Last time: GADTs

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This time: monads (etc.)

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What do monads give us?

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A way to structure effectful programs in a functional language Add WeChat powcoder

## Assignment Project Exam Help

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What's an effect?

## Assignment Protein a church in the Assignment of the contract of the contract

If an https://potwcoderhagom

## Add WeChat pewcoder

changes the behaviour then M also performs effects.

Effects available in OCaml

Effects unavailable in OCaml

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Effects available in OCaml

Effects unavailable in OCaml

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raise Not\_found

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raise Not\_found

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### Add WeChat powcoder

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raise Not\_found

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concurrency (interleaving)

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raise Not\_found

1/http://powcoder.com

concurrency (interleaving)

non-Addition We Chat powcoder

let rec f x = f x

(higher-order) state non-determinism

Assignment Project Exam Help exceptions

raise Not\_found

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non-tendition we chat powcoder

let rec f x = f x

concurrency (interleaving)

Effects available in OCaml Effects unavailable in OCaml non-det<u>erm</u>inism (higher-order) state Assignment Project Exam Help exceptions raise Not\_found escape x in e 1/16 traigus so/toowcoder.com concurrency (interleaving) non-Addition We Chat powcoder let rec f x = f x

Effects available in OCaml Effects unavailable in OCaml non-determinism (higher-order) state Assignment Project Exam Help exceptions raise Not\_found escape x in e I/Of various so/ts OWC polymerphic state concurrency (interleaving) non-tendition we chat powcoder let rec f x = f x

Effects unavailable in OCaml Effects available in OCaml non-determinism (higher-order) state Assignment Project Exam Help exceptions escape x in e raise Not\_found hof various so/to OWC polyinorphic state concurrency (interleaving) checked exceptions  $\underset{\text{non-tellible tiowed Chair}}{\text{GCA}_{\text{finalise}}} \overset{\text{GCA}_{\text{finalise}}}{\text{which the power of the powe$ let rec f x = f x

### Capturing effects in the types

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We might have two function arrows:

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and combinators for combining effectful functions

compose ignored (
$$a \rightarrow b$$
)  $\rightarrow (a \rightarrow c) \rightarrow (a \rightarrow c)$  ignored ( $a \rightarrow b$ )  $\rightarrow (a \rightarrow c) \rightarrow (a \rightarrow c)$  pair  $\rightarrow (a \rightarrow b) \rightarrow (a \rightarrow c) \rightarrow (a \rightarrow c)$ 

 $\mathsf{liftPure} \quad : \quad (a \to b) \to (a \leadsto b)$ 

### Separating application and performing effects

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Decompose effectful arrows into functions and computations <a href="https://powcoder.com">https://powcoder.com</a>

 $a \rightsquigarrow b$  becomes  $a \rightarrow T b$ 

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(let x = e in ...)

### Programming with monads

### Assignment Project Exam Help

let () = counter := id + 1 in

 $\underset{\tt u}{\text{https://powcoder.com}}$ 

A monadic program

#### Monads

```
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val return: 'a → 'a t

val (>=): 'a t → ('a → 'b t) → 'b t

end https://powcoder.com
```

#### Monads

```
Assignment Project Exam Help

val return: 'a \rightarrow 'a t

val (>=): 'a t \rightarrow ('a \rightarrow 'b t) \rightarrow 'b t

end

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```

### Assignment Project Exam Help

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# Assignment Project Exam Help

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# Assignment Project Exam Help

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```
Assignment Project Exam Help
```

https://powcoder.com

# Assignment Project Exam Help

```
type state

type state

in lude MONAD

val put D State

val put D State

val runState : 'a t \rightarrow init:state \rightarrow state * 'a

end
```

```
ssignment Project Exam Help
    val get : state t
    {\tt val} \  \, {\tt put} \  \, : \  \, {\tt state} \  \, \to \  \, {\tt unit} \  \, {\tt t}
  \texttt{end} \ https://powcoder.com}^{\texttt{val}} https://powcoder.com}
  type 'a t = state \rightarrow state * 'a
  Add WeChat powcoder
```

```
ssignment Project Exam Help
    val get : state t
    {\tt val} \  \, {\tt put} \  \, : \  \, {\tt state} \  \, \to \  \, {\tt unit} \  \, {\tt t}
  \texttt{end} \ https://powcoder.com}^{\texttt{vah}} https://powcoder.com}
  type 'a t = state \rightarrow state * 'a
  Add WeChat powcoder
```

```
ssignment Project Exam Help
    val get : state t
    {\tt val} \  \, {\tt put} \  \, : \  \, {\tt state} \  \, \to \  \, {\tt unit} \  \, {\tt t}
  \texttt{end} \ https://powcoder.com'^{\texttt{a}}
  type 'a t = state \rightarrow state * 'a
  Add We Chat powcoder
```

```
ssignment Project Exam Help
    val get : state t
    {\tt val} \  \, {\tt put} \  \, : \  \, {\tt state} \  \, \to \  \, {\tt unit} \  \, {\tt t}
  \texttt{end} \ https://powcoder.com}^{\texttt{val}} https://powcoder.com}
  type 'a t = state \rightarrow state * 'a
  Add We Chat powcoder
```

```
ssignment Project Exam Help
    val get : state t
    {\tt val} \  \, {\tt put} \  \, : \  \, {\tt state} \  \, \to \  \, {\tt unit} \  \, {\tt t}
  \texttt{end} \ https://powcoder.com}^{\texttt{vah}} https://powcoder.com}
  type 'a t = state \rightarrow state * 'a
  Add WieChat powcoder
```

```
module type STATE = sig
 type state
        ment Project Exam Help
 va Pput : state → unit
 val runState : 'a t \rightarrow init:state \rightarrow state * 'a
end
   https://powcoder.com
  : STATE with type state = S.t = struct
 type state = S.t
               Pechat powcoder
 let get s = (s, s)
 let put s' _ = (s', ())
 let runState m ~init = m init
end
```

type 'a tree =

```
Empty: 'a tree
signment Project Exam Help
let fresh_name : string IState.t =
           tps://powcoder.com
  return (Printf.sprintf "x%d" i)
 \underbrace{ \text{function} }_{\text{Empty}} \underbrace{ \text{tree} : \text{'a tree} \rightarrow \text{string tree IState.t = } }_{\text{return}} \underbrace{ \text{echat powcoder} }_{\text{empty}} 
   | Tree (1, v, r) 
ightarrow
     label_tree l \gg fun l \rightarrow
     fresh name \gg fun name \rightarrow
     label_tree r \gg fun r \rightarrow
     return (Tree (1, name, r))
```

State satisfies the monad laws

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#### State satisfies the monad laws

```
Assignment Project Exam Help

| definition of return, >>= |
| fun s -> let s', a = (fun s -> (s, v)) s in k a s'
| https://powcoder.com
```

#### State satisfies the monad laws

```
Assignment Project Exam Help

| definition of return, >>= |
| fun s \rightarrow let s', a = (fun s \rightarrow (s, v)) s in k a s'
| fun type://powcoder.com
```

#### State satisfies the monad laws

```
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\begin{array}{l}
\text{fun s} \to \text{let s', a} = (\text{fun s} \to (\text{s, v})) \text{ s in k a s'} \\
\text{fun littes.} \not/\text{powcoder.com} \\
\text{fun s} \to \text{k v s} \\
\text{Add WeChat powcoder}
```

#### State satisfies the monad laws

```
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| fun s \rightarrow let s', a = (fun s \rightarrow (s, v)) s in k a s'

| fun type / powcoder.com

| (\beta for let)
| fun s \rightarrow k v s

| Add WeChat powcoder
```

module type ERROR = sig

```
Assignment Project Exam Help
```

```
let lettips://.powcoderictom t =

fun p l → match l with

[] → raise "Not found!"

| x :: when p x → return x

| Add | Wie P | Nat powcoder
```

```
_try_ (
  find (greater ~than:3) l >>= fun v →
  return (string_of_int v)
) ~catch:(fun error → error)
```

### Assignment Project Exam Help

```
val raise : error \rightarrow 'a t val type: 'a t \rightarrow catch:(error \rightarrow 'a) \rightarrow 'a end https://powcoder.com
```

```
val: 'a → 'a t

ExA:drd WeChat powcoder
```

let return v = Val v

```
ment Project Exam Help
  val raise : error \rightarrow 'a t
  val _try_ : 'a t \rightarrow catch:(error \rightarrow 'a) \rightarrow 'a
end https://powcoder.com
type 'a t
     Add WeChat powcoder
  {\tt Val} \ {\tt v} \ \to \ {\tt k} \ {\tt v} \ | \ {\tt Exn} \ {\tt e} \ \to \ {\tt Exn} \ {\tt e}
```

### Assignment Project Exam Help

```
val raise : error \rightarrow 'a t

val typ: 'a't \rightarrow catch:(error \rightarrow 'a) \rightarrow 'a

end https://powcoder.com
```

```
type 'a t = Val : 'a → 'a t ExA:dd WeChat powcoder
```

let raise e = Exn e

```
nment Project Exam Help
  val raise : error \rightarrow 'a t
  val _try_ : 'a t \rightarrow catch:(error \rightarrow 'a) \rightarrow 'a
end https://powcoder.com
type 'a t
Add We Chat powcoder
  \texttt{Val} \ \texttt{v} \ \rightarrow \ \texttt{v} \ | \ \texttt{Exn} \ \texttt{e} \ \rightarrow \ \texttt{catch} \ \texttt{e}
```

```
module type ERROR = sig
type error
include MONAD
```

### Assignment Project Exam Help

```
module Error (E:, sig type t end)
: Preps://powcoder.com
   type 'a t =
         Val: 'a \rightarrow 'a t
   Andd We Chat powcoder
   let (\gg) m k = match m with
       \mathtt{Val} \ \mathtt{v} \ \rightarrow \ \mathtt{k} \ \mathtt{v} \ | \ \mathtt{Exn} \ \mathtt{e} \ \rightarrow \ \mathtt{Exn} \ \mathtt{e}
   let raise e = Exn e
   let _try_ m ~catch = match m with
      \texttt{Val} \ \texttt{v} \ \rightarrow \ \texttt{v} \ | \ \texttt{Exn} \ \texttt{e} \ \rightarrow \ \texttt{catch} \ \texttt{e}
end
```

else return v)

#### Exception satisfies the monad laws

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#### Exception satisfies the monad laws

### Assignment Project Exam Help

```
v >>= return

= (definition of return, >>=)
marktyp (val y power com
```

#### Exception satisfies the monad laws

### Assignment Project Exam Help

### Assignment Project Exam Help

ht/psa/motowiseddenocoda

({P} C {Q})

#### Parameterised monads and Hoare Logic

# Assignment Project Exam Help has precondition 'p has postcondition 'q httpsoduce posw Ender.com

i.e. ('A'dd We Chat powcoder

Strengthening the interface: parameterised monads

### Assignment-Project Exam Help

```
type ('s,'t,'a) t

val return : 'a → ('s,'s,'a) t

val ('r,'t,'b) t
```

end

#### A parameterised monad for state

### Assignment Project Exam Help

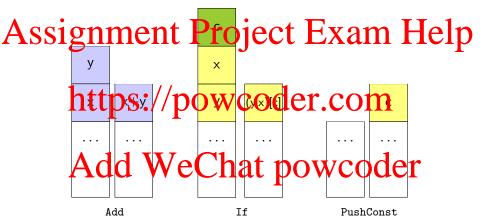
```
sig include PARAMETERISED_MONAD val pet ps://s/powcoder.com val put ps://s/powcoder.com val runState: ('s,'t,'a) t \rightarrow init:'s \rightarrow 't * 'a end
```

#### A parameterised monad for state

### Assignment Project Exam Help

```
struct type ('s, 't, 'a) t = 's \rightarrow 't * 'a let return v \cdot s \neq (s \cdot v) let put s = (s, ()) let get s = (s, s) let runState m init = m init end Add WeChat powcoder
```

### Programming with polymorphic state: a stack machine



#### Programming with polymorphic state: a stack machine

```
module type STACK_OPS =

sig

type ('s,'t,'a) t

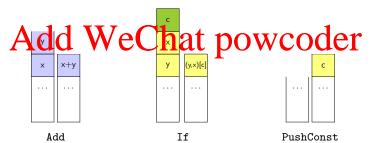
Assignment Introject Exam Help

val_if_: (bool * ('a * 's)'),

'a * 's, unit) t

val_push_const: 'a \to ('s,

end https://powcoder.com
```



#### Programming with polymorphic state

```
module type STACKM = sig
                      rojęct Exam Help
val execute : ('s,'t,'a) t \rightarrow 's \rightarrow 't * 'a
end
modulttps://powcoder.com
 include PState
               Ven tat, (y, s)) - put (x+y, s)

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let push_const k = get \gg fun s \rightarrow put (k, s)
let execute = runState
end
```

### Assignment Project Exam Help

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effectful programs
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#### Monadic effects are higher-order

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```
\underset{\mathsf{uncurryE}}{\text{https:}} ( \underset{(a \leadsto b \leadsto c)}{\overset{\mathsf{pairE}}{\rightarrow}} : \underset{(a \leadsto b \leadsto c)}{\overset{\mathsf{(a \leadsto d)}}{\rightarrow}} \underset{(a \times b \leadsto c)}{\overset{\mathsf{(a \times c \leadsto b \times d)}}{\rightarrow}} \\ \underset{\mathsf{uncurryE}}{\text{uncurryE}} : \underset{(a \leadsto b \leadsto c)}{\overset{\mathsf{(a \times b \leadsto b \times d)}}{\rightarrow}} \\ \underbrace{}
```

#### Higher-order effects with monads

gу

```
val composeM :
Assignment Project Exam Help
   let composeM f g x =
      f x \gg fun y \rightarrow
      <sup>e</sup>https://powcoder.com
   val uncurryM :
    'a Add WeChat powcoder
   let uncurryM f (x,y) =
      f x \gg fun g \rightarrow
```

Next time: arrows, applicatives (etc.)

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