MATH3075/3975 Financial Derivatives

School of Mathematics and Statistics University of Sydney

Semester 2, 2020

Tutorial sheet 5

Background: Section 2.2 – Single-Period Market Models.

Exercise 1 Consider the market model $\mathcal{M} = (B, S)$ introduced in Exercise 3 (Week 4). We thus have k = 3, $r = \frac{1}{9}$, $S_0 = 5$ and the stock prices at time 1 are given by the following table

Assignment Project Exam Help Are there are values for K such that the call option $(S_1 - K)^+$ represents an attainable contingent claim?

Exercise 2 philips he stock words the polynomial B, S introduced in Example 2.2.3 from the course notes. Hence $\Omega = \{\omega_1, \omega_2, \omega_3, \omega_4\}$, the volatility v is the random variable on Ω given by

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where 0 < l < h < 1 and the stock price S_1 satisfies: $S_0 > 0$ and

$$S_1(\omega) = \begin{cases} (1 + v(\omega))S_0 & \text{if } \omega = \omega_1, \omega_2, \\ (1 - v(\omega))S_0 & \text{if } \omega = \omega_3, \omega_4, \end{cases}$$

We assume, in addition, that $0 \le r < h$.

- (a) Characterise the class of all attainable contingent claims in \mathcal{M} and check whether the model \mathcal{M} is complete.
- (b) Describe the class \mathbb{M} of all risk-neutral probability measures for \mathcal{M} .
- (c) (MATH3975) Describe the set of all arbitrage prices for the call option $(S_1 K)^+$ where the strike K satisfies $S_0(1 + l) < K < S_0(1 + h)$.
- (d) (MATH3975) Assume that r = 0. Check directly whether the call option with strike K such that $S_0(1+l) < K < S_0(1+h)$ is attainable and find the range of values of its arbitrage price.