

Q → Given a char array of lower case characters.  
 count the # pairs  $(i, j)$  s.t.  $i < j$ , (a-z)  
 $A[i] = 'a'$  &  $A[j] = 'g'$ .

0 1 2 3 4 5  
 $A = [a \ b \ e \ g \ a \ g]$

$i < j$

0 3

0 5

Ans = 3

0 1 2 3 4 5 6  
 $A = [a \ c \ g \ d \ g \ a \ g]$

4 5

0 2

0 4

0 6

Ans = 4

0 1 2 3 4 5 6 7  
 $A = [b \ c \ a \ g \ g \ a \ a \ g]$

5 6

2 3

2 4

2 7

Ans = 5

5 7

6 7

Brute force →

cnt = 0

for  $i \rightarrow 0$  to  $(N-2)$  {

if  $(A[i] == 'a')$

for  $j \rightarrow (i+1)$  to  $(N-1)$  {

if  $(A[j] == 'g')$

cnt ++

}

}

} return cnt

TC =  $O(N^2)$

SC =  $O(1)$

→ count # 'g' from  
 $(i+1)$  to  $(N-1)$

└── end  
 $(i+1)$

$$A = [a \ c \ g \ d \ g \ a \ g]$$

$$\text{cnt \# 'g'} \rightarrow 3 \ 3 \ 3 \ 2 \ 2 \ 1 \ 1$$

$$\begin{array}{c} \text{---} \rightarrow \text{end} \\ \text{(i+1)} \end{array}$$

Prefix Sum done  $L \leftarrow R$   
 is Suffix Sum.

```

if (A[N-1] == 'g') cntg[N-1] = 1
else cntg[N-1] = 0
for i → (N-2) to 0 {
    if (A[i] == 'g')
        cntg[i] = 1 + cntg[i+1]
    else
        cntg[i] = cntg[i+1]
}
  
```

calculate

$TC = O(N)$

$SC = O(N)$

$$A = [g \ b \ e \ g \ a]$$

$$\text{cntg} = [2 \ 1 \ 1 \ 1 \ 0]$$

$\text{cntg}[i] \rightarrow \# 'g' \text{ from index } i \text{ to } (N-1).$

```

ans = 0
for i → 0 to (N-2) {
    if (A[i] == 'a')
        ans += cntg[i+1]
}
return ans
  
```

$TC = O(N)$

use

Total  $TC = O(N + N) = O(N)$  ✓

$SC = O(N)$

can it reduce?

calculate & use together

$ans = 0$

```

if (A[N-1] == 'g') cnt = 1
else cnt = 0
for i → (N-2) to 0 {
    → if (A[i] == 'g')
        cnt = 1 + cnt
    → if (A[i] == 'a')
        ans += cnt
} return ans

```

$i$   
 0 1 2 3 4 5 6  
 $A = [a, c, g, d, g, a, g]$   
 $cnt = 1, 2, 3$   
 $ans = 0 + 1 + 3 = \underline{4}$

calculate

&

use

carry forward

$TC = \underline{O(N)}$      $SC = \underline{O(1)}$

H.W → Try the same task by calculating # 'a' from index 0 to (i-1).

0 ← (i-1)

2a g <sup>2 pairs</sup>

$ans = \sum \text{count of 'a' on left of index } i$   
 $\forall i, A[i] = 'g'$

subarray → continuous part of array.

$A = [2, \boxed{4}, 1, 6, -3, \boxed{7, 8, 4}]$

single element ✓

complete array ✓

start ————— end

OR

start & length

$A = [1, 2, \boxed{3}]$   
 0 1 2

# subarray that start at  $i=2 \rightarrow \underline{1}$

$A = [4, 2, 10, 3, 12, -2, 15]$   
 0 1 2 3 4 5 6

# subarray starting

from index 0 = 7

A = [ 4<sup>0</sup> 2<sup>1</sup> 10<sup>2</sup> 3<sup>3</sup> 12<sup>4</sup> -2<sup>5</sup> 15<sup>6</sup> ]

# subarray start  
from index 1 = 6

Total # subarrays  
of array size N →

A = [ 4<sup>0</sup> 2<sup>1</sup> 10<sup>2</sup> 3<sup>3</sup> 12<sup>4</sup> -2<sup>5</sup> 15<sup>6</sup> ]

start	# subarray
0	7
1	6
2	5
3	4
4	3
5	2
6	1

$$N + (N-1) + (N-2) + \dots + 1 = \frac{N * (N+1)}{2}$$

$\textcircled{7} + 6 + 5 + \dots + 1$   
N ←

Q → Print all subarrays of the array.

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A = [ 1<sup>0</sup> 2<sup>1</sup> 3<sup>2</sup> ]

1  
1 2  
1 2 3  
2  
2 3  
3



min ————— max

∀ max element, find closest min element on left.

$A = [2 \ 2 \ 6 \ 4 \ 5 \ 1 \ 5 \ 2 \ 6 \ 4 \ 1]$   $[L \ R] \rightarrow R-L+1$

0 1 2 3 4 5 6 7 8 9 10  
i

min = 1      idx\_min = ~~1~~ 5 10      length  $\rightarrow [5 \ 8]$   
max = 6      ans = 4      =  $8 - 5 + 1 = \underline{4}$

max ————— min

$A = [2 \ 2 \ 6 \ 4 \ 5 \ 1 \ 5 \ 2 \ 6 \ 4 \ 1]$

0 1 2 3 4 5 6 7 8 9 10  
i

min = 1      idx\_max = ~~2~~ 8       $[2 \ 5] \rightarrow 5 - 2 + 1 = \underline{4}$   
max = 6      ans = ~~4~~ 3       $[8 \ 10] \rightarrow 10 - 8 + 1 = \underline{3}$

// calculate minA & maxA

idx\_max = -1

idx\_min = -1      ans = N // worst case answer

for  $i \rightarrow 0$  to  $(N-1)$  {

if  $(A[i] == \text{minA})$  {

if  $(\text{idx\_max} \neq -1)$

max  
|—— i

ans = min(ans,  $i - \text{idx\_max} + 1$ )

idx\_min = i

} else if  $(A[i] == \text{maxA})$  {

if  $(\text{idx\_min} \neq -1)$

min  
|—— i

ans = min(ans,  $i - \text{idx\_min} + 1$ )

idx\_max = i

}

}

$$TC = \underline{O(N)}$$

$$SC = \underline{O(1)}$$

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