

## Value Function Analysis



### Discriminator Maximizes

Correctly classify real and fake samples

$$\max_D V(D, G)$$



### Generator Minimizes

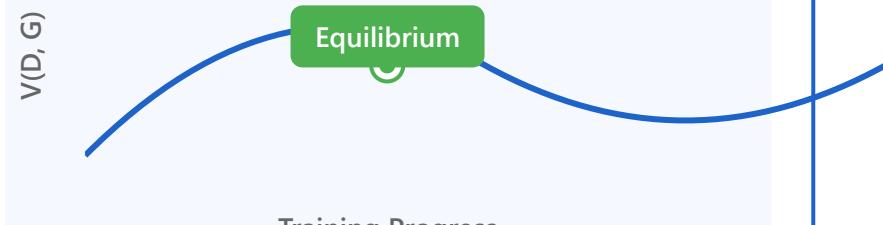
Fool the discriminator effectively

$$\min_G V(D, G)$$

### Theoretical Insights

- Cross-entropy loss interpretation
- Jensen-Shannon divergence connection
- Global optimality guarantees

### Value Function Landscape



### Optimal Discriminator

$$D^*(x) = p_{\text{data}}(x) / (p_{\text{data}}(x) + p_g(x))$$

Theoretical Optimum

Discriminator at Equilibrium

Value Function

$$p_g = p_{\text{data}}$$

$$D^*(x) = 1/2$$

$$V(D^*, G^*) = -\log(4)$$