Vectors

Chapter 2

Stats 20: Introduction to Statistical Programming with R

UCLA

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Learning Objectives

After studying this chapter, you should be able to:

- Create vectors with the c() function.
- Understand the distinction between numeric, character, and logical vectors.
- Extract values from a vector using subsetting.
- Compute vector arithmetic in R.
- Understand how R uses recycling in vector operations.
- Understand how R uses vectorization.
- Understand that R approximates numbers to identify and be aware of rounding errors. POWCOGEL.COM

1 The Essentials

1.1 Basic De Airigis gnment Project Exam Help

The most fundamental object in R is a **vector**, which is an ordered collection of values. The entries of a vector are also called *elements* or *components*. Single values (or **scalars**) are actually just vectors with a single element.

The possible values cortained in the total can be of sovered esse decayped, as known as (storage) modes: numeric, character, or logical.

- Numeric values are numbers (decimals).
- Character values at the string Or Wife Corts for Cubbs Character values are always contained in quotation marks "".
- Logical values are either TRUE or FALSE (must be in all caps), representing true and false values in formal logical statements of Walter to the contract of the contract of

Note: The (capital) letters T and F are technically valid shorthand for TRUE and FALSE, respectively, but you should *never* use them.

The c() function is used to collect values into a vector. The c stands for concatenate or combine. Here are a few examples:

```
c(1, 1, 2, 3, 5, 8, 13) # This is a numeric vector

[1] 1 1 2 3 5 8 13

fib <- c(1, 1, 2, 3, 5, 8, 13) # Assign the vector to a named object
fib

[1] 1 1 2 3 5 8 13

parks <- c("Leslie", "April", "Ron", "Tom", "Donna", "Jerry") # This is a character vector
parks

[1] "Leslie" "April" "Ron" "Tom" "Donna" "Jerry"

true_dat <- c(TRUE, FALSE, TRUE, T, F) # This is a logical vector
true_dat</pre>
```

[1] TRUE FALSE TRUE TRUE FALSE

The c() function can also concatenate vectors together by inputting vectors instead of single values.

```
c(c(1, 2), c(3, 4, 5)) # Can concatenate multiple vectors together
```

[1] 1 2 3 4 5

1.2 The Length of a Vector

The **length** of a vector is the number of elements in the vector. The **length()** function inputs a vector and outputs the length of the vector.

```
length(4) # A scalar/number is a vector of length 1
```

[1] 1

length(fib)

[1] 7

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length(parks)

[1] 6 Assignment Project Exam Help

[1] 5

1.3 The Assignment We Glat Exmontelp

In the examples above, we have created separate numeric, character, and logical vectors, where all the values in each vector are of the same type. A patural question is whether we can create a vector with mixed types.

It turns out that the answer is no. Due thow R (internally) stores vectors, every value in a vector must have the same type.

mode(fib)

[1] "numeric"

mode(parks)

[1] "character"

mode(true_dat)

[1] "logical"

When values of different types are concatenated into a single vector, the values are **coerced** into a single type.

Question: What is the output for the following commands?

- mode(c(fib, parks))
- mode(c(fib, true_dat))
- mode(c(parks, true_dat))
- mode(c(fib, parks, true dat))

These questions highlight the mode hierarchy:

logical < numeric < character

That is:

- Combining logical and numeric vectors will result in a numeric vector.
- Combining numeric and character vectors will result in a character vector.
- Combining logical and character vectors will result in a character vector.
- Combining logical, numeric, and character vectors will result in a character vector.

Note: When logical values are coerced into numeric values, TRUE becomes 1 and FALSE becomes 0.

The reason why knowing the types of our R objects is important is because we want to apply functions to the objects in order to describe it is or do a all short the classical fields of do a large the control of the c

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2 Sequences and Acquite Pour Example 1

R has some handy built-in functions for creating vectors of sequential or repeated values. One common use of sequences in statistics is to generate the category labels (or levels) for a designed experiment.

2.1 The seq() Fulltys://powcoder.com

The seq() function creates a sequence of evenly spaced numbers with specified start and end values. The start and end values determine whether the sequence is increasing or decreasing. The first argument is the from or starting value, and the concave ment is the form of the by the by default, the optional argument by is set to by = 1, which means the numbers in the sequence are incrementally increased by 1.

```
seq(0, 5) # numbers increase by 1
```

[1] 0 1 2 3 4 5

```
seq(0, 10, by = 2) # numbers now increase by 2
```

```
[1] 0 2 4 6 8 10
```

The seq() function can make decreasing sequences by specifying the from argument to be greater than the to argument. By default, the by argument will automatically change to by = -1.

```
seq(5, 0) # seq() can also make decreasing sequences
```

[1] 5 4 3 2 1 0

```
seq(10, 0, by = -3) # numbers now decrease by 3
```

```
[1] 10 7 4 1
```

Notice that seq(10, 0, by = -3) stops at the smallest number in the sequence greater than the to argument.

To obtain a sequence of numbers of a given length, use the optional length (or length.out) argument. The incremental increase (or decrease) will be calculated automatically.

```
seq(0, 1, length = 11)
```

```
[1] 0.0 0.1 0.2 0.3 0.4 0.5 0.6 0.7 0.8 0.9 1.0
```

We could also specify the increment and length instead of providing the end value.

```
seq(10, 55, length = 10)
```

```
[1] 10 15 20 25 30 35 40 45 50 55
```

```
seq(10, by = 5, length = 10) # The same sequence
```

[1] 10 15 20 25 30 35 40 45 50 55

2.1.1 Shorthands for Common Sequences

2.1.1.1 The Colon: Operator

The colon: operator is a shorthand for the default peq() with unit increment (i.e., by =1 or -1).

-2:5 # same as seq. S. SI gnment Project Exam Help

```
[1] -2 -1 0 1 2 3 4 5
```

```
Assignment/Peolet ExmoPelp
```

[1] 3.141593 4.141593 5.141593 6.141593 7.141593 8.141593 9.141593

Caution: The colon: operator takes precedence over multiplication and subtraction in the order of operations, but it does not take precedence over exponents. It is always recommended to use parentheses to make the order of operations explicit!

```
n <- 5
1:n - 1
```

[1] 0 1 2 3 4 Add WeChat powcoder

1:(n - 1)

[1] 1 2 3 4

2.1.1.2 The seq_len() Function

The seq_len() function inputs a single length.out argument and generates the sequence of integers 1, 2, ..., length.out unless length.out = 0, when it generates integer(0).

```
seq_len(8)
```

```
[1] 1 2 3 4 5 6 7 8
```

```
seq_len(10)
```

[1] 1 2 3 4 5 6 7 8 9 10

```
seq_len(0)
```

integer(0)

Notice that the output of 1:n and $seq_len(length.out = n)$ are the same for positive integers n. However, if n = 0, then $seq_len(n)$ will generate integer(0), whereas 1:n will produce the vector 1, 0, which is often not the intended behavior when using the 1:n notation (especially when used inside of functions). In addition, $seq_len()$ does not allow for negative inputs.

```
seq_len(-5)
```

Error in seq_len(-5): argument must be coercible to non-negative integer

Using seq_len(n) rather than the shorter 1:n helps prevent unexpected results if n is incorrectly specified. When creating an integer sequence of possibly variable length, the seq_len() notation is recommended best practice over the colon operator :.

2.1.1.3 The seq_along() Function

The **seq_along()** function inputs a single **along.with** argument and generates the sequence of integers 1, 2, ..., length(along.with).

seq_along(100)

https://powcoder.com

[1] 1

seq_along(c(1, 3, 5, 7, 9))

[1] 1 2 3 4 5 Assignment Project Exam Help seq_along(c("friends", "warfles", "work"))

[1] 1 2 3

The seq_alors Succion factor for the sequence of the sequence

2.2 The rep() Function

The rep() function creates a vector of repeated values. The first argument, generically called x, is the vector of values we want to repeat. The second argument is the times argument that specifies how many times we want to repeat the values in the x vector.

The times argument care (a fingle value tepest) Ad who cover of the values (repeats each individual value separately). If the length of the times vector is greater than 1, the vector needs to have the same length as the x vector. Each element of times corresponds to the number of times to repeat the corresponding element in x.

```
rep(3, 10) # Repeat the value 3, 10 times
```

```
[1] 3 3 3 3 3 3 3 3 3 3
```

rep(c(1, 2), 5) # Repeat the vector c(1,2), 5 times

```
[1] 1 2 1 2 1 2 1 2 1 2 1 2
```

rep(c(1, 2), c(4, 3)) # Repeat the value 1, 4 times, and the value 2, 3 times

[1] 1 1 1 1 2 2 2

```
rep(c(5, 3, 1), c(1, 3, 5)) # Repeat c(5,3,1), c(1,3,5) times
```

[1] 5 3 3 3 1 1 1 1 1

Question: How is rep(c(1, 2), 5) different from rep(c(1, 2), c(5, 5))?

Question: Why does rep(c(5, 3, 1), c(1, 3)) give an error?

We can also combine seq() and rep() to construct more interesting patterns.

```
rep(seq(2, 20, by = 2), 2)
```

[1] 2 4 6 8 10 12 14 16 18 20 2 4 6 8 10 12 14 16 18 20 rep(seq(2, 20, by = 2), rep(2, 10))

```
[1] 2 2 4 4 6 6 8 8 10 10 12 12 14 14 16 16 18 18 20 20
```

Note: The rep() function works with vectors of any mode, including character and logical vectors. This is particularly useful for creating vectors that represents categorical variables.

```
rep(c("long", "short"), c(2, 3))
```

[1] TRUE TRUE TRUE TRUE TRUE TRUE FALSE FALSE FALSE

3 Extracting and Assigning Vector Elements Help

3.1 Subsetting

Square brackets as Saldtole trackets in parts to be a subsetting. We input the index of the element(s) we want to extract.

To illustrate subsetting, we will consider the following example.

To keep his body in (literal tipe of the shape of the last ten days are:

51, 40, 57, 34, 47, 50, 50, 56, 41, 38

We first input the data in the rest very accessive tasther the transfer of the rest input the data in the rest of the rest input the data in the rest input the rest input the data in the rest input the rest input

```
# Input the data into R

running_times <- c(51, 40, 57, 34, 47, 50, 50, 56, 41, 38)

# Print the values

running_times
```

[1] 51 40 57 34 47 50 50 56 41 38

3.1.1 Positive Indices

Recall that the [1] in front of the output is an index, telling us that 51 is the first element of the vector running_times. By counting across the vector, we can see, for example, that the 5th element of running_times is 47. More efficiently, we can extract just the 5th element by typing running_times[5].

```
running_times[5] # Extract the 5th element
```

[1] 47

To extract multiple values at once, we can input a vector of indices:

```
running_times[c(3, 7)] # Extract the 3rd and 7th elements
```

[1] 57 50

```
running_times[4:8] # Extract the 4th through 8th elements
```

[1] 34 47 50 50 56

Reordering the indices will reorder the elements in the vector:

```
running_times[8:4] # Return the 4th through 8th elements in reverse order
```

[1] 56 50 50 47 34

3.1.2 Negative Indices

Negative indices allow us to avoid certain elements, extracting all elements in the vector except the ones with negative indices.

running_times[-4] # Return all elements except the 4th one

[1] 51 40 57 47 50 50 56 41 38

running_times[-c(1, 5)] # https://powcoder.com

[1] 40 57 34 50 50 56 41 38

running_times[-(1:4)] # Return all elements except the first four

[1] 47 50 50 56 Assignment Project Exam Help

Note: Notice that -(1:4) is not the same as -1:4.

Using a zero index returns nothing. Alzen when it not commonly used, but it can be useful to know for more complicated expression that the property of the pro

index_vector <- 0:5 # Create a vector of indices
running_times[index_vector] # Extract the values corresponding to the index.vector</pre>

[1] 51 40 57 34 47 https://powcoder.com

Caution: Do not mix positive and negative indices.

running_times[c(-1, 3)]

Add We Chat powcoder subscripts

The issue with indices of mixed signs is that R does not know the order in which the subsetting should occur: Do we want to return the third element before or after removing the first one?

Question: How could we code returning the third element of running_times after removing the first one?

3.1.3 Fractional Indices

Always use integer valued indices. Fractional indices will be truncated towards 0.

```
running_times[1.9] # Returns the 1st element (1.9 truncated to 1)
```

[1] 51

```
running_times[-1.9] # Returns everything except the 1st element (-1.9 truncated to -1)
```

[1] 40 57 34 47 50 50 56 41 38

```
running_times[0.5] # Returns an empty vector (0.5 truncated to 0)
```

numeric(0)

Note: The output numeric(0) is a numeric vector of length zero.

3.1.4 Blank Indices

Subsetting with a blank index will return everything.

running_times

[1] 51 40 57 34 47 50 50 56 41 38

running_times[] # Same output

[1] 51 40 57 34 47 50 50 56 41 38

Blank indices will be important later (when we have ordered indices).

3.2 Assigning Values to an Existing Vector

Suppose Chris Traeger made Inista S recor in Division Control of the ran 10k in 43 minutes, not 34 minutes. Rather than reentering all of his running times, how can we modify the existing running times vector?

R allows us to assign new values to existing rectors by again using the essignment operator to Pather than specifying a new object name on the left of the assignment, we can put the element or elements in the named vector that we want to change.

```
# Display Chris Traeger's running times
running_tim CC101
                      at Megbet Exmandelp
```

[1] 51 40 57 34 47 50 50 56 41 38

Assign 43 to the 4th element of the running_times vector running_times[4] <- 13ttps://proawbcoder.com running_times

[1] 51 40 57 43 47 50 50 56141 38 eChat powcoder.

If Chris found that the fast two values were also incorrect we can reassign multiple values at once using

vector indices.

```
# Assign 42 to the 9th element and 37 to the 10th element
running times [9:10] < c(42, 37)
# Verify that the running_times vector has been updated
running times
```

[1] 51 40 57 43 47 50 50 56 42 37

Note: The original value of 34 in the running_times vector has been overwritten, so reassigning values to an existing object is irreversible. Depending on the situation, it might be beneficial to first make a copy of the original data as a separate object before making changes This ensures that the original data is still retrievable if there is a mistake in the modifications.

Caution: You cannot use this syntax to create a new object. For example, the following code will not work: $bad[1:2] \leftarrow c(4, 8)$

```
Error in bad[1:2] <- c(4, 8): object 'bad' not found
```

The reason why this gives an error is that extracting or assigning individual vector elements using square brackets is actually done through functions (remember: everything is a function call). R cannot apply the extract/assign function to a vector that does not exist. The vector needs to be created first.

The following code fixes the issue:

```
good <- numeric(2) # Create an empty vector of length 2</pre>
good[1:2] \leftarrow c(4, 8)
good
```

[1] 4 8

Note: The numeric(), character(), and logical() functions can create empty vectors of a specified length for their respective modes. The default elements will all be 0, "", and FALSE, respectively.

```
numeric(3) # Create a numeric vector of length 3
```

[1] 0 0 0

```
character(5) # Create a haracter vector of length 5 der.com
```

[1] "" "" "" ""

```
logical(4) # Create a logical vector of length 4
```

[1] FALSE FA

Creating empty or blank vectors will be important when working with for and while loops.

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Arithmetic can be done on numeric vectors using the usual arithmetic operations. The operations are applied elementwise, i.e., to each individual element.

For example, if we want a tower Shris Tracer Wuchen tiles from Chints into hours, we can divide all of the elements of running times by 60.

```
# Divide the running times by 60
running_times_in_hours <- running_times_in_hours <- running_times_in_hours = 100 to 10
  running_times_in_hours
```

- [1] 0.8500000 0.6666667 0.9500000 0.7166667 0.7833333 0.8333333 0.8333333
- [8] 0.9333333 0.7000000 0.6166667

Here are some other examples:

```
# Create a vector of the integers from 1 to 10
first_ten <- 1:10
# Subtract 5 from each element
first_ten - 5
```

```
[1] -4 -3 -2 -1 0 1 2 3 4 5
# Square each element
first_ten^2
```

```
[1]
              16 25 36 49 64 81 100
```

Arithmetic operations can also be applied between two vectors. Just like with scalars, the binary operators work element-by-element.

For example:

```
x \leftarrow c(1, 3, 5) # Create a sample x vector
y \leftarrow c(2, 4, 3) # Create a sample y vector
```

```
# Add x and y
x + y
[1] 3 7 8
# Multiply x and y
x * y
[1] 2 12 15
# Exponentiate x by y
x^y
```

[1] 1 81 125

Symbolically, if $x = (x_1, x_2, x_3)$ and y_1/y_2 , y_2/y_2 , y_3/y_2 ,

- $x + y = (x_1 + y_1, x_2 + y_2, x_3 + y_3)$
- $x-y=(x_1-y_1,x_2-y_2,x_3-y_3)$ $x*y=(x_1*y_1,x_2-y_2,x_3-y_3)$ Project Exam Help
- $x/y = (x_1/y_1, x_2/y_2, x_3/y_3)$
- $x^y = (x_{14}^{y_1}, x_{2}^{y_2}, x_{39}^{y_3})$

only addition and subtraction can be applied between vectors. Standard multiplication, division, and exponentiation do not make sense.

https://powcoder.com Recycling

When applying arithmetic operations to two vectors of different lengths, R will automatically recycle, or repeat, the shorter vector until it is long enough to match the longer vector.

For example:

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```
c(1, 3, 5) + c(5, 7, 0, 2, 9, 11)
[1] 6 10 5 3 12 16
c(1, 3, 5, 1, 3, 5) + c(5, 7, 0, 2, 9, 11) # This is the same computation that R did
```

[1] 6 10 5 3 12 16

The basic arithmetic involving a vector and a scalar (i.e., a vector of length one) is implicitly using recycling.

```
c(1, 3, 5) + 5
[1] 6 8 10
c(1, 3, 5) + c(5, 5, 5) # This is the computation that R did
```

[1] 6 8 10

Caution: When the length of the longer vector is a multiple of the length of the smaller one, R does not give any indication that it needed to recycle the shorter vector. It is up to the user to know how the operation is interpreted by R.

If the length of the longer vector is not a multiple of the length of the smaller one, the operation will still be executed, but R will also return a warning. The warning is meant to alert the user in case the mismatched vector lengths are due to a mistake in the code.

```
c(1, 3, 5) + c(5, 7, 0, 2, 9)
Warning in c(1, 3, 5) + c(5, 7, 0, 2, 9): longer object length is not a multiple
of shorter object length
[1] 6 10 5 3 12
c(1, 3, 5, 1, 3) + c(5, 7, 0, 2, 9) # This is the computation that R did
```

```
[1] 6 10 5 3 12
```

Note: Notice the difference between warnings and errors. When a warning is given, R still executes the preceding command. When an error is given, R does not execute the preceding command.

Side Note: Recycling is not done in vector calculus or linear algebra. Vectors are required to have the same length (i.e., be of the same dimension) is be added to write the COM

5 Vectorization

Suppose we have a function by all Central to a vector will automatically apply the function to each individual element in the vector.

Vector arithmetic actually implements vectorized operations is also recorred for the property of the control of

```
squared_dev <- function(x, c) {

# This function inputs a vector x and a scalar c

# and outputs a vector squared deviations from 0

squared_dev(x = 1:5, A=0d WeChat powcoder
```

[1] 1 4 9 16 25

```
# Compute squared deviations from 3
squared_dev(x = 1:5, c = 3)
```

```
[1] 4 1 0 1 4
```

Notice how squared_dev() is a vectorized function built out of two vectorized arithmetic operations.

The built-in mathematical functions we considered in the previous chapter are also vectorized:

```
sqrt(1:30)
```

```
[1] 1.000000 1.414214 1.732051 2.000000 2.236068 2.449490 2.645751 2.828427 [9] 3.000000 3.162278 3.316625 3.464102 3.605551 3.741657 3.872983 4.000000 [17] 4.123106 4.242641 4.358899 4.472136 4.582576 4.690416 4.795832 4.898979 [25] 5.000000 5.099020 5.196152 5.291503 5.385165 5.477226 log(1:30)
```

```
[1] 0.0000000 0.6931472 1.0986123 1.3862944 1.6094379 1.7917595 1.9459101
```

^{[8] 2.0794415 2.1972246 2.3025851 2.3978953 2.4849066 2.5649494 2.6390573}

^{[15] 2.7080502 2.7725887 2.8332133 2.8903718 2.9444390 2.9957323 3.0445224}

^{[22] 3.0910425 3.1354942 3.1780538 3.2188758 3.2580965 3.2958369 3.3322045}

^{[29] 3.3672958 3.4011974}

exp(1:30)

- [1] 2.718282e+00 7.389056e+00 2.008554e+01 5.459815e+01 1.484132e+02
- [6] 4.034288e+02 1.096633e+03 2.980958e+03 8.103084e+03 2.202647e+04
- [11] 5.987414e+04 1.627548e+05 4.424134e+05 1.202604e+06 3.269017e+06
- [16] 8.886111e+06 2.415495e+07 6.565997e+07 1.784823e+08 4.851652e+08
- [21] 1.318816e+09 3.584913e+09 9.744803e+09 2.648912e+10 7.200490e+10
- [26] 1.957296e+11 5.320482e+11 1.446257e+12 3.931334e+12 1.068647e+13

Note: The e+ notation in the output of exp(1:30) represents scientific notation. The value for exp(30) means 1.068647×10^{13} .

Clever use of vectorized operations and functions can make computations in R more efficient than using a loop (discussed in a later chapter) to apply functions individually to each element.

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5.1 The vapply() Function

While many functions in R are vectorized by definition, there are also non-vectorized functions that we may want to apply to exclude the first period of the first per

The vapply() function applies a function to each element of a vector (or a list, which will be discussed later). The syntax of vapply() is vapply(1, FUN, VALVE, ...), where the arguments are:

- The syntax of vapply() is vapply(), function. While, ...), where the arguments are:

 x: A vecta S.S.1.2 Introduction by the control of the
 - FUN: The function to be applied.
 - FUN. VALUE: A "template" vector that specifies the type of return value you expect the FUN function to output.

 "template" vector that specifies the type of return value you expect the FUN function to output.
 - ...: Any optional arguments to be passed to the FUN function (for example, na.rm = TRUE).

If the applied function in the FUN argument of vapply() returns a single value, the output of the vapply() function will be a vector of (heapplied function fer runs a vector of the applied function fer runs a vector of the applied function fer runs a vector of the vapply() will be a matrix (a two-dimensional array of values). We will learn more about matrices in a later chapter.

5.1.1 Example: Vectorizing a Non-Vectorized Function

The istrue() function is used to determine if the input object is identically equal to the logical value TRUE.

isTRUE(TRUE)

[1] TRUE

isTRUE(FALSE)

[1] FALSE

isTRUE(NA)

[1] FALSE

The istrue() function checks if the entire input object is True, not the individual elements of the object, so the istrue() function is *not* vectorized.

isTRUE(c(TRUE, FALSE, NA))

[1] FALSE

The output is FALSE because the vector c(TRUE, FALSE, NA) is not the single value TRUE.

In order to check whether each element of the vector is TRUE, we can vectorize the isTRUE() function with vapply(). Since the isTRUE() function returns a single logical value, we would set FUN. VALUE = logical(1).

```
vapply(c(TRUE, FALSE, NA), isTRUE, logical(1))
```

TRUE FALSE FALSE

If the FUN. VALUE is set to a return type that is not what we are expecting, then vapply() will throw an error. vapply(c(TRUE, FALSE, NA), isTRUE, logical(3))

Error in vapply(c(TRUE, FALSE, NA), isTRUE, logical(3)): values must be length 3, but FUN(X[[1]]) result interpret.//powcoder.com

Basic Numeric Summary Functions 6

Built-In Assignment Project Exam Help

In statistics, one of the first steps in analyzing a numeric variable is to summarize the numeric data with descriptive statistics, such as a measure of center and a measure of spread.

There are many built-in functions are given below.

- sum(x) computes the sum of the values of x
- mean(x) computes the mean of x/powcoder.com
 sd(x) computes the standard deviation of x
- var(x) computes the variance of x
- median(x) computation dia We Chat powcoder
- IQR(x) computes the interquartile range of x
- min(x) computes the minimum value of x
- max(x) computes the maximum value of x
- range(x) computes the range (difference between the min and max) of x
- diff(x) computes consecutive differences of x
- cumsum(x) computes the cumulative sum of x
- sort(x) orders the values of x (increasing order by default)
- fivenum(x) computes the five-number summary of x
- summary(x) computes a few summary statistics of x

For example:

```
# Compute the mean of the running times
mean(running_times)
```

```
[1] 47.3
```

```
# Compute the standard deviation of the running times
sd(running_times)
```

[1] 6.700746

6.2 Example: Coding a Variance Function

As an exercise, we can verify the var() function by coding a variance function ourselves.

The standard formula for the sample variance of a sample of values x_1, x_2, \ldots, x_n is given by

$$s^{2} = \frac{1}{n-1} \sum_{i=1}^{n} (x_{i} - \bar{x})^{2},$$

where $\bar{x} = \frac{1}{n} \sum_{i=1}^{n} x_i$ is the sample mean.

A step-by-step function to compute variance is shown below. Notice the use of vectorization within the body of the function.

```
variance <- function(x) https://powcoder.com
# This function inputs a vector x and outputs the variance of x.

# Compute the sample size
n <- length(x)ASSIGNMENT Project Exam Help

# First compute the mean of x.
xbar <- mean(x) # Or sum(x)/length(x)
# Compute ASSIGNMENT PROJECT EXAMONED Project Exam Help

# Compute ASSIGNMENT PROJECT P
```

Note: Notice that we assigned the sample size (length(x)) and mean (mean(x)) to their own objects inside the variance() function. If a computed value needs to be used more than once, it is more computationally efficient to compute them once and assign them to an object name. This saves the computer from having to recompute these values multiple times throughout the function or program.

The variance() function codes every step of the variance formula explicitly for illustrative purposes. Once you are more comfortable with vectorization and how to translate between a mathematical formula and R code, the function can be written more compactly with less object assignments. For example, the entire body of the variance function can be written in one line:

```
variance2 <- function(x) {
    # This function inputs a vector x and outputs the variance of x.
    sum((x - mean(x))^2) / (length(x) - 1)
}</pre>
```

The added space inside the sum() function is not necessary, but it is included here for clarity.

We can verify that these functions both give us the same answer as the built-in var() function.

```
var(running_times)
```

[1] 44.9

variance(running_times)

[1] 44.9

variance2(running_times)

[1] 44.9

7 Technical Subtleties

7.1 Special Values

There are a few special values to be aware of in R.

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7.1.1 NA

One of the most common special values in R is the NA object. NA is used to represent missing or unknown values (NA stands for "not available"). The NA value has a logical mode by default, but it can be coerced into any other mode as leading III to the NA value has a logical mode by default.

For example, suppose Chris Traeger got the flu and missed a day of running between his fifth and sixth recorded runs. To keep the ordering in his running times, we could insert a missing value into the running_times vector.

running_times (running_times[1:5], NA, running_times[6:16]) running_times

[1] 51 40 57 43 47 https://documents.com/Missing values are important to identify and deal with for many statistical reasons. Some functions will not

Missing values are important to identify and deal with for many statistical reasons. Some functions will not compute the correct value when NA values are present. For example:

mean(running_times)

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[1] NA

sd(running_times)

[1] NA

One way to handle missing values for many built-in functions is to include the argument na.rm = TRUE, which removes NA values from the computations.

```
mean(running_times, na.rm = TRUE)
```

[1] 47.3

sd(running_times, na.rm = TRUE)

[1] 6.700746

7.1.2 NULL

The NULL object (in all caps) is used to represent an empty, undefined, or nonexistent value. Unlike the other special values, the NULL object is *not* a vector object; it has its own special mode called NULL.

```
nada <- NULL
mode(nada)</pre>
```

[1] "NULL"

length(nada)

[1] 0

Note: The use of NULL is distinct from the use of NA. NULL represents that the value does not exist, whereas NA represents a value that is existent but unknown or missing.

7.1.3 NaN

The NaN object is a numeric value used to represent an indeterminate form (NaN stands for "not a number"). Some functions will give a warning when an NaN is returned, as this typically occurs when a mathematically illegal operation has been attempted. For example:

0 / 0

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log(-1)

Warning in log(-A:SNigriment Project Exam Help

7.1.4 Inf

The Inf object's a number civilla is a trippe self of the x. This is a ratio for x mathematical expression is actually infinite (more precisely, has an infinite limit) or is a number too large for x to store (somewhere around x 10³¹⁰).

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[1] Inf

log(0) # Negative infinity

[1] -Inf

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exp(1000) # A non-infinite but very large number

[1] Inf

7.2 Approximate Storage of Numbers

7.2.1 Floating Point Representation

Computers are unable to represent all real numbers with infinite precision. For example, a computer is unable to store the true value of the irrational number $\pi \approx 3.1415927$. While a computer is technically able to represent rational numbers exactly, it is more common to use an approximate representation.

Humans represent numbers and perform arithmetic calculations using the decimal number system. In decimal representation, a positive number a is expressed as

$$r = \sum_{k} a_k 10^k,$$

where $a_k \in \{0, 1, 2, ..., 9\}$ are the digits of a, and 10 is the base of the number system. For example, the number 5413.29 carbon expressed as WCOGET.COM

$$5413.29 = 5 \times 10^3 + 4 \times 10^2 + 1 \times 10^1 + 3 \times 10^0 + 2 \times 10^{-1} + 9 \times 10^{-2}$$
.

R, and most other courses beganning through use flower to it representation which is a binary (base 2) variation on scientific notation.

For example, consider a number written to four significant digits as 6.926×10^{-4} . This approximate representation could represent any true value between 4.0069215 and 0.00069265. In floatile, point representation, the significant aignorphism of the property o

In the binary number system, digits are either 0 or 1. So 6.926×10^{-4} is written as $1.011_2 \times 2^{-11}$. The subscript of 2 in 1.011_2 denotes base 2. The number 1.011_2 represents

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Even though 6.926×10^{-4} is written as $1.011_2 \times 2^{-11}$, they are not identical representations. It turns out that four binary digits have less precision than four decimal digits. The representation of $1.011_2 \times 2^{-11}$ could represent any true value between about allow 0.00001 and 0.00002 The master 6.926×10^{-4} actually does not have an exact binary representation in a finite number of digits.

The standard precision in R, known as **double precision** in computer science, is 53 binary digits (or bits), which is equivalent to about 15 or 16 decimal digits. Floating point numbers using double precision are sometimes called **doubles**. Whole numbers, or **integers**, are often stored using 32 bit integer storage.

Note: In some programming languages, integers and doubles are considered separate numeric types. R actually also has separate integer and double types, but R will automatically switch between them to make computations easier. The "numeric" mode in R is a synonym for the double type (both names exist in R as a historical artifact). The "integer" type is technically separate from numeric, but calling mode() on an integer vector will still return "numeric".

Side Note: The typeof() function returns the internal storage type of an input object. This is the same as the mode of an object, except that the integer and double types both have numeric modes.

typeof(first_ten)

[1] "integer"

mode(first_ten)

[1] "numeric"

typeof(pi)

[1] "double"

```
mode(pi)
```

[1] "numeric"

7.2.2 Rounding Errors

The reason why we need to understand that numbers are stored approximately in R is that this inherent limitation of finite precision representations affects the accuracy of calculations. Any computations done on approximated numbers can accumulate **rounding errors**.

For example, using exact arithmetic, we know that $(5/4) \times (4/5) = 1$, so $(5/4) \times (n \times 4/5) = n$, for any number n. However, this simple calculation in R already has rounding errors:

```
n <- 1:10
1.25 * (n * 0.8) - n https://powcoder.com
```

- [1] 0.000000e+00 0.000000e+00 4.440892e-16 0.000000e+00 0.000000e+00
- [6] 8.881784e-16 8.881784e-16 0.000000e+00 0.000000e+00 0.000000e+00

The exact answer should be 1 to 11 1, but yet that they be cross for some values of t. The errors in this example are essentially negligible (around 10 10), but they are important to be aware of and acknowledge. Rounding errors tend to occur in most computations, so long series of computations tend to accumulate larger errors than shorter ones.

7.2.2.1 THE ASSIGNMENT OF THE PRINCIPLE TO THE PRINCIPLE OF THE PRINCIPLE

A common statistical example to illustrate the effect of rounding errors is in computing the variance.

The standard formula for the variance requires calculating the sample mean \bar{x} first and then the sum of squared deviations second, is the compute overly to collect the data values twice. This is considered computationally expensive, since it requires storing the data values in the computer's memory between passes over the data.

Through some algebraic manipulation of atternate "act pap" formulais give by

$$s^{2} = \frac{1}{n-1} \left(\sum_{i=1}^{n} x_{i}^{2} - n\bar{x}^{2} \right).$$

While this formula is mathematically equivalent and computationally less expensive, it can be numerically unstable when the variance is small relative to the mean. To illustrate this, we will first write the one-pass function.

```
var_one <- function(x) {
    # This function inputs a vector x
    # and computes the one-pass formula for the variance of x.
    n <- length(x)
    (sum(x^2) - n * mean(x)^2) / (n - 1)
}</pre>
```

This function will give the correct answer for small examples.

```
var(first_ten) # Built-in function
```

[1] 9.166667

```
variance(first_ten) # Two-pass function
```

[1] 9.166667

```
var_one(first_ten) # One-pass function
[1] 9.166667
Suppose we add a large value (like 10<sup>10</sup>) to every value in first_ten.
```

Question: What happens to the mean when we add a large value to every value? What about to the variance?

```
# Add 10^10 to the first_ten vector and assign the result to the whoh vector
whoh <- first_ten + 1e10
var(whoh) # Built-in function</pre>
```

[1] 9.166667

variance(uhoh) # Two-passhttps://powcoder.com

[1] 9.166667

Var_one(uhoh) # Assignment Project Exam Help

Since the inner terms $\sum_{i=1}^{n} x_i^2$ and $n\bar{x}^2$ are very close when the x_i values are large, then computing the difference results in a destriction of the computing the difference results in a destriction of the computing the difference results in a destriction of the computing the difference results in a destriction of the computing the difference results in a destriction of the computing the difference results in a destriction of the computing the difference results in a destriction of the computing the difference results in a destriction of the computing the difference results in a destriction of the computing the difference results in a destriction of the computing the difference results in a destriction of the computing the difference results in a destriction of the computing the difference results in a destriction of the computing the difference results in a destriction of the computing the comp

Caution: Do not use the one-pass variance formula in practice.

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