

DATA REPRESERVICAERAN NAMED IN CONTROLL REPRESERVIC

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Why Binary Numbers?

- Computers process binary patterns
 - Patterns of Os and 1s

- Assignment Project Exam Help
 To represent data within a computer, we need to code it as a binary https://powcoder.com pattern
- Most important to Addiside the tenant of the second of t
 - Convert into binary

Decimal to Binary

- Steps:
 - · Divide the nambig hypegitile of the cutting the premainder
 - Repeat previous http://withpreviewderoffentuntil a zero quotient is obtained
 - Add WeChat powcoder
 - Answer is obtained by reading the remainder column bottom to the top

Decimal to Binary (Example)

What is 98₁₀ in binary?

•		•	_	7	7	r 1	
Assignment		roiect	-	ivam			10
49915111116111		TUICL		Adda	V		
	75	delient		Neman		JUI	

98 ÷ 2 https://	powcoder	com ⁰
² A ḋ∂l W	VeChat por	wcoder
12 ÷ 2	6	0
6 ÷ 2	3	0
3 ÷ 2	1	1
1 ÷ 2	0	1

11000102

$$1100010_2 = 1 * 2^6 + 1 * 2^5 + 0 * 2^4 + 0 * 2^3 + 0 * 2^2 + 1 * 2^1 + 0 * 2^0$$

= $64 + 32 + 0 + 0 + 0 + 2 + 0 = 98_{10}$

Octal (Base 8)

- Used in the past as a more convenient base for representing long binary values
- · Converting to spingarment Project Exam Help
 - Starting from the rightmost (least significant) end, each group of 3 bits (why? 8 = 23) https://preseptowocaletight(malled octet)
- Example: What is 10101, in Octal? Add WeChat powcoder

Example: What is 357₈ in Binary?

	7	5	3	
= 11101111 ₂	\downarrow	\downarrow	\downarrow	
	111	101	011	

Hexadecimal (Base 16)

- Used by programmers to represent long binary values
 - Preferred over Octal
- 16 = 2⁴ → 4ABiniary migits Prepresent ane Hexadecimal digit (bits) starting from the rightmost end, each group of 4 bits represents 1https://poimapdgitcom
- Example: What is 19010100 in hexadecimal?

$$\frac{1001}{4}$$
 $\frac{100}{4}$ = 94₁₆

Example: What is 86₁₆ in Binary?

	6	8	
$= 10000110_{2}$	\downarrow	\downarrow	
	0110	1000	

Binary vs. Hexadecimal

Hex	0	1	2	3	4	5	6	7	8	9	Α	В	С	D	E	F
Decimal	0	1	2.	3	4	5	Dr	7. O 1.C	S	r L	10	11	I 12 1	13	14	15
Binary	0	1	10	S ₁₁	100	101	110		1000	7.7	1010	1011	1100	1101	1110	1111

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Generally:

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	1 byte =	8 binary digits =	2 hexadecimal digits
1 word =	2 bytes =	16 binary digits =	4 hexadecimal digits
1 long word =	4 bytes =	32 binary digits =	8 hexadecimal digits

Representing Data

- Data Types of interest
 - Integers (Unaignigghaigend)Project Exam Help
 - Reals (Floating Point) → later on in the course

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Text

Signed and Unsigned Integers

 Natural numbers can be represented by their binary value within the computer

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- Representation of signed integers is more important https://powcoder.com
- Several possibilited WeChat powcoder
 - Sign & Magnitude
 - One's Complement
 - Two's Complement
 - Excess-n (Bias-n)
 - Binary-Coded Decimal (BCD)

Signed and Unsigned Integers

- In any representation, desirable properties are:
 - Only one bit Apastign premal Peroject Exam Help
 - Equal number of btthe pawegative cares
 - Maximum range of values

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 - No gaps in the range
 - Fast, economic hardware implementation of integer arithmetic
 - Minimal number of transistors AND fast arithmetic, if possible

Sign & Magnitude

- Leftmost ("most significant") bit represents the sign of the integer
- Remaining bits to representation again the least of the l
- For n-bits, -(2ⁿ⁻¹-1) ≤ Sign & Magnitude ≤ +(2ⁿ⁻¹-1)
 https://powcoder.com
 Simplest for humans to understand
- Two representations of the representations of the representations of the representation of the re
- Costly to implement (need to compare signs and implement subtractors)

Bit Pattern	0000	0001	0010	0011	0100	0101	0110	0111	1000	1001	1010	1011	1100	1101	1110	1111
Unsigned	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Sign & Magnitude	+0	+1	+2	+3	+4	+5	+6	+7	-0	-1	-2	-3	-4	-5	-6	-7

One's Complement

- Negative numbers are the complement of the positive numbers
- -(2ⁿ⁻¹-1) ≤ Ansignment Projet € Exam Help
 - Same as Sign & Magnitude
- Less intuitive (for humans) than sign & Magnitude
- · Less costly to implement Chat powcoder
- Bit fiddly

Bit Pattern	0000	0001	0010	0011	0100	0101	0110	0111	1000	1001	1010	1011	1100	1101	1110	1111
Unsigned	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Sign & Magnitude	+0	+1	+2	+3	+4	+5	+6	+7	-0	-1	-2	-3	-4	-5	-6	-7
1s Complement	+0	+1	+2	+3	+4	+5	+6	+7	-7	-6	-5	-4	-3	-2	-1	-0

Two's Complement

- Negative of an integer is achieved by inverting each of the bits and adding 1 to it:
 - Two's complete of the feet of the signer of the signer
- -2ⁿ⁻¹ ≤ Two's comprehent ≤ 2 der com

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- Most useful property: X Y = X + (-Y)
 - No need for a separate subtractor (Sign & Magnitude) or carry-out adjustments (One's Complement)

Two's Complement

- Only one bit pattern for zero ©
 - Asymmetric one extra negative value

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 Minor disadvantage outweighed by the advantages https://powcoder.com

Bit Pattern	0000	0001	0010	001	de	We	Cl Pa	1 ⁶ 1 ⁶ 10	1000	od t	1010	1011	1100	1101	1110	1111
Unsigned	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Sign & Magnitude	+0	+1	+2	+3	+4	+5	+6	+7	-0	-1	-2	-3	-4	-5	-6	-7
1s Complement	+0	+1	+2	+3	+4	+5	+6	+7	-7	6	-5	-4	-3	-2	-1	-0
2s Complement	+0	+1	+2	+3	+4	+5	+6	+7	-8	-7	-6	-5	-4	-3	-2	-1

Excess-n (Bias-n) - Motivation

- Sorting in Two's complement is not easy
 - Assuming you could compare numbers it would always say negative numbers are greater !!!

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 Suppose we wanted to represent negative numbers, but wanted to keep the same ordering where 400 represents the smallest value and 111 represents the largest value in 3-bits?
 - This is the idea behind excess representation or biased representation
 - bitstring with N 0's maps to the smallest value and the bitstring with N 1's maps to the largest value

Excess-n (Bias-n)

- Using 3-bits as example, 3-bits gives us: 2³ = 8 values in total
 - · Assuming we start the hit Projection, Field -1, 0, 1, 2, 3
 - Smallest value = -4, so we shift by 4
 - Each value stored tisps: (pross cottler actual value → Excess-4 ⊕

A	Stored value	Actual value
	000	-4
	001	-3
	010	-2
	011	-1
	100	0
	101	1
	110	2
	111	3

Excess-n (Bias-n)

Bit Pattern	0000	0001	0010	•			0110	0111	1000		1010		1100	1101	1110	1111
Unsigned	0	1	2		4	5	Proj	91	8	9	10	11	12	13	14	15
Sign & Magnitude	+0	+1	+2	+ h	ttþs	:// ⁵ p	o₩c	ode	r.ec	om¹	-2	-3	-4	-5	-6	-7
1s Complement	+0	+1	+2	+3 A	‡4,	$\overset{\pm 5}{\mathrm{We}}$ e	Cha	+7 f n C	-7 W C	-6 Ode	-5 T	-4	-3	-2	-1	-0
2s Complement	+0	+1	+2	+3	+4	+5	+6	+7	-8	-7	-6	-5	-4	-3	-2	-1
Excess-8	-8	-7	-6	-5	-4	-3	-2	1	0	1	2	3	4	5	6	7

Binary Coded Decimal (BCD)

 Each decimal digit is represented by a fixed number of bits, usually four or eight

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- Easy for humans to understand https://powcoder.com
- Takes up much rache specenat powcoder
- Assuming 4-bits, the number 9876510 can be encoded as:

9	8	7	6	5	1	0
1001	1000	0111	0110	0101	0001	0000

Actual Binary: 10010110101010000011110 (24-bits)

Binary Coded Decimal (BCD)

Bit Pattern	0000	0001	0010	•	ı	I -	0110 D roi	0111	1000		1010	1011	1100	1101	1110	1111
Unsigned	0	1	2	2138	4	ent :	6	91	Exa	9	10	11	12	13	14	15
Sign & Magnitude	+0	+1	+2	+ h	ttps	:// ⁵ p	o₩c	ode	r.ec	ρħ	-2	-3	-4	-5	-6	-7
1s Complement	+0	+1	+2	+3 A	đđ	$\overset{\pm 5}{\mathbf{W}}\mathbf{e}$	Cha	+7 t n c	-7 WC	-6 OC	-5 T	-4	-3	-2	-1	-0
2s Complement	+0	+1	+2	+3	+4	+5	+6	+7	-8	-7	-6	-5	-4	-3	-2	-1
Excess-8	-8	-7	-6	-5	-4	-3	-2	1	0	1	2	3	4	5	6	7
BCD	0	1	2	3	4	5	6	7	8	9	-	-	-	-	-	-

Characters

- Characters are mapped to bit patterns
- · Common mapsinggement Asojean Exame Help

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- ASCII
 - Uses 7-bits (128 Medathers) hat powcoder
 - Most modern computer extend this to 8-bits yielding an extra 128 bit-patterns
 - 26 lowercase and uppercase letters, 10 digits, and 32 punctuation marks. Remaining 34 bit-patterns represent whitespace characters e.g. space (SP), tab (HT), return (CR), and special control characters

ASCII Character Set

Bit positions 654									
000	001	010	011	100	101	110	111	3210	
NUL	DLE	SP	0	@	Р	6	р	0000	
SOH	DC1	!	1	А	Q	а	q	0001	
STX	DC2	As [*] sig1	månt	Drogiac	t Elean	Llbln	r	0010	
ETX	DC3	W29181	mignt		t Egan	Ticip	S	0011	
EOT	DC4	\$	4	D	Т	d	t	0100	
ENQ	NAK	%	5 , ,	Ш	U	е	u	0101	
ACK	SYN	& n 1	tosa//o	OWCOO	er.con	1 f	V	0110	
BEL	ETB	6	7	G	W	g	W	0111	
BS	CAN	(8	Ι	Χ	h	Х	1000	
HT	EM) 🔥	dd 91/10	Chat p		lori	У	1001	
LF	SUB	* 1	dd W C	Charp	O VECO		Z	1010	
VT	ESC	+	,	K	[k	{	1011	
FF	FS	,	<	L	\	I		1100	
CR	GS	-	=	М]	m	}	1101	
SO	RS		>	Ν	٨	n	~	1110	
SI	US	/	?	0	_	0	DEL	1111	

Strings are represented as sequence of characters. E.g. **Fred** is encoded as follows:

English	F	r	е	d	
ASCII (Binary)	0100 0110	0111 0010	0110 0101	0110 0100	
ASCII (Hex)	46	72	65	64	

Unicode

- Newer, more complex standard
- Attempting to stiggide at probet for a series in a matter the language ©

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- Over 120,000 characters already defined Add WeChat powcoder
- First 65,536 (16-bit) characters cover the major alphabets of the world – more and more programming languages support this
- First 127 characters correspond to ASCII characters

Binary Experts now ©

