$\begin{array}{c} \mathrm{CS}\ 61\mathrm{A} \\ \mathrm{Spring}\ 2016 \end{array}$

Structure and Interpretation of Computer Programs

FINAL EXAMINATION SOLUTIONS (WITH CORRECTIONS)

INSTRUCTIONS

- This exam should have 19 pages. You have 3 hours to complete the exam.
- The exam is open book, open notes, closed computer, closed calculator. The official CS 61A midterm 1, 2, and final study guides will be provided.
- Mark your answers on the exam itself. We will not grade answers written on scratch paper.

Last name	
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Student ID numberttps://po	wcoder.com
BearFacts email (Oberkeley edu) Add We(Chat powcoder
If you took the HKN survey, your code.	
Room in which you are taking this exam	
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Name of the person to your left	
Name of the person to your right	
I pledge my honor that during this examination I have neither given nor received assistance. (please sign)	

Reference. Some questions make use of the following class definitions from labs and homework. There is one difference: we have changed the definition of Link.empty so that it is a kind of Link instead of the empty tuple.

```
class Link:
   def __init__(self, first, rest=None):
       # When called as Link(x), resets rest to empty
       if rest is None:
           rest = Link.empty
       self.first = first
       self.rest = rest
   def __repr__(self): ... # (Not shown)
class EmptyLink(Link):
   def __init__(self):
Link.empty = EmptyLink()
                         # This makes Link.empty a special kind of Link
class Tree:
   def __init__(self, label, children=()):
       self.label = label
       self.children = list(children)
                           ent Project Exam Help
       return not self.children
   def __repr__(se f)ttp$://powcoder.com
class BinTree:
   empty = ()
   def __init__(selAdd, 1W=exty.hiat=eprowcoder
       self.label = label
       self.left = left
       self.right = right
class Stream:
   class empty:
       pass
    empty = empty()
   def __init__(self, first, compute_rest=lambda: Stream.empty):
       self.first, self._compute_rest = first, compute_rest
   @property
   def rest(self):
       if self._compute_rest is not None:
           self._rest, self._compute_rest = self._compute_rest(), None
       return self._rest
```

Name: _______ 3

1. (8 points) Silence of the Lambdas

For each of the expressions in the table below, write the output displayed by the interactive Python interpreter when the expression is evaluated. The output may have multiple lines. If an error occurs, write "Error". If an expression yields (or prints) a function, write "<Function>". The first two rows have been provided as examples.

Important: The statements in the table are cumulative—assume that all preceding statements in the table have been executed before each entry.

Assume that python3 has executed the statements on the left initially:

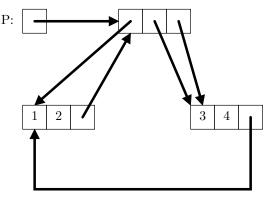
	Expression	Interactive Output
<pre>foster = 1 def f(foster): hopkins = foster+1 def g(glenn): nonlocal foster foster = glenn hopkins = 2*glern nent return (g, lambda. foster, hopkins])</pre> <pre>https://pov</pre>	pow(2, 3)	8
	print(4, 5) + 1	4 5
		Error
	levine, demme = $f(5)$	1
	foster	
	demme	<function></function>
	tally = demme()	5
	tally[0]	
	tally[1]	6
	ojectne xam He	lp-
	foster	1
	vally = demme()	9
	tally[1]	6

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2. (8 points) Point(er) of Order

(a) (3 pt) Fill in code on the left that, when executed, yields the situation on the right. Assume that the objects are Python lists. Single boxes with labels to their left denote variables, not list objects.

```
P = [ [ 1, 2, None], [ 3, 4, None ], None ]
P[0][2] = P
P[1][2] = P[0]
P[2] = P[1]
```



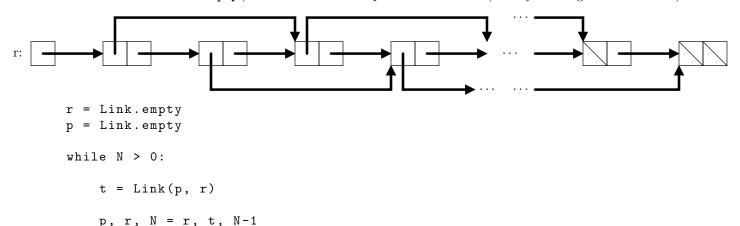
(b) (1 pt) Why can't the structure depicted in the diagram for part (a) be built from Python tuples, no matter what program is used on the left? Give a brief answer in a few sentences.

The contents of the items in a tuple have to be constructed before the tuple itself. Once created, a tuple cannot be changed Since P count by created be part of [6] [2] cannot be set later, which is impossible.

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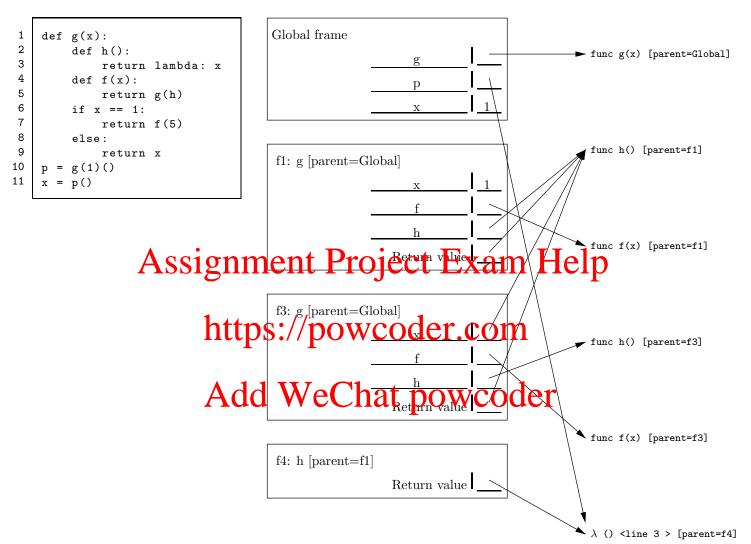
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(c) (4 pt) In the diagram below, the two-slot objects are Links (see page 2). There are N of these Link objects altogether, with each .first field pointing to the second Link following it (except for the last two, whose .first fields are Link.empty.) Fill in the blanks to produce such a list (for any non-negative value of N.)



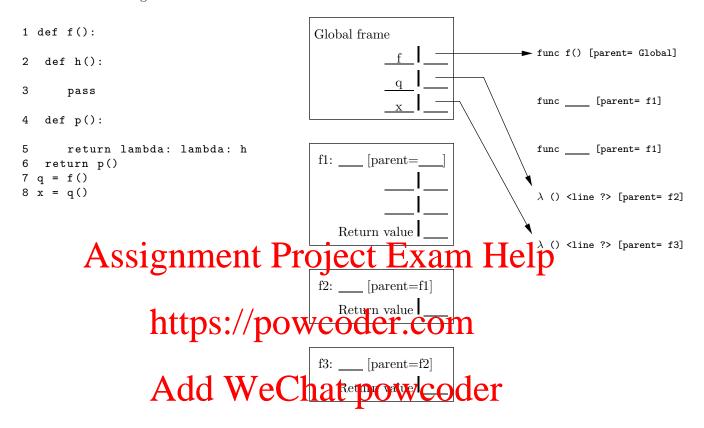
3. (8 points) Environmentally Sound

(a) (6 pt) Fill in the environment diagram that results from executing the code below until the entire program is finished. Fill in the function values (func ...[parent=...]) with all function values created during execution. As you can see from the numbering, some environment frames are not shown. Include only the environment frames for the functions indicated in the frames shown.



(b) (3 pt)

The diagram on the right below shows part of an environment diagram; various items are left blank, and various arrows are not shown. Fill in the blanks in the program on the left so as to create a situation consistent with the diagram on the right (you do not have to fill in any of the blanks in the environment diagram.) Assume that any variable or function is assigned or defined exactly once. Assume also that function values that start with func in the diagram are defined with def.



4. (10 points) Tiptoe through the Links

During the semester, we defined a __getitem__ method for the Link class. With a little revision, it allows us to use Python iteration:

```
def __getitem__(self, k):
    if self is Link.empty:
        raise IndexError
    elif k == 0:
        return self.first
    else:
        return self.rest[k-1]
```

(Here, we are making use of the definition of Link.empty on page 2, so that it works on empty lists.) If this definition is added to Link, Links become iterable: the Python iter function (used by for, and other constructs that deal with iterables) is able to create an iterator whose __next__ method calls __getitem__ with k set to 0, 1, 2, ..., until IndexError is raised.

(a) (1 pt) Assuming that Link.__getitem__ is defined as shown, what is the execution time of

```
for i in L:
    print(i)
```

if L is a LinAthst signification of the Project Exam Help

- A. $\Theta(1)$
- B. $\Theta(\log N)$

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- C. $\Theta(\sqrt{N})$
- D. $\Theta(N)$

E. $\Theta(N^2)$

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F. $\Theta(2^N)$

Problem continues on next page.

(b) (5 pt) Suppose that instead of defining Link.__getitem__, we instead want to define Link.__iter__ to return some kind of iterator whose __next__ method runs in constant time (so it won't work to count from the beginning of the list each time). Fill in the definition of ListIter (whose instances are intended to be iterators over linked lists) and Link.__iter__ to make Link an iterable class whose iterators take constant time to perform a __next__ operation. Warning: The Link class in this exam does not include __len__, so the len function does not work.

```
class ListIter:
    def __init__(self, lst):
        self.lst = lst

def __next__(self):
    if self is Link.empty:
        raise StopIteration
    r = self.lst.first
        self.lst = self.lst.rest
        return r

class Link:
    ...
    def __iter__(self):
```

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(c) (1 pt) For the revised Link class from part (b), what is the execution time of

```
for i in L: print(i) https://powcoder.com
```

if L is a Link that heads a linked list of length N? (Assume your solution in (b) works as specified, regardless of what you wrote).

A. $\Theta(1)$

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- B. $\Theta(\log N)$
- C. $\Theta(\sqrt{N})$
- D. $\Theta(N)$
- E. $\Theta(N^2)$
- F. $\Theta(2^N)$

(d) (3 pt) Now re-implement __iter__ from part (b) so that instead of using a separate iterator class, it creates a generator (so that from the user's point of view, execution of for i in L does not change). (Not all lines need be used.)

```
class Link:
    ...
    def __iter__(self):
        L = self
        while L is not Link.empty:
            yield L.first
        L = L.rest
```

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5. (12 points) Triangular!

In a (lower) triangular array (which we represent as a Python list of lists), row r has length r+1, like this:

Suppose that we choose one item from each row of this triangle in such a way that if we choose item #k in row #r, we choose either item #k or #k+1 from row #r+1. Assuming our arrays contain integers, you are to write a program to find the maximum sum of a proper choice of selected items from all rows.

In the example above, we can maximize our sum by choosing the boxed items: item 0 from row 0, item 0 from row 1, item 1 from row 2, and item 1 from row 3 (summing to 5). Choosing instead to take the last item (1) of the first three rows would only give us a sum of 4, since we could not then choose either of the 3's from the last row.

(a) (5 pt) Fill in the blanks in the following recursive program to find the maximum sum:

```
def triangle_sum(tri):
    """General Triangle of the from each row, where ref
    item #k is selected from row #r, either item #k or item #k+1 is
    selected from row #r+1."""
    rows = len(triangle of the from rows fr
```

- (b) (1 pt) As a function of the number of rows, R, of the input triangle, what is the running time of this program?
 - A. $\Theta(R)$
 - B. $\Theta(R^2)$
 - C. $\Theta(\sqrt{R})$
 - D. $\Theta(\log R)$
 - E. $\Theta(2^R)$

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- (c) (5 pt) The program may be sped up by noticing that
 - When the inner function gets called with the same arguments multiple times, it always returns the same
 - The values of the inner function when called on a given row depend only on the values of the function on the row below it.

Use these observations to create a faster, iterative version of the program.

```
def triangle_sum(tri):
    """Given that tri is a triangular array, return the maximum
    sum attainable by selecting one item from each row, where if
    item k is selected from row r, either item k or item k+1 is
    selected from row r+1."""
    # Create a deep copy of tri to avoid destroying the input data.
    tri = [ list(row) for row in tri ]
    rows = len(tri)
    r = rows - 2
    while r >= 0:
```

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tri[r][k] += max(tri[r+1][k], tri[r+1][k+1])

¹ https://powcoder.com

return tri[0][0]

- (d) (1 pt) As a function of the number of two, R, of the input triangle, what is the running time of this program?

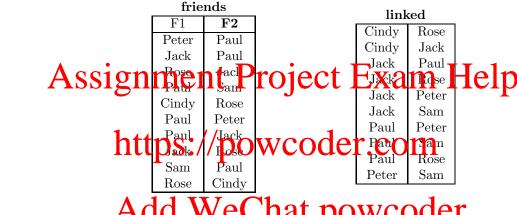
 A O(R)
 - A. $\Theta(R)$
 - B. $\Theta(R^2)$
 - C. $\Theta(\sqrt{R})$
 - D. $\Theta(\log R)$
 - E. $\Theta(2^R)$

6. (8 points) Six Degrees of Separation

You've probably heard that we are all within "six degrees of separation." That is, either we are friends (one degree), friends of friends (two degrees), friends of friends (three degrees), etc. up to six degrees. We may, of course, be separated by several different distances, as when our friend is also a friend of a friend. Although there are obviously many different paths leading from you back to yourself, however, we won't consider you as being connected with yourself.

Suppose that friends is an SQL table with two columns, F1 and F2, where in each row, F1 and F2 are the names of two friends—i.e., two people with one degree of separation between them. To make life easier, we'll assume that if (Peter, Paul) is in the table, then so is (Paul, Peter). We would like an SQL query that produces a two-column table named linked of people separated (by some chain of friends) by N or fewer degrees of separation, where N is some integer. In your solution, use 'N' as if it is an integer literal, like 6. (The idea of using 'N' instead of a specific number is to force your solution to be general.) Each pair in the resulting table should appear exactly once, with the name in the first column being first in alphabetical order.

For example, suppose that N=2, then given the friends table on the left, we should get the linked table on the right, in some order. (The column names don't matter for linked, and so are not shown.)



create table linked das WeChat powcoder

```
with sep(S1, S2, degrees) as (
    select F1, F2, 1 from friends union
    select F1, S2, degrees + 1 from friends, sep
        where degrees < N and F2 = S1
)
select distinct S1, S2 from sep where S1 < S2;</pre>
```

7. (4 points) Tail Recursing the Dog

Fill in the Scheme iota function so that (iota n) produces a list of the numbers from 1 to n (empty if n is not positive). The resulting add-iota function must be tail-recursive.

```
scm> (iota 5)
  (1 2 3 4 5)
  scm> (iota 0)
  ()
  scm> (iota -5)
  ()

(define (iota n)
  (define (add-iota lst m)

  (if (< m 1)</pre>
```

lst

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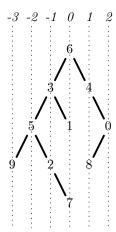
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- 8. (1 points) Sum of Human Knowledge What may be recognized by the following characteristics?
 - A meager and hollow, but crisp, taste.
 - A habit of getting up late.
 - A slowness in taking a jest.
 - A fondness for bathing machines.
 - Ambition.

A nerrore	A gnort	

9. (8 points) In the Trees

If you are careful about how you draw a binary tree, its nodes will line up in columns. Here, for example, is a tree with six columns of nodes (indicated by dotted lines; the numbers at top are column numbers):



Let's designate the column containing the root as column 0. For any node in column k, we'll says its left child is in column k-1 and its right in column k+1. In general, nodes will overlap when you do this, but we'll ignore that possibility.

Write a program to print all the nodes in a given column of a tree, given the tree and the column number. The type BinTree satisfied in the Column of page to of this test (Don't forget that the empty tree is a valid input to print_column.) You may not need all the lines.

```
def print_column(tree, col):
                         """Print the hatels of the odes in any order, the production of th
                          >>> e = BinTree.empty
                                                tree = BinTree(6,
                                                                                                                                                                                                                                                                                   \mathbf{Oo}_{\mathbf{n}}Ve\mathbf{Codel}_{\mathsf{Tree}(2,\ \mathsf{e},\ \mathsf{BinTree}(7))},
                                                                                                                                                           BinTree(4, e, BinTree(0, BinTree(8))))
                          >>> print_column(tree, -1)
                          >>> print_column(tree, 2)
                          0"""
                          def print_inner(t, k):
                                                     if t is BinTree.empty:
                                                                                 return
                                                     if k == col:
                                                                                print(t.label)
                                                     else:
                                                                                print_inner(t.left, k-1)
                                                                               print_inner(t.right, k+1)
```

print_inner(tree, 0)

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10. (10 points) Treebeard's Revenge

This problem combines Trees and Links (see the reference section on page 2). (Be careful not to confuse type Tree with type BinTree used earlier.)

(a) (5 pt) Fill in the tree_search function so that tree_search(tr, pred) returns a linked list of all labels in tr (of type Tree) that satisfy pred (that is, for which the one-argument function pred returns a true value). The order of the list is irrelevant.

(b) (5 pt) An Organizer is a kind of object that divides the labels in a tree into a sequence of disjoint lists, one for each of a given set of categories. To create an Organizer, one provides a sequence of predicates (one-argument functions) that define the categories. When this object is subsequently handed a Tree, it will return a sequence of linked lists of tree labels, one per category in the same order as the original sequence of category predicates. Once a tree label is included in one list, it must not appear again in that list, nor in any subsequent list. Fill in the class below to fulfill this specification. You may assume that labels are numbers or strings.

class Organizer:

```
def __init__(self, categories):
    """Create a new Organizer whose categories are defined by the
    predicates in CATEGORIES (an iterable)."""
    self._categories = categories
def categorize(self, tr):
    """Return a Python sequence of linked lists, where the kth
    list contains tree labels from TR that satisfy my kth
    category. Each tree label appears exactly once in the entire
    set of lists returned, regardless of how often it occurs in TR.
    NOTE: The order of values in the linked lists in the example
    below is just one possible result.
    >>> tr = Tree(6, [Tree(3, [ Tree(5, [Tree(9), Tree(2, [Tree(9)])]),
                            roject Exam
                      Tree(4, [Tree(0, [Tree(4)])])
    >>> or = Organizer([lambda x: x > 4, lambda x: x\%2 == 0])
    >>> or.categorize(tr)
    result = []
    labels_seen = []
                               at powcoder
    def take it
            labels_seen.append(x)
           return True
        return False
    for pred in self._categories:
        result.append(tree_search(tr, take_it))
    return result
```

11. (4 points) Exstream!

You may have seen the power series for computing the exponential function:

$$e^x = \sum_{k>0} \frac{x^k}{k!} = 1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots$$

By computing and adding one term at a time, one can get as close as desired to the value of e^x , giving an infinite sequence of approximations:

1,
$$1+x$$
, $1+x+\frac{x^2}{2!}$, $1+x+\frac{x^2}{2!}+\frac{x^3}{3!}$,....

Fill in the blanks below so that e2x(x) creates a Python Stream (see page 2) consisting of this sequence of approximations. Do not introduce any additional lambda expressions or def statements than are already there.

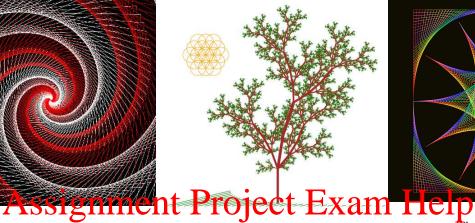
Scheme Art Contest Winners Featherweight Division

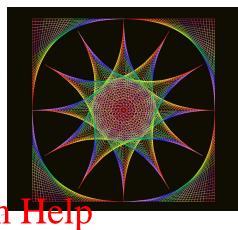
First Place Recursive Bleeding Carson Trinh

Second Place (tie) tree in early spring Matej Sebo

Second Place (tie) T.L.O.P Abraham Chen, Bill Cai







Hilfinger in spring and then Hilfinger in fall

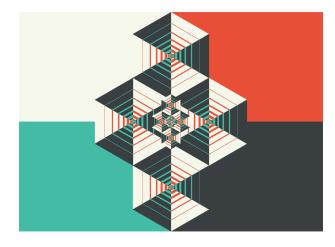
then Hilfinger in fall tree in early spring
Will it ever https://power.com/
Into myrida leaves

The Life of Pablo Vote yes and we'll love you like Kanye loves Kanye

Heavyweight Division Add WeChat powcoder

First Place Twisted Logic Kyla Woyshner

Second Place Stairway to Heaven Sharabesh Ramesh, Jared Gutierrez



What if you were lost, An endless kaleidoscope, No hope of square one



The one last project Alone it stands defeated 61A no more