# Assignment Project Exam Help

## https://powcoder.com



Statistics (MAST20005) & Elements of Statistics

Chat powerouser

School of Mathematics and Statistics University of Melbourne

Semester 2, 2022

#### Aims of this module

- A Superin Heart Institute of the concepts behind statistical hypothesis testing Help
  - Work through a number of common testing scenarios

#### Outline

**Preface** 

# Assignment Project Exam Help

Classical hypothesis testing (Neyman-Pearson)

Hypotheses

https://powcoder.com

Significance level & power

Alternative formulations

Add WeChat powcoder

Modern hypothesis testing

Common scenarios

Single proportion

Two proportions

Single mean

3 of 100ngle variance

#### What we are about to do...

- ASSI SALAR SILE IN THE WEEKS WE WILL LEARN ASSI SALAR STATES IN THE SALAR STATES IN TH practice...

  - ... by non-statisticians.
     It plating suith/tpowcoder.com

### Warning!

The approaches described here are largely ASSISNMEDISIDENT OF CONTROL OF THE STATE OF THE STATE

More appropriate procedures usually exist

// move the learn these anyway because:

Hypothesis testing is ubiquitous

Add Westernatusen owested et

## Factory example

# Assignment herojecturexam Help

- You want to try a new manufacturing process to reduce this
- How do you know if it is better?

  Sho not parch or power oder.com
- Run an experiment: make n=200 devices with the new process and summarise this by the number, Y, that are faulty
- You Acid dat We (i.e yat process

   You Acid dat We (i.e yat process

   You Acid dat We (i.e yat process
- Is this a sensible procedure?
- We can formulate this as a statistical hypothesis test

#### Outline

Preface

# Assignment Project Exam Help

Classical hypothesis testing (Neyman-Pearson)

Hypotheses

Teshttpistics//powcoder.com

Significance level & power

Alternative formulations

## Signifi Add WeChat powcoder

Modern hypothesis testing

Common scenarios

Single proportion

Two proportions

Single mean

7 of 100ngle variance

### Research questions as hypotheses

# Assignment Project Exam Help

- Run an experiment / collect data and then ask:
- Do the data support/contradict the hypothesis?
- · Can Netten Statist DOWGOOD IIs GOM
- Classical hypothesis testing (due to Neyman & Pearson) aims to do this

### Describing hypotheses

- A hypothesis is a statement about the population distribution the population distribution the population distribution
  - A null hypothesis is a hypothesis that specifies 'no effect' or 'no charget upoty der of WCOCET.COM
  - ullet An alternative hypothesis is a hypothesis that specifies the effect of interest, usually denoted  $H_1$

### Null hypotheses

Special importance is placed on the null hypothesis.

SMS THE STUDY REPORT IS THE PROPERTY OF THE STUDY REPORT IS THE PROPERTY OF THE PROPERTY

- · I.e. https://powcederscom
- Note: what is taken as the null hypothesis (i.e. the actual meaning of 'no change') will depend on the context of the study and where the ous of professional powcoder

10 of 100

## Example

Assignment Project ExamaHelp
devices

- Experiment gives:  $Y \sim \mathrm{Bi}(200,p)$ , where p is the proportion of faul properties://powcoder.com
- Null hypothesis:

$$H_0$$
:  $p = 0.06$ 

· Alter Ard drow : Chat powcoder

 $H_1: p < 0.06$ 

### Types of parametric hypotheses

- Assimple hypothesis, also called a sharp hypothesis, specifies only per learning the sharp hypothesis and sharp hypothesis.
  - A composite hypothesis specifies many possible values
  - Null hypotheses are almost always simple
  - · Alteratitos: the some war of the com

## Specification of hypotheses

# Sugnment of respective by alternative by the strength of the s

- It is the 'least favourable' element for the alternative hypothesis: it is harder differentiate between p=0.06 and p=0.05 (close to the boundary) than it is between p=0.06 and p=0.05 (for away from the boundary).
- For single parameters, the null is typically of the form  $\theta=\theta_0$  and the alternative is either organized and takes the form  $\theta<\theta_0$  or  $\theta>0$  or the standard of the standar

### Describing tests

- A statistical test (or hypothesis test or statistical hypothesis test, properties of the statistical hypothesis test, p
  - A test statistic, T, is a statistic on which the test is based
  - The decision rule usually takes the form: https://powcoder.com
  - The set A is called the critical region, or sometimes the rejection region of the article A is called the critical region, or sometimes the rejection region of the critical value.
  - For our example, the test statistic is Y, the decision rule is to reject  $H_0$  if  $Y \leqslant 7$ , the critical region is  $(-\infty,7)$  and the critical value is 7.

#### Describing test outcomes

# Assign ment Project Exam Help

2. Fail to reject  $H_0$ 

We never the wear of the wear of the second of the second

Often we don't actually believe the null hypothesis. Rather, it serves as the retail of sitivity of skentled judge what we miss of wince otherwise.

Similar to a court case: innocent until proven guilty  $(H_0 \text{ until proven not } H_0)$ 

## Type I error

# Assignment Project Exam Help

- The new process might produce the same number of faulty devices on average, but by chance we observe at most 7 failures
- The metup is switched to the control of the co
- We have rejected  $H_0$  when  $H_0$  is actually true; this incalled a type error  $h_0$
- This could be quite costly—changing production line without reducing faults would be expensive
- (Controlling the probability of a Type I error will help to mitigate against this; see later...)

#### Type II error

- Could anything else could go wrong if Type Lerror is managed?

  Schegen process and bedieve the could go wrong if Type Lerror is managed?

  more than 7 failures
  - Then we would give up on the new process, forgoing its benefits

  - In this case, the error would be less costly in the short term but might be not have estly long-term DOWCOCCT
  - (So, whilst Type I error is often the one that is specifically controlled, Type II error remains important)

## Summary of outcomes

## Assignment Project Exam Help

```
\begin{array}{c|c} \text{https://powereoferet!} & \text{Powereoferet!} \\ H_0 \text{ is false} & \text{Type II error} \\ \end{array}
```

# Assignment Project Exam Help

- This is called the significance level, or sometimes the size, of the test 1.44.0 C. 1/40 O. T. T. O. 1.00
- In our example, under the provenance of the p

## Add WeChat poweoder

Calculate in R using: pbinom(7, 200, 0.06)

### Probability of type II error

# Assignment Project Exam Help

... but need to actually condition on a simple hypothesis (an actual value of p) in order for  $\beta$  to be well-defined.

In our example, suppose the new process actually works better and produces only 3% faulty devices on average. Then we have

 $Y \sim \text{Bi}(200, 0.03)$ , giving  $\beta = \Pr(Y > 7 \mid p = 0.03) = 0.254$ .

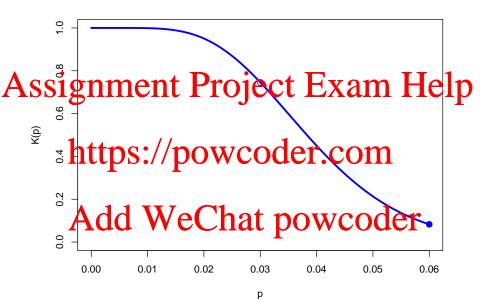
We have halved the rate of faulty devices but still have a 25% chance of not adopting the new process!

#### Power

# A solution of the lest, which is the power of the test, which is the power of the test of the test.

Typically, we would present this as a function of the true parameter value, ptps://powcoder.com

For our example, we have shown that K(0.03)=1-0.254=0.746



### Remarks about power

# Assignment in Project Exam Help This point is often forgetten because people talk about 'the' power

- This point is often forgotten because people talk about 'the' power of a study
- As right the spectron was good when p is close to  $p_0=0.06$ .
- $K(p_0) = \alpha$ , the type I error rate

### Controlling errors

- Typically, we construct a test so that it has a specified significance lent xir is from the pexing that co is run
  - In other words, we set the probability of a type I error to be some value (we 'control' it) and then try to minimise the probability of a typelittps://powcoder.com

    A widespread convention is to set  $\alpha=0.05$

  - I.e. we will incorrectly reject the null hypothesis about 1 time in 20
  - We for We instrease powers while o is fixed?
  - - Choosing good/optimal test statistics (see later...)
    - Increasing the sample size

#### Different ways to present a test

- There a other ways to present the result of a test
  SSI-SIMMET HAIF ALE TO BE THE TO BE
  - However, some are more popular than others, because they provide, or seem to provide, more information  $\frac{https://powcoder.com}{}$

#### Alternative formulation 1: based on a CI

- Instead of comparing a test statistic against a critical region of the statistic against a critical region of t
  - Reject  $H_0$  if  $p_0$  is not in the interval
  - · Thinteps:///poweoder.com
  - If the CI is constructed from a statistic T, this test is equivalent to using T as a test statistic.
  - The Angelian Wsing 95% That represents the ordered of setting  $\alpha=0.05$

### Alternative formulation 2: based on a p-value

# • Instead of comparing a test statistic against a critical region. SSIGNMENT The FOIECT Exam Help

- The p-value is the probability of observing data (in a hypothetical repetition of the experiment) that is as or more extreme than what was aftifility diserved marking as in the transfer that all the true.
- It is typically a tail probability of the test statistic, taking the tail(s) that are more likely under  $H_1$  as compared to  $H_0$ . (So, the exact details of the will vary between scenarios.)

  • Reject  $H_0$  if the p-value is less than the significance level
- **Note:** p-values are, strictly speaking, not part of classical hypothesis testing, but have been adopted as part of modern practice (more info later)

#### P-values

- A Schement Production of the positive of the production of the pr
  - In this case, values of T that are smaller are 'more extreme', in the sense of principle of T the classical field of T
  - If  $t_{\rm obs}=c$ , the p-value is the same as the significance level,  $\alpha$ .
  - If  $t_{\text{obs}} < c$ , the p-value is less than  $\alpha$ .
  - By calculating they value, we appted carcining to out the decision procedure is mathematically equivalent.
  - Many different ways that people refer to p-values:
     P, p, p, P-value, p-value, p-value, P value, p value

#### P-values for two-sided alternatives

# Assetismment form: roge Ct T x am Help

- Then the p-value is  $p = \Pr(|T| > |t_{\text{obs}}|)$
- This is a two-tailed probability
- The entry as careful to me for the form the fo

# 

• For more general two-sided rejection regions, we also always double the relevant tail probability. This gives an implicit definition for what it means to be 'more extreme' when the two tails are not symmetric to each other. (See the examples of testing variances later on, for which the distribution of the test statistic is  $\chi^2$ )

#### Example

# • We run our factory experiment. We obtain — 6 faulty devices SSI SNE Help

- According to our original decision rule  $(Y \leq 7)$ , we reject  $H_0$  and decide to adopt the new process.
- · Let https://powcoder.com
- Recall that  $\alpha = 0.085$ . Calculate a one-sided 91.7% confidence interval that gives an upper bound for p. The upper bound is: This is less than to therefore reject H. Let's try it using a p-value...
- The p-value is a binomial probability,  $Pr(Y \leq 6 \mid p = p_0) = 0.04$ . This is less than  $\alpha$ , so therefore reject  $H_0$ .

#### Outline

Preface

# Assignment Project Exam Help

Classical hypothesis testing (Neyman-Pearson)

Hypotheses

https://powcoder.com

Significance level & power

Alternative formulations

## Signific Add ng Wie Chat powcoder

Modern hypothesis testing

Common scenarios

Single proportion

Two proportions

Single mean

31 of 100 gle variance

## Significance testing

# Pre-dating the classical theory of hypothesis testing was 'significance and the standard of the significance of the significan

- Only use a null hypothesis, no reference to an alternative
- · Use https://spowecoeffreeom
- If the p-value is low, use as informal evidence that the null hypothesis is unlikely to be true.
- Otherwisel suspen Vuds (melt and collect more date der
- Use this procedure only if not much is yet known about the problem, to draw provisional conclusions only.
- This is not a decision procedure; do not talk about accepting or rejecting hypotheses.

### Disputes & disagreements

# Assignment erscoject Exam Help

- In particular, Fisher thought the classical approach was ill-suited for scientific research
- · Distattps://poweooder.com

#### Outline

# Assignment Project Exam Help

Classical hypothesis testing (Neyman-Pearson)

https://powcoder.com

Signific Add Ne We Chat powcoder Modern hypothesis testing

34 of 100 gle variance

### Modern practice

# Assignmentsisten of the Cybric Exam Help

- Largely use the terminology and formulation of the classical theory (Neyman & Pearson) but commonly report the results using a p-value and selecting report than accepting the null (both of which are ideas from Fisher)
- This has given rise to many problems
- · Will And bet West threatth prowcoder

#### Outline

# Assignment Project Exam Help

Classical hypothesis testing (Neyman-Pearson)

https://powcoder.com

Alternative formulations

Signific Add WeChat powcoder

Common scenarios

Single proportion

Two proportions

Single mean

36 of Magle variance

#### Common scenarios: overview

# Assignment Project Exam Help

• Two proportions

• Single variance

https://powcoder.scom

#### Single proportion

# Summent (Project Exam Help

- Test  $H_0$ :  $p=p_0$  versus  $H_1$ :  $p>p_0$ , and take  $\alpha=0.05$
- Reject  $H_0$  if observed value of Y is too large. That is the choosing product of the choosing product
- For large n, when  $H_0$  is true

### Add WeChat powcoder

This implies,

$$c = np_0 + \Phi^{-1}(1-\alpha)\sqrt{np_0(1-p_0)}$$

#### Example (single proportion)

We buy some dice and suspect they are not properly weighted.

Schange that the hope thirty of the last X right han the power of the conduct the test H = 1/6 versus H = 1/6

- Want to conduct the test  $H_0$ : p=1/6 versus  $H_1$ : p>1/6
- Roll the dice n=8000 times and observe Y sixes.
- · The https://powcoder.com

$$c = 8000/6 + 1.645\sqrt{8000(1/6)(5/6)} = 1388.162$$

• We significance and conclude that the die comes up with 6 too often

#### Single proportion, cont'd

# Assignmenta Projecte textain interp

Express Z as the standardised proportion of 6's,

- Decision ruled reject the Chat powcoder

$$z = \frac{1389/8000 - 1/6}{\sqrt{(1/6)(5/6)/8000}} = 1.67$$

and since  $z > \Phi^{-1}(0.95) = 1.645$  we reject  $H_0$ .

# Assignment Project Exam Help https://powcoder.com Add WeChat powcoder prob.

1.645

- Suppose we used a two-sided alternative,  $H_1: p \neq 1/6$
- This would me we want to be able detect deviations in either direction: whether rolling a six is either lower **or** higher than usual.

### Assignment Project Exam Help

$$Z = \frac{Y/n - p_0}{\sqrt{p_0(1 - p_0)/n}} \sim N(0, 1)$$

- $Z = \frac{Y/n p_0}{\sqrt{p_0(1-p_0)/n}} \sim N(0,1)$  but the critical region has changed. We reject  $R_0$  at level  $\alpha$  if  $|Z| > \Phi^{-1}(1 - \alpha/2)$
- In the previous example, we would use  $\Phi^{-1}(1-\alpha/2)=1.96$ . Since  $\Phi^{-1}(07, \text{ we will noticely } 100 \text{ WCOCCT}$

#### Summary of tests for a single proportion

### Assignment Project Exam Help

#### Example 2 (single proportion)

# Summent Project Exam Help

- Given 40 cups of tea and for each cup the order was determined by tossing a coin
- The name of the protein of the serious of the ser
- valid?

 $\bullet$  Let p be the probability the woman gets the correct order for a single cup of tea

# Assignment Project Examply Help guessing, the one-sided alternative is appropriate here.

• Data: y/n = 29/40 = 0.725https://powscoder.com  $\sqrt{0.5 \times 0.5/40} = 2.84$ 

- Critical value  $\Phi$  10/95)  $\epsilon$  1645, therefore reject  $H_0$  and conclude that the data supports the woman's carin WCO  $\epsilon$
- Alternatively, we could do this via a p-value:

p-value = 
$$Pr(Z > 2.84) = \Phi(-2.84) = 0.00226$$

• Since 0.00226 < 0.05, we reject  $H_0$ .

#### R code examples

# Assignment Project Exam Help > p1

### 1-samphttps://powtoder.comion

```
data: 29 out of 40, null probability 0.5
X-squared = 8.1, df = 1, p-value = 0.002213
alternative hypothesis; frid p is greater than 0.5
95 percent daridence interval at power of the control of the cont
```

46 of 100

0.725

# Assignment Project Exam Help > sqrt(p1\$statistic) X-squared 2.84605 https://powcoder.com

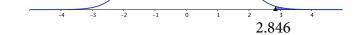
### Add WeChat powcoder

[1] 0.002213610

Z distributed Standard Normal

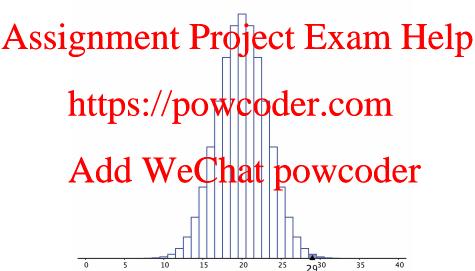
### Assignment Prøject Exam Help

https://powcoder.com



There is also an exact test based on the binomial probabilities:

Assignment Project Exam Help



#### Two proportions

# Assignment before $p_1$ and $p_2$ are the probabilities of $p_2$ and $p_3$ are the probabilities of $p_4$ and $p_5$ are the probabilities of $p_4$ and $p_5$ are the probabilities of $p_5$ are the probabilities of $p_5$ and $p_5$ are the prob

Wish to test:

### https://powcoder.com

based on independent samples (from the two populations) of size  $n_1$  and  $n_2$  with  $Y_1$  and  $Y_2$  successes.

• Know Add We Chat powcoder  $Z = \frac{Y_1/n_1 - Y_2/n_2 - (p_1 - p_2)}{\sqrt{p_1(1-p_1)/n_1 + p_2(1-p_2)/n_2}} \approx N(0,1)$ 

$$Z = \frac{Y_1/n_1 - Y_2/n_2 - (p_1 - p_2)}{\sqrt{p_1(1 - p_1)/n_1 + p_2(1 - p_2)/n_2}} \approx N(0, 1)$$

• Under  $H_0$  can assume that  $p_1 = p_2 = p$ ,

$$Z = \frac{Y_1/n_1 - Y_2/n_2}{\sqrt{p(1-p_1)(1/n_1 + 1/n_2)}} \approx N(0, 1)$$
**Assignment Project Exam Help**

• Reject  $H_0$  at level  $\alpha$  if

$$\text{https://powcoder}_{\sqrt{\hat{p}(1-\hat{p})(1/n_1+1/n_2)}}\text{com}$$

#### Example (two proportions)

We run a trial of two insecticides. The standard one kills 425 out of School 1997 of the experimental insecticide more effective?

Let  $p_1$  and  $p_2$  be the proportion of all morquitoes killed by experimental postandar gray respectively. COM

Alternatively, can use the R function prop.test() which calculates the statistic  $\chi^2 = Z^2$  and compares against a  $\chi^2_1$  distribution.

### Assignment Project Exam Help

2-sample test for equality of proportions without continuity correction

 $\underset{x-\mathrm{square}}{\mathtt{data}}: \underset{x-\mathrm{square}}{\mathtt{https}}: /_{\mathtt{df}} /_{\mathtt{p,own}} \\ \underset{x-\mathrm{square}}{\mathtt{data}}: /_{\mathtt{p,own}} /_{\mathtt{p,own}} \\ \underset{x-\mathrm{square}}{\mathtt{data}}: /_{\mathtt{p,own}} /_{\mathtt{p,own}} \\ \underset{x-\mathrm{square}}{\mathtt{data}}: /_{\mathtt{p,own}} \\ \underset{x-\mathrm{square}}{\mathtt{data}}: /_{\mathtt{p,own}} /_{\mathtt{p,o$ alternative hypothesis: greater 95 percent confidence interval: o.03487541 1.09000000 WeChat powcoder prop 1 prop 2

0.918 0.850

#### Summary of tests for two proportions

### Assignment Project Exam Help

$$H_0\colon p = p_1 + p_2 + p_3 \cdot p_4 + p_4 \cdot p_2 \cdot p_3 \cdot p_4 \cdot p_4 \cdot p_4 \cdot p_4 \cdot p_4 \cdot p_5 \cdot p_4 \cdot p_5 \cdot p_4 \cdot p_5 \cdot p_5 \cdot p_6 \cdot p$$

#### Example (normal, single mean, known $\sigma$ )

- $\sigma = 6012.60$  km. Is this evidence against the manufacturer's Let 1/2 be the mean the metime.

 $H_0$ :  $\mu = 48,000$  versus  $H_1$ :  $\mu < 48,000$ 

• Recall that,

$$\bar{X} \sim N\left(\mu, \frac{\sigma^2}{n}\right)$$

### Assignment Project Exam Help

$$Z = \frac{\bar{X} - \mu_0}{\sigma / \sqrt{50}} < \Phi^{-1}(\alpha)$$

. we https://powcoder.com

# Add $\vec{W} = \frac{45286 - 48000}{216} = -3.187$

so we reject  $H_0$  at the 5% level of significance and conclude the tyre life is lower than the claimed 48,000 km

#### Summary of tests for single mean, $\sigma$ known

### Assignment Project Exam Help

$$H_0 \qquad H_1 \qquad \text{Critical region}$$

$$\mu = \mu_0 \qquad \mu > \mu_0 \qquad z = \frac{\bar{x} - \mu_0}{\sigma / \sqrt{n}} \geqslant \Phi^{-1}(1 - \alpha) \qquad \text{or } \bar{x} \geqslant \mu_0 + \Phi^{-1}(1 - \alpha)$$

$$\mu = \mu_0 \qquad \mu \neq \mu_0 \qquad |z| = \frac{|\bar{x} - \mu_0|}{\sigma / \sqrt{n}} \geqslant \Phi^{-1}(1 - \alpha/2) \qquad \text{or } |\bar{x} - \mu_0| \geqslant \Phi^{-1}(1 - \alpha/2)$$

The critical regions are equivalent to the projective confidence intervals containing  $\mu_0$ .

#### Normal, single mean, unknown $\sigma$

Assignment from Quechen Exam Help

$$\underset{\text{and we may base our tests on }T}{\text{https://powcoder.com}} \sim t^{n-1}$$

• This is known as the t-test

#### Example (normal, single mean, unknown $\sigma$ )

# 

We have n=9, and want a test with significance level  $\alpha=0.1$ .

• Rejection Rejection Property Propert

$$|t| = \frac{|\bar{x} - 4|}{s/\sqrt{9}} > c$$

wher Act of the own of

• Conduct experiment with results:  $\bar{x}=4.3$ , s=1.2. Also, we can look up / calculate that c=1.86. Therefore our test comparison is,

# Assignment Project Exam Help

- At the 10% level of significance we cannot reject  $H_0$  and conclude there is not enough evidence that the tumour mean departs from 4 mattps://powcoder.com
- The p-value is

### Add We Chat powcoder

In R, you can calculate this with the command:

2 \* (1 - pt(0.75, 8)), which gives 0.4747312

#### Summary of tests for single mean, $\sigma$ unknown

### Assignment Project Exam Help

$$\mu = \mu_0 \quad \mu > \mu_0 \quad t = \frac{\bar{x} - \mu_0}{s/\sqrt{n}} \geqslant F^{-1}(1 - \alpha) \quad \text{or } \bar{x} \geqslant \mu_0 + F^{-1}(1 - \alpha)$$

$$\mu = \mu_0 \quad t \not = \underbrace{\sum_{k=0}^{n} \mu_0}_{|t|} \stackrel{\text{for } \bar{x} = \mu_0}{|t|} \stackrel{\text{for } \bar{x$$

intervals containing  $\mu_0$ .

#### Paired-sample t-test

As with confidence intervals, if we observe pairs of numbers  $(X_i, Y_i)$  papely methods for a single sample (in this case, a t-test).

https://powcoder.com

#### Example (normal, single variance)

# $A \overset{\circ}{s} \overset{\text{A test about the variance}}{\underset{H_0: \ \sigma^2}{\text{end}}} \overset{\text{Project}}{\underset{\text{versus}}{\text{Exam}}} \overset{\text{Exam}}{\underset{\text{Help}}{\text{Help}}}$

- n = 23,  $\alpha = 0.05$ ,  $s^2 = 147.82$ . Rechttps://powcoder.com  $\chi^2 = \frac{(n-1)S^2}{\sigma^2} \sim \chi^2_{n-1}$ 
  - So wAreidth WeChat powcoder  $\chi^2 < F^{-1}(\alpha/2) = 10.98$  or  $\chi^2 > F^{-1}(1 \alpha/2) = 36.78$

Where  $F^{-1}$  is the inverse cdf of  $\chi^2_{22}$ .

#### R code for quantiles

### Assignment Project Exam Help

```
> qchisq(0.975, 22) powcoder.com
```

```
> qchisq(0.025, 22)
[1] 10A8BB WeChat powcoder
```

#### Back to the example

# Assignment Project Exam Help $\chi^2 = \frac{22 \times 100}{100} = 32.52$

· and https://powcoder.com

so we cannot reject  $H_0$ .

#### Example (normal, two means, pooled variance)

# Assignment tropped the effect of two different hormone 1pt and the effect of two different hormone 1pt and 1pt

- Data: X and Y are the growth in the first 26 hours after treatment with hormone 1 & 2, respectively
- We into the less production of the Suppose  $X \sim N(\mu_X, \sigma^2)$  and  $Y \sim n(\mu_Y, \sigma^2)$ ,

• Samples of sizes n and m. We use the two-sample pivot but assuming  $H_0$  (which makes the  $\mu_X - \mu_Y$  term disappear),

# Assignments Project Exam Help

where  $S_P^2$  is the pooled variance estimate:

$$https: //powcoder.com$$
 $_{S_P} = \sqrt{\frac{n + m - 2}{n + m - 2}}$ 

- Reject  $H_0$  if t < c, where c is the  $\alpha$  quantile of  $t_{n+m-2}$ .
- Here n=11, m=13,  $\bar{x}=1.03$ ,  $s_X^2=0.24$ ,  $\bar{y}=1.66$ ,  $s_Y^2=0.35$ ,

# Assignment Project Exam Help

and thus

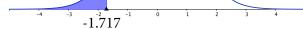
https://poweoder.com

- The critical value is c=-1.717 (corresponding to  $\alpha=0.05$  and n+m-2=22) so we reject  $H_0$  and conclude that there is statisfically significant endergo fees growth with hornors.
- The p-value is

$$\Pr(T < -2.81) = 0.0051 < 0.05$$

## Assignmenta Project Exam Help

https://powcoder.com



# Assignment Project Exam Help

https://powcoder.com

Add pro Se Chat powcoder
0.005

```
> x = c(0.8, 1.8, 1.0, 0.1, 0.9, 1.7,
Assignment Project Exam Help
  > y = c(1, 0.8, 1.6, 2.6, 1.3, 1.1, 2.4,
         1.8, 2.5, 1.4, 1.9, 2, 1.2)
      https://powcoder.com
   Hormone 1 (x)
   Hormon And d We Chat powcoder
          0.0
                 0.5
                       1.0
                             1.5
                                   2.0
                                          2.5
```

> t.test(x, y, alternative = "less", var.equal = TRUE)

## Assignment Project Exam Help

data: x and y

t = -1.8112, df = 22, p-value = 01005086

alternation proche powcoder.com

true difference in means is less than 0

95 percent confidence interval:

sample estimates:

mean of x mean of y 1.027273 1.661538

Example 2 (normal, two means, pooled variance)

## Assignment Paroject Exam Help

Interested in testing:

https://poweoder.com

Similar to before but two-sided alternative, so use a two-sided critical region. Add  $\begin{array}{c} \text{WeChat powcoder} \end{array}$ 

```
> x = c(1071, 1076, 1070, 1083, 1082, 1067,
      nment Project Exam Help
> v = c(1074, 1069, 1075, 1067, 1068, 1079,
      1082, 1064, 1070, 1073, 1072, 1075)
  Х
                  Chat powcoder
      1065
                1070
                         1075
                                   1080
```

> t.test(x, y, var.equal = TRUE)

```
data: x and y

t = 21053 df = 22/ p-value = 0.05215
alternation prottle powcoder.com

true difference in means is not equal to 0

95 percent confidence interval:
-0.04488733888822107 hat powcoder

mean of x mean of y

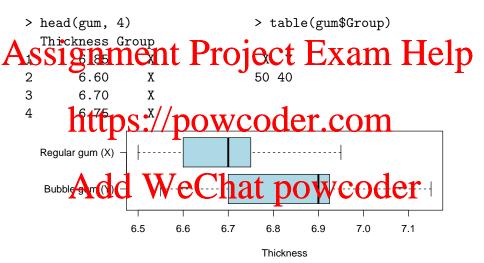
1076.750 1072.333
```

## Assignment Project Exam Help

Therefore, at the 5% level of significance we do not have enough evident the reject the full hypothesis der.com

Given the closeness of result, it would be worth trying to collect more data.

#### Example (normal, two means, different variances)



```
> t.test(Thickness ~ Group, data = gum)
```

```
data: Thickness by Group

t = -1.8604, df = 67.219, p-value = 7.357e-06

alternative hypothers OWCOGET.COM

true difference in means is not equal to 0

95 percent confidence interval:

-0.1974277-00865723 hat powcoder

sample estimates:

mean in group X mean in group Y

6.70100 6.84125
```

> t.test(Thickness ~ Group, data = gum, var.equal = TRUE)

```
data: Thickness by Group

t = -5.0524, df = 88, p-value = 21345e-06

alternation proche powcoder.com

true difference in means is not equal to 0

95 percent confidence interval:

-0.1941547-008508463 hat powcoder

sample estimates:

mean in group X mean in group Y

6.70100 6.84125
```

#### Normal, two variances

## Assignment Project Exam Help

Recall

https://powcoder.com

and since the samples are independent, these statistics are also independent.

• Want to test,

$$H_0 \colon \sigma_X^2 = \sigma_Y^2$$
 versus  $H_1 \colon \sigma_X^2 \neq \sigma_Y^2$ 

## Assignment Project ExamcHelp

https://powcoder.com

#### Example (normal, two variances)

## Assignment Project Exam Help

$$H_0\colon \sigma_X^2=\sigma_Y^2 \quad \text{versus} \quad H_1\colon \sigma_X^2\neq \sigma_Y^2$$

https://powcoder.com

> head(spiders, 4) > table(spiders\$Group) iment Project Exam Help 5.75 <sup>7</sup> https://powcoder.com Male spiders (X) WeChat powcoder 5 10 Length

## Assignment Project Exam Help

https://powcoder.com

so we reject  $H_0$  at 1% level of significance.

> var.test(Length ~ Group, data = spiders)

### Assignment-Project Exam Help

```
data: Length by Group

F = 312054, num df/= 29, denom df1= 29, p-value = 0.002458

alternative Dyposite DOWCOGET.COM

true ratio of variances is not equal to 1

95 percent confidence interval:

1.525637 d3444 eChat powcoder

sample estimates:

ratio of variances
```

3.205357

#### Outline

Preface

## Assignment Project Exam Help

Classical hypothesis testing (Neyman-Pearson)

Hypotheses

https://powcoder.com

Significance level & power

Alternative formulations

Add WeChat powcoder

Modern hypothesis testing

Common scenarios

Single proportion

Two proportions

Single mean

89 of 100 gle variance

#### Choice of significance level

# Somewhat arbitrary. Slanden tpePerrojectIIErxamprepelp balance is likely to depend on your problem.

• Whatever you choose, always remember that you are never guaranteed be en pre-wcoder.com

- $\alpha=0.05$  is a very common convention (c.f. 95% confidence level). If you don't have a good basis for choosing a specific  $\alpha$  for your problem, then following this convention will usually be acceptable.
- Specific Gilled of Vipolitation Farcular than Colored Testwhich are very different. For example:
  - $\circ$  Genome-wide association studies require p-values of around  $10^{-8}$
  - $\circ$  High-energy physics (particle physics) requires p-values under 0.003 ('3 sigma') for reporting 'evidence of a particle' and p-values under 0.0000003 (3  $\times$  10 $^{-7}$ ; '5 sigma') for reporting a 'discovery'.

#### Misinterpretations of p-values

Many misconceptions about p-values:

### SSTORMA CIQITO DIFFERENCE IN INTERPOLATION OF THE P-value is the probability that the alternative hypothesis is false

- A 'significant' p-value implies that the null hypothesis is false
- A 'significant' p-yalue implies that the alternative hypothesis is true
- o Anitificate physical importance has a large magnitude or of practical importance
- None of these are true
- Thesaardjust the tip of the leeberg! nowcoder
- Similar issues arise with oversimplified interpretations of confidence intervals
- Can read much more about this in various articles...

'Absence of evidence' versus 'evidence of absence'

## As support the null could be either because the null is As support in the could be either because the null is the support in the could be either because the null is the support in the could be either because the null is the null is the could be either because the null is the null i

- In this case, absence of evidence is not evidence of absence...
- ... but it could be, if only we quantified our evidence better! https://powcoder.com

#### Decisions versus inference

- Assiegnment Lilly in Jecrep Exam Help
  - Decisions are about **behaviour**, inference is about **knowledge**
  - Knowledge can drive behaviour, but they are not the same thing
  - · Decattas://kpawcoder.com
  - Decisions are black & white, knowledge is a shade of grey

#### Following the scientific process

- Does hypothesis testing parallel the scientific process?

  Sel Supported by to disprove it?
  - Perhaps... but a binary decision doesn't carry much informative contenting://powcoder.com
  - At best, this a very cartoonish view of science
  - Better to think of science as a process of cumulative evidence gathAinsId WeChat nowcoder
  - Talk about degrees of evidence rather than black & white truth claims

#### Why is hypothesis testing so popular?

## A Satement Project Exam Help

- Hypothesis testing, esp. when used with p-values, seemed to offer this, especially since it seems to have been 'blessed' by statisticians.
- In reality in stook good to wrong an end proper to misinterpretation. The ability to draw strong conclusions is a misconception about the nature of inference.
- But the ginid is out of the bottle. and has been rampint for more than had a century. That powcoder

- Statistical education hasn't helped.
- A circular problem: we teach the use of p=0.05 because it's 'in demand', but that only perpetuates it's use.

## As Sit ghnathfreefirm Petting sconger Evx am Help You are lucky, we are teaching you to set the right foot forward

You'are lucky, we are teaching you to set the right foot forward from day one!

https://powcoder.com

#### What's an alternative?

## A Salgament Project Exam Help

- Usually, it will be best formulated in terms of estimation or prediction.
- 'Homitpies of plows are interested in the second of simply 'Does smoking cause lung cancer?'
- Interval estimative techniques are a better way to answer such question of the power of the po

#### It's all about uncertainty

- If anything, we do the opposite: we quantify it so that it is plainly visible
- · This hat to Sime power der. com
- Always keep your critical thinking hat on: do the results look plausible in light of previous knowledge?
- And A chedould be you hat the pro will conclude of grey are you after this time?

#### When should we actually use hypothesis testing?

- Use it when convenient, to help inform further analyses
- If reporting the results, then set them in context and avoid pure black to Scorch WCOCET.COM
- It's helpful in designing studies, especially the concept of error probabilities (including power)
- Sometime we addalla qui e dactsions egyptation to the propositions (such as our factory example)
- Pure hypothesis testing is adequate for such settings, although more sophisticated procedures exist (statistical decision theory)

#### Why are we learning hypothesis testing?

- SSICHMENT Pario 1 Ectre x amakele 1p
  - To understand the concepts and language used by others

  - Sometimes it is useful and convenient
    Sometimes S simple On Webrack Characterian Growne procedures, even if we believe the latter are more 'correct'