

# MODULE II - FAI - EXERCISES

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1) We have to encode a knowledge in which

We have CONCEPTS and roles (Father, Mother...) and relations between them.

We need QUALIFIED NUMBER RESTRICTIONS (because in the description of the knowledge we have "at least 3", "at most 2" ...), therefore I think that ALCQ could be a good KRL in this situation.

2) In this point of the exercise we need to express which are the BASE (PRIMITIVE) CONCEPTS (those for which we don't express the definition in the TBOX)  
We have also to express BASE ROLES.

- So, to correctly encode our knowledge, we should assume and encode concept such as Male, female, Person.

(these concepts are primitive because we cannot describe the concept "female" for example and it's not in the scope of the exercise.)

These are important primitive concepts because allow us to DEFINE AND DIFFERENTIATE concepts in our knowledge such as Mother, Father etc...)

- BASE Roles:
  - hasChild
  - hasSister
  - hasBrother

- It could also be useful to define INVERSE RELATION between:
  - SisterOf and hasSister
  - brotherOf and hasBrother
  - childOf and hasChild.

- Therefore I suggest to use ALCQI as KRL.

### 3. Write the KB in the chosen KRL.

- We do not have the A-Box in our case because in the description of the knowledge there are not instances of the concepts.
- We define the TBox only.

TBOX: {

Father ≡ Male  $\sqcap \exists \text{hasChild}.\text{Person}$ ,

Mother ≡ Female  $\sqcap \exists \text{hasChild}.\text{Person}$ ,

Parent ≡ Father  $\sqcup$  Mother,

GrandMother ≡ Female  $\sqcap \exists \text{hasChild}.\text{Parent}$ ,

Grandfather ≡ Male  $\sqcap \exists \text{hasChild}.\text{Parent}$ ,

Aunt ≡ Female  $\sqcap (\exists \text{hasSister}.\text{Mother} \sqcup \exists \text{hasBrother}.\text{Father})$

Uncle ≡ Male  $\sqcap (\exists \text{hasSister}.\text{Mother} \sqcup \exists \text{hasBrother}.\text{Father})$

ChildOf ≡ inverse(hasChild),

Niece ≡ Female  $\sqcap (\exists \text{ChildOf}.\text{Parent} \sqcap$

(hasSister.Parent  $\sqcup$  hasBrother.Parent)),

Nephew ≡ Male  $\sqcap (\exists \text{ChildOf}.\text{Parent} \sqcap$

(hasSister.Parent  $\sqcup$  hasBrother.Parent))

Mother\_of\_AL\_3 ≡ Female  $\sqcap \geq 3 \text{hasChild}.\text{Male}$ ,

(sons)

moschi

Father\_of\_AM\_3\_D ≡ Male  $\sqcap \leq 3 \text{hasChild}.\text{Female}$

daughters

(femmine)

}

### 4) Queries to the KB.

Mother ≡ Parent?

GrandFather ≡ Male?

Father ≡ Male  
 Mother ≡ Female  
 GrandMother ≡ Female  
 Grandfather ≡ Male  
 Aunt ≡ Female  
 Uncle ≡ Male  
 ChildOf ≡ inverse(hasChild)  
 Niece ≡ Female  
 Nephew ≡ Male

la nonna è una  
 femmina che  
 fa almeno un figlio  
 il cui cuo è  
 "genitore".

Se non avesse  
 definito Parent avrei  
 scritto:

GrandMother ≡ Female  $\sqcap$   
 (hasChild.Mother  $\sqcup$   
 hasChild.Father)

la zia è una  
 femmina che  
 ha almeno una  
 sorella che è  
 maschio o  
 un fratello che  
 è padre

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1) For this knowledge we can use FOL<sub>I</sub>, since we do not need the additional features of DL or SC (situation calculus) as KRL

(we don't need to express complex roles or relations between concepts for which we need definition - we do not have a series of names such as Father, Mother... which need to be defined  $\Rightarrow$  NO DL)

- We do not have a situation that changes in time (non STATIC DOMAIN)  $\Rightarrow$  NO SC

- We have a series of sentences universally and existentially quantified  $\Rightarrow$  FOL

2) The exercise asks us to assume a set of individuals (invented by us)

- Let's assume a set of individuals for all the possible humans and animals:

Human (Carlo)	Dog (Fuffy)	+ WarmBlooded (Vipera)
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Human (Diego)	Animal (Vipera)	occur for those "there are animals that are not warmblooded"
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Human (Sofia)	Mammal (Macaco)
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Own(Carlo, Fuffy)	Own (Sofia, Vipera)
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- I think that before defining individuals (before) and axioms (later) we need to express a language. ("Assume and encode further elements...")

- human(x)

- Mammal(x)

- WarmBlooded(x) (+WarmBlooded(x))

- Dog(x)

- Own(x,y) binary predicate to express that x owns y.

- Animal(x)

3) Write an encoding of the KB using the chosen KRL.

$\forall x. (\text{Human}(x) \rightarrow \text{Mammal}(x))$

$\forall x. (\text{Mammal}(x) \rightarrow \text{WarmBlooded}(x))$

$\forall x. (\neg \text{Animal}(x) \wedge \text{Dog}(x) \rightarrow \text{Mammal}(x))$

$\exists x \exists y. (\text{Human}(x) \wedge \text{Animal}(y) \wedge \text{Own}(x,y))$

NON CI VA PROBLEMA PERCHÉ LA FRASE È SCRITTA SOTTO A QUANTIFICATORI

$\exists x (\text{Animal}(x) \wedge \neg \text{WarmBlooded}(x))$  la Vipera ad esempio

$\forall x (\text{Mammal}(x) \rightarrow \text{Animal}(x))$

SECONDO ESEMPIO  
NON SERVE AGGIUNGERE QUESTO TERMINE PERCHE SERVIRÀ CON GL INDIVIDUALS

$\exists x \exists y (\text{Human}(x) \wedge \text{Human}(y) \wedge (x \neq y) \wedge \text{Own}(x,y))$

Plus all the facts enumerated in point 2 plus the facts determining  
the language. (I think)

d) We can query our KB using for example Ridge and so we get:

? bagof((x,y), (Human(x), Animal(y)  $\wedge$  WarmBlood(y),  
Own(x,y)), S).

? findall(x, (Human(x), WarmBlood(y), WarmBlood(z)), S)

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1) we have a NON-STATIC DOMAIN therefore it's convenient to use SITUATION CALLEES which allows us to reason on actions and resulting states.

(we need to produce a sequence of actions that allows the robot to perform its objective  $\rightarrow$  a PLAN  $\rightarrow$  planning in situation calculus with situation varying over time).

2) A little cleaning robot moves in a room

the agent

goes from one position to another

ACTION

positions are encoded with coordinates

X, Y

↓

the STATES

represented by fluent "AT"

• A cat and a dog are also in the room and they do not move  $\rightarrow$  this condition is ATEMPORAL

↳ they are AT same position or they always stay there.

• Robot should clean the room (visit all the free squares) avoiding the cat and the dog.

↳ what we understand  $\rightarrow$  clean is an action

(but it could also be a state)

(squares Eleone - ved dogo -)

and so a fluent, if we consider that just going to a position, the robot automatically clean the space, so clean in that case is something that can change as an effect of the action go

(-> clean before going there, clean after going there)

• I have to encode the concept of free.

• Inner concept: non è scatto esattamente ma avvicinare due codicci che non sono solo tra colle adiacenti  $\rightarrow$  inserire un predicato "Adjacent" A temporal

# SOLUZIONE PROBLEMA

## • FLUENTS:

- $\text{At}(\text{Agent}, \text{cl}, \text{place}, s)$  #  $\text{cl}$  represents the list of cells to be cleaned  
# place is a pair constructed with coordinates  $(x,y)$

•  $\text{Free}(x) \rightarrow \neg \text{At}(\text{cat}, x) \wedge \neg \text{At}(\text{dog}, x)$

## • ATENTORIAL PREDICATES:

(What remains the same)

$\text{At}(\text{cat}, [x,y])$  (rimane sempre più dove è specificato nell'initial state)

$\text{At}(\text{dog}, [x,y])$

$\text{Adjacent}([x,y], [x',y'])$  (stessa cosa per le adiacenze)

$\text{Free}(x) \rightarrow \neg \text{At}(\text{cat}, x) \wedge \neg \text{At}(\text{dog}, x)$

## • INITIAL STATE:

$\text{At}(\text{robot}, [[1,2], [1,3], [2,1] \dots], [1,1], s_0)) \rightarrow \text{AND}$

$\downarrow$   
Initial position  
of the robot

$\text{At}(\text{cat}, [2,3]),$

$\text{At}(\text{dog}, [3,3]),$

$\text{Adjacent}([1,1], [1,2]),$

$\text{Adjacent}([2,1], [2,2]),$

$\text{Adjacent}([2,2], [3,1]),$

$\text{Adjacent}([2,2], [2,3]),$

$\text{Adjacent}([1,2], [2,2]),$

$\text{Adjacent}([1,2], [1,3]),$

$\text{Adjacent}([2,2], [2,3]),$

$\text{Adjacent}([2,2], [3,2]),$

$\text{Adjacent}([3,3], [2,3]),$

$\text{Adjacent}([3,3], [3,2]),$

✖ (sono free tutte le caselle dove non sono presenti gatto o cane, andrebbe scatto)  
(troppo lungo)

## ACTIONS:

- $\text{Go}(x, y)$  sarebbe  $\text{Go}(x^*, y, x^*, y')$  visto che abbiamo coordinate
- $\text{Clean}(x, \text{cl})$
- $\text{Finish}(x)$  to express that robot has finished in position  $x$ . ( $x, y$ )

## Possibility Axioms

$\text{Go}$ : posso andare in  $y$  se mi trovo in  $x$ , se  $x$  e  $y$  sono adiacenti  
 e se  $y$  non è occupato dal cane o dal gatto.

$\rightarrow$  2 POSSIBILITIES AXIOMS perché posso andare da  $x$  a  $y$   
 se  $x$  è adiacente a  $y$ , ma anche se  $y$  è adiacente a  $x$

$\text{At}(\text{robot}, \text{cl}, x, s) \wedge \text{Adjacent}(x, y) \wedge \text{Free}(y) \rightarrow \text{Poss}(\text{Go}(x, y), s)$

$\text{At}(\text{robot}, \text{cl}, x, s) \wedge \text{Adjacent}(y, x) \wedge \text{Free}(y) \rightarrow \text{Poss}(\text{Go}(x, y), s)$

$\text{At}(\text{robot}, \text{cl}, x, s) \wedge \underline{\text{member}}(x, \text{cl}) \rightarrow \text{Poss}(\text{Clean}(x, \text{cl}), s)$

↓

? questo predicato non è espresso  
 da nessuna parte, come viene  
 considerato? temporal o fluent?

$\text{At}(\text{robot}, [], x, s) \rightarrow \text{Poss}(\text{Finish}(x), s)$

## EFFECT AXIOMS:

$\text{Poss}(\text{Go}(x, y), s) \rightarrow \text{At}(\text{robot}, \text{cl}, y, \text{Result}(\text{Go}(x, y), s))$

$\text{Poss}(\text{Clean}(x, \text{cl}), s) \rightarrow \text{At}(\text{robot}, \underline{\text{remove}}(x, \text{cl}), x, \text{Result}(\text{Clean}(x, \text{cl}), s))$

↓  
 ? come member

$\text{Poss}(\text{Finish}(x), s) \rightarrow \text{At}(\text{robot}, \underline{\text{result}}, x, \text{Result}(\text{Finish}(x), s))$

↓

IO ANCHE DETTO:

$\text{At}(\text{robot}, [], x, \text{Result}(\text{Finish}(x), s))$

## GOAL:

$\exists \text{seq} \text{Finish}(x, \text{Result}(\text{seq}, s_0))$

E il frame problem? come viene risolto?

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1) To formalize the sentences we can use FOL because we do not need the expressivity of DL or SC.

Formalization:

- F1.  $\forall x. (\text{Student}(x) \rightarrow \text{Smart}(x))$
- F2.  $\exists x. \text{Student}(x)$
- F3.  $\exists x. (\text{Student}(x) \wedge \text{Smart}(x))$
- F4.  $\forall x. (\text{Student}(x) \rightarrow \exists y. (\text{Student}(y) \wedge \text{Loves}(x,y)))$
- F5.  $\forall x. (\text{Student}(x) \rightarrow \forall y. (\text{Student}(y) \wedge \text{Loves}(x,y) \wedge \neg(x=y)))$
- F6.  $\exists x. (\text{Student}(x) \wedge \forall y. (\text{Student}(y) \wedge \text{Loves}(x,y) \wedge \neg(x=y) \rightarrow \text{Loves}(y,x)))$
- F7.  $\text{Student}(\text{Mark})$
- F8.  $\text{Student}(\text{Paul})$
- F9.  $(\text{Takes}(\text{Mark}, \text{Analysis}) \wedge \text{Takes}(\text{Mark}, \text{Geometry})) \vee (\neg \text{Takes}(\text{Mark}, \text{Analysis}) \wedge \text{Takes}(\text{Mark}, \text{Geometry}))$
- F10.  $\text{Takes}(\text{Paul}, \text{Analysis}) \wedge \text{Takes}(\text{Paul}, \text{Geometry})$
- F11.  $\neg \text{Takes}(\text{Mark}, \text{Analysis})$
- F12.  $\neg \exists x. (\text{Student}(x) \wedge \text{Loves}(x, \text{Paul}))$

2) The KB is CONSISTENT, since it exists an interpretation that (the contrary) this.

Proof:

$D = \{ \text{Mark}, \text{USA} \}$  2 possible persons - DOMAIN -

Primed sentences

- By definition F7 and F8 are true in every interpretations (they are facts)
  - Moreover F9, F10, F11 are true in any interpretation.
- ▷ all ground variables

- By defining:

$$\text{Loves}(\text{Mark}, \text{Paul}) = \perp \quad (\text{false})$$

$$\text{Loves}(\text{Mark}, \text{Paul}) = \top$$

$$\text{Loves}(\text{USA}, \text{Paul}) = \perp$$

we get F12 = T

• from  $f_8 = T$  ( $\text{student}(\text{Mark})$ ) we get also  $f_2 = T$

• we make  $f_6 = T$  by defining:

$\text{loves}(\text{Paul}, \text{Mark})$

$\text{loves}(\text{Lisa}, \text{Mark})$

$\text{loves}(\text{Marg}, \text{Mark})$

• let's define

$\text{Smart}(\text{Mark})$

$\text{Smart}(\text{Paul})$

$\text{Smart}(\text{Lisa})$

$\text{Smart}(\text{Marg})$

and we get  $f_1 = T$  and consequently  $f_3 = T$

• By adding:

$\text{loves}(\text{Mark}, \text{Lisa})$

we get also  $f_4$  and  $f_5$  true

Therefore  $f_1 \wedge f_2 \wedge f_3 \wedge f_4 \wedge f_5 \wedge f_6 \wedge f_7 \wedge f_8 \wedge f_9 \wedge f_{10} \wedge f_{11} \wedge f_2 = T$

under the given interpretation and the KB is consistent.

3) I decide to use [Prolog] to write my query.

?-  $\text{takes}(\text{Paul}, x)$ .

$\alpha$ :  $\text{findall}(x, (\text{takes}(\text{Paul}, x)), S)$ .  $S$  will be the list containing all the exams taken by Paul.

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1) To formalize the sentences we can use FOL because we do not need the expressivity of DL or SC.

2) When we formalize with FOL we define a language (predicates that we will use) and a set of axioms using the specified language

LANGUAGE:

My Solution:

- carpool(Driver, Passenger)\* Professor Saurin:  
• Day(x) x is a day carpool(Driver, Passenger, Place, Day)
- Odd(x) x is odd (I don't specify "Even" predicate because I can express it as the negation of odd)
- hasDriverLicense(Person)
- Hill(Person)

\* I assume that the only possible carpooling can be done in order to go to work.

Formalization:

- $\forall x. \text{Day}(x) \wedge \neg \text{Odd}(x) \wedge \neg \text{hasDriverLicense}(\text{Clara}) \rightarrow \neg \text{carpool}(\text{Clara}, \text{Doris})$
- $\forall x. \text{Day}(x) \wedge \text{Odd}(x) \wedge \neg \text{hasDriverLicense}(\text{Doris}) \rightarrow \neg \text{carpool}(\text{Doris}, \text{Clara})$
- $\forall x. \text{Day}(x) \wedge \text{Hill}(\text{Doris}) \wedge \neg \text{hasDriverLicense}(\text{Clara}) \rightarrow \neg \text{carpool}(\text{Clara}, \text{Doris})$
- $\neg \text{hasDriverLicense}(\text{Clara})$
- $\neg \text{hasDriverLicense}(\text{Doris})$

We assume for each working day the facts:

- |                           |                           |
|---------------------------|---------------------------|
| $\text{odd}(\text{day1})$ | $\text{odd}(\text{day2})$ |
| $\text{odd}(\text{day3})$ | $\text{odd}(\text{day4})$ |
| $\text{odd}(\text{day5})$ |                           |
| $\text{odd}(\text{day6})$ |                           |

| Diverso da scrittore prof

Extension of KB:

- 3)  $\neg \text{odd}(\text{current\_day})$   
 $\neg \text{hasDriverLicense}(\text{Clara})$

If we extend the KB with  $\neg \text{hasDriverLicense}(\text{Clara})$ , it becomes inconsistent and it's not possible to prove that they are able to carpool to work.

To represent this extension a default logic is needed and an additional sentence should be added and formalized  $\rightarrow$