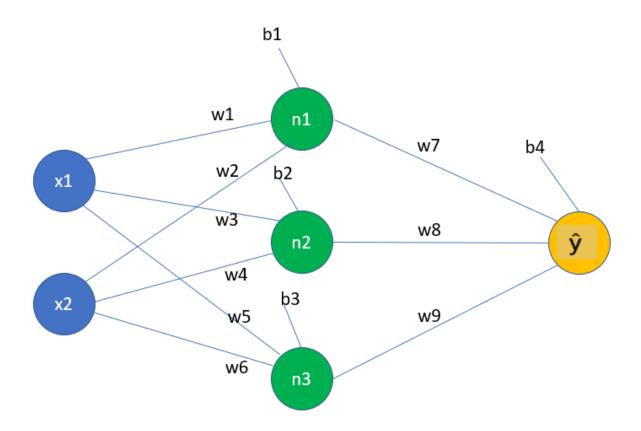
Problem 1 (8 pts): The figure below shows a 2-layer, feed-forward neural network with three hidden-layer nodes and one output node. x1 and x2 are the two inputs. For the following questions, assume the learning rate is $\alpha = 0.1$; activation function = sigmoid; loss function, MSE = $\frac{1}{2} (y - \hat{y})^2$; target output y = 1; For instance, the output of n1 equal sigmoid(w1 * x1 + w2 * x2 + b1). Compute one step of the backpropagation.

- a. Assume x1 = 0, x2 = 1; all weights and biases equal 1. Compute the updated weights for both the hidden layer and output layer. Show all steps in your calculations. (4 pts)
- b. Assume x1 = 1, x2 = 1; w1 = w3 = w5 = 0.5; w2 = w4 = w6 = -0.25; w7= 1, w8 = -1, w9 = 0 and biases weights equal 0.1. Compute the updated weights if your student id last digit is even then update weights: w2, w4, w6, w8; if odd update: w1, w5, w7, w9. You must show all steps in your calculations. (4 pts)



Coding!!!

Problem 2: We will develop an Artificial Neural Networks using MNIST digit data, where we will train an ANN model and then classify new instances. You can directly download the data using https://keras.io/api/datasets/mnist/ dataset currently contains 10 classes where each of the image sizes is (28×28). You should split the data into train and test data, where train data should be used for only training the model and test data should be kept separated and used only for evaluation purpose. You should select last two digits of your student ID – meaning that if your student id is 006000104, then you should select 0 and 4 for developing the binary classification model. If both last digit is identical, then select first and last digit.

- A. Build a NN for binary classification with **early stopping** criteria based on validation loss. Evaluate your model on the test data. Construct a confusion matrix. Present learning curve and include some examples of your prediction (3pts)
- B. Build three NNs for binary classification using three **different weight initializers** held other hyperparameters constant.
 - a. Construct three different confusion matrices and explain if there any difference in results for using three different initializers. (3pts)
 - b. Show three different learning curves and explain any differences (2 pts)

Problem 3 (2 pts): Build a NN for multi-class classification considering all the classes (10 classes) in the MNIST digit dataset: consider early stopping criteria based on the validation loss and finally construct confusion matrix and discuss the results.

Problem 4 (2 pts): Build a NN for multi-class classification considering all the classes (10 classes) in the MNIST digit dataset: consider three different optimization techniques: Batch Gradient Descent, Stochastic Gradient Descent and Mini- batch gradient descent (you can select mini-batch size between 4 and 64). Make a comparative analysis table columns including: method, accuracy, model size, training time, inference time.

You are required to submit:

- 1. An MS/PDF/Scanned document:
 - a. Include all the steps of your calculations.
 - b. Attach screenshots of the code output.
 - c. Include the summary of the model
 - d. Include a Table Mention all the hyperparameters you selected: activation function in hidden layer and output layer, weight initializer, number of hidden layers, neurons in hidden layers, loss function, optimizer, number of epochs, batch size, learning rate, evaluation metric

2. Source code:

- a. Python (Jupyter Notebook)
- b. Ensure it is well-organized with comments and proper indentation.
- Failure to submit the source code will result in a deduction of 5 points.
- Format your filenames as follows: "your_last_name_HW1.pdf" for the document and "your_last_name_HW1_source_code.ipynb" for the source code.
- Before submitting the source code, please double-check that it runs without any errors.
- Must submit the files separately.
- Do not compress into a zip file.
- HW submitted more than 24 hours late will not be accepted for credit.