

Homework 2

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Due January 23rd

Please do the following problems from the text book ISLR.

1. Question 3.7.5 pg 121

ANS:

We are given that

$$\hat{y}_i = x_i \hat{\beta}$$

and

$$\hat{\beta} = \frac{\sum_{i=1}^n x_i y_i}{\sum_{i=1}^n x_i^2}$$

Substituting the value of

$$\hat{\beta}$$

in

$$\hat{y}_i = x_i \hat{\beta}$$

, we get,

$$\hat{y}_i = x_i \frac{\sum_{i'=1}^n x_{i'} y_{i'}}{\sum_{k=1}^n x_k^2} = \sum_{i'=1}^n \frac{x_i x_{i'}}{\sum_{k=1}^n x_k^2} y_{i'} = \sum_{i'=1}^n a_{i'} y_{i'}$$

2. Question 3.7.10 pg 123

10. This question should be answered using the Carseats data set. (a) Fit a multiple regression model to predict Sales using Price, Urban, and US. (b) Provide an interpretation of each coefficient in the model. Be careful-some of the variables in the model are qualitative! (c) Write out the model in equation form, being careful to handle the qualitative variables properly. (d) For which of the predictors can you reject the null hypothesis $H_0 : \beta_j = 0$? (e) On the basis of your response to the previous question, fit a smaller model that only uses the predictors for which there is evidence of association with the outcome. (f) How well do the models in (a) and (e) fit the data? (g) Using the model

from (e), obtain 95% confidence intervals for the coefficient(s). (h) Is there evidence of outliers or high leverage observations in the model from (e)?

a

(a) Fit a multiple regression model to predict Sales using Price, Urban, and US.

```
##  
## Call:  
## lm(formula = Sales ~ Price + Urban + US, data = Carseats)  
##  
## Residuals:  
##      Min       1Q   Median       3Q      Max   
## -6.9206 -1.6220 -0.0564  1.5786  7.0581   
##  
## Coefficients:  
##              Estimate Std. Error t value Pr(>|t|)      
## (Intercept) 13.043469   0.651012  20.036 < 2e-16 ***  
## Price       -0.054459   0.005242 -10.389 < 2e-16 ***  
## UrbanYes    -0.021916   0.271650  -0.081  0.936      
## USYes       1.200573    0.259042   4.635 4.86e-06 ***  
## ---  
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1  
##  
## Residual standard error: 2.472 on 396 degrees of freedom  
## Multiple R-squared:  0.2393, Adjusted R-squared:  0.2335   
## F-statistic: 41.52 on 3 and 396 DF,  p-value: < 2.2e-16
```

b

(b) Provide an interpretation of each coefficient in the model. Be careful-some of the variables in the model are qualitative!

Ans: The coefficient of price suggest that as price increases the sales decrease since it has negative coefficient value. Price variable has significant relationship with sales since it has less p-value. The coefficient of Urban variable suggest that sales decreases when the stores are in urban area. The coefficient of US suggest that sales increases when stores are in the US.

c

(c) Write out the model in equation form, being careful to handle the qualitative variables properly.

The Model Equation is

$$\text{Sales} = 13.043469 + (-0.054459)\text{Price} + (-0.021916)\text{UrbanYes} + (1.200573)\text{USYes}$$

#d (d) For which of the predictors can you reject the null hypothesis $H_0 : \beta_j = 0$?

Ans: we can reject null hypothesis for the Price and US variables. Null hypothesis is rejected due to their small p-value

e

(e) On the basis of your response to the previous question, fit a smaller model that only uses the predictors for which there is evidence of association with the outcome.

```
##  
## Call:  
## lm(formula = Sales ~ Price + US)  
##  
## Residuals:  
##      Min       1Q   Median       3Q      Max   
## -6.9269 -1.6286 -0.0574  1.5766  7.0515   
##  
## Coefficients:  
##              Estimate Std. Error t value Pr(>|t|)      
## (Intercept) 13.03079    0.63098  20.652 < 2e-16 ***  
## Price       -0.05448    0.00523 -10.416 < 2e-16 ***  
## USYes       1.19964    0.25846   4.641 4.71e-06 ***  
## ---  
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1  
##  
## Residual standard error: 2.469 on 397 degrees of freedom  
## Multiple R-squared:  0.2393, Adjusted R-squared:  0.2354   
## F-statistic: 62.43 on 2 and 397 DF,  p-value: < 2.2e-16
```

f

(f) How well do the models in (a) and (e) fit the data?

```
## Analysis of Variance Table  
##  
## Model 1: Sales ~ Price + Urban + US  
## Model 2: Sales ~ Price + US  
##   Res.Df    RSS Df Sum of Sq    F Pr(>F)      
## 1     396 2420.8        
## 2     397 2420.9 -1   -0.03979 0.0065 0.9357
```

Here R-squared and RSE for both models are similar. Anova test also suggest that F-statistic is 0.0065 and it's P-value near to 1 hence the both model fit similarly with the data. Model in (e) fit slightly better. Both the model has less R-squared error which is not good for any model to fit data.

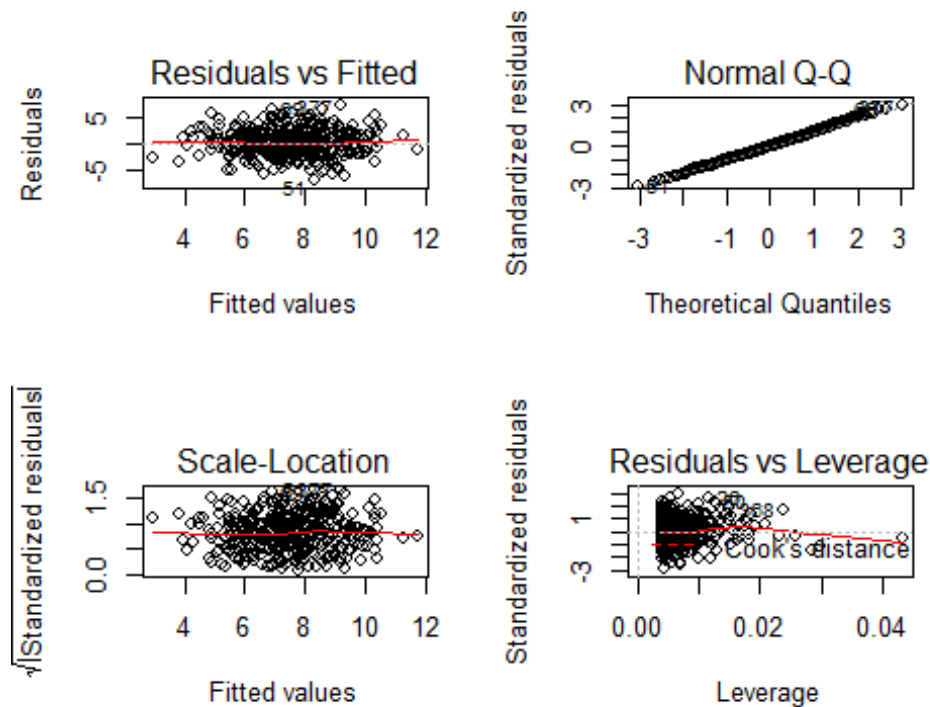
g

(g) Using the model from (e), obtain 95% confidence intervals for the coefficient(s).

```
##                2.5 %      97.5 %  
## (Intercept) 11.79032020 14.27126531  
## Price      -0.06475984 -0.04419543  
## USYes       0.69151957  1.70776632
```

h

(h) Is there evidence of outliers or high leverage observations in the model from (e)?



```
## 43
```

```
## 43
```

In the Residuals vs Leverage plot, there are few observations that are outliers and there are some leverage points because some of the points exceed the 0.01.

3. Question 3.7.15 pg 126

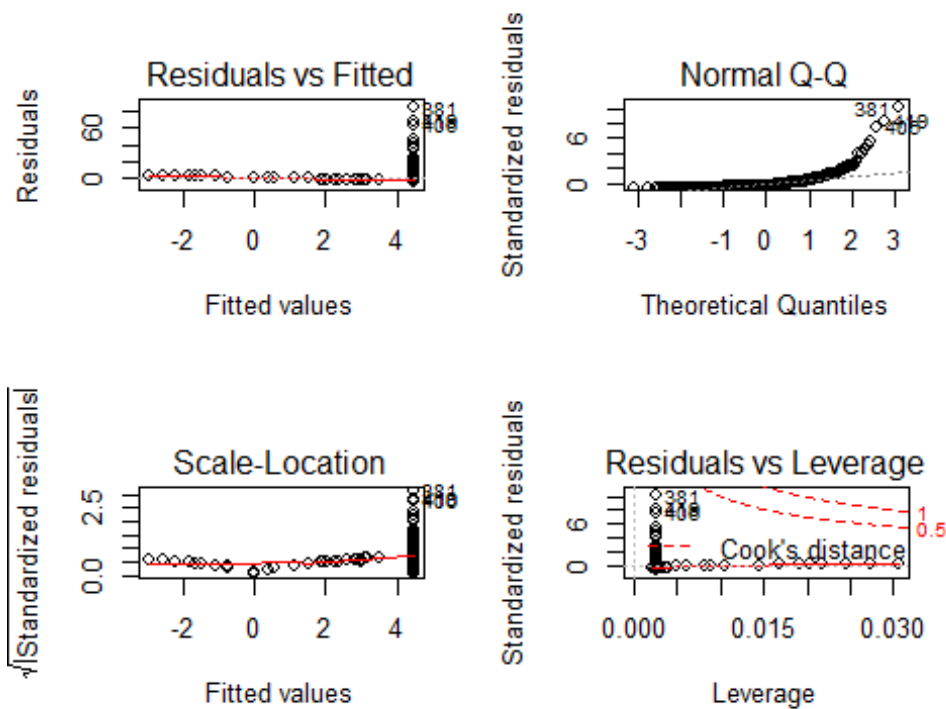
15. This problem involves the Boston data set, which we saw in the lab for this chapter. We will now try to predict per capita crime rate using the other variables in this data set. In other words, per capita crime rate is the response, and the other variables are the predictors. (a) For each predictor, fit a simple linear regression model to predict the response. Describe your results. In which of the models is there a statistically significant association between the predictor and the response? Create some plots to back up your

assertions. (b) Fit a multiple regression model to predict the response using all of the predictors. Describe your results. For which predictors can we reject the null hypothesis $H_0 : \beta_j = 0$? (c) How do your results from (a) compare to your results from (b)? Create a plot displaying the univariate regression coefficients from (a) on the x-axis, and the multiple regression coefficients from (b) on the y-axis. That is, each predictor is displayed as a single point in the plot. Its coefficient in a simple linear regression model is shown on the x-axis, and its coefficient estimate in the multiple linear regression model is shown on the y-axis. (d) Is there evidence of non-linear association between any of the predictors and the response? To answer this question, for each predictor X , fit a model of the form $Y = \beta_0 + \beta_1 X + \beta_2 X^2 + \beta_3 X^3 + E$.

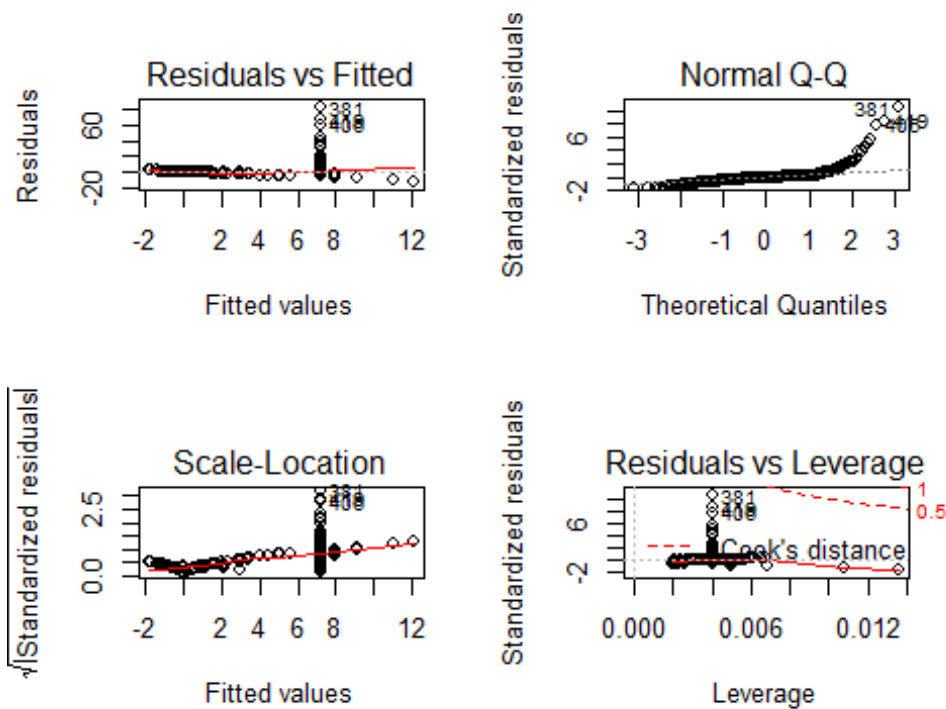
a

- (a) For each predictor, fit a simple linear regression model to predict the response. Describe your results. In which of the models is there a statistically significant association between the predictor and the response? Create some plots to back up your assertions.

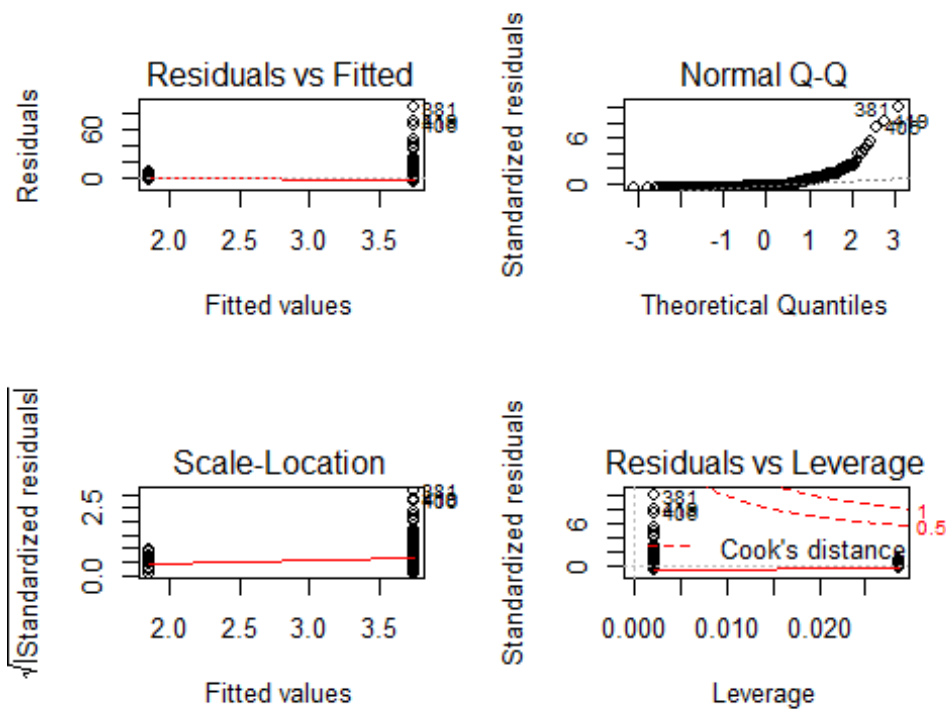
```
##
## Call:
## lm(formula = crim ~ zn, data = Boston)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -4.429 -4.222 -2.620  1.250 84.523
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  4.45369    0.41722  10.675  < 2e-16 ***
## zn          -0.07393    0.01609  -4.594 5.51e-06 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 8.435 on 504 degrees of freedom
## Multiple R-squared:  0.04019,    Adjusted R-squared:  0.03828
## F-statistic: 21.1 on 1 and 504 DF,  p-value: 5.506e-06
```



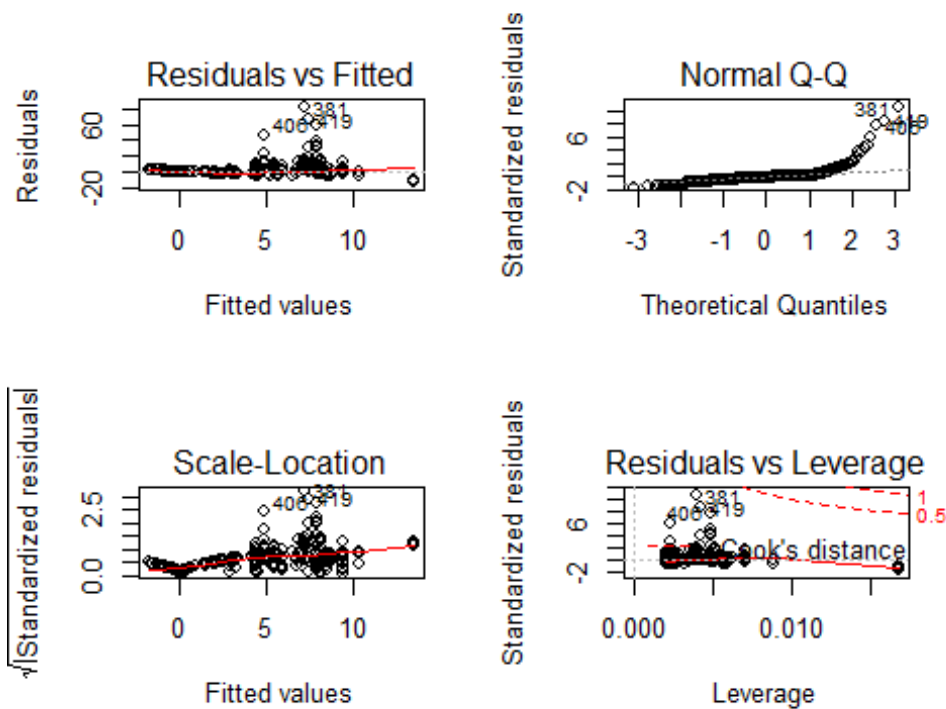
```
##
## Call:
## lm(formula = crim ~ indus, data = Boston)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -11.972  -2.698  -0.736   0.712   81.813
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -2.06374    0.66723  -3.093  0.00209 **
## indus        0.50978    0.05102   9.991 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 7.866 on 504 degrees of freedom
## Multiple R-squared:  0.1653, Adjusted R-squared:  0.1637
## F-statistic: 99.82 on 1 and 504 DF,  p-value: < 2.2e-16
```



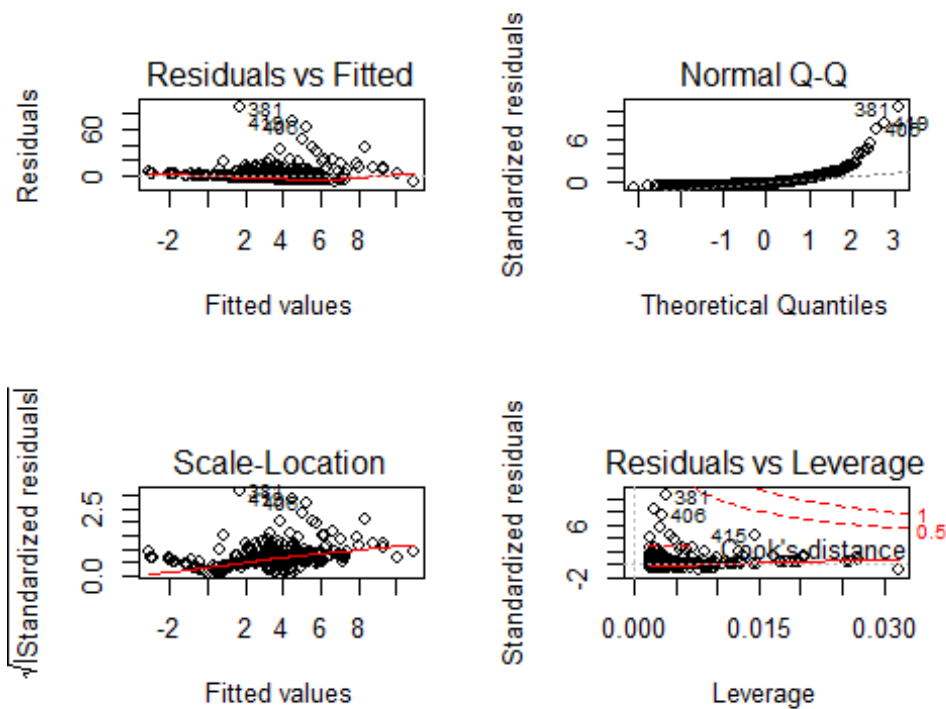
```
##
## Call:
## lm(formula = crim ~ chas, data = Boston)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -3.738 -3.661 -3.435  0.018 85.232
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   3.7444     0.3961   9.453  <2e-16 ***
## chas         -1.8928     1.5061  -1.257   0.209
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 8.597 on 504 degrees of freedom
## Multiple R-squared:  0.003124,    Adjusted R-squared:  0.001146
## F-statistic: 1.579 on 1 and 504 DF,  p-value: 0.2094
```



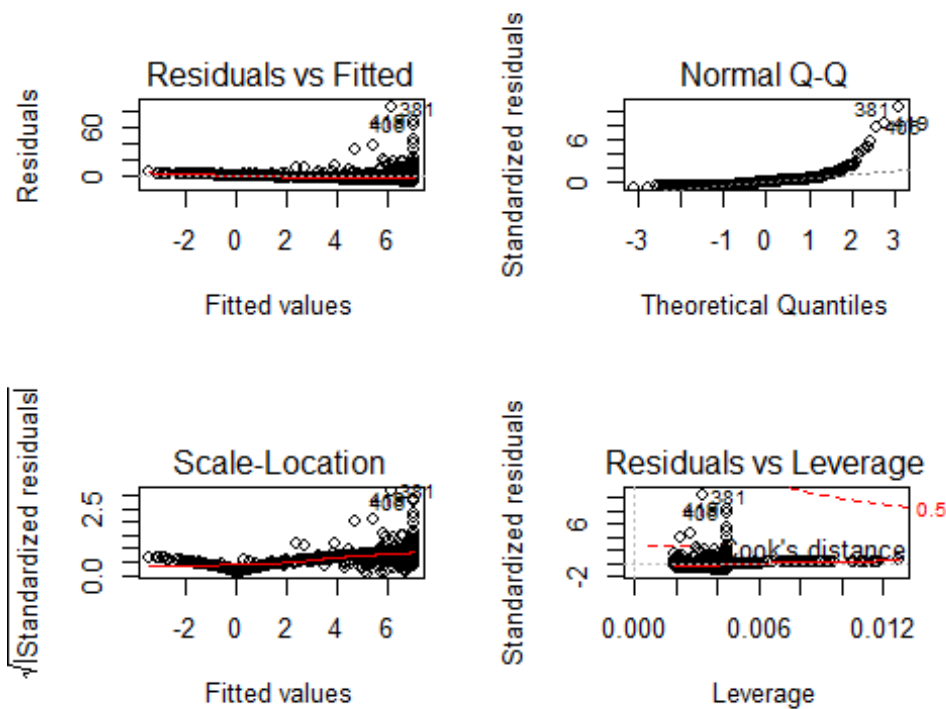
```
##
## Call:
## lm(formula = crim ~ nox, data = Boston)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -12.371  -2.738  -0.974   0.559   81.728
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  -13.720      1.699   -8.073 5.08e-15 ***
## nox           31.249      2.999  10.419 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 7.81 on 504 degrees of freedom
## Multiple R-squared:  0.1772, Adjusted R-squared:  0.1756
## F-statistic: 108.6 on 1 and 504 DF,  p-value: < 2.2e-16
```

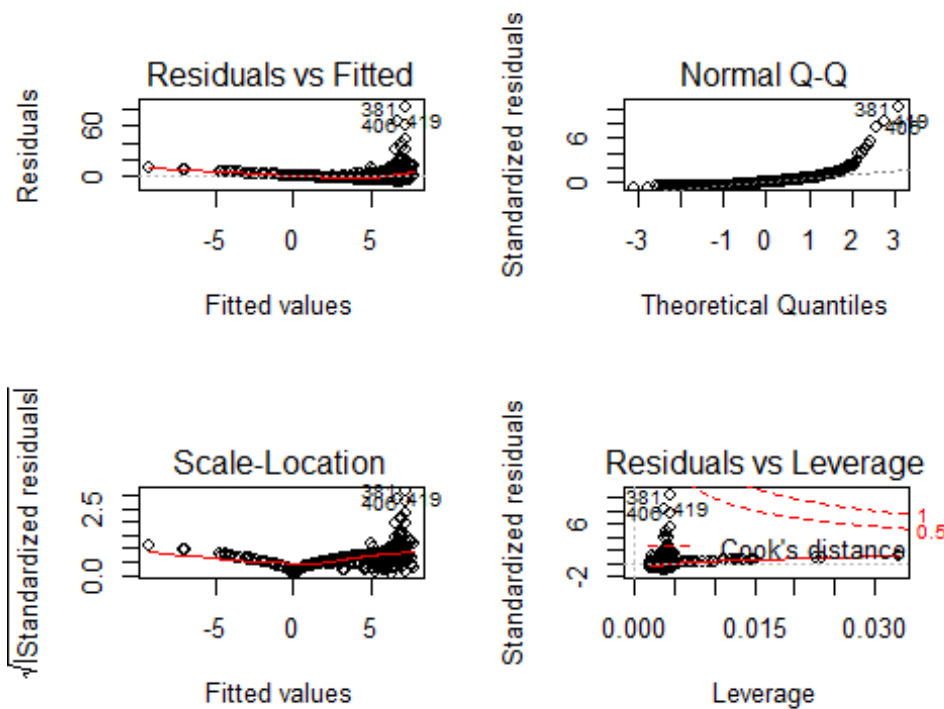
```
##
## Call:
## lm(formula = crim ~ rm, data = Boston)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -6.604  -3.952  -2.654   0.989  87.197
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   20.482     3.365    6.088 2.27e-09 ***
## rm           -2.684     0.532   -5.045 6.35e-07 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 8.401 on 504 degrees of freedom
## Multiple R-squared:  0.04807,    Adjusted R-squared:  0.04618
## F-statistic: 25.45 on 1 and 504 DF,  p-value: 6.347e-07
```



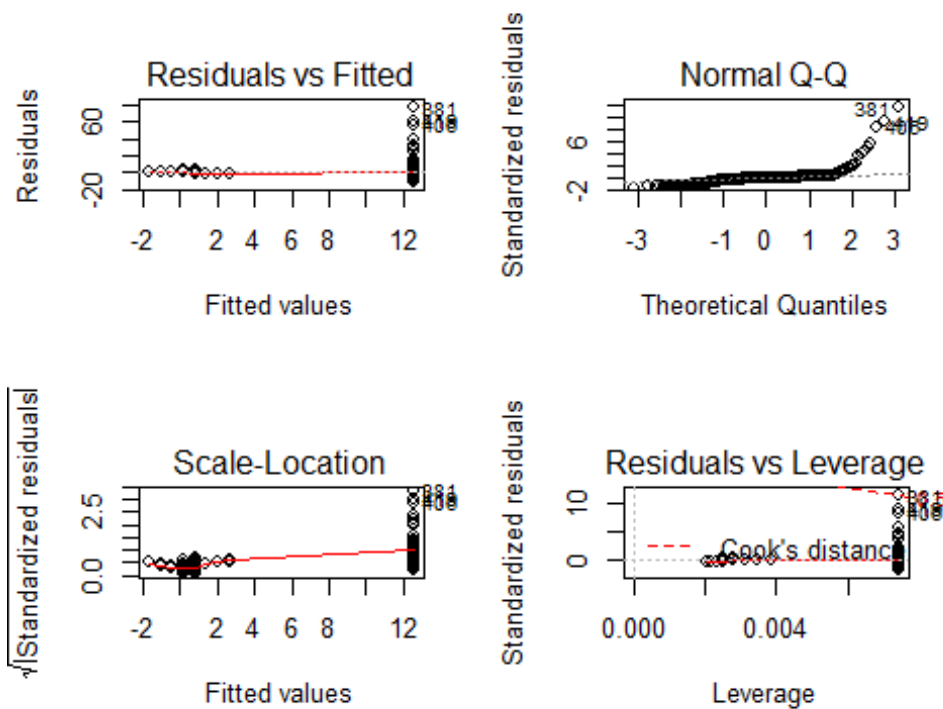
```
##
## Call:
## lm(formula = crim ~ age, data = Boston)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -6.789  -4.257  -1.230   1.527  82.849
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -3.77791     0.94398  -4.002 7.22e-05 ***
## age          0.10779     0.01274   8.463 2.85e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 8.057 on 504 degrees of freedom
## Multiple R-squared:  0.1244, Adjusted R-squared:  0.1227
## F-statistic: 71.62 on 1 and 504 DF, p-value: 2.855e-16
```



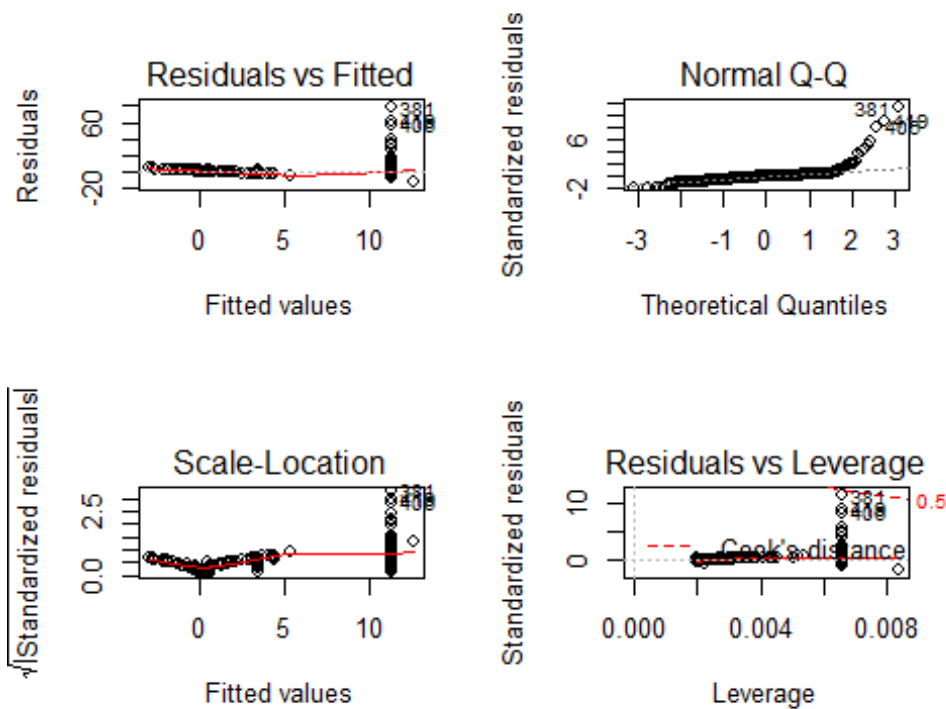
```
##
## Call:
## lm(formula = crim ~ dis, data = Boston)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -6.708  -4.134  -1.527   1.516  81.674
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   9.4993     0.7304   13.006  <2e-16 ***
## dis          -1.5509     0.1683   -9.213  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 7.965 on 504 degrees of freedom
## Multiple R-squared:  0.1441, Adjusted R-squared:  0.1425
## F-statistic: 84.89 on 1 and 504 DF,  p-value: < 2.2e-16
```



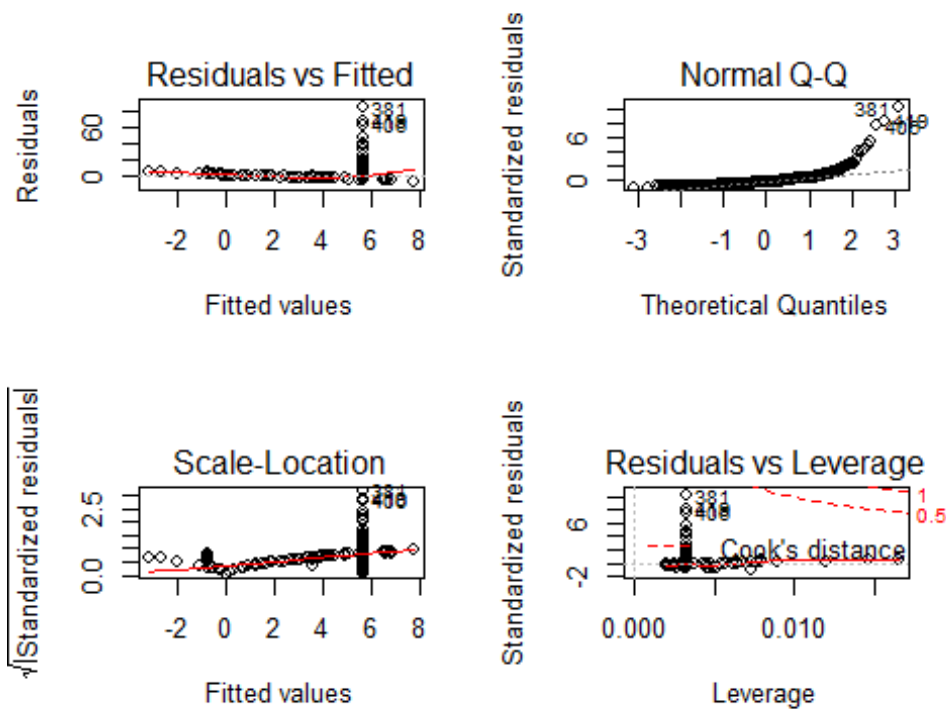
```
##
## Call:
## lm(formula = crim ~ rad, data = Boston)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -10.164  -1.381  -0.141   0.660   76.433
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -2.28716    0.44348  -5.157 3.61e-07 ***
## rad          0.61791    0.03433  17.998 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 6.718 on 504 degrees of freedom
## Multiple R-squared:  0.3913, Adjusted R-squared:  0.39
## F-statistic: 323.9 on 1 and 504 DF, p-value: < 2.2e-16
```



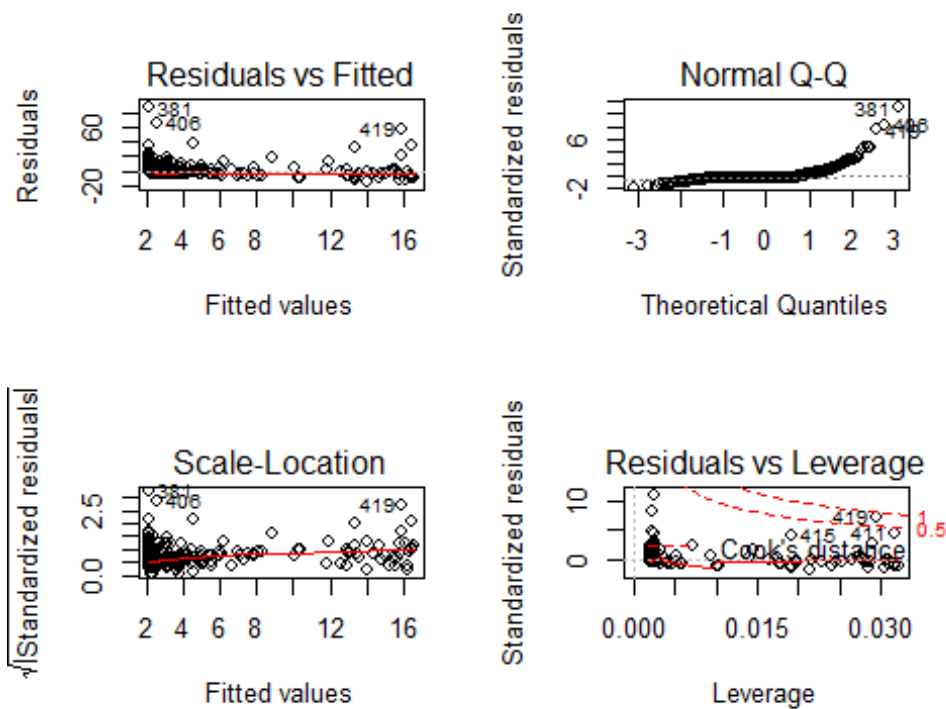
```
##
## Call:
## lm(formula = crim ~ tax, data = Boston)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -12.513  -2.738  -0.194   1.065   77.696
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -8.528369   0.815809  -10.45  <2e-16 ***
## tax          0.029742   0.001847   16.10  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 6.997 on 504 degrees of freedom
## Multiple R-squared:  0.3396, Adjusted R-squared:  0.3383
## F-statistic: 259.2 on 1 and 504 DF,  p-value: < 2.2e-16
```



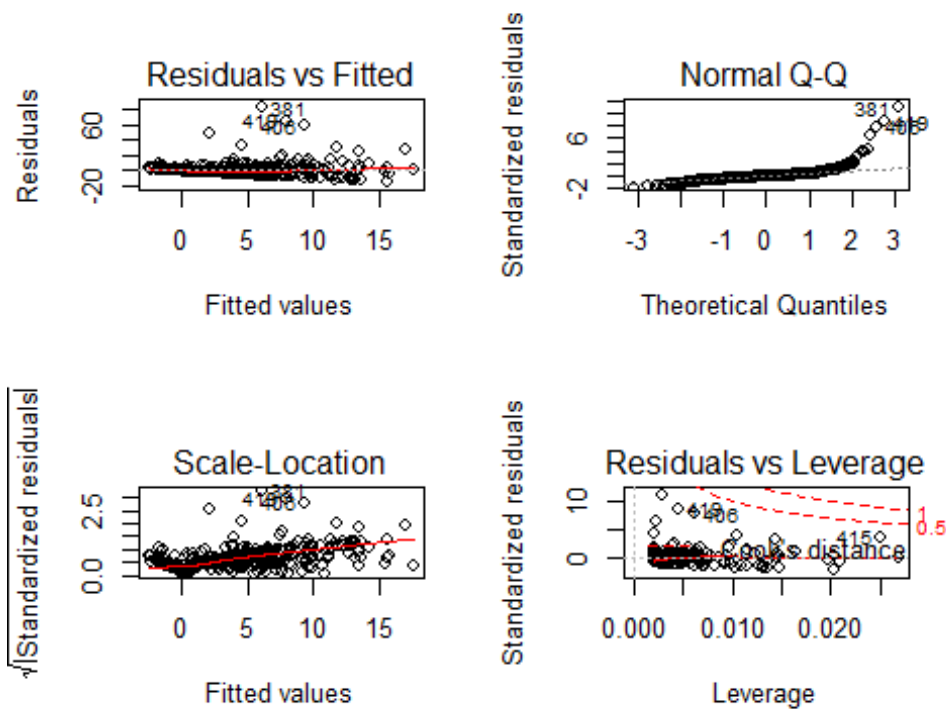
```
##
## Call:
## lm(formula = crim ~ ptratio, data = Boston)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -7.654  -3.985  -1.912   1.825  83.353
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -17.6469     3.1473  -5.607 3.40e-08 ***
## ptratio      1.1520     0.1694   6.801 2.94e-11 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 8.24 on 504 degrees of freedom
## Multiple R-squared:  0.08407,    Adjusted R-squared:  0.08225
## F-statistic: 46.26 on 1 and 504 DF,  p-value: 2.943e-11
```



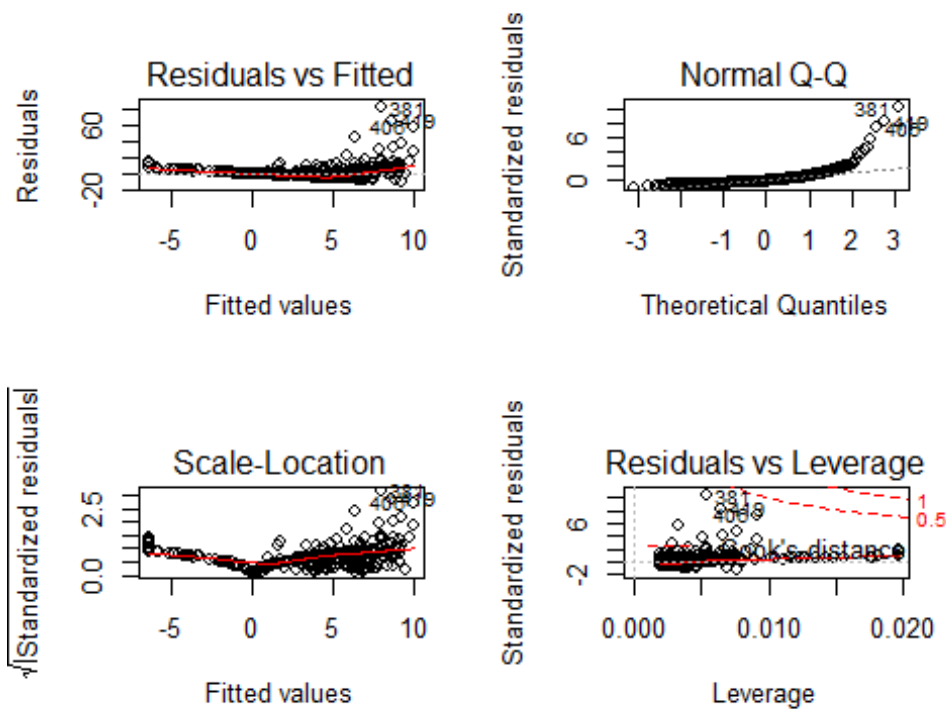
```
##
## Call:
## lm(formula = crim ~ black, data = Boston)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -13.756  -2.299  -2.095  -1.296   86.822
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 16.553529   1.425903  11.609  <2e-16 ***
## black       -0.036280   0.003873  -9.367  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 7.946 on 504 degrees of freedom
## Multiple R-squared:  0.1483, Adjusted R-squared:  0.1466
## F-statistic: 87.74 on 1 and 504 DF,  p-value: < 2.2e-16
```



```
##
## Call:
## lm(formula = crim ~ lstat, data = Boston)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -13.925  -2.822  -0.664   1.079   82.862
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -3.33054    0.69376  -4.801 2.09e-06 ***
## lstat       0.54880    0.04776  11.491 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 7.664 on 504 degrees of freedom
## Multiple R-squared:  0.2076, Adjusted R-squared:  0.206
## F-statistic: 132 on 1 and 504 DF, p-value: < 2.2e-16
```

```
##
## Call:
## lm(formula = crim ~ medv, data = Boston)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -9.071  -4.022  -2.343   1.298  80.957
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 11.79654    0.93419   12.63  <2e-16 ***
## medv        -0.36316    0.03839   -9.46  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 7.934 on 504 degrees of freedom
## Multiple R-squared:  0.1508, Adjusted R-squared:  0.1491
## F-statistic: 89.49 on 1 and 504 DF,  p-value: < 2.2e-16
```



All the variables reject null hypothesis except chas and have significant p-value which is less than 0.05. Hence all variable except chas has significant relationship with response variable crim.

b

(b) Fit a multiple regression model to predict the response using all of the predictors. Describe your results. For which predictors can we reject the null hypothesis $H_0: \beta_j = 0$?

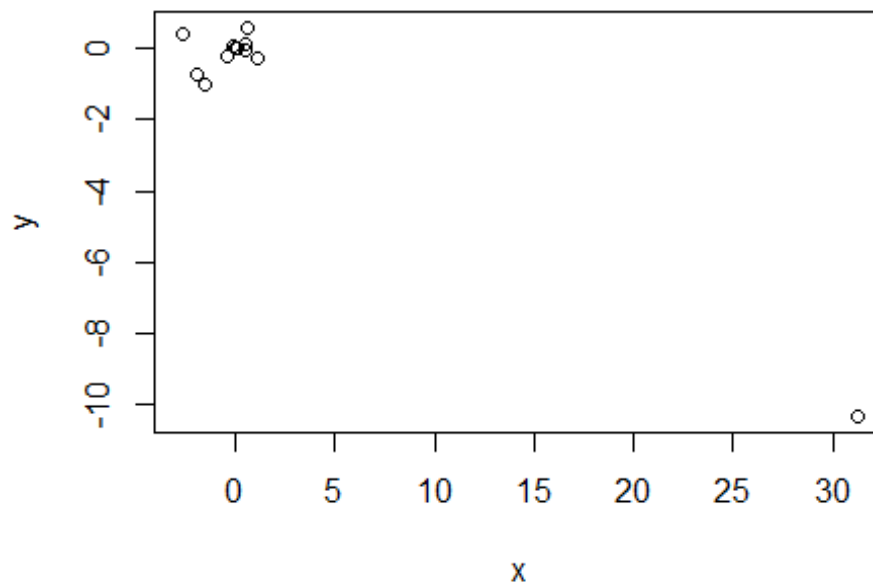
```
##
## Call:
## lm(formula = crim ~ ., data = Boston)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -9.924 -2.120 -0.353  1.019  75.051
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  17.033228   7.234903   2.354 0.018949 *
## zn           0.044855   0.018734   2.394 0.017025 *
## indus       -0.063855   0.083407  -0.766 0.444294
## chas        -0.749134   1.180147  -0.635 0.525867
## nox        -10.313535   5.275536  -1.955 0.051152 .
## rm          0.430131   0.612830   0.702 0.483089
```

```
## age          0.001452    0.017925    0.081 0.935488
## dis         -0.987176    0.281817   -3.503 0.000502 ***
## rad          0.588209    0.088049    6.680 6.46e-11 ***
## tax         -0.003780    0.005156   -0.733 0.463793
## ptratio     -0.271081    0.186450   -1.454 0.146611
## black       -0.007538    0.003673   -2.052 0.040702 *
## lstat        0.126211    0.075725    1.667 0.096208 .
## medv        -0.198887    0.060516   -3.287 0.001087 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 6.439 on 492 degrees of freedom
## Multiple R-squared:  0.454, Adjusted R-squared:  0.4396
## F-statistic: 31.47 on 13 and 492 DF, p-value: < 2.2e-16
```

We can reject the NULL hypothesis $H_0 : \beta_j = 0$ for variables zn, dis, rad, black and medv

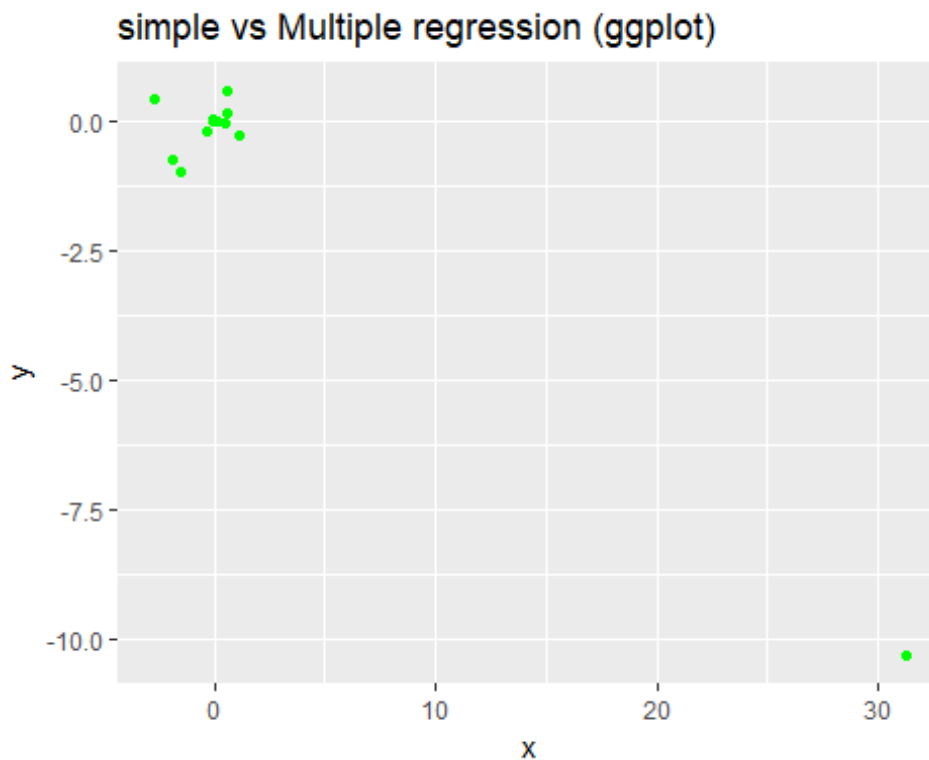
c

- (c) How do your results from (a) compare to your results from (b)? Create a plot displaying the univariate regression coefficients from (a) on the x-axis, and the multiple regression coefficients from (b) on the y-axis. That is, each predictor is displayed as a single point in the plot. Its coefficient in a simple linear regression model is shown on the x-axis, and its coefficient estimate in the multiple linear regression model is shown on the y-axis.



There is difference between simple and multiple regression coefficients. One of the variables, `nox`, has a coefficient value of 31.249 in simple regression and 10 in multiple regression. By observing the above plot, it shows that coefficient values are higher in simple regression than in multiple regression.

ggplot



d

(d) Is there evidence of non-linear association between any of the predictors and the response? To answer this question, for each predictor X , fit a model of the form $Y = \beta_0 + \beta_1 X + \beta_2 X^2 + \beta_3 X^3 + E$.

```
##
## Call:
## lm(formula = crim ~ poly(zn, 3))
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -4.821  -4.614  -1.294   0.473  84.130
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    3.6135     0.3722   9.709  < 2e-16 ***
## poly(zn, 3)1  -38.7498     8.3722  -4.628  4.7e-06 ***
```

```

## poly(zn, 3)2 23.9398      8.3722  2.859  0.00442 **
## poly(zn, 3)3 -10.0719      8.3722 -1.203  0.22954
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 8.372 on 502 degrees of freedom
## Multiple R-squared:  0.05824,    Adjusted R-squared:  0.05261
## F-statistic: 10.35 on 3 and 502 DF,  p-value: 1.281e-06

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## poly(zn, 3)1 -38.7498     8.3722  -4.628 4.7e-06 ***
## poly(zn, 3)2  23.9398     8.3722   2.859 0.00442 **
## poly(zn, 3)3 -10.0719     8.3722  -1.203 0.22954
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##
## Call:
## lm(formula = crim ~ poly(indus, 3))
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -8.278 -2.514  0.054  0.764 79.713
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    3.614      0.330  10.950 < 2e-16 ***
## poly(indus, 3)1  78.591      7.423  10.587 < 2e-16 ***
## poly(indus, 3)2 -24.395      7.423  -3.286 0.00109 **
## poly(indus, 3)3 -54.130      7.423  -7.292 1.2e-12 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 7.423 on 502 degrees of freedom
## Multiple R-squared:  0.2597, Adjusted R-squared:  0.2552
## F-statistic: 58.69 on 3 and 502 DF,  p-value: < 2.2e-16

```

```
##
## Call:
## lm(formula = crim ~ poly(nox, 3))
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -9.110 -2.068 -0.255  0.739 78.302
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    3.6135     0.3216  11.237 < 2e-16 ***
## poly(nox, 3)1  81.3720     7.2336  11.249 < 2e-16 ***
## poly(nox, 3)2 -28.8286     7.2336  -3.985 7.74e-05 ***
## poly(nox, 3)3 -60.3619     7.2336  -8.345 6.96e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 7.234 on 502 degrees of freedom
## Multiple R-squared:  0.297, Adjusted R-squared:  0.2928
## F-statistic: 70.69 on 3 and 502 DF, p-value: < 2.2e-16

##
## Call:
## lm(formula = crim ~ poly(rm, 3))
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -18.485  -3.468  -2.221  -0.015  87.219
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    3.6135     0.3703   9.758 < 2e-16 ***
## poly(rm, 3)1 -42.3794     8.3297  -5.088 5.13e-07 ***
## poly(rm, 3)2  26.5768     8.3297   3.191 0.00151 **
## poly(rm, 3)3  -5.5103     8.3297  -0.662 0.50858
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 8.33 on 502 degrees of freedom
## Multiple R-squared:  0.06779, Adjusted R-squared:  0.06222
## F-statistic: 12.17 on 3 and 502 DF, p-value: 1.067e-07

##
## Call:
## lm(formula = crim ~ poly(age, 3))
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -9.762 -2.673 -0.516  0.019 82.842
##
```

```

## Coefficients:
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)    3.6135     0.3485  10.368 < 2e-16 ***
## poly(age, 3)1  68.1820     7.8397   8.697 < 2e-16 ***
## poly(age, 3)2  37.4845     7.8397   4.781 2.29e-06 ***
## poly(age, 3)3  21.3532     7.8397   2.724 0.00668 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 7.84 on 502 degrees of freedom
## Multiple R-squared:  0.1742, Adjusted R-squared:  0.1693
## F-statistic: 35.31 on 3 and 502 DF,  p-value: < 2.2e-16

##
## Call:
## lm(formula = crim ~ poly(dis, 3))
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -10.757  -2.588   0.031   1.267  76.378
##
## Coefficients:
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)    3.6135     0.3259  11.087 < 2e-16 ***
## poly(dis, 3)1 -73.3886     7.3315 -10.010 < 2e-16 ***
## poly(dis, 3)2  56.3730     7.3315   7.689 7.87e-14 ***
## poly(dis, 3)3 -42.6219     7.3315  -5.814 1.09e-08 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 7.331 on 502 degrees of freedom
## Multiple R-squared:  0.2778, Adjusted R-squared:  0.2735
## F-statistic: 64.37 on 3 and 502 DF,  p-value: < 2.2e-16

##
## Call:
## lm(formula = crim ~ poly(rad, 3))
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -10.381  -0.412  -0.269   0.179  76.217
##
## Coefficients:
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)    3.6135     0.2971  12.164 < 2e-16 ***
## poly(rad, 3)1 120.9074     6.6824  18.093 < 2e-16 ***
## poly(rad, 3)2  17.4923     6.6824   2.618 0.00912 **
## poly(rad, 3)3   4.6985     6.6824   0.703 0.48231
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

```
##
## Residual standard error: 6.682 on 502 degrees of freedom
## Multiple R-squared: 0.4, Adjusted R-squared: 0.3965
## F-statistic: 111.6 on 3 and 502 DF, p-value: < 2.2e-16

##
## Call:
## lm(formula = crim ~ poly(tax, 3))
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -13.273  -1.389   0.046   0.536  76.950
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    3.6135     0.3047  11.860 < 2e-16 ***
## poly(tax, 3)1 112.6458     6.8537  16.436 < 2e-16 ***
## poly(tax, 3)2  32.0873     6.8537   4.682 3.67e-06 ***
## poly(tax, 3)3  -7.9968     6.8537  -1.167   0.244
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 6.854 on 502 degrees of freedom
## Multiple R-squared: 0.3689, Adjusted R-squared: 0.3651
## F-statistic: 97.8 on 3 and 502 DF, p-value: < 2.2e-16

##
## Call:
## lm(formula = crim ~ poly(ptratio, 3))
##
## Residuals:
##      Min       1Q   Median       3Q      Max
##  -6.833  -4.146  -1.655   1.408  82.697
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    3.614     0.361  10.008 < 2e-16 ***
## poly(ptratio, 3)1  56.045     8.122   6.901 1.57e-11 ***
## poly(ptratio, 3)2  24.775     8.122   3.050 0.00241 **
## poly(ptratio, 3)3 -22.280     8.122  -2.743 0.00630 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 8.122 on 502 degrees of freedom
## Multiple R-squared: 0.1138, Adjusted R-squared: 0.1085
## F-statistic: 21.48 on 3 and 502 DF, p-value: 4.171e-13

##
## Call:
## lm(formula = crim ~ poly(black, 3))
```



```
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -13.096  -2.343  -2.128  -1.439   86.790
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)      3.6135      0.3536   10.218  <2e-16 ***
## poly(black, 3)1 -74.4312      7.9546   -9.357  <2e-16 ***
## poly(black, 3)2   5.9264      7.9546    0.745    0.457
## poly(black, 3)3  -4.8346      7.9546   -0.608    0.544
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 7.955 on 502 degrees of freedom
## Multiple R-squared:  0.1498, Adjusted R-squared:  0.1448
## F-statistic: 29.49 on 3 and 502 DF,  p-value: < 2.2e-16

##
## Call:
## lm(formula = crim ~ poly(lstat, 3))
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -15.234  -2.151  -0.486   0.066   83.353
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)      3.6135      0.3392   10.654  <2e-16 ***
## poly(lstat, 3)1  88.0697      7.6294   11.543  <2e-16 ***
## poly(lstat, 3)2  15.8882      7.6294    2.082   0.0378 *
## poly(lstat, 3)3 -11.5740      7.6294   -1.517   0.1299
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 7.629 on 502 degrees of freedom
## Multiple R-squared:  0.2179, Adjusted R-squared:  0.2133
## F-statistic: 46.63 on 3 and 502 DF,  p-value: < 2.2e-16

##
## Call:
## lm(formula = crim ~ poly(medv, 3))
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -24.427  -1.976  -0.437   0.439   73.655
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)      3.614      0.292   12.374  < 2e-16 ***
```

```
## poly(medv, 3)1 -75.058      6.569 -11.426 < 2e-16 ***
## poly(medv, 3)2  88.086      6.569  13.409 < 2e-16 ***
## poly(medv, 3)3 -48.033      6.569  -7.312 1.05e-12 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 6.569 on 502 degrees of freedom
## Multiple R-squared:  0.4202, Adjusted R-squared:  0.4167
## F-statistic: 121.3 on 3 and 502 DF,  p-value: < 2.2e-16
```

For predictors "indus", "nox", "age", "dis", "ptratio" and "medv", p-values suggest that these variable's coefficient are cubic fit. For predictors "zn", "rm", "rad", "tax" and "lstat", P-values suggest that these variables are fit up to 2nd order polynomial. For predictor black, p-values suggest that it is significant up to 1st order. Hence there is non-linear association between all of the predictors and the response except black?