Assignment - 4

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Part 1: A simple linear regression: Power posing and testosterone

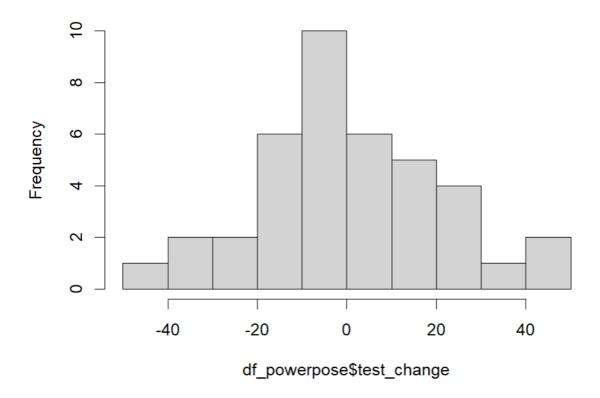
Let's load the dataset df powerpose.csv and see the dataset.

We are looking at testosterone levels measured before (testm1) and after (testm2) a treatment. The main thing we're interested in is the type of treatment each person received - either a **high-power pose** or a **low-power pose**.

To evaluate the effect of treatment, we will analyze the **change in testosterone levels** (i.e., the difference between testm2 and testm1) and examine how this change is influenced by the treatment condition (hptreat).

```
1. df_powerpose$test_change <- df_powerpose$testm2 - df_powerpose$testm1</pre>
head(df_powerpose)
3.
4. ## X id hptreat female age testm1 testm2 test_change
5. ## 1 2 29 High Male 19 38.725 62.375 23.650002
              Low Female 20 32.770 29.235
High Female 20 32.320 27.510
                                                 -3.534999
-4.810000
6. ## 2 3 30
7. ## 3 4 31
8. ## 4 5 32
                Low Female 18 17.995 28.655 10.660000
9. ## 5 7 34
                Low Female 21 73.580 44.670 -28.910004
10. ## 6 8 35
              High Female 20 80.695 105.485 24.790000
11.
12. hist(df_powerpose$test_change)
13.
```

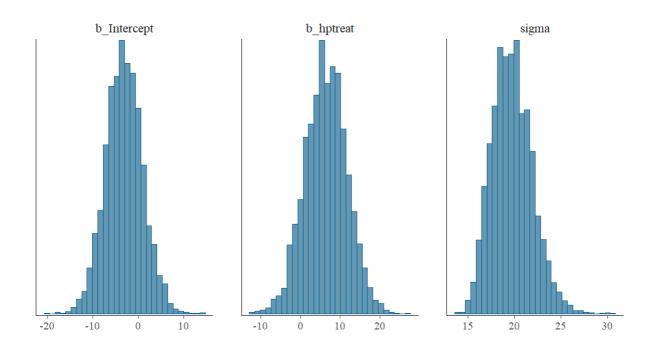
Histogram of df_powerpose\$test_change



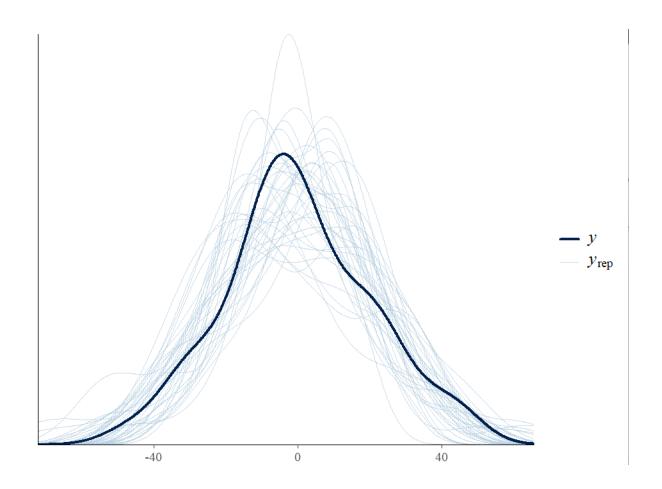
```
2.
 # Prior assumptions
 4.
 5.
 6. # test_change ~ N(mu, sigma)
 7. # mu ~ alpha + beta*tptreat
 8. # alpha \sim N(0, 10)
 9. # beta ~ N(0, 10)
10. # sigma ~ N(0, 10)
11.
12. install.packages("brms")
13. install.packages("rstan")
14. install.packages("rstudioapi")
15. library(brms)
16. library(rstan)
17. library(bayesplot)
18.
19. df_powerpose$hptreat <- ifelse(df_powerpose$hptreat == "High", 1, ∅)</pre>
20.
21. # priors
22. priors <- c(prior(normal(0, 10), class = Intercept),
23.
                 prior(normal(0, 10), class = b, coef = hptreat),
24.
                 prior(normal(0, 10), class = sigma))
25.
26. m1 <- brm(formula = test_change ~ 1+hptreat,
               data = df_powerpose,
27.
28.
               prior = priors,
29.
               family = gaussian(),
               chains = 4, cores = 4,
30.
               iter = 2000, warmup = 1000)
31.
```

```
33. ## Compiling Stan program...
34. ## Start sampling
35.
36. summary(m1)
37.
38. ## Family: gaussian
39. ## Links: mu = identity; sigma = identity
40. ## Formula: test_change ~ 1 + hptreat
41. ##
        Data: df_powerpose (Number of observations: 39)
42. ## Draws: 4 chains, each with iter = 2000; warmup = 1000; thin = 1;
43. ##
              total post-warmup draws = 4000
44. ##
45. ## Regression Coefficients:
46. ##
                Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
                                               5.09 1.00
47. ## Intercept
                  -3.11
                            4.09 -11.04
                                                              4115
48. ## hptreat
                              5.30
                    6.38
                                      -3.91
                                               16.69 1.00
                                                              3878
                                                                       2639
49. ##
50. ## Further Distributional Parameters:
51. ##
          Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
52. ## sigma
               19.74
                          2.17
                                  16.00
                                           24.39 1.00
53. ##
54. ## Draws were sampled using sampling(NUTS). For each parameter, Bulk_ESS
55. ## and Tail_ESS are effective sample size measures, and Rhat is the potential
56. ## scale reduction factor on split chains (at convergence, Rhat = 1).
57.
```

```
1. # plotting the histogram
2. mcmc_hist(m1, pars = c("b_Intercept", "b_hptreat", "sigma"))
3.
4. ## stat_bin()` using `bins = 30`. Pick better value with `binwidth
5.
```



```
1. # posterior prediction check
2. pp_check(m1, ndraws = 39, type = "dens_overlay")
3.
```



Part 2: Poisson regression models and hypothesis testing

2.1

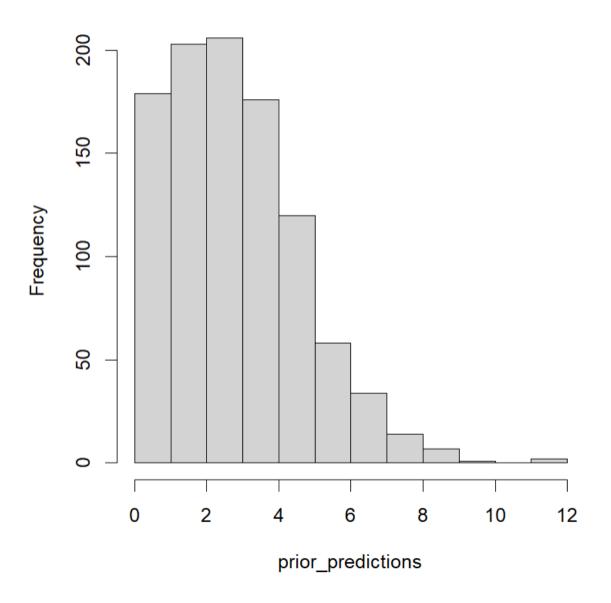
```
3. # Part 2
4.
5.
6. ### 2.1
7. crossing_model <- function(len, alpha, beta) {</pre>
8. lambda <- exp(alpha + len*beta)</pre>
9.
     N <- rpois(1, lambda)
10.
     return(N)
11. }
12.
13. a <- crossing_model(10, 0.15, 0.25)</pre>
14. a
15.
16. ## [1] 15
17.
```

2.2

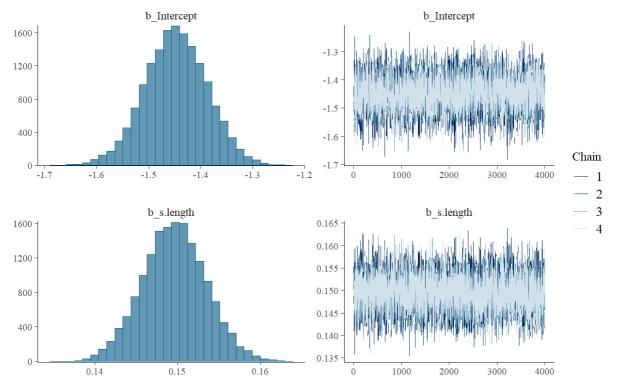
```
1. ### 2.2
2. # alpha ~ Normal_lb=0 (0.15, 0.1)
3. # beta ~ Normal_lb=0 (0.25, 0.05)
4.
5. library(truncnorm)
6. alpha_prior <- rtruncnorm(1000, a=0, mean=0.15, sd=0.1)</pre>
```

```
7. beta_prior <- rtruncnorm(1000, a=0, mean=0.25, sd=0.05)
8.
9. len <- 4
10. lambda <- exp(alpha_prior + len*beta_prior)
11. prior_predictions <- rpois(1000, lambda)
12. summary(prior_predictions)
13.
14. ## Min. 1st Qu. Median Mean 3rd Qu. Max.
15. ## 0.000 2.000 3.000 3.253 4.000 12.000
16.
17. hist(prior_predictions)
18.
```

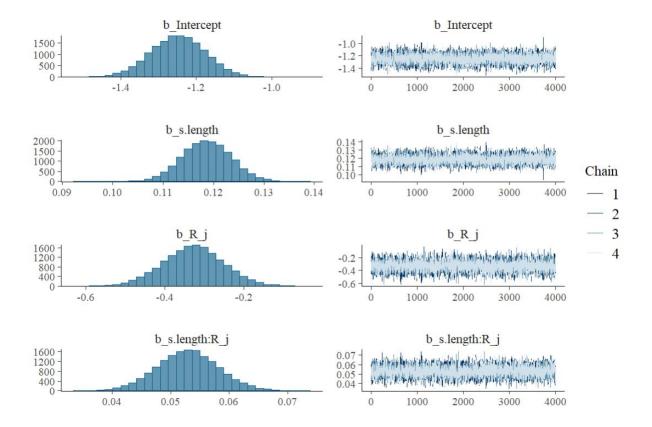
Histogram of prior_predictions



```
1. ### 2.3
2.
3. getwd()
4. df_crossings <- read.table("crossings.csv", header = TRUE, sep=",")
5. head(df_crossings)
6.
7.
8. ## Language s.id s.length nCross
9. ## 1 German 1
                           2
10. ## 2
         German
                    2
11. ## 3
          German
                    3
                             2
                                    0
12. ## 4
          German
                    4
                             2
                                    0
13. ## 5
                    5
                             2
          German
                                    2
14. ## 6
         German
                    6
15.
16. df_crossings$R_j <- ifelse(df_crossings$Language == "German", 1, 0)
17. len_ij <- df_crossings$s.length</pre>
18.
19. # model 1
20. priors <- c(prior(normal(0.15, 0.1), class = Intercept),
               prior(normal(0, 0.15), class = b, coef = s.length))
22.
23. model_1 <- brm(formula = nCross ~ 1 + s.length,
24.
                   data = df_crossings,
25.
                  prior = priors,
                  family = poisson(link = "log"),
26.
                  chains = 4, cores = 4,
27.
28.
                  iter = 8000, warmup = 4000)
29.
30. ## Compiling Stan program...
31. ## Start sampling
33. summary(model 1)
34.
35. ## Family: poisson
36. ##
       Links: mu = log
37. ## Formula: nCross ~ 1 + s.length
38. ##
        Data: df_crossings (Number of observations: 1900)
        Draws: 4 chains, each with iter = 8000; warmup = 4000; thin = 1;
39. ##
40. ##
               total post-warmup draws = 16000
41. ##
42. ## Regression Coefficients:
43. ##
                Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk ESS Tail ESS
44. ## Intercept -1.45
                            0.06
                                    -1.57 -1.34 1.00
                                                              5081
                                                                       6063
45. ## s.length
                    0.15
                              0.00
                                       0.14
                                                0.16 1.00
                                                              5756
                                                                       7403
46. ##
47. ## Draws were sampled using sampling(NUTS). For each parameter, Bulk ESS
48. ## and Tail_ESS are effective sample size measures, and Rhat is the potential
49. ## scale reduction factor on split chains (at convergence, Rhat = 1).
50.
51. library(ggplot2)
52. plot(model_1)
53.
```

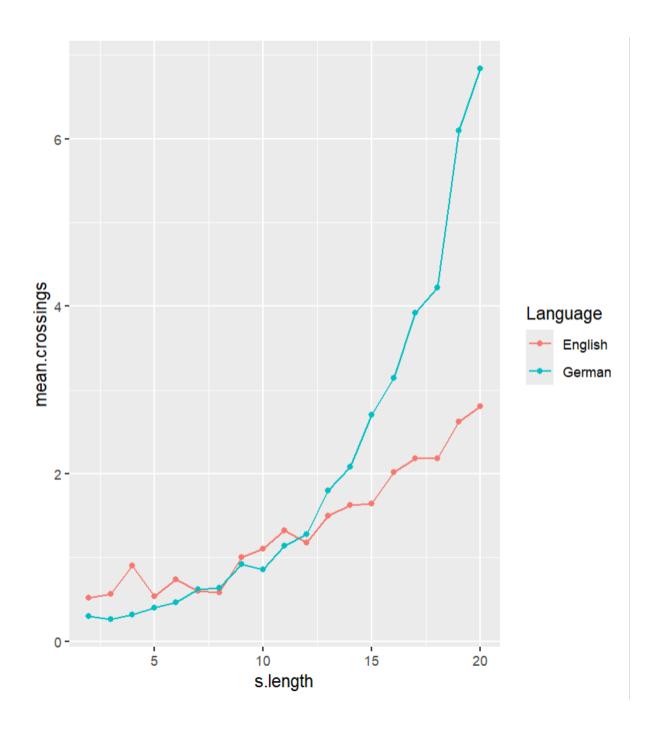


```
1. # model 2
3. priors <- c(prior(normal(0.15, 0.1), class = Intercept),</pre>
                prior(normal(0, 0.15), class = b, coef = s.length),
5.
                prior(normal(0.15, 0.1), class = b, coef = R_j),
6.
                prior(normal(0.15, 0.1), class = b, coef = s.length:R_j))
7.
8. model_2 <- brm(formula = nCross ~ 1 + s.length + R_j + s.length*R_j,</pre>
9.
                   data = df_crossings,
10.
                   prior = priors,
                   family = poisson(link = "log"),
11.
                   chain = 4, cores = 4,
12.
13.
                   iter = 8000, warmup = 4000)
14.
15. ## Compiling Stan program...
16. ## Start sampling
17.
18. summary(model_2)
19.
20. ##
        Family: poisson
21. ##
        Links: mu = log
22. ## Formula: nCross ~ 1 + s.length + R_j + s.length * R_j
23. ##
         Data: df_crossings (Number of observations: 1900)
24. ##
         Draws: 4 chains, each with iter = 8000; warmup = 4000; thin = 1;
25. ##
               total post-warmup draws = 16000
26. ##
27. ## Regression Coefficients:
28. ##
                    Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk ESS Tail ESS
29. ## Intercept
                                           -1.39
                       -1.25
                                  0.07
                                                    -1.11 1.00
                                                                    6086
                                                                             7387
30. ## s.length
                        0.12
                                  0.00
                                            0.11
                                                     0.13 1.00
                                                                    6198
                                                                             8203
31. ## R_j
                       -0.33
                                  0.08
                                           -0.48
                                                    -0.18 1.00
                                                                    6203
                                                                             7081
32. ## s.length:R_j
                        0.05
                                  0.01
                                            0.04
                                                     0.06 1.00
                                                                    5983
                                                                             6724
33. ##
34. ## Draws were sampled using sampling(NUTS). For each parameter, Bulk_ESS
35. ## and Tail ESS are effective sample size measures, and Rhat is the potential
36. ## scale reduction factor on split chains (at convergence, Rhat = 1).
37.
38. plot(model_2)
```



2.4

```
1. ### 2.4
library(plyr)
4. library(dplyr)
5.
6. ## Attaching package: 'dplyr'
7. ##
8. ##
      The following objects are masked from 'package:plyr':
9. ##
10. ##
           arrange, count, desc, failwith, id,
11. ##
           mutate, rename, summarise, summarize
12. ##
13. ##
      The following objects are masked from 'package:stats':
14. ##
15. ##
           filter, lag
16. ##
17. ## The following objects are masked from 'package:base':
18. ##
19. ##
           intersect, setdiff, setequal, union
20.
21. # Visualize average rate of crossings
22. observed <- read.table("crossings.csv", header = , sep = ",")</pre>
23.
24. observed %>% group_by(Language, s.length) %>%
25.
      summarise(mean.crossings = mean(nCross)) %>%
26.
      ggplot(aes(x = s.length, y = mean.crossings,
27.
                 group = Language, color = Language)) +
28.
      geom point() + geom line()
29.
30. ## `summarise()` has grouped output by 'Language'. You
31. ## can override using the `.groups` argument.
32.
```



```
1. # Code/center the predictors
 2. observed$s.length <- observed$s.length - mean(observed$s.length)</pre>
 3. observed$lang <- ifelse(observed$Language == "German", 0, 1)</pre>
 5. \# These two vector will store log predictive densities
 6. # in each fold
 7.
8. lpds.m1 <- c()
9. lpds.m2 <- c()
10. untested <- observed
11.
12. for (k in 1:5) {
      # prepare test data and training data
13.
14.
      y_test <- sample_n(untested, size = nrow(observed)/5)</pre>
      y_train <- setdiff(observed, y_test)
untested <- setdiff(untested, y_test)</pre>
15.
16.
```

```
17.
18.
      fit.m1 <- brm(nCross ~ 1 + s.length,</pre>
19.
                     data = y_train,
                     family = poisson(link = "log"),
20.
                     prior = c(prior(normal(0.15, 0.1), class = Intercept),
21.
22.
                                prior(normal(0, 0.15), class = b)),
                     cores = 4)
23.
24.
25.
      fit.m2 <- brm(nCross ~ 1 + s.length + lang +s.length*lang,</pre>
26.
                     data = y_train,
27.
                     family = poisson(link = "log"),
                     prior = c(prior(normal(0.15, 0.1), class = Intercept),
28.
                                prior(normal(0, 0.15), class = b)),
29.
30.
                     cores = 4)
31.
32.
      # retrieve posterior samples
33.
      post.m1 <- posterior_samples(fit.m1)</pre>
      post.m2 <- posterior_samples(fit.m2)</pre>
34.
35.
36.
      # Calculated log pointwise predictive density using test data
      lppd.m1 <- 0
37.
38.
      1ppd.m2 <- 0
39.
40.
      for (i in 1:nrow(y_test)) {
41.
        lpd_im1 <- log(mean(dpois(y_test[i,]$nCross,</pre>
42.
                                    lambda = exp(post.m1[,1] + post.m1[,2]*y_test[i,]$s.length))))
        lppd.m1 <- lppd.m1 + lpd im1</pre>
43.
44.
45.
        lpd_im2 <- log(mean(dpois(y_test[i,]$nCross,</pre>
46.
                                    lambda = exp(post.m2[,1] + post.m2[,2]*y_test[i,]$s.length +
47.
                                                    post.m2[,3]*y_test[i,]$lang +
post.m2[,4]*y_test[i,]$s.length*y_test[i,]$lang))))
49.
        lppd.m2 <- lppd.m2 + lpd_im2</pre>
50.
51.
      }
52.
53.
      lpds.m1 <- c(lpds.m1, lppd.m1)</pre>
54.
      lpds.m2 <- c(lpds.m2, lppd.m2)</pre>
55. }
56.
```

```
1. # predective accuracy of model M1
2. elpd.m1 <- sum(lpds.m1)</pre>
3. elpd.m1
4.
5. ## [1] -2817.517
6.
7.
8. # predective accuracy of model M2
9. elpd.m2 <- sum(lpds.m2)</pre>
10. elpd.m2
11.
12. ## [1] -2683.562
13.
14. # Evidence in favour of M2 over M1
15. difference elpd <- elpd.m2-elpd.m1</pre>
16. difference_elpd
17.
18. ## [1] 133.9556
19.
```