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Motivation

Throughout your studies, lecturers have (Hoperuny) expounded on the software engineering advantages of abstract data types.

So what is an abstract data type? Powcoder.com

An abstract data type is a type defined not by its internal representation but by the operations that can be performed or its an abstract data type is a type defined and the performed or its an abstract data type is a type defined and the performed or its an abstract data type is a type defined and the performed or its analysis of the performance of the performed or its analysis of the performance of the performed or its analysis of the performance of the perfo

implementation.

Language Examples: C

How do we do it in C?

```
stack Signment Project Exam Help typedef stack; Project Exam Help
Stack empty (hittps)://stack two coder.com
Stack pop(Stack, int*);
bool isEmpty(Stack);
                        struct_stack_impl {
void destroy Atack
                           Chat powcoder
                           Stack tail:
By only importing stack.h.
we hide the implementation.
                        Stack empty() { ... }
                         . . .
```

Language Examples: Haskell

Define a module but restrict what is exported: mody Ast Stack gnment Project Exam Help , empty https://powcoder.com . isEmpty) where data Stack Add WeChat powcoder empty :: Stack empty = Nil

4

. . .

Language Examples: Java

```
Typically Java accomplishes this with subtype polymorphism, something we discuss in the rest selection and the project exam Help
public interface Stack {
     public void push(int x);
    public interpretation boolean is Empty Funty Stack Full Com
public class Astrack() { ... };
```

Language Examples: Python

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Quote

"Python is very simple and nice when you start to use it, but you don't get too far down the road, if you're me, before you discover it has no data abstraction at all. That's not good because big programs require modularity and encapsulation and you'd like a language that could support that."

Barbara Liskov, Ah Pover With action 2013. DOWCOCCI

You don't need static types to enforce abstraction, but it helps.

MinHS

How can we support abstract data types in MinHS? Can we use existing features to do so? Washington Project Exam Help

recfun foo push pop isEmpty empty = https://powercoder.con

(type S.

The program *foo* is defined for any stack type S. Implementations of the operations must be provided as parameters.

Modules

We was saignment as Partio Jeccont in Xiahin phretains of the stack interface. It's too cumbersome to pass around each function implementation individually like before. This value is called a *module*.

Our toy foo program por carrie pieces to Ce Ce written as Com

Add WeChat powcoder

For some type STACKMODULE. Taking in a value of type STACKMODULE is analogous to importing the module.

Via Curry-Howard

Let's translate the type of *foo* into a proposition, then do logical transformations to it:

 $\begin{array}{c} \text{Assign} & \text{Athison the inhite hoard} \\ \forall \mathcal{S}. \ ((\mathcal{S} \to \mathtt{Int} \overset{\bullet}{\to} \mathcal{S}) \to (\mathcal{S} \to \mathcal{S} \times \mathtt{Int}) \to (\mathcal{S} \to \mathtt{Bool}) \to \mathcal{S} \to \mathtt{Bool}) \end{array}$

Existential Types

We have our STACKMODULE type:

(3SASSignment Projecto Examo Help

STACKMODULE

But what is thing?//powcoder.com

Existential vs Universal Types

- $\forall a. \ \tau$ When producing a value, a is an arbitrary, unknown type. When Conducting Walter hay be instantiated to onder
- $\exists a. \ \tau$ When consuming a value, a is an arbitrary, unknown type. When producing a value, a may be instantiated to any desired type.

Another, Smaller Example

```
An ART Bag is specified by three Project Exam Help
```

- 2 addToBag, which adds an integer to the bag.
- average, which gives the afithmetic mean of all integers in the bag. What's the type for this? POWCOGEL.COM



The type of a module is called its *signature*.

Making a Module

We can make a value of an existential type using the Pack expression.

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 Δ ; $\Gamma \vdash (\text{Pack } \tau \ e) : \exists a. \ \rho$

Just as the typhttpsid be produced to the type $\exists a. \ \tau$ could be viewed as a pair of a type and a value.

```
Pack (Int \times Int) CC Chat powcoder (0,0), recfun addToBag b i = (fst b+i, snd b+1), recfun average b = (fst b \div snd b) :: BAGMODULE
```

Importing a Module

If we are given a module as a parameter, we can access its contents using the Open expression:

```
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```

The last two premises ensure that the type ρ does not contain the abstract type that is only in scope inside e_2 .

```
Example (Averaging some numbers with a bag)

rectum example :: (BAGMODULL → Int) bagM =

Open bagM

(B. (empty, addToBag, average).

average (addToBag (addToBag empty 60) 30)

)
```

In Practice

Assignment Project Exam Help Generally, most programming languages have fairly poor support for modules.

- Dynamically typed languages typically don't support them at all¹.
- Haskell withput the ensions that the transfer of the them.
- Java and similar accomplish modularity via OOP, which don't support existential typing in its full generality.
- Languages Ather twill die that bowcochesupport for modules.

¹What they call "modules" aren't. Just like types.