# Assignment Project Exam Help

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#### Abstraction

### Assimn mentioned for the interactions of different components can be simplified by hiding the details of each component's implementation from the rest of the system. Details of a component with the component of the system. The rest of the system.

- protecting it with an interface.
- Abstraction is maintained by ensuring that the rest of the s/Aenic nva/htte change f ipenWation dtel not affect the interface.

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module IntSet = struct

```
Assignment Project Exam Help
     let is_empty = function
      https://powcoder.com
     let equal_member (x : int) (y : int) =
     -Add WeChat powcoder
        [] -> false
      | y :: rest ->
         if (equal_member x y) then true
         else mem x rest
     let add x t =
```

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```
let rec remove x = function

| [] -> []

| ttpequel_mphor xycoder.com
| else y :: (remove x rest)
```

# Assignment Project Exam Help

```
let one_two_three : IntSet.t =

IntSet_add 1

IntSet_add 2

POWCOder.com

(IntSet.add 3 IntSet.empty))
```

# Assignment Project Exam Help

```
open IntSet

let hettp::/powcoder.com
add 1 (add 2 (add 3 empty))
```

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Interpolation in the polarity of the polarity

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```
module IntSetPlus = struct
include IntSet
let singleton x = padd x empty
end
```

### Modules: signatures

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```
val empty: 'a list

val is_empty: 'a list -> bool

val trap ember pin vy coder.com

val mem pint -> pnt list -> bool

val add: int -> int list -> int list

val remove: int -> int list -> int list

val Add: We hat powcoder
```

### Modules: signatures

# Assignment Project Exam Help val empty: int list val is\_empty: int list -> bool val man : int fo/int list -> bool

val remove : int -> int list -> int list

val to\_list : int list -> int list

### Modules: signatures

```
ssignment Project Exam Help
  val is_empty : int list -> bool
  val mem : int -> int list -> bool
  val to list : int list -> int list
end
modulArded: We Chat powcoder
end
```

Modules: abstract types

```
Assignment reproject Exam Help

| x :: xs ->
| print_int x;
| https://powcoder.com
| [] -> ()

in
| print_string "{ ";
| Chat powcoder
| print_string "} eChat powcoder
```

### Modules: abstract types

```
ssignment Project Exam Help
  val is_empty : t -> bool
  val mem : int -> t -> bool
  valittpist.//pow.coder.com
  val to list : t -> int list
end
modulArded: We Chat powcoder
end
```

### Modules: abstract types

```
let rec loop = function
| x :: xs ->
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| loop xs | [] -> ()
```

# let print\_set (s : IntSet.t) : unit =

https://powcoder.com

# Character de Chara

Error: This expression has type IntSet.t but an expression was expected of type int list

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#### Invariants

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Abstraction has further implications beyond the ability to replace one implementation/with another:

\*\*TTDS://powcoder.com\*\*
Abstraction allows us to preserve invariants on types.

#### **Invariants**

# Assignments Project Exam Help val zero : t val succ : t -> t val titips://powcoder.com type t = int let zero = 0 let succ x = x + 1 let Actor end let Actor val titips://powcoder.com

### The meaning of types

# Assignment representation fundamentally changes the notion of what a type is:

- Inaffinguage without abstraction (Le the simply typed lambda calculus) types only represent particular data representations.
- In a language with abstraction (e.g. System F) types can represendably warrants art value WCOGET

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```
ssignment Project Exam Help
  val open_readonly : string -> t
  val read : t -> string
**https://powcoder.com
  type t = int
  let open_readwrite filename = ...
  let A dd We Chat powcoder
end
```

# Assignment Project Exam Help

```
# let f = File.open_readonly "foo" in
    File.write f "bar";;
    https://powcoder.com

Exception: Invalid argument "write: file is read-only".
```

```
ssignment Project Exam Help
  val open_readonly : string -> t
  val read : t -> string
**https://powcoder.com
  type t = int
  let open_readwrite filename = ...
  let A dd We Chat powcoder
end
```

```
module File : sig
  type readonly
ssignment Project Exam Help
   val open_readwrite : string -> readwrite t
  val open_readonly : string -> readonly t
  val read : 'a t/7 string val https://powender.com
  type readonly
  type readwrite
  typAddintWeChat powcoder
  let open_readonly filename = ...
  let read f = ...
  let write f s = \dots
 end
```

# Assignment Project Exam Help

Characters 51-52:

https://powcoder.com

Error: This expression has type File.readonly File.t

but an expression was expected of type

Afder We Finat powcoder
Type File readonly is no compatible with type

File.readwrite

### The meaning of types (continued)

# Assignment by reogeneent mox and st Help particular data representation, higher-kinded abstraction allows types to represent an even wider set of concepts:

- last kinded abstraction restricts types to directly representing invariants on values, with each type corresponding to particular set of values.
- Higher kinded abstraction allows types to represent more general cancelity without addlect to lepwdence to takes.

# Assignment Project Exam Help

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if p  $[\alpha]$  x y

# Assignment Project Exam Help $\Lambda_{\alpha::*,\lambda_{p}:Bool.\lambda_{x}:\alpha.\lambda_{y}:\alpha.}$

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# Assignment Project Exam Help

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# Assignment Project Exam Help

https://powcoder.com

 $\begin{array}{c} \forall \alpha :: *. \forall \beta :: *. \ \, \text{Bool} \ \, \rightarrow \ \, \alpha \rightarrow \beta \rightarrow \exists \gamma :: *. \gamma \\ Add \ \, \textbf{WeChat powcoder} \end{array}$ 

```
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E: 'a * ('a -> 'a)* ('a -> string) -> t

let ints =
E(0) https://powieoder.com

let floats =
E(0.0, (fun x -> x +. 1.0), string_of_float)

let Add WheChat powcoder
p (s (s z))
```

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Example: lightweight static capabilities

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Example: lightweight static capabilities

```
Signment Project Exam Help
  else begin
    let mid = (high + low)/2 in
        S#/#powcoder.com
     if res = 0 then Some mid
     else if res < 0 then look low (mid - 1)
  Add WeChat powcoder
  look 0 (Array.length arr)
```

Example: lightweight static capabilities

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## Assignment Project Exam Help

```
# let test1 = search compare arr 'c';;
val thttps://powcoder.com
```

## Assignment Project Exam Help

```
# let test1 = search compare arr 'c';;
val thttps://powcoder.com
# let test2 = search compare arr 'a';;
val test2 : int option = Some 0
```

## Assignment Project Exam Help

```
# let test1 = search compare arr 'c';;

val that tint option = Some 2 coder.com

# let test2 = search compare arr 'a';;

val test2 : int option = Some 0

# let Ae t3 compare arr 'a';

Exception: Invalid_argument "index out of bounds".
```

```
let search cmp arr v =
Assignment Project Exam Help
        let mid = (high + low)/2 in
     https://pow.coder.com
         if res = 0 then Some mid
         else if res < 0 then look low (mid -
     Add WeChat powcoder
      end
    in
      look 0 (Array.length arr)
```

```
let search cmp arr v =
Assignment Project Exam Help
        let mid = (high + low)/2 in
     https://pow.coder.com
         if res = 0 then Some mid
          else if res < 0 then look low (mid -
      Add WeChat powcoder
      end
     in
      look 0 ((Array.length arr) - 1)
```

## Assignment Project Exam Help

## Assignment Project Exam Help

```
type ('s, 'a) t

type 's index

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val set : ('s, 'a) t -> 's index -> 'a -> unit

val get : ('s, 'a) t -> 's index -> 'a

Add WeChat powcoder
```

## Assignment Project Exam Help

```
type 'a brand =
| Brand : ('s, 'a) t -> 'a brand
| https://powcoder.com
val brand : 'a array -> 'a brand
```

## Assignmenta Project Exam Help

https://powcoder.com

Error, This expression has type s#1 BArray.index

out and xpression has type s#1 BArray.index

Type s#1 is not compatible with type s#2

## Assignment Project Exam Help

```
val index: ('s, 'a) t -> int -> 's index option
val hostion s: 's powcoder.com
val middle: 's index -> 's index -> 's index

val next: 's index -> 's index -> 's index option
val pavened: wire c-haind bowcoder
```

```
struct
   type ('s,'a) t = 'a array
```

## Assignment Project Exam Help

https://gpawcoder.com

```
type 's index = int
Add avechat powcoder
if i >= 0 && i < Array.length arr then Some i
else None

let position idx = idx

let zero = 0</pre>
```

```
let last arr = (Array.length arr) - 1
  let middle idx1 idx2 = (idx1 + idx2)/2
     nment Project Exam Help
      if next <= limit then Some next
      else None
     ttps://powcoder.com
    let prev = idx - 1 in
      if prev >= limit then Some prev
              VeChat powcoder
  let get = Array.get
end
```

```
let bsearch cmp arr v =
      let open BArray in
      let rec look barr low high =
Assignment Project Exam Help
        Tet res = cmp v x in
          if res = 0 then Some (position mid)
           tps://powcoder.com
             Some prev —> look barr low prev
             None -> None
       Add h Weddhatwpowcoder | Some next -> look barr next high
             None -> None
      in
        match brand arr with
         Brand barr -> look barr zero (last barr)
         Empty -> None
```

## Assignment Project Exam Help

```
let set = Array unsafe_set

https://powcoder.com
```

## Assignment Project Exam Help

Abstraction in System  $F\omega$  https://powcoder.com

## Assignment Project Exam Help

https://powcoder.com

```
Assignment Project Exam Help

(Nat - \alpha - \beta - \beta \)

(Nat - \alpha - \beta - \alpha - \beta \)

(Nat - \alpha - \alpha - \alpha - \alpha \)

(Nat - \alpha - \alpha - \alpha - \alpha \)

(Nat - \alpha - \alpha - \alpha - \alpha \)

(Nat - \alpha - \alpha - \alpha - \alpha \)

(Nat - \alpha - \alpha - \alpha - \alpha \)

(Nat - \alpha - \alpha - \alpha - \alpha \)

(Nat - \alpha - \alpha - \alpha - \alpha \)

(Nat - \alpha - \alpha - \alpha - \alpha - \alpha \)

(Nat - \alpha - \alpha - \alpha - \alpha - \alpha - \alpha \)

(Nat - \alpha - \alpha
```

```
empty = \Lambda \alpha :: *.\lambda s: \text{NatSetImpl} \alpha . \pi_1 s is_empty = \Lambda \alpha :: *.\lambda s: \text{NatSetImpl} \alpha . \pi_2 s \longrightarrow nem = \Lambda \alpha :: *.\lambda s: \text{NatSetImpl} \alpha . \pi_4 s \longrightarrow nemove = \Lambda \alpha :: *.\lambda s: \text{NatSetImpl} \alpha . \pi_5 s to_list = \Lambda \alpha :: *.\lambda s: \text{NatSetImpl} \alpha . \pi_6 s
```

```
nat_set_package =
 signment Project Exam Help
          isempty [Nat],
          \lambdan:Nat.fold [Nat] [Bool]
             (\lambda x: Nat, \lambda y: Bool.or y (equal_nat n x))
                            wcoder.com
          \lambdan:Nat.fold [Nat] [List Nat]
             (\lambda x: Nat. \lambda 1: List Nat)
          \lambda1:List Nat.1 \rangle
  as \exists \alpha :: *. \texttt{NatSetImpl} \ \alpha
```

## Assignment Project Exam Help

```
(add [NatSet] hat_set) two
((add [NatSet] hat_set) three
((empty [NatSet] nat_set)))

Add WeChat powcoder
```

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## Assignment Project Exam Help

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#### Relational abstraction

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We can give a precise description of abstraction using relations nttps://poetweconder.com

#### Definable relations

## Assignment Project Exam Help We define relations between types

https://poweder.com

where A and B are System F types, and  $\phi[x,y]$  is a logical formula involving x and y.

#### Definable relations

Logical connectives:

## Assignment Project Exam Help

 $\underset{\text{Existential quantifications:}}{\text{https:}} \forall x : A.\phi \mid \forall \alpha.\phi \mid \forall R \subset A \times B.\phi$ 

## $\underset{\text{Relations:}}{\text{Add}} \overset{\text{def}}{\text{WeChat}} \overset{\exists \alpha.\phi}{\text{powcoder}}$

$$\phi ::= R(t, u)$$

Term equality:

$$\phi ::= (t =_A u)$$

## Assignment Project Exam Help

```
val empty: t

val https://powcoder.com

val mem: t -> int -> bool

val add: t d > int -> t -> t hat powcoder

val add: t d > int -> t -> t hat powcoder
```

```
type t_{list} = int list
   let_empty_{list} = []
Assignment Project Exam Help
       -> false
   https://powcoder.com
     y :: rest ->
       if x = y then true
     Add We Chat powcoder
```

```
let add<sub>list</sub> x t =
  if (mem<sub>list</sub> x t) then t
  else x :: t
```

## Assignment Project Exam Help

```
let if_empty_list t x y =

match t with

pys://powcoder.com
```

 $\begin{array}{c} \texttt{type} \quad \texttt{t}_{tree} \; = \\ \mid \; \texttt{Empty} \end{array}$ 

```
Assignment Project Exam Help
    let is_empty<sub>tree</sub> = function
     https://powcoder.com
    let rec mem_{tree} x = function
     | Empty -> false
     Add, WeChat powcoder
         else if x < y then mem_{tree} x
         else mem tree x r
    let rec add tree x t =
       match t with
       | Empty -> Node(Empty, x, Empty)
```

# Assignment Project Exam Help if x = y then t else if x < y then Node(add<sub>tree</sub> x 1, y, r)

https://powcoder.com

atch t with

| Empty -> x

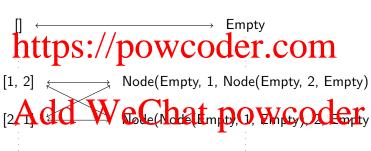
```
Assignment Project Examt Help
```

https://powcoder.com

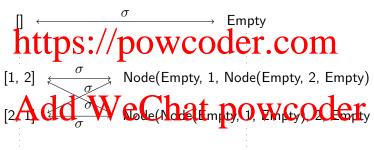
```
Assignment Project Examt Help
```

 $\overset{\texttt{1}}{https://powcoder.com}\overset{\texttt{Empty}}{coder.com}$ 

```
Assignment Project Examt Help
```



# Assignment Project Examt Help



#### Relations between values

## Assignment Project Exam Help

#### Relations between values

## Assignment Project Exam Help

```
let empty_{list} = [] ~ let empty_{tree} = Empty https://powcoder.com \sigma(empty_{list}, empty_{tree}) Add WeChat powcoder
```

#### Relations between values

### 

https://powcoder.eom

```
\sigma(x,y) \Rightarrow (\mathsf{is\_empty}_{list} \, x \, = \, \mathsf{is\_empty}_{tree} \, y)
```

```
Assignment | Prest | Assignment | Assignment
```

```
\begin{array}{c} https://pow-coder.com \\ \sim \\ \text{Node}(I,\ y,\ r) \rightarrow \\ \text{if } x = y \text{ then true} \\ \text{else if } x < y \text{ then mem}_{tree} \times I \\ \\ Add \ Weelse \ matree powcoder \end{array}
```

```
| let rec mem<sub>list</sub> x = function
| [] -> false
| y :: rest -> | Project Exam Help
| Assignment | Rest | Project Exam Help
```

```
https://powcoder.com

if x = y then true

else if x < y then mem<sub>tree</sub> x |

Add Welsenatreepowcoder
```

```
\begin{split} \forall x: t_{list}. \, \forall y: t_{tree}. \, \forall i: Int. \, \forall j: Int. \\ \sigma(x,y) &\Rightarrow (i=j) \Rightarrow (\mathsf{mem}_{list} \, xi \, = \, \mathsf{mem}_{tree} \, yj) \end{split}
```

```
let add_{list} \times t =
     if (mem_{list} \times t) then t
     else x :: t
Assignment Project Exam Help
             match t with
               Empty -> Node(Empty, x, Empty)
      https://pow.coder.com
                 else if x < y then
                   Node (add _{tree} \times I, y, r)
       Add W&Chat powcoder
```

let  $add_{list} \times t =$ 

```
Assignment Project Exam Help

match t with

| Empty -> Node(Empty, x, Empty)
```

https://powcoder.com

## Add W&Chat.powcoder

```
\begin{split} \forall x: t_{list}. \, \forall y: t_{tree}. \, \forall i: Int. \, \forall j: Int. \\ \sigma(x,y) &\Rightarrow (i=j) \Rightarrow \sigma(\mathsf{add}_{list} \, xi, \, \mathsf{add}_{tree} \, yj) \end{split}
```

let if\_empty<sub>list</sub> t x y =

```
Assignment Project Exam Help
```

```
https://poweder.com
```

```
let if_empty<sub>list</sub> t x y =
  match t with
```

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$$\begin{array}{c} \text{A} \stackrel{\gamma}{\text{Ad}} \underset{list.}{\text{We}} \underset{y:t_{ree}.}{\text{Nat}} \underset{\gamma.}{\text{powcoder}} \\ \sigma(x,y) \Rightarrow (a=c) \Rightarrow (b=d) \Rightarrow \\ (\text{if\_empty}_{list} x a b = \text{if\_empty}_{tree} y c d) \end{array}$$

```
Given t : t_{list} and s : t_{tree} such that \sigma(t, s):
```

# Assignment Project Exam Help

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```
Given {\tt t} : {\tt t_{\it list}} and {\tt s} : {\tt t_{\it tree}} such that \sigma({\tt t},~{\tt s}):
```

# Assignment Project Exam Help

```
\begin{array}{c} \text{if\_empty}_{\textit{list}} \text{ t t (add}_{\textit{list}} \text{ t 1)} \\ \textbf{https://powcoder.com}_{\text{if\_empty}_{\textit{tree}} \text{ s s (add}_{\textit{tree}} \text{ s 1)} \end{array}
```

```
Given t : t_{list} and s : t_{tree} such that \sigma(t, s):
```

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## if And d. Wee Chat powcoder

 $\sim$ 

 $\mathsf{if}\_\mathsf{empty}_\mathit{tree} \;\; \mathsf{t} \;\; \mathsf{mem}_\mathit{tree} \;\; \mathsf{mem}_\mathit{tree}$ 

```
let if_empty<sub>list</sub> t x y =
  match t with
```

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### 

```
let if_empty<sub>list</sub> t x y =
  match t with
```

# Assignment Project Exam Help

https://poweoer.com

$$\begin{array}{c} \mathbf{A} \forall \mathbf{W} \not\in \mathbf{Chat} \ \mathbf{powcoder} \\ \sigma(x,y) \Rightarrow \rho(a,\,c) \Rightarrow \rho(b,\,d) \Rightarrow \\ \rho(\mathrm{if\_empty}_{list} \, x \, a \, b, \, \mathrm{if\_empty}_{tree} \, y \, c \, d) \end{array}$$

val empty:

t

 $\sigma(\mathsf{empty}_{list},\,\mathsf{empty}_{tree})$ 

val is\_empty:

# Assignment Projector Examulelp

val mem:

$$\forall x: t_{list}. \ \forall y: t_{tree}. \ \forall i: Int. \ \forall j: Int.$$

thttps://powcodericom

val add:

$$\forall x: t_{list}. \ \forall y: t_{tree}. \ \forall i: Int. \ \forall j: Int.$$

## Add WeChat, poi viceder

$$\forall \gamma. \ \forall \delta. \ \forall \rho \subset \gamma \times \delta.$$

$$\begin{split} \forall x: t_{list}. \ \forall y: t_{tree}. \ \forall a: \gamma. \ \forall b: \gamma. \ \forall c: \delta. \ \forall d: \delta. \\ \sigma(x,y) \Rightarrow & \rho(a,\ c) \Rightarrow & \rho(b,\ d) \Rightarrow \\ \rho(\text{if\_empty}_{list}\ x\ ab, \ \text{if\_empty}_{tree}\ y\ c\ d) \end{split}$$

val empty:

t

 $\sigma(\mathsf{empty}_{list}, \, \mathsf{empty}_{tree})$ 

val is\_empty:

# Assignment Projector Examulelp

val mem:

 $\forall x: t_{list}. \ \forall y: t_{tree}. \ \forall i: Int. \ \forall j: Int.$ 

thttps://powcoderist / powcoderist

val add:

 $\forall x: t_{list}. \ \forall y: t_{tree}. \ \forall i: Int. \ \forall j: Int.$ 

## Add WeChat, poi viceder

val if\_empty:

$$\forall \gamma. \ \forall \delta. \ \forall \rho \subset \gamma \times \delta.$$

 $\rho(\mathsf{if\_empty}_{list} \, x \, a \, b, \, \mathsf{if\_empty}_{tree} \, y \, c \, d)$ 

val empty:

t

 $\sigma(\mathsf{empty}_{list},\,\mathsf{empty}_{tree})$ 

val is\_empty:

# Assignment Projector Examulelp

val mem:

$$\forall x: t_{list}. \ \forall y: t_{tree}. \ \forall i: Int. \ \forall j: Int.$$

## thttps://powcoder.icom

val add:

$$\forall x: t_{list}. \ \forall y: t_{tree}. \ \forall i: Int. \ \forall j: Int.$$

## Add WeChat, poi wiccoder

val if\_empty:

$$\forall \gamma. \ \forall \delta. \ \forall \rho \subset \gamma \times \delta.$$

$$\begin{split} \forall x: t_{list}. \ \forall y: t_{tree}. \ \forall a: \gamma. \ \forall b: \gamma. \ \forall c: \delta. \ \forall d: \delta. \\ \sigma(x,y) \Rightarrow & \rho(a,\ c) \Rightarrow & \rho(b,\ d) \Rightarrow \end{split}$$

 $\rho(\mathsf{if\_empty}_{list} \, x \, a \, b, \, \mathsf{if\_empty}_{tree} \, y \, c \, d)$ 

val empty:

t

 $\sigma(\mathsf{empty}_{list},\,\mathsf{empty}_{tree})$ 

val is\_empty:

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val mem:

$$\forall x: t_{list}. \ \forall y: t_{tree}. \ \forall i: Int. \ \forall j: Int.$$

thttps://powcoder.icom

val add:

$$\forall x: t_{list}. \ \forall y: t_{tree}. \ \forall i: Int. \ \forall j: Int.$$

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val if\_empty:

$$\forall \gamma. \ \forall \delta. \ \forall \rho \subset \gamma \times \delta.$$

$$\begin{split} \forall x: t_{list}. \ \forall y: t_{tree}. \ \forall a: \gamma. \ \forall b: \gamma. \ \forall c: \delta. \ \forall d: \delta. \\ \sigma(x,y) \Rightarrow & \rho(a,\ c) \Rightarrow & \rho(b,\ d) \Rightarrow \end{split}$$

 $\rho(\mathsf{if\_empty}_{list} \, x \, a \, b, \, \mathsf{if\_empty}_{tree} \, y \, c \, d)$ 

val empty:

t

 $\sigma(\mathsf{empty}_{list},\,\mathsf{empty}_{tree})$ 

val is\_empty:

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val mem:

$$\forall x: t_{list}. \ \forall y: t_{tree}. \ \forall i: Int. \ \forall j: Int.$$

thttps://powcodericom

val add:

$$\forall x: t_{list}. \ \forall y: t_{tree}. \ \forall i: Int. \ \forall j: Int.$$

## Add WeChat, poi viceder

$$\forall \gamma. \ \forall \delta. \ \forall \rho \subset \gamma \times \delta.$$

$$\begin{split} \forall x: t_{list}. \ \forall y: t_{tree}. \ \forall a: \gamma. \ \forall b: \gamma. \ \forall c: \delta. \ \forall d: \delta. \\ \sigma(x,y) \Rightarrow & \rho(a,\ c) \Rightarrow & \rho(b,\ d) \Rightarrow \\ \rho(\text{if\_empty}_{list} \ x \ a \ b, \ \text{if\_empty}_{tree} \ y \ c \ d) \end{split}$$

### Relational substitution

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- $\blacktriangleright$  type T with free variables  $\overrightarrow{\alpha}=\alpha_1,\dots,\alpha_n$
- https://powcoder.com

We define the relation:  $Add \ \ We \ \ Chat \\ P \cap Chat \\ P \cap Chat \\ P \cap Chat \\ N \cap Cha$ 

Relational substitution: free variables

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 $\mathbf{https://poweoder.com}$ 

Relational substitution: products

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### Relational substitution: sums

```
If T is T' + T'' then
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                                                                                                                                                                                                                                                                           \exists u': T'[\overrightarrow{A}]. \ \exists v': T'[\overrightarrow{B}].
                                                                                           https://pow condition and condition are supported by the condition of th
                                                                                            Add We Charle powcoder
                                                                                                                                                                                                                                                                                                                            \wedge T''[\vec{\rho}](u'', v'')
```

Relational substitution: functions

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$$\begin{array}{c} \mathbf{h}_{\mathsf{T}[\vec{\rho}]}^{T[\vec{\rho}]} = \frac{f' + T[\vec{A}], \ g : T[\vec{B}]}{p_{\mathsf{v}}} \underbrace{\mathbf{der}}_{[\vec{A}]} \underbrace{\mathbf{der}}_{[\vec{B}]} \underbrace{\mathbf{com}}_{T'[\vec{\rho}](u, \ v) \Rightarrow T''[\vec{\rho}](f \ u, \ g \ v)} \\ \end{array}$$

Relational substitution: univerals

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### Relational substitution: existentials

```
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\exists \gamma. \ \exists \delta. \ T' \text{ then} \\ \exists \gamma. \ \exists \delta. \ \exists \rho' \subset \gamma \times \delta. \\ \text{https://powcoder:com} \\ x = \mathsf{pack} \ \gamma. \ u \text{ as } T[A]
```

Add WeChatTpowooder

val empty:

t.

 $\sigma(\mathsf{empty}_{list}, \, \mathsf{empty}_{tree})$ 

val is\_empty:

# Assignment Projector Examulelp

val mem:

 $\forall x: t_{list}. \, \forall y: t_{tree}. \, \forall i: Int. \, \forall j: Int.$ 

 $\text{`https:'/powcoder': } com_{yj}$ 

val add:

 $\forall x: t_{list}. \, \forall y: t_{tree}. \, \forall i: Int. \, \forall j: Int.$ 

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$$\forall \gamma. \ \forall \delta. \ \forall \rho \subset \gamma \times \delta.$$

val empty:

t.

 $(\alpha)[\sigma](\mathsf{empty}_{list},\,\mathsf{empty}_{tree})$ 

val is\_empty:

# Assignment Projector Examulelp

val mem:

$$\forall x: t_{list}. \, \forall y: t_{tree}. \, \forall i: Int. \, \forall j: Int.$$

 $\text{thttps://powcoder.}^{intps://powcoder.}^{intps://powcoder.}^{(i,y)}$ 

val add:

$$\forall x: t_{list}. \, \forall y: t_{tree}. \, \forall i: Int. \, \forall j: Int.$$

## 

$$\forall \gamma. \ \forall \delta. \ \forall \rho \subset \gamma \times \delta.$$

$$\begin{split} \forall x: t_{list}. \ \forall y: t_{tree}. \ \forall a: \gamma. \ \forall b: \gamma. \ \forall c: \delta. \ \forall d: \delta. \\ \sigma(x,y) &\Rightarrow \rho(a,\ c) \Rightarrow \rho(b,\ d) \Rightarrow \\ \rho(\text{if\_empty}_{list} \ x \ ab, \ \text{if\_empty}_{tree} \ y \ c \ d) \end{split}$$

val empty:

t.

 $(\alpha)[\sigma](\mathsf{empty}_{list},\,\mathsf{empty}_{tree})$ 

val is\_empty:

# Assignment Project Exam Help

val mem:

 $\forall x: t_{list}. \, \forall y: t_{tree}. \, \forall i: Int. \, \forall j: Int.$ 

 $\text{thttps://powcoder.}^{intpowcoder.}/\text{powcoder.}^{(i,y)}$ 

val add:

 $\forall x: t_{list}. \, \forall y: t_{tree}. \, \forall i: Int. \, \forall j: Int.$ 

## 

$$\forall \gamma. \ \forall \delta. \ \forall \rho \subset \gamma \times \delta.$$

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val empty:

t.

 $(\alpha)[\sigma](\mathsf{empty}_{list},\,\mathsf{empty}_{tree})$ 

val is\_empty:

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 $\text{thttps://powcoder.com}^{\text{total}}/\text{powcoder.com}^{(\alpha \to \beta \to \gamma)[\sigma, \text{distance}]}$ 

val add:

 $\forall x: t_{list}. \, \forall y: t_{tree}. \, \forall i: Int. \, \forall j: Int.$ 

## 

val if\_empty:

 $\forall \gamma. \ \forall \delta. \ \forall \rho \subset \gamma \times \delta.$ 

 $\forall x: t_{list}. \ \forall y: t_{tree}. \ \forall a: \gamma. \ \forall b: \gamma. \ \forall c: \delta. \ \forall d: \delta.$   $\sigma(x,y) \Rightarrow \rho(a,\ c) \Rightarrow \rho(b,\ d) \Rightarrow$   $\rho(\mathsf{if\_empty}_{list}, x \, a \, b, \ \mathsf{if\_empty}_{tree}, y \, c \, d)$ 

val empty:  $\label{eq:alpha} \mathbf{t} \qquad \qquad (\alpha)[\sigma](\mathsf{empty}_{list},\,\mathsf{empty}_{tree})$ 

val is\_empty:

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 $\text{thttps://powcoder.com}^{\text{total}} / \text{powcoder.com}^{(\alpha \to \beta \to \gamma)[\sigma, \text{deg.}](\text{mem}_{list}, \text{mem}_{tree})}$ 

val add:

## $A\overrightarrow{dd} \overrightarrow{W}eChat \overrightarrow{powcoder}^{\text{\tiny cold}}$

 $\begin{array}{lll} \text{val if\_empty:} & \forall \gamma. \ \forall \delta. \ \forall \rho \subset \gamma \times \delta. \\ \\ \text{t -> 'a -> 'a -> 'a} & \forall x: t_{list}. \ \forall y: t_{tree}. \ \forall a: \gamma. \ \forall b: \gamma. \ \forall c: \delta. \ \forall d: \delta. \\ & \sigma(x,y) \Rightarrow \rho(a,\ c) \Rightarrow \rho(b,\ d) \Rightarrow \\ & \rho(\text{if\_empty}_{list} \ x \ ab, \ \text{if\_empty}_{tree} \ y \ c \ d) \end{array}$ 

val empty:  $(\alpha)[\sigma](\mathsf{empty}_{list},\,\mathsf{empty}_{tree})$ 

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val mem:

val is\_empty:

 $\text{thttps://powcoder.com}^{\text{total}} / \text{powcoder.com}^{(\alpha \to \beta \to \gamma)[\sigma, \text{degr.com}](\text{mem}_{list}, \text{mem}_{tree})}$ 

val add:

## Add WeChat powcoder

val if\_empty:

 $\texttt{t -> 'a -> 'a -> 'a } (\forall \delta.\,\alpha \rightarrow \delta \rightarrow \delta) [\sigma] (\texttt{if\_empty}_{list},\, \texttt{if\_empty}_{tree})$ 

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```
\hat{\tap{s}://powcoder.com}
\times(\alpha \rightarrow \beta \rightarrow \beta \rightarrow \alpha \rightarrow \alpha \rightarrow \beta \
```

### Relational abstraction

# $\mathbf{A} \underset{\forall \beta_1 \dots \forall \beta_n. \ \forall x: \ (\exists \alpha. T). \ \forall y: \ (\exists \alpha. T).}{\mathsf{Given a type}} \overset{\text{Given a type } T \ \text{with free variables,}}{\mathsf{Project}} \overset{\alpha, \beta_1, \dots}{\mathsf{Exam}} \overset{\beta}{\mathsf{Help}}$

$$\begin{array}{c} \mathbf{https:}/\!\!/\!\!\operatorname{poweder.com}_{\exists u\,:\,T[\gamma,\,\beta_1,\,\dots\,\beta_n].\,\exists v\,:\,T[\delta,\,\beta_1,\,\dots\,\beta_n].} \\ x=y \quad \Leftrightarrow \quad x=\operatorname{pack}\,\gamma,\,u\text{ as }T[\overline{A}]\\ \mathbf{Add}\,\,\mathbf{WeChat}\,\,\operatorname{poweder}_{\wedge\,T[\sigma,\,\equiv_{\beta_1},\,\dots\,,\,\equiv_{\beta_n}](u,\,v)} \end{array}$$

#### Relational abstraction

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If there is a relation between the implementation types of two values with prigrential types use their implementations behave the same with respect to this relation, then the two values are equal.

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#### Invariants

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#### Invariants

# Assignment Project Exam Help Given a type T with free variable $\alpha$ :

http
$$\overset{f}{\text{s.}}$$
  $\overset{f}{\text{p.}}$   $\overset{g}{\text{p.}}$   $\overset{g}{\text{p.}$ 

#### Invariants

Note that:

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https:// $\overset{(\Lambda\alpha.\ \lambda x\ :\ T[\alpha].\ t)}{\text{powcoder.com}}^{u}$ 

So

$$\bigcap_{\rho} \bigcap_{\text{open (pack } \gamma, \text{ } u \text{ as } \exists \alpha. \ T[\alpha])} \bigcap_{\text{open (pack } \gamma, \text{ } u \text{ as } \exists \alpha. \ T[\alpha]) \text{ as } x, \text{ } \alpha \text{in } t)} \bigcap_{\text{open (pack } \gamma, \text{ } u \text{ as } \exists \alpha. \ T[\alpha]) \text{ as } x, \text{ } \alpha \text{ in } t)}$$

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### Identity extension

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Given a type T with free variables  $\alpha_1,\dots,\alpha_n$  :

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$$T[=_{\alpha_1}, \dots, =_{\alpha_n}](x, y)$$

Next time

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