

## Clustering Problem Definition

### Core Objective



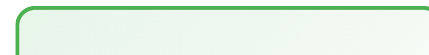
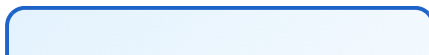
Partition  $n$  observations into  $k$  groups



Maximize intra-cluster similarity  
Minimize inter-cluster similarity

**Distance Metrics:** Euclidean • Manhattan • Cosine • Mahalanobis

### Types of Clustering Approaches





### Hard Clustering

Each point belongs to exactly one cluster

*Binary membership*



### Soft Clustering

Points have probability distribution over clusters

*Fuzzy membership*



### Hierarchical

Nested clusters forming tree structure

*Dendrogram output*



### Density-Based

Clusters as high-density regions

*Arbitrary shapes*

## Model-Based Approach



Data generated from mixture of probability distributions