# $\begin{array}{c} \texttt{MC-ChemDB User's Manual} \\ v\_1.0 \end{array}$

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# Chapter 1

## Introduction

MC-ChemDB is a database of reactions rates and photoprocesses cross-sections for the simulation of cold chemical plasmas. The originality of MC-ChemDB is to encode uncertainty one the reaction rate parameters and cross-sections. This additional feature makes that MC-ChemDB is not directly readable by usual simulation codes, but it must be processed to produce samples of readable databases (for instance in the KiDA-type format [1], with one line per reaction).

Running a simulation code over a set of these samples amounts to what is known as Monte Carlo uncertainty propagation (MCUP), and enables to quantify the uncertainty on the predictions of chemical models due to the uncertainty on the chemical parameters. It also enables to perform sensitivity analysis to identify key reactions in need of better determination.

### 1.1 Data and code adaptations

The database consists of three modules: one for the reactions between neutral species, one for the reactions involving ions, and one for the photo-processes (photodissociation and photoionization). This segregation reflects different approaches to describe reaction rates and handle uncertainty.

#### 1.1.1 Rate constants

Following a common practice in atmospheric chemistry, one considers here a representation of a temperature-dependent uncertainty band by a specific function, called hereafter the "f/g representation" [2, 3, 4].

The five parameters necessary to calculate the Kooij expression of a bimolecular rate constant k(T) and its T-dependent multiplicative uncertainty  $u_k(T)$  are  $\{\alpha, \beta, \gamma, f, g\}$ :

$$k'(T) = k(T) \times u_k(T) \tag{1.1}$$

$$k(T) = \alpha \times (T/T_0)^{\beta} \times \exp(-\gamma/T)$$
(1.2)

$$u_k(T) = \exp\left(r \times \log\left(f \times \exp(g|1/T - 1/T_0|)\right)\right) \tag{1.3}$$

where  $r \sim N(0,1)$  is a standard normal random number, and  $T_0$  is a reference temperature,

typically 300 K.

With current databases, the user reads the values of f and g and generates random realizations of  $u_k(T)$  curves. In the perspective of transferring the random number generation on the database/server side, one can take advantage of the fact that Eq. 1.3 can be rewritten as

$$u_k(T) = f^r \times \exp\left(g \times r \left| 1/T - 1/T_0 \right| \right),\tag{1.4}$$

which shows that random realizations of  $u_k(T)$  curves can still be parameterized by only two numbers  $f' = f^r$  and  $g' = g \times r$ . Without changing the initial database format, one can thus replace the nominal values in the database by random values

$$\{\alpha, \beta, \gamma, f, g\} \longrightarrow \{\alpha, \beta, \gamma, f' = f^r, g' = g \times r\}.$$
 (1.5)

In order to benefit from this solution, the end user has to adapt the rate expression in his code to include the  $f * exp(g|1/T - 1/T_0|)$  term.

### 1.1.2 Branching ratios

When branching ratios (BR) have been measured instead of *partial* rate constants, one has to use a specific representation separating the global rate constant from the BRs. For the global rate constant, the uncertainty model can be any of the two cases detailed previously.

Random values of the BRs,  $b_i$ , are sampled from probabilistic trees built from Dirichlettype distributions [5]. This way, sets of BRs are generated consistently with the sum-to\_one constraint ( $\sum b_i = 1$ ), avoiding the spurious effects demonstrated in [6, 7].

To derive a partial rate constant, one has thus to generate random parameters on the database side

$$\{\alpha' = \alpha * b_i', \beta, \gamma, f', g'\}$$

(for instance), where  $b'_i$  is a realization of the BR for the  $i^{th}$  pathway. Here again, no change of database format is required. On the user side, the changes are the same as described above, depending on the description of the global rate's uncertainty.

### 1.1.3 Photo-processes

A special treatment has to be considered for photo-processes which are described by wavelength-dependent properties (cross-sections, branching ratios) [8]. The database has to provide random samples of wavelength-dependent cross-sections and branching ratios as sets of files.

#### 1.1.3.1 Cross-sections

The uncertainty on the cross-section is defined by the uncertainty factor  $XS_F$ . Samples of cross-sections are thus obtained by

$$\sigma_{MC}(\lambda, R) = \sigma_0(\lambda, R) \times u_F$$
 $u_F \sim LN(1, XS\_F)$ 

where  $\sigma_0(\lambda, R)$  is the reference photo-absorption cross-section for species M and  $u_F$  is a random number with a log-normal distribution centered on 1 with uncertainty factor  $XS_F$ . This scheme assumes only systematic, wavelength-independent, uncertainty.

#### 1.1.3.2 Branching ratios

As for the ionic reactions, probabilistic trees are used to get sum-to-one constrained random branching ratios. For most photodissociations, one does not have extensive information about the individual channel uncertainties [?], and the main partition is made between ionic channels and neutral channels because they are often issued from different experiments [9]. The proposed uncertainty scheme is therefore identical for all molecules.

A nested probabilistic tree was proposed in Ref. [9], on the basis that the sum of all ionic channels is less uncertain that individual channels. In this hypothesis, the probabilistic tree has two levels:

1. The first one deals with the neutrals/ions separation, with branching rations  $b_N$  and  $b_I$ , respectively:

$$(b_N, b_I) \sim \text{Dirg}(b_{N,0} < \text{Neutrals} >, (1 - b_{N,0}) < \text{Ionic} >; r_{NI}b_{N,0}, r_{NI}(1 - b_{N,0}))$$

where one uses a generalized Dirichlet distribution with parameters  $b_{N,0} = \sum_{i \in Neutrals} b_i$  and  $r_{NI}$ .  $b_{N,0}$  is the sum of the reference branching ratios of the neutral channels at a given wavelength.  $r_{NI}$  is the relative uncertainty on the total charged species measurement of about 3% on  $b_I$  [5, 9].

2. If one has more than one neutral channel, a secondary tree is specified by a generalized Dirichlet distribution with the corresponding branching ratios as parameters (renormalized) and a relative uncertainty  $r_N$  of about 20 %. A similar sub-tree is designed for ionic channels  $(r_I)$ .

This representation ensures that the sum of the ionic channels has a small uncertainty, while the branching ratios of individual channels might be more uncertain.

I found that this approach might result in strong uncertainty discontinuities along the wavelength, and I propose an alternative one-level model based on partial cross-sections. One assumes that all neutral channels cross-sections are measured within 20 %  $(r_N)$  and all ionic

channels within 10 %  $(r_I)$ . The uncertainty on the branching ratios is derived by linear uncertainty propagation. Starting from

$$\sigma_T = \sum_i \sigma_i \tag{1.6}$$

and

$$b_i^0 = \frac{\sigma_i}{\sigma_T} \tag{1.7}$$

one gets

$$u_i = \sqrt{\frac{1}{\sigma_T^2} u_{\sigma_i}^2 + \left(\frac{\sigma_i}{\sigma_T^2}\right)^2 u_{\sigma_T}^2 - 2\frac{\sigma_i}{\sigma_T^3} u_{\sigma_i}^2}$$

$$\tag{1.8}$$

where  $u_{\sigma_i} = r_{N/I}\sigma_i$  is the uncertainty on the  $\sigma_i$  cross-section (Neutral or Ionic), and  $u_{\sigma_T} = \sqrt{\sum_i u_{\sigma_i}^2}$  is the uncertainty on their sum. The third term in the LUP expression results from the covariance between  $\sigma_i$  and  $\sigma_T$ :  $cov(\sigma_i, \sigma_T) = cov(\sigma_i, \sigma_i) = u_{\sigma_i}^2$ , assuming independent measurement errors for all cross-sections.

One can then use a generalized Dirichlet distribution based on the estimated uncertainties

$$(b_1, \dots, b_n) \sim Dirg(b_1^0, \dots, b_n^0; u_1, \dots, u_n)$$
 (1.9)

The sampling is done independently for each wavelength, leading to purely random errors. Several options are tested in Chem-DBUI to introduce some level of serial correlation.

# Chapter 2

# Database structure

There is presently a discrepancy on the uncertainty representations of reaction rates for reactions involving neutrals and the ones involving ions. The sum-to-one of branching ratios has been extensively implemented in ionic reactions by Pernot and coworkers [10, 6, 5]. This has not yet been done for neutrals [11, 12]. Moreover, a special treatment has to be considered for photo-processes which are described by wavelength-dependent properties (cross-sections, branching ratios) [8].

The database consists therefore of three independent sections (Ions, Neutrals and Photoprocesses).

### 2.1 Reaction rate expressions

The temperature- and density-dependence of reactions rates between neutrals and ions are described by different rate laws. The dependence on temperature (T in Kelvin) is typically expressed by the following laws, depending globally on three parameters ( $\alpha$ ,  $\beta$ ,  $\gamma$ ):

kooij 
$$\alpha\times (T/T_0)^{\beta}\times exp(-\gamma/T)\equiv k(\alpha,\beta,\gamma,T_0)$$
 
$$\alpha\times (T_0/T)^{\beta}=k(\alpha,-\beta,0,T_0)$$
 ionpol1 
$$\alpha\times (0.62+0.4767\times\beta\times (T_0/T)^{0.5})$$
 ionpol2 
$$\alpha\times (1+0.0967\times\beta\times (T_0/T)^{0.5}+\beta^2\times T_0/(10.526\times T))$$

The density-dependence (M in cm<sup>-3</sup>) for reactions between neutral species is expressed as a combination of two or three kooij-type reactions for the high-density limit ( $k_{\infty}$  in cm<sup>3</sup>. $s^{-1}$ ), the low-density limit ( $k_0$  in cm<sup>6</sup>. $s^{-1}$ ), and the recombination ??? rate ( $k_R$  in cm<sup>3</sup>. $s^{-1}$ ). This is globally parameterized by 10 values ( $\alpha_{i=1,3}$ ,  $\beta_{i=1,3}$ ,  $\gamma_{i=1,3}$ ,  $F_c$ ):

3-body the Troe formula[1] 
$$k_{\infty} \times (R/(1+R)) \times F_c^{1/E}$$
 
$$R = k_0 \times M/k_{\infty}$$
 
$$E = 1 + \left( \left(\log_{10}(R) + C\right) / \left(N - 0.14 \times \left(\log_{10}(R) + C\right)\right) \right)^2$$

$$\begin{split} C &= -0.4 - 0.67 \times \log_{10} F_c \\ N &= 0.75 - 1.27 \times \log_{10} F_c \\ \text{with } F_c &= 0.64, \, k_0 = k(\alpha_1, \beta_1, \gamma_1, 300) \text{ and } k_\infty = k(\alpha_2, \beta_2, \gamma_2, 300) \end{split}$$

assocVV a modified Troe formula for pressure-dependent association reactions[13]  $k_r + F_c^{1/E} \times (k_\infty - k_r) \times k_0 \times M / ((k_\infty - k_r) + k_0 \times M)$  with E defined above,  $k_\infty = k(\alpha_1, \beta_1, \gamma_1, 1), k_0 = k(\alpha_2, \beta_2, \gamma_2, 1)$  and  $k_r = k(\alpha_3, \beta_3, \gamma_3, 1)$ . Note the different parameterization of the Kooij formula  $(T_0 = 1)$  and the inverse

assocMD another expression for pressure-dependent association reactions,[14, 15] using also a simplified broadening factor

$$k_{\infty} \times (k_0 \times M \times F_c^{1/E'} + k_r)/(k_0 \times M + k_{\infty})$$
 
$$E' = 1 + (\log_{10}(R)/N)^2$$
 with  $R$ ,  $N$  as above,  $k_0 = k(\alpha_1, \beta_1, \gamma_1, 300)$ ,  $k_{\infty} = k(\alpha_2, \beta_2, \gamma_2, 300)$  and  $k_r = k(\alpha_3, \beta_3, \gamma_3, 300)$ 

### 2.2 Ion reactions

For ion reactions, one describes separately the T-dependence of the global rate constant (kooij, dr or ionpol 1/2), and the set of branching ratios (BR) which are assumed to be T-independent.

The database is stored in a 'ionsDB.csv' file, in which one has one line per *global* reaction (meaning that each line might describe several partial reactions or channels) with 14 fields:

**REACTANTS** the reactants in 'A + B' form

The global reaction rate is defined by four main fields:

order for parameters of  $k_{\infty}$  and  $k_0$ .

TYPE the reaction type, either kooij, dr, ionpol1 or ionpol2. See Sect. 2.1 for definitions.

ALPHA, BETA, GAMMA the probability density functions of the (independent) rate parameters, i.e.  $p(\alpha, \beta, \gamma) = p(\alpha)p(\beta)p(\gamma)$ . For the available distributions, see Table2.1.

the next two fields encode the probabilistic tree describing the uncertain BRs

NBR the number of channels. It is mostly used to ensure that the STRINGBR distribution is properly formatted and interpreted.

STRINGBR is a string that encodes a probabilistic tree used to generate random samples of the BRs. To learn to build a probabilistic tree, see the article by Plessis *et al.* [16] and examples below. For the available distributions, see Table 2.2. Note that the syntax is slightly different from the mathematical notations of the article as it interleaves the identity of the products for each channel.

<sup>&</sup>lt;sup>1</sup>At the moment, there is practically no information on *T*-dependence of BRs, and no provision has been made in the database for this opportunity. The database contains thus only information to generate *T*-independent BRs.

pdfNames	Note
$\overline{\text{Delta}(x_0)}$	fixed value $x_0$ , no uncertainty
Unif $(x_{min}, x_{max})$	uniform distribution over an interval
$Logu(x_{min}, x_{max})$	log-uniform distribution over an interval
$\mathtt{Norm}(x_0,u_x)$	normal distribution, mean $x_0$ , stdev $u_x$
$Logn(x_0, f_x)$	log-normal distribution, mean $x_0$ ,
	uncertainty factor $f_x$
Nort( $x_0, u_x, x_{min}, x_{max}$ )	truncated normal distribution

Table 2.1: Available distributions for rate constant parameters used in the ALPHA, BETA, and GAMMA fields of the ionsDB database.

pdfNamesBR	Note
extstyle  ext	Dirichlet distribution with mean $b_1, \ldots, b_N$
	and precision $\Gamma$ . The uniform distribution is
	encoded as $Diri(1,, 1; 1)$ .
$\mathtt{Dirg}(b_1,\ldots,b_N;u_{b_1},\ldots,u_{b_N})$	Generalized Dirichlet distribution with
	mean $b_i$ and stdev $u_{b_i}$
${\tt Dior}(k_1,\ldots,k_N)$	Ordered uniform Dirichlet distribution
	respecting the order of $k_1, \ldots, k_N$ (integers).
$ exttt{Diut}(b_1^-,\ldots,b_N^-;b_1^+,\ldots,b_N^+)$	Intervals-constrained Dirichlet distribution,
	with each component $i$ within $[b_i^-, b_i^+]$ .
$\mathtt{Mlgn}(b_1,\ldots,b_N;f_{b_1},\ldots,f_{b_N})$	Uncorrelated multivariate lognormal
<u> </u>	distribution, with mean $b_i$ , uncert. factor $f_{b_i}$

Table 2.2: Available distributions for branching ratios used in the STRINGBR field of the ionsDB database.

the four following fields contain the bibliographic references for the previous data

REF\_ALPHA, REF\_BETA, REF\_GAMMA, REF\_BR should contain **semicolumn**-separated *bibtex* keys appearing in the Doc/refsDR.bib file.

finally, the two last fields are

COMMENTS any useful information on the reaction

TIMESTAMP the date and time of creation/modification of this reaction

### 2.2.1 STRINGBR examples

Products are encoded between brackets as terminal leaves of the tree.

ArH+ + C2H4 there are two channels with measured BRs (0.73  $\pm$  0.05 for C2H3+ + Ar + H2 and 0.27  $\pm$  0.05 for C2H5+ + Ar). This is encoded via a generalized Dirichlet distribution:

```
0.27 < C2H5+ + Ar >;
0.05,0.05)
which is compacted to
"Dirg(0.73 < C2H3+ + Ar + H2 >, 0.27 < C2H5+ + Ar >; 0.05,0.05)"
```

C2H2+ + E a more involved case with several levels of information. One has five primary channels with measured BRs, and a secondary splitting for CH2 between singlet and triplet with no preferred value (uniform Dirichlet)

```
Dirg(
             0.5 < C2H + H > ,
             0.3 < 1C2 + H + H >,
             0.02 < 1C2 + H2 >,
             0.05*Diri(
                 1 < 1 CH2 + C >,
                 1 < 3 CH2 + C > ;
             1),
             0.13 < CH + CH > ;
          0.06,0.05,0.03,0.01,0.01)
         compacted to
          "Dirg(0.5<C2H + H>,0.3<1C2 + H + H>,0.02<1C2 + H2>,0.05*Diri(1<1CH2 +
         C>,1<3CH2 + C>;1),0.13<CH + CH>;0.06,0.05,0.03,0.01,0.01)"
C2H3+ + N4S in this case, one has only limits for the BRs of two channels (e.g.
         >0.9 for the first one, or <0.1 for the second one). This is expressed
         by
          Diut(
             0.9 < CHCN + + H2 >,
             0.0 < CHCNH+ + H>;
          1.0,0.1)
         or in compact form
          "Diut(0.9<CHCN+ + H2>,0.0<CHCNH+ + H>;1.0,0.1)"
```

#### 2.3 Neutral reactions

The branching ratios formalism for ions has not been implemented for reactions between neutral species, as partial rates are often measured independently, and the database contains on line per channel. The actual format derives from M. Dobrijevic's implementation [15] for neutral association reactions, with a few extra fields:

R1, R2, R3 one reactant per field

P1, P2, P3, P4, P5 one product per field (P5 is not used)

TYPE reaction type (kooij, assocMD or assocVV)

- A1, B1, C1, F1, G1 parameters of a kooij rate k(A1, B1, C1) and corresponding uncertainty factors for the f/g model. See Sect. 2.1 for reaction-type-dependent definition  $(k_0 \text{ or } k_\infty)$ .
- A2, B2, C2, F2, G2 parameters of a kooij rate k(A2, B2, C2) and corresponding uncertainty factors for the f/g model. See Sect. 2.1 for reaction-type-dependent definition  $(k_{\infty}$  or  $k_0)$ .
- A3, B3, C3, F3, G3 parameters of a kooij rate k(A3, B3, C3) and corresponding uncertainty factors for the f/g model. Defines  $k_R$  in association reactions model (Sect. 2.1).

FC broadening factor  $F_c$ 

REFS comma-separated bitex keys of references

COMMENTS any useful information on the reaction

TIMESTAMP the date and time of creation/modification of this reaction

### 2.4 Photo-processes

The database is stored in a 'photoDB.csv' file, containing the following fields (one line per channel):

R1, R2 the reactants (R2 = HV)

P1, P2, P3, P4 the products

CHANNEL the index of the channel for the current reaction

XS\_SOURCE source for the cross-section (Leiden, SWRI or Hebrard)

XS\_F uncertainty factor for the cross-section. If not specified, one uses Leiden value for XS\_SOURCE = LEIDEN, otherwise one uses default value (1.2).

BR\_SOURCE source for the wavelength-dependent branching ratios (typically SWRI, or Plessis for CH4)

REFS semi-column-separated *bitex* keys of references. Considered only if on "CHANNEL = 1" line.

COMMENTS any useful information on the reaction. Considered only if on "CHANNEL = 1" line.

TIMESTAMP the date and time of creation/modification of this line

### 2.4.1 Uncertainty modeling

- The default value of XS\_F depends on the data source: the Leiden database contains generally an estimate of XS\_F; but for the SWRI or Hebrard cross-sections, a default value of 1.2 is used. These default values can be superseded by specifying a different XS\_F value in the photoDB.csv file.
- As an example, let us consider the photolysis of  $N_2$ , with three products channels: N4S + N2D  $(b_1)$ , N2+ + E  $(b_2)$ , and N4S + N3P+ + E  $(b_3)$ . The branching ratios are sampled for each wavelength from the following distribution

```
Dirg(
    b1<N4S + N2D>,
    (b2+b3)*Dirg(
        b2/(b2+b3)<N2+ + E>,
        b3/(b2+b3)<N4S + N3P+ + E>;
    b2*r_I, b3*r_I);
b1*r_NI, (b2+b3)*r_NI)
```

# Bibliography

- [1] V. Wakelam, E. Herbst, J.-C. Loison, I. W. M. Smith, V. Chandrasekaran, B. Pavone, N. G. Adams, M.-C. Bacchus-Montabonel, A. Bergeat, K. Béroff, V. M. Bierbaum, M. Chabot, A. Dalgarno, E. F. van Dishoeck, A. Faure, W. D. Geppert, D. Gerlich, D. Galli, E. Hébrard, F. Hersant, K. M. Hickson, P. Honvault, S. J. Klippenstein, S. L. Picard, G. Nyman, P. Pernot, S. Schlemmer, F. Selsis, I. R. Sims, D. Talbi, J. Tennyson, J. Troe, R. Wester, and L. Wiesenfeld. A kinetic database for astrochemistry (KIDA). The Astrophysical Journal Supplement Series, 199:21, 2012.
- [2] W. B. DeMore, S. P. Sander, D. M. Golden, R. F. Hampson, M. J. Kurylo, C. J. Howard, A. R. Ravishankara, C. E. Kolb, and M. J. Molina. Chemical kinetics and photochemical data for use in stratospheric modeling. Evaluation number 11. *JPL Publication*, 94-26:1– 273, 1994.
- [3] S. P. Sander, A. R. Ravishankara, D. M. Golden, C. E. Kolb, M. J. Kurylo, M. J. Molina, G. K. Moortgat, B. J. Finlayson-Pitts, W. P. H., and R. E. Huie. Chemical kinetics and photochemical data for use in atmospheric studies. Evaluation number 15. *JPL Publication*, 06-2:1-522, 2006.
- [4] E. Hébrard, M. Dobrijevic, Y. Bénilan, and F. Raulin. Photochemical kinetics uncertainties in modeling Titan's atmosphere: A review. *Journal of Photochemistry and Photobiology A: Chemistry*, 7:211–230, 2006.
- [5] S. Plessis, N. Carrasco, and P. Pernot. Knowledge-based probabilistic representations of branching ratios in chemical networks: the case of dissociative recombinations. *J. Chem. Phys.*, 133:134110, 2010.
- [6] N. Carrasco and P. Pernot. Modeling of branching ratio uncertainty in chemical networks by Dirichlet distributions. *Journal of Physical Chemistry A*, 11(18):3507–3512, 2007.
- [7] N. Carrasco, S. Plessis, and P. Pernot. Towards a reduction of the bimolecular reaction model for Titan ionosphere. *International Journal of Chemical Kinetics*, 40(11):699-709, 2008. URL: http://dx.doi.org/10.1002/kin.20374.
- [8] B. Gans, Z. Peng, N. Carrasco, D. Gauyacq, S. Lebonnois, and P. Pernot. Impact of a new wavelength-dependent representation of methane photolysis branching ratios on the modeling of Titan's atmospheric photochemistry. *Icarus*, 223:330 343, 2013.

- [9] Z. Peng, N. Carrasco, and P. Pernot. Modeling of synchrotron-based laboratory simulations of Titan's ionospheric photochemistry. *GeoResJ*, 1-2:33-53, 2014.
- [10] N. Carrasco, O. Dutuit, R. Thissen, M. Banaszkiewicz, and P. Pernot. Uncertainty analysis of bimolecular reactions in Titan ionosphere chemistry model. *Planetary and Space Science*, 55:141–157, 2007.
- [11] E. Hébrard. Incertitudes photochimiques dans les modèles de l'atmosphère de Titan : revue et conséquences. PhD thesis, Université Paris VII Denis Diderot, 2006.
- [12] E. Hébrard, M. Dobrijevic, P. Pernot, N. Carrasco, A. Bergeat, K. M. Hickson, A. Canosa, S. D. Le Picard, and I. R. Sims. How measurements of rate coefficients at low temperature increase the predictivity of photochemical models of Titan's atmosphere. The Journal of Physical Chemistry A, 113:11227–11237, 2009.
- [13] V. Vuitton, R. Yelle, S. Klippenstein, S. Hörst, and P. Lavvas. Simulating the density of organic species in the atmosphere of titan with a coupled ion-neutral photochemical model. *Icarus*, 324:120 197, 2019.
- [14] V. Vuitton, R. V. Yelle, P. Lavvas, and S. J. Klippenstein. Rapid association reactions at low pressure: Impact on the formation of hydrocarbons on Titan. *Astrophys. J.*, 744:11, 2012.
- [15] M. Dobrijevic, J. Loison, K. Hickson, and G. Gronoff. 1D-coupled photochemical model of neutrals, cations and anions in the atmosphere of Titan. *Icarus*, 268:313–339, 2016.
- [16] S. Plessis, N. Carrasco, and P. Pernot. Knowledge-based probabilistic representations of branching ratios in chemical networks: the case of dissociative recombination. *Journal of Chem. Phys.*, 133(13):134110–134131, 2010.