

gaussian_diffusion.py

1. $\text{q_sample}(\mathbf{x}_0, t, \boldsymbol{\epsilon} \sim \mathcal{N}(\mathbf{0}, \mathbf{I}))$: $//q(\mathbf{x}_t|\mathbf{x}_0)$

$$\text{return } \mathbf{x}_t = \underbrace{\sqrt{\bar{\alpha}_t}}_{\text{sqrt_alphas_cumprod}} \cdot \mathbf{x}_0 + \underbrace{\sqrt{1 - \bar{\alpha}_t}}_{\text{sqrt_one_minus_alphas_cumprod}} \cdot \boldsymbol{\epsilon}$$

2. $\text{_predict_xstart_from_eps}(\mathbf{x}_t, t, \boldsymbol{\epsilon}_\theta)$:

$$\text{return } \mathbf{x}_0 = \frac{\mathbf{x}_t - \sqrt{1 - \bar{\alpha}_t} \cdot \boldsymbol{\epsilon}_\theta}{\sqrt{\bar{\alpha}_t}} = \underbrace{\sqrt{1/\bar{\alpha}_t}}_{\text{sqrt_recip_alphas_cumprod}} \cdot \mathbf{x}_t - \underbrace{\sqrt{1/\bar{\alpha}_t - 1}}_{\text{sqrt_recipm1_alpha_cumprod}} \cdot \boldsymbol{\epsilon}_\theta$$

3. $\text{_predict_eps_from_xstart}(\mathbf{x}_t, t, \mathbf{x}_0)$:

$$\text{return } \hat{\boldsymbol{\epsilon}}_t = \left(\underbrace{\sqrt{1/\bar{\alpha}_t}}_{\text{sqrt_recip_alphas_cumprod}} \cdot \mathbf{x}_t - \mathbf{x}_0 \right) / \underbrace{\sqrt{1/\bar{\alpha}_t - 1}}_{\text{sqrt_recipm1_alpha_cumprod}}$$

4. $\text{q_posterior_mean_variance}(\mathbf{x}_0, \mathbf{x}_t, t)$: $//q(\mathbf{x}_{t-1}|\mathbf{x}_t, \mathbf{x}_0)$

$$\text{return } \mathbf{x}_{t-1} = \underbrace{\frac{\sqrt{\bar{\alpha}_{t-1}}\beta_t}{1 - \bar{\alpha}_t}}_{\text{posterior_mean_coef1}} \mathbf{x}_0 + \underbrace{\frac{\sqrt{\bar{\alpha}_t}(1 - \bar{\alpha}_{t-1})}{1 - \bar{\alpha}_t}}_{\text{posterior_mean_coef2}} \mathbf{x}_t$$

5. $\text{p_mean_variance}(\boldsymbol{\epsilon}_\theta, \mathbf{x}_t, t)$:

$$\text{return } \begin{cases} \boldsymbol{\epsilon}_t, \mathbf{v} = \boldsymbol{\epsilon}_\theta(\mathbf{x}_t, t) \\ \Sigma_\theta(\mathbf{x}_t, t) = \exp(\mathbf{v} \log \beta_t + (1 - \mathbf{v}) \log \tilde{\beta}_t) & //\text{model_variance} \\ \mathbf{x}_0 = \text{_predict_xstart_from_eps}(\mathbf{x}_t, t, \boldsymbol{\epsilon}_t) & //(\mathbf{x}_t - \sqrt{1 - \bar{\alpha}_t} \cdot \boldsymbol{\epsilon}_\theta) / \sqrt{\bar{\alpha}_t} \\ \mathbf{x}_0 = \text{process_xstart}(\mathbf{x}_0) & //\text{pred_xstart:clamp}(\mathbf{x}_0, -1, 1) \\ \mathbf{x}_{t-1} = \text{q_posterior_mean_variance}(\mathbf{x}_0, \mathbf{x}_t, t) & //\text{model_mean: } q(\mathbf{x}_{t-1}|\mathbf{x}_t, \mathbf{x}_0) \end{cases}$$

6. $\text{condition_score}(s_\phi, \mathbf{x}_{t-1}, \mathbf{x}_0, \mathbf{x}_t, t)$: $//s_\phi = \nabla_{\mathbf{x}_t} \log p_\phi(\mathbf{y}|\mathbf{x}_t)$: condition function

$$\text{return } \begin{cases} \hat{\boldsymbol{\epsilon}}_t = \boldsymbol{\epsilon}_\theta(\mathbf{x}_t) - \sqrt{1 - \bar{\alpha}_t} \cdot s_\phi & //s_\phi = \nabla_{\mathbf{x}_t} \log p_\phi(\mathbf{y}|\mathbf{x}_t) \\ \mathbf{x}_0 = \text{_predict_xstart_from_eps}(\mathbf{x}_t, t, \hat{\boldsymbol{\epsilon}}_t) & //\text{pred_xstart: } (\mathbf{x}_t - \sqrt{1 - \bar{\alpha}_t} \cdot \boldsymbol{\epsilon}_\theta) / \sqrt{\bar{\alpha}_t} \\ \mathbf{x}_{t-1} = \text{q_posterior_mean_variance}(\mathbf{x}_0, \mathbf{x}_t, t) & //\text{model_mean: } q(\mathbf{x}_{t-1}|\mathbf{x}_t, \mathbf{x}_0) \end{cases}$$

7. $\text{condition_mean}(s, \mathbf{x}_{t-1}, \sigma_t, \mathbf{x}_t, t)$: $//$

$$\text{return } \mathbf{x}_{t-1} + \sigma_t \cdot s(\mathbf{x}_t, t)$$

7. $\text{ddim_sample}(\boldsymbol{\epsilon}_\theta, \mathbf{x}_t, t)$: $//\text{sample } \mathbf{x}_{t-1}$

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 $\mathbf{x}_0, \mathbf{x}_{t-1}, \Sigma_{\theta} = \text{p\_mean\_variance}(\epsilon_{\theta}, \mathbf{x}_t, t)$  //mean: $\mathbf{x}_{t-1}$ , pred_xstart:  $\mathbf{x}_0$ , variance:  $\Sigma_{\theta}$ 
 $\mathbf{x}_0, \mathbf{x}_{t-1} = \text{condition\_score}(s_{\phi}, \mathbf{x}_{t-1}, \mathbf{x}_0, \mathbf{x}_t, t)$  //
 $\hat{\epsilon}_t = \text{predict\_eps\_from\_xstart}(\mathbf{x}_t, t)$ 
 $\sigma = \eta \cdot \sqrt{(1 - \bar{\alpha}_{t-1}) / (1 - \bar{\alpha}_t)} \cdot \sqrt{1 - \bar{\alpha}_t / \bar{\alpha}_{t-1}}$ 
 $\mathbf{x}_{t-1} = \sqrt{\bar{\alpha}_{t-1}} \cdot \mathbf{x}_0 + \sqrt{1 - \bar{\alpha}_{t-1} - \sigma^2} \cdot \hat{\epsilon}_t + \sigma \cdot \epsilon$ 

 $\sigma = \eta \cdot \sqrt{(1 - \bar{\alpha}_{t-1}) / (1 - \bar{\alpha}_t)} \cdot \sqrt{1 - \bar{\alpha}_t / \bar{\alpha}_{t-1}}$ 
8. p_sample ( $\epsilon_{\theta}, \mathbf{x}_t, t$ ): //sample  $\mathbf{x}_{t-1}$ 

 $\mathbf{x}_0, \mathbf{x}_{t-1}, \Sigma_{\theta} = \text{p\_mean\_variance}(\epsilon_{\theta}, \mathbf{x}_t, t)$  //mean: $\mathbf{x}_{t-1}$ , pred_xstart:  $\mathbf{x}_0$ , variance:  $\Sigma_{\theta}$ 
 $\hat{\mathbf{x}}_{t-1} = \text{condition\_mean}(s, \mathbf{x}_{t-1}, \sigma_t, \mathbf{x}_t, t)$  //
return  $\mathbf{x}_{t-1} = \hat{\mathbf{x}}_{t-1} + \exp(0.5 \cdot \log \sigma_t) \cdot \epsilon$ 

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