

5. Basis Step:

Let  $T_0$  be the FBT that is just the root.

Then,  $e(T_0) = 1$  and  $i(T) = 0$

$$\text{so, } 1 = 0 + 1 \quad \checkmark$$

Inductive Step:

Let  $T_1$  and  $T_2$  be FBTs and  $T_3 = T_1 \cdot T_2$

Assume as the IH that  $e(T_1) = i(T_1) + 1$

and  $e(T_2) = i(T_2) + 1$

$$e(T_3) = e(T_1) + e(T_2)$$

$$= i(T_1) + i(T_2) + 1 + 1 \quad \text{by IH}$$

$$= i(T_3) + 1 \quad (i(T_3) = i(T_1) + i(T_2) + 1)$$