

## Conditional Probability and Bayes' Theorem

### Conditional Probability

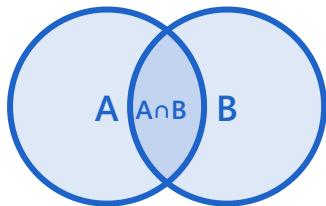
$$P(A|B) = P(A \cap B) / P(B)$$

Probability of A given B has occurred

### Multiplication Rule

$$P(A \cap B) = P(A|B)P(B)$$

### Visual Representation



### Independence: $X \perp Y$

$$P(X|Y) = P(X)$$

### Bayes' Theorem

$$P(A|B) = P(B|A)P(A) / P(B)$$

Prior  
 $P(A)$

Likelihood  
 $P(B|A)$

Posterior  
 $P(A|B)$

### Applications

Updating beliefs with new data

Medical diagnosis and testing

Spam filtering and classification

### ML Foundation

Bayesian regression and inference