

# Assignment Project Exam Help

## Predictive Analytics

Week 13: ARIMA models (optional)

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Semester 2, 2018

Discipline of Business Analytics, The University of Sydney Business School

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## Week 13: ARIMA models (optional)

1. Stationarity and Box-Jenkins methodology

2. Differencing

3. Models for stationary series

4. ARIMA models

5. Seasonal ARIMA models

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This module provides a discussion of **ARIMA models**, the most widely used methods for univariate time series forecasting.

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ARIMA models aim to describe the serial dependence in the data, rather than to directly describe the time series components as in exponential smoothing. The two approaches are complementary.

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**Stationarity and Box-Jenkins**

**methodology**  
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## Stationarity (key concept)

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Intuitively, a **stationary** time series is one whose properties do not depend on the time at which we observe it.

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Time series with trend and seasonality are not stationary, since these patterns affect the change the mean of the series over time.

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## Strict stationarity (key concept)

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Formally, a time series process is **strictly stationary** when the joint distribution of  $Y_t, Y_{t-1}, \dots, Y_{t-k}$  does not depend on  $t$ . That is, the joint density

$$p(y_t, y_{t-1}, \dots, y_{t-k})$$

does not depend on  $t$ .

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## Weak stationarity (key concept)

A process is **weakly stationary** or **covariance stationary** if its mean, variance and autocovariances do not change over time. That is,

$$E(Y_t) = \mu,$$

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$$\text{Var}(Y_t) = \sigma^2,$$

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$$\text{Cov}(Y_t, Y_{t-k}) = \text{Cov}(Y_t, Y_{t-k}) = \gamma_k,$$

for all  $t$  and  $k$ .

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- Introduced in the seminal book "Time Series Analysis: Forecasting and Control" (1970) by Box and Jenkins.

- The Box-Jenkins approach relies on (a) finding a stationary transformation of the data (b) modeling the autocorrelations in the transformed data.

- This approach contrast with exponential smoothing, where we explicitly model the different time series components through additive or multiplicative specifications.



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- We consider log or Box-Cox transformations to stabilise the variance of series.

- Differencing (next section) leads to stationarity in the mean by removing changes in the level of the series (due for example to trend and seasonality).

- Autocorrelation (ACF) and partial autocorrelation (PACF) plots help us to assess stationarity and to identify suitable specification for the stationary transformation of the series.

## Partial autocorrelation function (PACF)

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- The partial autocorrelation of order  $k$  (labelled  $\rho_{kk}$ ) is the correlation between  $Y_t$  and  $Y_{t-k}$  net of effects at times  $t-1, t-2, \dots, t-k+1$ .

- $r_{kk}$  estimates  $\rho_{kk}$ .

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$$Y_t = \rho_{10} + \rho_{11}Y_{t-1} + a_t$$
$$Y_t = \rho_{20} + \rho_{21}Y_{t-1} + \rho_{22}Y_{t-2} + a_t$$

$$Y_t = \rho_{k0} + \rho_{k1}Y_{t-1} + \rho_{k2}Y_{t-2} + \dots + \rho_{kk}Y_{t-k} + a_t$$

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**Differencing**  
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## Differencing (key concept)

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Box and Jenkins advocate difference transforms to achieve stationarity. The first difference of a time series is

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$$\Delta Y_t = Y_t - Y_{t-1}$$

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## Example: random walk

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In the random walk model

$Y_t = Y_{t-1} + \varepsilon_t$   
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the first difference leads to stationary white noise series

$\Delta Y_t = Y_t - Y_{t-1} = \varepsilon_t$   
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## Second order differencing

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In rare cases, it may be necessary to difference the series a second time to obtain stationarity:

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$$\Delta^2 Y_t = (Y_t - Y_{t-1}) - (Y_{t-1} - Y_{t-2}) = Y_t - 2Y_{t-1} + Y_{t-2}$$

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## Differencing

The ACF helps us to determine whether the time series needs differencing (or further differencing).

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- The ACF of a non-stationary series will decrease slowly.

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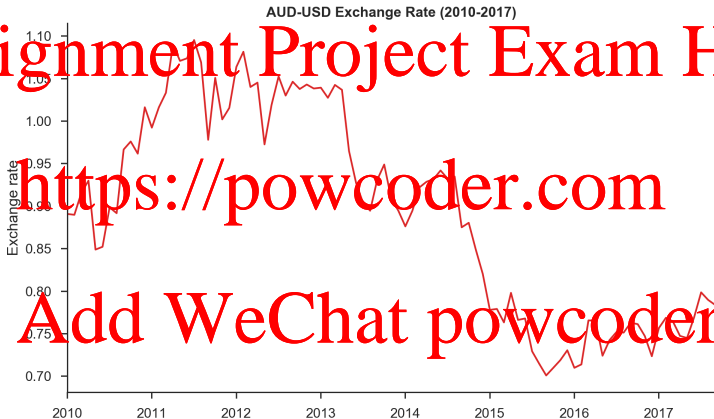
- The ACF of a stationary series should drop to zero relatively quickly.

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**Unit root tests** are also common for determining the need for differencing, but sensitive to assumptions. When in doubt, use model selection for model selection, not hypothesis testing.



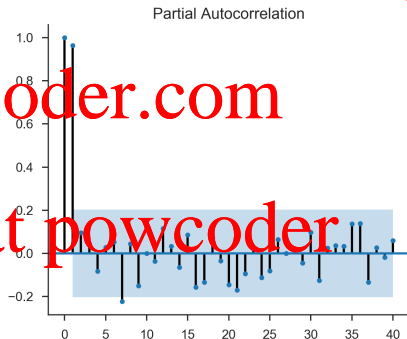
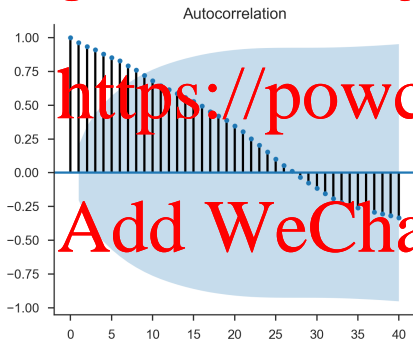
## Example: AUD/USD exchange rate



## Example: AUD/USD exchange rate

ACF and PACF for the time series

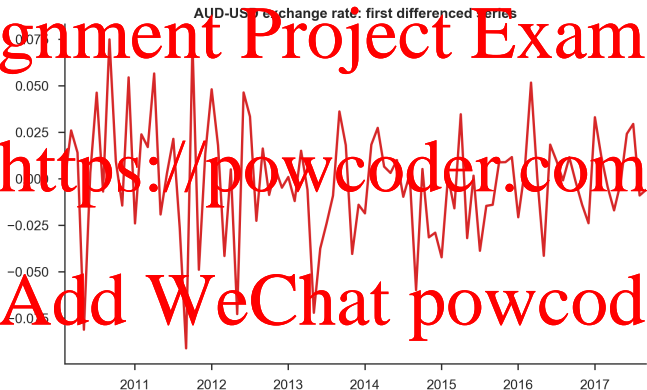
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## Example: AUD/USD exchange rate

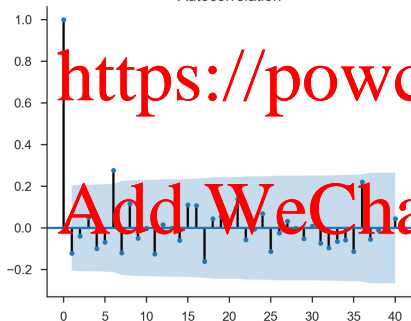


## Example: AUD/USD exchange rate

ACF and PACF for the first differenced series

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Autocorrelation



Partial Autocorrelation



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We can use seasonal differencing to address non-stationarity caused by seasonality:

$$\Delta_m Y_t = Y_t - Y_{t-m}$$

where  $m$  is the number of seasons.

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The ACF of a series that needs seasonal differencing will decrease slowly at the seasonal lags  $m$ ,  $2m$ ,  $3m$ , etc.

## First and seasonal differencing

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Time series that have a changing level and a seasonal pattern may require both first and seasonal differencing for stationarity.

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The first and seasonally differenced series is

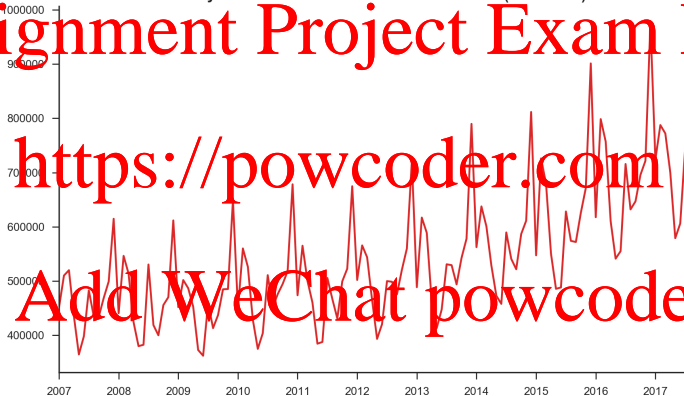
$$\Delta_m(\Delta Y_t) = (Y_t - Y_{t-1}) - (Y_{t-m} - Y_{t-m-1}),$$

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noting that the order of differencing does not matter.

## Example: Visitor Arrivals in Australia

Monthly Short Term Visitor Arrivals in Australia (2007-2017)



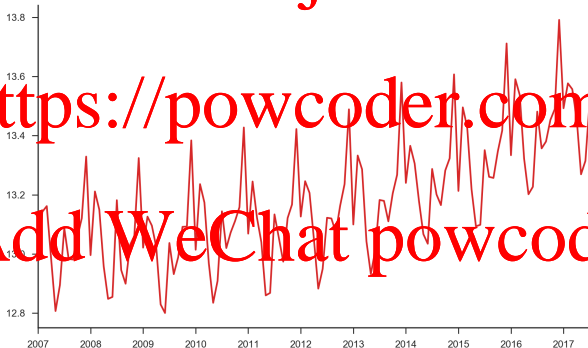
## Example: Visitor Arrivals in Australia

Log transformation

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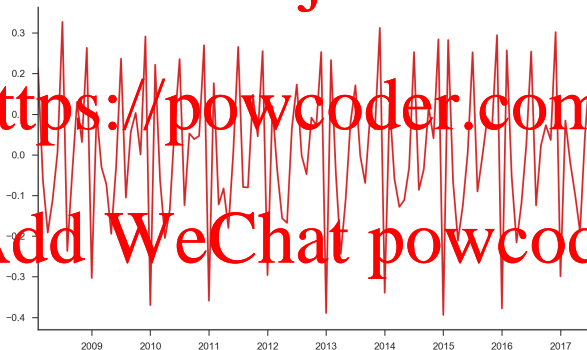
## Example: Visitor Arrivals in Australia

First differenced log series

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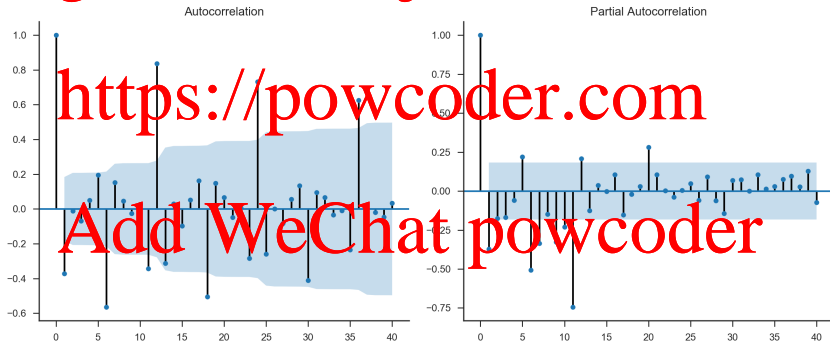
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## Example: Visitor Arrivals in Australia

ACF and PACF for the first differenced log series

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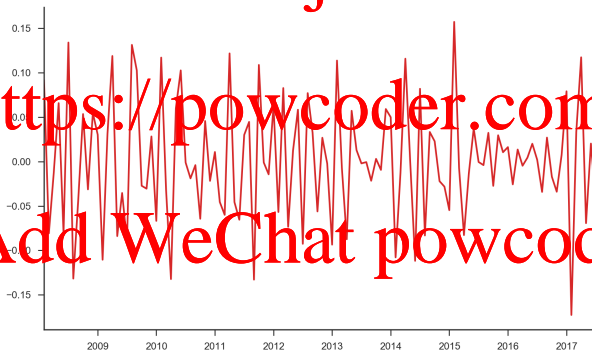
## Example: Visitor Arrivals in Australia

First and seasonally differenced series

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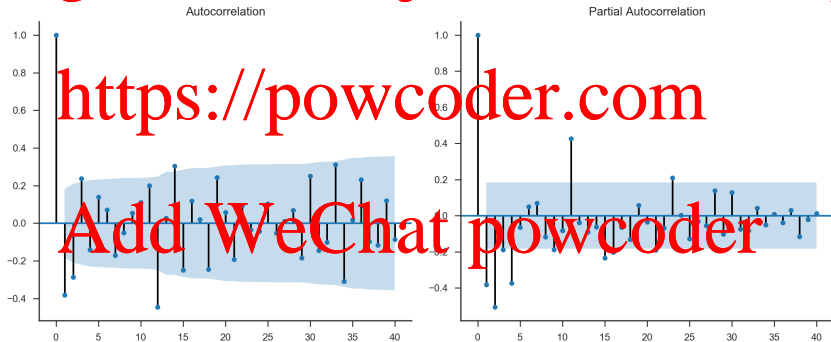
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## Example: Visitor Arrivals in Australia

ACF and PACF for the first and seasonally differenced log series

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## Backshift notation

The **backshift operator** is a useful notational device for ARIMA models.

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$$BY_t = Y_{t-1}$$

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We can manipulate the backshift operator with standard algebra, for example

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Therefore,

$$B^k Y_t = Y_{t-k}.$$

## Differencing in backshift notation

First differenced series:

$$(1 - B)Y_t = Y_t - BY_t = Y_t - Y_{t-1}$$

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Seasonally differenced series:

$$(1 - B^m)Y_t = Y_t - B^m Y_t = Y_t - Y_{t-m}$$

First and seasonally differenced series:

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$$\begin{aligned}(1 - B)(1 - B^m)Y_t &= (1 - B - B^m + B^{m+1}) \\ &= (Y_t - Y_{t-1}) - (Y_{t-m} - Y_{t-m-1})\end{aligned}$$

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~~Models for stationary series~~  
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## Autoregressive (AR) model (key concept)

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The **autoregressive model** of order  $p$ , or **AR( $p$ )** model, is

$$Y_t = c + \phi_1 Y_{t-1} + \phi_2 Y_{t-2} + \dots + \phi_p Y_{t-p} + \varepsilon_t,$$

where  $\varepsilon_t$  is a white noise series.

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## Example: AR(1) model

AR(1) model:

$$Y_t = c + \phi_1 Y_{t-1} + \varepsilon_t,$$

where  $\varepsilon_t$  is i.i.d. with mean zero and variance  $\sigma^2$ .

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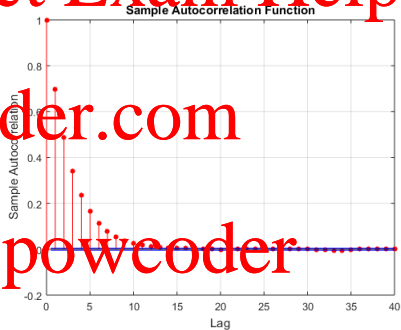
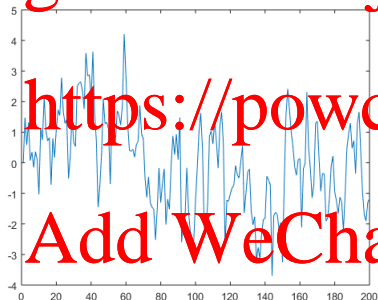
$$E(Y_t|y_1, \dots, y_{t-1}) = E(Y_t|y_{t-1}) = c + \phi_1 y_{t-1}.$$

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$$\text{Var}(Y_t|y_1, \dots, y_{t-1}) = \text{Var}(Y_t|y_{t-1}) = \sigma^2.$$

AR(1) illustration:  $\phi = 0.7$

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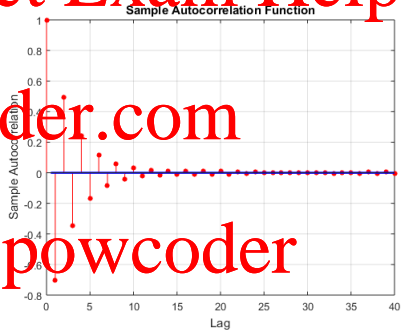
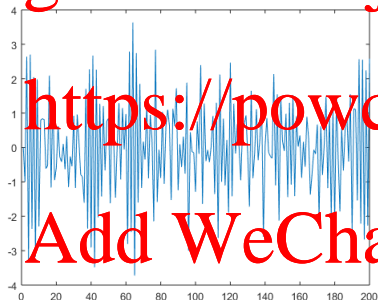


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AR(1) illustration:  $\phi = -0.7$

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## AR model: ACF and PACF identification (key concept)

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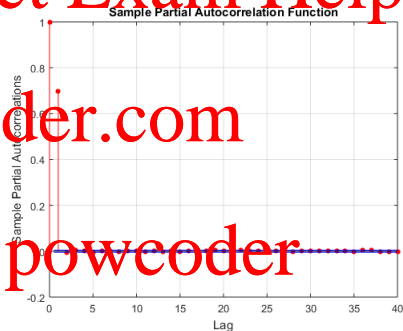
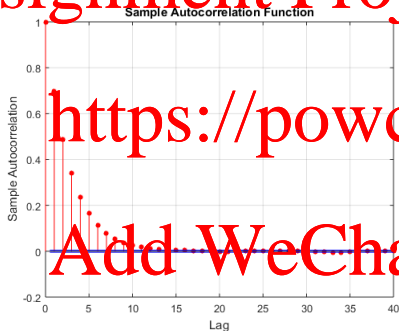
For an AR( $p$ ) process, we can show that:

- The theoretical autocorrelations  $\rho_k$  decrease exponentially.
- The theoretical partial autocorrelation  $\rho_{kk}$  cuts off to zero after lag  $p$ .

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- The  $p$ th partial autocorrelation  $\rho_{pp}$  is  $\phi_p$ .

## AR(1) with $\phi = 0.7$ : ACF (left) and Partial ACF (right)



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From the linearity of expectations,

$$E(Y_{t+h}|y_{1:t}) = c + \phi_1 E(Y_{t+h-1}|y_{1:t}) + \dots + \phi_p E(Y_{t+h-p}|y_{1:t}),$$

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where

$$E(Y_{t+h-i}|y_{1:t}) = \begin{cases} \hat{y}_{t+h-i} & \text{if } h > i \\ y_{t+h-i} & \text{if } h \leq i. \end{cases}$$

## Example: AR(1) model

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$$Y_t = c + \phi_1 Y_{t-1} + \varepsilon_t$$

For  $t + 1$ ,

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$$\hat{y}_{t+1} = E(Y_{t+1}|y_{1:t})$$

$$= E(c + \phi_1 Y_t + \varepsilon_{t+1}|y_{1:t}) = c + \phi_1 y_t$$

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$$\text{Var}(Y_{t+1}|y_{1:t}) = \sigma^2.$$

## Example: AR(1) model

For  $t + 2$ ,

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$$\hat{y}_{t+2} = c + \phi_1 \hat{y}_{t+1}$$

$$= c(1 + \phi_1) + \phi_1^2 y_t.$$

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$$\text{Var}(Y_{t+2}|y_{1:t}) = \text{Var}(\phi_1 Y_{t+1} + \varepsilon_{t+2}|y_{1:t})$$

$$= \phi_1^2 \text{Var}(Y_{t+1}|y_{1:t}) + \sigma^2$$

$$= (1 + \phi_1^2)\sigma^2$$



## Example: AR(1) model

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$$\begin{aligned}\hat{y}_{t+h} &= c + \phi_1 y_{t+h-1} \\ &= c(1 + \phi_1 + \phi_1^2 + \dots + \phi_1^{h-1}) + \phi_1^h y_t\end{aligned}$$

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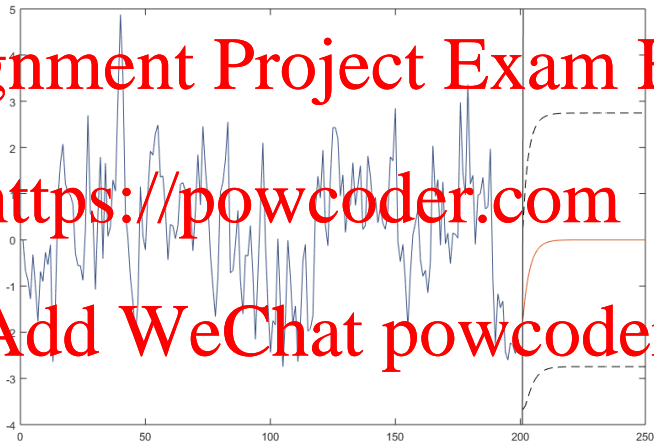
$$\text{Var}(Y_{t+h}|y_{1:t}) = \phi_1^2 \text{Var}(Y_{t+h-1}|y_{1:t}) + \sigma^2$$

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$$= \sigma^2(1 + \phi_1^2 + \dots + \phi_1^{2(h-1)})$$

As  $h$  gets larger, both the point forecast and the conditional variance converge exponentially to a constant.

## Illustration: AR(1) forecast



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## Stationarity conditions

AR( $p$ ) model:

$$Y_t = c + \phi_1 Y_{t-1} + \phi_2 Y_{t-2} + \dots + \phi_p Y_{t-p} + \epsilon_t$$

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We need to impose restrictions on the AR coefficients such that the model is stationary

$$\text{AR}(1): -1 < \phi_1 < 1.$$

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$$\text{AR}(2): -1 < \phi_2 < 1, \phi_1 + \phi_2 < 1, \phi_2 - \phi_1 < 1.$$

AR( $p$ ) with  $p > 2$ : more technical.

## Moving average (MA) model (key concept)

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The **moving average** model of order  $q$ , or **MA**( $q$ ) model, is

$$Y_t = c + \varepsilon_t + \theta_1 \varepsilon_{t-1} + \theta_2 \varepsilon_{t-2} + \dots + \theta_q \varepsilon_{t-q},$$

where  $\varepsilon_t$  is a white noise series.

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## Example: MA(1) process

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$$Y_t = c + \varepsilon_t + \theta_1 \varepsilon_{t-1}.$$

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$$E(Y_t | y_{t-1}) = c + \theta_1 \varepsilon_{t-1}$$

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$$\text{Var}(Y_t | y_{t-1}) = \sigma^2$$

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For an  $MA(q)$  process, we can show that:

- The theoretical autocorrelation  $\rho_k$  cuts off after lag  $q$ .
- The theoretical partial autocorrelations  $\rho_{kk}$  decrease exponentially.

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- An  $MA(q)$  process is **invertible** when we can write it as a linear combination of its past values (an  $AR(\infty)$  process) plus the contemporaneous error term.

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- Estimation and forecasting methods for MA models rely on invertibility. We therefore impose restrictions on the MA coefficients such that invertibility holds.

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## ARMA( $p, q$ ) model (key concept)

The **ARMA**( $p, q$ ) model is

$$Y_t = c + \phi_1 Y_{t-1} + \dots + \phi_p Y_{t-p} + \theta_1 \varepsilon_{t-1} + \dots + \theta_q \varepsilon_{t-q} + \varepsilon_t$$

where  $\varepsilon_t$  is a white noise series

In backshift notation, <https://powcoder.com>

$$\left(1 - \sum_{i=1}^p \phi_i B^i\right) Y_t = c + \left(1 + \sum_{i=1}^q \theta_i B^i\right) \varepsilon_t.$$

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The autocorrelations and partial autocorrelations decrease exponentially for ARMA processes.



Example: ARMA(1, 1)

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The ARMA(1,1) model is

$$Y_t = c + \phi_1 Y_{t-1} + \theta_1 \varepsilon_{t-1} + \varepsilon_t.$$

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In backshift notation,

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$$(1 - \phi_1 B)Y_t = c + (1 - \theta_1 B)\varepsilon_t.$$

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ARIMA models  
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## ARIMA( $p,d,q$ ) model (key concept)

The ARIMA( $p,d,q$ ) model is

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$$\left(1 - \sum_{i=1}^p \phi_i B^i\right) (1 - B)^d Y_t = c + \left(1 + \sum_{i=1}^q \theta_i B^i\right) \varepsilon_t,$$

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$p$  : autoregressive order.

$d$  : degree of first differencing (nearly always  $d = 0$  or  $d = 1$ ).

$q$  : moving average order.

## ARIMA( $p, d, q$ ) model

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ARIMA( $p, d, q$ ) model:

$$\underbrace{\left(1 - \sum_{i=1}^p \phi_i B^i\right)}_{\text{AR } (p) \text{ component}} \underbrace{(1 - B)^d}_{\text{Differencing}} Y_t = c + \underbrace{\left(1 + \sum_{i=1}^q \theta_i B^i\right)}_{\text{MA } (q) \text{ component}} \varepsilon_t.$$

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The ARIMA( $p, d, q$ ) model specifies a stationary ARMA( $p, q$ ) model for the differenced series.

## Example: ARIMA(0,1,1) model

The ARIMA(0,1,1) model is an MA(1) model for the first differenced series,

$$Y_t - Y_{t-1} = \varepsilon_t + \theta_1 \varepsilon_{t-1}.$$

In backshift notation,

$$(1 - B)Y_t = (1 + \theta_1 B)\varepsilon_t.$$

With an intercept:

$$Y_t - Y_{t-1} = c + \varepsilon_t + \theta_1 \varepsilon_{t-1}$$

## ARIMA(0,1,1): relation to exponential smoothing

$$\text{ARIMA}(0,1,1): Y_t = Y_{t-1} + \varepsilon_t + \theta_1 \varepsilon_{t-1}$$

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$$E(Y_t | y_{1:t-1}) = y_{t-1} + \theta_1 \varepsilon_{t-1}$$

$$\begin{aligned} &= y_{t-1} + \theta_1 (y_{t-1} - y_{t-2} - \theta_1 \varepsilon_{t-2}) \\ &= (1 + \theta_1) y_{t-1} - \theta_1 (y_{t-2} + \theta_1 \varepsilon_{t-2}) \end{aligned}$$

Now, label  $\ell_{t-1} = y_{t-1} + \theta_1 \varepsilon_{t-1}$  and  $\alpha = (1 + \theta_1)$ . We get:

$$\ell_{t-1} = \alpha y_{t-1} + (1 - \alpha) \ell_{t-2}$$

The simple exponential smoothing model.

## Intercept in a first differenced series

The inclusion of an intercept induces a linear trend in an  $\text{ARIMA}(p,1,q)$  model.

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For example, in the **random walk plus drift** model

$$Y_t = c + Y_{t-1} + \varepsilon_t,$$

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we can derive

$$Y_{t+h} = Y_t + \sum_{i=1}^h (c + \varepsilon_{t+i}),$$

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$$\hat{y}_{t+h} = y_t + c \times h,$$

$$\text{Var}(Y_{t+h}|y_{1:t}) = h\sigma^2.$$

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- Estimation: maximum likelihood.
- Order selection ( $p, q$ ): visual identification, AIC, and model validation.
- Intercept terms induce permanent trends. Use model selection.

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Seasonal ARIMA models  
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## Seasonal ARIMA: ACF and PACF identification (key concept)

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We refer to a seasonal ARIMA model as

$$\text{ARIMA } \underbrace{(p, d, q)}_{\text{Non-seasonal}} \underbrace{(P, D, Q)}_{\text{Seasonal}}_m$$

where  $D$  is the order of seasonal differencing,  $P$  and  $Q$  are the orders of the seasonal AR and MA components, and  $m$  is the number of seasons.

## Seasonal ARIMA: ACF and PACF identification (key concept)

ARIMA(0,0,0)(P,0,0)

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- Sample autocorrelations decrease exponentially for lags  $m$ ,  $2m$ ,  $3m$ , etc.
- Sample partial autocorrelations cuts off at lag  $Pm$ .

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ARIMA(0,0,0)(0,0,Q)

- Sample autocorrelations cuts off at lag  $Qm$ .
- Sample partial autocorrelations decrease exponentially for lags  $m$ ,  $2m$ ,  $3m$ , etc.

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Seasonal AR(1) or ARIMA(0,0,0)(1,1,0)<sub>12</sub>:

$$Y_t - Y_{t-12} = c + \phi_1(Y_{t-12} - Y_{t-24}) + \varepsilon_t$$

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Seasonal MA(1) or ARIMA(0,0,0)(0,1,1)<sub>12</sub>:

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$$Y_t - Y_{t-12} = c + \theta_1 \varepsilon_{t-12} + \varepsilon_t$$

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ARIMA(1,0,0)(0,1,1)<sub>12</sub> model:

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$$(1 - \phi_1 B)(1 - B^{12})Y_t = c + (1 + \theta_1 B^{12})\varepsilon_t$$

$$Y_t - Y_{t-12} = c + \phi_1(Y_{t-1} - Y_{t-13}) + \varepsilon_t + \theta_1\varepsilon_{t-12}$$

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## Seasonal ARIMA models

ARIMA(1,1,1)(1,1,0)<sub>12</sub> model:

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$$(1 - \phi_1 B)(1 - \phi_2 B^{12})(1 - B)(1 - B^{12})Y_t = c + (1 + \theta_1 B)\varepsilon_t$$

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$$\begin{aligned}(Y_t - Y_{t-1}) - (Y_{t-12} - Y_{t-13}) &= c + \phi_1 [(Y_{t-1} - Y_{t-2}) - (Y_{t-13} - Y_{t-14})] \\ &+ \phi_2 [(Y_{t-12} - Y_{t-13}) - (Y_{t-24} - Y_{t-25})] \\ &+ \phi_1 \phi_2 [(Y_{t-13} - Y_{t-14}) - (Y_{t-25} - Y_{t-26})] \\ &+ \varepsilon_t + \theta_1 \varepsilon_{t-1}\end{aligned}$$

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- Estimation: maximum likelihood.

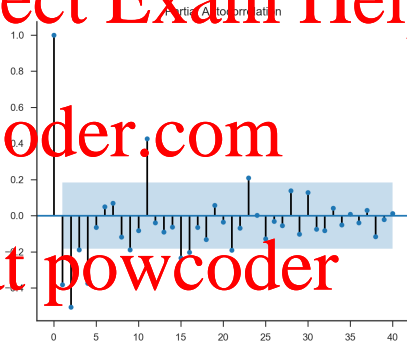
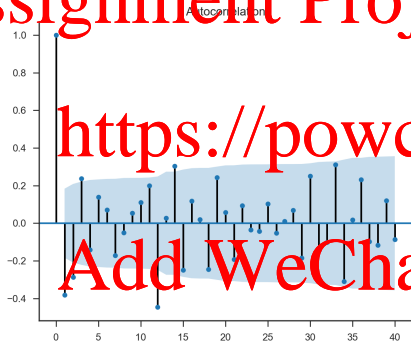
- Order selection ( $p, q, P, Q$ ): visual identification, AIC, and model validation.

- Usually only one seasonal AR or MA term is needed.

## Example: Visitor Arrivals in Australia

Recall that we obtained the following ACF and PACF plots the first and seasonally differenced log series:

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We select an  $\text{ARIMA}(3,1,0)(0,1,1)_{12}$  specification based on the AIC.



## Example: Visitor Arrivals in Australia

### Statespace Model Results

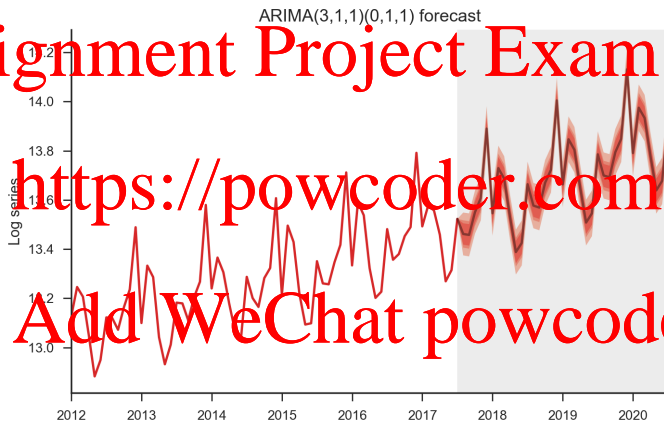
```
=====
Dep. Variable:                Arrivals    No. Observations:           127
Model:                SARIMAX(3, 1, 1)x(0, 1, 1, 12)    Log Likelihood           212.670
Date:                AIC                -411.39
Time:                BIC                -391.33
Sample:                01-31-2007    HQIC                -403.250
                    - 07-31-2017
```

Covariance Type: opg

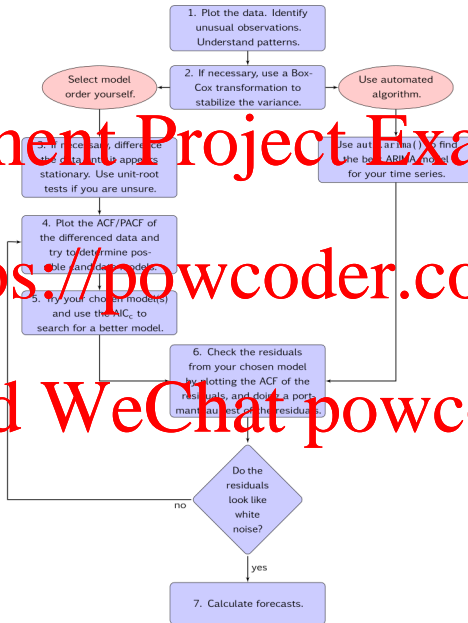
```
=====
              coef      std err          z      P>|z|      [0.025      0.975]
-----
intercept      0.0007      0.000      2.957      0.003      -0.000      0.001
ar.L1           0.0532      0.118      0.450      0.652      -0.178      0.285
ar.L2          -0.0454      0.112     -0.403      0.687      -0.266      0.175
ar.L3           0.2426      0.112      2.166      0.030      0.023      0.462
ma.L1          -0.9726      0.166     -5.873      0.000     -1.297     -0.648
ma.S.L1         -1.9976      0.773     -2.583      0.089     -3.522     -0.474
sigma2          0.0010      0.000      0.125      0.899     -0.013      0.014
=====
```

```
=====
Ljung-Box (Q):                65.43    Jarque-Bera (JB):                0.72
Prob(Q):                      0.01     Prob(JB):                0.70
Heteroskedasticity (H):        0.49     Skew:                    0.10
Prob(H) (two-sided):          0.03     Kurtosis:                2.66
=====
```

## Example: Visitor Arrivals in Australia



## Summary of modelling process (FPP)



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## Review questions

- What is stationarity and why is it a fundamental concept in ARIMA modelling?

- What transformation do we apply to a time series to make it stationary?

- How do we identify AR vs MA processes from ACF and PACF plots?

- What is an ARIMA model?

- Write the equation for a seasonal ARIMA model using backshift notation.

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