

Today's Content

→ Binary Tree

→ Traversal

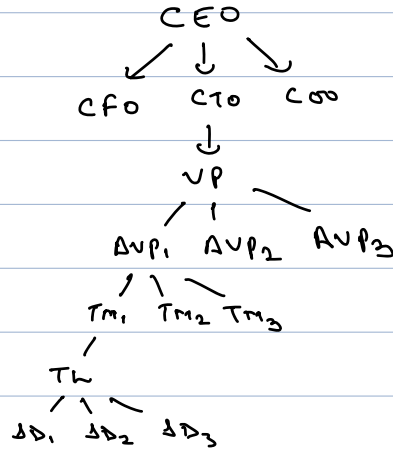
→ Iterative traversals

→ Construct B.T from Preorder to Inorder

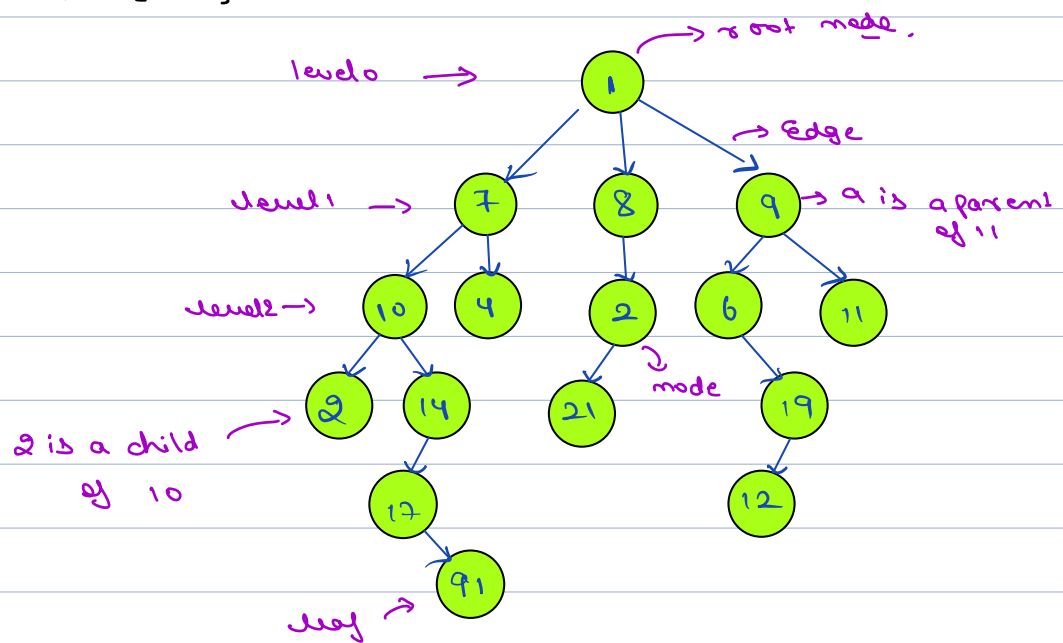
Trees Basics & terminologies

1) Linear data structures → arrays, stacks, LL.

1) Hierarchical :-



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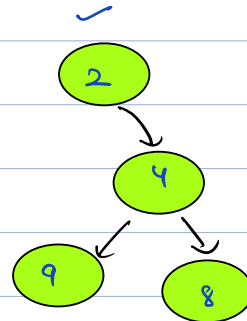
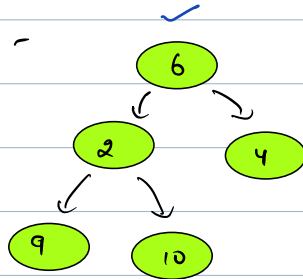


root → It is a node with no parent.

leaf → It is a node with no children.

Binary Tree :- for every node, no. of children ≤ 2 .

Ex 1 :-



class Node {

int data;

Node left;

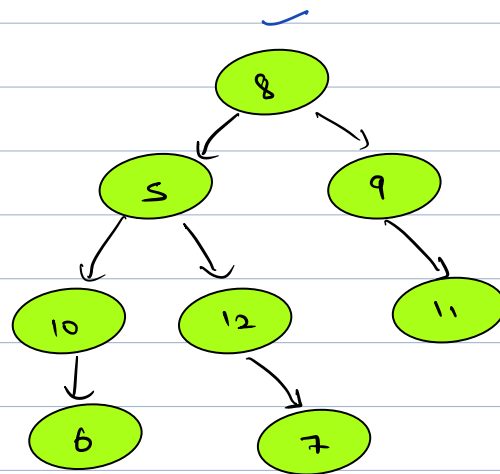
Node right;

Node(x) {

data = x;

left = null;

right = null;

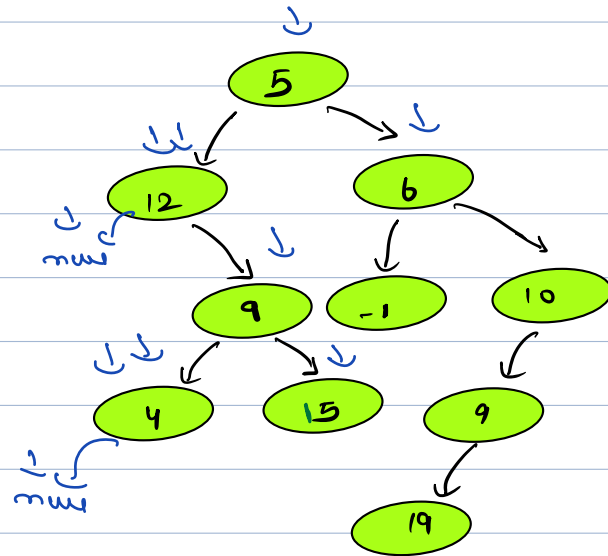


Tree Traversals :-

- Inorder ✓
- Preorder ✓
- Postorder ✓

1) Inorder (L > R)

12 4 9 15 5
-1 6 19 9 10



T.C → O(N)

S.C → O(H)

```
void inorder (Node root) {
```

```
    if (root == null) { return; }
```

```
    inorder (root->left);
```

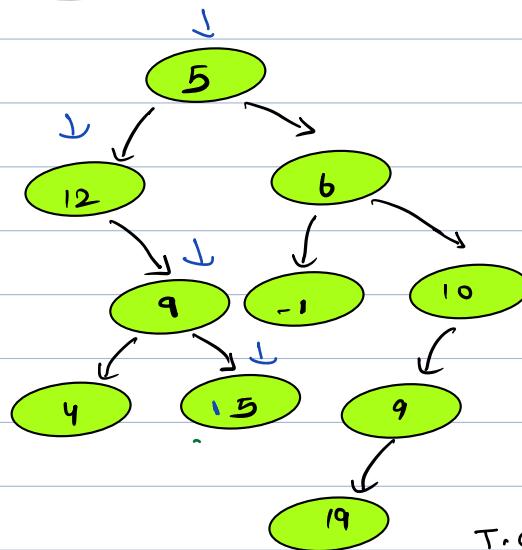
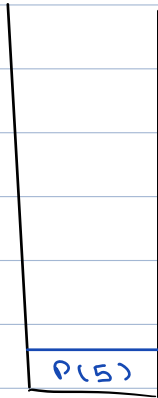
```
    Print (root->data);
```

```
    inorder (root->right);
```

```
}
```

2) PreOrder

D L R



5 12 9 4 15 6 -1 10 9 19

T.C $\rightarrow O(n)$
S.C $\rightarrow O(H)$

```

void preorder (Node root) {
    if (root == null) return;

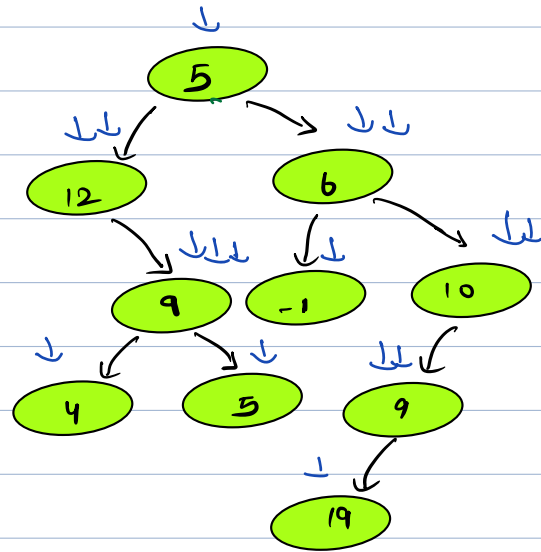
    print (root.data);
    preorder (root.left);
    preorder (root.right);
}
  
```

Note:- (Each node is touched 3 times).

3) Post Order :-

L R D

4 5 9 12 -1 19 9
10 6 5



void postorder (Node root) {

if (root == null) { return; }

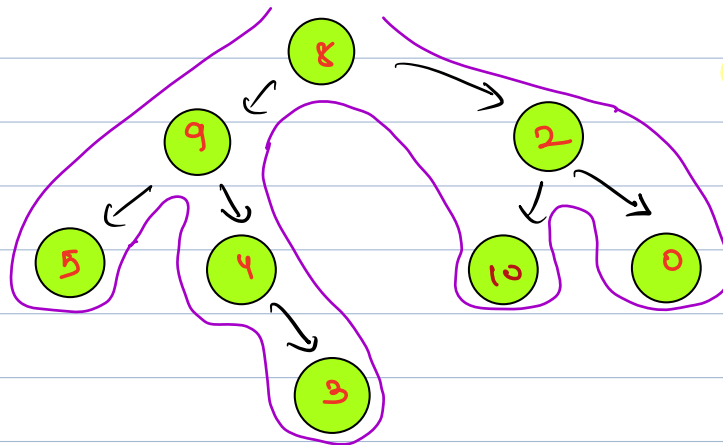
postorder (root->left);

postorder (root->right);

print (root->data);

}

T.C → O(n)
S.C → O(n)



Euler Path

(LDR) Inorder: 5 9 4 3 8 10 2 0

(DLR) Preorder: 8 9 5 4 3 2 10 0

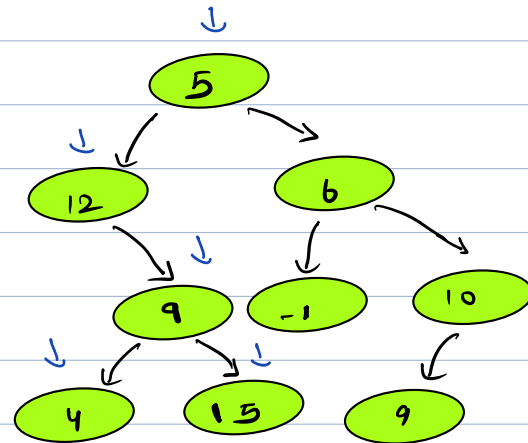
(LRD) Postorder: 5 3 4 9 10 0 2 8

Break 8:20 Am - 8:30 Am

InOrder Iterative :- (LDR).

Steps involved

- 1) call left child
- 2) print data
- 3) call right child



node task



12 4 9 15 5

class Pair {

Node node

int task;

Pair (Node t) {

node = t

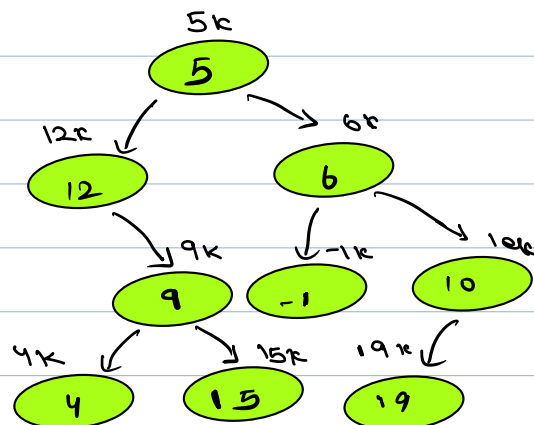
task = 1

}

T.C → O(n)

S.C → O(1)

mode = 9k task = 1
mode = 12k task = 1 2 3 4
mode = 5k task = 2



public void inorder (Node ^{5k}root) {

Stack <Pair> st;

Pair p = new Pair (root);

st.push(p);

while (st.size() > 0) {

Pair top = st.Peek();

if (top.task == 1) {

top.task++;

if (top.node.left != null) {

Pair temp = new Pair (top.node.left);

st.push(temp);

elseif (top.task == 2) {

top.task++;

print (top.node.data);

else if (top.task == 3) {

top.task++;

if (top.node.right != null) {

pair temp = new pair(
top node . right)
st . push (temp);

else {

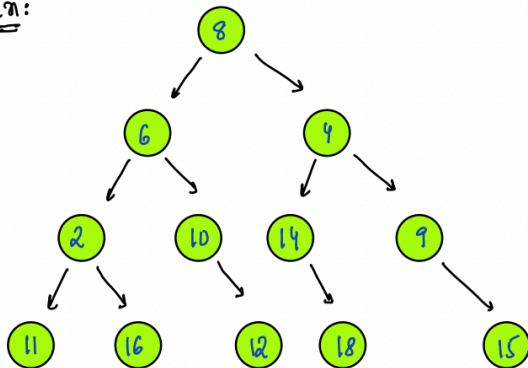
st . pop ();

}

}

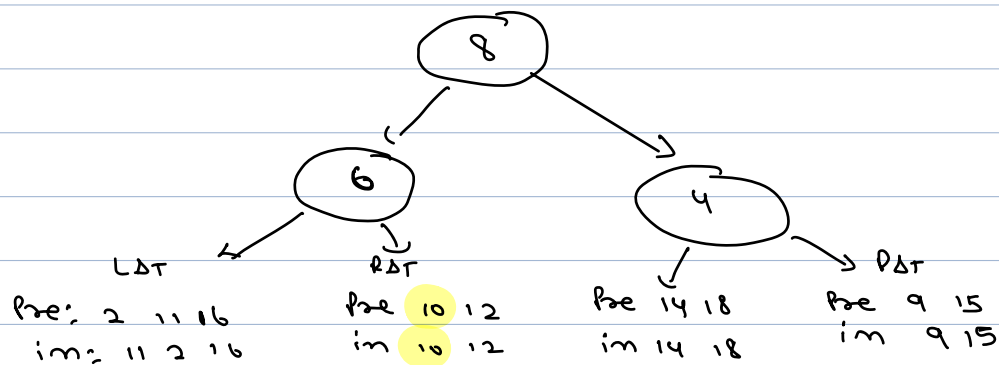
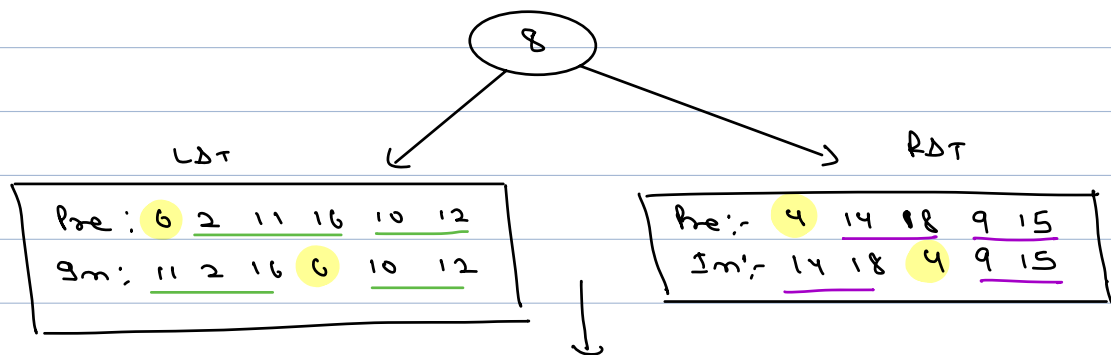
Ques) Given Preorder & inorder of a B.T.
with distinct values.
create it.

Ex:



(DLR) Preorder :- 8 6 2 11 16 10 12 4 14 18 9 15
(LDR) InOrder :- 11 2 16 6 10 12 8 14 18 4 9 15

Annotations: PE (Preorder End) at 8 and 15. GE (Inorder End) at 15. LST (Left Subtree) and RST (Right Subtree) markers are shown below the InOrder sequence.



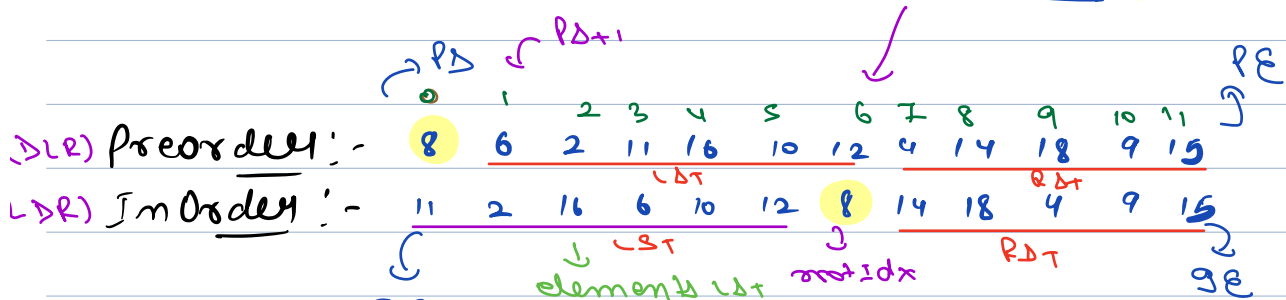
$$\text{elements LST} = (93, \text{rootIdx} - 1);$$

$$\Rightarrow \text{rootIdx} - 1 - 93 + 1 \Rightarrow \text{rootIdx} - 93$$

$$(p_{s+1}, e) = \text{elements LST}$$

$$\Rightarrow e - p_{s+1} + 1 = \text{elements LST}$$

$$\Rightarrow e = \text{elements LST} + p_s$$



Pseudo Code :- // pre [], in []

Node create (int ps, int pe, int is, int ie) {
 if (ps > pe || is > ie) return null;

```
int rootData = pre[ps];
Node root = new Node (rootData);
int rootIdx = find(is, ie, rootData); // (HashMap)
int elementsLST = rootIdx - 93
```

$$\text{elements LST} + p_s$$

root.left = create (ps+1, , 93, rootIdx-1);

root.right = create (, pe, rootIdx+1, ie);

$$\text{elements LST} + p_s + 1$$

return root;

|
2

T.C $\rightarrow O(n)$

S.C $\rightarrow O(1)$

5 \rightarrow 1 2 3 4 5

B = 2

map

a \rightarrow 1
b \rightarrow 12 d \rightarrow 1
c \rightarrow 1

a b d c

a b a d b c

a a b b d

a a b b d d

a b a d b c

a a b b d d

map

a → x 2
b → x 2 e → 1
d → 1

~~a~~ ~~b~~ d c

map

a b c a b c
↓ ↓ ↓ ↓ ↓ ↓
a a a b c #

a → x 2
b → x 2
c → x 2

~~a~~ ~~b~~ ~~c~~

a b b a d b c
↓ ↓ ↓ ↓
a a a #

a → x 2
b → x 2

~~a~~ ~~b~~

