CS 61A Spring 2015

Structure and Interpretation of Computer Programs

FINAL EXAM SOLUTIONS

INSTRUCTIONS

- You have 3 hours to complete the exam.
- The exam is closed book, closed notes, closed computer, closed calculator, except one hand-written $8.5" \times 11"$ crib sheet of your own creation and the 3 official 61A midterm study guides attached to the back of this exam.
- Mark your answers ON THE EXAM ITSELF. If you are not sure of your answer you may wish to provide a brief explanation.

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All the work on this exam is my own. (please sign)	

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Q. 1	Q. 2	Q. 3	Q. 4	Q. 5	Q. 6	Total	
/1.0	/- 4	10	/10	/- 4	/10	100	
/16	/14	/8	/18	/14	/10	/80	

THIS PAGE CONTAINS NO QUESTIONS

For your reference, a complete implementation of the Tree class appears below.

```
class Tree:
   """A tree with entry as its root value.
   >>> Tree(1)
   Tree(1)
   >>> Tree(1, [])
   Tree(1)
   >>> Tree(Tree(1))
   Tree(Tree(1))
   >>> t = Tree(1, [Tree(2), Tree(3)])
   >>> t
   Tree(1, [Tree(2), Tree(3)])
   >>> t.entry
   1
   >>> t.branches
    [Tree(2), Tree(3)]
   def __init__(self, entry, branches=()): selfArSSI-genment Project Exam Help
        for branch in branches:
            assert isinstance(branch, Tree)
        self.branches = list(branches)
                               powcoder.com
   def __repr__(self):
        if self.branches:
           branches_str = ', ' + re
                               + repr(self.branches)
                                     hat powcoder
        return 'Tree({0}{1})'.format(self.entry, branches_str)
```

1. (16 points) Lumberjack

For each row below, fill in the blanks in the output displayed by the interactive Python interpreter when the expression is evaluated. Expressions are evaluated in order, and expressions may affect later expressions.

Whenever the interpreter would report an error, write ERROR. You *should* include any lines displayed before an error. *Reminder*: The interactive interpreter displays the **repr** string of the value of a successfully evaluated expression, unless it is **None**. The first two rows are completed for you.

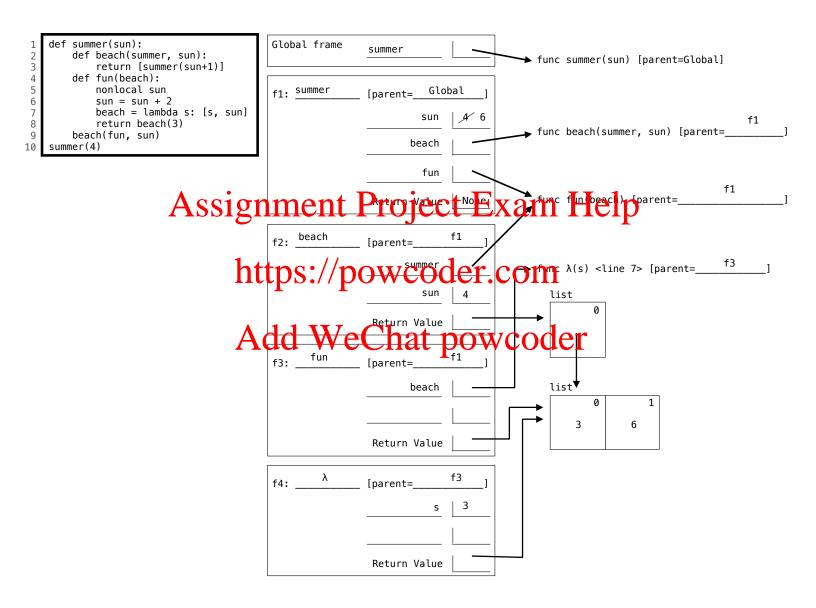
The Tree class appears on the previous page. It's also on the Midterm 2 Study Guide, but the exam version is complete. Assume you have started Python 3, executed the Tree class statement, then executed the following:

Expression	Output
Tree(2, [Tree(3)])	rehat by wooder
1/0 Aud VV	PRICE POWCOUCE
<pre>tuple(map(odd, filter(big, range(5))))</pre>	(True, False)
	1
<pre>sum(filter(f(big)(print), range(1, 5)))</pre>	2
	3
lumber	Tree(Tree(2))
jack.branches	[Tree(2), Tree(2)]
<pre>print(choose([1], big))</pre>	None
print(oncode([i], big//	Note
-1([0 2 4] -11)	m/4 [m//\]\
choose([2, 3, 4], odd)	Tree(1, [Tree(4)])
choose([4, 3, 2], f(big)(odd))	Tree(2)
Wood(Tree(2))	Tree(Tree(3)))

2. (14 points) Hot and Cold

- (a) (8 pt) Fill in the environment diagram that results from executing the code below until the entire program is finished, an error occurs, or all frames are filled. You may not need to use all of the spaces or frames.

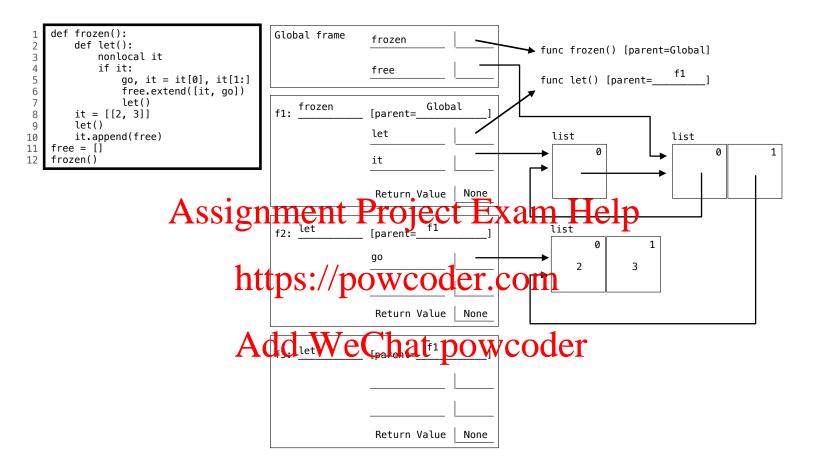
 A complete answer will:
 - Add all missing names and parent annotations to all local frames.
 - Add all missing values created during execution.
 - Show the return value for each local frame.



(b) (6 pt) Fill in the environment diagram that results from executing the code below until the entire program is finished, an error occurs, or all frames are filled. You may not need to use all of the spaces or frames. Examples of using the append and extend methods of lists appear on the Midterm 2 Study Guide.

A complete answer will:

- Add all missing names and parent annotations to all local frames.
- Add all missing values created during execution.
- Show the return value for each local frame.



3. (8 points) Team Stream

```
When you complete all the questions on this page, all of the doctests of append should pass.
```

```
def append(s, t):
    """Return a stream with the elements of s followed by the elements of t.
    >>> bits = Stream(0, lambda: Stream(1))
                                                # 0, 1
    >>> taipei = append(bits.rest, bits)
                                                # 1, 0, 1
    >>> taipei.first, taipei.rest.first, taipei.rest.rest.first
    (1, 0, 1)
                                                # 0, 1, 0, (1), 0, ...
    >>> repeat(bits).rest.rest.rest.first
    >>> repeat(bits).rest.rest.rest.rest.first # 0, 1, 0, 1, (0), ...
    >>> ten = unique(taipei) # 1, 0
    >>> ten.first, ten.rest.first, ten.rest.rest
    (1, 0, Stream.empty)
    11 11 11
    if s is Stream.empty:
        return t
    return Stream(s.first, lambda: append(s.rest, t))
```

(a) (2 pt) Imperial regard of the Stream class. It returns an infinite stream that cycles through the elements of s in order. You may use the append function.

```
def repeat(s):

"""Return https://powcificely.com the elements of s."""

return Stream(s.first,
```

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(b) (2 pt) Implement unique, which takes a finite stream that is either Stream.empty or a Stream instance. It returns a stream of the unique elements in s. filter_stream appears on the Final Study Guide.

```
def unique(s):
    """Return a stream of the unique elements of s in the order that they
    first appear in s. The result contains no repeated elements."""

if s is Stream.empty:
    return s

t = filter_stream(lambda x: x != s.first, s.rest)

return Stream(s.first, lambda: unique(t))
```

(c) (2 pt) Circle all Θ expressions below that describe the total number of elements in the stream append(s, t) for a finite stream s of length m and a finite stream t of length n.

```
\Theta(1) \Theta(m) \Theta(m+n) \Theta(m*n)
```

(d) (2 pt) Circle all Θ expressions below that describe the total number of function calls required to evaluate append(s, t) for a finite stream s of length m and a finite stream t of length n.

```
\Theta(1) \Theta(m) \Theta(m+n) \Theta(m*n)
```

4. (18 points) Apply That Again

(a) (4 pt) Implement amplify, a generator function that takes a one-argument function f and a starting value x. The element at index k that it yields (starting at 0) is the result of applying f k times to x. It terminates whenever the next value it would yield is a false value, such as 0, '', [], False etc.

```
def amplify(f, x):
    """Yield the longest sequence x, f(x), f(f(x)), ... that are all true values.

>>> list(amplify(lambda s: s[1:], 'boxes'))
['boxes', 'oxes', 'xes', 'es', 's']
>>> list(amplify(lambda x: x//2-1, 14))
[14, 6, 2]
    """

while x:
    yield x
    x = f(x)
```

(b) (6 pt) Answer the following three questions about the echo function below, which you should try to understand by reading its implementation Assure that amplify implemented correctly.

```
ef echo():
    x = 0
    def gecko(y):
        nonlochttps://powcoder.com
        x = x + 1
        return y - x
    return gecko
```

Circle the value of enacted (We Chat powcoder

1 2 3 4 5

Circle all values of n below for which the expression list(amplify(echo(), n)) terminates.

5 10 15 20 25

Write the largest integer n less than 40 for which the expression list(amplify(echo(), n)) terminates

- ***Definition***: A shrinking function f is a function for which f(x) < x for all positive integers x. In addition, for any x, applying f a finite number of times will result in a number less than or equal to f.
- (c) (4 pt) Implement near_zero, which takes a shrinking function f and a positive starting number x. It returns the smallest positive value that results from applying f to x zero or more times. Assume that amplify (previous page) is implemented correctly. You may use it in your solution.

```
def near_zero(f, x):
    """Return the value nearest zero obtained by repeatedly applying the
    shrinking function f to a non-zero number x.

>>> [near_zero(lambda x: x-4, k) for k in [3, 4, 5, 6, 7, 8, 9]]
    [3, 4, 1, 2, 3, 4, 1]
    """

last = x

for v in amplify(f, x):

if v < 0:</pre>
```

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last = v

return lashttps://powcoder.com

(d) (4 pt) Implement count_sums which counts the number of ways that a positive integer n can be partitioned into a subset of the positive values m, f(m), f(f(m)), ... for a shrinking function f. No negative values or repeated values can be included in the sum.

def count_sums Add (dn): We Chat powcoder

"""Return the number of ways that n can be partitioned into unique positive values obtained by applying the shrinking function f repeatedly to m.

```
>>> count_sums(6, lambda k: k-1, 4) # 4+2, 3+2+1
2
>>> count_sums(12, lambda k: k-2, 12) # 12, 10+2, 8+4, 6+4+2
4
>>> count_sums(11, lambda k: k//2, 8) # 8+2+1
1
"""
if n == 0:
    return 1
elif m <= 0 or n < 0:
    return 0
else:
    yes = count_sums(n-m, f, f(m))

    no = count_sums(n, f, f(m))</pre>
```

5. (14 points) Treasure Hunt

(a) (4 pt) Leaprechauns leap from one pot-o'-gold to the next, collecting treasure. However, they can't collect two adjacent pots. Implement leap, which takes a list of pots. It returns the maximal sum of values in pots that doesn't include two adjacent pot values. Hint: sum([]) is 0, sum([2]) is 2, and max(3, 4) is 4.

```
def leap(pots):
    """Return the maximal value of collecting pots that are not adjacent.

>>> leap([2, 4, 3]) # Collect 2 and 3
5
>>> leap([4, 20, 9, 3, 6, 2]) # Collect 20 and 6
26
    """
if len(pots) <= 1:
    return sum(pots)

return max(pots[0] + leap(pots[2:]), leap(pots[1:]))</pre>
```

- (b) (6 pt) The *Leap* rechaum Ida Clare declares, "Let's use a declarative language!" The pots table contains indexed pot values. A path is a comma-separated list of values from pots, ordered by their places.
 - **A path cannot contain values from diagent places.

 Implement a select statement characteristic by the black that the maximal path through pots. The second column should contain the total value of the maximal path. Your solution should provide the correct result even if the contents of the pots table were to change.

```
create table phttaps.
  select 1
                     20
  select 2
                                    t powcoder
  select 3
  select 4
  select 5
with
  paths(path, last, total) as (
    select value, place, value from pots union
    select path || ", " || value, place, total + value
        from paths, pots
        where place - last > 1
  )
select path, max(total) from paths;
-- Expected result:
     20,6|26
```

(c) (4 pt) Higher-order Leaprechauns can collect any pots they wish, but get a bonus when they jump over some pots. They always take the first pot before jumping. Implement gather, which takes a list of pots and a function bonus(k) that returns the bonus for jumping over exactly k pots. gather returns the maximum total gold plus bonus that is possible to attain, along with a linked list of the pot values collected. The Link class appears on the Midterm 2 Study Guide.

```
def gather (pots, bonus):
   """Return the maximum total value of pots gathered *plus* jump bonuses.
   Also return a linked list of pot values gathered to reach this total.
   >>> gold = [4, 20, 9, 3, 6, 2]
   >>> gather (gold, lambda k: 0) # No jumping bonus, so gather everything
   (44, Link(4, Link(20, Link(9, Link(3, Link(6, Link(2)))))))
   >>> hop = lambda k: [0, 10, 0, 0, 0, 0, 0][k]
   >>> gather(gold, hop) # Jump 0, Jump 1 (+10), Jump 1 (+10) to end
   (59, Link(4, Link(20, Link(9, Link(6)))))
   >>> leap = lambda k: [0, 0, 30, 20, 0, 0, 0, 0][k]
   >>> gather(gold, leap) # Jump 2 (+30), Jump 2 to end (+30)
   (67, Link(4, Link(3)))
     Assignment Project Exam Help
   if pots == []:
```

return https://powcoder.com

def total (kA:dd WeChat powcoder

```
return pots[0] + bonus(k) + gather(pots[k+1:], bonus)[0]
best = max(range(len(pots)), key=total)
rest = gather(pots[best+1:], bonus)[1]
return total(best), Link(pots[0], rest)
```

6. (10 points) SQL in Scheme

A SQL-like table can be implemented in Scheme as a list of lists. The first element of a table is a list of column names. Each subsequent element is a list of values in a row. (*Note*: The semicolon line is just a comment.)

```
scm> (define cafes (list
    '(cafe item )
; -----
'(nefeli espresso)
'(nefeli bagels )
'(fsm coffee )
'(fsm bagels )
'(fsm espresso)))
```

(a) (2 pt) The get procedure takes a symbol column, a list of columns and a list of values. It returns the value at the same index that column appears in columns. Assume that column appears within columns.

```
scm> (get 'cafe '(cafe item) '(nefeli bagels))
nefeli
scm> (get 'item '(cafe item) '(nefeli bagels))
bagels
```

Cross out whole lines below so that get is implemented to match the examples above.

```
; Get an SSI-GIAMONT by mrole Ctime Xamel and p columns (define (get column columns values) (if (equal? column (car columns)) (car values) (get column (GS: columns))
```

(b) (2 pt) The insert procedure takes a key, a value, and a list of groups. A group is a list that begins with a key, followed by values. The insert procedure returns an updated list of groups with value added to the beginning of the group forker. Here is not have proper the group scaded to the end.

```
scm> (insert 'b 5 nil)
((b 5))
scm> (insert 'a 1 (insert 'b 2 (insert 'a 3 (insert 'c 4 (insert 'b 5 nil)))))
((b 2 5) (c 4) (a 1 3))
```

Cross out whole lines below so that insert is implemented to match the examples above.

The following procedure is implemented correctly for you as a reference.

```
(define (map fn s) (if (null? s) s (cons (fn (car s)) (map fn (cdr s)))))
```

(c) (3 pt) Implement from, a procedure that takes a table (e.g., cafes) and returns a list of row procedures. A row procedure represents a row; it takes a column name and returns the value for that column in the row.

```
scm> (define first-row (car (from cafes))) ; first-row is a procedure
first-row
scm> (first-row 'cafe)
nefeli
scm> (first-row 'item)
espresso
```

You may use get, map, and list manipulation procedures such as car, cdr, cons, and list. You may only use lambda and call expressions. No other special forms (such as if) are allowed.

The following procedure is implemented correctly for you, but you must discover its behavior and purpose.

(d) (3 pt) Implement spect, yield takes the results of calling from and group-by. It returns a list of two-element lists, which each contain a group key and a list of column values.

```
scm> (select 'item (from cafes) (group-by 'cafe))
((nefeli (bagel espress)) (from (espresso bagels coffee)))
scm> (select 'cafe (from cafes) (group by 'item))
((espresso (fsm nefeli)) (bagels (fsm nefeli)) (coffee (fsm)))
```

You may use the map procedure, as well as list manipulation procedures such as car, cdr, cons, and list. You may only use lambda and call expressions. No other special forms (such as if) are allowed.