MAST20005/MAST90058: Week 8 Problems

Some useful information for many of the problems is shown at end of this problem sheet.

1. Random digits (group activity). A volunteer in each group should write down a string of 51 random digits, such as:

3 7 2 4 1 6 8 5...

For each digit, record whether: (i) the next digit is the same as the preceding one (e.g. '2 2') and (ii) the next digit differs from the preceding one by 1 (e.g. '2 3'). For the purpose of this exercise, assume that the digits 0 and 9 only differ by 1. After the volunteer writes down 51 numbers, the entire group should carry out a hypothesis test at the 5% level of significance to determine whether the volunteer's sequence of numbers is truly random (you will need to think carefully about what this means and how to translate it into an appropriate null hypothesis).

- 2. Strawberries are being packed for the market. It is claimed that the median weight, m, of these boxes is 40 kilograms.
 - (a) Use the following data and a Wilcoxon test statistic at an approximate significance level of $\alpha = 0.05$ to test the null hypothesis H_0 : m = 40 against H_1 : m < 40.

Assignment₃₆84r,05 ect. 817, xam₄13,e1p₅, 31.031, 40.780, 38.050, 30.906

It may help to complete the following table. Ties are assigned the average rank.

nttps://powcoder eetat powcoder 4 36.840 5 38.050 6 40.890 38.345 8 34.9309 39.24510 31.031 11 40.78012 38.05013 30.906

- (b) Give limits for the p-value of this test.
- (c) Use the sign test to test the same hypothesis.
- (d) Compare the results of the two tests.
- 3. In a biology laboratory the mating of two red-eye fruit flies yielded n=432 offspring among which 254 were red-eyed, 69 were brown-eyed, 87 were scarlet-eyed, and 22 were white-eyed. Use these data to test, with $\alpha=0.05$, the hypothesis that the ratio among the offspring would be 9:3:3:1 respectively.

4. We wish to determine if two groups of nurses distribute their time in six different categories about the same way. That is, the hypothesis under consideration is H_0 : $p_{i1} = p_{i2}$, $i = 1, \ldots, 6$. To test this, nurses are observed at random throughout several days, each observation resulting in a mark in one of the six categories. The summary data are given in the following frequency table:

	Category						
	1	2	3	4	5	6	Total
Group I Group II							

Do a chi-squared test with $\alpha = 0.05$.

Some potentially helpful R output: