

Automatic Differentiation (Autograd)

Automatic differentiation computes derivatives algorithmically by applying the chain rule to elementary operations, enabling efficient gradient computation without manual derivation

Manual

Derive gradients by hand using calculus

- ✓ Full control
- ✓ Symbolic form
- ✗ Error-prone
- ✗ Time-consuming
- ✗ Not scalable

Numerical

Approximate using finite differences

- ✓ Easy to implement
- ✗ Approximation errors
- ✗ Slow ($O(n)$ evaluations)
- ✗ Numerical instability

Automatic (AD)

Compute exact derivatives automatically

- ✓ Exact derivatives
- ✓ Efficient $O(1)$ overhead
- ✓ Scalable to complex models
- ✓ No manual derivation

PyTorch Example

```
import torch # Create tensors with gradient tracking
x = torch.tensor([2.0], requires_grad=True)
w = torch.tensor([0.5], requires_grad=True)
b = torch.tensor([1.0], requires_grad=True)
# Forward pass (build computation graph)
y = torch.sigmoid(w * x + b)
```

Key Features

- 1 Dynamic Graph:** Built during forward pass
- 2 Chain Rule:** Applied automatically layer by layer

```
loss = (y - 1)**2 # Backward pass (compute
gradients) loss.backward() # Access gradients
print(w.grad) #  $\partial \text{loss} / \partial w$  print(b.grad) #  $\partial \text{loss} / \partial b$ 
```

Efficient: Reuses intermediate values

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Flexible: Supports arbitrary operations



Why It Matters: Autograd eliminates the need for manual gradient derivation, making deep learning accessible and enabling rapid experimentation with complex architectures.



PyTorch

Dynamic
graphs



TensorFlow

Eager
execution



JAX

Functional
AD