Last time: staging basics

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Staging recap

Assignment Project Exam Help Goal: Specialise with available data to improve future performance

 $\frac{\text{New-constructs:}}{\text{nttps:}}/\text{powcoder.com}$ Example: pow

Power, staged

let rec pow x n =

```
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          let pow_code n = .< fun x \rightarrow . (pow .<x>. n) >.
           https://powcoder.com
          # pow_code 3;;
          .<fun x \rightarrow x * x * x * 1>.
          \# \underset{\mathtt{val} \ \mathtt{pow3}}{\textbf{Atdows}}, \underset{\mathtt{int} \ \to \ \mathtt{int}}{\textbf{we cohert3}} \\ \texttt{pow some of the total pow coder}
          # pow3 '4;;
          -: int = 64
```

1. Write the program as usual:

```
val program : t_sta \rightarrow t_dyn \rightarrow t
```

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1. Write the program as usual:

```
{\tt val} \  \, {\tt program} \  \, : \  \, {\tt t\_sta} \  \, \rightarrow \  \, {\tt t\_dyn} \  \, \rightarrow \  \, {\tt t}
```

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1. Write the program as usual:

```
{\tt val} \  \, {\tt program} \  \, : \  \, {\tt t\_sta} \  \, \rightarrow \  \, {\tt t\_dyn} \  \, \rightarrow \  \, {\tt t}
```

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3. Compile using back:

```
https://powcoder.com
```

1. Write the program as usual:

```
{\tt val} \  \, {\tt program} \  \, : \  \, {\tt t\_sta} \  \, \rightarrow \  \, {\tt t\_dyn} \  \, \rightarrow \  \, {\tt t}
```

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3. Compile using back:

```
https://powcoder.code
```

4. Construct static inputs:

1. Write the program as usual:

```
	exttt{val} program : 	exttt{t_sta} 
ightarrow 	exttt{t_dyn} 
ightarrow 	exttt{t}
```

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3. Compile using back:

```
https://powcoder.com
```

4. Construct static inputs:

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5. Apply code generator to static inputs:

```
val specialized_code : (t_dyn \rightarrow t) code
```

1. Write the program as usual:

```
val program : t_sta \rightarrow t_dyn \rightarrow t
```

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3. Compile using back:

```
https://powcoder.com
```

4. Construct static inputs:

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5. Apply code generator to static inputs:

```
val specialized_code : (t_dyn \rightarrow t) code
```

6. Run specialized code to build a specialized function:

```
{\tt val} \  \  {\tt specialized\_function} \  \  : \  \  {\tt t\_dyn} \  \, \to \  \, {\tt t}
```

Inner product

Assignment Project Exam Help : int > float array > float array > float = fun n 1 r > https://powcoder.com else 1.(i) *. r.(i) +. loop (i + 1) Add WeChat powcoder

Inner product, loop unrolling

```
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: int -> float array code -> float array code -> float code

= fun n 1 r ->

https://powcoder.com

else .< ((.~1).(i) *. (.~r).(i))

+. .~(loop (i + 1)) >.

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```

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```
#.< fun 1 r \rightarrow . (dot' 3.<1>..<r>) >;;
-: {float array \rightarrow float array \rightarrow float) code =
.< fun type (0,0) . f. (0) +. ((1.(2) *. r.(2)) +. 0.))>.
```

Inner product, eliding no-ops

Assignment Project Exam Help fun 1 r -> let n = Array.length 1 in the trops then powcoder.com else match 1.(i) with 0.0 -> loop (i + 1) 1.0 -> ...(r).(i) +...(loop (i + 1)) >. Ard (Web) hat powcoder in 1000

Inner product, eliding no-ops

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```
 \begin{array}{l} \text{\#.< fun } r \to \text{``(dot'') [| 1.0; 0.0; 3.5 |] .< r>)>;;} \\ \text{-: https://pto.w.coder.com} \\ \text{.< full properties of the content of t
```

Binding-time analysis

let dot'

```
Classify variables into dynamic ('a code) / static ('a)
```

```
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```

```
dynamic: 1, r
static n
ttps://powcoder.com
```

Classify expressions into static (no dynamic variables) / dynamic

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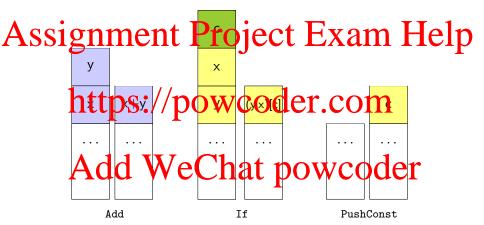
```
dynamic: 1.(i) *. r.(i)
static: i = n
```

Goal: reduce static expressions during code generation.

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https://powcoder.com Partially-static data structures

Stack machines again



Stack machines: higher-order vs first-order

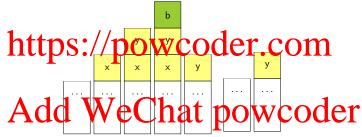
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```
type ('s, 't) t = 's \rightarrow 't let add (x, (y, s)) = (x + y, s)  \frac{\text{https://powcoder.com}}{\text{type ('s, 't) t = ('s, 't) instrs}}  let add = Add :: Stop
```

Recap: optimising stack machines

```
val (>>=) : 'a t \rightarrow ('a \rightarrow 'b t) \rightarrow 'b t
```

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PushConst x
PushConst y
PushConst true
If

PushConst y

Stack machines: basic interface

```
module type STACKM =
signment Project Exam Help
 val nothing : ('s, 's) t
 val (\otimes) : ('r, 's) t \rightarrow
 https://powcoder.com
 val _if_ : (bool * ('a * ('a * 's)),
 vaAddaWeChat powcoder
 val execute : ('s, 't) t \rightarrow 's \rightarrow 't
end
```

Higher-order stack machines

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```
type ('s, 't) t = 's \rightarrow 't let nothing s = 's let
```

push_const 3 ⊗

```
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let push_const v s = (v, s)
let add (x, (y, s)) = ((x + y, s))

https://powcoder.com
```

```
Assignment Project Exam Help
     let push_const v s = (v, s)
     let add (x, (y, s)) = ((x + y, s))
   Inlining push const. adpower der.com
     (fun s \rightarrow (3, s)) \otimes
     (fun s dd d4 We Chat powcoder
```

```
Why are the higher-order machines hard to optimize?

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let add (x, (y, s)) = ((x + y, s))
```

Inlinia https://powcoder.com

```
(\underset{(\text{fun }(x,\ (y,\ s))}{\text{fun }(x,\ (y,\ s))} \rightarrow ((x+y,\ s)))
```

```
Why are the higher-order machines hard to optimize?

Assignment Project Exam Help

let add (x, (y, s)) = ((x + y, s))
```

Inlinia https://powcoder.com

```
(\underset{(\text{fun }(x,\ (y,\ s))\ \rightarrow\ ((x+y,\ s)))}{\text{(Andd WeChat powcoder})}
```

Difficulty: evaluating under lambda

Stack machines: higher-order vs first-order vs staged

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type https://spoweoder.com

type Asdd W. Echat powcoder

Staging the higher-order stack machine

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```
module type STACKM_staged =

sig
in https://powcoder.com
val compile.
```

Staging the higher-order stack machine

```
module StackM_staged : STACKM_staged =
 struct
ssignment Project Exam Help
  let (\otimes) f x s = x (f s)
  let add p =
  .< let (c, (x, (y, s))) = .\tilde{p} in
       ((if c then x else y), s) >.
  1etAudd WeChat powcoder
  let compile f = .< fun s \rightarrow . (f .< s>.) >.
  let execute f s = !.(compile f) s
 end
```

Staging the higher-order stack machine: output

compile (push_const true \otimes _if_);;

```
- : ('_a * ('_a * '_b) \rightarrow '_a * '_b) code =
 .< fun s_59 \rightarrow
ssignment Project Exam Help
  # compile (push_const 3 \otimes push_const 4 \otimes
         tps://powcoder.com
     let (c,(x,(y,s))) = (false, (4, (3, s))) in
         c then x else y), s>.
 # comprie Chat powcoder
            push_const false & _if_);;
   - : ('_a \rightarrow int * '_a) code =
 .< fun s \rightarrow
     let (c,(x,(y,s))) = (false, (4, (3, s))) in
     ((if c then x else y), s)>.
```

Possibly-static values

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function

 $\texttt{Sta} \ \mathtt{v} \ \to . <\!\mathtt{v}\!>\!.$

Partially-static stacks

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```
Tail: 'a code \( \times 'a stack \)
| :::: 'a sd * 'b stack \( \times ('a * 'b) stack \)
| ttps://powcoder.com
| function
| Tail s \( \times \)
| cA:: dd WeChat powcoder
```

Stack machine: binding-time analysis

type ('s, 't) t = 's \rightarrow 't

```
let add (x, (y, s)) = (x + y, s)
ssignment Project Exam Help
 let add = Add :: Stop
 https://powcoder.com
 let add p = . < let (x, (y, s)) = . \tilde{p} in (x + y, s)>.
     Add WeChat, powcoder
 let rec add : type s.(int * (int * s), int * s) t =
  function
    Sta x :: Sta y :: s \rightarrow Sta (x + y) :: s
   1 ...
```

Stack machine: optimising add

Stack machine: optimising branches

Assignment Project Exam Help function | Sta true :: x :: y :: s \rightarrow x :: s | Shaftles: //ypowcoder.com | Dyn < if .~c then .~(unsd y) else .~(unsd x) >. :: s | (Tail _ as s) \rightarrow _if__ (extend s) | c \rightarrow ... (Tail _ as s) \rightarrow _if__ (c :: extend s) | c \rightarrow ... (Tail _ as s) \rightarrow _if__ (c :: extend s) | c \rightarrow ... (Tail _ as s) \rightarrow _if__ (c :: extend s) | c \rightarrow ... (Tail _ as s) \rightarrow _if__ (c :: extend s) | c \rightarrow ... (Tail _ as s) \rightarrow _if__ (c :: extend s) | c \rightarrow ... (Tail _ as s) \rightarrow _if__ (c :: extend s) | c \rightarrow ... (Tail _ as s) \rightarrow _if__ (c :: extend s) | c \rightarrow ... (Tail _ as s) \rightarrow _if__ (c :: extend s) | c \rightarrow ... (Tail _ as s) \rightarrow _if__ (c :: extend s) | c \rightarrow _if__ (c :: extend s) |

Stack machine: top-level compilation

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```
val compile : ('s, 't) t \rightarrow ('s \rightarrow 't) code

let  
let  
| The properties of the
```

Stack machine: flexible optimisation

```
# compile add;;
Assignment-Project Exam Help
    # compile _if_;;
    -: {bool * ('_a * ('_a * '_b)) \rightarrow '_a * '_b) code = 
.< fattps://powcoder.com
           then fst (snd (snd s))
           else fst (snd s)),
        Add We Chat powcoder
    # compile (push_const true & _if_);;
    - : ('_a * ('_a * '_b) \rightarrow '_a * '_b) code =
     .< fun s \rightarrow (fst s, snd (snd s))>.
```

Stack machine: flexible optimisation

```
Assignment-Project Stam Help
     # compile (push_const 3 \otimes push_const 4 \otimes
     # compile (push_const 3 \otimes push_const 4 \otimes
     - : ('_a \rightarrow int * '_a) code =
     .< fun s \rightarrow (7, s)>.
```

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Shatepieg/genewicoulogremming

```
\begin{array}{c} {\tt val~gshow:~\'a~data~\rightarrow~(\'a~\rightarrow~string)~code} \\ Add~WeChat~powcoder \end{array}
```

Generic programming: binding-time analysis

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Type representations are static Values are dynamic.

Note: Type representations are static values are dynamic.

Particular values are dynamic.

Now we'll use type representations to generate code.

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Goal: generate code that contains no typeable or data values.

Desired code for gshow

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```
type tree =
Empty: tree
| Blanch: branch proweder.com
```

```
let rec show tree = function

Empto empto
```

Generic programming

Type equality

```
type 'a typeable
```

Assignment Project Exam Help 'a typeable -> 'b typeable -> ('a,'b) eql option

Travhttps://powcoder.com

```
type 'a data
and 'u genericQ =
{ \q: 't data =
```

*Andidint Wata Chat powcoder

```
{\tt val} \ {\tt gmapQ} \ : \ {\tt 'u} \ {\tt genericQ} \ \to \ {\tt 'u} \ {\tt list} \ {\tt genericQ}
```

Generic functions

```
val gshow: string genericQ
```

Generic programming, staged

Type equality

```
type 'a typeable
```

Assignment Project Exam Help 'a typeable -> 'b typeable -> ('a,'b) eql option

Travhttps://powcoder.com

```
and 'u genericQ =

Add d' We Chat powcoder

vaf And d' int Wata Chat powcoder
```

```
val gmapQ : 'u genericQ \rightarrow 'u list genericQ
```

Generic functions

```
val gshow: string genericQ
```

Staging gmapQ

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```
\begin{array}{l} \text{gmapQ = fun \{ q \} (x, y) \rightarrow [q a x; q b y];} \\ \text{ $https://powcoder.com} \\ \text{let (*) a b = \{} \\ \dots \\ \text{gmapQ = fun } \text{ $w$ powcoder.} \\ \text{ $\sim$ $Atdd y $w$ en hat powcoder.} \end{array}
```

Staging gshow

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```
fun data v ->

"("^ data.constructor v

https://powcoder.com v)
```

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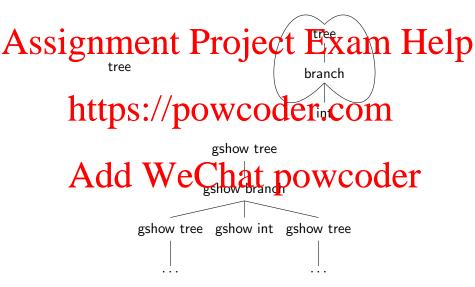
https://pow.coder.com Cyclic static structures

Cyclic type structures

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https://powcoderocom

Cyclic type structures



```
Assignment Project Exam Help
```

https://powcoder.com

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Assignment Project Exam Help
```

https://poweoder.com

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https://powcoder.com
```

```
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https://powcoder.com

Add We Chat proveder
```

```
Assignment Project Exam Help
    https://poweoder.com
    Add WeChat powcoder
         fib 1
            fib 0
```

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```
let rec fib n =

try List.assoc n !table

with Not_found
let rec fib n =

try List.assoc n !table

with Not_found
let rec fib n =

fib 3

fib 3

fib 2

and fib_aux = function

| 1 Add WeChat powcode |
| n → fib (n - 1) + fib (n - 2)
```

Memoization, factored

```
val memoize : (('a \rightarrow 'b) \rightarrow ('a \rightarrow 'b)) \rightarrow 'a \rightarrow 'b
ssignment Project Exam Help
     try List.assoc n !table
     with Not found \rightarrow
     https://powcoder.com
   in f'n
 Add WeChat powcoder
   0 \rightarrow 0
  n \rightarrow fib (n - 1) + fib (n - 2)
 let fib = memoize open_fib
```

Typed maps

```
type t
val empty: t
val add: t \rightarrow 'a data \rightarrow ('a \rightarrow string) code \rightarrow t

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```

https://powcoder.com

Typed maps

type t

```
Assignment Project Exam Help

type t =

Nil : t

| https://powcoder.com
```

Typed maps

type t

val empty : t

```
Assignment Project Exam Help
    type t =
      https://powcoder.com
    let empty = Nil
    let add t d x = Cons (d, x, t)
    type of a with a trpowooder
         Nil \rightarrow None
        | Cons (r, d, rest) 
ightarrow
         match 1.typeable =~= r.typeable with
           Some Refl \rightarrow Some d
         \mid None \rightarrow lookup rest 1
```

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https://powcoder.com Generating recursive definitions Add WeChat powcoder

Mutually-recursive definitions

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```
and oddp x =

noh(eyenp x)//powcoder.com
```

Difficulty: building up arbitrary-size let rec ... and ... and n-ary operator are difficulty about to about the control of the control o

Recursion via mutable state

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What if even and odd generated in different parts of the code? Plan: use let-insertion to interleave bindings and assignments.

Let insertion

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Let rec insertion

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```
https://powcoder.com
```

```
let r = genlet (< ref (fun _ -> assert false) >) in
let _ = genlet (< r := . ~(k . < ! . ~r >) >) in
. < !Ardd WeChat powcoder
```

Generating code for gshow

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```
let memofix h =

{ q fint point of my owcoder.com
let rec result d x = match lookup !tbl d with
Some f -> .< î . îx >.

None of with classification of the coder
.< fun y -> . ~(h result . y>) >)
in .< . ~g . ~x >.
```

Generating code for gshow

Assignments Froject Exam Help

```
let gshow_gen : string genericQ = string genericQ = https://apowcoder.com

.< "("^.~(data.constructor v)

^ String.concat " " .~((gmapQ gshow).q

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```

let gshow = memofix gshow_gen

Generated code for gshow

```
let show_tree = ref (fun \_ \rightarrow assert false) in
let show_branch = ref (fun _ → assert false) in
let show_int = ref (fun _ → assert false) in
                       Project Exam Help
       show_branch :=
 fun b \rightarrow
            s://powcoder.com
          [!show_tree l; !show_int v; !show_tree r]))
                   eChat powcoder
                       Branch _ + "Branch")
          ((String.concat
              (match t with
               | Empty \rightarrow []
               | Branch b \rightarrow [!show branch b])) ^")")) in
!show tree
```

Next time: reagents

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