

# Deep Dive into Score Function

Part 3/7: Reverse Process

## Score Definition

$$\nabla_{\mathbf{x}} \log p(\mathbf{x})$$

Indicates direction of density increase



### Connection

Denoising  $\approx$  Score matching



### Tweedie's Formula

Score relates to optimal denoising estimation



### Score Estimation

$$\varepsilon_{\theta}(\mathbf{x}_t, t) \approx -\sqrt{(1-\bar{\alpha}_t)} \cdot \nabla_{\{\mathbf{x}_t\}} \log p(\mathbf{x}_t)$$



### Langevin Dynamics

Reverse process as Langevin sampling from the score function



### Continuous Limit

Score-based SDEs when  $T \rightarrow \infty$



## Unified View

Diffusion and score-based models are equivalent