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COMP3161/9164
Concepts of Programming Languages

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Safety and Liveness; Exceptions

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Program Properties

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Consider a sequence of states, representing the evaluation of a program in a small step semantics (a **trace**):

$\sigma_1 \mapsto \sigma_2 \mapsto \sigma_3 \mapsto \dots \mapsto \sigma_n$
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Observe that some traces are finite, whereas others are infinite. To simplify things, we'll make all traces infinite by repeating the final state of any terminating state infinitely. Such infinite sequences of states are called **behaviours**.

A correctness **property** of a program is defined to be a **set of behaviours**.

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Safety vs Liveness

- 1 A *safety* property states that something **bad** does not happen. For example:

I will never run out of money.

These are properties that may be violated by a *finite prefix* of a behaviour.

- 2 A *liveness* property states that something **good** will happen. For example:

If I start drinking now, eventually I will be smashed.

These are properties that cannot be violated by a *finite prefix* of a behaviour.

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Combining Properties

Safety properties we've seen before

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Partial correctness (Hoare Logic)

Static semantics properties

Liveness properties we've seen before

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Termination

Confluence

Theorem

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Every property is the **intersection** of a **safety** and a **liveness** property.

The proof of this involves **topology** (specifically **metric spaces**).

Types

What sort of properties do **types** give us?

Adding types to λ -calculus eliminates terms with no normal forms.

$$\frac{(x : \tau) \in \Gamma}{\Gamma \vdash x : \tau} \quad \frac{x : \tau_1, \Gamma \vdash e : \tau_2}{\Gamma \vdash \lambda x. e : \tau_1 \rightarrow \tau_2} \quad \frac{\Gamma \vdash e_1 : \tau_1 \rightarrow \tau_2 \quad \Gamma \vdash e_2 : \tau_1}{\Gamma \vdash e_1 e_2 : \tau_2}$$

Remember $(\lambda x. x x) (\lambda x. x x)$? Trying to type this requires an **infinite** type $\tau_1 = \tau_1 \rightarrow \tau_2$.

Theorems

Each well typed λ -term always reduces to a normal form (**strong normalisation**). Furthermore, the normal form has the same type as the original term (**subject reduction**).

This means that all typed λ -terms terminate!

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With Recursion

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MinHS, unlike lambda calculus, has **built in recursion**. We can define terms like:

$$\text{recfun } f : (\text{Int} \rightarrow \text{Int}) \leftarrow f \text{ } \lambda \beta$$
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Which has no normal form or final state, despite being typed. **What now?**

The **liveness** parts of the typing theorems can't be salvaged, but the **safety** parts can...

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Type Safety

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Type safety is the property that states:

Well-typed programs do not go wrong.

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By “go wrong”, we mean reaching a *stuck state* — that is, a non-final state with no outgoing transitions. *What are some examples of stuck states?*

There are many other definitions of things called “type safety” on the internet, but they are all incorrect.

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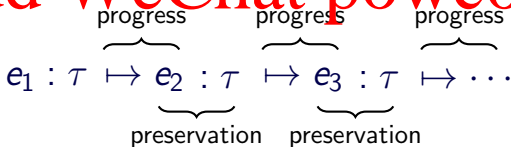
Progress and Preservation

We want to prove that a well-typed program either goes on forever or reaches a final state. We prove this with two lemmas.

How to prove type safety

- 1 **Progress**, which states that well-typed states are not stuck states. That is, if an expression $e : \tau$ then either e is a final state or there exists a state e' such that $e \mapsto e'$.
- 2 **Preservation**, which states that evaluating one step preserves types. That is, if an expression $e : \tau$ and $e \mapsto e'$, then $e' : \tau$.

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In the real world

Which of the following languages are type safe?

- C **No**
- C++ **No**
- Haskell **Yes**
- Java **Yes**
- Python **Yes**
- Rust **Yes** (except for unsafe)
- MinHS **Not type safe yet!**

Why is MinHS **not type safe**?

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Division by Zero

We can assign a type to a division by zero:

$$\frac{\frac{}{(\text{Num } 3) : \text{Int}} \quad \frac{}{(\text{Num } 0) : \text{Int}}}{(\text{Div } (\text{Num } 3) (\text{Num } 0)) : \text{Int}}$$

But there is no outgoing transition from this state (nor is it final)!

⇒ We have violated **progress**.

We have two options:

- 1 **Change the static semantics** to exclude division by zero. This reduces to the **halting problem**, so we would be forced to overapproximate.
- 2 **Change the dynamic semantics** so that the above state has an outgoing transition.

Our Cop-Out

Add a new state, Error, that is the successor state for any partial function:

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$$\frac{}{(\text{Div } v \ (\text{Num } 0)) \mapsto_M \text{Error}}$$

Any state containing Error evaluates to Error:

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$$\frac{}{(\text{Plus } e \ \text{Error}) \mapsto_M \text{Error}} \quad \frac{}{(\text{Plus } \text{Error } e) \mapsto_M \text{Error}}$$

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$$\frac{}{(\text{If } \text{Error } t \ e) \mapsto_M \text{Error}}$$

(and so on – this is much easier in the C machine!)

Type Safety for Error

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We've satisfied **progress** by making a successor state for partial functions, but how should we satisfy **preservation**?

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Error : τ

That's right, we give Error any type.

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Dynamic Types

Some languages (e.g. Python, JavaScript) are called *dynamically typed*. This is more accurately called *untyped* as they achieve type safety with the trivial type system containing only one type, here written \star , and only one typing rule¹:

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They achieve type safety by defining execution for every syntactically valid expression, *even* those that are not well typed.

Some languages make sensible decisions like evaluating to an error state, whereas other languages make alternative decisions like trying to perform operations on diverse kinds of data.

¹The things these languages call types are part of values. They aren't types.

Exceptions

Error may satisfy type safety but it's not satisfying as a programming language feature — when an error occurs, we may not want to crash the program. We will add more fine grained error control — *exceptions* — to MinHS.

Example (Exceptions)

try/catch/throw in Java, setjmp/longjmp in C, try/except/raise in Python.

Exceptions Syntax

Raising an Exception

Concrete

raise e

Abstract

(Raise e)

Handling an Exception

try e_1 **handle** $x \Rightarrow e_2$

(Try e_1 (x . e_2))

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Informal Semantics

Example

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```
try  
  if  $y \leq 0$  then  
    raise DivisorError  
  else  
     $(x/y)$   
handle err  $\Rightarrow -1$ 
```

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For an expression $(\text{try } e_1 \text{ handle } x \Rightarrow e_2)$ we

- 1 Evaluate e_1
- 2 If **raise** v is encountered while evaluating e_1 , we bind v to x and evaluate e_2 .

Note that it is possible for **try** expressions to be **nested**.

- The inner-most **handle** will catch exceptions.
- Handlers may **re-raise** exceptions.

Static Semantics

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The type given to ~~exception values~~ is usually some specific blessed type τ_E that is specifically intended for that purpose. For example, the Throwable type in Java. In dynamically typed languages, the type is just the same as everything else (i.e. \star).

Typing Rules

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$$\frac{\Gamma \vdash e : \tau_E}{\Gamma \vdash (\text{Raise } e) : \tau} \quad \frac{\Gamma \vdash e_1 : \tau \quad x : \tau_E, \Gamma \vdash e_2 : \tau}{\Gamma \vdash (\text{Try } e_1(x) e_2) : \tau}$$

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Dynamic Semantics

Easier to describe using the C Machine. We introduce a new type of state, $s \Leftarrow v$, that means an exception value v has been raised. The exception is bubbled up the stack until a handler is found.

Evaluating a Try Expression

$$s \succ (\text{Try } e_1 (x. e_2)) \mapsto_C (\text{Try } \square (x. e_2)) \triangleright s \succ e_1$$

Returning from a Try without raising

$$(\text{Try } \square (x. e_2)) \triangleright s \Leftarrow v \mapsto_C s \Leftarrow v$$

Evaluating a Raise expression

$$s \succ (\text{Raise } e) \mapsto_C (\text{Raise } \square) \triangleright s \succ e$$

Raising an exception

$$(\text{Raise } \square) \triangleright s \Leftarrow v \mapsto_C s \Leftarrow v$$

Catching an exception

$$(\text{Try } \square (x. e_2)) \triangleright s \Leftarrow v \mapsto_C s \succ e_2[x := v]$$

Propagating an exception

$$f \triangleright s \Leftarrow v \mapsto_C s \Leftarrow v$$

Efficiency Problems

The approach described above is highly inefficient. Throwing an exception takes linear time with respect to the depth of stack frames!

Only the most simplistic implementations work this way. A much more efficient approach is to keep a separate stack of handler frames.

Handler frames

A *handler frame* contains:

- 1 A copy of the control stack above the Try expression.
- 2 The exception handler that is given in the Try expression.

We write a handler frame that contains a control stack s and a handler $(x. e_2)$ as $(\text{Handle } s (x. e_2))$.

Efficient Exceptions

Evaluating a Try now pushes the handler onto the handler stack and a marker onto the control stack.

$$(h, s) \succ (\text{Try } e_1 (x. e_2)) \mapsto_C (\text{Handle } s (x. e_2) \triangleright h, (\text{Try } \square) \triangleright s) \succ e_1$$

Returning without raising in a Try block removes the handler again:

$$(\text{Handle } s (x. e_2) \triangleright h, (\text{Try } \square) \triangleright s) \prec v \mapsto_C (h, s) \prec v$$

Raising an exception now uses the handler stack to immediately jump to the handler:

$$(\text{Handle } s (x. e_2) \triangleright h, (\text{Raise } \square) \triangleright s') \prec v \mapsto_C (h, s) \succ e_2[x := v]$$

Exceptions in Practice

While exceptions are undoubtedly useful, they are a form of **non-local** control flow and therefore must be used carefully.

In Haskell, exceptions tend to be avoided as they make a liar out of the type system:

$\text{head} :: [a] \rightarrow a$
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In Java, **checked exceptions** may be used to allow the possibility of exception throws to be tracked in the type system.

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Monads

One of the most common uses of the Haskell **monad** construct is for a kind of error handling that is honest about what can happen in the types.