

Deep Dive into Score Function

Part 3/7: Reverse Process

Score Definition

$$\nabla_{\mathbf{x}} \log p(\mathbf{x})$$

Indicates direction of density increase

Connection

Denoising \approx Score matching

Tweedie's Formula

Score relates to optimal denoising estimation

Score Estimation

$$\varepsilon_{\theta}(\mathbf{x}_t, t) \approx -\sqrt{1-\bar{\alpha}_t} \cdot \nabla_{\mathbf{x}_t} \log p(\mathbf{x}_t)$$

Langevin Dynamics

Reverse process as Langevin sampling from the score function

Continuous Limit

Score-based SDEs when $T \rightarrow \infty$



Unified View

Diffusion and score-based models are equivalent