

Report of Assignment 4 Problem 1

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Question 1

Proof The setting is shown in Figure 1. From reflection law, \mathbf{r} , \mathbf{n} and \mathbf{l} lie in the same plane and $\angle(\mathbf{r}, \mathbf{n}) = \angle(\mathbf{n}, \mathbf{l})$. From the definition of \mathbf{h} , we know that \mathbf{v} , \mathbf{h} and \mathbf{l} lie in the same plane and $\angle(\mathbf{v}, \mathbf{h}) = \angle(\mathbf{h}, \mathbf{l})$.

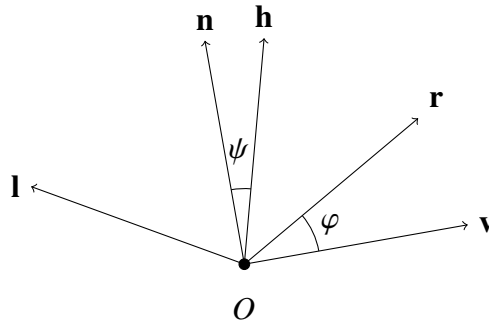


Figure 1 The angles ϕ and ψ

If \mathbf{v} lies in the plane of \mathbf{l} , \mathbf{n} and \mathbf{r} , then all the five vectors lie in the same plane. Therefore, we have

$$\begin{aligned}
 \psi &= \angle(\mathbf{h}, \mathbf{n}) = \angle(\mathbf{h}, \mathbf{l}) - \angle(\mathbf{n}, \mathbf{l}) \\
 &= \frac{1}{2} (\angle(\mathbf{v}, \mathbf{l}) - \angle(\mathbf{r}, \mathbf{l})) \\
 &= \frac{1}{2} \angle(\mathbf{v}, \mathbf{r}) = \frac{1}{2} \phi
 \end{aligned} \tag{1}$$

and equivalently $2\psi = \phi$ as desired.

□