Computer Architecture

Tutorial 3 – Number Representation and Binary Arithmetic - Answers

1) Convert the following binary numbers to decimal:

(a) 0110 = 6, (b) 1011 = 11, (c) 10101010 = 170

- 2) Convert the following binary numbers to hexadecimal: (a) 1110 = E, (b) 11011 = 1B, (c) 1010111101110010 = AF72
- 3) Convert the following decimal numbers to binary and hexadecimal: (a) 12 = 1100 & C, (b) 27 = 11011 & 1B, (c) 96 = 1100000 & 60
- 4) For an 8-bit group, work out the representation for -37₁₀ in

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a) Sign & Magnitude

10100101

- b) One's Competteps://powcoder.com
- c) Two's Complement

11011011

- d) Excess-25 Add We Chat powcoder
- e) Excess-128

$$-37 = -37 + 128 = 91 = 01011011$$

5) Express 9876510 in Binary Coded Decimal

- 6) Form the negative equivalent of the following 8-bit Two's Complement numbers.
 - (a) 00011001, (b) 00011110, (c) 01101000, (d) 01110100
- (a) $00011001 = 16 + 8 + 1 = 25_{10}$

"invert the bits and add 1" 11100110 + 1 = 11100111

check: $11100111 = -128 + (64 + 32 + 4 + 2 + 1) = -25_{10}$

(b)
$$00011110 = 16 + 8 + 4 + 2 = 30_{10}$$

"invert the bits and add 1" 11100001 + 1 = 11100010

check:
$$11100010 = -128 + (64 + 32 + 2) = -30_{10}$$

(c)
$$01101000 = 64 + 32 + 8 = 104_{10}$$

"invert the bits and add 1" 10010111 + 1 = 10011000

check:
$$10011000 = -128 + (16 + 8) = -104_{10}$$

(d)
$$01110100 = 64 + 32 + 16 + 4 = 116_{10}$$

"invert the bits and add 1" 10001011 + 1 = 10001100 Assignment Project Exam Help check: 10001169 = -128 + (8 + 4) = -116 n

by comparing the resulting bit patterns to the originals, can you spot a "short cut" method for the conversion. // powcoder.com

Take another look at the bit patterns:

positive: 00011001 00011110 0101000 0111 1000 00011000 100011000 100011000

"starting from the rightmost bit (lsb), copy each bit unchanged up to and including the first 1 then invert all the remaining bits"

7) Perform the following 12-bit two's complement subtraction

Two's Complement subtraction: "negate the subtrahend and add"

Two's Complement negation: "invert the bits and add 1"

$$101100001101 = 010011110010 + 1 = 010011110011$$

1010 1010 1011 + 0100 1111 0011 ------1111 1001 1110 Check your answer by determining the decimal representation of the numbers and the result

$$1010\ 1010\ 1011 = -2048 + 683 = -1365$$

$$-1011\ 0000\ 1101 = -(-2048 + 781 = -1267)$$

$$-----$$

$$1111\ 1001\ 1110 = -2048 + 1950 = -98$$

8) Perform the binary multiplication 10011 x 1101

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11110111

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In decimal: $19 \times 13 = 247$

9) Divide the binary number 1011111 by 101 powcoder

In Decimal: 95 / 5 = 19