CS 61A Fall 2014

Structure and Interpretation of Computer Programs

FINAL EXAM SOLUTIONS

INSTRUCTIONS

- You have 3 hours to complete the exam.
- The exam is closed book, closed notes, closed computer, closed calculator, except one hand-written 8.5" × 11" crib sheet of your own creation and the 3 official 61A midterm study guides attached to the back of this exam.
- Mark your answers ON THE EXAM ITSELF. If you are not sure of your answer you may wish to provide a brief explanation.

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Name of the person to your right	
All the work on this exam is my own. (please sign)	

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Q. 1	Q. 2	Q. 3	Q. 4	Q. 5	Q. 6	Total	
/14	/16	/12	/12	/18	/8	/80	

1. (14 points) Representing Scheme Lists

For each row below, write the output displayed by the interactive Python interpreter when the expression is evaluated. Expressions are evaluated in order, and **expressions may affect later expressions**.

Whenever the interpreter would report an error, write ERROR. You *should* include any lines displayed before an error. *Reminder*: The interactive interpreter displays the **repr** string of the value of a successfully evaluated expression, unless it is None.

The Pair class from Project 4 is described on your final study guide. Recall that its <code>__str__</code> method returns a Scheme expression, and its <code>__repr__</code> method returns a Python expression. The full implementation of Pair and nil appear at the end of the exam as an appendix. Assume that you have started Python 3, loaded Pair and nil from <code>scheme_reader.py</code>, then executed the following:

```
blue = Pair(3, Pair(4, nil))
gold = Pair(Pair(6, 7), Pair(8, 9))

def process(s):
    cal = s
    while isinstance(cal, Pair):
        cal.bear = s
        cal = cal.second
    if cal is s:
        return cal
    else Assignment Project Exam Help

def display(f, s):
    if isinstance(ttpsir)//powcoder.com
        print(s.first)//powcoder.com
```

y = lambda f: lambda x: f(f, x)

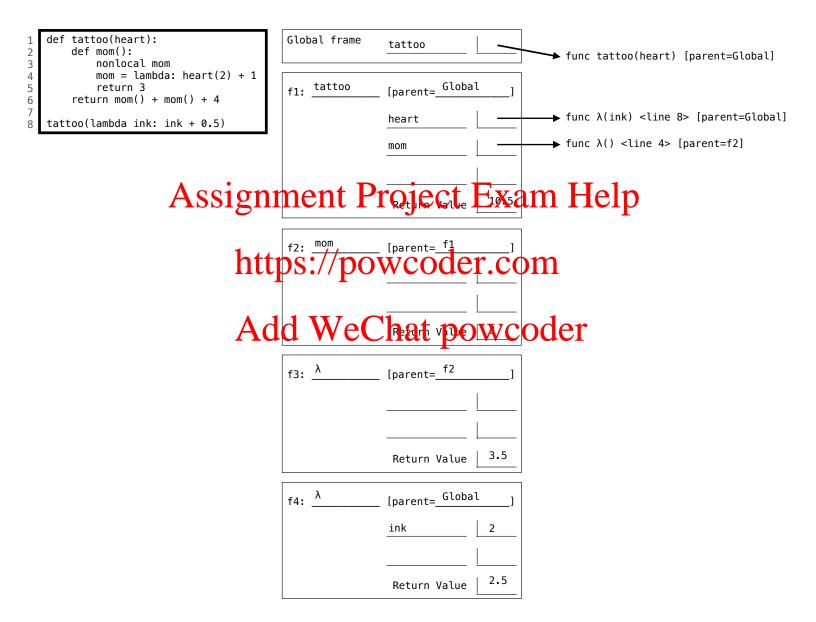
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Expression	Output	Expression	Output
Pair(1, nil)	Pair(1, nil)		Pair(nil, Pair(4, nil))
<pre>print(Pair(1, nil))</pre>	(1)	nmasagg(hlus gasand)	
1/0	Error	process(blue.second)	
	3		
	Error		(9 (6 . 7) 9 8 . 9)
<pre>print(print(3), 1/0)</pre>		<pre>print(process(gold))</pre>	
<pre>print(Pair(2, blue))</pre>	(2 3 4)	gold.second.bear.first	8
print(gold)	((6 . 7) 8 . 9)	y(display)(gold)	8 None (6 . 7) None

2. (16 points) Environments

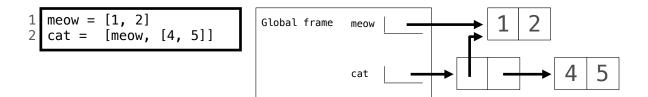
- (a) (8 pt) Fill in the environment diagram that results from executing the code below until the entire program is finished, an error occurs, or all frames are filled. You may not need to use all of the spaces or frames.

 A complete answer will:
 - Add all missing names and parent annotations to all local frames.
 - Add all missing values created during execution.
 - Show the return value for each local frame.



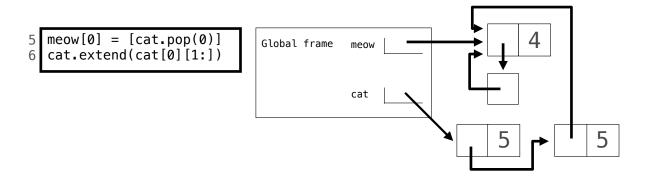
(b) (6 pt) For the six-line program below, fill in the three environment diagrams that would result after executing each pair of lines in order. You must use box-and-pointer diagrams to represent list values. You do not need to write the word "list" or write index numbers.

Important: All six lines of code are executed in order! Line 3 is executed after line 2 and line 5 after line 4.





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(c) (2 pt) Circle the value, True or False, of each expression below when evaluated in the environment created by executing all six lines above. If you leave this question blank, you will receive 1 point.

```
(True / False) meow is cat[0] (True / False) meow[0][0] is cat[0][0]
```

3. (12 points) Expression Trees

Your partner has created an interpreter for a language that can add or multiply positive integers. Expressions are represented as instances of the Tree class and must have one of the following three forms:

- (Primitive) A positive integer entry and no branches, representing an integer
- (Combination) The entry '+', representing the sum of the values of its branches
- (Combination) The entry '*', representing the product of the values of its branches

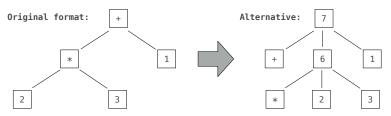
The Tree class is on the Midterm 2 Study Guide. The sum of no values is 0. The product of no values is 1.

(a) (6 pt) Unfortunately, multiplication in Python is broken on your computer. Implement eval_with_add, which evaluates an expression without using multiplication. You may fill the blanks with names or call expressions, but the only way you are allowed to combine two numbers is using addition.

```
def eval_with_add(t):
   """Evaluate an expression tree of * and + using only addition.
   >>> plus = Tree('+', [Tree(2), Tree(3)])
   >>> eval_with_add(plus)
   >>> times = Tree('*', [Tree(2), Tree(3)])
   >>> eval_with_add(times)
                         t.Project.Exam Help
   >>> eval_with_add(deep)
   60
   *** eval_whttps://powcoder.com
   .....
   if t.entry == '+':
       return Add wallie Chatepowcoder])
   elif t.entry == '*':
       total = 1
       for b in t.branches:
           term, total = total, 0
           for _ in range(eval_with_add(b)):
               total = total + term
       return total
   else:
       return t.entry
```

(b) (6 pt) A TA suggests an alternative representation of an expression, in which the entry is the value of the expression. For combinations, the operator appears in the left-most (index 0) branch as a leaf.

Note: This question was updated from its original published version, which had a flaw in the provided code.



Implement transform, which takes an expression and mutates all combinations so that their entries are values and their first branches are operators. In addition, transform should return the value of its argument. You may use the calc_apply function defined below.

```
def calc_apply(operator, args):
   if operator == '+':
       return sum(args)
   elif operator == '*':
       return product(args)
def project Exam Help
   for v in vals:
       total *= v
              ttps://powcoder.com
def transform(t):
   """Transform expression tree t to have value entries and operators leaves.
                     Wechat pow, Goder, Tree (1)])
   >>> transform(seven)
   7
   >>> seven
   Tree(7, [Tree(+), Tree(6, [Tree(*), Tree(2), Tree(3)]), Tree(1)])
   if t.entry in ('*', '+'):
       args = []
       for b in t.branches:
           args.append(transform(b))
       t.branches = [Tree(t.entry)] + t.branches
       t.entry = calc_apply(t.entry, args)
   return t.entry
```

4. (12 points) Lazy Sunday

(a) (4 pt) A flat-map operation maps a function over a sequence and flattens the result. Implement the flat_map method of the FlatMapper class. You may use at most 3 lines of code, indented however you choose.

class FlatMapper:

"""A FlatMapper takes a function fn that returns an iterable value. The flat_map method takes an iterable s and returns a generator over all values that are within the iterables returned by calling fn on each element of s.

```
>>> stutter = lambda x: [x, x]
>>> m = FlatMapper(stutter)
>>> g = m.flat_map((2, 3, 4, 5))
>>> type(g)
<class 'generator'>
>>> list(g)
[2, 2, 3, 3, 4, 4, 5, 5]
"""
```

def __init__(self, fn):

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def flat_mhttps://powcoder.com

for x in s:

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yield r

(b) (2 pt) Define cycle that returns a Stream repeating the digits 1, 3, 0, 2, and 4. Hint: (3+2)%5 equals 0.

```
"""Return a stream repeating 1, 3, 0, 2, 4 forever.

>>> first_k(cycle(), 11) # Return the first 11 elements as a list
[1, 3, 0, 2, 4, 1, 3, 0, 2, 4, 1]
"""

def compute_rest():

   return cycle((start+2) % 5)

return Stream(start, compute_rest)
```

(c) (4 pt) Implement the Scheme procedure directions, which takes a number n and a symbol sym that is bound to a nested list of numbers. It returns a Scheme expression that evaluates to n by repeatedly applying car and cdr to the nested list. Assume that n appears exactly once in the nested list bound to sym.

Hint: The implementation searches for the number **n** in the nested list **s** that is bound to **sym**. The returned expression is built during the search. See the tests at the bottom of the page for usage examples.

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(rest (search (cdr s) (list 'cdr exp))))

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(search (eval sym) sym))

```
(define a '(1 Add'4WeChat powcoder
(directions 1 a)
(directions 2 'a)
(directions 2 'a)
(define b '((3 4) 5))
(directions 4 'b)
( expect (car (cdr (car b)))
```

(d) (2 pt) What expression will (directions 4 'a) evaluate to?

```
(car (car (cdr (cdr a)))))
```

5. (18 points) Basis Loaded

Ben Bitdiddle notices that any positive integer can be expressed as a sum of powers of 2. Some examples:

```
11 = 8 + 2 + 1
23 = 16 + 4 + 2 + 1
24 = 16 + 8
45 = 32 + 8 + 4 + 1
2014 = 1024 + 512 + 256 + 128 + 64 + 16 + 8 + 4 + 2
```

A basis is a linked list of decreasing integers (such as powers of 2) with the property that any positive integer n can be expressed as the sum of elements in the basis, starting with the largest element that is less than or equal to n.

(a) (4 pt) Implement sum_to, which takes a positive integer n and a linked list of decreasing integers basis. It returns a linked list of elements of the basis that sum to n, starting with the largest element of basis that is less than or equal to n. If no such sum exists, raise an ArithmeticError. Each number in basis can only be used once (or not at all). The Link class is described on your Midterm 2 Study Guide.

```
def sum_to(n, basis):
   """Return a sublist of linked list basis that sums to n.
   >>> twos = Link(32, Link(16, Link(8, Link(4, Link(2, Link(1))))))
   **Assignment, Project Exam Help
   Link(8, Link(2)
   >>> sum_to(24, twos)
   Link(16, Link(8))
   >>> sum_to https://powcoder.com
   >>> sum_to(32, twos)
   Link(32)
   11 11 11
            Add WeChat powcoder
   if n == 0:
       return Link.empty
   elif basis == Link.empty:
       raise ArithmeticError
   elif basis.first > n:
       return sum_to(n, basis.rest)
   else:
       return Link(basis.first, sum_to(n-basis.first, basis.rest))
```

(b) (6 pt) Cross out as many lines as possible in the implementation of the FibLink class so that all doctests pass. A FibLink is a subclass of Link that contains decreasing Fibonacci numbers. The up_to method returns a FibLink instance whose first element is the largest Fibonacci number that is less than or equal to positive integer n.

```
class FibLink(Link):
   """Linked list of Fibonacci numbers.
   >>> ten = FibLink(2, FibLink(1)).up_to(10)
   >>> ten
   Link(8, Link(5, Link(3, Link(2, Link(1)))))
   >>> ten.up_to(1)
   Link(1)
   >>> six, thirteen = ten.up_to(6), ten.up_to(13)
   Link(5, Link(3, Link(2, Link(1))))
   >>> thirteen
   Link(13, Link(8, Link(5, Link(3, Link(2, Link(1))))))
   @property
   def successor(self):
       ssignment Project Exam Help
       if self.first == n:
          return self
       elif shttps://powcoder.com
       elif self.successor > n:
          return self
                dd.WeChat.powcoder
       else:
```

(c) (2 pt) Circle the Θ expression below that describes the number of calls made to FibLink.up_to when evaluating FibLink(2, FibLink(1)).up_to(n). The constant ϕ is $\frac{1+\sqrt{5}}{2}=1.618...$

 $\Theta(1)$ $\Theta(\log_{\phi} n)$ $\Theta(n)$ $\Theta(n^2)$ $\Theta(\phi^n)$

(d) (2 pt) Alyssa P. Hacker remarks that Fibonacci numbers also form a basis. How many total calls to FibLink.up_to will be made while evaluating all the doctests of the fib_basis function below? Assume that sum_to and FibLink are implemented correctly. Write your answer in the box.

```
def fib_basis():
    """Fibonacci basis with caching.
                                                           10
   >>> r = fib_basis()
   >>> r(11)
   Link(8, Link(3))
   >>> r(23)
   Link(21, Link(2))
   >>> r(24)
   Link(21, Link(3))
   >>> r(45)
   Link(34, Link(8, Link(3)))
   fibs = FibLink(2, FibLink(1))
   def represent(n):
       nonlocal fibs
       fibs = fibs.up_to(n)
       return sum_to(n, fibs)
                            Project Exam Help
```

(e) (4 pt) Implement fib_sums, a function that takes positive integer n and returns the number of ways that n can be expressed as a sum of unique Fibonacci numbers. Assume that FibLink is implemented correctly.

```
def fib_sums(nhttps://powcoder.com
"""The number of ways r can be expressed as a sum of unique Fibonacci numbers.
```

```
>>> fib_sums(9) # 8+1, 5+3+1
2
>>> fib_sums(12) # 8+3+1
1
>>> fib_sums(13) # 13, 8+5, 8+3+2
3
"""

def sums(n, fibs):
    if n == 0:
        return 1
    elif fibs == Link.empty or n < 0:
        return 0
        a = sums(n-fibs.first, fibs.rest)
        b = sums(n, fibs.rest)
        return a + b

return sums(n, FibLink(2, FibLink(1)).up_to(n))</pre>
```

6. (8 points) Sequels

Assume that the following table of movie ratings has been created.

```
create table ratings as
                                                               Correct output
  select "The Matrix" as title, 9 as rating union
                                                                Judgment Day
  select "The Matrix Reloaded",
                                                  union
                                                                 Terminator
  select "The Matrix Revolutions", 5
                                                  union
                                                                 The Matrix
  select "Toy Story",
                                                  union
                                                                 Toy Story
  select "Toy Story 2"
                                                  union
                                                                 Toy Story 2
  select "Toy Story 3",
                                                  union
                                                                 Toy Story 3
  select "Terminator",
                                                  union
  select "Judgment Day",
                                                  union
  select "Rise of the Machines",
                                     5;
```

The correct output table for both questions below happens to be the same. It appears above to the right for your reference. **Do not hard code your solution to work only with this table!** Your implementations should work correctly even if the contents of the ratings table were to change.

(a) (2 pt) Select the titles of all movies that have a rating greater than 7 in alphabetical order.

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select title from ratings where rating > 7 order by title;

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(b) (6 pt) Select the tales of all notics to which at least 2 other provies have the same rating. The results should appear in alphabetical order. Repeated results are acceptable. You may only use the SQL features introduced in this course.

```
with
  groups(name, score, n) as (
  select title, rating, 1 from ratings union
  select title, score, n+1 from groups, ratings
  where title > name and rating=score
)
select title from groups, ratings
where rating=score and n > 2 order by title;
```