \{1, \dots, N\}, \ h_i(\mathbf{x}) = \left(\sum_{j=1}^{N} 1(x_j = i)\right) - 1 = 0 \qquad 1(x_j = i) = \begin{cases} 1, & \text{if } x_j = i \\ 0, & \text{if } x_j \neq i \end{cases}$$

### Designing Objective Functions to Deal With Constraints

 The original objective function of a problem can be modified to deal with constraints.

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• A penalty can be added for infeasible solutions, increasing their cost.

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## Designing Objective Functions to Deal With Constraints

• E.g.: assume that the representation is a list of any size, and that our initialisation procedure is uniformly at random with replacement.

Objetive function:

minimise totalDistance(
$$\mathbf{x}$$
) =  $\left(\sum_{i=1}^{\text{Size}(\mathbf{x})-1} D_{x_i,x_{i+1}}\right) + D_{x_{\text{Size}(\mathbf{x})},x_1}$ 

How to modify the objective function to deal with the constraint that each city must appear once and only once?

## Designing Objective Functions to Deal With Constraints

 E.g.: assume that the representation is a list of any size, and that our initialisation procedure is uniformly at random with replacement.

Objetive function:

$$\text{minimise totalDistance}(\mathbf{x}) = \left(\sum_{i=1}^{\text{size}(\mathbf{x})-1} D_{x_i,x_{i+1}}\right) + D_{x_{\text{size}(\mathbf{x})},x_1} + n_m P + n_d P$$

where  $n_m$  is the number of cities missing,  $n_d$  is the number of duplications of cities and P is a large positive constant.

#### Generalising The Strategy

Minimise  $f(\mathbf{x})$ 

Subject to 
$$g_i(\mathbf{x}) \leq 0$$
,  $i = 1, \dots, m$ 

Assignment; Project  $\mathbb{Q}$  xam j  $\mathbb{H}_{e}$   $\mathbb{I}_{p}$ , ..., n

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Add WeChat powcoder Penalty Minimise  $f(\mathbf{x})+Q(\mathbf{x})$ 

$$Q(\mathbf{x}) = \begin{cases} 0 \text{ if } \mathbf{x} \text{ is feasible} & \text{Only sum here the violated constraints} \\ P \times [g_a(\mathbf{x})^2 + g_b(\mathbf{x})^2 + \dots + h_{a'}(\mathbf{x})^2 + h_{b'}(\mathbf{x})^2 + \dots] & \text{otherwise} \end{cases}$$

where *P* is a large positive constant.

#### Generalising The Strategy

Minimise 
$$f(\mathbf{x})$$

Subject to  $g_i(\mathbf{x}) \leq 0$ ,  $i = 1, \dots, m$ 

Assignments  $f(\mathbf{x})$  ject  $f(\mathbf{x})$  is  $f(\mathbf{x})$ . Assignments  $f(\mathbf{x})$  is  $f(\mathbf{x})$  is  $f(\mathbf{x})$ . Add WeChat powcoder  $f(\mathbf{x})$  is  $f(\mathbf{x})$ . We have  $f(\mathbf{x})$  is  $f(\mathbf{x})$  is  $f(\mathbf{x})$ .

$$Q(\mathbf{x}) = P \times [v_{g1}g_1(\mathbf{x})^2 + v_{g2}g_2(\mathbf{x})^2 + \dots + v_{gm}g_m(\mathbf{x})^2 + \dots + v_{h1}h_1(\mathbf{x})^2 + v_{h2}h_2(\mathbf{x})^2 + \dots + v_{hn}h_n(\mathbf{x})^2]$$

where P is a large positive constant, and  $v_{gi}$  and  $v_{hi}$  are 1 if the corresponding constraint is violated and 0 otherwise.

# Dealing with Constraints Based on Objective Functions

- Advantage:
  - Easier to designsignment Project Exam Help
- Disadvantage: https://powcoder.com
  - Algorithm has to seed the form to as it is a seed of the form to as it is a

#### Completeness

 If we use a strategy to deal with constraints that never enables any infeasible solution to be generated, algorithms such as Hill Climbing and Simulated Annealing are complete.

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- Otherwise:
  - https://powcoder.com

    Hill Climbing: not complete if the objective function has local optima.

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  - Simulated Annealing: not guaranteed to find a feasible solution within a reasonable amount of time.

#### Summary

- We need to design strategies to deal with the constraints.
- Examples of strategies:
  - Representationsi in the signification of the significant of the significant
  - Objective function https://powcoder.com

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Example applications.