CS 61A Fall 2014

Structure and Interpretation of Computer Programs

Midterm 1

INSTRUCTIONS

- You have 2 hours to complete the exam.
- The exam is closed book, closed notes, closed computer, closed calculator, except one hand-written $8.5" \times 11"$ crib sheet of your own creation and the official 61A midterm 1 study guide attached to the back of this exam.
- Mark your answers ON THE EXAM ITSELF. If you are not sure of your answer you may wish to provide a brief explanation.

Last name Assignmen	t Project Exam Help
sid https://	powcoder.com
Login Add W TA & section time	VeChat powcoder
Name of the person to your left	
Name of the person to your right	
All the work on this exam is my own. (please sign)	

For staff use only

I of Staff also only					
Q. 1	Q. 2	Q. 3	Q. 4	Total	
/12	/14	/8	/6	/40	

1. (12 points) World Cup

(a) (10 pt) For each of the expressions in the tables below, write the output displayed by the interactive Python interpreter when the expression is evaluated. The output may have multiple lines.

Whenever the interpreter would report an error, write ERROR. You *should* include any lines displayed before an error.

Reminder: the interactive interpreter displays the value of a successfully evaluated expression, unless it is None.

The first three rows have been provided as examples.

Assume that you have started Python 3 and executed the following statements:

```
def square(x):
    return x * x

def argentina(n):
    print(n)
    if n > 0:
        return lambda k: k(n+1)
    else:
        return 1 / n

def gerAany nignment Project Exam Help
    print('hallo')
    if argentina(n-2) >= 0:
        print(|bye')
    return arghina S+2//powcoder.com
```

Expression	Interactive Output	Expression	Interactive Output
5*5	Add WeC	nat powcode	r
print(5)	5	_	
1/0	Error	argentina(1)(square)	
<pre>print(1, print(2))</pre>		germany(1)(square)	
argentina(0)		germany(2)(germany)	

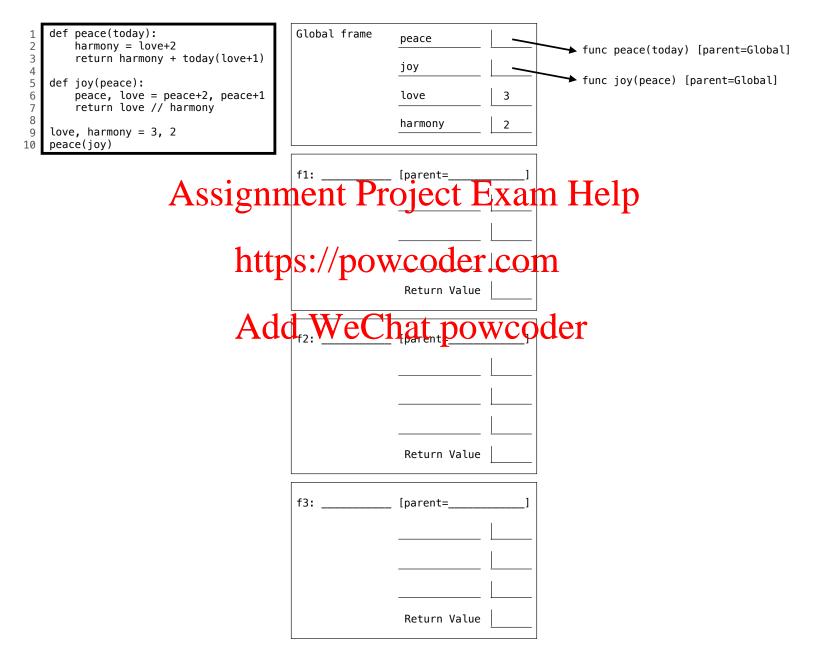
(b) (2 pt) Fill in the blank with an expression so that the whole expression below evaluates to a number. *Hint*: The expression abs > 0 causes a TypeError.

```
(lambda t: argentina(t)(germany)(square))(_____)
```

2. (14 points) Envy, Iron, Mint

- (a) (6 pt) Fill in the environment diagram that results from executing the code below until the entire program is finished, an error occurs, or all frames are filled. You may not need to use all of the spaces or frames.

 A complete answer will:
 - Add all missing names, labels, and parent annotations to all local frames.
 - Add all missing values created during execution.
 - Show the return value for each local frame.



- (b) (8 pt) Fill in the environment diagram that results from executing the code below until the entire program is finished, an error occurs, or all frames are filled. You may not need to use all of the spaces or frames.

 A complete answer will:
 - Add all missing names, labels, and parent annotations to all local frames.
 - Add all missing values created during execution.
 - Show the return value for each local frame.

<pre>def k(g, b): def n(s, a): return g-p return b(n(b, p)) g, p = 3, 7 k(p+1, lambda s: g+3)</pre>	Global frame	k
Ass		t Project Exam Help
	https://j	powcoder.com
	Add W	eChat powcoder
		Return Value
	f3:	[parent=]
		Return Value

3. (8 points) Express Yourself

return total

(a) (3 pt) A k-bonacci sequence starts with K-1 zeros and then a one. Each subsequent element is the sum of the previous K elements. The 2-bonacci sequence is the standard Fibonacci sequence. The 3-bonacci and 4-bonacci sequences each start with the following ten elements:

```
n: 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, ...
kbonacci(n, 2): 0, 1, 1, 2, 3, 5, 8, 13, 21, 35, ...
kbonacci(n, 3): 0, 0, 1, 1, 2, 4, 7, 13, 24, 44, ...
kbonacci(n, 4): 0, 0, 0, 1, 1, 2, 4, 8, 15, 29, ...
```

positive integer k and returns element n of a k-bonacci sequence.

```
Fill in the blanks of the implementation of kbonacci below, a function that takes non-negative integer n and
def kbonacci(n, k):
   """Return element N of a K-bonacci sequence.
   >>> kbonacci(3, 4)
   >>> kbonacci(9, 4)
       ssignment Project Exam Help
   >>> kbonacci(8, 2)
           https://powcoder.com
      Add WeChat powcoder
   elif n == k - 1:
      return 1
   else:
      total = 0
      while i < n:
          total = total + ______
          i = i + 1
```

(b) (5 pt) Fill in the blanks of the following functions defined together in the same file. Assume that all arguments to all of these functions are positive integers that do not contain any zero digits. For example, 1001 contains zero digits (not allowed), but 1221 does not (allowed). You may assume that reverse is correct when implementing remove.

```
reverse is correct when implementing remove.
def combine(left, right):
    """Return all of LEFT's digits followed by all of RIGHT's digits."""
    factor = 1
    while factor <= right:
        factor = factor * 10
    return left * factor + right
def reverse(n):
    """Return the digits of \ensuremath{\mathbb{N}} in reverse.
    >>> reverse(122543)
    345221
    if n < 10:
         ssignment Project Exam Help
        return_combine(__
             https://powcoder.com
def remove(n, digit):
    """Return all digits of N that are not DIGIT, for DIGIT less than 10.
                      WeChat powcoder
    >>> remove(243132, 2)
    4313
    >>> remove(remove(243132, 1), 2)
    433
    11 11 11
    removed = 0
    while n != 0:
```

return reverse (removed)

- 4. (6 points) Lambda at Last
- (a) (2 pt) Fill in the blank below with an expression so that the second line evaluates to 2014. You may only use the names two_thousand, two, k, four, and teen and parentheses in your expression (no numbers, operators, etc.).

```
two_thousand = lambda two: lambda k:
two_thousand(7)(lambda four: lambda teen: 2000 + four + teen)
```

Assignment Project Exam Help

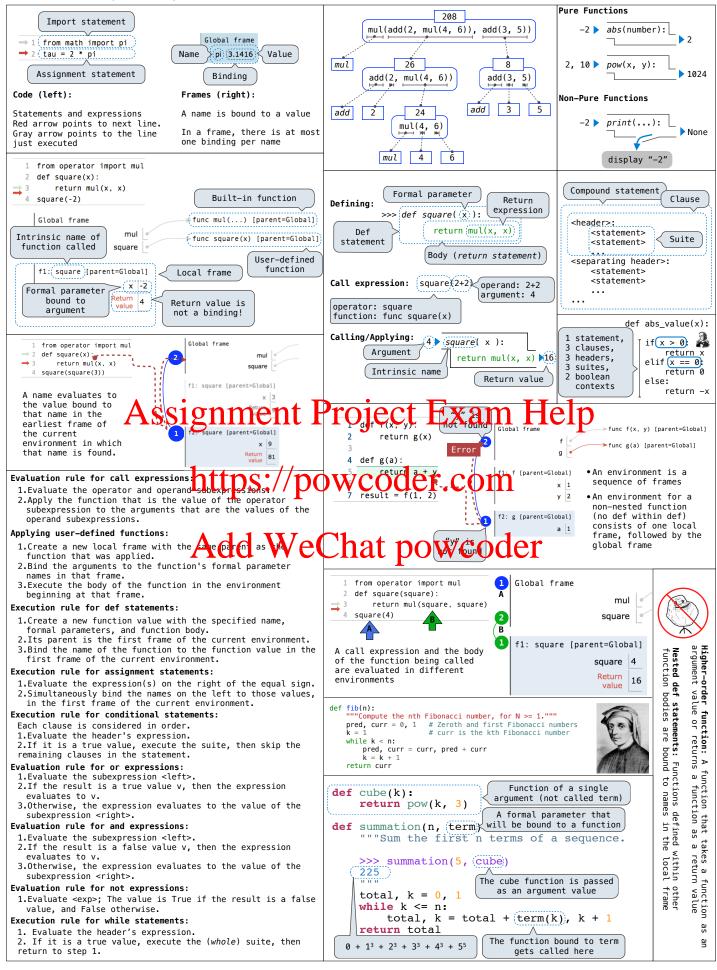
(b) (4 pt) The if_fn returns a two-argument function that can be used to select among alternatives, similar to an if statement. Filting turn expression (record to to that it specified correctly for non-negative arguments. You may only use the names if_fn, condition, a, b, n, factorial, base, and recursive and parentheses in your expression (no numbers, operators, etc.).

Assignment Project Exam Help https://powcoder.com Add WeChat powcoder

Scratch Paper

Assignment Project Exam Help https://powcoder.com Add WeChat powcoder

Assignment Project Exam Help https://powcoder.com Add WeChat powcoder



 $grow = lambda n: f_then_g(grow, print, n//10)$

shrink = lambda n: f_then_g(print, shrink, n//10)

1

```
def square(x):
                                                                                                                  VS
                                                                                 square = lambda x: x * x
 square = \frac{x,y}{x * y}
                                                                                                                                return x * x
                                  Evaluates to a function.
                                    No "return" keyword!
                                                                               • Both create a function with the same domain, range, and behavior.
           A function
               with formal parameters x and y
                                                                               • Both functions have as their parent the environment in which they
                     that returns the value of "\times \times y,"
                                                                               · Both bind that function to the name square.
                  Must be a single expression
                                                                               • Only the def statement gives the function an intrinsic name.
                       A function that returns a function
def make_adder(n):
        'Return a function that takes one argument k and returns k + n.
                                                                               When a function is defined:
    >>>(add_three = make_adder(3))
                                          The name add three is

    Create a function value: func <name>(<formal parameters>)

                                           bound to a function
                                                                               2. Its parent is the current frame.
     7
                              A local
                                                                                        f1: make_adder
                                                                                                               func adder(k) [parent=f1]
    def adder(k):
                           def statement
         return k +(n)
                                                                               3. Bind <name> to the function value in the current frame
                                                                                   (which is the first frame of the current environment).
                           Can refer to names in
     return adder
                          the enclosing function
                                                                               When a function is called:
                                                                                1. Add a local frame, titled with the <name> of the function being
• Every user-defined function has
                                                                                   called.
  a parent frame
                                                                                   Copy the parent of the function to the local frame: [parent=<label>]
 • The parent of a function is the

    Bind the <formal parameters> to the arguments in the local frame.
    Execute the body of the function in the environment that starts with

  frame in which it was defined
                                               A function's signature
 • Every local frame has a parent
                                                                                   the local frame.
                                               has all the information
  frame
                                               to create a local frame
 • The parent of a frame is the
  parent of the function called
                                3
                                    Global frame
                                                                 func make adder(n) [parent=Global]
                                                                                                    def fact(n):
                                              make_adder
                                                                                                        if n == 0:
   1 def make_adder(n):
                                                               func adder(k) [parent=f1]
                                                add_three
                                                                                                             return 1
     def adder(k):
return k + n
                                                                                                         else:
 Nested
                                     f1: make_adder [parent=G]
         return adder
                                                                                                             return n * fact(n-1)
  def
   6 add_three = make_adder(3)
                                                   adder
                                                                                                  7 fact(3)
   7 add_three(4)
                                                  Return
                                                                                                                                 func fact(n) [parent=Global]
                                                                                 ect
                                                                                               f1: fact [parent=Global]
 def curry2(f):
       ""Returns a function g such that
     def g(x):
         def h(y):
                               Currying: Transforming a multi-argument function into a single-argument,
             return f(x, y)
         return h
                                higher-order function.
     return q
                                                                                               f3: fact [parent=Global]
 Anatomy of a recursive function:
                                                                             at powco
 • The def statement header is similar to
                                                                                                f4: fact [parent=Global]

    Conditional statements check for base cases

    Base cases are evaluated without recursive calls

                                                                                                                   n 0

    Recursive cases are evaluated with recursive calls

                                                                                                               Return 1
 def sum digits(n):
  """Return the sum of the digits of positive integer n.""" if \frac{n}{l} < 10 \colon
       return n
                                                                                            Is fact implemented correctly?
   else:
                                                                                                  Verify the base case.
       all_but_last, last = n // 10, n % 10
                                                                                                  Treat fact as a functional abstraction!
                                                                                            2.
       return sum_digits(all_but_last) + last
                                                                                            3.
                                                                                                  Assume that fact(n-1) is correct.
                                                                                                  Verify that fact(n) is correct.
                                                                                            4.
                                                                                                  assuming that fact(n-1) correct.
                          Global frame
   def cascade(n):
                                                    >> func cascade(n) [parent=Global]
       if n < 10:
                                       cascade e
          print(n)
       else:
                          f1: cascade [parent=Global] * Each cascade frame is n \mid_{123} from a different call
          print(n)
                                         n 123
           cascade(n//10)
                                                  to cascade.

    Recursive decomposition:

                                                                                                                 def count_partitions(n, m):
          print(n)
                          f2: cascade [parent=Global]
                                                                                 finding simpler instances of
                                                • Until the Return value
                                                                                                                     if n == 0:
                                        n 12
                                                                                 a problem.
                                                                                                                         return 1
                                                 appears, that call has not completed.
  9 cascade(123)
                                      Return
value None
                                                                               E.g., count_partitions(6, 4)
                                                                                                                     elif n < 0:
                                                                               Explore two possibilities:Use at least one 4
                                                                                                                         return 0
Program output:
Any statement can
                                                                                                                     elif m == 0:
                                                  appear before or after
                                                                                 Don't use any 4
                                                                                                                         return 0
1 12
                                                                               Solve two simpler problems:count_partitions(2, 4)
                                                  the recursive call.
                                      Return
value None
                                                                                                                     else:
                                                                                                                     with_m = count_partitions(n-m, m)
                                                                                  count_partitions(6, 3)
                                                                                                                         without_m = count_partitions(n, m-1)
                                                                               • Tree recursion often involves
                                                                                                                          return with_m + without_m
                                                                                exploring different choices.
                                             n: 0, 1, 2, 3, 4, 5, 6, 7, 8,
           def inverse_cascade(n):
1
                                        fib(n): 0, 1, 1, 2, 3, 5, 8, 13, 21,
               grow(n)
                                                                               from operator import floordiv, mod
12
               print(n)
                                                                                def divide exact(n, d):
                                       def fib(n):
    if n == 0:
                shrink(n)
                                                                                    """Return the quotient and remainder of dividing N by D.
123
                                            if n == 0:
return 0
elif n == 1:
           def f_then_g(f, g, n):
1234
                                                                                    >>> (q, r = divide\_exact(2012, 10)) < Multiple assignment
                if n:
                                                return 1
                                                                                    >>> 'q
                                                                                                                                to two names
123
                                            else:
return fib(n-2) + fib(n-1)
                    f(n)
                                                                                    201
                    q(n)
                                                                                    >>> r
12
```

000

return floordiv(n, d), mod(n, d) <

Multiple return values,

separated by commas