Homework 1. Fixpoints and grammar filters

[131 home > Homework]

Introduction

You are a reader for Computer Science 181, which asks students to submit grammars that solve various problems. However, many of the submitted grammars are trivially wrong, in several ways. Here is one. Some grammars contain unreachable rules, that is, rules that can never be reached from the start symbol by applying zero or more rules. Unreachable rules do not affect the language or parse trees generated by a grammar, so in some sense they don't make the answers wrong, but they're noise and they make grading harder. You'd like to filter out the noise, and just grade the useful parts of each grammar.

You've heard that OCaml is a good language for writing compilers and whatnot, so you decide to give it a try for this application. While you're at it, you have a background in fixed point and periodic point theory, so you decide to give it a try too.

Definitions

Assignment Project Exam Help fixed point

(of a function f) A point x such that f x = x. In this description we are using OCaml notation, in which functions always have one argument and parentheses are not needed around arguments.

computed fixed point

(of a function f with respect to an initial point x) A fixed point of f computed by calculating x, f x, f (f x), f (f (f x)), etc., stopping when a fixed point is found for f. If no fixed point is ever found by this procedure, the computed fixed point is not defined for f and x.

Aga weChat powcoder periodic point

(of a function f with period p) A point x such that f (f \cdot ... (f x)) = x, where there are p occurrences of f in the call. That is, a periodic point is like a fixed point, except the function returns to the point after p iterations instead of 1 iteration. Every point is a periodic point for p=0. A fixed point is a periodic point for p=1.

computed periodic point

(of a function f with respect to a period p and an initial point x) A periodic point of f with period p, computed by calculating x, f x, f (f x), f (f (f x)), etc., stopping when a periodic point with period p is found for f. The computed periodic point need not be equal to x. If no periodic point is ever found by this procedure, the computed periodic point is not defined for f, p, and x.

symbol

A symbol used in a grammar. It can be either a nonterminal symbol or a terminal symbol; each kind of symbol has a value, whose type is arbitrary. A symbol has the following OCaml type:

```
type ('nonterminal, 'terminal) symbol =
   N of 'nonterminal
   T of 'terminal
```

right hand side

A list of symbols. It corresponds to the right hand side of a single grammar rule. A right hand side can be empty.

rule

A pair, consisting of (1) a nonterminal value (the left hand side of the grammar rule) and (2) a right hand side.

grammar

A pair, consisting of a start symbol and a list of rules. The start symbol is a nonterminal value.

Assignment

Let's warm up by modeling sets using OCaml lists. The empty list represents the empty set, and if the list t represents the set T, then the list h::t represents the set {h}UT. Although sets by definition do not contain duplicates, the lists that represent sets can contain duplicates. Another set of warmup exercises will compute fixed points. Finally, you can write a function that filters unreachable rules.

- 1. Write a function subset a b that returns true iff (i.e., if and only if) a⊆b, i.e., if the set represented by the list a is a subset of the set represented by the list b. Every set is a subset of itself. This function should be generic to lists of any type: that is, the type of subset should be a generalization of 'a list -> 'a list -> bool.
- 2. Write a function equal_sets a b that returns true iff the represented sets are equal.
- 3. Write a function set union a b that returns a list representing $a \cup b$.
- 4. Write a function set_symdiff a b that returns a list representing $a \ominus b$, the <u>symmetric difference</u> of a and b, that is, the set of all members of a\bullet b that are not also members of a\bullet b.
- 5. <u>Russell's Paradox</u> involves asking whether a set is a member of itself. Write a function self_member s that returns true iff the set represented by s is a member of itself, and explain in a comment why your function is correct; or, if it's not possible to write such a function in OCaml, explain why not in a comment.
- 6. Write a function computed, fixed point to f x that returns the computed fixed joint for f with respect to x, assuming that eq is the equality predicate for J'S domain. A common case is that eq will be (=), that is, the builtin equality predicate of OCaml; but any predicate can be used. If there is no computed fixed point, your implementation can do whatever it wants: for example, it can print a diagnostic, or go into a loop, or send nasty emathrics ages to the users velatives en computed fixed point. OK, now for the real work. Write a function filter_reachable g that returns a copy of the grammar g
- 7. OK, now for the real work. Write a function filter_reachable g that returns a copy of the grammar g with all unreachable rules removed. This function should preserve the order of rules: that is, all rules that are returned should be in the same order as the rules in g.
- 8. Supply at least one test cases the least one test cases below. When testing the function F call the test cases my_F_test0, my_F_test1, etc. For example, for subset your first test case should be called my_subset_test0. Your test cases should exercise all the above functions, even though the sample test cases do not.

Your code should follow these guidelines:

- 1. Your code may use the <u>stdlib</u> and <u>List</u> modules, but it should use no other modules other than your own code.
- 2. It is OK (and indeed encouraged) for your solutions to be based on one another; for example, it is fine for filter_reachable to use equal_sets and computed_fixed_point.
- 3. Your code should prefer pattern matching to conditionals when pattern matching is natural.
- 4. Your code should be free of <u>side effects</u> such as loops, assignment, input/output, incr, and decr. Use recursion instead of loops.
- 5. Simplicity is more important than efficiency, but your code should avoid using unnecessary time and space when it is easy to do so. For example, instead of repeating a expression, compute its value once and reuse the computed value.
- 6. The test cases below should work with your program. You are unlikely to get credit for it otherwise.

Assess your work by writing a brief after-action report that summarizes why you solved the problem the way you did, other approaches that you considered and rejected (and why you rejected them), and any weaknesses in your solution in the context of its intended application. This report should be a <u>plain text</u> file that is no more than 2000 bytes long. See <u>Resources for oral presentations and written reports</u> for advice on how to write assessments; admittedly much of the advice there is overkill for the simple kind of report we're looking for here.

Submit

Submit three files via CourseWeb. The file hwl.ml should implement the abovementioned functions, along with any auxiliary types and functions and required comments; in particular, it should define the symbol type as shown above. The file hwltest.ml should contain your test cases. The file hwl.txt should hold your assessment. Please do not put your name, student ID, or other personally identifying information in your files.

Sample test cases

See <u>hw1sample.ml</u> for a copy of these tests.

```
let subset_test0 = subset [] [1;2;3]
let subset_test1 = subset [3;1;3] [1;2;3]
let subset_test2 = \underline{not} (subset [1;3;7] [4;1;3])
let equal_sets_test0 = equal_sets [1;3] [3;1;3]
let equal_sets_test1 = not (equal_sets [1;3;4] [3;1;3])
let set_union_test0 = equal_sets (set_union [] [1;2;3]) [1;2;3]
let set_union_test1 = equal_sets (set_union [3;1;3] [1;2;3]) [1;2;3]
let set_union_test2 = equal_sets (set_union [] []) []
let set symdiff test0 =
equal_sets (setAsmSignment1Project Exam Help
  equal_sets (set_symdiff [3;1;3] [1;2;3]) [2]
let set symdiff test2 =
  let computed fixed point test =
  computed fixed point (=) (fun x \rightarrow x \angle 2) 1000000000 = 0
computed_fixed_point_test_ weChat powCoder let computed_fixed_point_test2
  computed_fixed_point (=) sqrt 10. = 1.
let computed fixed point test3 =
  ((computed_fixed_point (fun x y \rightarrow abs_float (x \rightarrow y) < 1.)
                        (fun x -> x /. 2.)
                        10.)
   = 1.25)
(* An example grammar for a small subset of Awk. *)
type awksub nonterminals =
  | Expr | Lvalue | Incrop | Binop | Num
let awksub rules =
   [Expr, [T"("; N Expr; T")"];
    Expr, [N Num];
    Expr, [N Expr; N Binop; N Expr];
   Expr, [N Lvalue];
    Expr, [N Incrop; N Lvalue];
    Expr, [N Lvalue; N Incrop];
   Lvalue, [T"$"; N Expr];
    Incrop, [T"++"];
    Incrop, [T"--"];
    Binop, [T"+"];
    Binop, [T"-"];
    Num, [T"0"];
    Num, [T"1"];
    Num, [T"2"];
```

```
Num, [T"3"];
   Num, [T"4"];
   Num, [T"5"];
   Num, [T"6"];
   Num, [T"7"];
   Num, [T"8"];
   Num, [T"9"]]
let awksub_grammar = Expr, awksub_rules
let awksub test0 =
  filter_reachable awksub_grammar = awksub_grammar
let awksub test1 =
  filter_reachable (Expr, <u>List.tl</u> awksub_rules) = (Expr, List.tl awksub_rules)
let awksub test2 =
  filter_reachable (Lvalue, awksub_rules) = (Lvalue, awksub_rules)
let awksub test3 =
  filter_reachable (Expr, List.tl (List.tl awksub_rules)) =
    (Expr,
     [Expr, [N Expr; N Binop; N Expr];
     Expr, [N Lvalue];
     Expr, [N Incrop; N Lvalue];
     Expr, [N Lvalue; N Incrop];
     Lvalue, [T A: Signment Project Exam Help Incrop, [T A: Signment Project Exam Help
      Binop, [T "+"];
      Binop, [T "-"]])
                        https://powcoder.com
let awksub test4 =
  filter reachable (Expr, List.tl (List.tl awksub rules))) =
    (Expr,
     [Expr, [N Lvalue];
     Expr, [N Incrop; N And d: WeChat powcoder
     Expr, [N Lvalue; N Incrop];
     Lvalue, [T "$"; N Expr];
      Incrop, [T "++"];
      Incrop, [T "--"]])
type giant nonterminals =
  | Conversation | Sentence | Grunt | Snore | Shout | Quiet
let giant grammar =
  Conversation,
  [Snore, [T"ZZZ"];
   Quiet, [];
   Grunt, [T"khrgh"];
   Shout, [T"aooogah!"];
   Sentence, [N Quiet];
   Sentence, [N Grunt];
   Sentence, [N Shout];
   Conversation, [N Snore];
   Conversation, [N Sentence; T","; N Conversation]]
let giant test0 =
  filter_reachable giant_grammar = giant_grammar
let giant test1 =
  filter reachable (Sentence, List.tl (snd giant grammar)) =
    (Sentence,
     [Quiet, []; Grunt, [T "khrgh"]; Shout, [T "aooogah!"];
      Sentence, [N Quiet]; Sentence, [N Grunt]; Sentence, [N Shout]])
```

```
let giant_test2 =
  filter_reachable (Quiet, snd giant_grammar) = (Quiet, [Quiet, []])
```

Sample use of test cases

When testing on SEASnet, use one of the machines lnxsrv06.seas.ucla.edu, lnxsrv07.seas.ucla.edu, lnxsrv09.seas.ucla.edu, and lnxsrv10.seas.ucla.edu. Make sure /usr/local/cs/bin is at the start of your path, so that you get the proper version of OCaml. To do this, append the following lines to your \$HOME/.profile file if you use bash or ksh:

```
export PATH=/usr/local/cs/bin:$PATH

or the following line to your $HOME/.login file if you use tesh or csh:
set path=(/usr/local/cs/bin $path)
```

The command ocaml should output the version number 4.11.1.

If you put the <u>sample test cases</u> into a file hwlsample.ml, you should be able to use it as follows to test your hwl.ml solution on the SEASnet implementation of OCaml. Similarly, the command #use "hwltest.ml";; should run your own test cases on your solution.

```
* ocaml ocaml versingnment Project Exam Help
```

```
# #use "hw1.ml";;
type ('a, 'b) symbol = Nhttps://powcoder.com
# #use "hwlsample.ml";;
val subset test0 : bool = true
val subset_test1 : bool = true
val subset_test2 : bool = Ardd WeChat powcoder val equal_sets_test0 : bool = true
val equal sets test1 : bool = true
val set_union_test0 : bool = true
val set union test1 : bool = true
val set union test2 : bool = true
val set symdiff test0 : bool = true
val set_symdiff_test1 : bool = true
val set symdiff test2 : bool = true
val computed fixed point test0 : bool = true
val computed_fixed_point_test1 : bool = true
val computed_fixed_point_test2 : bool = true
val computed_fixed_point_test3 : bool = true
type awksub nonterminals = Expr | Lvalue | Incrop | Binop | Num
val awksub rules:
  (awksub_nonterminals * (awksub_nonterminals, string) symbol list) list =
  [(Expr, [T "("; N Expr; T ")"]); (Expr, [N Num]);
   (Expr, [N Expr; N Binop; N Expr]); (Expr, [N Lvalue]);
   (Expr, [N Incrop; N Lvalue]); (Expr, [N Lvalue; N Incrop]);
   (Lvalue, [T "$"; N Expr]); (Incrop, [T "++"]); (Incrop, [T "--"]);
   (Binop, [T "+"]); (Binop, [T "-"]); (Num, [T "0"]); (Num, [T "1"]);
   (Num, [T "2"]); (Num, [T "3"]); (Num, [T "4"]); (Num, [T "5"]);
   (Num, [T "6"]); (Num, [T "7"]); (Num, [T "8"]); (Num, [T "9"])]
val awksub grammar:
  awksub nonterminals *
  (awksub_nonterminals * (awksub_nonterminals, string) symbol list) list =
   [(Expr, [T "("; N Expr; T ")"]); (Expr, [N Num]);
    (Expr, [N Expr; N Binop; N Expr]); (Expr, [N Lvalue]);
```

```
(Expr, [N Incrop; N Lvalue]); (Expr, [N Lvalue; N Incrop]);
    (Lvalue, [T "$"; N Expr]); (Incrop, [T "++"]); (Incrop, [T "--"]);
    (Binop, [T "+"]); (Binop, [T "-"]); (Num, [T "0"]); (Num, [T "1"]);
    (Num, [T "2"]); (Num, [T "3"]); (Num, [T "4"]); (Num, [T "5"]);
    (Num, [T "6"]); (Num, [T "7"]); (Num, [T "8"]); (Num, [T "9"])])
val awksub_test0 : bool = true
val awksub_test1 : bool = true
val awksub test2 : bool = true
val awksub_test3 : bool = true
val awksub_test4 : bool = true
type giant_nonterminals =
   Conversation
   Sentence
   Grunt
   Snore
   Shout
  Quiet
val giant_grammar :
  giant_nonterminals *
  (giant_nonterminals * (giant_nonterminals, string) symbol list) list =
  (Conversation,
   [(Snore, [T "ZZZ"]); (Quiet, []); (Grunt, [T "khrgh"]);
    (Shout, [T "aooogah!"]); (Sentence, [N Quiet]); (Sentence, [N Grunt]);
    (Sentence, [N Shout]); (Conversation, [N Snore]);
    (Conversation, [N Sentence; T ","; N Conversation])])
val giant_test0 : bool = true
val giant_test1 : bool ₹ true
val giant_test2 ASSIGNment Project Exam Help
```

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