

## Assignment Project Exam Help The Drill https://powcoder.com

Add WeChat powcoder

Nicholas J.J. Smith and John Cusbert

Copyright © 2012 by Nicholas Jeremy Josef Smith and John Cusbert

## Assignment Project Exam Help Cover photograph: Alser Straße, Vienna. © Nicholas J.J. Smith

https://powcoder.com

Add WeChat powcoder 30 May 2012: first published.

29 November 2014: corrections. 16 May 2017: corrections.

#### **Preface**

The first part of this volume contains all the exercise questions that appear in *Logic: The Laws of Truth* by Nicholas J.J. Smith (Princeton University Press, 2012). The second part contains answers to almost all of these exercises. Both the questions and the answers are a collaborative effort between Nicholas J.J. Smith and John Cusbert.

One obvious use of this work is as a solutions manual for readers of Logic: The Tuss I gut The I should Did GCL use the Dogic books. Students of logic need a large number of worked examples and exercise problems with solutions: the more the better. This volume should help to meet that the decimal of the power of the

After each question, a cross-reference of the form '[A p.x]' appears. This indicates the page on which the answer to that question can be found. You can click on the cross-reference to be taken divertion that question can be found. You can click on the cross-reference of the form '[Q p.x]' which leads back to the corresponding question. Other blue items are also links: for example, clicking on an entry in the Contents pages takes you directly to the relevant section, and at the end of each exercise set and each answer set there is a link back to the Contents.

If you find any errors—or have any other comments or suggestions—please email us at:

logicthedrill@gmail.com

The latest version of this work can be found at:

http://www.personal.usyd.edu.au/~njjsmith/lawsoftruth/

Any significant revisions (e.g. corrections or additions to the exercises or answers) will be documented on the copyright page.

## **Contents**

Preface	iii
Questions	2
1. Assignment Project Exam Help	2
Exercises 1.2.1	2
Exercises 1.3 https://powcoder.com	3
Exercises 1.4.1	3
Exercises 1.5.1 Add WeChat powcoder	4
Exercises 1.6.1.1	4
Exercises 1.6.2.1	5
Exercises 1.6.4.1	5
Exercises 1.6.6	6
2. The Language of Propositional Logic	7
Exercises 2.3.3	7
Exercises 2.3.5	8
Exercises 2.3.8	8

Exercises 2.5.1	10
Exercises 2.5.3.1	11
Exercises 2.5.4.1	11
Exercises 2.5.5.1	11
3. Semantics of Propositional Logic	13
Exercises 3.2.1	13
Exercises 3.3.1	14
Exercises 3.4.1	14
ExeAissignment Project Exam Help	15
4. Uses of Truth Tables https://powcoder.com	16 16
Exercises 4.2. Add WeChat powcoder Exercises 4.3.1	17 18
Exercises 4.4.1	18
5. Logical Form	20
Exercises 5.1.1	20
Exercises 5.2.1	20
Exercises 5.3.1	21
Exercises 5.4.1	22
Evercises 5 5 1	23

6. Connectives: Translation and Adequacy	24
Exercises 6.5.1	24
Exercises 6.6.3	25
7. Trees for Propositional Logic	27
Exercises 7.2.1.1	27
Exercises 7.2.2.1	27
Exercises 7.2.3.1	28
Exercises 7.3.1.1	28
Exalissignment Project Exam Help	29
Exercises 7.3.3.1	30
Exercises 7.3 Attps://powcoder.com	30
Exercises 7.3.5.1	31
Add WeChat powcoder 8. The Language of Monadic Predicate Logic	32
Exercises 8.2.1	32
Exercises 8.3.2	33
Exercises 8.3.5	34
Exercises 8.4.3.1	35
Exercises 8.4.5.1	36
9. Semantics of Monadic Predicate Logic	38
Exercises 9.1.1	38
Evercises 9 2 1	39

Exercises 9.3.1	39
Exercises 9.4.3	40
Exercises 9.5.1	43
10. Trees for Monadic Predicate Logic	44
Exercises 10.2.2	44
Exercises 10.3.8	45
11. Models, Propositions, and Ways the World Could Be	47
12. Assignment Project Exam Help	48
Exercises 12.1.3.1	48
Exercises 12 https://powcoder.com	49
Exercises 12.1.9	50
Exercises 12 Add WeChat powcoder	52
Exercises 12.3.1	54
Exercises 12.4.1	57
Exercises 12.5.4	57
13. Identity	58
Exercises 13.2.2	58
Exercises 13.3.1	60
Exercises 13.4.3	61
Exercises 13.5.1	63

Exercises 13.6.1.1	64
Exercises 13.6.2.1	65
Exercises 13.6.3.1	66
Exercises 13.7.4	66
14. Metatheory	70
Exercises 14.1.1.1	70
Exercises 14.1.2.1	71
Exercises 14.1.3.1	<b>71</b>
Assignment Project Exam Help	72
Exercises 15.1.5 https://powcoder.com	72
Exercises 15.2.3 Exercises 15.2.3	74
Add WeChat powcoder	75
16. Set Theory	76
Answers	78
1. Propositions and Arguments	78
Answers 1.2.1	78
Answers 1.3.1	78
Answers 1.4.1	79
Answers 1.5.1	79

Answers 1.6.1.1	80
Answers 1.6.2.1	80
Answers 1.6.4.1	80
Answers 1.6.6	81
2. The Language of Propositional Logic	84
Answers 2.3.3	84
Answers 2.3.5	84
Answers 2.3.8	85
An Arssignment Project Exam Help	87
Answers 2.5.3.1	89
Answers 2.5 Attps://powcoder.com	90
Answers 2.5.5.1	90
Add WeChat powcoder 3. Semantics of Propositional Logic	92
Answers 3.2.1	92
Answers 3.3.1	93
Answers 3.4.1	95
Answers 3.5.1	98
4. Uses of Truth Tables	99
Answers 4.1.2	99
Answers 4.2.1	102
Answers 4 3 1	105

Answers 4.4.1	109
5. Logical Form	112
Answers 5.1.1	112
Answers 5.2.1	113
Answers 5.3.1	114
Answers 5.4.1	116
Answers 5.5.1	117
6. Connectives: Translation and Adequacy Assignment Project Exam Help	118 118
https://powcoder.com	128
7. Trees for Propositional Logic	134
Answers 7.2 Add WeChat powcoder	134
Answers 7.2.2.1	135
Answers 7.2.3.1	136
Answers 7.3.1.1	137
Answers 7.3.2.1	141
Answers 7.3.3.1	144
Answers 7.3.4.1	148
Answers 7.3.5.1	151
8. The Language of Monadic Predicate Logic	156

Answers 8.2.1	156
Answers 8.3.2	158
Answers 8.3.5	159
Answers 8.4.3.1	161
Answers 8.4.5.1	163
9. Semantics of Monadic Predicate Logic	165
Answers 9.1.1	165
Answers 9.2.1	165
An Assignment Project Exam Help	166
Answers 9.4.3	167
Answers 9.5https://powcoder.com	171
10. Trees for Monadic Predicate Logic Add WeChat powcoder	172
Answers 10.2.2	172
Answers 10.3.8	180
11. Models, Propositions, and Ways the World Could Be	190
12. General Predicate Logic	191
Answers 12.1.3.1	191
Answers 12.1.6	192
Answers 12.1.9	193
Answers 12.2.2	196

Answers 12.3.1	200
Answers 12.4.1	217
Answers 12.5.4	220
13. Identity	221
Answers 13.2.2	221
Answers 13.3.1	223
Answers 13.4.3	226
Answers 13.5.1	244
An Assignment Project Exam Help	258
Answers 13.6.2.1	259
Answers 13. https://powcoder.com	260
Answers 13.7.4	261
Add WeChat powcoder  14. Metatheory	265
Answers 14.1.1.1	265
Answers 14.1.2.1	265
Answers 14.1.3.1	267
15. Other Methods of Proof	269
15. Other Methods of Proof	209
Answers 15.1.5	269
Answers 15.2.3	284
Answers 15.3.3	303

**16. Set Theory 304** 

# Assignment Project Exam Help https://powcoder.com Add WeChat powcoder

## Questions Assignment Project Exam Help

https://powcoder.com

Add WeChat powcoder

## Chapter 1

## **Propositions and Arguments**

#### **Exercises 1.2.1**

Classify the following as propositions or nonprepositions.  ASSIGNMENT PROJECT EXAM  1. Los Angeles is a long way from New York.	lelp
2. Let's go to Los Angeles!  https://powcoder.com	[A p.78]
3. Los Angeles, whoopee!	[A p.78]
4. Would that Los Angeles were not so far away.	[A p.78]
5. I really wish Los Angeles were nearer to New York.	[A p.78]
6. I think we should go to Los Angeles.	[A p.78]
7. I hate Los Angeles.	[A p.78]
8. Los Angeles is great!	[A p.78]
9. If only Los Angeles were closer.	[A p.78]
10. Go to Los Angeles!	[A p.78]
	[Contents]

#### Exercises 1.3.1

Represent the following lines of reasoning as arguments.

- 1. If the stock market crashes, thousands of experienced investors will lose a lot of money. So the stock market won't crash. [A p.78]
- 2. Diamond is harder than topaz, topaz is harder than quartz, quartz is harder than calcite, and calcite is harder than talc, therefore diamond is harder than talc.

  [A p.79]
- 3. Any friend of yours is a friend of mine; and you're friends with everyone on the volleyball team. Hence, if Sally's on the volleyball team, she's a friend of mine. [A p.79]
- 4. When a politician engages in shady business dealings, it ends up on page one of the newspapers. No South Australian senator has ever Aappeared on page one of the newspaper. Thus appeared on the senator and senator engages in shady business dealings.

  [Ap.79]

[Contents]

## https://powcoder.com

#### **Exercises 1.4.1**

State whethe According to the Vote Ving Jetun DO WOOD Grandlid.

1.	All dogs are mammals. All mammals are animals.	
	All dogs are animals.	[A p.79]
2.	All dogs are mammals. All dogs are animals.	
	All mammals are animals.	[A p.79]
3.	All dogs are mammals. No fish are mammals.	
	No fish are dogs.	[A p.79]

4. All fish are mammals.
All mammals are robots.

All fish are robots.

[A p.79]

[Contents]

#### **Exercises 1.5.1**

	1. Which of the arguments in Exercise 1.4.1 are sound?	[A 1	p.79	1
--	--	------	------	---

- 2. Find an argument in Exercise 1.4.1 that has all true premises and a true conclusion but is not valid and hence not sound. [A p.79]
- 3. Find an argument in Exercise 1.4.1 that has false premises and a false Assignment is Project Exam Help.<sup>79</sup>
  [Contents]

## Exercises 1.495. // powcoder.com

1. What is the negard of: Add WeChat powcode	er
(i) Bob is not a good student	[A p.80]
(ii) I haven't decided not to go to the party.	[A p.80]
(iii) Mars isn't the closest planet to the sun.	[A p.80]
(iv) It is not the case that Alice is late.	[A p.80]
(v) I don't like scrambled eggs.	[A p.80]
(vi) Scrambled eggs aren't good for you.	[A p.80]
2. If a proposition is true, its double negation is?	[A p.80]
3. If a proposition's double negation is false, the proposit	ion is?
	[A p.80]
	[Contents]

#### **Exercises 1.6.2.1**

What are the conjuncts of the following propositions?

Assignment Project Evan Help		
6. The road to the campsite is long and uneven.	[A p.80]	
	[A p.80]	
5. Sue does not want the red bicycle, and she does not like the blue one.		
4. We watched the movie and ate popcorn.	[A p.80]	
3. Sailing is fun, and snowboarding is too.	[A p.80]	
2. Maisie and Rosie are my friends.	[A p.80]	
1. The sun is shining, and I am happy.	[A p.80]	

## Assignment Project Exam Help Exercises 1.6.4.1

What are the late the seden productions?

- 1. If that's pistachio ice cream, it doesn't taste the way it should.

  Add WeChat powcoder

  [A p.80]
- 2. That tastes the way it should only if it isn't pistachio ice cream.

[A p.80]

3. If that is supposed to taste that way, then it isn't pistachio ice cream.

[A p.81]

4. If you pressed the red button, then your cup contains coffee.

[A p.81]

5. Your cup does not contain coffee if you pressed the green button.

[A p.81]

6. Your cup contains hot chocolate only if you pressed the green button.

[A p.81]

[Contents]

#### Exercises 1.6.6

State what sort of compound proposition each of the following is, and identify its components. Do the same for the components.

1. If it is sunny and windy tomorrow, we shall go sailing or kite flying.

[A p.81]

2. If it rains or snows tomorrow, we shall not go sailing or kite flying.

[A p.81]

- 3. Either he'll stay here and we'll come back and collect him later, or he'll come with us and we'll all come back together. [A p.81]
- 4. Jane is a talented painter and a wonderful sculptor, and if she remains interested in art, her work will one day be of the highest qual
  Aity signment Project Exam Helpp.81]
- 5. It's not the case that the unemployment rate will both increase and decrease in the next quarter. [A p.82]
- 6. Your sunburn will ge worse and become painful if you don't stop swimming during the daytime. [A p.82]
- 7. Either Avendow he he had the place and exclients will leave. [A p.82]
- 8. The Tigers will not lose if and only if both Thompson and Thomson get injured. [A p.82]
- 9. Fido will wag his tail if you give him dinner at 6 this evening, and if you don't, then he will bark. [A p.82]
- 10. It will rain or snow today—or else it won't. [A p.83]

[Contents]

## Chapter 2

## The Language of Propositional Logic

## Exercises 2333 ent Project Exam Help

Using the glossary:

A: Anistoth was a prior wheroder.com

B: Paper lurns

*F*: Fire is hot

## Add WeChat powcoder translate the following from PL into English.

1. ¬ <i>A</i>	[A p.84]
2. $(A \wedge B)$	[A p.84]
3. $(A \land \neg B)$	[A p.84]
4. $(\neg F \land \neg B)$	[A p.84]
5. $\neg(F \land B)$	[A p.84]
	[Contents]

#### Exercises 2.3.5

Using the glossary of Exercise 2.3.3, translate the following from PL into English.

1. $((A \wedge B) \vee F)$	[A p.84]
2. $(\neg A \lor \neg B)$	[A p.84]
3. $((A \lor B) \land \neg (A \land B))$	[A p.84]
4. $\neg (A \lor F)$	[A p.84]
5. $(A \wedge (B \vee F))$	[A p.85]
	[Contents]

## Exersignment Project Exam Help

1. Using the glossary:

the type in powcoder.com *B*:

*G*: Grass is green

R: Roses are red We Chat powcoder
W: Sports Whit We Chat powcoder

Y: Bananas are yellow

translate the following from PL into English.

(i)	$(W \to B)$	[A p.85]
(ii)	$(W \leftrightarrow (W \land \neg R))$	[A p.85]
(iii)	$\neg (R \to \neg W)$	[A p.85]
(iv)	$((R \lor W) \to (R \land \neg W))$	[A p.85]
(v)	$((W \wedge W) \vee (R \wedge \neg B))$	[A p.85]
(vi)	$(G \vee (W \to R))$	[A p.85]
(vii)	$((Y \leftrightarrow Y) \land (\neg Y \leftrightarrow \neg Y))$	[A p.85]
(viii)	$((B \to W) \to (\neg W \to \neg B))$	[A p.85]
(ix)	$(((R \land W) \land B) \to (Y \lor G))$	[A p.85]

2. Trai	nslate the following from English into PL.	
(i)	Only if the sky is blue is snow white.	[A p.86]
(ii)	The sky is blue if, and only if, snow is white and	-
	not red.	[A p.86]
(iii)	It's not true that if roses are red, then snow is not whit	æ.
		[A p.86]
(iv)	If snow and roses are red, then roses are red and/or si	
		[A p.86]
(v)	Jim is tall if and only if Maisy is, and Maisy is tall only	-
(:)	is not.	[A p.86]
, ,	Jim is tall only if Nora or Maisy is.	[A p.86]
	signmentei Projectal Exam't Ho	
(V111)	Either snow is white and Maisy is tall, or snow is whit isn't.	e and sne [A p.86]
(ix)	If https and poweroderte omth is a	
(23)	blue.	[A p.86]
(x)	If Maisy is tall and the sky is blue, then Jim is tall and	the sky is
	noAldd WeChat powcoder	[A p.86]
3. Trai	nslate the following from English into PL.	
(i)	If it is snowing, we are not kite flying.	[A p.87]
(ii)	If it is sunny and it is windy, then we are sailing or kit	e flying.
		[A p.87]
(iii)	Only if it is windy are we kite flying, and only if it is v	-
	we sailing.	[A p.87]
	We are sailing or kite flying—or skiing.	[A p.87]
	If—and only if—it is windy, we are sailing.	[A p.87]
(vi)	We are skiing only if it is windy or snowing.	[A p.87]
	We are skiing only if it is both windy and snowing.	[A p.87]
(viii)	If it is sunny, then if it is windy, we are kite flying.	[A p.87]
(ix)	We are sailing only if it is sunny, windy, and not snow	O
		[A p.87]

[A p.85]

(x)  $\neg(\neg R \land (\neg W \lor G))$ 

(x) If it is sunny and windy, we're sailing, and if it is snowing and not windy, we're skiing. [A p.87]

[Contents]

#### Exercises 2.5.1

1. State whether each of the following is a wff of PL.

(i)	$((A \rightarrow B))$	[A p.87]
(ii)	$(A \rightarrow \rightarrow B)$	[A p.87]
(iii)	$(A \to (A \to A))$	[A p.87]
(iv)	$A \to ((A \to A))$	[A p.87]
, ,	$((A \wedge B) \wedge)A$	[A p.87]
A(Si)	signment Project Exam H	e[p.87]
(viii)	$((A \lor A) \land BC))$	[A p.87]
(ix)	Ahttps://powcoder.com	[A p.87]
(x)	$((A \lor \overline{A}) \land ((A \lor A) \land ((A \lor A) \land A)))$	[A p.87]
2. Give redirive delivities of the following wooder		
(i)	The set of all odd numbers.	[A p.88]
(ii)	The set of all numbers divisible by five.	[A p.88]
(iii)	The set of all "words" (finite strings of letters) that use not necessarily both of) the letters $a$ and $b$ .	e only (but [A p.88]
(iv)	The set containing all of Bob's ancestors.	[A p.88]
(v)	The set of all cackles: hah hah hah, hah hah hah hah hah hah, and so on.	n, hah hah [A p.88]
		[Contents]

#### Exercises 2.5.3.1

Write out a construction for each of the following wffs, and state the main connective.

1. $(\neg P \lor (Q \land R))$	[A p.89]
2. $\neg (P \land (Q \lor R))$	[A p.89]
3. $((\neg P \land \neg Q) \lor \neg R)$	[A p.89]
4. $((P \rightarrow Q) \lor (R \rightarrow S))$	[A p.89]
5. $(((P \leftrightarrow Q) \leftrightarrow R) \leftrightarrow S)$	[A p.89]
6. $((\neg P \land \neg \neg P) \to (P \land \neg P))$	[A p.90]

[Contents]

## Assignment Project Exam Help

#### Exercises 2.5.4.1

1. For each tips emailing wile in §2.5.4, state which disambiguation (1–5) results from restoring parentheses to our original expression in this order.

## Add WeChat powcoder [Ap.90]

[Contents]

#### Exercises 2.5.5.1

1. Write the following in the notation of this book:

(i) $\vee \neg P \wedge QR$	[A p.90]
(ii) $\neg \land \lor PQR$	[A p.90]
(iii) $\land \neg \lor PQR$	[A p.90]
(iv) $\vee \wedge \neg P \neg Q \neg R$	[A p.90]
$(v) \leftrightarrow \leftrightarrow PQRS$	[A p.90]

2. Write the following in Polish notation:

(i) 
$$\neg (P \land (Q \lor R))$$
 [A p.91]

(ii) 
$$([P \rightarrow (Q \lor R)] \rightarrow S)$$
 [A p.91]  
(iii)  $[(P \rightarrow Q) \lor (R \rightarrow S)]$  [A p.91]  
(iv)  $(P \rightarrow [(Q \lor R) \rightarrow S])$  [A p.91]  
(v)  $[(\neg P \land \neg \neg P) \rightarrow (P \land \neg P)]$  [A p.91]  
[Contents]

## Assignment Project Exam Help

https://powcoder.com

Add WeChat powcoder

## **Chapter 3**

## **Semantics of Propositional Logic**

#### **Exercises 3.2.1**

Determine the truth values of the following wiffs, given the truth values for the basic components.

	$(\neg P \land (Q \lor R))$	[A p.92]
2.	$\begin{array}{c} {}^{T} \underset{T}{https://powcoder.com} \\ {}^{T} \underset{T}{\overset{T}{powcoder.com}} \\ {}^{R))} \end{array}$	[A p.92]
3.	(¬¬FAdd We Chat) powcoder	[A p.92]
4.	$ \begin{array}{ccccc} (\neg \neg P & \wedge & (Q & \rightarrow & (R & \vee & P))) \\ T & F & F & T \end{array} $	[A p.92]
5.	$ \begin{array}{ccccc} ((P & \vee & Q) & \rightarrow & (P & \vee & P)) \\ F & T & F & F \end{array} $	[A p.92]
6.	$ \begin{array}{ccccc} ((P & \vee & Q) & \rightarrow & (P & \vee & P)) \\ T & & F & & T & & T \end{array} $	[A p.93]
7.	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	[A p.93]
8.	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	[A p.93]
9.	$\neg (((\neg P \leftrightarrow P) \leftrightarrow Q) \rightarrow R) F F F F$	[A p.93]

10. 
$$\neg (((\neg P \leftrightarrow P) \leftrightarrow Q) \rightarrow R)$$
 $T T T T T$ 
[A p.93]

[Contents]

#### **Exercises 3.3.1**

Draw up truth tables for the following propositions.

1. $((P \land Q) \lor P)$	[A p.93]
2. $(P \wedge (P \vee P))$	[A p.94]
3. $\neg(\neg P \land \neg Q)$	[A p.94]
4. $(Q \rightarrow (Q \land \neg Q))$	[A p.94]
Assignment Project Exam H	[el/p <sup>.94]</sup>
6. $((P \lor Q) \leftrightarrow (P \land Q))$	[A p.94]
7. ¬((P) Attps://powcoder.com	[A p.94]
8. $(((P \rightarrow \neg P) \xrightarrow{\bullet} \neg P) \xrightarrow{\bullet} \neg P)$	[A p.94]
9. ¬(P ^ Add WeChat powcoder	[A p.95]
10. $((\neg R \lor S) \land (S \lor \neg T))$	[A p.95]
	[Contents]

#### **Exercises 3.4.1**

Draw up a joint truth table for each of the following groups of propositions.

1. $(P \rightarrow Q)$ and $(Q \rightarrow P)$	[A p.95]
2. $\neg (P \leftrightarrow Q)$ and $((P \lor Q) \land \neg (P \land Q))$	[A p.95]
3. $\neg (P \land \neg Q)$ and $\neg Q$	[A p.95]
4. $((P \rightarrow Q) \land R)$ and $(P \lor (Q \lor R))$	[A p.96]
5. $((P \land Q) \land (\neg R \land \neg S))$ and $((P \lor (R \rightarrow Q)) \land S)$	[A p.96]

6. $(P \land \neg P)$ and $(Q \land \neg Q)$	[A p.96]
7. $(P \lor (Q \leftrightarrow R))$ and $((Q \rightarrow P) \land Q)$	[A p.96]
8. $\neg((P \land Q) \land R)$ and $((P \rightarrow Q) \leftrightarrow (P \rightarrow R))$	[A p.97]
9. $(P \lor Q)$ , $\neg P$ and $(Q \lor Q)$	[A p.97]
10. $(P \rightarrow (Q \rightarrow (R \rightarrow S)))$ and $\neg S$	[A p.97]
	[Contents]

#### Exercises 3.5.1

- 1. Can the meaning of any of our two-place connectives  $(\land, \lor, \rightarrow, \leftrightarrow)$  be specified as the truth function  $f_2^2$  defined in Figure 3.2? [A p.98]
- Apply guth friend f and f and f and f (respectively) can be specified as these truth functions. [A p.98]
- 3. Suppose we introduce a new one-place connective  $\star$  and specify its meaning to be such protein G defined in G large. What is the truth value of  $\star A$  when A is T? [A p.98]
- 4. What truth salties to you need to know to determine the truth value of  $\star(A \to B)$ ?
  - (i) The truth values of *A* and *B*.
  - (ii) The truth value of *A* but not of *B*.
  - (iii) The truth value of *B* but not of *A*.
  - (iv) None. [A p.98]

5. Which of our connectives could have its meaning specified as the two-place function g(x, y) defined as follows?

$$g(x,y) = f_3^2(f_2^1(x),y)$$

[A p.98]

[Contents]

## **Chapter 4**

#### **Uses of Truth Tables**

#### **Exercises 4.1.2**

Use truth tables to determine whether each of the following arguments is valid SSangare under that is no Oak Give a Water ample 10

1. 
$$A \lor B$$
 $A \to Chttps://powcoder.com$ 
 $\therefore (B \to C) \not\models e://powcoder.com$ 
[A p.99]

2.  $\neg A$ 
 $\therefore \neg ((Add) (WeChat powcoder)$ 

3.  $(A \land \neg B) \to C$ 
 $\neg C$ 
 $B$ 
 $\therefore \neg A$ 
[A p.100]

4.  $(A \land B) \leftrightarrow C$ 
 $A$ 
 $\therefore C \to B$ 
[A p.100]

5.  $(\neg A \land \neg B) \leftrightarrow \neg C$ 
 $\neg (A \lor B)$ 
 $\therefore C \to \neg C$ 
[A p.100]

6.  $A \lor B$ 
 $\neg A \lor C$ 
 $B \to C$ 
 $\therefore C$ 
[A p.101]

7. 
$$\neg (A \lor B) \leftrightarrow \neg C$$
  
 $\neg A \land \neg B$   
 $\therefore C \land \neg C$  [A p.101]  
8.  $\neg (A \land B) \rightarrow (C \lor A)$   
 $\neg A \lor \neg B$   
 $A$   
 $\therefore \neg (C \lor \neg C)$  [A p.101]  
9.  $A \rightarrow (B \land C)$   
 $B \leftrightarrow \neg C$   
 $\therefore \neg A$  [A p.102]  
10.  $A \rightarrow B$   
 $B \rightarrow C$   
 $\neg C$   
Assignment Project Exam Helphonents]

## Exercise https://powcoder.com

Write out truth tables for the following propositions, and state whether each is a tautology, a contradiction, or neither

acri	15 a tautope, acommon to he the Wich der	
1.	((P \( Q \) \( \rightarrow P \))	[A p.102]
2.	$(\neg P \land (Q \lor R))$	[A p.103]
3.	$((\neg P \lor Q) \leftrightarrow (P \land \neg Q))$	[A p.103]
4.	$(P \to (Q \to (R \to P)))$	[A p.103]
5.	$(P \to ((P \to Q) \to Q))$	[A p.103]
6.	$(P \to ((Q \to P) \to Q))$	[A p.104]
7.	$((P \to Q) \lor \neg (Q \land \neg Q))$	[A p.104]
8.	$((P \to Q) \lor \neg (Q \land \neg P))$	[A p.104]
9.	$((P \land Q) \leftrightarrow (Q \leftrightarrow P))$	[A p.104]
10.	$\neg((P \land Q) \to (Q \leftrightarrow P))$	[A p.104]
		[Contents]

#### Exercises 4.3.1

Write out joint truth tables for the following pairs of propositions, and state in each case whether the two propositions are (a) jointly satisfiable, (b) equivalent, (c) contradictory, (d) contraries.

1. $(P \rightarrow Q)$ and $\neg (P \land \neg Q)$	[A p.105]
2. $(P \wedge Q)$ and $(P \wedge \neg Q)$	[A p.105]
3. $\neg (P \leftrightarrow Q)$ and $\neg (P \rightarrow Q) \lor \neg (P \lor \neg Q)$	[A p.105]
4. $(P \rightarrow (Q \rightarrow R))$ and $((P \rightarrow Q) \rightarrow R)$	[A p.106]
5. $(P \land (Q \land \neg Q))$ and $\neg(Q \rightarrow \neg(R \land \neg Q))$	[A p.106]
6. $(P \land \neg P)$ and $(R \lor \neg R)$	[A p.107]
Assignment Project Exam F	[e4p107]
8. $((P \rightarrow Q) \rightarrow R)$ and $\neg (P \lor \neg (Q \land \neg R))$	[A p.108]
9. (P +> Phttps://powcoder.com	[A p.108]
10. $(P \leftrightarrow Q)$ and $((P \land Q) \lor (\neg P \land \neg Q))$	[A p.109]

## Add WeChat powcoder [Contents]

#### **Exercises 4.4.1**

Write out a joint truth table for the propositions in each of the following sets, and state whether each set is satisfiable.

1. $\{(P \vee Q), \neg (P \wedge Q), P\}$	[A p.109]
2. $\{\neg(P \to Q), (P \leftrightarrow Q), (\neg P \lor Q)\}$	[A p.109]
3. $\{(P \rightarrow \neg P), (P \vee \neg P), (\neg P \rightarrow P)\}$	[A p.109]
4. $\{((P \lor Q) \lor R), (\neg P \to \neg Q), (\neg Q \to \neg R), \neg P\}$	[A p.110]
5. $\{(P \leftrightarrow Q), (Q \lor R), (R \rightarrow P)\}$	[A p.110]
6. $\{(\neg P \to \neg Q), (P \leftrightarrow Q), P\}$	[A p.110]
7. $\{\neg P, (P \to (P \to P)), (\neg P \leftrightarrow P)\}$	[A p.110]

8. 
$$\{(P \lor \neg Q), (P \to R), \neg R, (\neg R \to Q)\}$$
 [A p.111]  
9.  $\{\neg R, \neg P, ((Q \to \neg Q) \to R)\}$  [A p.111]  
10.  $\{(\neg P \lor \neg Q), \neg (P \land \neg Q), (P \lor \neg Q), \neg (\neg P \land \neg Q)\}$  [A p.111]  
[Contents]

## Assignment Project Exam Help

https://powcoder.com

Add WeChat powcoder

## Chapter 5

## **Logical Form**

#### Exercises 5.1.1

For each of the following propositions, give three correct answers to the question Significant of this possition of the following propositions, give three correct answers to the question Significant of the following propositions, give three correct answers to the question Significant of the following propositions, give three correct answers to the question of the following propositions, give three correct answers to the question of the following propositions of the following proposition of the follo

1. $\neg (R \rightarrow (R \rightarrow Q))$	[A p.112]
2. (R \rightarrow Phttpsp)//powcoder.com	[A p.112]
3. $P \wedge (\neg P \rightarrow Q)$	[A p.112]
4. ((¬P VAdd +WeChat powcoder	[A p.112]
	[Contents]

#### Exercises 5.2.1

1. The following propositions all have three logical forms in common. State what the three forms are, and in each case, show what replacements of variables by propositions are required to obtain the three propositions from the form.

(i) 
$$\neg \neg C$$
  
(ii)  $\neg \neg (A \land B)$   
(iii)  $\neg \neg (C \land \neg D)$  [A p.113]

2. State whether the given propositions are instances of the given form. If so, show what replacements of variables by propositions are required to obtain the proposition from the form.

(i) Form: $\neg(\alpha \to \beta)$	
Propositions:	
(a) $\neg (P \rightarrow Q)$	[A p.113]
(b) $\neg (R \rightarrow Q)$	[A p.113]
(c) $\neg (R \rightarrow (R \rightarrow Q))$	[A p.113]

(ii) Form:  $\neg(\alpha \to (\alpha \to \beta))$  Propositions:

(a) 
$$\neg (P \to (P \to Q))$$
 [A p.113]  
(b)  $\neg (P \to (P \to P))$  [A p.113]  
(c)  $\neg (P \to (Q \to P))$  [A p.113]

## Assignment Project Exam Help Propositions:

(a) $(\neg P \lor Q)  (\neg P \land Q)$	[A p.113]
(a) (¬P \ Q) (¬P \ Q) (¬P \ Q) coder.com	[A p.113]
(c) $\neg (R \lor S) \to \neg (R \land S)$	[A p.113]

## (iv) Form: 1 (1) (1) Wa Chat powcoder

(a) $(P \lor Q) \lor (Q \lor (P \lor Q))$	[A p.113]
(b) $Q \lor (\neg Q \lor (Q \land Q))$	[A p.113]
(c) $\neg P \lor (\neg \neg P \lor \neg P)$	[A p.113]

[Contents]

#### Exercises 5.3.1

For each of the following arguments, give four correct answers to the question "what is the form of this argument?" For each form, show what replacements of variables by propositions are required to obtain the argument from the form.

1. 
$$\neg (R \to (R \to Q))$$
  
 $\therefore R \lor (R \to Q)$  [A p.114]

2. 
$$(P \land Q) \rightarrow Q$$
  
 $\neg Q$   
 $\therefore \neg (P \land Q)$  [A p.114]  
3.  $\neg Q \rightarrow (R \rightarrow S)$   
 $\neg Q$   
 $\therefore R \rightarrow S$  [A p.115]  
4.  $(P \rightarrow \neg Q) \lor (\neg Q \rightarrow P)$   
 $\neg (\neg Q \rightarrow P)$   
 $\therefore P \rightarrow \neg Q$  [A p.115]

#### Exercises 5.4.1

For Act of the following at a protection of the form:

$${\overset{\alpha}{\underset{...}{\alpha}}} {\overset{\beta}{\rightarrow}} https://powcoder.com$$

by stating what substitutions of propositions for variables have to be made to otbain the argument from the form and (ii) show by producing a truth table for the argument that it is valid.

1. 
$$P$$
 $P \to Q$ 
 $\therefore Q$ 

[A p.116]

2.  $(A \land B)$ 
 $(A \land B) \to (B \lor C)$ 
 $\therefore (B \lor C)$ 

[A p.116]

3.  $(A \lor \neg A)$ 
 $(A \lor \neg A) \to (A \land \neg A)$ 
 $\therefore (A \land \neg A)$ 
 $\therefore (A \land \neg A)$ 
[A p.116]

4.  $(P \to \neg P)$ 
 $(P \to \neg P) \to (P \to (Q \land \neg R))$ 
 $\therefore (P \to (Q \land \neg R))$ 
[A p.116]

[Contents]

#### Exercises 5.5.1

1. (i) Show by producing a truth table for the following argument form that it is invalid:

$$\alpha$$

$$\therefore \beta$$
[A p.117]

(ii) Give an instance of the above argument form that is valid; show that it is valid by producing a truth table for the argument.

[A p.117]

2. While it is not true in general that every instance of an invalid argument form is an invalid argument, there are some invalid argument forms whose instances are always invalid arguments. Give an example of such an argument form.

[A p.117]

Assignment Project Exam Help

https://powcoder.com

Add WeChat powcoder

# Connectives: Translation and Adequacy

# Exercises 6.5.1 ent Project Exam Help

Translate the following arguments into PL and then assess them for validity (you may use shortcuts in your truth tables).

- https://powcoder.com

  1. Bob is happy if and only if it is raining. Either it is raining or the sun is shining. So Bob is happy only if the sun is not shining. [A p.118]
- 2. If I have a rest. So if I have a rest, I have money. [A p.119]
- 3. Maisy is upset only if there is thunder. If there is thunder, then there is lightning. Therefore, either Maisy is not upset, or there is lightning.

  [A p.121]
- 4. The car started only if you turned the key and pressed the accelerator. If you turned the key but did not press the accelerator, then the car did not start. The car did not start—so either you pressed the accelerator but did not turn the key, or you neither turned the key nor pressed the accelerator.

  [A p.122]
- 5. Either Maisy isn't barking, or there is a robber outside. If there is a robber outside and Maisy is not barking, then she is either asleep or depressed. Maisy is neither asleep nor depressed. Hence Maisy is barking if and only if there is a robber outside.

  [A p.123]

- 6. If it isn't sunny, then either it is too windy or we are sailing. We are having fun if we are sailing. It is not sunny and it isn't too windy either—hence we are having fun.

  [A p.124]
- 7. Either you came through Singleton and Maitland, or you came through Newcastle. You didn't come through either Singleton or Maitland—you came through Cessnock. Therefore, you came through both Newcastle and Cessnock. [A p.125]
- 8. We shall have lobster for lunch, provided that the shop is open. Either the shop will be open, or it is Sunday. If it is Sunday, we shall go to a restaurant and have lobster for lunch. So we shall have lobster for lunch.

  [A p.126]

9. Catch Billy a fish, and you will feed him for a day. Teach him to fish, and you'll feed him for life. So either you won't feed Billy for life, or you will teach him to fish.

Assignment Project Exam Help

10. I'll be happy if the Tigers win. Moreover, they will win—or else they won't. However, assuming they don't, it will be a draw. Therefore, if it's not a draw, and they don't win I'll be happy.

[A p.128]

[Contents]

### Exercises Add WeChat powcoder

1. State whether each of the following is a functionally complete set of connectives. Justify your answers.

	(1)	$\{\rightarrow, \neg\}$	[A p.128]
	(ii)	$\{\leftrightarrow, \veebar\}$	[A p.129]
(	iii)	$\{\mathfrak{Q}_{15}\}\$ (The connective $\mathfrak{Q}_{15}$ is often symbolized by $\downarrow$ ;	
		another common symbol for this connective is NOR.)	[A p.130]
(	iv)	$\{\rightarrow, \land\}$	[A p.130]
	(v)	$\{\neg, ②_{12}\}$	[A p.131]
(	vi)	$\{\lor, @_4\}$	[A p.131]

2. Give the truth table for each of the following propositions.

(i)  $B \otimes_{14} A$  [A p.131]

(ii) $(A @_{11} B) @_{15} B$	[A p.131]
(iii) $\neg (A \lor (A @_6 B))$	[A p.131]
(iv) $A \leftrightarrow (A \otimes_3 \neg B)$	[A p.131]
(v) $(A @_{12} B) \veebar (B @_{12} A)$	[A p.132]
(vi) $(A @_{12} B) \lor (B @_{16} A)$	[A p.132]

3. Consider the three-place connectives  $\sharp$  and  $\natural$ , whose truth tables are as follows:

	α	β	$\gamma$	$\sharp(\alpha,\beta,\gamma)$	$\natural(\alpha,\beta,\gamma)$	
	T	T	T	T	F	
	T	T	F	F	F	
	T	F	T	T	T	
	T	F	F	T	T	
	F	T	T	T	T	
Assignme	h	$\mathbf{t}_{\mathrm{F}}^{\mathrm{T}}$	Pr	oject	Exan	n Help
	F	F	F	T	F	•

- (i) Defired busing only but not necessarily all pf) the connectives [A p.132]
- (ii) Do the same for  $\natural$ . [A p.132]
- 4. State a projection of Cingaty proposition.

	(i)	$\neg(A \to B)$	[A p.132]
	(ii)	$\neg(A \lor B)$	[A p.132]
	(iii)	$\neg A \lor \neg B$	[A p.132]
	(iv)	$\neg(\neg A \lor B)$	[A p.132]
	(v)	$A \leftrightarrow B$	[A p.132]
	(vi)	$(A \to B) \lor (B \to A)$	[A p.132]
5.	(i)	What is the dual of $\mathbb{O}_1$ ?	[A p.132]
	(ii)	What is the dual of $\rightarrow$ ?	[A p.133]
	(iii)	Which one-place connectives are their own duals?	[A p.133]
	(iv)	Which two-place connectives are their own duals?	[A p.133]
			[Contents]

### **Trees for Propositional Logic**

#### **Exercises 7.2.1.1**

Apply the appropriate tree rule to each of the following proportion $ASSIS nment Project Exam H$ 1. $(\neg A \lor \neg B)$	itions. EIP [A p.134]
	[A p.134]
$\underset{3. ((A \rightarrow B) \land B)}{\overset{2. (\neg A \rightarrow B)}{\rightarrow}} \text{ttps://powcoder.com}$	[A p.134]
$ \overset{4. \ ((A \leftrightarrow B) \leftrightarrow B)}{\underset{5. \ \neg (A \leftrightarrow \neg \neg A)}{}} \overset{4. \ ((A \leftrightarrow B) \leftrightarrow B)}{\underset{7. \ \neg (A \leftrightarrow \neg \neg A)}{}} \overset{B)}{\overset{A}{\overset{A}{\overset{A}{\overset{A}{\overset{A}{\overset{A}{\overset{A}{$	[A p.134] [A p.134]
5. $\neg (A \leftrightarrow \neg \neg A)$	[A p.134]
6. $\neg(\neg A \lor B)$	[A p.135]
	[Contents]

#### **Exercises 7.2.2.1**

Construct finished trees for each of the following propositions.

$1. \ ((A \to B) \to B)$	[A p.135]
$2. \ ((A \to B) \lor (B \to A))$	[A p.135]
$3. \neg (\neg A \rightarrow (A \lor B))$	[A p.135]
$4. \ \neg\neg((A \land B) \lor (A \land \neg B))$	[A p.135]
	[Contents]

#### Exercises 7.2.3.1

Construct finished trees for each of the following propositions; close paths as appropriate.

$1. \ \neg(A \to (B \to A))$	[A p.136]
$2. ((A \rightarrow B) \lor (\neg A \lor B))$	[A p.136]
$3. \neg ((A \to B) \lor (\neg A \lor B))$	[A p.136]
4. $\neg\neg\neg(A \lor B)$	[A p.136]
5. $\neg(A \land \neg A)$	[A p.136]
6. $\neg(\neg(A \land B) \leftrightarrow (\neg A \lor \neg B))$	[A p.137]

[Contents]

# Assignment Project Exam Help

#### Exercises 7.3.1.1

Using trees, deterpise where We GOV to a agent are valid. For any arguments that are invalid, give a counterexample.

- 1. Add WeChat powcoder [A p.137] 2.  $(A \vee B)$ ∴ B [A p.137] 3.  $(A \vee B)$  $(A \rightarrow C)$  $(B \rightarrow D)$  $(C \vee D)$ [A p.138]  $((A \vee \neg B) \to C)$ 4.  $(B \rightarrow \neg D)$ D ∴ C [A p.138]
- 5. B  $(A \rightarrow B)$   $\therefore A$ [A p.138]

6. 
$$A$$
 $(A \rightarrow B)$ 
 $\therefore B$ 

[A p.138]

7.  $(A \lor (B \land C))$ 
 $(A \rightarrow B)$ 
 $(B \leftrightarrow D)$ 
 $\therefore (B \land D)$ 

8.  $\neg (\neg A \rightarrow B)$ 
 $\neg (C \leftrightarrow A)$ 
 $(A \lor C)$ 
 $\neg (C \rightarrow B)$ 
 $\therefore \neg (A \rightarrow B)$ 

9.  $(A \leftrightarrow B)$ 
 $(B \rightarrow C)$ 

Assignment Project Exam Help
 $(A \lor (B \land \neg B))$ 
 $\therefore C$ 

[A p.140]

10.  $(Attps://powcoder.com)$ 
 $(B \rightarrow C)$ 
 $(C \rightarrow D)$ 
 $(DAdd_E)$  We Chat powcoder
[A p.140]

[Contents]

#### Exercises 7.3.2.1

1. Using trees, test whether the following propositions are contradictions. For any proposition that is satisfiable, read off from an open path a scenario in which the proposition is true.

(i)	$A \wedge \neg A$	[A p.141]
(ii)	$(A \lor B) \land \neg (A \lor B)$	[A p.141]
(iii)	$(A \to B) \land \neg (A \lor B)$	[A p.141]
(iv)	$(A \to \neg(A \lor B)) \land \neg(\neg(A \lor B) \lor B)$	[A p.141]
(v)	$\neg((\neg B \lor C) \leftrightarrow (B \to C))$	[A p.142]
(vi)	$(A \leftrightarrow \neg A) \lor (A \rightarrow \neg (B \lor C))$	[A p.142]

2. Using trees, test whether the following sets of propositions are satisfiable. For any set that is satisfiable, read off from an open path a scenario in which all the propositions in the set are true.

(i) 
$$\{(A \lor B), \neg B, (A \to B)\}$$
 [A p.142]  
(ii)  $\{(A \lor B), (B \lor C), \neg (A \lor C)\}$  [A p.142]  
(iii)  $\{\neg (\neg A \to B), \neg (C \leftrightarrow A), (A \lor C), \neg (C \to B), (A \to B)\}$  [A p.143]  
(iv)  $\{(A \leftrightarrow B), \neg (A \to C), (C \to A), (A \land B) \lor (A \land C)\}$  [A p.143] [Contents]

#### Exercises 7.3.3.1

Test whether the following pale of propositions are contraries contradictories, or jointly satisfiable.

1. $(\neg A \rightarrow B)$ and $(B \rightarrow A)$	[A p.144]
2. (A -> https://pow.coder.com	[A p.144]
3. $\neg (A \leftrightarrow \neg B)$ and $\neg (A \lor \neg B)$	[A p.145]
4. ¬(A V A)dd(WeC)hat powcoder	[A p.146]
5. $(\neg A \land (A \rightarrow B))$ and $\neg (\neg A \rightarrow (A \rightarrow B))$	[A p.147]
6. $((A \rightarrow B) \leftrightarrow B)$ and $\neg (A \rightarrow B)$	[A p.147]
	[Contents]

#### Exercises 7.3.4.1

Test whether the following propositions are tautologies. (Remember to restore outermost parentheses before adding the negation symbol at the front—recall §2.5.4.) For any proposition that is not a tautology, read off from your tree a scenario in which it is false.

1. 
$$A \to (B \to A)$$
 [A p.148]  
2.  $A \to (A \to B)$  [A p.148]

3.	$((A \land B) \lor \neg(A \to B)) \to (C \to A)$	[A p.148]
4.	$(A \land (B \lor C)) \leftrightarrow ((A \land B) \lor (A \land C))$	[A p.149]
5.	$\neg A \lor \neg (A \land B)$	[A p.149]
6.	$A \lor (\neg A \land \neg B)$	[A p.149]
7.	$(A \to B) \lor (A \land \neg B)$	[A p.150]
8.	$(B \land \neg A) \leftrightarrow (A \leftrightarrow B)$	[A p.150]
9.	$(A \vee (B \vee C)) \leftrightarrow ((A \vee B) \vee C)$	[A p.150]
10.	$(A \land (B \lor C)) \leftrightarrow ((A \lor B) \land C)$	[A p.151]
		[Contents]

### Exasignment Project Exam Help

Test whether the following are equivalent. Where the two propositions are not equivalent of the company with the tenaround the have different truth values.

1. $P \text{ and } (P \wedge P)$ We Chat powered are	[A p.151]
1. $P \text{ and } (R \wedge R)$ 2. $(P \to (Q \vee \neg Q)) \text{ and } (R \to R)$ <b>WeChat powcoder</b>	[A p.151]
3. $\neg (A \lor B)$ and $(\neg A \land \neg B)$	[A p.152]
4. $\neg (A \lor B)$ and $(\neg A \lor \neg B)$	[A p.152]
5. $\neg (A \land B)$ and $(\neg A \land \neg B)$	[A p.152]
6. $\neg (A \land B)$ and $(\neg A \lor \neg B)$	[A p.153]
7. $A$ and $((A \land B) \lor (A \land \neg B))$	[A p.153]
8. $\neg (P \leftrightarrow Q)$ and $((P \land \neg Q) \lor (\neg P \land Q))$	[A p.154]
9. $((P \land Q) \rightarrow R)$ and $(P \rightarrow (\neg Q \lor R))$	[A p.154]
10. $\neg (P \leftrightarrow Q)$ and $(Q \land \neg P)$	[A p.155]
	[Contents]

# The Language of Monadic **Predicate Logic**

# Exercises 8.2.1 ent Project Exam Help Translate the following propositions from English into MPL:

1.	The Parific Ocean is heautiful coder.com	[A p.156]
2.	New York is heavily populated.	[A p.156]
3.	Mary is Aiced WeChat powcoder	[A p.156]
4.	John is grumpy.	[A p.157]
5.	Seven is a prime number.	[A p.157]
6.	Pluto is a planet.	[A p.157]
7.	Bill and Ben are gardeners	[A p.157]
8.	If Mary is sailing or Jenny is kite flying, then Bill and Ben ar	e grumpy.
		[A p.157]
9.	Mary is neither sailing nor kite flying.	[A p.157]
10.	Only if Mary is sailing is Jenny kite flying.	[A p.157]
11.	John is sailing or kite flying but not both.	[A p.157]
12.	If Mary isn't sailing, then unless he's kite flying, John is sa	iling.
		[A p.157]

13. Jenny is sailing only if both Mary and John are.	[A p.157]
14. Jenny is sailing if either John or Mary is.	[A p.157]
15. If—and only if—Mary is sailing, Jenny is kite flying.	[A p.157]
16. If Steve is winning, Mary isn't happy.	[A p.157]
17. Two is prime, but it is also even.	[A p.157]
18. Canberra is small—but it's not tiny, and it's a capital city	y. [A p.157]
19. If Rover is kite flying, then two isn't prime.	[A p.157]
20. Mary is happy if and only if Jenny isn't.	[A p.157]
	[Contents]

### Exasignment Project Exam Help

Translate the following from English into MPL. 1. If Independence Hall is red, then something is red. [A p.158] 2. If everything is red, then Independence Hall is red. [A p.158] 3. Nothing is both green and red. powcoder [A p.158] 4. It is not true that nothing is both green and red. [A p.158] 5. Red things aren't green. [A p.158] [A p.158] 6. All red things are heavy or expensive. 7. All red things that are not heavy are expensive. [A p.158] 8. All red things are heavy, but some green things aren't. [A p.158] 9. All red things are heavy, but not all heavy things are red. [A p.158] 10. Some red things are heavy, and furthermore some green things are heavy too. [A p.158] 11. Some red things are not heavy, and some heavy things are not red. [A p.158]

12. If Kermit is green and red, then it is not true that nothin green and red.	g is both [A p.159]
13. Oscar's piano is heavy, but it is neither red nor expensive.	[A p.159]
14. If Spondulix is heavy and expensive, and all expensive things are red and all heavy things are green, then Spondulix is red and green. <sup>1</sup>	
	[A p.159]
15. If Kermit is heavy, then something is green and heavy.	[A p.159]
16. If everything is fun, then nothing is worthwhile.	[A p.159]
17. Some things are fun and some things are worthwhile, but n both.	nothing is [A p.159]
0 1	[A p.159]
19 Assitgramentol Projector Extarma Help.	
	[A p.159]
20. If something serval powereder.com	[A p.159]
	Contents]
Add WeChat powcoder	

# Exercises 8.3.5

Translate the following propositions from English into MPL.

1. Everyone is happy.	[A p.159]
2. Someone is sad.	[A p.159]
3. No one is both happy and sad.	[A p.159]
4. If someone is sad, then not everyone is happy.	[A p.159]
5. No one who isn't happy is laughing.	[A p.160]
6. If Gary is laughing, then someone is happy.	[A p.160]
7. Whoever is laughing is happy.	[A p.160]

<sup>&</sup>lt;sup>1</sup>"Spondulix" is the name of a famous gold nugget, found in 1872.

8. Everyone is laughing if Gary is.	[A p.160]
9. Someone is sad, but not everyone and not Gary.	[A p.160]
10. Gary isn't happy unless everyone is sad.	[A p.160]
11. All leaves are brown and the sky is gray.	[A p.160]
12. Some but not all leaves are brown.	[A p.160]
13. Only leaves are brown.	[A p.160]
14. Only brown leaves can stay.	[A p.160]
15. Everyone is in trouble unless Gary is happy.	[A p.160]
16. Everyone who works at this company is in trouble unless happy.  1. Assignment herriojtect mexicing. H	[A p.160]
18. If no one is lying, then Stephanie is telling the truth.	[A p.160]
19. Either Stephpis is ly in Concleting Go Irinh and is in trouble.	d everyone [A p.160]
20. If Gary is lying the not everyone in this room is telling to	he truth.
ridd weenat poweoder	[A p.160]
	[Contents]

#### Exercises 8.4.3.1

Write out a construction for each of the following wffs, and state the main operator.

$1. \ \forall x (Fx \to Gx)$	[A p.161]
2. $\forall x \neg Gx$	[A p.161]
3. $\neg \exists x (Fx \land Gx)$	[A p.161]
4. $(Fa \land \neg \exists x \neg Fx)$	[A p.161]
5. $\forall x (Fx \land \exists y (Gx \rightarrow Gy))$	[A p.162]

6. $(\forall x (Fx \to Gx) \land Fa)$	[A p.162]
7. $((\neg Fa \land \neg Fb) \rightarrow \forall x \neg Fx)$	[A p.162]
8. $\forall x \forall y ((Fx \land Fy) \rightarrow Gx)$	[A p.163]
9. $\forall x(Fx \to \forall yFy)$	[A p.163]
$10. \ (\forall x Fx \to \forall y Fy)$	[A p.163]
	[Contents]

#### **Exercises 8.4.5.1**

Identify any free variables in the following formulas. State whether each formula is open or closed.

14-	Assignment Project Exam H	<b>1</b> [0163]
2.	$Tx \wedge Ty$	[A p.163]
3.	3xTx https://powcoder.com	[A p.163]
4.	$\exists xTx \land \forall yFx$	[A p.163]
5.	∃xTx \ Axdd WeChat powcoder	[A p.164]
6.	$\exists x (Tx \land Fx)$	[A p.164]
7.	$\forall y \exists x T y$	[A p.164]
8.	$\exists x (\forall x Tx \to \exists y Fx)$	[A p.164]
9.	$\exists y \forall x Tx \to \exists y Fx$	[A p.164]
10.	$\forall x(\exists xTx \wedge Fx)$	[A p.164]
11.	$\forall x \exists x Tx \wedge Fx$	[A p.164]
12.	$\exists x T y$	[A p.164]
13.	$\forall xTx \to \exists xFx$	[A p.164]
14.	$\exists x \forall y (Tx \vee Fy)$	[A p.164]
15.	$\forall x Fx \wedge Gx$	[A p.164]

$16. \ \forall x \forall y Fx \to Gy$	[A p.164]
17. $\forall x \forall y (Fx \rightarrow \forall x Gy)$	[A p.164]
18. $\exists yGb \wedge Gc$	[A p.164]
$19. \ \exists yGy \land \forall x(Fx \to Gy)$	[A p.164]
20. $\forall x((Fx \to \exists xGx) \land Gx)$	[A p.164]
	[Contents]

### Assignment Project Exam Help

https://powcoder.com

Add WeChat powcoder

### **Semantics of Monadic Predicate Logic**

#### Exercises 911 Assignment Project Exam Help

For each of the propositions:

### https://poweoder.com

state whether it is true or false on each of the following models.

Add WeChat nowcoder

1.	Domain: $\{1, 2, 3, \dots\}^2$ Referent of $a$ : 1	
	Extension of <i>P</i> : $\{1, 3, 5,\}^3$	[A p.165]
2.	Domain: $\{1,2,3,\}$ Referent of $a$ : 1 Extension of $P$ : $\{2,4,6,\}^4$	[A p.165]
3.	Domain: $\{1,2,3,\ldots\}$ Referent of $a$ : 2 Extension of $P$ : $\{1,3,5,\ldots\}$	[A p.165]
4.	Domain: {1,2,3,}	[A p.100]
	Referent of $a$ : 2 Extension of $P$ : $\{2,4,6,\}$	[A p.165]

<sup>&</sup>lt;sup>2</sup>That is, the set of positive integers.

<sup>&</sup>lt;sup>3</sup>That is, the set of odd numbers.

<sup>&</sup>lt;sup>4</sup>That is, the set of even numbers.

5. Domain: {1,2,3,...}
Referent of *a*: 1
Extension of *P*: {1,2,3,...}

[A p.165]
6. Domain: {1,2,3,...}
Referent of *a*: 2
Extension of *P*: Ø

[A p.165]

#### Exercises 9.2.1

State whether each of the following propositions is true or false in each of the six models given in Exercises 9.1.1.

$$\inf_{\text{(iv)}} \Pr_{(\exists x P x)}^{(\exists x P x)} \text{s://powcoder.com}$$

(v)  $\neg (\forall x Px \land \neg \exists x Px)$  WeChat powcoder [Contents]

#### Exercises 9.3.1

1. If  $\alpha(x)$  is  $(Fx \wedge Ga)$ , what is

(i)	$\alpha(a/x)$	[A p.166]
(ii)	$\alpha(b/x)$	[A p.166]

2. If  $\alpha(x)$  is  $\forall y(Fx \rightarrow Gy)$ , what is

(i) 
$$\alpha(a/x)$$
 [A p.166]  
(ii)  $\alpha(b/x)$  [A p.166]

3. If  $\alpha(x)$  is  $\forall x(Fx \to Gx) \land Fx$ , what is

(i) 
$$\alpha(a/x)$$
 [A p.166]

(ii) $\alpha(b/x)$	[A p.166]
4. If $\alpha(x)$ is $\forall x(Fx \land Ga)$ , what	is
(i) $\alpha(a/x)$	[A p.166]
(ii) $\alpha(b/x)$	[A p.166]
5. If $\alpha(y)$ is $\exists x(Gx \to Gy)$ , wha	t is
(i) $\alpha(a/y)$	[A p.166]
(ii) $\alpha(b/y)$	[A p.166]
6. If $\alpha(x)$ is $\exists y(\forall x(Fx \to Fy) \lor$	Fx), what is
(i) $\alpha(a/x)$	[A p.166]
(ii) $\alpha(b/x)$	[A p.166]
Assignment Pr	oject Exam Helpots
1. Here is a model:  Domain: {1,2,3,4}	vcoder.com  lowing propositions is true or false in
State whether each of the fo	llowing propositions is true or false in
(i) $\forall x E x$	[A p.167]
(ii) $\forall x (Ex \lor Ox)$	[A p.167]
(iii) $\exists x E x$	[A p.167]

- 2. State whether the given proposition is true or false in the given models.
  - (i)  $\forall x (Px \lor Rx)$

(iv)  $\exists x (Ex \land Ox)$ 

(v)  $\forall x (\neg Ex \rightarrow Ox)$ 

(vi)  $\forall x E x \vee \exists x \neg E x$ 

(a) Domain: {1,2,3,4,5,6,7,8,9,10} Extensions: *P*: {1,2,3} *R*: {5,6,7,8,9,10} [A p.167]

[A p.167]

[A p.167]

[A p.167]

(b) Domain: {1,2,3,4,5,6,7,8,9,10} Extensions: <i>P</i> : {1,2,3,4} <i>R</i> : {4,5,6,7,8,9,10} [A p.167]
(ii) $\exists x (\neg Px \leftrightarrow (Qx \land \neg Rx))$
(a) Domain: $\{1,2,3,\ldots\}$ Extensions: $P: \{2,4,6,\ldots\}$ $Q: \{1,3,5,\ldots\}$ $R: \{2,4,6,\ldots\}$ [A p.167]
(b) Domain: $\{1,2,3,\ldots\}$ Extensions: $P: \{2,4,6,\ldots\}$ $Q: \{2,4,6,\ldots\}$ $R: \{1,3,5,\ldots\}$ [A p.167]
(iii) $\exists x Px \land Ra$
(a) Domain: {1,2,3,}  Referent of <i>a</i> : 7  Extensions: <i>P</i> : {2,3,5,7,11,}  (b) Domain: {Alice, Ben, Carol, Daye}  ASSIGNMENT Arcroject Exam Help  Extensions: <i>P</i> : {Alice, Ben} <i>R</i> : {Carol, Dave}  [Ap.167]
3. Here is a model: https://powcoder.com Domain: {Bill, Ben, Alison, Rachel} Referents: a: Alison r: Rachel Extensions: MyBill Ben} F: {Alison, Rachel} J: {Bill, Alison} S: {Ben, Rackel}

State whether each of the following propositions is true or false in this model.

(i) $(Ma \wedge Fr) \rightarrow \exists x (Mx \wedge Fx)$	[A p.167]
(ii) $\forall x \forall y (Mx \rightarrow My)$	[A p.167]
(iii) $(\neg Ma \lor \neg Jr) \to \exists x \exists y (Mx \land Fy)$	[A p.167]
(iv) $\forall x Mx \rightarrow \forall x Jx$	[A p.167]
(v) $\exists x \exists y (Mx \land Fy \land Sr)$	[A p.167]
(vi) $\exists x (Fx \land Sx) \rightarrow \forall x (Fx \rightarrow Sx)$	[A p.167]

<sup>&</sup>lt;sup>5</sup>That is, the set of prime numbers.

4. For each of the following propositions, describe (a) a model in which it is true, and (b) a model in which it is false. If there is no model of one of these types, explain why.

(i)	$\forall x (Fx \to Gx)$	[A p.167]
(ii)	$\forall xFx \land \neg Fa$	[A p.167]
(iii)	$\exists x Fx \land \neg Fa$	[A p.168]
(iv)	$\exists x (Fx \wedge Gx)$	[A p.168]
(v)	$\forall x (Fx \to Fx)$	[A p.168]
(vi)	$\exists x Fx \land \exists x Gx$	[A p.168]
(vii)	$\forall xFx \to \exists xFx$	[A p.168]
(viii)	$\exists x (Fx \land \neg Fx)$	[A p.168]
	$\exists x Fx \land \exists x \neg Fx$	[A p.168]
Ass	signment Project Exam H	<b>CA</b> [ <b>D</b> 169]
(xi)	$\exists x F x \to \exists x G x$	[A p.169]
(xii)	https://powcoder.com	[A p.169]
(xiii)	$\forall x \in A = A = A = A = A = A = A = A = A = A$	[A p.169]
` ,	$\forall x (Fx \to Fa)$	[A p.169]
(xv)	FaAdd WeChat powcoder	[A p.169]
	$\forall x (Fx \vee Gx)$	[A p.170]
(xvii)	$\exists x (Fx \vee Gx)$	[A p.170]
(xviii)	$\forall x(Fx \land \neg Fx)$	[A p.170]
(xix)	$\forall x \exists y (Fx \to Gy)$	[A p.170]
(xx)	$\forall x (Fx \to \exists y Gy)$	[A p.170]
5. (i)	Is $\forall x(Fx \to Gx)$ true or false in a model in which the of <i>F</i> is the empty set?	e extension [A p.170]
(ii)	Is $\exists x (Fx \land Gx)$ true in every model in which $\forall x (Fx)$ true?	$x \to Gx$ ) is [A p.170]
		[Contents]

#### Exercises 9.5.1

For each of the following arguments, either produce a countermodel (thereby showing that the argument is invalid) or explain why there cannot be a countermodel (in which case the argument is valid).

1.  $\exists xFx \land \exists xGx$   $\therefore \exists x(Fx \land Gx)$  [A p.171] 2.  $\exists x(Fx \land Gx)$   $\therefore \exists xFx \land \exists xGx$  [A p.171] 3.  $\forall x(Fx \lor Gx)$   $\neg \forall xFx$   $\therefore \forall xGx$  [A p.171] 4.  $\forall x(Fx \rightarrow Gx)$   $\Rightarrow x(Fx \rightarrow Hx)$  [A p.171] 5.  $\forall x(Fx \rightarrow Hx)$  [A p.171] 5.  $\forall x(Fx \rightarrow Hx)$  [A p.171] 5.  $\forall x(Fx \rightarrow Hx)$  [A p.171]

Add WeChat powcoder [Contents]

### **Trees for Monadic Predicate Logic**

#### **Exercises 10.2.2**

1. Using trees, determine whether the following propositions are log-Action for the proposition of the state of the state

(i)	$\frac{F_{xFx}}{\exists xFx} = \frac{F_{x}F_{x}}{\forall x \neg F_{x}} = \frac{F_{x}F_{x}}{\forall x \neg F_{x}}$	[A p.172]
(ii)	$\exists x F x \to \neg \forall x \neg F x$	[A p.172]
(iii)	$\forall x((Fx \land \neg Gx) \to \exists xGx)$	[A p.173]
(iv)	$\forall x ((Fx \land \neg Gx) \rightarrow \exists xGx) \\ \forall x Add x F We Chat powcoder$	[A p.173]
(v)	$(Fa \wedge (Fb \wedge Fc)) \to \forall xFx$	[A p.173]
(vi)	$\exists x Fx \land \exists x \neg Fx$	[A p.174]
(vii)	$\exists x (Fx \to \forall y Fy)$	[A p.174]
(viii)	$\forall x (Fx \to Gx) \to (Fa \to Ga)$	[A p.174]
(ix)	$\neg \forall x (Fx \land Gx) \leftrightarrow \exists x \neg (Fx \land Gx)$	[A p.175]
(x)	$\neg \exists x (Fx \land Gx) \leftrightarrow \forall x (\neg Fx \land \neg Gx)$	[A p.175]

2. Using trees, determine whether the following arguments are valid. For any argument that is not valid, read off from your tree a model in which the premises are true and the conclusion false.

(i) 
$$\exists x Fx \land \exists x Gx$$
  
 $\therefore \exists x (Fx \land Gx)$  [A p.176]  
(ii)  $\exists x \forall y (Fx \rightarrow Gy)$   
 $\therefore \forall y \exists x (Fx \rightarrow Gy)$  [A p.176]

(iii) 
$$Fa \rightarrow \forall xGx$$
  
 $\therefore \forall x(Fa \rightarrow Gx)$  [A p.177]  
(iv)  $Fa \rightarrow \forall xGx$   
 $\therefore \exists x(Fa \rightarrow Gx)$  [A p.177]  
(v)  $\forall x(Fx \lor Gx)$   
 $\neg \forall xFx$   
 $\therefore \forall xGx$  [A p.177]  
(vi)  $\exists x(Fx \land Gx)$   
 $\therefore \exists xFx \land \exists xGx$  [A p.178]  
(vii)  $\forall x(Fx \rightarrow Gx)$   
 $Fa$   
 $\therefore Ga$  [A p.178]  
(viii)  $\neg \forall x(Fx \lor Gx)$   
 $\therefore \exists x(\neg Fx \land \neg Gx)$   
 $A(SSignment Project Exam Help)$   
 $\forall x(Gx \rightarrow Hx)$   
 $\therefore \neg \exists x(\neg Fx \land Hx)$  [A p.179]  
(x)  $\forall x(Fx \lor Gx)$   
 $\therefore \neg \exists x(Fx \land Gx)$  [A p.179]  
(x)  $\forall x(Fx \lor Gx)$  [A p.179]  
(x)  $\forall x(Fx \lor Gx)$  [A p.179]

## Add WeChat powcoder

#### Exercises 10.3.8

Translate the following arguments into MPL, and then test for validity using trees. For any argument that is not valid, read off from your tree a model in which the premise(s) are true and the conclusion false.

- 1. All dogs are mammals. All mammals are animals. Therefore, all dogs are animals. [A p.180]
- 2. If everything is frozen, then everything is cold. So everything frozen is cold. [A p.181]
- 3. If a thing is conscious, then either there is a divine being, or that thing has a sonic screwdriver. Nothing has a sonic screwdriver. Thus, not everything is conscious. [A p.182]
- 4. All cows are scientists, no scientist can fly, so no cow can fly.

[A p.183]

- 5. Someone here is not smoking. Therefore, not everyone here is smoking. [A p.184]
- 6. If Superman rocks up, all cowards will shake. Catwoman is not a coward. So Catwoman will not shake. [A p.185]
- 7. Each car is either red or blue. All the red cars are defective, but some of the blue cars aren't. Thus, there are some defective cars and some nondefective cars.

  [A p.186]
- 8. For each thing, it swims only if there is a fish. Therefore, some things don't swim. [A p.187]
- 9. All robots built before 1970 run on kerosene. Autovac 23E was built before 1970, but it doesn't run on kerosene. So it's not a robot.

[A p.188]

10 Eggyore pin seath is electron at the electron of them is tall. Graham is a person. Therefore, if he's an athlete, then either he's not an intellectual, or he isn't tall. //powcoder.com

[A p.189]

[Contents]

### Add WeChat powcoder

# Models, Propositions, and Ways the World Could Be

There are no exercises for chapter 11. Assignment Project Exam Help

https://powcoder.com

Add WeChat powcoder

# **General Predicate Logic**

#### **Exercises 12.1.3.1**

State whether each of the following is a wff of EPL. ASSIGNMENT Project Exam H	elp [Ap.191]
2. $\forall x \exists y F^1 y$	[A p.191]
$\lim_{3. \ \forall x \in \mathbb{R}^2} h^y \text{ttps://powcoder.com}$	[A p.191]
$_{5.\ R^{2}x}^{4.\ \forall x\exists xR^{2}yy}$ Add WeChat powcoder	[A p.191]
5. R <sup>2</sup> x Add WeChat powcodel	[A p.191]
6. $\forall x R^2 x$	[A p.191]
7. $\forall x (F^1 x \to R^2 x)$	[A p.191]
8. $\forall x \exists y (F^1 x \to R^2 x y)$	[A p.191]
9. $\forall x \exists y (F^1 x y \to R^2 y)$	[A p.191]
10. $\forall x \exists y \forall x \exists y R^2 x y$	[A p.191]
	[Contents]

#### Exercises 12.1.6

Translate the following into GPL.

1. Bill heard Alice.	[A p.192]
2. Bill did not hear Alice.	[A p.192]
3. Bill heard Alice, but Alice did not hear Bill.	[A p.192]
4. If Bill heard Alice, then Alice heard Bill.	[A p.192]
5. Bill heard Alice if and only if Alice heard Alice.	[A p.192]
6. Bill heard Alice, or Alice heard Bill.	[A p.192]
7. Clare is taller than Dave, but she's not taller than Edward	d. [A p.192]
8. Mary prefers Alice to Clare.	[A p.192]
Assignmentav Project de xamer L	eto Dave.
<b>3</b>	[A p.192]
10. Edwartlig taller than Clare, but he's dot tall com	[A p.192]
11. The Eiffel tower is taller than both Clare and Dave.	[A p.192]
12. If Dave is tallen than the Eiffel tower, then he's tall. Add WeChat powcoder	
Add Weenat poweoder	[A p.192]
13. Although the Eiffel tower is taller, Clare prefers Dave.	[A p.193]
14. If Alice is taller than Dave, then he prefers himself to her	. [A p.193]
15. Dave prefers Edward to Clare only if Edward is taller that tower.	n the Eiffel [A p.193]
16. Dave prefers Edward to Clare only if she's not tall.	[A p.193]
17. Mary has read <i>Fiesta</i> , and she likes it.	[A p.193]
18. Dave doesn't like <i>Fiesta</i> , but he hasn't read it.	[A p.193]
19. If Dave doesn't like <i>The Bell Jar</i> , then he hasn't read it.	[A p.193]
20. Dave prefers <i>The Bell Jar</i> to <i>Fiesta</i> , even though he hasn't	read either.
	[A p.193]
	[Contents]

### Exercises 12.1.9

Translate the following into GPL.

1. (i)	Something is bigger than everything.	[A p.193]	
(ii)	Something is such that everything is bigger than it.	[A p.193]	
(iii)	If Alice is bigger than Bill, then something is bigger than	nan Bill.	
		[A p.193]	
(iv)	If everything is bigger than Bill, then Alice is bigger than	nan Bill.	
		[A p.193]	
(v)	If something is bigger than everything, then something than itself.	g is bigger [A p.193]	
	If Alice is bigger than Bill and Bill is bigger than A everything is bigger than itself.	[A p.193]	
ASS	citemments Rarsige that wannth	fice is big-	
	ger than.	[A p.193]	
(viii)		_	
(i.e)	Antipset powcoder.com	[A p.193]	
` '	Every room contains at least one chair.	[A p.193]	
(x) In some rooms some of the chairs are broken; in some rooms all of the chairs are broken.			
	r a company of constant	[A p.194]	
2. (i)	Every person owns a dog.	[A p.194]	
(ii)	For every dog, there is a person who owns that dog.	[A p.194]	
(iii)	There is a beagle that owns a chihuahua.	[A p.194]	
(iv)	No beagle owns itself.	[A p.194]	
(v)	No chihuahua is bigger than any beagle.	[A p.194]	
(vi)	Some chihuahuas are bigger than some beagles.	[A p.194]	
(vii)	Some dogs are happier than any person.	[A p.194]	
(viii)	People who own dogs are happier than those who do	n't.	
		[A p.194]	
(ix)	The bigger the dog, the happier it is.	[A p.194]	
(x)	There is a beagle that is bigger than every chihuahua a than every person.	nd smaller [A p.194]	

3. (i) Alice is a timid dog, and some cats are bigger than her.		
	[A p.195]	
(ii) Every dog that is bigger than Alice is bigger than Bill	. [A p.195]	
(iii) Bill is a timid cat, and every dog is bigger than him.	[A p.195]	
(iv) Every timid dog growls at some gray cat.	[A p.195]	
(v) Every dog growls at every timid cat.	[A p.195]	
(vi) Some timid dog growls at every gray cat.	[A p.195]	
(vii) No timid dog growls at any gray cat.	[A p.195]	
(viii) Alice wants to buy something from Woolworths, but I	Bill doesn't.	
	[A p.195]	
(ix) Alice wants to buy something from Woolworths that I	Bill doesn't.	
	[A p.195]	
Assiigenthemyth Pathotice tvalus x bunfron I	columnths.	
$\mathcal{L}$	[A-p.195]	
4. (i) Dave admires everyone. (ii) No one parires pace. Wcoder.com	[A p.196]	
(ii) No one admires pave. W COUEL. COIII	[A p.196]	
(iii) Dave doesn't admire himself.	[A p.196]	
(iv) No Anelodmi Whinselfiat powcoder	[A p.196]	
(v) Dave admires anyone who doesn't admire himself. <sup>7</sup>	[A p.196]	
(vi) Every self-admiring person admires Dave.	[A p.196]	
(vii) Frank admires Elvis but he prefers the Rolling Stones	. [A p.196]	
(viii) Frank prefers any song recorded by the Rolling Stor	nes to any	
song recorded by Elvis.	[A p.196]	
(ix) The Rolling Stones recorded a top-twenty song, but El		
	[A p.196]	
(x) Elvis prefers any top-twenty song that the Rolling Stor		
to any song that he himself recorded.	[A p.196] [Contents]	
6Read "himself" here as gender-neutral—that is, the claim is that no one s	•	

<sup>&</sup>lt;sup>6</sup>Read "himself" here as gender-neutral—that is, the claim is that no one self-admires. <sup>7</sup>Read "himself" here as gender-neutral—that is, the claim is that Dave admires anyone who doesn't self-admire.

#### **Exercises 12.2.2**

1. Here is a model:

Domain:		$\{1,2,3,\ldots\}$
Referents:		a: 1 b: 2 c: 3
<b>Extensions:</b>	E:	$\{2,4,6,\ldots\}$
	P:	$\{2,3,5,7,11,\ldots\}^8$
	L:	$\{\langle 1,2\rangle,\langle 1,3\rangle,\langle 1,4\rangle,\ldots,\langle 2,3\rangle,\langle 2,4\rangle,\ldots,\langle 3,4\rangle,\ldots\}^9$
State whether	r 020	h of the following propositions is true or false in

State whether each of the following propositions is true or false in this model.

(i) Lba	[A p.196]
(ii) Lab∨ Lba	[A p.196]
(iii) Laa	[A p.196]
Assignment Project Exam H	eA p.196]
(vi) $\exists x L x x$	[A p.197]
(vii) \https://powcoder.com	[A p.197]
(viii) $\forall x \exists y L y x$	[A p.197]
(ix) $\exists x (Px \wedge Lxb)$	[A p.197]
(ix) $\exists x Px \land Lxb$ WeChat powcoder	[A p.197]
(xi) $\forall x \exists y (Ey \land Lxy)$	[A p.197]
(xii) $\forall x \exists y (Py \land Lxy)$	[A p.197]
(xiii) $\forall x(Lcx \rightarrow Ex)$	[A p.197]
(xiv) $\forall x((Lax \wedge Lxc) \rightarrow Ex)$	[A p.197]
$(xv) \ \forall x \forall y (Lxy \lor Lyx)$	[A p.197]
(xvi) $\exists x \exists y \exists z (Ex \land Py \land Ez \land Pz \land Lxy \land Lyz)$	[A p.197]
(xvii) $\exists x \exists y \exists z (Lxy \land Lyz \land Lzx)$	[A p.197]
(xviii) $\forall x \forall y \forall z ((Lxy \land Lyz) \rightarrow Lxz)$	[A p.197]
8That is, the set of prime numbers.  9That is, the set of all pairs /x 1/2 such that x is less than 1/2 A more com-	mast way of

<sup>&</sup>lt;sup>9</sup>That is, the set of all pairs  $\langle x, y \rangle$  such that x is less than y. A more compact way of writing this set is  $\{\langle x, y \rangle : x < y\}$ . See §16.1 for an explanation of this kind of notation for sets.

2. Here is a model:

Domain:  $\{1, 2, 3\}$ 

Referents: *a*: 1 *b*: 2 *c*: 3

Extensions: F:  $\{1,2\}$ 

(i)  $\forall x \forall y (Rxy \rightarrow Ryx)$ 

 $G: \{2,3\}$ 

 $R: \{\langle 1,2\rangle,\langle 2,1\rangle,\langle 2,3\rangle\}$ 

 $S: \{\langle 1,2,3\rangle \}$ 

State whether each of the following propositions is true or false in this model.

$(1) \forall x \forall y (\mathbf{K} x y \to \mathbf{K} y x)$	[K p.177]
(ii) $\forall x \forall y (Ryx \rightarrow Rxy)$	[A p.197]
$(:::) \ \forall u \exists u (Cu \land Duu)$	[4 - 107]

[A n 197]

(iii)  $\forall x \exists y (Gy \land Rxy)$  [A p.197]

(iv)  $\forall x(Fx \to \exists y(Gy \land Rxy))$  [A p.197]

### Assignment Project Exam Help<sup>197</sup>

(vi)  $\exists x \exists y Sxay$  [A  $\uparrow$ .197]

(vii) 
$$\exists x \exists y S x b y$$
 [A p.197]

(ix) 
$$\exists x \exists y (Fx \land Fy \land Sxby)$$
 [A p.197]

3. Here is a model:

Domain: {Alice, Bob, Carol, Dave, Edwina, Frank}

Referents: *a*:Alice *b*: Bob *c*: Carol *d*: Dave *e*: Edwina

*f*: Frank

Extensions: *M*: {Bob, Dave, Frank}

F: {Alice, Carol, Edwina}

L: {\langle Alice, Carol\rangle, \langle Alice, Dave\rangle, \langle Alice, Alice\rangle, \langle Dave, Carol\rangle, \langle Edwina, Dave\rangle, \langle Frank, Bob\rangle}

S:  $\{\langle Alice, Bob \rangle, \langle Alice, Dave \rangle, \langle Bob, Alice \rangle, \langle Bob, Dave \rangle\}$ 

 $\langle Dave, Bob \rangle, \langle Dave, Alice \rangle \}$ 

State whether each of the following propositions is true or false in this model.

(i) 
$$\forall x \forall y (Lxy \rightarrow Lyx)$$
[A p.197](ii)  $\exists x Lxx$ [A p.198](iii)  $\neg \exists x Sxx$ [A p.198]

(iv)	$\forall x \forall y (Sxy \to Syx)$	[A p.198]
(v)	$\forall x \forall y \forall z ((Sxy \land Syz) \rightarrow Sxz)$	[A p.198]
(vi)	$\forall x (Mx \to \exists y Ly x)$	[A p.198]
(vii)	$\forall x (Fx \to \exists y Ly x)$	[A p.198]
(viii)	$\forall x (Fx \to \exists y Lxy)$	[A p.198]
(ix)	$\exists x \exists y (Lax \wedge Lyb)$	[A p.198]
(x)	$\forall x((Lxd \vee Ldx) \vee Mx)$	[A p.198]

4. For each of the following propositions, describe (a) a model in which it is true and (b) a model in which it is false. If there is no model of one of these types, explain why.

(i)  $\forall x F x x$ [A p.198]  $\underset{\text{(ii)}}{\overset{\text{(ii)}}{\text{Signm}}} \overset{\text{(ii)}}{\overset{\text{(ii)}}{\text{Exp}}} \overset{\text{(ii)}}{\overset{\text{(iii)}}{\text{Exp}}} \overset{\text{(iii)}}{\overset{\text{(iii)}}{\text{Exp}}} \overset{\text{(iii)}}{\overset{\text{(iii)}}{\overset{\text{(iii)}}{\text{Exp}}}} \overset{\text{(iii)}}{\overset{\text{(iii)}}{\text{Exp}}} \overset{\text{(iii)}}{\overset{\text{(iii)}}{\overset{\text{(iii)}}{\text{Exp}}}} \overset{\text{(iii)}}{\overset{\text{(iii)}}{\overset{\text{(iii)}}{\overset{\text{(iii)}}{\text{Exp}}}} \overset{\text{(iii)}}{\overset{\text{$ (iv)  $\exists x \forall y Fxy$ [A p.198] (v) \https://powcoder.com [A p.198] (vi)  $\exists x \exists y Fxy$ [A p.198] (vii)  $\forall x \forall y F x y \ dy dy = Chat powcoder$ [A p.199] [A p.199] (ix)  $\forall x \forall y Fxy \land \neg Faa$ [A p.199] (x)  $\forall x \forall y (Fxy \leftrightarrow Fyx) \land Fab \land \neg Fba$ [A p.199] [Contents]

#### Exercises 12.3.1

1. Using trees, determine whether the following propositions are logical truths. For any proposition that is not a logical truth, read off from your tree a model in which it is false.

(i)	$\forall x(Rxx \to \exists yRxy)$	[A p.200]
(ii)	$\forall x (\exists y Rxy \to \exists z Rzx)$	[A p.200]
(iii)	$\forall x Rax \rightarrow \forall x \exists y Ryx$	[A p.200]
(iv)	$\forall x \exists y \exists z Ryxz \rightarrow \exists x \exists y Rxay$	[A p.201]

(v) $\neg \forall x \exists y Rxy$	[A p.201]
(vi) $\forall x \forall y \forall z ((Rxy \land Ryz) \rightarrow Rxz)$	[A p.202]
(vii) $\exists x \forall y Rxy \rightarrow \forall x \exists y Rxy$	[A p.202]
(viii) $\exists y \forall x Rxy \rightarrow \forall x \exists y Rxy$	[A p.203]
(ix) $\exists x \forall y Rxy \rightarrow \exists x \exists y Rxy$	[A p.203]
$(x) \ \forall x \forall y \exists z Rxyz \lor \forall x \forall y \forall z \neg Rxyz$	[A p.204]

2. Using trees, determine whether the following arguments are valid. For any argument that is not valid, read off from your tree a model in which the premises are true and the conclusion false.

(i)  $\forall x \forall y \forall z ((Rxy \land Ryz) \rightarrow Rxz)$ Rab Rba

# Assignment Project Exam Help<sup>204</sup>

 $\exists x F x a$ 

 $\underset{\text{(iii)}}{\text{:-}hteps://powcoder.com}$ [A p.205]

 $\exists xRxx$ [A p.205]

(iv) \forall x \text{Act del-W&Chat powcoder}

 $\therefore \exists x Rax$ [A p.206]

(v)  $\forall x \forall y (\neg Rxy \rightarrow Ryx)$ 

 $\therefore \forall x \exists y R y x$ [A p.206]

(vi)  $\forall x \forall y (Rxy \rightarrow (Fx \land Gy))$ 

 $\therefore \neg \exists x R x x$ [A p.206]

(vii)  $\forall x (Fx \rightarrow (\forall y Rxy \lor \neg \exists y Rxy))$ Fa

 $\neg Rab$ 

∴ ¬Raa [A p.207]

(viii)  $\forall x \forall y (\exists z (Rzx \land Rzy) \rightarrow Rxy)$  $\forall x Rax$ 

> $\therefore \forall x \forall y Rxy$ [A p.207]

(ix)  $\forall x \exists y Rxy$ 

 $\therefore \exists xRxb$ [A p.208]  $(x) \exists x \forall y (Fy \to Rxy) \\ \exists x \forall y \neg Ryx \\ \therefore \exists x \neg Fx$ 

[A p.208]

- 3. Translate the following arguments into GPL and then test for validity using trees. For any argument that is not valid, read off from your tree a model in which the premises are true and the conclusion false.
  - (i) Alice is older than Bill, and Bill is older than Carol, so Alice must be older than Carol. [A p.209]
  - (ii) Alice is older than Bill. Bill is older than Carol. Anything older than something is older than everything that that something is older than. It follows that Alice is older than Carol. [A p.209]
  - (iii) I trust everything you trust. You trust all bankers. Dave is a banker. Thus, I trust Dave. [A p.210]

## A(s) significants Projecter Existing Helps-

- (v) Nancy is a restaurateur. She can afford to feed all and only those retaurateurs who can't afford to feed themselves. So Nancy is very wealthy.

  [A p.212]
- (vi) Everything in Paris is more beautiful than anything in Canberra. The Rifel tower is in Paris, and Lake Burley Griffin is in Canberra. Therefore, the Eiffel tower is more beautiful than Lake Burley Griffin.

  [A p.213]
- (vii) Politicians only talk to politicians. No journalist is a politician. So no politician talks to any journalist. [A p.214]
- (viii) There is no object that is smaller than all objects; therefore, there is no object such that every object is smaller than it. [A p.215]
  - (ix) Either a movie isn't commercially successful or both Margaret and David like it. There aren't any French movies that Margaret and David both like. So there aren't any commercially successful French movies.

    [A p.216]
  - (x) There's something that causes everything. Thus, there's nothing that is caused by everything. [A p.217]

[Contents]

#### Exercises 12.4.1

For each of the following arguments, first translate into GPL and show that the argument is invalid using a tree. Then formulate suitable postulates and show, using a tree, that the argument with these postulates added as extra premises is valid.

- 1. Roger will eat any food; therefore, Roger will eat that egg. [A p.217]
- 2. Bill weighs 180 pounds. Ben weighs 170 pounds. So Bill is heavier than Ben. [A p.218]
- 3. John ran 5 miles; Nancy ran 10 miles; hence, Nancy ran farther than John. [A p.218]
- 4. Sophie enjoys every novel by Thomas Mann, so she enjoys *Budden-brooks*. [A p.219]
- Assignment Project Exam Help
  5. Chris cooys novels and nothing else; therefore, he does not enjoy anything by Borges.

  [A p.219]

https://powcoder.com [Contents]

# Exercises 12,5,4 WeChat powcoder

For each of the following wffs, find an equivalent wff in prenex normal form.

1. $(\forall x Px \lor \forall x Qx)$	[A p.220]
$2. \ (\exists x Px \lor \exists x Qx)$	[A p.220]
$3. \ (\forall x Px \to \forall x Px)$	[A p.220]
$4. \ (\forall x Px \leftrightarrow \forall x Px)$	[A p.220]
$5. \ \neg \forall x (Sx \land (\exists y Ty \rightarrow \exists z Uxz))$	[A p.220]
	[Contents]

# **Identity**

### Exercises 13.2.2

Tran 1.	Assignment Project Exam Hongies Chris is larger than everything (except himself).	elp [A p.221]
<ul><li>2.</li><li>3.</li></ul>	All dogs are beagles / except Chris, who is a chihuahua.  **DOG COME	[A p.221] e.
4.	Chris is happy if he is by anyone's she but Jonathan's.	[A p.221]
5.	Jonathan is larger than any dog.	[A p.222]
6.	Everything that Mary wants is owned by someone else.	[A p.222]
7.	Mary owns something that someone else wants.	[A p.222]
8.	Mary owns something she doesn't want.	[A p.222]
9.	If Mary owns a beagle, then no one else does.	[A p.222]
10.	No one other than Mary owns anything that Mary wants.	[A p.222]
11.	Everyone prefers Seinfeld to Family Guy.	[A p.222]
12.	Seinfeld is Adam's most preferred television show.	[A p.222]
13.	Family Guy is Adam's least preferred television show.	[A p.222]

14.	Jonathon watches <i>Family Guy</i> , but he doesn't watch any of sion shows.	ther televi- [A p.222]
15.	Jonathon is the only person who watches Family Guy.	[A p.222]
16.	Diane is the tallest woman.	[A p.222]
17.	Edward is the only man who is taller than Diane.	[A p.222]
18.	Diane isn't the only woman Edward is taller than.	[A p.222]
19.	No one whom Diane's taller than is taller than Edward.	[A p.222]
20.	Edward and Diane aren't the only people.	[A p.222]
21.	You're the only one who knows Ben.	[A p.222]
	I know people other than Ben.	[A p.222]
23.	essignment Project Exam H	<b>e</b> lp
		[A p.222]
24.	The on https://pre/soptiwe oder.com	[A p.222]
25.	Ben is the tallest happy person I know.	[A p.222]
26.	Jindaby Acid the compative postive and telepost	urne.
	ridd Weenat poweoder	[A p.222]
27.	There's a colder town than Canberra between Sydney and	Melbourne.
		[A p.222]
28.	For every town except Jindabyne, there is a colder town.	[A p.222]
29.	No town between Sydney and Melbourne is larger than C colder than Jindabyne.	anberra or [A p.222]
30.	Jindabyne is my most preferred town between Sydney and	Melbourne.
		[A p.223]
		[Contents]

### Exercises 13.3.1

1. Here is a model:

Domain: {Clark, Bruce, Peter}

Referents: a: Clark b: Clark e: Peter f: Peter

Extensions: *F*: {Bruce, Peter}

 $R: \{\langle Clark, Bruce \rangle, \langle Clark, Peter \rangle, \langle Bruce, Bruce \rangle, \}$ 

⟨Peter, Peter⟩}

State whether each of the following propositions is true or false in this model.

(i) 
$$\forall x (\neg Fx \rightarrow x = a)$$
 [A p.223]

(ii) 
$$\forall x(x = a \rightarrow \forall yRxy)$$
 [A p.223]

(iii) 
$$\exists x (x \neq f \land Ff \land Rxf)$$
 [A p.223]

# $A_{(v)}^{(iy)} \stackrel{\forall x(x) \neq b}{\underset{\neq}{\text{in}}} \stackrel{\rightarrow}{\underset{\neq}{\text{project Exam He}}} P_{(v)}^{(iy)} \stackrel{\forall x(x) \neq b}{\underset{\neq}{\text{project Exam He}}} P_{(x)}^{(223)}$

(vi) 
$$\exists x (x \neq e \land Rxx)$$
 [A p.223]

2. Here is a more: //powcoder.com

Domain:  $\{1, 2, 3, ...\}$ 

Referents: Letter in the Reference R

 $G: \{1,3,5,\ldots\}$ 

 $R: \{\langle 1,2\rangle,\langle 2,3\rangle,\langle 3,4\rangle,\langle 4,5\rangle,\ldots\}$ 

State whether each of the following propositions is true or false in this model.

(i) 
$$\exists x (Rax \land \neg Rbx)$$
 [A p.223]

(ii) 
$$\forall x ((Fx \land \neg Gx) \rightarrow x = c)$$
 [A p.223]

(iii) 
$$\forall x (x \neq a \rightarrow \exists y R y x)$$
 [A p.223]

(iv) 
$$\forall x (Gx \to \exists y \exists z (Rxy \land Ryz \land Gz))$$
 [A p.223]

(v) 
$$\forall x ((x = a \lor x = b) \rightarrow x \neq c)$$
 [A p.223]

(vi) 
$$\exists x (\neg Fx \land x \neq e \land \exists y (Fy \land Ryx))$$
 [A p.223]

3. For each of the following propositions, describe (a) a model in which it is true and (b) a model in which it is false. If there is no model of one of these types, explain why.

```
(i) \forall x(Fx \rightarrow x = a)
                                                                                            [A p.223]
     (ii) \exists x(x = a \land x = b)
                                                                                            [A p.223]
    (iii) \exists x \forall y (x \neq y \rightarrow Rxy)
                                                                                            [A p.223]
    (iv) \forall x \forall y (Rxy \rightarrow x = y)
                                                                                            [A p.224]
     (v) \forall x \forall y (x \neq y \rightarrow \exists z R x y z)
                                                                                            [A p.224]
    (vi) \exists x (x = a \land a \neq x)
                                                                                            [A p.224]
   (vii) \forall x \forall y ((Fx \land Fy) \rightarrow x = y)
                                                                                            [A p.224]
  (viii) \exists x (Fx \land \forall y (Gy \rightarrow x = y))
                                                                                            [A p.224]
    (ix) \forall x(Fx \rightarrow \exists y(x \neq y \land Rxy))
                                                                                            [A p.224]
     (x) \forall x ((Fx \land Rax) \rightarrow x \neq a)
                                                                                            [A p.224]
    (xi) \exists x \exists y \exists z (x \neq y \land y \neq z \land x \neq z \land Rxyz)
                                                                                            [A p.224]
   (xii) \forall x \forall y \forall z (Rxyz \rightarrow (x \neq y \land y \neq z \land x \neq z))
                                                                                            [A p.224]
Assignment Project Exam Help225
  (xiv) \exists x (Fx \land \forall y ((Fy \land x \neq y) \rightarrow Rxy))
                                                                                            [A p.225]
  (xv) \forall x \forall x \forall x (Rxyz) / powcoder.com 
(xvi) \forall x (Rxxx) \forall y (x = y \rightarrow Rxy))
                                                                                            [A p.225]
                                                                                            [A p.225]
 (xvii) (Fa \wedge Fb) \wedge \forall x \forall y ((Fx \wedge Fy) \rightarrow x = y)
                                                                                            [A p.225]
 (xviii) 3x40dFWeChatpowooder
                                                                                            [A p.225]
                                                                                          [Contents]
```

### Exercises 13.4.3

1. Using trees, determine whether the following sets of propositions are satisfiable. For any set that is satisfiable, read off from your tree a model in which all propositions in the set are true.

(i) $\{Rab \rightarrow \neg Rba, Rab, a = b\}$	[A p.226]
(ii) $\{Rab, \neg Rbc, a = b\}$	[A p.226]
(iii) $\{ \forall x (Fx \rightarrow x = a), Fa, a \neq b \}$	[A p.227]
(iv) $\{ \forall x (Fx \to Gx), \exists x Fx, \neg Ga, a = b \}$	[A p.227]
(v) $\{ \forall x (x \neq a \rightarrow Rax), \ \forall x \neg Rxb, \ a \neq b \}$	[A p.228]
(vi) $\{\exists x \forall y (Fy \rightarrow x = y), Fa, Fb\}$	[A p.228]

```
(vii) \{ \forall x \forall y (Rxy \rightarrow x = y), Rab, a \neq b \}
                                                                                      [A p.229]
  (viii) \{ \forall x ((Fx \land Rxa) \rightarrow x \neq a), Fb \land Rba, a = b \}
                                                                                      [A p.229]
    (ix) \{\exists x \exists y \exists z Rxyz, \forall x(x = x \rightarrow x = a)\}
                                                                                      [A p.230]
     (x) \{ \forall x \neg Rxx, \ \forall x \forall yx = y, \ \exists x Rax \}
                                                                                      [A p.231]
2. Using trees, determine whether the following arguments are valid.
   For any argument that is not valid, read off from your tree a model
   in which the premises are true and the conclusion false.
     (i) \exists x F x
          ∃yGy
          \forall x \forall yx = y
          \exists x(Fx \land Gx)
                                                                                      [A p.231]
     (ii) \exists x \exists y (Fx \land Gy \land \forall z (z = x \lor z = y))
          \exists x (Fx \land Gx)
                                                                                      [A p.232]
   Assignment Project Exam Help
          \therefore \forall x \forall y \forall z (((Rxy \land Ryz) \land x = z) \rightarrow Ryy)
                                                                                      [A p.233]
    (iv) \forall x \forall y (Rxy \rightarrow Ryx)
          \exists x \text{ interps.} \exists x \text{ interps.} \forall powcoder.com
\therefore \exists x (Rxa \land x \neq b)
                                                                                      [A p.233]
     (v) \forall x \forall yx = y
          AddxWeChat powcoder
                                                                                      [A p.234]
    (vi) \forall x \forall y \forall z ((Rxy \land Rxz) \rightarrow y = z)
          Rab \wedge Rcd
          b \neq d
          \therefore a \neq c
                                                                                      [A p.234]
```

[A p.235]

[A p.235]

[A p.236]

[A p.236]

(vii)  $\exists x \exists y (Rxy \land x = y)$  $\therefore \neg \forall x Rxx$ 

(viii)  $\forall x(x = a \lor x = b)$  $\therefore \forall xx = a$ 

 $\neg \forall x \forall yx = y$ 

 $\therefore \forall xx = b$ 

 $\therefore \exists x \exists y \exists z (Rxy \land Rxz \land y \neq z)$ 

(ix)  $\forall x Rax$ 

(x)  $\forall xx = a$ 

- 3. Translate the following propositions into GPLI and then test whether they are logical truths using trees. For any proposition that is not a logical truth, read off from your tree a model in which it is false.
  - (i) If Stan is the only firefighter, then nothing else is a firefighter.

[A p.237]

- (ii) If Julius Caesar is left-handed but Lewis Carroll isn't, then Lewis Carroll isn't Julius Caesar. [A p.237]
- (iii) If the sun is warming all and only things other than itself, then the sun is warming Apollo. [A p.238]
- (iv) If Kevin Bacon isn't Kevin Bacon, then he's Michael J. Fox.

[A p.238]

(v) If no one who isn't Twain is a witty author, and Clemens is an author, then Clemens is not witty. [A p.239]

## Assignment Project Exam Help<sup>240</sup>

(vii) Either everything is identical to this ant, or nothing is.

[A p.240]

- (viii) If **Augit Strain De Wything out Sinta Outs** then either he's afraid of himself, or else he's Santa Claus. [A p.241]
  - (ix) If Mark respects Samuel and only Samuel, then Mark doesn't respect thins We Chat powcoder [A p.242]
  - (x) Either I am a physical body, or I am identical to something that's not a physical body. [A p.243]

[Contents]

### Exercises 13.5.1

- 1. Translate the following propositions into GPLI and then test whether they are logical truths using trees. For any proposition that is not a logical truth, read off from your tree a model in which it is false.
  - (i) There are at most two gremlins.

[A p.244]

(ii) There are at least three Beatles.

[A p.245]

(iii) There is exactly one thing that is identical to Kevin Bacon.

[A p.246]

(iv) If there are at least two oceans, then there is an ocean. [A p.247]

- (v) Take any two distinct dogs, the first of which is larger than the second; then the second is not larger than the first. [A p.247]
- (vi) If there is exactly one apple, then there is at least one apple.

[A p.248]

- (vii) It's not the case both that there are at least two apples and that there is at most one apple. [A p.248]
- (viii) Either there are no snakes, or there are at least two snakes.

[A p.249]

- 2. Translate the following arguments into GPLI and then test for validity using trees. For any argument that is not valid, read off from your tree a model in which the premises are true and the conclusion false.
  - (i) There are at least three things in the room. It follows that there are at least two things in the room. [A p.250]

## A (ii) There are at least two bears in Canalla, so there are I tember two [A D.251]

- (iii) There is at most one barber. So either every barber cuts his own hair, or no barber cuts any barber's hair. [A p.252]
- (iv) There are at most two things. If you pick a first thing and then pick a second thing (which may or may not be a different object from the first thing), then one of them is heavier than the other. So excluting it either the deav of the Whole the thing.

[A p.253]

- (v) Some football players are athletes. Some golfers are athletes. Thus, there are at least two athletes. [A p.254]
- (vi) Everything is a part of itself. So everything has at least two parts. [A p.255]
- (vii) There are at least two things that are identical to the Eiffel tower. Therefore, there is no Eiffel tower. [A p.256]
- (viii) I'm afraid of Jemima and the chief of police. So either Jemima is the chief of police, or I'm afraid of at least two things. [A p.257]

[Contents]

### **Exercises 13.6.1.1**

Translate the following into GPLI, using Russell's approach to definite descriptions.

- 1. Joseph Conrad is the author of *The Shadow Line*. [A p.258]
- 2. The author of *The Shadow Line* authored *Lord Jim*. [A p.258]
- 3. The author of *The Shadow Line* is the author of *Lord Jim*. [A p.258]
- 4. Vance reads everything authored by the author of Lord Jim.

[A p.258]

- 5. Joseph Conrad authored *The Inheritors*, but it's not the case that he is the author of *The Inheritors*. [A p.258]
- 6. The author of *The Shadow Line* is taller than any author of *Lord Jim*.

[A p.258]

7. There is something taller than the author of *The Shadow Line*.

### Assignment Project Exam Help. 258

- 8. The author of *The Shadow Line* is taller than Joseph Conrad, who is taller than the author of *Lord Jim*. [A p.258]
- 9. The fathettps authpo We Good Cre i Ctorthan Joseph Conrad. [A p.258]
- 10. The father of the author of The Shadow Line is talled than the author of The Shadow Line. [A p.258]

[Contents]

### **Exercises 13.6.2.1**

Translate the claims in Exercises 13.6.1.1 into GPLID, using the definite description operator to translate definite descriptions. [A p.259]

[Contents]

### **Exercises 13.6.3.1**

Translate the claims in Exercises 13.6.1.1 into GPLI, treating definite descriptions as names and stating appropriate uniqueness assumptions as postulates. [A p.260]

[Contents]

### Exercises 13.7.4

1. Translate the following into GPLIF.

(i)	2 + 2 = 4	[A p.261]
(ii)	2  imes 2 = 4	[A p.261]
(iii)	$2+2=2\times 2$	[A p.261]
Ass	signment Project Exam H	<b>CA</b> [D261]
(v)	$(x+y)^2 = (x+y)(x+y)$	[A p.261]
(vi)		[A p.262]
(vii)	Whether $x$ is even or odd, $2x$ is even.	[A p.262]
(viii)	Tripling an odd number results in an odd number; t	ripling an
	even pumber coder	[A p.262]
(ix)	5x < 6x	[A p.262]
(x)	If $x < y$ , then $3x < 4y$	[A p.262]

#### 2. Here is a model:

Domain: {Alison, Bruce, Calvin, Delilah}

Referents: a: Alison b: Bruce c: Calvin d: Delilah

Extensions: F: {Alison, Delilah}

*M*: {Bruce, Calvin}

S: {\langle Alison, Bruce \rangle, \langle Alison, Calvin \rangle, \langle Alison, Delilah \rangle, \langle Bruce, Calvin \rangle,

⟨Bruce, Delilah⟩,⟨Calvin, Delilah⟩}

Values of

function symbols: f: { $\langle$ Alison, Bruce $\rangle$ , $\langle$ Bruce, Calvin $\rangle$ ,

 $\langle Calvin, Bruce \rangle, \langle Delilah, Calvin \rangle \}$ 

m: { $\langle Alison, Delilah \rangle$ ,  $\langle Bruce, Alison \rangle$ ,

 $\{\langle Calvin, Delilah \rangle, \langle Delilah, Alison \rangle\}$ 

s: { $\langle$ Alison, Alison, Bruce $\rangle$ ,  $\langle$ Alison, Bruce, Calvin $\rangle$ ,

# Assignment Page 6 dia Exist Help

〈Bruce, Alison, Calvin〉, 〈Bruce, Bruce, Calvin〉,

# https://powecederpeliam

Calvin, Alison, Delilah),

# Add We Calvin, Bruce, Delilah), der

〈Calvin, Delilah, Alison〉, 〈Delilah, Alison, Alison〉,

⟨Delilah, Bruce, Alison⟩, ⟨Delilah, Calvin, Alison⟩,

(Delilah, Delilah, Alison)

State whether each of the following propositions is true or false in this model.

(i) $\forall x M f(x)$	[A p.262]
------------------------	-----------

(ii) 
$$\exists x Mm(x)$$
 [A p.262]

(iii) 
$$s(c,b) = d$$
 [A p.262]

(iv) 
$$s(a, a) = f(c)$$
 [A p.262]

(v) 
$$Ff(b) \rightarrow Mf(b)$$
 [A p.262]

(vi) 
$$\forall x \forall y \exists z \forall w (s(x, y) = w \leftrightarrow w = z)$$
 [A p.262]

(vii) 
$$\exists x \exists y \exists z \exists w (s(x,y) = z \land s(x,y) = w \land z \neq w)$$
 [A p.262]

```
(viii) s(s(b,a),s(d,a)) = s(b,c) [A p.262]

(ix) \exists x \exists y s(x,y) = m(y) [A p.262]

(x) \forall x \exists y s(y,x) = x [A p.262]
```

3. Here is a model:

Domain:  $\{1, 2, 3, ...\}$ Referents:  $a_1: 1 \ a_2: 2 \ a_3: 3 \ ...$ Extensions:  $E: \{2, 4, 6, ...\}$   $O: \{1, 2, 3, ...\}$  $L: \{\langle x, y \rangle : x < y\}$  10

Values of

function symbols: q:  $\{\langle x,y\rangle:y=x^2\}^{11}$  s  $\{\langle x,y,z\rangle:z=x+y\}^{12}$ p  $\{\langle x,y,z\rangle:z=x\times y\}^{13}$ 

State whether each of the following propositions is true or false in Aussignment Project Exam Help

		_
(i)	$s(a_2,a_2)=a_5$	[A p.262]
(ii)	$\frac{p(https://powcoder.com}{s(a_2,a_2)} = \frac{p(a_2,a_2)}{p(a_2,a_2)}$	[A p.262]
(iii)	$s(a_2, a_2) = p(a_2, a_2)$	[A p.262]
(iv)	$q(a_2) = p(a_1, a_2)$	[A p.262]
(v)	$y = p(a_1, a_2)$ $\forall x \in Cxh$ at $x$ , powcoder	[A p.262]
	$\forall x \forall y q(s(x,y)) = s(s(q(x), p(a_2, p(x,y))), q(y))$	[A p.262]
(vii)	$\forall x Ep(a_2, x)$	[A p.262]
(viii)	$\forall x((Ox \to Op(a_3, x)) \land (Ex \to Ep(a_3, x)))$	[A p.262]
(ix)	$\exists x L p(a_5, x) p(a_5, x)$	[A p.262]
(x)	$\forall x \forall y (Lyx \to Lp(a_3, x)p(a_4, y))$	[A p.262]

<sup>&</sup>lt;sup>10</sup>That is,  $\{\langle 1,2\rangle, \langle 1,3\rangle, \langle 2,3\rangle, \langle 1,4\rangle, \langle 2,4\rangle, \langle 3,4\rangle, \langle 1,5\rangle, \langle 2,5\rangle, \langle 3,5\rangle, \langle 4,5\rangle, \ldots\}$ .

<sup>&</sup>lt;sup>11</sup>That is,  $\{\langle 1,1\rangle, \langle 2,4\rangle, \langle 3,9\rangle, \langle 4,16\rangle, \ldots\}$ .

<sup>&</sup>lt;sup>12</sup>That is,  $\{\langle 1,1,2\rangle, \langle 2,1,3\rangle, \langle 2,2,4\rangle, \langle 1,2,3\rangle, \langle 3,1,4\rangle, \langle 3,2,5\rangle, \langle 3,3,6\rangle, \langle 2,3,5\rangle, \langle 1,3,4\rangle, \langle 4,1,5\rangle, \ldots\}$ .

<sup>&</sup>lt;sup>13</sup>That is,  $\{\langle 1,1,1\rangle, \langle 2,1,2\rangle, \langle 2,2,4\rangle, \langle 1,2,2\rangle, \langle 3,1,3\rangle, \langle 3,2,6\rangle, \langle 3,3,9\rangle, \langle 2,3,6\rangle, \langle 1,3,3\rangle, \langle 4,1,4\rangle, \ldots\}$ .

4. For each of the following propositions, describe (a) a model in which it is true and (b) a model in which it is false. If there is no model of one of these types, explain why.

(i)  f(a) = f(b)	[A p.263]
(ii) $f(a) \neq f(b)$	[A p.263]
(iii) $f(a) \neq f(a)$	[A p.263]
(iv) $\forall x \exists y f(x) = y$	[A p.263]
$(v) \exists x \forall y f(x) = y$	[A p.263]
(vi) $\forall x \forall y s(x, y) = s(y, x)$	[A p.263]
(vii) $\forall x \forall y f(s(x,y)) = s(f(x), f(y))$	[A p.263]
(viii) $\exists x \exists y s(x,y) = f(x) \rightarrow \exists x \exists y s(x,y) = f(y)$	[A p.264]
(ix) $\exists x \exists y s(x,y) = f(x) \rightarrow \exists x \exists y f(s(x,y)) = f(x)$	[A p.264]
Assignment Project Exam	HeA [5264]
	[Contents]

# https://powcoder.com

Add WeChat powcoder

## Chapter 14

## Metatheory

### **Exercises 14.1.1.1**

```
What is the complexity of each of the following wffs? Assignment Project Exam Help
[Ap.265]
                    \lim_{x \to \infty} \frac{dx}{dx} = \lim_{x \to \infty} \frac{dx}{dx} 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  [A p.265]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 [A p.265]

\begin{array}{l}
4. \ \forall x \exists y \neg Rxy \\
5. \ \neg \forall xa \neq x
\end{array}

dd WeChat powcoder
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 [A p.265]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 [A p.265]
                      6. \forall x(Fx \rightarrow \exists yRxy)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 [A p.265]
                      7. (\forall xa = x \land \neg \exists xa \neq x)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  [A p.265]
                      8. (Fa \wedge (Fa \wedge (Fa \wedge (Fa \wedge (Fa \wedge Fa)))))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 [A p.265]
                      9. \forall x(Fx \to Fx))))) [A p.265]
              10. (((\neg \exists x (\neg Fx \lor Gx) \land a \neq b) \rightarrow \neg Fa) \lor (\neg \exists x (\neg Fx \lor Gx) \lor \neg Fa))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  [A p.265]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       [Contents]
```

### **Exercises 14.1.2.1**

In  $\S10.1$  we showed that the tree rules for (negated and unnegated) disjunction and the quantifiers are truth-preserving (in the precise sense spelled out in  $\S14.1.2$ ), and in  $\S13.4$  we showed that the tree rule SI is truth-preserving. Complete the soundness proof by showing that the remaining tree rules are truth-preserving:

https://powcoder.com	[Contents]	
7. Negated negation.	[A p.267]	
Assignment Project Exam Help267		
5. Unnegated biconditional.	[A p.266]	
4. Negated conditional.	[A p.266]	
3. Unnegated conditional.	[A p.266]	
2. Negated conjunction.	[A p.266]	
1. Unnegated conjunction.	[A p.265]	

# Exercises A4113 We Chat powcoder

Fill in the remaining cases in step (III) of the completeness proof.

- 1.  $\gamma$  is of the form  $\neg \alpha$ , and  $\alpha$ 's main operator is conjunction. [A p.267]
- 2.  $\gamma$  is of the form  $\neg \alpha$ , and  $\alpha$ 's main operator is the conditional.

[A p.267]

3.  $\gamma$  is of the form  $\neg \alpha$ , and  $\alpha$ 's main operator is the biconditional.

[A p.268]

4.  $\gamma$  is of the form  $\neg \alpha$ , and  $\alpha$ 's main operator is the existential quantifier.

[A p.268]

5.  $\gamma$ 's main operator is the biconditional. [A p.268]

[Contents]

## Chapter 15

### Other Methods of Proof

### Exercises 15.1.5

Assignment Project Exam Help [Ap.269]		
(iii) P - ¬Q -> P / powcoder.com	[A p.269]	
	[A p.269]	
$(\mathrm{iv})  \vdash P \to P$	[A p.269]	
(vi) ¬(A)dd WeChat powcoder	[A p.270]	
(vi) P, ¬P + Q	[A p.270]	
(vii) $P \land Q \vdash (P \rightarrow \neg Q) \rightarrow \neg (P \rightarrow \neg Q)$	[A p.270]	

2. Show the following in  $A_1$  by producing formal or informal proofs.

$$\begin{array}{ll} \text{(i)} \vdash \neg (P \rightarrow \neg Q) \rightarrow Q & \text{[A p.270]} \\ \text{(ii)} \vdash P \rightarrow (P \lor Q) & \text{[A p.270]} \\ \text{(iii)} \vdash ((P \rightarrow Q) \rightarrow (P \rightarrow R)) \rightarrow (P \rightarrow (Q \rightarrow R)) & \text{[A p.271]} \\ \text{(iv)} \vdash (P \rightarrow Q) \rightarrow (\neg Q \rightarrow \neg P) & \text{[A p.271]} \\ \text{(v)} P \rightarrow Q, P \rightarrow \neg Q \vdash \neg P & \text{[A p.271]} \\ \text{(vi)} P \rightarrow Q, \neg Q \rightarrow P \vdash Q & \text{[A p.272]} \\ \text{(vii)} \vdash (P \rightarrow (Q \rightarrow R)) \rightarrow (Q \rightarrow (P \rightarrow R)) & \text{[A p.272]} \\ \end{array}$$

3. Show the following in  $A_2$  by producing formal or informal proofs.

(i) 
$$\vdash P \rightarrow \neg \neg P$$
 [A p.272]

(ii) $P \rightarrow \neg P \vdash \neg P$	[A p.273]
(iii) $P \to Q \vdash \neg Q \to \neg P$	[A p.273]
(iv) $\vdash \neg Q \rightarrow (Q \rightarrow P)$	[A p.273]
(v) $P \wedge Q \vdash P \rightarrow Q$	[A p.273]
(vi) $\neg Q \vdash (P \lor Q) \to P$	[A p.274]
(vii) $\neg P \land \neg Q \vdash \neg (P \lor Q)$	[A p.274]
(viii) $\neg (P \lor Q) \vdash \neg P \land \neg Q$	[A p.275]
$(ix) \vdash \neg (P \land \neg P)$	[A p.275]
$(x) \vdash (P \land \neg P) \to Q$	[A p.276]
(xi) $\vdash P \leftrightarrow P$	[A p.276]
(xii) $\vdash P \to (\neg P \to Q)$	[A p.277]

# 4AShow the following in Ap by producing formal or informal proofs. ASSIGNMENT Project Exam Help

(i)	$\forall x(Fx \to Gx), Fa \vdash Ga$	[A p.277]
(ii)	Thirtings: / RyP, Rab Coder.com	[A p.277]
(iii)	VXVy(RLyS, RyP), Raby Rod GET. COTTI	[A p.277]
(iv)	$\exists x Fx \to \neg Ga \vdash Ga \to \forall x \neg Fx$	[A p.278]
(v)	+AddrWeChat powcoder	[A p.279]
(vi)	$Fa, a = b \vdash Fb$	[A p.280]
(vii)	$\forall x \forall y x = y \vdash a = b$	[A p.280]
(viii)	$a = b$ , $a = c \vdash c = b$	[A p.280]
(ix)	$\vdash a = b \rightarrow b = a$	[A p.281]
(x)	$Fa$ , $\neg Fb \vdash \neg a = b$	[A p.281]
(xi)	$\neg b = a, \forall x (\neg Fx \to x = a) \vdash Fb$	[A p.283]
(xii)	$\vdash \forall x F x \to \forall y F y$	[A p.283]

5. Explain why the original unrestricted deduction theorem does not hold in  $A_1^{\forall=}$  and why the restricted version stated at the end of §15.1.1.1 does hold. [A p.283]

[Contents]

### Exercises 15.2.3

1. Show the following in  $N_1$ .

[A p.284]		
[A p.284]		
[A p.284]		
[A p.285]		
[A p.285]		
[A p.285]		
[A p.286]		
[A p.286]		
[A p.287]		
elp <sup>287</sup> ]		
2. Establish each of the following in each of the systems $N_2$ through $N_5$ .		
[A p.288]		
[A p.289]		
[A p.289]		

3. Show the following in  $N_1^{\forall \exists =}$ .

(i)	$\vdash \forall x (Fx \to Fx)$	[A p.291]
(ii)	$\exists x (Fx \land Gx) \vdash \exists x Fx \land \exists x Gx$	[A p.291]
(iii)	$\forall x (Fx \to Gx), \neg \exists x Gx \vdash \neg \exists x Fx$	[A p.292]
(iv)	$\forall x (Fx \to x = a) \vdash Fb \to a = b$	[A p.292]
(v)	$\forall x \forall yx = y, Raa \vdash \forall x \forall y Rxy$	[A p.293]
(vi)	$\vdash \forall x R x x \to \forall x \exists y R x y$	[A p.293]
(vii)	$\vdash \exists x Fx \to \neg \forall x \neg Fx$	[A p.294]
(viii)	$\neg \exists x Fx \vdash \forall x \neg Fx$	[A p.294]
(ix)	$\forall xx = a \vdash b = c$	[A p.294]
(x)	$\vdash \forall x \forall y ((Fx \land \neg Fy) \to \neg x = y)$	[A p.295]

(i) Reformulate the rules of system  $N_1$  in list style. Re-present your answers to Question 1 above as proofs in the list style.

[A p.295]

(ii) Reformulate the rules of system  $N_1$  in stack style. Re-present your answers to Question 1 above as proofs in the stack style.

[A p.299]

5. State natural deduction rules (i.e., introduction and elimination rules) for  $\leftrightarrow$ . [A p.302]

[Contents]

### Exercises 15.3.3

1. Define the following notions in terms of sequents. ssignment Project Exam Help

(a) a contradiction [A p.303]

(ii) Propositions  $\alpha$  and  $\beta$  are: [A p.303]

(a) jointly satisfiable (bAquidlerWeChat powcoder [A p.303] [A p.303]

- 2. Redo some of Exercise 7.3.1.1 and Exercise 7.3.2.1 using the sequent [A p.303] calculus  $S_1$  instead of trees.
- 3. Redo some of Exercise 10.2.2, Exercise 12.3.1 and Exercise 13.4.3 using the sequent calculus  $S_1^{\forall \exists =}$  instead of trees. [A p.303]
- 4. State sequent rules (i.e., left and right introduction rules) for  $\leftrightarrow$ .

[A p.303]

5. State a (new) tree rule that is the analogue of Cut. [A p.303]

[Contents]

# Chapter 16 Set Theory

There are no exercises for chapter 16.

[Contents]

Assignment Project Exam Help

https://powcoder.com

Add WeChat powcoder

## Answers Assignment Project Exam Help

https://powcoder.com

Add WeChat powcoder

## **Chapter 1**

# **Propositions and Arguments**

### **Answers 1.2.1**

1 2.	Proposition SS1gnment Project Exam H	$[e]_{\mathbb{Q}_{p,2]}}^{\mathbb{Q}_{p,2]}}$
3.	Non-proposition (Exclamation)	[Q p.2]
4.	https://powcoder.com	[Q p.2]
5.	Proposition (Not a wish: the speaker is making a statement by utwhat he rishes.) powcoder	[Q p.2]
6.	Proposition	[Q p.2]
7.	Proposition	[Q p.2]
8.	Proposition	[Q p.2]
9.	Non-proposition (Wish)	[Q p.2]
10.	Non-proposition (Command)	[Q p.2]
		[Contents]

### **Answers 1.3.1**

1.	If the stock market crashes, thousands of experienced
	investors will lose a lot of money.

The stock market won't crash. [Q p.3]

2.	Diamond is harder than topaz. Topaz is harder than quartz. Quartz is harder than calcite. Calcite is harder than talc.	
	Diamond is harder than talc.	[Q p.3]
3.	Any friend of yours is a friend of mine. You're friends with everyone on the volleyball tea	m.
	If Sally's on the volleyball team, she's a friend of r	nine. [Q p.3]
4.	When a politician engages in shady business dea up on page one of the newspapers No South Australian senator has ever appeared or a newspaper.	G
As	SNESOUTH Australian senative Congression shady out ings.	sinces deal- [Q p.3]
	https://powcoder.com	[Contents]
<b>Ansv</b> 1. Va	vers 1.4.1 Add WeChat powcode	r [Q p.3]
2. In	valid.	[Q p.3]
3. Va	alid.	[Q p.3]
4. Va	alid.	[Q p.4]
		[Contents]
Ansv	vers 1.5.1	
1. A:	rguments 1 and 3.	[Q p.4]
2. A	rgument 2.	[Q p.4]
3. A	rgument 4.	[Q p.4]
		[Contents]

## **Answers 1.6.1.1**

1. (i) Bob is a good student	[Q p.4]
(ii) I have decided not to go to the party.	[Q p.4]
(iii) Mars is the closest planet to the sun.	[Q p.4]
(iv) Alice is late.	[Q p.4]
(v) I like scrambled eggs.	[Q p.4]
(vi) Scrambled eggs are good for you.	[Q p.4]
2. True.	[Q p.4]
3. False.	[Q p.4]
[1	Contents]
AAssignment Project Exam He	elp
1. The sun is shining. I am happy.	[Q p.5]
2. Maisie is my friend. Roste is my friend.	[Q p.5]
3. Sailing is fun. Snowboarding is fun.	[Q p.5]
4. We watched the movie we attempt the work of the watched the movie we attempt the work of the work o	[Q p.5]
5. Sue does not want the red bicycle. Sue does not like the blu	ıe bicycle.
·	[Q p.5]
6. The road to the campsite is long. The road to the campsite i	s uneven.
	[Q p.5]
[	Contents]
Answers 1.6.4.1	
1. (a) That's pistachio ice cream.	
(b) That doesn't taste the way it should.	[Q p.5]
2. (a) That tastes the way it should.	
(b) That isn't pistachio ice cream.	[Q p.5]

- 3. (a) That is supposed to taste that way.
  - (b) That isn't pistachio ice cream. [Q p.5]
- 4. (a) You pressed the red button.
  - (b) Your cup contains coffee. [Q p.5]
- 5. (a) You pressed the green button.
  - (b) Your cup does not contain coffee. [Q p.5]
- 6. (a) Your cup contains hot chocolate.
  - (b) You pressed the green button. [Q p.5]

[Contents]

Answers 1.6.6 Assignment Project Exam Help

- 1. This is a conditional with antecedent 'It will be sunny and windy tomorrow' and consequent 'We shall go sailing or kite flying tomorrow'. The antecedent is a conjunction with conjuncts 'It will be sunny tomorrow' and 'It will be windy tomorrow'. The consequent is a disjunction with disjuncts 'We shall go sailing tomorrow' and 'We shall go kite flying tomorrow'.

  [Q p.6]
- 2. This is a conditional with antecedent It will rain or snow tomorrow' and consequent 'We shall not go sailing or kite flying tomorrow'. The antecedent is a disjunction with disjuncts 'It will rain tomorrow' and 'It will snow tomorrow'. The consequent is a negation with negand 'We shall go sailing or kite flying tomorrow'. The negand, as mentioned in answer to the previous question, is a disjunction with disjuncts 'We shall go sailing tomorrow' and 'We shall go kite flying tomorrow'.

  [Q p.6]
- 3. This is a disjunction with disjuncts 'He'll stay here and we'll come back and collect him later' and 'He'll come with us and we'll all come back together'. The first of these disjuncts is a conjunction with conjuncts 'He'll stay here' and 'We'll come back and collect him later'; the second of the disjuncts is also a conjunction, with conjuncts 'He'll come with us' and 'We'll all come back together'. [Q p.6]
- 4. This is a conjunction with conjuncts 'Jane is a talented painter and a wonderful sculptor' and 'If she remains interested in art, her work

will one day be of the highest quality.' The first of these conjuncts is itself a conjunction, with conjuncts 'Jane is a talented painter' and 'Jane is a wonderful sculptor'; the second conjunct is a conditional, with antecedent 'Jane remains interested in art' and consequent 'Jane's work will one day be of the highest quality'. [Q p.6]

- 5. This is a negation with negand 'The unemployment rate will both increase and decrease in the next quarter'. The negand is a conjunction with conjuncts 'The unemployment rate will increase in the next quarter' and 'The unemployment rate will decrease in the next quarter'.

  [Q p.6]
- 6. This is a conditional with antecedent 'You don't stop swimming during the daytime' and consequent 'Your sunburn will get worse and become painful'. The antecedent is a negation with negand 'You stop swimming during the daytime'; the consequent is a conjunction with Aconjuncts 'Your sunburn vill get worse' and 'Your sunburn vill become painful.
- 7. This is a disjunction with disjuncts 'Steven won't get the job' and 'I'll leave and tallow clients will leave disjunct is a negation with negand 'Steven will get the job'; the second disjunct is a conjunction with conjuncts 'I'll leave' and 'All my clients will leave'. Add WeChat powcoder
- 8. This is a biconditional with components 'The Tigers will not lose' and 'Both Thompson and Thomson will get injured'. The first is a negation with negand 'The Tigers will lose'; the second is a conjunction with conjuncts 'Thompson will get injured' and 'Thomson will get injured'.

  [Q p.6]
- 9. This is a conjunction with conjuncts 'Fido will wag his tail if you give him dinner at 6 this evening' and 'Fido will bark if you do not give him dinner at 6 this evening'. The first of these conjuncts is a conditional with antecedent 'You will give Fido dinner at 6 this evening' and consequent 'Fido will wag his tail [at 6 this evening]'; the second conjunct is a conditional with antecedent 'You do not give Fido dinner at 6 this evening' and consequent 'Fido will bark [at 6 this evening]'. Finally, the antecedent of this last conditional is a negation with negand 'You give Fido dinner at 6 this evening'.

[Q p.6]

10. This is a disjunction with disjuncts 'It will rain or snow today' and 'It will not rain or snow today'. The first of these disjuncts is itself a disjunction, with disjuncts 'It will rain today' and 'It will snow today'. The second of these disjuncts is a negation with negand 'It will rain or snow today'. The latter, as already mentioned, is a disjunction, with disjuncts 'It will rain today' and 'It will snow today'. [Q p.6]

[Contents]

# Assignment Project Exam Help https://powcoder.com

Add WeChat powcoder

## Chapter 2

# The Language of Propositional Logic

Answers 2.3.3 ASSIGnment Project Exam E	<b>l</b> elp
1. Aristotle was not a philosopher.	[Q p.7]
2. Aristotle was a philosopher and paper burns.  3. Aristotle was a philosopher and paper doesn't burn.	[Q p.7]
3. Aristotle was a philosopher and paper doesn't burn.	[Q p.7]
4. Fire is not hot and per does not burn Add Wechat powcoder  5. It's not true both that fire is hot and that paper burns.	[Q p.7]
5. It's not true <i>both</i> that fire is hot <i>and</i> that paper burns.	[Q p.7]
	[Contents]

### Answers 2.3.5

- 1. Either Aristotle was a philosopher and paper burns, or fire is hot.
  - [Q p.8]
- 2. Either Aristotle wasn't a philosopher, or paper doesn't burn. [Q p.8]
- 3. Aristotle was a philosopher or paper burns—but not both. [Q p.8]
- 4. It's not the case either that Aristotle was a philosopher or that fire is hot. [Q p.8]

5. Aristotle was a philosopher, and either paper burns or fire is hot.

[Q p.8]

[Contents]

### **Answers 2.3.8**

- 1. (i) If snow is white, then the sky is blue. [Q p.8]
  - (ii) Snow is white if and only if both snow is white and roses are not red. [Q p.8]
  - (iii) It's not the case that if roses are red then snow is not white.

[Q p.8]

- (iv) If roses are red or snow is white, then roses are red and snow is not white.
- Assignment Project Fxam He of the sky is not blue.
  - (vi) Either grass is green, or if snow is white then roses are red.  $\begin{array}{c} \text{NUPS.}/\text{POWCOGET.COM} \\ \text{[Q p.8]} \end{array}$
  - (vii) Bananas are yellow if and only if they're yellow; and they're not if and only if they're not powcoder [Q p.8] (viii) If, if the sky is blue then snow is white, then if snow isn't white
  - (viii) If, if the sky is blue then snow is white, then it snow isn't white then the sky isn't blue. [Q p.8]
  - (ix) If roses are red, snow is white and the sky is blue, then either bananas are yellow or grass is green. [Q p.8]
  - (x) It's not the case both that roses aren't red and that either snow isn't white or grass is green. [Q p.9]

### 2. Glossary:

- B: The sky is blueE: Snow is redJ: Jim is tallM: Maisy is tallN: Nora is tallR: Roses are redW: Snow is white
- (i)  $(W \rightarrow B)$  [Q p.9] (ii)  $(B \leftrightarrow (W \land \neg R))$  [Q p.9] (iii)  $\neg (R \rightarrow \neg W)$  [Q p.9] Assignment Project Exam Helpp.9] (v)  $((P \leftrightarrow M) \land (M \rightarrow \neg N))$  [Q p.9] (vi)  $(J \rightarrow (N \lor M))$  [Q p.9] (vii)  $(J \rightarrow (N \lor M))$  [Q p.9] (viii)  $((W \land M) \lor (W \land \neg M))$  [Q p.9] (ix)  $((J \land A) \land (W \land B) \rightarrow (J \land B))$  hat powcoder [Q p.9] (x)  $((M \land B) \rightarrow (J \land B))$  hat powcoder

### 3. Glossary:

G: We are skiingK: We are kite flyingL: We are sailingS: It is snowingU: It is sunnyW: It is windy

(i) $(S \rightarrow \neg K)$	[Q p.9]
(ii) $((U \land W) \rightarrow (L \lor K))$	[Q p.9]
(iii) $((K \to W) \land (L \to W))$	[Q p.9]
(iv) $((L \vee K) \vee G)$	[Q p.9]
Assignment Project Exam	$Hel_{p,9]}^{[0,p,9]}$
(vii) $(G \to (W \land S))$	[Q p.9]
(viii) (https://powcoder.com (ix) $(L \rightarrow (U \land W) \land \neg S)$ )	[Q p.9]
(ix) $(L \to ((U \land W) \land \neg S))$	[Q p.9]
$ \begin{array}{c} \text{(x) } (((U \land W) \rightarrow L) \land ((S \land \neg W) \rightarrow G)) \\ \textbf{Add WeChat powcod} \end{array} $	[Q p.10]
Add weChat powcod	[Contents]

### Answers 2.5.1

1. (i)	No	[Q p.10]
(ii)	No	[Q p.10]
(iii)	Yes	[Q p.10]
(iv)	No	[Q p.10]
(v)	No	[Q p.10]
(vi)	No	[Q p.10]
(vii)	No	[Q p.10]
(viii)	No	[Q p.10]
(ix)	No	[Q p.10]
(x)	Yes	[Q p.10]

- (i) (a) 1 is an odd number.
  - (b) If x is an odd number then so is x + 2.
  - (c) Nothing else is an odd number.

Note: We are assuming here that 'number' means 'positive integer'. If it is taken to mean 'integer' (i.e. positive, negative or zero) then the answer is:

- (a) 1 is an odd number.
- (b) If x is an odd number then so are x + 2 and x 2.
- (c) Nothing else is an odd number.

[Q p.10]

- (ii) (a) 5 is divisible by five.
  - (b) If x is divisible by five then so is x + 5.
  - (c) Nothing else is divisible by five.

Note: We are assuming here that 'number' means 'positive integer'. If it is taken to mean 'integer' (i.e. positive, negative or Assignment Project Exam Heip

- (a) 5 is divisible by five.
- (b) If x is divisible by five then so are x + 5 and x 5.
- (ANTIPIRE else is a Willie D. G.E. COM

[Q p.10]

- (iii) (a) *a* is such a word; *b* is such a word.
  - (b) Alf dissurby we cathen so are xa and xh der

(c) Nothing else is such a word.

[Q p.10]

- (iv) (a) Bob's mother is in the set; Bob's father is in the set.
  - (b) If *x* is in the set then so are *x*'s mother and *x*'s father.
  - (c) Nothing else is in the set.

[Q p.10]

- (v) (a) hah hah hah is a cackle.
  - (b) If *x* is a cackle then so is *x* hah.
  - (c) Nothing else is a cackle.

[Q p.10]

[Contents]

### **Answers 2.5.3.1**

```
1. 1. P
                             / (2i)
    2. Q
                             / (2i)
    3. R
                             / (2i)
    4. \neg P
                             1/(2ii\neg)
    5. (Q \wedge R)
                             2, 3 / (2ii \land)
    6. (\neg P \lor (Q \land R)) 4, 5 / (2ii \lor)
                                                                            [Q p.11]
   Main connective is \vee.
2. 1. P
                             / (2i)
    2. Q
                             / (2i)
    3. R
                             / (2i)
    4. (Q \vee R)
                             2, 3 / (2ii \lor)
    5. (P \land (Q \lor R))
                             1, 4 / (2ii \land)
    6. \neg (P \land (Q \lor R)) 5 / (2ii\neg)
Assignment Project Exam Help.11]
3. 1. P
                                 / (2i)
    <sup>2. Q</sup><sub>3. R</sub> https://pogivcoder.com
    4. \neg P
                                 1 / (2ii¬)
    5. ¬O
    6. ¬RA
    7. (\neg P \land \neg Q)
                                 4, 5 / (2ii \land)
    8. ((\neg P \land \neg Q) \lor \neg R) 6, 7 / (2ii\lor)
                                                                            [Q p.11]
   Main connective is \vee.
4. 1. P
                                     / (2i)
    2. Q
                                     / (2i)
    3. R
                                     / (2i)
    4. S
                                     / (2i)
    5. (P \rightarrow Q)
                                     1, 2 / (2ii \rightarrow)
    6. (R \rightarrow S)
                                     3, 4 / (2ii \rightarrow)
    7. ((P \to Q) \lor (R \to S)) 5, 6 / (2ii\lor)
   Main connective is \vee.
                                                                            [Q p.11]
```

5. 1. 
$$P$$
 / (2i)  
2.  $Q$  / (2i)  
3.  $R$  / (2i)  
4.  $S$  / (2i)  
5.  $(P \leftrightarrow Q)$  1, 2 / (2ii $\leftrightarrow$ )  
6.  $((P \leftrightarrow Q) \leftrightarrow R)$  3, 5 / (2ii $\leftrightarrow$ )  
7.  $(((P \leftrightarrow Q) \leftrightarrow R) \leftrightarrow S)$  4, 6 / (2ii $\leftrightarrow$ )

Main connective is  $\leftrightarrow$ . [Q p.11]

6. 1. 
$$P$$
 / (2i)  
2.  $\neg P$  1 / (2ii $\neg$ )  
3.  $\neg \neg P$  2 / (2ii $\neg$ )  
4. ( $\neg P \land \neg \neg P$ ) 2, 3 / (2ii $\land$ )  
5. ( $P \land \neg P$ ) 1, 2 / (2ii $\land$ )  
6. (( $\neg P \land \neg \neg P$ )  $\rightarrow$  ( $P \land \neg P$ )) 4, 5 / (2ii $\rightarrow$ )

# Assignment Project Exam Help. [Contents]

# Answershttps://powcoder.com

1.	ordering	disambiguation	4	[Q p.11]
	2 <b>A</b>	aa weer	nat powcoder	
	3	3	•	
	4	4		
	5	2		
	6	5		

[Contents]

### **Answers 2.5.5.1**

1. (i) 
$$(\neg P \lor (Q \land R))$$
 [Q p.11]  
(ii)  $\neg ((P \lor Q) \land R)$  [Q p.11]  
(iii)  $(\neg (P \lor Q) \land R)$  [Q p.11]  
(iv)  $((\neg P \land \neg Q) \lor \neg R)$  [Q p.11]  
(v)  $([(P \leftrightarrow Q) \leftrightarrow R] \leftrightarrow S)$  [Q p.11]

2. (i) 
$$\neg \land P \lor QR$$
 [Q p.11]  
(ii)  $\rightarrow \rightarrow P \lor QRS$  [Q p.12]  
(iii)  $\lor \rightarrow PQ \rightarrow RS$  [Q p.12]  
(iv)  $\rightarrow P \rightarrow \lor QRS$  [Q p.12]  
(v)  $\rightarrow \land \neg P \neg \neg P \land P \neg P$  [Q p.12]  
[Contents]

# Assignment Project Exam Help

https://powcoder.com

Add WeChat powcoder

## **Chapter 3**

## **Semantics of Propositional Logic**

### **Answers 3.2.1**

```
ignment Project Exam Help Toject Exam Help
   phase 1:
   phase 2:
       https://powcoder.com
                                                 [Q p.13]
   phase 0:
   phase 1:
   phase Add WeChat powcoder
   phase 3:
                                                 [Q p.13]
   phase 0:
   phase 1:
             Τ
   phase 2:
            F
   phase 3:
4.
                                                 [Q p.13]
   phase 0:
   phase 1:
            F
            Τ
                          Τ
   phase 2:
                  Τ
   phase 3:
5.
                                                 [Q p.13]
   phase 0:
   phase 1:
               T
                              F
                       F
   phase 2:
```

```
P))
                                                            [Q p.13]
 6.
                                        Τ
    phase 0:
    phase 1:
                   T
    phase 2:
 7.
                                       S)))
                                                            [Q p.13]
    phase 0:
    phase 1:
    phase 2:
                            F
                   F
    phase 3:
                                                            [Q p.13]
 8.
    phase 0:
                                     T
    phase 1:
    phase 2:
                            T
                   T
    phase 3:
    phase 0:
    phase 1:
    phase 3:ttps://powcoder.com
    phase 3:
    phase 4:
    phase 5
10.
                                                            [Q p.14]
    phase 0:
    phase 1:
                   F
                         F
    phase 2:
                                  F
    phase 3:
    phase 4:
                                           T
    phase 5:
              F
                                                         [Contents]
```

### **Answers 3.3.1**

1.	P	Q	((P	$\wedge$	Q)	V	<i>P</i> )
	T	T		7		T	
	T	F		F		T	
	F	T		F		F	
	F	F		F		F	

```
P))
                                                                   [Q p.14]
2.
                 (P
             \land
                      7
             T
    T
    F
             F
                      F
                                                                   [Q p.14]
        Q
T
                         \neg Q)
            \neg(\neg P
3.
    T
            T F
                     F
                         F
    T
            T ₽
        F
                         7
    F
        T
            T 7
                         F
            F 7
    F
                           ¬Q))

F
                                                                   [Q p.14]
        \overline{(Q)}
              \frac{\rightarrow}{F}
                   (Q
    F
                                     R))
                                                                   [Q p.14]
                         t Project Exam Help
        F
            F
    T
                      7/powcoder.com
    F
    F
        F
            T
    F
    F
        F
            F
                      T
                                         powcoder
        Q^{\prime}
6.
    P
    T
        T
                            T
                                      7
                  7
    T
                  7
                            F
                                      F
        F
                  7
                            F
                                      F
    \mathbf{F}
        \mathbf{T}
                  F
                            T
    F
        F
                                      F
            \neg((P
        Q
T
7.
    P
                        Q)
                                   Q)
                                                                   [Q p.14]
            F
                    7
    T
                              7
                              7
    T
        F
            F
                    F
                              F
        T
            T
                    F
    F
            F
                              7
    F
        F
                    F
                                                                   [Q p.14]
8.
    P
                    \neg P)
                               \neg P)
                                            \neg P)
                F
                    F
                           7
                                       F
    T
                               F
                                           F
```

T

7

7

7

F

7

7

# Answers Add WeChat powcoder

 $Q \mid (P \to Q) \mid (Q \to P)$ 

	T	T	T	T		
	T	F	F	T		
	F	T	T	F		
	F	F	T	T		
2.	P	Q	$\neg (P \leftrightarrow Q)$	$((P \lor Q)$	$\land \neg (P \land Q))$	[Q p.14]
	T	T	F 7	7	F <b>F</b> 7	
	T	F	T	7	T 7 F	
	F	T	T	7	T 7 F	
	F	F	F 7	F	F 77 F	
3.	P	Q	$\neg (P \land \neg$	$\neg Q) \mid \neg Q$		[Q p.14]
	T	T	T	F		
	T	F	F 7/7	$T \mid T$		
	F	T	T F J	F		
	F	F	T ⊮ 7,	T T		
			·	·	_	

[Q p.14]

4.	P	Q	R	(P)	$\rightarrow$	Q)	$\wedge$	R))	(P	V	(Q	V	R))	[Q p.14]
	T	T	T		7		T			T		7		
	T	T	F		7		F			T		7		
	T	F	T		¥		F			T		7		
	T	F	F		¥		F			T		F		
	F	T	T		7		T			T		7		
	F	T	F		7		F			T		7		
	F	F	T		7		T			T		7		
	F	F	F		7		F			F		F		

5.	P	Q	R	S	$((P \land Q)$	$\wedge$	$(\neg R$	$\wedge$	$\neg S))$	$  (P \lor$	$(R \rightarrow$	$Q)) \wedge S)$
	T	T	T	T	7	F	F	F	F	7	7	T
	T	T	T	F	7	F	₽	F	7	7	7	F
	T	T	F	T	7	F	7	F	₽	7	7	T
	T	T	F	F	7	T	7	7	7	7	7	F
	T	F	T	T	₽	F	¥	F	₽	7	₽	T
	T	F	T	F	₽	F	¥	F	7	7	₽	F
Λ	T <sub>1</sub>	ςĒ	Fr	T	neţit	D۱		F	<b>4</b> ₩ 🔽 -	vath	<b>LIZ</b> 1	T T
	Ψ	Эħ.	<b>Zpl.</b>	ŢţŢ	10 ti	L <sub>F</sub> L		/ <u>Y</u>	رند پرا	varti		l J F
	F	T	T	T	₽	F	F	F	F	7	7	T
	F	T	T	F	₽	F	¥	F	7	7	7	F
	F	T	F <sub>4</sub>	<b>4</b> T	Q • \$ /~	F	- T	F	E		7	T
	F	T	LH	Uυ	s:#/p	$\Theta$	<b>₩</b> (			COHI	7	F
	F	F	T	Ť		F	¥	F	F	₽	F	F
	F	F	T	F	₽	F	¥	F	7	₽	F	F
	F	F	Æ	1	1 177	F	1 7	F	<b>₽</b>	71	7	T
	F	F	A	Ut(	ı ₩e	E	nai	7	) (V V	cod	er 7	F

[Q p.14]

[Q p.15]

7.	P	Q	R	(P	$\vee$	$(Q \leftrightarrow R))$	$((Q \rightarrow P)$	$\wedge$	Q)
	T	T	T		T	7	7	T	
	T	T	F		T	¥	7	T	
	T	F	T		T	¥	7	F	
	T	F	F		T	7	7	F	
	F	T	T		T	7	<b>₽</b>	F	
	F	T	F		F	F	<b>₽</b>	F	
	F	F	T		F	¥	7	F	
	F	F	F		T	7	7	F	

[Q p.15]

8.	P	Q	R	$\neg$	$((P \wedge Q)$	$\wedge$	R)	$((P \rightarrow Q)$	$\leftrightarrow$	$(P \rightarrow R))$
	T	T	T	F	7	7		7	T	7
	T	T	F	T	7	F		7	F	<b>F</b>
	T	F	T	T	¥	F		¥	F	7
	T	F	F	T	¥	F		¥	T	<b>F</b>
	F	T	T	T	¥	F		7	T	7
	F	T	F	T	¥	F		7	T	7
	F	F	T	T	¥	F		7	T	7
	F	F	F	T	¥	F		7	T	7

[Q p.15]

9.	P	Q	( <i>P</i>	$\vee$ $Q$	$(P) \mid \neg P \mid$	$(Q \lor Q)$			[Q p.15]
	T	T	Ì	T	F	T			•
	T	F		T	F	F			
	F	T		T	T	T			
<b>A</b>	F	F		F	$T_{\bullet}$	$\mathbf{D}^{F}$ :	_4 T	7	TT-1
A	S	515	<u>yn</u>	m	ent	Proje	ect E	<u>txam</u>	Help
10.	P	Q	R	S	$(P \rightarrow$	$(Q \xrightarrow{\bullet}$	$(R \rightarrow$	///	[ <b>Q</b> p.15]
	T	T	T	T	Т	7	7	F	
	T	T	า <del>T</del> t	159	<'/∱	$\mathbf{OW}^{\mathbf{F}}$	odeř	.com	
	T	T <sup>*</sup>	F	<b>P</b> '	3.//P	The state of the s	+	*	
	T	T	F	F	T	eChat	7	T	
	T	F	T	$1^{T}$			T	F <sub>1</sub>	10
	T	F.	<u> T</u> (		. <b>VV</b> IC	<b>C</b> Hāl		<i>N</i> COLU	
	T	F	F	T	T	7	7	F	
	T	F	F	F	T	<b>Y</b>	<b>Y</b>	T	
	F	T	T	T	T	7	7	F	
	F	T	T	F	T	¥	F	T	
	F	T	F	T	T	7	7	F	
	F	T	F	F	T	7	7	T	
	F	F	T	T	T	7	7	F	
	F	F	T	F	T	7	¥	T	
	F	F	F	T	T	7	7	F	
	F	F	F	F	T	7	7	T	

[Contents]

#### Answers 3.5.1

1. No. None of our connectives has a truth table which matches the outputs of this truth function in all cases. [Q p.15]

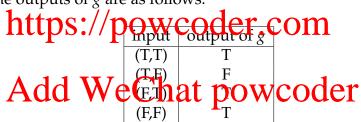
2.	input	output of function $f_4^2$	output of function $f_5^2$
	(T,T)	T	T
	(T,F)	F	F
	(F,T)	F	T
	(F.F)	F	Т

[Q p.15]

3. T [Q p.15]

4. (iv) You do not need to know any truth values. Whether  $(A \rightarrow B)$  is  $A^T \circ F = A^T \circ F \circ A^T \circ A^T \circ F \circ A^T \circ A^T \circ F \circ A^T \circ A$ 

5.  $\rightarrow$ . The outputs of *g* are as follows:



These outputs match the truth table for  $\rightarrow$  in every case.

NB To get the output of g where the input is (x, y), we first take x as input to  $f_2^1$ , and then take the output of *this*, and y—in that order—as the inputs to  $f_3^2$ . The output of *that* is the output of g for input (x, y):

$\boldsymbol{\chi}$	y	$f_2^1(x)$	$f_3^2(f_2^1(x),y)$
T	T	F	T
T	F	F	F
F	T	T	T
F	F	T	Т

The rightmost column of this table gives us the outputs of g for all possible values of x and y, since  $g(x,y) = f_3^2(f_2^1(x),y)$ . [Q p.15]

[Contents]

# **Chapter 4**

### **Uses of Truth Tables**

#### Answers 4.1.2

Assignment Project Exam Help. 16]

$\mid A \mid$	В	C	A	$\vee$	В	A	$\rightarrow$	C	(B	$\rightarrow$	C)	$\rightarrow$	C
T	T	T		T			T		1	7		T	
T	T	1#1	105	Τ/	/n	O	XFC	coc	de <sup>-</sup>	rFC	on	ηT	
T	F	Т	P	Ť	'P		Т			7		Т	
T	F	F		T			F			7		F	
F	T	T	1,1	T	17		1T	4	00	<b>T</b> .	00	T	40
F	Τ	Ť(	IU	TV	VE		140	ll	μυ	<b>V</b> /	CO	UP.	L
F	F	T		F			T			7		T	
F	F	F		F			T			7		F	

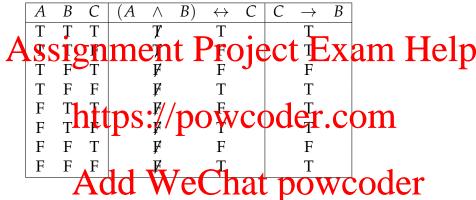
2. Invalid. Counterexample: *A* false, *B* false, *C* false (row 8). [Q p.16]

A	В	С	$\neg A$	$\neg$	((A	$\rightarrow$	<i>B</i> )	$\wedge$	(B	$\rightarrow$	<i>C</i> ))	V	C
T	T	T	F	¥		7		7		7		T	
T	T	F	F	7		7		F		F		T	
T	F	T	F	7		F		F		7		T	
T	F	F	F	7		F		¥		7		T	
F	T	T	T	¥		7		7		7		T	
F	T	F	T	7		7		F		F		T	
F	F	T	T	¥		7		7		7		T	
* F	F	F	T	F		7		7		7		F	

3. Invalid. Counterexample: *A* true, *B* true, *C* false (row 2). [Q p.16]

A	В	С	A	$\wedge$	$\neg B)$	$\rightarrow$	С	$\neg C$	$\neg A$
T	T	T		F	F	T		F	F
* T	T	F		F	${F}$	T		T	F
T	F	T		7	7	T		F	F
T	F	F		7	7	F		T	F
F	T	T		F	₽	T		F	T
F	T	F		F	₽	T		T	T
F	F	T		F	7	T		F	T
F	F	F		F	7	T		T	T

4. Valid. [Q p.16]



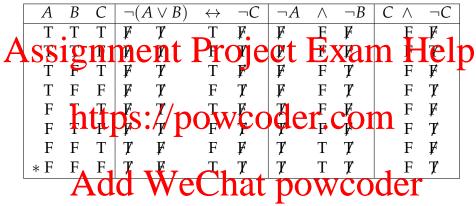
5. Valid. [Q p.16]

A	В	C	$(\neg A$	$\wedge$	$\neg B)$	$\leftrightarrow$	$\neg C$	$\neg(A)$	$\vee$	B)	$C \rightarrow$	$\neg C$
T	T	T	<b>F</b>	F	F	T	F	F	7		F	F
T	T	F	₽	F	F	F	7	F	7		T	7
T	F	T	₽	F	7	T	F	F	7		F	F
T	F	F	F	F	7	F	7	F	7		T	7
F	T	T	7	F	₽	T	F	F	7		F	F
F	T	F	7	F	F	F	7	F	7		T	7
F	F	T	7	7	7	F	F	T	F		F	F
F	F	F	7	7	7	T	7	Т	F		T	7

6. Valid [Q p.16]

A	В	С	$A \vee B$	$\neg A$	V C	$B \rightarrow C$
T	T	T	T	F	T	T
T	T	F	T	₽	F	F
T	F	T	T	₽	T	T
T	F	F	T	<b>₽</b>	F	T
F	T	T	T	7	T	T
F	T	F	T	7	T	F
F	F	T	F	7	T	T
F	F	F	F	7	T	T

7. Invalid. Counterexample: *A* false, *B* false, *C* false (row 8). [Q p.17]



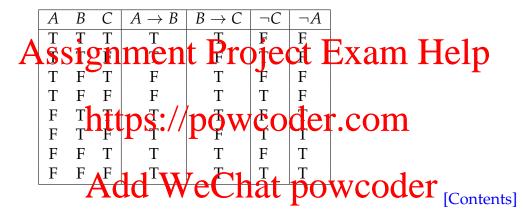
8. Invalid. Counterexample: *A* true, *B* false, *C* true (row 3). [Q p.17]

A	В	С	一(.	$A \wedge B$	$\rightarrow$	$(C \lor A)$	$\neg A$	V	$\neg B$	¬ (C	V	$\neg C)$
T	T	T	F	7	T	7	F	F	F	F	7	F
T	T	F	¥	7	T	7	₽	F	F	F	7	7
* T	F	T	7	₽	T	7	₽	T	7	F	7	¥
T	F	F	7	¥	T	7	₽	T	7	F	7	7
F	T	T	7	₽	T	7	77	T	F	F	7	₽
F	T	F	7	₽	F	₽	7	T	F	F	7	7
F	F	T	7	₽	T	7	7	T	7	F	7	¥
F	F	F	7	F	F	F	7	T	7	F	7	7

9. Valid. [Q p.17]

A	В	С	A	$\rightarrow$	$(B \wedge C)$	В	$\leftrightarrow$	$\neg C$	$\neg A$
T	T	T		T	7		F	F	F
T	T	F		F	₽		T	7	F
T	F	T		F	F		T	F	F
T	F	F		F	F		F	7	F
F	T	T		T	7		F	¥	T
F	T	F		T	F		T	7	T
F	F	T		T	F		T	¥	T
F	F	F		T	F		F	7	T

10. Valid. [Q p.17]



#### **Answers 4.2.1**

1. Neither [Q p.17]

P	Q	(P)	V	Q)	$\rightarrow$	<i>P</i> )
T	T		7		T	
T	F		7		T	
F	T		7		F	
F	F		F		T	

2. Neither [Q p.17]

P	Q	R	$\neg P$	$\wedge$	(Q	V	R))
T	T	T	F	F		7	
T	T	F	₽	F		7	
T	F	T	₽	F		7	
T	F	F	F	F		F	
F	T	T	7	T		7	
F	T	F	7	T		7	
F	F	T	7	T		7	
F	F	F	7	F		F	

3. Contradiction [Q p.17]

4. Tautology [Q p.17]

P	Q T.	A <sub>r</sub> (	ld V	vec#	at p	P)))) <b>WC</b>	oder
T	T	F	Т	7	7		
T	F	T	Т	7	7		
T	F	F	Т	7	7		
F	T	T	Т	¥	F		
F	T	F	Т	7	7		
F	F	T	Т	7	F		
F	F	F	T	7	7		

5. Tautology [Q p.17]

P	Q	$(P \rightarrow$	$((P \rightarrow$	$Q) \rightarrow$	Q))
T	T	T	7	7	
T	F	T	¥	7	
F	T	T	7	7	
F	F	T	7	¥	

6. Neither [Q p.17]

P	Q	$(P \rightarrow$	$((Q \rightarrow P)$	$\rightarrow Q))$
T	T	T	7	7
T	F	F	7	₽
F	T	T	¥	7
F	F	T	7	F

7. Tautology [Q p.17]

1	D	Q	$((P \rightarrow Q)$	V	$\neg(Q$	$\wedge$	$\neg Q))$
	Γ	T	7	T	7	F	<b>F</b>
]	Γ	F	<b>₽</b>	T	7	F	7
1	F	T	7	T	7	F	F
1	F	F	7	T	7	F	7

# Assignment Project Exam Help.17]

9. Neither [Q p.17]

P	Q	$((P \wedge Q)$	$\leftrightarrow$	$(Q \leftrightarrow P))$
T	T	7	T	7
T	F	₽	T	¥
F	T	₽	T	¥
F	F	¥	F	7

10. Contradiction [Q p.17]

P	Q	一((	$(P \wedge Q)$	$\rightarrow$	$(Q \leftrightarrow P))$
T	_		7	7	7
T	F	F	₽	7	¥
	T	F	₽	7	¥
F	F	F	F	7	7

[Contents]

#### Answers 4.3.1

1.	P	Q	(P	$\rightarrow$	Q)	$\neg(P)$	$\wedge$	$\neg Q)$
	* T	T		T		T	F	F
	T	F		F		F	7	7
	F	T		T		T	F	F
	F	F		T		T	F	7

- (a) jointly satisfiable, because both true on e.g. \*'ed row.
- (b) equivalent, because same truth value on every row
- (c) not contradictory, because jointly satisfiable
- (d) not contrary, because jointly satisfiable [Q p.18]

# 

- (a) jointly unsatisfiable, because no row on which both true
- (b) not qualent be austriate part Godet g. \*'ed row.
- (c) not contradictory, because both false on e.g.  $t^\prime ed$  row.
- (d) contrary because jointly unsatisfiable and not contradictory

[Q p.18]

3.	P	Q	$\neg (P)$	$\leftrightarrow$	Q)	$\neg(P)$	$\rightarrow$	Q)	V	$\neg(P$	V	$\neg Q)$
	T	T	F	7		F	7		F	F	7	F
	* T	F	T	¥		7	F		T	₽	7	7
	F	T	T	¥		₽	7		T	7	F	F
	F	F	F	7		F	7		F	F	7	7

- (a) jointly satisfiable, because both true on e.g. \*'ed row.
- (b) equivalent because same truth value on every row
- (c) not contradictory, because jointly satisfiable
- (d) not contrary, because jointly satisfiable [Q p.18]

4.	P	Q	R	( <i>P</i>	$\rightarrow$	(Q	$\rightarrow$	R))	((P	$\rightarrow$	Q)	$\rightarrow$	R)
	* T	Т	Т		Т		7			7		Т	
	T	T	F		F		¥			7		F	
	T	F	T		T		7			F		T	
	T	F	F		T		7			F		T	
	F	T	T		T		7			7		T	
	† F	T	F		T		F			7		F	
	F	F	T		T		7			7		T	
	F	F	F		T		7			7		F	

- (a) jointly satisfiable because both true on e.g. \*'ed row.
- (b) not equivalent because different truth values on e.g. t'ed row.
- (c) not contradictory, because jointly satisfiable

Assignment Project Exam Help

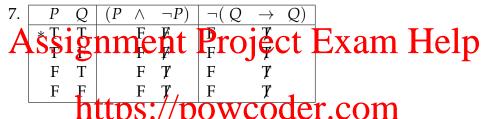
5.	P	Q	R	P	$\wedge$	(Q	Λ	$\neg \zeta$	2))	$\neg(Q)$	$\rightarrow$	$\neg(R$	$\wedge$	$\neg Q))$
	* T	T	Ţ		F,		F	F	1	F	7	7	F	F
	T	h'	ter	DS:	/₮1	$\mathbf{OC}$	<b>₩</b> (	CO	de	er.c	COI	$\mathbf{m}$	F	F
	T	F	T		F		F	7		F	7	F	7	7
	T	F	F		F		F	7		F	7	7	F	7
	F	<b>T</b>	X,	4 7	XF/		TE.		n	Exx.	<b>6</b>	der	F	F
	F	T	F	u '	ř		7	q.	P'	<b>գ</b> ₩	Cy)	<b>Y</b> CI	F	F
	F	F	T		F		F	7		F	7	¥	7	7
	F	F	F		F		F	7		F	7	7	F	7

- (a) jointly unsatisfiable, because no row on which both true
- (b) equivalent because same truth value on every row
- (c) not contradictory, because both false on e.g. \*'ed row.
- (d) contrary, because jointly unsatisfiable and not contradictory

[Q p.18]

6.	P	R	(P	$\wedge$	$\neg P)$	(R	V	$\neg R)$
	* T	T		F	F		T	F
	T	F		F	F		T	7
	F	T		F	7		T	F
	F	F		F	7		T	7

- (a) jointly unsatisfiable, because no row on which both true
- (b) not equivalent because different truth values on e.g. \*'ed row.
- (c) contradictory, because jointly unsatisfiable and no row on which both false
- (d) not contrary, because no row on which both false [Q p.18]

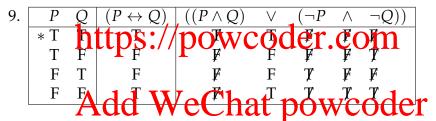


- (a) jointly unsatisfiable, because no row on which both true
- (b) equivalent because same truth value on every row Add WeChat powcoder (c) not contradictory, because both false on e.g. \*'ed row.
- (d) contrary, because jointly unsatisfiable and not contradictory

[Q p.18]

8.	P	Q	R	$((P \rightarrow Q)$	$\rightarrow$	R)	$\neg(P$	V	$\neg (Q$	$\wedge$	$\neg R))$
	* T	T	Т	7	T		F	7	7	F	F
	† T	T	F	7	F		F	7	F	7	7
	T	F	T	₽	T		F	7	7	F	F
	T	F	F	<b>₽</b>	T		F	7	7	F	7
	F	T	T	7	T		F	7	7	F	F
	F	T	F	7	F		T	F	F	7	7
	F	F	T	7	T		F	7	7	F	F
	F	F	F	7	F		F	7	7	F	7

- (a) jointly unsatisfiable, because no row on which both true
- (b) not equivalent because different truth values on e.g. \*'ed row.
- (c) not contradictory, because both false on e.g. t'ed row.
- Assignment Project Exam Help



- (a) jointly satisfiable, because both true on e.g. row 1
- (b) equivalent because same truth value on every row
- (c) not contradictory, because jointly satisfiable
- (d) not contrary, because jointly satisfiable [Q p.18]

10.	P	Q	$(P \leftrightarrow Q)$	$((P \wedge Q)$	$\vee$	$(\neg P$	$\wedge$	$\neg Q))$
	* T	T	T	7	T	<b>F</b>	F	¥
	T	F	F	¥	F	F	F	7
	F	T	F	₽	F	7	F	¥
	F	F	T	<b>₽</b>	T	7	7	7

- (a) jointly satisfiable, because both true on e.g. row 1
- (b) equivalent because same truth value on every row
- (c) not contradictory, because jointly satisfiable
- (d) not contrary, because jointly satisfiable

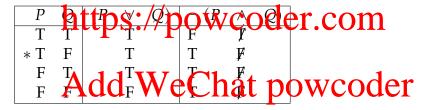
[Q p.18]

[Contents]

# Answers 4.4.1 Project Exam Help

1. Satisfiable (\*'ed row)

[Q p.18]



2. Unsatisfiable [Q p.18]

P	Q	$\neg (P)$	$\rightarrow$ Q)	$(P \leftrightarrow Q)$	$(\neg P$	$\vee$	Q)
T	T	F	7	T	F	T	
T	F	T	₽	F	₽	F	
F	T	F	7	F	7	T	
F	F	F	7	T	7	T	

3. Unsatisfiable [Q p.18]

P	( <i>P</i>	$\rightarrow$	$\neg P)$	$\bigcap$ $(P)$	V	$\neg P)$	$(\neg P$	$\rightarrow$	P)
T		F	F		T	F	F	T	
F		T	7		T	7	7	F	

4. Unsatisfiable [Q p.18]

P	Q	R	$(P \lor Q)$	V	R	$\neg P$	$\rightarrow$	$\neg Q)$	$(\neg Q$	$\rightarrow$	$\neg R)$	$\neg P$
T	T	T	7	T		F	T	F	F	T	F	F
T	T	F	7	T		₽	T	¥	₽	T	7	F
T	F	T	7	T		₽	T	7	7	F	₽	F
T	F	F	7	T		F	T	7	7	T	7	F
F	T	T	7	T		7	F	F	₽	T	₽	T
F	T	F	7	T		7	F	F	₽	T	7	T
F	F	T	₽	T		7	T	7	7	F	₽	T
F	F	F	¥	F		7	T	7	7	T	7	T

5. Satisfiable (\*'ed row)

[Q p.18]

	$\mid P \mid$	Q	R	$(P \leftrightarrow Q)$	$(Q \vee R)$	$(R \rightarrow P)$		
	* T	T	T	T	T	T		
A	T	T	F	T	T •	. 4 T		TT.1
A	LSS:		nr	nent J	rroje	ct Ex	am	Help
	T	F	F	nent l	F	T		1
	F	т	Т	F	Т	F		
	F	ħ	tfr	ps:‡/po	ONTCO	der c	om	
	F	F	11	12.4 P		G F	OIII	
	F	F	F	T	F	T		

6. Satisfield ded We Chat powcoder [Qp.18]

P	Q	$(\neg P$	$\rightarrow$	$\neg Q)$	$(P \leftrightarrow Q)$
* T	T	F	T	F	T
T	F	₽	T	7	F
F	T	7	F	F	F
F	F	7	T	7	T

7. Unsatisfiable [Q p.18]

		$(P \rightarrow$	$P \rightarrow$	$P)) \mid (\neg \cdot$	$P \leftrightarrow$	P)
T	F	Т	7	F	F	
F		T	7	T	F	

8. Unsatisfiable [Q p.19]

P	Q	R	$(P \lor$	$\neg Q)$	$(P \rightarrow R)$	$\neg R$	$(\neg R$	$\rightarrow$	Q)
T	T	T	T	F	T	F	F	T	
T	T	F	T	F	F	T	7	T	
T	F	T	T	7	T	F	₽	T	
T	F	F	T	7	F	T	7	F	
F	T	T	F	F	T	F	₽	T	
F	T	F	F	F	T	T	7	T	
F	F	T	T	7	T	F	₽	T	
F	F	F	T	7	T	T	7	F	

9. Satisfiable (\*'ed row)

[Q p.19]

	P	Q	R	$\neg R$	$\mid \neg P \mid$	((Q	$\rightarrow$	$\neg Q)$	$\rightarrow R)$		
	T	Т	T	F	F		F	F	T		
<b>A</b>	T	• T	F	T	F -	<b></b>	¥	F	$T_{-}$		Help
A	LSS.	lg	nr	ne	M.	Prc	)1 <del>/</del> C	OT.	Exai	$\mathbf{n}$	Help
	T	F	F	T	F		7	7	F		1
	F	T	T	F	T		¥	F	T		
	* F	ħ	<b>†</b> ††	· ZC	/ <b>7</b> n	$\mathbf{O}(\mathbf{X})$	AC.	Me	r.coi	m	
	F	F	11	F •/	TP		7	Ţ	T		
	F	F	F	T	T		7	7	F		

10. Unsaticated WeChat powcoder [Qp.19]

P	Q	$(\neg P$	V	$\neg Q)$	$\neg (P$	$\wedge$	$\neg Q)$	( <i>P</i>	V	$\neg Q)$	$\neg (\neg P$	$\wedge$	$\neg Q)$
T	T	F	F	F	T	F	F		T	F	T ₽	F	F
T	F	₽	T	7	F	7	7		T	7	T ₽	¥	7
F	T	7	T	¥	T	F	F		F	F	T 7	F	F
F	F	7	T	7	T	F	7		T	7	F 7	7	7

[Contents]

## **Chapter 5**

# **Logical Form**

#### Answers 5.1.1

```
Note: There are also other correct answers to questions 1–4. Help

1. (i) \neg(\alpha \to \beta) (ii) \neg(\alpha \to (\beta \to \gamma)) (iii) \neg \text{Attps:} \beta) powcoder.com

[Q p.20]

2. (i) (\alpha \to \beta) (ii) (\alpha \text{Add WeChat powcoder}(\text{iii})) ((\alpha \lor \beta) \to (\alpha \lor \beta))

3. (i) \alpha (ii) \alpha \land \beta (iii) \alpha \land \beta (iv) \alpha \Leftrightarrow \beta
```

#### **Answers 5.2.1**

- 1. First form:  $\neg \neg \alpha$ 
  - (i)  $\alpha$  : C
  - (ii)  $\alpha : (A \wedge B)$
  - (iii)  $\alpha : (C \wedge \neg D)$

Second form:  $\neg \alpha$ 

- (i)  $\alpha : \neg C$
- (ii)  $\alpha : \neg (A \wedge B)$
- (iii)  $\alpha : \neg (C \land \neg D)$

Third form:  $\alpha$ 

## Assignment Project Exam Help

(ii)  $\alpha : \neg \neg (A \wedge B)$  $\inf_{(i)} \inf_{(a)} \frac{\nabla \nabla (C \wedge \nabla D)}{\text{ttps:}} / \underbrace{powcoder.com}$ [Q p.20] [Q p.21] (b) Yes:  $\alpha : R ; \beta : Q$ . [Q p.21] Add: WeChat powcoder [Q p.21] (ii) (a) Yes:  $\alpha : P ; \beta : Q$ . [Q p.21] (b) Yes:  $\alpha : P$ ;  $\beta : P$ . [Q p.21] (c) No. [Q p.21] (iii) (a) Yes:  $\alpha : \neg P$ ;  $\beta : Q$ . [Q p.21] (b) Yes:  $\alpha : P ; \beta : \neg P$ . [Q p.21] (c) No. [Q p.21] (iv) (a) No. [Q p.21] (b) No. [Q p.21] (c) Yes:  $\alpha : \neg P$ ;  $\beta : \neg P$ [Q p.21]

#### Answers 5.3.1

Note: There are also other correct answers to questions 1–4.

```
1. (i) \neg(\alpha \to (\alpha \to \beta))

\therefore (\alpha \lor (\alpha \to \beta))

replacements: \alpha : R ; \beta : Q
```

(ii) 
$$\neg(\alpha \to \beta)$$
  
 $\therefore (\alpha \lor \beta)$   
replacements:  $\alpha : R ; \beta : (R \to Q)$ 

(iii) 
$$\neg(\alpha \to (\beta \to \gamma))$$
  
  $\therefore (\alpha \lor (\beta \to \gamma))$   
replacements:  $\alpha : R ; \beta : R ; \gamma : Q$ 

(iv)  $\alpha$ 

# Assignment Project, Fxan Help.21]

- 2. (i)  $(\alpha \land \beta) \rightarrow \beta$ Thttps://powcoder.com

  replacements:  $\alpha : P ; \beta : Q$ 
  - (ii) a Abdd WeChat powcoder

replacements:  $\alpha : (P \wedge Q)$ ;  $\beta : Q$ 

- (iii)  $\alpha \to \beta$   $\gamma$   $\therefore \neg \alpha$ replacements:  $\alpha : (P \land Q) ; \beta : Q ; \gamma : \neg Q$
- (iv)  $\alpha$   $\beta$   $\therefore \gamma$ replacements:  $\alpha: (P \land Q) \rightarrow Q; \beta: \neg Q; \gamma: \neg (P \land Q)$  [Q p.22]

```
(i) \neg \alpha \rightarrow (\beta \rightarrow \gamma)
       \beta \rightarrow \gamma
       replacements: \alpha : Q ; \beta : R ; \gamma : S
 (ii) \neg \alpha \rightarrow \beta
        \neg \alpha
        ∴ β
        replacements: \alpha : Q : \beta : (R \to S)
(iii) \alpha \rightarrow \beta
        α
        ... β
        replacements: \alpha : \neg Q ; \beta : (R \rightarrow S)
(iv) \alpha
        β
  ssignment Project Exam Help replacements: \alpha: \neg Q \rightarrow (R \rightarrow S); \beta: \neg Q; \gamma: (R \rightarrow S)
                                                                                                  [Q p.22]
  (i) (ahttps://powcoder.com
        \neg(\neg\beta\rightarrow\alpha)
       replacements W: e @ loat powcoder
 (ii) (\alpha \rightarrow \beta) \lor (\beta \rightarrow \alpha)
        \neg(\beta \to \alpha)
        \therefore \alpha \rightarrow \beta
        replacements: \alpha : P ; \beta : \neg Q
(iii) \alpha \vee \beta
        \neg \beta
        replacements: \alpha: (P \to \neg Q); \beta: (\neg Q \to P)
(iv) \alpha
        β
       replacements: \alpha:(P\to\neg Q)\lor(\neg Q\to P);
       \beta: \neg(\neg Q \rightarrow P) ; \gamma: (P \rightarrow \neg Q)
                                                                                                  [Q p.22]
                                                                                              [Contents]
```

#### **Answers 5.4.1**

- 1. (i)  $\alpha : P ; \beta : Q$ 
  - (ii)  $\begin{array}{c|cccc} P & Q & P \rightarrow Q \\ \hline T & T & T \\ T & F & F \\ F & T & T \\ F & F & T \end{array}$

[Q p.22]

- 2. (i)  $\alpha:(A\wedge B)$ ;  $\beta:(B\vee C)$

Assignment Project Exam Help

- $\frac{\text{nttps://powcoder.coi}}{\beta}$ 
  - (ii)  $P (A \lor \neg A) (A \lor \neg A) \to (A \land \neg A) (A \land \neg A)$ TAdd WeChat Powcode T

[Q p.22]

4. (i)  $\alpha:(P \to \neg P)$ ;  $\beta:(P \to (Q \land \neg R))$ 

(ii)	P	Q	R	$(P \rightarrow \neg P)$	$(P \to \neg P)  \to  (P \to (Q \land \neg R))$	$(P \rightarrow$	$(Q \land \neg R))$
	T	T	T	F	T	F	
	T	T	F	F	T	T	
	T	F	T	F	T	F	
	T	F	F	F	T	F	
	F	T	T	T	T	T	
	F	T	F	T	T	T	
	F	F	T	T	T	T	
	F	F	F	T	T	T	

[Q p.22]

[Contents]

#### Answers 5.5.1

1. (i)  $\begin{array}{c|cc}
\alpha & \beta \\
\hline
T & T \\
* T & F \\
F & T
\end{array}$ 

Invalid: in \*'ed row, the premise is T and the conclusion is F.

[Q p.23]

(ii) Instance: P  $\therefore P$ 

Truth table: P

Assignment Project Exam Help ward: there is no row in which the premise (P) is true and the conclusion (P) is false. [Q p.23]

2. https://powcoder.com

[Q p.23]

Add WeChat powcoder [Contents]

## Chapter 6

# **Connectives: Translation and** Adequacy

# Answers 6.5.1 ASSignment Project Exam Help

- 1. Glossary:
  - B: Ben is training. //powcoder.com

  - The sun is shining.

# Add WeChat powcoder

 $(B \leftrightarrow R)$  $(R \vee S)$ 

 $\therefore (B \rightarrow \neg S)$ 

#### Truth Table:

В	R	S	$(B \leftrightarrow R)$	$(R \vee S)$	$(B \rightarrow \neg S)$
* T	T	T	T	T	F
T	T	F	T	T	T
T	F	T	$F \times$		
T	F	F	$F \times$		
F	T	T	$F \times$		
F	T	F	$F \times$		
F	F	T	T	T	T
F	F	F	T	$F \times$	

[Q p.24]

Invalid. Counterexample (\*'ed row), where *B* is T, *R* is T and *S* is T.

*M*: I have money.

C: I have a card.

W: I shall walk.

*T*: I shall get tired.

*R*: I shall have a rest.

#### Translation:

$$(\neg M \land \neg C) \to W$$

$$W \to (T \lor R)$$

$$\therefore (R \to M)$$

# Assignment Project Exam Help

https://powcoder.com

Add WeChat powcoder

Truth Table:

	M	С	W	T	R	$(\neg M \land \neg C)$	$\rightarrow W$	$W \rightarrow$	$(T \vee R)$	$R \to M$
	T	T	T	T	T	¥	T	T	7	T
	T	T	T	T	F	₽	T	T	7	T
	T	T	T	F	T	₽	T	T	7	T
	T	T	T	F	F	₽	T	F	F	T
	T	T	F	T	T	₽	T	T	7	T
	T	T	F	T	F	₽	T	T	7	T
	T	T	F	F	T	₽	T	T	7	T
	T	T	F	F	F	₽	T	T	₽	T
	T	F	T	T	T	₽	T	T	7	T
	T	F	T	T	F	₽	T	T	7	T
	T	F	T	F	T	₽	T	T	7	T
	T	F	T	F	F	₽	T	F	F	T
Λ	T	F	F	T	T P1	t Proje	T E	T	T T 1	T T T
A	722	IB	IFI.	lt		l Phoje	Ct C	Xaiti	пец	<b>)</b> T
	T	F	F	F	T	l <b>⊮</b>	Π'	T	7	
	T	F	F	F	F	₽	Ţ	T	F	T
	F	ħ	ttr	<b>)</b> \$	<u>'</u> /t/	$\mathbf{n}$ owco	đer.	com	<b>₽</b> <b>T</b> <b>T</b>	F
	F	T	TI	T	F		T	T	7	T
	F	T	T	F	T	₽	T	T	7	F
	F	TA	Ţ	F	<b>\</b> \\\\	Chat	TOU	r	er#	T
	F		E	ЦŢ	<b>VIV</b>	eChat	how	COFIG	<b>_</b>	F
	F	T	F	T	F	<b> </b>	T	T	7	T
	F	T	F	F	T	₽	T	T	7	F
	F	T	F	F	F	<b>F</b>	T	T	<b>₽</b>	T
	* F	F	T	T	T	<u>7</u>	T	T	7	F
	F	F	T	T	F	<u>7</u>	T	T	7	T
	F	F	T	F	T	<u>7</u>	T	T	7	F
	F	F	T	F	F	<u>7</u>	T	F	<u>F</u>	T
	F	F	F	T	T	7	F	T	7	F
	F	F	F	T	F	7	F	T	7	T
	F	F	F	F	T	7	F	T	7	F
	F	F	F	F	F	7	F	T	¥	T

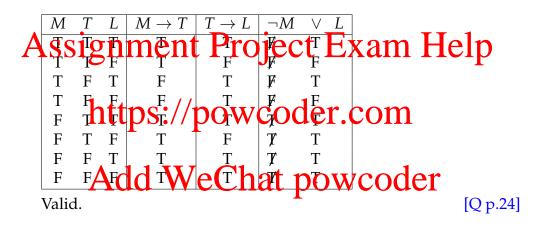
Invalid. Counterexample (\*'ed row), where M is F, C is F, W is T, T is T and R is T. [Q p.24]

M: Maisy is upset.T: There is thunder.L: There is lightning.

#### Translation:

 $\begin{aligned} M &\to T \\ T &\to L \\ \therefore &\neg M \lor L \end{aligned}$ 

#### Truth Table:



*C*: The car started.

*K*: You turned the key.

*A*: You pressed the accelerator.

#### Translation:

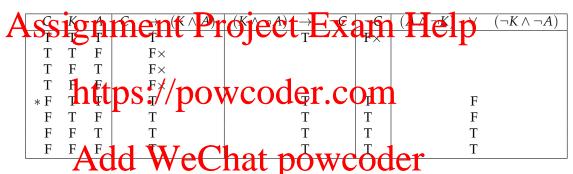
$$C \to (K \land A)$$

$$(K \land \neg A) \to \neg C$$

$$\neg C$$

$$\therefore (A \land \neg K) \lor (\neg K \land \neg A)$$

#### Truth Table:



Invalid. Counterexample (\*'ed row), where C is F, K is T and A is T.

[Q p.24]

- *B*: Maisy is barking.
- *R*: There is a robber outside.
- *A*: Maisy is asleep.
- *D*: Maisy is depressed.

#### Translation:

$$\begin{array}{l} (\neg B \lor R) \\ (R \land \neg B) \to (A \lor D) \\ \neg A \land \neg D \\ \therefore (B \leftrightarrow R) \end{array}$$

# Arssighment Project Exam Help

В	R	A	D	$\neg B \lor R$	$(R \wedge \neg B) \rightarrow (A \vee D)$	$\neg A \wedge \neg D$	$B \leftrightarrow R$
T	T	h <del>I</del> 4	T	1. //T	vcoder <sub>F</sub> com	F	T
T	T		DS	5.// <b>□</b> ∪ ∨	vcouel <sub>r</sub> com	F	T
T	T	F	T	T	T	F	T
T	T	F	F	T	T	T	T
T	F	Æι	17	We()	hat powcode	r F	F
T	F	T	F	F	nat po i coac	F	F
T	F	F	T	F	T	F	F
T	F	F	F	F	T	T	F
F	T	T	T	T	T	F	F
F	T	T	F	T	T	F	F
F	T	F	T	T	T	F	F
F	T	F	F	T	F	T	F
F	F	T	T	T	T	$\mathbf{F}$	T
F	F	T	F	T	T	F	T
F	F	F	T	T	T	F	T
F	F	F	F	T	T	T	T

Valid. [Q p.24]

*S*: It is sunny.

W: It is too windy.

*L*: We are sailing.

*F*: We are having fun.

#### Translation:

$$\neg S \to (W \lor L)$$

$$L \to F$$

$$\neg S \land \neg W$$

$$\therefore F$$

#### Truth Table:

A	SS	sig	m	m	er	it Pro	oiect	Exa	m Heln
	5	W	>L	F	$\neg S$	$\rightarrow$ (	$(W \lor L)$	$(L \rightarrow F)$	$(\neg S \land \neg M)$
	T	Т	T	T	F	T	7	T	F
	T	T <sub>1</sub>	T	F	. ₹ /	/ <sub>40</sub> T	T	$F \times$	
	T	T	lţl	<b>₽</b>	<b> </b>	/ppw	/Cøu	er.co	III F
	T	T	F	F	¥	T	7	T	F
	T	F	T	T	<b>F</b> _	T	7	T	F
	T	F	<b>4</b> T(	F	<b>F</b>	Ve(C)t	nat n	OWCC	der_
	T	F	F	T	₽	T	TO F	T	F
	T	F	F	F	F	T	₽	T	F
	F	T	T	T	7	T	7	T	F
	F	T	T	F	7	T	7	F	
	F	T	F	T	7	T	7	T	F
	F	T	F	F	7	T	7	T	F
	F	F	T	T	7	T	7	T	T
	F	F	T	F	7	T	7	$F \times$	
	F	F	F	T	7	$F \times$	¥		
	F	F	F	F	7	$F \times$	¥		

Valid. [Q p.25]

*S*: You came through Singleton.

*M*: You came through Maitland.

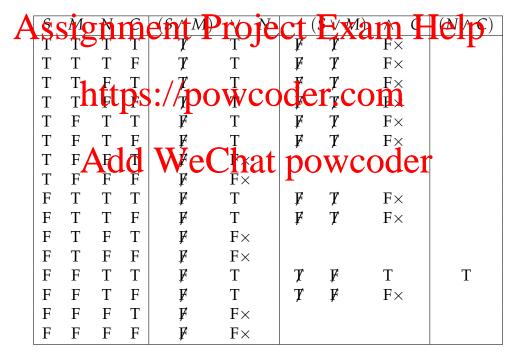
*N*: You came through Newcastle.

*C*: You came through Cessnock.

#### Translation:

$$(S \wedge M) \vee N$$
$$\neg (S \vee M) \wedge C$$
$$\therefore (N \wedge C)$$

#### Truth Table:



Valid. [Q p.25]

- *S*: The shop will be open.
- *L*: We shall have lobster for lunch.
- *T*: It is Sunday.
- R: We shall go to a restaurant.

#### Translation:

$$\begin{array}{l} S \rightarrow L \\ S \lor T \\ T \rightarrow (R \land L) \\ \therefore L \end{array}$$

#### Truth Table:

#### Т Т https://powcoder.com T T F T F T T T F T eChat powcoder T F T F T F F $F \times$ F F $\mathsf{T}$ $\mathsf{T}$ T T T 7 T T F F F T T F T F T F T T $F \times$ F F T T F $\mathsf{F} \times$ F F T T T T F F T Τ F F F F T F F F F T T $\mathsf{F} \times$ F F F F T $F \times$

Valid. [Q p.25]

C: You will catch Billy a fish.

*D*: You will feed Billy for a day.

*T*: You will teach Billy to fish.

*L*: You will feed Billy for life.

#### Translation:

 $C \rightarrow D$ 

 $T \to L$ 

 $\therefore \neg L \lor T$ 

#### Truth Table:

#### F× T T \* T Τ T T $F \times$ T F T F T T F T T T T T F T F T T F T $F \times$ F T T F F T Τ F T F F T T 7 T F F T T T F T T F T F $F\times$ T F F F T T T F F F F T F F Τ 7 T

Invalid. Counterexample (\*'ed row), where C is T, D is T and T is F and L is T. [Q p.25]

*H*: I shall be happy.

W: The Tigers will win.

*D*: It will be a draw.

#### Translation:

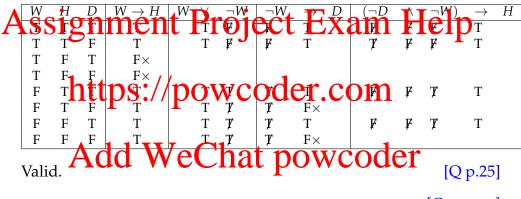
$$W \to H$$

$$W \lor \neg W$$

$$\neg W \to D$$

$$\therefore (\neg D \land \neg W) \to H$$

#### Truth Table:



[Contents]

#### Answers 6.6.3

1. (i) Functionally complete:

α	β	$\neg(\alpha \to \neg\beta)$	$(\neg \alpha \to \beta)$
T	T	T	T
T	F	F	T
F	T	F	T
F	F	F	F

The second last column is the same as the truth table for  $\alpha \wedge \beta$ , and the last column is the same as the truth table for  $\alpha \vee \beta$ , so we have defined  $\wedge$  and  $\vee$  in terms of  $\neg$  and  $\rightarrow$ . We already know

that  $\{\land, \lor, \neg\}$  is functionally complete, so this establishes that  $\{\neg, \rightarrow\}$  is functionally complete.

(Where do the columns come from? That is, it is easy to see, once the formula  $\neg(\alpha \to \neg \beta)$  is given, that this formula is equivalent to  $(\alpha \land \beta)$ —and similarly for  $(\neg \alpha \to \beta)$  and  $(\alpha \lor \beta)$ —but where do these formulas come from in the first place? The answer is: they come by trial and error, guided by knowledge of the relevant truth tables. We know what truth table we want to end up with—say, the truth table for  $(\alpha \land \beta)$ —and we know what connectives we are allowed to use—in this case  $\neg$  and  $\rightarrow$ —and what their truth tables are; we then play around with formulas involving different combinations of the allowed connectives until we find one that has the desired truth table.)

[A p.25]

(ii) Not functionally complete: we cannot define any connective Assympthas a pold temper of temperature one Type (three T's) or \(\lambda\) (one T).

Consider the truth table for  $\alpha \leftrightarrow \beta$ . (We make no assumptions about how complex  $\alpha$  and  $\beta$  are i.e. about how many connectives and basic propositions they contain hence no assumptions about how many rows there are in this truth table.)  $\alpha \leftrightarrow \beta$ is T iff  $\alpha$  and  $\beta$  have the *same* truth value (both T or both F); α A 6 S F M and A have on S Wruth a test (one T and the other F). Let us call a row in which  $\alpha \leftrightarrow \beta$  is true a 'T row' and a row in which it is false an 'F row', and let us say that a T is worth 1 point and an F is worth 0 points (this has no deep significance: it simply allows the following discussion to be presented in a simple way). If we sum the number of points in the  $\alpha$ and  $\beta$  columns (combined), each F row contributes 1 point, and each T row contributes either 2 points or 0 points. Now suppose there is an *odd* number of T rows (and hence an odd number of F rows, as there is an even number of rows in total in any truth table). Then the total number of points in the  $\alpha$  and  $\beta$  columns (combined) is an odd number (the number of F rows) plus some 2's and 0's—i.e. an odd number. That means that either  $\alpha$  is true in an odd number of rows and  $\beta$  is true in an even number of rows, or vice versa. Either way, it follows that  $\alpha \leftrightarrow \beta$  is true in an odd number of rows iff one of  $\alpha$  and  $\beta$  is true in an odd number of rows.

Consider the truth table for  $\alpha \vee \beta$ .  $\alpha \vee \beta$  is T iff  $\alpha$  and  $\beta$  have *op*-

posite truth values (one T and the other F);  $\alpha \veebar \beta$  is F iff  $\alpha$  and  $\beta$  have the *same* truth value (both T or both F). If we sum the number of points in the  $\alpha$  and  $\beta$  columns (combined), each T row contributes 1 point, and each F row contributes either 2 points or 0 points. Now suppose there is an *odd* number of T rows (and hence an odd number of F rows). Then the total number of points in the  $\alpha$  and  $\beta$  columns (combined) is an odd number (the number of T rows) plus some 2's and 0's—i.e. an odd number. That means that either  $\alpha$  is true in an odd number of rows and  $\beta$  is true in an even number of rows, or vice versa. Either way, it follows that  $\alpha \veebar \beta$  is true in an odd number of rows iff one of  $\alpha$  and  $\beta$  is true in an odd number of rows.

Now think about formulas that we can define using only  $\leftrightarrow$ ,  $\veebar$  and basic propositions. Each basic proposition is true in an even number of rows (half the rows in the table: recall how the matrix is laid out); and as we have just seen, any proposition of Silution and proposition which had true appear number of rows, is itself true in an even number of rows. So

number of rows, is itself true in an even number of rows. So every proposition that we can define using only  $\leftrightarrow$ ,  $\veebar$  and basic propositions has an every number of  $\mathsf{T}'$  sincity but table.

[Q p.25]

T F

(iii) Funct	ion	ally	comple	ete:	
lacksquare	4	<u>1</u>	$\mathbf{W}_{\mathbf{A}}$	Chat nou	reoder
$oldsymbol{\Gamma}$	a	$\beta$	$\alpha \downarrow \alpha$	$(\alpha \downarrow \alpha) \downarrow (\beta \downarrow \beta)$	$(\alpha \downarrow \beta) \downarrow (\alpha \downarrow \beta)$
	T	T	F	T	T
	T	F	F	F	T

F

F T

Τ

The third last column is the same as the truth table for  $\neg \alpha$ , the second last column is the same as the truth table for  $\alpha \land \beta$ , and the last column is the same as the truth table for  $\alpha \lor \beta$ , so we have defined  $\neg$ ,  $\land$  and  $\lor$  in terms of  $\downarrow$ . We already know that  $\{\land,\lor,\neg\}$  is functionally complete, so this establishes that  $\{\downarrow\}$  is functionally complete. [Q p.25]

(iv) Not functionally complete: we cannot define any connective which has an F in the top row. When  $\alpha$  and  $\beta$  are both T,  $(\alpha \to \beta)$  is T and  $(\alpha \land \beta)$  is T—hence so is *any* formula, however complex, built up from  $\alpha$ 's,  $\beta$ 's,  $\rightarrow$ 's and  $\wedge$ 's. Hence no such formula is equivalent to  $\neg \alpha$ , which is F when  $\alpha$  is T. [Q p.25]

(v) Functionally complete:

α	β	$\neg(\neg\alpha @_{12}\beta)$	$\alpha @_{12} \neg \beta$
T	T	T	T
T	F	T	F
F	T	T	F
F	F	F	F

The second last column is the same as the truth table for  $\alpha \vee \beta$ , and the last column is the same as the truth table for  $\alpha \wedge \beta$ , so we have defined  $\wedge$  and  $\vee$  in terms of  $\neg$  and  $@_{12}$ . We already know that  $\{\wedge, \vee, \neg\}$  is functionally complete, so this establishes that  $\{\neg, @_{12}\}$  is functionally complete. [Q p.25]

- (vi) Not functionally complete:  $(\alpha @_4 \beta)$  and  $(\alpha @_4 \alpha)$  are both equivalent to  $\alpha$ , and  $(\beta @_4 \beta)$  and  $(\beta @_4 \alpha)$  are both equivalent to  $\beta$ , so we cannot express anything more with  $\alpha$ 's,  $\beta$ 's,  $\vee$ 's and  $\mathbb{Q}_4$ 's otherwise cap with jist  $\alpha$ 's,  $\beta$ 's and  $\mathbb{Q}_4$ 's But  $\{\gamma\}$  is not a func-
- As Sthan we can with just  $\alpha'$ s,  $\beta'$ s and  $\gamma'$ s. But  $\{\gamma'\}$  Is het a functionally complete set of connectives (why not:), hence neither is  $\{\gamma, 2, 4\}$ .
- 2. (i) https://powcoder.com
  T F T
  Add WeChat powcoder
  - В  $((A@_{11}B)$  $(2_{15} B)$ [Q p.26] (ii) Α T T F T F 7 F F F T F F F 7 F
  - (iii) Α В (A) $(A@_{6}B))$ [Q p.26] T T F 7 Ţ F T F Ţ F F T F Ţ 7 F F T F F
  - В Α 23  $\neg B$ ) [Q p.26] (iv) Α  $\leftrightarrow$ (AT T T 7 F T F T 7 7 F F T 7 F F T F F T

(v)	A	В	$(A @_{12} B)$	V	$(B \otimes_{12} A)$
	T	T	<b>F</b>	F	<b>F</b>
	T	F	7	T	<b>F</b>
	F	T	<b>₽</b>	T	7
	F	F	¥	F	¥
(vi)	A	В	$(A @_{12} B)$	V	$(B \otimes_{16} A)$
	T	T	<b>F</b>	F	F
	T	F	T	T	F

F

3. Here are two ways to answer each part.

T

First, we can form a disjunction of row descriptions, in the way explained in §6.6.2, pp.129–131. This gives:

## ssignment Project Exam Help.261

(ii) 
$$(\alpha \wedge \neg \beta \wedge \gamma) \vee (\alpha \wedge \neg \beta \wedge \neg \gamma) \vee (\neg \alpha \wedge \beta \wedge \gamma) \vee (\neg \alpha \wedge \beta \wedge \neg \gamma)$$

[Q p.26]

## https://powcoder.com Alternatively, we can use the following hints, to get:

(i) (¬A\d) dr Wher that power [Q p.26] (Hint: dok at the truth table prower of that it is equivalent to  $(\beta \rightarrow \gamma)$ .)

(ii)  $(\alpha \vee \beta) \wedge \neg (\alpha \wedge \beta)$ [Q p.26] (Hint: Look at the truth table for  $\natural(\alpha, \beta, \gamma)$ , and note that it is equivalent to  $(\alpha \vee \beta)$ .)

There are also other correct answers to (i) and (ii).

4.	(i) $(A \land \neg B)$	[Q p.26]
	(ii) $(\neg A \land \neg B)$	[Q p.26]
	(iii) $\neg (A \land B)$	[Q p.26]
	(iv) $A \wedge \neg B$	[Q p.26]
	(v) $\neg (A \land \neg B) \land \neg (B \land \neg A)$	[Q p.26]
	(vi) $\neg (A \land \neg A)$	[Q p.26]
5.	(i) ① <sub>4</sub>	[Q p.26]

 (ii)  $@_{14}$  [Q p.26]

 (iii)  $@_2$  and  $\neg$  [Q p.26]

 (iv)  $@_4$ ,  $@_6$ ,  $@_{11}$  and  $@_{13}$  [Q p.26]

 [Contents]

# Assignment Project Exam Help https://powcoder.com Add WeChat powcoder

#### Chapter 7

#### **Trees for Propositional Logic**

#### **Answers 7.2.1.1**

## Assignment Project Exam Help

2.

https://powcoder.com

Add WeChat powcoder  $(A \rightarrow B)$  B[Q p.27]

[Q p.27]

[Q p.27]

4.

$$((A \leftrightarrow B) \leftrightarrow B) \checkmark$$

$$(A \leftrightarrow B) \neg (A \leftrightarrow B)$$

$$B \neg B$$

[Q p.27]

5.

$$\neg (A \leftrightarrow \neg \neg A) \checkmark$$

$$\overrightarrow{A} \neg A$$

$$\neg \neg \neg A \neg \neg A$$

[Q p.27]

6. 
$$\neg(\neg A \lor B) \checkmark \\ \neg \neg A \\ \neg B$$

[Q p.27]

[Contents]

#### **Answers 7.2.2.1**

1.  $(A \to B) \to B \checkmark$   $\neg (A \to B) \checkmark B$  A  $\neg B$ 

[Q p.27]

## Assignment Project Exam Help

https://powcoder.com

[Q p.27]

Add WeChatapowcoder  $\neg (A \lor B) \lor \neg (A \lor B$ 

[Q p.27]

4.  $\neg \neg ((A \land B) \lor (A \land \neg B)) \checkmark$   $((A \land B) \lor (A \land \neg B)) \checkmark$   $(A \land B) \checkmark (A \land \neg B) \checkmark$   $A \qquad A \qquad A \qquad B \qquad \neg B$ 

[Q p.27]

[Contents]

#### **Answers 7.2.3.1**

1. 
$$\neg (A \to (B \to A)) \checkmark
A
\neg (B \to A) \checkmark
B
\neg A
\times$$

$$(A \to B) \lor (\neg A \lor B) \checkmark$$

$$(A \to B) \checkmark (\neg A \lor B) \checkmark$$

[Q p.28]

## Assignment Project Exam Help

## https://powcoder.com Add WeChat powcoder

[Q p.28]

4. 
$$\neg \neg (A \lor B) \checkmark \\ \neg (A \lor B) \checkmark \\ \neg A \\ \neg B$$

[Q p.28]

[Q p.28]

6. 
$$\neg(\neg(A \land B) \leftrightarrow (\neg A \lor \neg B)) \checkmark$$

$$\neg(A \land B) \checkmark \qquad \neg\neg(A \land B) \checkmark$$

$$\neg(\neg A \lor \neg B) \checkmark \qquad (\neg A \lor \neg B) \checkmark$$

$$\neg\neg A \checkmark \qquad (A \land B) \checkmark$$

$$\neg B \checkmark \qquad A$$

$$A \qquad B$$

$$B \qquad \neg A \qquad B$$

$$B \qquad \neg A \qquad B$$

$$A \qquad B \qquad B$$

[Q p.28]

[Contents]

## Amssignihent Project Exam Help

1. Valid. [Q p.28]

https://poweoder.com

Add WeChat powcoder

2. Invalid. Counterexample: A is T, B is F.

[Q p.28]

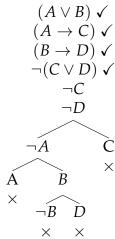
$$(A \lor B) \checkmark$$

$$\neg B$$

$$\widehat{A} \quad B$$

$$\uparrow \quad \times$$

3. Valid. [Q p.28]



4. Valid. [Q p.28]

#### $((A \lor \neg B) \to C) \checkmark$ bject Exam Help Assignment Pr

# https://poweoder.com Add WeChat powcoder

5. Invalid. Counterexample: *A* is F, *B* is T.

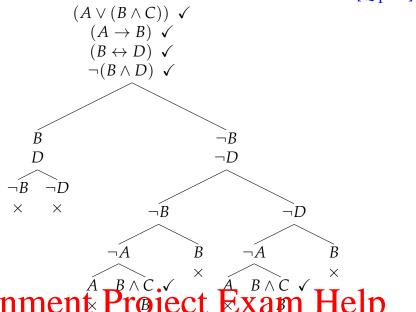
 $(A \to B) \checkmark \neg A$ 

[Q p.28]

[Q p.29] 6. Valid.

 $\begin{array}{c} A \\ (A \to B) \checkmark \\ \neg B \end{array}$ 

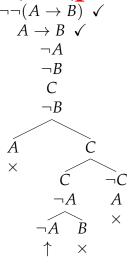
7. Valid. [Q p.29]



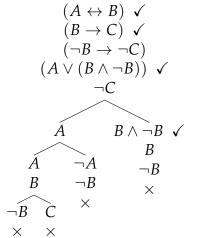
×

8. Invalid to prevent the second power of the property of the

Add WeCharpowcoder



9. Valid. [Q p.29]

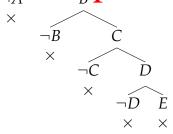


10. Valid. [Q p.29]

## Assignment $(P, B) \checkmark (E, A) \checkmark$

https://powooder.com

Add Wechat, powcoder



[Contents]

#### **Answers 7.3.2.1**

1.

(i) Contradiction.

[Q p.29]

$$\begin{array}{c} (A \wedge \neg A) \checkmark \\ A \\ \neg A \\ \times \end{array}$$

(ii) Contradiction.

[Q p.29]

$$(A \lor B) \land \neg (A \lor B) \checkmark$$

$$(A \lor B) \checkmark$$

$$\neg (A \lor B) \checkmark$$

$$\neg A$$

$$\neg B$$

$$\widehat{A} \quad \widehat{B}$$

Assignment Project Exam Help.29

 $\neg B$ 

Add WeChatapowcoder

(iv) Contradiction.

[Q p.29]

$$(A \to \neg(A \lor B)) \land \neg(\neg(A \lor B) \lor B) \checkmark$$

$$(A \to \neg(A \lor B)) \checkmark$$

$$\neg(\neg(A \lor B) \lor B) \checkmark$$

$$\neg(A \lor B) \checkmark$$

$$\neg B$$

$$(A \lor B) \checkmark$$

$$\neg A \qquad \neg(A \lor B)$$

$$\checkmark$$

$$A \qquad B$$

$$\times \qquad \times$$

$$\neg((\neg B \lor C) \leftrightarrow (B \to C)) \checkmark$$

$$\neg B \lor C \checkmark \qquad \neg(\neg B \lor C) \checkmark$$

$$\neg(B \to C) \checkmark \qquad B \to C \checkmark$$

$$B \qquad \neg \neg B \checkmark$$

$$\neg C \qquad \neg C$$

$$B \qquad \Rightarrow C \qquad \Rightarrow B$$

$$\neg C \qquad \neg C \qquad \Rightarrow B$$

$$\times \times \times \qquad \Rightarrow B \qquad C$$

$$\times \times \times \qquad \Rightarrow B \qquad \Rightarrow C$$

(vi) Satisfiable. True when *A* is F, *B* is F and *C* is F. 
$$(A \leftrightarrow \neg A) \lor (A \rightarrow \neg (B \lor C)) \checkmark$$

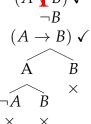
[Q p.29]

## 

https://powcoder.com

2.

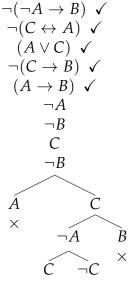
## (i) Unatiatiable We Chat, powcoder [Q p.30]



(ii) Satisfiable. All true when *A* is F, *B* is T and *C* is F. [Q p.30]

$$(A \lor B) \checkmark 
(B \lor C) \checkmark 
\neg (A \lor C) \checkmark 
\neg A 
\neg C 
A B 
× B C 
↑ ×$$

(iii) Satisfiable. All true when *A* is F, *B* is F and *C* is T. [Q p.30]

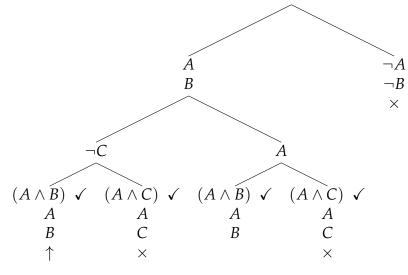


### Assignment Project<sup>A</sup>

(iv) Satisfiable. All true when *A* is T, *B* is T and *C* is F. [Q p.30]

https://powcoder.@om $\checkmark$   $(C \rightarrow A) \checkmark$   $(A \land B) \lor (A \land C) \checkmark$ 

## Add WeChat powcoder



[Contents]

#### **Answers 7.3.3.1**

1. Can both be true, e.g. when *A* is T and *B* is F:

$$(\neg A \to B) \checkmark$$

$$(B \to A) \checkmark$$

$$\neg \neg A \checkmark B$$

$$A \qquad \neg B \qquad A$$

$$\neg B \qquad A \qquad \times$$

Therefore, jointly satisfiable.

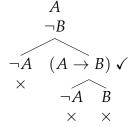
[Q p.30]

2. Cannot both be true:

## Assignment Project Exam Help

 $\underset{\text{Cannot both be false:}}{\text{https://powcoder.com}}$ 

## Add WeCharpowcoder



Therefore, contradictories.

[Q p.30]

3. Cannot both be true:

$$\neg (A \leftrightarrow \neg B) \checkmark \\
\neg (A \lor \neg B) \checkmark \\
\neg A \\
\neg \neg B \checkmark \\
B \\
A \\
\neg A \\
\neg B \\
\times \times$$

Can both be false, e.g. when *A* is T and *B* is F:

$$\neg\neg(A \leftrightarrow \neg B) \checkmark$$
$$\neg\neg(A \lor \neg B) \checkmark$$
$$(A \leftrightarrow \neg B) \checkmark$$
$$(A \lor \neg B) \checkmark$$

Assignment Project Exam Help

https://powcoder.com

Therefore, contraries.

[Q p.30]

Add WeChat powcoder

4. Cannot both be true:

$$\neg (A \lor \neg B) \checkmark 
(\neg A \to \neg B) \checkmark 
\neg A 
\neg \neg B \checkmark 
B 
A 
× 
×$$

Cannot both be false:

$$\neg\neg(A \lor \neg B) \checkmark \\ \neg(\neg A \to \neg B) \checkmark \\ (A \lor \neg B) \checkmark \\ \neg A$$

Assignment Project Exam Help

Therefore types. Therefore types were der. com

[Q p.30]

Add WeChat powcoder

5. Cannot both be true:

$$(\neg A \land (A \to B)) \checkmark$$

$$\neg (\neg A \to (A \to B)) \checkmark$$

$$\neg A$$

$$(A \to B) \checkmark$$

$$\neg A$$

$$\neg (A \to B) \checkmark$$

$$A$$

$$\neg (A \to B) \checkmark$$

$$A$$

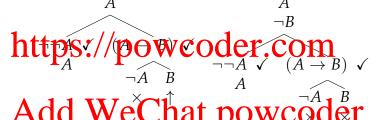
$$\neg B$$

$$\times$$

Can both be false, e.g. when *A* is T and *B* is T:

$$\neg(\neg A \land (A \to B)) \checkmark \\ \neg\neg(\neg A \to (A \to B)) \checkmark \\ (\neg A \to (A \to B)) \checkmark$$

Assignment Project-Exam Help



Therefore, contraries.

[Q p.30]

6. Can both be true, e.g. when *A* is T and *B* is F:

$$(A \to B) \leftrightarrow B \checkmark$$

$$\neg (A \to B) \checkmark$$

$$A$$

$$\neg B$$

$$(A \to B) \checkmark \neg (A \to B) \checkmark$$

$$B \qquad \neg B$$

$$\times \qquad A$$

$$\neg B$$

$$\uparrow$$

Therefore, jointly satisfiable.

[Q p.30]

[Contents]

#### **Answers 7.3.4.1**

1. Tautology:

$$\neg(A \to (B \to A)) \checkmark$$

$$A$$

$$\neg(B \to A) \checkmark$$

$$B$$

$$\neg A$$

[Q p.30]

2. Not a tautology. False when *A* is T and *B* is F:

$$\neg (A \to (A \to B)) \checkmark$$

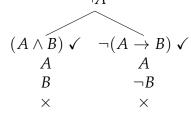
$$A \to A$$

$$\neg (A \to B) \checkmark$$

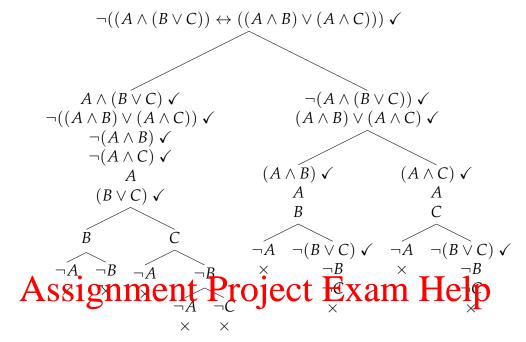
$$A \to B$$

Assignment Project Exam Help

3. Tautol Pritps: A/powcoder(com)  $((A \land B) \lor \neg (A \rightarrow B)) \checkmark$ Add WeChat powcoder [Q p.31]

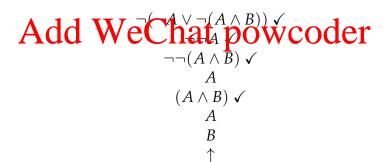


4. Tautology: [Q p.31]



https://powcoder.com

5. Not a tautology. False when A is T and B is T: [Q p.31]



6. Not a tautology. False when *A* is F and *B* is T: [Q p.31]

$$\neg(A \lor (\neg A \land \neg B)) \checkmark \\ \neg A \\ \neg(\neg A \land \neg B) \checkmark \\ \neg \neg A \checkmark \quad \neg \neg B \checkmark \\ A \qquad B \\ \times \qquad \uparrow$$

7. Tautology.

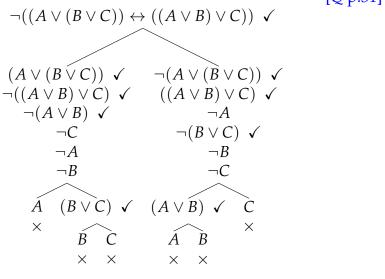
$$\neg((A \to B) \lor (A \land \neg B)) \checkmark \\ \neg(A \to B) \checkmark \\ \neg(A \land \neg B) \checkmark \\ A \\ \neg B \\ \hline \neg A \quad \neg B \checkmark \\ \times B \\ \times$$

8. Not a tautology. False when *A* is F and *B* is T:

[Q p.31]

 $\neg((B \land \neg A) \leftrightarrow (A \leftrightarrow B)) \checkmark$ 

[Q p.31]



10. Not a tautology. False when, e.g., *A* is T, *B* is T and *C* is F: [Q p.31]

$$\neg((A \land (B \lor C)) \leftrightarrow ((A \lor B) \land C)) \checkmark$$

$$(A \land (B \lor C)) \checkmark \qquad \neg(A \land (B \lor C)) \checkmark$$

$$\neg((A \lor B) \land C) \checkmark \qquad ((A \lor B) \land C) \checkmark$$

$$A \qquad (A \lor B) \checkmark \qquad C$$

$$\neg(A \lor B) \checkmark \qquad \neg C \qquad \neg A \qquad \neg(B \lor C) \checkmark$$

$$\neg A \qquad \qquad \neg B \qquad \qquad \neg B$$

$$\neg B \qquad \qquad B \qquad C \qquad A \qquad B \qquad \neg C$$

$$\times \qquad \uparrow \qquad \times \qquad \times \qquad \times$$

[Contents]

#### Assignment Project Exam Help Answers 7.3.5.1

1. Equivalent tps://powcoder.com [Q p.31]

## Add Wechat powcoder

2. Equivalent: [Q p.31]

$$\neg((P \to (Q \lor \neg Q)) \leftrightarrow (R \to R)) \checkmark$$

$$(P \to (Q \lor \neg Q)) \quad \neg(P \to (Q \lor \neg Q)) \checkmark$$

$$\neg(R \to R) \checkmark \qquad (R \to R)$$

$$R \qquad P$$

$$\neg R \qquad \qquad \neg(Q \lor \neg Q) \checkmark$$

$$\times \qquad \qquad \neg Q$$

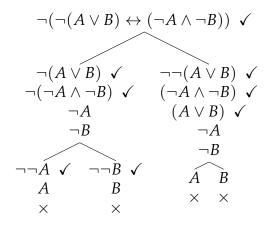
$$\neg \neg Q \checkmark$$

$$Q$$

$$\times$$

3. Equivalent:

[Q p.31]



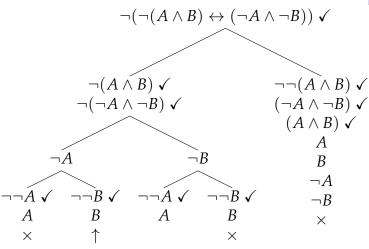
4. Not equivalent. Different truth values when, e.g., A is F and B is T: [Q p.31]

Assignment Project Exam Help

https://powcoder.com

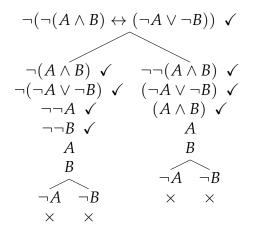
Add Wechat powceder

5. Not equivalent. Different truth values when, e.g., A is F and B is T: [Q p.31]



6. Equivalent.

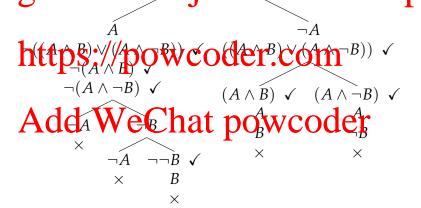
[Q p.31]

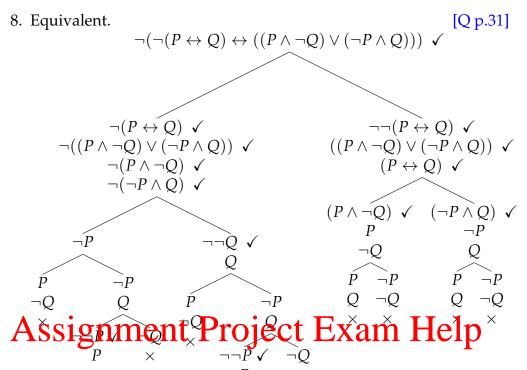


7. Equivalent.

[Q p.31]

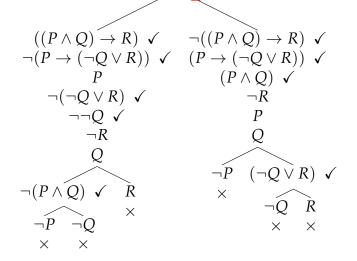
 $\neg (A \leftrightarrow ((A \land B) \lor (A \land \neg B))) \checkmark$ A ssignment Project Exam I





https://powcoder.com

9. Equivalent. [Q p.31] Add((WeChat(Powcoder



10. Not equivalent. Different truth values when *P* is T and *Q* is F:

 $\neg(P \leftrightarrow Q) \leftrightarrow (Q \land \neg P)) \checkmark$   $\neg(P \leftrightarrow Q) \checkmark \qquad \neg\neg(P \leftrightarrow Q) \checkmark$   $\neg(Q \land \neg P) \checkmark \qquad (Q \land \neg P) \checkmark$   $P \qquad \neg P \qquad Q$   $\neg Q \qquad Q \qquad \neg P$   $\neg Q \qquad Q \qquad \neg P$   $\neg Q \qquad Q \qquad P \qquad \neg P$   $\neg Q \qquad Q \qquad P \qquad \neg P$   $\neg Q \qquad Q \qquad P \qquad \neg P$   $\neg Q \qquad Q \qquad \neg P \checkmark \qquad Q \qquad \neg P$   $\neg Q \qquad \neg P \checkmark \qquad Q \qquad \neg P$   $\neg Q \qquad \neg P \checkmark \qquad Q \qquad \neg P$   $\Rightarrow \qquad P \qquad \times \qquad \times \qquad \times$ 

Assignment Project Exam Help

https://powcoder.com

Add WeChat powcoder

#### Chapter 8

### The Language of Monadic **Predicate Logic**

## Answers 8.2.1 ASSignment Project Exam Help

Glossary:

## the best powers of the problem of the best powers o

## e:A Jenny WeCha:t popy coder

Pluto is kite flying

*N*: is nice *m*: Mary

New York P: is a prime number n:

The Pacific Ocean *R*: is grumpy *p*: S: is smallT: is a planetV: is heavily populated seven (7) q: r: Rover

Steve

W: is winning t: two (2) A: is sailing  $\Upsilon$ : is tiny

#### **Translations:**

1. <i>Bp</i>	[Q p.32]
2. <i>Vn</i>	[Q p.32]
3. Nm	[Q p.32]

4. <i>Rj</i>	[Q p.32]
5. <i>Pq</i>	[Q p.32]
6. Tl	[Q p.32]
7. $Gb \wedge Gd$	[Q p.32]
8. $(Am \lor Ke) \rightarrow (Rb \land Rd)$	[Q p.32]
9. $\neg(Am \lor Km)$	[Q p.32]
10. $Ke \rightarrow Am$	[Q p.32]
11. $(Aj \lor Kj) \land \neg (Aj \land Kj)$	[Q p.32]
12. $\neg Am \rightarrow (\neg Kj \rightarrow Aj)$	[Q p.32]
<sup>13</sup> Assignment Project Exam 1	He <sup>[Q p.33]</sup>
14. $(Aj \lor Am) \rightarrow Ae$	[Qp.33]
15. $Am \leftrightarrow het{tps://powcoder.com}$	[Q p.33]
16. $Ws \rightarrow \neg Hm$	[Q p.33]
Add WeChat powcode	[Q p.33]
18. $Sc \land \neg Yc \land Cc$	[Q p.33]
19. $Kr \rightarrow \neg Pt$	[Q p.33]
20. $Hm \leftrightarrow \neg He$	[Q p.33]
	[Contents]

#### Answers 8.3.2

Cx: x is certain

#### Glossary:

	Ex:	x is certain $x$ is expensive	Wx:	<i>x</i> is red <i>x</i> is worthwhile	
	Fx:	x is fun	<i>i</i> :	Independence Hall	l
	Gx:	<i>x</i> is green	k:	Kermit	
	Hx:	x is heavy	<i>p</i> :	Oscar's piano	
	Px:	x is probable	s:	Spondulix	
Tra	anslations:				
1. 1	$Ri \to \exists x Rx$	£			[Q p.33]
2A 3.	$\forall xRx \rightarrow Rx$ $SS121$ $\neg \exists x (Gx \land x)$	iment Pr	oje	ct Exam F	Help [Q p.33]
4.	$\neg\neg\exists x(Gx)$	(Rx)		1	[Q p.33]
5 -	This can be	tps://pov	VCO Wave	<b>GET.COM</b> The most natural ir	ternretation
		*		ould also take it to r	-
				d things are not pree	
	(i) $\forall x (Rx)$	$(uu \lor v \in C)$	Hat	powcode	_
	` '	,	f it is red	d, then it is not greer	າ.")
		ivalently: $\neg \exists x (R)$		,	,
	("The	re does not exist a	nything	g which is both red a	nd green.")
	(ii) $\neg \forall x (F)$	$Rx \to Gx$ ) or equivariately	valently	$\forall : \exists x (Rx \land \neg Gx)$	[Q p.33]
6. \	$\forall x (Rx \to ($	$Hx \vee Ex))$			[Q p.33]
7. \	$\forall x((Rx \land \neg$	$\neg Hx) \to Ex$			[Q p.33]
(	("Pick anyt	hing at all: if it is r	red and	not heavy, then it is	
0 \	$\forall x (Rx \to R)$				expensive.")
ð. \		$\exists x (Gx \land \neg F)$	Hx)		expensive.") [Q p.33]
	$\forall x (Rx \to F)$	$\exists x (Gx \land \neg Hx) \land \exists x (Hx \rightarrow Hx) \land \neg \forall x (Hx \rightarrow Hx) \land x (Hx $			
9. \	•		Rx)		[Q p.33]

Rx: x is red

12.	$(Gk \wedge Rk) \to \neg\neg\exists x (Gx \wedge Rx)$	[Q p.34]
13.	$Hp \wedge \neg (Rp \vee Ep)$	[Q p.34]
14.	$(Hs \land Es \land \forall x(Ex \to Rx) \land \forall x(Hx \to Gx)) \to (Rs \land Gs)$	[Q p.34]
15.	$Hk \to \exists x (Gx \land Hx)$	[Q p.34]
16.	$\forall x Fx \to \neg \exists x Wx$	[Q p.34]
17.	$\exists x Fx \wedge \exists x Wx \wedge \neg \exists x (Fx \wedge Wx)$	[Q p.34]
18.	$\neg \exists x C x \to \neg \exists x P x$	[Q p.34]
19.	$\exists x P x \land \exists x \neg P x \land \neg \exists x C x$	[Q p.34]
20.	$\forall x(Cx \to Px)$	[Q p.34]

## Assignment Project Exam Help

#### Answers 8.3.5

## Glossary: https://powcoder.com

Ax:	x can stay	Rx:	<i>x</i> is telling the truth
<i>Bx</i> :	AddnWeChat	100	weoder
Cx:	<i>x</i> works at this company	Tx:	<i>x</i> is in trouble
<i>Fx</i> :	x is a leaf	Ux:	<i>x</i> is laughing
Gx:	<i>x</i> is grey	<i>Yx</i> :	<i>x</i> is lying
<i>Hx</i> :	x is happy	g:	Gary
Lx:	<i>x</i> is laughing	s:	the sky
Ox:	<i>x</i> is in this room	t:	Stephanie
Px:	x is a person		_

#### **Translations:**

1. $\forall x (Px \to Hx)$	[Q p.34]
$2. \ \exists x (Px \land Sx)$	[Q p.34]
3. $\neg \exists x (Px \land Hx \land Sx)$	[Q p.34]
$4. \ \exists x (Px \land Sx) \rightarrow \neg \forall x (Px \rightarrow Hx)$	[Q p.34]

```
5. \forall x (Px \rightarrow (\neg Hx \rightarrow \neg Lx))
              or \forall x((Px \land Lx) \rightarrow Hx)
              or \neg \exists x (Px \land Lx \land \neg Hx)
                                                                                                                                                                                                                                              [Q p.34]
    6. Lg \rightarrow \exists x (Px \land Hx)
                                                                                                                                                                                                                                              [Q p.34]
    7. \forall x((Px \land Lx) \rightarrow Hx)
                                                                                                                                                                                                                                              [Q p.34]
   8. Lg \rightarrow \forall x (Px \rightarrow Lx)
                                                                                                                                                                                                                                             [Q p.35]
   9. \exists x (Px \land Sx) \land \neg \forall x (Px \rightarrow Sx) \land \neg Sg
                                                                                                                                                                                                                                              [Q p.35]
10. \neg \forall x (Px \rightarrow Sx) \rightarrow \neg Hg
                                                                                                                                                                                                                                              [Q p.35]
11. \forall x(Fx \rightarrow Bx) \land Gs
                                                                                                                                                                                                                                              [Q p.35]
12. \exists x (Fx \land Bx) \land \neg \forall x (Fx \rightarrow Bx)
                                                                                                                                                                                                                                              [Q p.35]
1Assignment Project Exam Help.35]
14. This could be saying either of two things:
             (i) that the one stay was to order the order of the order
              \forall x((Ax \land Fx) \rightarrow \underline{Bx}) \text{ or } \forall \underline{x}(Fx \rightarrow (Ax \rightarrow Bx))
              (ii) that the day the state hatty powered er
              \forall x(Ax \rightarrow (Fx \land Bx))
                                                                                                                                                                                                                                              [Q p.35]
15. \neg Hg \rightarrow \forall x (Px \rightarrow Tx)
                                                                                                                                                                                                                                              [Q p.35]
16. \neg Hg \rightarrow \forall x((Px \land Cx) \rightarrow Tx)
                                                                                                                                                                                                                                              [Q p.35]
17. Rt \rightarrow \exists x (Px \land Yx)
                                                                                                                                                                                                                                              [Q p.35]
18. \neg \exists x (Px \land Yx) \rightarrow Rt
                                                                                                                                                                                                                                             [Q p.35]
19. Yt \vee (\neg \exists x (Px \wedge Rx) \wedge \forall x (Px \rightarrow Tx))
                                                                                                                                                                                                                                              [Q p.35]
20. Yg \rightarrow \neg \forall x ((Px \land Ox) \rightarrow Rx)
                                                                                                                                                                                                                                              [Q p.35]
                                                                                                                                                                                                                                    [Contents]
```

#### **Answers 8.4.3.1**

1. Main operator:  $\forall$ 

[Q p.35]

Step	Wff constructed at this step	from steps/by clause:
1.	Fx	/ (3i)
2.	Gx	/ (3i)
	$(Fx \rightarrow Gx)$	1, 2 / (3ii) line 5
4.	$\forall x(Fx \to Gx)$	3 / (3ii) line 7

2. Main operator:  $\forall$ 

[Q p.35]

Step	Wff constructed at this step	from steps/by clause:
1.	Gx	/ (3i)
2.	$\neg Gx$	1 / (3ii) line 1
3.	$\forall x \neg Gx$	2 / (3ii) line 7

## Assignment Project Exam Help. 35. Main operator: In Project Exam Help. 35. Mai

Step	Wff constructed at this step	from steps/by clause:
1.	<b>k</b> ttps://powcod	(4 <sup>3</sup> i) com
2.	rextps.//powcod	(3i) COIII
3.	$(Fx \wedge Gx)$	1, 2 / (3ii) line 2
4.	$\exists x (Ex \land Gx)$	3 / (3ii) line 8
5.	Add WeChat	oowcoder

4. Main operator: ∧

[Q p.35]

Step	Wff constructed at this step	from steps/by clause:
1.	Fa	/ (3i)
2.	Fx	/ (3i)
3.	$\neg Fx$	2/ (3ii) line 1
4.	$\exists x \neg Fx$	3/ (3ii) line 8
5.	$\neg \exists x \neg Fx$	4/ (3ii) line 1
6.	$(Fa \land \neg \exists x \neg Fx)$	1,5/ (3ii) line 2

5. Main operator:  $\forall$ 

IO.	- 25
ĮŲ	[c.50]

Step	Wff constructed at this step	from steps/by clause:	
1.	Fx	/ (3i)	
2.	Gx	/ (3i)	
3.	Gy	/ (3i)	
4.	$(Gx \rightarrow Gy)$	2, 3 / (3ii) line 5	
5.	$\exists y(Gx \to Gy)$	4 / (3ii) line 8	
6.	$Fx \wedge \exists y (Gx \rightarrow Gy)$	1, 5 / (3ii) line 2	
7.	$\forall x (Fx \land \exists y (Gx \rightarrow Gy))$	6 / (3ii) line 7	

6. Main operator: ∧

[Q p.36]

	Step	Wff constructed at this step	from steps/by clause:
	1.	Fx	/ (3i)
	2.	Gx	/ (3i)
A	3. <b>S</b> S1	gnment Projec	1, 27 (3ii) line 5 Help
	5.	Fa	/ (3i)
	6.	$(\forall x(Fx \to Gx) \land Fa)$	4, 5 / (3ii) line 2
•		https://powcod	der.com

7. Main operator:  $\rightarrow$ 

[Q p.36]

Step	Wff constructed at this step	from steps/by clause:
1.	Add WeChat	powcoder
2.	Fb	/ (3i)
3.	$\neg Fa$	1 / (3ii) line 1
4.	$\neg Fb$	2 / (3ii) line 1
5.	$(\neg Fa \wedge \neg Fb)$	3, 4 / (3ii) line 2
6.	Fx	/ (3i)
7.	$\neg Fx$	6 / (3ii) line 1
8.	$\forall x \neg Fx$	7 / (3ii) line 7
9.	$((\neg Fa \land \neg Fb) \to \forall x \neg Fx)$	5, 8 / (3ii) line 5

8. Main operator:  $\forall$ 

[Q p.36]

Step	Wff constructed at this step	from steps/by clause:
1.	Fx	/ (3i)
2.	Fy	/ (3i)
3.	$(Fx \wedge Fy)$	1, 2 / (3ii) line 2
4.	Gx	/ (3i)
5.	$((Fx \wedge Fy) \rightarrow Gx)$	3, 4 / (3ii) line 5
6.	$\forall y((Fx \land Fy) \rightarrow Gx)$	5 / (3ii) line 7
7.	$\forall x \forall y ((Fx \land Fy) \rightarrow Gx)$	6 / (3ii) line 7

9. Main operator:  $\forall$ 

[Q p.36]

	Step	Wff constructed at this step	from steps/by clause:	
	1.	Fx	/ (3i)	
	2.	Fy	/ (3i)	
Λ	3.	∀yFy ont Drois	2/ <del>(3</del> ii) line 7	
$\mathcal{H}$	<b>LASI</b>	ghment Projec	L, 37 & idelle 5 FICI	)
	5.	$\forall x(Fx \rightarrow \forall yFy)$	4 / (3ii) line 7	•

10. Main ohttps://powcoder.com

[Q p.36]

Step	Wff constructed at this step	from steps/by clause:
1. 2.	Add WeChat	oowgoder
3.	Fy	/ (3i)
4.	$\forall y F y$	3 / (3ii) line 7
5.	$(\forall x Fx \to \forall y Fy)$	2, 4 / (3ii) line 5

[Contents]

#### **Answers 8.4.5.1**

Free variables are underlined:

1. $T\underline{x} \wedge F\underline{x}$ Open	[Q p.36]
2. $T\underline{x} \wedge T\underline{y}$ Open	[Q p.36]
3. $\exists x Tx \land \exists x Fx$ Closed	[Q p.36]
4. $\exists x Tx \land \forall y F\underline{x}$ Open	[Q p.36]

5. $\exists x Tx \land F\underline{x}$ Open	[Q p.36]
6. $\exists x (Tx \land Fx)$ Closed	[Q p.36]
7. $\forall y \exists x Ty$ Closed	[Q p.36]
8. $\exists x(\forall xTx \rightarrow \exists yFx)$ Closed	[Q p.36]
9. $\exists y \forall x Tx \rightarrow \exists y F\underline{x}$ Open	[Q p.36]
10. $\forall x(\exists xTx \land Fx)$ Closed	[Q p.36]
11. $\forall x \exists x Tx \land F\underline{x}$ Open	[Q p.36]
12. $\exists x T \underline{y}$ Open	[Q p.36]
13. $\forall xTx \rightarrow \exists xFx$ Closed	[Q p.36]
Assignment Project Exam F	[Qp.36]
15. $\forall x Fx \land G\underline{x}$ Open	[Q p.36]
16. $\forall x \forall y F_x \rightarrow Gy$ Open https://powcoder.com	[Q p.37]
17. $\forall x \forall y (Fx \rightarrow \forall x Gy)$ Closed	[Q p.37]
Add WeChat powcoder	[Q p.37]
19. $\exists yGy \land \forall x(Fx \rightarrow G\underline{y})$ Open	[Q p.37]
20. $\forall x((Fx \to \exists xGx) \land Gx)$ Closed	[Q p.37]
	[Contents]

## **Chapter 9**

## **Semantics of Monadic Predicate Logic**

•	newers ASS12	nmer	it Pro	ject Exam I	Help
	1. (i) True				[Q p.38]
	2. (i) Fals	t(ii) True/	/(iii) False	coder.com	[Q p.38]
	3. (i) False	(ii) True	(iii) False		[Q p.38]
	4. (i) True	(ji) Tjue	(iii) False	at powcode	[Q p.38]
	5. (i) True	(ii) True	(iii) True	at poweode	[Q p.39]
	6. (i) False	(ii) False	(iii) False		[Q p.39]
					[Contents]

#### Answers 9.2.1

Model 1:	Model 2:	
(i) False	(i) True	
(ii) True	(ii) False	
(iii) True	(iii) False	
(iv) True	(iv) True	
(v) True	(v) True	[Questions p.39]

Mode	el 3:	Model 5:	
(i) T	True	(i) False	
(ii) ]	False	(ii) True	
(iii) ]	False	(iii) True	
(iv)	True	(iv) True	
(v) T	True	(v) True	
Mode	el 4:	Model 6:	
(i) ]	False	(i) True	
(ii)	True	(ii) False	
(iii)	True	(iii) True	
(iv)		. ,	uestions p.39]
Assignment Project (Exam Helports)			
Answers 9.3.1 //powcoder.com			
Allowe	https://powcod	ler.com	
1. (1)	(Fu /\ Gu)		[Q p.39]
$A_{ii} \overset{\text{(ii)}}{\leftarrow} \overset{(Fb \land Ga)}{\leftarrow} WeChat powcoder$			[Q p.39]
2. (i)	$\forall y (1 u \rightarrow 0 y)$	owedae	[Q p.39]
(ii) \	$\forall y (Fb \to Gy)$		[Q p.39]
3. (i)	$\forall x(Fx \to Gx) \land Fa$		[Q p.39]
(ii) \	$\forall x (Fx \to Gx) \land Fb$		[Q p.40]
4. (i) \	$\forall x (Fx \wedge Ga)$		[Q p.40]
(ii)	$\forall x (Fx \wedge Ga)$		[Q p.40]
	( $x$ ), i.e. $\forall x(Fx \land Ga)$ , contains n ame $\underline{a}$ , $\alpha(\underline{a}/x)$ is just $\alpha(x)$ . For w		
$x$ with $\underline{a}$ ; if there are no free occurrences, nothing gets replaced.			
5. (i)	$\exists x (Gx \to Ga)$		[Q p.40]
(ii)	$\exists x (Gx \to Gb)$		[Q p.40]
6. (i)	$\exists y (\forall x (Fx \to Fy) \lor Fa)$		[Q p.40]
(ii)	$\exists y (\forall x (Fx \to Fy) \lor Fb)$		[Q p.40]

#### **Answers 9.4.3**

1. (i) False	[Q p.40]
(ii) True	[Q p.40]
(iii) True	[Q p.40]
(iv) False	[Q p.40]
(v) True	[Q p.40]
(vi) True	[Q p.40]
2. (i) (a) False	[Q p.40]
(b) True	[Q p.41]
Assignment Project Exam H	elp <sup>.41</sup> ]
(b) Faise	[Q p.41]
(iii) (a) True	[Q p.41]
https://powcoder.com	[Q p.41]
3. (i) True	[Q p.41]
(ii) Faladd WeChat powcoder	[Q p.41]
(iii) True	[Q p.41]
(iv) True	[Q p.41]
(v) True	[Q p.41]
(vi) False	[Q p.41]
4. (i) (a) Domain: {1,2,3,}	
Extensions: $F : \{1,2\}$ $G : \{1,2,3\}$	
(b) Domain: $\{1, 2, 3,\}$ Extensions: $F : \{1, 2\}  G : \{1\}$	[Q p.42]
(ii) (a) No such model. For the formula to be true on	[Q p.42]

(ii) (a) No such model. For the formula to be true on a model, it would have to be the case that all members of the (non-empty) domain were in the extension of *F* (so that the first conjunct were true) and also that a certain member of the domain were not in the extension of *F* (so that the second conjunct were true).

```
(b) Domain: \{1, 2, 3, \dots\}
          Referent of a: 2
          Extension of F : \{2, 4, 6, ...\}
                                                               [Q p.42]
 (iii) (a) Domain: \{1, 2, 3, \dots\}
          Referent of a:1
          Extension of F : \{2, 4, 6, ...\}
      (b) Domain: \{1, 2, 3, \dots\}
          Referent of a:1
          Extension of F : \{1, 3, 5, ...\}
                                                               [Q p.42]
 (iv) (a) Domain: \{1, 2, 3, \dots\}
          Extensions: F : \{1, 2, 3, ...\} G : \{2, 4, 6, ...\}
      (b) Domain: \{1, 2, 3, \dots\}
          Extensions: F : \{1, 3, 5, ...\} G : \{2, 4, 6, ...\}
                                                              [Q p.42]
 (v) (a) Domain: \{1, 2, 3, \dots\}
         Extension of F D1,35
 ssignment Project Lyane
          would have to be the case that, in that model, some member
          of the domain were both in the extension of F and not in the
       https://powcoder.com
                                                               [Q p.42]
 (vi) (a) Domain: \{1, 2, 3, \dots\}
          Extensions: F : \{1, 3, 5, ...\} G : \{2, 4, 6, ...\}
      (bApprain: WæC. hat powcoder Extensions: F: \{1, 3, 5, ...\} G: \emptyset
                                                               [Q p.42]
(vii) (a) Domain: \{1, 2, 3, \dots\}
          Extension of F : \{1, 3, 5, ...\}
      (b) No such model. For the formula to be false on a model,
          it would have to be the case that all members of the (non-
          empty) domain were in the extension of F (to make the an-
          tecedent true) and that no members of the domain were in
          the extension of F (to make the consequent false). [Q p.42]
(viii) (a) No such model. For the formula to be true on a model,
          it would have to be the case that, in that model, a single
          member of the domain were both in the extension of F and
          not in the extension of F.
      (b) Domain: \{1, 2, 3, \dots\}
          Extension of F : \{1, 3, 5, ...\}
                                                               [Q p.42]
 (ix) (a) Domain: \{1, 2, 3, \dots\}
```

Extension of  $F : \{1, 3, 5, ...\}$ 

	(b)	Domain: $\{1,2,3,\dots\}$ Extension of $F:\emptyset$	[Q p.42]
(x)	(a)	Domain: {1,2,3,}	121
		Extension of $F : \{1, 3, 5,\}$	
	(b)	No such model. For the formula to be false or	a model,
		it would have to be the case that, in that mode	l, a single
		member of the domain were both in the extensio	n of F and
		not in the extension of <i>F</i> .	[Q p.42]
(xi)	(a)	Domain: {1,2,3,}	
		Extensions: $F: \{1\}$ $G: \{2\}$	
	(h)	Domain: {1,2,3,}	
	(0)	Extensions: $F: \{1\}$ $G: \emptyset$	[Q p.42]
(xii)	(a)	Domain: {1,2,3,}	[ × [ · ·]
(7122)	(01)	Extensions: $F : \{1\}$ $G : \{1, 2, 3,\}$	_
Ass	ije	Extensions: F: {1} G: {1,2,3}}  Shape of the project Exam H	eln
	(b)	Domain: {1,2,3,}	UIP
	` /	Extensions: $F : \{1\}$ $G : \{1\}$	[Q p.42]
(xiii)	(a)	ptps://powcoder.com	_
	_	Referents: a -1	
		Extensions: $F: \{1\}$	
	/	Add We Chat powceder a	
	(b)		
		would have to be that all members of the doma	
		the extension of $F$ , but the referent of $a$ was not.	[Q p.42]
(xiv)	(a)	Domain: {1,2,3,}	
		Referents: a:1	
		Extensions: $F : \{1, 2, 3,\}$	
	(b)	Domain: {1,2,3,}	
	(~)	Referents: <i>a</i> : 2	
		Extensions: $F: \{1\}$	[Q p.42]
(xv)	(a)	Domain: {1,2}	
()	()	Referents: $a:1$ $b:2$	
		Extensions: $F: \{1,2\}$	
	(b)	Domain: [1.2]	
	(D)	Domain: $\{1,2\}$ Referents: $a:1$ $b:2$	
		Extensions: $U: V: Z$	[Q p.42]
		LACTIOIOTIO, 1 . \1\	[Q p.44]

- (xvi) (a) Domain:  $\{1, 2, 3, ...\}$ Extensions:  $F : \{1, 3, 5, ...\}$   $G : \{2, 4, 6, ...\}$ 
  - (b) Domain:  $\{1, 2, 3, ...\}$  Extensions:  $F : \{1\}$   $G : \{2\}$  [Q p.42]
- (xvii) (a) Domain:  $\{1, 2, 3, ...\}$ Extensions:  $F : \{1\}$   $G : \emptyset$ 
  - (b) Domain:  $\{1, 2, 3, \dots\}$ Extensions:  $F : \emptyset \quad G : \emptyset$ [Q p.42]
- (xviii) (a) No such model. For the formula to be true on a model, it would have to be that each member of the domain was both in the extension of *F* and also not in the extension of *F*.
  - (b) Domain:  $\{1, 2, 3, \dots\}$

# Ssignment Project Exam Help Extensions: $F: \mathcal{P}$ Extensions: $F: \mathcal{O} \subseteq G: \{1\}$

# (b) ttps: $\{1, p, o, w \text{ coder.com}\}$ Extensions: $F: \{1, 2, 3, ...\}$ $G: \emptyset$

[Q p.42]

- (xx) (a) Domain (1,2,3) hat powcoder
  - (b) Domain:  $\{1, 2, 3, \dots\}$ Extensions:  $F: \{1, 2, 3, \dots\}$   $G: \emptyset$ [Q p.42]
- 5. (i) True.

Suppose there are no F's. Then, whatever in the domain d (a new name) refers to, Fd is false—so  $Fd \rightarrow Gd$  is true (because its antecedent is false). So  $\forall x(Fx \rightarrow Gx)$  is *true* when there are no F's. [Q p.42]

(ii) No.

If there are no F's,  $\forall x(Fx \rightarrow Gx)$  is true (previous question), but  $\exists x (Fx \land Gx)$  is false. [Q p.42]

[Contents]

#### Answers 9.5.1

1. Countermodel:

Domain: {1,2}

Extensions:  $F : \{1\}$   $G : \{2\}$  [Q p.43]

- 2. No countermodel. For the premise to be true, there must be at least one object in the domain which is in the extension of *F* and is also in the extension of *G*. If this is so, then any such object is *a fortiori* in the extension of *F*—making the left conjunct of the conclusion true—and in the extension of *G*—making the right conjunct of the conclusion true: hence the conclusion is true. [Q p.43]
- 3. Countermodel:

Domain: {1,2}

Extensions:  $F : \{2\}$   $G : \{1\}$  [Q p.43]

A Solution Metal of the first premise to K and the extension of F must be a subset of the extension of G. For the second premise to be true, the extension of G must be a subset of the extension of H. It follows that the extension of F is a subset of the extension of H—and this makes the conclusion true. [Q p.43]

5. Countermodel:

Domair  $A\{t_{i}\}$  We Chat powcoder Extensions:  $F:\{1\}$   $G:\{1,2\}$   $H:\{1,2,3\}$ 

[Q p.43]

[Contents]

## Chapter 10

## **Trees for Monadic Predicate Logic**

#### **Answers 10.2.2**

```
Assignment Project Exam Help
```

https://powcoder.com

Logical truth. [Q p.44]

# Add WeChat powcoder $\neg (\exists x Fx \rightarrow \neg \forall x \neg Fx) \checkmark$

(ii) 
$$\neg(\exists x Fx \to \neg \forall x \neg Fx) \checkmark \\ \exists x Fx \checkmark a \\ \neg \neg \forall x \neg Fx \checkmark \\ \forall x \neg Fx \setminus a \\ Fa \\ \neg Fa \\ \times$$

Logical truth. [Q p.44]

(iii) 
$$\neg \forall x ((Fx \land \neg Gx) \to \exists x Gx) \checkmark \\ \exists x \neg ((Fx \land \neg Gx) \to \exists x Gx) \checkmark a \\ \neg ((Fa \land \neg Ga) \to \exists x Gx) \checkmark \\ Fa \land \neg Ga \checkmark \\ \neg \exists x Gx \checkmark \\ Fa \\ \neg Ga \\ \forall x \neg Gx \setminus a \checkmark \\ \neg Ga \\ \uparrow$$

Not a logical truth. Countermodel:

Domain: {1}

Extensions:  $F: \{1\}$   $G: \emptyset$  [Q p.44]

[Q p.44]

# Assignment Project August Help $\begin{array}{c} A_{ssignment} & P_{ssignment} & P_{ssig$

## https://powcoder.com

Add WeChat powcoder

(v) 
$$\neg((Fa \land (Fb \land Fc)) \rightarrow \forall xFx) \checkmark$$

$$Fa \land (Fb \land Fc) \checkmark$$

$$\neg \forall xFx \checkmark$$

$$Fa$$

$$(Fb \land Fc) \checkmark$$

$$Fb$$

$$Fc$$

$$\exists x \neg Fx \checkmark d$$

$$\neg Fd \checkmark$$

Not a logical truth. Countermodel:

Domain:  $\{1, 2, 3, 4\}$ 

Extension of  $F : \{1, 2, 3\}$  [Q p.44]

(vi) 
$$\neg(\exists xFx \land \exists x\neg Fx) \checkmark$$
$$\neg\exists xFx \checkmark \quad \neg\exists x\neg Fx \checkmark$$
$$\forall x\neg Fx \setminus a \quad \forall x\neg \neg Fx \setminus a$$
$$\neg Fa \quad \neg \neg Fa \checkmark$$
$$\uparrow \qquad Fa$$

Not a logical truth. Countermodel:

Domain: {1}

Extension of  $F : \emptyset$ [Q p.44]

(vii) 
$$\neg \exists x (Fx \to \forall y Fy) \checkmark \\
\forall x \neg (Fx \to \forall y Fy) \setminus ab \\
\neg (Fa \to \forall y Fy) \checkmark$$

#### Assignment Pro Exam Help

 $\exists y \neg Fy \checkmark b$ https://poweoder.com

Add WeChat powcoder

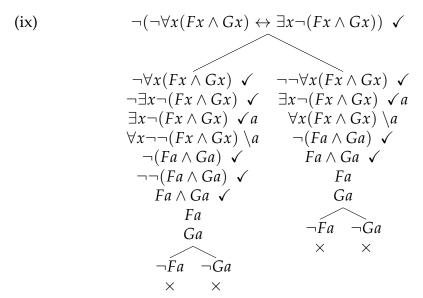
(viii)  $\neg(\forall x(Fx \to Gx) \to (Fa \to Ga)) \checkmark$  $\forall x(Fx \to Gx) \setminus a$  $\neg(Fa \rightarrow Ga) \checkmark$ Fa  $\neg Ga$  $Fa \rightarrow Ga \checkmark$ 

ƒa Ĝa X X

Logical truth.

[Q p.44]

[Q p.44]



Assignment Project Exam Help

(x) 
$$\neg(\neg \exists x (Fx \land Gx) \leftrightarrow \forall x (\neg Fx \land \neg Gx)) \checkmark$$

$$https://powcoder.com$$

$$\neg \exists x (Fx \land Gx) \checkmark \qquad \neg \neg \exists x (Fx \land Gx) \checkmark$$

$$\neg \forall x (\neg Fx \land \neg Gx) \checkmark \qquad \forall x (\neg Fx \land \neg Gx) \land a$$

$$\neg \forall x (\neg Fx \land \neg Gx) \checkmark \qquad \forall x (\neg Fx \land \neg Gx) \land a$$

$$\exists x \neg (\neg Fx \land \neg Gx) \checkmark \qquad Fa \land Ga \checkmark$$

$$\neg (\neg Fa \land \neg Ga) \checkmark \qquad Ga$$

$$\neg Fa \land \neg Ga \checkmark \qquad \neg Fa$$

 $\neg Fa \quad \neg Ga \quad \neg Fa \quad \neg Ga$   $\times \quad \uparrow \quad \times$ rical truth. Countermodal:

Ga

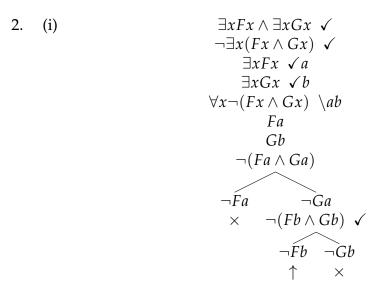
Not a logical truth. Countermodel:

Fa

Domain: {1}

Extension of  $F: \{1\}$   $G: \emptyset$  [Q p.44]

 $\neg Ga$ 



Invalid. Countermodel:

#### Domain: {1,2} ssignment Project Exam Help.441

(ii) https://pow.com
$$\exists y \neg \exists x (Fx \rightarrow Gy) \checkmark b$$

$$\exists y \neg \exists x (Fx \rightarrow Gy) \lor b$$

$$\forall y (Fa \rightarrow Gy) \lor b$$

$$\forall y (Fa \rightarrow Gy) \lor b$$

$$\forall x \neg (Fx \rightarrow Gb) \lor a$$

$$\neg (Fa \rightarrow Gb) \checkmark$$

$$\lor X$$
Valid
(iii) https://pow.com
$$\forall x \neg (Fx \rightarrow Gb) \checkmark$$

$$\lor X$$

[Q p.44] Valid.

(iii) 
$$Fa \rightarrow \forall xGx \checkmark \\ \neg \forall x(Fa \rightarrow Gx) \checkmark$$

$$\exists x \neg (Fa \rightarrow Gx) \checkmark b \quad \exists x \neg (Fa \rightarrow Gx) \checkmark b$$

$$\neg (Fa \rightarrow Gb) \checkmark \quad \neg (Fa \rightarrow Gb) \checkmark$$

$$Fa \qquad Fa \qquad Fa$$

$$\neg Gb \qquad \neg Gb \qquad \\ \times \qquad Gb$$

$$\times$$

Valid. [Q p.45]

(iv) 
$$Fa \to \forall xGx \checkmark \\ \neg \exists x(Fa \to Gx) \checkmark \\ \forall x \neg (Fa \to Gx) \setminus a$$

## Assignment Profeçata Exam Help

https://poweoder.com

validd WeChat powcoder [Qp.45]

 $\neg Ga$ 

Invalid. Countermodel:

Domain: {1,2}

Extensions:  $F : \{2\}$   $G : \{1\}$  [Q p.45]

[Q p.45] Valid.

 $\forall x(Fx \to Gx) \setminus a$ (vii)

### Assignment Project Exam Help $Fa \rightarrow Ga \checkmark$

https://powcoder.com

Valid. [Q p.45]

Add WeChat powcoder  $\neg \forall x (Fx \forall Gx) \checkmark$ (viii)  $\neg \exists x (\neg Fx \land \neg Gx) \checkmark$ 

$$\neg\exists x(\neg Fx \land \neg Gx) \lor \exists x\neg(Fx \lor Gx) \lor a$$

$$\forall x\neg(Fx \lor Gx) \lor a$$

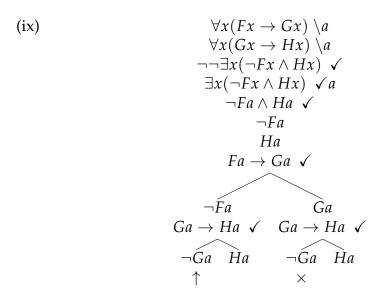
$$\neg(Fa \lor Ga) \lor \neg Fa$$

$$\neg Ga$$

$$\neg(\neg Fa \land \neg Ga) \lor \neg Fa \lor Ga$$

$$\Rightarrow Ga$$

Valid. [Q p.45]



Invalid. Countermodel:

# Assignimient Project Exam Help, 45]

# (x) https://powerements.com $\exists x (Fx \land Gx) \checkmark a$

# Add WeChat powcoder

Fa∨Ga ✓ Fa Ga

Invalid. Countermodel:

Domain: {1}

Extensions:  $F : \{1\}$   $G : \{1\}$ 

[Q p.45]

[Contents]

#### **Answers 10.3.8**

```
1. Dx: x is a dog
Mx: x is a mammal
Ax: x is an animal

\forall x(Dx \to Mx) \\
\forall x(Mx \to Ax) \\
\therefore \forall x(Dx \to Ax)

\forall x(Dx \to Mx) \setminus a \\
\forall x(Mx \to Ax) \setminus a \\
\neg \forall x(Dx \to Ax) \checkmark \\
\exists x \neg (Dx \to Ax) \checkmark a \\
\neg (Da \to Aa) \checkmark Da
```

Assignment Project Exam Help

 $\neg Aa$ 

https://powcoder.com

Valid. Add WeChat powcoder [Q p.45]

2. Fx: x is frozen Cx: x is cold  $\forall xFx \rightarrow \forall xCx$   $\therefore \forall x(Fx \rightarrow Cx)$ 

$$\forall xFx \rightarrow \forall xCx \checkmark$$

$$\neg \forall x(Fx \rightarrow Cx) \checkmark$$

$$\exists x \neg (Fx \rightarrow Cx) \checkmark a$$

$$\neg (Fa \rightarrow Ca) \checkmark \neg (Fa \rightarrow Ca) \checkmark$$

$$Fa \qquad Fa$$

$$\neg Ca \qquad \neg Ca$$

$$\exists x \neg Fx \checkmark b \qquad Ca$$

$$\neg Fb \qquad \times$$

# Assignment Project Exam Help

Domain: {1,2}

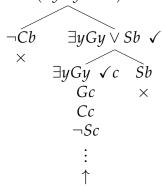
Extensions: F: {1}//powcoder.com

[Q p.45]

## Add WeChat powcoder

```
3. Cx: x is conscious
    Gx: x is a divine being
    Sx: x has a sonic screwdriver
    \forall x(Cx \rightarrow (\exists yGy \lor Sx))
    \neg \exists x S x
    \therefore \neg \forall x C x
                           \neg \exists x Sx \checkmark
                                       \neg\neg\forall xCx \checkmark
                                        \forall xCx \setminus abc
                                       \forall x \neg Sx \setminus abc
                                              Ca
                                             \neg Sa
                                Ca \rightarrow (\exists yGy \vee Sa) \checkmark
Assignmen
```

ct Exam Help



Invalid. Countermodel:

Domain:  $\{1, 2, 3, ...\}$ 

Extensions:  $C : \{1, 2, 3, ...\}$   $G : \{2, 3, 4, ...\}$   $S : \emptyset$ [Q p.45]

```
4. Cx: x is a cow
   Sx: x is a scientist
   Fx: x can fly
   \forall x(Cx \rightarrow Sx)
   \neg \exists x (Sx \land Fx)
   \therefore \neg \exists x (Cx \land Fx)
                               \forall x(Cx \to Sx) \setminus a
                               \neg \exists x (Sx \land Fx) \checkmark
                               \neg\neg\exists x(Cx\wedge Fx) \checkmark
                                \exists x (Cx \land Fx) \checkmark a
                               \forall x \neg (Sx \wedge Fx) \setminus a
                                   Ca ∧ Fa ✓
                                        Ca
                                        Fa
                                   Ca → Sa ✓
                                          ect Exam Help
Assignment Proj
                                       \neg (Sa \wedge Fa) \checkmark
           https://powcoderacom
   Valid.
           Add WeChat powcoder
                                                                          [Q p.45]
```

```
5. Px: x is a person
   Hx: x is here
   Sx:
         x is smoking
   \exists x ((Px \land Hx) \land \neg Sx)
   \therefore \neg \forall x ((Px \land Hx) \rightarrow Sx)
                           \exists x((Px \land Hx) \land \neg Sx) \checkmark a
                          \neg\neg\forall x((Px\wedge Hx)\to Sx) \checkmark
                           (Pa \wedge Ha) \wedge \neg Sa \checkmark
                                  (Pa \wedge Ha) \checkmark
                                       \neg Sa
                                        Pa
                                       Ha
                               (Pa \wedge Ha) \rightarrow Sa \checkmark
Assignment Project Exam Help
                             \neg \widehat{Pa} \quad \neg Ha
   Valid. https://powcoder.com
                                                                      [Q p.46]
          Add WeChat powcoder
```

6. Cx: x is a coward

Rx: x rocks up Sx: x will shake *c*: Catwoman Superman s:

$$Rs \to \forall x (Cx \to Sx)$$
$$\neg Cc$$

$$\therefore \neg Sc$$

$$Rs \to \forall x (Cx \to Sx) \checkmark \\ \neg Cc \\ \neg \neg Sc \checkmark \\ Sc$$

# Assignment ProjectsEx am Help

# https://powcoder.com ¬Cs Ss ¬Cs Ss Invalid Add WeChat powcoder

Domain: {1,2}

Referents: c:1 s:2

Extensions:  $C : \emptyset \quad R : \emptyset \quad S : \{1\}$ [Q p.46] 7. Bx: x is blue Cx: x a car

Dx: x is defective

Rx: x is red

$$\forall x(Cx \to (Rx \lor Bx))$$

$$\forall x((Cx \land Rx) \to Dx)$$

$$\exists x(Bx \land Cx \land \neg Dx)$$

$$\therefore \exists x(Cx \land Dx) \land \exists x(Cx \land \neg Dx)$$

$$\forall x(Cx \to (Rx \lor Bx)) \land a$$

$$\forall x((Cx \land Rx) \to Dx) \land a$$

$$\exists x(Bx \land Cx \land \neg Dx) \lor a$$

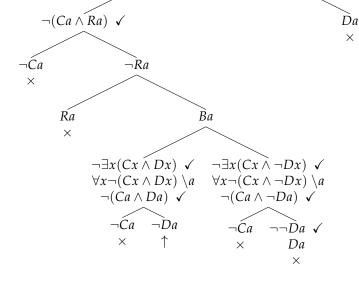
$$\neg (\exists x(Cx \land Dx) \land \exists x(Cx \land \neg Dx)) \lor a$$

$$Ba \land Ca \land \neg Da \checkmark$$

# Assignment Project Exam Help

# https://powcoder.com $(Ca \wedge Ra) \rightarrow Da \checkmark$

## Add WeChat powcoder



```
Invalid. Countermodel:
    Domain: {1}
    Extensions: B: \{1\} C: \{1\} D: \emptyset R: \emptyset
                                                                                          [Q p.46]
8. Fx: x is a fish
    Sx: x \text{ swims}
    \forall x(Sx \rightarrow \exists yFy)
    \therefore \exists x \neg Sx
                              \forall x(Sx \rightarrow \exists yFy) \setminus abc
                                       \neg \exists x \neg Sx
                                    \forall x \neg \neg Sx \setminus abc
                                       \neg \neg Sa \checkmark
                                           Sa
                                   Sa \rightarrow \exists y Fy \checkmark
                                    Project, Exam Help
Assignmen
             Add WeChat powcoder
                                                        \neg \neg Sc \checkmark
                                                           Sc
                                                   Sc \rightarrow \exists yFy \checkmark
                                                     \neg \hat{S}c \quad \exists y F y \checkmark d
```

Invalid. Countermodel:

Domain:  $\{1, 2, 3, ...\}$ Extensions:  $F : \{2, 3, 4, ...\}$   $S : \{1, 2, 3, ...\}$ 

[Q p.46]

Fd

```
9. Bx: x was built before 1970
   Kx: x runs on kerosene
   Rx: x is a robot
         Autovac 23E
   a:
   \forall x((Rx \land Bx) \rightarrow Kx)
   Ba \wedge \neg Ka
   ∴ ¬Ra
                           \forall x((Rx \wedge Bx) \rightarrow Kx) \setminus a
                                 Ba \wedge \neg Ka \checkmark
                                   \neg \neg Ra \checkmark
                                       Ra
                                       Ва
                                      \neg Ka
                              (Ra \wedge Ba) \rightarrow Ka \checkmark
Assignment Pr
          https://powoder.com
                                                                    [Q p.46]
   Valid.
          Add WeChat powcoder
```

10. Ax: x is an athlete

*Ix*: *x* is an intellectual

Px: *x* is a person

Tx: x is tall

Graham g:

$$\forall x((Tx \land Px) \to (Ax \lor Ix))$$

$$\exists x (Px \land Ax \land Ix)$$

$$\forall x ((Px \land Ax \land Ix) \to \neg Tx)$$

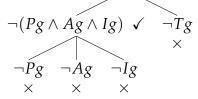
 $\therefore Ag \rightarrow (\neg Ig \lor \neg Tg)$ 

# Assignment Project Exam Help

 $\neg(\neg Ig \lor \neg Tg) \checkmark$ 

https://powcoder.com

Add WeChatspowcoder



Valid. [Q p.46]

[Contents]

## **Chapter 11**

# Models, Propositions, and Ways the World Could Be

There are no exercises for chapter 11. Assignment Project Exam Help

https://powcoder.com

Add WeChat powcoder

# **Chapter 12**

# **General Predicate Logic**

#### **Answers 12.1.3.1**

1AY 2. Y	ssignment Project Exam He	[Q p.48] [Q p.48]
3. Y	https://powcoder.com	[Q p.48]
4. Y	es Intps.//powcoder.com	[Q p.48]
5. N	Add WeChat powcoder	[Q p.48]
6. N	Add Weenat poweoder	[Q p.48]
7. N	Го	[Q p.48]
8. Y	es	[Q p.48]
9. N	Го	[Q p.48]
10. Y	es	[Q p.48]
	[C	Contents]

## **Answers 12.1.6**

Glossary:	•
-----------	---

a:	Alice
<i>b</i> :	Bill
<i>c</i> :	Clare
<i>d</i> :	Dave
<i>e</i> :	Edward
<i>f</i> :	Fiesta
<i>j</i> :	The Bell Jar
<i>m</i> :	Mary
<i>t</i> :	the Eiffel tower
Tx:	x is tall
Hxy:	x heard y
Lxy:	x likes y
Rxy	signment Project Exam Help
Txy:	x is taller than y
Pxyz:	x prefers y to z
	https://porygodor.com

# Translations: https://powcoder.com

	Hba	[Q p.49]
2.	¬Hba Add WeChat powcoder	[Q p.49]
3.	$Hba \wedge \neg Hab$	[Q p.49]
4.	Hba  o Hab	[Q p.49]
5.	$Hba \leftrightarrow Haa$	[Q p.49]
6.	$Hba \lor Hab$	[Q p.49]
7.	$Tcd \land \neg Tce$	[Q p.49]
8.	Pmac	[Q p.49]
9.	$\neg Pmdc \wedge \neg Pmcd$	[Q p.49]
10.	$Tec \land \neg Te$	[Q p.49]
11.	$Ttc \wedge Ttd$	[Q p.49]
12.	Tdt  o Td	[Q p.49]

13. $Ttd \wedge Pcdt$	[Q p.49]
14. $Tad \rightarrow Pdda$	[Q p.49]
15. $Pdec \rightarrow Tet$	[Q p.49]
16. $Pdec \rightarrow \neg Tc$	[Q p.49]
17. $Rmf \wedge Lmf$	[Q p.49]
18. $\neg Ldf \land \neg Rdf$	[Q p.49]
19. $\neg Ldj \rightarrow \neg Rdj$	[Q p.49]
20. $Pdjf \wedge \neg Rdj \wedge \neg Rdf$	[Q p.49]
	[Contents]

# AAssignment Project Exam Help

L.	GIOSS	ıry:		•
		httng	nouveod	or com
	a:	TALITY 5./	/powcod	

Bill *b*:

Cx: *x* is a chair

Bx: Aide We Chat powcoder

Bxy: x is bigger than y

Cxy: x contains y

#### Translations:

(i)	$\exists x \forall y Bxy$	[Q p.50]
(ii)	$\exists x \forall y By x$	[Q p.50]
(iii)	$Bab  o \exists x Bx b$	[Q p.50]
(iv)	$\forall xBxb \rightarrow Bab$	[Q p.50]
(v)	$\exists x \forall y Bxy \to \exists x Bxx$	[Q p.50]
(vi)	$(Bab \wedge Bba) \to \forall xBxx$	[Q p.50]
(vii)	$\exists x \forall y (Bay \to Bxy)$	[Q p.50]
(viii)	$\forall x (Bxa \to \forall y (Bay \to Bxy))$	[Q p.50]
(ix)	$\forall x (Rx \to \exists y (Cy \land Cxy))$	[Q p.50]

(x)  $\exists x (Rx \land \exists y (Cy \land Cxy \land By)) \land \exists x (Rx \land \forall y ((Cy \land Cxy) \rightarrow By)) \land \neg \exists x (Rx \land \forall y ((Cy \land Cxy) \rightarrow \neg By))$  [Q p.50]

#### 2. Glossary:

Bx: x is a beagleCx: x is a chihuahua

Dx: x is a dog
Px: x is a person
Bxy: x is bigger than y
Hxy: x is happier than y

Oxy: x owns y

#### Translations:

Assignment Project Exam Here	[Q p.50] <b>e</b> [ <b>0</b> .50]
(iii) $\exists x \exists y (Bx \land Cy \land Oxy)$	[Q p.50]
$\inf_{(v)} \neg \inf_{\neg\exists x\exists y} p_{x} \land c_{y} p_{yx} wcoder.com$	[Q p.50]
$(v) \neg \exists x \exists y (Bx \land cy PByx)$ Code1. Colli	[Q p.50]
(vi) $\exists x \exists y (Cx \land By \land Bxy)$	[Q p.50]
(vii) $\exists x \mathbf{Addy}(\mathbf{We}(\mathbf{x})\mathbf{hat} \mathbf{powcoder})$ (viii) $\forall x \forall y ((Px \land Py \land \exists z (Dz \land Oxz) \land \neg \exists w (Dw \land Oyw))$	[Q p.50]
(viii) $\forall x \forall y ((Px \land Py \land \exists z (Dz \land Oxz) \land \neg \exists w (Dw \land Oyw))$	$\rightarrow Hxy$ )
	[Q p.50]
(ix) $\forall x \forall y ((Dx \land Dy) \rightarrow (Bxy \rightarrow Hxy))$	[Q p.50]
$(x) \ \exists x (Bx \land \forall y (Cy \to Bxy) \land \forall z (Pz \to Bzx))$	[Q p.50]

#### 3. Glossary:

a: Aliceb: Bill

o: Woolworths
Cx: x is a cat
Dx: x is a dog
Gx: x is grey
Tx: x is timid

Bxy: x is bigger than y Gxy: x growls at y

Wxyz: x wants to buy y from z

#### Translations:

(i) $Ta \wedge Da \wedge \exists x (Cx \wedge Bxa)$	[Q p.51]
Asis Example 1 Project Exam He	e[[0p.51] [0p.51]
(iv) $\forall x ((Tx \land Dx) \rightarrow \exists y (Gy \land Cy \land Gxy))$	[Q p.51]
(v) \datapsy\dipoweoder.com	[Q p.51]
(vi) $\exists x (Tx \land Dx \land \forall y ((Gy \land Cy) \rightarrow Gxy))$	[Q p.51]
(viii) ¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬	[Q p.51]
(viii) $\exists x wax y \neg \exists x w b x o \Box \Box$	[Q p.51]
(ix) $\exists x (Waxo \land \neg Wbxo)$	[Q p.51]
$(x) \ \forall x (Waxo \to Gbx)$	[Q p.51]

#### 4. Glossary:

*d*: Dave

e: Elvis

*f*: Frank

*r*: the Rolling Stones

Px: x is a person

Sx: x is a song

Tx: x was in the top twenty

Axy: x is admires yRxy: x recorded yPxyz: x prefers y to z

#### **Translations:**

(i)  $\forall x (Px \rightarrow Adx)$  [Q p.51]

Assignment Project Exam Heip.51]

(iv)  $\neg \exists x (Px \land Axx)$  [Q p.51]

(iv)  $\forall x (Px \land Axx)$  [Q p.51]

(v)  $\forall x (Px \land Axx) \rightarrow Powcoder.com$  [Q p.51]

(vi)  $\forall x (Px \land Axx) \rightarrow Axd$  [Q p.51]

(vii)  $Af \land Pf re \ VeChat \ Powcoder$  [Q p.51]

(viii)  $\forall x \forall y (Sx \land Rrx \land Sy \land Rey) \rightarrow Poxy$  [Q p.51]

(ix)  $\exists x (Sx \land Tx \land Rrx) \land \neg \exists x (Sx \land Tx \land Rex)$  [Q p.51]

(x)  $\forall x \forall y ((Sx \land Tx \land Rrx \land Sy \land Rey) \rightarrow Pexy)$  [Q p.51]

(Contents]

#### **Answers 12.2.2**

1.	(i)	False	[Q p.52]
	(ii)	True	[Q p.52]
	(iii)	False	[Q p.52]
	(iv)	True ( $Ldb$ is true if we let the new name $d$ refer to 1.)	[Q p.52]
	(v) False (The extension of <i>L</i> contains no ordered pair whose second member is 1, which is the referent of <i>a</i> ; so no matter what		
		the new name <i>d</i> refers to, <i>Lda</i> is false.)	[Q p.52]

(vi)	False (The extension of $L$ contains no ordered pair which has the same object in both first and second place, so there is no possible choice of referent for the new name $d$ which makes $Ldd$ true.) [Q p.52]		
(vii)	True (No matter what we pick as the referent of $d$ , we pick a referent for $e$ such that $Lde$ is true.)	can then [Q p.52]	
(viii)	False (If we pick 1 as the referent of $d$ , then we cannereferent for $e$ such that $Led$ is true.)	ot pick a [Q p.52]	
(ix)	False (There is no object in the domain which is both in the extension of $P$ , and in the first place of an ordered pair in the extension of $L$ which has 2, which is the referent of $b$ , in second place; so there is no possible choice of referent for the new name $d$ which makes both $Pd$ and $Ldb$ true.) [Q p.52]		
(x)	True	[Q p.52]	
Assignment Project Exam Help.52			
(xii)	True	[ <b>Q</b> p.52]	
	False	[Q p.52]	
(xiv)	Thttps://powcoder.com	[Q p.52]	
(xv)	False	[Q p.52]	
(xvi)	False dd WeChat powcoder	[Q p.52]	
( " " " )		[Q p.52]	
(xviii)	True	[Q p.52]	
2. (i)	False	[Q p.53]	
(ii)	False	[Q p.53]	
(iii)	False	[Q p.53]	
(iv)	True	[Q p.53]	
` '	True	[Q p.53]	
` ,	False	[Q p.53]	
, ,	True	[Q p.53]	
,	False	[Q p.53]	
` '	False	[Q p.53]	
(x)	True	[Q p.53]	
3. (i)	False	[Op.53]	

(ii)	True	[Q p.53]
(iii)	True	[Q p.53]
(iv)	True	[Q p.54]
(v)	False (e.g. $\langle$ Alice, Bob $\rangle$ and $\langle$ Bob, Alice $\rangle$ are in the ext $S$ but $\langle$ Alice $\rangle$ isn't. $\rangle$	tension of [Q p.54]
(vi)	False	[Q p.54]
(vii)	False	[Q p.54]
(viii)	False	[Q p.54]
(ix)	True	[Q p.54]
(x)	True	[Q p.54]
4. (i)	(a) Domain: {1,2,3}	
. ,	Extension of $F : \{\langle 1, 1 \rangle, \langle 2, 2 \rangle, \langle 3, 3 \rangle\}$	
Ass	Signation of F: {\1,1,1,\2,2\} Exam Ho	elp <sub>[Qp.54]</sub>
(ii)	(a) Domain: {1,2,3}	
	https://powcoder.com	
	Extension of $F: \{\langle 1,2 \rangle \}$	[Q p.54]
(iii)	(a) Pohain: W2-3 Chat powcoder Extension of F: {\(1,1\),\\\2,1\),\\\3,2\}	
	(b) Domain: $\{1,2,3\}$ Extension of $F: \{\langle 1,1\rangle, \langle 2,3\rangle\}$	[Q p.54]
(iv)	(a) Domain: $\{1,2,3\}$ Extension of $F: \{\langle 1,1\rangle, \langle 1,2\rangle, \langle 1,3\rangle\}$	
	(b) Domain: $\{1,2,3\}$ Extension of $F: \{\langle 1,2\rangle, \langle 1,3\rangle\}$	[Q p.54]
(v)	(a) Domain: $\{1,2,3\}$ Extension of $F: \{\langle 1,2\rangle, \langle 2,3\rangle, \langle 3,1\rangle\}$	
	(b) Domain: {1,2,3}	
	Extension of $F : \{\langle 1, 1 \rangle, \langle 1, 2 \rangle, \langle 1, 3 \rangle\}$	[Q p.54]
(vi)	(a) Domain: $\{1,2,3\}$ Extension of $F: \{\langle 1,1\rangle \}$	
	(b) Domain: $\{1,2,3\}$ Extension of $F:\emptyset$	[Q p.54]

- (vii) (a) Domain:  $\{1\}$ Extension of  $F : \{\langle 1, 1 \rangle\}$ 
  - (b) Domain:  $\{1\}$  Extension of  $F : \{\emptyset\}$  [Q p.54]
- (viii) (a) Domain:  $\{1,2,3\}$ Referent of a: 1 Extension of  $F: \{\langle 1,2 \rangle \}$ 
  - (b) Domain:  $\{1,2,3\}$ Referent of a: 1 Extension of F:  $\{\langle 1,1\rangle\}$

[Q p.54]

(ix) (a) No such model. For the proposition to be true, the ordered pair consisting of the referent of *a*, followed by the referent of *a*, would have to both be in the extension of *F* and not in the extension of *F* 

# Assignment Project Exam Help

Extension of  $F: \{\langle 1, 1 \rangle\}$ 

[Q p.54]

- (x) (a) No such model. For the second and third conjuncts to be **Attracts** extension Ordered pair of the referent of *a* followed by the referent of *b*, but must not contain the ordered pair obtained by switching the order Attack the ordered pair obtained by switching the order Attack.
  - (b) Domain:  $\{1,2,3\}$ Referents: a: 1 b: 2 Extension of F:  $\{\langle 1,1\rangle\}$

[Q p.54]

[Contents]

#### **Answers 12.3.1**

```
1.
      (i)
                                            \neg \forall x (Rxx \rightarrow \exists y Rxy) \checkmark
                                           \exists x \neg (Rxx \rightarrow \exists yRxy) \ \checkmark a
                                              \neg (Raa \rightarrow \exists y Ray) \checkmark
                                                           Raa
                                                      ¬∃yRay ✓
                                                     \forall y \neg Ray \setminus a
                                                          \neg Raa
                                                             X
                                                                                                    [Q p.54]
            Logical truth.
      (ii)
                                          \neg \forall x (\exists y Rxy \rightarrow \exists z Rzx) \checkmark
                                         \exists x \neg (\exists y Rxy \rightarrow \exists z Rzx) \checkmark a
                                            \neg(\exists yRay \rightarrow \exists zRza) \checkmark
Assignment Project Exam Help
                                                    \forall z \neg Rza \setminus ab
              https://powcoder.com
            Extension of R : \{\langle 1, 2 \rangle\}
                                                                                                    [Q p.54]
    (iii)
                                          \neg(\forall x Rax \rightarrow \forall x \exists y Ryx) \checkmark
                                                      \forall x Rax \setminus b
                                                   \neg \forall x \exists y R y x \checkmark
                                                   \exists x \neg \exists y R y x \checkmark b
                                                      \neg \exists y R y b \checkmark
                                                     \forall y \neg Ryb \setminus a
                                                           Rab
                                                          \neg Rab
                                                             \times
```

Logical truth.

[Q p.54]

```
(iv)
                                  \neg(\forall x\exists y\exists zRyxz \rightarrow \exists x\exists yRxay)
                                            \forall x \exists y \exists z R y x z \setminus a
                                             \neg \exists x \exists y Rxay \checkmark
                                             \forall x \neg \exists y R x a y \setminus b
                                              \exists y \exists z R y a z \checkmark b
                                               \exists zRbaz \checkmark c
                                                    Rbac
                                               ¬∃yRbay ✓
                                               \forall y \neg Rbay \setminus c
                                                   \neg Rbac
                                                      \times
           Logical truth.
                                                                                         [Q p.54]
     (v)
                                             \neg\neg\forall x\exists yRxy \checkmark
                                             \forall x \exists y Rxy \setminus abc
Assignment Project Exam Help
                                                ∃yRby √c
             https://poweoder.com
             Add WeChat powcoder
          Not a logical truth. Countermodel:
          Domain: \{1, 2, 3, ...\}
          Extension of R : {\langle 1, 2 \rangle, \langle 2, 3 \rangle, \langle 3, 4 \rangle, ...}
                                                                                         [Q p.55]
```

```
(vi)
                              \neg \forall x \forall y \forall z ((Rxy \land Ryz) \rightarrow Rxz) \checkmark
                             \exists x \neg \forall y \forall z ((Rxy \land Ryz) \rightarrow Rxz) \checkmark a
                                \neg \forall y \forall z ((Ray \land Ryz) \rightarrow Raz) \checkmark
                               \exists y \neg \forall z ((Ray \land Ryz) \rightarrow Raz) \checkmark b
                                   \neg \forall z ((Rab \land Rbz) \rightarrow Raz) \checkmark
                                 \exists z \neg ((Rab \land Rbz) \rightarrow Raz) \checkmark c
                                    \neg((Rab \land Rbc) \rightarrow Rac) \checkmark
                                               Rab ∧ Rbc ✓
                                                     \neg Rac
                                                      Rab
                                                      Rbc
       Not a logical truth. Countermodel:
      Domain: {1,2,3}
      Extension of R : \{\langle 1, 2 \rangle, \langle 2, 3 \rangle\}
                                                                                              [Q p.55]
                                                                Exam Help
                                              \exists x \forall y Rxy \checkmark a
         https://poweder.com
                                                      Rab
                                                     \neg Rba
                                                     \neg Rbb
       Not a logical truth. Countermodel:
       Domain: {1,2}
                                                                                              [Q p.55]
       Extension of R : \{\langle 1, 1 \rangle, \langle 1, 2 \rangle\}
```

```
(viii)
                                     \neg(\exists y \forall x R x y \to \forall x \exists y R x y) \checkmark
                                                 \exists y \forall x R x y \checkmark a
                                                \neg \forall x \exists y Rxy \checkmark
                                               \exists x \neg \exists y R x y \checkmark b
                                                   \forall xRxa \setminus b
                                                  \neg \exists yRby \checkmark
                                                  \forall y \neg Rby \setminus a
                                                       Rba
                                                      \neg Rba
                                                         \times
           Logical truth.
                                                                                             [Q p.55]
     (ix)
                                     \neg(\exists x \forall y Rxy \to \exists x \exists y Rxy) \checkmark
                                                 \exists x \forall y Rxy \checkmark a
                                                \neg \exists x \exists y Rxy \checkmark
Assignment Project Exam Help
                                                  ¬∃yRay ✓
              https://powcoder.com
           Located th We Chat powcoder
```

```
(x)
                                             \neg(\forall x \forall y \exists z Rxyz \lor \forall x \forall y \forall z \neg Rxyz) \checkmark
                                                                      \neg \forall x \forall y \exists z R x y z \checkmark
                                                                    \neg \forall x \forall y \forall z \neg Rxyz \checkmark
                                                                     \exists x \neg \forall y \exists z R x y z \checkmark a
                                                                   \exists x \neg \forall y \forall z \neg Rxyz \checkmark b
                                                                          \neg \forall y \exists z Rayz \checkmark
                                                                         \exists y \neg \exists z Rayz \checkmark c
                                                                        \neg \forall y \forall z \neg Rbyz \checkmark
                                                                      \exists y \neg \forall z \neg Rbyz \checkmark d
                                                                              \neg \exists z Racz \checkmark
                                                                        \forall z \neg Racz \setminus abcde
                                                                           \neg \forall z \neg Rbdz \checkmark
                                                                          \exists z \neg \neg Rbdz \checkmark e
                                                                               \neg \neg Rbde \checkmark
                                                                                       Rbde
```

# Assignment Project Exam Help

 $\neg Racd$ 

#### https://powcoder.com

Not a logical truth. Countermodel:

Domain: \$1,23,4.5 Chat powcoder

2. (i) 
$$\forall x \forall y \forall z ((Rxy \land Ryz) \rightarrow Rxz) \land a$$

$$Rab$$

$$Rba$$

$$\neg \exists x Rxx \checkmark$$

$$\forall x \neg Rxx \land a$$

$$\forall y \forall z ((Ray \land Ryz) \rightarrow Raz) \land b$$

$$\forall z ((Rab \land Rbz) \rightarrow Raz) \land a$$

$$(Rab \land Rba) \rightarrow Raa \checkmark$$

$$\neg (Rab \land Rba) \qquad Raa$$

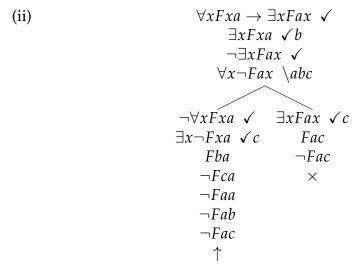
$$\neg Raa$$

$$\neg Rab \qquad \neg Rba$$

$$\times$$

$$\times$$

Valid. [Q p.55]



Invalid. Countermodel:

Domain:  $\{1, 2, 3\}$ 

# Assignment Project Exam Help.55]

# https://powcoder.com \[ \sizemax \alpha \text{Rzy} \cdot \alpha \text{dbc} \\ \text{Add WeChart \begin{subarrange}{c} \alpha \text{Rzy} \sizema \text{b} \\ \text{Rab} \cdot \text{Rcb} \sizema \text{Rab} \langle \text{Rcb} \sizema \text{Rab} \langle \text{Rab}

Rab Rcb ¬Raa ¬Rbb ¬Rcc

[Q p.55]

Invalid. Countermodel:

Domain: {1,2,3}

Extension of  $F: \{\langle 1,2\rangle, \langle 3,2\rangle \}$ 

(iv) 
$$\forall x \forall y (Rxy \rightarrow Ryx) \setminus b \\ \exists x Rxa \checkmark b \\ \neg \exists x Rax \checkmark \\ \forall x \neg Rax \setminus b \\ Rba$$
 
$$\forall y (Rby \rightarrow Ryb) \setminus a \\ Rba \rightarrow Rab \checkmark$$
 
$$\neg Rba \quad Rab \\ \times \quad \neg Rab \\ \times \quad \neg Rab$$
 
$$\times \quad \forall x \forall y (\neg Rxy \rightarrow Ryx) \setminus a \\ \neg \forall x \exists y Ryx \checkmark \\ \exists x \neg \exists y Ryx \checkmark a$$
 
$$\exists x \neg \exists y Ryx \checkmark a$$
 
$$Assignment \quad Projecy \quad \text{Exam Help} \\ \neg Raa \quad Raa \\ \land V(\neg Ray \rightarrow Rya) \setminus a \\ https://poweogler.com \\ \neg \neg Raa \quad Raa \\ Add \quad WeChat \quad poweoder \\ \text{Valid.}$$
 [Q p.55]

(vi) 
$$\forall x \forall y (Rxy \rightarrow (Fx \land Gy)) \setminus a \\ \neg \neg \exists x Rxx \checkmark a \\ Raa \\ \forall y (Ray \rightarrow (Fa \land Gy)) \setminus a \\ Raa \rightarrow (Fa \land Ga) \checkmark \\ \neg Raa \quad Fa \land Ga \land \\ \neg Raa \quad \\ \neg Ra$$

Invalid. Countermodel:

Domain: {1}

Extensions:  $F : \{1\}$   $G : \{1\}$   $R : \{\langle 1, 1 \rangle\}$  [Q p.55]

 $\uparrow$ 

(vii) 
$$\forall x (Fx \rightarrow (\forall y Rxy \lor \neg \exists y Rxy)) \land a$$

$$Fa$$

$$\neg Rab$$

$$\neg Raa \checkmark$$

$$Raa$$

$$Fa \rightarrow (\forall y Ray \lor \neg \exists y Ray) \checkmark$$

$$\times$$

$$\forall y Ray \lor b \quad \neg \exists y Ray \checkmark$$

$$\times$$

$$\forall y Ray \lor b \quad \neg \exists y Ray \checkmark$$

$$\times$$

$$Rab \quad \forall y \neg Ray \land a$$

$$\times$$

$$\neg Raa$$

$$\times$$

Valid. [Q p.55]

# Assignment Project Exam Help

 $\neg \forall x \forall y Rxy \checkmark$ 

https://powerder.com

 $\exists y \neg Rby \checkmark c$ 

# Add We Chat Powcoder $\exists z(Rzb \land Rzc) \rightarrow Rbc \checkmark$

 $\neg \exists z (Rzb \land Rzc) \lor Rbc$   $\forall z \neg (Rzb \land Rzc) \lor a \times \\ \neg (Rab \land Rac) \lor \\ Rab$  Rac  $\neg Rab \quad \neg Rac$   $\times \times$ 

Valid. [Q p.55]

```
(ix)
                                                \forall x \exists y Rxy \setminus bacde
                                                    \neg \exists x R x b \checkmark
                                                    \forall x \neg Rxb \setminus b
                                                         \neg Rbb
                                                     ∃yRby √a
                                                          Rba
                                                     ∃yRay √c
                                                           Rac
                                                     \exists yRcy \checkmark d
                                                           Rcd
                                                     ∃yRdy √e
                                                           Rde
                                                     \exists y Rey \checkmark f
                                                           Ref
```

# nent Project Exam Help

Domain:  $\{1, 2, 3, 4, 5, \dots\}$ 

Referent of b: 2 Extending St.  $\mathbb{R}$  / PLOWICO (14.6 OM)...} [Q p.55]

#### $\forall y (Fy \to Rxy) \checkmark a$ (x) Add WeC hat powcoder

Valid. [Q p.56]

```
3. (i) a: Alice b: Bill c: Carol
```

Oxy: x is older than y

Oab Obc ∴ Oac

> Oab Obc ¬Oac ↑

Invalid. Countermodel:

Domain: {1, 2, 3}

Referents: a:1 b:2 c:3

### Assignment (Project Exam Help.56)

(ii) a: Alice b: http://powcoder.com

Oxy: x is older than y

### Add WeChat powcoder

Obc

 $\forall x \forall y \forall z ((Oxy \land Oyz) \rightarrow Oxz))$   $\therefore Oac$ 

$$\begin{array}{c} Oab \\ Obc \\ \forall x \forall y \forall z ((Oxy \land Oyz) \rightarrow Oxz)) \ \backslash a \\ \neg Oac \\ \forall y \forall z ((Oay \land Oyz) \rightarrow Oaz)) \ \backslash b \\ \forall z ((Oab \land Obz) \rightarrow Oaz)) \ \backslash c \\ ((Oab \land Obc) \rightarrow Oac)) \ \checkmark \\ \hline \neg (Oab \land Obc) \ \checkmark \ Oac \\ \neg Oab \ \neg Obc \\ \times \ \times \end{array}$$

Valid. [Q p.56]

```
(iii) a:
             me
       b:
             you
       d:
             Dave
       Bx:
             x is a banker
       Txy:
             x trusts y
       \forall x (Tbx \rightarrow Tax)
       \forall x (Bx \rightarrow Tbx)
       Bd
       ∴ Tad
                         \forall x(Bx \to Tbx) \setminus d
                                 Bd
                                \neg Tad
                            Bd \rightarrow Tbd \checkmark
Assignment Pra
                                      Exam Help
                                 Tbd \rightarrow Tad \checkmark
        https://powcoder.com
       Valid.
                                                         [Q p.56]
        Add WeChat powcoder
```

(iv) Px: x is a person Lxy: x loves y

$$\forall x (Px \to \exists y (Py \land Lxy))$$

$$\therefore \forall x (Px \to \exists y (Py \land Lyx))$$

$$\forall x (Px \to \exists y (Py \land Lxy)) \land ab$$

$$\neg \forall x (Px \to \exists y (Py \land Lyx)) \checkmark$$

$$\exists x \neg (Px \to \exists y (Py \land Lyx)) \checkmark a$$

$$\neg (Pa \to \exists y (Py \land Lya)) \checkmark$$

$$Pa$$

$$\neg \exists y (Py \land Lya) \checkmark$$

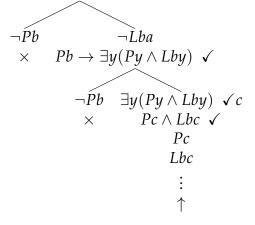
$$\forall y \neg (Py \land Lya) \land ab$$

$$\neg (Pa \land Laa) \checkmark$$

Assignment Project Exam Help  $\times Pa \rightarrow \exists y (Py \land Lay) \checkmark$ 

https://poweoder.com

Add WeChat, plaky coder



Invalid. Countermodel:

Domain:  $\{1, 2, 3...\}$ 

Extensions:  $L: \{\langle 1,2 \rangle, \langle 2,3 \rangle, \langle 3,4 \rangle \dots \}$   $P: \{1,2,3,\dots \}$ 

[Q p.56]

```
(v) n:
               Nancy
        Rx:
               x is a restaurateur
               x can afford to feed y
        Wx:
               x is very wealthy
        Rn
        \forall x (Rx \rightarrow (Anx \leftrightarrow \neg Axx))
        ∴ Wn
                                      Rn
                       \neg Wn
                          Rn \rightarrow (Ann \leftrightarrow \neg Ann) \checkmark
                              \neg Rn \quad Ann \leftrightarrow \neg Ann \checkmark
Assignment Project
        valttps://powcoder.com
                                                                [Q p.56]
```

Add WeChat powcoder

(vi) *e*: the Eiffel tower

l: Lake Burley Griffin

Cx: x is in CanberraPx: x is in Paris

*Bxy*: *x* is more beautiful than *y* 

$$\forall x \forall y ((Px \land Cy) \rightarrow Bxy)$$

$$Pe \land Cl$$

$$\therefore Bel$$

$$\forall x \forall y ((Px \land Cy) \rightarrow Bxy) \land e$$

$$Pe \land Cl \checkmark$$

$$\neg Bel$$

$$Pe$$

$$Cl$$

Assignment Project Linkam Help

https://powcoder.com

Valld dd WeChat powcoder [Q p.56]

(vii) Jx: x is a journalist Px: x is a politician Txy: x talks to y

$$\forall x \forall y ((Px \land Txy) \to Py) \\ \neg \exists x (Px \land Jx) \\ \therefore \neg \exists x \exists y (Px \land Jy \land Txy)$$

$$\forall x \forall y ((Px \land Txy) \rightarrow Py) \land a$$

$$\neg \exists x (Px \land Jx) \checkmark$$

$$\neg \neg \exists x \exists y (Px \land Jy \land Txy) \checkmark$$

$$\exists x \exists y (Px \land Jy \land Txy) \checkmark a$$

$$\exists y (Pa \land Jy \land Tay) \checkmark b$$

$$Pa \land Jb \land Tab \checkmark$$

$$Pa$$

### Assignment Project Exam Help

 $\frac{\forall x \neg (Px \land Jx) \land ab}{\neg (Pa \land Ja)} \checkmark$  https://powcoder.com

# Add WeChat powcoder

Valid. [Q p.56]

```
(viii) Sxy: x is smaller than y
          \neg \exists x \forall y S x y
          \therefore \neg \exists x \forall y S y x
                                           \neg \exists x \forall y S x y \checkmark
                                          \neg\neg\exists x\forall ySyx \checkmark
                                            \exists x \forall y S y x \checkmark a
                                        \forall x \neg \forall y Sxy \checkmark abcd
                                            ∀ySya \abcd
                                                  Saa
                                             ¬∀ySay ✓
                                             \exists y \neg Say \checkmark b
                                                 \neg Sab
                                                  Sba
Assignment Project Exam Help
                                                 \neg Sbc
            https://poweoder.com
            Add WeCha
                                               \exists y \neg Sdy
                                                    \uparrow
          Invalid. Countermodel:
```

Extension of  $S : \{\langle 1, 1 \rangle, \langle 2, 1 \rangle, \langle 3, 1 \rangle, \langle 4, 1 \rangle \dots \}$ 

[Q p.56]

Domain:  $\{1, 2, 3, 4, \dots\}$ 

```
(ix) d:
                                                          David
                                                           Margaret
                        m:
                        Fx:
                                                            x is French
                        Mx:
                                                              x is a movie
                        Sx:
                                                            x is commercially successful
                                                            x likes y
                        Lxy:
                        \forall x (Mx \to (\neg Sx \lor (Lmx \land Ldx)))
                        \neg \exists x (Fx \land Mx \land Lmx \land Ldx)
                        \therefore \neg \exists x (Fx \land Mx \land Sx)
                                                             \forall x (Mx \rightarrow (\neg Sx \lor (Lmx \land Ldx))) \setminus a
                                                                           \neg \exists x (Fx \land Mx \land Lmx \land Ldx) \checkmark
                                                                                              \neg\neg\exists x(Fx\wedge Mx\wedge Sx) \checkmark
                                                                                                   \exists x (Fx \land Mx \land Sx) \checkmark a
                                                                                           entalia entre la compart de la
                                                                                                                                                          Fa
                                                                                                                                             Shat powcoder
                                                                                                                                                \neg \hat{S}a
                                                                                                                                                                                                                          Lma ∧ Lda ✓
                                                                                                                                                                                                                                                  Lma
                                                                                                                                                      X
                                                                                                                                                                                                                                                    Lda
                                                                                                                                                                                  \neg (Fa \land Ma \land Lma \land Lda) \checkmark
                                                                                                                                                                                   \neg Fa
                                                                                                                                                                                                                           \neg Ma
                                                                                                                                                                                                                                                                    \neg Lma
                                                                                                                                                                                                                                                                                                               \neg Lda
                                                                                                                                                                                                                                    ×
                                                                                                                                                                                                                                                                               \times
                                                                                                                                                                                         \times
                                                                                                                                                                                                                                                                                                                           \times
                        Valid.
                                                                                                                                                                                                                                                                                                                                      [Q p.56]
```

#### (x) Cxy: x causes y

$$\exists x \forall y Cxy \\ \therefore \neg \exists x \forall y Cyx$$

```
\exists x \forall y Cxy \checkmark a
\neg\neg\exists x \forall y Cyx \checkmark
  \exists x \forall y Cyx \checkmark b
     \forall y Cay \setminus ab
     \forall yCyb \setminus ab
             Caa
             Cab
             Cab
            Cbb
```

### Assigning Project Exam Help

Extension of C: { $\langle 1, 1 \rangle$ ,  $\langle 1, 2 \rangle$ ,  $\langle 2, 2 \rangle$ }

[Q p.56]

#### https://powcoder.com

[Contents]

**Answers 12.4.1** Add WeChat powcoder
The trees are not given in these answers.

#### 1. Glossary:

e: that egg r: Roger *Fx*: *x* is a food

Exy: *x* will eat *y* 

Translation:

$$\forall x(Fx \to Erx) \\ \therefore Ere$$

Postulate:

Fe

[Q p.57]

```
2. Glossary:
```

a: 180b: 170l: Billn: Ben

Gxy: x is greater than yWxy: x weighs y poundsVxy: x is heavier than y

#### Translation:

Wla Wnb ∴ Vln

#### Postulates:

#### Assignment Project Exam Help

 $\forall x \forall y \forall z \forall w ((Wxy \land Wzw \land Gyw) \rightarrow Vxz)$ 

### https://powcoder.com

[Q p.57]

3. Glossary:

# <sup>a</sup>Add WeChat powcoder

*j*: John *n*: Nancy

Fxy: x ran further than yGxy: x is greater than yRxy: x ran y miles

#### Translation:

Rja Rnb ∴ Fnj

#### Postulates:

Gba $\forall x \forall y \forall z \forall w ((Rxy \land Rzw \land Gyw) \rightarrow Fxz)$ 

[Q p.57]

#### 4. Glossary:

b: Buddenbrooks

s: Sophie

t: Thomas Mann Nx: x is a novel

Axy: x is the author of y

Exy: x enjoys y

#### Translation:

$$\forall x((Nx \land Atx) \rightarrow Esx)$$

$$\therefore Esb$$

#### Postulates:

# Assignment Project Exam Help

[Q p.57]

#### 5. Glossah:ttps://powcoder.com

b: Borges

C: Adds We Chat powcoder

Axy: x is the author of y

Exy: x enjoys y

#### Translation:

$$\forall x (Ecx \leftrightarrow Nx) \\ \therefore \neg \exists x (Abx \land Ecx)$$

#### Postulate:

$$\neg \exists x (Nx \land Abx)$$

[Q p.57]

[Contents]

#### **Answers 12.5.4**

Note that a formula may have more than one prenex equivalent (i.e. there may be other correct answers).

1. $\forall x \forall y (Px \vee Qy)$	[Q p.57]
2. $\exists x \exists y (Px \lor Qy)$	[Q p.57]
3. $\exists x \forall y (Px \rightarrow Py)$	[Q p.57]
$4. \ \exists x \forall y \exists z \forall w ((Pz \to Pw) \land (Px \to Py))$	[Q p.57]
$5. \ \exists x \exists y \forall z \neg (Sx \land (Ty \rightarrow Uxz))$	[Q p.57]
	[Contents]

### Assignment Project Exam Help

https://powcoder.com

Add WeChat powcoder

#### Chapter 13

#### **Identity**

#### **Answers 13.2.2**

```
Glossary
   Assignment Project, Exam Help
          Ben
    b:
                              Mx:
                                      x is a man
    c:
          Chris
                              Ox:
                                      x is a town
    d:
                                     x is a felevision show
    e:
                              Wx:
    f:
          Family Guy
                             ecy.hat.powcoder
    g:
          Sydney (
    h:
    i:
          Jindabyne
                              Lxy:
                                      x is larger than y
    j:
          Jonathon
                              Oxy:
                                      x owns y
    k:
                                      x is by y's side
          Melbourne
                              Sxy:
    l:
          Canberra
                              Txy:
                                      x is taller than y
          Mary
                              Vxy:
    m:
                                      x watches y
          I/me
                              Wxy:
    n:
                                      x wants y
          Seinfeld
                              Bxyz:
                                     y is between x and z
    s:
          x is a chihuahua
                             Pxyz:
                                     x prefers y to z
    Dx:
          x is a dog
Translations:
  1. \forall x (x \neq c \rightarrow Lcx)
                                                                    [Q p.58]
  2. \forall x((x \neq c \land Dx) \rightarrow Bx) \land Cc
                                                                    [Q p.58]
  3. \exists x (Dx \land Sxb \land x \neq c) \rightarrow Hb
                                                                    [Q p.58]
```

[Q p.58]

4.  $\forall x ((Px \land Scx \land x \neq j) \rightarrow Hc)$ 

```
5. \forall x(Dx \rightarrow Ljx)
                                                                                                                            [Q p.58]
  6. \forall x (Wmx \rightarrow \exists y (Py \land y \neq m \land Oyx))
                                                                                                                            [Q p.58]
  7. \exists x \exists y (Px \land x \neq m \land Wxy \land Omy)
                                                                                                                            [Q p.58]
  8. \exists x (Omx \land \neg Wmx)
                                                                                                                            [Q p.58]
  9. \exists x (Bx \land Omx) \rightarrow \forall y \forall z ((Py \land Bz \land y \neq m) \rightarrow \neg Oyz)
                                                                                                                            [Q p.58]
10. \forall x \forall y ((Px \land x \neq m \land Wmy) \rightarrow \neg Oxy)
                                                                                                                            [Q p.58]
11. \forall x (Px \rightarrow Pxsf)
                                                                                                                            [Q p.58]
12. \forall x ((Tx \land x \neq s) \rightarrow Pasx)
                                                                                                                            [Q p.58]
13. \forall x ((Tx \land x \neq f) \rightarrow Paxf)
                                                                                                                            [Q p.58]
\underset{15.}{\overset{14}{\text{A}}} \underset{Vjf}{\overset{Vjf}{\text{N}}} \underset{x}{\overset{\vee}{\text{N}}} \underset{x}{\overset{\vee}{\text{M}}} \underset{x}{\overset{\vee}{\text{Proj}}} \underset{x}{\overset{\vee}{\text{Proj}}} \text{ect Exam He} \underset{[p.59]}{\overset{[p.59]}{\text{Proj}}}
16. Wd \land \forall x((Wx \land x \neq d) \rightarrow Tdx)
17. \forall x((Mx \land t) \neq d) \leftrightarrow x \neq e)
16. Vd \land \forall x((Wx \land x \neq d) \rightarrow Tdx)
17. \forall x((Mx \land t) \neq d) \leftrightarrow x \neq e)
                                                                                                                            [Q p.59]
                                                                                                                            [Q p.59]
18. Ted \wedge \exists x (Wx \wedge x \neq d \wedge Tex)
19. \neg \exists x (Px \wedge dd \wedge Txe) eChat powcoder
                                                                                                                            [Q p.59]
                                                                                                                            [Q p.59]
20. \exists x (Px \land x \neq e \land x \neq d)
                                                                                                                            [Q p.59]
21. \forall x((Px \land Kxb) \leftrightarrow x = g)
                                                                                                                            [Q p.59]
22. \exists x (Px \land Knx \land x \neq b)
                                                                                                                            [Q p.59]
23. \forall x ((Kbx \land Px \land x \neq c \land x \neq n) \rightarrow Hx)
                                                                                                                            [Q p.59]
24. \forall x((Px \land Hx \land Knx) \leftrightarrow x = b)
                                                                                                                            [Q p.59]
25. Pb \wedge Hb \wedge Knb \wedge \forall x((Px \wedge Hx \wedge Knx \wedge x \neq b) \rightarrow Tbx)
                                                                                                                            [Q p.59]
26. Oi \wedge Bhik \wedge \forall x((Ox \wedge Bhxk \wedge x \neq i) \rightarrow Cix)
                                                                                                                            [Q p.59]
27. \exists x(Ox \land Bhxk \land Cxl)
                                                                                                                            [Q p.59]
28. \forall x((Ox \land x \neq i) \rightarrow \exists y(Oy \land Cyx))
                                                                                                                            [Q p.59]
29. \neg \exists x (Ox \land Bhxk \land (Lxl \lor Cxi))
                                                                                                                            [Q p.59]
```

30. $Oi \wedge Bhik \wedge \forall x((Ox \wedge Bhxk \wedge x \neq i) \rightarrow Pnix)$	[Q p.59]
	[Contents]
Answers 13.3.1	
1. (i) True	[Q p.60]
(ii) False	[Q p.60]
(iii) True	[Q p.60]
(iv) True	[Q p.60]
(v) False	[Q p.60]
(vi) True	[Q p.60]
Assignment Project Exam	Help.60]
(iii) True	[Q p.60]
(iv) True (iv) T	[Q p.60]
(v) True	[Q p.60]
(vi) False	[Q p.60]
3. (i) (a) Domain: {1,2,3} Chat powcode  Referent of <i>a</i> : 1  Extension of <i>F</i> : {1}  (b) Domain: {1,2,3}	er
Referent of $a:1$ Extension of $F:\{1,2\}$	[Q p.61]
(ii) (a) Domain: $\{1,2\}$ Referents: $a:1$ $b:1$	
(b) Domain: $\{1,2\}$ Referents: $a:1$ $b:2$	[Q p.61]
(iii) (a) Domain: $\{1,2,3\}$ Extension of $R: \{\langle 1,2\rangle, \langle 1,3\rangle\}$	
(b) Domain: $\{1,2,3\}$ Extension of $R:\{\langle 1,2\rangle\}$	[Q p.61]

```
(iv) (a) Domain: {1,2,3}
            Extension of R : \{\langle 1, 1 \rangle, \langle 2, 2 \rangle\}
       (b) Domain: {1,2,3}
            Extension of R : \{\langle 1, 1 \rangle, \langle 1, 2 \rangle\}
                                                                           [Q p.61]
  (v) (a) Domain: {1,2,3}
            Extension of R : \{\langle 1, 2, 1 \rangle, \langle 1, 3, 1 \rangle, \langle 2, 1, 2 \rangle, \langle 2, 3, 2 \rangle, \langle 3, 1, 3 \rangle, \langle 3, 2, 3 \rangle\}
       (b) Domain: \{1, 2, 3\}
            Extension of R : {\langle 1, 2, 1 \rangle, \langle 1, 3, 1 \rangle}
                                                                           [Q p.61]
 (vi) (a) No such model: symmetry of identity.
       (b) Domain: {1,2,3}
            Referent of a:1
                                                                           [Q p.61]
(vii) (a) Domain: {1,2,3}
            Extension of F : \{1\}
       (b) Domain: \{1, 2, 3\}
  ssignment Project Exam Help.61]
(viii) (a) Domain: {1,2,3}
            Extensions: F : \{1,2\} G : \{1\}
       (bhptpin: //powcoder.com
                                                                           [Q p.61]
 (ix) (a) Domain: \{1, 2, 3\}
           Attai WeChat powedder
       (b) Domain: {1,2,3}
            Extensions: F: \{1,2\} R: \{\langle 1,2\rangle, \langle 2,2\rangle\}
                                                                           [Q p.61]
  (x) (a) Domain: \{1, 2, 3\}
            Referents: a : 1
            Extensions: F: \{1\} R: \emptyset
       (b) Domain: \{1, 2, 3\}
            Referents: a : 1
            Extensions: F : \{1\} R : \{\langle 1, 1 \rangle\}
                                                                           [Q p.61]
 (xi) (a) Domain: \{1, 2, 3\}
            Extensions: R : \{\langle 1, 2, 3 \rangle\}
       (b) Domain: {1,2,3}
            Extensions: R : \{\langle 1, 2, 1 \rangle\}
                                                                           [Q p.61]
 (xii) (a) Domain: {1,2,3}
            Extensions: R : \{\langle 1, 2, 3 \rangle\}
       (b) Domain: {1,2,3}
            Extensions: R : \{\langle 1, 2, 1 \rangle\}
                                                                           [Q p.61]
```

```
(xiii) (a) Domain: {1,2,3}
            Extensions: F : \{2,3\}
        (b) Domain: {1,2,3}
            Extensions: F : \{2\}
                                                                      [Q p.61]
 (xiv) (a) Domain: \{1, 2, 3\}
            Extensions: F : \{1, 2\}
                                      R:\{\langle 1,2\rangle\}
        (b) Domain: {1,2,3}
            Extensions: F : \{1, 2\} R : \{\langle 1, 1 \rangle\}
                                                                      [Q p.61]
  (xv) (a) Domain: \{1,2,3\}
            Extensions: R : \{\langle 1,2,3 \rangle, \langle 1,1,1 \rangle, \langle 2,2,2 \rangle, \langle 3,3,3 \rangle\}
        (b) Domain: {1,2,3}
            Extensions: R : \{\langle 1, 2, 3 \rangle, \langle 1, 1, 1 \rangle, \langle 2, 2, 2 \rangle\}
                                                                      [Q p.61]
 (xvi) (a) Domain: \{1, 2, 3\}
            Extensions: R : \{\langle 1, 1 \rangle\}
     Stop Hyprophel Preorie citen is a transport is the p.61]
(xvii) (a) Domain: {1,2,3}
            Referents: a:1 b:1
          https://powcoder.com
        (b) Domain: {1,2,3}
            Referents: a:1 b:2
           Add We Chat powcoder
                                                                      [Q p.61]
(xviii) (a) Domain: {1,2,3}
            Extensions: F : \{1, 2\}
        (b) Domain: {1,2,3}
            Extensions: F : \{1, 2, 3\}
                                                                      [Q p.61]
                                                                   [Contents]
```

#### **Answers 13.4.3**

1. (i)  $Rab \rightarrow \neg Rba \checkmark$  Rab a = b  $\neg Rab \rightarrow \neg Rba$  × Raa × Raa Rba ×

Unsatisfiable. [Q p.61]

Assignment Project Exam Help

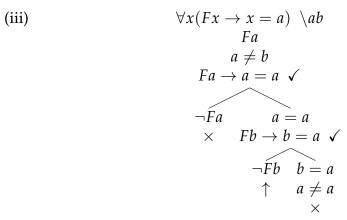
https://powcoder.com

Satisfiable.

Donaid: a:1 We Chat powcoder

Referents: a:1 b:1 c:2

Extension of  $R : \{\langle 1, 1 \rangle\}$  [Q p.61]



Satisfiable.

Domain: {1,2}

Referents: a:1 b:2Extension of  $F : \{1\}$ 

[Q p.61]

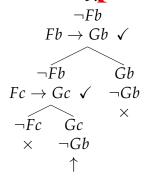
### Assignment Project, Exam Help

 $\exists x Fx \sqrt{c}$ 

https://powcoden.com

Fa  $\rightarrow$  Ga  $\checkmark$ Add WeChat powcoder

$$Fa \rightarrow Ga \checkmark$$



Satisfiable.

Domain: {1,2}

Referents: a:1 b:1 c:2Extensions:  $F : \{2\}$   $G : \{2\}$ 

[Q p.61]

$$\forall x (x \neq a \rightarrow Rax) \ \ \ \, \forall x \neg Rxb \ \ \, \langle ab \ \ \, a \neq b \ \ \, \neg Rab \ \ \, \neg Rbb \ \ \, b \neq a \rightarrow Rab \ \ \, \langle \ \ \, \langle a \neq a \ \ \, \rangle \ \ \, \langle a \neq a \ \ \, \rangle \ \ \, \langle a \neq a \ \ \, \rangle$$

Unsatisfiable. [Q p.61]

(vi) 
$$\exists x \forall y (Fy \to x = y) \ \checkmark c$$

# Assignment $\Pr_{y(F,y)} \notin E_{x}$ Exam Help

https://powcoder.com  $\times Fb \rightarrow c = b \checkmark$ 

# Add WeChat powcoder

 $\begin{array}{ccc}
\neg Fc & c = c \\
\neg Fa & \uparrow \\
\times
\end{array}$ 

Satisfiable. Domain: {1}

Referents: a:1 b:1 c:1

Extensions:  $F : \{1\}$ 

[Q p.61]

(vii) 
$$\forall x \forall y (Rxy \rightarrow x = y) \setminus a$$

$$a \neq b$$

$$\forall y (Ray \rightarrow a = y) \setminus b$$

$$Rab \rightarrow a = b \checkmark$$

$$\neg Rab \quad a = b$$

$$\times \quad a \neq a$$

$$\times$$

Unsatisfiable. [Q p.62]

(viii) 
$$\forall x((Fx \land Rxa) \rightarrow x \neq a) \ \ b$$

$$Fb \land Rba \ \checkmark$$

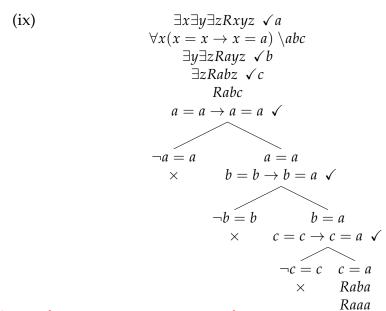
$$a = b$$

$$Fb$$

Assignment Project Exam Help

 $\begin{array}{c} \textbf{https://powcoder} \underset{\times}{\overset{(Fb \wedge Rba)}{\sim}} \overset{b \neq a}{\overset{b \neq a}{\leftarrow}} om \\ \overset{\times}{\overset{\times}} \end{array}$ 

UnAtialiable We Chat powcoder [Q p.62]



# Assignment Project Exam Help

Rabb

https://powcoder.com

Racc Rbaa

Rbba

## Add WeChat powceder

Rbbb Rbca Rbcb Rbcc Rcaa Rcab Rcac Rcba Rcbb Rcbc

Rccb Rccc ↑

Satisfiable. (See next page for model.)

Domain: {1}

Referents: a:1 b:1 c:1Extensions:  $R:\{\langle 1,1,1\rangle\}$ 

[Q p.62]

$$\forall x \neg Rxx \setminus a \\ \forall x \forall yx = y \setminus a \\ \exists x Rax \checkmark b \\ Rab \\ \forall ya = y \setminus b \\ a = b \\ Raa \\ \neg Raa \\ \times$$

Unsatisfiable. [Q p.62]

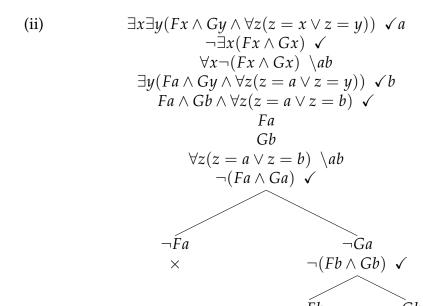
# Assignment Project/Exam Help

https://power.com

Add WeChat powcoder

Ga  $\neg (Fa \land Ga) \checkmark$   $\neg Fa \quad \neg Ga$   $\times \qquad \times$ 

Valid. [Q p.62]



Assignment Project Exam Help

# https://poweoder.com b = a b = b Add WeChat powcoder

Invalid. Countermodel:

Domain: {1,2}

Referents: a:1 b:2

[Q p.62] Extensions:  $F : \{1\}$   $G : \{2\}$ 

```
(iii)
                                                                 Rab
                           \neg \forall x \forall y \forall z (((Rxy \land Ryz) \land x = z) \rightarrow Ryy) \checkmark
                          \exists x \neg \forall y \forall z (((Rxy \land Ryz) \land x = z) \rightarrow Ryy) \checkmark c
                              \neg \forall y \forall z (((Rcy \land Ryz) \land c = z) \rightarrow Ryy) \checkmark
                             \exists y \neg \forall z (((Rcy \land Ryz) \land c = z) \rightarrow Ryy) \checkmark d
                                \neg \forall z (((Rcd \land Rdz) \land c = z) \rightarrow Rdd) \checkmark
                               \exists z \neg (((Rcd \land Rdz) \land c = z) \rightarrow Rdd) \checkmark e
                                   \neg (((Rcd \land Rde) \land c = e) \rightarrow Rdd) \checkmark
                                              (Rcd \wedge Rde) \wedge c = e) \checkmark
                                                               \neg Rdd
                                                        Rcd \wedge Rde \checkmark
                                                                c = e
                                                                 Rcd
                                                                 Rde
                                                                 Red
```

# Assignment Project Exam Help

Invalid. Countermodel:

Domain: {1,2,3,4}

Refrections of  $R: \{1,2\}, \{3,4\}, \{4,3\}\}$ 

[Q p.62]

### (iv) Add Werthat powcoder

$$\neg\exists x (Rax \land x \neq b) \checkmark c$$

$$\neg\exists x (Rxa \land x \neq b) \checkmark c$$

$$Rac \land c \neq b \checkmark$$

$$Rac \qquad c \neq b$$

$$\forall y (Ray \rightarrow Rya) \land c$$

$$Rac \rightarrow Rca \checkmark$$

$$\neg Rac \qquad Rca$$

$$\times \qquad \neg (Rca \land c \neq b) \checkmark$$

$$\times \qquad c = b$$

Valid.

[Q p.62]

$$\forall x \forall y x = y \setminus a$$

$$\neg \forall x \forall y (Rxy \to Ryx) \checkmark$$

$$\exists x \neg \forall y (Rxy \to Ryx) \checkmark a$$

$$\neg \forall y (Ray \to Rya) \checkmark$$

$$\exists y \neg (Ray \to Rya) \checkmark b$$

$$\neg (Rab \to Rba) \checkmark$$

$$Rab$$

$$\neg Rba$$

$$\forall ya = y \setminus b$$

$$a = b$$

$$Raa$$

$$Rba$$

$$Rba$$

$$\times$$

Valid. [Q p.62]

#### Assignment Project Exama Help

https://powcoder.com

$$(Rab \land Rad) \rightarrow b = d \checkmark$$

$$\neg (Rab \land Rad) \checkmark b = d$$

$$\neg Rab \neg Rad \lor b \neq b$$

$$\lor \neg Rcd \lor$$

[Q p.62] Valid.

(vii) 
$$\exists x \exists y (Rxy \land x = y) \checkmark a$$

$$\neg \neg \forall x Rxx \checkmark$$

$$\forall x Rxx \land ab$$

$$\exists y (Ray \land a = y) \checkmark b$$

$$Rab \land a = b \checkmark$$

$$Rab$$

$$a = b$$

$$Raa$$

$$Rbb$$

$$Rba$$

$$\uparrow$$

Invalid. Countermodel:

Domain: {1}

Referents: a:1 b:1Extension of  $R:\{\langle 1,1\rangle\}$ 

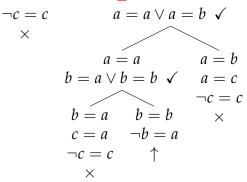
[Q p.62]

[Q p.62]

## Assignment, Project, Exam Help

https://pow-coder.com

### Add WeChat powcoder



Invalid. Countermodel:

Domain: {1,2}

Referents: a:1 b:2 c:2

```
(ix)
                                                     \forall x Rax \setminus abc
                                                   \neg \forall x \forall yx = y \checkmark
                                     \neg \exists x \exists y \exists z (Rxy \land Rxz \land y \neq z) \checkmark
                                                  \exists x \neg \forall yx = y \checkmark b
                                                     \neg \forall yb = y \checkmark
                                                    \exists y \neg b = y \checkmark c
                                                          \neg b = c
                                                            Raa
                                                            Rab
                                                            Rac
                                     \forall x \neg \exists y \exists z (Rxy \land Rxz \land y \neq z) \setminus a
                                       \neg \exists y \exists z (Ray \land Raz \land y \neq z) \checkmark
                                       \forall y \neg \exists z (Ray \land Raz \land y \neq z) \setminus b
                                          \neg \exists z (Rab \land Raz \land b \neq z) \checkmark
                                         \forall z \neg (Rab \land Raz \land b \neq z) \setminus c
Assignment Project Exam Help
                                           \neg \hat{Rab}
                                                          \neg Rac \quad \neg b \neq c \checkmark
               https://powcoder.com
            Add WeChat powcoder
                                                                                                    [Q p.62]
                                                     \forall xx = a \setminus bc
      (x)
                                                    \neg \forall xx = b \checkmark
                                                    \exists x \neg x = b \checkmark c
                                                          \neg c = b
                                                          b = a
                                                          c = a
                                                          b = c
                                                         \neg b = b
                                                              \times
```

[Q p.62]

Valid.

3. (i) s: Stan

> Fx: x is a firefighter

$$(Fs \land \forall x (Fx \to x = s)) \to \neg \exists x (Fx \land x \neq s)$$

$$\neg ((Fs \land \forall x (Fx \to x = s)) \to \neg \exists x (Fx \land x \neq s))$$

$$Fs \land \forall x (Fx \to x = s) \checkmark$$

$$\neg \neg \exists x (Fx \land x \neq s) \checkmark$$

$$\exists x (Fx \land x \neq s) \checkmark a$$

$$Fs$$

$$\forall x (Fs \to x = s) \land a$$

$$Fa \land a \neq s \checkmark$$

$$Fa$$

$$a \neq s$$

 $Fs \rightarrow a = s \checkmark$ 

### Assignment Project Exam Help

Logical truth.

[Q p.63]

https://powcoder.com

Julius Caesar

dd WeChat powcoder

$$\neg((Lj \land \neg Lc) \to c \neq j) \checkmark$$

$$Lj \land \neg Lc \checkmark$$

$$\neg c \neq j \checkmark$$

$$c = j$$

$$Lj$$

$$\neg Lc$$

$$\neg Lj$$

$$\times$$

Logical truth.

[Q p.63]

(iii) a: Apollo

the sun s:

Wxy: x is warming y

$$\forall x(s \neq x \leftrightarrow Wsx) \rightarrow Wsa$$

# Assignment Project Exam Help

https://powcoder.com

Not a logical truth. Countermodel: Dencial 1 We Chat powcoder

Referents: a:1 s:1

Extension of  $W: \emptyset$ [Q p.63]

(iv) *k*: Kevin Bacon

Michael J. Fox m:

$$k \neq k \rightarrow k = m$$

$$\neg(k \neq k \to k = m) \checkmark \\
k \neq k \\
k \neq m \\
\times$$

Logical truth. ( $k \neq k$  is logically false; any conditional with a logically false antecedent is logically true.) [Q p.63]

Ax: x is an author Wx: x is witty

$$(\forall x ((Ax \land Wx) \to x = t) \land Ac) \to \neg Wc$$

$$\neg((\forall x((Ax \land Wx) \to x = t) \land Ac) \to \neg Wc) \checkmark \\ \forall x((Ax \land Wx) \to x = t) \land Ac \checkmark \\ \neg \neg Wc \checkmark \\ Wc \\ \forall x((Ax \land Wx) \to x = t) \land ct \\ Ac \\ (Ac \land Wc) \to c = t \checkmark$$

## Assignment Project Exam Help $(At \land Wt) \rightarrow t = t \checkmark$

https://powcoder.wom\_= t

Add WeChat powcoder

Not a logical truth. Countermodel:

Domain: {1}

Referents: c:1 t:1

Extensions:  $A : \{1\}$   $W : \{1\}$  [Q p.63]

(vi) Sx: x is a spy Txy: x trusts y

 $\forall x \forall y ((Sx \land Sy \land x \neq y) \rightarrow \neg Txy)$ 

$$\neg \forall x \forall y ((Sx \land Sy \land x \neq y) \rightarrow \neg Txy) \checkmark 
\exists x \neg \forall y ((Sx \land Sy \land x \neq y) \rightarrow \neg Txy) \checkmark a 
\neg \forall y ((Sa \land Sy \land a \neq y) \rightarrow \neg Tay) \checkmark 
\exists y \neg ((Sa \land Sy \land a \neq y) \rightarrow \neg Tay) \checkmark b 
\neg ((Sa \land Sb \land a \neq b) \rightarrow \neg Tab) \checkmark 
Sa \land Sb \land a \neq b \checkmark 
\neg \neg Tab \checkmark 
Tab 
Sa 
Sb$$

Assignment Project Exam Help

Not a logical truth. Countermodel:

Domain:  $\{1,2\}$ 

Referents: a // p/o/w/coder.com

[Q p.63]

(vii) a: this ant WeChat powcoder

 $\forall xx = a \lor \neg \exists xx = a$ 

$$\neg(\forall xx = a \lor \neg \exists xx = a) \checkmark \neg \forall xx = a \checkmark \neg \neg \exists xx = a \checkmark \exists xx = a \checkmark b \exists x\neg x = a \checkmark c b = a \neg c = a \neg c = b \uparrow$$

Not a logical truth. Countermodel:

Domain: {1,2}

Referents: a:1 b:1 c:2 [Q p.63]

(viii) 
$$d$$
: Doug  
 $s$ : Santa Claus  
 $Axy$ :  $x$  is afraid of  $y$   

$$\forall x(x \neq s \rightarrow Adx) \rightarrow (Add \lor d = s)$$

$$\neg(\forall x(x \neq s \rightarrow Adx) \rightarrow (Add \lor d = s)) \checkmark$$

$$\forall x(x \neq s \rightarrow Adx) \backslash d$$

$$\neg(Add \lor d = s) \checkmark$$

$$\neg Add$$

$$\neg d = s$$

$$d \neq s \rightarrow Add$$

$$\neg d = s$$

$$d \neq s \rightarrow Add$$

$$\neg d = s$$

$$d = s$$

$$d = s$$

$$\neg d = d$$

Assignment Project Exam Help

[Q p.63]

https://powcoder.com

Add WeChat powcoder

(ix) 
$$m$$
: Mark  
 $s$ : Samuel  
 $Rxy$ :  $x$  respects  $y$   

$$(Rms \land \forall x (Rmx \rightarrow x = s)) \rightarrow \neg Rmm$$

$$\neg ((Rms \land \forall x (Rmx \rightarrow x = s)) \rightarrow \neg Rmm) \checkmark$$

$$Rms \land \forall x (Rmx \rightarrow x = s) \checkmark$$

$$\neg \neg Rmm \qquad \qquad Rms$$

$$Rms$$

$$\forall x (Rmx \rightarrow x = s) \land ms$$

$$Rmm \rightarrow m = s \checkmark$$

# Assignment Project $\sum_{Rms}^{Rms} \sum_{s=s}^{s=s} M$ Help

https://powcoder.com

Not a logical truth. Countermodel:

Domail d<sup>1</sup> We Chat powcoder

Extension:  $R : \{\langle 1, 1 \rangle\}$  [Q p.63]

Rss

(x) 
$$m$$
: I/me  
 $Px$ :  $x$  is a physical body  
 $Pm \lor \exists x (x = m \land \neg Px)$ 

Logical truth.

[Q p.63]

# Assignment Project Exam Help [Contents]

https://powcoder.com

Add WeChat powcoder

#### **Answers 13.5.1**

1. (i) Gx: x is a gremlin

```
\neg \forall x \forall y \forall z ((Gx \land Gy \land Gz) \rightarrow (x = y \lor x = z \lor y = z)) \checkmark
\exists x \neg \forall y \forall z ((Gx \land Gy \land Gz) \rightarrow (x = y \lor x = z \lor y = z)) \checkmark a
\neg \forall y \forall z ((Ga \land Gy \land Gz) \rightarrow (a = y \lor a = z \lor y = z)) \checkmark
\exists y \neg \forall z ((Ga \land Gy \land Gz) \rightarrow (a = y \lor a = z \lor y = z)) \checkmark b
\neg \forall z ((Ga \land Gb \land Gz) \rightarrow (a = b \lor a = z \lor b = z)) \checkmark
\exists z \neg ((Ga \land Gb \land Gz) \rightarrow (a = b \lor a = z \lor b = z)) \checkmark c
\neg ((Ga \land Gb \land Gc) \rightarrow (a = b \lor a = c \lor b = c)) \checkmark
```

 $\forall x \forall y \forall z ((Gx \land Gy \land Gz) \rightarrow (x = y \lor x = z \lor y = z))$ 

 $Ga \wedge Gb \wedge Gc \checkmark$  $\neg (a = b \lor a = c \lor b = c) \checkmark$ 

## Assignment Project Exam Help

Gc

https://powcoder.com

 $\neg b = c$ 

## Notation 1333 Contato powcoder

Domain: {1,2,3}

Referents: a : 1 b : 2 c : 3Extension of  $G : \{1, 2, 3\}$ 

[Q p.63]

#### (ii) Bx: x is a Beatle

$$\exists x \exists y \exists z (Bx \land By \land Bz \land (x \neq y \land x \neq z \land y \neq z))$$

```
\neg \exists x \exists y \exists z (Bx \land By \land Bz \land (x \neq y \land x \neq z \land y \neq z)) \checkmark
\forall x \neg \exists y \exists z (Bx \land By \land Bz \land (x \neq y \land x \neq z \land y \neq z)) \ \ \langle a \rangle
    \neg \exists y \exists z (Ba \land By \land Bz \land (a \neq y \land a \neq z \land y \neq z)) \checkmark
   \forall y \neg \exists z (Ba \land By \land Bz \land (a \neq y \land a \neq z \land y \neq z)) \ \ \langle a \rangle
       \neg \exists z (Ba \land Ba \land Bz \land (a \neq a \land a \neq z \land a \neq z)) \checkmark
      \forall z \neg (Ba \land Ba \land Bz \land (a \neq a \land a \neq z \land a \neq z)) \setminus a
         \neg (Ba \land Ba \land Ba \land (a \neq a \land a \neq a \land a \neq a)) \checkmark
```

## Assignment Project Exam Help \(^{a \neq a}\)

https://powcoder.com

Not a logical truth. Countermodel:

De Add WeChat powcoder

Referent of a:1Extension of  $B: \emptyset$ 

[Q p.63]

#### (iii) *k*: Kevin Bacon

$$\exists xx = k \land \forall x \forall y ((x = k \land y = k) \rightarrow x = y)$$

$$\neg (\exists xx = k \land \forall x \forall y ((x = k \land y = k) \rightarrow x = y)) \checkmark$$

$$\forall x \neg x = k \land \forall x \forall y ((x = k \land y = k) \rightarrow x = y) \checkmark$$

$$\forall x \neg x = k \land k \quad \exists x \neg \forall y ((x = k \land y = k) \rightarrow x = y) \checkmark$$

$$\neg k = k \quad \neg \forall y ((a = k \land y = k) \rightarrow a = y) \checkmark$$

$$\exists y \neg ((a = k \land y = k) \rightarrow a = y) \checkmark$$

$$\exists y \neg ((a = k \land b = k) \rightarrow a = b) \checkmark$$

$$a = k \land b = k \checkmark$$

$$\neg a = b$$

## Assignment Project Exam Help

 $\neg k = b$  $\neg k = k$ 

https://powcoder.com

Logical truth. (This may seem odd at first sight—but note what it means: on every model of the fragment of GPLI used to state the wff in quastion. (the fragment which contains the name k—the wff comes out true. Of course!—that's not strange at all: every such model assigns exactly one referent to k.) [Q p.63]

#### (iv) Ox: x is an ocean

$$\exists x \exists y (Ox \land Oy \land x \neq y) \rightarrow \exists x Ox$$

$$\neg (\exists x \exists y (Ox \land Oy \land x \neq y) \rightarrow \exists x Ox)$$

$$\exists x \exists y (Ox \land Oy \land x \neq y) \checkmark a$$

$$\neg \exists x Ox \checkmark$$

$$\forall x \neg Ox \land a$$

$$\exists y (Oa \land Oy \land a \neq y) \checkmark b$$

$$Oa \land Ob \land a \neq b \checkmark$$

$$Oa$$

$$Ob$$

$$a \neq b$$

$$\neg Oa$$

$$\checkmark$$

## Assigniment Project Exam Help.63]

(v) Dx: x is a dog

```
Add x y ((Dx \land Dy \land x \neq y \land Lxy) \rightarrow Lyx) \checkmark a

\neg \forall y ((Da \land Dy \land a \neq y \land Lay) \rightarrow \neg Lya) \checkmark

\exists y \neg ((Da \land Dy \land a \neq y \land Lay) \rightarrow \neg Lya) \checkmark b

\neg ((Da \land Db \land a \neq b \land Lab) \rightarrow \neg Lba) \checkmark

Da \land Db \land a \neq b \land Lab \checkmark

\neg \neg Lba \checkmark

Lba

Da

Db

a \neq b

Lab

\uparrow
```

Not a logical truth. Countermodel:

Domain: {1,2}

Referents: a:1 b:2

Extensions:  $D: \{1,2\}$   $L: \{\langle 1,2\rangle, \langle 2,1\rangle\}$  [Q p.64]

#### (vi) Ax: x is an apple

$$(\exists x A x \land \forall x \forall y ((Ax \land Ay) \to x = y)) \to \exists x A x$$

$$\neg ((\exists x A x \land \forall x \forall y ((Ax \land Ay) \to x = y)) \to \exists x A x) \checkmark$$

$$\exists x A x \land \forall x \forall y ((Ax \land Ay) \to x = y) \checkmark$$

$$\neg \exists x A x \checkmark$$

$$\forall x \neg A x \land a$$

$$\exists x A x \checkmark a$$

$$\forall x \forall y ((Ax \land Ay) \to x = y)$$

$$Aa$$

$$\neg Aa$$

$$\land Aa$$

$$\land Aa$$

Logical truth.

[Q p.64]

## Assignment Project Exam Help

 $\begin{array}{l} \neg (\exists x \exists y (Ax \land Ay \land x \neq y) \land \forall x \forall y ((Ax \land Ay) \rightarrow x = y)) \\ \textbf{https://powcoder.com} \end{array}$ 

Logical truth.

[Q p.64]

#### (viii) Sx: x is a snake

$$\neg \exists x Sx \lor \exists x \exists y (Sx \land Sy \land x \neq y)$$

$$\neg (\neg \exists x Sx \lor \exists x \exists y (Sx \land Sy \land x \neq y)) \checkmark$$

$$\neg \neg \exists x Sx \checkmark$$

$$\neg \exists x \exists y (Sx \land Sy \land x \neq y) \checkmark$$

$$\exists x Sx \checkmark$$

$$Sa$$

$$\forall x \neg \exists y (Sx \land Sy \land x \neq y) \land a$$

$$\neg \exists y (Sa \land Sy \land a \neq y) \checkmark$$

$$\forall y \neg (Sa \land Sy \land a \neq y) \land a$$

$$\neg (Sa \land Sa \land a \neq a) \checkmark$$

## Assignment Project Exam Help

Not a logical truth. Countermodel: Dahar PS: // powcoder.com

Referent of a:1

Extension of S: {1}
Add WeChat powcoder

[Q p.64]

#### 2. (i) Rx: x is in the room

$$\exists x \exists y \exists z (Rx \land Ry \land Rz \land x \neq y \land x \neq z \land y \neq z)$$

$$\therefore \exists x \exists y (Rx \land Ry \land Ry \land Rz \land x \neq y \land x \neq z \land y \neq z) \checkmark a$$

$$\neg \exists x \exists y (Rx \land Ry \land Ry \land Ry \land x \neq y) \checkmark$$

$$\exists y \exists z (Ra \land Ry \land Rz \land a \neq y \land a \neq z \land y \neq z) \checkmark b$$

$$\exists z (Ra \land Rb \land Rz \land a \neq b \land a \neq z \land b \neq z) \checkmark c$$

$$Ra \land Rb \land Rc \land a \neq b \land a \neq c \land b \neq c \checkmark$$

$$Ra$$

$$Rb$$

$$Rc$$

$$a \neq b$$

$$a \neq c$$

$$Assignment Project Exam Help$$

$$\neg \exists y (Ra \land Ry \land x \neq y) \checkmark$$

$$\neg \exists y (Ra \land Ry \land a \neq y) \checkmark$$

$$https://po(Ra \land Ry \land a \neq y) \land b$$

$$https://po(Ra \land Ry \land a \neq y) \land b$$

$$Add WeClat powcoder$$

$$Valid. [Q p.64]$$

```
(ii) c:
                                   Canada
                                   x is a bear
                       Bx:
                       Nxy: x is in y
\exists x \exists y (Bx \land By \land Nxc \land Nyc \land x \neq y)
\therefore \forall x \forall y \forall z ((Bx \land By \land Bz \land Nxc \land Nyc \land Nzc) \rightarrow (x = y \lor x = z \lor y = z))
                                  \exists x \exists y (Bx \land By \land Nxc \land Nyc \land x \neq y) \checkmark a
        \neg \forall x \forall y \forall z ((Bx \land By \land Bz \land Nxc \land Nyc \land Nzc) \rightarrow (x = y \lor x = z \lor y = z)) \checkmark
                                    \exists y (Ba \land By \land Nac \land Nyc \land a \neq y) \checkmark b
                                         Ba \wedge Bb \wedge Nac \wedge Nbc \wedge a \neq b \checkmark
                                                              Ва
                                                              Bb
                                                             Nac
                                                             Nbc
                                                            a \neq b
       \exists x \neg \forall y \forall z ((Bx \land By \land Bz \land Nxc \land Nyc \land Nzc) \rightarrow (x = y \lor x = z \lor y = z)) \checkmark d
ASSIGNAME AND OCT (E-XAM \lor y = z)) \checkmark d
         \exists y \neg \forall z ((Ba \land By \land Bz \land Ndc \land Nyc \land Nzc) \rightarrow (d = y \lor d = z \lor y = z)) \checkmark e
             \neg \forall z ((Bd \land Be \land Bz \land Ndc \land Nec \land Nzc) \rightarrow (d = e \lor d = z \lor e = z)) \checkmark
            Bd \wedge Be \wedge Bf \wedge Ndc \wedge Nec \wedge Nfc
                                              \neg (d = e \lor d = f \lor e = f)
                        Add WeChat powcoder
                                                              Bf
                                                             Ndc
                                                             Nec
                                                             Nfc
                                                           \neg d = e
                                                           \neg d = f
                                                           \neg e = f
                                                               \uparrow
                     Invalid. Countermodel:
                     Domain: {1,2,3,4,5,6}
                     Referents: a:1 b:2 c:3 d:4 e:5 f:6
                     Extensions: B : \{1, 2, 4, 5, 6\}
                      N: \{\langle 1,3\rangle, \langle 2,3\rangle, \langle 4,3\rangle, \langle 5,3\rangle, \langle 6,3\rangle\}
                                                                                                               [Q p.64]
```

(iii) Bx: x is a barber Hxy: x cuts y's hair

$$\forall x \forall y ((Bx \land By) \rightarrow x = y)$$
  
 
$$\therefore \forall x (Bx \rightarrow Hxx) \lor \forall x \forall y ((Bx \land By) \rightarrow \neg Hxy)$$

$$\forall x \forall y ((Bx \land By) \rightarrow x = y) \land a$$

$$\neg(\forall x (Bx \rightarrow Hxx) \lor \forall x \forall y ((Bx \land By) \rightarrow \neg Hxy)) \checkmark$$

$$\neg \forall x (Bx \rightarrow Hxx) \checkmark$$

$$\neg \forall x \forall y ((Bx \land By) \rightarrow \neg Hxy) \checkmark$$

$$\exists x \neg (Bx \rightarrow Hxx) \checkmark a$$

$$\exists x \neg \forall y ((Bx \land By) \rightarrow \neg Hxy) \checkmark b$$

$$\neg(Ba \rightarrow Haa) \checkmark$$

$$Ba$$

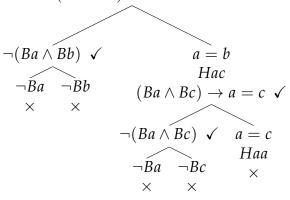
$$\neg Haa$$

Assignment  $F(Bb \land By) \rightarrow F(Bb \land By) \rightarrow F(Bb \land Bc) \rightarrow F(Bb$ 

https://powcoder.com

Bc

Add We Chat powcoder  $(Ba \wedge Bb) \rightarrow a = b \checkmark$ 



Valid. [Q p.64]

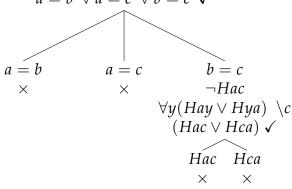
#### (iv) Hxy: x is heavier than y

```
\forall x \forall y \forall z (x = y \lor x = z \lor y = z)
\forall x \forall y (Hxy \lor Hyx)
\therefore \forall x (\forall y (x \neq y \to Hxy) \lor \forall y (x \neq y \to Hyx))
\forall x \forall y \forall z (x = y \lor x = z \lor y = z) \land a
\forall x \forall y (Hxy \lor Hyx) \land a
\neg \forall x (\forall y (x \neq y \to Hxy) \lor \forall y (x \neq y \to Hyx)) \checkmark a
\neg (\forall y (x \neq y \to Hxy) \lor \forall y (x \neq y \to Hyx)) \checkmark a
\neg (\forall y (a \neq y \to Hay) \lor \forall y (a \neq y \to Hya)) \checkmark
\neg \forall y (a \neq y \to Hay) \checkmark
\neg \forall y (a \neq y \to Hay) \checkmark b
\neg (a \neq y \to Hay) \checkmark b
\neg (a \neq b \to Hab) \checkmark
```

## Assignment Project Exam Help

https://powcoder.com

 $y \lor a = z \lor y = z) \lor b$ 



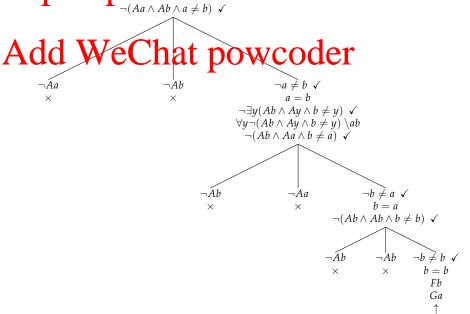
Valid. [Q p.64]

```
(v) Ax: x is an athlete
                                x is a footballer
                  Fx:
                  Gx:
                                x is a golfer
                \exists x (Fx \land Ax)
               \exists x (Gx \land Ax)
               \therefore \exists x \exists y (Ax \land Ay \land x \neq y)
         \exists x (Fx \wedge Ax) \ \checkmark a
         \exists x (Gx \land Ax) \checkmark b
 \neg \exists x \exists y (Ax \land Ay \land x \neq y) \checkmark
\forall x \neg \exists y (Ax \land Ay \land x \neq y) \ \backslash ab
              Fa∧Ăa ✓
                    Fa
                    Aa
              Gb \wedge Ab \checkmark
                    Gb
                    Ab
   \neg \exists y (Aa \land Ay \land a \neq y) \checkmark
  \forall y \neg (Aa \land Ay \land a \neq y) \setminus ab
      \neg(Aa \land Aa \land a \neq a)
```

¬Áa

## Assignment Project Exam Help

https://powcoder.com



Invalid. Countermodel:

Domain: {1}

Referents: a:1 b:1

Extensions:  $F : \{1\}$   $G : \{1\}$   $A : \{1\}$  [Q p.64]

#### (vi) Pxy: x is a part of y

 $\forall x P x x$  $\therefore \forall x \exists y \exists z (Pyx \land Pzx \land y \neq z)$ 

> $\forall x P x x \setminus a$  $\neg \forall x \exists y \exists z (Pyx \land Pzx \land y \neq z) \checkmark$  $\exists x \neg \exists y \exists z (Pyx \land Pzx \land y \neq z) \checkmark a$  $\neg \exists y \exists z (Pya \land Pza \land y \neq z) \checkmark$  $\forall y \neg \exists z (Pya \land Pza \land y \neq z) \setminus a$  $\neg \exists z (Paa \land Pza \land a \neq z) \checkmark$  $\forall z \neg (Paa \land Pza \land a \neq z) \setminus a$  $\neg(Paa \land Paa \land a \neq a) \checkmark$

### Assignment Project Extan Help Paa

Inhttps://powcoder.com

Domain: {1}

Referent of a:1
Example of We that powcoder

(vii) *e*: the Eiffel tower

$$\exists x \exists y (x = e \land y = e \land x \neq y)$$

$$\therefore \neg \exists x x = e$$

$$\exists x \exists y (x = e \land y = e \land x \neq y) \checkmark a$$

$$\neg \neg \exists x x = e$$

$$\exists y (a = e \land y = e \land a \neq y) \checkmark b$$

$$a = e \land b = e \land a \neq b \checkmark$$

$$a = e$$

$$b = e$$

$$a \neq b$$

$$e \neq b$$

$$e \neq b$$

$$e \neq e$$

Assign mentis Projectale xenny Helm at all follows logically from it.) [Qp.64]

https://powcoder.com

Add WeChat powcoder

```
(viii) c:
                  the Chief of Police
          j:
                  Jemima
                  I/me
          m:
          Axy: x is afraid of y
         Amj \wedge Amc
         \therefore j = c \vee \exists x \exists y (Amx \wedge Amy \wedge x \neq y)
                                     Amj \land Amc \checkmark
                      \neg (j = c \lor \exists x \exists y (Amx \land Amy \land x \neq y)) \checkmark
                                            Amj
                                           Amc
                                           j \neq c
                           \neg \exists x \exists y (Amx \land Amy \land x \neq y) \checkmark
                           \forall x \neg \exists y (Amx \land Amy \land x \neq y) \setminus j
Assignment Lange Exam Help
                               \neg (Amj \land Amc \land j \neq c) \checkmark
           https://pow.coder.com
         Add WeChat powcoder
                                                                          [Q p.64]
                                                                       [Contents]
```

#### **Answers 13.6.1.1**

- Vance a: Joseph Conrad c: The Inheritors i: 1: Lord Jim The Shadow Line s: Axy: *x* authored *y* Fxy: *x* is father of *y* Rxy: x reads y Txy: *x* is taller than *y* 1.  $\exists x (\forall y (Ays \leftrightarrow y = x) \land c = x)$ [Q p.65] 2.  $\exists x (\forall y (Ays \leftrightarrow y = x) \land Axl)$ [Q p.65] 5.  $Aci \land \exists x (\forall y (Ayi \leftrightarrow y = x) \land c = x)$ Another possible translation: VCOder.com  $Aci \land \exists x (\forall y (Ayi \leftrightarrow y = x) \land c \neq x)$ The first translated knows that The Inheritors was authored by two persons, one of whom was Joseph Conrad. [Q p.65] 6.  $\exists x (\forall y (Ays \leftrightarrow y = x) \land \forall y (Ayl \rightarrow Txy))$ [Q p.65] 7.  $\exists x (\forall y (Ays \leftrightarrow y = x) \land \exists y Tyx)$ [Q p.65]
  - 8.  $\exists x (\forall y (Ays \leftrightarrow y = x) \land Txc) \land \exists x (\forall y (Ayl \leftrightarrow y = x) \land Tcx) \ [Q p.65]$
  - 9.  $\exists x (\forall y (Ays \leftrightarrow y = x) \land \exists z (\forall y (Fyx \leftrightarrow y = z) \land Tzc))$ [Q p.65]
- 10.  $\exists x (\forall y (Ays \leftrightarrow y = x) \land \exists z (\forall y (Fyx \leftrightarrow y = z) \land Tzx))$ [Q p.65]

[Contents]

#### **Answers 13.6.2.1**

#### Glossary:

<ul> <li>a: Vance</li> <li>c: Joseph Conrad</li> <li>i: The Inheritors</li> <li>l: Lord Jim</li> <li>s: The Shadow Line</li> <li>Axy: x authored y</li> <li>Fxy: x is father of y</li> <li>Rxy: x reads y</li> <li>Txy: x is taller than y</li> </ul>		
$1. c = \imath x A x s$	[Q p.65]	
Assignment Project Exam Help.65] 3. 1xAxs = 1xAxl [Qp.65]		
4. $\forall y (A1x Axy p) Ray)$ powcoder.com 5. $Aci \land c \neq 1x Axi$	[Q p.65]	
Note that this corresponds to the second translation given swers 1250 100 uesto C (see 218) DOWCOCCT	in An- [Q p.65]	
6. $\forall y (Ayl \rightarrow TixAxsy)$	[Q p.65]	
7. $\exists y Ty x Axs$	[Q p.65]	
8. $T1xAxsc \wedge Tc1xAxl$	[Q p.65]	
9. TıyFyıxAxsc	[Q p.65]	
10. TıyFyıxAxsıxAxs	[Q p.65]	
	[Contents]	

#### **Answers 13.6.3.1**

Vance

Joseph Conrad

The Inheritors

#### Glossary:

a:

c:

i:

*l*: Lord Jim The Shadow Line s: the father of the author of *The Shadow Line* the author of *The Inheritors*  $i_2$ :  $l_2$ : the author of Lord Jim the author of The Shadow Line  $s_2$ : x authored y Fxy: *x* is father of *y* Rxy: x reads yAssignment Project Exam Help 1. translation  $\frac{1}{2}$  / powcoder.com uniqueness postulate for  $s_2$  (the author of *The Shadow Line*):  $\forall x (Axs \leftrightarrow x = s_2)$ [Q p.66] 2. translation de la WeChat powcoder uniqueness postulate for  $s_2$ : as above [Q p.66] 3. translation:  $s_2 = l_2$ uniqueness postulate for  $s_2$ : as above uniqueness postulate for  $l_2$  (the author of *Lord Jim*):  $\forall x (Axl \leftrightarrow x = l_2)$ [Q p.66] 4. translation:  $\forall x (Al_2x \rightarrow Rax)$ uniqueness postulate for  $l_2$ : as above [Q p.66] 5. translation:  $Aci \land c \neq i_2$ uniqueness postulate for  $i_2$  (the author of *The Inheritors*):  $\forall x (Axi \leftrightarrow x = i_2)$ Note that this corresponds to the second translation given in An-

[Q p.66]

swers 13.6.1.1 Question 5 (see p.258).

- 6. translation:  $\forall x (Axl \rightarrow Ts_2x)$  uniqueness postulate for  $s_2$ : as above [Q p.66]
- 7. translation:  $\exists x T x s_2$  uniqueness postulate for  $s_2$ : as above [Q p.66]
- 8. translation:  $Ts_2c \wedge Tcl_2$  uniqueness postulates for  $s_2$  and  $l_2$ : as above [Q p.66]
- 9. translation: Tfc uniqueness postulate for f (the father of the author of The Shadow Line):  $\forall x (Fxs_2 \leftrightarrow x = f)$  uniqueness postulate for  $s_2$  (which features in the uniqueness postulate for f): as above [Q p.66]

## 10Atranslation: Thent Project Exam Help uniqueness postulates for f and s2: as above [Qp.66]

## https://powcoder.com

[Contents]

#### **Answers 13.7.4**

## 1. Glossary: Add WeChat powcoder

 $a_n$ : n s(x,y): x + y p(x,y):  $x \times y$  q(x): x squared Ex: x is even Ox: x = x

(i) s	$s(a_2, a_2) = a_4$	[Q p.66]
(ii)	$p(a_2, a_2) = a_4$	[Q p.66]
(iii) s	$s(a_2,a_2)=p(a_2,a_2)$	[Q p.66]
(iv)	$q(a_2) = p(a_2, a_2)$	[Q p.66]
(v)	$\forall x \forall y q(s(x,y)) = p(s(x,y),s(x,y))$	[Q p.66]

(vi)	$\forall x \forall y q(s(x,y)) = s(s(q(x), p(a_2, p(x,y))), q(y))$ Note that we have represented $2xy$ using the $two$ -place symbol $p$ . This means that we have to represent it as $p(a_1, b_2, b_3)$	$a_2, p(x,y)$
	i.e. $2 \times (x \times y)$ —or as $p(p(a_2, x), y)$ —i.e. $(2 \times x) \times y$ . Both are equally good. Similar comments apply to represent $2xy + y^2$ using the <i>two-place</i> function symbol $s$ .	
(vii)	$\forall x((Ex \lor Ox) \to Ep(a_2, x))$	[Q p.66]
(viii)	$\forall x((Ox \to Op(a_3, x)) \land (Ex \to Ep(a_3, x)))$	[Q p.66]
(ix)	$\forall x L p(a_5, x) p(a_6, x)$	[Q p.66]
(x)	$\forall x \forall y (Lxy \to Lp(a_3, x)p(a_4, y))$	[Q p.66]
2. (i)	True	[Q p.67]
(ii)	False	[Q p.67]
A <sup>(iii)</sup>	argnment Project Exam He	[Q p.67]
` '	True	[Q p.67]
	Trattps://powcoder.com	[Q p.67]
	m	[Q p.68]
(ix)	True dd WeChat powcoder	[Q p.68]
	False	[Q p.68]
3. (i)	False	[Q p.68]
(ii)	False	[Q p.68]
(iii)	True	[Q p.68]
(iv)	False	[Q p.68]
(v)	True	[Q p.68]
(vi)	True	[Q p.68]
(vii)	True	[Q p.68]
(viii)	True	[Q p.68]
(ix)	False	[Q p.68]
(x)	False	[Q p.68]

```
(i) (a) Domain: {1,2}
                Referents: a: 1
                                          b: 2
                Value of f: \{\langle 1, 1 \rangle, \langle 2, 1 \rangle\}
           (b) Domain: {1,2}
                Referents: a: 1
                                          b: 2
                Value of f: \{\langle 1, 1 \rangle, \langle 2, 2 \rangle\}
                                                                                        [Q p.69]
     (ii) (a) Domain: {1,2}
                Referents: a: 1
                Value of f: \{\langle 1,1\rangle, \langle 2,2\rangle\}
           (b) Domain: {1,2}
                Referents: a: 1
                Value of f: \{\langle 1,1\rangle, \langle 2,1\rangle\}
                                                                                        [Q p.69]
    (iii) (a) No model: reflexivity of identity.
           (b) Domain: {1,2}
Assignment Project Exam Help.69]
    (iv) (a) Domain: {1,2}
          Value of f; \{\langle 1,1\rangle, \langle 2,1\rangle\} (b) Walle of f; \{\langle 1,1\rangle, \langle 2,1\rangle\} codes from Canal American
                                                                                        [Q p.69]
     (v) (a) Domain: {1}
          (b) Alueof (1,2) Chat powcoder
                Value of f: \{\langle 1,1\rangle, \langle 2,1\rangle\}
                                                                                        [Q p.69]
    (vi) (a) Domain: {1,2}
                Value of s: \{(1,1,1), (1,2,2), (2,1,2), (2,2,1)\}
           (b) Domain: {1,2}
                Value of s: \{(1,1,1), (1,2,1), (2,1,2), (2,2,1)\}
                                                                                        [Q p.69]
   (vii) (a) Domain: {1,2}
                Values: f: \{\langle 1, 1 \rangle, \langle 2, 2 \rangle\}
                s: \{\langle 1,1,1\rangle, \langle 1,2,2\rangle, \langle 2,1,2\rangle, \langle 2,2,1\rangle\}
           (b) Domain: {1,2}
                Values: f: \{\langle 1,2\rangle, \langle 2,2\rangle\}
                s: \{\langle 1,1,1\rangle, \langle 1,2,2\rangle, \langle 2,1,2\rangle, \langle 2,2,1\rangle\}
                                                                                        [Q p.69]
```

```
(viii) (a) Domain: {1,2}
                 Values: f: \{\langle 1,2 \rangle, \langle 2,1 \rangle\}
                 s: \{\langle 1,1,1\rangle,\langle 1,2,2\rangle,\langle 2,1,2\rangle,\langle 2,2,1\rangle\}
           (b) Domain: {1,2}
                Values: f: \{\langle 1, 2 \rangle, \langle 2, 1 \rangle\}
                s: \{\langle 1,1,1\rangle, \langle 1,2,2\rangle, \langle 2,1,1\rangle, \langle 2,2,2\rangle \}
                                                                                            [Q p.69]
    (ix) (a) Domain: \{1,2\}
                 Values: f: \{\langle 1,2\rangle, \langle 2,1\rangle\}
                 s: \{\langle 1,1,1\rangle, \langle 1,2,1\rangle, \langle 2,1,2\rangle, \langle 2,2,2\rangle\}
           (b) Domain: {1,2}
                 Values: f: \{\langle 1,2 \rangle, \langle 2,1 \rangle\}
                 s: \{\langle 1,1,2\rangle, \langle 1,2,2\rangle, \langle 2,1,1\rangle, \langle 2,2,1\rangle\}
                                                                                            [Q p.69]
     (x) (a) Domain: \{1,2\}
                 Value of s: \{(1,1,1), (1,2,1), (2,1,2), (2,2,1)\}
ASSI Such a three is exactly by Cobject 2 And the dontar Guld that
                 s(x,y) = z; it is built into the semantics of GPLIF that on
                 every model, s (a two-place function symbol) is assigned a
             https://poweodencom
                                                                                            [Q p.69]
                                                                                        [Contents]
```

### Add WeChat powcoder

## **Chapter 14**

## Metatheory

#### **Answers 14.1.1.1**

1A <sup>0</sup> 2. 3	ssignment Project Exam H	e[Q p.70] [Q p.70]
3. 1	https://powcoder.com	[Q p.70]
4. 3	https://powcoder.com	[Q p.70]
5. 3	Add WeChat powender	[Q p.70]
6. 3	Add WeChat powcoder	[Q p.70]
7. 5		[Q p.70]
8. 5		[Q p.70]
9. 10		[Q p.70]
10. 15		[Q p.70]
		[Contents]

#### **Answers 14.1.2.1**

1. Let p be a path featuring  $(\alpha \wedge \beta)$ . Suppose there is a model  $\mathfrak{M}$  on which every proposition on p is true. Let p' be the path obtained from p by adding  $\alpha$  and  $\beta$ . By clause 3 of §9.4.2, we know that  $\alpha$  must be true on  $\mathfrak{M}$ , since  $(\alpha \wedge \beta)$  is. By clause 3 of §9.4.2, we know that  $\beta$  must

be true on  $\mathfrak{M}$ , since  $(\alpha \land \beta)$  is. Since  $\alpha$  and  $\beta$  are the only propositions that were added to p to get p', we know that every proposition on p' is true on  $\mathfrak{M}$ . So there is a model on which all propositions on p' are true. Therefore the tree rule for unnegated conjunction is truth-preserving. [Q p.71]

- 2. Let p be a path featuring  $\neg(\alpha \land \beta)$ . Suppose there is a model  $\mathfrak{M}$  on which every proposition on p is true. Let q be the path obtained from p by adding  $\neg \alpha$ , and let r be the path obtained from p by adding  $\neg \beta$ . Since  $\neg(\alpha \land \beta)$  is true on  $\mathfrak{M}$ , we know that  $(\alpha \land \beta)$  is false on  $\mathfrak{M}$ , by clause 2 of  $\S 9.4.2$ . Thus, either  $\alpha$  is false on  $\mathfrak{M}$  or  $\beta$  is true on  $\mathfrak{M}$ , by clause 2 of  $\S 9.4.2$ . Thus, either  $\neg \alpha$  is true on  $\mathfrak{M}$  or  $\neg \beta$  is true on  $\mathfrak{M}$ , or all propositions on r are true on  $\mathfrak{M}$ . So either there is a model on which every proposition on q is true, or there is a model on which every proposition on r is true. Therefore the tree rule for negated **Acquiremental proposition Therefore Therefor**
- 3. Let p be a path featuring  $(\alpha \to \beta)$ . Suppose there is a model  $\mathfrak{M}$  on which every proposition on p is true. Let q be the path obtained from p by adding  $\beta$  and let by  $\alpha$  be the path obtained from p by adding  $\beta$ . Since  $(\alpha \to \beta)$  is true on  $\mathfrak{M}$ , we know that either  $\alpha$  is false on  $\mathfrak{M}$  or  $\beta$  is true on  $\mathfrak{M}$ , by clause 6 of §9.4.2. Thus, either  $\neg \alpha$  is true on  $\mathfrak{M}$  or  $\beta$  is true on  $\mathfrak{M}$ , or all propositions on q are true on  $\mathfrak{M}$ , or all propositions on q are true on  $\mathfrak{M}$ , or all propositions on q is true, or there is a model on which every proposition on q is true, or there is a model on which every proposition on r is true. Therefore the tree rule for negated conjunction is truth-preserving. [Q p.71]
- 4. Let p be a path featuring  $\neg(\alpha \to \beta)$ . Suppose there is a model  $\mathfrak{M}$  on which every proposition on p is true. Let p' be the path obtained from p by adding  $\alpha$  and  $\neg\beta$ . Since  $\neg(\alpha \to \beta)$  is true on  $\mathfrak{M}$ , we know that  $\alpha \to \beta$  is false on  $\mathfrak{M}$ , by clause 2 of §9.4.2. So  $\alpha$  is true on  $\mathfrak{M}$  and  $\beta$  is false on  $\mathfrak{M}$ , by clause 6 of §9.4.2. So  $\alpha$  is true on  $\mathfrak{M}$  and  $\neg\beta$  is true on  $\mathfrak{M}$ , by clause 2 of §9.4.2. So all propositions on p' are true on  $\mathfrak{M}$ . So there is a model on which all propositions on p' are true. Therefore the tree rule for negated conditional is truth-preserving. [Q p.71]
- 5. Let p be a path featuring  $(\alpha \leftrightarrow \beta)$ . Suppose there is a model  $\mathfrak{M}$  on which every proposition on p is true. Let q be the path obtained from p by adding  $\alpha$  and  $\beta$ , and let r be the path obtained from p by adding  $\neg \alpha$  and  $\neg \beta$ . Either  $\alpha$  and  $\beta$  are both true on  $\mathfrak{M}$ , or  $\alpha$  and  $\beta$  are both

false on  $\mathfrak{M}$ , by clause 7 of §9.4.2. Thus either  $\alpha$  and  $\beta$  are both true on  $\mathfrak{M}$ , or  $\neg \alpha$  and  $\neg \beta$  are both true on  $\mathfrak{M}$ , by clause 2 of §9.4.2. .So either there is a model on which every proposition on q is true, or there is a model on which every proposition on r is true. Therefore the tree rule for unnegated biconditional is truth-preserving. [Q p.71]

6. Let p be a path featuring  $\neg(\alpha \leftrightarrow \beta)$ . Suppose there is a model  $\mathfrak{M}$  on which every proposition on p is true. Let q be the path obtained from p by adding  $\alpha$  and  $\neg\beta$ , and let r be the path obtained from p by adding  $\neg\alpha$  and  $\beta$ . We know that  $(\alpha \leftrightarrow \beta)$  is false on  $\mathfrak{M}$ , by clause 2 of §9.4.2. So either  $\alpha$  is true on  $\mathfrak{M}$  and  $\beta$  is false on  $\mathfrak{M}$ , or  $\alpha$  is false on  $\mathfrak{M}$  and  $\beta$  is true on  $\mathfrak{M}$ , by clause 7 of §9.4.2. So either  $\alpha$  and  $\neg\beta$  are true on  $\mathfrak{M}$ , or  $\neg\alpha$  and  $\beta$  are true on  $\mathfrak{M}$ , by clause 2 of §9.4.2. So either every proposition on q is true on  $\mathfrak{M}$ , or every proposition on r is true on  $\mathfrak{M}$ . So either there is a model on which every proposition on r is true. Therefore the true of the pregated bic proditional is true.

Athereforether remains the properties of the pro

7. Let p be a path featuring  $\neg \neg \alpha$ . Suppose there is a model  $\mathfrak{M}$  on which every proposition on plante. Let path blained from p by adding  $\alpha$ . We know that  $\neg \alpha$  is false on  $\mathfrak{M}$ , by clause 2 of §9.4.2. And so we know that  $\alpha$  is true on  $\mathfrak{M}$ , again by clause 2 of §9.4.2. So there is a modal on which the true paints  $\alpha$  of  $\alpha$  the true of  $\alpha$  rule for negated conditional is truth preserving. [Q p.71]

[Contents]

#### **Answers 14.1.3.1**

- 1.  $\alpha$  is of the form  $(\beta \wedge \delta)$ ; so the formula  $\neg \alpha$  which we are considering is of the form  $\neg(\beta \wedge \delta)$ . Then  $\neg \beta$  or  $\neg \delta$  also occurs on p. The complexities of these wffs are less than the complexity of  $\neg(\beta \wedge \delta)$ , so by the induction hypothesis, whichever of them is on p is true on  $\mathfrak{M}$ . So  $\neg(\beta \wedge \delta)$  is also true on  $\mathfrak{M}$ . [Q p.71]
- 2.  $\alpha$  is of the form  $(\beta \to \delta)$ ; so the formula  $\neg \alpha$  which we are considering is of the form  $\neg(\beta \to \delta)$ . Then  $\beta$  and  $\neg \delta$  also occur on  $\rho$ . The complexities of these wffs are less than the complexity of  $\neg(\beta \to \delta)$ , so by the induction hypothesis,  $\beta$  and  $\neg \delta$  are true on  $\mathfrak{M}$ . So  $\neg(\beta \to \delta)$  is also true on  $\mathfrak{M}$ .

- 3.  $\alpha$  is of the form  $(\beta \leftrightarrow \delta)$ ; so the formula  $\neg \alpha$  which we are considering is of the form  $\neg(\beta \leftrightarrow \delta)$ . Then either  $\beta$  and  $\neg \delta$ , or  $\neg \beta$  and  $\delta$ , also occur on p. The complexities of all these wffs are less than the complexity of  $\neg(\beta \leftrightarrow \delta)$ , so by the induction hypothesis, whichever pair of them is on p, both formulas in the pair are true on  $\mathfrak{M}$ . Either way,  $\neg(\beta \leftrightarrow \delta)$  is also true on  $\mathfrak{M}$ .
- 4.  $\alpha$  is of the form  $\exists \underline{x}\beta$ ; so the formula  $\neg \alpha$  which we are considering is of the form  $\neg \exists \underline{x}\beta$ . Then  $\forall \underline{x} \neg \beta$  also occurs on p. By the clause earlier in step (III) covering the case of wffs on p whose main operator is the universal quantifier,  $\forall \underline{x} \neg \beta$  is true on  $\mathfrak{M}$ . So by the reasoning in §10.1.1 (which establishes that  $\neg \exists \underline{x}\beta$  and  $\forall \underline{x} \neg \beta$  are true and false in exactly the same models),  $\neg \exists \underline{x}\beta$  is also true on  $\mathfrak{M}$ . [Q p.71]
- 5.  $\gamma$  is of the form  $(\alpha \leftrightarrow \beta)$ . Then either  $\alpha$  and  $\beta$ , or  $\neg \alpha$  and  $\neg \beta$ , also occur on p. (i) Suppose it is the former pair. The complexities of  $\alpha$ and  $\beta$  are less than the complexity of  $(\alpha \leftrightarrow \beta)$ , so by the influction hypothesis a aria pare true on It. So by the full governing the fruth of biconditionals in models,  $(\alpha \leftrightarrow \beta)$  is also true on  $\mathfrak{M}$ . (ii) Suppose it is the latter pair. The complexities of  $\neg \alpha$  and  $\neg \beta$  are not necessarily less than the complex to of W & O Bis to atomic wff (i.e. it has complexity  $(\mathfrak{I})$ , then  $\neg \mathfrak{A}$  and  $(\alpha \leftrightarrow \beta)$  have the same complexity; if  $\alpha$ is an atomic wff, then  $\neg \beta$  and  $(\alpha \leftrightarrow \beta)$  have the same complexity. If neither  $\alpha$  had  $\beta$  satisfies, then the complexities of  $\alpha$  and  $\beta$  are less than the complexity of  $(\alpha \leftrightarrow \beta)$  so by the induction hypothesis  $\neg \alpha$  and  $\neg \beta$  are true on  $\mathfrak{M}$ ; and so by the rule governing the truth of biconditionals in models,  $(\alpha \leftrightarrow \beta)$  is also true on  $\mathfrak{M}$ . If one or both of  $\alpha$  or  $\beta$  is atomic, we need to reason in a way similar to that used in the clause earlier in step (III) covering the case of wffs on p whose main operator is the conditional. [Q p.71]

[Contents]

### Chapter 15

#### Other Methods of Proof

#### **Answers 15.1.5**

# Assignment Project Exam Help

https://powcoder.com

[Q p.72]

(ii) 1. P A
2. P (Q) P (A1)
3Add WeChatrpowcoder

[Q p.72]

(iii) 1. 
$$\neg Q$$
 A  
2.  $\neg Q \rightarrow (\neg P \rightarrow \neg Q)$  (A1)  
3.  $(\neg P \rightarrow \neg Q) \rightarrow ((\neg P \rightarrow Q) \rightarrow P)$  (A3)  
4.  $(\neg P \rightarrow \neg Q)$  1, 2 (MP)  
5.  $(\neg P \rightarrow Q) \rightarrow P$  3, 4 (MP)

[Q p.72]

(iv) 1. 
$$P \to (P \to P)$$
 (A1)  
2.  $P \to ((P \to P) \to P)$  (A1)  
3.  $(P \to ((P \to P) \to P)) \to ((P \to (P \to P)) \to (P \to P))$  (A2)  
4.  $(P \to (P \to P)) \to (P \to P)$  2, 3 (MP)  
5.  $P \to P$  1, 4 (MP)

```
(v) 1. \neg(P \rightarrow \neg Q) A

2. (\neg Q \rightarrow \neg(P \rightarrow \neg Q)) \rightarrow ((\neg Q \rightarrow (P \rightarrow \neg Q)) \rightarrow Q) (A3)

3. \neg(P \rightarrow \neg Q) \rightarrow (\neg Q \rightarrow \neg(P \rightarrow \neg Q)) (A1)

4. \neg Q \rightarrow \neg(P \rightarrow \neg Q) 1, 3 (MP)

5. (\neg Q \rightarrow (P \rightarrow \neg Q)) \rightarrow Q 2, 4 (MP)

6. \neg Q \rightarrow (P \rightarrow \neg Q) (A1)

7. Q 5, 6 (MP)

[Q p.72]
```

(vi) 1. 
$$P$$
 A  
2.  $\neg P$  A  
3.  $(\neg Q \rightarrow \neg P) \rightarrow ((\neg Q \rightarrow P) \rightarrow Q)$  (A3)  
4.  $\neg P \rightarrow (\neg Q \rightarrow \neg P)$  (A1)

## Assignment Project Exame Help

7.  $P \rightarrow (\neg Q \rightarrow P)$  (A1) 8.  $\neg Q \rightarrow P$  1,7 (MP) https://powcoder.comP)

[Q p.72]

## (vii) PAdd (WeChat powcoder

1. 
$$\neg (P \rightarrow \neg Q)$$
 A  
2.  $\neg (P \rightarrow \neg Q) \rightarrow ((P \rightarrow \neg Q) \rightarrow \neg (P \rightarrow \neg Q))$  (A1)  
3.  $(P \rightarrow \neg Q) \rightarrow \neg (P \rightarrow \neg Q)$  1, 2 (MP)

[Q p.72]

[Q p.72]

2. (i) 1. 
$$\neg (P \rightarrow \neg Q) \vdash Q$$
 \*
2.  $\vdash \neg (P \rightarrow \neg Q) \rightarrow Q$  1, DT

\* Lines 1–7 of proof in Answer 1v. [Q p.72]

(ii) 
$$(P \lor Q) := (\neg P \to Q)$$
  
1.  $P, \neg P \vdash Q$  \*  
2.  $P \vdash (\neg P \to Q)$  1, DT  
3.  $\vdash P \to (\neg P \to Q)$  2, DT

\* Lines 1–9 of proof in Answer 1vi.

```
(iii)
                                                                                                   Α
                                                                                                   A
                 Q \atop (Q \to (P \to Q))
                                                                                                   A
                                                                                                   (A1)
                 \begin{array}{c} (P \to Q) \\ (P \to R) \end{array}
                                                                                                   3, 4 (MP)
         6.
                                                                                                   1, 5 (MP)
         7.
                                                                                                   2, 6 (MP)
                  ((P \to Q) \to (P \to R)), P, Q \vdash R
         8.
                                                                                                   1-7
                  ((P \rightarrow Q) \rightarrow (P \rightarrow R)), P \vdash (Q \rightarrow R)
         9.
                                                                                                   8, DT
         10. ((P \rightarrow Q) \rightarrow (P \rightarrow R)) \vdash (P \rightarrow (Q \rightarrow R))
                                                                                                   9, DT
         11. \vdash ((P \rightarrow Q) \rightarrow (P \rightarrow R)) \rightarrow (P \rightarrow (Q \rightarrow R))
                                                                                                   10, DT
                                                                                                     [Q p.72]
```

(v) 1. 
$$P \to Q$$
 A  
2.  $P \to \neg Q$  A  
3.  $(\neg \neg P \to \neg Q) \to ((\neg \neg P \to Q) \to \neg P)$  (A3)  
4.  $\neg \neg P \to Q$  \*  
5.  $\neg \neg P \to \neg Q$  †  
6.  $(\neg \neg P \to Q) \to \neg P$  3, 5 (MP)  
7.  $\neg P$  4, 6 (MP)

- \* 1, line 7 of proof in Fig. 15.8 (p.396).
- † 1, line 7 of a proof which is just like that in Fig. 15.8 (p.396) except that it has  $\neg Q$  in place of Q throughout. [Q p.72]

```
(vi) 1. P \rightarrow Q
                                                                                                                                                                                                                                                                                                                                                                                                                    Α
                                                                        2. \neg O \rightarrow P
                                                                                                                                                                                                                                                                                                                                                                                                                    A
                                                                        3. (P \rightarrow Q) \rightarrow (\neg Q \rightarrow \neg P)
                                                                                                                                                                                                                                                                                                                                                                                                                     *
                                                                        4. \neg Q \rightarrow \neg P
                                                                                                                                                                                                                                                                                                                                                                                                                    1, 3 (MP)
                                                                       5. (\neg Q \rightarrow \neg P) \rightarrow ((\neg Q \rightarrow P) \rightarrow Q) (A3)
                                                                       6. (\neg Q \rightarrow P) \rightarrow Q
                                                                                                                                                                                                                                                                                                                                                                                                                   4, 5 (MP)
                                                                        7. Q
                                                                                                                                                                                                                                                                                                                                                                                                                    2, 6 (MP)
                                                                              * Line 11 of proof in Answer 2iv.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       [Q p.72]
                     (vii) 1. P \rightarrow (Q \rightarrow R)
                                                                                                                                                                                                                                                                                                                                                                                                                                                            Α
                                                                        2. Q
                                                                                                                                                                                                                                                                                                                                                                                                                                                            A
                                                                        3. P
                                                                                                                                                                                                                                                                                                                                                                                                                                                            Α
                                                                        4. Q \rightarrow R
                                                                                                                                                                                                                                                                                                                                                                                                                                                            1, 3 (MP)
                                                                                                                                                                                                                                                                                                                                                                                                                                                            2, 4 (MP)
                                                                                                                                                                                                                                                                                                                                                                                                                                                           1-5
  Assignment (Q \rightarrow R) \rightarrow (Q \rightarrow R) \rightarrow (P 
                                                                        8. P \rightarrow (Q \rightarrow R) \vdash Q \rightarrow (P \rightarrow R)
                                                                                                                                                                                                                                                                                                                                                                                                                                                            7, DT
                                                                       9. \vdash (P \rightarrow (Q \rightarrow R)) \rightarrow (Q \rightarrow (P \rightarrow R)) 8, DT
                                                                            https://powcoder.com
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      [Q p.72]
3.
                                                                      <sup>1</sup>Add We Chat powsoder
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             Α
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             (A9')
                                                                                                                  P \to (\neg P \to P)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             (A1)
                                                                                                                  \neg P \rightarrow P
                                                                         4.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             1, 3 (MP)
                                                                                                                  (\neg P \rightarrow \neg P) \rightarrow \neg \neg P
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             2, 4 (MP)
                                                                                                                  \neg P \rightarrow (\neg P \rightarrow \neg P)
                                                                         6.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             (A1)
                                                                         7.
                                                                                                                (\neg P \to (\neg P \to \neg P)) \to ((\neg P \to ((\neg P \to \neg P) \to \neg P)) \to (\neg P \to \neg P))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            (A2')
                                                                                                                  (\neg P \to ((\neg P \to \neg P) \to \neg P)) \to (\neg P \to \neg P)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             6,7 (MP)
                                                                                                                \neg P \rightarrow ((\neg P \rightarrow \neg P) \rightarrow \neg P)
                                                                        9.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             (A1)
                                                                        10. \neg P \rightarrow \neg P
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            8,9 (MP)
                                                                        11. \neg \neg P
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             5, 10 (MP)
                                                                        12. P \vdash \neg \neg P
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             1 - 11
                                                                         13. \vdash P \rightarrow \neg \neg P
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             12, DT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       [Q p.72]
```

```
(ii) 1. P \rightarrow \neg P
              2. (P \rightarrow \neg P) \rightarrow ((P \rightarrow \neg \neg P) \rightarrow \neg P) (A9')
3. (P \rightarrow \neg \neg P) \rightarrow \neg P 1.2 (1
              3. (P \rightarrow \neg \neg P) \rightarrow \neg P
                                                                                     1, 2 (MP)
              4. P \rightarrow \neg \neg P
              5. \neg P
                                                                                     3, 4 (MP)
               * Line 13 of proof in Answer 3i
                                                                                                            [Q p.73]
    (iii) 1. P \rightarrow Q
                                                                                A
              2. \neg Q
                                                                                Α
              3. (P \rightarrow Q) \rightarrow ((P \rightarrow \neg Q) \rightarrow \neg P) (A9')

4. (P \rightarrow \neg Q) \rightarrow \neg P 1, 3 (No. 1)

5. \neg Q \rightarrow (P \rightarrow \neg Q) (A1)

6. P \rightarrow \neg Q 2, 5 (No. 1)
                                                                                1, 3 (MP)
                                                                                2, 5 (MP)
                                                                                4,6 (MP)
Assignment Project Exam Help
                                                                                                            [p.73]
    (iv) https://powcoder.com
                                                                                           1,4 (MP)
                      (\neg P \to Q) \to ((\neg P \to \neg Q) \to \neg \neg P) \quad (A9')(\neg P \to \neg Q) \to \neg \neg P \qquad 5,7 \text{ (A9')}
                                                                                           5, 7 (MP)
              9.
                       \neg \neg P
                                                                                           6,8 (MP)
               10. \neg \neg P \rightarrow P
                                                                                           (A10')
              11. P
                                                                                           9, 10 (MP)
              12. \neg Q, Q \vdash P
                                                                                           1-11
              13. \neg Q \vdash Q \rightarrow P
                                                                                           12, DT
               14. \vdash \neg Q \rightarrow (Q \rightarrow P)
                                                                                           13, DT
                                                                                                            [Q p.73]
      (v) 1. P \wedge Q
              2. (P \land Q) \to Q (A5')
3. Q 1, 2 (MP)
              4. \overrightarrow{Q} \rightarrow (P \rightarrow Q) (A1)
5. P \rightarrow Q 3,4 (1)
                                                 3, 4 (MP)
```

[Q p.73]

(vi) 1. 
$$\neg Q$$
 A  
2.  $(P \to P) \to ((Q \to P) \to ((P \lor Q) \to P))$  (A8')  
3.  $P \to P$  \*  
4.  $(Q \to P) \to ((P \lor Q) \to P)$  2, 3 (MP)  
5.  $\neg Q \to (Q \to P)$  †  
6.  $Q \to P$  1, 5 (MP)  
7.  $(P \lor Q) \to P$  4, 6 (MP)

- \* Mimic lines 6–10 of the proof in Answer 3i, with P in place of  $\neg P$  throughout. Alternatively, line 3 of the following proof:
  - 1. *P* A
  - 2.  $P \vdash P$  1 (i.e. 1–1)
  - 3.  $\vdash P \rightarrow P$  2, DT

## Assignment Project Exam Help

```
(viii) 1.
                 \neg (P \lor Q)
                                                                                 Α
                                                                                 (A6')
                  P \to (P \vee Q)
                 \neg(P \lor Q) \to (P \to \neg(P \lor Q))
                                                                                 (A1)
                  P \rightarrow \neg (P \lor Q)
                                                                                 1, 3 (MP)
                  (P \to (P \lor Q)) \to ((P \to \neg(P \lor Q)) \to \neg P)
                                                                                 (A9')
                  (P \to \neg (P \lor Q)) \to \neg P
                                                                                 2, 5 (MP)
           7.
                  \neg P
                                                                                 4, 6 (MP)
           8.
                  Q \rightarrow (P \lor Q)
                                                                                 (A7')
                  \neg(P \lor Q) \to (Q \to \neg(P \lor Q))
           9.
                                                                                 (A1)
           10. Q \rightarrow \neg (P \lor Q)
                                                                                 1, 9 (MP)
           11. (Q \to (P \lor Q)) \to ((Q \to \neg (P \lor Q)) \to \neg Q)
                                                                               (A9')
                 (Q \to \neg (P \lor Q)) \to \neg Q
           12.
                                                                                 8, 11 (MP)
           13.
                 \neg Q
                                                                                 10, 12 (MP)
           14. \neg P \rightarrow (\neg Q \rightarrow (\neg P \land \neg Q))
15. \neg Q \rightarrow (\neg P \land \neg Q)
                                                                                 (A3')
                                                                                 7, 14 (MP)
Assignment Project Exam Help.73]
          16. \neg P \land \neg Q
```

(ix) 
$$\frac{1}{2} \frac{(P \wedge P)}{(P \wedge P)} \frac{P}{P} \text{powcoder.com}$$

$$3. \quad ((P \wedge \neg P) \rightarrow P) \rightarrow (((P \wedge \neg P) \rightarrow \neg P) \rightarrow \neg (P \wedge \neg P))$$

$$4. \quad ((P \wedge \neg P) \rightarrow \neg P) \rightarrow \neg (P \wedge \neg P)$$

$$5 \text{Add} \quad \text{we Chat powcoder}$$

$$1, 3 \text{ (MP)}$$

$$[Q p.73]$$

```
(x) 1.
                P \wedge \neg P
                                                                                 Α
        2.
                (P \land \neg P) \rightarrow P
                                                                                 (A4')
                (P \land \neg P) \rightarrow \neg P
                                                                                 (A5')
        4.
                                                                                 1, 2 (MP)
        5.
                \neg P
                                                                                 1, 3 (MP)
                P \rightarrow (\neg Q \rightarrow P)
                                                                                 (A1)
             \neg P \to (\neg Q \to \neg P)
                                                                                 (A1)
                \neg O \rightarrow P
        8.
                                                                                 4, 6 (MP)
                \neg O \rightarrow \neg P
        9.
                                                                                 5,7 (MP)
       10. (\neg Q \rightarrow P) \rightarrow ((\neg Q \rightarrow \neg P) \rightarrow \neg \neg Q)
                                                                                 (A9')
        11. (\neg Q \rightarrow \neg P) \rightarrow \neg \neg Q
                                                                                 8, 10 (MP)
        12. \neg \neg O
                                                                                 9, 11 (MP)
        13. \neg \neg Q \rightarrow Q
                                                                                 (A10')
        14. Q
                                                                                 12, 13 (MP)
        15. P \wedge \neg P \vdash Q
                                                                                 1-14
```

## Assignment Project Exam Help.73]

```
(xi) Phttps://powcoder.com
        2. (P \rightarrow P) \rightarrow (((P \rightarrow P) \rightarrow \neg (P \rightarrow P)) \rightarrow (P \rightarrow P))
                                                                                           (A1)
        1, 2 (MP)
                                                                                            (A9)
              ((((P \to P) \to \neg(P \to P)) \to \neg(P \to P)) \to \neg((P \to P) \to \neg(P \to P)))
                                                                                            3, 4 (MP)
        5. (((P \rightarrow P) \rightarrow \neg (P \rightarrow P)) \rightarrow \neg (P \rightarrow P)) \rightarrow \neg ((P \rightarrow P) \rightarrow \neg (P \rightarrow P))
        6. ((P \rightarrow P) \rightarrow \neg (P \rightarrow P)) \rightarrow \neg (P \rightarrow P)
        7. \neg((P \rightarrow P) \rightarrow \neg(P \rightarrow P))
                                                                                            5, 6 (MP)
         * See line 3 of the proof in Answer 3vi.
         † The proof in Answer 3ii plus DT gives \vdash (P \rightarrow \neg P) \rightarrow \neg P.
            Mimic this proof, with (P \rightarrow P) in place of P throughout,
            and the resulting proof plus DT gives:
```

[Q p.73]

 $\vdash ((P \rightarrow P) \rightarrow \neg (P \rightarrow P)) \rightarrow \neg (P \rightarrow P).$ 

(xii) 1. 
$$P$$
 A
2.  $\neg P$  A
3.  $P \to (\neg Q \to P)$  (A1)
4.  $\neg Q \to P$  1,3 (MP)
5.  $(\neg Q \to P) \to ((\neg Q \to \neg P) \to \neg \neg Q)$  (A9')
6.  $(\neg Q \to \neg P) \to \neg \neg Q$  4,5 (MP)
7.  $\neg P \to (\neg Q \to \neg P)$  (A1)
8.  $\neg Q \to \neg P$  2,7 (MP)
9.  $\neg \neg Q$  6,8 (MP)
10.  $\neg \neg Q \to Q$  (A10')
11.  $Q$  9, 10 (MP)
12.  $P, \neg P \vdash Q$  1–11
13.  $P \vdash \neg P \to Q$  12, DT
14.  $\vdash P \to (\neg P \to Q)$  13, DT

#### Assignment Project Exam Help

3.  $\forall x(Fx \rightarrow Gx) \rightarrow (Fa \rightarrow Ga)$  (A4)  $\frac{4}{5}$   $\frac{Fa}{4}$   $\frac{\rightarrow Ga}{5}$  /powcoder, 40 mm

[Q p.73]

#### (ii) \(\forall x\) Add \(\forall \) We Chat \(x\) powcoder

- 1.  $\forall xFx$  A 2.  $\forall xFx \rightarrow Fx$  (A4) 3. Fx 1, 2 (MP) 4.  $Fx \rightarrow (\neg Gx \rightarrow Fx)$  (A1)
- 5.  $(\neg Gx \rightarrow Fx)$  3, 4 (MP)
- 6.  $\forall x(\neg Gx \rightarrow Fx)$  4 (Gen)

[Q p.73]

(iii) 1. 
$$\forall x \forall y (Rxy \rightarrow Ryx)$$
 A  
2.  $Rab$  A  
3.  $\forall x \forall y (Rxy \rightarrow Ryx) \rightarrow \forall y (Ray \rightarrow Rya)$  (A4)  
4.  $\forall y (Ray \rightarrow Rya)$  1, 3 (MP)  
5.  $\forall y (Ray \rightarrow Rya) \rightarrow (Rab \rightarrow Rba)$  (A4)  
6.  $Rab \rightarrow Rba$  4, 5 (MP)  
7.  $Rba$  2, 6 (MP)

```
(iv) \exists x Fx := \neg \forall x \neg Fx
          1. \neg \forall x \neg Fx \rightarrow \neg Ga
                                                                                                                         A
          2. Ga
                                                                                                                          A
          3. Ga \rightarrow (\neg \forall x \neg Fx \rightarrow Ga)
                                                                                                                          (A1)
          4. \neg \forall x \neg Fx \rightarrow Ga
                                                                                                                          2, 3 (MP)
          5. (\neg \forall x \neg Fx \rightarrow \neg Ga) \rightarrow ((\neg \forall x \neg Fx \rightarrow Ga) \rightarrow \forall x \neg Fx)
                                                                                                                         (A3)
          6. (\neg \forall x \neg Fx \rightarrow Ga) \rightarrow \forall x \neg Fx
                                                                                                                          1, 5 (MP)
          7. \forall x \neg Fx
                                                                                                                         4, 6 (MP)
          8. \neg \forall x \neg Fx \rightarrow \neg Ga, Ga \vdash \forall x \neg Fx
                                                                                                                          1-7
          9. \neg \forall x \neg Fx \rightarrow \neg Ga \vdash Ga \rightarrow \forall x \neg Fx
                                                                                                                          8, DT
                                                                                                                  [Q p.73]
```

#### Assignment Project Exam Help

https://powcoder.com

Add WeChat powcoder

(v) Auxiliary proof:

1. 
$$\neg\neg\forall x\neg Fx$$
 A
2.  $\neg\neg\forall x\neg Fx \rightarrow (\neg\forall x\neg Fx \rightarrow \neg\neg\forall x\neg Fx)$  (A1)
3.  $(\neg\forall x\neg Fx \rightarrow \neg\neg\forall x\neg Fx) \rightarrow ((\neg\forall x\neg Fx \rightarrow \neg\forall x\neg Fx) \rightarrow \forall x\neg Fx)$  (A3)
4.  $\neg\forall x\neg Fx \rightarrow \neg\neg\forall x\neg Fx$  1, 2 (MP)
5.  $(\neg\forall x\neg Fx \rightarrow \neg\forall x\neg Fx) \rightarrow \forall x\neg Fx$  4, 3 (MP)
6.  $\neg\forall x\neg Fx \rightarrow \neg\forall x\neg Fx$  †
7.  $\forall x\neg Fx$  5, 6 (MP)
8.  $\forall x\neg Fx \rightarrow \neg Fa$  (A4)
9.  $\neg Fa$  7, 8 (MP)
10.  $\neg\neg\forall x\neg Fx \vdash \neg Fa$  1–9

10, DT

† Look at the proof that  $\vdash_{A_2} P \to P$  in the commentary on line 3 of the proof in Answer 3vi (marked \*). Mimic this proof, with any wff  $\alpha$  in place of P throughout, and the resulting

Assignment the project (Letythat the project on the use (Gen), so the restriction on DT in  $A_1^{\forall=}$  is automatically satisfied.)

#### Matters://powcoder.com

 $\exists x Fx := \neg \forall x \neg Fx$ 

11.  $\vdash \neg \neg \forall x \neg Fx \rightarrow \neg Fa$ 

# 

- 3.  $\neg \neg \forall x \neg Fx \rightarrow \neg Fa$
- 4.  $(\neg\neg\forall x\neg Fx \to Fa) \to \neg\forall x\neg Fx$  2, 3 (MP)
- 5.  $Fa \to (\neg \neg \forall x \neg Fx \to Fa)$  (A1)
- 6.  $\neg \neg \forall x \neg Fx \rightarrow Fa$  1, 5 (MP)
- 7.  $\neg \forall x \neg Fx$  4, 6 (MP)
- 8.  $Fa \vdash \neg \forall x \neg Fx$  1–7
- 9.  $\vdash Fa \rightarrow \neg \forall x \neg Fx$  8, DT
- \* Line 11 of Auxiliary (above). [Q p.73]

```
(vi)
        1.
                 Fa
                                                                     Α
         2.
                 a = b
                                                                     A
         3.
                 x = y \rightarrow (Fx \rightarrow Fy)
                                                                      (A7)
         4.
                 \forall y(x=y\to (Fx\to Fy))
                                                                     3 (Gen)
         5.
                 \forall x \forall y (x = y \rightarrow (Fx \rightarrow Fy))
                                                                     4 (Gen)
                 \forall x \forall y (x = y \rightarrow (Fx \rightarrow Fy)) \rightarrow
                 \forall y(a=y\rightarrow (Fa\rightarrow Fy))
                                                                     (A4)
         7.
                 \forall y (a = y \rightarrow (Fa \rightarrow Fy))
                                                                     5, 6 (MP)
         8.
                 \forall y(a=y\rightarrow (Fa\rightarrow Fy))\rightarrow
                 (a = b \rightarrow (Fa \rightarrow Fb))
                                                                     (A4)
         9.
                 a = b \rightarrow (Fa \rightarrow Fb)
                                                                     7,8 (MP)
                                                                     2,9 (MP)
         10.
                Fa \rightarrow Fb
         11.
                Fb
                                                                     1, 10 (MP)
                                                                                                [Q p.73]
```

#### Project Exam Help

 $2. \forall x \forall y x = y \rightarrow \forall y a = \mathbf{y}$ 3.

1, 2 (MP)  $\forall ya = y$ 

bowcoder.com

[Q p.73]

## dd WeChat powcoder

(viii) 2. a = c3.  $(x = y \rightarrow (x = b \rightarrow y = b))$ (A7)4.  $\forall x(x = y \rightarrow (x = b \rightarrow y = b))$ 3 (Gen) 5.  $\forall x(x=y \rightarrow (x=b \rightarrow y=b)) \rightarrow$  $(a = y \to (a = b \to y = b))$ (A4) 6.  $(a = y \rightarrow (a = b \rightarrow y = b))$ 4, 5 (MP) 7.  $\forall y (a = y \rightarrow (a = b \rightarrow y = b))$ 6 (Gen)  $\forall y (a = y \rightarrow (a = b \rightarrow y = b)) \rightarrow$  $(a = c \rightarrow (a = b \rightarrow c = b))$ (A4) 9.  $(a = c \rightarrow (a = b \rightarrow c = b))$ 7,8 (MP)  $(a = b \rightarrow c = b)$ 2,9 (MP) 10. 11. c = b1, 10 (MP)

[Q p.73]

```
(ix) 1.
              a = b
                                                             Α
                                                             (A7)
       2.
              (x = y \rightarrow (x = a \rightarrow y = a))
             \forall x(x = y \rightarrow (x = a \rightarrow y = a))
                                                             2 (Gen)
              \forall x(x = y \rightarrow (x = a \rightarrow y = a)) \rightarrow
              (a = y \rightarrow (a = a \rightarrow y = a))
                                                             (A4)
              (a = y \rightarrow (a = a \rightarrow y = a))
                                                             3, 4 (MP)
              \forall y(a=y\to(a=a\to y=a))
                                                             5 (Gen)
             \forall y(a=y \rightarrow (a=a \rightarrow y=a)) \rightarrow
                                                             (A4)
              (a = b \rightarrow (a = a \rightarrow b = a))
       8.
              a = b \rightarrow (a = a \rightarrow b = a)
                                                             6, 7 (MP)
              a = a \rightarrow b = a
       9.
                                                             1,8 (MP)
       10. \forall xx = x
                                                             (A6)
       11.
             \forall xx = x \rightarrow a = a
                                                             (A4)
       12. a = a
                                                             10, 11 (MP)
       13. b = a
                                                             9, 12 (MP)
Assignment Project Exam Help
                                                                              [Qp.73]
```

#### (x) Ahttps://powcoder.com

1.		A
2	Add WeChat powcoder	(A1)
3.	$(\neg a = b \to \neg \neg a = b) \to ((\neg a = b \to \neg a = b) \to a = b)$	(A3)
4.	$\neg a = b \rightarrow \neg \neg a = b$	1, 2 (MP)
5.	$(\neg a = b \to \neg a = b) \to a = b$	4, 3 (MP)
6.	$\neg a = b \rightarrow \neg a = b$	*
7.	a = b	6, 5 (MP)
8.	$\neg \neg a = b \vdash a = b$	1–7
9.	$\vdash \neg \neg a = b \rightarrow a = b$	8, DT

\* See comment on line 6 of proof in Answer 4v (marked †).

#### Auxiliary proof B:

1. 
$$\neg Fb$$
 A
2.  $\neg \neg a = b$  A
3.  $\neg \neg a = b \rightarrow a = b$  \*
4.  $a = b$  2, 3 (MP)
5.  $a = b \rightarrow b = a$  †
6.  $b = a$  4, 5 (MP)
7.  $b = a \rightarrow (\neg Fb \rightarrow \neg Fa)$  ‡
8.  $\neg Fb \rightarrow \neg Fa$  6, 7 (MP)
9.  $\neg Fa$  1, 8 (MP)
10.  $\neg Fb, \neg \neg a = b \vdash \neg Fa$  1–9

- 11.  $\neg Fb \vdash \neg \neg a = b \rightarrow \neg Fa$  10, DT
- \* Line 9 of Auxiliary proof A (above)
- † Line 15 of proof in Answer 4ix.

Assignmente Renject state and life of post the proof in Answer 4vi.

#### Mattern ://powcoder.com

- 1. Fa2. Add We Chat powcoder

  3.  $(\neg \neg a = b \rightarrow Fa) \rightarrow \neg a = b)$  (A3)

  4.  $\neg \neg a = b \rightarrow Fa) \rightarrow \neg a = b$  \*

  5.  $(\neg \neg a = b \rightarrow Fa) \rightarrow \neg a = b$  3, 4 (MP)

  6.  $Fa \rightarrow (\neg \neg a = b \rightarrow Fa)$  (A1)

  7.  $\neg \neg a = b \rightarrow Fa$  1, 6 (MP)

  8.  $\neg a = b$  5, 7 (MP)
- \* 2, line 11 of Auxiliary proof B (above).

[Q p.73]

(xii) 1. 
$$\forall xFx$$
 A  
2.  $\forall xFx \rightarrow Fy$  (A4)  
3.  $Fy$  1, 2 (MP)  
4.  $\forall yFy$  3 (Gen)

#### Assignment Project Exam Help

[Q p.73]

#### https://powcoder.com

5. Sketch of answer: Adding new *axioms* does not affect the proof of DT in §15.1.1.1 (provided we retain (MP) and the existing axioms which feature in the proof). Edding the proof axioms which rule requires separate treatment in the induction step. For the rule (MP), the treatment of it in the induction step employs axiom (A2) (see pp.394–5). For the rule (Gen), the treatment of it in the induction step must employ axiom (A5). But (A5) includes a restriction (i.e. " $\alpha$  contains no free  $\underline{x}$ "). This means that only uses of (Gen) *with a corresponding restriction* (i.e. the rule is not applied "using a variable which is free in  $\beta$ ") can be handled. [Q p.73]

[Contents]

#### **Answers 15.2.3**

1. (i)

$$\begin{array}{c|cccc} 1 & & \neg P \rightarrow P \\ 2 & & & \neg P \\ 3 & & P & & 1,2 \ (\rightarrow E) \\ 4 & & \neg P & & 2 \ (RI) \\ 5 & P & & 2-4 \ (\neg E) \\ 6 & (\neg P \rightarrow P) \rightarrow P & 1-5 \ (\rightarrow I) \\ \end{array}$$

[Q p.74]

(ii)

## Assignment Project Exam Help

# Add WeChat powcoder $\begin{array}{c|c} & C & powcoder \\ \hline & C & 3, 4-5, 6-7 (\lor E) \end{array}$

[Q p.74]

(iii)

$$\begin{array}{c|cccc}
1 & & \neg P \\
2 & & \neg P \\
3 & & \neg P \\
4 & & \neg P \\
5 & P & 2-4 (\neg E) \\
6 & \neg P \rightarrow P & 1-5 (\rightarrow I)
\end{array}$$

## Assignment Project Exam Help.74]

(v)

# 

[Q p.74]

(vi)
$$\begin{array}{c|cccc}
1 & A \rightarrow B \\
2 & B \rightarrow C \\
3 & A \\
4 & B \\
5 & C \\
2,4 (\rightarrow E) \\
6 & A \rightarrow C & 3-5 (\rightarrow I)
\end{array}$$

3, 4–8, 9–10 (VE)

11

(ix)
$$\begin{array}{c|cccc}
1 & P \rightarrow R \\
2 & Q \rightarrow R \\
3 & P \lor Q \\
4 & P \\
5 & R & 1, 4 (\rightarrow E) \\
6 & Q \\
7 & R & 2, 6 (\rightarrow E) \\
8 & R & 3, 4-5, 6-7 (\lor E)
\end{array}$$





2. (i) 
$$\vdash_{N_2} A \lor \neg A$$

# Assignment Project Exam Help $_{11}$ $_{A \wedge \neg A}$ $_{5,10}$ $_{(\wedge I)}$

#### Add WeChat powcoder

$$1 \qquad A \lor (A \to \bot) \qquad \text{(TND)}$$

$$\vdash_{N_4} A \lor (A \to \bot)$$

$$\begin{array}{c|cccc}
1 & A \\
2 & A \lor (A \to \bot) & 1 (\lor I) \\
3 & A \to \bot \\
4 & A \lor (A \to \bot) & 3 (\lor I)
\end{array}$$

5 
$$A \lor (A \rightarrow \bot)$$
 1–2, 3–4 (NCD)

$$\begin{array}{c|cccc} \vdash_{N_5} & A \lor (A \to \bot) \\ & 1 & ((A \lor (A \to \bot)) \to \bot \\ & 2 & A \to \bot \\ & 3 & A \lor (A \to \bot) & 2 (\lor I) \\ & 4 & \bot & 1, 3 (\to E) \\ & 5 & A & 2-4 (RAA) \\ & 6 & A \lor (A \to \bot) & 5 (\lor I) \\ & 7 & \bot & 1, 6 (\to E) \\ & 8 & A \lor (A \to \bot) & 1-7 (RAA) \end{array}$$

## Assignment, Project Exam Help

https://powgoder.com

#### Add WeChat powcoder

$$\begin{array}{c|cccc}
1 & A \land (A \to \bot) \\
2 & A & 1 (\land E) \\
3 & A \to \bot & 1 (\land E) \\
4 & \bot & 2, 3 (\to E) \\
5 & B & 4 (\bot E)
\end{array}$$

(iii) 
$$\vdash_{N_2} (\neg \neg A \to A)$$

$$\begin{array}{c|cccc}
 & 1 & \neg \neg A \\
 & 2 & A & 1 (\neg \neg E) \\
 & 3 & \neg \neg A \to A & 1-2 (\to I)
\end{array}$$

#### Assignment Project Exam Help

https://p@wcoder.com
$$Add^4W$$
 eChat powcoder
 $Add^4W$  eChat powcoder
 $Add^4W$  and  $Add^4W$  because  $Add^4$  in  $Add^4$  in

$$\begin{array}{c|cccc}
1 & A \land (A \to \bot) \\
2 & A & 1 (\land E) \\
3 & A \to \bot & 1 (\land E) \\
4 & \bot & 2, 3 (\to E)
\end{array}$$

# Assignment Project Exam Help. $^{5}$ Help. $^{1-4}$ ( $\rightarrow$ $^{1}$ )

3. (i) https://powcoder.com

# Add We can be at power der $4 \forall x(Fx \rightarrow Fx) \rightarrow 3 (\forall I)$

$$4 \quad \forall x (Fx \to Fx) \qquad 3 \ (\forall I)$$

[Q p.74]

(ii)

$$\begin{array}{c|cccc}
1 & \exists x(Fx \land Gx) \\
2 & Fa \land Ga \\
3 & Fa & 2(\land E) \\
4 & \exists xFx & 3(\exists I) \\
5 & Ga & 2(\land E) \\
6 & \exists xGx & 5(\exists I) \\
7 & \exists xFx \land \exists xGx & 4, 6(\land I) \\
8 & \exists xFx \land \exists xGx & 1, 2-7(\exists E)
\end{array}$$

(v)

1 
$$\forall x \forall y x = y$$

2  $Raa$ 

3  $\neg Rbc$ 

4  $\forall y b = y$  1  $(\forall E)$ 

5  $b = a$  4  $(\forall E)$ 

6  $\forall y (a = y)$  1  $(\forall E)$ 

7  $a = c$  6  $(\forall E)$ 

8  $\neg Rac$  3, 5  $(= E)$ 

9  $Raa$  2  $(RI)$ 
 $\neg Raa$  7, 8  $(= E)$ 

Help

 $\forall y Rby$  11  $(\forall I)$ 

https://powcoder.com

(vi) Add Wechat powcoder

2  $Raa$  1  $(\forall E)$ 

3  $\exists y Ray$  2  $(\exists I)$ 

4  $\forall x \exists y Rxy$  3  $(\forall I)$ 

 $\forall xRxx \rightarrow \forall x \exists yRxy$  1–4 ( $\rightarrow$ I)

(vii)
$$\begin{array}{c|cccc}
1 & \exists xFx \\
2 & Fa \\
3 & \forall x\neg Fx \\
4 & Fa & 2 (RI) \\
5 & \neg Fa & 3 (\forall E) \\
6 & \neg \forall x\neg Fx & 3-5 (\neg I) \\
7 & \neg \forall x\neg Fx & 1, 2-6 (\exists E) \\
8 & \exists xFx \rightarrow \neg \forall x\neg Fx & 1-7 (\rightarrow I)
\end{array}$$

Assignment Project Exam Help

[Q p.74]

(ix)

1 
$$\forall xx = a$$

2  $b = c$ 

3  $b = a$  1 ( $\forall E$ )

4  $c = a$  1 ( $\forall E$ )

5  $\neg a = c$  2, 3 (= E)

6  $a = a$  (= I)

7  $\neg a = a$  4, 5 (= E)

8  $b = c$  2-7 ( $\neg E$ )

(x)
$$\begin{array}{c|cccc}
1 & Fa \land \neg Fb \\
2 & a = b \\
3 & Fa \land \neg Fa & 1, 2 (= E) \\
4 & Fa & 3 (\land E) \\
5 & \neg Fa & 3 (\land E) \\
6 & \neg a = b & 2-5 (\neg I) \\
7 & (Fa \land \neg Fb) \rightarrow \neg a = b & 1-6 (\rightarrow I) \\
8 & \forall y((Fa \land \neg Fy) \rightarrow \neg a = y) & 7 (\forall I) \\
9 & \forall x \forall y((Fx \land \neg Fy) \rightarrow \neg x = y) & 8 (\forall I)
\end{array}$$

# Assignment Project Exam Help [Q p.74]

• Rules of  $N_1$  reformulated in list style:

## -https://powcoder.com $\Delta \cup \{m\} \quad n. \quad \beta$

### $A_{\text{elimination:}}^{\Delta dd} W^{k} e Ch^{\beta} a t^{m, n} \stackrel{(\rightarrow I)}{pow} coder$

$$\Gamma$$
  $m$ .  $\alpha$   
 $\Delta$   $n$ .  $\alpha \to \beta$   
 $\Gamma \cup \Delta$   $k$ .  $\beta$   $m$ ,  $n (\to E)$ 

#### $\wedge$ introduction:

$$\Gamma \qquad m. \quad \alpha \\
\Delta \qquad n. \quad \beta \\
\Gamma \cup \Delta \quad k. \quad \alpha \wedge \beta \quad m, n \ (\wedge I)$$

#### $\wedge$ elimination:

$$\Gamma$$
  $m$ .  $\alpha \wedge \beta$   
 $\Gamma$   $k$ .  $\alpha$  (or  $\beta$ )  $m$  ( $\wedge E$ )

#### ¬ introduction:

$$\begin{cases} m \end{cases} & m. \quad \alpha \quad A \\ \Delta \text{ or } \Delta \cup \{m\} \quad n. \quad \beta \\ \Gamma \text{ or } \Gamma \cup \{m\} \quad o. \quad \neg \beta \\ \Delta \cup \Gamma \qquad k. \quad \neg \alpha \quad m, n, o \ (\neg I)$$

```
\neg elimination:
            {m}
                                   m.
                                           \neg \alpha
                                                  Α
           \Delta or \Delta \cup \{m\}
                                           β
                                   n.
           \Gamma or \Gamma \cup \{m\}
                                           \neg \beta
                                   0.
           \Delta \cup \Gamma
                                   k.
                                                   m, n, o (\neg E)
                                           α
   \vee introduction:
           \Gamma m. \alpha
                        \alpha \vee \beta (or \beta \vee \alpha) m (\vee I)
           \Gamma k.
   ∨ elimination:
           Γ
                                     \alpha \vee \beta
                              m.
            {n}
                                                 Α
                                     α
           \Delta \cup \{n\}
                                     \gamma
                                                 A
            {p}
                              р.
           \Lambda \cup \{p\}
                              q.
           \Gamma \cup \Delta \cup \Lambda
                              k.
                                                 m, n, o, p, q (\forall E)
                              \neg P \rightarrow P
  1.(i)
                                                          2, 3 (\neg E)
                                                       1,4 (\rightarrow I)
                                                                                         [Q p.74]
1.(ii)
            {1}
                                 B \rightarrow C
            {2}
                           2.
                                                A
                                 A \vee B
            {3}
                           3.
                                                A
            \{4\}
                                 \boldsymbol{A}
                                                A
                                 C
                                               1, 4 (\rightarrow E)
            \{1,4\}
                           5.
                           6.
                                В
            {6}
                                                A
                           7. C
                                               2, 6 (\rightarrow E)
            {2,6}
            \{1,2,3\}
                           8.
                                               3, 4, 5, 6, 7 (\forall E)
                                                                                         [Q p.74]
1.(iii)
           \{1\} 1. \neg \neg P
                                              A
            {2}
                    2.
                           \neg P
                                              A
           {1}
                    3.
                                              1, 2 (\neg E)
                                             1,3 (\rightarrow I)
                                                                                         [Q p.74]
```

```
\{1\} 1. \neg (A \lor B) A
      1.(iv)
              {2}
                    2.
                        A
                                     A
              {2}
                  3. A \vee B
                                     2(\forall I)
              {1}
                   4. \neg A
                                     1, 2, 3 (\neg I)
              {6}
                   5. B
              {6}
                   6. A \vee B
                                     5(\forall I)
                   7. ¬B
              \{1\}
                                     1, 5, 6 (\neg I)
              {1}
                    8. \neg A \land \neg B 4, 7 (\land I)
                                                                    [Q p.74]
      1.(v)
              {1}
                      1. A
                                 A
              \{2\}
                      2. \neg A
                                A
                      3. \neg B
              {3}
                                 A
              {1,2}
                      4. B
                                 1, 2, 3 (\neg E)
                                                                    [Q p.74]
Assignment Project Exam Help
              \{3\}
                                       1,3 \rightarrow E
              {1,3}
                             В
                                                                    [Q p.74]
                      WeChat<sub>A</sub>powcoder
              \hat{2}
                                        A
                         P
              {3}
                      3.
                                        A
                      4. Q
              {1,3}
                                        1,3 (\rightarrow E)
              {1,2}
                      5. \neg P
                                        2, 3, 4 (\neg I)
              {1}
                      6. \neg Q \rightarrow \neg P 2, 5 (\rightarrow I)
                                                                    [Q p.74]
    1.(viii)
              {1}
                      1. A \lor B
                                   A
              \{2\}
                      2. \neg A
                                   A
              {3}
                      3. A
                                   A
                      4. ¬B
              \{4\}
                      5. B
              \{2,3\}
                                   2, 3, 4 (\neg E)
                      6. B
              {6}
              {1,2}
                      7.
                         В
                                   1, 3, 5, 6 (\forall I)
                                                                    [Q p.74]
```

```
1.(ix)
               {1}
                          1. P \rightarrow R
               \hat{2}
                          2. Q \rightarrow R
                          3. P \lor Q
               {3}
               \{4\}
                                          A
                          5. R
                                         1,4 (\rightarrow E)
               \{1,4\}
               {6}
                                         2, 6 (\rightarrow E)
                          7. R
               \{2,6\}
                                        3, 4, 5, 6, 7 (\forall E)
               \{1,2,3\}
                                                                        [Q p.74]
       1.(x)
               {1}
                        1. P \rightarrow Q
                        2. P \land \neg Q
3. P
               \{2\}
                                            A
               {2}
                                            2(\wedge E)
               \{1,2\} 4. Q
                                            1,3 (\rightarrow E)
Assignment Project Exam Help
[Qp.74]
```

https://powcoder.com

Add WeChat powcoder

(ii)

- Rules of  $N_1$  reformulated in stack style:
  - $\rightarrow$  introduction:

$$\begin{array}{c}
[\alpha]_n \\
\vdots \\
\frac{\beta}{\alpha \to \beta} (\to I)_n
\end{array}$$

 $\rightarrow$  elimination:

$$\frac{\alpha \qquad \alpha \to \beta}{\beta} \ (\to E)$$

 $\wedge$  introduction:

## Assignment Project Exam Help

 $\underset{\frac{\alpha \ (\text{or} \ \beta)}{\alpha \ (\text{or} \ \beta)}}{\text{https://powcoder.com}}$ 

## - Ardet WeChat powcoder

$$\begin{array}{c} [\alpha]_n \\ \vdots \\ \beta \\ \frac{\neg \beta}{\neg \alpha} (\neg I)_n \end{array}$$

 $\neg$  elimination:

$$\begin{bmatrix} \neg \alpha \end{bmatrix}_{n} \\
\vdots \\
\beta \\
\underline{\neg \beta}_{\alpha} (\neg E)_{n}$$

∨ introduction:

$$\frac{\alpha}{\alpha \vee \beta \ (\text{or } \beta \vee \alpha)} \ (\vee I)$$

∨ elimination:

repetition (R):

$$\frac{\alpha \quad \beta}{\alpha}$$
 (R)

(This is the analogue of repetition inward (RI). We need this rule to facilitate certain applications of  $(\neg I)$  and  $(\neg E)$ ; see how it is used in the answers below. Not every stack-style natural deduction system requires this rule. For example,

Assignment i Pthe system in Dirk gam Paled, dais and Structure [Springer, Berlin, fourth edition, 2004], which is a stack form of something similar to system  $N_5$  in the text

• Answers to Question 1, reformulated in stack style:

Add We Chat powcoder  $\frac{\frac{P}{P}(\neg E)_1}{(\neg P \rightarrow P) \rightarrow P} (\rightarrow I)_2$ 

$$\frac{\frac{P}{P}(\neg E)_1}{(\neg P \to P) \to P} (\to I)_2$$

[Qp.74]

1.(ii)
$$A \lor B \qquad A \to C \qquad [A]_1 \ (\to E) \qquad B \to C \qquad [B]_1 \ (\to E)$$

$$C \qquad C \qquad (\lor E)_1$$

[Q p.74]

1.(iii) 
$$\frac{[\neg P]_2 \quad [\neg P]_1}{\frac{\neg P}{P} (\neg E)_1} (R) \\ \frac{\neg P}{\neg P} (\rightarrow I)_2$$

1.(iv) 
$$\frac{\neg (A \lor B) \quad \frac{[A]_1}{A \lor B} (\lor I)}{\frac{\neg (A \lor B)}{A \lor B} (\neg I)_1} \frac{\neg (A \lor B) \quad \frac{[B]_2}{A \lor B} (\lor I)}{\frac{\neg (A \lor B)}{\neg A} (\land I)_2} (R)$$

1.(v) 
$$\frac{A \qquad [\neg B]_1}{A} (R) \qquad \neg A \\ \frac{\neg A}{B} (\neg E)_1 (R)$$

[Q p.74]

[Q p.74]

Assignment 
$$P_{\overline{A} \to C}^{A \to B} \xrightarrow{[A]_1} (\to E)$$

1.(vihttps://powcoder.com  $\frac{P \to Q}{Q} \xrightarrow{[P]_1} (\to E) \qquad [\neg Q]_2 \text{(R)}$   $Add WeChat_Ipowcoder$   $\frac{\neg Q}{\neg Q \to \neg P} \xrightarrow{(\to I)_2} (\to I)_2$ 

[Q p.74]

1.(viii)

$$\frac{A \lor B}{A \lor B} = \frac{[A]_2 \quad [\neg B]_1}{A \quad \neg A \quad (R)} (R) \\
B \quad [B]_2 \quad (\lor E)_2$$

$$[Q p.74]$$

1.(ix) 
$$\frac{P \rightarrow R \qquad [P]_1}{R} (\rightarrow E) \qquad \frac{Q \rightarrow R \qquad [Q]_1}{R} (\rightarrow E)$$
 [Q p.74]

1.(x) 
$$\frac{P \to Q \qquad \frac{[P \land \neg Q]_1}{P} (\land E) \qquad [P \land \neg Q]_2}{Q} (\land E)}{\frac{\neg Q}{\neg (P \land \neg Q)} (\neg I)_1} (\land E)$$

$$\frac{\neg Q}{\neg (P \land \neg Q)} (\neg I)_2$$

5. Introduction:



## Add WeChat powcoder

 $\alpha \leftrightarrow \beta$  $\alpha \text{ (or } \beta)$ 

 $\triangleright \beta$  (or  $\alpha$ , if  $\beta$  above)

[Q p.75]

[Contents]

#### **Answers 15.3.3**

1. (i) (a) $\{\alpha\} \Rightarrow \emptyset$ holds logically	[Q p.75]		
(b) $\{\alpha\} \Rightarrow \emptyset$ does not hold logically	[Q p.75]		
(ii) (a) $\{\alpha, \beta\} \Rightarrow \emptyset$ does not hold logically	[Q p.75]		
(b) $\{\alpha\} \Rightarrow \{\beta\}$ and $\{\beta\} \Rightarrow \{\alpha\}$ both hold logically	[Q p.75]		
2. No answers supplied. [Q p.75]			
3. No answers supplied.			
4.			
$\frac{\{\alpha,\beta\} \cup \Gamma \Rightarrow \Delta \qquad \Gamma \Rightarrow \Delta \cup \{\alpha,\beta\}}{\{\alpha \leftrightarrow \beta\} \cup \Gamma \Rightarrow \Delta} \ (\leftrightarrow \Rightarrow)$			
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$			
5. https://powcoder.com			

nttps://powcoaer.com

Add WeChat powcoder [Contents]

# Chapter 16 Set Theory

There are no exercises for chapter 16.

[Contents]

Assignment Project Exam Help

https://powcoder.com

Add WeChat powcoder