

# Automatic Differentiation (Autograd)

Automatic differentiation computes derivatives algorithmically by applying the chain rule to elementary operations, enabling efficient gradient computation without manual derivation

## Manual

Derive gradients by hand using calculus

- ✓ Full control
- ✓ Symbolic form
- ✗ Error-prone
- ✗ Time-consuming
- ✗ Not scalable

## Numerical

Approximate using finite differences

- ✓ Easy to implement
- ✗ Approximation errors
- ✗ Slow ( $O(n)$ ) evaluations
- ✗ Numerical instability

## Automatic (AD)

Compute exact derivatives automatically

- ✓ Exact derivatives
- ✓ Efficient  $O(1)$  overhead
- ✓ Scalable to complex models
- ✓ No manual derivation

## PyTorch Example

```
import torch # Create tensors with gradient tracking
x = torch.tensor([2.0],
requires_grad=True) w = torch.tensor([0.5],
requires_grad=True) b = torch.tensor([1.0],
requires_grad=True) # Forward pass (build computation graph)
y = torch.sigmoid(w * x + b)
```

## Key Features

- 1 **Dynamic Graph:** Built during forward pass
- 2 **Chain Rule:** Applied automatically layer by layer

```
loss = (y - 1)**2 # Backward pass (compute  
gradients) loss.backward() # Access gradients  
print(w.grad) # ∂loss/∂w print(b.grad) # ∂loss/∂b
```

 **Efficient:** Reuses intermediate values

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**Flexible:** Supports arbitrary operations



**Why It Matters:** Autograd eliminates the need for manual gradient derivation, making deep learning accessible and enabling rapid experimentation with complex architectures.



**PyTorch**

Dynamic graphs



**TensorFlow**

Eager execution



**JAX**

Functional AD