

Introduction to Computers

LECTURE 14 - CRYPTOGRAPHY



Announcements

This lecture: Cryptography

Reading: Read Chapter 5 of “Blown to Bits”

Acknowledgement: Some of this lecture slides are based on CSE 101 lecture notes by Prof. Kevin McDonald at SBU

Cryptography

- The field of **cryptography** (literally, “secret writing”) has a long history
- Modern cryptography contains a large amount of terminology
 - **Plaintext** refers to unencrypted data that can be intercepted by some means
 - Encryption scrambles data in a way that makes it unintelligible to those unauthorized to view it
 - The encrypted data is called **ciphertext**
- Modern encryption schemes often use **public-key cryptography**
 - In public-key cryptography, each user has two related **keys**, one public and one private
 - Each person’s public key is distributed freely
- In practice, both secret key and public key cryptography are used in certain cases
 - Content (i.e. email) is encrypted with a random symmetric key (secret key cryptography)
 - The random key is encrypted with the recipient’s public key (public-key cryptography)

Cryptography

- The public/private key pairs are generated by a computer program in such a way:
 - that decryption of content encrypted with the public key is only possible with the private key
 - Decryption of content encrypted with the private key is only possible with the public key
 - The keys themselves are modular inverses around a large composite number based on the product of two very large primes
 - The large composite is difficult to factor so knowing the public key does not yield the related private key
 - The mathematical details are otherwise beyond the scope of the course
 - ➔ But if you are REALLY interested, look here: [https://en.wikipedia.org/wiki/RSA_\(cryptosystem\)](https://en.wikipedia.org/wiki/RSA_(cryptosystem))
 - Other illustration: <https://www.youtube.com/watch?v=E5FEqGYLL0o>
- In this Lecture some simpler, but much less secure techniques for encrypting text are covered

Example: Email Encryption

- A random key is generated and used to encrypt a message with a symmetric algorithm like AES
 - The random key is called a Content-Encryption Key or CEK
- The random key is encrypted with the receiver's public key
 - The public key is called a Key Encryption Key or KEK
- Only the receiver's private key can decrypt the random key needed to decrypt the content
- Why do this?
 - Public Key operations are computationally expensive
 - Better to use efficient secret key cryptography on larger blocks of data (the content)
 - Then use public key cryptography on only a small piece of data (the CEK)

Caesar Cipher

- One of the simplest **ciphers** (algorithms for encrypting and decrypting text) is the **single substitution cipher**
 - One variant of the single substitution cipher is known as a shift cipher which works by replacing each letter of a word with the letter of the alphabet that is k letters later in the alphabet
 - One variant of the shift cipher is known as the **Caesar cipher**. This cipher sets k to 3
- K is the **key** of the encryption scheme and provides the shift amount: a number in the range 1 through 25, inclusive
- In general, the **key** for a cipher is the secret piece of information that both parties must exchange ahead of time
- Julius Caesar used $k=3$ in his military communications, hence the name Caesar cipher given to a shift cipher with a **key** of 3

Caesar Cipher

- For example, to encode letters with $k=3$ the following is done:
 - Replace “A” with “D”, “B” with “E”, and so on
- For letters at the end of the alphabet, “wrap-around” to the front of the alphabet
 - For $k=3$, we would replace “X” with “A”, “Y” with “B”, and “Z” with “C”
- The phrase “Stony Brook” with a shift amount of 2 would be encrypted as “Uvqpa Dtqqm”
- To decrypt a message, shift each letter of the encrypted message leftward in the alphabet by the shift amount

Caesar Cipher

- Let's consider functions **caesar_encrypt** and **caesar_decrypt**
- Both functions will take a string and a shift amount
 - For **caesar_encrypt**, the string is a plaintext message
 - For **caesar_decrypt**, the string is an encrypted message
 - Non-letter characters will be left unencrypted

Caesar Cipher

- The encryption algorithm is pretty straightforward:
 - First map each letter to a number in the range 0 through 25: A \rightarrow 0, B \rightarrow 1, ..., Z \rightarrow 25
 - Next add k to the number and *mod* by 26
 - Finally, map the shifted value to a letter from the alphabet
- So, the encryption formula is $E(x) = (x + k) \bmod 26$, where x is the number for the plaintext letter, k is the key, and $E(x)$ gives the number for the ciphertext letter
- To decrypt, subtract the key from the encrypted value, add 26 (to eliminate any negative differences), and mod by 26 to recover the original number

caesar_encrypt()

```
def caesar_encrypt(plaintext, shift_amt):  
    ciphertext = ''  
    for ch in plaintext:  
        if ch.isupper():  
            replacement = (ord(ch) - ord('A') + shift_amt) % 26 + ord('A')  
            ciphertext += chr(replacement)  
        elif ch.islower():  
            replacement = (ord(ch) - ord('a') + shift_amt) % 26 + ord('a')  
            ciphertext += chr(replacement)  
        else:  
            ciphertext += ch  
    return ciphertext
```

See [caesar_cipher.py](#)

caesar_decrypt()

```
def caesar_decrypt(ciphertext, shift_amt):  
    plaintext = ''  
    for ch in ciphertext:  
        if ch.isupper():  
            replacement = (ord(ch) - ord('A') - shift_amt + 26) % 26 + ord('A')  
            plaintext += chr(replacement)  
        elif ch.islower():  
            replacement = (ord(ch) - ord('a') - shift_amt + 26) % 26 + ord('a')  
            plaintext += chr(replacement)  
        else:  
            plaintext += ch  
    return plaintext
```

See [caesar_cipher.py](#)

Multiplicative Cipher

- The Caesar cipher encrypts and decrypts numbers by adding or subtracting the key to a plaintext letter's number (where $A \rightarrow 0$, $B \rightarrow 1$, ..., $Z \rightarrow 25$)
- Suppose multiplication is used instead \rightarrow multiply each number by the key?
 - This is a **multiplicative cipher**
- Provided that the key is relatively prime to 26, no two letters will be encrypted to the same cipher letter
 - Two numbers are relatively prime if they have no common factors except for 1
- The encryption formula is $E(x) = kx \bmod 26$

Multiplicative Cipher

- Suppose the key is 7
 - The letter A (0) is mapped to $(0 \times 7) \bmod 26 = 0$, which is also A
 - The letter J (9) is mapped to $(9 \times 7) \bmod 26 = 11$, which is L
- Although this cipher seems to be more complex than a shift cipher, it is less secure than the shift cipher because the number of possible keys is smaller

Multiplicative Cipher

- Example with $k=7$. So, $E(x)=7x \bmod 26$.

Plaintext	x	$E(x)$	Ciphertext	Plaintext	x	$E(x)$	Ciphertext
A	0	0	A	N	13	13	N
B	1	7	H	O	14	20	U
C	2	14	O	P	15	1	B
D	3	21	V	Q	16	8	I
E	4	2	C	R	17	15	P
F	5	9	J	S	18	22	W
G	6	16	Q	T	19	3	D
H	7	23	X	U	20	10	K
I	8	4	E	V	21	17	R
J	9	11	L	W	22	24	Y
K	10	18	S	X	23	5	F
L	11	25	Z	Y	24	12	M
M	12	6	G	Z	25	19	T

multiplicative_encrypt()

```
def multiplicative_encrypt(plaintext, k):  
    ciphertext = ''  
    for ch in plaintext:  
        if ch.isupper():  
            replacement = ((ord(ch) - ord('A')) * k) % 26 + ord('A')  
            ciphertext += chr(replacement)  
        elif ch.islower():  
            replacement = ((ord(ch) - ord('a')) * k) % 26 + ord('a')  
            ciphertext += chr(replacement)  
        else:  
            ciphertext += ch  
    return ciphertext
```

Multiplicative Cipher

- To decrypt a message encrypted using this scheme some arithmetic is needed to determine the *modular multiplicative inverse of k with respect to 26*
- Going into that much math is a bit out of scope of the course
- So instead, to decrypt simply encrypt the entire alphabet to find the 26 mappings, and then perform the reverse mapping for each encrypted letter
 - Remember that the recipient knows the value of k
- To help write this *brute force* algorithm use Python's **zip** function
- **zip** allows iterating over two or more collections simultaneously

Aside: the zip() Function

```
names = ['Adam', 'Chris', 'Mary', 'Frank']  
ages = [21, 19, 24, 22]  
for name, age in zip(names, ages):  
    print(name + ' ' + str(age))
```

•Output:

```
Adam 21  
Chris 19  
Mary 24  
Frank 22
```

Multiplicative Cipher

- Two other Python tricks/features to use:
 - a dictionary comprehension, which was explored in an earlier Lecture, and
 - the string called **`string.ascii_letters`**, which contains all 26 letters of the Latin alphabet in uppercase and lowercase

multiplicative_decrypt()

```
reverse_mapping = {}
decrypt_key = -1
def multiplicative_decrypt(ciphertext, k):
    global reverse_mapping, decrypt_key
    if k != decrypt_key:
        decrypt_key = k
        encrypted_letters = [multiplicative_encrypt(letter, k)
                             for letter in string.ascii_letters]
        reverse_mapping = {encrypted_letter: letter
                           for letter, encrypted_letter in
                           zip(string.ascii_letters, encrypted_letters)}
    plaintext = ''
    for ch in ciphertext:
        if ch in reverse_mapping:
            plaintext += reverse_mapping[ch]
        else:
            plaintext += ch
    return plaintext
```

See [multiplicative_cipher.py](#)

Affine Cipher

- An **affine cipher** combines ideas from the shift cipher and multiplicative cipher, performing both a multiplication and an addition
- The value x of some letter is encrypted using the formula $(ax+b) \bmod 26$ where a is the *multiplier* and b is the *shift* amount
 - a and b together form the encryption key
- In some sense, the affine cipher should be stronger than the shift cipher and multiplicative cipher, but it's still inherently weak because it's still a substitution cipher
- The encryption function looks similar to the one for the multiplicative cipher

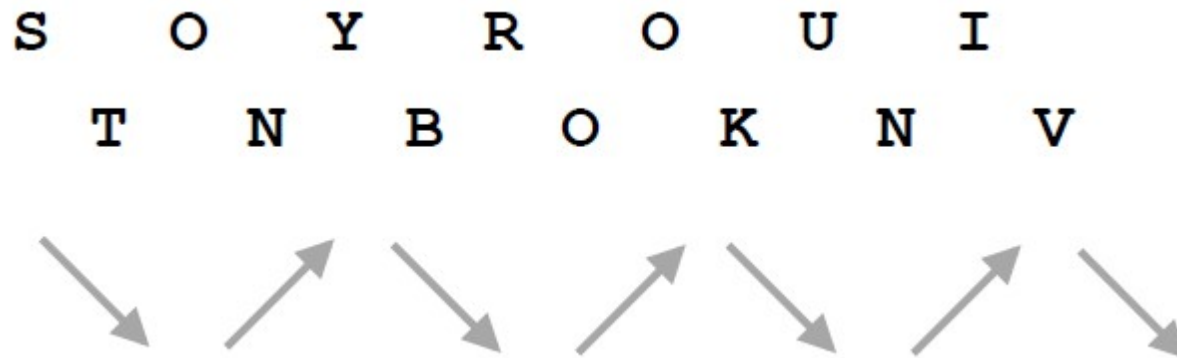
affine_encrypt()

```
def affine_encrypt(plaintext, a, b):  
    ciphertext = ''  
    for ch in plaintext:  
        if ch.isupper():  
            replacement = ((ord(ch) - ord('A')) * a + b) % 26 + ord('A')  
            ciphertext += chr(replacement)  
        elif ch.islower():  
            replacement = ((ord(ch) - ord('a')) * a + b) % 26 + ord('a')  
            ciphertext += chr(replacement)  
        else:  
            ciphertext += ch  
    return ciphertext
```

See [affine_cipher.py](#)

Rail Fence Cipher

- The **rail fence cipher** is a type of **transposition cipher**
- In a **transposition cipher**, the characters in the original message are rearranged somehow (as opposed to being substituted)
- The rail fence cipher rearranges the characters in a zigzag pattern
- The key is the number of rows used to create the zigzag
- For example, the message **STONYBROOKUNIV** written over two rows would look like this:



Rail Fence Cipher: Encryption

S O Y R O U I
T N B O K N V

- To produce the final encrypted message read off the characters row-by-row:
SOYROUTNBOKNV
- The same message written over three rows would look like this:

S Y O I
T N B O K N V
O R U

- The encrypted message would be: **SYOITNBOKNVORU**

Rail Fence Cipher: Encryption

- To implement the rail fence cipher create a list of empty strings, one per row, and append characters one-by-one to each string
- Use a variable **row** (initialized to 0) that first increases towards **num_rows**, then decreases back towards 0, then increase again, etc., until the entire plaintext message has been encrypted
- This computation will be encapsulated in a helper function called **next_row**

next_row() Helper Function

```
def next_row(row, step, num_rows):  
    if row == 0:  
        step = 1  
    elif row == num_rows - 1:  
        step = -1  
    row += step  
    return row, step
```

- To get a sense of how this function works, pretend that there are 4 rows in the grid and the plaintext message has 10 characters

See [railfence_cipher.py](#)

next_row() Helper Function

```
def next_row(row, step, num_rows):  
    if row == 0:  
        step = 1  
    elif row == num_rows - 1:  
        step = -1  
    row += step  
    return row, step
```

Test Code

```
row = 0  
step = 1  
num_rows = 4  
for i in range(10):  
    print(row, step)  
    row, step = next_row(row, step, num_rows)
```

Output:

row increasing	0	1
	1	1
	2	1
	3	1
row decreasing	2	-1
	1	-1
	0	-1
row increasing	1	1
	2	1
	3	1

railfence_encrypt()

```
def railfence_encrypt(plaintext, num_rows):  
    row = 0  
    step = 1  
    # create num_rows empty strings in a list  
    rows = [''] * num_rows  
    for ch in plaintext:  
        rows[row] += ch  
        row, step = next_row(row, step, num_rows)  
    return ''.join(rows)
```

- The **join** function creates a string by concatenating the elements of a list together
- See [railfence_cipher.py](#)

Example: railfence_encrypt()

- Function call: **railfence_encrypt('STONY', 3)**
rows = ['', '', '']
for ch in plaintext:
 rows[row] += ch
 row, step = next_row(row, step, num_rows)
- Contents of rows list:
rows = ['SY',
 'TN',
 'O']
- Then call **".join(rows)** to generate the final ciphertext: **'SYTNO'**

Rail Fence Cipher: Decryption

- The idea for decryption is to first construct a grid using lists of lists of empty strings
- The key tells how many rows are in the grid
- The length of the message tells the number of columns
- Using the same zigzag path from the encryption algorithm, place a **None** object (or some other marker) where the characters will go
- Then, take letters one at a time from the encrypted text and move across the grid row by row, replacing the **None** values with characters from the encrypted message
- Finally, trace out the zigzag pattern once more to read off the plaintext characters

Rail Fence Cipher: Decryption

- Example for ciphertext '**SYOITNBOKNVORU**' with **num_rows = 3**
- The input contains 14 letters, so create a grid with 3 rows and 14 columns by creating a list containing 3 lists of 14 empty strings each:

Rail Fence Cipher: Decryption

Next, travel in a zigzag pattern, inserting **None** objects, which are visualized below as dots:

•				•				•				•	
	•		•		•		•		•		•		•
		•				•				•			

Rail Fence Cipher: Decryption

- Then travel across each row, inserting characters from the ciphertext whenever a **None** object is found
- The ciphertext is '**SYO****ITNBOKNVORU**'
- First row completed:

S				Y				O				I	
	•		•		•		•		•		•		•
		•				•				•			

Rail Fence Cipher: Decryption

- The ciphertext is '**SYOITNBOKNVORU**'
- Second row completed:

S				Y				O				I	
	T		N		B		O		K		N		V
		•				•				•			

- Third row completed: '**SYOITNBOKNVORU**'

S				Y				O				I	
	T		N		B		O		K		N		V
		O				R				U			

Rail Fence Cipher: Decryption

- It is now easy to read off the original message by traversing the grid once again in zigzag order

S				Y				O				I	
	T		N		B		O		K		N		V
		O				R				U			

railfence_decrypt()

```
def railfence_decrypt(ciphertext, num_rows):  
    grid = []  
    for i in range(num_rows):  
        grid += [ ' ' * len(ciphertext) ]  
    # set up the grid, placing a None value  
    # where each letter will go  
    row = 0  
    step = 1  
    for col in range(len(ciphertext)):  
        grid[row][col] = None  
        row, step = next_row(row, step, num_rows)
```

See [railfence_cipher.py](#)

railfence_decrypt()

```
# place characters from the encrypted  
# message into the grid  
next_char_index = 0  
for row in range(num_rows):  
    for col in range(len(ciphertext)):  
        if grid[row][col] is None:  
            grid[row][col] = ciphertext[next_char_index]  
            next_char_index += 1
```

See [railfence_cipher.py](#)

railfence_decrypt()

```
# read the characters from the grid in  
# zigzag order  
plaintext = ''  
row = 0  
step = 1  
for col in range(len(ciphertext)):  
    plaintext += grid[row][col]  
    row, step = next_row(row, step, num_rows)  
return plaintext
```

See [railfence_cipher.py](#)

The Vigenère Cipher

- The **Vigenère Cipher** was invented in the 16th century by Frenchman Blaise de Vigenère
 - Uses a series of substitution ciphers to encode a message
 - Took about three centuries before cryptographers figured out a reliable way of cracking this cipher
 - Based on the use of a 26x26 grid of substitution ciphers, each one shifted to the right by one spot
 - A keyword or phrase also needs to be picked that determines which rows of this grid to use

See [vigenere_cipher.py](#)

The Vigenère Cipher

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
A	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
B	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A
C	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B
D	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C
E	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D
F	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E
G	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F
H	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G
I	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H
J	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I
K	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J
L	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K
M	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L
N	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M
O	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N
P	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O
Q	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P
R	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q
S	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R
T	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S
U	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T
V	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U
W	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V
X	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W
Y	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X
Z	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y

	A	B	C	D	E	F	G
A	A	B	C	D	E	F	G
B	B	C	D	E	F	G	H
C	C	D	E	F	G	H	I
D	D	E	F	G	H	I	J

The Vigenère Cipher: Example #1

- Suppose the keyword chosen is **PYTHON**
- Then use this part of the grid:

A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O
Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X
T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S
H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G
O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N
N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M

- If the message is longer than the key, repeat the key as many times as needed to encode the message

The Vigenère Cipher: Example #1

A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O
Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X
T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S
H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G
O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N
N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M

- To encrypt each plaintext letter, find its column along the top row of the table
- Then find the row for the corresponding letter from the key
- The cell at the intersection of that row and column gives the letter for the encrypted message

The Vigenère Cipher: Example #1

A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O
Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X
T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S
H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G
O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N
N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M

- Example: encode **COMPUTER**
- Key: **PYTHONPY**
- Plaintext: **COMPUTER**
- Ciphertext : **R**

The Vigenère Cipher: Example #1

A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O
Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X
T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S
H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G
O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N
N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M

- Example: encode **COMPUTER**
- Key: **PYTHONPY**
- Plaintext: **COMPUTER**
- Ciphertext : **RM**

The Vigenère Cipher: Example #1

A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O
Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X
T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S
H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G
O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N
N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M

- Example: encode **COMPUTER**
- Key: **PYTHONPY**
- Plaintext: **COMPUTER**
- Ciphertext : **R M F**

The Vigenère Cipher: Example #1

A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O
Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X
T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S
H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G
O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N
N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M

- Example: encode **COMPUTER**
- Key: **PYTHONPY**
- Plaintext: **COMPUTER**
- Ciphertext : **RMFW**

The Vigenère Cipher: Example #1

A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O
Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X
T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S
H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G
O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N
N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M

- Example: encode **COMPUTER**
- Key: **PYTHONPY**
- Plaintext: **COMPUTER**
- Ciphertext : **RMFWI**

The Vigenère Cipher: Example #1

A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O
Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X
T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S
H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G
O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N
N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M

- Example: encode **COMPUTER**
- Key: **PYTHONPY**
- Plaintext: **COMPUTER**
- Ciphertext : **RMFWIG**

The Vigenère Cipher: Example #1

A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O
Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X
T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S
H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G
O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N
N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M

- Example: encode **COMPUTER**
- Key: **PYTHONPY**
- Plaintext: **COMPUTER**
- Ciphertext : **RMFWIGT**

The Vigenère Cipher: Example #1

A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O
Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X
T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S
H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G
O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N
N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M

Example: encode **COMPUTER**

Key: **PYTHONPY**

Plaintext: **COMPUTER**

Ciphertext : **RMFWIGTP**

The Vigenère Cipher: Example #2

- Decryption follows the reverse procedure as for encryption
- Suppose the keyword is **JOKE** and the ciphertext is **OIXGCWYR**
- To decrypt, first arrange the repeated keyword and encrypted message as follows:
- Key: **J O K E J O K E**
- Ciphertext: **O I X G C W Y R**

The Vigenère Cipher: Example #2

- Then, search for each letter from the encrypted message in the row for the corresponding letter from the key
- The column label provides the decrypted letter
- The ciphertext is **OIXGCWYR**
- For this ciphertext, look up **O** in the row for **J**. Looking at the top row, notice that the column is **F**

A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I
O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N
K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J
E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D

The Vigenère Cipher: Example #2

- The ciphertext is **O I X G C W Y R**
- The plaintext so far is **F**
- Then look up the **I** from the encrypted message in row **O**.
- The **I** is in column **U**. The decrypted message so far is **FU**.

A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I
O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N
K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J
E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D

The Vigenère Cipher: Example #2

- The ciphertext is **O I X G C W Y R**
- The plaintext so far is **F U**
- Next look up the letter **X** in row **K**. **X** is in column **N**.
- The decrypted message is now **F U N**.

A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I
O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N
K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J
E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D

The Vigenère Cipher: Example #2

- The ciphertext is **O I X G C W Y R**
- The plaintext so far is **FUN**
- Next look up the letter **G** in row **E**. **G** is in column **C**.
- The decrypted message is now **FUNC**.

A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I
O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N
K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J
E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D

The Vigenère Cipher: Example #2

- Continue in this fashion until the last letter. The final decrypted message is generated:
- Key: **J O K E J O K E**
- Ciphertext: **O I X G C W Y R**
- Plaintext: **F U N C T I O N**

A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I
O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N
K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J
E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D

The Vigenère Cipher

- To implement the Vigenère Cipher, there is no need to represent the table in the computer's memory
- Instead, use the algorithm below, which computes the table entries “on the fly”:
 1. Map each letter from the plaintext to a number in the range 0 to 25, as was done with the other ciphers. ($A \rightarrow 0, B \rightarrow 1, \dots, Z \rightarrow 25$)
 2. Add this number to the number corresponding to the keyword's letter (and then mod by 26).
 - Example: for plaintext **COMPUTER** and keyword **PYTHON**
 - 2 is the number for C and 15 is the number for P
 - To encode C: $C \rightarrow 2 \rightarrow (2 + 15) \bmod 26 = 17$
 3. Convert the sum (mod 26) to its corresponding letter of the alphabet (with $0 \rightarrow A, 1 \rightarrow B, \dots, 25 \rightarrow Z$).

The Vigenère Cipher

- The decryption algorithm performs a similar series of steps, but in reverse order:
 1. Map each letter from the encrypted message to a number in the range 0 to 25.
 2. Subtract from this number the number corresponding to the keyword's letter.
 3. Add 26 in case the subtraction resulted in a negative difference, and then compute the remainder mod 26.
 4. Convert the resulting number to its corresponding letter of the alphabet ($0 \rightarrow A$, $1 \rightarrow B$, ..., $25 \rightarrow Z$).

vigenere_encrypt()

```
def vigenere_encrypt(plaintext, keyword):  
    # duplicate the keyword as many times as needed  
    keyword = keyword * (len(plaintext) // len(keyword) + 1)  
    # convert plaintext letters to numbers  
    plaintext_nums = [ord(ch) - ord('A') for ch in plaintext]  
    # convert keyword letters to numbers  
    keyword_nums = [ord(ch) - ord('A') for ch in keyword]  
    # generate ciphertext  
    ciphertext = ''  
    for i in range(len(plaintext)):  
        # add the two numerical codes and map sum (mod 26)  
        # back to a letter  
        ciphertext += chr((plaintext_nums[i]+keyword_nums[i]) % 26 + ord('A'))  
    return ciphertext
```

vigenere_decrypt()

```
def vigenere_decrypt(ciphertext, keyword):  
    # duplicate the keyword as many times as needed  
    keyword = keyword * (len(ciphertext) // len(keyword) + 1)  
    # convert ciphertext letters to numbers  
    ciphertext_nums = [ord(ch)-ord('A') for ch in ciphertext]  
    # convert keyword letters to numbers  
    keyword_nums = [ord(ch)-ord('A') for ch in keyword]  
    # generate plaintext  
    plaintext = ''  
    for i in range(len(ciphertext)):  
        # subtract keyword num from ciphertext num, add 26  
        # and map difference (mod 26) back to a letter  
        plaintext += chr((ciphertext_nums[i]-keyword_nums[i] + 26) % 26 + ord('A'))  
    return plaintext
```

Encryption Algorithms

- A major drawback of the shift, multiplicative, affine, transposition and Vigenère ciphers (beside the obvious drawback that they can be broken) is the use of a *shared private key*
- The private key must first be exchanged, presumably in a face-to-face manner or some other “secure” way
- **Public-key cryptography does not have this shortcoming:** each person has a private key that is never shared and a public key that is shared
- **The only known way at the moment to crack the hardest public-key encryption algorithms is to try virtually all the possible keys, which is an *intractable* problem**
- Public key cryptography is not a panacea:
 - Operations to encrypt/decrypt are ‘expensive’ computationally
 - Public key ownership is an issue
 - To assure an attacker cannot create a man-in-the-middle attack, authentication is needed with certificates
 - Generation and use of certificates is beyond the scope of this course.
 - Here’s a starting reference if you’re interested: https://en.wikipedia.org/wiki/Public_key_certificate

Cryptography Website

- www.counton.org/explorer/codebreaking/index.php
- This is an excellent website that covers the basics of encryption.
- It includes programs that can be used to test knowledge of the ciphers studied in this Lecture

Questions?
