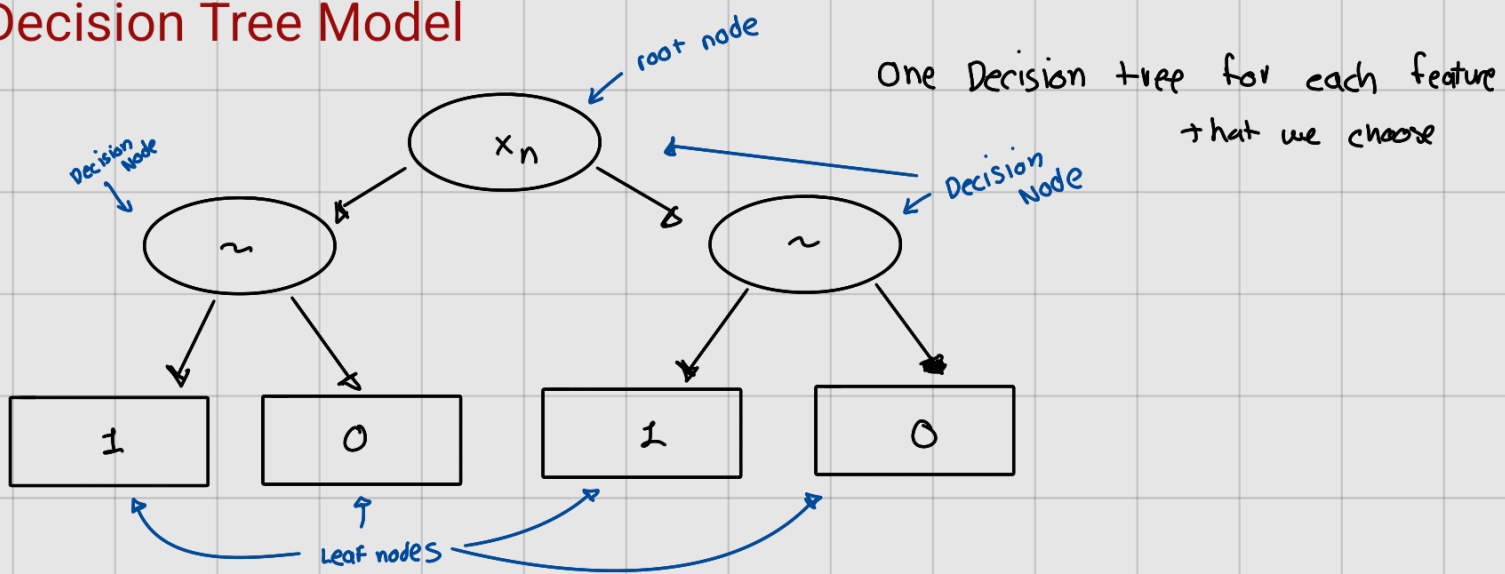


Decision Tree Model



Decision tree learning

① How to choose what feature to split on at each node?

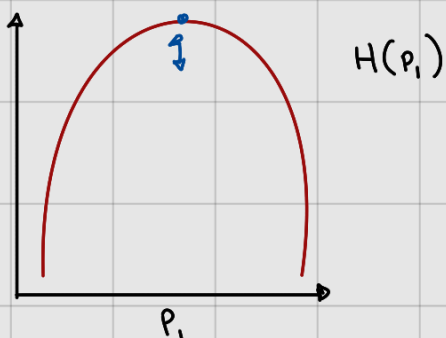
- Maximize purity (or minimize impurity)

② When do you stop splitting?

- When a node is 100% one class
- When splitting a node will result in the tree exceeding a maximum depth
- When improvements in purity score are below a threshold
- When number of examples in a node is below a threshold

Entropy as a measure of impurity

p_1 = fractions of examples that are cats



$$p_0 = 1 - p_1$$

$$\begin{aligned} H(p_1) &= -p_1 \log_2(p_1) - p_0 \log_2(p_0) \\ &= -p_1 \log_2(p_1) - (1-p_1) \log_2(1-p_1) \end{aligned}$$

Note : " $0 \log(0)$ " = 0

Choosing a split

$$p_1 = 5/10 = 0.5$$

$$H(0.5) = 1$$

Ear Shape

Pointy

Floppy



$$p_1 = 4/5 = 0.8$$

$$p_1 = 1/5 = 0.2$$

$$H(0.8) = 0.72$$

$$H(0.2) = 0.72$$

$$H(0.5) = \left(\frac{5}{10} H(0.8) + \frac{5}{10} H(0.2) \right)$$

$$= 0.28$$

Information Gain

Ear Shape

$$p_1^{\text{root}} = 5/10 = 0.5$$

Pointy

Floppy



$$p_1^{\text{left}} = 4/5$$

$$p_1^{\text{right}} = 1/5$$

$$w^{\text{left}} = 5/10$$

$$w^{\text{right}} = 5/10$$

Information gain formula

$$H(p_1^{\text{root}}) - (w^{\text{left}} H(p_1^{\text{left}}) + w^{\text{right}} H(p_1^{\text{right}}))$$

Random Forest Algorithm

Given training set of size m

For $b = 1$ to B :

Use sampling with replacement to create a new training set of size m

Train a decision tree on the new dataset

Randomizing the feature choice

At each node, when choosing a feature to use to split, if n features are available, pick a random subset of $k < n$ features and allow the algorithm to only choose from that subset of features

$$k = \sqrt{n}$$

XGBoost

Given training set of size m

For $b = 1$ to B :

Use sampling with replacement to create a new training set of size m

But instead of picking from all examples with equal $(1/m)$ probability, make it more likely to pick misclassified examples from previously trained trees.

Train a decision tree on the new dataset

XGBoost (eXtreme Gradient Boosting)

- Open source implementation of boosted trees
- Fast efficient implementation
- Good choice of default splitting criteria for when to stop splitting
- Built in regularization to prevent overfitting
- Highly competitive algorithm for ML competitions

XGBoost implementation

Classification

```
from xgboost import XGBClassifier
```

```
model = XGBClassifier()
```

```
model.fit(x_train, y_train)
```

```
y_pred = model.predict(x_test)
```

Regression

```
from xgboost import XGBRegressor
```

```
model = XGBRegressor()
```

```
model.fit(x_train, y_train)
```

```
y_pred = model.predict(x_test)
```