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Week 3: K-Nearest Neighbours https://powcoder.com

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Week 3: K-Nearest Neighbours

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2. KNN properties

3. chttps://powcoder.com

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Reading: Chapter 3.5 of ISL.

Exercise questions: Chapter 3.7 of ISL, Q1, Q3 and Q4.

Introduction

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- A parametric model has a fixed number of parameters.

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 | A parame
- In a nanparametric prodel, the number of parameters grows with Chairing and a population of parameters grows are more flexible, but have larger variance and can be computationally infeasible for large datasets.

Introduction

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In this lecture, we consider the K-nearest neighbours method, a nonpartition of the K-nearest neighbours method.

Studying this method will also allow you to learn and consolidate

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K-nearest neighbours

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- K-nearest neighbours can be used for regression or Astition S. Thipokwello Cating Colors sion.
- KNN requires no distribution assumptions.
- · Supervised of unsupervised learning algorithm? Add WeChat powcoder

K-nearest neighbours

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for a training sample $\mathcal{D} = \{(y_i, \boldsymbol{x}_i)\}_{i=1}^N$.

Interpretable: the Creditart is possible possib

K-nearest neighbours

To understand the intuition behind the method, suppose that k=1 and there is an observation i for which $x_i=x$. Then, $\textbf{Assignment}_E(\textbf{Project}_x) \textbf{Exam Help}$

- That is, the KNN method can potentially approximate any regression by Wilson Good Tassur Dibathe form of this function.
- If the new value of the large of the larg
- The bais and variance of KNN is dependent on the selection of k. More details will be discussed later.

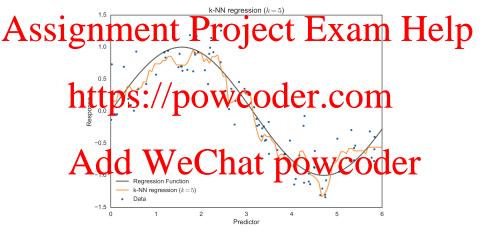
Illustration

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where we set $\sigma^2 = 0.1$ and restrict X to be between 0 and 6.

• In the slive impart = properties for the model and fit a KNN regression to this training sample.

Illustration (k = 5)



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Modelling choices

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for a training sample $\mathcal{D} = \{(y_i, x_i)\}_{i=1}^N$.

The https://powcoder.com

- 1. A distance metric Add WeChat powcoder
- 2. The number of neighbours k.
- 3. The predictors.

Distance

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We wind form se wheating at x point degree x (Euclidean) norm of the vector $x_i - x_l$.

Choosing the number of neighbours

The number of neighbours k is a hyperparameter: we need Assignment Perojectes Exam Help

- We cannot use the training data to pick k since we would then always choose k=1 and fit the data perfectly! $\frac{1}{1} \frac{1}{1} \frac{$
- Instead, we select \overline{k} based on bias-variance trade-off considerations.

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We will use model selection and estimate the test error for

We will use model selection and estimate the test error for each candidate value of k. We then select the value of k with the lowest error according to this criterion.

Overfitting and underfitting

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- With a small k, the bias will be relatively small since the restriction of the close to $f(x_0)$ (x_0 is prediction point). However, a small k means that we averaging only a few observations, leading to high variance $f(x_0)$ and $f(x_0)$ are the contraction of the production of the contraction of the contr
- As we increase k we reduce the variance, at the cost of higher bias. => Tend to underfitting.

Illustration

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Play the animation to see how the estimates change as we vary k.

Curse of dimensionality

Assignment is Ruli ojects Exama Help breaks down with high-dimensional inputs (high p).

- The poist has a point of the predictors of the predictors of the prediction point x.
- Add of Wine Chat production nonparametric methods.

Curse of dimensionality

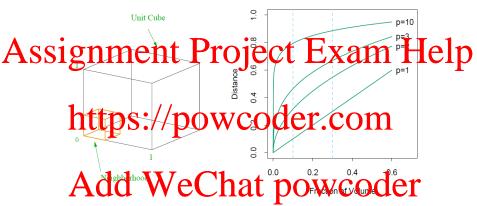


FIGURE 2.6. The curse of dimensionality is well illustrated by a subcubical neighborhood for uniform data in a unit cube. The figure on the right shows the side-length of the subcube needed to capture a fraction r of the volume of the data, for different dimensions p. In ten dimensions we need to cover 80% of the range of each coordinate to capture 10% of the data.

Computational considerations

The KNN method is a memory intensive method. It requires

Assignment repaire progression the method. It requires

Example 1. The KNN method is a memory intensive method. It requires

Assignment repaire progression the method. It requires

• Generating predictions is computationally costly. For each new input points we need to compute distances of the training points, and sort these values. That contrasts with linear regression, where computing predictions is cheap.

• Sorting algorithms have require a number of computations which is proportional to $N\log(N)$ on average, such that the KNN method does not scale well to large datasets.

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Comparison with linear regression

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Comparison with linear regression

The linear regression and KNN methods represent two

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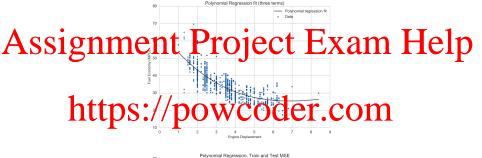
- Linear regression assumes a linear form for the regression function f(x). This assumption leads to stable predictions f(x), the second converge of the converge of the sumption of linearity in the parameters is incorrect.
- Manufeles in the uransampto the Wilcombig to highly flexible predictions (low bias). But its predictions can be very unstable (high variance), since only a few training observations contribute to each prediction.

Linear regression and KNN: illustration

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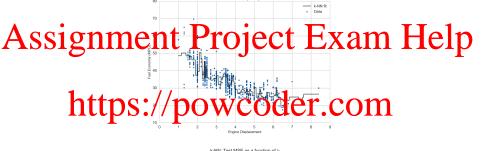
- Polynomial regressions and KNN are two alternatives for multiples for relationship between ghray Chiles per gallon (MPG) of the car and engine displacement.
- The defent was the sense of model complexity.

Linear regression and KNN: illustration

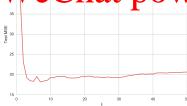




Linear regression and KNN: Illustration



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Parametric or nonparametric?

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- As always, the choice of method should be based on stimating the test performance with the available data. https://powcoder.com
- In general, we can say that a parametric model will outperform the nonparametric approach if the parametric form assumed for the greek of the tree of the control of the

Advanced: Mahalanobis distance

The Euclidean distance only makes sense if the predictors are in the same scale. An alternative is use the normalised Euclidean

Assignment Project Exam Help $d(\boldsymbol{x}_i, \boldsymbol{x}_l) = \sqrt{\sum_{j=1}^{p} \left(\frac{x_{ij} - x_{lj}}{s_{x_j}}\right)},$ where has same powd Gooder production the

$$d(\boldsymbol{x}_i, \boldsymbol{x}_l) = \sqrt{\sum_{j=1}^{D} \left(\frac{x_{ij} - x_{lj}}{s_{x_j}}\right)^2},$$

training sample.

A more that the remarker power of effects the Mahalanobis distance

$$d(\boldsymbol{x}_i, \boldsymbol{x}_l) = \sqrt{(\boldsymbol{x}_i - \boldsymbol{x}_l)^T S^{-1} (\boldsymbol{x}_i - \boldsymbol{x}_l)},$$

where S^{-1} is the sample covariance matrix of the predictors.

Advanced: effective number of parameters

- At first glance, it may difficult to relate our formal definition Assignment more than the image of the seems the KNN method only has one hyperparameter: the number of neighbours k.
 - Lettipus need per wooder of parameters of a model. For the KNN method, it is N/k

Add WeChat powcoder The intuition is the following: if the neighbourhoods were nonoverlapping, there would be N/k neighbourhoods. We fit one parameter (the mean) for each neighbourhood.

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Summary

Assignment Project Exam Help The KNN algorithm is a highly flexible method that does not

- The KNN algorithm is a highly flexible method that does not explicitly assume a form for the regression function f(X).
- https://powecoderexcom, with low bias but high variance.
- A arger value of the cost of a less flexible approximation, with low variance but high bias.

Summary

However, the KNN method has disadvantages that we need to

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- The estimate of the regression function can be very unstable, since it is the average of only a few points. This is the price that the for file of the composition of the price that the
- Curse of dimensionality.
- Addivere Chathan powcodernt predictors.
- Generating predictions is computationally expensive.

Review questions

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- What is a hyperparameter?
- . https://powcoder.com
- What is the curse of dimensionality?
- · What are the advantages and disappear ges or the driver method?