Midterm 2 Review

October 13, 2017

Instructions

Form a small group. Start on the first problem. Check off with a helper or discuss your *solution process* with another group once everyone understands how to solve the first problem and then repeat for the second problem ...

You may not move to the next problem until you check off or discuss with another group and everyone understands why the solution is what it is. You may use any course resources at your disposal: the purpose of this review session is to have everyone learning together as a group.

0.1 What would Python display?

1 Lists & Tree AddsiWeChat powcoder

Mutative (*destructive*) operations change the state of a list by adding, removing, or otherwise modifying the list itself.

- lst.append(element)
- lst.extend(lst)
- lst.pop(index)
- lst += lst (not lst = lst + lst)
- lst[i] = x
- lst[i:j] = lst

Non-mutative (non-destructive) operations include the following.

- lst + lst
- lst * n
- lst[i:j]
- list(lst)

Recall: To execute assignment statements,

- Evaluate all expressions to the right of the = sign
- Bind all names to the left of the = to those resulting values

The Golden Rule of Equals describes how this rule behaves with composite values. *Composite values*, such as functions and lists, are connected by a pointer. When an expression evaluates to a composite value, we are returned the pointer to that value, rather than the value itself.

In an environment diagram, we can summarize this rule with,

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- 1.1 Write a list comprehension that accomplishes each of the following tasks.

[x ** 2 for x in 1st]

(b) Compute the dot product of two lists 1st1 and 1st2 P_{Hint} : The dot product is defined as $lst1[0] \cdot lst2[0] + lst1[1] \cdot lst2[1] + ... + lst1[n] \cdot lst2[n]$. The Python **zip** function may be useful here.

```
sum([x * y for x, y in zip(lst1, lst2)])
```

(c) [[0], [0, 1], [0, 1, 2], [0, 1, 2, 3], [0, 1, 2, 3, 4]]

```
[[x for x in range(y)] for y in range(1, 6)]
```

(d) Return the same list as above, except now excluding every instance of the number 2: [[0], [0, 1], [0, 1], [0, 1, 3], [0, 1, 3, 4]].

```
[[x for x in range(y) if x != 2] for y in range(1, 6)]
```

1.2 Draw the environment diagram that results from running the following code.

```
pom = [16, 15, 13]
   pompom = pom * 2
   pompom.append(pom[:])
   pom.extend(pompom)
   https://goo.gl/ZU1V7h
1.3 Draw the environment diagram that results from running the following code.
   bless, up = 3, 5
   another = [1, 2, 3, 4]
   one = another[1:]
   another[bless] = up
   another.append(one.remove(2))
   another[another[0]] = one
   one[another[0]] = another[1]
   one = one + [another.pop(3)]
another[1] = one Signment Project Exam Help
   one.append([one.pop(1)])
   https://goo.gl/FyMmbJ https://powcoder.com
1.4 def jerry(jerry):
       def jerome(alex):
           alex.append(jerry, dd WeChat powcoder
           return alex
       return jerome
   ben = ['nice', ['ice']]
   jerome = jerry(ben)
   alex = jerome(['cream'])
   ben[1].append(alex)
   ben[1][1][1] = ben
   print(ben)
   https://goo.gl/uhSClr
```

1.5 Implement $subset_sum$, which takes in a list of integers and a number k and returns whether there is a subset of the list that adds up to k? *Hint*: The **in** operator can determine if an element belongs to a list.

```
def subset_sum(seq, k):
    """
    >>> subset_sum([2, 4, 7, 3], 5)  # 2 + 3 = 5
    True
    >>> subset_sum([1, 9, 5, 7, 3], 2)
    False
    """

    if len(seq) == 0:
        return False
    elif k in seq:
        return True
    else:
        return Aubset sum(seq): Projecte Exami Help

2 Trees
        https://powcoder.com

def tree(label, branches=[]):
```

2 Trees
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def tree(label, branches=[]):
 return [label] + list(branches)
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def label(tree):
 return tree[0]

def branches(tree):
 return tree[1:]

2.1 A min-heap is a tree with the special property that every node's value is less than or equal to the values of all of its branches.



Implement is_min_heap which takes in a tree data abstraction and returns whether the tree satisfies the min-heap property or not.

```
def is_min_heap(t):
    for b in branches(t):
        if label(t) > label(b) or not is_min_heap(b):
            return False
    return True
```

3 Growth

3.1 Give a tight asymptotic gatime bound for the following functions in Help notation, or "Infinite" if the program does not terminate.

```
(a) def one(n): https://powcoder.com

n = n // 2

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```

(b) def two(n)

```
(b) def two(n):
    for i in range(n):
        for j in range(i):
            print(str(i), str(j))

Θ(n²)

(c) def three(n):
    i = 1
    while i <= n:
        for j in range(i):
            print(j)
        i *= 2</pre>
```

4 Nonlocals & OOP

4.1 Draw the environment diagram that results from running the code.

```
def campa(nile):
    def ding(ding):
        nonlocal nile
        def nile(ring):
            return ding
    return nile(ding(1914)) + nile(1917)

ring = campa(lambda nile: 103)

https://goo.gl/G1Kmbw
```

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4.2 Implement the classes so that the code to the right runs.

```
class Plant:
   def __init__(self):
       self.leaf = Leaf(self)
       self.materials = []
       self.height = 1
   def absorb(self):
       self.leaf.absorb()
   def grow(self):
       for sugar in self.materials:
           sugar.activate()
           self.height += 1
class Leaf:
               ssignment Project Exam Help
       self.sugars_used = 0
       self.plant = phttps://powcoder.com
   def absorb(self):
                                                                >>> p = Plant()
                                                               🗪 p.height
                                                                >>> p.materials
   def __repr__(self):
                                                                return 'Leaf'
                                                                >>> p.absorb()
                                                                >>> p.materials
class Sugar:
                                                                [Sugar]
   sugars_created = 0
                                                                >>> Sugar.sugars_created
   def __init__(self, leaf, plant):
                                                                >>> p.leaf.sugars_used
       self.leaf = leaf
       self.plant = plant
                                                                >>> p.grow()
       Sugar.sugars_created += 1
                                                                >>> p.materials
                                                                def activate(self):
                                                                >>> p.height
       self.leaf.sugars_used += 1
                                                                2
       self.plant.materials.remove(self)
                                                                >>> p.leaf.sugars_used
   def __repr__(self):
       return 'Sugar'
```

5 Exam Preparation Extra Practice

5.1 Implement slice_reverse which takes a linked list s and mutatively reverses the elements on the interval, [i,j) (including i but excluding j). Assume s is zero-indexed, i > 0, i < j, and that s has at least j elements.

```
def slice_reverse(s, i, j):
   >>> s = Link(1, Link(2, Link(3)))
   >>> slice_reverse(s, 1, 2)
   >>> s
   Link(1, Link(2, Link(3)))
   >>> s = Link(1, Link(2, Link(3, Link(4, Link(5)))))
   >>> slice_reverse(s, 2, 4)
   >>> s
   Link(1, Link(2, Link(4, Link(3, Link(5)))))
   start = sAssignment Project Exam Help
    \begin{array}{c} \text{for $\_$ in $range(i$ $^-$ 1):$} \\ \text{$https://powcoder.com} \end{array} 
       start = start.re
   reverse = Link.emptAdd WeChat powcoder
   current = start.rest
   for _ in range(j - i):
       rest = current.rest
       current.rest = reverse
       reverse = current
       current = rest
   start.rest.rest = current
   start.rest = reverse
```

5.2 A Binary Search Tree is a tree where each node contains either 0, 1, or 2 nodes and where the left branch (if present) contains values *strictly less than* (<) the root value, and the right branch (if present) contains values *strictly greater than* (>) the root value. The definition is recursive: both the left and right branches must also be BSTs for the entire tree to be a BST.

Implement is_binary which that takes in a Tree t, and returns True if t is a Binary Search Tree and False otherwise. Trees can contain any number of branches, but if a tree contains only one branch, interpret it as a left branch.

- 5.3 Give a tight asymptotic runtime bound for the following scenarios in $\Theta(\cdot)$ notation, or "Infinite" if the program does not terminate. Assume the implementation of is_binary is optimal.
 - (a) is_binary on a well-formed binary search tree with n nodes.

 $\Theta(n)$

(b) is_binary on a tree where each node contains 3 branches and the overall height of the tree is n.

 $\Theta(1)$