

Multiple Features (variables) - multiple linear regression

	Size	Number of Bedrooms	Number of floors	Age of home in years	Price (\$) in \$1000
	x_1	x_2	x_3	x_4	
$i=1$	2000	5	1	45	460
$i=2$	1000	3	2	20	500
$i=3$	800	2	2	30	350
$i=4$	600	1	1	10	700
$i=n$

$$j = 1 \dots 4$$

$$n = 4$$

$$x_j = j^{\text{th}} \text{ feature}$$

vector

n = number of features

$$\vec{x}^{(2)} = [1000, 3, \underline{2}, 20]$$

$\vec{x}^{(i)}$ = features of i^{th} training example

$$\vec{x}_3^{(2)} = \underline{2}$$

$x_j^{(i)}$ = value of feature j in i^{th} training example

Model

$$\text{Previously: } f_{w,b}(x) = wx + b$$

$$f_{w,b}(x) = w_1 x_1 + w_2 x_2 + w_3 x_3 + b$$

Example

$$f_{w,b}(x) = 0.1 \underset{\substack{\uparrow \\ \text{Size}}}{x_1} + 4 \underset{\substack{\uparrow \\ \text{\# Bedrooms}}}{x_2} + 10 \underset{\substack{\uparrow \\ \text{\# Floors}}}{x_3} + -2 \underset{\substack{\uparrow \\ \text{years}}}{x_4} + 100 \underset{\substack{\uparrow \\ \text{base price}}}{b}$$

The definition of the model with n features

$$f_{w,b}(x) = w_1 x_1 + w_2 x_2 + \dots + w_n x_n + b$$

$$\vec{w} = [w_1 \ w_2 \ w_3 \ \dots \ w_n]$$

b is a number

parameters of the model

$$\vec{x} = [x_1 \ x_2 \ x_3 \ \dots \ x_n]$$

Then

$$f_{\vec{w},b}(\vec{x}) = \vec{w} \cdot \vec{x} + b$$

↑
Dot product

Vectorization

in python:

$$f = \text{np.dot}(w, x) + b$$

Gradient descent for multiple linear regression

One feature

$$w = w - \alpha \frac{1}{m} \sum_{i=1}^m \underbrace{(f_{w,b}(x^{(i)}) - y^{(i)}) x^{(i)}}_{\frac{\partial}{\partial w} J(w,b)}$$

$$b = b - \alpha \frac{1}{m} \sum_{i=1}^m (f_{w,b}(x^{(i)}) - y^{(i)})$$

Simultaneously update w, b

n features ($n > 2$)

$j=1$

$$w_1 = w_1 - \alpha \frac{1}{m} \sum_{i=1}^m \underbrace{(f_{\vec{w},b}(\vec{x}^{(i)}) - y^{(i)}) x_1^{(i)}}_{\frac{\partial}{\partial w_1} J(\vec{w},b)}$$

$j=n$

$$w_n = w_n - \alpha \frac{1}{m} \sum_{i=1}^m (f_{\vec{w},b}(\vec{x}^{(i)}) - y^{(i)}) x_n^{(i)}$$
$$b = b - \alpha \frac{1}{m} \sum_{i=1}^m (f_{\vec{w},b}(\vec{x}^{(i)}) - y^{(i)})$$

Simultaneously update w_j (for $j = 1 \dots n$) and b