

1 Printing and parsing

The `Printf` and `Scanf` modules in the OCaml standard library expose functions for printing and parsing using format strings. For example, here is a call to `sprintf` to build a string from a pair of integers:

```
# Printf.sprintf "(%d, %d)" 3 4;;  
- : string = "(3, 4)"
```

And here is a call to `sscanf` to read a pair of integers from a string:

```
# Scanf.sscanf "(3, 4)" "(%d, %d)" (fun x y -> (x, y));;  
- : int * int = (3, 4)
```

The full implementations of `Printf` and `Scanf` consist of many thousands of lines of code. (See the files `camlinternalFormat.ml`, `camlinternalFormatBasics.ml`, and `scanf.ml` in the OCaml distribution.) This exercise focuses on cut-down variants of the functions consisting of only a few lines.

The OCaml implementation processes a format string such as `"(%d,%d)"` in two steps. First, the string is converted by the compiler into a typed AST. You can see a representation of the AST by ascribing the type `_ format` to the string at the OCaml prompt:

```
# ("(%d, %d)" : _ format);;  
- : (int -> int -> 'a, 'b, 'a) format =  
Format  
  (Char_literal ('(',  
    Int (Int_d, No_padding, No_precision,  
      String_literal ("", "  
        Int (Int_d, No_padding, No_precision,  
          Char_literal (')', End_of_format))))),  
    "(%d,%d)"))
```

Second, when the program runs, the `sprintf` and `sscanf` functions interpret the AST to determine how to turn values into strings or to read values from strings.

This question focuses on the second step, and so we'll write ASTs directly rather than using format strings. Our goal is to build staged versions of `sprintf` and `sscanf` that avoid interpretative overhead by generating code specialized to the format strings.

The file `exercise3_printf.ml` contains an implementation of format specifiers as a data type:

```
type (_,_) fmt =  
  | Int : (int -> 'a, 'a) fmt  
  | Lit : string -> ('a, 'a) fmt  
  | Bool : (bool -> 'a, 'a) fmt  
  | Cat : ('a, 'b) fmt * ('b, 'c) fmt -> ('a, 'c) fmt  
let (%) x y = Cat (x, y)
```

and an implementation of a function `sprintf` that interprets format specifiers to turn values into strings:

```
val sprintf : ('a, string) fmt -> 'a
```

For example, here is a call to `sprintf` equivalent to the call to the standard library function on page 3:

```
# sprintf (Lit "(" % Int % Lit ", " % Int % Lit ")") 3 4;;
- : string = "(3, 4)"
```

(a) Build a staged version of `sprintf` with the following type:

```
val sprintf_staged : ('a, string) fmt -> 'a code
```

that generates code to print a string rather than printing the string directly:

```
# sprintf_staged (Lit "(" % Int % Lit ", " % Int % Lit ")");;
- : (int -> int -> string) code =
.< fun i ->
  fun j ->
    ((((" " ^ string_of_int i) ^ ", ") ^ string_of_int j) ^ ")")>.
```

The goal is to eliminate interpretative overhead, and so the generated code should not contain any values of the `fmt` type (`Int`, `Lit`, etc.).

(b) Following the idealized staging process for `sprintf` results in less than optimal code. For example, adjacent literals in a format specifier result in a call to the string concatenation operator in the generated code, even though the information needed for concatenation is available during code generation:

```
# sprintf_staged (Lit "a" % Lit "b");;
- : string code = .<"a" ^ "b">.
```

As is often the case, the problem can be solved by using partially-static data.

Give an implementation of the following module for partially-static strings:

```
module Ps_string : sig
  type t
  (** The type of partially-static strings *)

  val sta : string -> t
  (** Build a partially-static string from a static string *)

  val dyn : string code -> t
  (** Build a partially-static string from a dynamic string *)

  val cd : t -> string code
  (** Turn a partially-static string into a dynamic string *)

  val (++) : t -> t -> t
  (** Concatenate two partially-static strings *)
end
```

that eliminates as much concatenation as possible from the code returned by `cd`:

```
# .< fun c -> .~(cd (sta "a" ++ sta "b" ++ dyn .<c>.
                    ++ sta "d" ++ sta "e")) >.;;
- : (string -> string) code = .<fun c -> "ab" ^ (c ^ "de")>.
```

- (c) Use your implementation of `Ps_string` to build an improved version of `sprintf_staged` that concatenates adjacent literal strings during code generation:

```
# sprintf_improved (Lit "a" % Lit "b");;
- : string code = .<"ab">.
```

- (d) A second way to improve generated code is to take advantage of the fact that the `bool` type has only two inhabitants. A straightforward implementation of `sprintf_staged` might generate the following code for printing booleans

```
# sprintf_staged (Lit "(" % Bool % Lit ", " % Bool % Lit ")");;
- : (bool -> bool -> string) code =
  .< fun b -> fun c -> "(" ^ string_of_bool b ^ ", " ^
                        string_of_bool c ^ ")">.
```

However, with branches on the possible `bool` values we could write equivalent code without any concatenations:

```
fun b -> fun c -> if b then
  if c then "(true, true)"
  else "(true, false)"
else
  if c then "(false, true)"
  else "(false, false)"
```

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Implement the following *if-insertion* interface (analogous to the *let-insertion* discussed in the lectures):

```
val split : bool code -> bool
val if_locus : (unit -> 'a code) -> 'a code
```

and use it to give a third implementation of the staged printf function:

```
val sprintf_improved2 : ('a, string) fmt -> 'a code
```

that generates concatenation-free code for the format specifier above.

(NB: the continuations bound in effect handlers can only be invoked once. The function `Obj.clone`, that builds a copy of a continuation, can be used to work around this limitation.)

- (e) The format specifiers used for printing with `sprintf` can also be used for parsing. Give an implementation of the parsing function `sscanf` with the following type:

```
val sscanf : ('a, 'b) fmt -> string -> 'a -> 'b
```

using the supplied helper functions `read_exact`, `read_int`, and `read_bool`, or otherwise.

- (f) Give a staged implementation of `sscanf` that accepts a format specifier and returns code for a parsing function:

```
val sscanf_staged ('a, 'r) fmt -> ('string -> 'a -> 'r) code =
```

For example, your function might generate code like this for parsing an integer between parentheses:

```
# sscanf_staged (Lit "(" % Int % Lit ")");;
- : (string -> (int -> '_a) -> '_a) code =
.< fun s -> fun k -> fst (let (k,s) =
    let (k,s) =
      let (_,s) = read_exact "(" s in
      (k, s) in
    let (k,s) =
      let (i,s) = read_int s in
      (k i, s) in
    (k, s) in
  let (k,s) =
    let (_,s) = read_exact ")" s in
    (k, s) in
  (k, s))>.
```

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As with `sprintf_staged`, the goal is to eliminate interpretative overhead, and so the generated code should not contain any values of the `fmt` type (`Int`, `Lit`, etc.).

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- (g) The code in part (f) does not look much like a typical hand-written implementation, due to the nested `let` bindings and unnecessary intermediate tuples.

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`Let` insertion can help generate code that is more idiomatic, and probably more efficient. However, the implementation of `let` insertion presented in lectures only builds variable bindings (`let x = e in ...`), not tuple bindings (`let (x, y) = e in ...`).

Implement the following interface for `let` insertion with tuple bindings:

```
val genlet2 : ('a * 'b) code -> ('a code * 'b code)
val let_locus2 : (unit -> 'a code) -> 'a code
```

and use it to give a second implementation of `sscanf_staged` that generates code without nested `let` bindings or superfluous tuple values:

```
# sscanf_staged_improved (Lit "(" % Int % Lit ")");;
- : (string -> (int -> '_a) -> '_a) code =
.< fun s ->
  fun k ->
    let (x1,s) = read_exact "(" s in
    let (x2,s) = read_int s in
    let (x3,s) = read_exact ")" s in
    k x2>.
```

(20 marks)

2 Staged searching

Multi-stage programming is a good fit for algorithms that involve a preparatory step, since the preparation can typically be performed during code generation to build specialized code. For example, the performance of string searching can be improved by building a table with information that avoids more comparisons than necessary.

As a concrete example, consider the task of searching for a string `aab` (the “needle”) within a second string (the “haystack”). A naive implementation might proceed as follows:

First, compare `aab` with the first three characters `ab?` (\leadsto failure!)

a	?	?	?	?	?
a	a	b			

a	b	?	?	?	?
a	a				

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Next, compare `aab` with the second three characters `b??` (\leadsto failure!)

a	b	?	?	?	?
	a	a	b		

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Next, compare `aab` with the third three characters `aaa` (\leadsto failure!)

a	b	a	?	?	?
		a	a	b	

a	b	a	a	?	?
		a	a	b	

a	b	a	a	a	?
		a	a	b	

Finally, compare `aab` with the fourth three characters `aab` (\leadsto success!)

a	b	a	a	a	?
		a	a	b	

a	b	a	a	a	?
			a	a	b

a	b	a	a	a	b
			a	a	b

This approach is obviously correct, but it involves unnecessary work, repeatedly examining the same characters. For example, the fourth comparison starts by examining the fourth and fifth characters of the haystack, even though the previous comparison has already determined that those character are both a. The efficiency of the search strategy can be improved by using the information revealed by each comparison to determine where to restart the search.

Information about where to restart after failure depends only on the needle, not the haystack. If the comparison fails at the i th character of the needle, then the previous $i-1$ characters of the haystack must match the first i characters of the needle. For example, for the needle aab, if the comparison fails after the second a (as in the third comparison illustrated above), then the previous two characters of the haystack must both be a

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a	b	a	a	a	?
			a	a	b

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and so the search can skip the first character of the next search, and begin on the second:

a	b	a	a	a	?
			a	a	b

Similar reasoning for each character of the needle leads to the following table:

a	a	b
0	1	0

where the entry for the i th character indicates that, if a comparison fails after i characters, the first $i - \text{table}[i]$ characters of the next comparison can be skipped.

More precisely, each new comparison should start after the portion of the haystack just examined, unless there is some overlap between the end of the successfully

matched portion and the beginning of the needle. If the i most recent characters examined in the haystack correspond to the i characters at the beginning of the needle then the new comparison should begin with the beginning of the needle moved back i characters from the failure point; however, the characters in the overlapping portion can be skipped.

In the example above, at most one character can be skipped. Longer needles typically allow skipping more characters. For example, here is the table for `abcdabd`:

a	b	c	d	a	b	d
0	0	0	0	1	2	0

If the comparison fails after successfully matching `abc`

a	b	c	x	?	?	?	?	?	?
a	b	c	d	a	b	d			

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then the next comparison can skip forward three ($3 - \text{table}[\text{needle}[3]]$) characters, since neither `bc` nor `c` matches the beginning of the needle.

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a	b	c	x	?	?	?	?	?	?
a	b	c	d	a	b	d	a	b	d

(a) Implement the naive search functions

```
val naive_search_from : string -> string -> int -> bool
val naive_search : string -> string -> bool
```

so that `naive_search_from n h i` compares `n` with each `length(n)` substring of `h`, starting from index `i` in `h`, and using character-wise comparison, and so that `naive_search` simply calls `naive_search_from`, passing `0` as the third argument.

(b) Following the idealized staging process described in the lectures, implement a staged version of `naive_search` that accepts the needle string and builds code for a search function specialized to the needle:

```
val naive_search_staged : string -> (string -> bool) code
```

For example, your implementation might generate code like the following for the needle `aab`:

```
# naive_search_staged "aab";;
- : (string -> bool) code =
.< fun s ->
```

```
let rec loop i =
  ((s.[i] = 'a' && s.[i+1] = 'a' && s.[i+2] = 'b')
   || loop (i + 1)) in
try loop 0 with Invalid_argument _ -> false >.
```

(c) (i) Implement the functions

```
val proper_prefixes : string -> string list
val proper_suffixes : string -> string list
```

that respectively compute the proper prefixes and proper suffixes of a string. A proper prefix or suffix of s is a prefix or suffix of s that is shorter than s . For example,

```
# proper_prefixes "abcd";;
- : string list = ["abc"; "ab"; "a"]
# proper_suffixes "abcd";;
- : string list = ["bcd"; "cd"; "d"]
```

(ii) Either using proper prefixes and proper suffixes or otherwise, implement a function that computes the skip table:

```
val skip_table : string -> (char * int) list
```

The skip for the i th entry may be computed as the length of the longest proper prefix of $\text{pat}[0..i]$ that is also a proper suffix of the same string.

(d) Using skip table from part (c)(ii), implement and stage the improved search algorithm as a function of the following type:

```
val fancy_search_staged : string -> (string -> bool) code
```

For example, your function might generate code like the following for the needle abab:

```
.< fun s ->
  let rec match_b i =
    if s.[i + 3] = 'b'
    then true
    else match_bab (i + 2)
  and match_ab i =
    if s.[i + 2] = 'a'
    then match_b i
    else match_abab (i + 2)
  and match_bab i =
    if s.[i + 1] = 'b'
    then match_ab i
    else match_abab (i + 1)
  and match_abab i =
    if s.[i] = 'a'
    then match_bab i
    else match_abab (i + 1) in
try match_abab 0 with Invalid_argument _ -> false >.
```


Note that when `match_b` fails, it restarts the search by calling `match_ab`, not `match_abab`. And note, too, that the failure case in `match_b` and `match_ab` bumps the index by 2 to avoid unnecessarily re-scanning parts of the haystack already seen.

Although the example code above uses `let rec`, you may need to use an encoding of recursive functions, such as the reference-based approach discussed in Lecture 15, since generating `let rec` binding groups of arbitrary size is difficult or impossible. (However, solutions that use `let rec` are welcome, if you can find an approach that works.)

(15 marks)

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