

8. Claim:  $3n^2 + 5n + 1$  is  $\Theta(n^2)$

$3n^2 + 5n + 1$  is  $O(n^2)$ :

$$\begin{aligned} 3n^2 + 5n + 1 &\leq 3n^2 + 3n^2 + 3n^2 \\ &\leq 9n^2 \end{aligned}$$

$$c = 9, n_0 = 1$$

$3n^2 + 5n + 1$  is  $\Omega(n^2)$ :

$$3n^2 + 5n + 1 \geq n^2$$

$$c = 1, n_0 = 1$$

Since  $3n^2 + 5n + 1$  is  $O(n^2)$  and  $\Omega(n^2)$ ,  
it is  $\Theta(n^2)$