

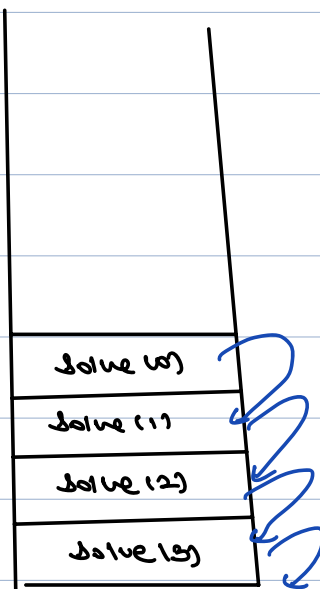
Quiz 1 :-

(N=3)

```
void solve(int N){  
    if(N == 0)  
        return;  
    solve(N-1);  
    print(N);  
}
```

→ Postorder

1 2 3



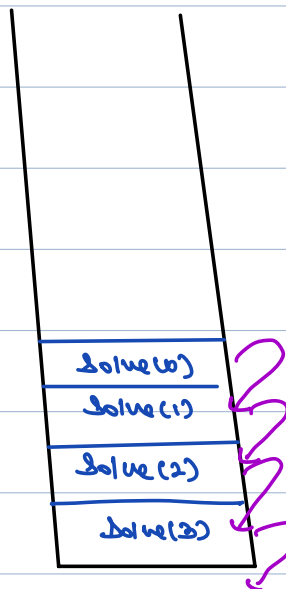
Quiz 2 :-

solve(3)

```
void solve(int N){  
    if(N == 0)  
        return;  
    print(N);  
    solve(N-1);  
}
```

→ Pre order

3 2 1

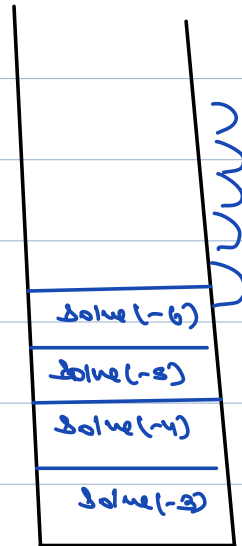


Ques 9

N = -5

```
void solve(int N){  
1   if(N == 0) ~  
2       return;  
3   print(N);  
4   solve(N-1);  
}
```

-3 -4 -5



TLE → Time limit Exceeded.

Stack Overflow Error ✓

← Tower of Hanoi →

There are n disks placed on tower A of different sizes.

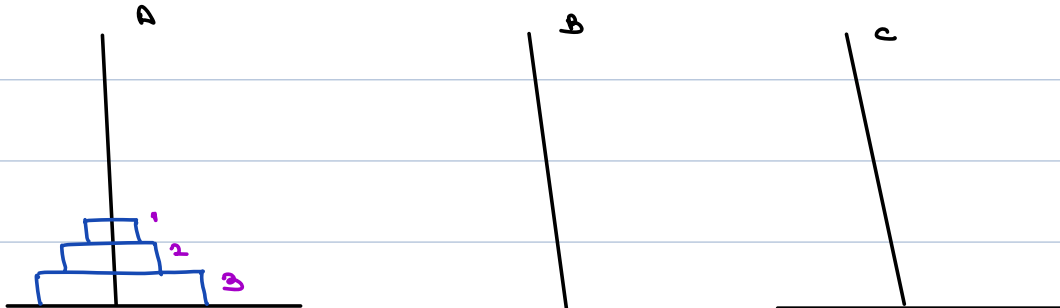
Goal

Move all disks from tower A to C using tower B if needed.

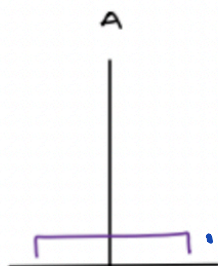
Constraint

- Only 1 disk can be moved at a time.
- Larger disk can not be placed on a small disk at any step.

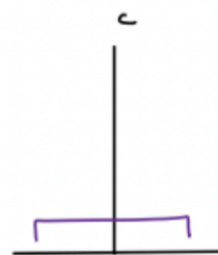
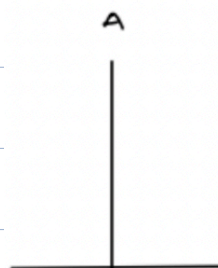
3 disks



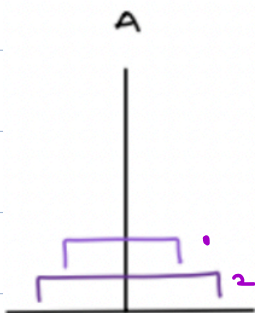
$n=1$



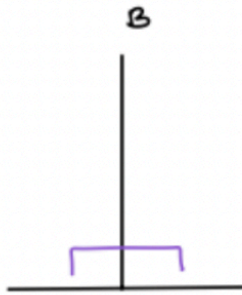
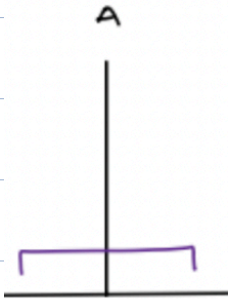
$1: A \rightarrow C$



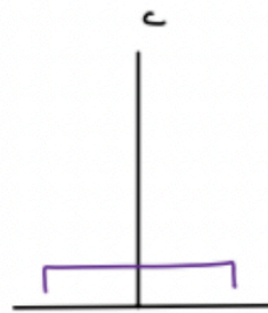
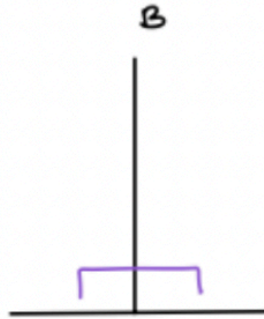
$m=2$



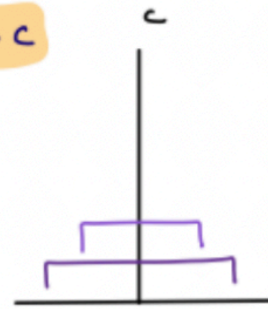
1: $A \rightarrow B$



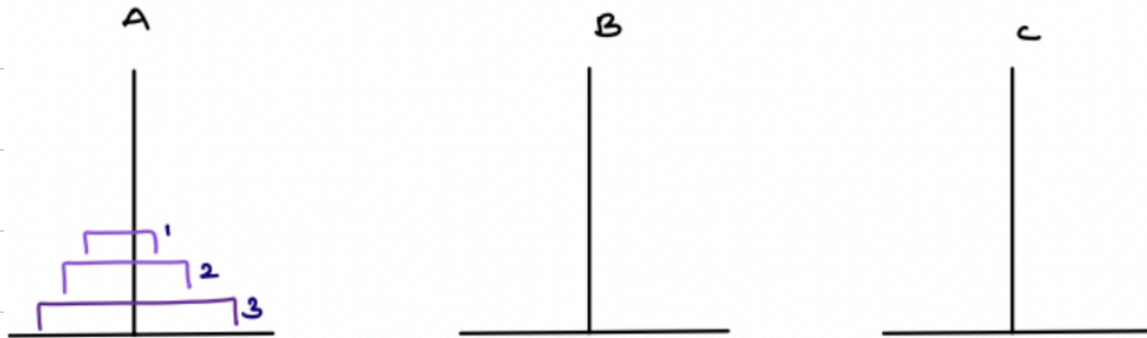
2: $A \rightarrow C$



1: $B \rightarrow C$



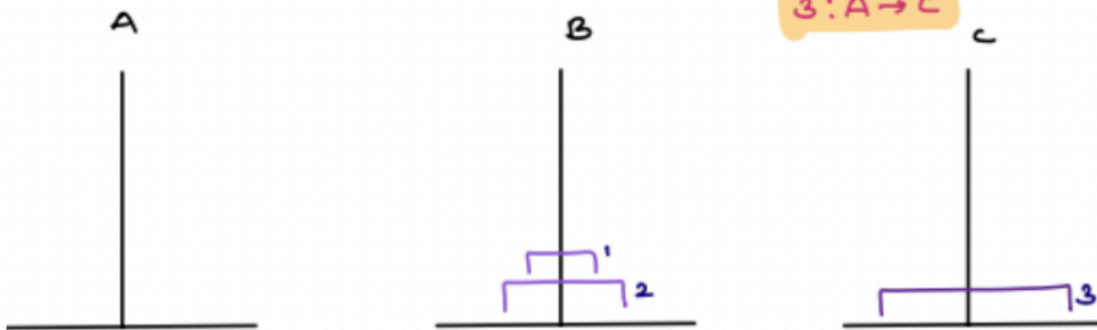
N := B



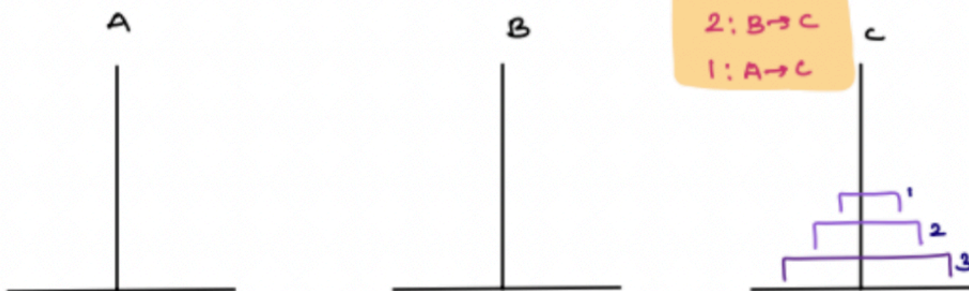
current problem,
move 2 disks from A to B
with help of C.

1: $A \rightarrow C$
2: $A \rightarrow B$
1: $C \rightarrow B$





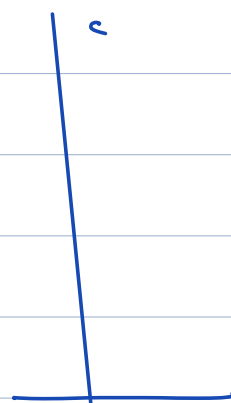
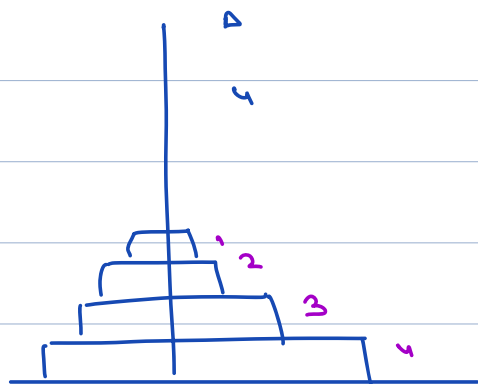
$1: B \rightarrow A$
 $2: B \rightarrow C$
 $1: A \rightarrow C$



Output:

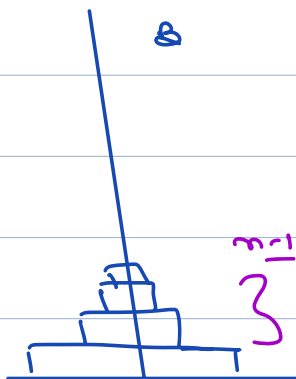
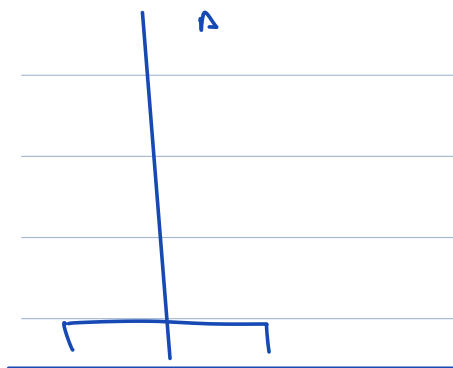
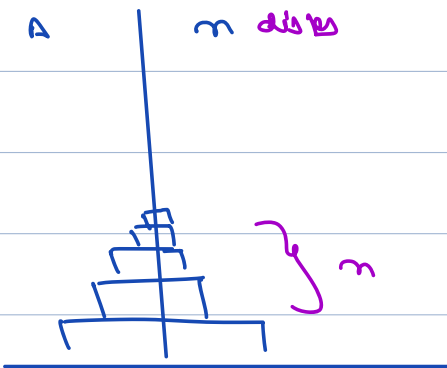
$1: A \rightarrow C$
 $2: A \rightarrow B$
 $1: C \rightarrow B$
 $3: A \rightarrow C$
 $1: B \rightarrow A$
 $2: B \rightarrow C$
 $1: A \rightarrow C$

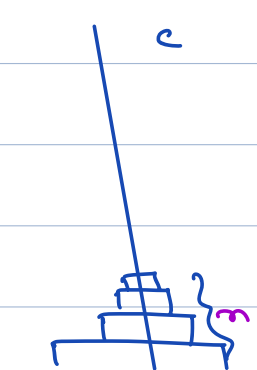
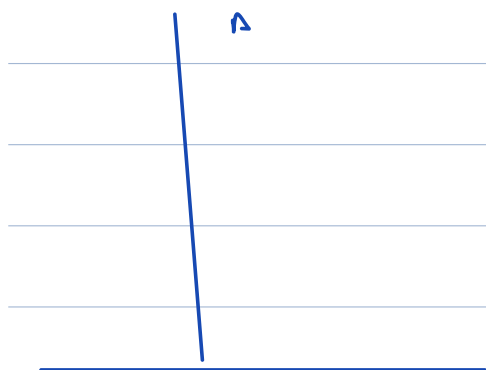
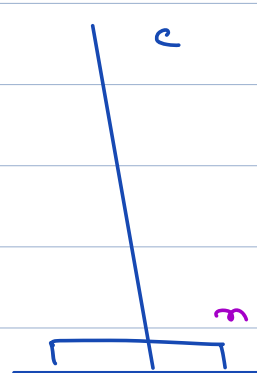
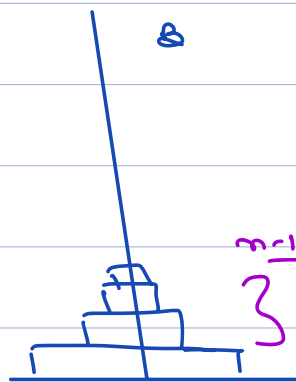
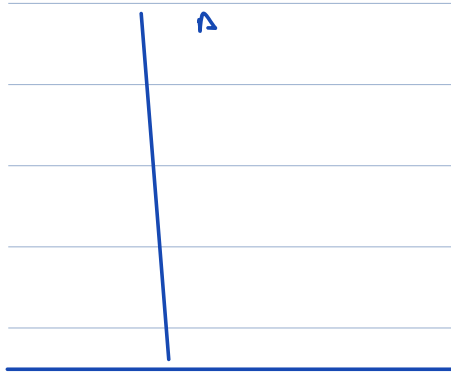
$n=4$



e.g. n disk

A n disks





Recurrence Relation

$$T(m) = 2T(m-1) + 1 \rightarrow \text{solve}$$

picking
2
helper
2
drop
2

```

void ToH ( int n, char s, char H, char D ) {
    if (n == 0) { return; }

    ToH ( n-1, s, D, H );
    Print ( n: s → D );
    ToH ( n-1, H, s, D );
}
  
```

3

Recursive code :-

- 1) High level understanding. ✓
- 2) Low level understanding X.

1: A → C
 2: A → B
 1: C → B
 3: A → C
 1: B → A
 2: B → C
 1: A → C



```

void ToH ( int n, char s, char H, char D ) {
    if (n==0) { return; }

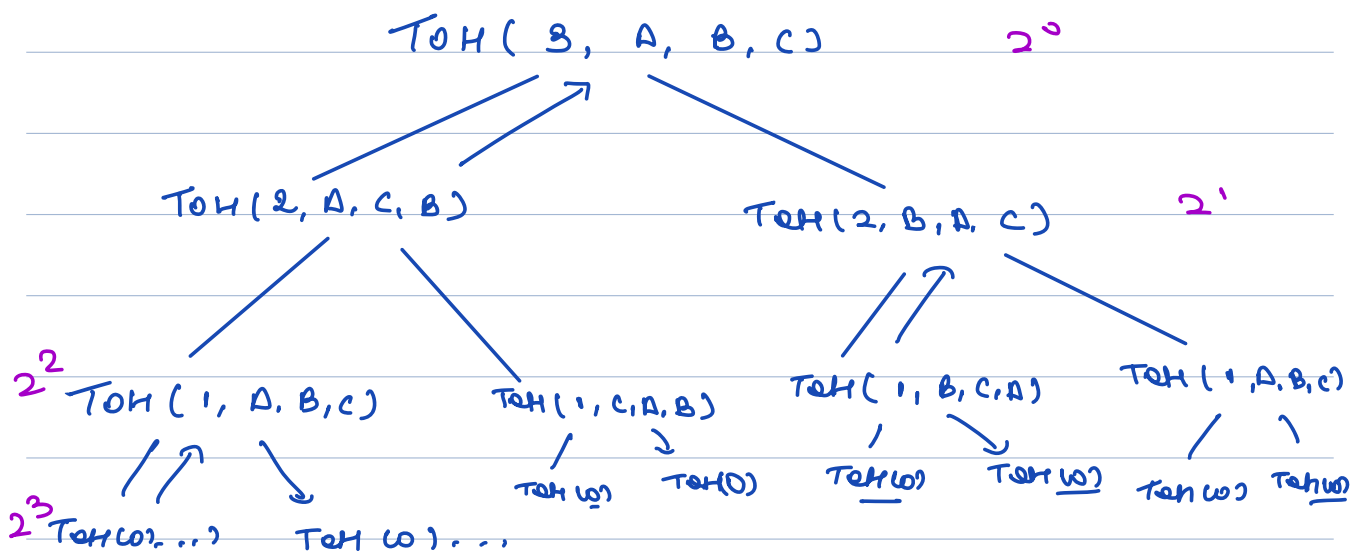
    ToH ( n-1, s, D, H );
    Print ( n: s → D );
    ToH ( n-1, H, s, D );
}

```

Picking
Helper
Drop

↓
↓
↓

3



input $\Rightarrow 3$

$$2^0 + 2^1 + 2^2 + 2^3 \quad \checkmark$$

input $= 4$

$$2^0 + 2^1 + 2^2 + 2^3 + 2^4$$

input $= n$,

$$2^0 + 2^1 + 2^2 + 2^3 + 2^4 + \dots \quad 2^n \rightarrow \text{g.p.}$$

$$\rightarrow \underline{2^{n+1}} \Rightarrow T.C \rightarrow O(\underline{2^n})$$

S.C $\rightarrow O(\infty)$.

recursive \hookleftarrow
stack space.

$$T(n) = 2T(n-1) + 1 \Rightarrow 2^1 T(n-1) + 2^1 - 1$$

$$\hookleftarrow T(n-1) = 2T(n-2) + 1$$

$$T(n) = 4T(n-2) + 3 \Rightarrow 2^2 T(n-2) + 2^2 - 1$$

$$\hookleftarrow T(n-2) = 2T(n-3) + 1$$

$$T(n) = 8T(n-3) + 7 \Rightarrow 2^3 T(n-3) + 2^3 - 1$$

\vdots

// generalized expression:-

$$T(n) = 2^k T(n-k) + 2^k - 1$$

$$T(0) = 1$$

when $k = n$,

$$T(n) = 2^n T(0) + 2^n - 1$$

$$T(n) = 2^n + 2^n - 1$$

$$T(n) = 2 \times 2^n - 1$$

$$T(n) = 2^{n+1} - 1$$

$$T(n) = O(2^n).$$

$$\text{S.C} \rightarrow O(\infty).$$

Indoor \rightarrow (X)

Break 8:36 Am - 8:46 Am

Ques) Print all valid parenthesis of len 2n,
for given n, '(' ')' ,

e.g. n=1, (),)() X

n=2, ()(), (()),

X
)() X n=3, ((()), ()()(), (())() X
(())(), ()(()), (())().

n=4, ((())(), ((())(),

()((()), ((())(), ...

string,

()

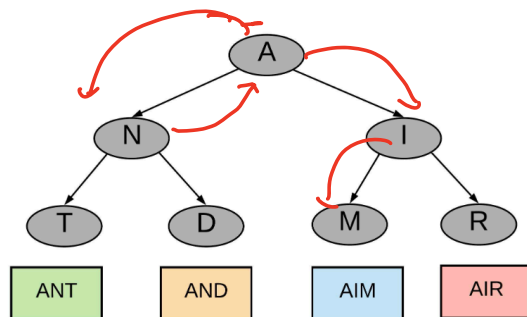
2n, (), check their validity,

n=3,

()...

Backtracking → recursively trying all the
solutions,

words



AIM





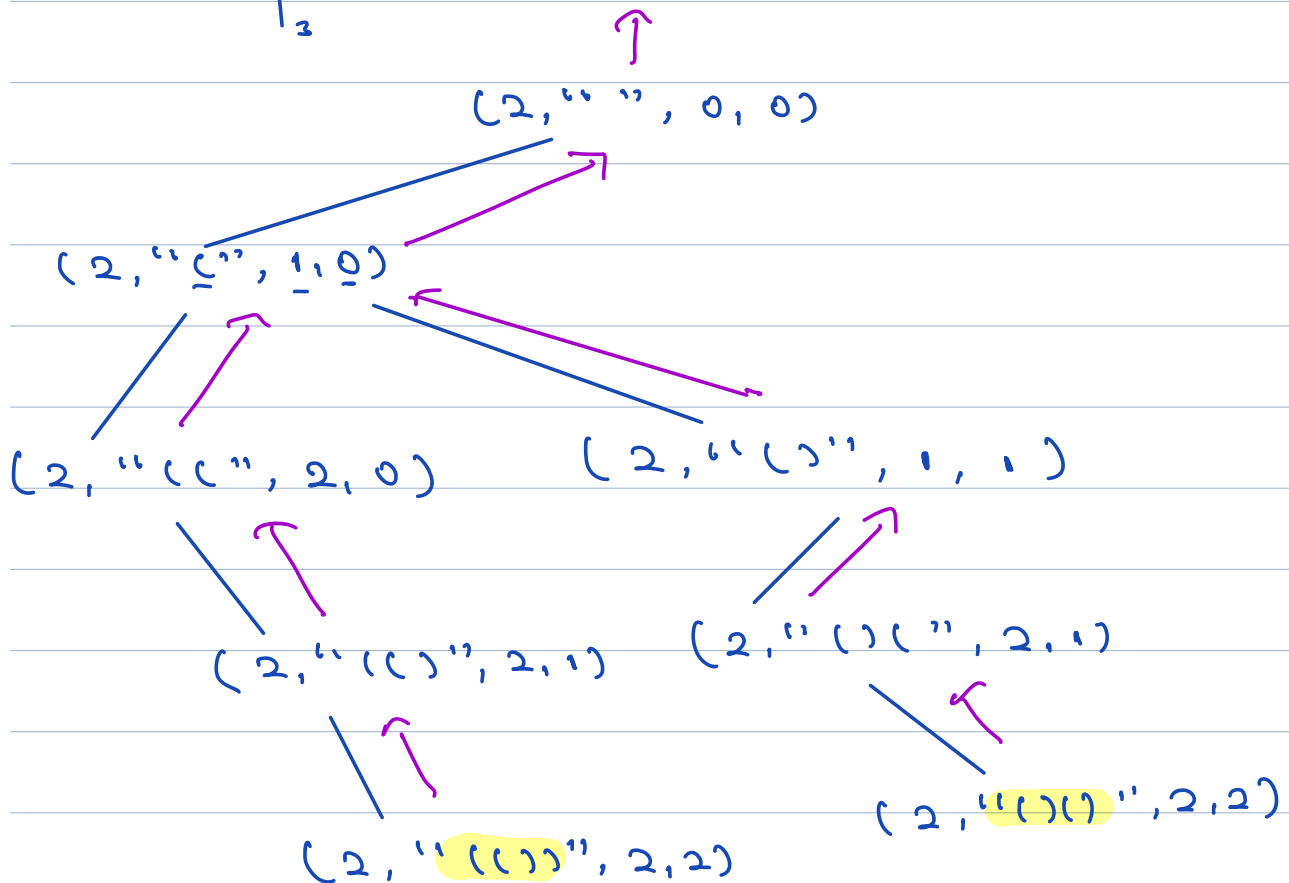
② open-bracket > close-bracket \rightarrow ']'.

$$\underline{2 = 2}$$

```

void solve (n, str, open_br, close_br) {
1 |   if (str.length == 2*n) { print(str); return }
2 |   if (open_br < n) {
3 |       |
4 |       |   solve (n, str + '(', open_br+1, close_br);
5 |       |   }
6 |       |
7 |       |   if (close_br < n) {
8 |       |       |
9 |       |       |   solve (n, str + ')', open_br, close_br+1);
10 |      |       |   }
11 |      |       }
12 |      }
13 |  }

```



T.C $\rightarrow O(\underline{2^n})$

$S.C \rightarrow O(N)$ (actual stack space $2 \times N$):

$x \rightarrow$

	1	0	1	0	
	1	0	0	0	0

\rightarrow

	1	0	1	0
2	0	1	0	1
