

Recruitment rate stochasticity at the design stage of a clinical trial

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Why recruitment rates?

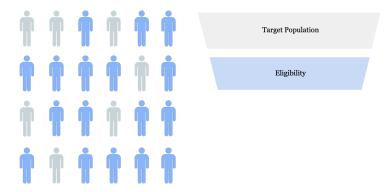
- Timely recruitment vital to the success of a clinical trial
- Inadequate number of subjects → lack of power
- Recruitment period too long → competing treatments
- Recruitment of patients varies at each stage
- Accrual = Cumulative Recruitment
- Carter (2004)

Target Population

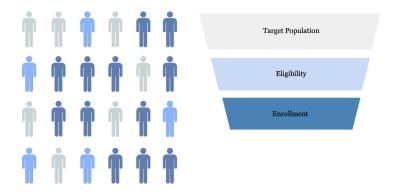


Target Population

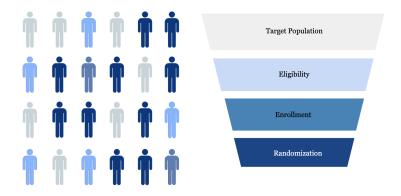
Eligibility



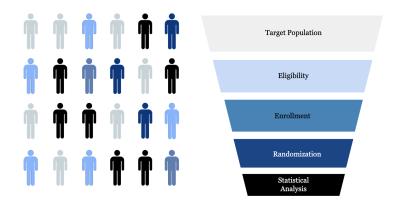
Enrollment



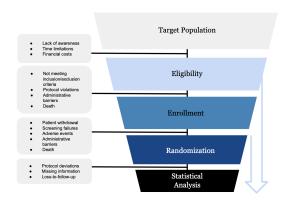
Randomization



Statistical Analysis



Patient Attrition





Uncertainty

- Aleatory: randomness inherent and unpredictable
- Epistemic: arises from limited knowledge about parameters

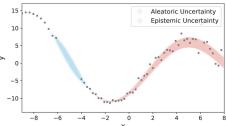


Figure: Visualization of two types of uncertainty (Yang and Li, 2023)

Models for Counts

Methods	Counts	Expectation	Variance	Aleatory	Epistemic
Expectation	$C(t) = \lambda t$	λt	0	No	No
Poisson	${\it C}(t) \sim { m Po}(\lambda { m t})$	λt	λt	Yes	No
Negative Binomial	$C(t) \sim \text{Po}(\bar{t}); \Lambda \sim G(\alpha, \beta)$	$\frac{\alpha}{\beta}$	$\frac{\alpha(\beta+1)}{\beta^2}$	Yes	Yes

Table: Aleatory and epistemic uncertainty in accrual shown by different models for counts.

- Time t = 550 days
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- Models for Counts:
 - Expectation: EC(t) = $\lambda t = 0.591 \cdot 550 = 325$
 - Poisson: $C(t) \sim Po(\lambda t)$
 - Negative Binomial: $C(t) \sim \text{Po}(\tilde{t}); \Lambda \sim G(\alpha, \beta)$

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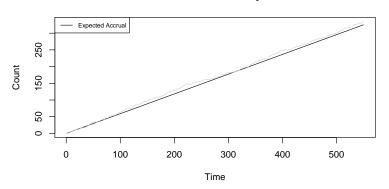
Accrual at time point t

- **Expectation**:
$$EC(t) = \underbrace{EC + \ldots + C}_{t \text{ times}} = tEC = \lambda t$$

- **Poisson**:
$$\underbrace{\operatorname{Po}(\lambda) + \ldots + \operatorname{Po}(\lambda)}_{t \text{ times}} = \operatorname{Po}(\lambda t)$$

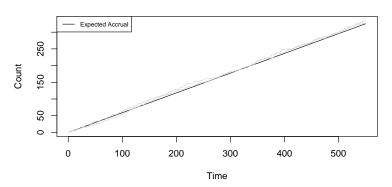
Accrual of 1 study

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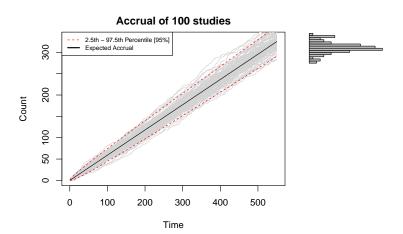


Accrual of 2 studies

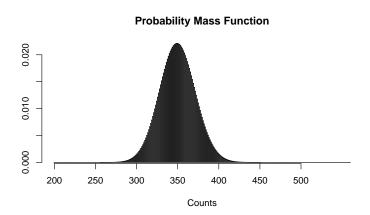
Accrual of 2 studies



Accrual of 100 studies

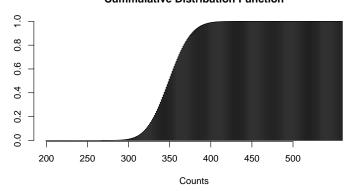


Theoretical PMF

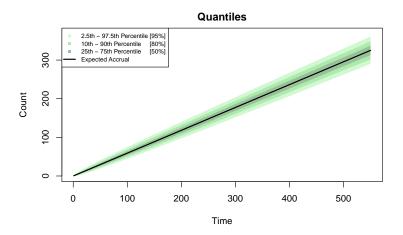


Theoretical CDF

Cummulative Distribution Function



Uncertainty bands



Negative binomial derived from Poisson-Gamma model

Recruitment in one unit of time (t = 1)

. . . .



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- Models for Counts:
 - − Expectation: $EC(t) = \lambda t = 0.591 \cdot 550 = 325$
 - − **Poisson**: $C(t) \sim Po(\lambda t)$
 - Negative Binomial: $C(t) \sim Po(\Lambda t)$; $\Lambda \sim G(\alpha, \beta)$



Comparison between Poisson and Negative Binomial - PMF



Comparison between Poisson and Negative Binomial - CDF



Shrunk Slide 1



Results



Conclusion



Next steps



References

- Carter, R. E. (2004). Application of stochastic processes to participant recruitment in clinical trials. *Controlled clinical trials*, 25(5):429–436.
- Liu, J., Jiang, Y., Wu, C., Simon, S., Mayo, M. S., Raghavan, R., and Gajewski, B. J. (2023). *accrual: Bayesian Accrual Prediction*. R package version 1.4.
- Spiegelhalter, D., Pearson, M., and Short, I. (2011). Visualizing uncertainty about the future. *Science*, 333(6048):1393–1400.
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