

# $R^2$ , Adjusted $R^2$

## $R^2$

*Coefficient of Determination*

$$R^2 = 1 - (SS_{res} / SS_{tot})$$

Proportion of variance explained

- Range:  $-\infty$  to 1 (typically 0 to 1)
- $R^2 = 1$ : Perfect predictions
- $R^2 = 0$ : No better than mean
- Negative  $R^2$ : Worse than baseline

## Adjusted $R^2$

*Penalized  $R^2$*

$$R^2_{adj} = 1 - [(1-R^2)(n-1)/(n-p-1)]$$

Adjusts for number of predictors

- Penalizes adding features
- Decreases if feature doesn't help
- Use for model comparison
- Better for high-dimensional data

### $R^2$ Interpretation Scale



**< 0**  
Terrible

**0.25**  
Weak

**0.50**  
Moderate

**0.75**  
Strong

**1.0**  
Perfect

⚡ When to Use Which?

$R^2$

Single model evaluation

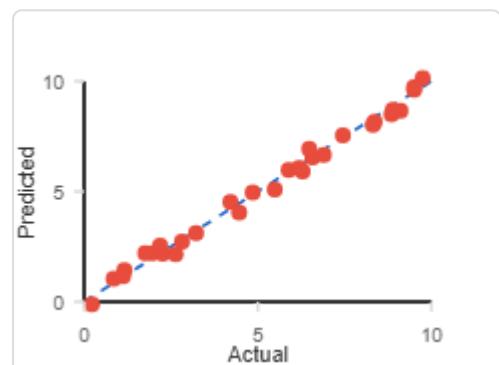
Adjusted  $R^2$

Comparing multiple models

## 📊 Predicted vs Actual Values

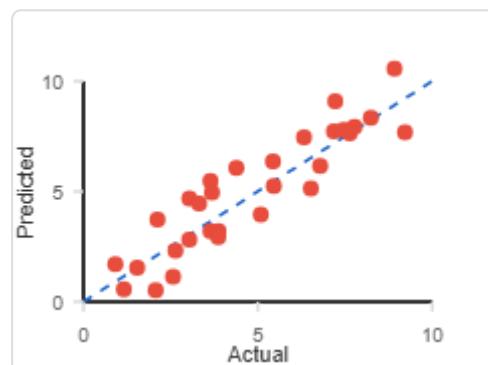
$R^2 \approx 0.95$

Strong Fit



$R^2 \approx 0.50$

Moderate Fit



$R^2 \approx 0.10$

Weak Fit

