CS 61A Fall 2014

Structure and Interpretation of Computer Programs

FINAL EXAM

INSTRUCTIONS

- You have 3 hours to complete the exam.
- The exam is closed book, closed notes, closed computer, closed calculator, except one hand-written $8.5" \times 11"$ crib sheet of your own creation and the 3 official 61A midterm study guides attached to the back of this exam.
- Mark your answers ON THE EXAM ITSELF. If you are not sure of your answer you may wish to provide a brief explanation.

Last name Assignmen	t Project Exam Help
sid https://	powcoder.com
Login Add W TA & section time	VeChat powcoder
Name of the person to your left	
Name of the person to your right	
All the work on this exam is my own. (please sign)	

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Q. 1	Q. 2	Q. 3	Q. 4	Q. 5	Q. 6	Total
/1.4	/10	/10	/10	/10	/0	/00
/14	/16	/12	/12	/18	/8	/80

1. (14 points) Representing Scheme Lists

For each row below, write the output displayed by the interactive Python interpreter when the expression is evaluated. Expressions are evaluated in order, and **expressions may affect later expressions**.

Whenever the interpreter would report an error, write ERROR. You *should* include any lines displayed before an error. *Reminder*: The interactive interpreter displays the **repr** string of the value of a successfully evaluated expression, unless it is **None**.

The Pair class from Project 4 is described on your final study guide. Recall that its <code>__str__</code> method returns a Scheme expression, and its <code>__repr__</code> method returns a Python expression. The full implementation of Pair and nil appear at the end of the exam as an appendix. Assume that you have started Python 3, loaded Pair and nil from <code>scheme_reader.py</code>, then executed the following:

```
blue = Pair(3, Pair(4, nil))
gold = Pair(Pair(6, 7), Pair(8, 9))

def process(s):
    cal = s
    while isinstance(cal, Pair):
        cal.bear = s
        cal = cal.second
    if cal is s:
        return cal
    else Assignment Project Exam Help

def display(f, s):
    if isinstance(ttpair):/powcoder.com
        print(s.first), process(s.second)))
```

y = lambda f: lambda x: f(f, x)

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Expression Output Expression Output Pair(1, nil) Pair(1, nil) process(blue.second) print(Pair(1, nil)) (1)1/0 ERROR print(process(gold)) print(print(3), 1/0) gold.second.bear.first print(Pair(2, blue)) y(display)(gold) print(gold)

2. (16 points) Environments

- (a) (8 pt) Fill in the environment diagram that results from executing the code below until the entire program is finished, an error occurs, or all frames are filled. You may not need to use all of the spaces or frames. A complete answer will:
 - Add all missing names and parent annotations to all local frames.
 - \bullet Add all missing values created during execution.
 - Show the return value for each local frame.

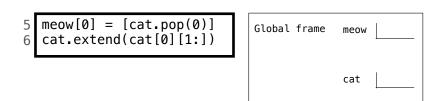
<pre>1 def tattoo(heart): 2 def mom(): 3 nonlocal mom</pre>	Global frame	tattoo func tattoo(heart) [parent=Global]						
<pre>4</pre>	f1:	_ [parent=]						
7 8 tattoo(lambda ink: ink + 0.5)								
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https://powcoder.com								
Add WeChat powcoder								
	f3:	_ [parent=]						
		Return Value						
	f4:	_ [parent=]						
		Return Value						

(b) (6 pt) For the six-line program below, fill in the three environment diagrams that would result after executing each pair of lines in order. You must use box-and-pointer diagrams to represent list values. You do not need to write the word "list" or write index numbers.

Important: All six lines of code are executed in order! Line 3 is executed after line 2 and line 5 after line 4.







(c) (2 pt) Circle the value, True or False, of each expression below when evaluated in the environment created by executing all six lines above. If you leave this question blank, you will receive 1 point.

Circle *True* or *False*: meow is cat[0]

Circle True or False: meow[0][0] is cat[0][0]

3. (12 points) Expression Trees

Your partner has created an interpreter for a language that can add or multiply positive integers. Expressions are represented as instances of the Tree class and must have one of the following three forms:

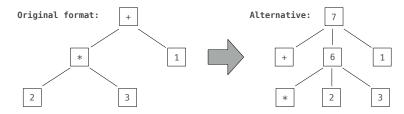
- (Primitive) A positive integer entry and no branches, representing an integer
- (Combination) The entry '+', representing the sum of the values of its branches
- (Combination) The entry '*', representing the product of the values of its branches

The Tree class is on the Midterm 2 Study Guide. The sum of no values is 0. The product of no values is 1.

(a) (6 pt) Unfortunately, multiplication in Python is broken on your computer. Implement eval_with_add, which evaluates an expression without using multiplication. You may fill the blanks with names or call expressions, but the only way you are allowed to combine two numbers is using addition.

```
def eval_with_add(t):
  """Evaluate an expression tree of st and + using only addition.
  >>> plus = Tree('+', [Tree(2), Tree(3)])
  >>> eval_with_add(plus)
  >>> times = Tree('*', [Tree(2), Tree(3)])
  >>> eval_with_add(times)
  »Assignment-Project-Exam Help
  >>> eval_w\h_add(deep)
  60
  if t.entry == '+':
     return Audd-WeChat-powcoder-----
  elif t.entry == '*':
     for b in t.branches:
        total, term = 0, ______
        for _____:
           total = total + term
     return total
  else:
     return t.entry
```

(b) (6 pt) A TA suggests an alternative representation of an expression, in which the entry is the value of the expression. For combinations, the operator appears in the left-most (index 0) branch as a leaf.



Implement transform, which takes an expression and mutates all combinations so that their entries are values and their first branches are operators. In addition, transform should return the value of its argument. You may use the calc_apply function defined below.

```
def calc_apply(operator, args):
   if operator == '+':
       return sum(args)
   elif operator == '*':
       return product(args)
def product(vals):
   total = 1
        ssignment Project Exam Help
       total 🕶 v
   return total
def transform(https://powcoder.com
"""Transform expression tree t to have value entries and operator leaves.
   >>> seven = Tree('+', [Tree('*', [Tree(2), Tree(3)]), Tree(1)])
>>> transform Gere WeChat powcoder
   7
   >>> seven
   Tree(7, [Tree(+), Tree(6, [Tree(*), Tree(2), Tree(3)]), Tree(1)])
   if t.branches:
       args = []
       for b in t.branches:
           args.append(_____)
       t.entry = _____
```

4. (12 points) Lazy Sunday

(a) (4 pt) A flat-map operation maps a function over a sequence and flattens the result. Implement the flat_map method of the FlatMapper class. You may use at most 3 lines of code, indented however you choose.

```
class FlatMapper:
```

"""A FlatMapper takes a function fn that returns an iterable value. The flat_map method takes an iterable s and returns a generator over all values in the iterables returned by calling fn on each element of s.

```
>>> stutter = lambda x: [x, x]
>>> m = FlatMapper(stutter)
>>> g = m.flat_map((2, 3, 4, 5))
>>> type(g)
<class 'generator'>
>>> list(g)
[2, 2, 3, 3, 4, 4, 5, 5]
"""
```

def __init__(self, fn):

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def flat_mhttps://powcoder.com

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(b) (2 pt) Define cycle that returns a Stream repeating the digits 1, 3, 0, 2, and 4. Hint: (3+2)%5 equals 0. def cycle(start=1):

"""Return a stream repeating 1, 3, 0, 2, 4 forever.

>>> first_k(cycle(), 12) # Return the first 12 elements as a list [1, 3, 0, 2, 4, 1, 3, 0, 2, 4, 1, 3]

def compute_rest():

return _____

return Stream(______)

(c) (4 pt) Implement the Scheme procedure directions, which takes a number n and a symbol sym that is bound to a nested list of numbers. It returns a Scheme expression that evaluates to n by repeatedly applying car and cdr to the nested list. Assume that n appears exactly once in the nested list bound to sym.

Hint: The implementation searches for the number **n** in the nested list **s** that is bound to **sym**. The returned expression is built during the search. See the tests at the bottom of the page for usage examples.

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; Search a nested list s for n and return an expression based on \exp .

```
(let (firsps://powcoder.com
```

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```
(if (null? first) rest first)))
```

```
(search (eval sym) sym))
(define a '(1 (2 3) ((4))))
(directions 1 'a)
; expect (car a)
(directions 2 'a)
; expect (car (car (cdr a)))
(define b '((3 4) 5))
(directions 4 'b)
; expect (car (cdr (car b)))
```

(d) (2 pt) What expression will (directions 4 'a) evaluate to?

5. (18 points) Basis Loaded

Ben Bitdiddle notices that any positive integer can be expressed as a sum of powers of 2. Some examples:

```
11 = 8 + 2 + 1
23 = 16 + 4 + 2 + 1
24 = 16 + 8
45 = 32 + 8 + 4 + 1
2014 = 1024 + 512 + 256 + 128 + 64 + 16 + 8 + 4 + 2
```

A basis is a linked list of decreasing integers (such as powers of 2) with the property that any positive integer n can be expressed as the sum of elements in the basis, starting with the largest element that is less than or equal to n.

(a) (4 pt) Implement sum_to, which takes a positive integer n and a linked list of decreasing integers basis. It returns a linked list of elements of the basis that sum to n, starting with the largest element of basis that is less than or equal to n. If no such sum exists, raise an ArithmeticError. Each number in basis can only be used once (or not at all). The Link class is described on your Midterm 2 Study Guide.

```
only be used once (or not at all). The Link class is described on your Midterm 2 Study Guide.
def sum_to(n, basis):
   """Return elements of linked list basis that sum to n.
   >>> twos = Link(32, Link(\underline{16}, Link(8, Link(4, Link(\underline{2}, Link(\underline{1})))))
   >> Assignment, Project Exam Help
   >>> sum_to(23, twos)
   Link(16, Link(4, Link(2, Link(1))))
   >>> sum_to https://powcoder.com
   >>> sum_to(45, twos)
   Link(32, Link(8, Link(4, Link(1))))
            Add WeChat powcoder
       return Link.empty
   elif _____:
       raise ArithmeticError
   elif basis.first > n:
       return sum_to(n, basis.rest)
   else:
```

(b) (6 pt) Cross out as many lines as possible in the implementation of the FibLink class so that all doctests pass. A FibLink is a subclass of Link that contains decreasing Fibonacci numbers. The up_to method returns a FibLink instance whose first element is the largest Fibonacci number that is less than or equal to positive integer n.

```
class FibLink(Link):
   """Linked list of Fibonacci numbers.
   >>> ten = FibLink(2, FibLink(1)).up_to(10)
   >>> ten
   Link(8, Link(5, Link(3, Link(2, Link(1))))
   >>> ten.up_to(1)
   Link(1)
   >>> six, thirteen = ten.up_to(6), ten.up_to(13)
   Link(5, Link(3, Link(2, Link(1))))
   >>> thirteen
   Link(13, Link(8, Link(5, Link(3, Link(2, Link(1))))))
   successor = self.first + self.rest
   @property
   def successor():
       essignment Project Exam Help
       return self.first + self.rest.first
   def up_to(https://powcoder.com
       while self.first > n:
           self = self.rest.first
           selAdd WeChat powcoder
       if self.first == n:
           return self
       elif self.first > n:
           return self.up_to(n)
           return self.rest.up_to(n)
       elif self.successor > n:
       elif self.first < n:</pre>
           return self
       else:
           return FibLink(self.successor(self), self).up_to(n)
           return FibLink(self.successor, self).up_to(n)
           return FibLink(self.successor(self), self.rest).up_to(n)
           return FibLink(self.successor, self.rest).up_to(n)
```

(c) (2 pt) Circle the Θ expression below that describes the number of calls made to FibLink.up_to when evaluating FibLink(2, FibLink(1)).up_to(n). The constant ϕ is $\frac{1+\sqrt{5}}{2}=1.618...$

 $\Theta(1)$ $\Theta(\log_{\phi} n)$ $\Theta(n)$ $\Theta(n^2)$ $\Theta(\phi^n)$

(d) (2 pt) Alyssa P. Hacker remarks that Fibonacci numbers also form a basis. How many total calls to FibLink.up_to will be made while evaluating all the doctests of the fib_basis function below? Assume that sum_to and FibLink are implemented correctly. Write your answer in the box.

```
def fib_basis():
       """Fibonacci basis with caching.
       >>> r = fib_basis()
       >>> r(11)
       Link(8, Link(3))
       >>> r(23)
       Link(21, Link(2))
       >>> r(24)
       Link(21, Link(3))
       >>> r(45)
       Link(34, Link(8, Link(3)))
       fibs = FibLink(2, FibLink(1))
       def represent(n):
           nonlocal fibs
           fibs = fibs.up_to(n)
           return sum_to(n, fibs)
(e) (4 pt) Implement fib_sums, a function that takes positive integer n and returns the number of ways that n
   can be expressed as a sum of unique Fibonacci numbers. Assume that FibLink is implemented correctly.
   def fib_sums(nhttps://powcoder.com of unique Fibonacci numbers.
       >>> fib_sums(9) # 8+1, 5+3+1
       2 systib_surAdd WeChat powcoder
       >>> fib_sums(13) # 13, 8+5, 8+3+2
       3
       11 11 11
       def sums(n, fibs):
           """Ways n can be expressed as a sum of elements in fibs."""
           if n == 0:
                return 1
                return 0
```

return sums(n, FibLink(2, FibLink(1)).up_to(n))

return a + b

6. (8 points) Sequels

Assume that the following table of movie ratings has been created.

```
create table ratings as
                                                               Correct output
  select "The Matrix" as title,
                                     9 as rating union
                                                                Judgment Day
  select "The Matrix Reloaded",
                                                   union
                                                                 Terminator
  select "The Matrix Revolutions", 5
                                                   union
                                                                 The Matrix
  select "Toy Story",
                                                   union
                                                                  Toy Story
  select "Toy Story 2"
                                                   union
                                                                 Toy Story 2
  select "Toy Story 3",
                                                   union
                                                                 Toy Story 3
  select "Terminator",
                                                   union
  select "Judgment Day",
                                                   union
  select "Rise of the Machines",
```

The correct output table for both questions below happens to be the same. It appears above to the right for your reference. **Do not hard code your solution to work only with this table!** Your implementations should work correctly even if the contents of the ratings table were to change.

(a) (2 pt) Select the titles of all movies that have a rating greater than 7 in alphabetical order.

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(b) (6 pt) Select the titles of all movies for which at least 2 other movies have the same rating. The results should appear in alphabetical order. Repeated results are acceptable. You may only use the SQL features introduced in this course.

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groups(name, score, n) as (
select,, not select from ratings uni	on
select,, rating	s
where	-
)	
select title from	-
where	-
and an her	

Appendix: Pair and nil Implementations

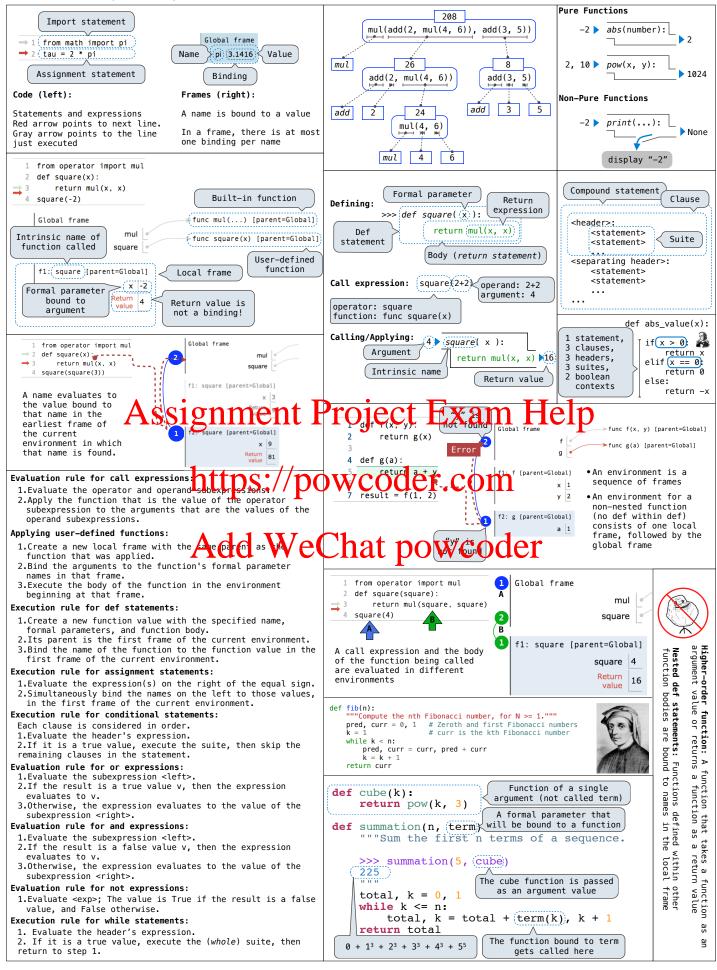
return self

```
This page does not contain a question. These classes were originally defined in scheme_reader.py.
class Pair:
   """A pair has two instance attributes: first and second. For a Pair to be
   a well-formed list, second is either a well-formed list or nil. Some
   methods only apply to well-formed lists.
   >>> s = Pair(1, Pair(2, nil))
   >>> s
   Pair(1, Pair(2, nil))
   >>> print(s)
   (1 \ 2)
   def __init__(self, first, second):
       self.first = first
       self.second = second
   def __repr__(self):
       return "Pair({0}, {1})".format(repr(self.first), repr(self.second))
       Assignment Project Exam Help
       second = self.second
       while isinstance (second, Pair):
           s += " " + str(second.first)
       seconittps://d.powcoder.com
           s += " . " + str(second)
       return s + ")"
               Add WeChat powcoder
class nil:
   """The empty list"""
   def __repr__(self):
       return "nil"
   def __str__(self):
       return "()"
   def __len__(self):
       return 0
   def __getitem__(self, k):
       if k < 0:
           raise IndexError("negative index into list")
       raise IndexError("list index out of bounds")
   def map(self, fn):
```

nil = nil() # Assignment hides the nil class; there is only one instance

Scratch Paper

Scratch Paper



 $grow = lambda n: f_then_g(grow, print, n//10)$

shrink = lambda n: f_then_g(print, shrink, n//10)

1

```
def square(x):
                                                                                                                  VS
                                                                                 square = lambda x: x * x
 square = \frac{x,y}{x * y}
                                                                                                                                return x * x
                                  Evaluates to a function.
                                    No "return" keyword!
                                                                               • Both create a function with the same domain, range, and behavior.
           A function
               with formal parameters x and y
                                                                               • Both functions have as their parent the environment in which they
                     that returns the value of "\times \times y,"
                                                                               · Both bind that function to the name square.
                  Must be a single expression
                                                                               • Only the def statement gives the function an intrinsic name.
                       A function that returns a function
def make_adder(n):
        'Return a function that takes one argument k and returns k + n.
                                                                               When a function is defined:
    >>>(add_three = make_adder(3))
                                          The name add three is

    Create a function value: func <name>(<formal parameters>)

                                           bound to a function
                                                                               2. Its parent is the current frame.
     7
                              A local
                                                                                        f1: make_adder
                                                                                                               func adder(k) [parent=f1]
    def adder(k):
                           def statement
         return k +(n)
                                                                               3. Bind <name> to the function value in the current frame
                                                                                   (which is the first frame of the current environment).
                           Can refer to names in
     return adder
                          the enclosing function
                                                                               When a function is called:
                                                                                1. Add a local frame, titled with the <name> of the function being
• Every user-defined function has
                                                                                   called.
  a parent frame
                                                                                   Copy the parent of the function to the local frame: [parent=<label>]
 • The parent of a function is the

    Bind the <formal parameters> to the arguments in the local frame.
    Execute the body of the function in the environment that starts with

  frame in which it was defined
                                               A function's signature
 • Every local frame has a parent
                                                                                   the local frame.
                                               has all the information
  frame
                                               to create a local frame
 • The parent of a frame is the
  parent of the function called
                                3
                                    Global frame
                                                                 func make adder(n) [parent=Global]
                                                                                                    def fact(n):
                                              make_adder
                                                                                                        if n == 0:
   1 def make_adder(n):
                                                               func adder(k) [parent=f1]
                                                add_three
                                                                                                             return 1
     def adder(k):
return k + n
                                                                                                         else:
 Nested
                                     f1: make_adder [parent=G]
         return adder
                                                                                                             return n * fact(n-1)
  def
   6 add_three = make_adder(3)
                                                   adder
                                                                                                  7 fact(3)
   7 add_three(4)
                                                  Return
                                                                                                                                 func fact(n) [parent=Global]
                                                                                 ect
                                                                                               f1: fact [parent=Global]
 def curry2(f):
       ""Returns a function g such that
     def g(x):
         def h(y):
                               Currying: Transforming a multi-argument function into a single-argument,
             return f(x, y)
         return h
                                higher-order function.
     return q
                                                                                               f3: fact [parent=Global]
 Anatomy of a recursive function:
                                                                             at powco
 • The def statement header is similar to
                                                                                                f4: fact [parent=Global]

    Conditional statements check for base cases

    Base cases are evaluated without recursive calls

                                                                                                                   n 0

    Recursive cases are evaluated with recursive calls

                                                                                                               Return 1
 def sum digits(n):
  """Return the sum of the digits of positive integer n.""" if \frac{n}{l} < 10 \colon
       return n
                                                                                            Is fact implemented correctly?
   else:
                                                                                                  Verify the base case.
       all_but_last, last = n // 10, n % 10
                                                                                                  Treat fact as a functional abstraction!
                                                                                            2.
       return sum_digits(all_but_last) + last
                                                                                            3.
                                                                                                  Assume that fact(n-1) is correct.
                                                                                                  Verify that fact(n) is correct.
                                                                                            4.
                                                                                                  assuming that fact(n-1) correct.
                          Global frame
   def cascade(n):
                                                    >> func cascade(n) [parent=Global]
       if n < 10:
                                       cascade e
          print(n)
       else:
                          f1: cascade [parent=Global] * Each cascade frame is n \mid_{123} from a different call
          print(n)
                                         n 123
           cascade(n//10)
                                                  to cascade.

    Recursive decomposition:

                                                                                                                 def count_partitions(n, m):
          print(n)
                          f2: cascade [parent=Global]
                                                                                 finding simpler instances of
                                                • Until the Return value
                                                                                                                     if n == 0:
                                        n 12
                                                                                 a problem.
                                                                                                                         return 1
                                                 appears, that call has not completed.
  9 cascade(123)
                                      Return
value None
                                                                               E.g., count_partitions(6, 4)
                                                                                                                     elif n < 0:
                                                                               Explore two possibilities:Use at least one 4
                                                                                                                         return 0
Program output:
Any statement can
                                                                                                                     elif m == 0:
                                                  appear before or after
                                                                                 Don't use any 4
                                                                                                                         return 0
1 12
                                                                               Solve two simpler problems:count_partitions(2, 4)
                                                  the recursive call.
                                      Return
value None
                                                                                                                     else:
                                                                                                                     with_m = count_partitions(n-m, m)
                                                                                  count_partitions(6, 3)
                                                                                                                         without_m = count_partitions(n, m-1)
                                                                               • Tree recursion often involves
                                                                                                                          return with_m + without_m
                                                                                exploring different choices.
                                             n: 0, 1, 2, 3, 4, 5, 6, 7, 8,
           def inverse_cascade(n):
1
                                        fib(n): 0, 1, 1, 2, 3, 5, 8, 13, 21,
               grow(n)
                                                                               from operator import floordiv, mod
12
               print(n)
                                                                                def divide exact(n, d):
                                       def fib(n):
    if n == 0:
                shrink(n)
                                                                                    """Return the quotient and remainder of dividing N by D.
123
                                            if n == 0:
return 0
elif n == 1:
           def f_then_g(f, g, n):
1234
                                                                                    >>> (q, r = divide\_exact(2012, 10)) < Multiple assignment
                if n:
                                                return 1
                                                                                    >>> 'q
                                                                                                                                to two names
123
                                            else:
return fib(n-2) + fib(n-1)
                    f(n)
                                                                                    201
                    q(n)
                                                                                    >>> r
12
```

000

return floordiv(n, d), mod(n, d) <

Multiple return values,

separated by commas

```
Numeric types in Python:
                                                                                      List comprehensions:
                                                                                                                                                                                                                     List & dictionary mutation:
                                                                                           [<map exp> for <name> in <iter exp> if <filter exp>]
                                                                                                                                                                                                                    >>> a = [10]
  >>> type(2)
                                         Represents
                                                                                                                                                                                                                                                          >>> a = [10]
                                                                                                                                                                                                                    >>> b = a
  <class 'int'>-
                                                                                                                                                                                                                                                          >>> b = [10]
                                           integers
                                                                                           Short version: [<map exp> for <name> in <iter exp>]
                                                                                                                                                                                                                    >>> a == b
                                                                                                                                                                                                                                                          >>> a == b
                                           exactly
  >>> type(1.5)
                                                                                      A combined expression that evaluates to a list using this
                                                                                                                                                                                                                    True
                                                                                                                                                                                                                                                          True
                                                                                                                                                                                                                    >>> a.append(20)
                                                                                                                                                                                                                                                          >>> b.append(20)
  <class 'float'> <
                                                                                      evaluation procedure:
                                    Represents real
                                                                                                                                                                                                                    >>> a == b
                                                                                                                                                                                                                                                          >>> a
                                                                                      1. Add a new frame with the current frame as its parent
                                           numbers
   >>> type(1+1j)
                                                                                                                                                                                                                    True
                                                                                                                                                                                                                                                          [10]
                                                                                      2. Create an empty result list that is the value of the
                                      approximately
  <class 'complex'>
                                                                                                                                                                                                                     >>> a
                                                                                                                                                                                                                                                          >>> b
                                                                                           expression
                                                                                                                                                                                                                     [10, 20]
                                                                                                                                                                                                                                                          [10, 20]
                                                                                      3. For each element in the iterable value of <iter exp>:
  Functional pair implementation:
                                                                                                                                                                                                                     >>> h
                                                                                                                                                                                                                                                          >>> a == b
                                                                                          A. Bind <name> to that element in the new frame from step 1
                                                                                                                                                                                                                    [10, 20]
                                                                                                                                                                                                                                                         False
                                                                                          B. If <filter exp> evaluates to a true value, then add
                                                                                                                                                                                                                    >>> nums = {'I': 1.0, 'V': 5, 'X': 10}
  def pair(x, y):
                                                                                                the value of <map exp> to the result list
          """Return a functional pair."""
                                                                                                                                                                                                                     >>> nums['X']
                                                                                      def apply_to_all(map_fn, s):
         def get(index):
                if index == 0:
                                                                                                  "Apply map_fn to each element of s.
                                                                                                                                                                              0, 1, 2, 3, 4
                                                                                                                                                                                                                    >>> nums['I'] = 1
                                                    This function
                        return x
                                                                                                                                                                                                                    >>> nums['L'] = 50
                                                     represents a
                 elif index == 1:
                                                                                              >>> apply_to_all(lambda x: x*3, range(5))
                                                             pair
                                                                                                                                                                                   λx: x*3
                                                                                                                                                                                                                    >>> nums
                        return y
                                                                                              [0, 3, 6, 9, 12]
                                                                                                                                                                                                                     {'X': 10, 'L': 50, 'V': 5, 'I': 1}
          return get
                                                                                                                                                                                                                     >>> sum(nums.values())
                                                                                                                                                                              0, 3, 6, 9, 12
                                                                                              return [map_fn(x) for x in s]
                                           Constructor is a
                                                                                                                                                                                                                    >>> dict([(3, 9), (4, 16), (5, 25)])
{3: 9, 4: 16, 5: 25}
  def select(p, i): higher-order function
                                                                                      def keep_if(filter_fn, s):
                                                                                                 "List elements x of s for which
                                                                                                                                                                              0, 1, 2, 3, 4, 5, 6, 7, 8, 9
         """Return element i of pair p."""
                                                                                                                                                                                                                    >>> nums.get('A', 0)
                                                                                              filter_fn(x) is true.
         return p(i) _
                                                                                                                                                                                                                    0
                                                                                                                                                                                                                    >>> nums.get('V'. 0)
                                          Selector defers to
                                                                                              >>> keep_if(lambda x: x>5, range(10))
                                                                                                                                                                                   \lambda x: x>5
                                           the object itself
  >>> p = pair(1, 2)
                                                                                              [6, 7, 8, 9]
                                                                                                                                                                                                                     >>> {x: x*x for x in range(3,6)}
  >>> select(p, 0)
                                                                                                                                                                                                                     {3: 9, 4: 16, 5: 25}
                                                                                                                                                                                 6, 7, 8, 9
                                                                                              return [x for x in s if filter_fn(x)]
                                                                                                                                                                                                                     >>> suits = ['coin', 'string', 'myriad']
  >>> select(p, 1)
                                                                                                                                                                                                                     >>> original_suits = suits
                                                                                              reduce(reduce_fn, s, initial):
                                                                                                                                                                                                                    >>> suits.pop()
                                                                                               ""Combine elements of s pairwise using reduce_fn,
Lists:
                                                                                              starting with initial.
                                                                                                                                                                                                                     'mvriad'
                                                                                                                                                            16,777,216
                                                                                                                                                                                                                    >>> suits.remove('string')
 >>> digits = [1, 8, 2, 8]
                                                                                                                                                                                                                     >>> suits.append('cup')
                                                                                              r = initial
 >>> len(digits)
                                                                                                                                                                                                                     >>> suits.extend(['sword', 'club'])
                                                    list
                                                                                              for x in s:
                                                                                                                                               pow
                             digits ___
                                                                                                    r = reduce_fn(r, x)
                                                                                                                                                                                                                    >>> suits[2] = 'spade'
 >>> digits[3]
                                                                                                                                                                                                                    >>> suits
['coln' 'cup', 'spade', 'club']

suits[0:2] = ['heart', 'diamond']

Suits
                                                                   2 8
                                                                                                                                                                                           3
                                                                                                                                                  woa
 >>> [2, 7] + digits * 2 [2, 7, 1, 8, 2, 8, 1, 8, 2, 8] ASSI gradement
                                                                                                                                                                   2
                                                                                                                                                                                                                     ['heart
                                                                                                                                                                                                                                       'diamond', 'spade', 'club']
 >>> pairs = [[10, 20], [30, 40]]
                                                                                                                                                                   2
                                                                                                                                                                            1
                                                                                                                                                        pow
                                                                                                                                                                                                                     >>> original_suits
 >>> pairs[1]
                                                                list
                                                                                                                                                                                                                                       'diamond', 'spade', 'club']
                             pairs__
 [30, 40]
                                               0 1
                                                                                    Type dispatching. Look up a cross-type implementation of an operation cased out in Cycles of the conference of the confe
 >>> pairs[1][0]
                                                                         20
                                                                  10
                                                                                                                                                                                                                     Identity:
 30
                                                                                                                                                                                                                      <exp0> is <exp1>
                                                                                                                                                                                                                     evaluates to True if both <exp0> and
                                                                list
                                                                                    another, then apply a type-specific implementation.
 Executing a for statement:
                                                                                                                                                                                                                      <exp1> evaluate to the same object
 for <name> in <expression>:
                                                                                                               \Theta(b^n) Exponential growth. Recursive fib takes
                                                                                                                                                                                                                     Equality:
                                                                  30
                                                                        40
                                                                                          recositive schemat k
                                                                                                                            \Theta(\phi^n) steps, where \phi=\frac{1+\sqrt{5}}{1+\sqrt{5}}\approx 1.61828 by a factor the property of \Theta
        <suite>
                                                                                                                                                                                                                      <exp0> == <exp1>
 1. Evaluate the header <expression>,
                                                                                                                                                                                                                     evaluates to True if both <exp0> and
      which must yield an iterable value
                                                                                                                                                                                                                      <exp1> evaluate to equal values
      (a sequence)
                                                                                                                                                                                                                    Identical objects are always equal values
                                                                                          oldsymbol{k_2} s \leq k_2
 2. For each element in that sequence.
                                                                                                               \Theta(n^2)
                                                                                                                                                                                                                      You can copy a list by calling the list
                                                                                                                              Quadratic growth. E.g., overlap
      in order:
                                                                                         it there is ki and \mathbf{k} \leq R(n) :
                                                                                                                                                                                                                     constructor or slicing the list from the
                                                                                                                              Incrementing n increases R(n) by the
    A. Bind <name> to that element in
                                                                                     f(n)
                                                                                                                                                                                                                     beginning to the end.
          the current frame
                                                                                                                              problem size n
                                                                                                                                                                                                                   Constants: Constant terms do not affect
    B. Execute the <suite>
                                                                                                                \Theta(n)
                                                                                                                              Linear growth. E.g., factors or exp
                                                                                                                                                                                                                   the order of growth of a process
                                                                                    R(n) = \Theta(n) means that constants f_1 \cdot f(n) \le f_1 \cdot f
                                                                                                                                                                                                                   \Theta(n) \qquad \Theta(500 \cdot n) \qquad \Theta(\frac{1}{500} \cdot n) 
 \textbf{Logarithms:} \ \ \text{The base of a logarithm does}
  Unpacking in a
                                                                                                           \Theta(\log n)
                                                                                                                              Logarithmic growth. E.g., exp_fast
                                           A sequence of
  for statement:
                                  fixed-length sequences
                                                                                                                              Doubling the problem only increments R(n)
                                                                                                                 \Theta(1)
                                                                                                                              Constant. The problem size doesn't matter
                                                                                                                                                                                                                   not affect the order of growth of a process
 >>> pairs=[[1, 2], [2, 2], [3, 2], [4, 4]]
                                                                                                                                                                                                                     \Theta(\log_2 n) ~~ \Theta(\log_{10} n)
                                                                                                                                                                                                                                                                   \Theta(\ln n)
 >>> same_count = 0
                                                                                                                                                                                                                   Nesting: When an inner process is repeated
                                                                                                                                                 → func make withdraw(balance) [parent=Global
                                                                                      Global frame
           A name for each element in a
                                                                                                                                                                                                                   for each step in an outer process, multiply
                 fixed-length sequence
                                                                                                              make_withdraw
                                                                                                                                                                                                                   the steps in the outer and inner processes
                                                                                                                                                  func withdraw(amount) [parent=f1]
                                                                                                                      withdraw
                                                                                                                                                                                                                   to find the total number of steps
>>> for (x, y) in pairs:
... if x == y:
                                                                                                                                                 >>> withdraw = make_withdraw(100)
                                                                                                                                                                                                                   def overlap(a, b):
                                                                                                                                                 >>> withdraw(25)
                                                                                      f1: make withdraw [parent=Global]
                                                                                                                                                                                                                           count = 0
                       same_count = same_count + 1
                                                                                                                                                 75
                                                                                                                                                                                                                                                             Outer: length of a
                                                                                                                                                                                                                           for item in a: —
                                                                                                                      balance 50
                                                                                                                                                 >>> withdraw(25)
                                                                                           The parent
                                                                                                                                                                                                                                 if item in b:
count += 1 Inner: length of b
                                                                                                                     withdraw
                                                                                                                                                50
 >>> same_count
                                                                                        frame contains
                                                                                                                                                def make_withdraw(balance):
                                                                                                                       Return
                                                                                       the balance of
                                                                                                                                                                                                                          return count
                                                                                                                         value
                                                                                                                                                     def withdraw(amount):
                                                                                             withdraw
                                                                                                                                                                                                                   If a and b are both length n,
        \dots, -3, -2, -1, 0, 1, 2, 3, 4, \dots
                                                                                                                                                               nonlocal balance
                                                                                                                                                                                                                   then overlap takes \Theta(n^2) steps
                                                                                      f2: withdraw [parent=f1]
                                                                                                                                                               if amount > balance:
    return 'No funds
                                                                                                                                                                                                                   Lower-order terms: The fastest-growing part
                                                                                                                      amount 25
                                                                                           Every call
                                                                                                                                                                                                                  of the computation dominates the total
                                                                                                                                                               balance = balance - amount
                                                                                                                       Return
value 75
                                                                                        decreases the
                                                                                                                                                               return balance
                         range(-2, 2)
                                                                                                                                                                                                                   \Theta(n^2) \quad \Theta(n^2 + n) \quad \Theta(n^2 + 500 \cdot n + \log_2 n + 1000)
                                                                                         same balance
                                                                                                                                                       return withdraw
  Length: ending value - starting value
                                                                                      f3: withdraw [parent=f1]
                                                                                                                                                     Status
                                                                                                                                                                                                           Effect
                                                                                                                                                                                      x = 2
 Element selection: starting value + index
                                                                                                                     amount 25
                                                                                                                                                  •No nonlocal statement
                                                                                                                                                                                                       Create a new binding from name "x" to number 2
                                                                                                                                                   •"x" is not bound locally
                                                                                                                                                                                                       in the first frame of the current environment
                                                                                                                       Return
value 50
  >>> list(range(-2, 2)) { List constructor
                                                                                                                                                                                                       Re-bind name "x" to object 2 in the first frame
  [-2, -1, 0, 1]
                                                                                                                                                  •No nonlocal statement
                                                                                       Strings as sequences:
                                                                                                                                                  •"x" is bound locally
                                                                                                                                                                                                       of the current environment
                                          Range with a 0
  >>> list(range(4)) <
                                                                                      >>> city = 'Berkeley'
                                                                                                                                                  •nonlocal x
                                          starting value
                                                                                                                                                                                                      Re-bind "x" to 2 in the first non-local frame of
                                                                                      >>> len(city)
  [0, 1, 2, 3]
                                                                                                                                                  •"x" is bound in a
                                                                                                                                                                                                       the current environment in which "x" is bound
                                                                                      8
                                                                                                                                                   non-local frame
Membership:
                                                 Slicing:
                                                                                       >>> city[3]
                                                 >>> digits[0:2]
>>> digits = [1, 8, 2, 8]
                                                                                                                                                  •nonlocal x
                                                                                                                                                                                                      SyntaxError: no binding for nonlocal 'x' found
                                                 [1, 8]
                                                                                                                                                  •"x" is not bound in
>>> 2 in digits
                                                                                      >>> 'here' in "Where's Waldo?'
                                                  >>> digits[1:]
True
                                                                                                                                                   a non-local frame
                                                                                      True
 >>> 1828 not in digits
                                                 [8, 2, 8]
                                                                                                                                                  •nonlocal x
                                                                                      >>> 234 in [1, 2, 3, 4, 5]
                                                                                                                                                  •"x" is bound in a
                                                  Slicing creates
                                                                                      False
                                                                                                                                                                                                       SyntaxError: name 'x' is parameter and nonlocal
                                                                                                                                                   non-local frame
```

>>> [2, 3, 4] in [1, 2, 3, 4]

False

•"x" also bound locally

a new object

return self.branches[1]

```
Linked list data abstraction:
                                                                             Python object system:
                                                                              Idea: All bank accounts have a balance and an account holder;
                            def partitions(n, m):
 empty = 'empty'
                                                                              the Account class should add those attributes to each of its instances
                                  "Return a linked list of partitions
                                of n using parts of up to m.
 def link(first, rest):
                                                                                                       >>> a = Account('Jim')
                                                                                A new instance is
                                Each partition is a linked list.
    return [first, rest]
                                                                                                        >>> a.holder
                                                                               created by calling a
                                                                                                        'Jim'
                                                                                       class
 def first(s):
                                if n == 0:
                                                                                                        >>> a.balance
                                                                                                                                 An account instance
    return s[0]
                                    return link(empty, empty)
                                                                             When a class is called:
                                                                                                                                         holder: 'Jim'
                                elif n < 0:
                                                                                                                           balance: 0
                                                                             1.A new instance of that class is created:
 def rest(s):
                                    return empty
                                                                             2. The __init__ method of the class is called with the new object as its first
    return s[1]
                                elif m == 0:
                                                                               argument (named self), along with any additional arguments provided in the
                                    return empty
                                                                                call expression.
 def len_link(s):
                                else:
                                    # Do I use at least one m?
      = 0
                                                                                                   class Account:
                                                                                                            __init__(self, account_holder):
     while s != empty:
                                    yes = partitions(n-m, m)
                                                                                                       ⊳def
        s, x = rest(s), x+1
                                    no = partitions(n, m-1)
                                                                                 init is called a
                                                                                                            self.balance = 0
                                    add_m = lambda s: link(m, s)
yes = apply_to_all_link(add_m, yes)
     return x
                                                                                   constructor
                                                                                                            self.holder = account_holder
                                                                                                        def deposit(self, amount)
                                     return extend(yes, no)
 def getitem_link(s, i):
                                                                                                            self.balance = self.balance + amount
    while i > 0:
                                                                                                            return self.balance
                                                                               self should always be
                                                                                                            withdraw(self, amount):
  if amount > self.balance:
    return 'Insufficient funds'
         s, i = rest(s), i - 1
                                                                                                        def
                                                                              bound to an instance of
     return first(s)
                                                                               the Account class or a
                                                   subclass of Account
def extend(s, t):
    assert is_link(s) and is_link(t)
                                                                                                            self.balance = self.balance - amount
                                                                                                            return self.balance
     if s == empty:
                                                                                                     >>> type(Account.deposit)
         return t
                                                                               Function call: all
                                                                                                    <class 'function'
     else:
                                                                                                    >>> type(a.deposit)
                                                                                arguments within
         return link(first(s), extend(rest(s), t))
                                                                                   parentheses
                                                                                                    <class 'method'>
def apply_to_all_link(f, s):
    if s == empty:
                                                                                                     >>> Account.deposit(a, 5)
                                                                               Method invokation:
         return s
                                                                                One object before
     else:
                                                                                                        a.deposit(2)
                                                                                the dot and other
                                                                                                                                 Call expression
         return link(f(first(s)), apply_to_all_link(f, rest(s)))
                                                                                arguments within
                                                                                   parentheses
                           link(1, link(2, link(3, link(4, empty)
                                                                                                          Dot expression
          A linked list
                                   represents the sequence
            is a pair
                                        1 2 3
                                                                "empty"
                                                    4
                                                                                  resion
must
                                                                                               can be an laid ytherexpession.
                                                                 e emp
          list
                        list
                                                                              Evaluates to the value of the attribute looked up by <name> in the object
           0
                         0
                                       0
                                                     0
                                                                              that is the value of the <expression>.
                          2
                                        3
            1
                                                      4
                                                           "empty"
                                                                              To evaluate a dot expression:
                                                                                 Evaluate the <expression> to the left of the dot, which yields
                                                                                   The spin ssion he instance attributes of that object;
                                        The __n
      The 0-indexed element of the
                                                      the rest
                                                                                   if an attribute with that name exists, its value is returned
      pair is the first element of
                                       of the pair
             the linked list
                                          of the linked list
                                                                                  If not, <name> is looked up in the class, which yields a class
                                                                                   attribute value
The result of calling repr on a value is
                                                                                   That value is returned unless it is a function, in which case a
                                               Memoization:
                                                                               bound method is returned istead

Actinment statements with the object of that dot expression
what Python prints in an interactive session
                                                     m((°):
che = ·
The result of calling str on a value is
                                                         = {}
what Python prints using the print function
                                                       memoized(n):
                                                       if n not in cache:
                                                                               • If the object is an instance, then assignment sets an instance attribute
 >>> 12e12
                           >>> print(today)
                                                           cache[n] = f(n)
                                                                               • If the object is a class, then assignment sets a class attribute
 120000000000000.0
                           2014-10-13
                                                        return cache[n]
 >>> print(repr(12e12))
                                                                                        Account class
                                                                                                            interest: 0.02 0.04 0.05
                                                   return memoized
 120000000000000.0
                                                                                          attributes
                                                                                                            (withdraw, deposit, _
                                                                                                                                   init
str and repr are both polymorphic; they apply to any object
repr invokes a zero-argument method __repr__ on its argument
                                                                                   Instance
                                                                                                  balance:
                                                                                                             0
                                                                                                                                        balance:
                                                                                                                         Instance
                                                                                                             'Jim'
                                                                                                                                                   'Tom'
                                                                                                                                        holder:
                                                                                attributes of
                                                                                                  holder:
                                                                                                                      attributes of
                                  >>> today.__str__()
>>> today.__repr__()
'datetime.date(2014, 10, 13)'
>>> today._
                                                                                                  interest: 0.08
                                                                                 jim_account
                                                                                                                       tom account
                                                                                                                         >>> jim_account.interest = 0.08
                                                                               >>> jim_account = Account('Jim')
                   Some zero
class Link:
                                                                                   tom_account = Account('Tom')
                                                                                                                        >>> jim_account.interest
   empty = () < length sequence</pre>
                                                                                                                        0.08
                                                                               >>> tom_account.interest
                                                                              0.02
                                                                                                                        >>> tom account.interest
          _init__(self, first, rest=empty):
                                                                                                                        0.04
        self.first = first
                                                                              >>> jim_account.interest
                                                                                                                         >>> Account.interest = 0.05
                                                                              0.02
        self.rest = rest
                                    Sequence abstraction special names:
                                                                                                                         >>> tom_account.interest
         _getitem__(self, i):
                                                                              >>> Account.interest = 0.04
                                                                                                                        0.05
                                      _getitem__ Element selection []
                                                                               >>> tom_account.interest
        if i == 0:
                                                                                                                         >>> jim_account.interest
            return self.first
                                                  Built-in len function
                                                                                                                        0.08
                                       len.
                                                                               >>> jim_account.interest
        else:
                                                                              0.04
            return self.rest[i-1]
          <u>len__(self):</u>
                                                                              class CheckingAccount(Account):
                                      Yes, this call is recursive
        return 1 + len(self.rest)
                                                                                     "A bank account that charges for withdrawals."""
                                                                                  withdraw_fee = 1
class Tree:
          <u>_init</u>__(self, entry, branches=()):
                                                   Built-in isinstance
                                                                                   interest = 0.01
    def
                                                                                  function: returns True if
         self.entry = entry
         for branch in branches:
                                                 branch has a class that
             assert (isinstance(branch, Tree))
                                                is or inherits from Tree
         self.branches = list(branches)
                                                                                       return (super().withdraw(
                                                                                                                      amount + self.withdraw_fee)
class BinaryTree(Tree):
                                            E: An empty tree
                                                                               To look up a name in a class:
    empty = Tree(None)
                                                                               1. If it names an attribute in the class, return the attribute value.
    empty.is_empty = True
        __init__(self, entry, left=empty, right=empty):
Tree.__init__(self, entry, (left, right))
                                                                               2. Otherwise, look up the name in the base class, if there is one.
                                                           1
                                                                               >>> ch = CheckingAccount('Tom') # Calls Account.__init_
        self.\overline{is}\_empty = False
                                                                               >>> ch.interest
                                                                                                    # Found in CheckingAccount
    @property
                                                                               0.01
    def left(self):
                                  Bin = BinaryTree
                                                                               >>> ch.deposit(20) # Found in Account
        return self.branches[0] | t = Bin(3, Bin(1),
                                                                               20
    @property
                                              Bin(7, Bin(5),
                                                                        11
                                                                               >>> ch.withdraw(5) # Found in CheckingAccount
                                                     Bin(9, Bin.empty,
    def right(self):
                                                             Bin(11)))) E
```

```
class LetterIter:
                                                                                                                                                     >>> a_to_c = LetterIter('a', 'c')
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                                                                                                  def __init__(self, start='a', end='e'):
                                                                                                                                                    >>> next(a_to_c)
                                                                                                      self.next_letter = start
self.end = end
Exceptions are raised with a raise statement.
                                                                                                                                                    >>> next(a_to_c)
                           raise <expression>
                                                                                                      __next__(self):
if self.next letter >= self.end:
                                                                                                                                                     >>> next(a_to_c)
<expression> must evaluate to a subclass of BaseException or
                                                                                                                                                    Traceback (most recent call last):
an instance of one.
                                                                                                          raise StopIteration
Exceptions are constructed like any other object. E.g.,
                                                                                                      result = self.next_letter
                                                                                                                                                    StopIteration
TypeError('Bad argument!')
                                                                                                       self.next letter = chr(ord(result)+1)
                                                                                                      return result
                                                                                                                                                    >>> b to k = Letters('b', 'k')
 try:
                                                                                                                                                     >>> first_iterator =
                                                >>> try:
      <try suite>
                                                                                                                                                    b_to_k.__iter__()
>>> next(first_iterator)
                                                                                              class Letters:
                                                                                                  def __init__(self, start='a', end='e'):
    self.start = start
    self.end = end
 except <exception class> as <name>:
                                                         x = 1/0
      <except suite>
                                                    except ZeroDivisionError as e:
                                                                                                                                                     >>> next(first_iterator)
                                                         print('handling a', type(e))
The <trv suite> is executed first.
                                                                                                                                                     >>> second_iterator = iter(b_to_k)
                                                                                                       __iter__(self):
return LetterIter(self.start, self.end)
                                                                                                                                                    >>> second_iterator.__next__()
If, during the course of executing the
                                                         x = 0
<try suite>, an exception is raised that is not handled otherwise, and
                                                                                              def letters_generator(next_letter, end):
                                                                                                                                                     >>> first iterator. next ()
                                                                                                  while next_letter < end:
    yield next_letter</pre>
If the class of the exception inherits
                                                handling a <class 'ZeroDivisionError'>
 from <exception class>, then
                                                                                                      next letter = chr(ord(next letter)+1)
                                                                                                                                                     >>> for letter in
 The <except suite> is executed, with
                                                                                                                                                    letters_generator('a', 'e'):
 <name> bound to the exception.
                                                                                                                                                             print(letter)
                                                                                                A generator is an iterator backed
                                                                                                 by a generator function.
                                for <name> in <expression>:
     <suite>
                                                                                              • Each time a generator function is
                                                                                                 called, it returns a generator.
  1. Evaluate the header <expression>, which yields an iterable object.
   2. For each element in that sequence, in order:
      A. Bind <name> to that element in the first frame of the current
                                                                                                  A table has columns and rows
                                                                                                                                         A column has a name and a type
         environment.
      B. Execute the <suite>.
   An iterable object has a method __iter__ that returns an iterator.
                                                                                                         Latitude
                                                                                                                                 Longitude
                                             >>> items = counts.__iter__()
        >>> counts = [1, 2, 3]
>>> for item in counts:
                                             >>> trv:
                                                                                                                                                          ..Berkeley.....
                                                                                                   .....38.....
                                                                                                                            122
                                                     while True:
   item = items.__next__()
   print(item)
                print(item)
                                                                                                                                                           Cambridge
                                                 except StopIteration:
                                                                                                            45
                                                                                                                                     93
                                                                                                                                                          Minneapolis
                                                     pass
                                                                                                   A row has a value for each column
                                        >>> fibs = FibIter()
  class FibIter:
                                        >>> [next(fibs) for _ in range(10)]
[0, 1, 1, 2, 3, 5, 8, 13, 21, 34]
      def __init__(self):
    self(_next = 0)
                                                                                              select [expression] as [name], [expression] as [name], ...;
                                                                                              seer tournel from table | wer too distrion | order by [order];
           self._addend = 1
                    "Please do r't
          __next__(self):
result = self._next
                                                                                                 select "abraham"
                                                                                                                                    "barack" as child union
                                                                                                                      as parent,
                                                                                                 select "abraham"
                                                                                                                                    "clinton"
                                                                                                                                                          union
           self._addend, self._next = self._next, self._addend + self._next
                                                                                                 select "delano"
                                                                                                                                    "herbert"
                                                                                                                                                          union
           return result
                                                                                                 select "fillmore"
                                                                                                                                    "abraham'
                                                                                                                                                          union
  A stream is a linked list, but the re
                                                                                                 selet "fillmore"
Date frame om ;
                                                                                                                                    "delano"
                                                                                                                                                          union
                                                           Ochmputed in ted tists
                                                                                                                                   "grover"
"fillmore";
  of the list is computed on demand.
  Once created, Streams and Rlists can be
                                                                                              create table dogs as
                                                                                                select "abraham" as name, select "barack"
  used interchangeably using first and rest.
                                                                                                                                 "long" as fur union
                                                                                                                                 "short"
                                                                                                                                                  union
                                                                                                select "clinton"
                                                                                                                                 "long"
          'A lazily computed linked list.""
                                                                                                                                                  union
       class empty:

def __repr__(self):
    return 'Stream.e
                                                                                               select "delano"
select "delano"
select "filmore"
                                                                                                                                "long"
Short"
"curty"
                                                                         E alated
                                                                                                                                                  union
                                                                                                                                                            B 🗓 C
                       'Stream.emptv
                                                                                                                                                  union
        empty = empty()
                                                                                                select "grover"
                                                                                                                                 "short"
                                                                                                                                                  union
           __init__(self, first, compute_rest=lambda: Stream.empty):
assert callable(compute_rest), 'compute_rest must be callable.'
self.first = first
                                                                                                select "herbert"
                                                                                                                                "curly";
                                                                                                                                                                  First
                                                                                              select a.child as first, b.child as second
            self._compute_rest = compute_rest
                                                                                                                                                                 barack
                                                                                                from parents as a, parents as b
                                                                                                                                                                abraham
                                                                                                where a.parent = b.parent and a.child < b.child;
       @property
       def rest(self):
                                                                                                                                                                abraham
           icst():
""Return the rest of the stream, computing it if necessary."""
if self._compute_rest is not None:
    self._rest = self._compute_rest()
    self._compute_rest = None
return self._rest
                                                                                                                                                                 delano
                                                                                                ancestors(ancestor, descendent) as (
  select parent, child from parents union
                                                                                                   select ancestor, child
                                                                                                           from ancestors, parents
                                                                                                           where parent = descendent
   def integer_stream(first=1):
       def compute_rest():
    return integer stream(first+1)
                                                                                              select ancestor from ancestors where descendent="herbert";
        return Stream(first, compute_rest)
                                                                                              create table pythagorean_triples as
   def filter_stream(fn, s):
                                                 def map_stream(fn, s):
                                                                                                with
       if s is Stream, empty:
                                                     if s is Stream.empty:
                                                                                                   i(n) as (
        return s
def compute_rest():
                                                         return s
compute_rest():
                                                                                                     select 1 union select n+1 from i where n < 20
                                                     return map_stream(fn, s.rest)
return Stream(fn(s.first),
            return filter_stream(fn, s.rest)
        if fn(s.first):
                                                                                                 select a.n as a. b.n as b. c.n as c
            return Stream(s.first, compute_rest)
                                                                   compute_rest)
                                                                                                          from i as a, i as b, i as c
       else:
                                                                                                         where a.n < b.n and a.n*a.n + b.n*b.n = c.n*c.n;
           return compute_rest()
   def primes(positives):
                                                                                                                  Message sequence of a TCP connection
           def not_divisible(x):
           return x % positives.first != 0

def compute_rest():
    return primes(filter_stream(not_divisible, positives.rest))
return Stream(positives.first, compute_rest)
                                                                                                               Acknowledgement & synchronization request
                                                                                                                               Acknowledgement
    The way in which names are looked up in Scheme and Python is
    called lexical scope (or static scope).
                                                                                                 Ø
                                                                                                                          Data message from A to B \,
    Lexical scope: The parent of a frame is the environment in
                                                                                                 Computer
                                                                                                                    Acknowledgement
    which a procedure was defined. (lambda ...)
    Dynamic scope: The parent of a frame is the environment in
                                                                                                                          Data message from B to A
    which a procedure was called. (mu ...)
                                                                                                                  Acknowledgement
       > (define f (mu (x) (+ x y)))
> (define g (lambda (x y) (f (+ x x))))
```

> (g 3 7)

E

F

i D À,

н

а b С

3 4 5

5 12 13

6

8 15 17

9

12 16 20

G

Second

clinton

delano

grover

grover

ancestor

delano

fillmore

eisenhower

8 10

12 15

Computer

₩

Termination signal Acknowledgement & termination signal Acknowledgement

CS 61A Final Exam Study Guide - Page 2 A basic interpreter has two parts: a parser and an evaluator. scheme_reader.pv scalc.py Scheme programs consist of expressions, which can be: Primitive expressions: 2, 3.3, true, +, quotient,... Combinations: (quotient 10 2), (not true),... lines Parser Evaluator value expression Numbers are self-evaluating; symbols are bound to values. Call expressions have an operator and 0 or more operands. '(+ 2 2)' Pair('+', Pair(2, Pair(2, nil))) A combination that is not a call expression is a special form: • If expression: (if <predicate> <consequent> <alternative>) • Binding names: (define <name> <expression>) '(* (+ 1' Pair('*', Pair(Pair('+', ...))) New procedures: (define (<name> <formal parameters>) <body>) (- 23)' > (define pi 3.14) > (define (abs x) (* (+ 1 (- 23) (* 4 5.6)) 10) 10)' (if (< x 0) (- x)> (* pi 2) Lines forming A number or a Pair with an operator as its first element x)) a Scheme expression (abs -3)A Scheme list is written as elements in parentheses: Lambda expressions evaluate to anonymous procedures. (lambda (<formal-parameters>) <body>) A Scheme list (<element₀>)<element₁> ... <element_n>) Two equivalent expressions: Each <element> can be a combination or atom (primitive). (define (plus4 x) (+ x 4))(define plus4 (lambda (x) (+ x 4)))(+ (* 3 (+ (* 2 4) (+ 3 5))) (+ (- 10 7) 6)) An operator can be a combination too: The task of parsing a language involves coercing a string representation of an expression to the expression itself. ((lambda (x y z) (+ x y (square z))) 1 2 3)Parsers must validate that expressions are well-formed. In the late 1950s, computer scientists used confusing names. cons: Two-argument procedure that creates a pair car: Procedure that returns the first element of a pair cdr: Procedure that returns the second element of a pair A Parser takes a sequence of lines and returns an expression. Lexical Syntactic Lines Tokens Expression nil: The empty list analysis analysis They also used a non-obvious notation for linked lists. (linked) Scheme list is a pair in which the second element is nil or a Scheme list. Scheme lists are written as space-separated combinations. Pair('+', Pair(1, ...)) '(()(-(23)' '(', '-', 23, ')' printed as A dotted list has an arbitrary value for the second element of the last pair. Dotted lists may not be well-formed lists. (* 4 5.6)) '(', '*', 4, 5.6, ')', ')' (+ 1 (- 23) (* 4 5.6)) > (define x (cons 1 2)) Tree-recursive process Iterative process • Checks for malformed tokens Balances parentheses (1) 2) < Not a well-formed list! • Determines types of tokens • Returns tree structure > (car x) Processes one line at a time Processes multiple lines (cdr x) (cons 1 (cons 2 (cons 3 (cons 4 hi (1234)Each call to scheme_read consumes the input tokens for exactly Symbols normally refer to values; how do we refer to symbols? one expression. > (define a 1) Base case: symbols and numbers > (define b 2) > (list a b) (1 2) No sign of "1" and "b" in the result of vite S Quotation is used to refer to symbols directly in Lisp. Recursive call: scheme_read sub-expressions and combine them coder. The structure of the Scheme Primitive values (numbers) interpreter > (list 'a 'b) Look up values bound to symbols Symbols are now values Creates a new Recursive calls: > (list 'a b) environment each time a user-Eval(operator, operands) of call expressions (a 2) Apply (procedure argument Ev l) sub excessions) of Quotation can also be applied to complete defined procedure Ev > (car '(a b c)) а > (cdr '(a b c)) Requires an Apply (b c) Base cases: environment Built-in primitive procedures Dots can be used in a quoted list to specify the second for name element of the final pair. Recursive calls: Eval(body) of user-defined procedures > (cdr (cdr '(1 2 . 3))) 3 However, dots appear in the output only of ill-formed lists. To apply a user-defined procedure, create a new frame in which formal parameters are bound to argument values, whose parent '(1 2 . 3) 1 • 2 3 (1 2 . 3) > '(1 2 . (3 4)) (1 2 3 4) is the $\mbox{\it env}$ of the procedure, then evaluate the body of the procedure in the environment that starts with this new frame. \rightarrow 2 \bullet 3 \bullet 4 \bullet nil (define (f s) (if (null? s) '(3) (cons (car s) (f (cdr s))))) '(1 2 3 . nil) $\rightarrow 2 \rightarrow 3 \rightarrow nil$ $(1\ 2\ 3)$ (f (list 1 2)) > (cdr '((1 2) . (3 4 . (5)))) g: Global frame (3 4 5) LambdaProcedure instance [parent=g] The Calculator language has primitive expressions and call expressions "A Pair has first and second attributes. 1 2 [parent=q] s For a Pair to be a well-formed list, second is either a well-formed list or nil. [parent=g] s Calculator Expression init (self, first, second): [parent=g] self.first = first self.second = second (* 6 7 8)) A procedure call that has not yet returned is active. Some procedure calls are tail calls. A Scheme interpreter should >>> s = Pair(1, Pair(2, Pair(3, nil))) Expression Tree support an unbounded number of active tail calls. A tail call is a call expression in a tail context, which are: >>> print(s) The last body expression in a lambda expression Expressions 2 & 3 (consequent & alternative) in a tail context >>> len(s) >>> print(Pair(1, 2)) if expression (define (factorial n k) (define (length s) >>> print(Pair(1, Pair(2, 3))) (if (= n 0) k(i,f..(null?..s)..0..... Representation as Pairs

8 nil

3

nil

5

(factorial (- n 1) (+ 1 (length (cdr s))))) (* k n)))) Not a tail call (define (length-tail s) (Recursive call is a tail call (define (length-iter s n) (if (null? s) n (length-iter (cdr s) (+ 1 n));)) (length-iter s 0))

is applied