

Value Function Analysis



Discriminator Maximizes

Correctly classify real and fake samples

$$\max_D V(D, G)$$



Generator Minimizes

Fool the discriminator effectively

$$\min_G V(D, G)$$

Theoretical Insights

- Cross-entropy loss interpretation
- Jensen-Shannon divergence connection
- Global optimality guarantees

Value Function Landscape

$V(D, G)$

Equilibrium

Training Progress

Optimal Discriminator

$$D^*(x) = p_{\text{data}}(x) / (p_{\text{data}}(x) + p_g(x))$$

Theoretical Optimum

$$p_g = p_{data}$$

Discriminator at Equilibrium

$$D^*(x) = 1/2$$

Value Function

$$V(D^*, G^*) = -\log(4)$$