

Chapter 0

Introduction

1. We are trying to understand Mizar. So I am transcribing the source code into a literate program, following the order of compilation. Perhaps this “goes against the spirit” of literate programming, but it makes the most sense to understand what is going on for programmers.

We will begin with the “Parser module” (`base/parser.pas`), and all the dependencies needed to compile it. For clarity (or at least ease of reference) each “chapter” appearing in the table of contents corresponds to a different file.

We are studying Mizar’s source code as of Git commit `9e814a9568cfb44253d677e5209c360390fe6437` (dated 2023 October 11).

2. **Files are chapters.** We will organize the text by compiler dependencies. It makes sense to treat each file as a separate “chapter”. With the exception of this introductory chapter (“chapter 0”), all future chapters are called “File n ”.

Just as Knuth’s *T_EX: The Program* (Addison–Wesley, 1986) was organized into modules which are presented “bottom-up”, each module is discussed and programmed “top-down”, we shall try to do likewise. File $n + 1$ can only depend on code appearing in Files 1 through File n .

There are natural ways to “cluster” the discussion in each File, which motivates the “section” and “subsections”. Each section (*but not subsections!*) starts on a new page, written in sans serif bold prefixed with explicit an “Section”. Subsections are written in sans serif bold prefixed with an explicit “Subsection”, with vertical whitespace separating it. This chapter has two sections (one discussing the flow of Mizar, and the other enumerating observations and “to do” items).

3. Each chapter is written using numbered paragraphs, since we are using Donald Knuth’s **WEB** to write a literate program. References will be made to the paragraphs. Index entries give the paragraph numbers associated with each entry. And even though I just used the term “paragraph number”, they really group several paragraphs into a unit of writing.

Paragraphs are numbered *independently* of chapter, section, subsection. This is a quirk of **WEB**. This was how Mathematicians wrote texts back in Euler’s day. We will refer to a paragraph by writing (§ n) to refer to paragraph n . Again, this was the conventions used by Euler.

Each paragraph consists of three parts: the “text part” (informal prose written in English), the “macros part” (which introduces macros written in the **WEB** language), and the “code part” (which contains a pretty-printed snippet of PASCAL code). A paragraph may omit any of these parts but has at least one of them. Thus far, all our numbered paragraphs have consisted of “text parts” only. The “code part” can optionally have a name in angled brackets. If the name is missing, then it continues the previous chunk of code from the previous numbered paragraph.

4. The Mizar program is released under the GNU license. So let us place this license in one place early on. (This is an example of a numbered paragraph with a “named code part”.)

⟨GNU License 4⟩ ≡

{ This file is part of the Mizar system. Copyright (c) Association of Mizar Users. License terms: GNU General Public License Version 3 or any later version. }

This code is used in sections [34](#), [79](#), [88](#), [126](#), [150](#), [152](#), [166](#), [184](#), [197](#), [306](#), [591](#), [592](#), [614](#), [641](#), [681](#), [715](#), [774](#), [808](#), [846](#), [862](#), [997](#), [1340](#), [1346](#), and [1639](#).

5. Asides and opinions. Some paragraphs will be labeled as “asides” which are tangential remarks not directly relevant to understanding the code, but will enrich the reader’s life. [[The author will offer opinions about the design and implementation of Mizar in parenthetical sentences like this one, surrounded by double brackets.]] If the reader is unsatisfied by the arbitrary opinions of a random programmer, then they can disable the asides by redefining the `\Ithink` macro to have an empty body.

6. Aside: Typography of “Modern” Pascal. We will be following the typographical style as found in Niklaus Wirth’s *Algorithms + Data Structures = Programs* (Prentice–Hall, 1975) and Donald Knuth’s *T_EX: The Program* (Addison–Wesley, 1986). But there are a few typographical situations which requires thinking hard about, since “classical” PASCAL does not have *object* or inheritance (or *unit* modules).

First, we need to know that “modern PASCAL” differs from the PASCAL Knuth worked with, in several ways. Mizar uses “units” which are a module system introduced by UCSD PASCAL (*c.* 1977). We will need to format them for **WEAVE**.

Documentation and tutorials frequently compare **unit** to **program**, so we should probably typeset it as such. The big question is whether the **interface**, **implementation**, and **uses** keywords are **var**-like or **const**-like. I ultimately decided for the latter (since **var**-like typography would have them appear in the index underlined).

We will treat **implementation** typographically *as if* it were a **const** because the **end** will not be indented properly otherwise.

```
format unit ≡ program
format interface ≡ const
format implementation ≡ const
format uses ≡ const
```

7. Objects appear in Free PASCAL, and they behave like records. There are also **constructor** and **destructor** functions.

```
format object ≡ record
format constructor ≡ function
format destructor ≡ function
```

8. Primitive functions. We have several primitive functions which should be formatted especially. For example, **shr** is an infix operator like **mod** or **div**. It corresponds to bitwise shifting right.

```
format shr ≡ div
```

9. Cases. Following Knuth’s “T_EX: The Program” (§4), we will use **endcases** to pair with **case**. The “default case” will be **othercases** (because **else** gets too confusing).

```
define othercases ≡ others: { default for cases not listed explicitly }
define endcases ≡ end { follows the default case in an extended case statement }
format othercases ≡ else
format endcases ≡ end
```

10. Debugging. There are conditional compiler directives for debugging purposes. Importantly, these *must* be printed to the source code when we invoke **TANGLE**.

```
define mdebug ≡ @{@&$IFDEF MDEBUG@}
define end_mdebug ≡ @{@&$ENDIF@}
format mdebug ≡ begin
format end_mdebug ≡ end
```

11. Actually, it may be useful just to have helper macros.

```

define if_def(#)  $\equiv$  @{@&$IFDEF#@}
define if_not_def(#)  $\equiv$  @{@&$IFNDEF#@}
define else_if_def(#)  $\equiv$  @{@&$ELSEIF DEFINED(#}@}
define else_def  $\equiv$  @{@&$ELSE@}
define endif  $\equiv$  @{@&$ENDIF@}
define end_if  $\equiv$  endif
format if_def  $\equiv$  if
format if_not_def  $\equiv$  if
format else_if_def  $\equiv$  else
format else_def  $\equiv$  else
format endif  $\equiv$  end
format end_if  $\equiv$  end

```

12. **Toggling IO Checking.** Another compiler directive enables and disables IO checking

```

define disable_io_checking  $\equiv$  @{@&$I-@}
define enable_io_checking  $\equiv$  @{@&$I+@}
define without_io_checking(#)  $\equiv$  disable_io_checking; #; enable_io_checking

```

13. **Logging.** There appears to be a *CHReport* logger introduced in `kernel/prephan.pas`, but its type is defined in `kernel/req_info.pas`.

14. **References.** I have inline citations to the literature, but there’s some references worth explicitly drawing the reader’s attention to (which may or may not make it to an inline citation):

- (1) Andrzej Trybulec, “Some Features of the Mizar Language”, ESPRIT Workshop, Torino, 1993.
Eprint: mizar.uwb.edu.pl/project/trybulec93.pdf — §4 discusses grammatical aspects of Mizar
- (2) Freek Wiedijk, “Mizar’s Soft Type System”. In K. Schneider and J. Brandt, eds., *Theorem Proving in Higher Order Logics. TPHOLs 2007*, Springer, doi:10.1007/978-3-540-74591-4_28 (Eprint pdf).
- (3) Adam Grabowski, Artur Korniłowicz, and Adam Naumowicz’s “Mizar in a Nutshell”
(doi:10.6092/issn.1972-5787/1980)
- (4) Artur Korniłowicz’s “Registrations vs Redefinitions in Mizar” (in A. Kohlhase, P. Libbrecht, BR. Miller, A. Naumowicz, W. Neuper, P. Quaresma, F. Wm. Tompa, M. Suda (eds) *Joint Proc. FM4M, MathUI, and ThEdu*, 2016, pp.17–20, ceur-ws.org/Vol-1785/F5.pdf)
- (5) Artur Korniłowicz’s “On rewriting rules in Mizar” (*J. Autom. Reason.* **50** no.2 (2013) 203–210, doi:10.1007/s10817-012-9261-6)
- (6) Mario Carneiro, “Reimplementing Mizar in Rust”. Eprint [arXiv:2304.08391](https://arxiv.org/abs/2304.08391), see especially the first two sections for an overview of Mizar’s workflow. (The code is available at github.com/digama0/mizar-rs.)

I should also credit Wayne Sewell’s *Weaving a Program: Literate Programming in Web* (Van Nostrand Reinhold Computer, 1989) for discussing how to take a pre-existing PASCAL program and turn it into a WEB. Or, depending on the quality of writing in this literate program, it’s all his fault.

Section 0.1. MIZAR'S WORKFLOW

15. This section will give a brief overview of what Mizar “does” when we run it. The analogy to bear in mind is with a batch compiler: there’s parsing, some intermediate steps, then emits some output.

Just to give some rough estimates of where Mizar spends most of its time, there are four phases Mizar reports when checking an article:

- (1) Parser (transforms input into an abstract syntax tree, writes it to an XML file);
- (2) MSM (transforms the abstract syntax tree into an explicitly typed intermediate representation) — `base/first_identification.pas`, the *MSMAnalyzer* procedure; this will require transcribing `kernel/limits.pas` (which is mostly just a bunch of constant parameters);
- (3) Analyzer (performs type checking, tracks the goals, and other miscellaneous jobs) — the *Analyze* procedure in `kernel/analyzer.pas`; this requires transcribing kernel code (`lexicon.pas`, `inout.pas`, `iocorrel.pas`, `correl.pas`, `generato.pas`, `builtin.pas`, `justhan.pas`, `enums.pas`, `formats.pas`, `identify.pas`) and base code (`xmldict.pas`), approximately 19590 lines (16764 lines of code, the rest is whitespace and comments)
- (4) Checker (performs the proof checking for validity) — the *InferenceChecker* procedure in `kernel/checker.pas`. This requires transcribing kernel files (`checker.pas` `prechecker.pas` `equalizer.pas` `unifier.pas` `justhan.pas`), approximately 8191 lines of code.

Using numbers Mario Carneiro reported in his github repository, roughly 14/15 of Mizar’s runtime (as measured in CPU time) is spent on the Analyzer and Checker phases (among which, Mizar spends about 5 times longer in the Checker phase than the Analyzer phase). Parsing and MSM transforms the input into an intermediate representation used in the latter two phases. Mizar spends about 1/15 of its time here.

16. Accommodator. This will produce, among other outputs, the “.dct” file (and its XML counterpart, the “.dcx” file). The “.dct” file contains all the identifiers imported from other articles and reserved keywords for Mizar. The Tokeniser needs it to properly tokenise an article.

17. Parsing phase. We can look at `kernel/verfinit.pas` to find the parsing phase of the Mizar program is handled by the following lines of code:

```
InitPass(`ParserUU`); FileExam(EnvFileName + `.dct`);
InitScanning(MizFileName + ArticleExt, EnvFileName); InitWSMizarArticle; Parse;
gFormatsColl.StoreFormats(EnvFileName + `.frx`); gFormatsColl.Done; FinishScanning;
Write_WSMizArticle(gWSTextProper, EnvFileName + `.wsx`);
```

Our goal is to examine these functions, and understand what is going on. We know *Parse* is defined in `base/parse.pas`, it populates the *gWSTextProper* global variable using `base/parseraddition.pas`, and *Write_WSMizArticle* is defined in `base/wsmarticle.pas`. The *Parse* function continuously invokes *ReadToken* (§853).

This phase will be responsible for generating a “.frx” (formats XML) and a “.wsx” (weakly strict Mizar XML) file.

Subsection 0.1.1. Map of Mizar

18. It will be useful to provide a summary of the files, to give the reader an idea where to find various things. We offer the following grouping of files. We will enumerate them by the chapter wherein the file is discussed.

19. System-dependent code.

- (1) `base/mizenv.pas` provides functions for manipulating strings and file I/O
- (2) `base/pcmizver.pas` contains the major and minor version for Mizar, and data about the build
- (3) `base/mconsole.pas` provides common functions for printing messages to the console and parsing command line optional arguments
- (4) `base/errhan.pas` contains the *Position* type, functions for reporting errors, writing them in particular files
- (5) `base/info.pas` for debugging purposes, logging to a `.inf` file
- (6) `base/monitor.pas` code for signal processing, reports errors, and when calamity strikes exit Mizar
- (7) `base/mtime.pas` uniform framework for timing things
- (8) `base/mstate.pas` code for reset the current position in an article and marking the time

20. Infrastructure for the rest of Mizar’s object-oriented code.

- (9) `base/numbers.pas` contains code for arbitrary-precision integers, rational numbers, and rational complex numbers
- (10) `base/mobjects.pas` contains the common data structures used in Mizar, things like dynamic arrays and the *MObject* base class;

21. XML infrastructure.

- (11) `base/xml_dict.pas` contains only constant parameters and enumerated types
- (12) `base/librenv.pas` code for accessing the `pre1/` subdirectories of the current article and of `$MIZFILES/` — this is only here because it defines the *MizFiles* global variable which stores the full path of the `$MIZFILES/` environmental variable, and *MizFiles* is needed in `xml_inout.pas`; [This *MizFiles* global variable should be refactored out to an earlier unit, because `librenv.pas` seems out of place here;]
- (13) `base/xml_parser.pas` provides an abstract syntax tree for XML and parses XML
- (14) `base/xml_inout.pas` handles reading from and writing to XML files, plus escaping strings, etc.

22. Tokenisation and other “intermediate file management”.

- (15) `base/dicthan.pas` loading “.voc” files, and transform them into “.vct” and XML “.vcx” files
- (16) `base/scanner.pas` the Tokeniser and Scanner are implemented here (the naming is a little confusing, the *Scanner* class is the Tokeniser, and the *Tokeniser* class is an “abstract Tokeniser” operating on an arbitrary input stream accessed by an abstract *GetPhrase* method); also note, if we want to extend Mizar to support UTF-8 character encoding instead of ASCII, then this is the file we would modify;
- (17) `base/_formats.pas` contains the data structures for “formats” (basically a (Identifier, Number of arguments to left, Number of arguments to right) triple) used for parsing expressions;

23. Abstract syntax tree class hierarchies.

- (18) `base/syntax.pas` provides “abstract” classes *Subexpression* and *Expression* for expressions, *Item* and *Block* for statements; the actual subclasses used by the parser are in the `parseraddition.pas` file;
- (19) `base/mscanner.pas` provides a number of important global variables for the parser, “.prf” file management, as well as the *gScanner* global variable for the parser;
- (20) `base/abstract_syntax.pas` provides the abstract syntax tree for terms, types, attributes, formulas, and “within expressions”;
- (21) `base/wsmarticle.pas` “weakly strict Mizar” is the name for the initial internal representation of Mizar, which has its own class hierarchy here, as well as writing a “weakly strict Mizar” article to an XML file and reading back from an XML file into a “weakly strict Mizar” abstract syntax tree;

24. Parser “proper”.

- (22) `base/pragmas.pas` for parsing pragmas like “`::$P-`”, and global variables related to them;
- (23) `base/parseraddition.pas` for subclasses of the syntax tree class hierarchy from `syntax.pas`, used for constructing a “weakly strict Mizar” AST when parsing
- (24) `base/parser.pas` for parsing a token stream into an abstract syntax tree

Section 0.2. LOG OF TODOS, BUGS, IMPROVEMENTS

25. I have a number of observations from transcribing Mizar into `WEB`. They're the last thing I have included in the introductory chapter.

26. Possible improvements.

- (1) In quicksort, picking the pivot is done by $P \leftarrow (Low + High)/2$, but it should be done by $P \leftarrow Low + ((High - Low)/2)$ to avoid overflow.
- (2) Actually, quicksort should delegate work to a different sorting algorithm when there is less than 10 items in the list. Sedgewick pointed this out in his PhD thesis. (If quicksort *were* a culprit for slowness, we could even hardcode sort networks for small lists.)
- (3) We should also determine the pivot by looking at the median value of $P = (3 * Low + High)/4$, $P2 \leftarrow (Low + High)/2$, $P3 \leftarrow (Low + 3 * High)/4$. This will improve the performance of quicksort.
- (4) In §233, *GCD* could be optimized to avoid calculating $Mul(i, i)$ in every loop iteration.
- (5) In §455, *MStringList.ObjectOf* has duplicate code.
- (6) It seems that parsing Mizar text, emitting XML, and parsing XML seem to contain a lot of code which could be autogenerated from a grammar (a hypothetical “`.ebnf`” file). This would avoid duplicate work.

27. Possible bugs. I have been working through the source code with the mindset of, “How can I possibly break this?” This has led me to identify a number of situations where things can “go badly”. But they are not all bugs (some are impossible to occur).

- (1) In §401, *MSortedExtList.FindInterval* appears to assume that *MSortedExtList.Find* returns the left-most index.
- (2) In §422, *MSortedCollection.Search* may not return the correct index when there are duplicates. This is not terrible, since *IndexOf* corrects for this possibility.
- (3) In §654, I think *TXTStreamObj.Done* needs to close the associated file.
- (4) In §690, *TSymbol.Init* expects an *fInfinite* argument, but does not use it — shouldn’t it initialize *Infinite* \leftarrow *fInfinite*?
- (5) In §628, escaped quotation marks are not properly handled.
- (6) For *StreamObj* (§647), the constructors and destructors are not virtual which would impact *XMLOutStreamObj* (§660) — well, we just do duplicate work in *XMLOutStreamObj*’s constructors and destructors.
- (7) Shouldn’t *TokensCollection.InitTokens* (§721) invoke the inherited constructor?
- (8) Shouldn’t *MTokenObj.Init* (§729) invoke inherited constructors? At least to insulate itself from changes to any of its parent (or grandparent) classes?
- (9) The constructor *OutWSMizFileObj.OpenFileWithXSL* (§1162) expects the XML-stylesheet located at "file:///+*\$MIZFILES*+’/wsmiz.xml", but that file is not present in Mizar.
- (10) In *extItemObj.FinishFunctorPattern* (§1470), the default case does not add a new format to the *gFormatsColl* dictionary.
- (11) In *CreateArgs* (§1540) in *parseraddition.pas*, when *aBase* ≤ 0 , this will set *TermNbr* to a negative number.
- (12) In the *Subexpression* class, there is duplicate code (§1544) — the *CompleteAttributeArguments* and *FinishAttributeArguments* are identical, but only the latter is consistent with the naming conventions for the Parser. Or (probably more likely) I am misunderstanding the naming conventions?
- (13) In *CompleteArgument* (§1680), we should also test that *fParenthCnt* is positive, shouldn’t we?
- (14) The *CreateSubexpression* method (§1638), for extended expression objects, may result in a memory leak when *gSubexpPtr* \neq **nil** — that is to say, if *KillSubexpression* has not been invoked prior to *CreateSubexpression*.
- (15) Misnamed variable: *gIdentifyEqLociList* should be *gIdentifyEqLociList* (i.e., “identify” should be “identify” — with a ‘t’). (This typo has been corrected in the literate presentation of the code.)
- (16) As discussed in (§1433), there is a mismatch between the documentation and the Parser when it comes to parsing loci declarations in a definition block. The *syntax.txt* file is more restrictive than the Parser, and should be updated to reflect the Parser.
- (17) The *gSuchThat* global variable is never used anywhere (§1439)
- (18) In *ATTSubexpression* (§1862), in the **else** block when the conditional **if** *lAttrExp* \vee (*aExpKind* = *exAdjectiveCluster*) is executed, *aExpKind* = *exAdjectiveCluster* is never true (so there’s no need for it).

28. To do list. There are some things I should revisit, revise, and edit — specifically about this running commentary (*not* the Mizar source code).

- (1) [Missing transcription] I skipped over transcribing the *ItemName* and other constants from `wsmarticle.pas`, which I should probably include.
- (2) [Revise] The XML schema should use the `doc/mizar/xml/Mizar.rnc` schema snippets.
- (3) [Revise] Make an introduction to dynamic arrays as a data structure, just to standardize the terminology used. (Make sure I stick to the standardized terminology!) Including pictures may help...
- (4) [Revise] Review quicksort. I should prove that it works, too. (Has this been done in Mizar? `exchsort` seems to be the closest match.)
- (5) [Improve] Give a “big picture” summary of the architecture. For example, the most interesting routine in parsing Mizar, well, it’s all handled in *MTokenizer.SliceIt* (§739).
- (6) [Linting] Standardize the names of basic data types. PASCAL accepts *integer* as synonymous with *Integer*, but they give different index entries.
- (7) [Cosmetics] Check the typography is correct for the code
- (8) [Cosmetics] Create more `WEB` macros for conditional compilation
- (9) [Cosmetics] Would it help to include more UML class diagrams?
- (10) [Improve] It may be useful to use UML State diagrams to explain the parser — or it may be a huge distraction?

29. Formatting types. This is still a finicky aspect of `WEB`. Strings are a type in Free PASCAL, like *Boolean*.

Looking at Wirth’s book, he typesets a type in *italics* and lowercase — so we have *boolean* and not **boolean** or *Boolean* (or **Boolean** or **boolean** or...). Knuth’s “`TEX`: the program” follows this convention (using *integer*, *boolean*, *char*, etc.).

30. Using Twill (or not). Knuth invented Twill as a “hack” atop `WEAVE` to include “mini-indices” every couple pages. The problem I have with Twill is that it does not adequately index local variables (in the sense that: Knuth’s `TEX` is a giant monolithic program, and any **var** appearing in it is almost certainly a global variable — hence it makes sense to index *all* variables, since they are almost certainly global).

I *want* to use Twill, but it is designed specifically *for* Knuth. Consequently it is not terribly useful for our purposes. We would have to tailor it quite heavily, and I don’t have the energy or patience to do so.

31. Caution: Knuth takes advantage of `WEB` to use `snake_case` when naming things instead of Pascal’s idiomatic `PascalCase`. This probably greatly improves the readability of the code. We should probably think hard about using it.

When `WEAVE` extracts the PASCAL code, it will remove all underscores from the identifiers and capitalize all letters. So instead of “*screaming_run_on_case*” (which appears in the PDF), we will instead obtain “`SCREAMINGRUNONCASE`”, which... yeah, that’s a hot mess.

Section 0.3. REVIEW OF PASCAL

32. Following Wirth's *Systematic Programming: An Introduction* (Prentice-Hall, 1973; viz., Chapter 7), we can offer the following axiomatic semantics for most of PASCAL's statements.

Assignment statements:

$$\frac{}{\{P[w/v]\} v \leftarrow w \{P\}}$$

Compound statements:

$$\frac{\frac{\{P\} S_1 \{Q\} \quad \{Q\} S_2 \{R\}}{\{P\} S_1; S_2 \{R\}}}{\{P\} S_1; S_2 \{R\}}$$

Conditional statements:

$$\frac{\frac{\{P \wedge B\} S_1 \{Q\} \quad \{P \wedge \neg B\} S_2 \{Q\}}{\{P\} \text{ if } B \text{ then } S_1 \text{ else } S_2 \{Q\}}}{\{P\} \text{ if } B \text{ then } S_1 \text{ else } S_2 \{Q\}}$$

Simpler conditional statements:

$$\frac{\frac{\{P \wedge B\} S \{Q\} \quad \{P \wedge \neg B\} \Rightarrow \{Q\}}{\{P\} \text{ if } B \text{ then } S \{Q\}}}{\{P\} \text{ if } B \text{ then } S \{Q\}}$$

While statements:

$$\frac{\{P \wedge B\} S \{P\}}{\{P\} \text{ while } B \text{ do } S \{P \wedge \neg B\}}$$

Repeat statements:

$$\frac{\frac{\{P\} S \{Q\} \quad \{Q \wedge \neg B\} S \{Q\}}{\{P\} \text{ repeat } S \text{ until } B \{Q \wedge B\}}}{\{P\} \text{ repeat } S \text{ until } B \{Q \wedge B\}}$$

Selective statement (and $i = L_k$ for some k):

$$\frac{\{P \wedge (i = L_k)\} S_k \{Q\} \text{ for all } k = 1, \dots, n}{\{P\} \text{ case } i \text{ of} \\ L_1: S_1; \\ L_2: S_2; \\ \vdots \\ L_n: S_n; \\ \text{end; } \{Q\}}$$

When there is no k such that $i = L_k$, the **case** statement is the same as evaluating i .

We can weaken the precondition:

$$\frac{P_1 \Rightarrow P_2, \quad \{P_2\} S \{Q\}}{\{P_1\} S \{Q\}}$$

We can strengthen the postcondition (Equation (11.16), page 85, of Wirth's book):

$$\frac{Q_2 \Rightarrow Q_1, \quad \{P\} S \{Q_2\}}{\{P\} S \{Q_1\}}$$

These rules are justified as *a priori* valid in Chapter 5 of Wirth.

For-loops may be derived as:

$$\frac{\frac{\{ (V = a) \wedge P \} S \{ Q(a) \} \quad \{ Q(pred(x)) \} S \{ Q(x) \} \text{ for all } a < x \leq b}{\{ (a \leq b) \wedge P \} \text{ for } V \leftarrow a \text{ to } b \text{ do } S \{ Q(b) \}}}{\{ (a > b) \wedge P \} \text{ for } V \leftarrow a \text{ to } b \text{ do } S \{ P \}}$$

33. The *exit* procedure may be invoked in a procedure or function, and it terminates the function or procedure. It roughly corresponds to C's **return** statement.

File 1

Mizar environment

34. We want to abstract away all the system dependent code, and provide a set of common functions Mizar will use to interact with the file system. This will include some helper functions for trimming whitespace from a String.

```

< mizenv.pas 34 > ≡
  < GNU License 4 >
unit mizenv;
  interface
    < interface for mizenv.pas 35 >
  implementation
    < Modules used by mizenv.pas 36 >
    < implementation of mizenv.pas 37 >
end .

```

35. There are a few common “global variables” used by the rest of Mizar. Specifically, Mizar will be processing a file (“article”). The file may be an absolute path (e.g., /path/to/article.miz), a relative path (../article.miz), or just the filename (article.miz). In any event, we will want to refer to the filename (article.miz) as well as what Mizar calls the “article ID” (in this case, “ARTICLE” — the filename without the file extension, transformed to all capital letters).

Modern programmers may find discomfort working with global variables (and for good reason!). We remind such readers that it was common practice, until very recently, for compilers and interpreters to use global variables to describe the state of the compiler (or interpreter). We will freely refer to these global variables as “state variables”, since that captures the role they play more accurately.

```

< interface for mizenv.pas 35 > ≡
var MizFileName: string; { the article “article.miz” }
    ArticleName: string; { the “article” without the “.miz” }
    ArticleID: string; { “ARTICLE” in screaming snake case }
    ArticleExt: string; { “.miz” from the MizFileName }
    EnvFileName: string; { the file name given to Mizar as a command-line argument }
procedure SetStringLength(var aString : string; aLength : integer);

```

See also sections 38, 40, 42, 46, 48, 50, 52, 54, 56, 58, 60, 62, and 64.

This code is used in section 34.

36. The implementation begins with various “uses”. Depending on the PASCAL compiler and operating system, different libraries need to be loaded.

```

< Modules used by mizenv.pas 36 > ≡
uses { compiler dependent imports }
    if_def (DELPHI) IOUtils, SysUtils, windows, endif
    if_def (FPC) dos, SysUtils, endif
    mconsole; { the only Mizar module mizenv.pas uses }

```

This code is used in section 34.

37. As far as setting the String length, this is a straightforward implementation. When the desired $aLength$ is less than the actual length of $aString$, simply delete all characters after $aLength$.

Otherwise, $aString$ has fewer characters than desired, so we pad it on the right with however many spaces until the String is as long as $aLength$.

(implementation of mizenv.pas 37) \equiv

```
procedure SetStringLength(var  $aString$  : string;  $aLength$  : integer);
  var  $I, L$ : integer;
  begin  $L \leftarrow \text{length}(aString)$ ;
  if  $aLength \leq L$  then Delete( $aString$ ,  $aLength + 1$ ,  $L - aLength$ )
  else for  $I \leftarrow 1$  to  $aLength - L$  do  $aString \leftarrow aString + \text{' '}$ ;
  end;
```

See also sections 39, 41, 43, 47, 49, 51, 53, 55, 57, 59, 61, 63, 65, 69, 71, 72, 73, 74, 76, and 77.

This code is used in section 34.

38. Trimming whitespace. Trimming the left String will repeatedly delete any leading whitespace, until the String is empty or has no leading whitespace.

Similarly, trimming the right String will repeatedly delete the *last* character until it is no longer whitespace (or until the String becomes empty).

Remember, PASCAL is call-by-value, so the string arguments are copied when these functions are invoked. We are mutating the copy of the argument, and returning them to the user.

(interface for mizenv.pas 35) \equiv

```
function TrimStringLeft( $aString$  : string): string;
function TrimStringRight( $aString$  : string): string;
```

39. (implementation of mizenv.pas 37) \equiv

```
function TrimStringLeft( $aString$  : string): string;
  begin while ( $\text{length}(aString) > 0$ )  $\wedge$  ( $aString[1] = \text{' '}$ ) do Delete( $aString$ , 1, 1);
  TrimStringLeft  $\leftarrow aString$ ;
  end;

function TrimStringRight( $aString$  : string): string;
  begin while ( $\text{length}(aString) > 0$ )  $\wedge$  ( $aString[\text{length}(aString)] = \text{' '}$ ) do
    Delete( $aString$ ,  $\text{length}(aString)$ , 1);
  TrimStringRight  $\leftarrow aString$ ;
  end;
```

40. Trimming a String amounts to trimming it on the left and right.

(interface for mizenv.pas 35) \equiv

```
function TrimString(const  $aString$ : string): string;
```

41. (implementation of mizenv.pas 37) \equiv

```
function TrimString(const  $aString$ : string): string;
  begin TrimString  $\leftarrow$  TrimStringRight(TrimStringLeft( $aString$ ));
  end;
```

42. Uppercase and lowercase strings. We have a few more String manipulation functions for changing case, and turning an integer into a String.

(interface for mizenv.pas 35) \equiv

```
function UpperCase(const  $aStr$ : string): string;
function MizLoCase( $aChar$  : char): char;
function LowerCase(const  $aStr$ : string): string;
function IntToStr( $aInt$  : integer): string;
```

43. Now, uppercase strings are obtained by uppercasing each character.

⟨implementation of mizenv.pas 37⟩ +≡

```
function UpperCase(const aStr: string): string;
  var k: integer; { index ranging over aStr }
      lStr: string; { the uppercased String being built and returned }
  begin lStr ← aStr;
  for k ← 1 to length(aStr) do lStr[k] ← UpCase(aStr[k]);
  UpperCase ← lStr;
end;
```

44. Lowercasing a String can be done by iteratively replacing each character with its lowercase version. This “lowercase a single character” function is precisely *MizLoCase*.

If the reader wished for a UTF-8 version of Mizar, then this function would require thinking very hard about how to generalize.

```
function MizLoCase(aChar : char): char;
  begin if aChar ∈ [‘A’ .. ‘Z’] then MizLoCase ← Chr(Ord(‘a’) + Ord(aChar) − Ord(‘A’))
  else MizLoCase ← aChar;
  end;
```

```
function LowerCase(const aStr: string): string;
  var i: integer; { index ranging over aStr’s length }
      lStr: String; { result being built up }
  begin lStr ← aStr;
  for i ← 1 to length(aStr) do lStr[i] ← MizLoCase(aStr[i]);
  LowerCase ← lStr;
end;
```

45. We also want a *function* to convert an integer to a String. PASCAL provides us with a *procedure*.

```
function IntToStr(aInt : integer): string;
  var lStr: string;
  begin Str(aInt, lStr); IntToStr ← lStr;
end;
```

46. **File name manipulation.** We will want to test if a file exists, or split a path (represented as a String) into a directory and a filename.

Testing if a file exists uses the Free Pascal’s primitive *FileExists* function.

Similarly, *EraseFile* is just relying on Free Pascal’s *SysUtils.DeleteFile* function.

⟨interface for mizenv.pas 35⟩ +≡

```
function MFileExists(const aFileName: string): Boolean;
procedure EraseFile(const aFileName: string);
```

47. ⟨implementation of mizenv.pas 37⟩ +≡

```
function MFileExists(const aFileName: String): Boolean;
  begin MFileExists ← FileExists(aFileName); end;
procedure EraseFile(const aFileName: String);
  begin SysUtils.DeleteFile(aFileName); end;
```

48. We will destructively rename a file. If a file with the name already exists, we delete it. CAUTION: This function is not used anywhere, and it appears to be buggy (the file is deleted and then renamed, which begs the question—why is it deleted?).

```
<interface for mizenv.pas 35> +≡
procedure RenameFile(const aName1, aName2: string);
```

```
49. <implementation of mizenv.pas 37> +≡
procedure RenameFile(const aName1, aName2: String); { unused }
  begin if MFileExists(aName1) then EraseFile(aName2);
    SysUtils.RenameFile(aName1, aName2);
  end;
```

50. Again, relying on Free Pascal's *FileAge* function, which returns the modification time of the file. CAUTION: this will return a signed 32-bit integer, which will run into problems after 03:14:07 UTC on 19 January 2038 because that's $2^{31} - 1$ seconds since the UNIX epoch.

```
<interface for mizenv.pas 35> +≡
function GetFileTime(aFileName : string): Longint;
```

```
51. <implementation of mizenv.pas 37> +≡
function GetFileTime(aFileName : String): Longint;
  begin GetFileTime ← FileAge(aFileName); end;
```

52. Split a file name into components, namely (1) the directory, (2) the file name, (3) its extension. For example, */path/to/my/file.exe* will be split into */path/to/my/*, *file*, and *exe*.

This implementation depends on the compiler used (Delphi or Free Pascal).

```
<interface for mizenv.pas 35> +≡
procedure SplitFileName (const aFileName: string;
  var aDir, aName, aExt: string ) ;
```

```
53. <implementation of mizenv.pas 37> +≡
procedure SplitFileName (const aFileName: string; { input }
  var aDir, aName, aExt: string ) ; { output }

  begin
    if_def (FPC)
      aDir ← SysUtils.ExtractFilePath(aFileName);
      aName ← SysUtils.ExtractFileName(aFileName);
      aExt ← SysUtils.ExtractFileExt(aFileName);
    endif
    if_def (DELPHI)
      aDir ← TPath.GetDirectoryName(aFileName);
      aName ← TPath.GetFileName(aFileName);
      aExt ← TPath.GetExtension(aFileName);
    endif
  end ;
```

54. “Truncating a directory” means “throw away the directory part of the path” so we end up with just a filename and the file extension.

```
<interface for mizenv.pas 35> +≡
function TruncDir(const aFileName: string): string;
```

55. \langle implementation of mizenv.pas 37 $\rangle + \equiv$

```
function TruncDir(const aFileName: string): string;
  var Dir, lName, Ext: string;
  begin SplitFileName(aFileName, Dir, lName, Ext); TruncDir  $\leftarrow$  lName + Ext;
  end;
```

56. “Truncating the extension” means throwing away the extension part of a path.

\langle interface for mizenv.pas 35 $\rangle + \equiv$

```
function TruncExt(const aFileName: string): string;
```

57. \langle implementation of mizenv.pas 37 $\rangle + \equiv$

```
function TruncExt(const aFileName: string): string;
  var Dir, lName, Ext: string;
  begin SplitFileName(aFileName, Dir, lName, Ext); TruncExt  $\leftarrow$  Dir + lName;
  end;
```

58. Extracting the file directory will return *just* the directory part of a path.

\langle interface for mizenv.pas 35 $\rangle + \equiv$

```
function ExtractFileDir(const aFileName: string): string;
```

59. \langle implementation of mizenv.pas 37 $\rangle + \equiv$

```
function ExtractFileDir(const aFileName: string): string;
  var Dir, lName, Ext: string;
  begin SplitFileName(aFileName, Dir, lName, Ext); ExtractFileDir  $\leftarrow$  Dir;
  end;
```

60. Extracting the file name will throw away both the directory and extension. For example, extracting the file name from the path “/path/to/file.ext” gives us “file”. Extracting the file extension from the same path gives us “.ext”.

\langle interface for mizenv.pas 35 $\rangle + \equiv$

```
function ExtractFileName(const aFileName: string): string;
```

```
function ExtractFileExt(const aFileName: string): string;
```

61. \langle implementation of mizenv.pas 37 $\rangle + \equiv$

```
function ExtractFileName(const aFileName: string): string;
  var Dir, lName, Ext: string;
  begin SplitFileName(aFileName, Dir, lName, Ext); ExtractFileName  $\leftarrow$  lName;
  end;
```

```
function ExtractFileExt(const aFileName: string): string;
```

```
  var Dir, lName, Ext: string;
```

```
  begin SplitFileName(aFileName, Dir, lName, Ext); ExtractFileExt  $\leftarrow$  Ext;
```

```
  end;
```

62. Changing a file name’s extension. See:

freepascal.org/docs-html/rtl/sysutils/changefileext.html

Note this does not actually change the filename in the file system, it just changes it *as a string*.

\langle interface for mizenv.pas 35 $\rangle + \equiv$

```
function ChangeFileExt(const aFileName, aFileExt: string): string;
```


63. \langle implementation of mizenv.pas 37 $\rangle + \equiv$
function *ChangeFileExt*(**const** *aFileName*, *aFileExt*: *string*): *string*;
begin *ChangeFileExt* \leftarrow *SysUtils.ChangeFileExt*(*aFileName*, *aFileExt*); **end**;

64. Environment variables. Getting an environment variable. The reader wishing to learn more about what POSIX says about environmental variables may consult the POSIX standard, Volume 1 Chapter 8:

pubs.opengroup.org/onlinepubs/9799919799/basedefs/V1_chap08.html

The Free PASCAL compiler handles this situation far friendlier than Delphi.

\langle interface for mizenv.pas 35 $\rangle + \equiv$
function *GetEnvStr*(*aEnvName* : *string*): *string*;

65. \langle implementation of mizenv.pas 37 $\rangle + \equiv$
function *GetEnvStr*(*aEnvName* : *string*): *string*;
if_def (*FPC*)
begin *GetEnvStr* \leftarrow *GetEnv*(*aEnvname*); **end**;
endif
if_def (*DELPHI*) \langle Get environment variable, Delphi-compatible mode 66 \rangle
endif

66. The Delphi-compatible version of obtaining an environment variable is rather involved: copy the string, make it null terminated, look up the value.

\langle Get environment variable, Delphi-compatible mode 66 $\rangle \equiv$
const *cchBuffer* = 255;
var *lName*, *lpszTempPath*: **array** [0 .. *cchBuffer*] **of** *char*;
i: *integer*; *lStr*: *string*;
begin \langle Copy the variable name as a null-terminated string 67 \rangle ;
if *GetEnvironmentVariable*(*lName*, *lpszTempPath*, *cchBuffer*) > 0 **then**
begin \langle Copy environment variable's value into *lStr* until we find null character 68 \rangle ;
end;
GetEnvStr \leftarrow *lStr*;
end;

This code is used in section 65.

67. \langle Copy the variable name as a null-terminated string 67 $\rangle \equiv$
lStr \leftarrow '';
for *i* \leftarrow 1 **to** *length*(*aEnvname*) **do** *lName*[*i* - 1] \leftarrow *aEnvname*[*i*];
lName[*length*(*aEnvname*)] \leftarrow #0

This code is used in section 66.

68. \langle Copy environment variable's value into *lStr* until we find null character 68 $\rangle \equiv$
for *i* \leftarrow 0 **to** *cchBuffer* **do**
begin **if** *lpszTempPath*[*i*] = #0 **then** *break*;
lStr \leftarrow *lStr* + *lpszTempPath*[*i*];
end

This code is used in section 66.

69. Common printing routines. Examining a file amounts to testing if we can open the file. We close the file after opening it (because we don't want to actually want to do anything with it).

We should tweak how WEB formats a file to make it resemble the other types, rather than leave it as a “type operator” like **array** (which is the default due to Knuth).

format *file* \equiv *integer* ;

(implementation of mizenv.pas 37) \equiv

```
procedure FileExam(const aFileName: string);
var Source: file; { the file named aFileName }
    I: byte; { IOResult from trying to open the file }
begin if aFileName = `` then (Halt: we can't open the file 70);
    FileMode  $\leftarrow$  0; Assign(Source, aFileName); without_io_checking(Reset(Source)); I  $\leftarrow$  IOResult;
if I  $\neq$  0 then DrawIOResult(aFileName, I); { (§121) }
    close(Source); FileMode  $\leftarrow$  2;
end;
```

70. (Halt: we can't open the file 70) \equiv

```
begin DrawMessage(`Can't open ` + aFileName + `.miz`, ``); { (§117) } halt(1);
end
```

This code is used in section 69.

71. The user provides a file to Mizar as the command line argument. This typically looks like a relative path “**tex/article**” without any file extension. Before even trying to open “**tex/article.miz**”, or any of the related autogenerated intermediate files, we should test the file exists.

This procedure will notify the user if the file does not exist, otherwise it is silent.

Again, *DrawMessage* comes from *mconsole.pas* (§117).

(implementation of mizenv.pas 37) \equiv

```
procedure EnvFileExam(const aFileExt: string);
begin if  $\neg$  MFileExists(EnvFileName + aFileExt) then
    begin DrawMessage(`Can't open ` + EnvFileName + aFileExt + `.`, ``); Halt(1);
    end;
end;
```

72. This function isn't used anywhere in Mizar. It's also misnamed: we are not “getting” the file name, we are *updating* the file extension if the file lacks one. A better name might be “populate missing file extension”. Further, this does not test if the *Nr* command line argument is actually a file name or not, which is a possible source of bugs.

Remember, the *ParamCount* is PASCAL's way of counting the command-line parameters passed to the program.

(implementation of mizenv.pas 37) \equiv

```
procedure GetFileName(ParamNr : byte; DefaultExt : string; var aFileName : string);
var lFileExt: string;
begin if ParamNr  $\leq$  ParamCount then
    begin aFileName  $\leftarrow$  ParamStr(ParamNr); lFileExt  $\leftarrow$  ExtractFileExt(aFileName);
    if lFileExt = `` then aFileName  $\leftarrow$  ChangeFileExt(aFileName, DefaultExt);
    exit
    end;
    aFileName  $\leftarrow$  ``;
end;
```

73. This procedure will take the *Nr* command line argument. If it lacks a file extension, then it will append the *DefaultExt* to it. At the end, this will populate *aFileName* and *aFileExt* based on the command line. It's only used in the *GetMizFileName* procedure, and nowhere else in Mizar.

The *ParamStr(Nr)* returns the Nr^{th} parameter as a String (it's a PASCAL primitive).

⟨implementation of *mizenv.pas* 37⟩ +≡

```
procedure GetFileExtName(Nr : byte; DefaultExt : string; var aFileName : string; var aFileExt : string);
begin if Nr ≤ ParamCount then
  begin aFileName ← ParamStr(Nr); aFileExt ← ExtractFileExt(aFileName);
  if aFileExt = '' then aFileExt ← DefaultExt
  else aFileName ← ChangeFileExt(aFileName, '');
  exit
  end;
aFileName ← ''; aFileExt ← '';
end;
```

74. Populate the state variables using the command-line arguments. We need to find the first command-line argument which resembles a Mizar article name. Note that Mizar articles have several files associated with it (the article's contents in a *.miz* file, the vocabulary in a *.voc* file, and XML related intermediate representation in *.xml* files, as well as *.evl* files).

Command line flags prefixed with a dash ("-") will not be interpreted as the name of a Mizar article.

If there are multiple articles passed to Mizar as command-line arguments, then this function finds the first one (and uses it to populate the state variables).

A possible bug: if there are multiple files passed to Mizar and the first file passed is not a ".miz" file, then Mizar will halt as a failure instead of continuing looking for the needle in the haystack.

⟨implementation of *mizenv.pas* 37⟩ +≡

```
procedure GetMizFileName(aFileExt : String);
var i : integer;
begin MizFileName ← ''; ArticleName ← ''; ArticleExt ← ''; EnvFileName ← '';
for i ← 1 to ParamCount do
  if ParamStr(i)[1] ≠ '-' then
    begin MizFileName ← ParamStr(i); GetFileExtName(i, aFileExt, MizFileName, ArticleExt);
    ArticleName ← ExtractFileName(MizFileName); ArticleID ← UpperCase(ArticleName);
    if ¬IsMMLIdentifier(ArticleName) then ⟨Halt: invalid article name 75⟩;
    EnvFileName ← MizFileName; exit;
    end;
end;
```

75. ⟨Halt: invalid article name 75⟩ ≡

```
begin DrawMessage('Only letters, numbers and _ allowed in Mizar file names', ''); halt(1);
end
```

This code is used in section 74.

76. We will provide a standard way to populate the global variables.

⟨implementation of *mizenv.pas* 37⟩ +≡

```
procedure GetArticleName;
begin GetMizFileName('.miz');
end;
```

$$\langle \text{implementation of mizenv.pas } 37 \rangle + \equiv$$

78. The valid characters which can appear in a Mizar article name (an “MML Identifier”) are uppercase Latin letters (A-Z), lowercase Latin letters (a-z), decimal digits (0-9), and underscores (_).

[illegible]

File 2

PC Mizar Version

79. This is used to track the version of Mizar.

```

< pcmizver.pas 79 > ≡
  < GNU License 4 >
unit pcmizver;
interface
  const < Constants for pcmizver.pas 80 >
    < Public functions for pcmizver.pas 83 >
implementation
  < Implementation for pcmizver.pas 84 >
end .

```

80. Note the slight variant of terminology compared to semantic versioning “Major.Minor.Patch”, Mizar uses “Release.Version.Variant”. This appears to be just a minor difference in vocabulary.

```

< Constants for pcmizver.pas 80 > ≡
  PCMizarReleaseNbr = 8;
  PCMizarVersionNbr = 1;
  PCMizarVariantNbr = 14;

```

See also sections 81 and 82.

This code is used in section 79.

81. The current year could probably be determined from the PASCAL system utilities, but it is hardcoded to 2025. The *CurrentYear* is only used in one procedure in this module, so we could easily replace it with (the possibly non-portable) *FormatDateTime*(‘YYYY’, *Now*).

```

< Constants for pcmizver.pas 80 > +≡
  CurrentYear = 2025;

```

82. The directory separator for the file system supports Windows and UNIX-like file systems. So Classic macOS and QNX users would have to request this changed.

Note: it might be wiser, for Free PASCAL users, to use the *DirectorySeparator* constant from the *system* unit.

```

< Constants for pcmizver.pas 80 > +≡
  @{@&$IFDEF WIN32@}DirSeparator = ‘\’;
  @{@&$ELSE@}DirSeparator = ‘/’;
  @{@&$ENDIF@}

```

83. There are only four functions provided by this module.

⟨Public functions for `pcmizver.pas` 83⟩ ≡

```
function PCMizarVersionStr: string;
function VersionStr: string;
function PlatformNameStr: string;
function Copyright: string;
```

This code is used in section 79.

84. Their implementation is relatively straightforward: just print the appropriate constants to the screen.

⟨Implementation for `pcmizver.pas` 84⟩ ≡

```
function Copyright: string;
  var s: string;
  begin Str(CurrentYear, s);
  Copyright ← ‘Copyright_␣(c)_1990-’ + s + ‘_␣Association_␣of_␣Mizar_␣Users’;
  end;
```

See also sections 85, 86, and 87.

This code is used in section 79.

85. ⟨Implementation for `pcmizver.pas` 84⟩ +≡

```
function VersionStr: string;
  var lRel, lVer, lVar: string[2]; lStr: string;
  begin Str(PCMizarReleaseNbr, lRel); Str(PCMizarVersionNbr, lVer); Str(PCMizarVariantNbr, lVar);
  if length(lVar) = 1 then lVar ← ‘0’ + lVar;
  @{{&$IFDEF VERALPHA@}}lStr ← ‘-alpha’;
  @{{&$ELSE@}}lStr ← ‘’;
  @{{&$ENDIF@}}
  VersionStr ← lRel + ‘.’ + lVer + ‘.’ + lVar + lStr;
  end;
```

86. There are a number of platforms supported, a surprisingly large number. If we were to support more platforms (other BSDs, BeOS, GNU Hurd, etc.), then we would need to update this function. To see what platforms are predefined for FreePascal, consult:

- https://wiki.freepascal.org/Platform_defines

Ostensibly, we could extend the platform name string to display “generic UNIX” (and even “generic BSD”), as well as “generic Windows”.

⟨Implementation for `pcmizver.pas` 84⟩ +≡

```
function PlatformNameStr: string;
  var lStr: string;
  begin lStr ← ‘’;
  if_def (WIN32)lStr ← lStr + ‘Win32’; end_if
  if_def (LINUX)lStr ← lStr + ‘Linux’; end_if
  if_def (SOLARIS)lStr ← lStr + ‘Solaris’; end_if
  if_def (FREEBSD)lStr ← lStr + ‘FreeBSD’; end_if
  if_def (DARWIN)lStr ← lStr + ‘Darwin’; end_if
  if_def (FPC)lStr ← lStr + ‘/FPC’; end_if
  if_def (DELPHI)lStr ← lStr + ‘/Delphi’; end_if
  PlatformNameStr ← lStr;
  end ;
```

87. The last function in the `pcmizver.pas` file provides a string for the Mizar version.

⟨Implementation for `pcmizver.pas` 84⟩ +≡

```
function PCMizarVersionStr: string;  
  begin PCMizarVersionStr ← 'Mizar_Ver.' + VersionStr;  
  end;
```

File 3

Mizar Console

88. The Mizar Console unit is used for interacting with the command line. Specifically, this module will be used for printing error messages, reporting progress, and parsing command-line arguments for configuration options.

```

⟨ mconsole.pas 88 ⟩ ≡
  ⟨ GNU License 4 ⟩
unit mconsole;
  interface ⟨ Report results to command line 107 ⟩
    ⟨ Constants for common error messages reported to console 123 ⟩
    ⟨ Interface for accommodator command line options 91 ⟩
    ⟨ Interface for MakeEnv command line options 101 ⟩
    ⟨ Interface for transfer-specific command line options 105 ⟩
    ⟨ Interface for other command line options 92 ⟩
  implementation
    ⟨ Import units for mconsole.pas 89 ⟩
    ⟨ Implementation for mconsole.pas 95 ⟩
end

```

89. We import two modules, *pcmizver* and *mizenv*,

```

⟨ Import units for mconsole.pas 89 ⟩ ≡
uses pcmizver, mizenv;

```

This code is used in section 88.

90. We want to have a method which allows us to flag an error (*fErrNbr*) on a given line of the article being processed. But the user may request Mizar to silence these messages. We can facilitate this by having a *DisplayLine* procedure constant.

```

⟨ DisplayLine global constant 90 ⟩ ≡
const DisplayLine: procedure (fLine, fErrNbr : integer) = NoDisplayLine;

```

This code is used in section 107.

Section 3.1. PARSING COMMAND-LINE ARGUMENTS

91. Now, we have accommodator specific options.

```

⟨Interface for accommodator command line options 91⟩ ≡
  { Accommodator specific options: }
var SignatureProcessing, { unused }
      TheoremListsProcessing, { unused }
      SchemeListsProcessing, { unused }
      InsertHiddenFiles, { Include HIDDEN automatically? }
      FormatsProcessing: Boolean;
var { Registrations-related configuration for Accommodator }
      ClustersProcessing, IdentifyProcessing, ReductionProcessing, PropertiesProcessing: Boolean;
var { The environ-specific Accommodator options }
      VocabulariesProcessing, { Accommodator will run ProcessVocabularies }
      NotationsProcessing, { Accommodator processes notations directive }
      ConstructorsProcessing, { Will the Accommodator determine which constructor to use for identifier? }
      DefinitionsProcessing, EqualitiesProcessing, ExpansionsProcessing, { Definition environs }
      TheoremsProcessing, SchemesProcessing: Boolean; { unused variables }

```

See also sections 94 and 98.

This code is used in section 88.

92. Among the state variables introduced in the **mconsole** unit, there is one for handling **SIGINT**, **SIGQUIT**, and **SIGTERM** signals. [[The other UNIX signals should probably be supported, as well.]]

```

⟨Interface for other command line options 92⟩ ≡
  { Other options: }
var CtrlCPressed: Boolean = false; { SIGINT, SIGQUIT, or SIGTERM signal received? }
      LongLines: Boolean = false; { Allow lines longer than 80 characters }
      QuietMode: Boolean = false; { Don't print anything to the console? }
      StopOnError: Boolean = false;
      FinishingPass: Boolean = false; ParserOnly: Boolean = false; { No analyzing or checking }
      AnalyzerOnly: Boolean = false; { Analyze, but no parsing or checking }
      CheckerOnly: Boolean = false; { Check, but do not re-analyze or re-parse }
      SwitchOffUnifier: Boolean = false;
      AxiomsAllowed: Boolean = false;

```

See also section 103.

This code is used in section 88.

93. The implementation begins by initializing the Accommodator specific options. The default situation is every configuration option is *true* except for the unused variables *TheoremListsProcessing* and *SchemeListsProcessing* (both are *false*).

94. ⟨Interface for accommodator command line options 91⟩ +≡
procedure *InitAccOptions*;

95. \langle Implementation for `mconsole.pas` 95 $\rangle \equiv$

```
procedure InitAccOptions;
  begin InsertHiddenFiles  $\leftarrow$  true; VocabulariesProcessing  $\leftarrow$  true; FormatsProcessing  $\leftarrow$  true;
  NotationsProcessing  $\leftarrow$  true; SignatureProcessing  $\leftarrow$  true; ConstructorsProcessing  $\leftarrow$  true;
  ClustersProcessing  $\leftarrow$  true; IdentifyProcessing  $\leftarrow$  true; ReductionProcessing  $\leftarrow$  true;
  PropertiesProcessing  $\leftarrow$  true; DefinitionsProcessing  $\leftarrow$  true; EqualitiesProcessing  $\leftarrow$  true;
  ExpansionsProcessing  $\leftarrow$  true; TheoremsProcessing  $\leftarrow$  true; SchemesProcessing  $\leftarrow$  true;
  TheoremListsProcessing  $\leftarrow$  false; SchemeListsProcessing  $\leftarrow$  false;
  end;
```

See also sections 97, 99, 102, 104, 106, 108, 110, 112, 113, 115, 118, 120, 122, and 125.

This code is used in sections 88 and 116.

96. Similarly, we want to be able to *reset* the configuration for the accommodator make everything false. The motivation is that we want to enable only certain specific flags, and it's faster to set everything to *false* and then manually toggle the flags we want.

This is a private helper function for other things in the `mconsole`.

97. \langle Implementation for `mconsole.pas` 95 $\rangle + \equiv$

```
procedure ResetAccOptions;
  begin InsertHiddenFiles  $\leftarrow$  true; VocabulariesProcessing  $\leftarrow$  false; FormatsProcessing  $\leftarrow$  false;
  NotationsProcessing  $\leftarrow$  false; SignatureProcessing  $\leftarrow$  false; ConstructorsProcessing  $\leftarrow$  false;
  ClustersProcessing  $\leftarrow$  false; IdentifyProcessing  $\leftarrow$  false; ReductionProcessing  $\leftarrow$  false;
  PropertiesProcessing  $\leftarrow$  false; DefinitionsProcessing  $\leftarrow$  false; EqualitiesProcessing  $\leftarrow$  false;
  ExpansionsProcessing  $\leftarrow$  false; TheoremsProcessing  $\leftarrow$  false; SchemesProcessing  $\leftarrow$  false;
  TheoremListsProcessing  $\leftarrow$  false; SchemeListsProcessing  $\leftarrow$  false;
  end;
```

98. **Accommodator options.** We will get options for the accommodator passed in from the command line. Broadly, these are:

- `-v` resets the accommodator options, and then toggles *VocabulariesProcessing* to true
- `-f`, `-p` resets the accommodator options, and then toggles *VocabulariesProcessing* to true (so far like `-v`), and then toggles *FormatsProcessing* to true.
- `-P` resets the accommodator options, and then toggles *VocabulariesProcessing* to true (so far like `-v`), and then toggles *FormatsProcessing* to true (so far like `-f` and `-p`), then toggles *TheoremListsProcessing* and *SchemeListsProcessing* to both be true.
- `-e` will do everything `-f` does, and then toggles *ConstructorsProcessing*, *SignatureProcessing*, *ClustersProcessing*, and *NotationsProcessing* to all be true.
- `-h` will set *InsertHiddenFalse* to false (presumably preventing Mizar from loading the “hidden” article, i.e., the primitive notions of “object”, “<>”, “in”, and “strict” will not be loaded).
- `-l` will toggle *LongLines* to true (allowing lines with more than 80 characters)
- `-q` will toggle *QuietMode* to true
- `-s` will toggle *StopOnError* to true

Note this processes *all* command line options *in order*. So `-e -v` will produce the same results as `-v` alone.

\langle Interface for accommodator command line options 91 $\rangle + \equiv$

```
procedure GetAccOptions;
```

99. \langle Implementation for `mconsole.pas` 95 $\rangle + \equiv$

```

procedure GetAccOptions;
  var i, j: integer;
  begin InitAccOptions;
  for j  $\leftarrow$  1 to ParamCount do
    if ParamStr(j)[1] = '-' then
      for i  $\leftarrow$  2 to length(ParamStr(j)) do
        case ParamStr(j)[i] of
          'v': begin ResetAccOptions; VocabulariesProcessing  $\leftarrow$  true
            end;
          'f', 'p': begin ResetAccOptions; VocabulariesProcessing  $\leftarrow$  true; FormatsProcessing  $\leftarrow$  true;
            end;
          'P': begin ResetAccOptions; VocabulariesProcessing  $\leftarrow$  true; FormatsProcessing  $\leftarrow$  true;
              TheoremListsProcessing  $\leftarrow$  true; SchemeListsProcessing  $\leftarrow$  true;
            end;
          'e': begin ResetAccOptions; VocabulariesProcessing  $\leftarrow$  true; FormatsProcessing  $\leftarrow$  true;
              ConstructorsProcessing  $\leftarrow$  true; SignatureProcessing  $\leftarrow$  true; ClustersProcessing  $\leftarrow$  true;
              NotationsProcessing  $\leftarrow$  true;
            end;
          'h': begin InsertHiddenFiles  $\leftarrow$  false; end;
          'l': LongLines  $\leftarrow$  true;
          'q': QuietMode  $\leftarrow$  true;
          's': StopOnError  $\leftarrow$  true;
        endcases;
      end;
  end;

```

100. Similarly, we have *MakeEnv* specific options parsed from the command line flags.

101. \langle Interface for *MakeEnv* command line options 101 $\rangle \equiv$

{ *MakeEnv* specific options: }

var *Accommodation*: *Boolean* = *false*; *NewAccom*: *Boolean* = *false*;

procedure *GetMEOptions*;

This code is used in section 88.

102. \langle Implementation for `mconsole.pas` 95 $\rangle + \equiv$

```

procedure GetMEOptions;
  var i, j: integer;
  begin for j  $\leftarrow$  1 to ParamCount do
    if ParamStr(j)[1] = '-' then
      for i  $\leftarrow$  2 to length(ParamStr(j)) do
        case ParamStr(j)[i] of
          'n': NewAccom  $\leftarrow$  true;
          'a': Accommodation  $\leftarrow$  true;
          'l': LongLines  $\leftarrow$  true;
          'q': QuietMode  $\leftarrow$  true;
          's': StopOnError  $\leftarrow$  true;
        endcases;
      end;
  end;

```

103. The “other” options.

Notably, there is a feature to allow axioms, which is completely undocumented (and probably for good reason!). The user may automatically enable axioms by placing them all in “.axm” files.

⟨Interface for other command line options 92⟩ +≡
procedure *GetOptions*;

104. ⟨Implementation for mconsole.pas 95⟩ +≡
procedure *GetOptions*;

```

var i, j: integer;
begin for j ← 1 to ParamCount do
  if ParamStr(j)[1] = '-' then
    for i ← 2 to length(ParamStr(j)) do
      case ParamStr(j)[i] of
        'q': QuietMode ← true;
        'p': ParserOnly ← true;
        'a': AnalyzerOnly ← true;
        'c': CheckerOnly ← true;
        'l': LongLines ← true;
        's': StopOnError ← true;
        'u': SwitchOffUnifier ← true;
        'x': AxiomsAllowed ← true;
      othercases break;
    endcases;
  if ArticleExt = '.axm' then AxiomsAllowed ← true;
end;
```

105. Transfer specific options.

⟨Interface for transfer-specific command line options 105⟩ ≡

{ Transfer specific options: }

var *PublicLibr*: Boolean; { use “pre1/⟨Article-name⟩/” subdirectory? }

procedure *GetTransfOptions*;

This code is used in section 88.

106. ⟨Implementation for mconsole.pas 95⟩ +≡

procedure *GetTransfOptions*;

```

var lOption: string;
begin PublicLibr ← false;
if ParamCount ≥ 2 then
  begin lOption ← ParamStr(2);
    if (length(lOption) = 2) ∧ (lOption[1] ∈ [ '/', '- ']) then PublicLibr ← UpCase(lOption[2]) = 'P';
  end
end;
```

Section 3.2. REPORTING RESULTS TO THE CONSOLE

107. We have a number of functions useful for “drawing”, i.e., reporting progress and results (and so on).

```

⟨ Report results to command line 107 ⟩ ≡
procedure InitDisplayLine(const aComment: string);
procedure NoDisplayLine(fLine, fErrNbr : integer);
⟨ DisplayLine global constant 90 ⟩

```

See also sections 109, 111, 114, 116, 117, 119, 121, and 124.

This code is used in section 88.

108. The *gComment* is used only within this module. Mizar stores the name of the pass (parser, MSM, analyzer, checker) in *gComment*, which is used in a helper function to print the progress to the console.

```

⟨ Implementation for mconsole.pas 95 ⟩ +≡
var gComment: string = ``; { The pass currently being run }
    disable_io_checking;
procedure NoDisplayLine(fLine, fErrNbr : integer);
    begin end;
procedure InitDisplayLine(const aComment: string);
    begin gComment ← aComment; WriteLn; write(aComment); DisplayLine ← DisplayLineInCurPos
    end;

```

```

109. ⟨ Report results to command line 107 ⟩ +≡
procedure DrawMizarScreen(const aApplicationName: string);
procedure DrawArticleName(const fName: string);
procedure DrawStr(const aStr: string);
procedure FinishDrawing;

```

```

110. ⟨ Implementation for mconsole.pas 95 ⟩ +≡
procedure DrawStr(const aStr: string);
    begin write(aStr) end;
procedure FinishDrawing;
    begin WriteLn;
    end;
procedure DrawTPass(const fPassName: string);
    begin write(fPassName) end;
procedure DrawMizarScreen(const aApplicationName: string);
    begin WriteLn(aApplicationName, ` , □ `, PCMizarVersionStr, ` □ ` ( ` , PlatformNameStr, ` ) `);
    WriteLn(Copyright);
    end;

```

111. The *Noise* parameter rings the bell three times (the ↑*G* is Caret notation “Ctrl+G”, which is ASCII code 10 BEL). For non-Windows systems, this will write three BEL characters to the standard output stream. Windows will do nothing.

```

⟨ Report results to command line 107 ⟩ +≡
procedure EmptyParameterList;
procedure Noise;

```

112. \langle Implementation for mconsole.pas 95 $\rangle + \equiv$

```

procedure Noise;
  begin
    if_not_def (WIN32) write( $\uparrow G \uparrow G \uparrow G$ ); endif ;
  end ;
procedure EmptyParameterList;
  begin Noise; WriteLn; WriteLn(`****_Empty_Parameter_List_?_****`); halt(2);
end;

```

113. When the user asks Mizar to verify an article, Mizar will begin by writing to the standard output stream “Processing: \langle Article name \rangle ”.

\langle Implementation for mconsole.pas 95 $\rangle + \equiv$

```

procedure DrawArticleName(const fName: string);
  begin WriteLn(`Processing:_`, fName); end;

```

114. \langle Report results to command line 107 $\rangle + \equiv$

```

procedure DrawPass(const aName: string);
procedure DrawTime(const aTime: string);
procedure DrawVerifierExit(const aTime: string);

```

115. \langle Implementation for mconsole.pas 95 $\rangle + \equiv$

```

procedure DrawPass(const aName: string);
  begin WriteLn; write(aName); end;
procedure DrawTime(const aTime: string);
  begin write(aTime); end;
procedure DrawVerifierExit(const aTime: string);
  begin WriteLn; WriteLn(`Time_of_mizaring:`, aTime);
  end;

```

116. On non-Windows machines, $\uparrow M$ is used in *write* to add a carriage return. Windows machines will require #13 instead. This is because $\uparrow M$ is “Ctrl+M” which has ASCII code 77-64=13 (see, it’s the same as #13).

\langle Report results to command line 107 $\rangle + \equiv$

```

procedure DisplayLineInCurPos(fLine, fErrNbr : integer);  $\langle$  Implementation for mconsole.pas 95  $\rangle =$ 
  procedure DisplayLineInCurPos(fLine, fErrNbr : integer);
    begin if ( $\neg$ CtrlCPressed)  $\wedge$  ( $\neg$ QuietMode) then
      begin write( $\uparrow M + gComment + \_ \_$ , fLine : 4);
      if fErrNbr > 0 then write( $\_ \_ * \_$ , fErrNbr);
      write( $\_ \_$ );
      end;
    if FinishingPass then
      begin write( $\_ \_$ , fLine : 4);
      if fErrNbr > 0 then write( $\_ \_ * \_$ , fErrNbr);
      write( $\_ \_$ );
      end;
    end;

```

117. When Mizar needs to notify the user that a critical error has occurred, *DrawMessage* will be used for communicating it. By “critical error”, I mean things like Mizar cannot open the file, or there was a stack overflow, or the hard drive exploded.

⟨Report results to command line 107⟩ +≡

```
procedure DrawMessage(const Msg1, Msg2: string);
```

118. ⟨Implementation for *mconsole.pas* 95⟩ +≡

```
procedure DrawMessage(const Msg1, Msg2: string);
  var Lh: byte;
  begin Noise; WriteLn; write('***_ ', Msg1); Lh ← length(Msg1);
  if length(Msg2) > Lh then Lh ← length(Msg2);
  if Lh > length(Msg1) then write('_ ': Lh - length(Msg1));
  WriteLn('_*** ');
  if Msg2 ≠ '' then
    begin write('***_ ', Msg2);
    if Lh > length(Msg2) then write('_ ': Lh - length(Msg2));
    WriteLn('_*** ');
    end;
  end;
```

119. The *monitor.pas* file uses *BugInProcessor* when reporting errors. It's a logging function for severe situations.

⟨Report results to command line 107⟩ +≡

```
procedure BugInProcessor;
```

120. ⟨Implementation for *mconsole.pas* 95⟩ +≡

```
procedure BugInProcessor;
  begin DrawMessage('Internal_Error', ''); end;
```

121. When *reset* (or *rewrite*) fails, Mizar will cease. We should specifically report the situation to the user, because they can address the situation whereas we cannot.

⟨Report results to command line 107⟩ +≡

```
procedure DrawIOResult(const FileName: string; I: byte);
```

122. ⟨Implementation for *mconsole.pas* 95⟩ +≡

```
procedure DrawIOResult(const FileName: string; I: byte);
  begin if I ∈ [2 .. 6, 12, 100] then
    begin if I = 12 then I ← 7
    else if I = 100 then I ← 8;
    DrawMessage(ErrMsg[I], 'Can''t_open_' + FileName + '_ ');
    end
  else DrawMessage('Can''t_open_' + FileName + '_ ', '');
  halt(1);
  end;
```

123. We also have a constant for error messages commonly encountered.

⟨ Constants for common error messages reported to console 123 ⟩ ≡

```
const ErrMsg: array [1..6] of string[20] =
  (
    'File_not_found',
    'Path_not_found',
    'Too_many_open_files',
    'Disk_read_error',
    'Disk_write_error');
```

This code is used in section 88.

124. ⟨ Report results to command line 107 ⟩ +≡

```
procedure DrawErrorsMsg(aErrorNbr : integer);
```

125. ⟨ Implementation for mconsole.pas 95 ⟩ +≡

```
procedure DrawErrorsMSg(aErrorNbr : integer);
```

```
  begin if aErrorNbr > 0 then
```

```
    begin WriteLn;
```

```
    if aErrorNbr = 1 then WriteLn('***_1_error_detected')
```

```
    else WriteLn('***_', aErrorNbr, '_errors_detected');
```

```
    end;
```

```
  end;
```


File 4

Error handling

126. There are a few common error reporting routines bundled together. We should recall Borland PASCAL’s *RunError* method stops the execution of the program and generates a run-time error. The other primitive PASCAL function worth remembering is *Halt* which takes an error exit code, halts the program, and returns control to the calling program. For PASCAL specific error codes, consult:

<https://wiki.freepascal.org/RunError>

```

⟨errhan.pas 126⟩ ≡
  ⟨GNU License 4⟩
unit errhan;
  interface
    ⟨Interface for errhan.pas 127⟩
  implementation
    uses mconsole, mizenv;
    ⟨Implementation for errhan.pas 130⟩
  end ;

```

127. We have a few custom types and internal variables describing the state of the Mizar error handler.

The *Position* type is especially important for the Parser, which will store the metadata in the abstract syntax tree. The starchy reader may wish to consult the POSIX Standard’s [definition](#) (3.75 of Volume I) for “column position” which states, “Column positions are numbered starting from 1.” Coincidentally, this would imply Mizar cannot properly parse files longer than $2^{31} - 1$ columns wide (or $2^{63} - 1$ columns wide for 64-bit computers).

```

⟨Interface for errhan.pas 127⟩ ≡
type Position = ⟨Declare Position as record 128⟩;
  ErrorReport = procedure (Pos : Position; ErrNr : integer);
const ZeroPos: Position = (Line : 0; Col : 0);
var CurPos: Position; { current position }
    ErrorNbr: integer; { current error number }
    PutError: ErrorReport = nil; { reporter for errors }
    RTErrCode: integer = 0; { runtime error code }
    OverflowError: boolean = false; { overflow error? They’re horrible, treat accordingly }

```

See also sections [129](#), [131](#), [133](#), [138](#), [140](#), [142](#), [144](#), [146](#), and [148](#).

This code is used in section [126](#).

128. Position is just a pair of integers recording the line and offset (“column”).

```

⟨Declare Position as record 128⟩ ≡
  record Line, Col: integer
  end

```

This code is used in section [127](#).

129. The implementation begins as we would expect/hope. If we have a *preferred* error reporter already present in *PutError*, then we just use it. If we have toggled *StopOnError* to true, then we should end the program here (with a message).

If we want to report an error at the *CurrPos* (current position), then we have a helper function do that for us.

The *Error* and *ErrImm* procedures are both used in the parser.

⟨Interface for **errhan.pas** 127⟩ +≡

procedure *Error*(*Pos* : *Position*; *ErrNr* : *integer*);

procedure *ErrImm*(*ErrNr* : *integer*);

130. ⟨Implementation for **errhan.pas** 130⟩ ≡

procedure *Error*(*Pos* : *Position*; *ErrNr* : *integer*);

begin *inc*(*ErrorNbr*);

if @*PutError* ≠ **nil** **then** *PutError*(*Pos*, *ErrNr*);

if *StopOnError* **then**

begin *DrawMessage*(‘Stopped on first error’, ‘’); *Halt*(1); **end**;

end;

procedure *ErrImm*(*ErrNr* : *integer*);

begin *Error*(*CurPos*, *ErrNr*);

end;

See also sections 132, 134, 139, 141, 143, 145, 147, and 149.

This code is used in section 126.

131. We also can write errors to a file. This requires keeping track of the file (dubbed *Errors*) and whether it has been opened or not (in the Boolean condition *OpenedErrors*).

Note this takes advantage of **with** to destructure *Pos* into a *Line* and *Col* for us.

⟨Interface for **errhan.pas** 127⟩ +≡

procedure *WriteError*(*Pos* : *Position*; *ErrNr* : *integer*);

132. ⟨Implementation for **errhan.pas** 130⟩ +≡

var *Errors*: *text*; { file name for errors file }

OpenedErrors: *boolean* = *false*; { have we opened it yet? }

procedure *WriteError*(*Pos* : *Position*; *ErrNr* : *integer*);

begin **if** ¬*OpenedErrors* **then** *RunTimeError*(2001);

with *Pos* **do** *WriteLn*(*Errors*, *Line*, ‘_’, *Col*, ‘_’, *ErrNr*);

end;

133. Opening an errors file. We can open an errors file, which will reset the *ErrorNbr* counter to zero and re-initialize *CurPos* to line 1 and column 1.

When *PutError* is **nil**, we initialize it to be *WriteError*.

⟨Interface for **errhan.pas** 127⟩ +≡

procedure *OpenErrors*(*FileName* : *string*);

134. \langle Implementation for `errhan.pas` 130 $\rangle + \equiv$

```
procedure OpenErrors(FileName : string);
  begin if ExtractFileExt(FileName) = `` then FileName  $\leftarrow$  FileName + `.err`;
  Assign(Errors, FileName);
  without_io_checking(Rewrite(Errors)); { Open the FileName }
   $\langle$  If cannot open the FileName, report an error and halt 135  $\rangle$ ;
   $\langle$  Initialize errhan.pas state variables 136  $\rangle$ ;
   $\langle$  Set current position to first line, first column 137  $\rangle$ ;
  if @PutError = nil then PutError  $\leftarrow$  WriteError;
end;
```

135. \langle If cannot open the *FileName*, report an error and halt 135 $\rangle \equiv$

```
if IOResult  $\neq$  0 then
  begin DrawMessage(Can't open errors file + FileName + for writing, ``); halt(1);
end
```

This code is used in section 134.

136. \langle Initialize `errhan.pas` state variables 136 $\rangle \equiv$

```
OpenedErrors  $\leftarrow$  true; ErrorNbr  $\leftarrow$  0
```

This code is used in sections 134 and 139.

137. \langle Set current position to first line, first column 137 $\rangle \equiv$

```
with CurPos do
  begin Line  $\leftarrow$  1; Col  $\leftarrow$  1
end
```

This code is used in sections 134, 139, and 186.

138. Appending errors to the errors file. This isn't used anywhere in Mizar. It may be instructive for the reader to compare this to *OpenErrors*.

\langle Interface for `errhan.pas` 127 $\rangle + \equiv$

```
procedure AppendErrors(FileName : string);
```

139. \langle Implementation for `errhan.pas` 130 $\rangle + \equiv$

```
procedure AppendErrors(FileName : string); { unused }
  begin if ExtractFileExt(FileName) = `` then FileName  $\leftarrow$  FileName + `.err`;
  Assign(Errors, FileName);
   $\langle$  Initialize errhan.pas state variables 136  $\rangle$ ;
   $\langle$  Set current position to first line, first column 137  $\rangle$ ;
  without_io_checking(append(Errors));
  if IOResult  $\neq$  0 then Rewrite(Errors);
end;
```

140. We can also close the errors file and unset the *Errors* variable, “forgetting” where we logged the errors. This does not appear to be used anywhere in Mizar.

\langle Interface for `errhan.pas` 127 $\rangle + \equiv$

```
procedure EraseErrors;
```

141. \langle Implementation for `errhan.pas` 130 $\rangle + \equiv$

```
procedure EraseErrors;
  begin if OpenedErrors then
    begin OpenedErrors  $\leftarrow$  false; close(Errors); erase(Errors);
    end;
  end;
```

142. We can also just close the errors file. This is used in `monitor.pas`.

\langle Interface for `errhan.pas` 127 $\rangle + \equiv$

```
procedure CloseErrors;
```

143. \langle Implementation for `errhan.pas` 130 $\rangle + \equiv$

```
procedure CloseErrors;
  begin if OpenedErrors then
    begin OpenedErrors  $\leftarrow$  false; close(Errors);
    end;
  end;
```

144. Like I said, overflow errors are especially problematic. If/when they occur, we should just bail out immediately. Curiously, Free PASCAL uses the 202 error for stack overflow errors, and 203 for heap overflow errors. Mizar uses the 97 error code for overflow errors.

\langle Interface for `errhan.pas` 127 $\rangle + \equiv$

```
procedure OverflowError(ErrorCode : word);
```

145. \langle Implementation for `errhan.pas` 130 $\rangle + \equiv$

```
procedure OverflowError(ErrorCode : word);
  begin RTErrCode  $\leftarrow$  ErrorCode; OverflowError  $\leftarrow$  true; RunError(97);
  end;
```

146. We have an assertion utility to check if a *Cond* is *true*. When it is *false*, we should report a runtime error (i.e., update *RTErrCode* and invoke *RunError*(98)). Free PASCAL's *assert* function generates a 227 "Assertion failed error" error code upon failure.

\langle Interface for `errhan.pas` 127 $\rangle + \equiv$

```
procedure MizAssert(ErrorCode : word; Cond : Boolean);
```

147. \langle Implementation for `errhan.pas` 130 $\rangle + \equiv$

```
procedure MizAssert(ErrorCode : word; Cond : Boolean);
  begin if  $\neg$ Cond then
    begin RTErrCode  $\leftarrow$  ErrorCode; RunError(98);
    end;
  end;
```

148. Last, we have a catchall for runtime errors encountered.

\langle Interface for `errhan.pas` 127 $\rangle + \equiv$

```
procedure RunTimeError(ErrorCode : word);
```

149. \langle Implementation for `errhan.pas` 130 $\rangle + \equiv$

```
procedure RunTimeError(ErrorCode : word);
  begin RTErrCode  $\leftarrow$  ErrorCode; RunError(99);
  end;
```

File 5

Info file handling

150. I don't think this is actually used anywhere, but I am including it for completeness.

```

⟨ info.pas 150 ⟩ ≡
  ⟨ GNU License 4 ⟩
unit info;
  interface uses errhan;
  var InfoFile: text;

  procedure InfoChar(C : char);
  procedure InfoInt(I : integer);
  procedure InfoWord(C : char; I : integer);
  procedure InfoNewLine;
  procedure InfoString(S : string);
  procedure InfoPos(Pos : Position);
  procedure InfoCurPos;
  procedure OpenInfoFile;
  procedure CloseInfofile;

  implementation
  uses mizenv, mconsole;

  procedure InfoChar(C : char);
    begin write(InfoFile, C)
    end;

  procedure InfoInt(I : integer);
    begin write(InfoFile, I, '␣')
    end;

  procedure InfoWord(C : char; I : integer);
    begin write(InfoFile, C, I, '␣')
    end;

  procedure InfoNewLine;
    begin WriteLn(InfoFile)
    end;

  procedure InfoString(S : string);
    begin write(InfoFile, S)
    end;

  procedure InfoPos(Pos : Position);
    begin with Pos do write(InfoFile, Line, '␣', Col, '␣')
    end;

  procedure InfoCurPos;
    begin with CurPos do write(InfoFile, Line, '␣', Col, '␣')
    end;

```

151. There are a few helper functions which is more than “Write \langle data type \rangle to info file”.

```

var _InfoExitProc: pointer;
procedure InfoExitProc;
  begin CloseInfoFile; ExitProc  $\leftarrow$  _InfoExitProc;
  end;

procedure OpenInfoFile;
  begin Assign(InfoFile, MizFileName +  $\text{'\texttt{.inf'}}$ ); Rewrite(InfoFile);
  WriteLn(InfoFile,  $\text{'Mizared\_article:\_'\texttt{'}}$ , MizFileName,  $\text{'\texttt{'}}$ ); _InfoExitProc  $\leftarrow$  ExitProc;
  ExitProc  $\leftarrow$  @InfoExitProc;
  end;

procedure CloseInfofile;
  begin close(InfoFile)
  end;

end .

```

File 6

Monitor

152. There is only one single public-facing procedure in the `monitor.pas` file: *InitExitProc*. This just assigns the *_Halt_* function (defined in this module) to the *ExitProc* pointer global variable.

```

⟨ monitor.pas 152 ⟩ ≡
  ⟨ GNU License 4 ⟩
unit monitor;
interface
  procedure InitExitProc;
implementation
  ⟨ Units used by monitor.pas 153 ⟩;
var _ExitProc: pointer; _IOResult: integer;
  ⟨ Implementation for monitor.pas 154 ⟩
end

```

153. The monitor is used for reporting errors, which is heavily system dependent. The modules used by it are...wonky. We need the *baseunix* unit for UNIX systems, and the *windows* unit for Windows-based systems.

```

⟨ Units used by monitor.pas 153 ⟩ ≡
uses
  @{@&$IFDEF FPC@}
    @{@&$IFDEF WIN32@}
      baseunix,
    @{@&$ENDIF@}
  @{@&$ENDIF@}
  mizenv, errhan, mconsole
  @{@&$IFDEF WIN32@} , windows @{@&$ENDIF@}
  mdebug , info end_mdebug

```

This code is used in section 152.

154. There are a few private helper functions in this module.

⟨Implementation for `monitor.pas` 154⟩ \equiv

```

procedure _Halt_(ErrorCode : word);
begin IOResult  $\leftarrow$  IOResult; ErrorAddr  $\leftarrow$  nil;
if ErrorCode > 1 then
  case ErrorCode of
    2 .. 4: begin ErrImm(1000 + ErrorCode); DrawMessage('I/O_error', ErrMsg[ErrorCode]) end;
    5 .. 6: begin ErrImm(1000 + ErrorCode); BugInProcessor end;
    12: begin ErrImm(1000 + ErrorCode); BugInProcessor end;
    97, 98, 99: begin ErrImm(RTErrorCode); ⟨Handle runtime error cases for monitor.pas 155⟩
      end;
    100 .. 101: begin ErrImm(1000 + ErrorCode); DrawMessage('I/O_error', ErrMsg[ErrorCode - 95]);
      end;
    102 .. 106: begin ErrImm(1000 + ErrorCode); BugInProcessor end;
    150 .. 162: begin ErrImm(1000 + ErrorCode);
      DrawMessage('I/O_error', 'Critical_disk_error');
      end;
    200 .. 201: begin ErrImm(1000 + ErrorCode); BugInProcessor end;
    202: begin ErrImm(1000 + ErrorCode); DrawMessage('Stack_overflow_error', '') end;
    203, 204: begin ErrImm(1000 + ErrorCode); DrawMessage('Heap_overflow_error', '') end;
    208: begin ErrImm(1000 + ErrorCode); DrawMessage('Overlay_manager_not_installed', '') end;
    209: begin ErrImm(1000 + ErrorCode); DrawMessage('Overlay_file_read_error', '') end;
    210 .. 212: begin ErrImm(1000 + ErrorCode); BugInProcessor end;
    213: begin ErrImm(1000 + ErrorCode); DrawMessage('Collection_Index_out_of_range', '') end;
    214: begin ErrImm(1000 + ErrorCode); DrawMessage('Collection_overflow_error', '') end;
    215: begin ErrImm(1000 + ErrorCode); DrawMessage('Arithmetic_overflow_error', '') end;
    216: begin ErrImm(1000 + ErrorCode); DrawMessage('General_Protection_fault', '') end;
    217: begin ErrImm(1000 + ErrorCode); DrawMessage('Segmentation_fault', '') end;
    218 .. 254: begin ErrImm(1000 + ErrorCode); BugInProcessor end;
    255: ErrImm(1000 + ErrorCode);
  othercases begin ErrImm(ErrorCode);
    if OverflowError then DrawMessage('Mizar_parameter_overflow_error', '')
    else BugInProcessor
    end;
  endcases;
  CloseErrors; ExitProc  $\leftarrow$  ExitProc;
if (ErrorCode = 0)  $\wedge$  (ErrorNbr  $\neq$  0) then Halt(1)
else Halt(ErrorCode);
end;

```

See also section 156.

This code is used in section 152.

155. \langle Handle runtime error cases for `monitor.pas` 155 $\rangle \equiv$

```

case RTErrorCode of
800,804: DrawMessage('Library_Corrupted', ``);
857: DrawMessage('Connection_Fault', ``);
      { 900..999: DrawMessage('Mizar parameter overflow: ' + IntToStr(RTErrorCode), ""); }
1255: DrawMessage('User_break', ``);
othercases if OverflowError then
      DrawMessage('Mizar_parameter_overflow: ' + IntToStr(RTErrorCode), ``)
else BugInProcessor
endcases;

```

This code is used in section 154.

156. The *MizExitProc* is a private “bail out” function.

\langle Implementation for `monitor.pas` 154 $\rangle + \equiv$

```

procedure MizExitProc;
begin
  @{@&$IFDEF IODEBUG@} ExitProc  $\leftarrow$  _ExitProc;
  @{@&$ELSE@} _Halt_(ExitCode);
  @{@&$ENDIF@}
end;

```

157. We use the *MizExitProc* to initialize the *ExitProc* pointer.

```

procedure InitExitProc;
begin ExitProc  $\leftarrow$  @MizExitProc
end;

```

158. Initializing Control. This is a *heavily* system dependent piece of code. There are two ways to implement it (one way for Windows, another way for everyone else). Once we’re done, we have to initialize the *_ExitProc* and invoke *InitCtrl*.

\langle Non-windows FreePascal implemenation for *InitCtrl* 159 \rangle

\langle Windows implemenation for *InitCtrl* 160 \rangle

```

begin _ExitProc  $\leftarrow$  ExitProc; InitCtrl;
end.

```

159. \langle Non-windows FreePascal implemenation for *InitCtrl* 159 $\rangle \equiv$

```

@{@&$IFDEF FPC@}  @{@&$IFNDEF WIN32@}
procedure CatchSignal(aSig : integer); cdecl;
begin
  case aSig of
    SIGINT, SIGQUIT, SIGTERM: begin CtrlCPressed  $\leftarrow$  true; RunTimeError(1255); end;
  endcases;
end;
var NewSignal, OldSigInt: SignalHandler;
procedure InitCtrl;
begin NewSignal  $\leftarrow$  SignalHandler(@CatchSignal); OldSigInt  $\leftarrow$  fpSignal(SIGINT, NewSignal);
  OldSigInt  $\leftarrow$  fpSignal(SIGQUIT, NewSignal); OldSigInt  $\leftarrow$  fpSignal(SIGTERM, NewSignal);
end;
  @{@&$ENDIF@}@{@&$ENDIF@}

```

This code is used in section 158.

160. Microsoft breaks everything. This is a mess because of them.

```

⟨ Windows implemenation for InitCtrl 160 ⟩ ≡
  @{ @&$IFDEF WIN32 @}
    ⟨ Windows implemenation for CtrlSignal 163 ⟩
    @{ @&$IFDEF FPC @}
      ⟨ FreePascal implemenation of InitCtrl for Windows 161 ⟩
      @{ @&$ENDIF @}
    @{ @&$IFDEF DELPHI @}
      ⟨ Delphi implemenation of InitCtrl for Windows 162 ⟩
      @{ @&$ENDIF @}
    @{ @&$ENDIF @}

```

This code is used in section 158.

161. The FreePascal implementation is pretty succinct thanks to the libraries they provide.

```

⟨ FreePascal implementation of InitCtrl for Windows 161 ⟩ ≡
procedure InitCtrl;
  begin SetConsoleCtrlHandler(CtrlSignal, TRUE); end;

```

This code is used in section 160.

```

162. ⟨ Delphi implementation of InitCtrl for Windows 162 ⟩ ≡
procedure InitCtrl;
  var ConsoleMode, lConsoleMode: DWORD;
  begin if GetConsoleMode(GetStdHandle(STD_INPUT_HANDLE), ConsoleMode) then
    begin lConsoleMode ← ConsoleMode ∨ ENABLE_PROCESSED_INPUT;
      { Treat Ctrl+C as a signal }
    if SetConsoleMode(GetStdHandle(STD_INPUT_HANDLE), lConsoleMode) then
      begin SetConsoleCtrlHandler(@CtrlSignal, TRUE);
        end;
      end;
    end;
  end;

```

This code is used in section 160.

163. Windows requires a helper function *CtrlSignal* for this Microsoft mania.

```

⟨ Windows implemenation for CtrlSignal 163 ⟩ ≡
  ⟨ FreePascal declaration of CtrlSignal for Windows 164 ⟩
  ⟨ Delphi declaration of CtrlSignal for Windows 165 ⟩
  begin { TRUE: do not call next handler in the queue, FALSE: call it }
    CtrlCPressed ← true; RunTimeError(1255); CtrlSignal ← true; { ExitProcess(1); }
  end;

```

This code is used in section 160.

```

164. ⟨ FreePascal declaration of CtrlSignal for Windows 164 ⟩ ≡
  @{ @&$IFDEF FPC @}
function CtrlSignal(aSignal : DWORD): WINBOOL; stdcall;
  @{ @&$ENDIF @}

```

This code is used in section 163.

```

165. ⟨ Delphi declaration of CtrlSignal for Windows 165 ⟩ ≡
  @{ @&$IFDEF DELPHI @}
function CtrlSignal(aSignal : DWORD): BOOL; cdecl;
  @{ @&$ENDIF @}

```

This code is used in section 163.

File 7

Time utilities

166. We will want to report to the user how much time Mizar takes during various phases of execution. This is another heavily “system dependent” library.

```

<mtime.pas 166> ≡
  <GNU License 4>
unit mtime;
  interface
    <Interface for mtime.pas 171>
  implementation
    <Implementation for mtime.pas 167>
  end ;

```

167. The implementation begins with a rather *thorny* digression depending on which compiler we’re using.

```

<Implementation for mtime.pas 167> ≡
  <Timing utilities uses for Delphi 168>
  <Timing utilities uses for FreePascal 169>

```

See also sections 170, 172, 174, 176, 177, 179, and 183.

This code is used in section 166.

168. Delphi simply requires us to introduce a constant for milliseconds.

```

<Timing utilities uses for Delphi 168> ≡
  @{@&$IFDEF DELPHI@}
  uses windows;
const cmSecs = 1000;
  @{@&$ENDIF@}

```

This code is used in section 167.

169. FreePascal requires a bit more work, alas. We can use the *GetTime* procedure to populate the hours, minutes, seconds, and hundredths of a second. American readers forgetful of the metric system should know that $0.01\text{ s} = 10\text{ ms}$ (one hundredth of a second is ten milliseconds).

Note: the *wMilliseconds* parameter is misnamed, it does not measure in units of milliseconds but centiseconds.

```

< Timing utilities uses for FreePascal 169 > ≡
  @{@&$IFDEF FPC@}
    uses dos;
const cmSecs = 100; { = 100 centiseconds per 1 second }
type TSystemTime =
  record wHour: word;
    wMinute: word;
    wSecond: word;
    wMilliseconds: word;
  end;
procedure GetLocalTime(var aTime : TSystemTime);
  begin with aTime do GetTime(wHour, wMinute, wSecond, wMilliseconds);
  end;
  @{@&$ENDIF@}

```

This code is used in section 167.

170. Now we can happily plug along implementing the functions we need. This is slightly misnamed, the result will be *centiseconds* (hundredths of a second).

```

< Implementation for mtime.pas 167 > +≡
function SystemTimeToMiliSec(const fTime: TSystemTime): longint;
  begin SystemTimeToMiliSec ← fTime.wHour * (3600 * cmSecs) +
    fTime.wMinute * longint(60 * cmSecs) + fTime.wSecond * cmSecs + fTime.wMilliseconds;
  end;

```

171. Time since we “started the clock”. The result is stored in the variable *W*.

```

< Interface for mtime.pas 171 > ≡
procedure TimeMark(var W : longint);

```

See also sections 173, 175, 178, and 182.

This code is used in section 166.

```

172. < Implementation for mtime.pas 167 > +≡
procedure TimeMark(var W : longint);
  var SystemTime: TSystemTime;
  begin GetLocalTime(SystemTime); W ← SystemTimeToMiliSec(SystemTime);
  end;

```

173. When we have measured the time already *W* since the system started (in “milliseconds”), and we want to get the elapsed time *since we measured W*, then this function will accomplish the task. If *W* is greater than the lifetime of Mizar’s run, then clearly something has gone awry. Mizar assumes a day has passed (in that case).

Note that $86400 = 24 \times 60 \times 60$ is the number of minutes in one day.

```

< Interface for mtime.pas 171 > +≡
function ElapsedTime(W : longint): longint;

```

174. \langle Implementation for `mtime.pas 167` $\rangle + \equiv$

```
function ElapsedTime(W : longint): longint;
  var T: longint; SystemTime: TSystemTime;
  begin GetLocalTime(SystemTime); T  $\leftarrow$  SystemTimeToMiliSec(SystemTime) - W;
  if T < 0 then T  $\leftarrow$  86400 * cmSecs + T;
  ElapsedTime  $\leftarrow$  T;
end;
```

175. We can transform an interval of time (in “milliseconds”) into hours, minutes, seconds, a fractional amount of time.

\langle Interface for `mtime.pas 171` $\rangle + \equiv$

```
procedure MUnpackTime(W : longint; var H, M, S, F : word);
```

176. \langle Implementation for `mtime.pas 167` $\rangle + \equiv$

```
procedure MUnpackTime(W : longint; var H, M, S, F : word);
  begin H  $\leftarrow$  W div (3600 * cmSecs); M  $\leftarrow$  (W - H * 3600 * cmSecs) div (60 * cmSecs);
  S  $\leftarrow$  (W - H * 3600 * cmSecs - M * 60 * cmSecs) div cmSecs;
  F  $\leftarrow$  W - H * 3600 * cmSecs - M * 60 * cmSecs - S * cmSecs;
end;
```

177. When reporting time, we want to pad the time by a zero. This is standard conventional stuff (e.g., I have an appointment at 11:01 AM, not 11:1 AM).

\langle Implementation for `mtime.pas 167` $\rangle + \equiv$

```
function LeadingZero(w : word): String;
  var lStr: String;
  begin Str(w : 0, lStr);
  if length(lStr) = 1 then lStr  $\leftarrow$  '0' + lStr;
  LeadingZero  $\leftarrow$  lStr;
end;
```

178. Reporting time transforms a time interval (measured in milliseconds) into a human readable String.

\langle Interface for `mtime.pas 171` $\rangle + \equiv$

```
function ReportTime(W : longint): String;
```

179. \langle Implementation for `mtime.pas 167` $\rangle + \equiv$

```
function ReportTime(W : longint): String;
  var H, M, S, F: word; lTimeStr: String;
  begin MUnpackTime(ElapsedTime(W), H, M, S, F);  $\langle$  Round to nearest second 180  $\rangle$ ;
  if H  $\neq$  0 then  $\langle$  Report hours and minutes 181  $\rangle$ 
  else Str(M : 2, lTimeStr); {report minutes}
  ReportTime  $\leftarrow$  lTimeStr + ':' + LeadingZero(S); {...and seconds}
end;
```

180. \langle Round to nearest second 180 $\rangle \equiv$

```
if F  $\geq$  (cmSecs div 2) then inc(S)
```

This code is used in section 179.

181. \langle Report hours and minutes 181 $\rangle \equiv$

```
begin Str(H, lTimeStr); lTimeStr  $\leftarrow$  lTimeStr + ':' + LeadingZero(M)
end
```

This code is used in section 179.

182. We also have one global variable tracking the start time of Mizar. Every time Mizar starts up, it will “mark the time” (i.e., assign to the *gStartTime* global variable the current time).

⟨Interface for `mtime.pas` 171⟩ +≡
var *gStartTime*: *longint*;

183. When we run the program, we should mark the time.

⟨Implementation for `mtime.pas` 167⟩ +≡
 begin *TimeMark*(*gStartTime*);
 end.

File 8

Mizar internal state

184. As far as *processing* an article, Mizar works like a “batch compiler” and works in multiple “passes”. We will want to report on each “pass”, informing the user how long it took or how many errors were encountered.

```

⟨ mstate.pas 184 ⟩ ≡
  ⟨ GNU License 4 ⟩
unit mstate;
  interface
    ⟨ Interface for mstate.pas 185 ⟩
  implementation
    uses mizenv, pcmizver, monitor, errhan, mconsole, mtime
    mdebug , info end_mdebug ;
    ⟨ Implementation for mstate.pas 186 ⟩
  end

```

185. We have a local (well, “module”-wide) variable *PassTime* to “start the clock” for measuring how long a pass took.

The implementation amounts to, well, these four functions. We have a couple “private” functions to help us: *MError* and *MizarExitProc*.

```

⟨ Interface for mstate.pas 185 ⟩ ≡
procedure InitPass(const aPassName: string);

```

See also sections 187, 191, and 195.

This code is used in section 184.

```

186. ⟨ Implementation for mstate.pas 186 ⟩ ≡
var PassTime: longint;
procedure InitPass(const aPassName: string);
  begin ⟨ Set current position to first line, first column 137 ⟩;
  InitDisplayLine(aPassName); { (§108) }
  TimeMark(PassTime);
  end;

```

See also sections 188, 190, 192, and 196.

This code is used in section 184.

```

187. ⟨ Interface for mstate.pas 185 ⟩ +≡
procedure FinishPass;

```

```

188. ⟨ Implementation for mstate.pas 186 ⟩ +≡
procedure FinishPass;
  begin FinishingPass ← true;
  if QuietMode then DisplayLine(CurPos.Line, ErrorNbr);
  FinishingPass ← false; DrawTime(⌈⌋ + ReportTime(PassTime));
  end;

```

189. We also have *MizarExitProc* as a private “helper” function.

190. \langle Implementation for *mstate.pas* 186 $\rangle + \equiv$

```
var _ExitProc: pointer;
procedure MizarExitProc;
  begin ExitProc  $\leftarrow$  _ExitProc;
  disable_io_checking;
  if IOResult  $\neq$  0 then ;
  if  $\neg$ StopOnError then DisplayLine(CurPos.Line, ErrorNbr);
  PutError  $\leftarrow$  WriteError; { (§131) }
  DrawVerifierExit(ReportTime(gStartTime));
  enable_io_checking;
end;
```

191. \langle Interface for *mstate.pas* 185 $\rangle + \equiv$

```
procedure InitProcessing(const aProgName, aExt: String);
```

192. \langle Implementation for *mstate.pas* 186 $\rangle + \equiv$

```
procedure MError(Pos : Position; ErrNr : integer);
  begin WriteError(Pos, ErrNr); { (§131) }
  DisplayLine(CurPos.Line, ErrorNbr); { (§90) }
end;

procedure InitProcessing(const aProgName, aExt: string);
  begin DrawMizarScreen(aProgName);
  if ParamCount < 1 then EmptyParameterList;
   $\langle$  Parse the command-line arguments for article name and options 193  $\rangle$ ;
   $\langle$  Initialize the ExitProc 194  $\rangle$ ;
  PutError  $\leftarrow$  MError; OpenErrors(MizFileName);
  mdebug OpenInfoFile; end_mdebug
end;
```

193. \langle Parse the command-line arguments for article name and options 193 $\rangle \equiv$

```
GetArticleName; GetEnvironName; DrawArticleName(MizFileName + aExt); GetOptions
```

This code is used in section 192.

194. \langle Initialize the ExitProc 194 $\rangle \equiv$

```
InitExitProc; FileExam(MizFileName + aExt); _ExitProc  $\leftarrow$  ExitProc; ExitProc  $\leftarrow$  @MizarExitProc
```

This code is used in section 192.

195. At the end, we should report the number of errors (if any were encountered).

\langle Interface for *mstate.pas* 185 $\rangle + \equiv$

```
procedure ProcessingEnding;
```

196. \langle Implementation for *mstate.pas* 186 $\rangle + \equiv$

```
procedure ProcessingEnding;
  begin if ErrorNbr > 0 then
    begin DrawErrorsMsg(ErrorNbr); FinishDrawing;
    end;
  end;
```


File 9

Arbitrary precision arithmetic

197. Specifically, arbitrary precision arithmetic on *integers* and *rational complex* numbers. integers are represented as Strings of digits.

Note:

- (1) The naming convention dictates all functions suffixed with *_XXX* presuppose the arguments are positive.
- (2) Also there are *no checks* whether the parameters contain only digits (and an optional sign “-”).
- (3) Further, *DEBUGNUM* is a conditional variable that can be used (with *DEBUG*) for testing. We can easily turn this into a macro.

(I think we could even introduce a macro $\text{log_num}(\#) \equiv \text{debug_num}(\text{WriteLn}(\#)) \dots$)

define *debug_num*(#) \equiv @{@&\$IFDEF DEBUGNUM@} #@{@&\$ENDIF@}

< numbers.pas 197 > \equiv

< GNU License 4 >

unit *numbers*;

interface

< Basic arithmetic operations declarations 203 >

type < Types for arbitrary-precision arithmetic 255 >

const < Zero and units for arbitrary-precision 256 >

< Rational arithmetic declarations 257 >

< Predicate declarations for arbitrary-precision arithmetic 277 >

< Declare public complex-valued arbitrary precision arithmetic 283 >

< Declare public comparison operators for arbitrary-precision numbers 301 >

implementation

uses *mizenv*

if_def (*CH_REPORT*) , *req_info* , *prephan* , *builtin* **endif**

mdebug , *info* **end_mdebug**;

< Trim leading zeros from arbitrary-precision integers 199 >

< Check if arbitrary-precision integers are zero 200 >

< Absolute value for an arbitrary-precision number 204 >

< Test if one arbitrary-precision number is less than or equal to another 205 >

< Arithmetic for arbitrary-precision integers 210 >

< Arbitrary-precision rational arithmetic 258 >

< Complex-rational arbitrary-precision arithmetic 278 >

end .

Section 9.1. ARBITRARY-PRECISION INTEGERS

198. We will use “schoolbook arithmetic”, representing an arbitrary precision integer as a string of digits, possibly leading with an optional sign. We will “normalize” the representation by the constraint: if the leading digit is zero, then the number is zero. So we will need to trim superfluous leading zeros.

We will also adopt the convention that the empty string is a synonym for zero.

199. If we are given single character string consisting of zero or the empty string, then we are done.

If we are given anything else, we find the first index (from the left) of a nonzero character. Then we create a copy of the substring starting from the first nonzero digit to the rest of the string.

This will break if given a string of zeroes like $a = \text{'00'}$, in the sense that the empty string will be returned.

⟨Trim leading zeros from arbitrary-precision integers 199⟩ ≡

```
function trimlz( $a : \text{string}$ ):  $\text{string}$ ;
  var  $i$ :  $\text{integer}$ ;
  begin if ( $a = \text{'0'}$ )  $\vee$  ( $a = \text{''}$ ) then  $\text{trimlz} \leftarrow a$ 
  else begin  $i \leftarrow 0$ ;
    repeat  $i \leftarrow i + 1$ ;
      if  $a[i] \neq \text{'0'}$  then break;
    until  $i = \text{length}(a)$ ;
     $\text{trimlz} \leftarrow \text{copy}(a, i, \text{length}(a))$ ;
  end;
end;
```

This code is used in section 197.

200. First, we check if a starts with “−0”. If so, replace a with 0. Then we do the same thing with b .

We invoke *trimlz* on a and store the result in $a1$. If $a1 \neq a$, then we update $a \leftarrow a1$.

Then we do likewise on b .

⟨Check if arbitrary-precision integers are zero 200⟩ ≡

```
procedure checkzero(var  $a, b : \text{string}$ );
  var  $a1, b1 : \text{string}$ ;
  begin ⟨Convert “−0” into zero 201⟩;
  ⟨Trim leading zeros from numerator and denominator 202⟩;
  end;
```

This code is used in section 197.

201. ⟨Convert “−0” into zero 201⟩ ≡

```
if  $\text{copy}(a, 1, 2) = \text{'-0'}$  then
  begin  $\text{debug\_num}(\text{WriteLn}(\text{infofile}, \text{'a=-0'}))$ ;
   $a \leftarrow \text{'0'}$ ;
  end;
if  $\text{copy}(b, 1, 2) = \text{'-0'}$  then
  begin  $\text{debug\_num}(\text{WriteLn}(\text{infofile}, \text{'b=-0'}))$ ;
   $b \leftarrow \text{'0'}$ ;
  end
```

This code is used in section 200.

202. \langle Trim leading zeros from numerator and denominator 202 $\rangle \equiv$

```

a1  $\leftarrow$  trimlz(a);
if a1  $\neq$  a then
  begin debug_num(WriteLn(Infofile, 'ZEROS1:', a));
  a  $\leftarrow$  a1;
  end;
b1  $\leftarrow$  trimlz(b);
if b1  $\neq$  b then
  begin debug_num(WriteLn(Infofile, 'ZEROS2:', b));
  b  $\leftarrow$  b1;
  end

```

This code is used in section 200.

203. Since arbitrary precision numbers (as Strings) are negative if they begin with a leading “-” character, it is easy to obtain the absolute value (just delete the minus sign). This assumes there are “double negatives” like “--5”; the “absolute value” of “--5” would yield “-5”, which should be a bug.

\langle Basic arithmetic operations declarations 203 $\rangle \equiv$

function Abs(*a* : string): string;

See also sections 224, 231, 233, 235, 237, 242, 247, 249, 251, and 253.

This code is used in section 197.

204. \langle Absolute value for an arbitrary-precision number 204 $\rangle \equiv$

```

function Abs(a : string): string;
  begin if length(a) > 0 then
    if a[1] = '-' then delete(a, 1, 1);
    Abs  $\leftarrow$  a;
  end;

```

This code is used in section 197.

205. When checking $a \leq b$ for two non-negative integers, written as Strings (without leading zeros) you can check if the length of *a* is less than the length of *b*.

If the length of *b* is less than the length of *a*, then $b < a$.

When the length of the two Strings are equal, use lexicographic ordering to determine which is less.

\langle Test if one arbitrary-precision number is less than or equal to another 205 $\rangle \equiv$

function _leq(*a*, *b* : string): boolean; { compare two positive integers }

```

var i, x, y, z: integer;
begin debug_num(WriteLn(Infofile, '_leq(', a, ', ', b, ')'));
  checkzero(a, b);
  if length(a) < length(b) then _leq  $\leftarrow$  true
  else if length(a) > length(b) then _leq  $\leftarrow$  false
  else  $\langle$  Compare two positive integers with same number of digits 206  $\rangle$ ;
  end;

```

See also sections 207, 208, and 209.

This code is used in section 197.

206. $\langle \text{Compare two positive integers with same number of digits } 206 \rangle \equiv$

```

begin for  $i \leftarrow 1$  to  $\text{length}(a)$  do
  begin  $\text{val}(a[i], x, z); \text{val}(b[i], y, z);$ 
  if  $x > y$  then
    begin  $\_leq \leftarrow \text{false}; \text{exit};$ 
  end;
  if  $x < y$  then
    begin  $\_leq \leftarrow \text{true}; \text{exit};$ 
  end;
end;
 $\_leq \leftarrow \text{true};$ 
end

```

This code is used in section 205.

207. Now the *general* case is when a and b are arbitrary-precision *integers*. If a starts with a minus sign and b starts with a minus sign, then test if $a \geq b$.

When a does not start with a minus sign, but b *does* start with a minus sign, then we're done: $b < a$.

When neither a nor b starts with a minus sign, then we use $_leq(a, b)$ to determine the result.

$\langle \text{Test if one arbitrary-precision number is less than or equal to another } 205 \rangle + \equiv$

```

function  $\_leq(a, b : \text{string})$ : Boolean;
begin  $\text{debug\_num}(\text{WriteLn}(\text{infofile}, \text{'leq('}, a, \text{'}, \text{'}, b, \text{'})'}));$ 
 $\text{checkzero}(a, b);$ 
if  $a = b$  then  $\_leq \leftarrow \text{true}$ 
else begin if  $(a[1] = \text{'-'}) \wedge (b[1] \neq \text{'-'})$  then  $\_leq \leftarrow \text{true};$ 
  if  $(a[1] = \text{'-'}) \wedge (b[1] = \text{'-'})$  then  $\_leq \leftarrow \neg \_leq(\text{abs}(a), \text{abs}(b));$ 
  if  $(a[1] \neq \text{'-'}) \wedge (b[1] = \text{'-'})$  then  $\_leq \leftarrow \text{false};$ 
  if  $(a[1] \neq \text{'-'}) \wedge (b[1] \neq \text{'-'})$  then  $\_leq \leftarrow \_leq(a, b);$ 
end;
end;

```

208. Testing if $a \geq b$ is simply testing if $b \leq a$ after normalizing the Strings. Mizar implements this by $(a > b) \vee (a = b)$, since $\neg(a \leq b)$ is identical to $a > b$.

$\langle \text{Test if one arbitrary-precision number is less than or equal to another } 205 \rangle + \equiv$

```

function  $\_geq(a, b : \text{string})$ : Boolean;
begin  $\text{debug\_num}(\text{WriteLn}(\text{infofile}, \text{'geq('}, a, \text{'}, \text{'}, b, \text{'})'}));$ 
 $\text{checkzero}(a, b);$ 
 $\_geq \leftarrow (\neg \_leq(a, b)) \vee (a = b);$ 
end;

```

209. Similarly, we may check if $a < b$ by testing $a \neq b$ and $a \leq b$.

$\langle \text{Test if one arbitrary-precision number is less than or equal to another } 205 \rangle + \equiv$

```

function  $\_lt(a, b : \text{string})$ : Boolean;
begin  $\text{debug\_num}(\text{WriteLn}(\text{infofile}, \text{'lt('}, a, \text{'}, \text{'}, b, \text{'})'}));$ 
 $\text{checkzero}(a, b); \_lt \leftarrow (a \neq b) \wedge (\_leq(a, b));$ 
end;

function  $\_gt(a, b : \text{string})$ : Boolean;
begin  $\text{debug\_num}(\text{WriteLn}(\text{infofile}, \text{'gt('}, a, \text{'}, \text{'}, b, \text{'})'}));$ 
 $\text{checkzero}(a, b); \_gt \leftarrow \neg \_leq(a, b);$ 
end;

```

Subsection 9.1.1. Arithmetic operations

210. Now we get to some interesting bits.

We have `_Add` for the addition of two non-negative integers. The basic strategy is to go digit-by-digit, use the PASCAL-provided integer arithmetic, manually “carrying” 1 if necessary.

The basic strategy is to initialize `a1` to be the larger of the two numbers, and `b1` to the smaller of the two numbers. Then generically we will have

$$\begin{array}{r} a_n \dots a_{m+1} \ a_m \ a_{m-1} \dots a_1 \\ + \qquad \qquad \qquad b_m \ b_{m-1} \dots b_1 \\ \hline \end{array} \quad (210.1)$$

We will separate this out into two sums. First we compute

$$\begin{array}{r} a_m \ a_{m-1} \dots a_1 \\ + \ b_m \ b_{m-1} \dots b_1 \\ \hline c_{m+1} \ r_m \ r_{m-1} \dots r_1 \end{array} \quad (210.2)$$

Then we will compute

$$\begin{array}{r} a_n \dots a_{m+1} \\ + \qquad \qquad \qquad c_{m+1} \\ \hline r_{n+1} \ r_n \dots r_{m+1} \end{array} \quad (210.3)$$

The result is assembled from the digits $r_{n+1}r_n \dots r_1$.

⟨Arithmetic for arbitrary-precision integers 210⟩ ≡

```
function _Add(a, b : String): string;
  var c, x, y, z, v: integer; i: integer; a1, b1, s, r: string;
  begin ⟨Copy a and b into a1, b1 ensuring a1 is a longer string 211⟩;
  r ← “”; c ← 0;
  begin ⟨Add a1 and b1 as in step 1, Eq (210.2) 212⟩;
  ⟨Carry the cm+1 as in step 2, Eq (210.3) 213⟩;
  end; _Add ← trimlz(r);
end;
```

See also sections 214, 218, 220, 223, 225, 232, 234, 236, 238, 243, 248, 250, 252, and 254.

This code is used in section 197.

```
211. ⟨Copy a and b into a1, b1 ensuring a1 is a longer string 211⟩ ≡
  a1 ← a; b1 ← b; debug_num(WriteLn(infofile, “_Add(“, a1, “”, b1, “)”)); checkzero(a1, b1);
  if length(a1) < length(b1) then
    begin s ← b1; b1 ← a1; a1 ← s;
  end
```

This code is used in section 210.

```
212. ⟨Add a1 and b1 as in step 1, Eq (210.2) 212⟩ ≡
  for i ← 0 to length(b1) − 1 do {step 1, Eq (210.2)}
    begin val(a1[length(a1) − i], x, z); val(b1[length(b1) − i], y, z);
    if x + y + c > 9 then
      begin v ← (x + y + c) − 10; c ← 1;
    end
    else begin v ← x + y + c; c ← 0;
    end;
    Str(v, s); r ← s + r;
  end
```

This code is used in section 210.

213. $\langle \text{Carry the } c_{m+1} \text{ as in step 2, Eq (210.3) } \mathbf{213} \rangle \equiv$
for $i \leftarrow \text{length}(b1)$ **to** $\text{length}(a1) - 1$ **do** { step 2, Eq (210.3) }
 begin $\text{val}(a1[\text{length}(a1) - i], x, z);$
 if $x + c > 9$ **then**
 begin $v \leftarrow (x + c) - 10; c \leftarrow 1;$
 end
 else begin $v \leftarrow x + c; c \leftarrow 0;$
 end;
 $\text{Str}(v, s); r \leftarrow s + r;$
 end;
if $c = 1$ **then** $r \leftarrow \text{'1'} + r$

This code is used in section [210](#).

214. Subtraction is a bit trickier, because of the “borrowing” operation.

Also note that $\text{Sub}(a, b)$ will start by computing $a_1 \leftarrow \max(a, b)$ and $b_1 \leftarrow \min(a, b)$, then return $a_1 - b_1$. This means the result is always non-negative.

$\langle \text{Arithmetic for arbitrary-precision integers } \mathbf{210} \rangle + \equiv$
function $\text{Sub}(a, b : \text{string}) : \text{string};$
 var $x, y, z, v : \text{integer}; i : \text{integer}; a1, b1, s, r : \text{string};$
 $\langle \text{“Borrow 1” procedure for Sub } \mathbf{215} \rangle$
 begin $a1 \leftarrow a; b1 \leftarrow b;$
 $\text{debug_num}(\text{WriteLn}(\text{infofile}, \text{'_Sub('}, a1, \text{'}, \text{'}, b1, \text{'})'}));$
 $\text{checkzero}(a1, b1); \langle \text{Swap } a1 \text{ and } b1 \text{ if } b1 \leq a1 \mathbf{216} \rangle;$
 $r \leftarrow \text{''};$
 begin
 for $i \leftarrow 0$ **to** $\text{length}(b1) - 1$ **do** $\langle \text{Subtract the } i^{\text{th}} \text{ digit of } b1 \text{ from } a1 \mathbf{217} \rangle;$
 for $i \leftarrow \text{length}(a1) - \text{length}(b1)$ **downto** 1 **do** { nothing left to subtract }
 begin $r \leftarrow a1[i] + r;$ **end;** { so copy remaining digits of minuend }
 end;
 $\text{Sub} \leftarrow \text{trimlz}(r);$
end ;

215. This is a private “helper function” for subtraction.

$\langle \text{“Borrow 1” procedure for Sub } \mathbf{215} \rangle \equiv$
procedure $\text{Borrow}(k : \text{integer});$
 var $xx, zz : \text{integer}; sx : \text{string};$
 begin $\text{val}(a1[k - 1], xx, zz);$
 if $xx \geq 1$ **then**
 begin $xx \leftarrow xx - 1; \text{Str}(xx, sx); a1[k - 1] \leftarrow sx[1];$
 end
 else begin $a1[k - 1] \leftarrow \text{'9'}; \text{borrow}(k - 1);$
 end;
end;

This code is used in section [214](#).

216. $\langle \text{Swap } a1 \text{ and } b1 \text{ if } b1 \leq a1 \mathbf{216} \rangle \equiv$
 if $\neg \text{leq}(b1, a1)$ **then**
 begin $s \leftarrow b1; b1 \leftarrow a1; a1 \leftarrow s;$
 end

This code is used in section [214](#).

217. We compute $v = x - y$ where $x \leftarrow (a1)_i$ (possibly borrowing from the next digit of $a1$) and $y \leftarrow (b1)_i$. We store this as the next digit in the result r .

\langle Subtract the i^{th} digit of $b1$ from $a1$ 217 $\rangle \equiv$
begin $val(a1[length(a1) - i], x, z); val(b1[length(b1) - i], y, z);$
if $x < y$ **then**
 begin $borrow(length(a1) - i); x \leftarrow x + 10;$ **end**;
 $v \leftarrow x - y; Str(v, s); r \leftarrow s + r;$
end

This code is used in section 214.

218. Multiplication. Multiplication of a by b works digit-by-digit, in the sense that for each digit b_j of b , we need to multiply a by b_j . The function `_Mul1` does this.

\langle Arithmetic for arbitrary-precision integers 210 $\rangle + \equiv$
function `_Mul1` ($a : string; y : integer$): $string$;
 var $c, x, z, v : integer; i : integer; s, r : string$;
 begin $debug_num(WriteLn(Infofile, _Mul1(_, a, _, _, y, _)))$;
 $r \leftarrow _0$; $c \leftarrow 0$;
 for $i \leftarrow 0$ **to** $length(a) - 1$ **do** \langle Multiply i^{th} digit of a by y 219 \rangle ;
 if $c \neq 0$ **then**
 begin $Str(c, s); r \leftarrow s + r$;
 end;
 $_mul1 \leftarrow trimlz(r)$;
end;

219. \langle Multiply i^{th} digit of a by y 219 $\rangle \equiv$
begin $val(a[length(a) - i], x, z)$;
if $x * y + c > 9$ **then**
 begin $v \leftarrow (x * y + c) \bmod 10; c \leftarrow (x * y + c) \div 10$;
 end
else begin $v \leftarrow x * y + c; c \leftarrow 0$;
 end;
 $Str(v, s); r \leftarrow s + r$;
end

This code is used in section 218.

220. Then multiplication proper amounts to decomposing b into its decimal expansion $\sum_k b_k 10^k$ and computing $(a \times b_k) 10^k$.

\langle Arithmetic for arbitrary-precision integers 210 $\rangle + \equiv$
function `_Mul` ($a, b : string$): $string$;
 var $y, z : integer; i, j : integer; a1, b1, s, r : string$;
 begin \langle Copy a into $a1$ and b into $b1$, ensuring $b1$ is a shorter string 221 \rangle ;
 $r \leftarrow _0$;
 for $i \leftarrow 0$ **to** $length(b1) - 1$ **do** \langle Multiply i^{th} digit of $b1$ to $a1$ and add it to r 222 \rangle ;
 $_Mul \leftarrow trimlz(r)$;
end;

221. $\langle \text{Copy } a \text{ into } a1 \text{ and } b \text{ into } b1, \text{ ensuring } b1 \text{ is a shorter string } 221 \rangle \equiv$
 $a1 \leftarrow a; b1 \leftarrow b;$
 $debug_num(WriteLn(infofile, \text{'_Mul'}, a1, \text{'}, b1, \text{'})$);
 $checkzero(a1, b1);$
if $length(a1) < length(b1)$ **then**
 begin $s \leftarrow b1; b1 \leftarrow a1; a1 \leftarrow s;$ **end**

This code is used in section 220.

222. $\langle \text{Multiply } i^{\text{th}} \text{ digit of } b1 \text{ to } a1 \text{ and add it to } r \text{ } 222 \rangle \equiv$
begin $val(b1[length(b1) - i], y, z); s \leftarrow _mul1(a1, y);$
for $j \leftarrow 0$ **to** $i - 1$ **do** $s \leftarrow s + \text{'0'}$;
 $r \leftarrow _Add(r, s);$
end

This code is used in section 220.

223. Division. The basic design is similar to multiplication. We will try to divide a by b (which is zero whenever $b > a$). When $b \leq a$, then a/b is the largest digit $i \in \{1, 2, \dots, 9\}$ such that $bi \leq a$.

There appears to be an implicit assumption that $a < 10b$, and both $a \geq 0$ and $b \geq 0$ are non-negative integers.

[[There is no leading zero to r , so the $trimlz(r)$ statement is completely superfluous.]]

$\langle \text{Arithmetic for arbitrary-precision integers } 210 \rangle + \equiv$

function $_Div1(a, b : string) : string;$
var $i : integer; r : string;$
begin $debug_num(WriteLn(infofile, \text{'_Div1'}, a, \text{'}, b, \text{'})$);
 $checkzero(a, b);$
if $\neg_leq(b, a)$ **then** $_div1 \leftarrow \text{'0'}$ { $a/b = 0$ when $b > a$ }
else for $i \leftarrow 9$ **downto** 1 **do**
 begin $Str(i, r);$
 if $_leq(_mul(b, r), a)$ **then**
 begin $_div1 \leftarrow trimlz(r); exit;$
 end;
 end;
end;

224. Calculate q such that $a = bq + r$ for some $0 \leq r < b$, assuming $a \geq 0$ and $b \geq 0$.

$\langle \text{Basic arithmetic operations declarations } 203 \rangle + \equiv$

function $_Div(a, b : string) : string;$

225. $\langle \text{Arithmetic for arbitrary-precision integers } 210 \rangle + \equiv$

function $_Div(a, b : string) : string;$
var $z, c, i : integer; s, r, rs : string; b_GPC : Boolean;$
 $\langle \text{Get the next digit for dividing arbitrary-precision integers } 228 \rangle$
begin $debug_num(WriteLn(infofile, \text{'_Div'}, a, \text{'}, b, \text{'})$);
 $checkzero(a, b);$
if $a = b$ **then** $_div \leftarrow \text{'1'}$
else if $\neg_leq(b, a)$ **then** $_div \leftarrow \text{'0'}$
else $\langle \text{Long division of } a \text{ by } b \text{ } 226 \rangle;$
end;

226. We take the leading digits of a and treat them as a new integer $s = a_1 \cdots a_z$. We only take as many digits necessary to make $b \leq s$ but with $a_1 \cdots a_{z-1} < b$. Then we compute rs such that $s = b \times rs + r$ for some $0 \leq r < b$. We update $s \leftarrow s - rs \times b$ and move to the next digit of a (updating s) using the *gets* function. This reflects “long division” as taught in gradeschool.

```

⟨ Long division of  $a$  by  $b$  226 ⟩ ≡
  begin  $s \leftarrow \text{``}$ ;  $r \leftarrow \text{``}$ ;  $z \leftarrow 1$ ;
  for  $i \leftarrow 1$  to  $\text{length}(b)$  do  $s \leftarrow s + a[i]$ ; { copy leading digits of  $a$  into  $s$  }
  ⟨ Ensure  $b \leq s$  by adding another digit of  $a$ , initialize  $z$  227 ⟩; {  $z \leftarrow \text{length}(s)$  }
  repeat  $rs \leftarrow \text{div1}(s, b)$ ;  $r \leftarrow r + rs$ ; gets;  $b\_GPC \leftarrow \text{leq}(b, s)$ ;
  until  $\neg b\_GPC$ ;
   $\text{div} \leftarrow \text{trimlz}(r)$ ;
end

```

This code is used in section 225.

227. ⟨ Ensure $b \leq s$ by adding another digit of a , initialize z 227 ⟩ ≡

```

  if  $\text{leq}(b, s)$  then  $z \leftarrow \text{length}(b)$ 
  else begin  $s \leftarrow s + a[\text{length}(b) + 1]$ ;  $z \leftarrow \text{length}(b) + 1$ ; end

```

This code is used in section 226.

228. We just need to “get the next digit” of a , if available, and append it to s .

```

  define remaining_digits_are_zero ≡ ( $\text{trimlz}(\text{copy}(a, z + c, \text{length}(a))) = \text{``0``}$ )
⟨ Get the next digit for dividing arbitrary-precision integers 228 ⟩ ≡
  procedure gets;
  var  $j$ : integer;
  begin  $c \leftarrow 1$ ;  $s \leftarrow \text{Sub}(s, \text{mul}(rs, b))$ ; { i.e.,  $s \leftarrow s \bmod b$  }
  if  $(s = \text{``0``}) \wedge \text{remaining\_digits\_are\_zero}$  then
    ⟨ Copy remainder of  $a$  into  $s$ , and terminate the function 229 ⟩;
  if  $z + 1 \leq \text{length}(a)$  then ⟨ Append next digit of  $a$  onto  $s$ , incrementing  $c$  230 ⟩;
  while  $(\neg \text{leq}(b, s)) \wedge (z + c \leq \text{length}(a))$  do ⟨ Append next digit of  $a$  onto  $s$ , incrementing  $c$  230 ⟩;
   $z \leftarrow z + c - 1$ ;
  end; { gets }

```

This code is used in section 225.

229. ⟨ Copy remainder of a into s , and terminate the function 229 ⟩ ≡

```

  begin debug_num( $\text{WriteLn}(\text{infofile}, \text{``Rewriting\_zeros:``}, \text{copy}(a, z + c, \text{length}(a))))$ );
   $r \leftarrow r + \text{copy}(a, z + c, \text{length}(a))$ ; exit;
end

```

This code is used in section 228.

230. ⟨ Append next digit of a onto s , incrementing c 230 ⟩ ≡

```

  begin  $s \leftarrow s + a[z + c]$ ; inc( $c$ );
  if  $(\neg \text{leq}(b, s))$  then  $r \leftarrow r + \text{``0``}$ ; { shortcut: division will add a zero digit anyways }
end

```

This code is used in sections 228 and 228.

231. Modulo. We can compute $a \bmod b$ by observing if $a < b$ then we should obtain a . Otherwise, we should compute $q \leftarrow a \text{ div } b$, then $a - qb$ is $a \bmod b$.

⟨ Basic arithmetic operations declarations 203 ⟩ \vdash

```

function  $\text{Mod}(a, b : \text{string})$ : string;

```

232. \langle Arithmetic for arbitrary-precision integers 210 $\rangle + \equiv$

```
function _Mod(a, b : string): string;
  var r: string;
  begin debug_num( WriteLn( infofile, ^_Mod( ^, a, ^, ^, b, ^ ) ));
    checkzero(a, b);
    if le(a, b) then r ← a
    else r ← _Sub(a, _Mul(b, _Div(a, b)));
    _Mod ← trimlz(r);
    debug_num( WriteLn( infofile, ^End_ _Mod: ^, r ));
  end;
```

233. Greatest common divisor. We can compute $\gcd(a, b)$ first by setting $a_1 \leftarrow |a|$ and $b_1 \leftarrow |b|$ (since $\gcd(a, b) = \gcd(|a|, |b|)$). Then we handle the special cases:

- (1) $a_1 = 1$ or $b_1 = 1$, then $\gcd(a_1, b_1) = 1$
- (2) $a_1 = 0$ and $b_1 \neq 0$, then $\gcd(a_1, b_1) = b_1$
- (3) $a_1 \neq 0$ and $b_1 = 0$, then $\gcd(a_1, b_1) = a_1$
- (4) $a_1 = b_1$, then $\gcd(a_1, b_1) = a_1$

Otherwise, we end up in the default case, which is handled by the **while** loop.

```
define assign_gcd_and_jump(#) ≡
  begin r ← #; goto ex; end
 $\langle$  Basic arithmetic operations declarations 203  $\rangle + \equiv$ 
function GCD(a, b : string): string; { *Note: always returns a positive value }
```

234. \langle Arithmetic for arbitrary-precision integers 210 $\rangle + \equiv$

```
function GCD(a, b : string): string;
  label ex;
  var a1, b1, p, r: string;
  begin a1 ← a; b1 ← b;
    debug_num( WriteLn( infofile, ^GCD( ^, a1, ^, ^, b1, ^ ) ));
    checkzero(a1, b1); a1 ← abs(a1); b1 ← abs(b1);
    if (a1 = ^1^ ) ∨ (b1 = ^1^ ) then assign_gcd_and_jump(^1^ );
    if (a1 = ^0^ ) ∧ (b1 ≠ ^0^ ) then assign_gcd_and_jump(b1);
    if (b1 = ^0^ ) ∧ (a1 ≠ ^0^ ) then assign_gcd_and_jump(a1);
    if a1 = b1 then assign_gcd_and_jump(a1);
    while gt(b1, ^0^ ) do { 0 < b1 }
      begin p ← b1; b1 ← _Mod(a1, b1); a1 ← p end;
    r ← a1;
  ex: GCD ← r;
    debug_num( WriteLn( infofile, ^End_ GCD: ^, r ));
  end;
```

235. Least common multiple. We recall $\text{lcm}(a, b) = |ab| / \gcd(|a|, |b|)$.

\langle Basic arithmetic operations declarations 203 $\rangle + \equiv$
function LCM(a, b : string): string; { *Note: always returns a positive value }

236. $\langle \text{Arithmetic for arbitrary-precision integers 210} \rangle + \equiv$

```
function LCM( $a, b : \text{string}$ ):  $\text{string}$ ;
  var  $a1, b1, r : \text{string}$ ;
  begin  $a1 \leftarrow a$ ;  $b1 \leftarrow b$ ;
   $\text{debug\_num}(\text{WriteLn}(\text{infofile}, \text{'LCM('}, a1, \text{'}, \text{'}, b1, \text{'})'}));$ 
   $\text{checkzero}(a1, b1)$ ;  $a1 \leftarrow \text{abs}(a1)$ ;  $b1 \leftarrow \text{abs}(b1)$ ;  $r \leftarrow \text{DivA}(\text{Mul}(a1, b1), \text{GCD}(a1, b1))$ ;  $\text{LCM} \leftarrow r$ ;
   $\text{debug\_num}(\text{WriteLn}(\text{infofile}, \text{'End\_LCM: '}, r));$ 
  end;
```

237. Addition. This is a bit obfuscated with the reliance of **goto** *ex*, but the basic idea is (recalling that $\text{Sub}(a, b)$ calculates $\max(a, b) - \min(a, b)$ for $a \geq 0$ and $b \geq 0$):

- (1) If $a < 0$ and $b < 0$, then $a + b = -(|a| + |b|)$
- (2) Else if $a \geq 0$ and $b \geq 0$, then $a + b$ is computed using Add
- (3) Else if $a < 0$ and $b \geq 0$, then we have two cases
 - (i) If $|a| \geq b$, compute $a + b = -(|a| - b)$
 - (ii) Otherwise, $a + b = b - |a|$
- (4) Else if $a \geq 0$ and $b < 0$, then $a + b = a - |b|$
- (5) Otherwise, when $a \geq 0$ and $b \geq 0$, $a + b$ is computed using Add .

$\langle \text{Basic arithmetic operations declarations 203} \rangle + \equiv$

```
function Add( $a, b : \text{string}$ ):  $\text{string}$ ;
```

238. $\langle \text{Arithmetic for arbitrary-precision integers 210} \rangle + \equiv$

```
function Add( $a, b : \text{string}$ ):  $\text{string}$ ;
  label  $ex$ ;
  var  $r : \text{string}$ ;
  begin  $\text{debug\_num}(\text{WriteLn}(\text{infofile}, \text{'Add('}, a, \text{'}, \text{'}, b, \text{'})'}));$ 
   $\text{checkzero}(a, b)$ ;
  if ( $a[1] = \text{'-'} \wedge b[1] = \text{'-'} \wedge (a[2] \neq \text{'0'} \vee b[2] \neq \text{'0'})$ ) then  $\langle \text{Add two negative integers, and goto } ex \text{ 239} \rangle$ ;
  if ( $a[1] \neq \text{'-'} \wedge b[1] \neq \text{'-'} \wedge (a[2] \neq \text{'0'} \vee b[2] \neq \text{'0'})$ ) then
    begin  $r \leftarrow \text{Add}(a, b)$ ; goto  $ex$ ; end;
  if ( $a[1] = \text{'-'} \wedge b[1] \neq \text{'-'} \wedge (a[2] \neq \text{'0'} \vee b[2] \neq \text{'0'})$ ) then  $\langle \text{Calculate } (-a) + b = b - a \text{ and goto } ex \text{ 240} \rangle$ ;
  if ( $a[1] \neq \text{'-'} \wedge b[1] = \text{'-'} \wedge (a[2] \neq \text{'0'} \vee b[2] \neq \text{'0'})$ ) then  $\langle \text{Calculate } a + (-b) = a - b \text{ and goto } ex \text{ 241} \rangle$ ;
   $ex : \text{Add} \leftarrow r$ ;
   $\text{debug\_num}(\text{WriteLn}(\text{infofile}, \text{'End\_Add: '}, r));$ 
  end;
```

239. $\langle \text{Add two negative integers, and goto } ex \text{ 239} \rangle \equiv$

```
begin  $r \leftarrow \text{'-'} + \text{Add}(\text{abs}(a), \text{abs}(b))$ ;
if  $r = \text{'-0'}$  then  $r \leftarrow \text{'0'}$ ;
goto  $ex$ ;
end
```

This code is used in section 238.

240. $\langle \text{Calculate } (-a) + b = b - a \text{ and goto } ex \text{ 240} \rangle \equiv$

```
if  $gt(\text{abs}(a), b)$  then
  begin  $r \leftarrow \text{'-'} + \text{Sub}(\text{abs}(a), b)$ ;
  if  $r = \text{'-0'}$  then  $r \leftarrow \text{'0'}$ ;
  goto  $ex$ ;
  end
else begin  $r \leftarrow \text{Sub}(\text{abs}(a), b)$ ; goto  $ex$ ; end
```

This code is used in section 238.

241. $\langle \text{Calculate } a + (-b) = a - b \text{ and goto } ex \text{ 241} \rangle \equiv$
if $gt(abs(b), a)$ **then**
 begin $r \leftarrow '-' + _Sub(abs(b), a);$
 if $r = '-0'$ **then** $r \leftarrow '0';$
 goto $ex;$
 end
else begin $r \leftarrow _Sub(abs(b), a);$ **goto** $ex;$ **end**

This code is used in section 238.

242. Subtraction. Now, given two arbitrary precision integers, we can compute their difference. Again, **goto** ex obfuscates the flow here, but the basic logic is:

- (1) If $a < 0$ and $b \geq 0$, then $a - b = -(|a| + b)$
- (2) Else if $a \geq 0$ and $b < 0$, then $a - b = a + |b|$
- (3) Else if $a < 0$ and $b < 0$, then we have two cases
 - (i) If $|a| > |b|$, then $a - b = -(|a| - |b|)$
 - (ii) Otherwise $|a| \leq |b|$, so $a - b = |a| - |b|$
- (4) Else if $a \geq 0$ and $b \geq 0$, then we have two cases
 - (i) If $b > a$, then $a - b = -(b - a)$
 - (ii) Otherwise compute $a - b$ using $_Sub(a, b)$

Testing if $x < 0$ is done by checking $sgn(x) = -1$, and $x \geq 0$ tests if $sgn(x) \neq -1$.

$\langle \text{Basic arithmetic operations declarations 203} \rangle + \equiv$

function $Sub(a, b : string) : string;$

243. $\langle \text{Arithmetic for arbitrary-precision integers 210} \rangle + \equiv$

function $Sub(a, b : string) : string;$
label $ex;$
var $r : string;$
begin $debug_num(WriteLn(infofile, 'Sub(' , a, ', ', b, ')');$
 $checkzero(a, b);$
if $(a[1] = '-') \wedge (b[1] \neq '-')$ **then** $\langle \text{Calculate } (-a) - b = -(a + b) \text{ and goto } ex \text{ 244} \rangle;$
if $(a[1] \neq '-') \wedge (b[1] = '-')$ **then**
 begin $r \leftarrow _Add(a, abs(b));$ **goto** $ex;$ **end;**
if $(a[1] = '-') \wedge (b[1] = '-')$ **then** $\langle \text{Calculate } (-a) - (-b) \text{ and goto } ex \text{ 245} \rangle;$
if $(a[1] \neq '-') \wedge (b[1] \neq '-')$ **then** $\langle \text{Calculate difference of two positive integers 246} \rangle;$
 $ex : Sub \leftarrow r;$
 $debug_num(WriteLn(infofile, 'End_Sub: ', r));$
end;

244. $\langle \text{Calculate } (-a) - b = -(a + b) \text{ and goto } ex \text{ 244} \rangle \equiv$

begin $r \leftarrow '-' + _Add(abs(a), b);$
if $r = '-0'$ **then** $r \leftarrow '0';$
goto $ex;$
end

This code is used in section 243.

245. $\langle \text{Calculate } (-a) - (-b) \text{ and } \text{goto } ex \text{ 245} \rangle \equiv$
if $gt(abs(a), abs(b))$ **then**
 begin $r \leftarrow '-' + _Sub(abs(a), abs(b));$
 if $r = '-0'$ **then** $r \leftarrow '0'$;
 goto $ex;$
 end
else begin $r \leftarrow _Sub(abs(a), abs(b));$ **goto** $ex;$ **end**

This code is used in section 243.

246. $\langle \text{Calculate difference of two positive integers 246} \rangle \equiv$
if $gt(b, a)$ **then**
 begin $r \leftarrow '-' + _Sub(b, a);$
 if $r = '-0'$ **then** $r \leftarrow '0'$;
 goto $ex;$
 end
else begin $r \leftarrow _Sub(a, b);$ **goto** $ex;$ **end**

This code is used in section 243.

247. Multiplication of arbitrary-precision integers. We calculate the product of a with b by handling the case where $\text{sgn}(a) \neq \text{sgn}(b)$ as $ab = -|a| \cdot |b|$. Otherwise we can just rely on the $_Mul(a, b)$ to do our work.

$\langle \text{Basic arithmetic operations declarations 203} \rangle + \equiv$
function $Mul(a, b : string) : string;$

248. $\langle \text{Arithmetic for arbitrary-precision integers 210} \rangle + \equiv$
function $Mul(a, b : string) : string;$
 label $ex;$
 var $r : string;$
 begin $debug_num(WriteLn(infofile, 'Mul(' , a , ', ' , b , ')');$
 $checkzero(a, b);$
 if $((a[1] = '-' \wedge (b[1] \neq '-')) \vee ((a[1] \neq '-') \wedge (b[1] = '-')))$ **then**
 begin $r \leftarrow '-' + _Mul(abs(a), abs(b));$
 if $r = '-0'$ **then** $r \leftarrow '0'$;
 end
 else $r \leftarrow _Mul(abs(a), abs(b));$
 $ex : Mul \leftarrow r;$
 $debug_num(WriteLn(infofile, 'End_Mul: ' , r));$
 end;

249. DivA. This is the division for arbitrary-precision integers. Like multiplication, we handle the case $\text{sgn}(a) \neq \text{sgn}(b)$ by computing $a/b = -|a|/|b|$.

$\langle \text{Basic arithmetic operations declarations 203} \rangle + \equiv$
function $DivA(a, b : string) : string;$
 { *Note: divides absolute values and preserves the sign of the division }

250. \langle Arithmetic for arbitrary-precision integers 210 $\rangle + \equiv$

```
function DivA(a, b : string): string;
  label ex;
  var r: string;
  begin debug_num( WriteLn( infofile, 'DivA( ', a, ', ', b, ' )' ));
  checkzero(a, b);
  if ((a[1] = '-' )  $\wedge$  (b[1]  $\neq$  '-'))  $\vee$  ((a[1]  $\neq$  '-')  $\wedge$  (b[1] = '-')) then
    begin r  $\leftarrow$  '-' + _Div(abs(a), abs(b));
    if r = '-0' then r  $\leftarrow$  '0';
    end
  else r  $\leftarrow$  _Div(abs(a), abs(b));
ex: DivA  $\leftarrow$  r;
  debug_num( WriteLn( infofile, 'End_DivA: ', r ));
end;
```

251. Testing for primality. We can test if a given arbitrary-precision integer is prime or not. Specifically, we restrict attention to *positive* integers.

The **while** loop calculates $Mul(i, i)$ because Fermat observed we only need to check numbers *up to* $\lceil \sqrt{x} \rceil$ as prime factors of x . But this calculation is a bit costly. This could be approximated by taking the length of the underlying String $n = |s|$ and looking at the leading $\lceil n/2 \rceil$ digits s_{lead} . It's not hard to see that the number x_{lead} described by s_{lead} satisfies $x_{lead}^2 \geq x$.

\langle Basic arithmetic operations declarations 203 $\rangle + \equiv$

```
function IsPrime(a : string): Boolean;
```

252. \langle Arithmetic for arbitrary-precision integers 210 $\rangle + \equiv$

```
function IsPrime(a : string): Boolean;
  var i: string; r: Boolean;
  begin if leq('2', a) then
    begin r  $\leftarrow$  true; i  $\leftarrow$  '2';
    while leq(Mul(i, i), a) do
      begin if GCD(a, i) = i then
        begin r  $\leftarrow$  false; break; end;
      i  $\leftarrow$  Add(i, '1');
    end;
  end
  else r  $\leftarrow$  false;
  IsPrime  $\leftarrow$  r;
end;
```

253. Divides relation. We can check if “ x divides y ” by testing if $\gcd(x, y) = |x|$.

\langle Basic arithmetic operations declarations 203 $\rangle + \equiv$

```
function Divides(a, b : String): boolean;
```

254. \langle Arithmetic for arbitrary-precision integers 210 $\rangle + \equiv$

```
function Divides(a, b : string): Boolean;
  var r: Boolean;
  begin r  $\leftarrow$  GCD(a, b) = abs(a); Divides  $\leftarrow$  r;
end;
```

Section 9.2. ARBITRARY-PRECISION RATIONAL ARITHMETIC

255. Rational numbers are a pair of arbitrary precision integers (represented as a String). The convention is that the denominator is a *strictly positive* integer.

⟨Types for arbitrary-precision arithmetic 255⟩ ≡
`Rational = record Num, Den: string
 end;`

See also section 275.

This code is used in section 197.

256. “Zero” and “one” are frequently used rational numbers, so we should define them as constants.

⟨Zero and units for arbitrary-precision 256⟩ ≡
`RZero: Rational = (Num : ^0^; Den : ^1^);
 ROne: Rational = (Num : ^1^; Den : ^1^);`

See also section 276.

This code is used in section 197.

257. Rational arithmetic. Now we begin the rational arithmetic “in earnest”. The first thing to do is provide a way to compute the reduced form for a fraction, i.e.,

$$\frac{n}{d} = \frac{n/\gcd(n,d)}{d/\gcd(n,d)}$$

⟨Rational arithmetic declarations 257⟩ ≡
procedure *RationalReduce*(**var** *r* : *Rational*);

See also sections 259, 261, 263, 265, 267, 269, 271, and 273.

This code is used in section 197.

258. ⟨Arbitrary-precision rational arithmetic 258⟩ ≡
procedure *RationalReduce*(**var** *r* : *Rational*);
`var lGcd: String;
 begin lGcd ← gcd(r.Num, r.Den); r.Num ← diva(r.Num, lGcd); r.Den ← diva(r.Den, lGcd);
 end;`

See also sections 260, 262, 264, 266, 268, 270, 272, and 274.

This code is used in section 197.

259. Rational addition. We recall

$$\frac{a}{b} + \frac{c}{d} = \frac{ad + bc}{bd}$$

We should return the reduced form of the result.

⟨Rational arithmetic declarations 257⟩ +≡
function *RationalAdd*(**const** *r1*, *r2* : *Rational*): *Rational*;

260. ⟨Arbitrary-precision rational arithmetic 258⟩ +≡
function *RationalAdd*(**const** *r1*, *r2* : *Rational*): *Rational*;
`var lRes: Rational;
 begin lRes.Num ← Add(Mul(r1.Num, r2.Den), Mul(r1.Den, r2.Num));
 lRes.Den ← Mul(r1.Den, r2.Den); RationalReduce(lRes); RationalAdd ← lRes;
 end;`

261. Rational subtraction. Similar to addition, but the numerator is $ad - bc$.

\langle Rational arithmetic declarations 257 $\rangle + \equiv$
function *RationalSub*(**const** $r1, r2$: *Rational*): *Rational*;

262. \langle Arbitrary-precision rational arithmetic 258 $\rangle + \equiv$
function *RationalSub*(**const** $r1, r2$: *Rational*): *Rational*;
var $lRes$: *Rational*;
begin $lRes.Num \leftarrow Sub(Mul(r1.Num, r2.Den), Mul(r1.Den, r2.Num));$
 $lRes.Den \leftarrow Mul(r1.Den, r2.Den);$ *RationalReduce*($lRes$); *RationalSub* $\leftarrow lRes$;
end;

263. Negating a rational number amounts to multiplying the numerator by -1 .

\langle Rational arithmetic declarations 257 $\rangle + \equiv$
function *RationalNeg*(**const** $r1$: *Rational*): *Rational*;

264. \langle Arbitrary-precision rational arithmetic 258 $\rangle + \equiv$
function *RationalNeg*(**const** $r1$: *Rational*): *Rational*;
var $lRes$: *Rational*;
begin $lRes.Num \leftarrow Mul(\text{'-1'}, r1.Num);$ $lRes.Den \leftarrow r1.Den;$ *RationalNeg* $\leftarrow lRes$;
end;

265. Multiplying rational numbers. This uses the school-book formula

$$\frac{a}{b} \times \frac{c}{d} = \frac{ac}{bd}$$

\langle Rational arithmetic declarations 257 $\rangle + \equiv$
function *RationalMult*(**const** $r1, r2$: *Rational*): *Rational*;

266. \langle Arbitrary-precision rational arithmetic 258 $\rangle + \equiv$
function *RationalMult*(**const** $r1, r2$: *Rational*): *Rational*;
var $lRes$: *Rational*;
begin $lRes.Num \leftarrow Mul(r1.Num, r2.Num);$ $lRes.Den \leftarrow Mul(r1.Den, r2.Den);$ *RationalReduce*($lRes$);
RationalMult $\leftarrow lRes$;
end;

267. Inverting a rational number. This is easy, provided the numerator is nonzero. The convention is to make the numerator carry the sign of the number (so n/d has $n \in \mathbf{Z}$ while $d \in \mathbf{N}$).

When the rational number *is* zero, we simply take $0^{-1} = 0$ (as is conventional among proof assistants).

\langle Rational arithmetic declarations 257 $\rangle + \equiv$
function *RationalInv*(**const** r : *Rational*): *Rational*;

268. \langle Arbitrary-precision rational arithmetic 258 $\rangle + \equiv$

```
function RationalInv(const r: Rational): Rational;
  var lRes: Rational;
  begin if r.Num  $\neq$  '0' then
    begin if le(r.Num, '0') then lRes.Num  $\leftarrow$  Mul('−1', r.Den)
    else lRes.Num  $\leftarrow$  r.Den;
    lRes.Den  $\leftarrow$  Abs(r.Num);
    end
  else lRes  $\leftarrow$  RZero;
  RationalInv  $\leftarrow$  lRes;
  end;
```

269. Dividing rational numbers. We see that $r_1/r_2 = r_1 \times (r_2^{-1})$. That's the trick.

\langle Rational arithmetic declarations 257 $\rangle + \equiv$

```
function RationalDiv(const r1, r2: Rational): Rational;
```

270. \langle Arbitrary-precision rational arithmetic 258 $\rangle + \equiv$

```
function RationalDiv(const r1, r2: Rational): Rational;
  begin RationalDiv  $\leftarrow$  RationalMult(r1, RationalInv(r2));
  end;
```

271. Equality of rational numbers. Two rational numbers n_1/d_1 and n_2/d_2 are equal if $n_1 = n_2$ and $d_1 = d_2$. This assumes that both rational numbers are in reduced form.

\langle Rational arithmetic declarations 257 $\rangle + \equiv$

```
function RationalEq(const r1, r2: Rational): boolean;
```

272. \langle Arbitrary-precision rational arithmetic 258 $\rangle + \equiv$

```
function RationalEq(const r1, r2: Rational): boolean;
  begin RationalEq  $\leftarrow$  (r1.Num = r2.Num)  $\wedge$  (r1.Den = r2.Den);
  end;
```

273. Testing inequality of rational numbers. We have $n_1/d_1 \leq n_2/d_2$ if $n_1 d_2 \leq n_2 d_1$.

Similarly, we have $n_1/d_1 > n_2/d_2$ is just the negation of $n_1/d_1 \leq n_2/d_2$.

\langle Rational arithmetic declarations 257 $\rangle + \equiv$

```
function RationalLE(const r1, r2: Rational): boolean;
```

```
function RationalGT(const r1, r2: Rational): boolean;
```

274. \langle Arbitrary-precision rational arithmetic 258 $\rangle + \equiv$

```
function RationalLE(const r1, r2: Rational): boolean;
  begin RationalLE  $\leftarrow$  leq(Mul(r1.Num, r2.Den), Mul(r1.Den, r2.Num));
  end;
function RationalGT(const r1, r2: Rational): boolean;
  begin RationalGT  $\leftarrow$   $\neg$ RationalLE(r1, r2);
  end;
```

Section 9.3. RATIONAL COMPLEX NUMBERS

275. We now begin with $\mathbf{Q} + i\mathbf{Q} \subseteq \mathbf{C}$, the subset of complex-numbers where the real and imaginary parts are rational numbers.

That is to say, rational complex numbers are represented by a pair of rational numbers in Cartesian form $z = p + iq$.

\langle Types for arbitrary-precision arithmetic 255 $\rangle + \equiv$
 $RComplex = \mathbf{record} \text{ } Re, Im: Rational$
 $\mathbf{end};$

276. \langle Zero and units for arbitrary-precision 256 $\rangle + \equiv$
 $CZero: RComplex = (Re : (Num : ^0^; Den : ^1^); Im : (Num : ^0^; Den : ^1^));$
 $COne: RComplex = (Re : (Num : ^1^; Den : ^1^); Im : (Num : ^0^; Den : ^1^));$
 $CMinusOne: RComplex = (Re : (Num : ^-1^; Den : ^1^); Im : (Num : ^0^; Den : ^1^));$
 $CImUnit: RComplex = (Re : (Num : ^0^; Den : ^1^); Im : (Num : ^1^; Den : ^1^));$

277. We want to know when these numbers describe integers (i.e., the imaginary part is zero and the denominator of the real part is 1) and natural numbers (i.e., when furthermore the numerator of the real part is non-negative).

\langle Predicate declarations for arbitrary-precision arithmetic 277 $\rangle \equiv$
 $\mathbf{function} \text{ } IsIntegerNumber(\mathbf{const} \text{ } z: RComplex): Boolean;$
 $\mathbf{function} \text{ } IsNaturalNumber(\mathbf{const} \text{ } z: RComplex): Boolean;$
 $\mathbf{function} \text{ } IsPrimeNumber(\mathbf{const} \text{ } z: RComplex): Boolean;$

See also sections 279 and 281.

This code is used in section 197.

278. \langle Complex-rational arbitrary-precision arithmetic 278 $\rangle \equiv$
 $\mathbf{function} \text{ } IsIntegerNumber(\mathbf{const} \text{ } z: RComplex): Boolean;$
 $\mathbf{begin} \text{ } IsIntegerNumber \leftarrow (z.Im.Num = ^0^) \wedge (z.Re.Den = ^1^); \mathbf{end};$
 $\mathbf{function} \text{ } IsNaturalNumber(\mathbf{const} \text{ } z: RComplex): Boolean;$
 $\mathbf{begin} \text{ } IsNaturalNumber \leftarrow (z.Im.Num = ^0^) \wedge (z.Re.Den = ^1^) \wedge (geq(z.Re.Num, ^0^)); \mathbf{end};$
 $\mathbf{function} \text{ } IsPrimeNumber(\mathbf{const} \text{ } z: RComplex): boolean;$
 $\mathbf{begin} \text{ } \mathbf{if} \text{ } IsNaturalNumber(z) \wedge IsPrime(z.Re.Num) \mathbf{then} \text{ } IsPrimeNumber \leftarrow true$
 $\mathbf{else} \text{ } IsPrimeNumber \leftarrow false;$
 $\mathbf{end};$

See also sections 280, 282, 284, 286, 288, 290, 292, 295, 298, 300, 302, and 304.

This code is used in section 197.

279. Equality of complex numbers. This amounts to checking if the real and imaginary parts are equal to each other as rational numbers.

\langle Predicate declarations for arbitrary-precision arithmetic 277 $\rangle + \equiv$
 $\mathbf{function} \text{ } AreEqComplex(\mathbf{const} \text{ } z1, z2: RComplex): Boolean;$
 $\mathbf{function} \text{ } IsEqWithInt(\mathbf{const} \text{ } z: RComplex;$
 $\text{ } n: longint): Boolean;$

280. \langle Complex-rational arbitrary-precision arithmetic 278 $\rangle + \equiv$
function *AreEqComplex*(**const** $z1, z2$: *RComplex*): *Boolean*;
 begin *AreEqComplex* \leftarrow *RationalEq*($z1.Re, z2.Re$) \wedge *RationalEq*($z1.Im, z2.Im$); **end**;
function *IsEqWithInt*(**const** z : *RComplex*;
 n : *longint*): *Boolean*;
 var s : *string*;
 begin *Str*(n, s); *IsEqWithInt* \leftarrow ($z.Im.Num = \text{'0'}$) \wedge ($z.Re.Num = s$) \wedge ($z.Re.Den = \text{'1'}$); **end**;

281. “Inequalities”. We “induce” the binary relations $<$ and \geq on the subset $\{q + i0 \mid q \in \mathbf{Q}\} \subseteq \mathbf{C}$. Again, what we said earlier about *RationalGT* being badly named holds for *IsRationalGT* being badly named as well.

\langle Predicate declarations for arbitrary-precision arithmetic 277 $\rangle + \equiv$
function *IsRationalLE*(**const** $z1, z2$: *RComplex*): *Boolean*;
function *IsRationalGT*(**const** $z1, z2$: *RComplex*): *Boolean*;

282. \langle Complex-rational arbitrary-precision arithmetic 278 $\rangle + \equiv$
function *IsRationalLE*(**const** $z1, z2$: *RComplex*): *Boolean*;
 begin *IsRationalLE* \leftarrow ($z1.Im.Num = \text{'0'}$) \wedge ($z2.Im.Num = \text{'0'}$) \wedge *RationalLE*($z1.Re, z2.Re$); **end**;
function *IsRationalGT*(**const** $z1, z2$: *RComplex*): *Boolean*;
 begin *IsRationalGT* \leftarrow ($z1.Im.Num = \text{'0'}$) \wedge ($z2.Im.Num = \text{'0'}$) \wedge *RationalGT*($z1.Re, z2.Re$); **end**;

Subsection 9.3.1. Arithmetic operations

283. Converting integers to complex numbers. We have a function to convert an integer $x \in \mathbf{Z}$ to be the complex number $(x/1) + i(0/1) \in \mathbf{C}$.

\langle Declare public complex-valued arbitrary precision arithmetic 283 $\rangle \equiv$
function *IntToComplex*(x : *integer*): *RComplex*;

See also sections 285, 287, 289, 291, 294, 297, and 299.

This code is used in section 197.

284. \langle Complex-rational arbitrary-precision arithmetic 278 $\rangle + \equiv$
function *IntToComplex*(x : *integer*): *RComplex*;
 var $lRes$: *RComplex*;
 begin $lRes \leftarrow COne$; $lRes.Re.Num \leftarrow IntToStr(x)$; *IntToComplex* $\leftarrow lRes$;
 end;

285. Adding complex numbers. We compute the sum of $(x_1 + iy_1)$ and $x_2 + iy_2$ to be $(x_1 + x_2) + i(y_1 + y_2)$.

\langle Declare public complex-valued arbitrary precision arithmetic 283 $\rangle + \equiv$
function *ComplexAdd*(**const** $z1, z2$: *RComplex*): *RComplex*;

286. \langle Complex-rational arbitrary-precision arithmetic 278 $\rangle + \equiv$
function *ComplexAdd*(**const** $z1, z2$: *RComplex*): *RComplex*;
 var $lRes$: *RComplex*;
 begin $lRes.Re \leftarrow RationalAdd(z1.Re, z2.Re)$; $lRes.Im \leftarrow RationalAdd(z1.Im, z2.Im)$;
 if.def (*CH_REPORT*) *CHReport.Out_NumReq3*(*rqRealAdd*, $z1, z2, lRes$); **endif**
 ComplexAdd $\leftarrow lRes$;
 end ;

287. Subtracting complex numbers. We find the difference of complex numbers componentwise.

⟨ Declare public complex-valued arbitrary precision arithmetic 283 ⟩ +≡

function *ComplexSub*(**const** *z1*, *z2*: *RComplex*): *RComplex*;

288. ⟨ Complex-rational arbitrary-precision arithmetic 278 ⟩ +≡

function *ComplexSub*(**const** *z1*, *z2*: *RComplex*): *RComplex*;

var *lRes*: *RComplex*;

begin *lRes.Re* ← *RationalSub*(*z1.Re*, *z2.Re*); *lRes.Im* ← *RationalSub*(*z1.Im*, *z2.Im*);

if_def (*CH-REPORT*) *CHReport.Out_NumReq3*(*rqRealDiff*, *z1*, *z2*, *lRes*); **end_if**

ComplexSub ← *lRes*;

end ;

289. Negating complex numbers. We negate a complex number $-z$ by negating its real and imaginary parts.

⟨ Declare public complex-valued arbitrary precision arithmetic 283 ⟩ +≡

function *ComplexNeg*(**const** *z*: *RComplex*): *RComplex*;

290. ⟨ Complex-rational arbitrary-precision arithmetic 278 ⟩ +≡

function *ComplexNeg*(**const** *z*: *RComplex*): *RComplex*;

var *lRes*: *RComplex*;

begin *lRes.Re* ← *RationalNeg*(*z.Re*); *lRes.Im* ← *RationalNeg*(*z.Im*);

if_def (*CH-REPORT*) *CHReport.Out_NumReq2*(*rqRealNeg*, *z*, *lRes*); **end_if**

ComplexNeg ← *lRes*;

end ;

291. Multiplying complex numbers. We use the usual formula

$$(x_1 + iy_1)(x_2 + iy_2) = (x_1x_2 - y_1y_2) + i(x_1y_2 + y_1x_2).$$

⟨ Declare public complex-valued arbitrary precision arithmetic 283 ⟩ +≡

function *ComplexMult*(**const** *z1*, *z2*: *RComplex*): *RComplex*;

292. ⟨ Complex-rational arbitrary-precision arithmetic 278 ⟩ +≡

function *ComplexMult*(**const** *z1*, *z2*: *RComplex*): *RComplex*;

var *lRes*: *RComplex*;

begin if *IsEqWithInt*(*z1*, -1) **then** *ComplexMult* ← *ComplexNeg*(*z2*)

else if *IsEqWithInt*(*z2*, -1) **then** *ComplexMult* ← *ComplexNeg*(*z1*)

else ⟨ Calculate the usual multiplication of complex numbers 293 ⟩;

end;

293. ⟨ Calculate the usual multiplication of complex numbers 293 ⟩ ≡

begin *lRes.Re* ← *RationalSub*(*RationalMult*(*z1.Re*, *z2.Re*), *RationalMult*(*z1.Im*, *z2.Im*));

lRes.Im ← *RationalAdd*(*RationalMult*(*z1.Re*, *z2.Im*), *RationalMult*(*z1.Im*, *z2.Re*));

ComplexMult ← *lRes*;

if_def (*CH-REPORT*) *CHReport.Out_NumReq3*(*rqRealMult*, *z1*, *z2*, *lRes*); **end_if**

end

This code is used in section 292.

294. Dividing complex numbers. We recall

$$\frac{x_1 + iy_1}{x_2 + iy_2} = \frac{(x_1 + iy_1)(x_2 - iy_2)}{x_2^2 + y_2^2}$$

This is the case for nonzero $z_2 \neq 0$. When we try to divide $z_1/0$, we return 0.

⟨ Declare public complex-valued arbitrary precision arithmetic 283 ⟩ +≡
function *ComplexDiv*(**const** $z1, z2: RComplex$): *RComplex*;

295. ⟨ Complex-rational arbitrary-precision arithmetic 278 ⟩ +≡
function *ComplexDiv*(**const** $z1, z2: RComplex$): *RComplex*;
 var $lDenom: Rational; lRes: RComplex$;
 begin $lRes \leftarrow CZero$;
 with $z2$ **do** $lDenom \leftarrow RationalAdd(RationalMult(Re, Re), RationalMult(Im, Im))$;
 if $lDenom.Num \neq '0'$ **then** ⟨ Calculate quotient for nonzero divisor 296 ⟩;
 $ComplexDiv \leftarrow lRes$;
 end;

296. ⟨ Calculate quotient for nonzero divisor 296 ⟩ ≡
 begin
 $lRes.Re \leftarrow RationalDiv(RationalAdd(RationalMult($z1.Re, z2.Re$), $RationalMult($z1.Im, z2.Im$),$$
 $lDenom)$;
 $lRes.Im \leftarrow RationalDiv(RationalSub(RationalMult($z1.Im, z2.Re$), $RationalMult($z1.Re, z2.Im$),$$
 $lDenom)$;
 if_def (*CH_REPORT*) *CHReport.Out_NumReq3*(*rqRealDiv*, $z1, z2, lRes$); **end_if**
 end

This code is used in section 295.

297. Inverting complex numbers. We can now calculate z^{-1} as just $1/z$.

⟨ Declare public complex-valued arbitrary precision arithmetic 283 ⟩ +≡
function *ComplexInv*(**const** $z: RComplex$): *RComplex*;

298. ⟨ Complex-rational arbitrary-precision arithmetic 278 ⟩ +≡
function *ComplexInv*(**const** $z: RComplex$): *RComplex*;
 begin $ComplexInv \leftarrow ComplexDiv(COne, z)$; **end**;

299. Norm of complex numbers. The “norm” or *modulus* for a complex number is just the sum of the square of its components (well, the squareroot of this sum).

⟨ Declare public complex-valued arbitrary precision arithmetic 283 ⟩ +≡
function *ComplexNorm*(**const** $z: RComplex$): *Rational*;

300. ⟨ Complex-rational arbitrary-precision arithmetic 278 ⟩ +≡
function *ComplexNorm*(**const** $z: RComplex$): *Rational*;
 begin $ComplexNorm \leftarrow RationalAdd(RationalMult($Z.Re, Z.Re$), $RationalMult($Z.Im, Z.Im$))$; **end**;$

Section 9.4. COMPARISON FUNCTIONS

301. The remainder of `numbers.pas` defines functions which compares numbers. These must return a value in the set $\{-1, 0, +1\}$ as a PASCAL *integer*.

⟨ Declare public comparison operators for arbitrary-precision numbers 301 ⟩ \equiv

```
function CompareInt(X1, X2 : longint): integer;
function CompareIntStr(X1, X2 : string): integer;
```

See also section 303.

This code is used in section 197.

302. ⟨ Complex-rational arbitrary-precision arithmetic 278 ⟩ $+\equiv$

```
function CompareInt(X1, X2 : longint): integer;
  begin if X1 = X2 then CompareInt  $\leftarrow$  0
  else if X1 > X2 then CompareInt  $\leftarrow$  1
  else CompareInt  $\leftarrow$  -1;
  end;
function CompareIntStr(X1, X2 : string): integer;
  begin if X1 = X2 then CompareIntStr  $\leftarrow$  0
  else if gt(X1, X2) then CompareIntStr  $\leftarrow$  1
  else CompareIntStr  $\leftarrow$  -1;
  end;
```

303. There is also a function to “compare” complex numbers. This treats a complex number

$$z = \frac{n_1}{d_1} + i \frac{n_2}{d_2}$$

as a tuple (n_1, d_1, n_2, d_2) then uses lexicographic ordering based on the components.

⟨ Declare public comparison operators for arbitrary-precision numbers 301 ⟩ $+\equiv$

```
function CompareComplex(const z1, z2 : RComplex): integer;
```

304. ⟨ Complex-rational arbitrary-precision arithmetic 278 ⟩ $+\equiv$

```
function CompareComplex(const z1, z2 : RComplex): integer;
  var Unt : integer;
  begin Unt  $\leftarrow$  CompareIntStr(z1.Re.Num, z2.Re.Num);
  if Unt  $\neq$  0 then
    begin CompareComplex  $\leftarrow$  Unt; exit end;
  Unt  $\leftarrow$  CompareIntStr(z1.Re.Den, z2.Re.Den);
  if Unt  $\neq$  0 then
    begin CompareComplex  $\leftarrow$  Unt; exit end;
  Unt  $\leftarrow$  CompareIntStr(z1.Im.Num, z2.Im.Num);
  if Unt  $\neq$  0 then
    begin CompareComplex  $\leftarrow$  Unt; exit end;
  CompareComplex  $\leftarrow$  CompareIntStr(z1.Im.Den, z2.Im.Den);
  end;
```

File 10

Mizar Objects and Data Structures

305. This is one of the largest files in Mizar (it clocks in at 6594 lines of code). Its interface consists of 552 lines alone (roughly 1/13 of the file).

We should remind the reader PASCAL has “typed pointers”, meaning an object with type $\uparrow Foo$ is a pointer to a *Foo* object. We lookup the object for a pointer p : $\uparrow Foo$ by dereferencing it as $p\uparrow$. If $foo: Foo$ is an instance, we can have p point to it by writing $p \leftarrow @foo$.

Further, it is idiomatic PASCAL to have for each type *Foo* a pointer type $PFoo = \uparrow Foo$.

306. We will refer to “some data allocated in memory” as an “**Object**”. Alexander Stepanov and Paul McJones’s *Elements of Programming* (elementsofprogramming.com) discuss object-oriented programming from a rather baroque philosophical perspective, which the reader may find enjoyable.

```

< mobjects.pas 306 > ≡
  < GNU License 4 >
unit mobjects;
interface
uses numbers;
  < Public interface for mobjects.pas 309 >
implementation
mdebug uses info; end_mdebug
  < Implementation for mobjects.pas 307 >
end .

```

307. We have an error method for situations when a method is not implemented, for example when there is no ordering operator when the user invokes *MSortedCollection.Compare* (§417).

```

< Implementation for mobjects.pas 307 > ≡
procedure Abstract1;
  begin RunError(211);
end;

```

See also section 308.

This code is used in section 306.

308. The “roadmap” for the data structures implemented in this library may be summed up loosely as: we introduce a base “object” class, then we introduce a family of collections, then we conclude with classes for sequences and partial functions.

```

⟨Implementation for mobjects.pas 307⟩ +≡
  ⟨MObject implementation 312⟩
  ⟨MStrObj implementation 317⟩
  ⟨MList implementation 323⟩ { start of collections classes }
  ⟨MCollection implementation 349⟩
  ⟨MExtList implementation 365⟩
  ⟨MSortedList implementation 380⟩
  ⟨MSortedExtList implementation 397⟩
  ⟨MSortedStrList implementation 411⟩
  ⟨MSortedCollection implementation 416⟩
  ⟨String collection implementation 425⟩
  ⟨MIntCollection implementation 429⟩
  ⟨Stacked object implementation 437⟩
  ⟨String list implementation 439⟩
  ⟨Int relation implementation 480⟩ { start of partial functions }
  ⟨Partial integer function implementation 489⟩
  ⟨NatFunc implementation 509⟩
  ⟨NatSeq implementation 527⟩
  ⟨IntSequence implementation 532⟩
  ⟨IntSet Implementation 548⟩
  ⟨Partial Binary integer Functions 559⟩
  ⟨Partial integers to Pair of integers Functions 577⟩

```

309. Constant parameters.

```

⟨Public interface for mobjects.pas 309⟩ ≡
const { Maximum MCollection size }
  MaxSize = 2000000;
  MaxCollectionSize = MaxSize div SizeOf(Pointer);
  MaxListSize = MaxSize div (SizeOf(Pointer) * 2); { Maximum MStringList size }
  MaxIntegerListSize = MaxSize div (SizeOf(integer)); { Maximum IntegerList size }
  { MCollection error codes }
  coIndexError = -1; { Index out of range }
  coOverflow = -2; { Overflow }
  coConsistentError = -3;
  coDuplicate = -5; { Duplicate }
  coSortedListError = -6;
  coIndexExtError = -7;

```

See also sections 310, 311, 316, 320, 321, 348, 364, 379, 396, 410, 415, 424, 428, 436, 438, 469, 470, 479, 488, 508, 526, 531, 547, 558, 576, and 590.

This code is used in section 306.

310. Type aliases.

⟨Public interface for `mobjects.pas` 309⟩ +≡

type {String pointers}

$PString = \uparrow ShortString$; { $ShortString = String[255]$ }

{Character set type}

$PCharSet = \uparrow TCharSet$;

$TCharSet = \mathbf{set\ of}\ char$;

{General arrays}

$PByteArray = \uparrow TByteArray$;

$TByteArray = \mathbf{array}\ [0 \dots 32767]\ \mathbf{of}\ byte$; { $32767 = 2^{15} - 1$ }

$PWordArray = \uparrow TWordArray$;

$TWordArray = \mathbf{array}\ [0 \dots 16383]\ \mathbf{of}\ word$; { $16383 = 2^{14} - 1$ }

Section 10.1. BASE OBJECT

311. Object-oriented PASCAL is a bit crufty (like all Object-oriented ALGOL-descended languages).

The base *MObject* “class” has a constructor, destructor, a clone function named *CopyObject*, and a “move” function called *MCopy*.

```

⟨ Public interface for mobjects.pas 309 ⟩ +≡
  { MObject base object }
  PObject = ↑MObject;
  ObjectPtr = PObject;
  MObject = object
    constructor Init;
    procedure Free; { unused }
    destructor Done; virtual;
    function CopyObject: PObject;
    function MCopy: PObject; virtual;
  end ;

```

312. Note that the *VER70* conditional compilation only plays a role here, in the constructor *MObject.Init*. And nowhere else.

The constructor will initialize the memory allocated for the *MObject* to be zero. This is true when *VER70* is not defined, too, because the Free PASCAL compiler will allocate 1 word for the virtual methods table and 1 word for the data (“self”) and the default constructor (“*fpc_help_constructor*”) for Free PASCAL initializes the memory allocated with zeros.

```

⟨ MObject implementation 312 ⟩ ≡
  { MObject }
constructor MObject.Init;
  @{@&$IFDEF VER70@}
  type Image = record Link: word;
    Data: record
      end;
    end;
  @{@&$ENDIF@}
  begin
    @{@&$IFDEF VER70@} FillChar(Image(Self).Data, SizeOf(Self) - SizeOf(MObject), 0);
    @{@&$ENDIF@}
  end;

```

This code is used in section 308.

313. Destructor. The destructor is, well, what C++ programmers would call an “abstract method”.

The *MObject.Free* procedure frees all the memory allocated to the caller. It isn’t used anywhere.

```

procedure MObject.Free; { unused }
  begin Dispose(PObject(@Self), Done); end;
destructor MObject.Done;
  begin end;

```

314. Copying an object allocates new memory using the Free PASCAL *GetMem* function, then *copies* the contents of the caller to the new region. The *move* primitive function is poorly named (blame Borland): it is a copy function.

It then returns a pointer to the newly allocated object.

Note that this function is used in only two places: once in *MCopy*, and later in *MList.MCopy* (§328).

```
function MObject.CopyObject: PObject;
var lObject: PObject;
begin GetMem(lObject, SizeOf(Self));
      Move(Self, lObject↑, SizeOf(Self));
      CopyObject ← lObject;
end;
```

315. The virtual method for copying Mizar objects can be overridden by subclasses. But the default method is just *CopyObject*.

```
function MObject.MCopy: PObject;
begin MCopy ← CopyObject; end;
```

Section 10.2. MIZAR STRING OBJECT

316. We want to treat strings as *MObjects*, and the way object-oriented programming handles this situation is to create a subclass consisting of just a string field. This amounts to a “wrapper class”.

```

⟨ Public interface for mobjects.pas 309 ⟩ +≡
  { Specyfif objects based on MObjects for collections }
  PStr = ↑MStrObj;
  MStrPtr = PStr;
  MStrObj = object (MObject)
    fStr: String;
    constructor Init(const aStr: String);
  end ;

```

317. Constructor. The constructor for a string object expects a string, and simply initializes its contents to the given string.

```

⟨ MStrObj implementation 317 ⟩ ≡
  { Specyfif objects based on MObjects for collections }
constructor MStrObj.Init(const aStr: String);
  begin fStr ← aStr; end;

```

This code is used in section 308.

Section 10.3. MIZAR LIST

318. A *MList* is a dynamic array data structure, which represents a list using an array. We reserve an array whose length is referred to as its “**Capacity**” in the literature.

Not all of the underlying array is used by the user. The number of entries which are used by the dynamic array contents is referred to as its “**Logical Size**” (or just its *Size*) in the literature.

When the dynamic array is filled, it “grows”; i.e., it allocates a new array that’s larger, and copies over the contents of its old array, then frees the old array. The growth factor is controlled by the *GrowLimit*(*oldSize*) value.

319. Review of pointers in Pascal. We have a few parameters needed for collections. Remember, if T is a type, then $\uparrow T$ is the type of pointers to T objects. If we want to have a pointer without referring to the *type* of the object referenced, we can use *Pointer*.

The @ operator is the “address of” operator. When setting a pointer p to point to something Foo , we have $p \leftarrow @Foo$.

The \uparrow operator is the “dereferencing” operator which is appended to a pointer identifier. When we want to update the object referenced by a pointer p , we have $p\uparrow \leftarrow newValue$.

320. \langle Public interface for `mobjects.pas` 309 $\rangle + \equiv$
 { MCollection types }
 $PItemList = \uparrow MItemList$;
 $MItemList = \text{array } [0 \dots MaxCollectionSize - 1] \text{ of } Pointer$;

321. A *MList* object is known as a dynamic array. Java programmers would know that as an `ArrayList`.

```

⟨Public interface for mobjects.pas 309⟩ +≡
  { MList object }
  PList = ↑MList;
  MListPtr = PList;
  MList = object (MObject)
    Items: PItemList; { Contents of dynamic array }
    Count: integer; { Logical size of dynamic array }
    Limit: integer; { Capacity of dynamic array }
    constructor Init(ALimit : integer);
    constructor MoveList(var aAnother : MList);
    constructor CopyList(var aAnother : MList);
    destructor Done; virtual;
    function MCopy: PObject; virtual;
    procedure ListError(aCode, aInfo : integer); virtual;
    function At(Index : integer): Pointer;
    function Last: Pointer;
    procedure Insert(aItem : Pointer); virtual;
    procedure AtInsert(aIndex : integer; aItem : Pointer); virtual;
    procedure InsertList(var aAnother : MList); virtual;
    function GetObject(aIndex : integer): Pointer; virtual;
    function IndexOf(aItem : Pointer): integer; virtual;
    procedure DeleteAll; virtual;
    procedure FreeItem(Item : Pointer); virtual;
    procedure FreeAll; virtual;
    procedure FreeItemsFrom(aIndex : integer); virtual;
    procedure Pack; virtual;
    procedure SetLimit(ALimit : integer); virtual;
    procedure AppendTo(var fAnother : MList); virtual;
    procedure TransferItems(var fAnother : MList); virtual;
    procedure CopyItems(var fOrigin : MList); virtual;
end ;

```

322. It's worth pointing out that an *MList* does not “own” the items in it, in the sense that: when we delete an *MList* instance, we do not need to delete each item in it.

323. Growth factor. How quickly an Dynamic Array grows is a subject of debate. Just for a table of the growth factors:

Implementation	Growth Factor
Java's ArrayList	$3/2 = 1.5$
Microsoft's Visual C++	$3/2 = 1.5$
Facebook folly/FBVector	$3/2 = 1.5$
Unreal Engine's TArray	$n + ((3n) \gg 3) \sim 1.375$
Python PyListObject	$n + (n \gg 3) \sim 1.125$
Go slices	between 1.25 and 2
Gnu C++	2
Clang	2
Rust's Vec	2
Nim sequences	2
SBCL vectors	2
C#	2

The *MList* uses a staggered growth factor, specifically something like $s(n) \leftarrow s(n) + \text{GrowLimit}(s(n))$. The sequence of Dynamic Array size would be:

$$s(n) = (0, 4, 8, 12, 28, 44, 60, 76, \dots)$$

followed by $s(n+1) \leftarrow (5/4)s(n)$. I am not sure this is optimal, but I have no better solution.

CAUTION: If the memory allocator uses a first-fit allocation, then growth factors like $\alpha \geq 2$ can cause dynamic array expansion to run out of memory even though a significant amount of memory may still be available. For a discussion about this point, see:

- <http://www.gahcep.com/cpp-internals-stl-vector-part-1/>

The reader wondering what strategy Free PASCAL uses should consult §8.4.1 of the “Free PASCAL Programmer’s Guide” ([eprint](#)).

It seems that a growth factor $\alpha \leq \varphi = (1 + \sqrt{5})/2$ must be not bigger than the golden ratio. To see this, we need a dyanmic array of size S to have its first growth to allocate αS , then frees up the S bytes from the pre-growth allocation. The second allocation needs $\alpha^2 S$ bytes. Observe the first two allocations requires $S + \alpha S$ bytes available. Now suppose we want this to be able to fit into the newly freed space,

$$\alpha^2 S \leq S + \alpha S$$

which means

$$\alpha^2 - \alpha + 1 \leq 0$$

or (requiring $\alpha > 0$)

$$\alpha \leq \varphi = \frac{1 + \sqrt{5}}{2}.$$

When this fails to hold, a first-fit allocation could run out of memory.

$\langle MList \text{ implementation } 323 \rangle \equiv$

{ Simple Collection }

function *GrowLimit*(*aLimit* : integer): integer;

begin *GrowLimit* \leftarrow 4;

if *aLimit* > 64 **then** *GrowLimit* \leftarrow *aLimit* **div** 4

else if *aLimit* > 8 **then** *GrowLimit* \leftarrow 16;

end;

This code is used in section 308.

324. Constructor. The constructor creates an empty list. The initial capacity and initial size are both set to zero.

```
constructor MList.Init(aLimit : integer);
  begin MObject.Init; Items  $\leftarrow$  nil; Count  $\leftarrow$  0; Limit  $\leftarrow$  0; SetLimit(aLimit); end;
```

325. Moving a list into the caller. Since an *MList* does not own its contents, moving its contents around amounts to updating pointers. The *DeleteAll* (§337) method just updates the capacity of the caller to zero, it does not free anything from memory.

```
constructor MList.MoveList(var aAnother : MList);
  begin MObject.Init;
    Count  $\leftarrow$  aAnother.Count; Limit  $\leftarrow$  aAnother.Limit; Items  $\leftarrow$  aAnother.Items; { move }
    aAnother.DeleteAll; aAnother.Limit  $\leftarrow$  0; aAnother.Items  $\leftarrow$  nil; { delete aAnother }
  end;
```

326. Copying the contents of *aAnother* list into the current list will essentially reinitialize the current list, the insert all items from the other list into the current list using *InsertList* (§333).

```
constructor MList.CopyList(var aAnother : MList);
  begin MObject.Init; Items  $\leftarrow$  nil; Count  $\leftarrow$  0; Limit  $\leftarrow$  0; { initialize }
    SetLimit(aAnother.Limit); InsertList(aAnother);
  end;
```

327. A list is “done” frees all items in the list, sets the limit to zero, and then invokes the superclass’s *Done* method.

```
destructor MList.Done;
  begin FreeAll; SetLimit(0); inherited Done; end;
```

328. We override the *MObject.MCopy* method (§315). This will copy the base object using *CopyObject* (§314), allocate a new array of pointers, copy over the contents of the caller, and then returns the new list.

Importantly, this *will* allocate new objects on the heap, duplicating every entry in the caller *and* the caller’s data (capacity and size).

```
function MList.MCopy: PObject;
  var lList: PObject; i: integer;
  begin lList  $\leftarrow$  CopyObject; GetMem(PList(lList) $\uparrow$ .Items, Self.Limit * SizeOf(Pointer));
  for i  $\leftarrow$  0 to Self.Count - 1 do PList(lList) $\uparrow$ .Items $\uparrow$ [i]  $\leftarrow$  PObject(Self.Items $\uparrow$ [i]) $\uparrow$ .MCopy;
    MCopy  $\leftarrow$  lList;
  end;
```

329. This is the same as *MList.GetObject* (§334), and I am not sure why we have two versions of the same function.

```
function MList.At(Index : integer): Pointer;
  begin if (Index < 0)  $\vee$  (Index  $\geq$  Count) then
    begin ListError(coIndexError, 0); At  $\leftarrow$  nil; end
  else At  $\leftarrow$  Items $\uparrow$ [Index];
  end;
```

330. The *MList.Count* tracks the number of allocated items. So the last item would be located at *MList.Count* - 1 (since we count with zero offset).

```
function MList.Last: Pointer;
  begin Last  $\leftarrow$  At(Count - 1); end;
```


331. Inserting an item into a list requires checking there's enough free space to the list, then sets the first spot to the item.

```
procedure MList.Insert(aItem : Pointer);
  begin if Limit = Count then SetLimit(Limit + GrowLimit(Limit)); { ensure capacity }
  Items↑[Count] ← aItem; inc(Count);
end;
```

332. If we want to insert a pointer *at a specific index*, then we proceed as follows:

- (1) Check if the index is negative. If so, then we should flag an error using *ListError*, and exit.
- (2) Check if the index is larger than the logical size of the dynamic array; if so, then we grow the dynamic array using *SetLimit*

PUZZLE: What happens if the user calls *AtInsert*(*caller.Count* − *n*, *object*)? The code will set every pointer in *Items*[*Caller.Count* − *n* .. *Caller.Count* − 1] to **nil**, which seems buggy.

SOLUTION: The *SetLimit* method *does not* update the *Count* field of the caller, so the problem just stated will never happen.

```
procedure MList.AtInsert(aIndex : integer; aItem : Pointer);
  var i, lLimit: integer;
  begin if aIndex < 0 then
    begin ListError(coIndexError, 0); exit;
    end;
  if (aIndex ≥ Limit) ∨ ((aIndex = Count) ∧ (Limit = Count)) then { ensure capacity }
    begin lLimit ← Limit + GrowLimit(Limit);
    while aIndex + 1 > lLimit do lLimit ← lLimit + GrowLimit(lLimit);
    SetLimit(lLimit); { Copy contents }
    end;
  for i ← Count to aIndex − 1 do Items↑[i] ← nil; { fill new entries as nil }
  Items↑[aIndex] ← aItem; { set the entry at aIndex to the pointer }
  if aIndex ≥ Count then Count ← aIndex + 1; { update logical size, if necessary }
end;
```

333. When we insert *aAnother* list into the current list, we simply iterate through all the other list's items, and insert (a copy of the pointer to) each one into the current list. This should leave *aAnother* list unmodified.

Observe that this has, for each item in the argument supplied, the caller *Insert* a pointer to a copy of each item. That is to say, the caller *pushes* a new item to the end of the caller's contents.

```
procedure MList.InsertList(var aAnother : MList);
  var i: integer;
  begin for i ← 0 to pred(aAnother.Count) do Insert(PObject(aAnother.Items↑[i])↑.MCopy);
  end;
```

334. Given an index, find the item located there. Well, the pointer to the object. When the index is illegal (out of bounds or negative), then flag an error and return **nil**. Otherwise return the pointer located at the index.

```
function MList.GetObject(aIndex : integer): Pointer;
  begin if (aIndex < 0) ∨ (aIndex ≥ Count) then
    begin ListError(coIndexError, 0); GetObject ← nil; end
  else GetObject ← Items↑[aIndex];
  end;
```

335. We have a default error code for lists.

```
procedure MList.ListError(aCode, aInfo : integer);  
  begin RunError(212 - aCode); end;
```

336. Looking for the index of an item requires iterating through each item of the list, until we find the needle in the haystack. Once found, we return the index for the needle.

If the needle is not in the haystack, return -1 .

Note: this uses pointer comparison, so it will not compare the *contents* of the object for equality.

```
function MList.IndexOf(aItem : Pointer): integer;  
  var i: integer;  
  begin IndexOf  $\leftarrow -1$ ;  
  for i  $\leftarrow 0$  to pred(Count) do  
    if aItem = Items $\uparrow$ [i] then  
      begin IndexOf  $\leftarrow i$ ; break end  
  end;
```

337. Deleting all items from a list simply updates the list's logical size (i.e., *Count*) to zero. Important contracts which hold about this:

- This will not alter the underlying array allocated for the dynamic array.
- This will not free any allocated objects from memory.

```
procedure MList.DeleteAll;  
  begin Count  $\leftarrow 0$ ; end;
```

338. Freeing a single item will invoke PASCAL's primitive *Dispose* function (which frees up the memory in heap). This is a helper function to avoid accidentally invoking *Dispose*(*PObject*(**nil**), *Done*) which would throw errors.

[[This method appears to be used only by subclasses of *MList*, so I think this should be a protected method.]]

```
procedure MList.FreeItem(Item : Pointer);  
  begin if Item  $\neq$  nil then Dispose(PObject(Item), Done);  
  end;
```

339. We delegate all the heavy work of *FreeAll* to *FreeItemsFrom*.

```
procedure MList.FreeAll;  
  begin FreeItemsFrom(0); end;
```

340. We can iterate through a list from a start index, freeing the rest of the list starting from *aIndex*. Remember, the data structure for *MList* consists of an *MObject* extended with its capacity, logical size, and a *pointer* to the array on the heap. When freeing an item from the array, we dereference the pointer to look up item *I* in the array.

```
procedure MList.FreeItemsFrom(aIndex : integer);  
  var I: integer;  
  begin for I  $\leftarrow$  Count - 1 downto aIndex do FreeItem(Items $\uparrow$ [I]);  
  Count  $\leftarrow$  aIndex;  
  end;
```

341. If an item has become **nil** in the list, we should shift the rest of the list down. Basically, in Lisp, if `null (cadr 1)`, then `setf 1 (cdr 1)`.

Care must be taken to iterate over the items in the list. Shifting items down by one item requires iterating over k from i to $Count - 2$ (because the maximum index is $Count - 1$ due to zero offset indexing).

Once we have shifted everything down, we decrement the logical size of the dynamic array.

```

procedure MList.Pack;
  var  $i, k$ : integer;
  begin for  $i \leftarrow Count - 1$  downto 0 do
    if  $Items \uparrow[i] = \mathbf{nil}$  then
      begin for  $k \leftarrow i$  to  $Count - 2$  do  $Items \uparrow[k] \leftarrow Items \uparrow[k + 1]$ ;
         $dec(Count)$ ;
      end;
    end;
  end;

```

342. Growing a list handles a few edgecases:

- (1) If the new limit is *smaller* than the existing limit, then just set the new limit equal to the existing limit.
- (2) If the new limit is *larger* than the maximum limit, then just set the new limit equal to the maximum limit.
- (3) If the new limit is not equal to the existing limit, then we have the “standard situation”.
 - (i) When the new limit is zero, simply set the pointer to the item list to **nil**
 - (ii) Otherwise (for a new limit which is a nonzero number), allocate a new chunk of memory for the number of pointers needed, then move them. Be sure to free up the pointers, and update the variables.

```

procedure MList.SetLimit( $ALimit$  : integer);
  var  $lItems$ : PItemList;
  begin  $\langle \text{Ensure } Count \leq ALimit \leq MaxCollectionSize \text{ 343} \rangle$ ;
  if  $ALimit \neq Limit$  then
    begin if  $ALimit = 0$  then  $lItems \leftarrow \mathbf{nil}$ 
      else  $\langle \text{Allocate a new array, and copy old contents into new array 344} \rangle$ ;
      if  $Limit \neq 0$  then  $FreeMem(Items, Limit * SizeOf(Pointer))$ ;
       $Items \leftarrow lItems$ ;  $Limit \leftarrow ALimit$ ;
    end;
  end;

```

```

343.  $\langle \text{Ensure } Count \leq ALimit \leq MaxCollectionSize \text{ 343} \rangle \equiv$ 
  if  $ALimit < Count$  then  $ALimit \leftarrow Count$ ;
  if  $ALimit > MaxCollectionSize$  then  $ALimit \leftarrow MaxCollectionSize$ 

```

This code is used in section 342.

```

344.  $\langle \text{Allocate a new array, and copy old contents into new array 344} \rangle \equiv$ 
  begin  $GetMem(lItems, ALimit * SizeOf(Pointer))$ ;
  if  $((Count \neq 0) \wedge (Items \neq \mathbf{nil}))$  then  $Move(Items \uparrow, lItems \uparrow, Count * SizeOf(Pointer))$ ;
  end

```

This code is used in section 342.

345. Appending another list to the current list will expand the current list to support the new items, insert the other list's items at the end of the current list, and then free the other list from memory.

```
procedure MList.AppendTo(var fAnother : MList);
  var k: integer;
  begin SetLimit(Count + fAnother.Count);
  for k  $\leftarrow$  0 to fAnother.Count - 1 do Insert(fAnother.Items $\uparrow$ [k]);
  fAnother.DeleteAll; fAnother.Done;
end;
```

346. There is a comment in Polish at the beginning of this function stating “Przeznaczeniem tej procedury jest uzycie jej w konstruktorach *Move*, ktore wykonuja jakgdyby pelna instrukcje przypisania (razem z VMTP)” which Google translates as “The purpose of this procedure is to be used in *Move* constructors, which execute a full assignment statement (including VMTP [virtual method table pointer]).”

There is also another comment in Polish, “Nie wolno uzyc *SetLimit*, bo rozdysponuje Items” which I translated into English and kept inline (“You cannot use *SetLimit* because it will distribute the Items”).

The semantics of *Object* \leftarrow *Object* will *copy* the right-hand side to the left-hand side.

```
procedure MList.TransferItems(var fAnother : MList);
  begin Self  $\leftarrow$  fAnother; { copy contents of fAnother over to Self }
  fAnother.DeleteAll; fAnother.Limit  $\leftarrow$  0; fAnother.Items  $\leftarrow$  nil;
  { You cannot use SetLimit because it will distribute the Items. }
end;
```

347. Copying items from a list simply loops through the original list, inserting them into the caller.

```
procedure MList.CopyItems(var fOrigin : MList);
  var i: integer;
  begin for i  $\leftarrow$  0 to fOrigin.Count - 1 do Insert(PObject(fOrigin.Items $\uparrow$ [i]) $\uparrow$ .CopyObject);
end;
```

Section 10.4. MIZAR COLLECTION CLASS

348. Curiously, the “Collection” class extends the “List” class, which surprises me. This will change the growth rate from $s(n+1) = s(n) + \text{GrowLimit}(s(n))$ to be

$$s(n+1) = s(n) + \text{GrowLimit}(\Delta + s(n))$$

where $\Delta \geq 0$ is a field of the Collection object. When we move an *MList* into an *MCollection*, we have $\Delta \leftarrow 2$ be the default value.

```

<Public interface for mobjects.pas 309> +=
  { MCollection object }
  PCollection = ↑MCollection;
  MCollection = object (MList)
    Delta: integer;
    constructor Init(ALimit, ADelta : integer);
    destructor Done; virtual;
    procedure AtDelete(Index : integer);
    procedure AtFree(Index : integer);
    procedure AtInsert(Index : integer; Item : Pointer); virtual;
    procedure AtPut(Index : integer; Item : Pointer);
    procedure Delete(Item : Pointer);
    procedure Free(Item : Pointer);
    procedure Insert(aItem : Pointer); virtual;
    procedure Pack; virtual;
    constructor MoveCollection(var fAnother : MCollection);
    constructor MoveList(var aAnother : MList);
    constructor CopyList(var aAnother : MList);
    constructor CopyCollection(var AAnother : MCollection);
    constructor Singleton(fSing : PObject; fDelta : integer);
    procedure Prune; virtual;
  end ;

```

349. Constructor. When constructing a new Collection, we allocate an array of the desired limit (using the *SetLimit* (§342) to handle this allocation).

[[We should have preconditions that $\Delta \geq 0$ and $ALimit \geq 0$, enforced by assertions.]]

```

< MCollection implementation 349 > ≡
  { MCollection }
constructor MCollection.Init(ALimit, ADelta : integer);
  begin MObject.Init; Items ← nil; Count ← 0; Limit ← 0; Delta ← ADelta; SetLimit(ALimit);
  end;
destructor MCollection.Done;
  begin FreeAll; SetLimit(0);
  end;

```

This code is used in section 308.

350. When trying to delete an element at *Index*, we first check if the *Index* is within the bounds of the collection. If it's out of bounds, we invoke *ListError* and exit the function.

Otherwise, we shift everything in the collection down by one position.

```
procedure MCollection.AtDelete(Index : integer);
  var i: integer;
  begin if (Index < 0)  $\vee$  (Index  $\geq$  Count) then
    begin ListError(coIndexError, 0); exit; end;
  if Index < pred(Count) then
    for i  $\leftarrow$  Index to Count - 2 do Items $\uparrow$ [i]  $\leftarrow$  Items $\uparrow$ [i + 1];
  Dec(Count);
  end;
```

351. If we want to also *free* an object in a collection, we store it in a temporary variable, then invoke *AtDelete*(*Index*) to update the collection, and finally *Free* the item.

```
procedure MCollection.AtFree(Index : integer);
  var Item: Pointer;
  begin Item  $\leftarrow$  At(Index); AtDelete(Index); FreeItem(Item); end;
```

352. Inserting an item at an *Index*, we first need to check if the position is within the bounds of the collection. If it's out of bounds, then flag a *ListError* and exit the function.

Otherwise, we check if the collection is at capacity (*Limit* = *Count*). If so, we try to expand the collection by *Delta* items. When *Delta* is zero, then raise an error and exit.

Now we are at the “default” case. Simply shift items starting at *Index* up by one. Then set the item at *Index* to be the new *Item*, and increment the count of the collection.

```
procedure MCollection.AtInsert(Index : integer; Item : Pointer);
  begin if (Index < 0)  $\vee$  (Index > Count) then
    begin ListError(coIndexError, 0); exit; end;
  if Limit = Count then
    begin if Delta = 0 then
      begin ListError(coOverflow, 0); exit; end;
      SetLimit(Limit + Delta);
    end;
  if Index  $\neq$  Count then Move(Items $\uparrow$ [Index], Items $\uparrow$ [Index + 1], (Count - Index) * SizeOf(pointer));
  Items $\uparrow$ [Index]  $\leftarrow$  Item; inc(Count);
  end;
```

353. Overwrite contents at index. We can insert a new item at a given index without shifting the collection.

```
procedure MCollection.AtPut(Index : integer; Item : Pointer);
  begin if (Index < 0)  $\vee$  (Index  $\geq$  Count) then ListError(coIndexError, 0)
  else Items $\uparrow$ [Index]  $\leftarrow$  Item;
  end;
```

354. Deleting an item finds the index of the item, then invokes *AtDelete* on that index.

```
procedure MCollection.Delete(Item : Pointer);
  begin AtDelete(IndexOf(Item)); end;
```

355. Similarly, freeing an item is just *Delete*-ing the item, then calling *FreeItem* on the pointer.

```
procedure MCollection.Free(Item : Pointer);
  begin Delete(Item); FreeItem(Item); end;
```

356. Inserting an item at the end of the collection.

```
procedure MCollection.Insert(aItem : Pointer);  
  begin AtInsert(Count, aItem); end;
```

357. We can also “fit” the collection by deleting all **nil** elements.

```
procedure MCollection.Pack;  
  var i: integer;  
  begin for i  $\leftarrow$  pred(Count) downto 0 do  
    if Items $\uparrow$ [i] = nil then AtDelete(i);  
  end;
```

358. Move semantics for creating a new collection.

```
constructor MCollection.MoveCollection(var fAnother : MCollection);  
  begin Init(0, fAnother.Delta); TransferItems(fAnother) end;
```

359. Cloning a collection will simply create an empty collection, the loop through *AAnother* inserting each item from the original collection into the newly minted collection.

```
constructor MCollection.CopyCollection(var AAnother : MCollection);  
  var i: integer;  
  begin Init(AAnother.Limit, AAnother.Delta);  
  for i  $\leftarrow$  0 to AAnother.Count - 1 do Insert(aAnother.Items $\uparrow$ [i]);  
  end;
```

360. A singleton allocates as little as possible.

```
constructor MCollection.Singleton(fSing : PObject; fDelta : integer);  
  begin Init(2, fDelta); Insert(fSing) end;
```

361. Pruning a collection merely sets its limits to zero. It does not free the contents of the collection.

```
procedure MCollection.Prune;  
  begin SetLimit(0) end;
```

362. Moving an *MList* uses PASCAL’s inheritance semantics to invoke *MList.MoveList* and then sets the *Delta* to 2.

```
constructor MCollection.MoveList(var aAnother : MList);  
  begin inherited MoveList(aAnother); Delta  $\leftarrow$  2;  
  end;
```

363. Copying a list invokes *MList.CopyList* on the collection, then sets *Delta* \leftarrow 2.

```
constructor MCollection.CopyList(var aAnother : MList);  
  begin inherited CopyList(aAnother); Delta  $\leftarrow$  2; end;
```

Section 10.5. SIMPLE STACKED (EXTENDIBLE) LISTS

364. This is used to track newly registered clusters in Mizar.

The basic idea is that we partition the array into the first N entries, then the remaining k entries. The last k entries are the “extendible” entries.

We will eventually “digest” the extendible entries (by incrementing $N \leftarrow N+1$ and decrementing $k \leftarrow k-1$ until $k = 0$).

```

⟨ Public interface for mobjects.pas 309 ⟩ +=
  { MExtList object }
  MExtListPtr = ↑ MExtList;
  MExtList = object (MList)
    fExtCount: integer;
    constructor Init(aLimit : integer);
    destructor Done; virtual;
    procedure Insert(aItem : Pointer); virtual;
    procedure Mark(var aIndex : integer); virtual;
    procedure FreeItemsFrom(aIndex : integer); virtual;
    procedure DeleteAll; virtual;
    procedure FreeAll; virtual;
    procedure Pack; virtual;
    procedure InsertExt(AItem : Pointer); virtual;
    procedure SetLimit(ALimit : integer); virtual;
    procedure AddExtObject; virtual;
    procedure AddExtItems; virtual;
    procedure DeleteExtItems;
    procedure FreeExtItems;
  end ;

```

365. Simple Stacked (Extendable) Collection.

```

⟨ MExtList implementation 365 ⟩ ≡
constructor MExtList.Init(ALimit : integer);
  begin MObject.Init;
  Items ← nil;
  Count ← 0; Limit ← 0;
  SetLimit(ALimit); fExtCount ← 0;
end;

```

This code is used in section 308.

366. Destructor for MExtList. The destructor for *MExtList* invokes *self.FreeExtItems* and then calls the inherited destructor from the superclass.

```

destructor MExtList.Done;
  begin FreeExtItems; inherited Done; end;

```


367. Inserting an item. The *fExtCounter* field is unclear to me. But if it's nonzero, then an error has occurred and we bail out.

Otherwise, we possibly grow the extendible list, and we insert at the end the given pointer and increment the *Count* of items allocated.

```

procedure MExtList.Insert(aItem : Pointer);
  begin if fExtCount  $\neq$  0 then
    begin ListError(coIndexExtError, 0); exit; end;
  if Limit = Count then SetLimit(Limit + GrowLimit(Limit));
  Items↑[Count]  $\leftarrow$  aItem; { Append the item to the list }
  inc(Count);
end;

```

368. Deleting all entries. We can only call this when the extendible entries have been “digested” into the underlying array (i.e., when *fExtCount* = 0). Otherwise we need to flag an error. Otherwise, when all the extendible entries have been “digested”, we call the parent’s *DeleteAll* method.

```

procedure MExtList.DeleteAll;
  begin if fExtCount  $\neq$  0 then
    begin ListError(coIndexExtError, 0); exit;
    end;
  inherited DeleteAll;
end;

```

369. Free all entries. Like deleting all the entries, we need to fully digest all the extendible entries before invoking the parent class’s *FreeAll* method. If there are extendible entries not fully digested, then we get indigestion (i.e., a list error).

```

procedure MExtList.FreeAll;
  begin if fExtCount  $\neq$  0 then
    begin ListError(coIndexExtError, 0); exit;
    end;
  inherited FreeAll;
end;

```

370. Packing. When packing an extendible list, we assert the extendible items have been digested fully. If not, raise an error. If fully digested, then invoke the parent class’s *Pack* method.

```

procedure MExtList.Pack;
  begin if fExtCount  $\neq$  0 then
    begin ListError(coIndexExtError, 0); exit;
    end;
  inherited Pack;
end;

```

371. Insert extendible items. We can add an extendible item by first growing the list (if necessary), then adding an item at index $N + k$. Then increment the number of extendible items $k \leftarrow k + 1$.

```

procedure MExtList.InsertExt(AItem : Pointer);
  begin if Limit = Count + fExtCount then SetLimit(Limit + GrowLimit(Limit));
  Items↑[Count + fExtCount]  $\leftarrow$  AItem; inc(fExtCount);
end;

```

372. Ensure capacity of extendible list.

- (1) When the new limit is less than the logical size N and the extendible size k , we just set the capacity to $N + k$.
- (2) Else if the new limit is larger than $MaxCollectionSize$, then just use the maximum collection size as the capacity.
- (3) Else if the new limit is different than the existing capacity, then we have to check if the new limit is zero. When it is, just set the capacity to zero and the list of items to **nil**. Otherwise, allocate space for a new array, and move over the contents from the existing array (and then free the existing array). Update the capacity and pointer to the items.

```

procedure MExtList.SetLimit(ALimit : integer);
  var UItems: PItemList;
  begin if ALimit < Count + fExtCount then ALimit  $\leftarrow$  Count + fExtCount;
  if ALimit > MaxCollectionSize then ALimit  $\leftarrow$  MaxCollectionSize;
  if ALimit  $\neq$  Limit then
    begin if ALimit = 0 then UItems  $\leftarrow$  nil
    else begin GetMem(UItems, ALimit * SizeOf(Pointer));
      if ((Count + fExtCount)  $\neq$  0)  $\wedge$  (Items  $\neq$  nil) then
        Move(Items $\uparrow$ , UItems $\uparrow$ , (Count + fExtCount) * SizeOf(Pointer));
      end;
    if Limit  $\neq$  0 then FreeMem(Items, Limit * SizeOf(Pointer));
    Items  $\leftarrow$  UItems; Limit  $\leftarrow$  ALimit;
    end;
  end;

```

373. “Marking” an extendible list amounts to setting the procedure’s variable to the capacity of the extendible list.

```

procedure MExtList.Mark(var aIndex : integer);
  begin aIndex  $\leftarrow$  Count;
  end;

```

374. Freeing items starting at a given index requires the extendible items to be fully digested (if not, raise an error). Then simply free each object using the virtual destructor *MObject.Done*.

```

procedure MExtList.FreeItemsFrom(aIndex : integer);
  var I: integer;
  begin if fExtCount  $\neq$  0 then
    begin ListError(coIndexExtError, 0); exit;
    end;
  for I  $\leftarrow$  Count - 1 downto aIndex do
    if Items $\uparrow$ [I]  $\neq$  nil then Dispose(PObject(Items $\uparrow$ [I]), Done);
  Count  $\leftarrow$  aIndex;
  end;

```

375. Digesting one extendible item. We can instruct the extendible list to digest exactly one extendible item. This requires the number of extendible items to be positive $k > 0$. If not, raise an error. Otherwise increment the logical capacity $N \leftarrow N + 1$ and decrement the number of extendible items $k \leftarrow k - 1$.

```

procedure MExtList.AddExtObject;
  begin if fExtCount  $\leq$  0 then
    begin ListError(coIndexExtError, 0); exit;
    end;
  inc(Count); dec(fExtCount);
  end;

```

376. Digest all extendible items. This simply updates capacity to be incremented by the number of extendible items. Then the number of extendible items is set to zero. No error is raised if there are no extendible items (unlike digesting one single extendible item).

```
procedure MExtList.AddExtItems;  
  begin Count  $\leftarrow$  Count + fExtCount; fExtCount  $\leftarrow$  0;  
  end;
```

377. Deleting all extendible items simply sets the *number* of extendible items to zero. This is a “soft delete” which does not affect anything else on the heap.

```
procedure MExtList.DeleteExtItems;  
  begin fExtCount  $\leftarrow$  0;  
  end;
```

378. Freeing all the extendible items will “hard delete” each extendible item, removing them from the heap.

```
procedure MExtList.FreeExtItems;  
  var I: integer;  
  begin for I  $\leftarrow$  0 to fExtCount - 1 do  
    if Items $\uparrow$ [Count + I]  $\neq$  nil then Dispose(PObject(Items $\uparrow$ [Count + I]), Done);  
  fExtCount  $\leftarrow$  0;  
  end;
```

Section 10.6. SORTED LISTS

379. These are used in the equalizer and in the correlator, specifically for keeping a collection of identifiers.

A sorted list uses an array of indices (called *fIndex*). The array of indices are sorted according to a comparison of values.

Invariant: $Length(fIndex) = Length(Items)$

Invariant (sorted): for each $i = 0, \dots, Length(Items) - 2$, we have $Items \uparrow [fIndex \uparrow [i]] \leq Items \uparrow [fIndex \uparrow [i + 1]]$.

Also, we are taking the convention that $fCompare(x, y)$ returns -1 when $x < y$; returns 0 when $x = y$; returns $+1$ when $x > y$.

```

⟨Public interface for mobjects.pas 309⟩ +≡
  { MSortedList Object }
  IndexListPtr = ↑MIndexList;
  MIndexList = array [0 .. MaxCollectionSize - 1] of integer;
  CompareProc = function (aItem1, aItem2 : Pointer): integer;
  MSortedList = object (MList)
    fIndex: IndexListPtr;
    fCompare: CompareProc;
    constructor Init(aLimit : integer);
    constructor InitSorted(aLimit : integer; aCompare : CompareProc);
    constructor MoveList(var aAnother : MList);
    constructor CopyList(const aAnother: MList);
    procedure AtInsert(aIndex : integer; aItem : Pointer); virtual;
    procedure Insert(aItem : Pointer); virtual;
    function IndexOf(aItem : Pointer): integer; virtual;
    procedure Sort(aCompare : CompareProc);
    procedure SetLimit(ALimit : integer); virtual;
    function Find(aKey : Pointer; var aIndex : integer): boolean; virtual;
    function Search(aKey : Pointer; var aIndex : integer): boolean; virtual;
    procedure Pack; virtual;
    procedure FreeItemsFrom(aIndex : integer); virtual;
  end ;

```

380. Constructors. There are four constructors:

- (1) *Init* simply creates an empty list with a given capacity.
- (2) *InitSorted* is like *Init*, but expects an ordering operator.
- (3) *MoveList* moves all the items from another list into the caller, sorting as needed. This will also empty the other list.
- (4) *CopyList* is like *MoveList* but leaves the other list untouched.

```

⟨MSortedList implementation 380⟩ ≡
  { MSortedList object }
  constructor MSortedList.Init(aLimit : integer);
  begin MObject.Init; Items ← nil; Count ← 0; Limit ← 0; fIndex ← nil; fCompare ← nil;
  SetLimit(ALimit);
  end;
  constructor MSortedList.InitSorted(aLimit : integer; aCompare : CompareProc);
  begin MObject.Init; Items ← nil; Count ← 0; Limit ← 0; fIndex ← nil; fCompare ← aCompare;
  SetLimit(ALimit);
  end;

```

See also section 392.

This code is used in section 308.

381. Move constructor. When we move items from an *MList* into the caller, we also sort as we insert.

```

constructor MSortedList.MoveList(var aAnother : MList);
  var I: integer;
  begin Items  $\leftarrow$  aAnother.Items; Count  $\leftarrow$  aAnother.Count; Limit  $\leftarrow$  aAnother.Limit;
    GetMem(fIndex, Limit * SizeOf(integer)); fCompare  $\leftarrow$  nil;
    for I  $\leftarrow$  0 to pred(aAnother.Count) do fIndex $\uparrow$ [I]  $\leftarrow$  I;
      { Empty out the other list }
    aAnother.DeleteAll; aAnother.Limit  $\leftarrow$  0; aAnother.Items  $\leftarrow$  nil;
  end;

```

382. The *CopyList* constructor is like the *MoveList* **except** that the other list is not modified.

```

constructor MSortedList.CopyList(const aAnother: MList);
  var i: integer;
  begin MObject.Init; Items  $\leftarrow$  nil; Count  $\leftarrow$  0; Limit  $\leftarrow$  0; fIndex  $\leftarrow$  nil; fCompare  $\leftarrow$  nil;
    SetLimit(aAnother.Limit); Count  $\leftarrow$  aAnother.Count;
    for i  $\leftarrow$  0 to Count - 1 do
      begin Items $\uparrow$ [i]  $\leftarrow$  PObject(aAnother.Items $\uparrow$ [i]) $\uparrow$ .MCopy; fIndex $\uparrow$ [i]  $\leftarrow$  i;
      end;
    end;

```

383. Insert element at an index. We can insert (potentially overwriting an existing entry) at a given index.

```

  { used in CollectCluster not to repeat the search, should be used only when @fCompare  $\neq$  nil }
procedure MSortedList.AtInsert(aIndex : integer; aItem : Pointer);
  begin if Limit = Count then SetLimit(Limit + GrowLimit(Limit)); { Ensure capacity }
  if aIndex  $\neq$  Count then
    Move(fIndex $\uparrow$ [aIndex], fIndex $\uparrow$ [aIndex + 1], (Count - aIndex) * SizeOf(integer));
    Items $\uparrow$ [Count]  $\leftarrow$  aItem; fIndex $\uparrow$ [aIndex]  $\leftarrow$  Count; inc(Count);
  end;

```

384. Inserting an item. Inserting an item into a sorted list boils down to two cases:

- (1) If there is an ordering operator, we check if the item is in the underlying array using *Find* (§389), which will mutate the *lIndex* to be where it should be located. When the item is missing, simply insert it at *lIndex*. When the item is present, then we do nothing.
- (2) If there is no ordering operator, then check if the item already is present in the sorted list. If so, then don't do anything. Otherwise, insert the item at the start of the list.

```

procedure MSortedList.Insert(aItem : Pointer);
  var lIndex: integer;
  begin if @fCompare = nil then
    begin if Limit = Count then SetLimit(Limit + GrowLimit(Limit));
      Items $\uparrow$ [Count]  $\leftarrow$  aItem; fIndex $\uparrow$ [Count]  $\leftarrow$  Count; inc(Count); exit;
    end;
  if  $\neg$ Find(aItem, lIndex) then AtInsert(lIndex, aItem);
  end;

```

385. Resizing a sorted list. The invariant is that the list is sorted when it has an ordering operator (and so restricting to $aLimit$ preserves the list being sorted), and it is a “set” when it does not have an ordering (and so restricting to $aLimit$ preserves this property of being a finite set without duplicate entries).

```

procedure MSortedList.SetLimit( $aLimit$  : integer);
  var lItems: PItemList; lIndex: IndexListPtr;
  begin if  $aLimit < Count$  then  $aLimit \leftarrow Count$ ;
  if  $aLimit > MaxCollectionSize$  then  $aLimit \leftarrow MaxCollectionSize$ ;
  if  $aLimit \neq Limit$  then
    begin if  $aLimit = 0$  then
      begin lItems  $\leftarrow$  nil; lIndex  $\leftarrow$  nil; end
    else begin GetMem(lItems,  $aLimit * SizeOf(Pointer)$ ); GetMem(lIndex,  $aLimit * SizeOf(integer)$ );
      if  $Count \neq 0$  then
        begin if Items  $\neq$  nil then
          begin Move(Items $\uparrow$ , lItems $\uparrow$ ,  $Count * SizeOf(Pointer)$ );
            Move(fIndex $\uparrow$ , lIndex $\uparrow$ ,  $Count * SizeOf(integer)$ );
          end;
        end;
      end;
    end;
  if  $Limit \neq 0$  then
    begin FreeMem(Items,  $Limit * SizeOf(Pointer)$ ); FreeMem(fIndex,  $Limit * SizeOf(integer)$ );
    end;
  Items  $\leftarrow$  lItems; fIndex  $\leftarrow$  lIndex; Limit  $\leftarrow$  aLimit;
  end;
end;

```

386. Quick sort an array. We have a private helper function for quicksorting an *IndexListPtr* (§379). Initially $L \leftarrow 0$ and $R \leftarrow \text{length}(aList) - 1$. It may be instructive to compare this to Algorithm Q in *The Art of Computer Programming*, third ed., volume 3, §5.2.2. Specifically Mizar appears to use Hoare partitioning. We can summarize its algorithm thus:

Algorithm S (*Quicksort*). This uses Hoare partition. We assume that $L \leq R$, and that *aCompare* is a total order (it's transitive and the law of trichotomy holds on all pairs of elements). Steps S1 through S4 are better known as the “partition” procedure.

- S0.** [Initialize] Set $I \leftarrow L$, $J \leftarrow R$, and the pivot index $P_{idx} \leftarrow (L + R) \text{ shr } 1$, and the pivot value $P \leftarrow aList \uparrow [aIndex \uparrow [(L + R) \text{ shr } 1]]$. Observe $I \leq P_{idx} \leq J$ at this point.
- S1.** [Move *I* right] While $aList[I] < P$, we increment $I \leftarrow I + 1$. This is guaranteed to terminate since $I \leq P_{idx}$, so eventually we will get to $aList[i] = P$.
- S2.** [Move *J* left] While $P < aList[J]$, we decrement $J \leftarrow J - 1$. This is guaranteed to terminate since $P_{idx} \leq J$, so eventually we will get to $aList[J] = P$.
- S3.** [Keep going?] If $I > J$, then we're done “partitioning” (so everything to the left of the pivot is not greater than the pivot value, and everything to the right of the pivot is not lesser than the pivot value), and we go to step S5; otherwise go to the next step.
- S4.** [Swap entries *I* and *J*] We swap the entries located at *I* and *J*, then set $I \leftarrow I + 1$, and $J \leftarrow J - 1$. If $I \leq J$, then return to step S1.
- S5.** [Recur on left half] If $L < J$, then recursively call quicksort on the left half of the index (entries between $L \dots J - 1$).
- S6.** [Sort the right half] If $I \geq R$, then terminate. Otherwise, set $L \leftarrow I$ and return to step S0. ■

For readability, we also introduce a **WEB** macro for swapping the indices.

```

define steal_from(#)  $\equiv aIndex \uparrow [\#]$ ;  $aIndex \uparrow [\#] \leftarrow T$ ;
define swap_indices(#)  $\equiv T \leftarrow aIndex \uparrow [\#]$ ;  $aIndex \uparrow [\#] \leftarrow steal\_from$ 
procedure ListQuickSort(aList : PItemList; aIndex : IndexListPtr; L, R : integer;
    aCompare : CompareProc);
var I, J, T: integer; P: Pointer;
begin repeat  $I \leftarrow L$ ;  $J \leftarrow R$ ;  $P \leftarrow aList \uparrow [aIndex \uparrow [(L + R) \text{ shr } 1]]$ ;
  repeat
    {  $I \leq (L + R) \text{ shr } 1 \leq J$  }
    while  $aCompare(aList \uparrow [aIndex \uparrow [I]], P) < 0$  do inc(I);
    {  $P \leq aList \uparrow [aIndex \uparrow [I]]$  }
    while  $aCompare(aList \uparrow [aIndex \uparrow [J]], P) > 0$  do Dec(J);
    {  $aList \uparrow [aIndex \uparrow [J]] \leq P$  }
    {  $I \leq (L + R) \text{ shr } 1 \leq J$  }
    if  $I \leq J$  then
      begin
        {  $aList \uparrow [aIndex \uparrow [J]] < P < aList \uparrow [aIndex \uparrow [I]]$  }
        swap_indices(I)(J);
        {  $aList \uparrow [aIndex \uparrow [I]] < P < aList \uparrow [aIndex \uparrow [J]]$  }
        {  $I < J$  implies  $inc(I) \leq dec(J)$  }
        {  $I = J$  implies  $inc(I) > dec(J)$  }
        inc(I); Dec(J);
      end;
    until  $I > J$ ;
    {  $J \leq (L + R) \text{ shr } 2 \leq I$  and  $J < I$  }
    if  $L < J$  then ListQuickSort(aList, aIndex, L, J, aCompare); { quicksort left half }
     $L \leftarrow I$ ; { recursively quicksort the right half of the array }
  until  $I \geq R$ ;
end;

```

387. Remarks.

- (1) It is unclear to me whether we must have $aCompare$ be a linear order, and not a total pre-order. The difference is: do we really need $a \leq b \wedge b \leq a \implies a = b$ (i.e., a total order) or not (i.e., a total pre-order)?
- (2) PRECONDITION: We need to prove the *compare* operators are total orders for quicksort to work as expected.
- (3) ASSERT: Upon arriving to step Q5, the entries in $L \dots J - 1$ are partitioned (i.e., less than the pivot value) as is the entries in $I \dots R$. In particular, the maximal element in $L \dots J - 1$ is located at $J - 1$ while the minimal element in $I \dots R$ is located at I .
- (4) Robert Sedgewick's *Quicksort* (1980) is literally *the* book on the subject. An abbreviated reference may be found in Sedgewick's "The Analysis of Quicksort Programs" (*Acta Inform.* **7** (1977) 327–355, [eprint](#))
- (5) IMPROVEMENT: This can be improved when recursively sorting the left half of the arrays by first checking if $J - L \leq 9$ then use insertion sort otherwise recursively quicksort the left half. (Similarly, instead of iterating the outermost while-loop, we should test if $R - I \leq 9$ then invoking insertion on the subarray indexed by $I \dots R$.)
- (6) IMPROVEMENT: The pivot index P_{ind} is selected as $P_{ind} \leftarrow (L + R)/2$, which can lead to overflow. A safer way to compute this would be $P_{ind} \leftarrow L + ((R - L)/2)$.

According to the paper by Sedgewick we cited, when quicksorting a list of size less than M with a different sorting algorithm, the optimal choice of M (the cutoff for delegating to another sort algorithm) contributes to the runtime of quicksort,

$$f(M) = \frac{1}{6} \left(8M + 71 - 70H_{M+2} + \frac{270}{M+2} + \frac{54}{2M+3} - 36\frac{H_{M+1}}{M+2} \right).$$

We can use the approximation for Harmonic numbers

$$H_n = \ln(n) + \gamma + \frac{1}{2n} + O(n^{-2})$$

where $\gamma \approx 0.57721$ is Euler-Mascheroni constant. Using this replacement, we have

$$f'(M) \approx \frac{4}{3} + \frac{3}{(1+m)^2} - \frac{6}{1+m} + \frac{36\gamma - 253}{6(2+m)^2} - \frac{17}{3(2+m)} - \frac{18}{(3+2m)^2} + \frac{6\ln(1+m)}{(2+m)^2}.$$

We can numerically find the root for this to be $m_0 \approx 8.9888$ which gives a global minimum of $f(9) \approx -8.47671$.

This analysis is sketched out in Knuth's *The Art of Computer Programming*, volume III, but it may be worth sitting down and working this analysis out more fully.

388. Sorting a sorted list. We can update a sorted list to sort according to a new ordering operator, and also update the data structure to record this new ordering operator. This relies on *ListQuickSort* (§386) to do the actual sorting.

```

procedure MSortedList.Sort( $aCompare$  : CompareProc);
  var  $I$ : integer;
  begin  $fCompare \leftarrow aCompare$ ;
  for  $I \leftarrow 0$  to  $Count - 1$  do  $fIndex \uparrow[I] \leftarrow I$ ;
  if ( $Count > 0$ ) then ListQuickSort( $Items, fIndex, 0, Count - 1, aCompare$ );
  end;

```


389. Find item. Finding an item in a sorted list boils down to two cases: do we have *fCompare* populated or not? If so, then use a binary search. If not, then just iterate item-by-item testing if *aKey* is in the underlying array.

CAUTION: The “find” function returns the index for the *fIndex* field, **NOT** the index for the underlying array of values (inherited from the *MList* class).

```
function MSortedList.Find(aKey : Pointer; var aIndex : integer): boolean;
var L, H, I, C: integer;
begin Find  $\leftarrow$  False;
if @fCompare = nil then  $\langle$ Find needle in MSortedList by brute force 391 $\rangle$ ;
 $\langle$ Find needle in MSortedList by binary search 390 $\rangle$ 
end;
```

390. Binary search is a little clever. We have *L* be the lower bounds index, and *H* the upper bounds index. The midpoint is obtained by taking their sum $L + H$ and shifting to the right by 1 bit (which corresponds to dividing by 2, truncating the result).

We compare the item located at the midpoint to the given *aKey*, and store the result of this comparison in the variable *C*. If $C < 0$, then *aKey* is located to the right of the midpoint (so set $L \leftarrow I + 1$).

On the other hand, if $C \geq 0$, update $H \leftarrow I - 1$. When $C = 0$ (i.e., the midpoint *is equal to aKey*), then we set $L \leftarrow I + 1$ so we have $H < L$ to terminate the loop. We set the return value to *True* when $C = 0$, and we mutate the *aIndex* to the index where we found the needle in the haystack.

```
 $\langle$ Find needle in MSortedList by binary search 390 $\rangle \equiv$ 
L  $\leftarrow$  0; H  $\leftarrow$  Count - 1;
while  $L \leq H$  do
  begin  $I \leftarrow (L + H) \text{ shr } 1$ ;  $C \leftarrow fCompare(Items \uparrow [fIndex \uparrow [I]], aKey)$ ;
  if  $C < 0$  then  $L \leftarrow I + 1$ 
  else begin  $H \leftarrow I - 1$ ;
    if  $C = 0$  then
      begin Find  $\leftarrow$  True;  $L \leftarrow I$ ; end;
    end;
  end;
aIndex  $\leftarrow$  L;
```

This code is used in section 389.

391. We can simply iterate through the underlying array, testing item-by-item if each entry is equal to the needle or not.

```
 $\langle$ Find needle in MSortedList by brute force 391 $\rangle \equiv$ 
begin aIndex  $\leftarrow$  Count;
for  $I \leftarrow 0$  to Count - 1 do
  if  $aKey = Items \uparrow [I]$  then
    begin Find  $\leftarrow$  True; aIndex  $\leftarrow$  I; break end;
  exit;
end
```

This code is used in section 389.

392. Search. We recall that *Find* returns the index of the *fIndex* field matching the needle. Usually, we want to know the index of the value itself. This is what *Search* performs.

$\langle \text{MSortedList implementation } 380 \rangle + \equiv$
function *MSortedList.Search*(*aKey* : *Pointer*; **var** *aIndex* : *integer*): *boolean*;
 var *I*: *integer*;
 begin *aIndex* \leftarrow *Count*; *Search* \leftarrow *false*;
 if *Find*(*aKey*, *I*) **then**
 begin *Search* \leftarrow *true*; *aIndex* \leftarrow *fIndex* \uparrow [*I*];
 end;
 end;

393. Index of a needle. Given a “needle”, where in the haystack is it? Well, we require the ordering operator be non-nil for the sorted list — otherwise raise an error. Then using *Find* (§389), check if the entry is present. If it is, then return the index for the underlying array of values.

If the needle is not in the haystack, return -1 .

function *MSortedList.IndexOf*(*aItem* : *Pointer*): *integer*;
 var *I*: *integer*;
 begin **if** @*fCompare* = **nil** **then**
 begin *ListError*(*coSortedListError*, 0); *exit*;
 end;
 IndexOf \leftarrow -1 ;
 if *Find*(*aItem*, *I*) **then**
 begin { *if I < fCount then* }
 IndexOf \leftarrow *fIndex* \uparrow [*I*];
 end;
 end;

394. Packing a sorted list. Use the superclass’s *Pack* method. Then, when there is an ordering operator present, sort the list.

procedure *MSortedList.Pack*;
 var *lCount*: *integer*;
 begin *lCount* \leftarrow *Count*; *inherited Pack*;
 if (@*fCompare* \neq **nil**) \wedge (*lCount* > *Count*) **then** *Sort*(*fCompare*);
 end;

395. Free items starting at an index. When we want to remove all items starting at index a , we simply iterate through the array of indices starting at entry $i = a$ and delete the value associated with $Items[i]$ when it is non-**nil**.

This will also keep the indices for the non-deleted entries.

```

procedure MSortedList.FreeItemsFrom(aIndex : integer);
  var I, k: integer;
  begin if aIndex = Count then exit;
  { Delete entries from the array of values }
  for I  $\leftarrow$  aIndex to Count - 1 do
    if Items $\uparrow$ [I]  $\neq$  nil then Dispose(PObject(Items $\uparrow$ [I]), Done);
  { Update the array of indices }
  k  $\leftarrow$  0;
  for I  $\leftarrow$  0 to Count - 1 do
    begin if fIndex $\uparrow$ [I] < aIndex then
      begin fIndex $\uparrow$ [k]  $\leftarrow$  fIndex $\uparrow$ [I]; inc(k); end;
    end;
  if k  $\neq$  aIndex then ListError(coSortedListError, 0);
  Count  $\leftarrow$  aIndex;
end;

```

Section 10.7. SORTED EXTENDIBLE LISTS

396. We want to handle a sorted (§379) version of extendible lists — an *MSortedExtList*. It's used in the correlator for functorial registrations and inferred definition constants.

Like *MSortedList*, we add a field *fIndex* for the indices of the entries. This will track the *digested* items, not the extendible items.

An important invariant: the ordering operator (*fCompare*) must be non-**nil**.

⟨Public interface for `mobjects.pas` 309⟩ +≡

```
MSortedExtList = object (MExtList)
  fIndex: IndexListPtr;
  fCompare: CompareProc;
  constructor Init(ALimit : integer);
  constructor InitSorted(aLimit : integer; aCompare : CompareProc);
  destructor Done; virtual;
  function Find(aKey : Pointer; var aIndex : integer): boolean; virtual;
  function FindRight(aKey : Pointer; var aIndex : integer): boolean; virtual;
  function FindInterval(aKey : Pointer; var aLeft, aRight : integer): boolean; virtual;
  function AtIndex(aIndex : integer): Pointer; virtual;
  procedure Insert(aItem : Pointer); virtual;
  procedure Pack; virtual;
  procedure InsertExt(AItem : Pointer); virtual;
  procedure SetLimit(ALimit : integer); virtual;
  procedure FreeItemsFrom(aIndex : integer); virtual;
  procedure AddExtObject; virtual;
  procedure AddExtItems; virtual;
end ;
```

397. Constructors. The *Init* constructor should not be used, and should raise an error if anyone tries to use it.

Instead, the *InitSorted* should be used to construct a new [empty] sorted extendible list with a given ordering operator.

⟨*MSortedExtList* implementation 397⟩ ≡

```
{ MSortedExtList always with possible duplicate keys, always sorted }
constructor MSortedExtList.Init(ALimit : integer);
  begin ListError(coIndexExtError, 0); end;
constructor MSortedExtList.InitSorted(aLimit : integer; aCompare : CompareProc);
  begin inherited Init(aLimit); fCompare ← aCompare;
  end;
```

This code is used in section 308.

398. destructor The destructor for sorted extendible lists is just the inherited destructor from extendible lists.

```
destructor MSortedExtList.Done;
  begin inherited Done; end;
```

399. Finding a needle in the haystack. We require *fCompare* to be non-**nil** and enforce that invariant by raising an error when it is **nil**.

Then we just use bisection search to find the needle in the haystack. Once found, we mutate *aIndex* to the index *L* of the *fIndex* array which indexes the needle.

{ find the left-most if duplicates }

```
function MSortedExtList.Find(aKey : Pointer; var aIndex : integer): boolean;
  var L, H, I, C: integer;
  begin if ¬Assigned(fCompare) then ListError(coIndexExtError, 0);
    Find ← False; L ← 0; H ← Count - 1;
    while L ≤ H do
      begin I ← (L + H) shr 1; C ← fCompare(Items↑[fIndex↑[I]], aKey);
        if C < 0 then L ← I + 1
        else begin H ← I - 1;
          if C = 0 then Find ← True;
          end;
        end;
      end;
    aIndex ← L;
  end;
```

400. Find the rightmost index for a needle in the haystack. Since the underlying array is sorted, we check to see if the needle is in the haystack. If it is, we keep incrementing *aIndex* until it is no longer indexing the needle.

So upon return, if it returns *True*, then the *aIndex* parameter is mutated to equal the rightmost index for the needle's appearance in the haystack.

{ find the left-most with higher aKey, this is where we can insert }

```
function MSortedExtList.FindRight(aKey : Pointer; var aIndex : integer): boolean;
  begin if Find(aKey, aIndex) then
    begin while (aIndex < Count) ∧ (0 = fCompare(Items↑[fIndex↑[aIndex]], aKey)) do inc(aIndex);
      FindRight ← true;
    end
    else FindRight ← false;
  end;
```

401. Since we allow duplicate values in a sorted extendible list, we will sometimes wish to know the “interval” of entries equal to a needle. This will mutate *aLeft* and *aRight* to point to the beginning and end of the interval.

When the needle is not in the haystack, the function will mutate the variables to ensure *aRight* < *aLeft* to stress the point.

Possible bug: This assumes the *MSortedExtList.Find* returns the left-most index where the needle appears in the haystack.

{ find the interval of equal guys }

```
function MSortedExtList.FindInterval(aKey : Pointer; var aLeft, aRight : integer): boolean;
  begin if Find(aKey, aLeft) then
    begin aRight ← aLeft + 1;
      while (aRight < Count) ∧ (0 = fCompare(Items↑[fIndex↑[aRight]], aKey)) do inc(aRight);
        dec(aRight); FindInterval ← true;
      end
    else begin aRight ← aLeft - 1; FindInterval ← false;
      end;
  end;
```

402. Get value at index. We check if the index i is within bounds of the sorted extendible list. If not, then we raise an error.

Otherwise, the default course of action, we simply lookup the entry $fIndex[i]$ and then lookup the entry in the array of values located with that index.

```
function MSortedExtList.AtIndex(aIndex : integer): Pointer;
  begin if (aIndex < 0)  $\vee$  (aIndex  $\geq$  Count) then ListError(coIndexExtError, 0);
  AtIndex  $\leftarrow$  Items $\uparrow$ [fIndex $\uparrow$ [aIndex]];
end;
```

403. Inserting items. We can only insert an item into an extendible list when it has fully digested all its extendible items. This requirement carries over to sorted extendible lists.

When there are no extendible items, we delegate the work to *InsertExt*.

```
procedure MSortedExtList.Insert(aItem : Pointer);
  begin if fExtCount  $\neq$  0 then ListError(coIndexExtError, 0);
  InsertExt(aItem); AddExtObject;
end;
```

404. Packing a sorted extendible list is unsupported, so just raise an error if anyone tries to use it.

```
procedure MSortedExtList.Pack;
  begin ListError(coIndexExtError, 0);
end;
```

405. Adding an extendible item. We ensure there is sufficient capacity in the underlying array of items, then add *AItem* at the position located by the logical size of the array of items. We also increment the number of extendible items.

```
procedure MSortedExtList.InsertExt(AItem : Pointer);
  begin if Limit = Count + fExtCount then SetLimit(Limit + GrowLimit(Limit));
  Items $\uparrow$ [Count + fExtCount]  $\leftarrow$  AItem; inc(fExtCount);
end;
```

406. Ensure capacity. We can ensure the capacity of a sorted extendible list to be at least as large as $ALimit$.

When $ALimit$ is smaller than the current capacity of the sorted extendible list, we allocate new arrays and copy over the old data. More importantly: we keep the last $fExtCount$ items as (“undigested”) extendible items.

```

procedure MSortedExtList.SetLimit( $ALimit$  : integer);
  var lItems: PItemList; lIndex: IndexListPtr;
  begin Count  $\leftarrow$  Count + fExtCount;
  if aLimit < Count then aLimit  $\leftarrow$  Count;
  if aLimit > MaxCollectionSize then aLimit  $\leftarrow$  MaxCollectionSize;
  if aLimit  $\neq$  Limit then
    begin if aLimit = 0 then
      begin lItems  $\leftarrow$  nil; lIndex  $\leftarrow$  nil;
      end
    else begin { Allocate new arrays for indices and items }
      GetMem(lItems, aLimit * SizeOf(Pointer)); GetMem(lIndex, aLimit * SizeOf(integer));
      if Count  $\neq$  0 then { Copy items and indices from old arrays to new ones }
        begin if Items  $\neq$  nil then
          begin Move(Items $\uparrow$ , lItems $\uparrow$ , Count * SizeOf(Pointer));
            Move(fIndex $\uparrow$ , lIndex $\uparrow$ , Count * SizeOf(integer));
          end;
        end;
      end;
    if Limit  $\neq$  0 then { Free old arrays }
      begin FreeMem(Items, Limit * SizeOf(Pointer)); FreeMem(fIndex, Limit * SizeOf(integer));
      end;
    Items  $\leftarrow$  lItems; fIndex  $\leftarrow$  lIndex; Limit  $\leftarrow$  aLimit; { Update the caller to use new arrays }
    end;
  Count  $\leftarrow$  Count - fExtCount;
end;

```

407. Freeing items starting at an index. We have two exceptional situations:

- (1) The $fExtCount$ must be zero, and if it is nonzero, then an error is raised; and
- (2) If the index given is equal to the logical size of the sorted extendible list, then we terminate early (since there is nothing to do).

```

procedure MSortedExtList.FreeItemsFrom(aIndex : integer);
  var I, k: integer;
  begin if  $fExtCount \neq 0$  then ListError(coIndexExtError, 0);
  if  $aIndex = Count$  then exit;
  { Free items indexed by  $I \geq aIndex$  }
  for  $I \leftarrow aIndex$  to  $Count - 1$  do
    if  $Items \uparrow [I] \neq \text{nil}$  then Dispose(PObject( $Items \uparrow [I]$ ), Done);
  { Sort  $fIndex$  for entries less than  $aIndex$  }
   $k \leftarrow 0$ ;
  for  $I \leftarrow 0$  to  $Count - 1$  do
    begin if  $fIndex \uparrow [I] < aIndex$  then
      begin  $fIndex \uparrow [k] \leftarrow fIndex \uparrow [I]$ ; inc( $k$ );
      end;
    end;
  if  $k \neq aIndex$  then ListError(coSortedListError, 0);
   $Count \leftarrow aIndex$ ;
end;

```

408. Digest an extendible object. When there are extendible objects left to digest among the values (i.e., when $fExtCount > 0$), When $fExtCount \leq 0$, then raise an error (there's nothing left to digest).

The first extendible item left to be digested is located at $Count$ in the array of items. Then we find the right most index for the same extendible item. We digest all of them at once, shifting the $fIndex$ as needed.

Note that the need to shift $fIndex$ down by 1 is needed to keep the array of items sorted.

```

procedure MSortedExtList.AddExtObject;
  var UIndex: integer;
  begin if  $fExtCount \leq 0$  then ListError(coIndexExtError, 0);
  FindRight( $Items \uparrow [Count]$ , UIndex);
  if  $UIndex \neq Count$  then { shift  $fIndex$  to right by 1 }
    Move( $fIndex \uparrow [UIndex]$ ,  $fIndex \uparrow [UIndex + 1]$ ,  $(Count - UIndex) * SizeOf(integer)$ );
   $fIndex \uparrow [UIndex] \leftarrow Count$ ; { extendible item's index }
  inc( $Count$ ); Dec( $fExtCount$ );
end;

```

409. Digest all extendible items. We can simply iterate through all the extendible items, digesting them one-by-one.

```

procedure MSortedExtList.AddExtItems;
  begin while  $fExtCount > 0$  do AddExtObject;
end;

```


Section 10.8. SORTED LIST OF STRINGS

410. This is used in the kernel to track directives, as well as `makenv` and `accdict` needs it.

```

⟨Public interface for mobjects.pas 309⟩ +≡
  MSortedStrList = object (MSortedList)
    constructor Init(ALimit : integer);
    function IndexOfStr(const aStr: String): integer; virtual;
    function ObjectOf(const aStr: String): PObject; virtual;
  end ;

```

411. **Pointer comparison.** For strings, it is faster to use pointer comparison than lexicographic ordering. Although pointer comparison is a total linear order, it may not produce intuitive comparisons.

```

⟨MSortedStrList implementation 411⟩ ≡
  { MSortedStrList }
function CompareStringPtr(aKey1, aKey2 : Pointer): integer;
begin if PStr(aKey1)↑.fStr < PStr(aKey2)↑.fStr then CompareStringPtr ← -1
else if PStr(aKey1)↑.fStr = PStr(aKey2)↑.fStr then CompareStringPtr ← 0
else CompareStringPtr ← 1;
end;

```

This code is used in section 308.

412. **Constructor.** We just defer to the *InitSorted* constructor for sorted lists (§380).

As an invariant, the *fCompare* ordering operator is *always* assumed to be set to the *CompareStringPtr*. There is no other way to construct a sorted string list besides this constructor, which enforces this invariant.

```

constructor MSortedStrList.Init(ALimit : integer);
begin InitSorted(ALimit, CompareStringPtr);
end;

```

413. We can locate a string by *Find*-ing its entry in the *fIndex* array.

```

function MSortedStrList.IndexOfStr(const aStr: string): integer;
var I: integer; lStringObj: MStrObj;
begin IndexOfStr ← -1;
if @fCompare = nil then { Invariant violation }
begin ListError(coSortedListError, 0); exit;
end;
lStringObj.Init(aStr);
if Find(@lStringObj, I) then
begin if I < Count then IndexOfStr ← fIndex↑[I];
end;
end;

```

414. We also can return the pointer to the object, if it is present in the sorted string list.

```

function MSortedStrList.ObjectOf(const aStr: string): PObject;
var I: integer;
begin ObjectOf ← nil; I ← IndexOfStr(aStr);
if I ≥ 0 then ObjectOf ← Items↑[I];
end;

```

Section 10.9. SORTED COLLECTIONS**415.**

```

⟨ Public interface for mobjects.pas 309 ⟩ +≡
  { MSortedCollection object }
  PSortedCollection = ↑MSortedCollection;
  MSortedCollection = object (MCollection)
    Duplicates: boolean;
    fCompare: CompareProc;
    constructor Init(ALimit, ADelta : integer);
    constructor InitSorted(ALimit, ADelta : integer; aCompare : CompareProc);
    function Compare(Key1, Key2 : Pointer): integer; virtual;
    function IndexOf(aItem : Pointer): integer; virtual;
    procedure Insert(aItem : Pointer); virtual;
    procedure InsertD(Item : Pointer); virtual;
    function KeyOf(Item : Pointer): Pointer; virtual;
    function Search(Key : Pointer; var Index : integer): boolean; virtual;
  end ;

```

416. Constructors. We can construct a sorted collection without an ordering operator, and we can construct one with an ordering operator.

```

⟨ MSortedCollection implementation 416 ⟩ ≡
  { MSortedCollection }
constructor MSortedCollection.Init(aLimit, aDelta : integer);
  begin inherited Init(ALimit, ADelta); Duplicates ← False; fCompare ← nil;
  end;
constructor MSortedCollection.InitSorted(aLimit, aDelta : integer; aCompare : CompareProc);
  begin inherited Init(ALimit, ADelta); Duplicates ← False; fCompare ← aCompare;
  end;

```

This code is used in section 308.

417. Comparing entries. This will invoke *Abstract1* (§307) when there is no ordering operator, which itself raises an error 211.

Otherwise, this just invokes *fCompare* on the two entries.

```

function MSortedCollection.Compare(Key1, Key2 : Pointer): integer;
  begin if @fCompare = nil then Abstract1;
  Compare ← fCompare(Key1, Key2);
  end;

```

418. Find the right-most index for an item in the collection. Searching (§422) for the *KeyOf* (§421). This function corrects for the possible bug in *Search* (§422) which will return the index *just to the left* of an item.

```

function MSortedCollection.IndexOf(aItem : Pointer): integer;
  var I: integer;
  begin IndexOf ← -1;
  if Search(KeyOf(aItem), I) then
    begin if Duplicates then
      while (I < Count) ∧ (aItem ≠ Items↑[I]) do inc(I);
      if I < Count then IndexOf ← I;
    end;
  end;

```

419. Insert the item when it is not in the collection (or if duplicates are allowed). Otherwise do not mutate the caller.

```
procedure MSortedCollection.Insert(aItem : Pointer);
  var I: integer;
  begin if  $\neg$ Search(KeyOf(aItem), I)  $\vee$  Duplicates then AtInsert(I, aItem);
  end;
```

420. Insert an item if it's not in the collection (or if there are duplicates allowed in the collection). Otherwise, delete the item and do not mutate the caller.

```
procedure MSortedCollection.InsertD(Item : Pointer);
  var I: integer;
  begin if  $\neg$ Search(KeyOf(Item), I)  $\vee$  Duplicates then AtInsert(I, Item)
  else Dispose(PObject(Item), Done);
  end;
```

421. We treat the item itself as the key, so return the item. That is to say, this is the identity function. It does not mutate the caller.

```
function MSortedCollection.KeyOf(Item : Pointer): Pointer;
  begin KeyOf  $\leftarrow$  Item;
  end;
```

422. Binary search. This is binary search through a sorted collection. If there are duplicates, this will return the left-most index.

```
function MSortedCollection.Search(Key : Pointer; var Index : integer): boolean;
  var L, H, I, C: integer;
  begin Search  $\leftarrow$  False; L  $\leftarrow$  0; H  $\leftarrow$  Count - 1;
  while L  $\leq$  H do
    begin I  $\leftarrow$  (L + H) shr 1; C  $\leftarrow$  Compare(KeyOf(Items↑[I]), Key);
    if C < 0 then L  $\leftarrow$  I + 1
    else begin H  $\leftarrow$  I - 1;
      if C = 0 then
        begin Search  $\leftarrow$  True;
        if  $\neg$ Duplicates then L  $\leftarrow$  I;
        end;
      end;
    end;
  Index  $\leftarrow$  L;
  end;
```

423. Perform the lexicographic ordering of (x_1, y_1) against (x_2, y_2) .

```
function CompareIntPairs(X1, Y1, X2, Y2 : Longint): integer;
  var lRes: integer;
  begin lRes  $\leftarrow$  CompareInt(X1, X2);
  if lRes = 0 then lRes  $\leftarrow$  CompareInt(Y1, Y2);
  CompareIntPairs  $\leftarrow$  lRes;
  end;
```

Section 10.10. STRING COLLECTION**424.**

```

⟨Public interface for mobjects.pas 309⟩ +≡
  { MStringCollection object }
  PStringCollection = ↑MStringCollection;
  MStringCollection = object (MSortedCollection)
    function Compare(Key1, Key2 : Pointer): integer; virtual;
    procedure FreeItem(Item : Pointer); virtual;
  end ;
  { UnsortedStringCollection }
  PUnsortedStringCollection = ↑StringColl;
  StringColl = object (MCollection)
    procedure FreeItem(Item : pointer); virtual;
  end ;

```

425. String ordering operator. We have the usual lexicograph ordering as an operator ordering.

```

⟨String collection implementation 425⟩ ≡
  { MStringCollection }
function CompareStr(aStr1, aStr2 : string): integer;
  begin if aStr1 < aStr2 then CompareStr ← -1
  else if aStr1 = aStr2 then CompareStr ← 0
  else CompareStr ← 1;
  end;

```

This code is used in section 308.

426. We then have a convenience function to handle pointer dereferencing.

```

function MStringCollection.Compare(Key1, Key2 : Pointer): integer;
  begin Compare ← CompareStr(PString(Key1)↑, PString(Key2)↑);
  end;

```

427. Freeing items. We can free an item by simply freeing the string. This is the same for unsorted string collections, too.

```

procedure MStringCollection.FreeItem(Item : Pointer);
  begin DisposeStr(Item);
  end;
{ UnsortedStringCollection }
procedure StringColl.FreeItem(Item : pointer);
  begin DisposeStr(Item);
  end;

```

Section 10.11. INT COLLECTIONS

428. The *TIntItem* is needed for the unifier and equalizer.

```

⟨ Public interface for mobjects.pas 309 ⟩ +≡
  { MIntCollection object }
  IntPair = record X, Y: integer;
  end;
  IntPairItemPtr = ↑IntPairItem;
  IntPairItem = object (MObject)
    fKey: IntPair;
    constructor Init(X, Y : integer);
  end ;
  IntPtr = ↑integer;
  PIntItem = ↑TIntItem;
  TIntItem = object (MObject)
    IntKey: integer;
    constructor Init(fInt : integer);
  end ;
  PIntKeyCollection = ↑TIntKeyCollection;
  TIntKeyCollection = object (MSortedCollection)
    function KeyOf(Item : pointer): pointer; virtual;
    function Compare(Key1, Key2 : pointer): integer; virtual;
  end ;
  IntPairKeyCollectionPtr = ↑IntPairKeyCollection;
  IntPairKeyCollection = object (MSortedCollection)
    function Compare(Key1, Key2 : pointer): integer; virtual;
    function ObjectOf(X, Y : integer): IntPairItemPtr; virtual;
    function FirstThat(X : integer): IntPairItemPtr; virtual;
  end ;

```

429. **TIntItem constructor.** This just copies the given integer over to the newly allocated *TIntItem* object.

```

⟨ MIntCollection implementation 429 ⟩ ≡
  { MIntCollection }
  constructor TIntItem.Init(fInt : integer);
  begin IntKey ← fInt;
  end;

```

This code is used in section 308.

430. We use *TIntItems* as keys in a *TIntKeyCollection*.

```

function TIntKeyCollection.KeyOf(Item : pointer): pointer;
begin KeyOf ← addr(PIntItem(Item)↑.IntKey);
end;

```

431. Comparing items just looks at the integers referred by the pointers.

```
function TIntKeyCollection.Compare(Key1, Key2 : pointer): integer;
  begin Compare  $\leftarrow$  1;
  if IntPtr(Key1) $\uparrow$  < IntPtr(Key2) $\uparrow$  then
    begin Compare  $\leftarrow$  -1; exit
    end;
  if IntPtr(Key1) $\uparrow$  = IntPtr(Key2) $\uparrow$  then Compare  $\leftarrow$  0;
end;
```

432. Constructor for pairs of integers.

```
constructor IntPairItem.Init(X, Y : integer);
  begin fKey.X  $\leftarrow$  X; fKey.Y  $\leftarrow$  Y;
  end;
```

433. Comparing two keys in a collection indexed by *IntPairs* is done “in the obvious way”.

```
function IntPairKeyCollection.Compare(Key1, Key2 : pointer): integer;
  begin Compare  $\leftarrow$  CompareIntPairs(IntPairItemPtr(Key1) $\uparrow$ .fKey.X, IntPairItemPtr(Key1) $\uparrow$ .fKey.Y,
    IntPairItemPtr(Key2) $\uparrow$ .fKey.X, IntPairItemPtr(Key2) $\uparrow$ .fKey.Y);
  end;
```

434. We can lookup the value associated to the key (*X*, *Y*) leveraging the *MSortedCollection.Search* function.

```
function IntPairKeyCollection.ObjectOf(X, Y : integer): IntPairItemPtr;
  var lPairItem: IntPairItem; I: integer;
  begin ObjectOf  $\leftarrow$  nil; lPairItem.Init(X, Y);
  if Search(addr(lPairItem), I) then ObjectOf  $\leftarrow$  Items $\uparrow$ [I];
  end;
```

435. This is used in *justhan.pas* and *mizprep.pas*.

```
function IntPairKeyCollection.FirstThat(X : integer): IntPairItemPtr;
  var I: integer;
  begin FirstThat  $\leftarrow$  nil;
  for i  $\leftarrow$  0 to Count - 1 do
    if IntPairItemPtr(Items $\uparrow$ [I]) $\uparrow$ .fKey.X = X then
      begin FirstThat  $\leftarrow$  Items $\uparrow$ [I]; exit
      end;
  end;
```

Section 10.12. STACKED LIST OF OBJECTS

436. “Stacked” lists are really linked lists.

```

⟨ Public interface for mobjects.pas 309 ⟩ +≡
  { Stacked Object (List of objects) }
  StackedPtr = ↑StackedObj;
  StackedObj = object (MObject)
    Previous: StackedPtr;
    constructor Init;
    destructor Done; virtual;
  end ;

```

437. The constructors and destructors are not implemented, so if you try to use them, just raise an error.

```

⟨ Stacked object implementation 437 ⟩ ≡
  { Stacked Object (List of objects) }
constructor StackedObj.Init;
  begin Abstract1;
  end;
destructor StackedObj.Done;
  begin Abstract1;
  end;

```

This code is used in section 308.

Section 10.13. STRING LIST

438.

```

⟨ Public interface for mobjects.pas 309 ⟩ +≡
  { MStringList object }
  MDuplicates = (dupIgnore, dupAccept, dupError);
  PStringItem = ↑MStringItem;
  MStringItem = record fString: PString;
    fObject: PObject;
  end;
  PStringItemList = ↑MStringItemList;
  MStringItemList = array [0 .. MaxListSize] of MStringItem;
  PStringList = ↑MStringList;
  MStringList = object (MObject)
    fList: PStringItemList;
    fCount: integer;
    fCapacity: integer;
    fSorted: boolean;
    fDuplicate: MDuplicates;
    constructor Init(aCapacity : integer);
    constructor MoveStringList(var aAnother : MStringList);
    { – Internal methods- do not use them directly – }
    procedure StringListError(Code, Info : integer); virtual;
    procedure Grow;
    procedure QuickSort(L, R : integer);
    procedure ExchangeItems(Index1, Index2 : integer);
    procedure InsertItem(aIndex : integer;
      const aStr: String); { – – }
    procedure SetSorted(aValue : boolean);
    procedure Sort; virtual;
    function GetString(aIndex : integer): String; virtual;
    function GetObject(aIndex : integer): PObject; virtual;
    procedure PutString(aIndex : integer;
      const aStr: String); virtual;
    procedure PutObject(aIndex : integer; aObject : PObject); virtual;
    procedure SetCapacity(aCapacity : integer); virtual;
    destructor Done; virtual;
    function AddString(const aStr: String): integer; virtual;
    function AddObject(const aStr: String;
      aObject: PObject): integer; virtual;
    procedure AddStrings(var aStrings : MStringList); virtual;
    procedure Clear; virtual;
    procedure Delete(aIndex : integer); virtual;
    procedure Exchange(Index1, Index2 : integer); virtual;
    procedure MoveObject(CurIndex, NewIndex : integer); virtual;
    function Find (
      const aStr: String;
      var aIndex: integer ) : boolean; virtual;
    function IndexOf(const aStr: String): integer; virtual;
    function ObjectOf(const aStr: String): PObject; virtual;
    function IndexOfObject(aObject : PObject): integer;
    procedure Insert(aIndex : integer;
      const aStr: String); virtual;
    procedure InsertObject(aIndex : integer;

```

```

    const aStr: String;
    aObject: PObject);
end ;

```

439. Constructors. We can construct an empty string collection using *Init*. We can also move the contents of *aAnother* string collection into the caller using *MoveStringList*.

```

⟨String list implementation 439⟩ ≡
    {————— MStringList —————}
constructor MStringList.Init(aCapacity : integer);
    begin MObject.Init; fList ← nil; fCount ← 0; fCapacity ← 0; fSorted ← false;
    fDuplicate ← dupError; SetCapacity(aCapacity);
    end;
constructor MStringList.MoveStringList(var aAnother : MStringList);
    begin MObject.Init; fCount ← aAnother.fCount; fCapacity ← aAnother.fCapacity;
    fSorted ← aAnother.fSorted; fList ← aAnother.fList; fDuplicate ← aAnother.fDuplicate;
    { Empty out the other list }
    aAnother.fCount ← 0; aAnother.fCapacity ← 0; aAnother.fList ← nil;
    end;

```

See also section 444.

This code is used in section 308.

440. Destructor. Since a *MStringItem* is a pointer to a string and a pointer to an *MObject*, freeing an *MStringItem* should free both of these (when they are present).

```

destructor MStringList.Done;
    var I: integer;
    begin inherited Done;
    for I ← 0 to fCount - 1 do
        with fList↑[I] do { free fList↑[I] }
            begin DisposeStr(fString);
            if fObject ≠ nil then Dispose(fObject, Done);
            end;
        fCount ← 0; SetCapacity(0);
    end;

```

441. Adding a string. This boils down to determining the position where we will insert the new string, then inserting the string into that location, and finally returning the index to the user.

```

function MStringList.AddString(const aStr: string): integer;
    var lResult: integer;
    begin ⟨Set lResult to the index of the newly inserted string 442⟩;
    InsertItem(lResult, aStr); AddString ← lResult;
    end;

```

442. Determining the index for the string boils down to whether the collection is sorted or not. If it is unsorted, then just append the string at the end of the collection.

For sorted collections, find the location for the string. We need to give particular care when adding the new string would create a duplicate entry in the string list.

```

⟨Set lResult to the index of the newly inserted string 442⟩ ≡
  if ¬fSorted then lResult ← fCount
  else if Find(aStr, lResult) then
    begin AddString ← lResult; ⟨De-duplicate a string list 443⟩;
    end

```

This code is used in section 441.

443. When we ignore duplicates (i.e., the *fDuplicate* flag is equal to *dupIgnore*), we can just terminate adding a string to the collection here.

But when we want to flag an error upon inserting a duplicate entry, then we should raise an error.

All other situations “fall through”.

```

⟨De-duplicate a string list 443⟩ ≡
  case fDuplicate of
    dupIgnore: Exit;
    dupError: StringListError(coDuplicate, 0);
  endcases

```

This code is used in section 442.

444. Inserting an object. We can treat a string list as a dictionary whose keys are strings. This is because the entries are string-(pointer to object) pairs.

```

⟨String list implementation 439⟩ +≡
function MStringList.AddObject(const aStr: string; aObject: PObject): integer;
  var lResult: integer;
  begin lResult ← AddString(aStr); { Insert key }
        PutObject(lResult, aObject); { Insert value }
        AddObject ← lResult; { Return index }
  end;

```

445. Appending a string list. We can add all the entries from another *MStringList* to the caller, which is what we do in the *AddStrings* function. It does not mutate *aStrings*.

```

procedure MStringList.AddStrings(var aStrings : MStringList);
  var I, r: integer;
  begin for I ← 0 to aStrings.fCount − 1 do
    r ← AddObject(aStrings.fList↑[I].fString↑, aStrings.fList↑[I].fObject);
  end;

```

446. Clear a string list. We can delete all the strings from a string list. This *will not* free the “values” in each key-value pair.

```

procedure MStringList.Clear;
  var I: integer;
  begin if fCount ≠ 0 then
    begin for I ← 0 to fCount − 1 do DisposeStr(fList↑[I].fString);
    fCount ← 0; SetCapacity(0);
    end;
  end;

```

447. Deleting an entry by index. When given an index which is within the bounds of the caller, we free the string located at that index, decrement the size, and then shift all entries after it down by one.

```

procedure MStringList.Delete(aIndex : integer);
  begin if (aIndex < 0)  $\vee$  (aIndex  $\geq$  fCount) then StringListError(coIndexError, aIndex);
    DisposeStr(fList↑[aIndex].fString); Dec(fCount);
  if aIndex < fCount then
    Move(fList↑[aIndex + 1], fList↑[aIndex], (fCount - aIndex) * SizeOf(MStringItem));
  end;

```

448. Exchanging items. We have *Exchange* check if the indices are within the bounds of the string list, then *ExchangeItems* swaps the items around.

```

procedure MStringList.Exchange(Index1, Index2 : integer);
  begin if (Index1 < 0)  $\vee$  (Index1  $\geq$  fCount) then StringListError(coIndexError, Index1);
  if (Index2 < 0)  $\vee$  (Index2  $\geq$  fCount) then StringListError(coIndexError, Index2);
    ExchangeItems(Index1, Index2);
  end;

procedure MStringList.ExchangeItems(Index1, Index2 : integer);
  var Temp: MStringItem;
  begin Temp  $\leftarrow$  fList↑[Index1]; fList↑[Index1]  $\leftarrow$  fList↑[Index2]; fList↑[Index2]  $\leftarrow$  Temp;
  end;

```

449. Find an entry by bisection search. We can use bisection search to find the needle in the haystack.

```

function MStringList.Find ( const aStr: string; var aIndex: integer ) : boolean;
  var L, H, I, C: integer; lResult: boolean;
  begin lResult  $\leftarrow$  False; L  $\leftarrow$  0; H  $\leftarrow$  fCount - 1;
  while L  $\leq$  H do
    begin I  $\leftarrow$  (L + H) shr 1; C  $\leftarrow$  CompareStr(fList↑[I].fString↑, aStr);
    if C < 0 then L  $\leftarrow$  I + 1
    else begin H  $\leftarrow$  I - 1;
      if C = 0 then
        begin lResult  $\leftarrow$  True;
          if fDuplicate  $\neq$  dupAccept then L  $\leftarrow$  I;
        end;
      end;
    end;
  end;
  aIndex  $\leftarrow$  L; Find  $\leftarrow$  lResult;
end;

```

450. Reporting errors. We can propagate errors, adjusting the error code as needed. The comment here is in Polish “poprawic bledy” (which Google translates to “correct the errors”)

```

procedure MStringList.StringListError(Code, Info : integer);
  begin RunError(212 - Code); {! poprawic bledy }
  end;

```

451. Getting the string at an index. When given an index within bounds, we try to get the string located there. If there is no string located at that entry, return the empty string.

```

function MStringList.GetString(aIndex : integer): string;
  begin if (aIndex < 0)  $\vee$  (aIndex  $\geq$  fCount) then StringListError(coIndexError, aIndex);
    GetString  $\leftarrow$  ``;
  if fList↑[aIndex].fString  $\neq$  nil then GetString  $\leftarrow$  fList↑[aIndex].fString↑;
  end;

```

452. Get object at index. We can get the object at an index, provided it is within bounds.

```
function MStringList.GetObject(aIndex : integer): PObject;
  begin if (aIndex < 0) ∨ (aIndex ≥ fCount) then StringListError(coIndexError, aIndex);
    GetObject ← fList↑[aIndex].fObject;
  end;
```

453. Ensure capacity for string lists. The growth rate for string lists differs from the earlier discussion on the growth rate for dynamic arrays. Well, actually, recalling our discussion (§323), we find this is identical to the previous growth rate. So I am not sure why this code is duplicated.

```
procedure MStringList.Grow;
  var Delta: integer;
  begin if fCapacity > 64 then Delta ← fCapacity div 4
    else if fCapacity > 8 then Delta ← 16
      else Delta ← 4;
    SetCapacity(fCapacity + Delta);
  end;
```

454. Index of a string. There are two branches to this function: one for unsorted string lists, the second for sorted string lists.

```
function MStringList.IndexOf(const aStr: string): integer;
  var lResult: integer;
  begin if ¬fSorted then
    begin for lResult ← 0 to fCount - 1 do
      if CompareStr(fList↑[lResult].fString↑, aStr) = 0 then
        begin IndexOf ← lResult; Exit; end;
      lResult ← lResult + 1;
    end
  else if ¬Find(aStr, lResult) then lResult ← -1;
  { Assert: lResult = -1 if aStr is not in the caller }
  IndexOf ← lResult;
end;
```

455. Value for a key. This appears to duplicate code from *GetObject* (§452).

```
function MStringList.ObjectOf(const aStr: string): PObject;
  var I: integer;
  begin ObjectOf ← nil; I ← IndexOf(aStr);
  if I ≥ 0 then ObjectOf ← fList↑[I].fObject;
  end;
```

456. Insert a string at an index. This seems to involve duplicate code as *AddString* (§441), but allows duplicate entries (which might violate the invariants of a string list).

```
procedure MStringList.Insert(aIndex : integer;
  const aStr: string);
  begin if fSorted then StringListError(coSortedListError, 0);
  if (aIndex < 0) ∨ (aIndex > fCount) then StringListError(coIndexError, aIndex);
  InsertItem(aIndex, aStr);
end;
```

457. Inserting an item at an index. We ensure the capacity of the string list. Then we shift the entries to the right by 1, if needed. We insert the string associated with no object. Then increment the logical size of the dynamic array.

```

procedure MStringList.InsertItem(aIndex : integer;
  const aStr: string);
  begin if fCount = fCapacity then Grow;
  { Shift existing entries to right by 1 }
  if aIndex < fCount then
    Move(fList↑[aIndex], fList↑[aIndex + 1], (fCount - aIndex) * SizeOf(MStringItem));
  with fList↑[aIndex] do
    begin fObject ← nil; fString ← NewStr(aStr); end;
  inc(fCount);
end;

```

458. Find the index for an object. Find the first instance of a key-value entry whose value is equal to the given object. If the given object is absent from the string list, return -1 .

```

function MStringList.IndexOfObject(aObject : PObject): integer;
  var lResult: integer;
  begin for lResult ← 0 to fCount - 1 do
    if GetObject(lResult) = aObject then
      begin IndexOfObject ← lResult; Exit; end;
  IndexOfObject ← -1;
end;

```

459. Inserting an object associated with a string.

```

procedure MStringList.InsertObject(aIndex : integer;
  const aStr: string;
  aObject: PObject);
  begin Insert(aIndex, aStr); PutObject(aIndex, aObject);
end;

```

460. Moving a key-value entry around. We can take the key-value entry at *CurIndex*, remove it from the string list, then insert it at *NewIndex*. It is important to note: the *NewIndex* is the index *after* the delete operation has occurred.

```

procedure MStringList.MoveObject(CurIndex, NewIndex : integer);
  var TempObject: PObject; TempString: string;
  begin if CurIndex ≠ NewIndex then
    begin TempString ← GetString(CurIndex); TempObject ← GetObject(CurIndex);
    Delete(CurIndex); InsertObject(NewIndex, TempString, TempObject);
    end;
  end;

```

461. Inserting a string at an index. Well, if this is a sorted collection, then raise an error: you can't insert strings willy-nilly!

Then check the index is within bounds, raise an error for out-of-bounds indices.

Then mutate the entry at *aIndex* to have its string be equal to *NewStr(aStr)*.

This will always mutate the caller, even when the string located at the entry indexed by *aIndex* is identical to *aStr*.

```

procedure MStringList.PutString(aIndex : integer;
    const aStr: string);
begin if fSorted then StringListError(coSortedListError, 0);
if (aIndex < 0)  $\vee$  (aIndex  $\geq$  fCount) then StringListError(coIndexError, aIndex);
fList↑[aIndex].fString  $\leftarrow$  NewStr(aStr);
end;

```

462. Inserting an object at an index. When given an index within bounds of the caller's underlying array, mutate its object to be the given *aObject*. Again, this *always* mutates the caller.

```

procedure MStringList.PutObject(aIndex : integer; aObject : PObject);
begin if (aIndex < 0)  $\vee$  (aIndex  $\geq$  fCount) then StringListError(coIndexError, aIndex);
fList↑[aIndex].fObject  $\leftarrow$  aObject;
end;

```

463. Quicksorting a string list. See also §386 and §532.

```

procedure MStringList.QuickSort(L, R : integer);
var I, J: integer; P: string;
begin repeat I  $\leftarrow$  L; J  $\leftarrow$  R; P  $\leftarrow$  fList↑[(L + R) shr 1].fString↑;
    repeat while CompareStr(fList↑[I].fString↑, P) < 0 do inc(I);
    while CompareStr(fList↑[J].fString↑, P) > 0 do Dec(J);
    if I  $\leq$  J then
        begin ExchangeItems(I, J); inc(I); Dec(J); end;
    until I > J;
    if L < J then QuickSort(L, J);
    L  $\leftarrow$  I;
until I  $\geq$  R;
end;

```

464. Changing the capacity of a string list. Of particular note here, changing the capacity of a string list *does not* delete anything. That work must be delegated elsewhere when *aCapacity* < *Self.fCapacity* (if that case ever occurs).

```

procedure MStringList.SetCapacity(aCapacity : integer);
var lList: PStringItemList;
begin if aCapacity < fCount then aCapacity  $\leftarrow$  fCount;
if aCapacity > MaxListSize then aCapacity  $\leftarrow$  MaxListSize;
if aCapacity  $\neq$  fCapacity then
    begin if aCapacity = 0 then lList  $\leftarrow$  nil
    else begin GetMem(lList, aCapacity * SizeOf(MStringItem));
        if (fCount  $\neq$  0)  $\wedge$  (fList  $\neq$  nil) then Move(fList↑, lList↑, fCount * SizeOf(MStringItem));
        end;
    if fCapacity  $\neq$  0 then FreeMem(fList, fCapacity * SizeOf(MStringItem));
    fList  $\leftarrow$  lList; fCapacity  $\leftarrow$  aCapacity;
    end; { ReallocMem(fList, NewCapacity * SizeOf(MStringItem)); fCapacity := NewCapacity; }
end;

```

465. Toggle ‘sorted’ flag. Allow the user to toggle the “sorted” flag. When toggled to *True*, be sure to sort the string list.

```

procedure MStringList.SetSorted(aValue : boolean);
  begin if fSorted  $\neq$  aValue then
    begin if aValue then Sort;
    fSorted  $\leftarrow$  aValue;
    end;
  end;

```

466. Sorting. This is a wrapper around the quicksort function (§463), invoked when the *fSorted* flag is false.

This appears to be used in the *SetSorted* procedure, but that is not used anywhere.

```

procedure MStringList.Sort;
  begin if  $\neg$ fSorted  $\wedge$  (fCount > 1) then
    begin fSorted  $\leftarrow$  true; QuickSort(0, fCount - 1);
    end;
  end;

```

467. Allocating a new string. Allocating a new *PString* from a string. When the empty string is given, return **nil**. Otherwise allocate a new block of memory in the Heap, then set its contents equal to *S*.

{ Dynamic string handling routines }

```

function NewStr(const S: String): PString;
  var P: PString;
  begin if S = '' then P  $\leftarrow$  nil
  else begin GetMem(P, length(S) + 1); P $\uparrow$   $\leftarrow$  S;
  end;
  NewStr  $\leftarrow$  P;
end;

```

468. Deleting a string. A convenience function to avoid accidentally freeing a **nil** string pointer.

```

procedure DisposeStr(P : PString);
  begin if P  $\neq$  nil then FreeMem(P, length(P $\uparrow$ ) + 1);
  end;

```


Section 10.14. TUPLES OF INTEGERS**469.**

```

⟨Public interface for mobjects.pas 309⟩ +≡
  { Partial integers Functions }
  IntTriplet = record X1, X2, Y: integer;
  end;
const MaxIntPairSize = MaxSize div SizeOf(IntPair);
  MaxIntTripletSize = MaxSize div SizeOf(IntTriplet);

```

470. Now, this is the remainder of the interface

```

⟨Public interface for mobjects.pas 309⟩ +≡
type IntPairListPtr = ↑IntPairList; IntPairList = array [0 .. MaxIntPairSize - 1] of IntPair;
  IntPairSeqPtr = ↑BinIntFunc; IntPairSeq = object (MObject)
    Items: IntPairListPtr;
    Count: integer;
    Limit: integer;
    constructor Init(aLimit : integer);
    procedure NatSetError(Code, Info : integer); virtual;
    destructor Done; virtual;
    procedure SetLimit(aLimit : integer); virtual;
    procedure Insert(const aItem: IntPair); virtual;
    procedure AtDelete(aIndex : integer);
    procedure DeleteAll;
    procedure AssignPair(X, Y : integer); virtual;
  end ;

```

471. First, we have a helper function for flagging errors.

```

⟨Tuples of integers 471⟩ ≡
  { Pairs of an integers }
procedure IntPairSeq.NatSetError(Code, Info : integer);
  begin RunError(212 - Code); end;

```

472. Constructor.

```

constructor IntPairSeq.Init(aLimit : integer);
  begin MObject.Init; Items ← nil; Count ← 0; Limit ← 0; SetLimit(aLimit);
  end;

```

473. Destructor.

```

destructor IntPairSeq.Done;
  begin Count ← 0; SetLimit(0);
  end;

```

474. Insert an element.

```

procedure IntPairSeq.Insert(const aItem: IntPair);
  begin if Count ≥ MaxIntPairSize then NatSetError(coOverflow, 0);
  if Limit = Count then SetLimit(Limit + GrowLimit(Limit));
  Items↑[Count] ← aItem; inc(Count);
  end;

```

475. Delete an element at an index.

```

procedure IntPairSeq.AtDelete(aIndex : integer);
  var i: integer;
  begin if (aIndex < 0)  $\vee$  (aIndex  $\geq$  Count) then
    begin NatSetError(coIndexError, 0); exit; end;
  if aIndex < Count - 1 then
    for i  $\leftarrow$  aIndex to Count - 2 do Items $\uparrow$ [i]  $\leftarrow$  Items $\uparrow$ [i + 1];
  Dec(Count);
  end;

```

476. Resizing an IntPair sequence.

```

procedure IntPairSeq.SetLimit(aLimit : integer);
  var aItems: IntPairListPtr;
  begin if aLimit < Count then aLimit  $\leftarrow$  Count;
  if aLimit > MaxIntPairSize then ALimit  $\leftarrow$  MaxIntPairSize;
  if aLimit  $\neq$  Limit then
    begin if ALimit = 0 then ALimit  $\leftarrow$  nil
    else begin GetMem(ALimit * SizeOf(IntPair));
      if (Count  $\neq$  0)  $\wedge$  (Items  $\neq$  nil) then Move(Items $\uparrow$ , aItems $\uparrow$ , Count * SizeOf(IntPair));
      end;
    if Limit  $\neq$  0 then FreeMem(Items, Limit * SizeOf(IntPair));
    Items  $\leftarrow$  aItems; Limit  $\leftarrow$  aLimit;
    end;
  end;

```

477. Deleting all entries. We just set the logical size to zero. It leaves everything else untouched.

```

procedure IntPairSeq.DeleteAll;
  begin Count  $\leftarrow$  0; end;

```

478. Append a pair of integers. We create a new *IntPair* using *X* and *Y*, then append it to the caller.

```

procedure IntPairSeq.AssignPair(X, Y : integer);
  var UntPair: IntPair;
  begin UntPair.X  $\leftarrow$  X; UntPair.Y  $\leftarrow$  Y; Insert(UntPair);
  end;

```

Section 10.15. INT REL

479. This is used in the `iocorrel.pas`, `identify.pas`, `equalizer.pas`, the analyzer, and a polynomial library.

```

⟨Public interface for mobjects.pas 309⟩ +≡
  IntRelPtr = ↑IntRel;
  IntRel = object (IntPairSeq)
    constructor Init(aLimit : integer);
    procedure Insert(const aItem: IntPair); virtual;
    procedure AtInsert(aIndex : integer;
      const aItem: IntPair); virtual;
    function Search(X, Y : integer; var aIndex : integer): boolean; virtual;
    function IndexOf(X, Y : integer): integer;
    constructor CopyIntRel(var aFunc : IntRel);
    function IsMember(X, Y : integer): boolean; virtual;
    procedure AssignPair(X, Y : integer); virtual;
  end ;

```

480. Constructor. This is just the inherited constructor.

```

⟨Int relation implementation 480⟩ ≡
{ IntRel }
constructor IntRel.Init(aLimit : integer);
  begin inherited Init(aLimit);
  end;

```

This code is used in section 308.

481. Inserting an entry.

```

procedure IntRel.Insert(const aItem: IntPair);
  var I: integer;
  begin if ¬Search(aItem.X, aItem.Y, I) then
    begin if (I < 0) ∨ (I > Count) then
      begin NatSetError(coIndexError, 0); exit; end;
    if Count ≥ MaxIntPairSize then NatSetError(coOverflow, 0);
      { Finished with the possible errors }
    if Limit = Count then SetLimit(Limit + GrowLimit(Limit));
    if I ≠ Count then Move(Items↑[I], Items↑[I + 1], (Count - I) * SizeOf(IntPair));
    Items↑[I] ← aItem; inc(Count);
  end;
end;

```

482. Insert at a specific index.

```

procedure IntRel.AtInsert(aIndex : integer;
  const aItem: IntPair);
  begin if (aIndex < 0)  $\vee$  (aIndex > Count) then NatSetError(coIndexError, aIndex);
  if Count = Limit then SetLimit(Limit + GrowLimit(Limit));
    { Shift everything to the right by 1 }
  if aIndex < Limit then Move(Items $\uparrow$ [aIndex], Items $\uparrow$ [aIndex + 1], (Count - aIndex) * SizeOf(IntPair));
    { Update the items, increment the logical size }
  Items $\uparrow$ [aIndex]  $\leftarrow$  aItem; inc(Count);
  end;

```

483. Bisection search for a relation. Search through *IntRel* for a relation $X = Y$. Note that this is not symmetric, i.e., if we have $Y = X$ in the *IntRel*, then it will not match.

Mutates the *aIndex*. If the relation is missing, *aIndex* will return where it *should* be.

```

function IntRel.Search(X, Y : integer; var aIndex : integer): boolean;
  var L, H, I, C: integer;
  begin Search  $\leftarrow$  False; L  $\leftarrow$  0; H  $\leftarrow$  Count - 1;
  while L  $\leq$  H do
    begin I  $\leftarrow$  (L + H) shr 1; C  $\leftarrow$  CompareIntPairs(Items $\uparrow$ [I].X, Items $\uparrow$ [I].Y, X, Y);
    if C < 0 then L  $\leftarrow$  I + 1
    else begin H  $\leftarrow$  I - 1;
      if C = 0 then
        begin Search  $\leftarrow$  True; L  $\leftarrow$  I; end;
      end;
    end;
  aIndex  $\leftarrow$  L;
  end;

```

484. Copy constructor. This moves the contents of *aFunc* into the caller. It will mutate the caller *but not* the argument supplied. The *Move* function copies the contents of one region of memory to another.

```

constructor IntRel.CopyIntRel(var aFunc : IntRel);
  begin Init(aFunc.Limit); Move(aFunc.Items $\uparrow$ , Items $\uparrow$ , aFunc.Limit * SizeOf(IntPair));
  Count  $\leftarrow$  aFunc.Count;
  end;

```

485. Index of a relation. This will return the index of the $X = Y$ entry. If it is absent from the caller, then return -1.

```

function IntRel.IndexOf(X, Y : integer): integer;
  var I: integer;
  begin IndexOf  $\leftarrow$  -1;
  if Search(X, Y, I) then IndexOf  $\leftarrow$  I;
  end;

```

486. Test for membership. This just tests if $X = Y$ is contained in the caller.

```

function IntRel.IsMember(X, Y : integer): boolean;
  var I: integer;
  begin IsMember  $\leftarrow$  Search(X, Y, I); end;

```

487.

```
procedure IntRel.AssignPair(X, Y : integer);  
  begin if IsMember(X, Y) then exit;  
    inherited AssignPair(X, Y);  
  end;
```

Section 10.16. PARTIAL INTEGERS FUNCTIONS

488.

⟨Public interface for `mobjects.pas` 309⟩ +≡

```

NatSetPtr = ↑NatSet;
NatSet = object (IntRel)
  Delta: integer;
  Duplicates: boolean;
  constructor Init(aLimit, aDelta : integer);
  constructor InitWithElement(X : integer);
  destructor Done; virtual;
  procedure Insert(const aItem: IntPair); virtual;
  function SearchPair(X : integer; var Index : integer): boolean; virtual;
  function ElemNr(X : integer): integer;
    { ***** }
  constructor CopyNatSet(const fFunc: NatSet);
  procedure InsertElem(X : integer); virtual;
  procedure DeleteElem(fElem : integer); virtual;
  procedure EnlargeBy(const fAnother: NatSet); { ? virtual? }

  procedure ComplementOf(const fAnother: NatSet);
  procedure IntersectWith(const fAnother: NatSet);
    { ***** }
  function HasInDom(fElem : integer): boolean; virtual;
  function IsEqualTo(const fFunc: NatSet): boolean;
  function IsSubsetOf(const fFunc: NatSet): boolean;
  function IsSupersetOf(const fFunc: NatSet): boolean;
  function Misses(const fFunc: NatSet): boolean;
  constructor MoveNatSet(var fFunc : NatSet);
end ;

```

489. **Constructor.** The empty *NatSet* can be constructed with the usual initialization.

⟨Partial integer function implementation 489⟩ ≡

```

{ Partial integers Functions }
constructor NatSet.Init(aLimit, aDelta : integer);
  begin MObject.Init; Items ← nil; Count ← 0; Limit ← 0; Delta ← ADelta; SetLimit(ALimit);
  Duplicates ← False;
end;

```

This code is used in section 308.

490. **Singleton constructor.** This initializes the *Delta* set to 4, and the *aLimit* set to 0. Then insert the given integer.

```

constructor NatSet.InitWithElement(X : integer);
  begin Init(0, 4); InsertElem(X);
end;

```

491. **Destructor.** This delegates the heavy work to *SetLimit*(0).

```

destructor NatSet.Done;
  begin Count ← 0; SetLimit(0);
end;

```

492. Inserting a pair of integers. Using *Search* to find where to insert $X = Y$, possibly growing the underlying array if needed.

```

procedure NatSet.Insert(const aItem: IntPair);
  var I: integer;
  begin if  $\neg \text{SearchPair}(aItem.X, I) \vee \text{Duplicates}$  then
    begin if  $(I < 0) \vee (I > \text{Count})$  then { Out of bounds, raise an error }
      begin NatSetError(coIndexError, 0); exit; end;
    if Limit = Count then { Grow the capacity, if possible }
      begin if Delta = 0 then
        begin NatSetError(coOverflow, 0); exit; end;
        SetLimit(Limit + Delta);
      end;
    if  $I \neq \text{Count}$  then Move(Items $\uparrow$ [I], Items $\uparrow$ [I + 1], (Count - I) * SizeOf(IntPair));
    Items $\uparrow$ [I]  $\leftarrow$  aItem; inc(Count);
  end;
end;

```

493. Equality of IntPair objects. This just tests the componentwise equality of two *IntPair* objects.

```

function Equals(Key1, Key2 : IntPair): boolean;
  begin Equals  $\leftarrow$  (Key1.X = Key2.X)  $\wedge$  (Key1.Y = Key2.Y);
  end;

```

494. Search. This is a bisection search for any relation of the form $X = Y$ for some Y .

```

function NatSet.SearchPair(X : integer; var Index : integer): boolean;
  var L, H, I, C: integer;
  begin SearchPair  $\leftarrow$  False; L  $\leftarrow$  0; H  $\leftarrow$  Count - 1;
  while  $L \leq H$  do
    begin I  $\leftarrow$  (L + H) shr 1; C  $\leftarrow$  CompareInt(Items $\uparrow$ [I].X, X);
    if  $C < 0$  then L  $\leftarrow$  I + 1
    else begin H  $\leftarrow$  I - 1;
      if  $C = 0$  then
        begin SearchPair  $\leftarrow$  True;
        if  $\neg \text{Duplicates}$  then L  $\leftarrow$  I;
        end;
      end;
    end;
  end;
  Index  $\leftarrow$  L;
end;

```

495. Copy constructor. We can copy the contents of another *NatSet* into the caller. This mutates the caller, but leaves the given *NatSet* unchanged.

```

constructor NatSet.CopyNatSet(const fFunc: NatSet);
  begin Init(fFunc.Limit, fFunc.Delta); Move(fFunc.Items $\uparrow$ , Items $\uparrow$ , fFunc.Limit * SizeOf(IntPair));
  Count  $\leftarrow$  fFunc.Count;
  end;

```

496. Move constructor. We can also *move* the contents of another *NatSet* into the caller. This will mutate the other *NatSet* to have **nil** items and 0 capacity.

```

constructor NatSet.MoveNatSet(var fFunc : NatSet);
  begin Init(fFunc.Limit, fFunc.Delta); Self  $\leftarrow$  fFunc; fFunc.DeleteAll; fFunc.Limit  $\leftarrow$  0;
  fFunc.Items  $\leftarrow$  nil;
end;

```

497. Union operation. We can merge another *NatSet* into the caller.

```

procedure NatSet.EnlargeBy(const fAnother : NatSet);
  var I : integer;
  begin for I  $\leftarrow$  0 to fAnother.Count - 1 do InsertElem(fAnother.Items $\uparrow$ [i].X);
end;

```

498. Set complement. We can destructively remove from the caller all elements appearing in *fAnother* nat set.

```

procedure NatSet.ComplementOf(const fAnother : NatSet);
  var I : integer;
  begin for I  $\leftarrow$  0 to fAnother.Count - 1 do DeleteElem(fAnother.Items $\uparrow$ [i].X);
end;

```

499. Take intersection. This computes $Self \leftarrow Self \cap Other$

```

procedure NatSet.IntersectWith(const fAnother : NatSet);
  var k : integer;
  begin k  $\leftarrow$  0;
  while k < Count do
    if  $\neg fAnother.HasInDom(Items\uparrow[k].X)$  then AtDelete(k)
    else inc(k);
  end;

```

500. Insert an element. We can insert $X = 0$ into the caller.

```

procedure NatSet.InsertElem(X : integer);
  var UntPair : IntPair;
  begin UntPair.X  $\leftarrow$  X; UntPair.Y  $\leftarrow$  0; Insert(UntPair);
end;

```

501. Deleting an element. Similarly, we can delete the first element of the form $X = Y$ for some Y .

```

procedure NatSet.DeleteElem(fElem : integer);
  var I : integer;
  begin if SearchPair(fElem, I) then AtDelete(I);
end;

```

502. We can test if an element X is in the domain of the caller.

```

function NatSet.HasInDom(fElem : integer): boolean;
  var I : integer;
  begin HasInDom  $\leftarrow$  SearchPair(fElem, I);
end;

```


503. Set equality predicate. This assumes that there are no duplicate entries in a *NatSet* data structure.

```
function NatSet.IsEqualTo(const fFunc: NatSet): boolean;
  var I: integer;
  begin IsEqualTo ← false;
  if Count ≠ fFunc.Count then exit;
  for I ← 0 to Count - 1 do
    if ¬Equals(Items↑[I], fFunc.Items↑[I]) then exit;
  IsEqualTo ← true;
end;
```

504. Subset predicate. The comment is Polish for (according to Google translate): “If we’re checking if a small function is contained within a large one, commenting it out might be better.” There is a commented out function which I removed.

```
function NatSet.IsSubsetOf(const fFunc: NatSet): boolean;
  var i, j, k, c: integer; { Jezeli sprawdzamy, czy mala funkcja jest zawarta w duzej, to to wykomentowane
                             moze byc lepsze }
  begin IsSubsetOf ← false; c ← fFunc.Count;
  if c < Count then exit;
  j ← 0;
  for i ← 0 to Count - 1 do
    begin k ← Items↑[i].X;
    while (j < c) ∧ (fFunc.Items↑[j].X < k) do inc(j);
    if (j = c) ∨ ¬Equals(fFunc.Items↑[j], Items↑[i]) then exit;
    end;
  IsSubsetOf ← true;
end;
```

505. Superset predicate. This just takes advantage of the fact that $Y \supseteq X$ is the same as $X \subseteq Y$, then use the subset predicate.

```
function NatSet.IsSupersetOf(const fFunc: NatSet): boolean;
  begin IsSupersetOf ← fFunc.IsSubsetOf(Self);
end;
```

506. Test if two sets are disjoint. This iterates over the smaller of the two sets, checking if every element in the smaller set *does not* appear in the larger set.

```
function NatSet.Misses(const fFunc: NatSet): boolean;
  var I, k: integer;
  begin if Count > fFunc.Count then
    begin for k ← 0 to fFunc.Count - 1 do
      if SearchPair(fFunc.Items↑[k].X, I) then
        begin Misses ← false; exit end
      end
    else begin for k ← 0 to Count - 1 do
      if fFunc.SearchPair(Items↑[k].X, I) then
        begin Misses ← false; exit end;
      end;
    Misses ← true;
  end;
```

507. Index for an element. This searches for the index associated with relations of the form $X = Y$. If any such relation appears, return its index. Otherwise, return -1 .

It leaves the caller unmodified, so it is a pure function.

```
function NatSet.ElemNr( $X : integer$ ): integer;
  var  $I : integer$ ;
  begin  $ElemNr \leftarrow -1$ ;
  if SearchPair( $X, I$ ) then  $ElemNr \leftarrow I$ ;
  end;
```

Section 10.17. FUNCTION OF NATURAL NUMBERS

508. The *NatFunc* is used in the analyzer, equalizer, unifier, and elsewhere. Its destructor is the only place where $nConsistent \leftarrow false$.

⟨ Public interface for `mobjects.pas` 309 ⟩ \equiv

```

NatFuncPtr = ↑NatFunc;
NatFunc = object (NatSet)
  nConsistent: boolean;
  constructor InitNatFunc(ALimit, ADelta : integer);
  constructor CopyNatFunc(const fFunc: NatFunc);
  constructor MoveNatFunc(var fFunc : NatFunc);
  constructor LCM(const aFunc1, aFunc2: NatFunc);
  procedure Assign(X, Y : integer); virtual;
  procedure Up(X : integer); virtual;
  procedure Down(X : integer); virtual;
  function Value(fElem : integer): integer; virtual;
  procedure Join(const fFunc: NatFunc);
  destructor Refuted; virtual;
  procedure EnlargeBy(fAnother : NatFuncPtr); { ? virtual; }

  function JoinAtom(fLatAtom : NatFuncPtr): NatFuncPtr;
  function CompareWith(const fNatFunc: NatFunc): integer;
  function WeakerThan(const fNatFunc: NatFunc): boolean;
  function IsMultipleOf(const fNatFunc: NatFunc): boolean;
  procedure Add(const aFunc: NatFunc);
  function CountAll: integer; virtual;
end ;

```

509. Constructors. We have the basic constructors for an empty *NatFunc*, a copy constructor, and a move constructor. The move constructor is destructive on the supplied argument.

⟨ *NatFunc* implementation 509 ⟩ \equiv

```

constructor NatFunc.InitNatFunc(ALimit, ADelta : integer);
  begin inherited Init(ALimit, ADelta); nConsistent ← true;
  end;

constructor NatFunc.CopyNatFunc(const fFunc: NatFunc);
  begin Init(fFunc.Limit, fFunc.Delta); Move(fFunc.Items↑, Items↑, fFunc.Limit * SizeOf(IntPair));
  Count ← fFunc.Count; nConsistent ← fFunc.nConsistent;
  end;

constructor NatFunc.MoveNatFunc(var fFunc : NatFunc);
  begin Init(fFunc.Limit, fFunc.Delta); Self ← fFunc; fFunc.DeleteAll; fFunc.Limit ← 0;
  fFunc.Items ← nil;
  end;

```

See also section 525.

This code is used in section 308.

510. Constructor (LCM). The least common multiple between two *NatFunc* objects is another way to construct a *NatFunc* instance. This seems to be the LCM in the sense of commutative rings (if x and y are elements of a commutative ring R , then $\text{lcm}(x, y)$ is such that x divides $\text{lcm}(x, y)$ and y divides $\text{lcm}(x, y)$ — moreover, $\text{lcm}(x, y)$ is the smallest such quantity, in the sense that $\text{lcm}(x, y)$ divides any other such quantity).

For the ring (or ringoid) $\mathbf{N}^{\mathbf{N}}$, this amounts to

$$\text{lcm}(f, g) = \{ (x, y) \mid \exists y_1, y_2, (x, y_1) \in f, (x, y_2) \in g, y = \text{lcm}(y_1, y_2) \},$$

with the condition that when $y_1 = 0$, $y = y_2$ (and similarly $y_2 = 0$ implies $y = y_1$).

```

constructor NatFunc.LCM (const aFunc1, aFunc2: NatFunc);
  var i, j, m: integer;
  begin m  $\leftarrow$  aFunc2.Delta;
  if aFunc1.Delta > m then m  $\leftarrow$  aFunc1.Delta;
  InitNatFunc(aFunc1.Limit + aFunc2.Limit, m); i  $\leftarrow$  0; j  $\leftarrow$  0;
  while (i < aFunc1.Count)  $\wedge$  (j < aFunc2.Count) do
    case CompareInt(aFunc1.Items $\uparrow$ [i].X, aFunc2.Items $\uparrow$ [j].X) of
      -1: begin Insert(aFunc1.Items $\uparrow$ [i]); inc(i) end;
    0: begin { m = max(f(i), g(i) }
      m  $\leftarrow$  aFunc1.Items $\uparrow$ [i].Y;
      if aFunc2.Items $\uparrow$ [j].Y > m then m  $\leftarrow$  aFunc2.Items $\uparrow$ [j].Y;
      Assign(aFunc1.Items $\uparrow$ [i].X, m); { destructively set f(i)  $\leftarrow$  m }
      inc(i); inc(j);
    end;
    1: begin Insert(aFunc2.Items $\uparrow$ [j]); inc(j) end;
  endcases;
  if i  $\geq$  aFunc1.Count then
    for j  $\leftarrow$  j to aFunc2.Count - 1 do Insert(aFunc2.Items $\uparrow$ [j])
  else for i  $\leftarrow$  i to aFunc1.Count - 1 do Insert(aFunc1.Items $\uparrow$ [i]);
  end;

```

511. Extend a natural function. We can extend a natural function to assign a value y to a place where it is not yet defined $x \notin \text{dom}(f)$.

We should recall *HasInDom* (§502) which depends on *SearchPair* (§494) is relevant. When trying to assign a different value y to an already defined $f(x) \neq y$, then we have refuted something.

```

procedure NatFunc.Assign(X, Y: integer);
  var UntPair: IntPair;
  begin if nConsistent then
    begin if HasInDom(X)  $\wedge$  (Value(X)  $\neq$  Y) then
      begin Refuted; exit end;
    UntPair.X  $\leftarrow$  X; UntPair.Y  $\leftarrow$  Y; Insert(UntPair);
    end;
  end;

```

512. Increment $f(x)$. Given a *NatFunc* object f , and an integer x , $f.Up(x)$ will

- (1) If $x \in \text{dom}(f)$, then update the value $f(x) \geq f(x) + 1$
- (2) Otherwise, $x \notin \text{dom}(f)$, so this corresponds to $f(x) = 0$, then we mutate $f(x) \leftarrow 1$.

```

procedure NatFunc.Up( $X : \text{integer}$ );
  var  $I : \text{integer}$ ;  $\text{IntPair} : \text{IntPair}$ ;
  begin if  $n\text{Consistent}$  then
    begin if  $\text{SearchPair}(X, I)$  then  $\text{inc}(\text{Items}\uparrow[I].Y)$ 
    else begin  $\text{IntPair}.X \leftarrow X$ ;  $\text{IntPair}.Y \leftarrow 1$ ;  $\text{Insert}(\text{IntPair})$ ;
      end;
    end;
  end;

```

513. Decrement $f(x)$. Given a *NatFunc* object f , and an integer x , $f.Down(x)$ will

- (1) If $x \in \text{dom}(f)$, then update the value $f(x) \geq f(x) - 1$ and if this is then zero, remove it from the function.
- (2) Otherwise, $x \notin \text{dom}(f)$, so this corresponds to $f(x) = 0$, and we cannot mutate $f(x) \leftarrow -1$ without making it no longer natural-valued. So we raise an error.

```

procedure NatFunc.Down( $X : \text{integer}$ );
  var  $I : \text{integer}$ ;
  begin if  $n\text{Consistent}$  then
    begin if  $\text{SearchPair}(X, I)$  then
      begin  $\text{dec}(\text{Items}\uparrow[I].Y)$ ;
        if  $\text{Items}\uparrow[I].Y = 0$  then  $\text{AtDelete}(I)$ ;
        end
      else  $\text{NatSetError}(\text{coConsistentError}, 0)$ ;
      end;
    end;
  end;

```

514. Getting the value of $f(x)$ when $x \in \text{dom}(f)$. When $x \notin \text{dom}(f)$, raise an error.

```

function NatFunc.Value( $f\text{Elem} : \text{integer}$ ):  $\text{integer}$ ;
  var  $I : \text{integer}$ ;
  begin if  $\text{SearchPair}(f\text{Elem}, I)$  then  $\text{Value} \leftarrow \text{Items}\uparrow[I].Y$ 
  else  $\text{NatSetError}(\text{coDuplicate}, 0)$ ;
  end;

```

515. Destructor. We usually try to extend partial functions on \mathbf{N} , but if we end up trying to extend where it is already defined to a different value, then we arrive at an inconsistent extension. It is referred to as a “refuted” situation.

```

destructor NatFunc.Refuted;
  begin  $\text{inherited Done}$ ;  $n\text{Consistent} \leftarrow \text{false}$ 
  end;

```

516. Join. For two partial functions $f: \mathbf{N} \rightarrow \mathbf{N}$ and $g: \mathbf{N} \rightarrow \mathbf{N}$, we form $f \cup g$ provided

$$f \cap g = f|_{\text{dom}(f \cap g)} = g|_{\text{dom}(f \cap g)}.$$

That is to say, for all $x \in \text{dom}(f) \cap \text{dom}(g)$, we have $f(x) = g(x)$.

The comment is in Polish, which Google translates as: “It seems that the *Join* and *EnlargeBy* procedures below do the same thing. *EnlargeBy* should be faster for small collections. If not, it’s not worth the code waste and can be discarded. On the other hand, these procedures are primarily intended for (very) small collections.”

Also worth observing, this tests for consistency in the other *NatFunc*.

```
{ Wyglada na to, ze ponizej podane procedury "Join" i "EnlargeBy" robia to samo, "EnlargeBy"
  powinna byc szybsza dla malych kolekcji. Jezeli tak nie jest nie warto tracic kodu i mozna ja
  wyrzucic. Z drugiej strony procedury te maja byc glownie stosowane do (bardzo) malych kolekcji. }
procedure NatFunc.Join(const fFunc: NatFunc);
var I, k: integer;
begin if nConsistent then
  begin if ¬fFunc.nConsistent then
    begin Refuted; exit end;
  for k ← 0 to fFunc.Count − 1 do
    if SearchPair(fFunc.Items↑[k].X, I) then
      begin if ¬Equals(Items↑[I], fFunc.Items↑[k]) then
        begin Refuted; exit end;
      end
    else Insert(fFunc.Items↑[k]);
  end;
end;
```

517. This function performs the same task as the previous one (i.e., it merges another partial function into the caller, provided it is consistent on overlap).

```
procedure NatFunc.EnlargeBy(fAnother : NatFuncPtr); { ? virtual;? }
var i, j, lCount, lLimit: integer; lItems: IntPairListPtr;
begin if nConsistent then
  begin if ¬fAnother↑.nConsistent then
    begin Refuted; exit end;
  if fAnother↑.Count = 0 then exit;
  lCount ← Count; lItems ← Items; lLimit ← Limit; Limit ← 0; Count ← 0;
  SetLimit(lCount + fAnother↑.Count); i ← 0; j ← 0;
  while (i < lCount) ∧ (j < fAnother↑.Count) do
    case CompareInt(lItems↑[i].X, fAnother↑.Items↑[j].X) of
      −1: begin Insert(lItems↑[i]); inc(i) end;
      0: begin if Equals(lItems↑[i], fAnother↑.Items↑[j]) then Insert(lItems↑[i])
        else begin Refuted; FreeMem(lItems, lLimit * SizeOf(IntPair)); exit end;
        inc(i); inc(j);
      end;
      1: begin Insert(fAnother↑.Items↑[j]); inc(j) end;
    endcases;
  if i ≥ lCount then
    for j ← j to fAnother↑.Count − 1 do Insert(fAnother↑.Items↑[j])
  else for i ← i to lCount − 1 do Insert(lItems↑[i]);
  SetLimit(0); FreeMem(lItems, lLimit * SizeOf(IntPair));
  end;
end;
```

518. We want to join two partial functions $f: \mathbf{N} \rightarrow \mathbf{N}$ and $g: \mathbf{N} \rightarrow \mathbf{N}$ without accidentally mutating either f or g to be refuted. To do this, we copy the caller, then enlarge it with the other partial function. If the result is consistent, then return it. Otherwise, return **nil**.

This leaves both the caller and $fLatAtom$ unchanged, so it's a pure function.

```
function NatFunc.JoinAtom(fLatAtom : NatFuncPtr): NatFuncPtr;
var lEval: NatFunc;
begin JoinAtom  $\leftarrow$  nil; lEval.CopyNatFunc(Self); lEval.EnlargeBy(fLatAtom);
if lEval.nConsistent then JoinAtom  $\leftarrow$  NatFuncPtr(lEval.CopyObject);
end;
```

519. Comparing partial functions. Given two partial functions, $f: \mathbf{N} \rightarrow \mathbf{N}$ and $g: \mathbf{N} \rightarrow \mathbf{N}$, we want to compare them. We first start with comparing $\|f\|$ against $\|g\|$. If they are not equal, then this is the result.

When $\|f\| = \|g\|$, iterate through each $x \in \text{dom}(f)$, and then compare $f(x)$ against $g(x)$. If $f(x) < g(x)$, then return -1 . If $f(x) > g(x)$, then return $+1$. Otherwise keep iterating until we have examined all of $\text{dom}(f)$, and then we return 0 .

```
function CompareNatFunc(aKey1, aKey2 : Pointer): integer;
var i, lnt: integer;
begin with NatFuncPtr(aKey1) $\uparrow$  do
  begin lnt  $\leftarrow$  CompareInt(Count, NatFuncPtr(aKey2) $\uparrow$ .Count);
  if lnt  $\neq$   $0$  then
    begin CompareNatFunc  $\leftarrow$  lnt; exit end;
  for i  $\leftarrow$   $0$  to Count  $- 1$  do
    begin lnt  $\leftarrow$  CompareInt(Items $\uparrow$ [i].X, NatFuncPtr(aKey2) $\uparrow$ .Items $\uparrow$ [i].X);
    if lnt  $\neq$   $0$  then
      begin CompareNatFunc  $\leftarrow$  lnt; exit end;
      lnt  $\leftarrow$  CompareInt(Items $\uparrow$ [i].Y, NatFuncPtr(aKey2) $\uparrow$ .Items $\uparrow$ [i].Y);
      if lnt  $\neq$   $0$  then
        begin CompareNatFunc  $\leftarrow$  lnt; exit end;
      end;
    end;
  CompareNatFunc  $\leftarrow$   $0$ ;
end;
```

520. Let $f: \mathbf{N} \rightarrow \mathbf{N}$ and $g: \mathbf{N} \rightarrow \mathbf{N}$ be partial functions. We say that f is “weaker” than g when $\|f\| \leq \|g\|$ and for each $x \in \text{dom}(f)$ we have $f(x) = g(x)$. If there is some $x \in \text{dom}(f)$ such that $x \notin \text{dom}(g)$, then f is not weaker than g .

If there is some $x \in \text{dom}(f)$ such that $x \in \text{dom}(g)$ and $f(x) \neq g(x)$, then f is not weaker than g .

```
function NatFunc.WeakerThan(const fNatFunc: NatFunc): boolean;
var i, k: integer;
begin WeakerThan  $\leftarrow$  false;
if Count  $\leq$  fNatFunc.Count then
  begin for k  $\leftarrow$   $0$  to Count  $- 1$  do
    begin i  $\leftarrow$  Items $\uparrow$ [k].X;
    if  $\neg$ fNatFunc.HasInDom(i) then exit;
    if Items $\uparrow$ [k].Y  $\neq$  fNatFunc.Value(i) then exit;
    end;
  WeakerThan  $\leftarrow$  true;
end;
end;
```

521. Let $f: \mathbf{N} \rightarrow \mathbf{N}$ and $g: \mathbf{N} \rightarrow \mathbf{N}$ be partial functions. We will say that f is a “multiple” of g if $\|g\| \leq \|f\|$ and for each $x \in \text{dom}(g)$ we have $x \in \text{dom}(f)$ and $g(x) \leq f(x)$.

There was some commented code for this function, which I removed.

```
function NatFunc.IsMultipleOf(const fNatFunc: NatFunc): boolean;
var k, l: integer;
begin IsMultipleOf  $\leftarrow$  false;
if fNatFunc.Count  $\leq$  Count then
  begin for k  $\leftarrow$  0 to fNatFunc.Count - 1 do
    if  $\neg$ HasInDom(fNatFunc.Items $\uparrow$ [k].X) then exit
    else if Value(fNatFunc.Items $\uparrow$ [k].X) < fNatFunc.Items $\uparrow$ [k].Y then exit;
    IsMultipleOf  $\leftarrow$  true;
  end;
end;
```

522. Comparing partial functions. Let $f: \mathbf{N} \rightarrow \mathbf{N}$ and $g: \mathbf{N} \rightarrow \mathbf{N}$ be partial functions.

If $\|f\| \leq \|g\|$, for each $x \in \text{dom}(f)$ if $x \notin \text{dom}(g)$, then return 0. If $f(x) \neq g(x)$, then return 0. Otherwise return -1.

Else if $\|g\| \leq \|f\|$, for each $x \in \text{dom}(g)$ if $x \notin \text{dom}(f)$, then return 0. If $f(x) \neq g(x)$, then return 0. Otherwise return +1.

This is difficult for me to grasp. It does not seem to adequately satisfy $\text{compare}(f, g) = -\text{compare}(g, f)$, which is catastrophic. It is also unclear to me that this is transitive or reflexive. So it seems like it has no desirable properties.

I am confused why there is this function and also another similarly named function (§519).

The comment in Polish translates as, “Using *WeakerThan* you can shorten *CompareWith*!!!” At least, according to Google, that’s the translation.

{ Uzywajac *WeakerThan* mozna skrociac *CompareWith* !!! }

```
function NatFunc.CompareWith(const fNatFunc: NatFunc): integer;
var i, k: integer;
begin CompareWith  $\leftarrow$  0;
if Count  $\leq$  fNatFunc.Count then
  begin for k  $\leftarrow$  0 to Count - 1 do
    begin i  $\leftarrow$  Items $\uparrow$ [k].X;
    if  $\neg$ fNatFunc.HasInDom(i) then exit;
    if Items $\uparrow$ [k].Y  $\neq$  fNatFunc.Value(i) then exit;
    end;
    CompareWith  $\leftarrow$  -1; exit;
  end;
if fNatFunc.Count  $\leq$  Count then
  begin for k  $\leftarrow$  0 to fNatFunc.Count - 1 do
    begin i  $\leftarrow$  fNatFunc.Items $\uparrow$ [k].X;
    if  $\neg$ HasInDom(i) then exit;
    if fNatFunc.Items $\uparrow$ [k].Y  $\neq$  Value(i) then exit;
    end;
    CompareWith  $\leftarrow$  1; exit;
  end;
end;
```


523. Let $f: \mathbf{N} \rightarrow \mathbf{N}$ and $g: \mathbf{N} \rightarrow \mathbf{N}$ be partial functions. Then we define $f + g: \mathbf{N} \rightarrow \mathbf{N}$ to be the partial function defined on $\text{dom}(f + g) = \text{dom}(f) \cup \text{dom}(g)$ such that for each $x \in \text{dom}(f \cap g)$ we have $(f + g)(x) = f(x) + g(x)$, and for each $x \in \text{dom}(f) \setminus \text{dom}(g)$ we have $(f + g)(x) = f(x)$, and for each $x \in \text{dom}(g) \setminus \text{dom}(f)$ we have $(f + g)(x) = g(x)$.

There is some subtlety in the implementation because we have to check for overflows, i.e., when

$$g(x) \geq \text{High}(\text{integer}) - f(x)$$

for each $x \in \text{dom}(f) \cap \text{dom}(g)$.

```

procedure NatFunc.Add(const aFunc: NatFunc);
  var k, l: integer;
  begin l  $\leftarrow$  0;
  for k  $\leftarrow$  0 to aFunc.Count - 1 do
    begin while (l < Count)  $\wedge$  (Items $\uparrow$ [l].X < aFunc.Items $\uparrow$ [k].X) do inc(l);
    if (l < Count)  $\wedge$  (Items $\uparrow$ [l].X = aFunc.Items $\uparrow$ [k].X) then
      begin if  $\langle$  Has overflow occurred in NatFunc.Add? 524  $\rangle$  then RunError(215);
      inc(Items $\uparrow$ [l].Y, aFunc.Items $\uparrow$ [k].Y);
      end
    else AtInsert(l, aFunc.Items $\uparrow$ [k]);
    end;
  end;

```

524. An overflow occurs if $f(x) + g(x)$ is greater than $\text{High}(\text{integer})$ (the maximum value for an integer).

\langle Has overflow occurred in *NatFunc.Add*? 524 $\rangle \equiv$
 $\text{Items}\uparrow[l].Y > (\text{High}(\text{integer}) - \text{aFunc.Items}\uparrow[k].Y)$

This code is used in section 523.

525. Sum values of partial function. For a partial function $f: \mathbf{N} \rightarrow \mathbf{N}$, we have

$$\text{CountAll}(f) = \sum_{n \in \text{dom}(f)} f(n).$$

\langle *NatFunc* implementation 509 $\rangle + \equiv$

```

function NatFunc.CountAll: integer;
  var k, l: integer;
  begin l  $\leftarrow$  0;
  for k  $\leftarrow$  0 to Count - 1 do inc(l, Items $\uparrow$ [k].Y);
  CountAll  $\leftarrow$  l;
  end;

```

Section 10.18. SEQUENCES OF NATURAL NUMBERS**526.**

⟨Public interface for `mobjects.pas` 309⟩ \equiv

```

NatSeq = object (NatFunc)
  constructor InitNatSeq(ALimit, ADelta : integer);
  procedure InsertElem(X : integer); virtual;
  function Value(fElem : integer): integer; virtual;
  function IndexOf(Y : integer): integer;
end ;

```

527. Constructor.

⟨NatSeq implementation 527⟩ \equiv

```

constructor NatSeq.InitNatSeq(ALimit, ADelta : integer);
begin inherited Init(ALimit, ADelta); nConsistent ← true;
end;

```

This code is used in section 308.

528. If we have a finite sequence (a_0, \dots, a_{n-1}) , then inserting an element x into it will yield the finite sequence (a_0, \dots, a_{n-1}, x) .

```

procedure NatSeq.InsertElem(X : integer);
var lPair: IntPair;
begin lPair.X ← Count; lPair.Y ← X; inherited Insert(lPair);
end;

```

529. The value for the k^{th} element in a sequence (a_0, \dots, a_{n-1}) is a_k when $0 \leq k < n$, and we take it to be 0 otherwise.

```

function NatSeq.Value(fElem : integer): integer;
begin
  if { (0 ≤ ind) and }
    (fElem < count) then Value ← Items↑[fElem].Y
  else Value ← 0;
end ;

```

530. The index for a_i in the sequence (a_0, \dots, a_{n-1}) is i when a_i is in the sequence. Otherwise, we return -1 .

```

function NatSeq.IndexOf(Y : integer): integer;
var lResult: integer;
begin for lResult ← Count - 1 downto 0 do
  if Items↑[lResult].Y = Y then
    begin IndexOf ← lResult; exit
  end;
IndexOf ← -1;
end;

```

Section 10.19. INTEGER SEQUENCES

531.

```

⟨Public interface for mobjects.pas 309⟩ +≡
  IntegerListPtr = ↑IntegerList;
  IntegerList = array [0 .. MaxIntegerListSize - 1] of integer;
  PIntSequence = ↑IntSequence;
  IntSequencePtr = PIntSequence;
  IntSequence = object (MObject)
    fList: IntegerListPtr;
    fCount: integer;
    fCapacity: integer;
    constructor Init(aCapacity : integer);
    constructor CopySequence(const aSeq: IntSequence);
    constructor MoveSequence(var aSeq : IntSequence);
    destructor Done; virtual;
    procedure IntListError(Code, Info : integer); virtual;
    procedure SetCapacity(aCapacity : integer); virtual;
    procedure Clear; virtual;
    function Insert(aInt : integer): integer; virtual;
    procedure AddSequence(const aSeq: IntSequence); virtual;
    function IndexOf(aInt : integer): integer; virtual;
    procedure AtDelete(aIndex : integer); virtual;
    function Value(aIndex : integer): integer; virtual;
    procedure AtInsert(aIndex, aInt : integer); virtual;
    procedure AtPut(aIndex, aInt : integer); virtual;
  end ;

```

532. We will need to quicksort lists of integers. This will mutate the *aList* argument, making it sorted. See also §386 and §463.

This procedure does not appear to be used anywhere in Mizar.

```

⟨IntSequence implementation 532⟩ ≡
  { integer Sequences & Sets }
procedure IntQuickSort(aList : IntegerListPtr; L, R : integer);
var I, J, P, lTemp: integer;
begin repeat I ← L; J ← R; P ← aList↑[(L + R) shr 1];
  repeat while CompareInt(aList↑[I], P) < 0 do inc(I);
    while CompareInt(aList↑[J], P) > 0 do Dec(J);
    if I ≤ J then
      begin lTemp ← aList↑[I]; aList↑[I] ← aList↑[J]; aList↑[J] ← lTemp; inc(I); Dec(J);
      end;
    until I > J;
    if L < J then IntQuickSort(aList, L, J);
    L ← I;
  until I ≥ R;
end;

```

This code is used in section 308.

533. Constructor. We can create an empty sequence of integers, with a given capacity.

```
constructor IntSequence.Init(aCapacity : integer);
  begin inheritedInit; fList  $\leftarrow$  nil; fCount  $\leftarrow$  0; fCapacity  $\leftarrow$  0; SetCapacity(aCapacity);
end;
```

534. Copy constructor. We can copy an existing sequence.

```
constructor IntSequence.CopySequence(const aSeq : IntSequence);
  begin Init(aSeq.fCapacity); AddSequence(aSeq);
end;
```

535. Move constructor. We can create a new array in heap, and move all the elements from a given sequence over, then free up the given sequence.

```
constructor IntSequence.MoveSequence(var aSeq : IntSequence);
  begin inheritedInit; fCount  $\leftarrow$  aSeq.fCount; fCapacity  $\leftarrow$  aSeq.fCapacity; fList  $\leftarrow$  aSeq.fList;
  aSeq.fCount  $\leftarrow$  0; aSeq.fCapacity  $\leftarrow$  0; aSeq.fList  $\leftarrow$  nil;
end;
```

536. Destructor.

```
destructor IntSequence.Done;
  begin inheritedDone; fCount  $\leftarrow$  0; SetCapacity(0);
end;
```

537. Appending an element. Given a finite sequence of integers (a_0, \dots, a_{n-1}) , we can append a value x to produce the finite sequence (a_0, \dots, a_{n-1}, x) . This will mutate the caller.

```
function IntSequence.Insert(aInt : integer) : integer;
  begin if fCount = fCapacity then SetCapacity(fCapacity + GrowLimit(fCapacity));
  fList $\uparrow$ [fCount]  $\leftarrow$  aInt; Insert  $\leftarrow$  fCount; inc(fCount);
end;
```

538. Appending a sequence. This takes a finite sequence (a_0, \dots, a_{n-1}) and another finite sequence (b_0, \dots, b_{m-1}) , then forms a new finite sequence $(a_0, \dots, a_{n-1}, b_0, \dots, b_{m-1})$. It mutates the caller.

```
procedure IntSequence.AddSequence(const aSeq : IntSequence);
  var I, r : integer;
  begin for I  $\leftarrow$  0 to aSeq.fCount - 1 do r  $\leftarrow$  Insert(aSeq.fList $\uparrow$ [I]);
end;
```

539. Clearing a sequence.

```
procedure IntSequence.Clear;
  begin if fCount  $\neq$  0 then
    begin fCount  $\leftarrow$  0; SetCapacity(0);
    end;
  end;
```

540. Delete entry in sequence. Removing the i^{th} entry in the sequence $(a_0, \dots, a_{i-1}, a_i, a_{i+1}, \dots, a_{n-1})$ yields the finite sequence $(a_0, \dots, a_{i-1}, a_{i+1}, \dots, a_{n-1})$. If $i < 0$ or $n - 1 < i$, then we raise an error.

```
procedure IntSequence.AtDelete(aIndex : integer);
  begin if (aIndex < 0)  $\vee$  (aIndex  $\geq$  fCount) then IntListError(coIndexError, aIndex);
  Dec(fCount);
  if aIndex < fCount then Move(fList $\uparrow$ [aIndex + 1], fList $\uparrow$ [aIndex], (fCount - aIndex) * SizeOf(integer));
end;
```

541. We report errors using this helper function.

```
procedure IntSequence.IntListError(Code, Info : integer);
  begin RunError(212 - Code);  {! poprawic bledy }
  end;
```

542. Let (a_0, \dots, a_{n-1}) be a finite sequence. The value at index i is a_i when $0 \leq i \leq n-1$, otherwise it raises an error.

```
function IntSequence.Value(aIndex : integer): integer;
  begin if (aIndex < 0)  $\vee$  (aIndex  $\geq$  fCount) then IntListError(coIndexError, aIndex);
  Value  $\leftarrow$  fList $\uparrow$ [aIndex];
  end;
```

543. For a finite sequence (a_0, \dots, a_{n-1}) and a value x , if there is some entry $a_i = x$ with $a_j \neq x$ for $j < i$, then return i . Otherwise return -1 .

```
function IntSequence.IndexOf(aInt : integer): integer;
  var lResult: integer;
  begin for lResult  $\leftarrow$  fCount - 1 downto 0 do
    if fList $\uparrow$ [lResult] = aInt then
      begin IndexOf  $\leftarrow$  lResult; exit
      end;
  IndexOf  $\leftarrow$  -1;
  end;
```

544. Given a finite sequence (a_0, \dots, a_{n-1}) , an index i , and a value x :

- (1) If $i < 0$ or i is too big, raise an error.
- (2) If the logical size of the sequence equals its capacity, then grow the underlying array.
- (3) If i is less than the logical size $i < n-1$, then shift all the entries to the right by 1 so we have $(a_0, \dots, a_{i-1}, 0, a_i, \dots, a_{n-1})$
- (4) Set the i^{th} entry to x , so we end up with the caller becoming $(a_0, \dots, a_{i-1}, x, a_i, \dots, a_{n-1})$.

```
procedure IntSequence.AtInsert(aIndex, aInt : integer);
  begin if (aIndex < 0)  $\vee$  (aIndex > fCount) then IntListError(coIndexError, aIndex);
  if fCount = fCapacity then SetCapacity(fCapacity + GrowLimit(fCapacity));
  if aIndex < fCount then Move(fList $\uparrow$ [aIndex], fList $\uparrow$ [aIndex + 1], (fCount - aIndex) * SizeOf(integer));
  fList $\uparrow$ [aIndex]  $\leftarrow$  aInt; inc(fCount);
  end;
```

545. Update entry of sequence. For a sequence (a_0, \dots, a_{n-1}) , an index i , and a new value x , if $0 \leq i \leq n-1$ then we set $a_i \leftarrow x$. Otherwise we have the index be out of bounds ($0 < i$ or $n-1 < i$), and we should raise an error.

```
procedure IntSequence.AtPut(aIndex, aInt : integer);
  begin if (aIndex < 0)  $\vee$  (aIndex  $\geq$  fCount) then IntListError(coIndexError, aIndex);
  fList $\uparrow$ [aIndex]  $\leftarrow$  aInt;
  end;
```

546. Grow the underlying array. When we want to increase (or decrease) the capacity of the underlying array, we invoke this function. It will copy over the relevant contents.

```

procedure IntSequence.SetCapacity(aCapacity : integer);
  var lList: IntegerListPtr;
  begin if aCapacity < fCount then aCapacity  $\leftarrow$  fCount;
  if aCapacity > MaxListSize then aCapacity  $\leftarrow$  MaxListSize;
  if aCapacity  $\neq$  fCapacity then
    begin if aCapacity = 0 then lList  $\leftarrow$  nil
    else begin GetMem(lList, aCapacity * SizeOf(integer));
      if (fCount  $\neq$  0)  $\wedge$  (fList  $\neq$  nil) then Move(fList $\uparrow$ , lList $\uparrow$ , fCount * SizeOf(integer));
      end;
    if fCapacity  $\neq$  0 then FreeMem(fList, fCapacity * SizeOf(integer));
    fList  $\leftarrow$  lList; fCapacity  $\leftarrow$  aCapacity;
    end;
  end;

```

Section 10.20. INTEGER SETS

547.

```

⟨Public interface for mobjects.pas 309⟩ +≡
  PIntSet = ↑IntSet;
  IntSetPtr = pIntSet;
  IntSet = object (IntSequence)
    function Insert(aInt : integer): integer; virtual;
    function DeleteInt(aInt : integer): integer; virtual;
    function Find(aInt : integer; var aIndex : integer): boolean; virtual;
    function IndexOf(aInt : integer): integer; virtual;
    procedure AtInsert(aIndex, aInt : integer); virtual;
    function IsInSet(aInt : integer): boolean; virtual;
    function IsEqualTo(const aSet: IntSet): boolean; virtual;
    function IsSubsetOf(const aSet: IntSet): boolean; virtual;
    function IsSupersetOf(var aSet : IntSet): boolean; virtual;
    function Misses(var aSet : IntSet): boolean; virtual;
  end ;

```

548. When inserting an element x into a set A , we check if $x \in A$ is already a member. If so, then we're done.

Otherwise, we ensure the capacity of the set can handle adding another element. Then we shift all elements greater than x over to the right by 1. We finally insert x into the underlying array.

```

⟨IntSet Implementation 548⟩ ≡
function IntSet.Insert(aInt : integer): integer;
  var lIndex: integer;
  begin if Find(aInt, lIndex) then { already contains the element? }
    begin Insert ← lIndex; exit end;
  if fCount = fCapacity then SetCapacity(fCapacity + GrowLimit(fCapacity));
  if lIndex < fCount then Move(fList↑[lIndex], fList↑[lIndex + 1], (fCount - lIndex) * SizeOf(integer));
  fList↑[lIndex] ← aInt; inc(fCount); Insert ← lIndex;
  end;

```

This code is used in section 308.

549. Removing an element from a set. This will return the former index of the element in the underlying array.

```

function IntSet.DeleteInt(aInt : integer): integer;
  var lIndex: integer;
  begin DeleteInt ← -1;
  if Find(aInt, lIndex) then
    begin DeleteInt ← lIndex; AtDelete(lIndex) end
  end;

```

550. We can use bisection search to find an element $aInt$ in the underlying array. It will mutate $aIndex$ to be where the entry should be, and return *true* if the element is a member of the set (and *false* otherwise).

```
function IntSet.Find(aInt : integer; var aIndex : integer): boolean;
  var L, H, I, C: integer;
  begin Find  $\leftarrow$  False; L  $\leftarrow$  0; H  $\leftarrow$  fCount - 1;
  while L  $\leq$  H do
    begin I  $\leftarrow$  (L + H) shr 1; C  $\leftarrow$  CompareInt(fList $\uparrow$ [I], aInt);
    if C < 0 then L  $\leftarrow$  I + 1
    else begin H  $\leftarrow$  I - 1;
      if C = 0 then
        begin Find  $\leftarrow$  True; L  $\leftarrow$  I; end;
      end;
    end;
  aIndex  $\leftarrow$  L;
end;
```

551. We can find the index of an element (if it is present) by using bisection search.

```
function IntSet.IndexOf(aInt : integer): integer;
  var lResult: integer;
  begin if  $\neg$ Find(aInt, lResult) then lResult  $\leftarrow$  -1;
  IndexOf  $\leftarrow$  lResult;
end;
```

552. The *AtInsert* method is “grandfathered in”, but not supported, so we raise an error if anyone tries using it.

```
procedure IntSet.AtInsert(aIndex, aInt : integer);
  begin IntListError(coSortedListError, 0);
end;
```

553. We can test if an integer is an element of the set, again just piggy-backing off bisection search.

```
function IntSet.IsInSet(aInt : integer): boolean;
  var I: integer;
  begin IsInSet  $\leftarrow$  Find(aInt, I);
end;
```

554. Testing if two finite sets A and B of integers are equal requires $|A| = |B|$ and for each $x \in A$ we have $x \in B$. If these conditions are not both met, then $A \neq B$.

```
function IntSet.IsEqualTo(const aSet: IntSet): boolean;
  var I: integer;
  begin IsEqualTo  $\leftarrow$  false;
  if fCount  $\neq$  aSet.fCount then exit;
  for I  $\leftarrow$  0 to fCount - 1 do
    if fList $\uparrow$ [I]  $\neq$  aSet.fList $\uparrow$ [I] then exit;
  IsEqualTo  $\leftarrow$  true;
end;
```


555. Subset predicate. We can test $A \subseteq B$ by $|A| \leq |B|$ and for each $a \in A$ we have $a \in B$.

```
function IntSet.IsSubsetOf(const aSet: IntSet): boolean;
  var i, j, lnt: integer;
  begin IsSubsetOf ← false;
  if aSet.fCount < fCount then exit;
  j ← 0; { index of B }
  for i ← 0 to fCount - 1 do { loop over a ∈ A }
    begin lnt ← fList↑[i];
    while (j < aSet.fCount) ∧ (aSet.fList↑[j] < lnt) do inc(j);
    if (j = aSet.fCount) ∨ (aSet.fList↑[j] ≠ fList↑[i]) then exit;
    end;
  IsSubsetOf ← true;
end;
```

556. Superset predicate. We have $A \supset B$ if $B \subseteq A$.

```
function IntSet.IsSupersetOf(var aSet: IntSet): boolean;
  begin IsSupersetOf ← aSet.IsSubsetOf(Self);
end;
```

557. Test for disjointness. We have $A \cap B = \emptyset$ if every $a \in A$ is such that $a \notin B$.

```
function IntSet.Misses(var aSet: IntSet): boolean;
  var k: integer;
  begin if fCount > aSet.fCount then
    begin for k ← 0 to aSet.fCount - 1 do
      if IsInSet(aSet.fList↑[k]) then
        begin Misses ← false; exit end
      end
    else begin for k ← 0 to fCount - 1 do
      if aSet.IsInSet(fList↑[k]) then
        begin Misses ← false; exit end;
      end;
    Misses ← true;
  end;
```

Section 10.21. PARTIAL BINARY INTEGER FUNCTIONS

558. We want to describe partial functions like $f: \mathbf{Z} \times \mathbf{Z} \rightarrow \mathbf{Z}$. These are encoded as finite sets of triples $\{(x, y, f(x, y)) \in \mathbf{Z} \times \mathbf{Z} \times \mathbf{Z}\}$. So we need to introduce triples of integers.

```

⟨Public interface for mobjects.pas 309⟩ +≡
  IntTripletListPtr = ↑IntTripletList;
  IntTripletList = array [0 .. MaxIntTripletSize - 1] of IntTriplet;
  BinIntFuncPtr = ↑BinIntFunc;
  BinIntFunc = object (MObject)
    fList: IntTripletListPtr;
    fCount: integer;
    fCapacity: integer;
    constructor Init(aLimit : integer);
    procedure BinIntFuncError(aCode, aInfo : integer); virtual;
    destructor Done; virtual;

    procedure Insert(const aItem: IntTriplet); virtual;
    procedure AtDelete(aIndex : integer);
    procedure SetCapacity(aLimit : integer); virtual;
    procedure DeleteAll;
    function Search(X1, X2 : integer; var aIndex : integer): boolean; virtual;
    function IndexOf(X1, X2 : integer): integer;
    constructor CopyBinIntFunc(var aFunc : BinIntFunc);
    function HasInDom(X1, X2 : integer): boolean; virtual;
    procedure Assign(X1, X2, Y : integer); virtual;
    procedure Up(X1, X2 : integer); virtual;
    procedure Down(X1, X2 : integer); virtual;
    function Value(X1, X2 : integer): integer; virtual;
    procedure Add(const aFunc: BinIntFunc); virtual;
    function CountAll: integer; virtual;
  end ;

```

559. We have a convenience function for reporting errors.

```

⟨Partial Binary integer Functions 559⟩ ≡
procedure BinIntFunc.BinIntFuncError(aCode, aInfo : integer);
  begin RunError(212 - aCode); end;

```

This code is used in section 308.

560. Constructor. We initialize the empty partial function.

```

constructor BinIntFunc.Init(aLimit : integer);
  begin MObject.Init; fList ← nil; fCount ← 0; fCapacity ← 0; SetCapacity(aLimit);
  end;

```

561. Destructor.

```

destructor BinIntFunc.Done;
  begin fCount ← 0; SetCapacity(0);
  end;

```

562. If we have a partial function $f: \mathbf{Z} \times \mathbf{Z} \rightarrow \mathbf{Z}$ and a triple (x, y, z) , then check if $(x, y) \in \text{dom}(f)$. If so, we're done.

Otherwise we add $f(x, y) = z$ to the partial function.

```

procedure BinIntFunc.Insert(const aItem: IntTriplet);
  var I: integer;
  begin if  $\neg \text{Search}(aItem.X1, aItem.X2, I)$  then
    begin if  $(I < 0) \vee (I > fCount)$  then
      begin BinIntFuncError(coIndexError, 0); exit; end;
    if  $fCapacity = fCount$  then SetCapacity( $fCapacity + \text{GrowLimit}(fCapacity)$ );
    if  $I \neq fCount$  then Move( $fList \uparrow [I], fList \uparrow [I + 1], (fCount - I) * \text{SizeOf}(\text{IntTriplet})$ );
     $fList \uparrow [I] \leftarrow aItem$ ; inc( $fCount$ );
    end;
  end;

```

563. Given $f: \mathbf{Z} \times \mathbf{Z} \rightarrow \mathbf{Z}$, we represent it as an array of $\mathbf{Z} \times \mathbf{Z} \times \mathbf{Z}$. So we can remove the entry at index i when $0 \leq i < \|f\|$. Otherwise when $i < 0$ or $\|f\| \leq i$, raise an error.

```

procedure BinIntFunc.AtDelete(aIndex : integer);
  var i: integer;
  begin if  $(aIndex < 0) \vee (aIndex \geq fCount)$  then
    begin BinIntFuncError(coIndexError, 0); exit; end;
  if  $aIndex < fCount - 1$  then
    for  $i \leftarrow aIndex$  to  $fCount - 2$  do  $fList \uparrow [i] \leftarrow fList \uparrow [i + 1]$ ;
  Dec( $fCount$ );
  end;

```

564. Ensure capacity.

```

procedure BinIntFunc.SetCapacity(aLimit : integer);
  var aItems: IntTripletListPtr;
  begin if  $aLimit < fCount$  then  $aLimit \leftarrow fCount$ ;
  if  $aLimit > \text{MaxIntTripletSize}$  then  $ALimit \leftarrow \text{MaxIntTripletSize}$ ;
  if  $aLimit \neq fCapacity$  then
    begin if  $ALimit = 0$  then  $AItems \leftarrow \text{nil}$ 
    else begin GetMem( $AItems, ALimit * \text{SizeOf}(\text{IntTriplet})$ );
      if  $(fCount \neq 0) \wedge (fList \neq \text{nil})$  then Move( $fList \uparrow, aItems \uparrow, fCount * \text{SizeOf}(\text{IntTriplet})$ );
    end;
    if  $fCapacity \neq 0$  then FreeMem( $fList, fCapacity * \text{SizeOf}(\text{IntTriplet})$ );
     $fList \leftarrow aItems$ ;  $fCapacity \leftarrow aLimit$ ;
    end;
  end;

```

565. Deleting all entries in a partial function $\mathbf{Z} \times \mathbf{Z} \rightarrow \mathbf{Z}$ amounts to setting the logical size of the underlying dynamic array to zero.

```

procedure BinIntFunc.DeleteAll;
  begin  $fCount \leftarrow 0$ ; end;

```

566. We can use bisection search to find an entry (x_1, x_2) such that $(x_1, x_2) \in \text{dom}(f)$.

```
function BinIntFunc.Search(X1, X2 : integer; var aIndex : integer): boolean;
  var L, H, I, C: integer;
  begin Search  $\leftarrow$  False; L  $\leftarrow$  0; H  $\leftarrow$  fCount - 1;
  while L  $\leq$  H do
    begin I  $\leftarrow$  (L + H) shr 1; C  $\leftarrow$  CompareIntPairs(fList↑[I].X1, fList↑[I].X2, X1, X2);
    if C < 0 then L  $\leftarrow$  I + 1
    else begin H  $\leftarrow$  I - 1;
      if C = 0 then
        begin Search  $\leftarrow$  True; L  $\leftarrow$  I; end;
      end;
    end;
  aIndex  $\leftarrow$  L;
end;
```

567. Copy constructor. This leaves *aFunc* unchanged, and clones *aFunc*.

```
constructor BinIntFunc.CopyBinIntFunc(var aFunc : BinIntFunc);
  begin Init(aFunc.fCapacity); Move(aFunc.fList↑, fList↑, aFunc.fCapacity * SizeOf(IntTriplet));
  fCount  $\leftarrow$  aFunc.fCount;
end;
```

568. Given $f: \mathbf{Z} \times \mathbf{Z} \rightarrow \mathbf{Z}$ and (x_1, x_2) , find the index for the underlying dynamic array i such that it contains $(x_1, x_2, f(x_1, x_2))$. If there is no such entry, $i = -1$ is returned.

```
function BinIntFunc.IndexOf(X1, X2 : integer): integer;
  var I: integer;
  begin IndexOf  $\leftarrow$  -1;
  if Search(X1, X2, I) then IndexOf  $\leftarrow$  I;
end;
```

569. Test if $(x_1, x_2) \in \text{dom}(f)$.

```
function BinIntFunc.HasInDom(X1, X2 : integer): boolean;
  var I: integer;
  begin HasInDom  $\leftarrow$  Search(X1, X2, I);
end;
```

570. Given $f: \mathbf{Z} \times \mathbf{Z} \rightarrow \mathbf{Z}$, and $(x_1, x_2) \in \mathbf{Z} \times \mathbf{Z}$ and $y \in \mathbf{Z}$, try setting $f(x_1, x_2) = y$ provided $(x_1, x_2) \notin \text{dom}(f)$ or if $(x_1, x_2, y) \in f$ already. If $f(x_1, x_2) \neq y$ already exists, then raise an error.

```
procedure BinIntFunc.Assign(X1, X2, Y : integer);
  var lntTriplet: IntTriplet;
  begin if HasInDom(X1, X2)  $\wedge$  (Value(X1, X2)  $\neq$  Y) then
    begin BinIntFuncError(coDuplicate, 0); exit
    end;
  lntTriplet.X1  $\leftarrow$  X1; lntTriplet.X2  $\leftarrow$  X2; lntTriplet.Y  $\leftarrow$  Y; Insert(lntTriplet);
end;
```

571. Given $f: \mathbf{Z} \times \mathbf{Z} \rightarrow \mathbf{Z}$ and $(x_1, x_2) \in \mathbf{Z} \times \mathbf{Z}$. If $(x_1, x_2) \in \text{dom}(f)$, then set $f(x_1, x_2) \leftarrow f(x_1, x_2) + 1$. Otherwise set $f(x_1, x_2) \leftarrow 1$.

```

procedure BinIntFunc.Up( $X1, X2$  : integer);
  var  $I$ : integer;  $lntTriplet$ : lntTriplet;
  begin if Search( $X1, X2, I$ ) then inc( $fList \uparrow [I].Y$ )
  else begin  $lntTriplet.X1 \leftarrow X1$ ;  $lntTriplet.X2 \leftarrow X2$ ;  $lntTriplet.Y \leftarrow 1$ ; Insert( $lntTriplet$ );
    end;
  end;

```

572. Given $f: \mathbf{Z} \times \mathbf{Z} \rightarrow \mathbf{Z}$ and $(x_1, x_2) \in \mathbf{Z} \times \mathbf{Z}$. If $(x_1, x_2) \in \text{dom}(f)$, then set $f(x_1, x_2) \leftarrow f(x_1, x_2) - 1$. Further, if $f(x_1, x_2) = 0$, then remove it from the underlying dynamic array.

Otherwise for $(x_1, x_2) \notin \text{dom}(f)$, raise an error.

```

procedure BinIntFunc.Down( $X1, X2$  : integer);
  var  $I$ : integer;
  begin if Search( $X1, X2, I$ ) then
    begin dec( $fList \uparrow [I].Y$ );
    if  $fList \uparrow [I].Y = 0$  then AtDelete( $I$ );
    end
  else BinIntFuncError(coConsistentError, 0);
  end;

```

573. Given $f: \mathbf{Z} \times \mathbf{Z} \rightarrow \mathbf{Z}$, and $(x_1, x_2) \in \mathbf{Z} \times \mathbf{Z}$, if $(x_1, x_2) \notin \text{dom}(f)$ then raise an error. Otherwise when $(x_1, x_2) \in \text{dom}(f)$, return $f(x_1, x_2)$.

```

function BinIntFunc.Value( $X1, X2$  : integer): integer;
  var  $I$ : integer;
  begin if Search( $X1, X2, I$ ) then Value  $\leftarrow fList \uparrow [I].Y$ 
  else BinIntFuncError(coDuplicate, 0);
  end;

```

574. Given two partial functions $f, g: \mathbf{Z} \times \mathbf{Z} \rightarrow \mathbf{Z}$, compute $f + g: \mathbf{Z} \times \mathbf{Z} \rightarrow \mathbf{Z}$. This is defines by:

- (1) For $(x_1, x_2) \in \text{dom}(f) \cap \text{dom}(g)$, set $(f + g)(x_1, x_2) = f(x_1, x_2) + g(x_1, x_2)$
- (2) For $(x_1, x_2) \in \text{dom}(f) \setminus \text{dom}(g)$, set $(f + g)(x_1, x_2) = f(x_1, x_2)$
- (3) For $(x_1, x_2) \in \text{dom}(g) \setminus \text{dom}(f)$, set $(f + g)(x_1, x_2) = g(x_1, x_2)$.

{ **TODO**: this is inefficient, since the search is repeated in the *Assign* method; fix this both here and in other similar methods }

```

procedure BinIntFunc.Add(const  $aFunc$ : BinIntFunc);
  var  $k, l$ : integer;
  begin for  $k \leftarrow 0$  to  $aFunc.fCount - 1$  do
    if Search( $aFunc.fList \uparrow [k].X1, aFunc.fList \uparrow [k].X2, l$ ) then inc( $fList \uparrow [l].Y, aFunc.fList \uparrow [k].Y$ )
    else Assign( $aFunc.fList \uparrow [k].X1, aFunc.fList \uparrow [k].X2, aFunc.fList \uparrow [k].Y$ );
  end;

```

575. Sum. For $f: \mathbf{Z} \times \mathbf{Z} \rightarrow \mathbf{Z}$, we compute

$$\text{CountAll}(f) = \sum_{(m,n) \in \text{dom}(f)} f(m, n).$$

```

function BinIntFunc.CountAll: integer;
  var  $k, l$ : integer;
  begin  $l \leftarrow 0$ ;
  for  $k \leftarrow 0$  to  $fCount - 1$  do inc( $l, fList \uparrow [k].Y$ );
  CountAll  $\leftarrow l$ ;
  end;

```

Section 10.22. PARTIAL INTEGERS TO PAIR OF INTEGERS FUNCTIONS**576.**

```

⟨Public interface for mobjects.pas 309⟩ +≡
  Int2PairOfInt = record X, Y1, Y2: integer;
    end;
  Int2PairOfIntFuncPtr = ↑Int2PairOfIntFunc;
  Int2PairOfIntFunc = object (MObject)
    fList: array of Int2PairOfInt;
    fCount: integer;
    fCapacity: integer;
    constructor Init(aLimit : integer);
    procedure Int2PairOfIntFuncError(aCode, aInfo : integer); virtual;
    destructor Done; virtual;
    procedure Insert(const aItem: Int2PairOfInt); virtual;
    procedure AtDelete(aIndex : integer);
    procedure SetCapacity(aLimit : integer); virtual;
    procedure DeleteAll;
    function Search(X : integer; var aIndex : integer): boolean; virtual;
    function IndexOf(X : integer): integer;
    constructor CopyInt2PairOfIntFunc(var aFunc : Int2PairOfIntFunc);
    function HasInDom(X : integer): boolean; virtual;
    procedure Assign(X, Y1, Y2 : integer); virtual;
    function Value(X : integer): IntPair; virtual;
  end ;

```

577. We have a helper function for raising errors.

```

⟨Partial integers to Pair of integers Functions 577⟩ ≡
  { Partial integers to Pair of integers Functions }
procedure Int2PairOfIntFunc.Int2PairOfIntFuncError(aCode, aInfo : integer);
  begin RunError(212 - aCode);
  end;

```

This code is used in section 308.

578. Constructor. Creates an empty $f: \mathbf{Z} \rightarrow \mathbf{Z} \times \mathbf{Z}$ with an underlying dynamic array whose capacity is given as the argument *aLimit*.

```

constructor Int2PairOfIntFunc.Init(aLimit : integer);
  begin MObject.Init; fList ← nil; fCount ← 0; fCapacity ← 0; SetCapacity(aLimit);
  end;

```

579. Destructor.

```

destructor Int2PairOfIntFunc.Done;
  begin fCount ← 0; SetCapacity(0);
  end;

```

580. Inserting (x, y_1, y_2) into $f: \mathbf{Z} \rightarrow \mathbf{Z} \times \mathbf{Z}$ amounts to checking if $(x, y_1, y_2) \in f$. If not, then insert the entry.

Otherwise, if $(x, y_1, y_2) \notin f$ but $x \in \text{dom}(f)$, then raise an error.

Otherwise do nothing.

```
procedure Int2PairOfIntFunc.Insert(const aItem: Int2PairOfInt);
  var I: integer;
  begin if  $\neg \text{Search}(aItem.X, I)$  then
    begin if  $(I < 0) \vee (I > fCount)$  then
      begin Int2PairOfIntFuncError(coIndexError, 0); exit; end;
    if  $fCapacity = fCount$  then SetCapacity( $fCapacity + \text{GrowLimit}(fCapacity)$ );
    if  $I \neq fCount$  then Move( $fList[I], fList[I + 1], (fCount - I) * \text{SizeOf}(Int2PairOfInt)$ );
     $fList[I] \leftarrow aItem$ ; inc( $fCount$ );
    end
  else if  $(fList[I].Y1 \neq aItem.Y1) \vee (fList[I].Y2 \neq aItem.Y2)$  then
    begin Int2PairOfIntFuncError(coDuplicate, 0); exit; end;
  end;
```

581. Delete an entry from the underlying dynamic array. Raise an error if the index given is out of bounds.

```
procedure Int2PairOfIntFunc.AtDelete(aIndex : integer);
  var i: integer;
  begin if  $(aIndex < 0) \vee (aIndex \geq fCount)$  then
    begin Int2PairOfIntFuncError(coIndexError, 0); exit;
    end;
  if  $aIndex < fCount - 1$  then
    for  $i \leftarrow aIndex$  to  $fCount - 2$  do  $fList[i] \leftarrow fList[i + 1]$ ;
  dec( $fCount$ );
  end;
```

582.

```
procedure Int2PairOfIntFunc.SetCapacity(aLimit : integer);
  begin if  $aLimit < fCount$  then  $aLimit \leftarrow fCount$ ;
  setlength( $fList, aLimit$ );  $fCapacity \leftarrow aLimit$ ;
  end;
```

583. We can “soft delete” all entries in the partial function.

```
procedure Int2PairOfIntFunc.DeleteAll;
  begin  $fCount \leftarrow 0$ ;
  end;
```

584. We can bisection search on the domain.

```

function Int2PairOfIntFunc.Search(X : integer; var aIndex : integer): boolean;
  var L, H, I, C: integer;
  begin Search  $\leftarrow$  False; L  $\leftarrow$  0; H  $\leftarrow$  fCount - 1;
  while L  $\leq$  H do
    begin I  $\leftarrow$  (L + H) shr 1; C  $\leftarrow$  CompareInt(fList[I].X, X);
    if C < 0 then L  $\leftarrow$  I + 1
    else begin H  $\leftarrow$  I - 1;
      if C = 0 then
        begin Search  $\leftarrow$  True; L  $\leftarrow$  I;
        end;
      end;
    end;
  aIndex  $\leftarrow$  L;
end;

```

585. Copy constructor. This leaves the argument *aFunc* unchanged.

```

constructor Int2PairOfIntFunc.CopyInt2PairOfIntFunc(var aFunc : Int2PairOfIntFunc);
  begin Init(aFunc.fCapacity); Move(aFunc.fList[0], fList[0], aFunc.fCapacity * SizeOf(Int2PairOfInt));
  fCount  $\leftarrow$  aFunc.fCount;
end;

```

586. Find the index in the underlying dynamic array for $x \in \text{dom}(f)$. If $x \notin \text{dom}(f)$, then return -1 .

```

function Int2PairOfIntFunc.IndexOf(X : integer): integer;
  var I: integer;
  begin IndexOf  $\leftarrow$   $-1$ ;
  if Search(X, I) then IndexOf  $\leftarrow$  I;
end;

```

587. Test if $x \in \text{dom}(f)$.

```

function Int2PairOfIntFunc.HasInDom(X : integer): boolean;
  var I: integer;
  begin HasInDom  $\leftarrow$  Search(X, I);
end;

```

588. Attempt to insert (x, y_1, y_2) into $f: \mathbf{Z} \rightarrow \mathbf{Z} \times \mathbf{Z}$.

```

procedure Int2PairOfIntFunc.Assign(X, Y1, Y2 : integer);
  var lInt2PairOfInt: Int2PairOfInt;
  begin lInt2PairOfInt.X  $\leftarrow$  X; lInt2PairOfInt.Y1  $\leftarrow$  Y1; lInt2PairOfInt.Y2  $\leftarrow$  Y2;
  Insert(lInt2PairOfInt);
end;

```

589. Given $f: \mathbf{Z} \rightarrow \mathbf{Z} \times \mathbf{Z}$ and $x \in \mathbf{Z}$, if $x \in \text{dom}(f)$ return $f(x)$. Otherwise raise an error.

```

function Int2PairOfIntFunc.Value(X : integer): IntPair;
  var I: integer;
  begin if Search(X, I) then
    begin Result.X  $\leftarrow$  fList[I].Y1; Result.Y  $\leftarrow$  fList[I].Y2;
    end
  else Int2PairOfIntFuncError(coDuplicate, 0);
end;

```


590. We have a myriad of random declarations, so we just stick them all here.

```

⟨Public interface for mobjects.pas 309⟩ +≡
  { Comparing Strings wrt MStrObj }
function CompareStringPtr(aKey1, aKey2 : Pointer): integer;
  { Comparing Strings and integers }
function CompareStr(aStr1, aStr2 : String): integer;
function CompareIntPairs(X1, Y1, X2, Y2 : Longint): integer;
  { Dynamic String handling routines }
function NewStr(const S: String): PString;
procedure DisposeStr(P : PString);
function GrowLimit(aLimit : integer): integer;    { Abstract notification procedure }
function CompareNatFunc(aKey1, aKey2 : Pointer): integer;
procedure Abstract1;
var EmptyNatFunc: NatFunc;

```

File 11

XML Dictionary

591. We have several types declared in the `xml_dict.pas` file. These are enumerated types, and string constants for their names.

```

<xml_dict.pas 591> ≡
  <GNU License 4>
unit xml_dict;
interface
uses mobjects;

{ known (and only allowed) XML elements }
type XMLElemKind = (elUnknown, elAdjective, elAdjectiveCluster, elArticleID, elAncestors,
  elArguments, elBlock, elConditions, elCorrectnessConditions, elDefiniens, elDirective, elEnviron,
  elEquality, elFieldSegment, elFormat, elFormats, elIdent, elItem, elIterativeStep, elLabel, elLink,
  elLoci, elLociEquality, elLocus, elNegatedAdjective, elPartialDefiniens, elPriority, elProposition,
  elProvisionalFormulas, elRedefine, elRightCircumflexSymbol, elSchematicVariables, elScheme,
  elSelector, elSetMember, elSkippedProof, elSymbol, elSymbolCount, elSymbols, elSubstitution,
  elTypeSpecification, elTypeList, elVariable, elVariables, elVocabularies, elVocabulary);

{ known XML attributes }
  XMLAttrKind = (atUnknown, atAid, atArgNr, atArticleId, atArticleExt, atCol, atCondition,
  atConstrNr, atIdNr, atInfinitive, atKind, atLabelNr, atLeftArgNr, atLine, atMizfiles, atName,
  atNegated, atNr, atNumber, atOrigin, atPosLine, atPosCol, atPriority, atProperty,
  atRightSymbolNr, atSchNr, atSerialNr, atShape, atSpelling, atSymbolNr, atValue, atVarNr,
  atVarSort, atX, atX1, atX2, atY, atY1, atY2);
const XMLElemName: array [XMLElemKind] of string = ('Unknown', 'Adjective',
  'Adjective-Cluster', 'ArticleID', 'Ancestors', 'Arguments', 'Block', 'Conditions',
  'CorrectnessConditions', 'Definiens', 'Directive', 'Environ', 'Equality',
  'Field-Segment', 'Format', 'Formats', 'Ident', 'Item', 'Iterative-Step', 'Label', 'Link',
  'Loci', 'LociEquality', 'Locus', 'NegatedAdjective', 'Partial-Definiens', 'Priority',
  'Proposition', 'Provisional-Formulas', 'Redefine', 'Right-Circumflex-Symbol',
  'Schematic-Variables', 'Scheme', 'Selector', 'SetMember', 'elSkippedProof', 'Symbol',
  'SymbolCount', 'Symbols', 'Substitution', 'Type-Specification', 'Type-List',
  'Variable', 'Variables', 'Vocabularies', 'Vocabulary');
XMLAttrName: array [XMLAttrKind] of string = ('unknown', 'aid', 'argnr', 'articleid',
  'articleext', 'col', 'condition', 'constrnr', 'idnr', 'infinitive', 'kind', 'labelnr',
  'leftargnr', 'line', 'mizfiles', 'name', 'negated', 'nr', 'number', 'origin', 'posline',
  'poscol', 'priority', 'property', 'rightsymbolnr', 'schnr', 'serialnr', 'shape',
  'spelling', 'symbolnr', 'value', 'varnr', 'varsort', 'x', 'x1', 'x2', 'y', 'y1', 'y2');
implementation
end .

```

File 12

Environment library

592. We have a library to handle accessing the Mizar mathematical library files. This is used in `makeenv.dpr` and using local `prel/` directories.

This will execute *InitLibrEnv* (§611) and *CheckCompatibility* (§608).

```

<librenv.pas 592> ≡
  <GNU License 4>
unit librenv;
interface
  uses mobjects;
    <Interface for MIZFILES library 593>
implementation
  uses
    @{@&$IFDEF WIN32@}windows,
    @{@&$ENDIF@}mizenv, pcmizver, mconsole;
    <Implementation for librenv.pas 596>
  begin InitLibrEnv; CheckCompatibility;
end.

```

```

593. <Interface for MIZFILES library 593> ≡
const MML = 'mml'; EnvMizFiles = 'MIZFILES';
var MizPath, MizFiles: string;
function LibraryPath(fName, fExt: string): string;
procedure GetSortedNames(fParam: byte; var fList: MStringCollection);
procedure GetNames(fParam: byte; var fList: StringColl);
procedure ReadSortedNames(fName: string; var fList: MStringCollection);
procedure ReadNames(fName: string; var fList: StringColl);

```

See also section 594.

This code is used in section 592.

594. There are two public-facing classes.

```

<Interface for MIZFILES library 593> +≡
type <Declare FileDescr data type 595>
  <Declare FileDescrCollection data type 598>
var LocFilesCollection: FileDescrCollection;

```

595. File descriptors. We use file descriptors for things. These are just “a file name” and “a timestamp”.

```

⟨ Declare FileDescr data type 595 ⟩ ≡
  PFileDescr = ↑FileDescr;
  FileDescr = object (MObject)
    nName: PString;
    Time: LongInt;
    constructor Init(fIdent : string; fTime : LongInt);
    destructor Done; virtual;
  end ;

```

This code is used in section 594.

596. Constructor.

```

⟨ Implementation for librenv.pas 596 ⟩ ≡
constructor FileDescr.Init(fIdent : string; fTime : LongInt);
  begin nName ← NewStr(fIdent); Time ← fTime;
  end;

```

See also sections 599, 608, and 611.

This code is used in section 592.

597. Destructor.

```

destructor FileDescr.Done;
  begin DisposeStr(nName);
  end;

```

598. Collection of file descriptions.

```

⟨ Declare FileDescrCollection data type 598 ⟩ ≡
  PFileDescrCollection = ↑FileDescrCollection;
  FileDescrCollection = object (MSortedCollection)
    function Compare(Key1, Key2 : Pointer): integer; virtual;
    procedure StoreFIL(fName : string);
    constructor LoadFIL(fName : string);
    procedure InsertTimes;
  end ;

```

This code is used in section 594.

599. Comparing two entries in a file descriptor collection amounts to comparing the names for the file descriptors.

```

⟨ Implementation for librenv.pas 596 ⟩ +≡
function FileDescrCollection.Compare(Key1, Key2 : Pointer): integer;
  begin if PFileDescr(Key1)↑.nName↑ < PFileDescr(Key2)↑.nName↑ then Compare ← -1
  else if PFileDescr(Key1)↑.nName↑ = PFileDescr(Key2)↑.nName↑ then Compare ← 0
  else Compare ← 1;
  end;

```

600. Inserting file times into the file descriptors relies upon mizenv.pas’s *GetFileTime* (§50) function.

```

procedure FileDescrCollection.InsertTimes;
  var z: integer;
  begin for z ← 0 to Count - 1 do
    with PFileDescr(Items↑[z])↑ do Time ← GetFileTime(nName↑);
  end;

```

601. Constructor. This leverages a few primitive PASCAL functions: *assign(file, name)* assigns *name* to a file but does not open the file (it is still considered closed). Then *reset(file)* opens the file for reading.

Specifically, this will load a *.fil* file produced by Mizar. These contain $2N$ lines: a file path on line $2n-1$, then a timestamp on line $2n$ for $n = 1, \dots, N$. This appears to be used for local *prel/* files.

```
constructor FileDescrCollection.LoadFIL(fName : string);
  var FIL: text; lName: string; lTime: longint;
  begin Assign(FIL, fName); Reset(FIL); Init(0, 10);
  while  $\neg$ eof(FIL) do
    begin ReadLn(FIL, lName); ReadLn(FIL, lTime); Insert(new(PFileDescr, Init(lName, lTime)));
    end;
  close(FIL);
end;
```

602. Repopulate .fil file. This will erase the file named *fName*, then assign to *FIL* that file, and *rewrite(FIL)* will open it for writing.

This will loop through every item in the caller's underlying collection, writing the file names and times to the *.fil* file.

```
procedure FileDescrCollection.StoreFIL(fName : string);
  var FIL: text; i: integer;
  begin EraseFile(fName); Assign(FIL, fName); Rewrite(FIL); InsertTimes;
  for i  $\leftarrow$  0 to Count - 1 do
    with PFileDescr(Items $\uparrow$ [i]) $\uparrow$  do
      begin WriteLn(FIL, nName $\uparrow$ ); WriteLn(FIL, Time)
      end;
  Close(FIL);
end;
```

603. The library path tries to use the local version of a file, if it exists as tested with *MFileExists* (§46). Otherwise it looks at the Mizar MML version of a file, if it exists.

This returns the path to the file, as a string. If the file cannot be found either in the local *prel* directory or the MML *prel* directory, then it returns the empty string.

```
function LibraryPath(fName, fExt : string): string;
  begin LibraryPath  $\leftarrow$  '';
  if MFileExists('prel' + DirSeparator + fName + fExt) then
    begin LocFilesCollection.Insert(New(PFileDescr, Init('prel' + DirSeparator + fName + fExt, 0)));
    LibraryPath  $\leftarrow$  'prel' + DirSeparator + fName + fExt; exit
    end;
  if MFileExists(MizFiles + 'prel' + DirSeparator + fName[1] + DirSeparator + fName + fExt) then
    LibraryPath  $\leftarrow$  MizFiles + 'prel' + DirSeparator + fName[1] + DirSeparator + fName + fExt;
  end;
```

604. This function actually is not used anywhere, so I am not sure why we have it.

```
procedure ReadSortedNames(fName : string; var fList : MStringCollection);
  var NamesFile: text;
  begin if fName[1] = '@' then
    begin Delete(fName, 1, 1); FileExam(fName); Assign(NamesFile, fName); Reset(NamesFile);
    fList.Init(100, 100);
    while ¬seekEof(NamesFile) do
      begin ReadLn(NamesFile, fName); fList.Insert(NewStr(fName));
      end;
    exit;
  end;
  fList.Init(2, 10); fList.Insert(NewStr(fName));
end;
```

605. Again, this function is not used anywhere, so I am not sure why we have it.

```
procedure ReadNames(fName : string; var fList : StringColl);
  var NamesFile: text;
  begin if fName[1] = '@' then
    begin Delete(fName, 1, 1); FileExam(fName); Assign(NamesFile, fName); Reset(NamesFile);
    fList.Init(10, 10);
    while ¬seekEof(NamesFile) do
      begin ReadLn(NamesFile, fName); fList.Insert(NewStr(fName));
      end;
    exit;
  end;
  fList.Init(2, 10); fList.Insert(NewStr(fName));
end;
```

606. This function is used in `lisvoc.dpr`

```
procedure GetSortedNames(fParam : byte; var fList : MStringCollection);
  var FileName: string; NamesFile: text; i: integer;
  begin if ParamCount < fParam then
    begin fList.Init(0, 0); exit
    end;
  FileName ← ParamStr(fParam);
  if FileName[1] = '@' then
    begin Delete(FileName, 1, 1); FileExam(FileName); Assign(NamesFile, FileName);
    Reset(NamesFile); fList.Init(10, 10);
    while ¬seekEof(NamesFile) do
      begin ReadLn(NamesFile, FileName); fList.Insert(NewStr(TrimString(FileName)));
      end;
    exit;
  end;
  fList.Init(2, 8); fList.Insert(NewStr(FileName));
  for i ← fParam + 1 to ParamCount do
    begin FileName ← ParamStr(i); fList.Insert(NewStr(FileName));
    end;
end;
```

607. Continuing with the “this is not used anywhere” theme, this function is not used anywhere.

```

procedure GetNames(fParam : byte; var fList : StringColl);
  var FileName: string; NamesFile: text; i: integer;
  begin if ParamCount < fParam then
    begin fList.Init(0,0); exit
    end;
  FileName  $\leftarrow$  ParamStr(fParam);
  if FileName[1] = '@' then
    begin Delete(FileName, 1, 1); FileExam(FileName); Assign(NamesFile, FileName);
    Reset(NamesFile); fList.Init(10, 10);
    while  $\neg$ seekEof(NamesFile) do
      begin ReadLn(NamesFile, FileName); fList.Insert(NewStr(TrimString(FileName)));
      end;
    exit;
    end;
  fList.Init(2, 8); fList.Insert(NewStr(FileName));
  for i  $\leftarrow$  fParam + 1 to ParamCount do
    begin FileName  $\leftarrow$  ParamStr(i); fList.Insert(NewStr(FileName));
    end;
  end;

```

608. Check compatibility of Mizar with MML. We will load the `mml.ini` file for the MML version number, and we check it against the Mizar version. If they are not compatible, print a message to the screen, and halt as an error has occurred.

The `mml.ini` file looks something like:

```
[Mizar verifier]
MizarReleaseNbr=8
MizarVersionNbr=1
MizarVariantNbr=15
[MML]
NumberOfArticles=1493
MMLVersion=5.94
```

We will read line-by-line the `mml.ini` file to initialize several variables. This motivates the *Try_read_ini_var* macro.

```
define init_val_and_end(#) ≡ val(lLine,#,lCode);
end
define Try_read_ini_var(#) ≡ lPos ← Pos(#,lLine);
if lPos > 0 then
  begin delete(lLine,1,lPos + 15); init_val_and_end
<Implementation for librenv.pas 596> +≡
procedure CheckCompatibility;
var lFile: text; lLine,lVer1,lVer2,l: string; lPos,lCode: integer;
  lMizarReleaseNbr, lMizarVersionNbr, lMizarVariantNbr: integer;
begin <Open mml.ini file 609>
lMizarReleaseNbr ← -1; lMizarVersionNbr ← -1; lMizarVariantNbr ← -1;
while ¬seekEof(lFile) do
  begin ReadLn(lFile,lLine); Try_read_ini_var('MizarReleaseNbr=')(lMizarReleaseNbr);
    Try_read_ini_var('MizarVersionNbr=')(lMizarVersionNbr);
    Try_read_ini_var('MizarVariantNbr=')(lMizarVariantNbr);
  end;
close(lFile);
<Assert MML version is compatible with Mizar version 610>
end;
```

609. We open the `$MIZFILES/mml.ini` file for reading.

```
<Open mml.ini file 609> ≡
FileExam(MizFiles + MML + '.ini'); Assign(lFile, MizFiles + MML + '.ini'); Reset(lFile);
```

This code is used in section 608.

610. We need to check the MML version is compatible with the Mizar version. If they are not compatible, raise an error, print a warning to the user, and halt here.

```
<Assert MML version is compatible with Mizar version 610> ≡
if ¬((lMizarReleaseNbr = PCMizarReleaseNbr) ∧ (lMizarVersionNbr = PCMizarVersionNbr)) then
  begin Str(PCMizarReleaseNbr,l); lVer1 ← l; Str(PCMizarVersionNbr,l); lVer1 ← lVer1 + '.' + l;
    Str(PCMizarVariantNbr,l); lVer1 ← lVer1 + '.' + l; Str(lMizarReleaseNbr,l); lVer2 ← l;
    Str(lMizarVersionNbr,l); lVer2 ← lVer2 + '.' + l;
    Str(lMizarVariantNbr,l); lVer2 ← lVer2 + '.' + l; DrawMessage('Mizar_System_ver.□ + lVer1 +
      'is incompatible with the MML version imported(□ + lVer2 + '□',
      'Please check□ + MizFiles + 'mml.ini'); halt(1);
  end;
```

This code is used in section 608.

611. Initialize library environment. This will try to initialize the *MizFiles* variable to be equal to the \$MIZFILES environment variable (if that environment variable exists) or the directory of the program being executed. This *MizFiles* will always end in a directory separator.

We also initialize *MizFileName*, *EnvFileName*, *ArticleName*, *ArticleExt* to be empty strings.

```

define append_dir_separator(#)  $\equiv$  if #[length(#)]  $\neq$  DirSeparator then #  $\leftarrow$  # + DirSeparator;
 $\langle$  Implementation for librenv.pas 596  $\rangle$   $\equiv$ 
procedure InitLibrEnv;
begin LocFilesCollection.Init(0,20); MizPath  $\leftarrow$  ExtractFileDir(ParamStr(0));  $\langle$  Initialize Mizfiles 612  $\rangle$ 
MizFileName  $\leftarrow$  ``; EnvFileName  $\leftarrow$  ``; ArticleName  $\leftarrow$  ``; ArticleExt  $\leftarrow$  ``;
end;

```

612. Initializing *Mizfiles* requires a bit of work. We first guess it based on environment variables. Then we need to ensure it is a directory path.

```

 $\langle$  Initialize Mizfiles 612  $\rangle$   $\equiv$ 
 $\langle$  Guess MizFiles from environment variables or executable path 613  $\rangle$ 
if MizFiles  $\neq$  `` then append_dir_separator(MizFiles);
if MizFiles = `` then Mizfiles  $\leftarrow$  DirSeparator;

```

This code is used in section 611.

613. When the \$MIZFILES environment variable is set, we just use it. When it is empty or missing, then we guess the path of the executable invoked.

```

 $\langle$  Guess MizFiles from environment variables or executable path 613  $\rangle$   $\equiv$ 
MizFiles  $\leftarrow$  GetEnvStr(EnvMizFiles);
if MizFiles = `` then MizFiles  $\leftarrow$  MizPath;

```

This code is used in section 612.

File 13

XML Parser

614. The XML parser module is used for extracting information from XML files. It does not “validate” the XML (it’s assumed to already be valid). The scanner chops up the input stream into tokens, then the parser makes this available as tokens for the user.

Just to review some terminology from XML:

- (1) A **“tag”** is a markup construct that begins with a “<” and ends with a “>”. There are three types of tags:
 - (i) Start-tags: like “<foo>”
 - (ii) End-tags: like “</foo>”
 - (iii) Empty-element tags: like “
”
- (2) A **“Element”** is a logical document component that either (a) begins with a start-tag and ends with an end-tag, or (b) consists of an empty-element tag. The characters between the start-tag and end-tag (if any) are called its **“Contents”**, and may contain markup including other elements which are called **“Child Elements”**.
- (3) An **“Attribute”** is a markup construct consisting of a name-value pair which can exist in a start-tag or an empty-element tag. For example “” has two attributes: one named “src” whose value is “madonna.jpg”, and the other named “alt” whose value is “Madonna”.
- (4) XML documents may start with an **“XML declaration”** which looks something like (after some optional whitespace) “<?xml version=“1.0” encoding=“UTF-8”?>”

⟨xml_parser.pas 614⟩ ≡

⟨GNU License 4⟩

unit *xml_parser*;

interface *uses* *mobjects*, *errhan*;

⟨Constants for *xml_parser.pas* 615⟩

⟨Type declarations for *xml_parser.pas* 616⟩

procedure *XMLASSERT*(*aCond* : *boolean*);

procedure *UnexpectedXMLElement*(**const** *aElem* : *string*;
 aErr : *integer*);

implementation

mdebug ;

uses *info*;

end_mdebug;

⟨Implementation of XML Parser 618⟩

end .

615. Constant parameters. We have a few constant parameters for the error codes.

```

⟨ Constants for xml_parser.pas 615 ⟩ ≡
const InOutFileBuffSize = $4000;
{ for xml attribute tables }
const errElRedundant = 7500; { End of element expected, but child element found }
const errElMissing = 7501; { Child element expected, but end of element found }
const errMissingXMLAttribute = 7502; { Required XML attribute not found }
const errWrongXMLElement = 7503; { Different XML element expected }
const errBadXMLToken = 7506; { Unexpected XML token }

```

This code is used in section 614.

616. Public type declarations. We will defer the “PASCAL classes” until we start implementing them. Right now, we have syntactic classes for the tokens. Specifically we have the start of an XML declaration “<?”, the end of an XML declaration “>”, the start of a character data section “<!” , the start and end of tags, quotation marks, equalities, entities, identifiers, and end of text.

```

⟨ Type declarations for xml_parser.pas 616 ⟩ ≡
type XMLTokenKind = (Err, { an error symbol }
  BI, { <? }
  EI, { ?> }
  DT, { <! }
  LT, { < }
  GT, { > }
  ET, { </ }
  EE, { /> }
  QT, { " }
  EQ, { = }
  EN, { Entity }
  ID, { Identifier, Name }
  EOTX); { End of text }
TokensSet = set of XMLTokenKind;
⟨ Declare XML Scanner Object type 621 ⟩
TElementState = (eStart, eEnd); { high-level parser states, see procedure NextElementState }
⟨ Declare XML Attribute Object 617 ⟩
⟨ Declare XML Parser object 629 ⟩

```

This code is used in section 614.

617. XML Attribute Object. An XML attribute contains the attribute name and its value. We can represent it as “just” an *MStrObj* (§316) with an additional “value” field.

```

⟨ Declare XML Attribute Object 617 ⟩ ≡
XMLAttrPtr = ↑XMLAttrObj;
XMLAttrObj = object (MStrObj)
  nValue: string;
  constructor Init(const aName, aValue: string);
end ;

```

This code is used in section 616.

618. Constructor. This uses the *MStrObj.Init* constructor to initialize the name, then it sets the value.

⟨Implementation of XML Parser 618⟩ ≡

```
constructor XMLAttrObj.Init(const aName, aValue: string);
  begin inheritedInit(aName); nValue ← aValue;
  end;
```

See also sections 619, 620, 622, 624, 625, 628, 630, 635, and 637.

This code is used in section 614.

619. Assertion. We have a helper function for asserting things about XML. This is just a wrapper around *MizAssert* (§146).

⟨Implementation of XML Parser 618⟩ +≡

```
procedure XMLASSERT(aCond : boolean);
  begin MizAssert(errWrongXMLElement, aCond);
  end;
```

620. Unexpected XML Element. Another helper function for checking XML parsing.

⟨Implementation of XML Parser 618⟩ +≡

```
procedure UnexpectedXMLElem(const aElem: string;
  aErr: integer);
  mdebug ;
  var lEl: string;
  end_mdebug ;
  begin
  mdebug ; InfoNewLine; end_mdebug;
  RunTimeError(aErr);
  end;
```

621. XML Scanner Object. The scanner produces a stream of tokens, which is then consumed by the XML parser. Hence, besides the constructor and destructor, there is only one public facing method: get the next token.

⟨Declare XML Scanner Object type 621⟩ ≡

```
XMLScannObj = object (MObject)
  nSourceFile: text;
  nSourceFileBuff: pointer;
  nCurTokenKind: XMLTokenKind;
  nSpelling: string;
  nPos: Position;
  nCurCol: integer;
  nLine: string;
  constructor InitScanning(const aFileName: string);
  destructor Done; virtual;
  procedure GetToken; private
  procedure GetAttrValue;
  end ;
```

This code is used in section 616.

$$\langle \text{Implementation of XML Parser } 618 \rangle + \equiv$$

623. This prepares to read in from an XML file, setting up a text buffer, and opening the file in “read mode”.

```
Assign(nSourceFile, aFileName); GetMem(nSourceFileBuff, InOutFileBuffSize);
SetTextBuf(nSourceFile, nSourceFileBuff↑, InOutFileBuffSize); Reset(nSourceFile) { open for reading }
```

624. Destructor. We need to close the XML file, as well as free up the input buffer.

```

destructor XMLScannObj.Done;
begin close(nSourceFile); FreeMem(nSourceFileBuff, InOutFileBuffSize);
nLine  $\leftarrow$  ``; nSpelling  $\leftarrow$  ``;
inherited Done;
end;

```

$$\mathbf{define} \text{ } update_lexeme \equiv nSpelling \leftarrow Copy(nLine, nPos.Col, nCurCol - nPos.Col)$$

```
procedure XMLScannObj.GetToken;
```

[illegible]

626. If we're done in the file, then we've arrived at the “end-of-file” — i.e., $\text{eof}(nSourceFile)$ is true. In this case, the token returned should be an **EOTX** (end of text). We also end the function here.

On the other hand, if there is still more left in the file, we should read in a line, increment the line number, reset the column to 1, and skip over any whitespace (specifically, “SP” are skipped over — tabs or newlines are not skipped).

```

⟨ Skip whitespace for XML parser 626 ⟩ ≡
  while  $nCurCol = \text{length}(nLine)$  do
    begin if  $\text{eof}(nSourceFile)$  then
      begin  $nCurTokenKind \leftarrow EOTX$ ;  $nSpelling \leftarrow \text{``}$ ; exit end;
      ReadLn( $nSourceFile, nLine$ );  $\text{inc}(nPos.Line)$ ;  $nLine \leftarrow nLine + \text{``}\lfloor\text{``}$ ;  $nCurCol \leftarrow 1$ ;
      while  $(nCurCol < \text{length}(nLine)) \wedge (nLine[nCurCol] = \text{``}\lfloor\text{``})$  do  $\text{inc}(nCurCol)$ ;
    end

```

This code is used in section 625.

627. There are several situations when determining tokens. We will often want to keep accumulating alphanumeric characters, so we describe this in the “keep eating alphadigits” macro.

When we encounter a “<” character, this could begin or end a tag, or it could be something special if the next character is “?” or “!”. We determine the type in the “get tag kind” macro.

```

define keep_eating_alphadigits ≡
  begin  $nCurTokenKind \leftarrow ID$ ;
  repeat  $\text{inc}(nCurCol)$ 
  until  $\text{CharKind}[nLine[nCurCol]] = 0$ ;
end

define get_tag_kind ≡  $\text{inc}(nCurCol)$ ;
  case  $nLine[nCurCol]$  of
     $\text{``}/\text{``}$ : begin  $nCurTokenKind \leftarrow ET$ ;  $\text{inc}(nCurCol)$ ; end;
     $\text{``?}\text{``}$ : begin  $nCurTokenKind \leftarrow BI$ ;  $\text{inc}(nCurCol)$ ; end;
     $\text{``!}\text{``}$ : begin  $nCurTokenKind \leftarrow DT$ ;  $\text{inc}(nCurCol)$ ; end;
  othercases  $nCurTokenKind \leftarrow LT$ ;
  endcases

define keep_getting_until_end_of_tag(#) ≡ begin  $\text{inc}(nCurCol)$ ;
  if  $nLine[nCurCol] = \text{``}>\text{``}$  then
    begin  $nCurTokenKind \leftarrow \#$ ;  $\text{inc}(nCurCol)$ ; end
  else  $nCurTokenKind \leftarrow \text{Err}$ ;
  end;
end;

```

```

⟨ Get token kind based off of leading character 627 ⟩ ≡
  case  $nLine[nCurCol]$  of
     $\text{``a}\text{``} \dots \text{``z}\text{``}, \text{``A}\text{``} \dots \text{``Z}\text{``}, \text{``0}\text{``} \dots \text{``9}\text{``}, \text{``\_}\text{``}, \text{``-}\text{``}, \text{``\&}\text{``}$ : keep_eating_alphadigits;
     $\text{``"}\text{``}$ : begin  $nCurTokenKind \leftarrow QT$ ;  $\text{inc}(nCurCol)$  end;
     $\text{``=}\text{``}$ : begin  $nCurTokenKind \leftarrow EQ$ ;  $\text{inc}(nCurCol)$  end;
     $\text{``<}\text{``}$ : begin get_tag_kind; end;
     $\text{``>}\text{``}$ : begin  $nCurTokenKind \leftarrow GT$ ;  $\text{inc}(nCurCol)$  end;
     $\text{``}/\text{``}$ : keep_getting_until_end_of_tag( $EE$ );
     $\text{``?}\text{``}$ : keep_getting_until_end_of_tag( $EI$ );
  othercases begin  $nCurTokenKind \leftarrow \text{Err}$ ;  $\text{inc}(nCurCol)$  end;
  endcases

```

This code is used in section 625.

628. Scanners can obtain attribute values as tokens. This is used by the XML parser (§§633, 635). I think one possible source of bugs is that this does not handle escaped quotes (e.g., “\” is traditionally parsed as a quotation mark character).

This will not include the delimiting quotation marks, and it will also skip all whitespace *after* the attribute.

```
define skip_to_quotes  $\equiv$  while ( $nCurCol < length(nLine)$ )  $\wedge$  ( $nLine[nCurCol] \neq \text{"\text{'}}$ ) do inc( $nCurCol$ )
define is_space  $\equiv$  ( $nCurCol < length(nLine)$ )  $\wedge$  ( $nLine[nCurCol] \in [\text{'\text{ }'}, \text{'\text{ }'}, \text{'\text{ }'}]$ )
define skip_spaces  $\equiv$  while is_space do inc( $nCurCol$ )
```

(Implementation of XML Parser 618) \equiv

```
procedure XMLScannObj.GetAttrValue;
  var lCol: integer;
  begin lCol  $\leftarrow$  nCurCol; skip_to_quotes;
  nSpelling  $\leftarrow$  Copy(nLine, lCol, nCurCol - lCol); { save the lexeme }
  if nLine[nCurCol] = '\text{' then inc(nCurCol);
  skip_spaces;
  end;
```

629. XML Parser. We recall (§616) the type for element states (it’s an enumerated type with two values, *eStart* and *eEnd*).

(Declare XML Parser object 629) \equiv

```
XMLParserObj = object (XMLScannObj)
  nElName: string; { name of the current element }
  nState: TElementState;
  nAttrVals: MSortedStrList;

  constructor InitParsing(const aFileName: string);
  destructor Done; virtual;
  procedure ErrorRecovery(aErr: integer; aSym: TokensSet);
  procedure NextTag; virtual;
  procedure NextElementState; virtual;
  procedure AcceptEndState; virtual;
  procedure AcceptStartState; virtual;
  procedure OpenStartTag; virtual;
  procedure CloseStartTag; virtual;
  procedure CloseEmptyElementTag; virtual;
  procedure ProcessEndTag; virtual;
  procedure ProcessAttributeName; virtual;
  procedure ProcessAttributeValue; virtual;
  procedure SetAttributeValue(const aVal: string);
end ;
```

This code is used in section 616.

630. Constructor. The parser expects an XML file to start with “<?xml ...?>” (everything after the “xml” is ignored). If this is not the first non-whitespace entry, an error will be raised.

The constructor will then skip all other “<?...?>” entities.

```

define skip_xml_prolog  $\equiv$  while ( $nCurTokenKind \neq EOTX$ )  $\wedge$  ( $nCurTokenKind \neq EI$ ) do GetToken;
    if  $nCurTokenKind = EI$  then GetToken
define skip_all_other_ids  $\equiv$  while  $nCurTokenKind = BI$  do
    begin GetToken;
    while ( $nCurTokenKind \neq EOTX$ )  $\wedge$  ( $nCurTokenKind \neq EI$ ) do GetToken;
    if  $nCurTokenKind = EI$  then GetToken;
    end

```

⟨Implementation of XML Parser 618⟩ +≡

```

constructor XMLParserObj.InitParsing(const aFileName: string);
begin inherited InitScanning(aFileName); nElName  $\leftarrow$  ``; nAttrVals.Init(0);
if  $nCurTokenKind = BI$  then
    begin GetToken;
    if ( $nCurTokenKind = ID$ )  $\wedge$  ( $nSpelling = \text{`xml`}$ ) then GetToken
    else ErrorRecovery(10, [EI, LT]);
    skip_xml_prolog; skip_all_other_ids; { skip all other initial processing instructions }
    end;
end;

```

631. Destructor. We will set the element name to the empty string, and invoke the destructor for the attribute values.

```

destructor XMLParserObj.Done;
begin inherited Done; nAttrVals.Done; nElName  $\leftarrow$  ``;
end;

```

632. Error recovery. We just raise a runtime error. In fact, this is often used in situations like:

```

if  $nCurTokenKind = ID$  then { success }
else ErrorRecovery(5, [LT, ET]);

```

Consequently, it is probably more idiomatic to introduce a macro *xml_match(tokenKind)(aErr, aSym)* to assert the match and raise an error for mismatch. Unfortunately, WEB macros allow for only one argument, so we need two macros.

```

define report_mismatch(#)  $\equiv$  ErrorRecovery(#)
define xml_match(#)  $\equiv$  if  $nCurTokenKind \neq \#$  then report_mismatch
    { ErrorRecovery is no longer allowed for XML, bad XML is just RTE }
procedure XMLParserObj.ErrorRecovery(aErr : integer; aSym : TokensSet);
begin Mizassert(errBadXMLToken, false);
end;

```


633. The parser will consume the next tag or element. It's useful to recall the token kinds (§616).

Curiously, the attributes are skipped during this parsing function.

This will be using the inherited procedure *GetToken* (§625).

```

    { Parses next part of XML, used for skipping some part of XML }
    { setting the nState to eStart or eEnd. }
    { nElName is set properly }
    { nAttrVals are omitted (skipped). }

```

```

procedure XMLParserObj.NextTag;
begin case nCurTokenKind of
  EOTX: nState  $\leftarrow$  eEnd; { sometimes we need this }
  LT: begin nState  $\leftarrow$  eStart; GetToken; xml_match(ID)(6, [LT, ET]); OpenStartTag; GetToken;
    < Get contents of XML start tag 634 >;
  end;
  EE: begin nState  $\leftarrow$  eEnd; GetToken; end;
  ET: begin nState  $\leftarrow$  eEnd; GetToken; xml_match(ID)(8, [LT, ET]); OpenStartTag; GetToken;
    xml_match(GT)(7, [LT, ET]); GetToken
  end;
othercases ErrorRecovery(9, [LT, ET]);
endcases;
end;

```

634. When getting the contents of an XML start tag (or possibly an element), we keep going until we get to either “\>” (for an element) or “>” (for a tag). This will be using the inherited procedure *GetToken* (§625).

```

define get_attribute  $\equiv$  begin GetToken; xml_match(EQ)(4, [ID, GT, LT, ET]); GetToken;
  xml_match(QT)(3, [ID, GT, LT, ET]); GetAttrValue; GetToken;
end

```

```

< Get contents of XML start tag 634 >  $\equiv$ 
repeat case nCurTokenKind of
  GT: begin GetToken; break end;
  EE: begin break end;
  ID: get_attribute;
  othercases begin ErrorRecovery(5, [GT, LT, ET]); break end;
endcases;
until nCurTokenKind = EOTX

```

This code is used in section 633.

635. For Mizar, *everything* will be encoded as an element or an attribute on an element. So we do not really need to consider the case where we would encounter text in the body of an element.

⟨Implementation of XML Parser 618⟩ +≡

{ Parses next part of XML, setting the $nState$ to $eStart$ or $eEnd$. If $nState = eStart$, then $nElName$, $nAttrVals$ are set properly. It is possible to go from $nState = eStart$ to $nState = eStart$ (when the element is non empty), and similarly from $eEnd$ to $eEnd$. }

procedure XMLParserObj.NextElementState;

begin case $nCurTokenKind$ **of**

$EOTX$: $nState \leftarrow eEnd$; { sometimes we need this }

LT : ⟨Parse start of XML tag 636⟩;

EE : **begin** $nState \leftarrow eEnd$; $GetToken$; **end**;

ET : **begin** $nState \leftarrow eEnd$; $GetToken$; $xml_match(ID)(8, [LT, ET])$; $ProcessEndTag$; $GetToken$;
 $xml_match(GT)(7, [LT, ET])$; $GetToken$; **end**;

othercases $ErrorRecovery(9, [LT, ET])$;

endcases;

end;

636. We start parsing a start-tag because we have encountered an LT token. So at this point, the next token should be an identifier of some kind. A start-tag may actually be an empty-element tag, so we need to look out for the EE token kind.

Note: the XML parser does not handle comments, otherwise we would need to consider that situation here.

define $end_start_tag \equiv$ **begin** $GetToken$; $CloseStartTag$; $break$ **end**

define $end_empty_tag \equiv$ **begin** $CloseEmptyElementTag$; $break$ **end**

⟨Parse start of XML tag 636⟩ ≡

begin $nState \leftarrow eStart$; $GetToken$; $xml_match(ID)(6, [LT, ET])$; $OpenStartTag$;

{ Start-Tag or Empty-Element-Tag Name = nSpelling }

$GetToken$;

repeat case $nCurTokenKind$ **of**

GT : end_start_tag ; { End of a Start-Tag }

EE : end_empty_tag ; { End of a Empty-Element-Tag }

ID : **begin** $ProcessAttributeName$; $GetToken$; $xml_match(EQ)(4, [ID, GT, LT, ET])$; $GetToken$;
 $xml_match(QT)(3, [ID, GT, LT, ET])$; $GetAttrValue$; $ProcessAttributeValue$; $GetToken$;

end;

othercases begin $ErrorRecovery(5, [GT, LT, ET])$; $break$ **end**;

endcases;

until $nCurTokenKind = EOTX$;

end

This code is used in section 635.

637. We will want assertions reflecting the parser is in a “start” state or an “end” state.

⟨Implementation of XML Parser 618⟩ +≡

procedure XMLParserObj.AcceptEndState;

begin $NextElementState$; $MizAssert(errElRedundant, nState = eEnd)$;

end;

procedure XMLParserObj.AcceptStartState;

begin $NextElementState$; $MizAssert(errElMissing, nState = eStart)$;

end;

638.

```

procedure XMLParserObj.OpenStartTag;
  begin nElName  $\leftarrow$  nSpelling; nAttrVals.FreeAll;
  end;

```

639. We have a few procedures which are, well, empty. I am not sure why we have them. Regardless, here they are!

```

procedure XMLParserObj.CloseStartTag;
  begin end;
procedure XMLParserObj.CloseEmptyElementTag;
  begin end;
procedure XMLParserObj.ProcessEndTag;
  begin end;

```

640. We have a list of attributes. When the parser *ProcessAttributeName*, it will merely push a new *XMLAttrPtr* to the list with the given name. Then *ProcessAttributeValue* will associate to it the value which has been parsed. We can, of course, *manually* set the value for an attribute using *SetAttributeValue*.

```

procedure XMLParserObj.ProcessAttributeName;
  begin nAttrVals.Insert(new(XMLAttrPtr, Init(nSpelling, '')));
  end;
procedure XMLParserObj.ProcessAttributeValue;
  begin SetAttributeValue(nSpelling);
  end;
procedure XMLParserObj.SetAttributeValue(const aVal: string);
  begin with nAttrVals do XMLAttrPtr(Items↑[Count - 1])↑.nValue  $\leftarrow$  aVal;
  end;

```

File 14

I/O with XML

641. We will want to print some XML to a buffer or stream.

Note that XML seems to be frozen at version 1.0 (first published in 1998, last revised in its fifth edition released November 26, 2008).

```

⟨xml_inout.pas 641⟩ ≡
  ⟨GNU License 4⟩
unit xml_inout;
  interface
    uses errhan, mobjects, xml_parser;
    ⟨Type declarations for XML I/O 642⟩
    function QuoteStrForXML(const aStr: string): string;
    function XMLToStr(const aXMLStr: string): string;
    function QuoteXMLAttr(aStr : string): string;
    const gXMLHeader = `<?xml version="1.0"?>` + #10;
  implementation
    uses SysUtils, mizenv, pcmizver, librenv, xml_dict
    mdebug , info end_mdebug;
  ⟨Implementation for I/O of XML 643⟩
end .

```

642. There are only 4 types of streams we care about: Streams, Text Streams, XML Input Streams, and XML Output Streams.

```

⟨Type declarations for XML I/O 642⟩ ≡
  ⟨Public interface for XML Input Stream 655⟩;
  ⟨Public declaration for Stream Object 647⟩;
  ⟨Public declaration for Text Stream Object 651⟩;
  ⟨Public declaration for XML Output Stream 660⟩;

```

This code is used in section 641.

643. Escape for quote string. We want to allow only alphanumerics [a-zA-Z0-9] as well as dashes (“-”), spaces (“ ”), commas (“,”), periods (“.”), apostrophes (“’”), forward slashes (“/”), underscores (“_”), brackets (“[” and “]”), exclamation points (“!”), semicolons and colons (“;” and “:”), and equal signs (“=”). Everything else we transform into an XML entity of the form “&xx” where x is a hexadecimal digit.

$\langle \text{Implementation for I/O of XML } 643 \rangle \equiv$

```
function QuoteStrForXML(const aStr: string): string;
const ValidCharTable = ([`a` .. `z`, `A` .. `Z`, `0` .. `9`, `-`, `_`, `, `.`, `'`, `\`, `/`, `-`, `[`, `]`,
    `!`, `; `, `:`, `=`]);
var c: char; i: integer;
begin result ← aStr;
for i ← length(result) downto 1 do
    begin c ← result[i];
    if ¬(c ∈ ValidCharTable) then
        begin result[i] ← `&`; Insert(`#x' + IntToHex(Ord(c), 2) + `; `, result, i + 1);
        end;
    end;
end;
```

See also sections 646, 648, 652, 656, 661, and 667.

This code is used in section [641](#).

644. This appears to “undo” the previous function, transforming XML entities of the form “&xx” into characters.

```

function XMLToStr(const aXMLStr: string): string;
var i, h: integer; lHexNr: string;
begin result  $\leftarrow$  aXMLStr;
for i  $\leftarrow$  length(result) - 5 downto 1 do
    begin  $\langle$  Transform XML entity into character, if encountering an XML entity at i 645  $\rangle$ ;
    end;
result  $\leftarrow$  Trim(result);
end;

```

645. Transforming an XML entity into a character. This specifically checks for *hexadecimal* entities of the form “&#xXX” for some hexadecimal digits *X*. Note we must prepend “0x” to a numeric string for PASCAL to parse it as hexadecimal.

Since PASCAL does not have shortcircuiting Boolean operations, we need to make this a nested **if** statement.

$\langle \text{Transform XML entity into character, if encountering an XML entity at } i \text{ 645} \rangle \equiv$

```

if ( $result[i] = \text{'\&'}$ )  $\wedge$  ( $length(result) \geq i + 5$ ) then
  begin if ( $result[i + 1] = \text{'\#'}$ )  $\wedge$  ( $result[i + 2] = \text{'x'}$ ) then
    begin  $lHexNr \leftarrow result[i + 3] + result[i + 4]$ ;  $h \leftarrow StrToInt(\text{'0x'} + lHexNr)$ ;  $Delete(result, i, 5)$ ;
     $result[i] \leftarrow chr(h)$ ;
  end;
end

```

This code is used in section 644.

646. We can quote an XML attribute, escaping quotes, ampersands, and angled brackets. For non-ASCII characters, we escape it to a hexadecimal XML entity.

⟨Implementation for I/O of XML 643⟩ +≡

```
function QuoteXMLAttr(aStr : string): string;
  var i: integer;
  begin result ← ``;
  for i ← 1 to length(aStr) do
    case aStr[i] of
      `"`: result ← result + `&quot;;`
      `&`: result ← result + `&amp;;`
      `<`: result ← result + `&lt;;`
      `>`: result ← result + `&gt;;`
      othercases if integer(aStr[i]) > 127 then result ← result + `&#x` + IntToHex(Ord(aStr[i]), 2) + `;`
        else result ← result + aStr[i];
      endcases;
    end;
```

647. Stream object class. A stream consists of a file, a character buffer, as well as integers tracking the size of the buffer and (I think) the position in the buffer. This is the parent class to XML output buffers.

⟨Public declaration for Stream Object 647⟩ ≡

```
StreamObj = object (MObject)
  nFile: File;
  fFileBuff: ↑BuffChar;
  fBuffCount, fBuffInd: longint;
  constructor InitFile(const AFileName: string);
  procedure Error(Code, Info : integer); virtual;
  destructor Done; virtual;
end
```

This code is used in section 642.

648. We will have a wrapper function for conveniently reporting errors.

⟨Implementation for I/O of XML 643⟩ +≡

```
procedure StreamObj.Error(Code, Info : integer);
  begin RunError(2000 + Code);
  end;
```

649. Constructor. We begin by *Assign*-ing a name to a file, allocating a file buffer, then initializing the buffer size to zero, and the buffer position to zero. (The buffer position *fBuffInd* is needed only when writing to an output XML stream.)

```
constructor StreamObj.InitFile(const AFileName: string);
  begin Assign(nFile, AFileName); new(fFileBuff); fBuffCount ← 0; fBuffInd ← 0;
  end;
```

650. Destructor. We close the file, and free up the file buffer.

```
destructor StreamObj.Done;
  begin Close(nFile); dispose(fFileBuff);
  end;
```

651. Text Stream Object. A text stream is very similar to a Stream Object, except it is specifically for text.

```

⟨Public declaration for Text Stream Object 651⟩ ≡
  TXTStreamObj = object (MObject)
    nFile: text;
    nFileBuff: pointer;
    constructor InitFile(const AFileName: string);
    procedure Error(Code, Info : integer); virtual;
    destructor Done; virtual;
  end

```

This code is used in section 642.

652. We have the convenience function for reporting errors.

```

⟨Implementation for I/O of XML 643⟩ +≡
procedure TXTStreamObj.Error(Code, Info : integer);
  begin RunError(2000 + Code);
  end;

```

653. Constructor. Assign a name to the file, allocate an input buffer, then initialize the buffer.

```

constructor TXTStreamObj.InitFile(const AFileName: string);
  begin Assign(nFile, AFileName); GetMem(nFileBuff, InOutFileBuffSize);
  SetTextBuf(nFile, nFileBuff↑, InOutFileBuffSize);
  end;

```

654. Destructor. Simply free the underlying file buffer.

```

destructor TXTStreamObj.Done;
  begin FreeMem(nFileBuff, InOutFileBuffSize);
  end;

```

655. XML Input Streams. An input stream reads an XML file and produces an abstract syntax tree for its contents. This extends this XML parser class (§629). It may be tempting to draw similarities with, e.g., the StAX library (in Java), but the truth is there's only finitely many ways to parse XML, and some ways are just more natural.

```

⟨Public interface for XML Input Stream 655⟩ ≡
  XMLInStreamPtr = ↑XMLInStreamObj;
  XMLInStreamObj = object (XMLParserObj)
    constructor OpenFile(const AFileName: string);
    function GetOptAttr(const aAttrName: string; var aVal: string) : boolean;
    function GetAttr(const aAttrName: string): string;
    function GetIntAttr(const aAttrName: string): integer;
  end

```

This code is used in section 642.

656. Constructor. The non-debugging code just invokes the XML Parser's constructor (§630).

```

⟨Implementation for I/O of XML 643⟩ +≡
constructor XMLInStreamObj.OpenFile(const AFileName: string);
  begin
  mdebug ; write(InfoFile, AFileName); end_mdebug;
  InitParsing(AFileName);
  mdebug ; WriteLn(InfoFile, 'reset'); end_mdebug;
  end;

```

657. We use the inherited *XMLParserObj*'s *nAttrVals*: *MSortedStrList* to track the XML attributes. If *aAttrName* is stored there, this will mutate *aVal* to store the associated value and the function will return *true*. Otherwise, this will return *false*.

This is useful for getting the value of an *optional* XML attribute.

```
{ get string denoted by optional XML attribute aAttrName }
function XMLInStreamObj.GetOptAttr (const aAttrName: string; var aVal: string) : boolean;
var lAtt: XMLAttrPtr;
begin lAtt ← XMLAttrPtr(nAttrVals.ObjectOf(aAttrName));
if lAtt ≠ nil then
  begin aVal ← lAtt↑.nValue; GetOptAttr ← true; exit;
  end;
  GetOptAttr ← false;
end;
```

658. When we know an XML attribute is *required*, we can just get the associated value directly (and raise an error if it is missing).

```
{ get string denoted by required XML attribute aAttrName }
function XMLInStreamObj.GetAttr(const aAttrName: string): string;
var lAtt: XMLAttrPtr;
begin lAtt ← XMLAttrPtr(nAttrVals.ObjectOf(aAttrName));
if lAtt ≠ nil then
  begin GetAttr ← lAtt↑.nValue; exit;
  end;
  MizAssert(errMissingXMLAttribute, false);
end;
```

659. When the required attribute has an integer value, we should return the integer-value of it. Does this ever happen? Yes! For example, when writing an article named `article.miz`, then we run the verifier on it, we shall obtain `article.xml` which will contain tags of the form “<Adjective nr="5">”.

```
{ get integer denoted by required XML attribute aAttrName }
function XMLInStreamObj.GetIntAttr(const aAttrName: string): integer;
var lInt, ec: integer;
begin val(GetAttr(aAttrName), lInt, ec); GetIntAttr ← lInt;
end;
```


660. XML Output Streams. We will want to write data to an XML file. This gives us an abstraction for doing so.

```

⟨Public declaration for XML Output Stream 660⟩ ≡
  XMLOutputStreamPtr = ↑XMLOutputStreamObj;
  XMLOutputStreamObj = object (StreamObj)
    nIndent: integer; { indenting }
    constructor OpenFile(const AFileName: string);
    constructor OpenFileWithXSL(const AFileName: string);
    destructor EraseFile;
    procedure OutChar(AChar : char);
    procedure OutNewLine;
    procedure OutString(const AString: string);
    procedure OutIndent;
    procedure Out_XElStart(const fEl: string);
    procedure Out_XAttrEnd;
    procedure Out_XElStart0(const fEl: string);
    procedure Out_XElEnd0;
    procedure Out_XEl1(const fEl: string);
    procedure Out_XElEnd(const fEl: string);
    procedure Out_XAttr(const fAt, fVal: string);
    procedure Out_XIntAttr(const fAt: string;
      fVal: integer);
    procedure Out_PosAsAttrs(const fPos: Position);
    procedure Out_XElWithPos(const fEl: string;
      const fPos: Position);
    procedure Out_XQuotedAttr(const fAt, fVal: string);
    destructor Done; virtual;
  end

```

This code is used in section 642.

661. Constructor. We initialize a file, open it for writing, set the initial indentation amount to zero, and then print the XML header declaration.

```

⟨Implementation for I/O of XML 643⟩ +≡
constructor XMLOutputStreamObj.OpenFile(const AFileName: string);
  begin
    mdebug write(InfoFile, MizFileName + `.` + copy(AFileName, length(AFilename) - 2, 3));
    end_mdebug
    InitFile(AFileName); Rewrite(nFile, 1);
    mdebug WriteLn(InfoFile, `rewritten`); end_mdebug
    nIndent ← 0; OutString(gXMLHeader);
  end;

```

662. Constructor. Since XML supports custom style declarations (think of XSLT), we can also support writing an XML file which uses them. This specifically needs to adjust the XML declaration.

```

  { add the stylesheet procesing info }
constructor XMLOutputStreamObj.OpenFileWithXSL(const AFileName: string);
  begin OpenFile(AFileName);
    OutString(`<?xml-stylesheet`_type="text/xml"`_href="file://` + MizFiles + `miz.xml"?` + #10);
  end;

```

663. Destructor. We need to flush the buffer to the file before freeing up the buffer.

```
destructor XMLOutStreamObj.Done;
  begin if (fBuffInd > 0)  $\wedge$  (fBuffInd < InOutFileBuffSize) then
    BlockWrite(nFile, fFileBuff↑, fBuffInd, fBuffCount);
    inherited Done;
  end;
```

664. Destructor. Some times we want to further erase the output file (which seems, at first glance, like a really bad idea...).

```
destructor XMLOutStreamObj.EraseFile;
  begin Done; Erase(nFile);
end;
```

665. Writing a character to the buffer. When the buffer is full, we flush it.

```
procedure XMLOutStreamObj.OutChar(aChar : char);
  begin fFileBuff↑[fBuffInd] ← AnsiChar(aChar); inc(fBuffInd); ⟨Flush XML output buffer, if full 666⟩;
end;
```

666. The XML output buffer is full when the logical size (fBuffInd) is equal to the InOutFileBuffSize. When this happens, we should write everything to the file, then reset the logical size parameter to zero.

```
⟨Flush XML output buffer, if full 666⟩ ≡
  if fBuffInd = InOutFileBuffSize then
    begin BlockWrite(nFile, fFileBuff↑, InOutFileBuffSize, fBuffCount); fBuffInd ← 0;
  end
```

This code is used in section 665.

667. Print a newline ("␣") to the XML output stream.

```
⟨Implementation for I/O of XML 643⟩ +≡
procedure XMLOutStreamObj.OutNewLine;
  begin OutChar(#10);
end;
```

668. Printing a string to the output buffer.

```
procedure XMLOutStreamObj.OutString(const aString: string);
  var i: integer;
  begin for i ← 1 to length(aString) do OutChar(aString[i]);
end;
```

669. Printing nIndent spaces ("␣") to the output buffer.

```
{ print nIndent spaces }
procedure XMLOutStreamObj.OutIndent;
  var i: integer;
  begin for i ← 1 to nIndent do OutChar('␣');
end;
```

670. When printing a start-tag to the file, we start by printing the indentation, then we increment the indentation, then we print the “<” followed by the name of the tag.

```
{ print '<' and the representation of fEl with indenting }
procedure XMLOutStreamObj.Out_XElStart(const fEl: string);
  begin OutIndent; inc(nIndent); OutChar('<'); OutString(fEl);
  end;
```

671. When we are done writing the attributes of a tag, we print the “>” to the file, and we also print a newline to the file.

```
{ close the attributes with '>' }
procedure XMLOutStreamObj.Out_XAttrEnd;
  begin OutChar('>'); OutNewLine;
  end;
```

672. When we want to write the tag, but omit the attributes, we can do so.

```
{ no attributes expected }
procedure XMLOutStreamObj.Out_XElStart0(const fEl: string);
  begin Out_XElStart(fEl); Out_XAttrEnd;
  end;
```

673. For empty-element tags, we should close the tag with “/>”, print a new line, then *decrement* the indentation since there are no children to the tag.

```
{ print '/>' with indenting }
procedure XMLOutStreamObj.Out_XElEnd0;
  begin OutString('>'); OutNewLine; dec(nIndent);
  end;
```

674. When printing an empty-element tag without any attributes, we can combine the preceding functions together.

```
{ no attributes and elements expected }
procedure XMLOutStreamObj.Out_XEl1(const fEl: string);
  begin Out_XElStart(fEl); Out_XElEnd0;
  end;
```

675. Printing end-tags should first decrement the indentation *before* printing the indentation to the file (so that the end-tag vertically aligns with the associated start-tag). Then we print “</” followed by the tag name and then “>”. We should print a newline to the file, too.

```
{ close the fEl element using '</' }
procedure XMLOutStreamObj.Out_XElEnd(const fEl: string);
  begin dec(nIndent); OutIndent; OutString('</'); OutString(fEl); OutChar('>'); OutNewLine;
  end;
```

676. When printing one attribute to a tag, we need a whitespace printed (to separate the tag’s name — or preceding attribute — from the current attribute being printed), followed by the attribute’s name printed with an equality symbol, then enquoted the value of the attribute.

```
{ print one attribute key-value pair }
procedure XMLOutStreamObj.Out_XAttr(const fAt, fVal: string);
  begin OutChar(' '); OutString(fAt); OutString('=''); OutString(fVal); OutChar('"');
  end;
```

677. When the value of an attribute is an integer, invoke *IntToStr(fVal)* to pretend it is a string value. Then printing out to a file an attribute with an integer value boils down to printing out the attribute with a string value.

```
{ print one attribute key-value pair, where value is integer }
procedure XMLOutStreamObj.Out_XIntAttr(const fAt: string; fVal: integer);
  begin Out_XAttr(fAt, IntToStr(fVal));
  end;
```

678. We can now just compose writing the start of a tag (§670), followed by its attributes (§679), and then close the empty-element tag (§673).

```
procedure XMLOutStreamObj.Out_XElWithPos(const fEl: string; const fPos: Position);
  begin Out_XElStart(fEl); Out_PosAsAttrs(fPos); Out_XElEnd0;
  end;
```

679. We will want to treat a *position* (i.e., the line and column) as two attributes. We print this out using *Out_PosAsAttrs*. We rely on the *XMLDict*'s *XMLAttrName* for standardizing the name for the line and column.

```
procedure XMLOutStreamObj.Out_PosAsAttrs(const fPos: Position);
  begin Out_XIntAttr(XMLAttrName[atLine], fPos.Line);
  Out_XIntAttr(XMLAttrName[atCol], fPos.Col);
  end;
```

680. We print a quoted attribute, leveraging printing attributes out to the file (§676). We just need to escape the XML string (§643).

```
procedure XMLOutStreamObj.Out_XQuotedAttr(const fAt, fVal: string);
  begin Out_XAttr(fAt, QuoteStrForXML(fVal));
  end;
```

File 15

Vocabulary file dictionaries

681. Mizar works with vocabulary files (suffixed with `.voc`) for introducing new identifiers.

```

⟨dicthan.pas 681⟩ ≡
  ⟨GNU License 4⟩
unit dicthan;
interface
uses mobjects;
  ⟨Public constants for dicthan.pas 682⟩
type SymbolCounters = array [^A .. ^Z] of word;
      SymbolIntSeqArr = array [^A .. ^Z] of IntSequence;
  ⟨Class declarations for dicthan.pas 683⟩
  ⟨Public function declarations for dicthan.pas 684⟩
implementation
uses mizenv, xml_inout, xml_dict;
  ⟨Implementation for dicthan.pas 685⟩
end .

```

682. We recall from Adam Grabowski, Artur Kornilowicz, and Adam Naumowicz’s “Mizar in a Nutshell” (§4.3, [doi:10.6092/issn.1972-5787/1980](https://doi.org/10.6092/issn.1972-5787/1980)), the various prefixes for vocabulary file entries:

- G for structures
- K for left-functor brackets
- L for right-functor brackets
- M for modes
- O for functors
- R for predicates
- U for selectors
- V for attributes

```

⟨Public constants for dicthan.pas 682⟩ ≡
const
  StandardPriority = 64;
  AvailableSymbols = [^G, ^K, ^L, ^M, ^O, ^R, ^U, ^V];

```

This code is used in section 681.

683. There are only three classes in the dictionary handling module. We have an abstraction for a symbol appearing in a vocabulary file, a sort of “checksum” for the counts of symbols appearing in a vocabulary file, and a dictionary associating to each article name (string) a collection of symbols.

```

⟨Class declarations for dicthan.pas 683⟩ ≡
  ⟨Symbol for vocabulary 689⟩;
  ⟨Abstract vocabulary object declaration 698⟩;
  ⟨Vocabulary object declaration 700⟩;

```

This code is used in section 681.

684. \langle Public function declarations for `dicthan.pas` 684 $\rangle \equiv$
function *GetPrivateVoc*(**const** *fName*: *string*): *PVocabulary*;
function *GetPublicVoc* (**const** *fName*: *string*; **var** *fVocFile*: *text*) : *PVocabulary*;
procedure *LoadMmlVcb* (**const** *aFileName*: *string*; **var** *aMmlVcb*: *MStringList*) ;
procedure *StoreMmlVcb*(**const** *aFileName*: *string*; **const** *aMmlVcb*: *MStringList*);
procedure *StoreMmlVcbX*(**const** *aFileName*: *string*; **const** *aMmlVcb*: *MStringList*);

This code is used in section 681.

685. We can test if an entry in the dictionary is valid. Remember, only functor symbols can have a priority associated with it (and a priority is a number between 0 and $2^8 - 1$, inclusive).

Also remember, that a symbol in a dictionary entry **cannot** have whitespaces in it.

define *delete_prefix* \equiv *Delete*(*lLine*, 1, 1)

\langle Implementation for `dicthan.pas` 685 $\rangle \equiv$
function *IsValidSymbol*(**const** *aLine*: *string*): *boolean*;
var *lLine*: *string*; *lKind*: *char*; *lPriority*, *lPos*, *lCode*: *integer*;
begin *IsValidSymbol* \leftarrow *false*; *lLine* \leftarrow *TrimString*(*aLine*);
 \langle Initialize *lKind*, but exit if dictionary line contains invalid symbol 686 \rangle ;
delete_prefix;
case *lKind* **of**
 'O' : \langle Check if functor symbol is valid 687 \rangle ;
 'R' : \langle Check if predicate symbol is valid 688 \rangle ;
othercases **begin** **if** *Pos*('\u00a0' , *lLine*) > 0 **then** *exit*;
IsValidSymbol \leftarrow *true*;
end;
endcases;
end;

See also sections 690, 694, 699, 701, 705, 707, and 708.

This code is used in section 681.

686. An “invalid” line in the dictionary file would be empty lines (whose length is less than one), and lines which do not start with a valid prefix. At the end of this chunk, the *lKind* should be initialized to the prefix of the line.

\langle Initialize *lKind*, but exit if dictionary line contains invalid symbol 686 $\rangle \equiv$
if *length*(*lLine*) \leq 1 **then** *exit*;
lKind \leftarrow *lLine*[1];
if \neg (*lKind* \in *AvailableSymbols*) **then** *exit*

This code is used in section 685.

687. Recall the [specification](#) for *Val* sets *lCode* to zero for success, and the nonzero values store the index where the string is not a numeric value.

We copy the identifier (as determined from the start of the line until, but not including, the index of the first space in the line) and throw away everything after the first whitespace.

When the identifier for the functor symbol is not an empty string *and* the priority can be determined unambiguously, then the functor symbol entry is valid. Otherwise it is invalid.

```

< Check if functor symbol is valid 687 > ≡
  begin IsValidSymbol ← true; lPos ← Pos(‘␣’, lLine);
  if lPos ≠ 0 then
    begin { Parse priority for symbol }
      val(TrimString(Copy(lLine, lPos, length(lLine))), lPriority, lCode);
      lLine ← TrimString(Copy(lLine, 1, lPos − 1)); IsValidSymbol ← (lCode = 0) ∧ (lLine ≠ ‘’);
    end;
  end
end

```

This code is used in section [685](#).

688. A predicate entry in the dictionary file should not include a priority, nor should it include any whitespaces. This is the criteria for a valid predicate symbol entry in the dictionary.

We enforce this by finding the first “␣” character in the line. If there is one, then we trim both sides of the line (removing leading and trailing whitespace). We should have no more spaces in the line. If there is a space, then it is an invalid predicate symbol.

```

< Check if predicate symbol is valid 688 > ≡
  begin lPos ← Pos(‘␣’, lLine);
  if lPos ≠ 0 then { lLine contains a space }
    begin lLine ← TrimString(Copy(lLine, lPos, length(lLine)));
    if Pos(‘␣’, lLine) > 0 then exit;
    end;
  IsValidSymbol ← true;
  end
end

```

This code is used in section [685](#).

689. TSymbol. These are used in `kernel/accdict.pas`. The *Kind* is its one-letter kind (discussed in [§682](#)), and *Repr* is its lexeme. For functors, its priority is stored as its *Prior*.

The “infinite” appears to be only used for predicates.

```

< Symbol for vocabulary 689 > ≡
  PSymbol = ↑TSymbol;
  TSymbol = object (MObject)
    Kind: char;
    Repr, Infinitive: string;
    Prior: byte;
    constructor Init(fKind: char; fRepr, fInfinitive: string; fPriority: byte);
    constructor Extract(const aLine: string);
    function SymbolStr: string;
    constructor Load(var aText: text);
    procedure Store(var aText: text);
    destructor Done; virtual;
  end
end

```

This code is used in section [683](#).

690. Constructor. Given the “kind”, its “representation” and “infinitive”, and its priority (as a number between 0 and 255), we can construct a symbol.

⟨Implementation for `dicthan.pas` 685⟩ +≡

```
constructor TSymbol.Init(fKind : char; fRepr, fInfinitive : string; fPriority : byte);
  begin Kind ← fKind; Repr ← fRepr; Prior ← fPriority; Infinitive ← ``;
end;
```

691. Constructor. When we want to extract a symbol from a line in the dictionary file, care must be taken for functors (since they may contain an explicit priority) and for predicates. Predicates have an undocumented feature to allow “infinitives”, so an acceptable predicate line in a dictionary may look like

`Rpredicate infinitive`

Although what Mizar does with infinitives, I do not know...

```
constructor TSymbol.Extract(const aLine : string);
  var lPos, lCode : integer; lRepr : string;
  begin Kind ← aLine[1]; Repr ← TrimString(Copy(aLine, 2, length(aLine))); Prior ← 0;
  Infinitive ← ``;
  case Kind of
    '0': begin lPos ← Pos('□', Repr); Prior ← StandardPriority;
      if lPos ≠ 0 then ⟨Initialize explicit priority for functor entry in dictionary 693⟩;
      end;
    'R': begin lPos ← Pos('□', Repr);
      if lPos ≠ 0 then ⟨Initilize explicit infinitive for a predicate entry in dictionary 692⟩;
      end;
  endcases;
end;
```

692. Predicates can have an optional infinitive, separated from the lexeme by a single whitespace. It remains unclear what Mizar uses predicate infinitives for, but it is a feature. This is written out to the `.vcx` file, according to `xml_dict.pas`.

Note that there are 4 predicates with infinitives in Mizar:

- (1) `jumps_in` (infinitive: `jump_in`) occurs in the article `AMISTD_1`
- (2) `halts_in` (infinitive: `halt_in`) occurs in the article `EXTPRO_1`
- (3) `refers` (infinitive: `refer`) occurs in the article `SCMFSA7B`
- (4) `destroys` (infinitive: `destroy`) occurs in the article `SCMFSA7B`

⟨Initilize explicit infinitive for a predicate entry in dictionary 692⟩ ≡

```
begin lRepr ← Repr; Repr ← ``; Repr ← TrimString(Copy(lRepr, 1, lPos - 1));
  Infinitive ← TrimString(Copy(lRepr, lPos + 1, length(lRepr)));
end
```

This code is used in section 691.

693. Functors with explicit priorities require parsing that priority. It is assumed that a single whitespace separates the lexeme from the priority.

⟨Initialize explicit priority for functor entry in dictionary 693⟩ ≡

```
begin lRepr ← Repr; Repr ← ``;
  val (TrimString(Copy(lRepr, lPos + 1, length(lRepr))), Prior, lCode); { Store the priority }
  Repr ← TrimString(Copy(lRepr, 1, lPos - 1)); { Store the lexeme }
end
```

This code is used in section 691.

694. Serialize symbols. We can serialize a *TSymbol* object, which produces the sort of entry we'd expect to find in a dictionary. So we would have the symbol kind, the lexeme, and optional data (non-default priorities for functors, infinitives for predicates).

(Implementation for `dicthan.pas` 685) \equiv

```
function TSymbol.SymbolStr: string;
  var lStr, lntStr: string;
  begin lStr  $\leftarrow$  Kind + Repr;
  case Kind of
    'O': if Prior  $\neq$  StandardPriority then
      begin Str(Prior, lntStr); lStr  $\leftarrow$  lStr + '□' + lntStr;
      end;
    'R': if Infinitive  $\neq$  '' then lStr  $\leftarrow$  lStr + '□' + Infinitive;
  endcases;
  SymbolStr  $\leftarrow$  lStr;
end;
```

695. Given a text (usually the contents of a vocabulary file), we read in a line. When the line is a nonempty string, we initialize the lexeme representation, priority, and infinitives. Then, when the dictionary entry describes a valid symbol (§685), we populate the fields of the *TSymbol*.

```
constructor TSymbol.Load(var aText : text);
  var lDictLine: string;
  begin ReadLn(aText, lDictLine); lDictLine  $\leftarrow$  TrimString(lDictLine);
  if length(lDictLine) = 0 then exit;
  Repr  $\leftarrow$  ''; Prior  $\leftarrow$  0; Infinitive  $\leftarrow$  '';
  if IsValidSymbol(lDictLine) then Extract(lDictLine);
end;
```

696. Storing a *TSymbol* in a file amounts to writing its serialization (§694) to the file.

```
procedure TSymbol.Store(var aText : text);
  begin WriteLn(aText, SymbolStr);
end;
```

697. Destructor. We just reset the lexeme and infinitive strings to be empty strings.

```
destructor TSymbol.Done;
  begin Repr  $\leftarrow$  ''; Infinitive  $\leftarrow$  '';
end;
```

698. Abstract vocabulary objects. This is used in `kernel/impobjs.pas`. We recall (§681) that the *SymbolCounters* are just an enumerated type consisting of a single uppercase Latin Letter.

(Abstract vocabulary object declaration 698) \equiv

```
AbsVocabularyPtr =  $\uparrow$ AbsVocabularyObj;
AbsVocabularyObj = object (MObject)
  fSymbolCnt: SymbolCounters;
  constructor Init;
  destructor Done; virtual;
end
```

This code is used in section 683.

699. We only have the constructor and destructor for abstract vocabulary objects.

```

⟨Implementation for dicthan.pas 685⟩ +≡
constructor AbsVocabularyObj.Init;
  begin FillChar(fSymbolCnt, SizeOf(fSymbolCnt), 0);
  end;
destructor AbsVocabularyObj.Done;
  begin end;

```

700. Vocabulary objects. A “vocabulary object” is just a collection of *PSymbols* read in from a vocabulary file.

These are also used in **kernel/accdict.pas**.

```

⟨Vocabulary object declaration 700⟩ ≡
PVocabulary = ↑TVocabulary;
TVocabulary = object (AbsVocabularyObj)
  Reprs: MCollection;
  constructor Init;
  constructor ReadPrivateVoc(const aFileName: string);
  constructor LoadVoc(var aText : text);
  procedure StoreVoc (const aFileName: string; var aText: text );
  destructor Done; virtual;
end

```

This code is used in section 683.

701. Constructor (Empty vocabulary). We can construct the empty vocabulary by just initializing the underlying collection.

```

⟨Implementation for dicthan.pas 685⟩ +≡
constructor TVocabulary.Init;
  begin FillChar(fSymbolCnt, SizeOf(fSymbolCnt), 0); Reprs.Init(10, 10);
  end;

```

702. Destructor. We only need to free up the underlying collection.

```

destructor TVocabulary.Done;
  begin Reprs.Done;
  end;

```

703. Constructor. We can read from a private vocabulary file.

```

constructor TVocabulary.ReadPrivateVoc(const aFileName: string);
  var lDict: text; lDictLine: string; lSymbol: PSymbol;
  begin Init; Assign(lDict, aFileName);
  without_io_checking(reset(lDict));
  if ioresult ≠ 0 then exit; { file is not ready to be read, bail out! }
  while ¬seekEOF(lDict) do ⟨Read line into vocabulary from dictionary file 704⟩;
  Close(lDict);
end;

```

704. When reading dictionary lines into a vocabulary file, we skip over blank lines. Further, we only read *valid* entries into the vocabulary.

```

⟨ Read line into vocabulary from dictionary file 704 ⟩ ≡
  begin readln(lDict, lDictLine); lDictLine ← TrimString(lDictLine);
  if length(lDictLine) > 1 then { if dictionary line is not blank }
    begin lSymbol ← new(PSymbol, Extract(lDictLine));
    if IsValidSymbol(lDictLine) then { add the symbol }
      begin inc(fSymbolCnt[lSymbol↑.Kind]); Reprs.Insert(lSymbol); end;
    end;
  end
end

```

This code is used in section 703.

705. Constructor. We can read in the vocabulary from a file. If I am not mistaken, this is usually from `mml.vct`. We have the first line look like “G3 K0 L0 M1 07 R2 U4 V6”, which enumerates the number of different types of definitions appearing in an article.

```

⟨ Implementation for dicthan.pas 685 ⟩ +≡
constructor TVocabulary.LoadVoc(var aText : text);
  var i, lSymbNbr, lNbr: integer; lKind, lDummy, c: Char;
  begin lSymbNbr ← 0; ⟨ Count lNbr the number of dictionary entries for an article 706 ⟩;
  ReadLn(aText); Reprs.Init(10, 10);
  for i ← 1 to lSymbNbr do
    begin Reprs.Insert(new(PSymbol, Load(aText)));
    end;
  end;
end;

```

706. Since the first line counts the different sorts of definitions appearing in the article, we can parse the numbers, then add them up. This initializes the *fSymbolCnt* entry for *c*.

```

⟨ Count lNbr the number of dictionary entries for an article 706 ⟩ ≡
  for c ← 'A' to 'Z' do
    if c ∈ AvailableSymbols then
      begin Read(aText, lKind, lNbr, lDummy); fSymbolCnt[c] ← lNbr; Inc(lSymbNbr, fSymbolCnt[c]);
      end
    end
  end

```

This code is used in section 705.

707. Storing a dictionary entry. This appends to a `.vct` file the entries for an article. Specifically, this is just the “#ARTICLE” and then the counts of the different kinds of definitions.

```

⟨ Implementation for dicthan.pas 685 ⟩ +≡
procedure TVocabulary.StoreVoc (const aFileName: string; var aText: text );
  var i: Byte; c: Char;
  begin WriteLn(aText, '#', aFileName);
  for c ← 'A' to 'Z' do
    if c ∈ AvailableSymbols then Write(aText, c, fSymbolCnt[c], ' ');
  WriteLn(aText);
  for i ← 0 to Reprs.Count - 1 do PSymbol(Reprs.Items↑[i])↑.Store(aText);
  end;
end;

```

708. Miscellaneous public-facing functions.

⟨Implementation for `dicthan.pas` 685⟩ +≡

```
function GetPrivateVoc(const fName: string): PVocabulary;
  var lName: string;
  begin lName ← fName;
  if ExtractFileExt(lName) = `` then lName ← lName + `'.voc`;
  if ¬MFileExists(lName) then
    begin GetPrivateVoc ← nil; exit;
    end;
  GetPrivateVoc ← new(PVocabulary, ReadPrivateVoc(lName));
end;
```

709. Reading mml.vct entries. The `$MIZFILES/mml.vct` file contains all the vocabularies concatenated together into one giant vocabulary file. It uses lines prefixed with “#” followed by the article name to separate the vocabularies from different files. We search for the given article name (stored in the *fName* argument). When we find it, we construct the Vocabulary object (§705).

```
function GetPublicVoc (const fName: string; var fVocFile: text ) : PVocabulary;
  var lLine: string;
  begin GetPublicVoc ← nil; reset(fVocFile);
  while ¬eof(fVocFile) do
    begin readln(fVocFile, lLine);
    if (length(lLine) > 0) ∧ (lLine[1] = `#`) ∧ (copy(lLine, 2, length(lLine)) = fName) then
      begin GetPublicVoc ← new(PVocabulary, LoadVoc(fVocFile)); exit;
      end;
    end;
  end;
```

710. Reading from mml.vct. This function is used by `libtools/checkvoc.dpr` and in a couple user tools. In those other functions, they pass `$MIZFILES/mml.vct` as the value for *aFileName*. This procedure will then populate the *aMmlVcb* file associating to each article name its vocabulary.

```
procedure LoadMmlVcb (const aFileName: string; var aMmlVcb: MStringList ) ;
  var lFile: text; lDummy: char; lDictName: string; r: Integer;
  begin FileExam(aFileName); Assign(lFile, aFileName); Reset(lFile); { initialize file for reading }
  aMmlVcb.Init(1000); aMmlVcb.fSorted ← true;
  while ¬eof(lFile) do
    begin ReadLn(lFile, lDummy, lDictName);
    r ← aMmlVcb.AddObject(lDictName, new(PVocabulary, LoadVoc(lFile)));
    end;
  Close(lFile);
end;
```

711. Storing a vocabulary delegates much work (§707). However, since *fCount* is not initialized, I am uncertain how this works, exactly... Furthermore, this function is not used anywhere in Mizar.

```
procedure StoreMmlVcb(const aFileName: string; const aMmlVcb: MStringList);
  var lFile: text; i: Integer;
  begin Assign(lFile, aFileName); Rewrite(lFile);
  with aMmlVcb do
    for i ← 0 to fCount − 1 do PVocabulary(fList↑[i].fObject)↑.StoreVoc(fList↑[i].fString↑, lFile);
  Close(lFile);
end;
```

712. Like *StoreMmlVcb*, this function is not used anywhere in Mizar. This appears to produce the XML-equivalent to the previous function.

```
procedure StoreMmlVcbX (const aFileName: string; const aMmlVcb: MStringList);
  var i, s: Integer; c: char; VCXfile: XMLOutputStreamPtr;
  begin VCXfile ← new(XMLOutputStreamPtr, OpenFile(aFileName));
    VCXfile.Out_XElStart0(XMLElemName[elVocabularies]);
    with aMmlVcb do
      for i ← 0 to fCount − 1 do
        with PVocabulary(fList↑[i].fObject)↑ do
          begin VCXfile.Out_XElStart(XMLElemName[elVocabulary]);
            VCXfile.Out_XAttr(XMLAttrName[atName], fList↑[i].fString↑); VCXfile.Out_XAttrEnd;
            ⟨ Write vocabulary counts to XML file 713 ⟩;
            ⟨ Write symbols to vocabulary XML file 714 ⟩;
            VCXfile.Out_XElEnd(XMLElemName[elVocabulary]);
          end;
        VCXfile.Out_XElEnd(XMLElemName[elVocabularies]); dispose(VCXfile, Done);
      end;
```

713. We write out the counts of each kind of definition appearing in the article.

```
⟨ Write vocabulary counts to XML file 713 ⟩ ≡
  { Kinds }
  for c ← ‘A’ to ‘Z’ do
    if c ∈ AvailableSymbols then
      begin VCXfile.Out_XElStart(XMLElemName[elSymbolCount]);
        VCXfile.Out_XAttr(XMLAttrName[atKind], c);
        VCXfile.Out_XIntAttr(XMLAttrName[atNr], fSymbolCnt[c]); VCXfile.Out_XElEnd0;
      end
```

This code is used in section 712.

714. We write out each symbol appearing in the article’s vocabulary.

```
⟨ Write symbols to vocabulary XML file 714 ⟩ ≡
  { Symbols }
  VCXfile.Out_XElStart0(XMLElemName[elSymbols]);
  for s ← 0 to Reprs.Count − 1 do
    with PSymbol(Reprs.Items[s])↑ do
      begin VCXfile.Out_XElStart(XMLElemName[elSymbol]);
        VCXfile.Out_XAttr(XMLAttrName[atKind], Kind);
        VCXfile.Out_XAttr(XMLAttrName[atName], QuoteStrForXML(Repr));
        case Kind of
          ‘O’: VCXfile.Out_XIntAttr(XMLAttrName[atPriority], Prior);
          ‘R’: if Infinitive ≠ ‘’ then VCXfile.Out_XAttr(XMLAttrName[atInfinitive], Infinitive);
        end; VCXfile.Out_XElEnd0;
      end;
    VCXfile.Out_XElEnd(XMLElemName[elSymbols])
```

This code is used in section 712.

File 16

Scanner

715. The `scanner.pas` file contains the *MTokeniser* and the *MScanner*.

It is worth noting: if we want to extend Mizar to support Unicode, then we would want to hack this file accordingly. Or create a `utf8scanner` module, whichever. This scanner class is built specifically to work with ASCII characters, specifically accepting printable characters and the space (“`␣`”) characters as valid input.

```

< scanner.pas 715 > ≡
  < GNU License 4 >
unit scanner;
  interface ;
  uses errhan, mobjects;
  const MaxLineLength = 80;
    MaxConstInt = 2147483647; { = 231 - 1, maximal signed 32-bit integer }
  < Type declarations for scanner 716 >
implementation
  uses mizenv, librenv, mconsole, xml_dict, xml_inout;
  < Implementation for scanner.pas 717 >
end .

```

See also section 846.

716. Note that a *LexemRec* is really a standardized token. I was always raised to believe that a “lexeme” refers to the literal text underlying a token.

```

< Type declarations for scanner 716 > ≡
type ASCIIArr = array [chr(0) .. chr(255)] of byte;
  LexemRec = record Kind: char;
    Nr: integer;
  end;
  < Token object class 718 >;
  < Tokens collection class 720 >;
  < MToken object class 728 >;
  < MTokeniser class 731 >;
  < MScanner object class 759 >;

```

This code is used in section 715.

717. The “default allowed” characters are the 10 decimal digits, the 26 uppercase Latin letters, the 26 lowercase Latin letters, and the underscore (“_”) character.

⟨Implementation for scanner.pas 717⟩ ≡

```
var DefaultAllowed: AsciiArr =
  (0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
   0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
   0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0, 0, 0, 0, 1,
   { ' _ ' allowed in identifiers by default! }
  0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0, 0, 0, 0, 0,
  0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
  0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
  0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
  0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
  0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0);
```

See also sections 719, 721, 722, 723, 726, 727, 729, 730, 732, 735, 736, 740, 755, 756, 758, 760, 769, 770, 771, 772, and 773.

This code is used in section 715.

718. Tokens object. A token contains a lexeme, but it extends an *MStr* object.

⟨Token object class 718⟩ ≡

```
TokenPtr = ↑TokenObj;
TokenObj = object (MStrObj)
  fLexem: LexemRec;
  constructor Init(aKind: char; aNr: integer; const aSpelling: string);
end
```

This code is used in section 716.

719. The constructor for a token requires its kind (functor, mode, predicate, etc.), and its internal “number”, as well as its raw lexeme *aSpelling*.

⟨Implementation for scanner.pas 717⟩ +≡

```
constructor TokenObj.Init(aKind: char; aNr: integer; const aSpelling: string);
begin fLexem.Kind ← aKind; fLexem.Nr ← aNr; fStr ← aSpelling;
end;
```

Section 16.1. COLLECTIONS OF TOKENS

720. We can populate a token collection from a dictionary file, or we can start with an empty collection. We can save our collection to a file. We can also insert (or “collect”) a new token into the collection.

⟨Tokens collection class 720⟩ ≡

```
TokensCollection = object (MSortedStrList)
  fFirstChar: array [chr(30) .. chr(255)] of integer;
  constructor InitTokens;
  constructor LoadDct(const aDctFileName: string);
  procedure SaveDct(const aDctFileName: string);
  procedure SaveXDct(const aDctFileName: string);
  function CollectToken(const aLexem: LexemRec; const aSpelling: string): boolean;
end
```

This code is used in section 716.

721. Construct empty token collection.

⟨Implementation for scanner.pas 717⟩ +≡

```
constructor TokensCollection.InitTokens;
  begin Init(100);
end;
```

722. Insert. If the collection already contains the token described by *aLexem*, then we just free up the memory allocated for the token (avoid duplicates). Otherwise, we insert the token.

⟨Implementation for scanner.pas 717⟩ +≡

```
function TokensCollection.CollectToken(const aLexem: LexemRec; const aSpelling: string): boolean;
  var k: integer; lToken: TokenPtr;
  begin lToken ← new(TokenPtr, Init(aLexem.Kind, aLexem.Nr, aSpelling));
  if Search(lToken, k) then { already contains token? }
    begin CollectToken ← false; dispose(lToken, Done)
    end
  else begin CollectToken ← true; Insert(lToken)
  end
end;
```

723. Load a dictionary. We open the dictionary “.dct” file (expects the file name to be lacking that extension), and construct an empty token collection. Then we iterate through the dictionary, reading each line, forming a new token, then inserting it into the collection.

The “.dct” file contains all the identifiers from articles referenced in the **environ** part of an article, and it will always have the first 148 lines be for reserved keywords. The format for a “.dct” file consists of lines of the form

$$\langle kind \rangle \langle number \rangle \sqcup \langle name \rangle$$

The “kind” is a single byte, the *number* is an integer assigned for the identifier, and *name* is the lexeme (string literal) for the identifier. This also has an XML file for this same information, the “.dcx” file.

⟨Implementation for scanner.pas 717⟩ +≡

```
constructor TokensCollection.LoadDct(const aDctFileName: string);
  var Dct: text; lKind, lDummy: AnsiChar; lNr: integer; lString: string; i: integer; c: char;
  begin assign(Dct, aDctFileName + ‘.dct’); reset(Dct); InitTokens;
  ⟨Load all tokens from the dictionary 724⟩;
  close(Dct); ⟨Index first character appearances among definitions 725⟩;
end;
```


724. We just iterate through the dictionary, constructing a new token for each line we read.

```

⟨Load all tokens from the dictionary 724⟩ ≡
  while ¬seekEof(Dct) do
    begin readln(Dct, lKind, lNr, lDummy, lString);
           Insert(new(TokenPtr, Init(char(lKind), lNr, lString)));
    end

```

This code is used in section 723.

725. We index the first appearance of each leading character in a token.

```

⟨Index first character appearances among definitions 725⟩ ≡
  for c ← chr(30) to chr(255) do fFirstChar[c] ← -1;
  for i ← 0 to Count - 1 do
    begin c ← TokenPtr(Items↑[fIndex↑[i]]↑.fStr[1];
           if fFirstChar[c] = -1 then fFirstChar[c] ← i;
    end

```

This code is used in section 723.

726. We save a token collection to a “.dct” file. This appears to just produce the concatenation of the definition kind, the identifier number, then a whitespace separating it from the lexeme. **Caution:** this is *not* an XML format! For that, see *SaveDctX*.

```

⟨Implementation for scanner.pas 717⟩ +≡
procedure TokensCollection.SaveDct(const aDctFileName: string);
  var i: integer; DctFile: text;
  begin assign(DctFile, aDctFileName + ‘.dct’); rewrite(DctFile);
  for i ← 0 to Count - 1 do
    with TokenPtr(Items↑[i])↑, fLexem do writeln(DctFile, AnsiChar(Kind), Nr, ‘ ’, fStr);
  close(DctFile);
end;

```

727. Save dictionary to XML file. The RNC (compact Relax NG Schema): Local dictionary for an article. The symbol kinds still use very internal notation.

```

elSymbols =
  attribute atAid {xsd:string}?,
  element elSymbols {
    element elSymbol {
      attribute atKind {xsd:string},
      attribute atNr {xsd:integer},
      attribute atName {xsd:integer}
    }*
  }

```

This creates the .dct file for an article.

⟨Implementation for scanner.pas 717⟩ +≡

```

procedure TokensCollection.SaveXDct(const aDctFileName: string);
var lEnvFile: XMLOutStreamObj; i: integer;
begin lEnvFile.OpenFile(aDctFileName);
with lEnvFile do
  begin Out_XElStart(XMLElemName[elSymbols]); Out_XAttr(XMLAttrName[atAid], ArticleID);
    Out_XQuotedAttr(XMLAttrName[atMizfiles], MizFiles);
    Out_XAttrEnd; { print elSymbols start-tag }
  for i ← 0 to Count − 1 do { print children elSymbol elements }
    with TokenPtr(Items↑[i])↑, fLexem do
      begin Out_XElStart(XMLElemName[elSymbol]);
        Out_XQuotedAttr(XMLAttrName[atKind], Kind); Out_XIntAttr(XMLAttrName[atNr], Nr);
        Out_XQuotedAttr(XMLAttrName[atName], fStr); Out_XElEnd0;
      end;
    Out_XElEnd(XMLElemName[elSymbols]); { print elSymbols end-tag }
  end;
lEnvFile.Done;
end;

```

Section 16.2. MIZAR TOKEN OBJECTS

728. This appears to be tokens for a specific file. An MToken extends a Token (§718).

```

⟨ MToken object class 728 ⟩ ≡
  MTokenPtr = ↑MTokenObj;
  MTokenObj = object (TokenObj)
    fPos: Position;
    constructor Init(aKind : char; aNr : integer ; const aSpelling: string; const aPos: Position);
  end

```

This code is used in section 716.

729. Constructor. Construct a token. This might be a tad confusing, at least for me, because the lexeme is stored in the *fStr* field, whereas the standardized token is stored in the *fLexem* field.

We do not need to invoke the constructor for any ancestor class, because we just construct everything here. This seems like a bug waiting to happen. . .

```

⟨ Implementation for scanner.pas 717 ⟩ +≡
constructor MTokenObj.Init(aKind : char; aNr : integer;
  const aSpelling: string;
  const aPos: Position);
begin fLexem.Kind ← aKind; fLexem.Nr ← aNr; fStr ← aSpelling; fPos ← aPos;
end;

```

730. Token Kind constants. There are four kinds of tokens we want to distinguish: all valid tokens are either (1) numerals, or (2) identifiers. Then we also have (3) error tokens. But last, we have (4) end of text tokens.

These are for identifying everything which is neither an identifier defined in the vocabulary files, nor a reserved keyword.

```

⟨ Implementation for scanner.pas 717 ⟩ +≡
const Numeral = 'N'; Identifier = 'I'; ErrorSymbol = '?'; EOT = '!';

```

Section 16.3. TOKENISER

731. The first step in lexical analysis is to transform a character stream into a token stream. The Tokeniser extends the MToken object (§728), which in turn extends the Token object (§718).

In particular, we should take a moment to observe the new fields. The *fPhrase* field is a segment of the input stream which is expected to start at a non-whitespace character.

The *SliceIt* function populates the *TokensBuf* and the *fIdents* fields from the *fPhrase* field. I cannot find where *fTokens* is populated.

Note that the MTokeniser is not, itself, used anywhere *directly*. It's extended in the *MScannObj* class, which is used in `base/mscanner.pas` (and in `kernel/envhan.pas`).

The contract for *GetPhrase* ensures the *fPhrase* will be populated with a string ending with a space (“ ”) character or it will be the empty string. Any class extending *MTokeniser* must respect this contract.

⟨ MTokeniser class 731 ⟩ ≡

```

MTokeniser = object (MTokenObj)
  fPhrase: string;
  fPhrasePos: Position;
  fTokensBuf: MCollection;
  fTokens, fIdents: TokensCollection;
  constructor Init;
  destructor Done; virtual;
  procedure SliceIt; virtual;
  procedure GetToken; virtual;
  procedure GetPhrase; virtual;
  function EndOfText: boolean; virtual;
  function IsIdentifierLetter(ch : char): boolean; virtual;
  function IsIdentifierFirstLetter(ch : char): boolean; virtual;
  function Spelling(const aToken: LexemRec): string; virtual;
end

```

This code is used in section 716.

732. Spelling boils down to three cases (c.f., types of tokens §730): numerals, identifiers, and everything else. Numerals spell out the base-10 decimal expansion.

The other two cases boil down to finding the first matching token in the caller's collection of tokens with the same lexeme supplied as an argument, provided certain ‘consistency’ checks hold (the lexeme and token have the same *Kind*).

⟨ Implementation for scanner.pas 717 ⟩ +≡

```

function MTokeniser.Spelling(const aToken: LexemRec): string;
  var i: integer; s: string;
  begin Spelling ← ``;
  if aToken.Kind = Numeral then
    begin Str(aToken.Nr, s); Spelling ← s; end
  else if aToken.Kind = Identifier then ⟨ Spell an identifier for the MTokeniser 733 ⟩
    else ⟨ Spell an error or EOF for the MTokeniser 734 ⟩;
  end;

```

733. Spelling an identifier just needs to match the lexeme's number with the token's number. This finds the first matching token in the underlying collection, then terminates the function.

```

⟨ Spell an identifier for the MTokeniser 733 ⟩ ≡
  begin for  $i \leftarrow 0$  to  $fIdents.Count - 1$  do
    with  $TokenPtr(fIdents.Items \uparrow [i]) \uparrow$  do
      if  $fLexem.Nr = aToken.Nr$  then
        begin  $Spelling \leftarrow fStr$ ; exit
        end;
      end
    end
  end

```

This code is used in section 732.

734. Spelling anything else for the tokeniser needs the kind and number of the lexeme to match those of the token. Again, this finds the first matching token in the underlying collection, then terminates the function.

```

⟨ Spell an error or EOF for the MTokeniser 734 ⟩ ≡
  begin for  $i \leftarrow 0$  to  $fTokens.Count - 1$  do
    with  $TokenPtr(fTokens.Items \uparrow [i]) \uparrow$  do
      if  $(fLexem.Kind = aToken.Kind) \wedge (fLexem.Nr = aToken.Nr)$  then
        begin  $Spelling \leftarrow fStr$ ; exit
        end;
      end
    end
  end

```

This code is used in section 732.

735. Constructor. Initialising a tokeniser starts with a blank phrase and kind, with most fields set to zero.

```

⟨ Implementation for scanner.pas 717 ⟩ +≡
constructor MTokeniser.Init;
  begin  $fPos.Line \leftarrow 0$ ;  $fLexem.Kind \leftarrow \text{~}\sqcup\text{~}$ ;  $fPhrase \leftarrow \text{~}\sqcup\sqcup\text{~}$ ;  $fPhrasePos.Line \leftarrow 0$ ;
     $fPhrasePos.Col \leftarrow 0$ ;  $fTokensBuf.Init(80, 8)$ ;  $fTokens.Init(0)$ ;  $fIdents.Init(100)$ ;
  end;

```

736. Destructor. This chains to free up several fields, just invoking their destructors.

```

⟨ Implementation for scanner.pas 717 ⟩ +≡
destructor MTokeniser.Done;
  begin  $fPhrase \leftarrow \text{~}\text{~}$ ;  $fTokensBuf.Done$ ;  $fTokens.Done$ ;  $fIdents.Done$ ;
  end;

```

737. Aside on ASCII separators. Note: $\text{chr}(30)$ is the record separator in ASCII, and $\text{chr}(31)$ is the unit separator. Within a group (or table), the records are separated with the “RS” ($\text{chr}(30)$). As far as unit separators, Lammer Bies explains (lammertbies.nl/comm/info/ascii-characters):

The smallest data items to be stored in a database are called units in the ASCII definition. We would call them field now. The unit separator separates these fields in a serial data storage environment. Most current database implementations require that fields of most types have a fixed length. Enough space in the record is allocated to store the largest possible member of each field, even if this is not necessary in most cases. This costs a large amount of space in many situations. The US control code allows all fields to have a variable length. If data storage space is limited—as in the sixties—this is a good way to preserve valuable space. On the other hand is serial storage far less efficient than the table driven RAM and disk implementations of modern times. I can’t imagine a situation where modern SQL databases are run with the data stored on paper tape or magnetic reels...

We will introduce macros for the record separator and the unit separator, because Mizar’s front-end uses them specifically for the following purposes:

- (1) lines longer than 80 characters will contain a *record_separator* character (§764);
- (2) all other invalid characters are replaced with the *unit_separator* character (c.f., §765).

define *record_separator* $\equiv \text{chr}(30)$

define *unit_separator* $\equiv \text{chr}(31)$

738. Example of zeroeth step (“getting a phrase”) in tokenising. The *GetPhrase* function is left as an abstract method of the tokeniser, so it is worth discussing “What it is supposed to do” before getting to the tokenisation of strings.

Suppose we have the following snippet of Mizar:

```
begin

theorem
  for x being object
    holds x= x;
```

This is “sliced up” into the following “phrases” (drawn in boxes) which are clustered by lines:

```
begin_
theorem_
  for_ x_ being_ object_
  holds_ x=_ x;_
```

Observe that the “phrases” are demarcated by whitespaces (“_␣”) or linebreaks. This is the coarse “first pass” before we carve a “phrase” up into a token. A phrase contains at least one token, possibly multiple tokens (e.g., the phrase “x=_” contains the two tokens “x” and “=”).

What is the contract for a “phrase”? A phrase is *guaranteed* to either be equal to “_␣”, or it contains at least one token and it is *guaranteed* to end with a space “_␣” character (ASCII code #32). Further, there are no other possible “_␣” characters in a phrase *except* at the very end. A phrase is never an empty string.

The task is then to *slice up* each phrase into tokens.

739. Tokenise a phrase. When a “phrase” has been loaded into the tokeniser (which is an abstract method implemented by its descendent classes), we tokenise it — “slice it up” into tokens, thereby populating the *fTokensBuf* tokens buffer. This is invoked as needed by the *GetToken* method (§756).

This function is superficially complex, but upon closer scrutiny it is fairly straightforward.

Also note, despite being marked as “virtual”, this is not overridden anywhere in the Mizar program.

The contract ensures, barring catastrophe, the *fLexem*, *fStr*, and *fPos* be populated. **Importantly:** The *fLexem*’s token type is one of the four kinds given in the constant section (§730): **Numeral**, **Identifier**, **ErrorSymbol**, or **EOT**. What about the “reserved keywords” of Mizar? They are already present in the “.dct” file, which is loaded into the *fTokens* dictionary. So they will be discovered in step (§746) in this procedure.

```

⟨ Variables for slicing a phrase 739 ⟩ ≡
lCurrChar: integer; { index in fPhrase for current position }
EndOfSymbol: integer;
EndOfIdent: integer; { index in fPhrase for end of identifier }
FoundToken: TokenPtr; { most recently found token temporary variable }
lPos: Position; { position for debugging purposes }

```

See also sections 742, 745, 748, 750, and 752.

This code is used in section 740.

740. ⟨ Implementation for scanner.pas 717 ⟩ +≡

```

procedure MTokeniser.SliceIt;
  var ⟨ Variables for slicing a phrase 739 ⟩
  begin MizAssert(2333, fTokensBuf.Count = 0); { Requires: token buffer is empty }
  lCurrChar ← 1; lPos ← fPhrasePos;
  ⟨ Slice pragmas 741 ⟩;
  while fPhrase[lCurrChar] ≠ ‘␣’ do
    begin ⟨ Determine the ID 743 ⟩;
    ⟨ Try to find a dictionary symbol 746 ⟩;
    if EndOfSymbol < EndOfIdent then ⟨ Check identifier is not a number 749 ⟩;
    if FoundToken ≠ nil then
      with FoundToken↑ do
        begin lPos.Col ← fPhrasePos.Col + EndOfSymbol - 1;
        fTokensBuf.Insert(new(MTokenPtr, Init(fLexem.Kind, fLexem.Nr, fStr, lPos)));
        lCurrChar ← EndOfSymbol + 1; continue;
        end;
      { else FoundToken = nil }
      ⟨ Whoops! We found an unknown token, insert a 203 error token 754 ⟩;
    end;
  end;

```

741. We begin by slicing pragmas. This will insert the pragma into the tokens buffer.

Note that the “\$EOF” pragma indicates that we should treat the file as ending here. So we comply with the request, inserting the *EOT* (end of text) token as the next token to be offered to the user.

```

⟨ Slice pragmas 741 ⟩ ≡
if (lPos.Col = 1) ∧ (Pos(‘:’:$’, fPhrase) = 1) then
  begin fTokensBuf.Insert(new(MTokenPtr, Init(‘␣’, 0, copy(fPhrase, 3, length(fPhrase) - 3), lPos)));
  if copy(fPhrase, 1, 6) = ‘:’:$EOF’ then
    fTokensBuf.Insert(new(MTokenPtr, Init(EOT, 0, fPhrase, lPos)));
  exit
  end

```

This code is used in section 740.

742. We take the longest possible substring consisting of identifier characters as a possible identifier. The phrase is guaranteed to contain at least one token, maybe more, so we just keep going until we have exhausted the phrase or found a non-identifier character.

Note that all invalid characters are transformed into the “unit character” (c.f., §765). We should treat any occurrence of them as an error.

At the end of this stage of our tokenising journey, for valid tokens, we should have *EndOfIdent* and *IdentLength* both initialized here.

⟨ Variables for slicing a phrase 739 ⟩ +≡
IdentLength: integer;

743. ⟨ Determine the ID 743 ⟩ ≡
 { 1. attempt to determine the ID }
EndOfIdent ← *lCurrChar*;
if *IsIdentifierFirstLetter*(*fPhrase*[*EndOfIdent*]) **then**
 while (*EndOfIdent* < *length*(*fPhrase*)) ∧ *IsIdentifierLetter*(*fPhrase*[*EndOfIdent*]) **do**
 inc(*EndOfIdent*);
IdentLength ← *EndOfIdent* − *lCurrChar*;
if *fPhrase*[*EndOfIdent*] ≤ *unit_separator* **then**
 ⟨ Whoops! ID turns out to be invalid, insert an error token, then continue 744 ⟩;
 dec(*EndOfIdent*)

This code is used in section 740.

744. Recall (§764), we treat record separators as indicating the line is “too long” (i.e., more than 80 characters long). So we insert a 201 “Too long source line” error. But anything else is treated as an invalid identifier error.

⟨ Whoops! ID turns out to be invalid, insert an error token, then continue 744 ⟩ ≡
begin *lPos.Col* ← *fPhrasePos.Col* + *EndOfIdent* − 1;
if *fPhrase*[*EndOfIdent*] = *record_separator* **then**
 fTokensBuf.Insert(*new*(*MTokenPtr*, *Init*(*ErrorSymbol*, 200, ‘^’, *lPos*)))
else *fTokensBuf.Insert*(*new*(*MTokenPtr*, *Init*(*ErrorSymbol*, 201, ‘^’, *lPos*)));
 lCurrChar ← *EndOfIdent* + 1; *continue*;
end

This code is used in section 743.

745. We look at the current phrase and try to match against tokens found in the underlying dictionary. When we find a match, we check if there are *multiple* matches and return the last one (this reflects Mizar’s “the last version of the notation is preferred”). We implement this matching scheme using an infinite loop. Note that this uses a “**repeat...until false**” loop, which is identical to “**while true do begin ...end**” loop. (I am tempted to introduce a macro just to have this loop “**repeat...until end_of_time**”...)

Recall (§379), sorted lists have a field *fIndex* which is an array of indices (which are sorted while leaving the underlying array *Items* of data untouched).

Also, *lToken*, *lIndex* are used only in this code chunk. Here *lToken* is translated to an index of the underlying dictionary, so for clarity we introduce a macro to refer to the token directly. And *lIndex* is used as “the current character” index to compare the phrase to the token (indexed by *lToken*) as a match or not.

At the end of this chunk, if successful, then *FoundToken* will be set to a valid token pointer. Further, *EndOfPhrase* will be initialized.

A possible bug: what happens if we look through the entire phrase? We can’t “look any farther” down the phrase, so shouldn’t we throw an error? Or lazily read more characters? Or...something?

Never fear: this will never happen with Mizar’s grammar. The “reserved words” are *always* separated from the other stuff by at least one whitespace.

Also we note the list of symbols is sorted lexicographically.

This appears to match the phrase with the longest possible matching entry in the list of symbols (it is “maximal munch”).

```
define the_item(#)  $\equiv$  Items $\uparrow$ [fIndex $\uparrow$ [#]]
define the_token(#)  $\equiv$  TokenPtr(the_item(#)) $\uparrow$ 
```

⟨ Variables for slicing a phrase 739 ⟩ +≡

EndOfPhrase: integer; { index in *fPhrase* for candidate token }

lIndex: integer; { index for *fIndex* entry }

lToken: integer; { index for entries in dictionary starting with the first character of the current token }

746. Reserved keywords and defined terms are loaded into the *fTokens* dictionary.

⟨ Try to find a dictionary symbol 746 ⟩ ≡

```
EndOfPhrase  $\leftarrow$  lCurrChar; FoundToken  $\leftarrow$  nil; EndOfSymbol  $\leftarrow$  EndOfPhrase - 1;
{ initialized for comparison }
```

```
lToken  $\leftarrow$  fTokens.fFirstChar[fPhrase[EndOfPhrase]]; inc(EndOfPhrase);
```

```
if (lToken  $\geq$  0) then
```

```
  with fTokens do
```

```
    begin lIndex  $\leftarrow$  2;
```

```
    repeat { infinite loop }
```

```
      ⟨ If we matched a dictionary entry, then initialize FoundToken 747 ⟩;
```

```
      if fPhrase[EndOfPhrase] = ‘_’ then break; { we are done! }
```

```
      if (lIndex  $\leq$  length(the_token(lToken).fStr))  $\wedge$ 
```

```
        (the_token(lToken).fStr[lIndex] = fPhrase[EndOfPhrase]) then
```

```
        begin inc(lIndex); inc(EndOfPhrase) end { iterate, look at next character }
```

```
      else if (lToken < Count - 1) then { try looking for the last matching item }
```

```
        begin if (copy(the_token(lToken).fStr, 1, lIndex - 1) =
```

```
          copy(the_token(lToken + 1).fStr, 1, lIndex - 1)) then inc(lToken) { iterate }
```

```
        else break; { we are done! }
```

```
        end
```

```
      else break; { we are done! }
```

```
    until false;
```

```
  end
```

This code is used in section 740.

747. If we have *lIndex* (the index of the current phrase) be longer than the lexeme of the current dictionary entry's lexeme, then we should populate *FoundItem*.

```

⟨ If we matched a dictionary entry, then initialize FoundToken 747 ⟩ ≡
  if lIndex > length(the_token(lToken).fStr) then { we matched the token }
    begin FoundToken ← the_item(lToken); EndOfSymbol ← EndOfPhrase − 1;
    end

```

This code is used in section 746.

748. When the identifier is not a number, we insert an “identifier” token into the tokens buffer.

```

⟨ Variables for slicing a phrase 739 ⟩ +≡
lFailed: integer; { index of first non-digit character }
I: integer; { index ranging over the raw lexeme string }
lSpelling: string; { raw lexeme as a string }

```

```

749. ⟨ Check identifier is not a number 749 ⟩ ≡
  begin lSpelling ← copy(fPhrase, lCurrChar, IdentLength);
  lPos.Col ← fPhrasePos.Col + EndOfIdent − 1;
  if (ord(fPhrase[lCurrChar]) > ord(‘0’)) ∧ (ord(fPhrase[lCurrChar]) ≤ ord(‘9’)) then
    begin lFailed ← 0; { location of non-digit character }
    for I ← 1 to IdentLength − 1 do
      if (ord(fPhrase[lCurrChar + I]) < ord(‘0’)) ∨ (ord(fPhrase[lCurrChar + I]) > ord(‘9’)) then
        begin lFailed ← I + 1; break;
        end;
      if lFailed = 0 then { if all characters are digits }
        ⟨ Whoops! Identifier turned out to be a number! 753 ⟩;
      end;
    ⟨ Add token to tokens buffer and iterate 751 ⟩;
  end

```

This code is used in section 740.

750. We add an *Identifier* token to the tokens buffer.

```

⟨ Variables for slicing a phrase 739 ⟩ +≡
lIdent: TokenPtr;

```

```

751. ⟨ Add token to tokens buffer and iterate 751 ⟩ ≡
  lIdent ← new(TokenPtr, Init(Identifier, fIdents.Count + 1, lSpelling));
  if fIdents.Search(lIdent, I) then dispose(lIdent, Done)
  else fIdents.Insert(lIdent);
  fTokensBuf.Insert(new(MTokenPtr, Init(Identifier, TokenPtr(fIdents.Items↑[I])↑.fLexem.Nr, lSpelling,
    lPos)));
  lCurrChar ← EndOfIdent + 1; continue

```

This code is used in section 749.

752. If we goofed and all the characters turned out to be digits (i.e., the identifier *was* a numeral after all), we should clean things up here. Observe we will end up *continue*-ing along the loop.

When the numeral token is larger than $MaxConstInt = 2^{31} - 1$ (the largest 32-bit integer, §715), then we should raise a “Too large numeral” 202 error token. If we wanted to support “arbitrary precision” numbers, then this should be modified.

We can either insert into the tokens buffer an error token (in two possible outcomes) or a numeral token (in the third possible outcome).

⟨ Variables for slicing a phrase 739 ⟩ +≡
lNumber: *longint*;
J: *integer*;

753. ⟨ Whoops! Identifier turned out to be a number! 753 ⟩ ≡
begin if *IdentLength* > *length(IntToStr(MaxConstInt))* **then** { insert error token }
 begin *fTokensBuf.Insert(new(MTokenPtr, Init(ErrorSymbol, 202, lSpelling, lPos)))*;
 lCurrChar ← *EndOfIdent* + 1; *continue*;
 end;
lNumber ← 0; *J* ← 1;
for *I* ← *IdentLength* − 1 **downto** 0 **do**
 begin *lNumber* ← *lNumber* + (*ord(fPhrase[lCurrChar + I])* − *ord('0')*) * *J*; *J* ← *J* * 10;
 end;
if *lNumber* > *MaxConstInt* **then** { insert error token }
 begin *fTokensBuf.Insert(new(MTokenPtr, Init(ErrorSymbol, 202, lSpelling, lPos)))*;
 lCurrChar ← *EndOfIdent* + 1; *continue*;
 end; { insert numeral token }
fTokensBuf.Insert(new(MTokenPtr, Init(Numeral, lNumber, lSpelling, lPos)));
lCurrChar ← *EndOfIdent* + 1; *continue*;
end

This code is used in section 749.

754. If we have tokenised the phrase, but the token is not contained in the dictionary, then we should raise a 203 error.

⟨ Whoops! We found an unknown token, insert a 203 error token 754 ⟩ ≡
lPos.Col ← *fPhrasePos.Col* + *lCurrChar* − 1;
fTokensBuf.Insert(new(MTokenPtr, Init(ErrorSymbol, 203, fPhrase[lCurrChar], lPos))); *inc(lCurrChar)*

This code is used in section 740.

755. We have purely abstract methods which will invoke *Abstract1* (§307), which raises a runtime error.

⟨ Implementation for scanner.pas 717 ⟩ +≡
procedure *MTokeniser.GetPhrase*;
 begin *Abstract1*;
 end;
function *MTokeniser.EndOfText*: *boolean*;
 begin *Abstract1*; *EndOfText* ← *false*;
 end;
function *MTokeniser.IsIdentifierLetter*(*ch* : *char*): *boolean*;
 begin *Abstract1*; *IsIdentifierLetter* ← *false*;
 end;

756. Get a token. Getting a token from the tokeniser will check if we’ve exhausted the input stream (which tests if the kind of *fLexem* is *EOT*), and exit if we have.

Otherwise, it looks to see if we’ve got tokens left in the buffer. If so, just pop one and exit.

But when the token buffer is empty, we invoke the abstract method *GetPhrase* to read some of the input stream. If it turns out there’s nothing left to read, then update the tokeniser to be in the “end of text” state.

When we have some of the input stream read into the *fPhrase* field, we tokenise it using the *SliceIt* function. Then we pop a token from the buffer of tokens.

This will populate *fLexem*, *fStr*, and *fPos* with the new token, lexeme, and position...but that’s only because *GetPhrase* (§760) and *SliceIt* (§739) do the actual work.

⟨Implementation for scanner.pas 717⟩ +≡

```

procedure MTokeniser.GetToken;
  begin if fLexem.Kind = EOT then exit;
  if fTokensBuf.Count > 0 then
    begin ⟨Pop a token from the underlying tokens stack 757⟩;
    exit;
    end;
  GetPhrase;
  if EndOfText then
    begin fLexem.Kind ← EOT; fStr ← ‘ ’; fPos ← fPhrasePos; inc(fPos.Col);
    exit;
    end;
  SliceIt; ⟨Pop a token from the underlying tokens stack 757⟩;
end;

```

757. Popping a token will update the lexeme, str, and position fields to be populated from the first item in the tokens buffer. Then it will free that item from the tokens buffer, shifting everything down by one.

⟨Pop a token from the underlying tokens stack 757⟩ ≡

```

fLexem ← MTokenPtr(fTokensBuf.Items↑[0])↑.fLexem;
fStr ← MTokenPtr(fTokensBuf.Items↑[0])↑.fStr; fPos ← MTokenPtr(fTokensBuf.Items↑[0])↑.fPos;
fTokensBuf.AtFree(0)

```

This code is used in sections 756 and 756.

758. Testing if the given character is an identifier character or not requires invoking the abstract method *IsIdentifierLetter* (§755).

⟨Implementation for scanner.pas 717⟩ +≡

```

function MTokeniser.IsIdentifierFirstLetter(ch : char): boolean;
  begin IsIdentifierFirstLetter ← IsIdentifierLetter(ch);
  end;

```

Section 16.4. SCANNER OBJECT

759. This extends the Tokeniser class (§731). It is the only class extending the Tokeniser class.

⟨MScanner object class 759⟩ ≡

```

MScannPtr = ↑MScannObj;
MScannObj = object (MTokeniser)
  Allowed: ASCIIArr;
  fSourceBuff: pointer;
  fSourceBuffSize: word;
  fSourceFile: text;
  fCurrentLine: string;
  constructor InitScanning(const aFileName, aDctFileName: string);
  destructor Done; virtual;
  procedure GetPhrase; virtual;
  procedure ProcessComment(fLine, fStart : integer; cmt : string); virtual;
  function EndOfText: boolean; virtual;
  function IsIdentifierLetter(ch : char): boolean; virtual;
end

```

This code is used in section 716.

760. Get a phrase. We search through the lines for the “first phrase” (i.e., first non-whitespace character, which indicates the start of something interesting). Comments are thrown away as are Mizar pragmas.

This will update *fCurrentLine* as needed, setting it to the next line in the input stream buffer. It will assign a *copy* of the phrase to the field *fPhrase*, as well as update the *fPhrasePos*.

There is a comment in Polish, “uzyskanie pierwszego znaczącego znaku”, which Google translates as: “obtaining the first significant sign”. This seemed like a natural “chunk” of code to study in isolation.

The contract for *GetPhrase* ensures the *fPhrase* will be populated with a string ending with a space (“`␣`”) character, or it will be the empty string (when the end of text has been encountered).

⟨Implementation for scanner.pas 717⟩ +≡

```

procedure MScannObj.GetPhrase;
  const Prohibited: ASCIIArr = ⟨Characters prohibited by MScanner 761⟩;
  var i, k: integer;
  begin fPhrasePos.Col ← fPhrasePos.Col + length(fPhrase) - 1;
  ⟨Find the first significant ‘sign’ 762⟩;
  for i ← fPhrasePos.Col to length(fCurrentLine) do
    if fCurrentLine[i] = ‘␣’ then break;
  fPhrase ← Copy(fCurrentLine, fPhrasePos.Col, i - fPhrasePos.Col + 1);
  end;

```

761. The prohibited ASCII characters are everything *NOT* among the follow characters:

```

␣ ! " # $ % & ' ( ) * + , - . / : ; < = > ? @
[ \ ] ^ _ ` { | } ~ 0 1 2 3 4 5 6 7 8 9
A B C D E F G H I J K L M N O P Q R S T U V W X Y Z
a b c d e f g h i j k l m n o p q r s t u v w x y z

```

The reader will observe these are all the “graphic” ASCII characters, plus the space (“␣”) character.

```

⟨ Characters prohibited by MScanner 761 ⟩ ≡
(1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1,
1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,
1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,
1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,
1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,
1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1)

```

This code is used in section 760.

762. Note that the *fCurrentLine* will end with a whitespace, when we have not consumed the entire underlying input stream.

```

⟨ Find the first significant ‘sign’ 762 ⟩ ≡
  while fCurrentLine[fPhrasePos.Col] = ‘␣’ do
    begin if fPhrasePos.Col ≥ length(fCurrentLine) then ⟨ Populate the current line 763 ⟩;
      inc(fPhrasePos.Col);
    end
  end

```

This code is used in section 760.

763. Now, populating the current line requires a bit of work. We ensure the end of the current line will end with a space character (“␣”), which will guarantee the loop iteratively consumes all empty lines in the file.

Once we arrive at a non-space character, we will break the loop containing this chunk of code. If we have exhausted the underlying input stream, then we will have *EndOfText* be true. Should that occur, we exit the function.

```

⟨ Populate the current line 763 ⟩ ≡
  begin if EndOfText then exit;
    inc(fPos.Line); inc(fPhrasePos.Line); readln(fSourceFile, fCurrentLine);
    ⟨ Scan for pragmas, and exit if we found one 767 ⟩;
    ⟨ Skip comments 768 ⟩;
    ⟨ Trim whitespace from the right of the current line 766 ⟩;
    ⟨ Replace every invalid character in current line with the unit character 765 ⟩;
    fCurrentLine ← fCurrentLine + ‘␣’;
    if ¬LongLines then
      if length(fCurrentLine) > MaxLineLength then ⟨ Replace end of long line with record separator 764 ⟩;
      { Assert: we have fCurrentLine end in “␣” }
      fPhrasePos.Col ← 0; fPos.Col ← 0;
    end
  end

```

This code is used in section 762.

764. When we have excessively long lines, and we have not enabled “long line mode”, then we just delete everything after $MaxLineLength + 1$ and set $MaxLineLength - 1$ to the record separator (which is rejected by the Mizar lexer) and the last character in the line to the space character.

⟨ Replace end of long line with record separator 764 ⟩ \equiv
begin *delete*(*fCurrentLine*, $MaxLineLength + 1$, $length(fCurrentLine)$);
fCurrentLine[$MaxLineLength - 1$] \leftarrow *record_separator*;
fCurrentLine[$MaxLineLength$] \leftarrow ‘ \sqcup ’;
end

This code is used in section 763.

765. In particular, if we every encounter an “invalid” character, then we just replace it with the “unit separator” character.

⟨ Replace every invalid character in current line with the unit character 765 ⟩ \equiv
for $k \leftarrow 1$ **to** $length(fCurrentLine) - 1$ **do**
 if *Prohibited*[*fCurrentLine*[k]] > 0 **then** *fCurrentLine*[k] \leftarrow *unit_separator*

This code is used in section 763.

766. We will trim whitespace from the right of the current line at least twice.

⟨ Trim whitespace from the right of the current line 766 ⟩ \equiv
 $k \leftarrow length(fCurrentLine)$;
while ($k > 0$) \wedge (*fCurrentLine*[k] = ‘ \sqcup ’) **do** *dec*(k);
 delete(*fCurrentLine*, $k + 1$, $length(fCurrentLine)$)

This code is used in sections 763 and 767.

767. Pragmas in Mizar are special comments which start a line with “ $::\$$ ”. They are useful for naming theorems (“ $::\$N \langle name \rangle$ ”), or toggling certain phases of the Mizar checker. This will process the comment (§769).

Since pragmas are important, we treat it as a token (and not a comment to be thrown away).

Note: if you try to invoke a pragma, but do not place it at the start of a line, then Mizar will treat it like a comment.

⟨ Scan for pragmas, and exit if we found one 767 ⟩ \equiv
 $k \leftarrow Pos('::\$', fCurrentLine)$; { Preprocessing directive }
if ($k = 1$) **then**
 begin *ProcessComment*(*fPhrasePos.Line*, 1, *copy*(*fCurrentLine*, 1, $length(fCurrentLine)$));
 ⟨ Trim whitespace from the right of the current line 766 ⟩;
 fCurrentLine \leftarrow *fCurrentLine* + ‘ \sqcup ’; *fPhrase* \leftarrow *Copy*(*fCurrentLine*, 1, $length(fCurrentLine)$);
 fPhrasePos.Col \leftarrow 1; *fPos.Col* \leftarrow 0; *exit*
 end

This code is used in section 763.

768. Scanning a comment will effectively replace the start of the comment (“ $::$ ”) up to and including the end of the line, with a single space. This will process the comment (§769).

⟨ Skip comments 768 ⟩ \equiv
 $k \leftarrow Pos('::', fCurrentLine)$; { Comment }
if ($k \neq 0$) **then**
 begin *ProcessComment*(*fPhrasePos.Line*, k , *copy*(*fCurrentLine*, k , $length(fCurrentLine)$));
 delete(*fCurrentLine*, $k + 1$, $length(fCurrentLine)$); *fCurrentLine*[k] \leftarrow ‘ \sqcup ’;
 end

This code is used in section 763.

769. “Processing a comment” really means skipping the comment.

⟨Implementation for scanner.pas 717⟩ +≡

```
procedure MScannObj.ProcessComment(fLine, fStart : integer; cmt : string);
begin end;
```

770. Testing if the scanner has exhausted the input stream amounts to checking the current line has been completely read *and* the current source file has arrived at an *texttfeof* state.

⟨Implementation for scanner.pas 717⟩ +≡

```
function MScannObj.EndOfText: boolean;
begin EndOfText ← (fPhrasePos.Col ≥ length(fCurrentLine)) ∧ eof(fSourceFile);
end;
```

771. Testing if a character is an identifier letter amounts to testing if it is allowed (i.e., not disallowed).

⟨Implementation for scanner.pas 717⟩ +≡

```
function MScannObj.IsIdentifierLetter(ch : char): boolean;
begin IsIdentifierLetter ← Allowed[ch] ≠ 0;
end;
```

772. Constructor. The only way to construct a scanner. This expects an article to be read in *aFileName* and a dictionary to be loaded (*aDctFileName*, loaded with §723). The buffer size for reading *aFileName* is initially #4000.

⟨Implementation for scanner.pas 717⟩ +≡

```
constructor MScannObj.InitScanning(const aFileName, aDctFileName : string);
begin inherited Init; Allowed ← DefaultAllowed; fTokens.LoadDct(aDctFileName);
assign(fSourceFile, aFileName); fSourceBuffSize ← #4000; getmem(fSourceBuff, fSourceBuffSize);
settextbuf(fSourceFile, fSourceBuff↑, #4000); reset(fSourceFile); fCurrentLine ← ‘ ’; GetToken;
end;
```

773. Destructor. We must remember to close the source file, free the buffer, close the lights, and lock the doors.

⟨Implementation for scanner.pas 717⟩ +≡

```
destructor MScannObj.Done;
begin close(fSourceFile); FreeMem(fSourceBuff, fSourceBuffSize); fCurrentLine ← ‘ ’; inherited Done;
end;
```


File 17

Format

774. The first step towards disambiguating the meaning of identifiers is to use “formats”. Recall from, e.g., Andrzej Trybulec’s “Some Features of the Mizar Language” (ESPRIT Workshop, Torino, 1993; mizar.uwb.edu.pl/project/t §3) that the “Format” describes with how many arguments a “Constructor Symbol” may be used. The basic formats:

- Predicates ⟨lexeme, left arguments number, right arguments number⟩
- Modes ⟨lexeme, arguments number⟩ for “mode Foo of T_1, \dots, T_n ” where n is the arguments number
- Functors ⟨lexeme, left arguments number, right arguments number⟩
- Bracket functors ⟨left bracket lexeme, arguments number, right bracket lexeme⟩
- Selector ⟨lexeme, 1⟩
- Structure ⟨lexeme, arguments number⟩ for generic structures over [arguments number] parameters
- Structure ⟨lexeme, 1⟩ for situations where we write “the [structure] of [term]”

We store these format information in XML files. See also Adam Grabowski, Artur Korniłowicz, and Adam Naumowicz’s “Mizar in a Nutshell” (viz. §2.3, [doi:10.6092/issn.1972-5787/1980](https://doi.org/10.6092/issn.1972-5787/1980)) for a little more discussion about formats.

```

⟨_format.pas 774⟩ ≡
  ⟨GNU License 4⟩
unit _formats;
  interface
    uses mobjects, scanner, dicthan, xml_inout;
    ⟨Declare classes for _formats.pas 776⟩
    function CompareFormats(aItem1, aItem2 : Pointer): Integer;
    function In_Format(fInFile : XMLInStreamPtr): MFormatPtr;
    ⟨Global variables (_formats.pas) 775⟩
  implementation
    uses errhan, xml_dict, xml_parser
      mdebug, info end mdebug;
    ⟨Implementation for _formats.pas 777⟩
  end .

```

775.

```

⟨Global variables (_formats.pas) 775⟩ ≡
var gFormatsColl: MFormatsList; gPriority: BinIntFunc; gFormatsBase: integer;

```

This code is used in section 774.

776. Broadly speaking, there are only 3 types of “formats”: prefix formats, infix formats, bracket-like formats. These are viewed as “subclasses” of a base *MFormat* object.

We will want to collect the formats from articles referenced by the environment of an article being verified or parsed. This motivates the *MFormatList* object.

```

⟨ Declare classes for _formats.pas 776 ⟩ ≡
  ⟨ Declare MFormat object 778 ⟩;
  { TODO: add assertions that nr. of all format arguments is equal to the number of visible args
    (Visible) of a pattern }
  ⟨ Declare MPrefixFormat object 780 ⟩;
  ⟨ Declare MInfixFormat object 782 ⟩;
  ⟨ Declare MBracketFormat object 784 ⟩;
  ⟨ Declare MFormatsList object 792 ⟩;

```

This code is used in section 774.

777. The *presentation* of the code is a bit disorganized from the perspective of pedagogy, so I am going to re-organize for the sake of discussing it.

```

⟨ Implementation for _formats.pas 777 ⟩ ≡
  ⟨ Constructors for derived format classess 779 ⟩
  ⟨ Compare formats 786 ⟩
  ⟨ Implementation for MFormatsList 793 ⟩
  ⟨ Read formats from an XML input stream 804 ⟩
  ⟨ Implement MFormatObj 805 ⟩

```

This code is used in section 774.

778. Format base class. All format instances have a lexeme called its *fSymbol*. Recall that *LexemeRec* (§716) is a normalized token using a single character to describe its kind, and an integer to keep track of it (instead of relying on a raw string).

```

⟨ Declare MFormat object 778 ⟩ ≡
  MFormatPtr = ↑MFormatObj;
  MFormatObj = object (MObject)
    fSymbol: LexemRec;
    constructor Init(aKind : Char; aSymNr : integer);
    procedure Out_Format(var fOutFile : XMLOutputStreamObj; aFormNr : integer);
  end

```

This code is used in section 776.

779. The constructor expects the “kind” of the object and its symbol number.

```

⟨ Constructors for derived format classess 779 ⟩ ≡
constructor MFormatObj.Init(aKind : Char; aSymNr : integer);
  begin fSymbol.Kind ← aKind; fSymbol.Nr ← aSymNr;
  end;

```

See also sections 781, 783, and 785.

This code is used in section 777.

780. Prefix format object.

```

⟨ Declare MPrefixFormat object 780 ⟩ ≡
  MPrefixFormatPtr = ↑MPrefixFormatObj;
  MPrefixFormatObj = object (MFormatObj)
    fRightArgsNbr: byte;
    constructor Init(aKind : Char; aSymNr, aRArgsNbr : integer);
  end

```

This code is used in section 776.

781. Prefix formats track how many arguments are to the right of the prefix symbol.

```

⟨ Constructors for derived format classess 779 ⟩ +≡
constructor MPrefixFormatObj.Init(aKind : Char; aSymNr, aRArgsNbr : integer);
  begin fSymbol.Kind ← aKind; fSymbol.Nr ← aSymNr; fRightArgsNbr ← aRArgsNbr;
  end;

```

782. Infix format object.

```

⟨ Declare MInfixFormat object 782 ⟩ ≡
  MInfixFormatPtr = ↑MInfixFormatObj;
  MInfixFormatObj = object (MPrefixFormatObj)
    fLeftArgsNbr: byte;
    constructor Init(aKind : Char; aSymNr, aLArgsNbr, aRArgsNbr : integer);
  end

```

This code is used in section 776.

783. And just as prefix symbols tracks the number of arguments to the right, infix symbols tracks the number of arguments to both the left and right.

```

⟨ Constructors for derived format classess 779 ⟩ +≡
constructor MInfixFormatObj.Init(aKind : Char; aSymNr, aLArgsNbr, aRArgsNbr : integer);
  begin fSymbol.Kind ← aKind; fSymbol.Nr ← aSymNr; fLeftArgsNbr ← aLArgsNbr;
  fRightArgsNbr ← aRArgsNbr;
  end;

```

784. Bracket format object.

```

⟨ Declare MBracketFormat object 784 ⟩ ≡
  MBracketFormatPtr = ↑MBracketFormatObj;
  MBracketFormatObj = object (MInfixFormatObj)
    fRightSymbolNr: integer;
    fArgsNbr: byte;
    constructor Init(aLSymNr, aRSymNr, aArgsNbr, aLArgsNbr, aRArgsNbr : integer);
  end

```

This code is used in section 776.

785. ⟨ Constructors for derived format classess 779 ⟩ +≡

```

constructor MBracketFormatObj.Init(aLSymNr, aRSymNr, aArgsNbr, aLArgsNbr, aRArgsNbr : integer);
  begin fSymbol.Kind ← 'K'; fSymbol.Nr ← aLSymNr; fRightSymbolNr ← aRSymNr;
  fArgsNbr ← aArgsNbr; fLeftArgsNbr ← aLArgsNbr; fRightArgsNbr ← aRArgsNbr;
  end;

```

786. Ordering format objects. We need a *Compare* ordering function on formats. This is a lexicographic ordering on the (kind, number of right symbols, number of arguments, number of left symbols), more or less.

```

⟨ Compare formats 786 ⟩ ≡
function CompareFormats(aItem1, aItem2 : Pointer): Integer;
  begin CompareFormats ← 1;
  if MFormatPtr(aItem1)↑.fSymbol.Kind < MFormatPtr(aItem2)↑.fSymbol.Kind then
    CompareFormats ← -1
  else if MFormatPtr(aItem1)↑.fSymbol.Kind = MFormatPtr(aItem2)↑.fSymbol.Kind then
    ⟨ Compare symbols of the same kind 787 ⟩;
  end;

```

This code is used in section 777.

787. We then check the indexing number of the symbol. When they are the same, we look at the next “entry” in the tuple.

```

⟨ Compare symbols of the same kind 787 ⟩ ≡
  if MFormatPtr(aItem1)↑.fSymbol.Nr < MFormatPtr(aItem2)↑.fSymbol.Nr then
    CompareFormats ← -1
  else if MFormatPtr(aItem1)↑.fSymbol.Nr = MFormatPtr(aItem2)↑.fSymbol.Nr then
    ⟨ Compare same kinded symbols with the same number 788 ⟩

```

This code is used in section 786.

788. The next “entry” in the tuple depends on the kind of symbols we are comparing. Selectors (‘U’) are, at this point, identical (so we return zero). Note that ‘J’ is a historic artifact no longer used (in fact, I cannot locate its meaning in the literature I possess).

Structure (‘G’), right functor brackets (‘L’), modes (‘M’), and attributes (‘V’) can be compared as prefix symbols.

Functors (‘O’) and predicates (‘R’) can be compared as infix symbols.

Left functor brackets (‘K’) can be compared first with bracket-specific characteristics, then as infix symbols.

```

⟨ Compare same kinded symbols with the same number 788 ⟩ ≡
  case MFormatPtr(aItem1)↑.fSymbol.Kind of
    ‘J’, ‘U’: CompareFormats ← 0;
    ‘G’, ‘L’, ‘M’, ‘V’: ⟨ Compare prefix symbols 789 ⟩;
    ‘O’, ‘R’: ⟨ Compare infix symbols 791 ⟩;
    ‘K’: ⟨ Compare bracket symbols 790 ⟩;
  endcases

```

This code is used in section 787.

789. Comparing prefixing symbols, at this points, can only compare the number of arguments to the right.

```

⟨ Compare prefix symbols 789 ⟩ ≡
  if MPrefixFormatPtr(aItem1)↑.fRightArgsNbr < MPrefixFormatPtr(aItem2)↑.fRightArgsNbr then
    CompareFormats ← -1
  else if MPrefixFormatPtr(aItem1)↑.fRightArgsNbr = MPrefixFormatPtr(aItem2)↑.fRightArgsNbr then
    CompareFormats ← 0

```

This code is used in section 788.

790. Comparing bracket symbols first tries to compare the number of symbols to its right. If these are equal, then we try to compare the number of arguments. If these are equal, then we compare them “as if” they were infixing symbols.

```

⟨ Compare bracket symbols 790 ⟩ ≡
  if MBracketFormatPtr(aItem1)↑.fRightSymbolNr < MBracketFormatPtr(aItem2)↑.fRightSymbolNr
    then CompareFormats ← -1
  else if MBracketFormatPtr(aItem1)↑.fRightSymbolNr = MBracketFormatPtr(aItem2)↑.fRightSymbolNr
    then
      if MBracketFormatPtr(aItem1)↑.fArgsNbr < MBracketFormatPtr(aItem2)↑.fArgsNbr then
        CompareFormats ← -1
      else if MBracketFormatPtr(aItem1)↑.fArgsNbr = MBracketFormatPtr(aItem2)↑.fArgsNbr then
        ⟨ Compare infix symbols 791 ⟩

```

This code is used in section 788.

791. Comparing infixing symbols compares the number of arguments to the left. If these are equal, then we try to compare the number of arguments to the right. If these are equal, then we return 0.

```

⟨ Compare infix symbols 791 ⟩ ≡
  if MInfixFormatPtr(aItem1)↑.fLeftArgsNbr < MInfixFormatPtr(aItem2)↑.fLeftArgsNbr then
    CompareFormats ← -1
  else if MInfixFormatPtr(aItem1)↑.fLeftArgsNbr = MInfixFormatPtr(aItem2)↑.fLeftArgsNbr then
    if MInfixFormatPtr(aItem1)↑.fRightArgsNbr < MInfixFormatPtr(aItem2)↑.fRightArgsNbr then
      CompareFormats ← -1
    else if MInfixFormatPtr(aItem1)↑.fRightArgsNbr = MInfixFormatPtr(aItem2)↑.fRightArgsNbr
      then CompareFormats ← 0

```

This code is used in sections 788 and 790.

Section 17.1. LIST OF FORMATS

792. We have a collection of format objects managed by a *MFormatsList* object. There are two groups of public functions: “Lookup” functions (to find the format matching certain parameters), and “Collect” functions (to insert a new format).

```

⟨Declare MFormatsList object 792⟩ ≡
  MFormatsListPtr = ↑MFormatsList;
  MFormatsList = object (MSortedList)
    constructor Init(ALimit : Integer);
    constructor LoadFormats(fName : string);
    procedure StoreFormats(fName : string);
    function Lookup_PrefixFormat(aKind : char; aSymNr, aArgsNbr : integer): integer;
    function Lookup_FuncFormat(aSymNr, aLArgsNbr, aRArgsNbr : integer): integer;
    function Lookup_BracketFormat(aLSymNr, aRSymNr, aArgsNbr, aLArgsNbr, aRArgsNbr : integer):
      integer;
    function Lookup_PredFormat(aSymNr, aLArgsNbr, aRArgsNbr : integer): integer;
    function CollectFormat(aFormat : MFormatPtr): integer;
    function CollectPrefixForm(aKind : char; aSymNr, aArgsNbr : integer): integer;
    function CollectFuncForm(aSymNr, aLArgsNbr, aRArgsNbr : integer): integer;
    function CollectBracketForm(aLSymNr, aRSymNr, aArgsNbr, aLArgsNbr, aRArgsNbr : integer):
      integer;
    function CollectPredForm(aSymNr, aLArgsNbr, aRArgsNbr : integer): integer;
  end

```

This code is used in section 776.

793. We prefix format objects specified by its kind, its symbol number, and the number of arguments it expects.

When the format object is not found, then 0 will be returned. This is a standard convention in these functions to indicate the thing is missing.

```

⟨Implementation for MFormatsList 793⟩ ≡
const PrefixFormatChars = [‘M’, ‘V’, ‘U’, ‘J’, ‘L’, ‘G’];
function MFormatsList.LookUp_PrefixFormat(aKind : char; aSymNr, aArgsNbr : integer): integer;
  var lFormat: MPrefixFormatObj; i: integer;
  begin MizAssert(3300, aKind ∈ PrefixFormatChars);
  lFormat.Init(aKind, aSymNr, aArgsNbr);
  if Find(@lFormat, i) then LookUp_PrefixFormat ← fIndex↑i + 1
  else LookUp_PrefixFormat ← 0;
  end;

```

This code is used in section 777.

794. Looking up an infix functor format (§782). This returns the *index* for the entry.

The contract here is rather confusing. What *should* occur is: if there is a functor symbol with the given left and right number of arguments, then return the index for the entry. Otherwise (when there is no functor symbol) return -1 .

What happens instead is these values are incremented, so if the functor symbol with the given number of left and right arguments is contained in position k , then $k + 1$ will be returned. If there is no such functor symbol, then 0 will be returned.

```
function MFormatsList.LookUp_FuncFormat(aSymNr, aLArgsNbr, aRArgsNbr : integer): integer;
  var lFormat: MInfixFormatObj; i: integer;
  begin lFormat.Init(⋅0⋅, aSymNr, aLArgsNbr, aRArgsNbr);
  if Find(@lFormat, i) then LookUp_FuncFormat  $\leftarrow$  fIndex↑[i] + 1
  else LookUp_FuncFormat  $\leftarrow$  0;
  end;
```

795. Looking up a bracket.

```
function MFormatsList.LookUp_BracketFormat(aLSymNr, aRSymNr, aArgsNbr, aLArgsNbr,
  aRArgsNbr : integer): integer;
  var lFormat: MBracketFormatObj; i: integer;
  begin lFormat.Init(aLSymNr, aRSymNr, aArgsNbr, aLArgsNbr, aRArgsNbr);
  if Find(@lFormat, i) then LookUp_BracketFormat  $\leftarrow$  fIndex↑[i] + 1
  else LookUp_BracketFormat  $\leftarrow$  0;
  end;
```

796. Looking up a predicate.

```
function MFormatsList.LookUp_PredFormat(aSymNr, aLArgsNbr, aRArgsNbr : integer): integer;
  var lFormat: MInfixFormatObj; i: integer;
  begin lFormat.Init(⋅R⋅, aSymNr, aLArgsNbr, aRArgsNbr);
  if Find(@lFormat, i) then LookUp_PredFormat  $\leftarrow$  fIndex↑[i] + 1
  else LookUp_PredFormat  $\leftarrow$  0;
  end;
```

797. Insert a format, if it's missing.

```
function MFormatsList.CollectFormat(aFormat : MFormatPtr): integer;
  var lFormatNr, i: integer;
  begin lFormatNr  $\leftarrow$  0;
  if ¬Find(aFormat, i) then
    begin lFormatNr  $\leftarrow$  Count + 1; Insert(aFormat);
    end;
  CollectFormat  $\leftarrow$  lFormatNr;
  end;
```

798. Inserting a bracket, if it is missing. Returns the format number for the format, whether it is missing or not.

```
function MFormatsList.CollectBracketForm(aLSymNr, aRSymNr, aArgsNbr, aLArgsNbr,
    aRArgsNbr : integer): integer;
var lFormatNr: integer;
begin lFormatNr  $\leftarrow$  LookUp_BracketFormat(aLSymNr, aRSymNr, aArgsNbr, aLArgsNbr, aRArgsNbr);
if lFormatNr = 0 then
    begin lFormatNr  $\leftarrow$  Count + 1;
        Insert(new(MBracketFormatPtr, Init(aLSymNr, aRSymNr, aArgsNbr, aLArgsNbr, aRArgsNbr)));
    end;
    CollectBracketForm  $\leftarrow$  lFormatNr;
end;
```

799. Inserting a functor format, if it is missing. This returns the format number for the functor (whether it is missing or not).

```
function MFormatsList.CollectFuncForm(aSymNr, aLArgsNbr, aRArgsNbr : integer): integer;
var lFormatNr: integer;
begin lFormatNr  $\leftarrow$  LookUp_FuncFormat(aSymNr, aLArgsNbr, aRArgsNbr);
if lFormatNr = 0 then
    begin lFormatNr  $\leftarrow$  Count + 1;
        Insert(new(MInfixFormatPtr, Init(^0^, aSymNr, aLArgsNbr, aRArgsNbr)));
    end;
    CollectFuncForm  $\leftarrow$  lFormatNr;
end;
```

800. Insert a prefix format if it is missing. Then return the format number for the prefix format, missing or not.

```
function MFormatsList.CollectPrefixForm(aKind : char; aSymNr, aArgsNbr : integer): integer;
var lFormatNr: integer;
begin lFormatNr  $\leftarrow$  LookUp_PrefixFormat(aKind, aSymNr, aArgsNbr);
if lFormatNr = 0 then
    begin lFormatNr  $\leftarrow$  Count + 1; Insert(new(MPrefixFormatPtr, Init(aKind, aSymNr, aArgsNbr)));
    end;
    CollectPrefixForm  $\leftarrow$  lFormatNr;
end;
```

801. Insert a predicate format, if it is missing. Then return the format number, whether the predicate format is missing or not.

```
function MFormatsList.CollectPredForm(aSymNr, aLArgsNbr, aRArgsNbr : integer): integer;
var lFormatNr: integer;
begin lFormatNr  $\leftarrow$  LookUp_PredFormat(aSymNr, aLArgsNbr, aRArgsNbr);
if lFormatNr = 0 then
    begin lFormatNr  $\leftarrow$  Count + 1;
        Insert(new(MInfixFormatPtr, Init(^R^, aSymNr, aLArgsNbr, aRArgsNbr)));
    end;
    CollectPredForm  $\leftarrow$  lFormatNr;
end;
```


802. Constructor. Construct the empty list of formats.

```
constructor MFormatsList.Init(ALimit : Integer);
  begin InitSorted(ALimit, CompareFormats);
end;
```

803. Constructor. Parse an XML file for formats, and populate a format list object with the file's contents.

```
constructor MFormatsList.LoadFormats(fName : string);
  var lEnvFile: XMLInStreamPtr; lValue: integer; lLex: LexemRec;
  begin InitSorted(100, CompareFormats); lEnvFile ← new(XMLInStreamPtr, OpenFile(fName));
  with lEnvFile↑ do
    begin NextElementState; XMLASSERT(nElName = XMLElemName[elFormats]);
    NextElementState;
    while ¬(nState = eEnd) ∧ (nElName = XMLElemName[elFormat]) do Insert(In_Format(lEnvFile));
    gPriority.Init(10);
    while ¬(nState = eEnd) do
      begin XMLASSERT(nElName = XMLElemName[elPriority]);
      lLex.Kind ← GetAttr(XMLAttrName[atKind])[1];
      lLex.Nr ← GetIntAttr(XMLAttrName[atSymbolNr]); MizAssert(3300, lLex.Kind ∈ [ˆOˆ, ˆLˆ, ˆKˆ]);
      lValue ← GetIntAttr(XMLAttrName[atValue]); gPriority.Assign(ord(lLex.Kind), lLex.Nr, lValue);
      AcceptEndState; NextElementState;
      end;
    end;
  dispose(lEnvFile, Done);
end;
```

804. We can read exactly one format from an XML input stream.

⟨ Read formats from an XML input stream 804 ⟩ ≡

```
function In_Format(fInFile : XMLInStreamPtr): MFormatPtr;
  var lLex: LexemRec; lArgsNbr, lLeftArgsNbr, lRightSymNr: integer;
  begin with fInFile↑ do
    begin lLex.Kind ← GetAttr(XMLAttrName[atKind])[1];
    lLex.Nr ← GetIntAttr(XMLAttrName[atSymbolNr]);
    lArgsNbr ← GetIntAttr(XMLAttrName[atArgNr]);
    case lLex.Kind of
      ˆOˆ, ˆRˆ: begin lLeftArgsNbr ← GetIntAttr(XMLAttrName[atLeftArgNr]);
        In_Format ← new(MInfixFormatPtr, Init(lLex.Kind, lLex.Nr, lLeftArgsNbr,
          lArgsNbr − lLeftArgsNbr));
        end;
      ˆJˆ, ˆUˆ, ˆVˆ, ˆGˆ, ˆLˆ, ˆMˆ: In_Format ← new(MPrefixFormatPtr, Init(lLex.Kind, lLex.Nr, lArgsNbr));
      ˆKˆ: begin lRightSymNr ← GetIntAttr(XMLAttrName[atRightSymbolNr]);
        In_Format ← new(MBracketFormatPtr, Init(lLex.Nr, lRightSymNr, lArgsNbr, 0, 0));
        end;
    othercases RunTimeError(2019);
    endcases;
    AcceptEndState; NextElementState;
  end;
end;
```

This code is used in section 777.

805. Conversely, we can print to an output stream an XML representation for a format object.

⟨Implement *MFormatObj* 805⟩ ≡

```
procedure MFormatObj.Out_Format(var fOutFile : XMLOutStreamObj; aFormNr : integer);
begin with fOutFile do
  begin Out_XElStart(XMLElemName[elFormat]); Out_XAttr(XMLAttrName[atKind], fSymbol.Kind);
  if aFormNr > 0 then Out_XIntAttr(XMLAttrName[atNr], aFormNr);
  Out_XIntAttr(XMLAttrName[atSymbolNr], fSymbol.Nr);
  case fSymbol.Kind of
    'J', 'U', 'V', 'G', 'L', 'M':
      Out_XIntAttr(XMLAttrName[atArgNr], MPrefixFormatPtr(@Self)↑.fRightArgsNbr);
    'O', 'R': with MInfixFormatPtr(@Self)↑ do
      begin Out_XIntAttr(XMLAttrName[atArgNr], fLeftArgsNbr + fRightArgsNbr);
      Out_XIntAttr(XMLAttrName[atLeftArgNr], fLeftArgsNbr);
      end;
    'K': with MBracketFormatPtr(@Self)↑ do
      begin Out_XIntAttr(XMLAttrName[atArgNr], fArgsNbr);
      Out_XIntAttr(XMLAttrName[atRightSymbolNr], fRightSymbolNr);
      end;
  othercases RuntimeError(3300);
endcases;
  Out_XElEnd0;
end;
end;
```

This code is used in section 777.

806. Given a list of formats, we can store them to an XML file using the previous function.

```
procedure MFormatsList.StoreFormats(fName : string);
var lEnvFile : XMLOutStreamObj; z : integer;
begin lEnvFile.OpenFile(fName);
with lEnvFile do
  begin Out_XElStart0(XMLElemName[elFormats]);
  for z ← 0 to Count − 1 do MFormatPtr(Items↑[z])↑.Out_Format(lEnvFile, z + 1);
  with gPriority do
    for z ← 0 to fCount − 1 do
      begin Out_XElStart(XMLElemName[elPriority]);
      Out_XAttr(XMLAttrName[atKind], chr(fList↑[z].X1));
      Out_XIntAttr(XMLAttrName[atSymbolNr], fList↑[z].X2);
      Out_XIntAttr(XMLAttrName[atValue], fList↑[z].Y); Out_XElEnd0;
      end;
    Out_XElEnd(XMLElemName[elFormats]);
  end;
lEnvFile.Done;
end;
```

807. We clean up the formats collection and the priority. The *gPriority* is initialized and populated in other functions. The *gFormatsColl* is used heavily in *parseraddition.pas* and a few other places.

```
procedure DisposeFormats;
begin gFormatsColl.Done; gPriority.Done;
end;
```

File 18

Syntax

808. This describes the syntax for the Mizar language, using expressions, subexpressions, blocks, and “items” (statements).

We will need to recall *StackedObj* from `mobjects.pas` (§436).

```

<syntax.pas 808> ≡
  <GNU License 4>
unit syntax;
interface
  uses mobjects, errhan; <Interface for syntax.pas 815>
implementation
  uses mconsole
    mdebug , info end_mdebug;
    <Implementation for syntax.pas 810>
end .

```

809. The maximum number of “visible” arguments to an expression is set here, at 10.

```

<Public constants for syntax.pas 809> ≡
const MaxVisArgNbr = 10;

```

This code is used in section 815.

810. The implementation for the abstract syntax of Mizar is rather uninteresting, since most of the methods are abstract.

```

<Implementation for syntax.pas 810> ≡
  <Subexpression constructor 841>
  <Subexpression destructor 842>
  <Expression constructor 838>
  <Subexpression procedures 845>
  <Create a subexpression for an expression 839>
  <Item object implementation 831>
  <Block object implementation 821>
  <Public procedures implementation for syntax.pas 811>

```

This code is used in section 808.

811. Destructor wrappers. We have a few public-facing procedures to free the global subexpression, expression, etc., variables describing the state of the parser.

```

<Public procedures implementation for syntax.pas 811> ≡
procedure KillSubexpression;
begin if gSubexpPtr = nil then RunTimeError(2144)
else dispose(gSubexpPtr, Done);
end;

```

See also sections 812, 813, and 814.

This code is used in section 810.

812.

```

⟨Public procedures implementation for syntax.pas 811⟩ +≡
procedure KillExpression;
  begin if gExpPtr = nil then RunTimeError(2143)
  else dispose(gExpPtr, Done);
  end;

```

813. This method will not be used until we get to the parser, sadly. I am not sure why there are calls to *DisplayLine* in *KillItem* and *KillBlock*, though.

The *KillItem* is called in exactly two places: (1) *Semicolon* in *parser.pas*, (2) *SchemeBlock*, also in the parser. (And *KillBlock* is called only in the parser, as well.)

```

⟨Public procedures implementation for syntax.pas 811⟩ +≡
procedure KillItem;
  begin if gItemPtr = nil then RunTimeError(2142)
  else begin gItemPtr↑.Pop; dispose(gItemPtr, Done); end;
  DisplayLine(CurPos.Line, ErrorNbr);
  end;

```

814.

```

⟨Public procedures implementation for syntax.pas 811⟩ +≡
procedure KillBlock;
  begin if gBlockPtr = nil then RunTimeError(2141)
  else begin gBlockPtr↑.Pop; dispose(gBlockPtr, Done);
  end;
  DisplayLine(CurPos.Line, ErrorNbr);
  end;

```

815.

```

⟨Interface for syntax.pas 815⟩ ≡
  ⟨Public constants for syntax.pas 809⟩
type ⟨BlockKinds (syntax.pas) 819⟩
  ⟨ItemKinds (syntax.pas) 829⟩
  ⟨ExpKinds (syntax.pas) 836⟩
  ⟨Block object interface 820⟩;
  ⟨Class declaration for Item object 830⟩;
  ⟨Subexpression object class 840⟩;
  ⟨Expression class declaration 837⟩;
  ⟨Public procedures for syntax.pas 816⟩
  ⟨Public variables for syntax.pas 817⟩

```

This code is used in section 808.

```

816.  ⟨Public procedures for syntax.pas 816⟩ ≡
procedure KillBlock;
procedure KillItem;
procedure KillExpression;
procedure KillSubexpression;

```

This code is used in section 815.

817. These global public variables for syntax will be manipulated by the parser.

⟨Public variables for `syntax.pas` 817⟩ ≡

```
var gBlockPtr: BlockPtr = nil; gItemPtr: ItemPtr = nil; gExpPtr: ExpressionPtr = nil;  
    gSubexpPtr: SubexpPtr = nil;
```

This code is used in section 815.

Section 18.1. BLOCK OBJECT

818. The Mizar language is block-structured, so we have a Block represent a sequence of statements contained within a block.

This is extended in `parseraddition.pas`.



Fig. 1. UML class diagram for Block object class.

819. There are about a dozen different kinds of blocks.

```

⟨BlockKinds (syntax.pas) 819⟩ ≡
  BlockKind = (blMain, blDiffuse, blHereby, blProof, blDefinition, blNotation, blRegistration, blCase,
    blSuppose, blPublicScheme);

```

This code is used in section 815.

```

820. ⟨Block object interface 820⟩ ≡
  BlockPtr = ↑BlockObj;
  ItemPtr = ↑ItemObj;
  BlockObj = object (StackedObj)
    nBlockKind: BlockKind;
    constructor Init(fBlockKind : BlockKind);
    procedure Pop; virtual; { inheritance }
    destructor Done; virtual;
    procedure StartProperText; virtual;
    procedure ProcessLink; virtual;
    procedure ProcessRedefine; virtual;
    procedure ProcessBegin; virtual;
    procedure ProcessPragma; virtual;
    procedure StartAtSignProof; virtual;
    procedure FinishAtSignProof; virtual;
    procedure FinishDefinition; virtual;
    procedure CreateItem(fItemKind : ItemKind); virtual;
    procedure CreateBlock(fBlockKind : BlockKind); virtual;
    procedure StartSchemeDemonstration; virtual;
    procedure FinishSchemeDemonstration; virtual;
  end

```

This code is used in section 815.

821. The constructor for a Block will initialize its *Previous* pointer to point at the global *gBlockPtr* instance.

```

⟨Block object implementation 821⟩ ≡
constructor BlockObj.Init(fBlockKind : BlockKind);
  begin nBlockKind ← fBlockKind; Previous ← gBlockPtr;
  end;

```

See also sections 822, 823, 824, 825, 826, and 827.

This code is used in section 810.

822. Note that popping a block object is left for subclasses to handle.

⟨Block object implementation 821⟩ +≡
procedure *BlockObj.Pop*;
 begin end;

823. ⟨Block object implementation 821⟩ +≡
destructor *BlockObj.Done*;
 begin *gBlockPtr* ← *BlockPtr(Previous)*;
 end;

824. Abstract methods.

⟨Block object implementation 821⟩ +≡
procedure *BlockObj.StartProperText*;
 begin end;
procedure *BlockObj.ProcessRedefine*;
 begin end;
procedure *BlockObj.ProcessLink*;
 begin end;
procedure *BlockObj.ProcessBegin*;
 begin end;
procedure *BlockObj.ProcessPragma*;
 begin end;
procedure *BlockObj.StartAtSignProof*;
 begin end;
procedure *BlockObj.FinishAtSignProof*;
 begin end;
procedure *BlockObj.FinishDefinition*;
 begin end;

825. ⟨Block object implementation 821⟩ +≡
procedure *BlockObj.CreateItem*(*fItemKind* : *ItemKind*);
 begin *gItemPtr* ← *new(ItemPtr, Init(fItemKind))*;
 end;

826. ⟨Block object implementation 821⟩ +≡
procedure *BlockObj.CreateBlock*(*fBlockKind* : *BlockKind*);
 begin *gBlockPtr* ← *new(BlockPtr, Init(fBlockKind))*;
 end;

827. More abstract methods.

⟨Block object implementation 821⟩ +≡
procedure *BlockObj.StartSchemeDemonstration*;
 begin end;
procedure *BlockObj.FinishSchemeDemonstration*;
 begin end;

Section 18.2. ITEM OBJECTS

828. The class declaration for an *Item* object is depressingly long, with most of its virtual methods not used. The class diagram is worth drawing out.



Fig. 2. UML class diagram for Item object class.

829. Items are a tagged union, tagged by the “kind” of item.

⟨ItemKinds (syntax.pas) 829⟩ ≡

```

ItemKind = (itIncorrItem, itDefinition, itSchemeBlock, itSchemeHead, itTheorem, itAxiom,
            itReservation, itCanceled, itSection, itRegularStatement, itChoice, itReconsider, itPrivFuncDefinition,
            itPrivPredDefinition, itConstantDefinition, itGeneralization, itLocDeclaration,
            itExistentialAssumption, itExemplification, itPerCases, itConclusion, itCaseBlock, itCaseHead,
            itSupposeHead, itAssumption, itCorrCond, itCorrectness, itProperty, itDefPred, itDefFunc,
            itDefMode, itDefAttr, itDefStruct, itPredSynonym, itPredAntonym, itFuncNotation, itModeNotation,
            itAttrSynonym, itAttrAntonym, itCluster, itIdentify, itReduction, itPropertyRegistration, itPragma);

```

This code is used in section 815.

830. ⟨Class declaration for Item object 830⟩ ≡

```

ItemObj = object (StackedObj)
  nItemKind: ItemKind;
  constructor Init(fItemKind : ItemKind);
  procedure Pop; virtual;
  destructor Done; virtual;
  ⟨Method declarations for Item object 834⟩
end

```

This code is used in section 815.

831. It is particularly important to note, when constructing an *Item* object, the previous item will *automatically* be set to point to the global *gItem* variable.

⟨Item object implementation 831⟩ ≡

```

constructor ItemObj.Init(fItemKind : ItemKind);
begin nItemKind ← fItemKind; Previous ← gItemPtr;
end;
procedure ItemObj.Pop;
begin DisplayLine(CurPos.Line, ErrorNbr);
end;
destructor ItemObj.Done;
begin DisplayLine(CurPos.Line, ErrorNbr); gItemPtr ← ItemPtr(Previous);
end;

```

See also sections 832 and 835.

This code is used in section 810.

832. Creating an expression in an item is handled with this method.

⟨Item object implementation 831⟩ +≡

```
procedure ItemObj.CreateExpression(fExpKind : ExpKind);
  begin gExpPtr  $\leftarrow$  new(ExpressionPtr, Init(fExpKind));
  end;
```

833. Abstract methods. The methods of the *Item* class can be partitioned into two groups: those which will be implemented by a subclass, and those which will remain “empty” (i.e., whose body is just **begin end**).

⟨Methods overridden by extended Item class 833⟩ ≡

```

procedure StartSentence; virtual;
procedure StartAttributes; virtual;
procedure FinishAntecedent; virtual;
procedure FinishConsequent; virtual;
procedure FinishClusterTerm; virtual;
procedure StartFuncIdentify; virtual;
procedure ProcessFuncIdentify; virtual;
procedure CompleteFuncIdentify; virtual;
procedure ProcessLeftLocus; virtual;
procedure ProcessRightLocus; virtual;
procedure StartFuncReduction; virtual;
procedure ProcessFuncReduction; virtual;
procedure FinishPrivateConstant; virtual;
procedure StartFixedVariables; virtual;
procedure ProcessFixedVariable; virtual;
procedure ProcessBeing; virtual;
procedure StartFixedSegment; virtual;
procedure FinishFixedSegment; virtual;
procedure FinishFixedVariables; virtual;
procedure StartAssumption; virtual;
procedure StartCollectiveAssumption; virtual;
procedure ProcessMeans; virtual;
procedure FinishOtherwise; virtual;
procedure StartDefiniens; virtual;
procedure FinishDefiniens; virtual;
procedure StartGuard; virtual;
procedure FinishGuard; virtual;
procedure ProcessEquals; virtual;
procedure StartExpansion; virtual;
procedure FinishSpecification; virtual;
procedure StartConstructionType; virtual;
procedure FinishConstructionType; virtual;
procedure StartAttributePattern; virtual;
procedure FinishAttributePattern; virtual;
procedure FinishSethoodProperties; virtual;
procedure StartModePattern; virtual;
procedure FinishModePattern; virtual;
procedure StartPredicatePattern; virtual;
procedure ProcessPredicateSymbol; virtual;
procedure FinishPredicatePattern; virtual;
procedure StartFunctorPattern; virtual;
procedure ProcessFunctorSymbol; virtual;
procedure FinishFunctorPattern; virtual;
procedure ProcessAttrAntonym; virtual;
procedure ProcessAttrSynonym; virtual;
procedure ProcessPredAntonym; virtual;
procedure ProcessPredSynonym; virtual;

```

```

procedure ProcessFuncSynonym; virtual;
procedure ProcessModeSynonym; virtual;
procedure StartVisible; virtual;
procedure ProcessVisible; virtual;
procedure FinishPrefix; virtual;
procedure ProcessStructureSymbol; virtual;
procedure StartFields; virtual;
procedure FinishFields; virtual;
procedure StartAggrPattSegment; virtual;
procedure ProcessField; virtual;
procedure FinishAggrPattSegment; virtual;
procedure ProcessSchemeName; virtual;
procedure StartSchemeSegment; virtual;
procedure StartSchemeQualification; virtual;
procedure FinishSchemeQualification; virtual;
procedure ProcessSchemeVariable; virtual;
procedure FinishSchemeSegment; virtual;
procedure FinishSchemeThesis; virtual;
procedure FinishSchemePremise; virtual;

procedure StartReservationSegment; virtual;
procedure ProcessReservedIdentifier; virtual;
procedure FinishReservationSegment; virtual;
procedure StartPrivateDefiniendum; virtual;
procedure FinishLocusType; virtual;

procedure CreateExpression(fExpKind : ExpKind); virtual;

procedure StartPrivateConstant; virtual;
procedure StartPrivateDefiniens; virtual;
procedure FinishPrivateFuncDefinienition; virtual;
procedure FinishPrivatePredDefinienition; virtual;
procedure ProcessReconsideredVariable; virtual;
procedure FinishReconsideredTerm; virtual;
procedure FinishDefaultTerm; virtual;
procedure FinishCondition; virtual;
procedure FinishHypothesis; virtual;
procedure ProcessExemplifyingVariable; virtual;
procedure FinishExemplifyingVariable; virtual;
procedure StartExemplifyingTerm; virtual;
procedure FinishExemplifyingTerm; virtual;
procedure ProcessCorrectness; virtual;
procedure ProcessLabel; virtual;
procedure StartRegularStatement; virtual;
procedure ProcessDefiniensLabel; virtual;
procedure FinishCompactStatement; virtual;
procedure StartIterativeStep; virtual;
procedure FinishIterativeStep; virtual;

    { Justification }
procedure ProcessSchemeReference; virtual;
procedure ProcessPrivateReference; virtual;
procedure StartLibraryReferences; virtual;
procedure StartSchemeLibraryReference; virtual;
procedure ProcessDef; virtual;

```

```
procedure ProcessTheoremNumber; virtual;  
procedure ProcessSchemeNumber; virtual;  
procedure StartJustification; virtual;  
procedure StartSimpleJustification; virtual;  
procedure FinishSimpleJustification; virtual;
```

See also section [1371](#).

This code is used in sections [834](#) and [1372](#).

834. \langle Method declarations for Item object 834 $\rangle \equiv$
 \langle Methods overridden by extended Item class 833 \rangle

```

procedure FinishClusterType; virtual;
procedure FinishSentence; virtual;
procedure FinishReconsidering; virtual;
procedure StartNewType; virtual;
procedure StartCondition; virtual;
procedure FinishChoice; virtual;
procedure FinishAssumption; virtual;

procedure StartEquals; virtual;
procedure StartOtherwise; virtual;
procedure StartSpecification; virtual;
procedure ProcessAttributePattern; virtual;
procedure StartDefPredicate; virtual;

procedure CompletePredAntonymByAttr; virtual;
procedure CompletePredSynonymByAttr; virtual;

procedure StartPredIdentify; virtual;
procedure ProcessPredIdentify; virtual;
procedure CompleteAttrIdentify; virtual;
procedure StartAttrIdentify; virtual;
procedure ProcessAttrIdentify; virtual;
procedure CompletePredIdentify; virtual;

procedure FinishFuncReduction; virtual;
procedure StartSethoodProperties; virtual;
procedure ProcessModePattern; virtual;
procedure StartPrefix; virtual;
procedure FinishVisible; virtual;
procedure FinishSchemeHeading; virtual;
procedure FinishSchemeDeclaration; virtual;
procedure StartSchemePremise; virtual;
procedure StartTheoremBody; virtual;
procedure FinishTheoremBody; virtual;
procedure FinishTheorem; virtual;
procedure FinishReservation; virtual;
procedure ProcessIterativeStep; virtual;

    { Justification }
procedure StartSchemeReference; virtual;
procedure StartReferences; virtual;
procedure ProcessSch; virtual;
procedure FinishTheLibraryReferences; virtual;
procedure FinishSchLibraryReferences; virtual;
procedure FinishReferences; virtual;
procedure FinishSchemeReference; virtual;
procedure FinishJustification; virtual;

```

This code is used in section 830.

835. \langle Item object implementation 831 $\rangle + \equiv$

```

procedure ItemObj.StartAttributes;
  begin end;
procedure ItemObj.FinishAntecedent;
  begin end;
procedure ItemObj.FinishConsequent;
  begin end;
procedure ItemObj.FinishClusterTerm;
  begin end;
procedure ItemObj.FinishClusterType;
  begin end;
procedure ItemObj.StartSentence;
  begin end;
procedure ItemObj.FinishSentence;
  begin end;
procedure ItemObj.FinishPrivateConstant;
  begin end;
procedure ItemObj.StartPrivateConstant;
  begin end;
procedure ItemObj.ProcessReconsideredVariable;
  begin end;
procedure ItemObj.FinishReconsidering;
  begin end;
procedure ItemObj.FinishReconsideredTerm;
  begin end;
procedure ItemObj.FinishDefaultTerm;
  begin end;
procedure ItemObj.StartNewType;
  begin end;
procedure ItemObj.StartCondition;
  begin end;
procedure ItemObj.FinishCondition;
  begin end;
procedure ItemObj.FinishChoice;
  begin end;
procedure ItemObj.StartFixedVariables;
  begin end;
procedure ItemObj.StartFixedSegment;
  begin end;
procedure ItemObj.ProcessFixedVariable;
  begin end;
procedure ItemObj.ProcessBeing;
  begin end;
procedure ItemObj.FinishFixedSegment;
  begin end;
procedure ItemObj.FinishFixedVariables;
  begin end;
procedure ItemObj.StartAssumption;
  begin end;
procedure ItemObj.StartCollectiveAssumption;
  begin end;
procedure ItemObj.FinishHypothesis;

```

```

    begin end;
  procedure ItemObj.FinishAssumption;
    begin end;
  procedure ItemObj.ProcessExemplifyingVariable;
    begin end;
  procedure ItemObj.FinishExemplifyingVariable;
    begin end;
  procedure ItemObj.StartExemplifyingTerm;
    begin end;
  procedure ItemObj.FinishExemplifyingTerm;
    begin end;
  procedure ItemObj.ProcessMeans;
    begin end;
  procedure ItemObj.FinishOtherwise;
    begin end;
  procedure ItemObj.StartDefiniens;
    begin end;
  procedure ItemObj.FinishDefiniens;
    begin end;
  procedure ItemObj.StartGuard;
    begin end;
  procedure ItemObj.FinishGuard;
    begin end;
  procedure ItemObj.StartOtherwise;
    begin end;
  procedure ItemObj.ProcessEquals;
    begin end;
  procedure ItemObj.StartEquals;
    begin end;
  procedure ItemObj.ProcessCorrectness;
    begin end;
  procedure ItemObj.FinishSpecification;
    begin end;
  procedure ItemObj.FinishConstructionType;
    begin end;
  procedure ItemObj.StartSpecification;
    begin end;
  procedure ItemObj.StartExpansion;
    begin end;
  procedure ItemObj.StartConstructionType;
    begin end;
  procedure ItemObj.StartPredicatePattern;
    begin end;
  procedure ItemObj.ProcessPredicateSymbol;
    begin end;
  procedure ItemObj.FinishPredicatePattern;
    begin end;
  procedure ItemObj.StartFunctorPattern;
    begin end;
  procedure ItemObj.ProcessFunctorSymbol;
    begin end;
  procedure ItemObj.FinishFunctorPattern;

```

```

    begin end;
  procedure ItemObj.ProcessAttrAntonym;
    begin end;
  procedure ItemObj.ProcessAttrSynonym;
    begin end;
  procedure ItemObj.ProcessPredAntonym;
    begin end;
  procedure ItemObj.ProcessPredSynonym;
    begin end;
  procedure ItemObj.ProcessFuncSynonym;
    begin end;
  procedure ItemObj.CompletePredSynonymByAttr;
    begin end;
  procedure ItemObj.CompletePredAntonymByAttr;
    begin end;
  procedure ItemObj.ProcessModeSynonym;
    begin end;
  procedure ItemObj.StartFuncIdentify;
    begin end;
  procedure ItemObj.ProcessFuncIdentify;
    begin end;
  procedure ItemObj.CompleteFuncIdentify;
    begin end;
  procedure ItemObj.StartPredIdentify;
    begin end;
  procedure ItemObj.ProcessPredIdentify;
    begin end;
  procedure ItemObj.CompletePredIdentify;
    begin end;
  procedure ItemObj.StartAttrIdentify;
    begin end;
  procedure ItemObj.ProcessAttrIdentify;
    begin end;
  procedure ItemObj.CompleteAttrIdentify;
    begin end;
  procedure ItemObj.ProcessLeftLocus;
    begin end;
  procedure ItemObj.ProcessRightLocus;
    begin end;
  procedure ItemObj.StartFuncReduction;
    begin end;
  procedure ItemObj.ProcessFuncReduction;
    begin end;
  procedure ItemObj.FinishFuncReduction;
    begin end;
  procedure ItemObj.StartSethoodProperties;
    begin end;
  procedure ItemObj.FinishSethoodProperties;
    begin end;
  procedure ItemObj.StartModePattern;
    begin end;
  procedure ItemObj.ProcessModePattern;

```



```

    begin end;
  procedure ItemObj.FinishModePattern;
    begin end;
  procedure ItemObj.StartAttributePattern;
    begin end;
  procedure ItemObj.ProcessAttributePattern;
    begin end;
  procedure ItemObj.FinishAttributePattern;
    begin end;
  procedure ItemObj.StartDefPredicate;
    begin end;
  procedure ItemObj.StartVisible;
    begin end;
  procedure ItemObj.ProcessVisible;
    begin end;
  procedure ItemObj.FinishVisible;
    begin end;
  procedure ItemObj.StartPrefix;
    begin end;
  procedure ItemObj.FinishPrefix;
    begin end;
  procedure ItemObj.ProcessStructureSymbol;
    begin end;
  procedure ItemObj.StartFields;
    begin end;
  procedure ItemObj.FinishFields;
    begin end;
  procedure ItemObj.StartAggrPattSegment;
    begin end;
  procedure ItemObj.ProcessField;
    begin end;
  procedure ItemObj.FinishAggrPattSegment;
    begin end;
  procedure ItemObj.ProcessSchemeName;
    begin end;
  procedure ItemObj.StartSchemeSegment;
    begin end;
  procedure ItemObj.ProcessSchemeVariable;
    begin end;
  procedure ItemObj.StartSchemeQualification;
    begin end;
  procedure ItemObj.FinishSchemeQualification;
    begin end;
  procedure ItemObj.FinishSchemeSegment;
    begin end;
  procedure ItemObj.FinishSchemeHeading;
    begin end;
  procedure ItemObj.FinishSchemeDeclaration;
    begin end;
  procedure ItemObj.FinishSchemeThesis;
    begin end;
  procedure ItemObj.StartSchemePremise;

```

```

    begin end;
  procedure ItemObj.FinishSchemePremise;
    begin end;
  procedure ItemObj.StartTheoremBody;
    begin end;
  procedure ItemObj.FinishTheoremBody;
    begin end;
  procedure ItemObj.FinishTheorem;
    begin end;
  procedure ItemObj.StartReservationSegment;
    begin end;
  procedure ItemObj.ProcessReservedIdentifier;
    begin end;
  procedure ItemObj.FinishReservationSegment;
    begin end;
  procedure ItemObj.FinishReservation;
    begin end;
  procedure ItemObj.StartPrivateDefiniendum;
    begin end;
  procedure ItemObj.FinishLocusType;
    begin end;
  procedure ItemObj.StartPrivateDefiniens;
    begin end;
  procedure ItemObj.FinishPrivateFuncDefinienition;
    begin end;
  procedure ItemObj.FinishPrivatePredDefinienition;
    begin end;
  procedure ItemObj.ProcessLabel;
    begin end;
  procedure ItemObj.StartRegularStatement;
    begin end;
  procedure ItemObj.ProcessDefiniensLabel;
    begin end;
  procedure ItemObj.ProcessSchemeReference;
    begin end;
  procedure ItemObj.StartSchemeReference;
    begin end;
  procedure ItemObj.StartReferences;
    begin end;
  procedure ItemObj.ProcessPrivateReference;
    begin end;
  procedure ItemObj.StartLibraryReferences;
    begin end;
  procedure ItemObj.StartSchemeLibraryReference;
    begin end;
  procedure ItemObj.ProcessDef;
    begin end;
  procedure ItemObj.ProcessSch;
    begin end;
  procedure ItemObj.ProcessTheoremNumber;
    begin end;
  procedure ItemObj.ProcessSchemeNumber;

```

```
    begin end;  
procedure ItemObj.FinishTheLibraryReferences;  
    begin end;  
procedure ItemObj.FinishSchLibraryReferences;  
    begin end;  
procedure ItemObj.FinishReferences;  
    begin end;  
procedure ItemObj.FinishSchemeReference;  
    begin end;  
procedure ItemObj.StartJustification;  
    begin end;  
procedure ItemObj.FinishJustification;  
    begin end;  
procedure ItemObj.StartSimpleJustification;  
    begin end;  
procedure ItemObj.FinishSimpleJustification;  
    begin end;  
procedure ItemObj.FinishCompactStatement;  
    begin end;  
procedure ItemObj.StartIterativeStep;  
    begin end;  
procedure ItemObj.ProcessIterativeStep;  
    begin end;  
procedure ItemObj.FinishIterativeStep;  
    begin end;
```

Section 18.3. EXPRESSIONS**836.**

⟨ ExpKinds (syntax.pas) 836 ⟩ ≡
ExpKind = (*exNull*, *exType*, *exTerm*, *exFormula*, *exResType*, *exAdjectiveCluster*);

This code is used in section 815.

837. ⟨ Expression class declaration 837 ⟩ ≡

```

ExpressionPtr = ↑ExpressionObj;
ExpressionObj = object (MObject)
  nExpKind: ExpKind;
  constructor Init(fExpKind : ExpKind);
  procedure CreateSubexpression; virtual;
end

```

This code is used in section 815.

838. Constructor.

⟨ Expression constructor 838 ⟩ ≡
constructor *ExpressionObj.Init*(*fExpKind* : *ExpKind*);
begin *nExpKind* ← *fExpKind*;
end;

This code is used in section 810.

839. Observe that creating a subexpression (1) allocates a new *SubexpPtr* on the heap, and (2) mutates the *gSubexpPtr* global variable.

⟨ Create a subexpression for an expression 839 ⟩ ≡
procedure *ExpressionObj.CreateSubexpression*;
begin *gSubexpPtr* ← *new*(*SubexpPtr*, *Init*);
end;

This code is used in section 810.

Section 18.4. SUBEXPRESSIONS**840.**

```

⟨ Subexpression object class 840 ⟩ ≡
  SubexpPtr = ↑SubexpObj;
  SubexpObj = object (StackedObj)
    constructor Init;
    destructor Done; virtual;
    ⟨ Empty method declarations for SubexpObj 844 ⟩
end

```

This code is used in section 815.

841. Constructor. Importantly, constructing a new *Subexp* object will initialize its *Previous* field to point to the global *gSubexpPtr* object.

```

⟨ Subexpression constructor 841 ⟩ ≡
constructor SubexpObj.Init;
  begin Previous ← gSubexpPtr;
end;

```

This code is used in section 810.

842. Destructor.

```

⟨ Subexpression destructor 842 ⟩ ≡
destructor SubexpObj.Done;
  begin gSubexpPtr ← SubexpPtr(Previous);
end;

```

This code is used in section 810.

843. The remaining methods for subexpression objects are empty.

(Methods implemented by subclasses of *SubexpObj* 843) \equiv

```

procedure ProcessSimpleTerm; virtual;
procedure StartFraenkelTerm; virtual;
procedure StartPostqualification; virtual;
procedure StartPostqualifyingSegment; virtual;
procedure ProcessPostqualifiedVariable; virtual;
procedure StartPostqualificationSpecyfication; virtual;
procedure FinishPostqualifyingSegment; virtual;
procedure FinishFraenkelTerm; virtual;
procedure StartSimpleFraenkelTerm; virtual;
procedure FinishSimpleFraenkelTerm; virtual;
procedure ProcessThesis; virtual;
procedure StartPrivateTerm; virtual;
procedure FinishPrivateTerm; virtual;
procedure StartBracketedTerm; virtual;
procedure FinishBracketedTerm; virtual;
procedure StartAggregateTerm; virtual;
procedure FinishAggregateTerm; virtual;
procedure StartSelectorTerm; virtual;
procedure FinishSelectorTerm; virtual;
procedure StartForgetfulTerm; virtual;
procedure FinishForgetfulTerm; virtual;
procedure StartChoiceTerm; virtual;
procedure FinishChoiceTerm; virtual;
procedure ProcessNumeralTerm; virtual;
procedure ProcessItTerm; virtual;
procedure ProcessLocusTerm; virtual;
procedure ProcessQua; virtual;
procedure FinishQualifiedTerm; virtual;
procedure ProcessExactly; virtual;
procedure StartLongTerm; virtual;
procedure ProcessFunctorSymbol; virtual;
procedure FinishArgList; virtual;
procedure FinishLongTerm; virtual;
procedure FinishArgument; virtual;
procedure FinishTerm; virtual;
procedure StartType; virtual;
procedure ProcessModeSymbol; virtual;
procedure FinishType; virtual;
procedure CompleteType; virtual; { + }
procedure ProcessAtomicFormula; virtual;
procedure ProcessPredicateSymbol; virtual;
procedure ProcessRightSideOfPredicateSymbol; virtual;
procedure FinishPredicativeFormula; virtual;
procedure FinishRightSideOfPredicativeFormula; virtual;
procedure StartMultiPredicativeFormula; virtual;
procedure FinishMultiPredicativeFormula; virtual;
procedure StartPrivateFormula; virtual; { + }
procedure FinishPrivateFormula; virtual;
procedure ProcessContradiction; virtual;
procedure ProcessNegative; virtual;

```

{ This is a temporary solution, the generation of ExpNodes is such that it is not possible to handle negation uniformly. }

{ Jest to tymczasowe rozwiązanie, generowanie ExpNode'ów jest takie, że nie ma możliwości obsługi jednolitej negacji. }

```

procedure ProcessNegation; virtual;
procedure FinishQualifyingFormula; virtual;
procedure FinishAttributiveFormula; virtual;
procedure ProcessBinaryConnective; virtual;    { + }
procedure ProcessFlexDisjunction; virtual;
procedure ProcessFlexConjunction; virtual;
procedure StartRestriction; virtual;
procedure FinishRestriction; virtual;
procedure FinishBinaryFormula; virtual;
procedure FinishFlexDisjunction; virtual;
procedure FinishFlexConjunction; virtual;
procedure StartExistential; virtual;
procedure FinishExistential; virtual;
procedure StartUniversal; virtual;
procedure FinishUniversal; virtual;    { + }
procedure StartQualifiedSegment; virtual;
procedure StartQualifyingType; virtual;
procedure FinishQualifiedSegment; virtual;
procedure ProcessVariable; virtual;
procedure StartAttributes; virtual;

procedure ProcessNon; virtual;    { + }
procedure ProcessAttribute; virtual;    { + }
procedure StartAttributeArguments; virtual;    { + }
procedure CompleteAttributeArguments; virtual;    { + }
procedure FinishAttributeArguments; virtual;    { + }
procedure CompleteAdjectiveCluster; virtual;    { + }
procedure CompleteClusterTerm; virtual;

    { Errors Recovery }
procedure InsertIncorrTerm; virtual;
procedure InsertIncorrType; virtual;
procedure InsertIncorrBasic; virtual;
procedure InsertIncorrFormula; virtual;

```

See also section 1534.

This code is used in sections 844 and 1535.

844. \langle Empty method declarations for *SubexpObj* 844 $\rangle \equiv$
 \langle Methods implemented by subclasses of *SubexpObj* 843 \rangle

```

procedure FinishSample; virtual;
procedure ProcessThe; virtual;
procedure StartArgument; virtual;
procedure ProcessLeftParenthesis; virtual;
procedure ProcessRightParenthesis; virtual;
procedure StartAtomicFormula; virtual;

procedure ProcessHolds; virtual;
procedure FinishQuantified; virtual;
procedure ProcessNot; virtual;
procedure ProcessDoesNot; virtual;

procedure StartAdjectiveCluster; virtual;
procedure FinishAdjectiveCluster; virtual;

procedure FinishAttributes; virtual;
procedure CompleteAttributes; virtual;
procedure CompleteClusterType; virtual;
procedure FinishEquality; virtual;

```

This code is used in section 840.

845.

(Subexpression procedures 845) \equiv
procedure *SubexpObj.StartAttributes*;
 begin end;
procedure *SubexpObj.StartAdjectiveCluster*;
 begin end;
procedure *SubexpObj.FinishAdjectiveCluster*;
 begin end;
procedure *SubexpObj.ProcessNon*;
 begin end;
procedure *SubexpObj.ProcessAttribute*;
 begin end;
procedure *SubexpObj.FinishAttributes*;
 begin end;
procedure *SubexpObj.CompleteAttributes*;
 begin end;
procedure *SubexpObj.StartAttributeArguments*;
 begin end;
procedure *SubexpObj.CompleteAttributeArguments*;
 begin end;
procedure *SubexpObj.FinishAttributeArguments*;
 begin end;
procedure *SubexpObj.CompleteAdjectiveCluster*;
 begin end;
procedure *SubexpObj.CompleteClusterTerm*;
 begin end;
procedure *SubexpObj.CompleteClusterType*;
 begin end;
procedure *SubexpObj.ProcessSimpleTerm*;
 begin end;
procedure *SubexpObj.ProcessQua*;
 begin end;
procedure *SubexpObj.FinishQualifiedTerm*;
 begin end;
procedure *SubexpObj.ProcessExactly*;
 begin end;
procedure *SubexpObj.StartArgument*;
 begin end;
procedure *SubexpObj.FinishArgument*;
 begin end;
procedure *SubexpObj.FinishTerm*;
 begin end;
procedure *SubexpObj.StartType*;
 begin end;
procedure *SubexpObj.ProcessModeSymbol*;
 begin end;
procedure *SubexpObj.FinishType*;
 begin end;
procedure *SubexpObj.CompleteType*;
 begin end;
procedure *SubexpObj.StartLongTerm*;
 begin end;

```

procedure SubexpObj.FinishLongTerm;
  begin end;
procedure SubexpObj.FinishArgList;
  begin end;
procedure SubexpObj.ProcessFunctorSymbol;
  begin end;
procedure SubexpObj.StartFraenkelTerm;
  begin end;
procedure SubexpObj.FinishSample;
  begin end;
procedure SubexpObj.StartPostqualification;
  begin end;
procedure SubexpObj.StartPostqualificationSpecyfification;
  begin end;
procedure SubexpObj.StartPostqualifyingSegment;
  begin end;
procedure SubexpObj.ProcessPostqualifiedVariable;
  begin end;
procedure SubexpObj.FinishPostqualifyingSegment;
  begin end;
procedure SubexpObj.FinishFraenkelTerm;
  begin end;
procedure SubexpObj.StartSimpleFraenkelTerm;
  begin end;
procedure SubexpObj.FinishSimpleFraenkelTerm;
  begin end;
procedure SubexpObj.StartPrivateTerm;
  begin end;
procedure SubexpObj.FinishPrivateTerm;
  begin end;
procedure SubexpObj.StartBracketedTerm;
  begin end;
procedure SubexpObj.FinishBracketedTerm;
  begin end;
procedure SubexpObj.StartAggregateTerm;
  begin end;
procedure SubexpObj.FinishAggregateTerm;
  begin end;
procedure SubexpObj.ProcessThe;
  begin end;
procedure SubexpObj.StartSelectorTerm;
  begin end;
procedure SubexpObj.FinishSelectorTerm;
  begin end;
procedure SubexpObj.StartForgetfulTerm;
  begin end;
procedure SubexpObj.FinishForgetfulTerm;
  begin end;
procedure SubexpObj.StartChoiceTerm;
  begin end;
procedure SubexpObj.FinishChoiceTerm;
  begin end;

```

```

procedure SubexpObj.ProcessNumeralTerm;
  begin end;
procedure SubexpObj.ProcessItTerm;
  begin end;
procedure SubexpObj.ProcessLocusTerm;
  begin end;
procedure SubexpObj.ProcessThesis;
  begin end;
procedure SubexpObj.StartAtomicFormula;
  begin end;
procedure SubexpObj.ProcessAtomicFormula;
  begin end;
procedure SubexpObj.ProcessPredicateSymbol;
  begin end;
procedure SubexpObj.ProcessRightSideOfPredicateSymbol;
  begin end;
procedure SubexpObj.FinishPredicativeFormula;
  begin end;
procedure SubexpObj.FinishRightSideOfPredicativeFormula;
  begin end;
procedure SubexpObj.StartMultiPredicativeFormula;
  begin end;
procedure SubexpObj.FinishMultiPredicativeFormula;
  begin end;
procedure SubexpObj.FinishQualifyingFormula;
  begin end;
procedure SubexpObj.FinishAttributiveFormula;
  begin end;
procedure SubexpObj.StartPrivateFormula;
  begin end;
procedure SubexpObj.FinishPrivateFormula;
  begin end;
procedure SubexpObj.ProcessContradiction;
  begin end;
procedure SubexpObj.ProcessNot;
  begin end;
procedure SubexpObj.ProcessDoesNot;
  begin end;
procedure SubexpObj.ProcessNegative;
  begin end;
procedure SubexpObj.ProcessNegation;
  begin end;
procedure SubexpObj.StartRestriction;
  begin end;
procedure SubexpObj.FinishRestriction;
  begin end;
procedure SubexpObj.ProcessHolds;
  begin end;
procedure SubexpObj.ProcessBinaryConnective;
  begin end;
procedure SubexpObj.FinishBinaryFormula;
  begin end;

```

```

procedure SubexpObj.ProcessFlexDisjunction;
  begin end;
procedure SubexpObj.ProcessFlexConjunction;
  begin end;
procedure SubexpObj.FinishFlexDisjunction;
  begin end;
procedure SubexpObj.FinishFlexConjunction;
  begin end;
procedure SubexpObj.StartQualifiedSegment;
  begin end;
procedure SubexpObj.StartQualifyingType;
  begin end;
procedure SubexpObj.FinishQualifiedSegment;
  begin end;
procedure SubexpObj.FinishQuantified;
  begin end;
procedure SubexpObj.ProcessVariable;
  begin end;
procedure SubexpObj.StartExistential;
  begin end;
procedure SubexpObj.FinishExistential;
  begin end;
procedure SubexpObj.StartUniversal;
  begin end;
procedure SubexpObj.FinishUniversal;
  begin end;
procedure SubexpObj.ProcessLeftParenthesis;
  begin end;
procedure SubexpObj.ProcessRightParenthesis;
  begin end;
procedure SubexpObj.InsertIncorrType;
  begin end;
procedure SubexpObj.InsertIncorrTerm;
  begin end;
procedure SubexpObj.InsertIncorrBasic;
  begin end;
procedure SubexpObj.InsertIncorrFormula;
  begin end;
procedure SubexpObj.FinishEquality;
  begin end;

```

This code is used in section [810](#).

File 19

MScanner

846. We have the MScanner module transform an article (an input file) into a stream of tokens.

```

<scanner.pas 715> +≡
  <GNU License 4>
unit mscanner;
interface
  uses errhan, mobjects, scanner;
    <Public interface for MScanner 847>
implementation
  uses mizenv;
    <Implementation for MScanner 853>;

end .

```

847. Public types. We have enumerated types for each construction we'll encounter in Mizar.

```

<Public interface for MScanner 847> ≡
type <Token kinds for MScanner 851>;
  CorrectnessKind = (syCorrectness, syCoherence, syCompatibility, syConsistency, syExistence,
    syUniqueness, syReducibility);

  PropertyKind = (sErrProperty, sySymmetry, syReflexivity, syIrreflexivity, syAssociativity, syTransitivity,
    syCommutativity, syConnectedness, syAsymmetry, syIdempotence, syInvolutiveness, syProjectivity,
    sySethood, syAbstractness);

  LibraryReferenceKind = (syThe, syDef, sySch);

  DirectiveKind = (syVocabularies, syNotations, syDefinitions, syTheorems, sySchemes, syRegistrations,
    syConstructors, syRequirements, syEqualities, syExpansions);

  <Token type for MScanner 848>;

```

See also sections 849 and 850.

This code is used in section 846.

848. Token type for MScanner.

```

<Token type for MScanner 848> ≡
  Token = record Kind: TokenKind;
    Nr: integer;
    Spelling: string;
  end

```

This code is used in section 847.

849. Constants for MScanner

```

⟨Public interface for MScanner 847⟩ +≡
const {Homonymic and special symbols in buildin vocabulary}
  {Homonymic Selector Symbol}
  StrictSym = 1; {“strict”}
  {Homonymic Mode Symbol}
  SetSym = 1; {‘set’}
  {Homonymic Predicate Symbol}
  EqualitySym = 1; {‘=’}
  {Homonymic Circumfix Symbols}
  SquareBracket = 1; {‘[’ ‘]’}
  CurlyBracket = 2; {“_” “””}
  RoundedBracket = 3; {“(” “)”}
  scTooLongLineErrorNr = 200; {Error number: Too long line}
⟨Token names for MScanner 852⟩;
CorrectnessName: array [CorrectnessKind] of string = (‘correctness’, ‘coherence’,
  ‘compatibility’, ‘consistency’, ‘existence’, ‘uniqueness’, ‘reducibility’);
PropertyName: array [PropertyKind] of string = (‘’, ‘symmetry’, ‘reflexivity’, ‘irreflexivity’,
  ‘associativity’, ‘transitivity’, ‘commutativity’, ‘connectedness’, ‘asymmetry’,
  ‘idempotence’, ‘involutiveness’, ‘projectivity’, ‘sethood’, ‘abstractness’);
LibraryReferenceName: array [LibraryReferenceKind] of string = (‘the’, ‘def’, ‘sch’);
DirectiveName: array [DirectiveKind] of
  string = (‘vocabularies’, ‘notations’, ‘definitions’, ‘theorems’, ‘schemes’, ‘registrations’,
  ‘constructors’, ‘requirements’, ‘equalities’, ‘expansions’);
PlaceholderName: array [1 .. 10] of
  string = (‘$1’, ‘$2’, ‘$3’, ‘$4’, ‘$5’, ‘$6’, ‘$7’, ‘$8’, ‘$9’, ‘$10’);
Unexpected = sErrProperty;

```

850. Public facing procedures and global variables. Of particular importance, the global variable *gScanner* is declared here.

```

⟨Public interface for MScanner 847⟩ +≡
var PrevWord, CurWord, AheadWord: Token;
  PrevPos, AheadPos: Position;
procedure ReadToken;
procedure LoadPrf(const aPrfFileName: string);
procedure DisposePrf;
procedure StartScanner;
procedure InitSourceFile(const aFileName, aDctFileName: string);
procedure CloseSourceFile;
procedure InitScanning(const aFileName, aDctFileName: string);
procedure FinishScanning;
var gScanner: MScannPtr = nil; {This is important}
  ModeMaxArgs, StructModeMaxArgs, PredMaxArgs: IntSequence;

```

851. Token kinds. If I were cleverer, I would have some WEB macros to make this readable.

⟨Token kinds for MScanner 851⟩ ≡

```

TokenKind = (syT0, { #0 }
  syT1, { #1 }
  syT2, { #2 }
  syT3, { #3 }
  syT4, { #4 }
  syT5, { #5 }
  syT6, { #6 }
  syT7, { #7 }
  syT8, { #8 }
  syT9, { #9 }
  syT10, { #10 }
  syT11, { #11 }
  syT12, { #12 }
  syT13, { #13 }
  syT14, { #14 }
  syT15, { #15 }
  syT16, { #16 }
  syT17, { #17 }
  syT18, { #18 }
  syT19, { #19 }
  syT20, { #20 }
  syT21, { #21 }
  syT22, { #22 }
  syT23, { #23 }
  syT24, { #24 }
  syT25, { #25 }
  syT26, { #26 }
  syT27, { #27 }
  syT28, { #28 }
  syT29, { #29 }
  syT30, { #30 }
  syT31, { #31 }
  Pragma, { #32 }
  EOT = 33, { ! #33 }
  sy_from, { " #34 }
  sy_identify, { # #35 }
  sy_thesis, { $ #36 }
  sy_contradiction, { % #37 }
  sy_Ampersand, { & #38 }
  sy_by, { ' #39 }
  sy_LeftParanthesis, { ( #40 }
  sy_RightParanthesis, { ) #41 }
  sy_registration, { * #42 }
  sy_definition, { + #43 }
  sy_Comma, { , #44 }
  sy_notation, { - #45 }
  sy_Ellipsis, { . #46 }
  sy_proof, { / #47 }
  syT48, { 0 #48 }
  syT49, { 1 #49 }

```

syT50, { 2 #50 }
syT51, { 3 #51 }
syT52, { 4 #52 }
syT53, { 5 #53 }
syT54, { 6 #54 }
syT55, { 7 #55 }
syT56, { 8 #56 }
syT57, { 9 #57 }
sy_Colon, { : #58 }
sy_Semicolon, { ; #59 }
sy_now, { < #60 }
sy_Equal, { = #61 }
sy_end, { > #62 }
sy_Error, { ? #63 }
syT64, { @ #64 }
MMLIdentifier, { A #65 }
syT66, { B #66 }
syT67, { C #67 }
sy_LibraryDirective, { D #68 } { see DirectiveKind }
syT69, { E #69 }
syT70, { F #70 }
StructureSymbol, { G #71 }
syT72, { H #72 }
Identifier, { I #73 }
ForgetfulFunctor, { J #74 }
LeftCircumfixSymbol, { K #75 }
RightCircumfixSymbol, { L #76 }
ModeSymbol, { M #77 }
Numeral, { N #78 }
InfixOperatorSymbol, { O #79 }
syT80, { P #80 }
ReferenceSort, { Q #81 }
PredicateSymbol, { R #82 }
syT83, { S #83 }
syT84, { T #84 }
SelectorSymbol, { U #85 }
AttributeSymbol, { V #86 }
syT87, { W #87 }
sy_Property, { X #88 } { see PropertyKind }
sy_CorrectnessCondition, { Y #89 } { see CorrectnessKind }
sy_Dolar, { Z #90 } { \$1 \$2 \$3 \$4 \$5 \$6 \$7 \$8 \$9 \$10 }
sy_LeftSquareBracket, { [#91 }
syT92, { #92 }
sy_RightSquareBracket, {] #93 }
syT94, { ^ #94 }
syT95, { _ #95 }
syT96, { ' #96 }
sy_according, { a #97 }
syT98, { b #98 }
sy_reduce, { c #99 }
syT100, { d #100 }
sy_equals, { e #101 }


```

syT102, { f #102 }
syT103, { g #103 }
sy_with, { h #104 }
syT105, { i #105 }
syT106, { j #106 }
syT107, { k #107 }
syT108, { l #108 }
syT109, { m #109 }
syT110, { n #110 }
syT111, { o #111 }
syT112, { p #112 }
syT113, { q #113 }
sy_wrt = 114, { r #114 }
syT115, { s #115 }
sy_to, { t #116 }
syT117, { u #117 }
syT118, { v #118 }
sy_when, { w #119 }
sy_axiom, { x #120 }
syT121, { y #121 }
syT122, { z #122 }
sy_LeftCurlyBracket, { #123 }
syT124, { | #124 }
sy_RightCurlyBracket, { #125 }
syT126, { ~ #126 }
syT127, { #127 }
syT128, { #128 }
syT129, { #129 }
syT130, { #130 }
syT131, { #131 }
syT132, { #132 }
syT133, { #133 }
syT134, { #134 }
sy_correctness = 135, { #135 }
syT136, { #136 }
syT137, { #137 }
syT138, { #138 }
syT139, { #139 }
sy_if = 140, { #140 }
syT141, { #141 }
syT142, { #142 }
syT143, { #143 }
sy_is = 144, { #144 }
sy_are, { #145 }
syT146, { #146 }
sy_otherwise, { #147 }
syT148, { #148 }
syT149, { #149 }
syT150, { #150 }
syT151, { #151 }
syT152, { #152 }
syT153, { #153 }

```

```

syT154, { #154 }
syT155, { #155 }
sy-ex = 156, { #156 }
sy-for, { #157 }
syT158, { #158 }
sy-define, { #159 }
syT160, { #160 }
sy-being, { #161 }
sy-over, { #162 }
syT163, { #163 }
sy-canceled, { #164 }
sy-do, { #165 }
sy-does, { #166 }
sy-or, { #167 }
sy-where, { #168 }
sy-non, { #169 }
sy-not, { #170 }
sy-cluster, { #171 }
sy-attr, { #172 }
syT173, { #173 }
sy-StructLeftBracket, { #174 }
sy-StructRightBracket, { #175 }
sy-environ, { #176 }
syT177, { #177 }
sy-begin, { #178 }
syT179, { #179 }
syT180, { #180 }
syT181, { #181 }
syT182, { #182 }
syT183, { #183 }
syT184, { #184 }
sy-hence, { #185 }
syT186, { #186 }
syT187, { #187 }
sy-hereby, { #188 }
syT189, { #189 }
syT190, { #190 }
syT191, { #191 }
sy-then, { #192 }
sy-DotEquals, { #193 }
syT194, { #194 }
syT195, { #195 }
sy-synonym, { #196 }
sy-antonym, { #197 }
syT198, { #198 }
syT199, { #199 }
sy-let, { #200 }
sy-take, { #201 }
sy-assume, { #202 }
sy-thus, { #203 }
sy-given, { #204 }
sy-suppose, { #205 }

```

```

sy_consider, { #206 }
syT207, { #207 }
syT208, { #208 }
syT209, { #209 }
syT210, { #210 }
sy_Arrow, { #211 }
sy_as, { #212 }
sy_qua, { #213 }
sy_be, { #214 }
sy_reserve, { #215 }
syT216, { #216 }
syT217, { #217 }
syT218, { #218 }
syT219, { #219 }
syT220, { #220 }
syT221, { #221 }
syT222, { #222 }
syT223, { #223 }
sy_set, { #224 }
sy_selector, { #225 }
sy_cases, { #226 }
sy_per, { #227 }
sy_scheme, { #228 }
sy_redefine, { #229 }
sy_reconsider, { #230 }
sy_case, { #231 }
sy_prefix, { #232 }
sy_the, { #233 }
sy_it, { #234 }
sy_all, { #235 }
sy_theorem, { #236 }
sy_struct, { #237 }
sy_exactly, { #238 }
sy_mode, { #239 }
sy_iff, { #240 }
sy_func, { #241 }
sy_pred, { #242 }
sy_implies, { #243 }
sy_st, { #244 }
sy_holds, { #245 }
sy_provided, { #246 }
sy_means, { #247 }
sy_of, { #248 }
sy_defpred, { #249 }
sy_deffunc, { #250 }
sy_such, { #251 }
sy_that, { #252 }
sy_aggregate, { #253 }
sy_and { #254 });

```

This code is used in section [847](#).

852. We have string representation for each of the token kinds, which is useful for debugging purposes.

⟨Token names for MScanner 852⟩ ≡

TokenName: **array** [*TokenKind*] **of** *string* = (`` , { #0 }

```

`` , { #1 }
`` , { #2 }
`` , { #3 }
`` , { #4 }
`` , { #5 }
`` , { #6 }
`` , { #7 }
`` , { #8 }
`` , { #9 }
`` , { #10 }
`` , { #11 }
`` , { #12 }
`` , { #13 }
`` , { #14 }
`` , { #15 }
`` , { #16 }
`` , { #17 }
`` , { #18 }
`` , { #19 }
`` , { #20 }
`` , { #21 }
`` , { #22 }
`` , { #23 }
`` , { #24 }
`` , { #25 }
`` , { #26 }
`` , { #27 }
`` , { #28 }
`` , { #29 }
`` , { #30 }
`` , { #31 }
`` , { #32 }
`` , { ! #33 }
`from`, { " #34 }
`identify`, { # #35 }
`thesis`, { $ #36 }
`contradiction`, { % #37 }
`&`, { & #38 }
`by`, { ' #39 }
`(`, { ( #40 }
`)`, { ) #41 }
`registration`, { * #42 }
`definition`, { + #43 }
`,` , { , #44 }
`notation`, { - #45 }
`...`, { . #46 }
`proof`, { / #47 }
`` , { 0 #48 }
`` , { 1 #49 }

```

```

--, { 2 #50 }
--, { 3 #51 }
--, { 4 #52 }
--, { 5 #53 }
--, { 6 #54 }
--, { 7 #55 }
--, { 8 #56 }
--, { 9 #57 }
--, { : #58 }
--, { ; #59 }
now~, { < #60 }
=~, { = #61 }
end~, { > #62 }
--, { ? #63 }
--, { @ #64 }
--, { A #65 }
--, { B #66 }
--, { C #67 }
vocabularies~, { D #68 }
--, { E #69 }
--, { F #70 }
--, { G #71 }
--, { H #72 }
--, { I #73 }
--, { J #74 }
--, { K #75 }
--, { L #76 }
--, { M #77 }
--, { N #78 }
--, { O #79 }
--, { P #80 }
def~, { Q #81 }
--, { R #82 }
--, { S #83 }
--, { T #84 }
--, { U #85 }
--, { V #86 }
--, { W #87 }
symmetry~, { X #88 }
coherence~, { Y #89 }
$1~, { Z #90 }
[, { [ #91 }
~, { ' #92 }
], { ] #93 }
--, { ^ #94 }
--, { - #95 }
--, { ' #96 }
according~, { a #97 }
--, { b #98 }
reduce~, { c #99 }
--, { d #100 }
equals~, { e #101 }

```

```

 $\{f\}$  #102 }
 $\{g\}$  #103 }
with  $\{h\}$  #104 }
 $\{i\}$  #105 }
 $\{j\}$  #106 }
 $\{k\}$  #107 }
 $\{l\}$  #108 }
 $\{m\}$  #109 }
 $\{n\}$  #110 }
 $\{o\}$  #111 }
 $\{p\}$  #112 }
 $\{q\}$  #113 }
wrt  $\{r\}$  #114 }
 $\{s\}$  #115 }
to  $\{t\}$  #116 }
 $\{u\}$  #117 }
 $\{v\}$  #118 }
when  $\{w\}$  #119 }
axiom  $\{x\}$  #120 }
 $\{y\}$  #121 }
 $\{z\}$  #122 }
 $\{ \}$  #123 }
 $\{ | \}$  #124 }
 $\{ \}$  #125 }
 $\{ \sim \}$  #126 }
T127  $\{ \}$  #127 }
 $\{ \}$  #128 }
T129  $\{ \}$  #129 }
 $\{ \}$  #130 }
T131  $\{ \}$  #131 }
 $\{ \}$  #132 }
 $\{ \}$  #133 }
 $\{ \}$  #134 }
correctness  $\{ \}$  #135 }
T136  $\{ \}$  #136 }
 $\{ \}$  #137 }
 $\{ \}$  #138 }
 $\{ \}$  #139 }
if  $\{ \}$  #140 }
 $\{ \}$  #141 }
 $\{ \}$  #142 }
 $\{ \}$  #143 }
is  $\{ \}$  #144 }
are  $\{ \}$  #145 }
 $\{ \}$  #146 }
otherwise  $\{ \}$  #147 }
 $\{ \}$  #148 }
 $\{ \}$  #149 }
 $\{ \}$  #150 }
 $\{ \}$  #151 }
T152  $\{ \}$  #152 }
 $\{ \}$  #153 }

```

```

`', {#154}
`', {#155}
`ex`, {#156}
`for`, {#157}
`', {#158}
`define`, {#159}
`', {#160}
`being`, {#161}
`over`, {#162}
`', {#163}
`canceled`, {#164}
`do`, {#165}
`does`, {#166}
`or`, {#167}
`where`, {#168}
`non`, {#169}
`not`, {#170}
`cluster`, {#171}
`attr`, {#172}
`', {#173}
`(\#`, {#174}
`\#)`, {#175}
`environ`, {#176}
`', {#177}
`begin`, {#178}
`', {#179}
`', {#180}
`', {#181}
`', {#182}
`', {#183}
`', {#184}
`hence`, {#185}
`', {#186}
`', {#187}
`hereby`, {#188}
`', {#189}
`', {#190}
`', {#191}
`then`, {#192}
`.=`, {#193}
`', {#194}
`', {#195}
`synonym`, {#196}
`antonym`, {#197}
`', {#198}
`', {#199}
`let`, {#200}
`take`, {#201}
`assume`, {#202}
`thus`, {#203}
`given`, {#204}
`suppose`, {#205}

```

```

`consider`, {#206}
``, {#207}
``, {#208}
``, {#209}
``, {#210}
`->`, {#211}
`as`, {#212}
`qua`, {#213}
`be`, {#214}
`reserve`, {#215}
``, {#216}
``, {#217}
``, {#218}
``, {#219}
``, {#220}
``, {#221}
``, {#222}
``, {#223}
`set`, {#224}
`selector`, {#225}
`cases`, {#226}
`per`, {#227}
`scheme`, {#228}
`redefine`, {#229}
`reconsider`, {#230}
`case`, {#231}
`prefix`, {#232}
`the`, {#233}
`it`, {#234}
`all`, {#235}
`theorem`, {#236}
`struct`, {#237}
`exactly`, {#238}
`mode`, {#239}
`iff`, {#240}
`func`, {#241}
`pred`, {#242}
`implies`, {#243}
`st`, {#244}
`holds`, {#245}
`provided`, {#246}
`means`, {#247}
`of`, {#248}
`defpred`, {#249}
`deffunc`, {#250}
`such`, {#251}
`that`, {#252}
`aggregate`, {#253}
`and` {#254})

```

This code is used in section [849](#).

853. Reading a token. This tokenizes a Mizar article, using the scanner's *GetToken* method. We can trace this *GetToken* back to its implementation (§756). This, in turn, depends on the *SliceIt* method (§739).

This method is used to determine the next token in `parser.pas`'s *Parse* function.

This assumes that *StartScanner* (§856) has been invoked already, which initializes the *CurWord* token and other variables.

Also important to observe: the *Kind* of the token is populated here.

⟨Implementation for MScanner 853⟩ ≡

```
procedure ReadToken;
  begin PrevWord ← CurWord; PrevPos ← CurPos; CurWord ← AheadWord; CurPos ← AheadPos;
    { ' ' is not allowed in an identifiers in the text proper }
  if (CurWord.Kind = sy_Begin) then gScanner↑.Allowed[' ' ] ← 0;
  if (CurWord.Kind = sy_Error) ∧ (CurWord.Nr = scTooLongLineErrorNr) then
    ErrImm(CurWord.Nr);
  gScanner↑.GetToken;
  AheadWord.Kind ← TokenKind(gScanner↑.fLexem.Kind); AheadWord.Nr ← gScanner↑.fLexem.Nr;
  AheadWord.Spelling ← gScanner↑.fStr; AheadPos ← gScanner↑.fPos;
end;
```

See also sections 854, 855, 856, 857, 858, 859, and 860.

This code is used in section 846.

854. Loading a proof file. The `.prf` file is a file containing numerals, and its usage eludes me. The format consists of multiple lines:

Line 1: Three non-negative integers are on the first line “*M S P*”

Line 2: Contains *M* non-negative integers separated by a single whitespace

Line 3: Contains *S* non-negative integers separated by a single whitespace

Line 4: Contains *P* non-negative integers separated by a single whitespace.

This function loads the contents of the `.prf` file. This initializes the global variables *ModeMaxArgs*, *StructureModeMaxArgs*, *PredMaxArgs*, then populates them.

⟨Implementation for MScanner 853⟩ +≡

```
procedure LoadPrf(const aPrfFileName: string);
  var lPrf: text; lModeMaxArgsSize, lStructModeMaxArgsSize, lPredMaxArgsSize, i, lInt, r: integer;
  begin assign(lPrf, aPrfFileName + '.prf'); reset(lPrf);
  Read(lPrf, lModeMaxArgsSize, lStructModeMaxArgsSize, lPredMaxArgsSize);
  ModeMaxArgs.Init(lModeMaxArgsSize + 1); r ← ModeMaxArgs.Insert(0);
  StructModeMaxArgs.Init(lStructModeMaxArgsSize + 1); r ← StructModeMaxArgs.Insert(0);
  PredMaxArgs.Init(lPredMaxArgsSize + 1); r ← PredMaxArgs.Insert(0);
  for i ← 1 to lModeMaxArgsSize do
    begin Read(lPrf, lInt); r ← ModeMaxArgs.Insert(lInt);
    end;
  for i ← 1 to lStructModeMaxArgsSize do
    begin Read(lPrf, lInt); r ← StructModeMaxArgs.Insert(lInt);
    end;
  for i ← 1 to lPredMaxArgsSize do
    begin Read(lPrf, lInt); r ← PredMaxArgs.Insert(lInt);
    end;
  close(lPrf);
end;
```

855. We cleanup after using the `.prf` file.

⟨Implementation for MScanner 853⟩ +≡

```
procedure DisposePrf;
  begin ModeMaxArgs.Done; PredMaxArgs.Done; StructModeMaxArgs.Done;
  end;
```

856. We construct an MScann object to scan a file.

⟨Implementation for MScanner 853⟩ +≡

```
procedure StartScanner;
  begin CurPos.Line ← 1; CurPos.Col ← 0; AheadWord.Kind ← TokenKind(gScanner↑.fLexem.Kind);
  AheadWord.Nr ← gScanner↑.fLexem.Nr; AheadWord.Spelling ← gScanner↑.fStr;
  AheadPos ← gScanner↑.fPos;
  end;
```

857. We initialize a scanner for a file.

⟨Implementation for MScanner 853⟩ +≡

```
procedure InitSourceFile(const aFileName, aDctFileName: string);
  begin new(gScanner, InitScanning(aFileName, aDctFileName)); StartScanner;
  end;
```

858. When we're done with a scanner, we call the destructor for the MScanner.

⟨Implementation for MScanner 853⟩ +≡

```
procedure CloseSourceFile;
  begin dispose(gScanner, Done);
  end;
```

859. We can combine the previous functions together to initialize a scanner for a file (an article) and its dictionary file.

⟨Implementation for MScanner 853⟩ +≡

```
procedure InitScanning(const aFileName, aDctFileName: string);
  begin gScanner ← new(MScannPtr, InitScanning(aFileName, aDctFileName)); StartScanner;
  LoadPrf(aDctFileName);
  end;
```

860. We cleanup after scanning, saving a dictionary XML file to an `“.idx”` file. This uses the global variable `EnvFileName` declared in `mizenv.pas` (§35).

⟨Implementation for MScanner 853⟩ +≡

```
procedure FinishScanning;
  begin gScanner↑.fIdents.SaveXDct(EnvFileName + `.idx`); CloseSourceFile; DisposePrf;
  end;
```

File 20

Abstract Syntax

861. A crucial step in any interpreter, compiler, or proof assistant is to transform the concrete syntax into an abstract syntax tree. This module provides all the classes for the abstract syntax tree *of expressions, types, and formulas* in Mizar. The abstract syntax tree for “statements” will be found in the “Weakly Strict Text Proper” module.

This is a bit, well, “Java-esque”, in the sense that each different kind of node in the abstract syntax tree is represented by a different class. If you don’t know abstract syntax trees, I can heartily recommend Bob Nystrom’s *Crafting Interpreters* ([Ch. 5: Representing Code](#)) for an overview.

I’ll be quoting from the grammar for Mizar as we go along, since the class hierarchy names their classes after the nonterminal symbols in the grammar. (It’s what anyone would do.) You can find a local copy of the grammar on most UNIX machines with Mizar installed located at `/usr/local/doc/Mizar/syntax.txt`, which you can study at your leisure.

862. Warning: There is a lot of boiler plate code in the constructors and destructors. I am going to pass over them without much comment, because they are monotonous and uninteresting. The more interesting part will be discussed with the class declarations for each kind of node. I will simply entitle the paragraphs “Constructor” to indicate I am recognizing their existence and moving on.

```

<abstract_syntax.pas 862> ≡
  <GNU License 4>
unit abstract_syntax;
  interface uses errhan, mobjects, syntax;
    <Interface for abstract syntax 864>
  implementation
    <Implementation of abstract syntax 863>
  end .

```

863. The implementation requires discussing a few “special cases” (variables, qualified segments, adjectives) before getting to the usual syntactic classes (terms, types, formulas).

```

<Implementation of abstract syntax 863> ≡
  <Variable AST constructor 866>
  <Qualified segment AST constructor 869>
  <Adjective expression AST constructor 875>
  <Adjective AST constructor 879>
  <Negated adjective AST constructor 877>
  <Implementing term AST 884>
  <Implementing type AST 926>
  <Implementing formula AST 938>
  <Within expression AST implementation 978>

```

This code is used in section [862](#).

864. The interface consists mostly of classes, as well as a few enumerated types. The gambit resembles what we would do if we were programming in C: define an `enum TermSort`, then introduce a `struct TermAstNode` {`enum TermSort sort;`} to act as an abstract base class for terms (and do likewise for formulas, types, etc.). This allows us to use “struct inheritance” in C, as Bob Nystrom’s *Crafting Interpreters* (Ch. 19) calls it.

```

⟨ Interface for abstract syntax 864 ⟩ ≡
type ⟨ Abstract base class for types 924 ⟩;
  ⟨ Abstract base class for terms 880 ⟩;
  ⟨ Abstract base class for formulas 935 ⟩;
  ⟨ Adjective expression (abstract syntax tree) 874 ⟩;
  ⟨ Negated adjective expression (abstract syntax tree) 876 ⟩;
  ⟨ Adjective (abstract syntax tree) 878 ⟩;
  { Auxiliary structures }
  ⟨ Variable (abstract syntax tree) 865 ⟩;
  ⟨ Qualified segment (abstract syntax tree) 868 ⟩;
  ⟨ Classes for terms (abstract syntax tree) 882 ⟩
  ⟨ Classes for type (abstract syntax tree) 925 ⟩
  ⟨ Classes for formula (abstract syntax tree) 937 ⟩
  { _____ }
  ⟨ Class for Within expression 977 ⟩;

```

This code is used in section 862.

865. Variable. A variable in the abstract syntax tree is basically a de Bruijn index, in the sense that it is represented by an integer in the metalanguage (PASCAL).

Logicians may feel uncomfortable at variables being outside the term syntax tree. But what logicians think of as “variables” in first-order logic, Mizar calls them “Simple Terms” (§883).

```

⟨ Variable (abstract syntax tree) 865 ⟩ ≡
  VariablePtr = ↑VariableObj;
  VariableObj = object (MObject)
    nIdent: integer; { identifier number }
    nVarPos: Position;
    constructor Init(const aPos: Position; aIdentNr: integer);
end

```

This code is used in section 864.

866. Constructor.

```

⟨ Variable AST constructor 866 ⟩ ≡
constructor VariableObj.Init(const aPos: Position; aIdentNr: integer);
  begin nIdent ← aIdentNr; nVarPos ← aPos;
end;

```

This code is used in section 863.

867. Qualified segment. A qualified segment refers to situations in, e.g., “**consider** $\langle \text{qualified-segment} \rangle^+$ **such that** ...”. This also happens in quantifiers where the Working Mathematician writes $\forall \vec{x}. P[\vec{x}]$, for example (that quantifier prefix “ $\forall \vec{x}$ ” uses the qualifying segment \vec{x}).

The Mizar grammar for qualified segments looks like:

```
Qualified-Variables = Implicitly-Qualified-Variables
                    | Explicitly-Qualified-Variables
                    | Explicitly-Qualified-Variables "," Implicitly-Qualified-Variables .
Implicitly-Qualified-Variables = Variables .
Explicitly-Qualified-Variables = Qualified-Segment {"," Qualified-Segment }.
Qualified-Segment = Variables Qualification .
Variables = Variable-Identifier {"," Variable-Identifier }.
Qualification = ( "being" | "be" ) Type-Expression .
```

We will implement `Qualified-Variables` as an array of pointers to *QualifiedSegment* objects, each one being either implicit or explicit.

868. Abstract base class for qualified segments. We have *implicitly* qualified segments and *explicitly* qualified segments, which are “both” qualified segments. Object-oriented yoga teaches us to describe this situation using a “qualified segment” abstract base class, and then extend it with two subclasses.

```
< Qualified segment (abstract syntax tree 868) > ≡
SegmentKind = (ikImplQualifiedSegm, ikExplQualifiedSegm);
QualifiedSegmentPtr = ↑QualifiedSegmentObj;
QualifiedSegmentObj = object (MObject)
  nSegmPos: Position;
  nSegmentSort: SegmentKind;
  constructor Init(const aPos: Position; aSort: SegmentKind);
end
```

See also sections 870 and 872.

This code is used in section 864.

869. Constructor.

```
< Qualified segment AST constructor 869 > ≡
constructor QualifiedSegmentObj.Init(const aPos: Position; aSort: SegmentKind);
  begin nSegmPos ← aPos; nSegmentSort ← aSort;
  end;
```

See also sections 871 and 873.

This code is used in section 863.

870. Implicitly qualified segments. When we use “reserved variables” in the qualifying segment, we can suppress the type ascription (i.e., the “**being** $\langle \text{Type} \rangle$ ”). This makes the typing *implicit*. Hence the name *implicitly* qualified segments (the types are implicitly given).

```
< Qualified segment (abstract syntax tree 868) > +≡
ImplicitlyQualifiedSegmentPtr = ↑ImplicitlyQualifiedSegmentObj;
ImplicitlyQualifiedSegmentObj = object (QualifiedSegmentObj)
  nIdentifier: VariablePtr;
  constructor Init(const aPos: Position; aIdentifier: VariablePtr);
  destructor Done; virtual;
end ;
```

871. Constructor. The constructors and destructors for implicitly qualified segments are straightforward.

```

< Qualified segment AST constructor 869 > +≡
constructor ImplicitlyQualifiedSegmentObj.Init(const aPos: Position; aIdentifier: VariablePtr);
  begin inherited Init(aPos, ikImplQualifiedSegm); nIdentifier ← aIdentifier;
  end;
destructor ImplicitlyQualifiedSegmentObj.Done;
  begin dispose(nIdentifier, Done);
  end;

```

872. Explicitly qualified segment. The other possibility in Mizar is that we will have “explicitly typed variables” in the qualifying segment. The idea is that, in Mizar, we can permit the following situation:

consider *x, y, z* being set such that ...

This means the three variables *x, y, z* are explicitly qualified variables with the type “set”. We represent this using one *ExplicitlyQualifiedSegment* object, a vector for the identifiers (*x, y, z*) and a pointer to their type (set).

```

< Qualified segment (abstract syntax tree) 868 > +≡
  ExplicitlyQualifiedSegmentPtr = ↑ExplicitlyQualifiedSegmentObj;
  ExplicitlyQualifiedSegmentObj = object (QualifiedSegmentObj)
    nIdentifiers: PList; { of identifier numbers }
    nType: TypePtr;
    constructor Init(const aPos: Position; aIdentifiers: PList; aType: TypePtr);
    destructor Done; virtual;
  end

```

873. The constructors and destructors for explicitly qualified segments are straightforward.

```

< Qualified segment AST constructor 869 > +≡
constructor ExplicitlyQualifiedSegmentObj.Init(const aPos: Position;
  aIdentifiers: PList;
  aType: TypePtr);
  begin inherited Init(aPos, ikExplQualifiedSegm); nIdentifiers ← aIdentifiers; nType ← aType;
  end;
destructor ExplicitlyQualifiedSegmentObj.Done;
  begin dispose(nIdentifiers, Done); dispose(nType, Done);
  end;

```

874. Attributes. Attributes can have arguments *preceding* it. The relevant part of the Mizar grammar, I think, is:

```

  Adjective-Cluster = { Adjective } .
  Adjective = [ "non" ] [ Adjective-Arguments ] Attribute-Symbol .

```

```

< Adjective expression (abstract syntax tree) 874 > ≡
  AdjectiveSort = (wsNegatedAdjective, wsAdjective);
  AdjectiveExpressionPtr = ↑AdjectiveExpressionObj;
  AdjectiveExpressionObj = object (MObject)
    nAdjectivePos: Position;
    nAdjectiveSort: AdjectiveSort;
    constructor Init(const aPos: Position; aSort: AdjectiveSort);
    destructor Done; virtual;
  end

```

This code is used in section 864.

875. \langle Adjective expression AST constructor 875 $\rangle \equiv$
constructor *AdjectiveExpressionObj.Init*(**const** *aPos*: *Position*; *aSort*: *AdjectiveSort*);
 begin *nAdjectivePos* \leftarrow *aPos*; *nAdjectiveSort* \leftarrow *aSort*;
 end;
destructor *AdjectiveExpressionObj.Done*;
 begin end;

This code is used in section 863.

876. Negated adjective. We represent an adjective using the EBNF grammar (c.f., the WSM article-related function *InWSMizFileObj.Read_Adjective:AdjectiveExpressionPtr*):

Negated-Adjective ::= "non" Adjective-Expr;
 Positive-Adjective ::= [Adjective-Arguments] Attribute-Symbol;
 Adjective-Expr ::= Negated-Adjective | Positive-Adjective;

Hence we only really need a pointer to the “adjective being negated”.

\langle Negated adjective expression (abstract syntax tree) 876 $\rangle \equiv$
NegatedAdjectivePtr = \uparrow *NegatedAdjectiveObj*;
NegatedAdjectiveObj = **object** (*AdjectiveExpressionObj*)
 nArg: *AdjectiveExpressionPtr*; { of TermPtr, visible arguments }
 constructor *Init*(**const** *aPos*: *Position*; *aArg*: *AdjectiveExpressionPtr*);
 destructor *Done*; *virtual*;
 end

This code is used in section 864.

877. Constructor.

\langle Negated adjective AST constructor 877 $\rangle \equiv$
constructor *NegatedAdjectiveObj.Init*(**const** *aPos*: *Position*; *aArg*: *AdjectiveExpressionPtr*);
 begin *inherited Init*(*aPos*, *wsNegatedAdjective*); *nArg* \leftarrow *aArg*;
 end;
destructor *NegatedAdjectiveObj.Done*;
 begin *dispose*(*nArg*, *Done*);
 end;

This code is used in section 863.

878. Adjective objects. [[This is the preferred node for later intermediate representations for attributes, since *nNegated* is a field in the class.]]

\langle Adjective (abstract syntax tree) 878 $\rangle \equiv$
AdjectivePtr = \uparrow *AdjectiveObj*;
AdjectiveObj = **object** (*AdjectiveExpressionObj*)
 nAdjectiveSymbol: *integer*;
 nNegated: *boolean*;
 nArgs: *PList*; { of TermPtr, visible arguments }
 constructor *Init*(**const** *aPos*: *Position*; *aAdjectiveNr*: *integer* ; *aArgs*: *PList*);
 destructor *Done*; *virtual*;
 end

This code is used in section 864.

879. Constructor.

⟨ Adjective AST constructor 879 ⟩ ≡

```
constructor AdjectiveObj.Init(const aPos: Position; aAdjectiveNr: integer; aArgs: PList);
  begin inherited Init(aPos, wsAdjective); nAdjectiveSymbol ← aAdjectiveNr; nArgs ← aArgs;
  end;
destructor AdjectiveObj.Done;
  begin dispose(nArgs, Done);
  end;
```

This code is used in section 863.

Section 20.1. TERMS (ABSTRACT SYNTAX TREE)

880. We have an abstract base class for terms, along with the “sorts” (syntactic subclasses) allowed. This allows, e.g., formulas, to refer to terms without knowing the sort of term involved. The UML class diagram for term:

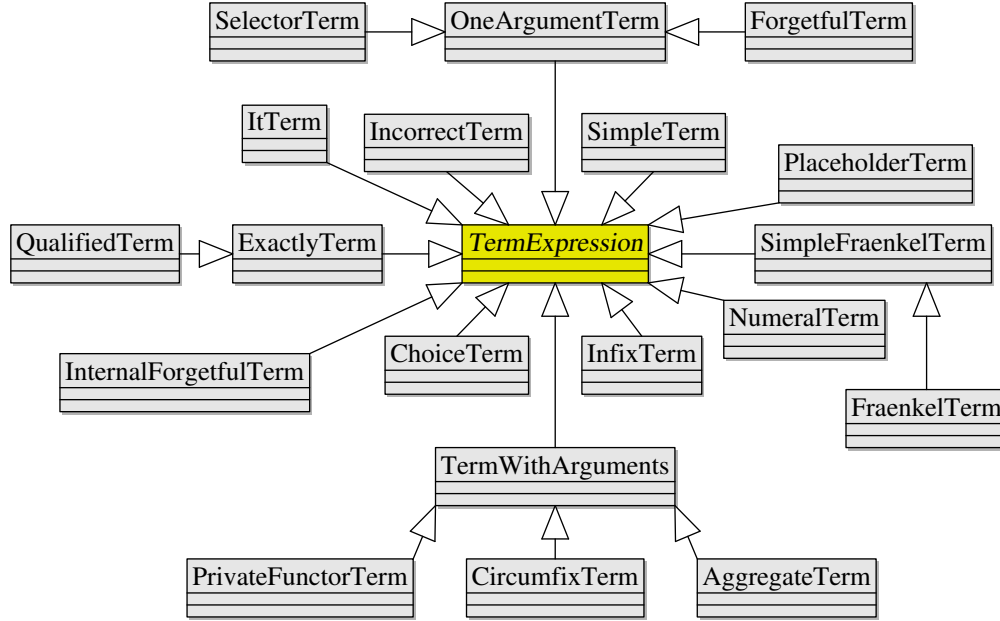


Fig. 3. UML class diagram for abstract syntax tree for terms.

The arrows indicate inheritance, pointing from the subclass to the parent superclass. The abstract base class *TermExpression* is italicized, but it is so difficult to distinguish we have colored it yellow.

NOTE: the class UML diagram may be missing a few descendents of *TermExpression*, but it contains the important subclasses which I could fit into it.

⟨ Abstract base class for terms 880 ⟩ ≡

```

TermSort = (wsErrorTerm, wsPlaceholderTerm, wsNumeralTerm, wsSimpleTerm,
            wsPrivateFunctorTerm, wsInfixTerm, wsCircumfixTerm, wsAggregateTerm, wsForgetfulFunctorTerm,
            wsInternalForgetfulFunctorTerm, wsSelectorTerm, wsInternalSelectorTerm, wsQualificationTerm,
            wsGlobalChoiceTerm, wsSimpleFraenkelTerm, wsFraenkelTerm, wsItTerm, wsExactlyTerm);
TermPtr = ↑TermExpressionObj;
TermExpressionObj = object (MObject)
  nTermSort: TermSort;
  nTermPos: Position;
end

```

This code is used in section 864.

881. The grammar for term expressions in Mizar as stated in `syntax.txt`:

```
Term-Expression = "(" Term-Expression ")"
| [ Arguments ] Functor-Symbol [ Arguments ]
| Left-Functor-Bracket Term-Expression-List Right-Functor-Bracket
| Functor-Identifier "(" [ Term-Expression-List ] ")"
| Structure-Symbol "(#" Term-Expression-List "#)"
| "the" Structure-Symbol "of" Term-Expression
| Variable-Identifier
| "{" Term-Expression { Postqualification } ":" Sentence "}"
| "the" "set" "of" "all" Term-Expression { Postqualification }
| Numeral
| Term-Expression "qua" Type-Expression
| "the" Selector-Symbol "of" Term-Expression
| "the" Selector-Symbol
| "the" Type-Expression
| Private-Definition-Parameter
| "it" .
```

But I think it might be clearer if we view it using the equivalent grammar:

```
Term-Expression = "(" Term-Expression ")"
| [ Arguments ] Functor-Symbol [ Arguments ]
| Left-Functor-Bracket Term-Expression-List Right-Functor-Bracket
| Functor-Identifier "(" [ Term-Expression-List ] ")"
| Aggregate-Term
| Forgetful-Functor-Term
| Variable-Identifier
| Fraenkel-Term
| Numeral
| Qualified-Term
| Selector-Functor
| Internal-Selector-Functor
| Choice-Term
| Private-Definition-Parameter
| "it" .

Aggregate-Term = Structure-Symbol "(#" Term-Expression-List "#)" .
Choice-Term = "the" Type-Expression.
Forgetful-Functor-Term = "the" Structure-Symbol "of" Term-Expression.
Fraenkel-Term = "{" Term-Expression {Postqualification} ":" Sentence "}"
| "the" "set" "of" "all" Term-Expression { Postqualification }.
Internal-Selector-Functor = "the" Selector-Symbol.
Selector-Functor = "the" Selector-Symbol "of" Term-Expression.
Qualified-Term = Term-Expression "qua" Type-Expression.
```

882. Class structure for this syntax tree.

```

⟨Classes for terms (abstract syntax tree) 882⟩ ≡
  { Terms }
  ⟨Simple term (abstract syntax tree) 883⟩;
  ⟨Placeholder term (abstract syntax tree) 885⟩;
  ⟨Numeral term (abstract syntax tree) 887⟩;
  ⟨Infix term (abstract syntax tree) 889⟩;
  ⟨Terms with arguments (abstract syntax tree) 891⟩;
  ⟨Circumfix term (abstract syntax tree) 893⟩;
  ⟨Private functor term (abstract syntax tree) 895⟩;
  ⟨One-argument term (abstract syntax tree) 897⟩;
  ⟨Selector term (abstract syntax tree) 899⟩;
  ⟨Internal selector term (abstract syntax tree) 901⟩;
  ⟨Aggregate term (abstract syntax tree) 903⟩;
  ⟨Forgetful functor (abstract syntax tree) 905⟩;
  ⟨Internal forgetful functors (abstract syntax tree) 907⟩;
  ⟨Fraenkel terms (abstract syntax tree) 909⟩;
  ⟨Exactly term (abstract syntax tree) 915⟩;
  ⟨Qualified term (abstract syntax tree) 913⟩;
  ⟨Choice term (abstract syntax tree) 917⟩;
  ⟨“It” term (abstract syntax tree) 919⟩;
  ⟨Incorrect term (abstract syntax tree) 921⟩;

```

This code is used in section 864.

883. Simple terms. Mizar describes variables *as terms* as a *SimpleTerm*.

```

⟨Simple term (abstract syntax tree) 883⟩ ≡
  SimpleTermPtr = ↑SimpleTermObj;
  SimpleTermObj = object (TermExpressionObj)
    nIdent: integer; { identifier number }
    constructor Init(const aPos: Position; aIdentNr: integer);
  end

```

This code is used in section 882.

884. Constructors.

```

⟨Implementing term AST 884⟩ ≡
constructor SimpleTermObj.Init(const aPos: Position; aIdentNr: integer);
  begin nTermPos ← aPos; nTermSort ← wsSimpleTerm; nIdent ← aIdentNr;
  end;

```

See also sections 886, 888, 890, 892, 894, 896, 898, 900, 902, 904, 906, 908, 910, 912, 914, 916, 918, 920, and 922.

This code is used in section 863.

885. Placeholder terms. These are the parameters “\$1”, “\$2”, etc., which appear in a private functor “`deffunc Foo(object) = ...`”.

```

⟨Placeholder term (abstract syntax tree) 885⟩ ≡
  PlaceholderTermPtr = ↑PlaceholderTermObj; { placeholder }
  PlaceholderTermObj = object (TermExpressionObj)
    nLocusNr: integer; { $1, ... }
    constructor Init(const aPos: Position; aLocusNr: integer);
  end

```

This code is used in section 882.

886. Constructor.

⟨Implementing term AST 884⟩ +≡

```
constructor PlaceholderTermObj.Init(const aPos: Position; aLocusNr: integer);
  begin nTermPos ← aPos; nTermSort ← wsPlaceholderTerm; nLocusNr ← aLocusNr;
  end;
```

887. Numeral terms. Mizar can handle 32-bit integers. If we wanted to extend this to, say, arbitrary precision arithmetic, then we would want to modify this class (and a few other places).

⟨Numeral term (abstract syntax tree) 887⟩ ≡

```
NumeralTermPtr = ↑NumeralTermObj;
NumeralTermObj = object (TermExpressionObj)
  nValue: integer;
  constructor Init(const aPos: Position; aValue: integer);
  end
```

This code is used in section 882.

888. Constructor.

⟨Implementing term AST 884⟩ +≡

```
constructor NumeralTermObj.Init(const aPos: Position; aValue: integer);
  begin nTermPos ← aPos; nTermSort ← wsNumeralTerm; nValue ← aValue;
  end;
```

889. Infix terms. When we have infix binary operators, they are terms with arguments on both sides of it. For example $x + 2$ will have “+” be an infix term with arguments $(x, 2)$.

We *could* permit multiple arguments on the left-hand side (and on the right-hand side), but they are comma-separated in Mizar. This could happen in finite group theory, for example, “p -signalizer over H, G” has two arguments on the right but only one argument on the left.

⟨Infix term (abstract syntax tree) 889⟩ ≡

```
InfixTermPtr = ↑InfixTermObj;
InfixTermObj = object (TermExpressionObj)
  nFunctorSymbol: integer;
  nLeftArgs, nRightArgs: PList;
  constructor Init(const aPos: Position; aFunctorNr: integer; aLeftArgs, aRightArgs: PList);
  destructor Done; virtual;
  end
```

This code is used in section 882.

890. Constructor.

⟨Implementing term AST 884⟩ +≡

```
constructor InfixTermObj.Init(const aPos: Position;
  aFunctorNr: integer;
  aLeftArgs, aRightArgs: PList);
  begin nTermPos ← aPos; nTermSort ← wsInfixTerm; nFunctorSymbol ← aFunctorNr;
  nLeftArgs ← aLeftArgs; nRightArgs ← aRightArgs;
  end;
destructor InfixTermObj.Done;
  begin dispose(nLeftArgs, Done); dispose(nRightArgs, Done);
  end;
```

891. Terms with arguments. This class seems to be used only internally to the `abstract_syntax.pas` module. Recalling the UML class diagram (§880), we remember there are three subclasses to this: private functor terms (which appear in Mizar when we use “`defunc F(...) = ...`”), circumfix (“bracketed”) terms, and aggregate terms (when we construct an instance of a structure).

```

⟨Terms with arguments (abstract syntax tree) 891⟩ ≡
  TermWithArgumentsPtr = ↑TermWithArgumentsObj;
  TermWithArgumentsObj = object (TermExpressionObj)
    nArgs: PList;
    constructor Init(const aPos: Position; aKind: TermSort; aArgs: PList);
    destructor Done; virtual;
  end

```

This code is used in section 882.

892. Constructor.

```

⟨Implementing term AST 884⟩ +≡
constructor TermWithArgumentsObj.Init(const aPos: Position; aKind: TermSort; aArgs: PList);
  begin nTermPos ← aPos; nTermSort ← aKind; nArgs ← aArgs;
  end;
destructor TermWithArgumentsObj.Done;
  begin dispose(nArgs, Done);
  end;

```

893. Circumfix terms. We can introduce different types of brackets in Mizar. For example, for groups, we have the commutator of group elements `[.x,y.]`. These “bracketed terms” are referred to as circumfix terms.

```

⟨Circumfix term (abstract syntax tree) 893⟩ ≡
  CircumfixTermPtr = ↑CircumfixTermObj;
  CircumfixTermObj = object (TermWithArgumentsObj)
    nLeftBracketSymbol, nRightBracketSymbol: integer;
    constructor Init(const aPos: Position; aLeftBracketNr, aRightBracketNr: integer; aArgs: PList);
    destructor Done; virtual;
  end

```

This code is used in section 882.

894. Constructor.

```

⟨Implementing term AST 884⟩ +≡
constructor CircumfixTermObj.Init(const aPos: Position;
                                aLeftBracketNr, aRightBracketNr: integer;
                                aArgs: PList);
  begin inherited Init(aPos, wsCircumfixTerm, aArgs); nLeftBracketSymbol ← aLeftBracketNr;
  nRightBracketSymbol ← aRightBracketNr;
  end;
destructor CircumfixTermObj.Done;
  begin dispose(nArgs, Done);
  end;

```

895. Private functor terms. We introduce private functor terms in Mizar when we have “**defpred** $F(\dots) = \dots$ ”.

```

⟨Private functor term (abstract syntax tree) 895⟩ ≡
  PrivateFunctorTermPtr = ↑PrivateFunctorTermObj;
  PrivateFunctorTermObj = object (TermWithArgumentsObj)
    nFunctorIdent: integer;
    constructor Init(const aPos: Position; aFunctorIdNr: integer; aArgs: PList);
    destructor Done; virtual;
  end

```

This code is used in section 882.

896. Constructor.

```

⟨Implementing term AST 884⟩ +≡
constructor PrivateFunctorTermObj.Init(const aPos: Position; aFunctorIdNr: integer; aArgs: PList);
  begin inherited Init(aPos, wsPrivateFunctorTerm, aArgs); nFunctorIdent ← aFunctorIdNr;
  end;
destructor PrivateFunctorTermObj.Done;
  begin dispose(nArgs, Done);
  end;

```

897. One-argument terms. Recalling the UML class diagram for terms (§880), we remember the class for *OneArgument* terms are either selector terms (“**the** ⟨field⟩ **of** ⟨aggregate⟩”) or forgetful functors (“**the** ⟨structure⟩ **of** ⟨aggregate⟩”).

```

⟨One-argument term (abstract syntax tree) 897⟩ ≡
  OneArgumentTermPtr = ↑OneArgumentTermObj;
  OneArgumentTermObj = object (TermExpressionObj)
    nArg: TermPtr;
    constructor Init(const aPos: Position; aKind: TermSort; aArg: TermPtr);
    destructor Done; virtual;
  end

```

This code is used in section 882.

898. Constructor.

```

⟨Implementing term AST 884⟩ +≡
constructor OneArgumentTermObj.Init(const aPos: Position; aKind: TermSort; aArg: TermPtr);
  begin nTermPos ← aPos; nTermSort ← aKind; nArg ← aArg;
  end;
destructor OneArgumentTermObj.Done;
  begin dispose(nArg, Done);
  end;

```

899. Selector terms. When we have an aggregate term (i.e., an instance of a structure), we want to refer to fields of the structure. This is done with selector terms. [[The selector number refers to the position in the underlying tuple of the structure instance.]]

```

⟨ Selector term (abstract syntax tree) 899 ⟩ ≡
  SelectorTermPtr = ↑SelectorTermObj;
  SelectorTermObj = object (OneArgumentTermObj)
    nSelectorSymbol: integer;
    constructor Init(const aPos: Position; aSelectorNr: integer; aArg: TermPtr);
    destructor Done; virtual;
  end

```

This code is used in section 882.

900. Constructor.

```

⟨ Implementing term AST 884 ⟩ +=
constructor SelectorTermObj.Init(const aPos: Position; aSelectorNr: integer; aArg: TermPtr);
  begin inherited Init(Apos, wsSelectorTerm, aArg); nSelectorSymbol ← aSelectorNr;
  end;
destructor SelectorTermObj.Done;
  begin dispose(nArg, Done);
  end;

```

901. Internal selector terms. An “internal selector” term refers to the case where we have in Mizar “the *⟨selector⟩*” treated as a term.

```

⟨ Internal selector term (abstract syntax tree) 901 ⟩ ≡
  InternalSelectorTermPtr = ↑InternalSelectorTermObj;
  InternalSelectorTermObj = object (TermExpressionObj)
    nSelectorSymbol: integer;
    constructor Init(const aPos: Position; aSelectorNr: integer);
  end

```

This code is used in section 882.

902. Constructor.

```

⟨ Implementing term AST 884 ⟩ +=
constructor InternalSelectorTermObj.Init(const aPos: Position; aSelectorNr: integer);
  begin nTermPos ← aPos; nTermSort ← wsInternalSelectorTerm; nSelectorSymbol ← aSelectorNr;
  end;

```

903. Aggregate terms. When we construct a new instance of a structure, well, that’s a term. Such terms are called “aggregate terms” in Mizar.

```

⟨ Aggregate term (abstract syntax tree) 903 ⟩ ≡
  AggregateTermPtr = ↑AggregateTermObj;
  AggregateTermObj = object (TermWithArgumentsObj)
    nStructSymbol: integer;
    constructor Init(const aPos: Position; aStructSymbol: integer; aArgs: PList);
    destructor Done; virtual;
  end

```

This code is used in section 882.

```

 $\langle \text{Implementing term AST } 884 \rangle + \equiv$ 
constructor AggregateTermObj.Init(const aPos: Position; aStructSymbol: integer; aArgs: PList);
  begin inherited Init(aPos, wsAggregateTerm, aArgs); nStructSymbol  $\leftarrow$  aStructSymbol;
  end;

destructor AggregateTermObj.Done;
  begin dispose(nArgs, Done);
  end;

```

```

⟨ Forgetful functor (abstract syntax tree) 905 ⟩ ≡
  ForgetfulFunctorTermPtr = ↑ForgetfulFunctorTermObj;
  ForgetfulFunctorTermObj = object (OneArgumentTermObj)
    nStructSymbol: integer;
    constructor Init(const aPos: Position; aStructSymbol: integer; aArg: TermPtr);
    destructor Done; virtual;
end

```

```

⟨Implementing term AST 884⟩ ≡
constructor ForgetfulFunctorTermObj.Init(const aPos: Position; aStructSymbol: integer;
                                           aArg: TermPtr);
  begin inherited Init(aPos, wsForgetfulFunctorTerm, aArg); nStructSymbol ← aStructSymbol;
end;
destructor ForgetfulFunctorTermObj.Done;
  begin dispose(nArg, Done);
end;

```

```

⟨ Internal forgetful functors (abstract syntax tree) 907 ⟩ ≡
  InternalForgetfulFunctorTermPtr = ↑InternalForgetfulFunctorTermObj;
  InternalForgetfulFunctorTermObj = object (TermExpressionObj)
    nStructSymbol: integer;
    constructor Init(const aPos: Position; aStructSymbol: integer);
  end

```

```

  ⟨Implementing term AST 884⟩  $\vdash$ 
constructor InternalForgetfulFunctorTermObj.Init(const aPos: Position; aStructSymbol: integer);
  begin nTermPos  $\leftarrow$  aPos; nTermSort  $\leftarrow$  wsInternalForgetfulFunctorTerm;
  nStructSymbol  $\leftarrow$  aStructSymbol;
end;

```


909. Simple Fraenkel terms. Fraenkel terms are set-builder notation in Mizar. But “simple” Fraenkel terms occurs when we have “the set of all $\langle termexpr \rangle$ ”.

```

⟨ Fraenkel terms (abstract syntax tree) 909 ⟩ ≡
  SimpleFraenkelTermPtr = ↑SimpleFraenkelTermObj;
  SimpleFraenkelTermObj = object (TermExpressionObj)
    nPostqualification: PList; { of segments }
    nSample: TermPtr;
    constructor Init(const aPos: Position; aPostqual: PList; aSample: TermPtr);
    destructor Done; virtual;
  end ;

```

See also section 911.

This code is used in section 882.

910. Constructor.

```

⟨ Implementing term AST 884 ⟩ +≡
constructor SimpleFraenkelTermObj.Init(const aPos: Position; aPostqual: PList; aSample: TermPtr);
  begin nTermPos ← aPos; nTermSort ← wsSimpleFraenkelTerm; nPostqualification ← aPostqual;
  nSample ← aSample;
  end;
destructor SimpleFraenkelTermObj.Done;
  begin dispose(nSample, Done);
  end;

```

911. Fraenkel terms. Fraenkel terms are sets given by set-builder notation, usually they look like

$$\{f(\vec{t}) \text{ where } \vec{t} \text{ being } \vec{T} : P[\vec{t}]\}$$

This is technically a higher-order object (look, it takes a functor f and a predicate P).

```

⟨ Fraenkel terms (abstract syntax tree) 909 ⟩ +≡
  FraenkelTermPtr = ↑FraenkelTermObj;
  FraenkelTermObj = object (SimpleFraenkelTermObj)
    nFormula: FormulaPtr;
    constructor Init(const aPos: Position; aPostqual: PList; aSample: TermPtr; aFormula:
      FormulaPtr);
    destructor Done; virtual;
  end

```

912. Constructor.

```

⟨ Implementing term AST 884 ⟩ +≡
constructor FraenkelTermObj.Init(const aPos: Position;
  aPostqual: PList;
  aSample: TermPtr;
  aFormula: FormulaPtr);
  begin nTermPos ← aPos; nTermSort ← wsFraenkelTerm; nPostqualification ← aPostqual;
  nSample ← aSample; nFormula ← aFormula;
  end;
destructor FraenkelTermObj.Done;
  begin dispose(nSample, Done); dispose(nPostqualification, Done); dispose(nFormula, Done);
  end;

```

913. Qualified terms. We may wish to explicitly type cast a term (e.g., “`term qua newType`”), which is what Mizar calls a “qualified term”.

```

⟨ Qualified term (abstract syntax tree) 913 ⟩ ≡
  QualifiedTermPtr = ↑QualifiedTermObj;
  QualifiedTermObj = object (ExactlyTermObj)
    nQualification: TypePtr;
    constructor Init(const aPos: Position; aSubject: TermPtr; aType: TypePtr);
    destructor Done; virtual;
  end

```

This code is used in section 882.

914. Constructor.

```

⟨ Implementing term AST 884 ⟩ +≡
constructor QualifiedTermObj.Init(const aPos: Position; aSubject: TermPtr; aType: TypePtr);
  begin nTermPos ← aPos; nTermSort ← wsQualificationTerm; nSubject ← aSubject;
  nQualification ← aType;
  end;
destructor QualifiedTermObj.Done;
  begin dispose(nSubject, Done); dispose(nQualification, Done);
  end;

```

915. Exactly terms. This is the base class for qualified terms. It does not appear to be used anywhere outside the abstract syntax module.

```

⟨ Exactly term (abstract syntax tree) 915 ⟩ ≡
  ExactlyTermPtr = ↑ExactlyTermObj;
  ExactlyTermObj = object (TermExpressionObj)
    nSubject: TermPtr;
    constructor Init(const aPos: Position; aSubject: TermPtr);
    destructor Done; virtual;
  end

```

This code is used in section 882.

916. Constructor.

```

⟨ Implementing term AST 884 ⟩ +≡
constructor ExactlyTermObj.Init(const aPos: Position; aSubject: TermPtr);
  begin nTermPos ← aPos; nTermSort ← wsExactlyTerm; nSubject ← aSubject;
  end;
destructor ExactlyTermObj.Done;
  begin dispose(nSubject, Done);
  end;

```

917. Choice terms. This refers to “the $\langle type \rangle$ ” terms. It is a “global choice term” of sorts, except it “operates” on soft types instead of arbitrary predicates.

```

⟨ Choice term (abstract syntax tree) 917 ⟩ ≡
  ChoiceTermPtr = ↑ChoiceTermObj;
  ChoiceTermObj = object (TermExpressionObj)
    nChoiceType: TypePtr;
    constructor Init(const aPos: Position; aType: TypePtr);
    destructor Done; virtual;
end

```

This code is used in section 882.

918. Constructor.

```

⟨ Implementing term AST 884 ⟩ +≡
constructor ChoiceTermObj.Init(const aPos: Position; aType: TypePtr);
  begin nTermPos ← aPos; nTermSort ← wsGlobalChoiceTerm; nChoiceType ← aType;
  end;
destructor ChoiceTermObj.Done;
  begin dispose(nChoiceType, Done);
  end;

```

919. It terms. When we define a new mode [type] or functors [terms], Mizar introduces an anaphoric keyword “it” referring to an example of the mode (resp., to the term being defined). Here I borrow the scary phrase “anaphoric” from Lisp macros, so blame Paul Graham for this pretentiousness.

```

⟨ “It” term (abstract syntax tree) 919 ⟩ ≡
  ItTermPtr = ↑ItTermObj;
  ItTermObj = object (TermExpressionObj)
    constructor Init(const aPos: Position);
  end

```

This code is used in section 882.

920. Constructor.

```

⟨ Implementing term AST 884 ⟩ +≡
constructor ItTermObj.Init(const aPos: Position);
  begin nTermPos ← aPos; nTermSort ← wsItTerm;
  end;

```

921. Incorrect terms. Generically, when we run into an error of some kind, we represent the term with an *Incorrect* term instance. This will allow Mizar to continue working when the user goofed.

```

⟨ Incorrect term (abstract syntax tree) 921 ⟩ ≡
  IncorrectTermPtr = ↑IncorrectTermObj;
  IncorrectTermObj = object (TermExpressionObj)
    constructor Init(const aPos: Position);
  end

```

This code is used in section 882.

922. Constructor.

```

⟨ Implementing term AST 884 ⟩ +≡
constructor IncorrectTermObj.Init(const aPos: Position);
  begin nTermPos ← aPos; nTermSort ← wsErrorTerm;
  end;

```

Section 20.2. TYPES (ABSTRACT SYNTAX TREE)

923. The grammar for Mizar types looks like:

```

Type-Expression = "(" Radix-Type ")"
| Adjective-Cluster Type-Expression
| Radix-Type .
Structure-Type-Expression =
  "(" Structure-Symbol ["over" Term-Expression-List] ")"
| Adjective-Cluster Structure-Symbol [ "over" Term-Expression-List ].
Radix-Type = Mode-Symbol [ "of" Term-Expression-List ]
| Structure-Symbol [ "over" Term-Expression-List ] .
Type-Expression-List = Type-Expression { "," Type-Expression } .

```

So there are several main sources of modes [types]: structures, primitive types (like “set” and “object”), and affixing adjectives to types.

For readers who are unfamiliar with types in Mizar, they are “soft types”. What does this mean? Well, we refer the reader to Free Wiedijk’s “Mizar’s Soft Type System” (in K. Schneider and J. Brandt, eds., *Theorem Proving in Higher Order Logics. TPHOLs 2007*, Springer, [doi:10.1007/978-3-540-74591-4_28](https://doi.org/10.1007/978-3-540-74591-4_28)). Essentially, a type ascription in Mizar of the form “for x being Foo st P[x] holds Q[x]”, this is equivalent to Foo being a unary predicate and the formula in first-order logic is “ $\forall x. \text{Foo}[x] \wedge Q[x] \implies P[x]$ ”.

924. We have an abstract base class for types.

```

⟨ Abstract base class for types 924 ⟩ ≡
  TypeSort = (wsErrorType, wsStandardType, wsStructureType, wsClusteredType, wsReservedDscrType);
  { Initial structures }
  TypePtr = ↑TypeExpressionObj;
  TypeExpressionObj = object (MObject)
    nTypeSort: TypeSort;
    nTypePos: Position;
  end

```

This code is used in section 864.

925. Radix type. A “radix type” refers to any type of the form “⟨RadixType⟩ of T_1, \dots, T_n ”. This usually appears when defining a new expandable mode, where we have:

“mode ⟨Expandable Mode⟩ is ⟨Adjective₁⟩ ... ⟨Adjective_n⟩ ⟨Radix Type⟩”

This appears to be used only in definitions.

```

⟨ Classes for type (abstract syntax tree) 925 ⟩ ≡
  { Types }
  RadixTypePtr = ↑RadixTypeObj;
  RadixTypeObj = object (TypeExpressionObj)
    nArgs: PList; { of }
    constructor Init(const aPos: Position; aKind: TypeSort; aArgs: PList);
    destructor Done; virtual;
  end ;

```

See also sections 927, 929, 931, and 933.

This code is used in section 864.

926. Constructor.

⟨Implementing type AST 926⟩ ≡
constructor *RadixTypeObj.Init*(**const** *aPos*: *Position*; *aKind*: *TypeSort*; *aArgs*: *PList*);
 begin *nTypePos* ← *aPos*; *nTypeSort* ← *aKind*; *nArgs* ← *aArgs*;
 end;
destructor *RadixTypeObj.Done*;
 begin *dispose*(*nArgs*, *Done*);
 end;

See also sections 928, 930, 932, and 934.

This code is used in section 863.

927. Standard type. When we want to refer to an expandable mode in a Mizar formula, then it is represented by a “standard type”. This contrasts it with “clustered types” (i.e., a type stacked with adjectives) and “structure types”.

⟨Classes for type (abstract syntax tree) 925⟩ +≡
 StandardTypePtr = ↑*StandardTypeObj*;
 StandardTypeObj = **object** (*RadixTypeObj*)
 nModeSymbol: *integer*;
 constructor *Init*(**const** *aPos*: *Position*; *aModeSymbol*: *integer*; *aArgs*: *PList*);
 destructor *Done*; *virtual*;
 end ;

928. Constructor.

⟨Implementing type AST 926⟩ +≡
constructor *StandardTypeObj.Init*(**const** *aPos*: *Position*; *aModeSymbol*: *integer*; *aArgs*: *PList*);
 begin *inherited Init*(*aPos*, *wsStandardType*, *aArgs*); *nModeSymbol* ← *aModeSymbol*;
 end;
destructor *StandardTypeObj.Done*;
 begin *inherited Done*;
 end;

929. Structure type. When we define a new structure, we are really introducing a new type. [[The *aArgs* tracks its parent structures and parameter types.]] The structure type extends the *RadixType* class because *RadixType* instances can be “stacked with adjectives”.

⟨Classes for type (abstract syntax tree) 925⟩ +≡
 StructTypePtr = ↑*StructTypeObj*;
 StructTypeObj = **object** (*RadixTypeObj*)
 nStructSymbol: *integer*;
 constructor *Init*(**const** *aPos*: *Position*; *aStructSymbol*: *integer*; *aArgs*: *PList*);
 destructor *Done*; *virtual*;
 end ;

930. Constructor.

⟨Implementing type AST 926⟩ +≡
constructor *StructTypeObj.Init*(**const** *aPos*: *Position*; *aStructSymbol*: *integer*; *aArgs*: *PList*);
 begin *inherited Init*(*aPos*, *wsStructureType*, *aArgs*); *nStructSymbol* ← *aStructSymbol*;
 end;
destructor *StructTypeObj.Done*;
 begin *inherited Done*;
 end;

931. Clustered type. The clustered type describes the situation where we accumulate *aCluster* of adjectives atop *aType*.

```

⟨ Classes for type (abstract syntax tree) 925 ⟩ +≡
  ClusteredTypePtr = ↑ClusteredTypeObj;
  ClusteredTypeObj = object (TypeExpressionObj)
    nAdjectiveCluster: PList;
    nType: TypePtr;
    constructor Init(const aPos: Position; aCluster: PList; aType: TypePtr);
    destructor Done; virtual;
end ;

```

932. Constructor.

```

⟨ Implementing type AST 926 ⟩ +≡
constructor ClusteredTypeObj.Init(const aPos: Position; aCluster: PList; aType: TypePtr);
  begin nTypePos ← aPos; nTypeSort ← wsClusteredType; nAdjectiveCluster ← aCluster;
  nType ← aType;
end;
destructor ClusteredTypeObj.Done;
  begin dispose(nAdjectiveCluster, Done); dispose(nType, Done);
end;

```

933. Incorrect type. We want Mizar to be resilient against typing errors, so we have an *IncorrectType* node for the syntax tree. The alternative would be to crash upon error.

```

⟨ Classes for type (abstract syntax tree) 925 ⟩ +≡
  IncorrectTypePtr = ↑IncorrectTypeObj;
  IncorrectTypeObj = object (TypeExpressionObj)
    constructor Init(const aPos: Position);
end

```

934. Constructor.

```

⟨ Implementing type AST 926 ⟩ +≡
constructor IncorrectTypeObj.Init(const aPos: Position);
  begin nTypePos ← aPos; nTypeSort ← wsErrorType;
end;

```

Section 20.3. FORMULAS (ABSTRACT SYNTAX TREE)

935. We have an abstract base class for formulas.

(Abstract base class for formulas 935) \equiv

```

FormulaSort = (wsErrorFormula, wsThesis, wsContradiction, wsRightSideOfPredicativeFormula,
wsPredicativeFormula, wsMultiPredicativeFormula, wsPrivatePredicateFormula,
wsAttributiveFormula, wsQualifyingFormula, wsUniversalFormula, wsExistentialFormula,
wsNegatedFormula, wsConjunctiveFormula, wsDisjunctiveFormula, wsConditionalFormula,
wsBiconditionalFormula, wsFlexaryConjunctiveFormula, wsFlexaryDisjunctiveFormula);
FormulaPtr =  $\uparrow$ FormulaExpressionObj;
FormulaExpressionObj = object (MObject)
  nFormulaSort: FormulaSort;
  nFormulaPos: Position;
end

```

This code is used in section 864.

936. The syntax for Mizar formulas looks like:

```

Formula-Expression = "(" Formula-Expression ")"
| Atomic-Formula-Expression
| Quantified-Formula-Expression
| Formula-Expression "&" Formula-Expression
| Formula-Expression "&" "." "&" Formula-Expression
| Formula-Expression "or" Formula-Expression
| Formula-Expression "or" "." "or" Formula-Expression
| Formula-Expression "implies" Formula-Expression
| Formula-Expression "iff" Formula-Expression
| "not" Formula-Expression
| "contradiction"
| "thesis" .

Atomic-Formula-Expression =
  [Term-Expression-List] [("does" | "do") "not"] Predicate-Symbol [Term-Expression-List]
  { [("does" | "do") "not"] Predicate-Symbol Term-Expression-List }
| Predicate-Identifier "[" [ Term-Expression-List ] "]"
| Term-Expression "is" Adjective { Adjective }
| Term-Expression "is" Type-Expression .

Quantified-Formula-Expression =
  "for" Qualified-Variables
  [ "st" Formula-Expression ]
  ( "holds" Formula-Expression | Quantified-Formula-Expression )
| "ex" Qualified-Variables "st" Formula-Expression .

```

937. Right-side of predicative formula.

⟨Classes for formula (abstract syntax tree) 937⟩ ≡
 { Formulas }
RightSideOfPredicativeFormulaPtr = ↑*RightSideOfPredicativeFormulaObj*;
RightSideOfPredicativeFormulaObj = **object** (*FormulaExpressionObj*)
 nPredNr: integer;
 nRightArgs: PList;
 constructor *Init*(**const** *aPos*: Position; *aPredNr*: integer; *aRightArgs*: PList);
 destructor *Done*; virtual;
end

See also sections 939, 941, 943, 945, 947, 949, 951, 953, 955, 957, 959, 961, 963, 965, 967, 969, 971, 973, and 975.

This code is used in section 864.

938. Constructor.

⟨Implementing formula AST 938⟩ ≡
constructor *RightSideOfPredicativeFormulaObj.Init*(**const** *aPos*: Position;
 aPredNr: integer;
 aRightArgs: PList);
begin *nFormulaPos* ← *aPos*; *nFormulaSort* ← *wsRightSideOfPredicativeFormula*;
 nPredNr ← *aPredNr*; *nRightArgs* ← *aRightArgs*;
end;
destructor *RightSideOfPredicativeFormulaObj.Done*;
begin *dispose*(*nRightArgs*, *Done*);
end;

See also sections 940, 942, 944, 946, 948, 950, 952, 954, 956, 958, 960, 962, 964, 966, 968, 970, 972, 974, and 976.

This code is used in section 863.

939. Predicative formula. A “predicative” formula refers to a formula involving predicates. A predicate will have a list of terms \vec{t} it expects as arguments, as well as two numbers ℓ, r such that t_1, \dots, t_ℓ are the arguments to its left, and $t_{\ell+1}, \dots, t_{\ell+r}$ are on the right. When $\ell = 0$, all arguments are on the right; and when $r = 0$, all arguments are on the left.

⟨Classes for formula (abstract syntax tree) 937⟩ +≡
PredicativeFormulaPtr = ↑*PredicativeFormulaObj*;
PredicativeFormulaObj = **object** (*RightSideOfPredicativeFormulaObj*)
 nLeftArgs: PList;
 constructor *Init*(**const** *aPos*: Position; *aPredNr*: integer; *aLeftArgs*, *aRightArgs*: PList);
 destructor *Done*; virtual;
end

940. Constructor.

⟨Implementing formula AST 938⟩ +≡
constructor *PredicativeFormulaObj.Init*(**const** *aPos*: Position;
 aPredNr: integer;
 aLeftArgs, *aRightArgs*: PList);
begin *nFormulaPos* ← *aPos*; *nFormulaSort* ← *wsPredicativeFormula*; *nPredNr* ← *aPredNr*;
 nLeftArgs ← *aLeftArgs*; *nRightArgs* ← *aRightArgs*;
end;
destructor *PredicativeFormulaObj.Done*;
begin *dispose*(*nLeftArgs*, *Done*); *dispose*(*nRightArgs*, *Done*);
end;

941. Multi-predicative formula. The Working Mathematician writes things like “ $1 \leq i \leq \|T\|$ ” and Mizar wants to support this. Multi-predicative formulas are of this form “ $1 \leq i \leq \|T\|$ ”. This occurs in VECTSP13, for example.

```

⟨ Classes for formula (abstract syntax tree) 937 ⟩ +=
  MultiPredicativeFormulaPtr = ↑MultiPredicativeFormulaObj;
  MultiPredicativeFormulaObj = object (FormulaExpressionObj)
    nScraps: PList;
    constructor Init(const aPos: Position; aScraps: PList);
    destructor Done; virtual;
end

```

942. Constructor.

```

⟨ Implementing formula AST 938 ⟩ +=
constructor MultiPredicativeFormulaObj.Init(const aPos: Position; aScraps: PList);
  begin nFormulaPos ← aPos; nFormulaSort ← wsMultiPredicativeFormula; nScraps ← aScraps;
  end;
destructor MultiPredicativeFormulaObj.Done;
  begin dispose(nScraps, Done);
  end;

```

943. Attributive formula. As part of Mizar’s soft type system, we can use attributes (adjectives) to form a formula like “ $\langle term \rangle$ is $\langle adjective \rangle$ ”. We can stack multiple adjectives in an attributive formula.

```

⟨ Classes for formula (abstract syntax tree) 937 ⟩ +=
  AttributiveFormulaPtr = ↑AttributiveFormulaObj;
  AttributiveFormulaObj = object (FormulaExpressionObj)
    nSubject: TermPtr;
    nAdjectives: PList;
    constructor Init(const aPos: Position; aSubject: TermPtr; aAdjectives: PList);
    destructor Done; virtual;
end

```

944. Constructor.

```

⟨ Implementing formula AST 938 ⟩ +=
constructor AttributiveFormulaObj.Init(const aPos: Position; aSubject: TermPtr; aAdjectives: PList);
  begin nFormulaPos ← aPos; nFormulaSort ← wsAttributiveFormula; nSubject ← aSubject;
  nAdjectives ← aAdjectives;
  end;
destructor AttributiveFormulaObj.Done;
  begin dispose(nSubject, Done); dispose(nAdjectives, Done);
  end;

```

945. Private predicative formula. When we have “**defpred** P[...] **means** ...” in Mizar, we refer to “P” as a private predicate. It is represented in the abstract syntax tree as a private predicative formula object.

```

⟨ Classes for formula (abstract syntax tree) 937 ⟩ +≡
  PrivatePredicativeFormulaPtr = ↑PrivatePredicativeFormulaObj;
  PrivatePredicativeFormulaObj = object (FormulaExpressionObj)
    nPredIdNr: integer;
    nArgs: PList;
    constructor Init(const aPos: Position; aPredIdNr: integer; aArgs: PList);
    destructor Done; virtual;
end

```

946. Constructor.

```

⟨ Implementing formula AST 938 ⟩ +≡
constructor PrivatePredicativeFormulaObj.Init(const aPos: Position;
    aPredIdNr: integer;
    aArgs: PList);

  begin nFormulaPos ← aPos; nFormulaSort ← wsPrivatePredicateFormula; nPredIdNr ← aPredIdNr;
  nArgs ← aArgs;
end;

destructor PrivatePredicativeFormulaObj.Done;
  begin dispose(nArgs, Done);
end;

```

947. Qualifying formula. Using Mizar’s soft type system, we may have formulas of the form “⟨term⟩ is ⟨type⟩”. These are referred to as “qualifying formulas”, at least when discussing the abstract syntax tree.

```

⟨ Classes for formula (abstract syntax tree) 937 ⟩ +≡
  QualifyingFormulaPtr = ↑QualifyingFormulaObj;
  QualifyingFormulaObj = object (FormulaExpressionObj)
    nSubject: TermPtr;
    nType: TypePtr;
    constructor Init(const aPos: Position; aSubject: TermPtr; aType: TypePtr); y
    destructor Done; virtual;
end

```

948. Constructor.

```

⟨ Implementing formula AST 938 ⟩ +≡
constructor QualifyingFormulaObj.Init(const aPos: Position; aSubject: TermPtr; aType: TypePtr);
  begin nFormulaPos ← aPos; nFormulaSort ← wsQualifyingFormula; nSubject ← aSubject;
  nType ← aType;
end;

destructor QualifyingFormulaObj.Done;
  begin dispose(nSubject, Done); dispose(nType, Done);
end;

```

949. Negative formula. Now we can proceed with the familiar formulas in first-order logic. Negative formulas are of the form $\neg\varphi$ for some formula φ .

```

⟨ Classes for formula (abstract syntax tree) 937 ⟩ +=
  NegativeFormulaPtr = ↑NegativeFormulaObj;
  NegativeFormulaObj = object (FormulaExpressionObj)
    nArg: FormulaPtr;
    constructor Init(const aPos: Position; aArg: FormulaPtr);
    destructor Done; virtual;
end

```

950. Constructor.

```

⟨ Implementing formula AST 938 ⟩ +=
constructor NegativeFormulaObj.Init(const aPos: Position; aArg: FormulaPtr);
  begin nFormulaPos ← aPos; nFormulaSort ← wsNegatedFormula; nArg ← aArg;
  end;
destructor NegativeFormulaObj.Done;
  begin dispose(nArg, Done);
  end;

```

951. Binary arguments formula. We have a class describing formulas involving binary logical connectives. We will extend it to describe conjunctive formulas, disjunctive formulas, conditionals, biconditionals, etc.

```

⟨ Classes for formula (abstract syntax tree) 937 ⟩ +=
  BinaryFormulaPtr = ↑BinaryArgumentsFormula;
  BinaryArgumentsFormula = object (FormulaExpressionObj)
    nLeftArg, nRightArg: FormulaPtr;
    constructor Init(const aPos: Position; aLeftArg, aRightArg: FormulaPtr);
    destructor Done; virtual;
end

```

952. Constructor.

```

⟨ Implementing formula AST 938 ⟩ +=
constructor BinaryArgumentsFormula.Init(const aPos: Position; aLeftArg, aRightArg: FormulaPtr);
  begin nFormulaPos ← aPos; nLeftArg ← aLeftArg; nRightArg ← aRightArg;
  end;
destructor BinaryArgumentsFormula.Done;
  begin dispose(nLeftArg, Done); dispose(nRightArg, Done);
  end;

```

953. Conjunctive formula. A conjunctive formula looks like $\varphi \wedge \psi$ where φ and ψ are logical formulas.

```

⟨ Classes for formula (abstract syntax tree) 937 ⟩ +=
  ConjunctiveFormulaPtr = ↑ConjunctiveFormulaObj;
  ConjunctiveFormulaObj = object (BinaryArgumentsFormula)
    constructor Init(const aPos: Position; aLeftArg, aRightArg: FormulaPtr);
end

```

954. Constructor.

⟨Implementing formula AST 938⟩ +≡

```
constructor ConjunctiveFormulaObj.Init(const aPos: Position; aLeftArg, aRightArg: FormulaPtr);
  begin inherited Init(aPos, aLeftArg, aRightArg); nFormulaSort ← wsConjunctiveFormula;
  end;
```

955. Disjunctive formula. Disjunctive formulas look like $\varphi \vee \psi$ where φ and ψ are formulas.

⟨Classes for formula (abstract syntax tree) 937⟩ +≡

```
DisjunctiveFormulaPtr = ↑DisjunctiveFormulaObj;
DisjunctiveFormulaObj = object (BinaryArgumentsFormula)
  constructor Init(const aPos: Position; aLeftArg, aRightArg: FormulaPtr);
  end
```

956. Constructor.

⟨Implementing formula AST 938⟩ +≡

```
constructor DisjunctiveFormulaObj.Init(const aPos: Position;
  aLeftArg, aRightArg: FormulaPtr);
  begin inherited Init(aPos, aLeftArg, aRightArg); nFormulaSort ← wsDisjunctiveFormula;
  end;
```

957. Conditional formula. Conditional formulas look like $\varphi \implies \psi$ where φ and ψ are formulas.

⟨Classes for formula (abstract syntax tree) 937⟩ +≡

```
ConditionalFormulaPtr = ↑ConditionalFormulaObj;
ConditionalFormulaObj = object (BinaryArgumentsFormula)
  constructor Init(const aPos: Position; aLeftArg, aRightArg: FormulaPtr);
  end
```

958. Constructor.

⟨Implementing formula AST 938⟩ +≡

```
constructor ConditionalFormulaObj.Init(const aPos: Position; aLeftArg, aRightArg: FormulaPtr);
  begin inherited Init(aPos, aLeftArg, aRightArg); nFormulaSort ← wsConditionalFormula;
  end;
```

959. Biconditional formula. Biconditional formulas look like $\varphi \iff \psi$ where φ and ψ are formulas.

⟨Classes for formula (abstract syntax tree) 937⟩ +≡

```
BiconditionalFormulaPtr = ↑BiconditionalFormulaObj;
BiconditionalFormulaObj = object (BinaryArgumentsFormula)
  constructor Init(const aPos: Position; aLeftArg, aRightArg: FormulaPtr);
  end
```

960. Constructor.

⟨Implementing formula AST 938⟩ +≡

```
constructor BiconditionalFormulaObj.Init(const aPos: Position; aLeftArg, aRightArg: FormulaPtr);
  begin inherited Init(aPos, aLeftArg, aRightArg); nFormulaSort ← wsBiconditionalFormula;
  end;
```

961. Flexary Conjunctive formula. Flexary conjunctive formulas are unique to Mizar, though the Working Mathematician would recognize them as “just a bunch of conjunctions”. These look like $\varphi[1] \wedge \dots \wedge \varphi[n]$ where $\varphi[i]$ is a formula parametrized by a natural number i .

```

⟨Classes for formula (abstract syntax tree) 937⟩ +≡
  FlexaryConjunctiveFormulaPtr = ↑FlexaryConjunctiveFormulaObj;
  FlexaryConjunctiveFormulaObj = object (BinaryArgumentsFormula)
    constructor Init(const aPos: Position; aLeftArg, aRightArg: FormulaPtr);
  end

```

962. Constructor.

```

⟨Implementing formula AST 938⟩ +≡
constructor FlexaryConjunctiveFormulaObj.Init(const aPos: Position;
                                              aLeftArg, aRightArg: FormulaPtr);
begin inherited Init(aPos, aLeftArg, aRightArg); nFormulaSort ← wsFlexaryConjunctiveFormula;
end;

```

963. Flexary Disjunctive formula. Flexary disjunctive formulas are unique to Mizar, though the Working Mathematician would recognize them as “just a bunch of disjunctions”. These look like $\varphi[1] \vee \dots \vee \varphi[n]$ where $\varphi[i]$ is a formula parametrized by a natural number i .

```

⟨Classes for formula (abstract syntax tree) 937⟩ +≡
  FlexaryDisjunctiveFormulaPtr = ↑FlexaryDisjunctiveFormulaObj;
  FlexaryDisjunctiveFormulaObj = object (BinaryArgumentsFormula)
    constructor Init(const aPos: Position; aLeftArg, aRightArg: FormulaPtr);
  end

```

964. Constructor.

```

⟨Implementing formula AST 938⟩ +≡
constructor FlexaryDisjunctiveFormulaObj.Init(const aPos: Position;
                                              aLeftArg, aRightArg: FormulaPtr);
begin inherited Init(aPos, aLeftArg, aRightArg); nFormulaSort ← wsFlexaryDisjunctiveFormula;
end;

```

965. Quantified formula. First-order logic is distinguished by the use of terms and quantifying formulas over terms. We have a base class for quantified formulas. Using the Mizar soft type system, quantified variables are “qualified segments”.

```

⟨Classes for formula (abstract syntax tree) 937⟩ +≡
  QuantifiedFormulaPtr = ↑QuantifiedFormulaObj;
  QuantifiedFormulaObj = object (FormulaExpressionObj)
    nSegment: QualifiedSegmentPtr;
    nScope: FormulaPtr;
    constructor Init(const aPos: Position; aSegment: QualifiedSegmentPtr; aScope: FormulaPtr);
    destructor Done; virtual;
  end

```

966. Constructor.

⟨Implementing formula AST 938⟩ +≡

```

constructor QuantifiedFormulaObj.Init(const aPos: Position;
                                         aSegment: QualifiedSegmentPtr;
                                         aScope: FormulaPtr);
    begin nFormulaPos ← aPos; nSegment ← aSegment; nScope ← aScope;
    end;
destructor QuantifiedFormulaObj.Done;
    begin dispose(nSegment, Done); dispose(nScope, Done);
    end;

```

967. Universal formula. When we want to describe a formula of the form “ $\forall x : T. \varphi[x]$ ” where T is a soft type and $\varphi[x]$ is a formula parametrized by x .

⟨Classes for formula (abstract syntax tree) 937⟩ +≡

```

UniversalFormulaPtr = ↑UniversalFormulaObj;
UniversalFormulaObj = object (QuantifiedFormulaObj)
    constructor Init(const aPos: Position; aSegment: QualifiedSegmentPtr; aScope: FormulaPtr);
end

```

968. Constructor.

⟨Implementing formula AST 938⟩ +≡

```

constructor UniversalFormulaObj.Init(const aPos: Position;
                                         aSegment: QualifiedSegmentPtr;
                                         aScope: FormulaPtr);
    begin inherited Init(aPos, aSegment, aScope); nFormulaSort ← wsUniversalFormula;
    end;

```

969. Existential formula. The other quantified formula are existentially quantified formulas, which resemble “ $\exists x : T. \varphi[x]$ ” where T is a soft type and $\varphi[x]$ is a formula parametrized by x .

⟨Classes for formula (abstract syntax tree) 937⟩ +≡

```

ExistentialFormulaPtr = ↑ExistentialFormulaObj;
ExistentialFormulaObj = object (QuantifiedFormulaObj)
    constructor Init(const aPos: Position; aSegment: QualifiedSegmentPtr; aScope: FormulaPtr);
end

```

970. Constructor.

⟨Implementing formula AST 938⟩ +≡

```

constructor ExistentialFormulaObj.Init(const aPos: Position;
                                         aSegment: QualifiedSegmentPtr;
                                         aScope: FormulaPtr);
    begin inherited Init(aPos, aSegment, aScope); nFormulaSort ← wsExistentialFormula;
    end;

```

971. Contradiction formula. The canonical contradiction \perp in Mizar is represented by the reserved keyword “contradiction”.

⟨Classes for formula (abstract syntax tree) 937⟩ +≡

```

ContradictionFormulaPtr = ↑ContradictionFormulaObj;
ContradictionFormulaObj = object (FormulaExpressionObj)
    constructor Init(const aPos: Position);
end

```

972. Constructor.

⟨ Implementing formula AST 938 ⟩ +≡
constructor *ContradictionFormulaObj.Init*(**const** *aPos*: *Position*);
 begin *nFormulaPos* ← *aPos*; *nFormulaSort* ← *wsContradiction*;
 end;

973. Thesis formula. When we are in the middle of a proof, the goal or obligation left to be proven is called the “thesis”.

⟨ Classes for formula (abstract syntax tree) 937 ⟩ +≡
 ThesisFormulaPtr = ↑*ThesisFormulaObj*;
 ThesisFormulaObj = **object** (*FormulaExpressionObj*)
 constructor *Init*(**const** *aPos*: *Position*);
 end

974. Constructor.

⟨ Implementing formula AST 938 ⟩ +≡
constructor *ThesisFormulaObj.Init*(**const** *aPos*: *Position*);
 begin *nFormulaPos* ← *aPos*; *nFormulaSort* ← *wsThesis*;
 end;

975. Incorrect formula. We also have a node in abstract syntax trees for “incorrect” formulas.

⟨ Classes for formula (abstract syntax tree) 937 ⟩ +≡
 IncorrectFormulaPtr = ↑*IncorrectFormula*;
 IncorrectFormula = **object** (*FormulaExpressionObj*)
 constructor *Init*(**const** *aPos*: *Position*);
 end

976. Constructor.

⟨ Implementing formula AST 938 ⟩ +≡
constructor *IncorrectFormula.Init*(**const** *aPos*: *Position*);
 begin *nFormulaPos* ← *aPos*; *nformulaSort* ← *wsErrorFormula*;
 end;

Section 20.4. WITHIN EXPRESSIONS (DEFERRED)

977. The “first identification” process needs to track “within expressions”. You should probably come back to this section when you’ve arrived at the “first identification” unit.

```

⟨ Class for Within expression 977 ⟩ ≡
  biStackedPtr = ↑biStackedObj;
  biStackedObj = object (MObject)
    end;
  WithinExprPtr = ↑WithinExprObj;
  WithinExprObj = object (MObject)
    nExpKind: ExpKind;
    nStackArr: array of biStackedPtr;
    nStackCnt: integer;
    constructor Init(aExpKind : ExpKind);
    destructor Done; virtual;
    function CreateExpressionsVariableLevel: biStackedPtr; virtual; { ?? }
    procedure Process_Adjective(aAttr : AdjectiveExpressionPtr); virtual;
    procedure Process_AdjectiveList(aCluster : PList); virtual;
    procedure Process_Variable(var aVar : VariablePtr); virtual;
    procedure Process_ImplicitlyQualifiedVariable(var aSegm : ImplicitlyQualifiedSegmentPtr); virtual;
    procedure Process_VariablesSegment(aSegm : QualifiedSegmentPtr); virtual;
    procedure Process_StartVariableSegment; virtual;
    procedure Process_FinishVariableSegment; virtual;
    procedure Process_Type(aTyp : TypePtr); virtual;
    procedure Process_BinaryFormula(aFrm : BinaryFormulaPtr); virtual;
    procedure Process_StartQuantifiedFormula(aFrm : QuantifiedFormulaPtr); virtual;
    procedure Process_QuantifiedFormula(aFrm : QuantifiedFormulaPtr); virtual;
    procedure Process_FinishQuantifiedFormula(aFrm : QuantifiedFormulaPtr); virtual;
    procedure Process_Formula(aFrm : FormulaPtr); virtual;
    procedure Process_TermList(aTrmList : PList); virtual;
    procedure Process_SimpleTerm(var aTrm : SimpleTermPtr); virtual;
    procedure Process_StartFraenkelTerm(aTrm : SimpleFraenkelTermPtr); virtual;
    procedure Process_FinishFraenkelTerm(var aTrm : SimpleFraenkelTermPtr); virtual;
    procedure Process_FraenkelTermsScope(var aFrm : FormulaPtr); virtual;
    procedure Process_SimpleFraenkelTerm(var aTrm : SimpleFraenkelTermPtr); virtual;
    procedure Process_Term(var aTrm : TermPtr); virtual;
  end ;

```

This code is used in section 864.

```

978. ⟨ Within expression AST implementation 978 ⟩ ≡
constructor WithinExprObj.Init(aExpKind : ExpKind);
  begin setlength(nStackArr, 50); nStackCnt ← 0; nExpKind ← aExpKind;
  end;

```

See also sections 979, 980, 981, 982, 983, 984, 985, 986, 987, 988, 989, 990, 991, 992, 993, 994, 995, and 996.

This code is used in section 863.

```

979. ⟨ Within expression AST implementation 978 ⟩ +≡
destructor WithinExprObj.Done;
  begin inherited Done;
  end;

```


980. ⟨ Within expression AST implementation 978 ⟩ +≡

```
function WithinExprObj.CreateExpressionsVariableLevel: biStackedPtr;  
  begin result  $\leftarrow$  new(biStackedPtr, Init);  
  end;
```

981. ⟨ Within expression AST implementation 978 ⟩ +≡

```
procedure WithinExprObj.Process_Adjective(aAttr : AdjectiveExpressionPtr);  
  begin case aAttr↑.nAdjectiveSort of  
    wsAdjective: begin Process_TermList(AdjectivePtr(aAttr)↑.nArgs); { nAdjectiveSymbol; }  
    end;  
    wsNegatedAdjective: Process_Adjective(NegatedAdjectivePtr(aAttr)↑.nArg);  
  endcases;  
  end;
```

982. ⟨ Within expression AST implementation 978 ⟩ +≡

```
procedure WithinExprObj.Process_AdjectiveList(aCluster : PList);  
  var i: integer;  
  begin with aCluster↑ do  
    for i  $\leftarrow$  0 to Count − 1 do Process_Adjective(Items↑[i]);  
  end;
```

983. ⟨ Within expression AST implementation 978 ⟩ +≡

```
procedure WithinExprObj.Process_Variable(var aVar : VariablePtr);  
  begin end;
```

984. ⟨ Within expression AST implementation 978 ⟩ +≡

```
procedure WithinExprObj.Process_ImplicitlyQualifiedVariable(var aSegm : ImplicitlyQualifiedSegmentPtr);  
  begin Process_Variable(aSegm↑.nIdentifier);  
  end;
```

985. ⟨ Within expression AST implementation 978 ⟩ +≡

```
procedure WithinExprObj.Process_VariablesSegment(aSegm : QualifiedSegmentPtr);  
  var i: integer;  
  begin Process_StartVariableSegment;  
  case aSegm↑.nSegmentSort of  
    ikImplQualifiedSegm: Process_ImplicitlyQualifiedVariable(ImplicitlyQualifiedSegmentPtr(aSegm));  
    ikExplQualifiedSegm: with ExplicitlyQualifiedSegmentPtr(aSegm)↑ do  
      begin for i  $\leftarrow$  0 to nIdentifiers.Count − 1 do Process_Variable(VariablePtr(nIdentifiers.Items↑[i]));  
      Process_Type(nType);  
    end;  
  endcases; Process_FinishVariableSegment;  
  end;
```

986. ⟨ Within expression AST implementation 978 ⟩ +≡

```
procedure WithinExprObj.Process_StartVariableSegment;  
  begin end;  
  
procedure WithinExprObj.Process_FinishVariableSegment;  
  begin end;
```

987. ⟨ Within expression AST implementation 978 ⟩ +≡

```
procedure WithinExprObj.Process_TermList(aTrmList : PList);
  var i: integer;
  begin for i ← 0 to aTrmList↑.Count − 1 do Process_Term(TermPtr(aTrmList↑.Items↑[i]));
  end;
```

988. ⟨ Within expression AST implementation 978 ⟩ +≡

```
procedure WithinExprObj.Process_Type(aTyp : TypePtr);
  begin with aTyp↑ do
    begin case aTyp↑.nTypeSort of
      wsStandardType: with StandardTypePtr(aTyp↑) do
        begin { nModeSymbol }
        Process_TermList(nArgs);
        end;
      wsStructureType: with StructTypePtr(aTyp↑) do
        begin { nStructSymbol }
        Process_TermList(nArgs);
        end;
      wsClusteredType: with ClusteredTypePtr(aTyp↑) do
        begin Process_AdjectiveList(nAdjectiveCluster); Process_Type(nType);
        end;
      wsErrorType: ;
    endcases;
  end;
end;
```

989. ⟨ Within expression AST implementation 978 ⟩ +≡

```
procedure WithinExprObj.Process_BinaryFormula(aFrm : BinaryFormulaPtr);
  begin Process_Formula(aFrm↑.nLeftArg); Process_Formula(aFrm↑.nRightArg);
  end;
```

990. ⟨ Within expression AST implementation 978 ⟩ +≡

```
procedure WithinExprObj.Process_StartQuantifiedFormula(aFrm : QuantifiedFormulaPtr);
  begin end;
procedure WithinExprObj.Process_FinishQuantifiedFormula(aFrm : QuantifiedFormulaPtr);
  begin end;
```

991. ⟨ Within expression AST implementation 978 ⟩ +≡

```
procedure WithinExprObj.Process_QuantifiedFormula(aFrm : QuantifiedFormulaPtr);
  begin Process_VariablesSegment(aFrm↑.nSegment); Process_Formula(aFrm↑.nScope);
  end;
```

992. \langle Within expression AST implementation 978 $\rangle + \equiv$

```

procedure WithinExprObj.Process_Formula(aFrm : FormulaPtr);
  var i: integer;
  begin case aFrm↑.nFormulaSort of
    wsNegatedFormula: Process_Formula(NegativeFormulaPtr(aFrm)↑.nArg);
    wsConjunctiveFormula, wsDisjunctiveFormula, wsConditionalFormula,
      wsBiconditionalFormula, wsFlexaryConjunctiveFormula, wsFlexaryDisjunctiveFormula:
      Process_BinaryFormula(BinaryFormulaPtr(aFrm));
    wsRightSideOfPredicativeFormula: with RightSideOfPredicativeFormulaPtr(aFrm)↑ do
      begin { nPredNr }
        Process_TermList(nRightArgs);
      end;
    wsPredicativeFormula: with PredicativeFormulaPtr(aFrm)↑ do
      begin Process_TermList(nLeftArgs); { nPredNr }
        Process_TermList(nRightArgs);
      end;
    wsMultiPredicativeFormula: with MultiPredicativeFormulaPtr(aFrm)↑ do
      begin for i ← 0 to nScraps.Count − 1 do Process_Formula(nScraps.Items↑[i]);
      end;
    wsPrivatePredicateFormula: with PrivatePredicativeFormulaPtr(aFrm)↑ do
      begin { nPredIdNr }
        Process_TermList(nArgs);
      end;
    wsAttributiveFormula: with AttributiveFormulaPtr(aFrm)↑ do
      begin Process_Term(nSubject); Process_AdjectiveList(nAdjectives);
      end;
    wsQualifyingFormula: with QualifyingFormulaPtr(aFrm)↑ do
      begin Process_Term(nSubject); Process_Type(nType);
      end;
    wsExistentialFormula, wsUniversalFormula: with QuantifiedFormulaPtr(aFrm)↑ do
      begin inc(nStackCnt);
      if nStackCnt > length(nStackArr) then setlength(nStackArr, 2 * length(nStackArr));
      nStackArr[nStackCnt] ← CreateExpressionsVariableLevel;
      Process_StartQuantifiedFormula(QuantifiedFormulaPtr(aFrm));
      Process_QuantifiedFormula(QuantifiedFormulaPtr(aFrm));
      Process_FinishQuantifiedFormula(QuantifiedFormulaPtr(aFrm));
      dispose(nStackArr[nStackCnt], Done); dec(nStackCnt);
      end;
    wsContradiction: ;
    wsThesis: ;
    wsErrorFormula: ;
  endcases;
end;

```

993. There are a few empty “abstract virtual” methods.

⟨ Within expression AST implementation 978 ⟩ +≡

```
procedure WithinExprObj.ProcessSimpleTerm(var aTrm : SimpleTermPtr);
  begin end;
```

```
procedure WithinExprObj.ProcessStartFraenkelTerm(aTrm : SimpleFraenkelTermPtr);
  begin end;
```

```
procedure WithinExprObj.ProcessFinishFraenkelTerm(var aTrm : SimpleFraenkelTermPtr);
  begin end;
```

994. ⟨ Within expression AST implementation 978 ⟩ +≡

```
procedure WithinExprObj.ProcessFraenkelTermsScope(var aFrm : FormulaPtr);
  begin ProcessFormula(aFrm);
  end;
```

995. ⟨ Within expression AST implementation 978 ⟩ +≡

```
procedure WithinExprObj.ProcessSimpleFraenkelTerm(var aTrm : SimpleFraenkelTermPtr);
  var i : integer;
  begin with aTrm↑ do
    begin for i ← 0 to nPostqualification↑.Count − 1 do
      ProcessVariablesSegment(QualifiedSegmentPtr(nPostqualification↑.Items↑[i]));
      ProcessTerm(nSample);
    end;
  end;
```

996. \langle Within expression AST implementation 978 $\rangle + \equiv$

```

procedure WithinExprObj.Process_Term(var aTrm : TermPtr);
  begin case aTrm↑.nTermSort of
    wsPlaceholderTerm : ; { PlaceholderTermPtr(aTrm)↑.nLocusNr }
    wsSimpleTerm : Process_SimpleTerm(SimpleTermPtr(aTrm));
    wsNumeralTerm : ; { NumeralTermPtr(aTrm)↑.nValue }
    wsInfixTerm : with InfixTermPtr(aTrm)↑ do
      begin Process_TermList(nLeftArgs); { nFunctorSymbol }
      Process_TermList(nRightArgs);
      end;
    wsCircumfixTerm : with CircumfixTermPtr(aTrm)↑ do
      begin { nLeftBracketSymbol }
      Process_TermList(nArgs); { nRightBracketSymbol }
      end;
    wsPrivateFunctorTerm : with PrivateFunctorTermPtr(aTrm)↑ do
      begin { nFunctorIdent }
      Process_TermList(nArgs);
      end;
    wsAggregateTerm : with AggregateTermPtr(aTrm)↑ do
      begin { nStructSymbol }
      Process_TermList(nArgs);
      end;
    wsSelectorTerm : with SelectorTermPtr(aTrm)↑ do
      begin { nSelectorSymbol }
      Process_Term(nArg);
      end;
    wsInternalSelectorTerm : ; { InternalSelectorTermPtr(aTrm)↑.nSelectorSymbol }
    wsForgetfulFunctorTerm : with ForgetfulFunctorTermPtr(aTrm)↑ do
      begin { nStructSymbol }
      Process_Term(nArg);
      end;
    wsInternalForgetfulFunctorTerm : ; { InternalForgetfulFunctorTermPtr(aTrm)↑.nStructSymbol }
    wsSimpleFraenkelTerm, wsFraenkelTerm : with FraenkelTermPtr(aTrm)↑ do
      begin inc(nStackCnt);
      if nStackCnt > length(nStackArr) then setlength(nStackArr, 2 * length(nStackArr));
      nStackArr[nStackCnt] ← CreateExpressionsVariableLevel;
      Process_StartFraenkelTerm(SimpleFraenkelTermPtr(aTrm));
      Process_SimpleFraenkelTerm(SimpleFraenkelTermPtr(aTrm));
      if aTrm↑.nTermSort = wsFraenkelTerm then
        Process_FraenkelTermsScope(FraenkelTermPtr(aTrm)↑.nFormula);
        Process_FinishFraenkelTerm(SimpleFraenkelTermPtr(aTrm));
        dispose(nStackArr[nStackCnt], Done); dec(nStackCnt);
      end;
    wsQualificationTerm : with QualifiedTermPtr(aTrm)↑ do
      begin Process_Term(nSubject); Process_Type(nQualification);
      end;
    wsExactlyTerm : Process_Term(ExactlyTermPtr(aTrm)↑.nSubject);
    wsGlobalChoiceTerm : Process_Type(ChoiceTermPtr(aTrm)↑.nChoiceType);
    wsItTerm : ;
    wsErrorTerm : ;
  endcases;
end;

```

File 21

Weakly strict Mizar article

997. The parser “eats in” a mizar article, then produces a `.wsx` (weakly strict Mizar) XML file containing the abstract syntax tree, and also a `.fmt` article containing the formats for the article.

This strategy should be familiar to anyone who has looked into compilers and interpreters: transform the abstract syntax tree into an intermediate representation, then transform the intermediate representations in various passes.

This module will transform the parse tree to an abstract syntax tree in XML format.

```

<wsmarticle.pas 997> ≡
  <GNU License 4>
unit wsmarticle;
interface
  uses mobjects, errhan, mscanner, syntax, abstract_syntax, xml_dict, xml_inout;
  <Publicly declared types in wsmarticle.pas 999>
const
  <Publicly declared constants in wsmarticle.pas 1002>
  <Publicly declared functions in wsmarticle.pas 1000>
  <Global variables publicly declared in wsmarticle.pas 1154>
implementation
  uses mizenv, mconsole, librenv, scanner, xml_parser
    mdebug, info end_mdebug;
  <Implementation for wsmarticle.pas 1001>
end .

```

998. Exercise. We will create a class hierarchy for the abstract syntax trees for Mizar. A lot of this is boiler-plate. The reader is invited to write a couple of programs which will:

- (1) read in an EBNF-like grammar and emit the class hierarchy for its abstract syntax tree.
- (2) read in an EBNF-like grammar, and emit the class hierarchy for generating the XML for it.

After all, if you look at the sheer number of sections in this file, it’s staggeringly huge. But a lot of it is boiler-plate.

999. <Publicly declared types in *wsmarticle.pas* 999> ≡

See also sections 1003, 1009, 1011, 1014, 1015, 1017, 1018, 1022, 1024, 1026, 1028, 1031, 1033, 1035, 1037, 1040, 1042, 1044, 1047, 1053, 1056, 1058, 1060, 1062, 1063, 1071, 1073, 1075, 1077, 1093, 1095, 1097, 1099, 1101, 1103, 1105, 1107, 1109, 1111, 1113, 1115, 1117, 1119, 1121, 1123, 1125, 1127, 1129, 1131, 1134, 1136, 1138, 1140, 1142, 1144, 1146, 1148, 1150, 1161, 1244, and 1295.

This code is used in section 997.

1000. <Publicly declared functions in *wsmarticle.pas* 1000> ≡

This code is used in section 997.

1001. \langle Implementation for `wsmarticle.pas 1001` $\rangle \equiv$

See also sections [1004](#), [1005](#), [1008](#), [1010](#), [1012](#), [1016](#), [1019](#), [1023](#), [1025](#), [1027](#), [1029](#), [1032](#), [1034](#), [1036](#), [1038](#), [1041](#), [1043](#), [1045](#), [1048](#), [1054](#), [1057](#), [1059](#), [1061](#), [1064](#), [1065](#), [1072](#), [1074](#), [1076](#), [1078](#), [1081](#), [1083](#), [1085](#), [1087](#), [1089](#), [1094](#), [1096](#), [1098](#), [1100](#), [1102](#), [1104](#), [1106](#), [1108](#), [1110](#), [1112](#), [1114](#), [1116](#), [1118](#), [1120](#), [1122](#), [1124](#), [1126](#), [1128](#), [1130](#), [1132](#), [1135](#), [1137](#), [1139](#), [1141](#), [1143](#), [1145](#), [1147](#), [1149](#), [1151](#), [1152](#), [1153](#), [1155](#), [1160](#), [1162](#), [1163](#), [1164](#), [1165](#), [1166](#), [1167](#), [1168](#), [1169](#), [1170](#), [1171](#), [1172](#), [1173](#), [1174](#), [1189](#), [1190](#), [1191](#), [1192](#), [1205](#), [1206](#), [1207](#), [1208](#), [1214](#), [1215](#), [1216](#), [1217](#), [1218](#), [1219](#), [1220](#), [1221](#), [1222](#), [1223](#), [1224](#), [1225](#), [1226](#), [1227](#), [1242](#), [1245](#), [1246](#), [1247](#), [1248](#), [1249](#), [1250](#), [1251](#), [1252](#), [1253](#), [1254](#), [1255](#), [1256](#), [1257](#), [1258](#), [1259](#), [1260](#), [1261](#), [1262](#), [1265](#), [1266](#), [1267](#), [1268](#), [1269](#), [1270](#), [1271](#), [1272](#), [1273](#), [1274](#), [1275](#), [1276](#), [1277](#), [1278](#), [1279](#), [1280](#), [1281](#), [1282](#), [1283](#), [1284](#), [1285](#), [1286](#), [1287](#), [1288](#), [1289](#), [1290](#), [1291](#), [1292](#), [1293](#), [1294](#), [1296](#), [1297](#), [1298](#), [1299](#), [1300](#), [1301](#), [1302](#), [1303](#), [1304](#), [1305](#), [1306](#), [1307](#), [1308](#), [1309](#), [1310](#), [1311](#), [1312](#), [1313](#), [1314](#), [1315](#), [1316](#), [1317](#), [1318](#), [1319](#), [1320](#), [1321](#), [1322](#), [1323](#), [1324](#), [1325](#), [1326](#), [1327](#), [1328](#), [1329](#), [1330](#), [1331](#), [1332](#), [1333](#), [1334](#), [1335](#), [1336](#), [1337](#), [1338](#), and [1339](#).

This code is used in section [997](#).

Section 21.1. WEAKLY STRICT TEXT PROPER

1002. Mizar provides a grammar for its syntax in the file
It uses a variant of EBNF:

/usr/local/doc/mizar/synta

- Terminal symbols are written "in quotes"
- Production rules are separated by vertical lines "|"
- Optional symbols are placed in [brackets]
- Repeated items zero or more times are placed in {braces}.
- Rules end in a period "."

We will freely quote from `syntax.txt`, rearranging the rules as needed to discuss the relevant parts of Mizar's grammar. We will write the `syntax.txt` passages in typewriter font.

We should recall the syntax for text items:

```
Text-Propor = Section { Section } .
Section = "begin" { Text-Item } .
Text-Item = Reservation
| Definitional-Item
| Registration-Item
| Notation-Item
| Theorem
| Scheme-Item
| Auxiliary-Item .
Definitional-Item = Definitional-Block ";" .
Registration-Item = Registration-Block ";" .
Theorem = "theorem" Compact-Statement .
Compact-Statement = Proposition Justification ";" .
Justification = Simple-Justification | Proof .
Auxiliary-Item = Statement | Private-Definition .
```

These are the different syntactic classes for "top-level statements" in the text (not the environment header) of a Mizar article. The interested reader can investigate the `syntax.txt` file more fully to get all the block statements in Mizar. We have already made these different kinds of blocks syntactic values of *BlockKind* earlier (§819). Now we want to be able to translate them into English. We will just skip ahead and make these different syntactic classes into values of an enumerated type.

(Publicly declared constants in `wsmarticle.pas` 1002) \equiv

```
BlockName: array [BlockKind] of string =
  ( `Text-Propor`, { blMain }
  `Now-Reasoning`, { blDiffuse }
  `Hereby-Reasoning`, { blHereby }
  `Proof`, { blProof }
  `Definitional-Block`, { blDefinition }
  `Notation-Block`, { blNotation }
  `Registration-Block`, { blRegistration }
  `Case`, { blCase }
  `Suppose`, { blSuppose }
  `Scheme-Block` { blPublicScheme } );
```

This code is used in section 997.

1003. Class hierarchy for blocks. We can now translate the grammar for blocks into a class hierarchy. The “text proper” extends an abstract “block” statement. We will provide factory methods “*wsTextProper.NewBlock*” and “*NewItem*” for adding a new block (and item) contained within the caller “block”. We will be tracking the “kind” of block (§819), and the text proper will need to track which article it belongs to.

All the various kinds of blocks are handled with this one class: proofs, definitions, notations, registrations, cases, suppose blocks, schemes, hereby statements, and so on. However, some of these blocks have extra content which needs their own nodes in the abstract syntax tree, especially Definitions (§§1090 *et seq.*) and Registrations (§§1133 *et seq.*).

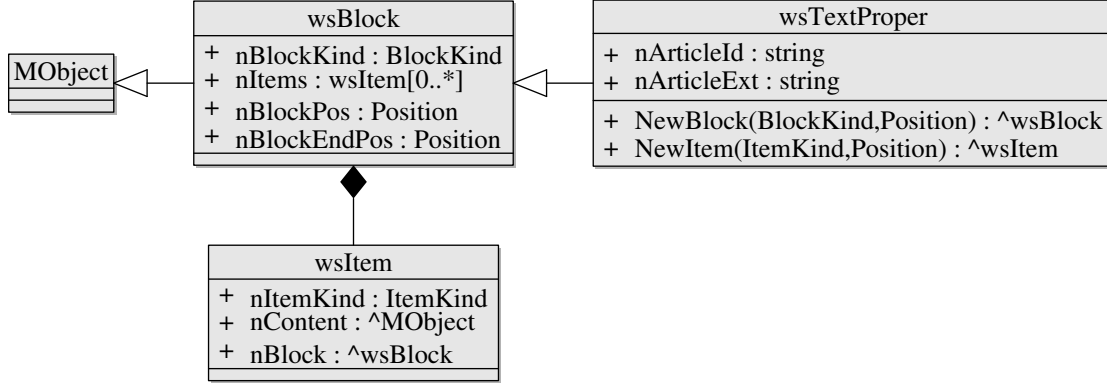


Fig. 4. UML class diagram for *wsBlock* and related classes.

It is important to stress: **wsBlock instances represent all statements which are block statements and all other statements are wsItem instances.** Looking back at the different kinds of blocks, you see that they are “block openers” and will expect to have a matching “end” statement closing it.

```

⟨ Publicly declared types in wsmarticle.pas 999 ⟩ +≡
  wsBlockPtr = ↑wsBlock;
  wsBlock = object (MObject)
    nBlockKind: BlockKind;
    nItems: PList; { list of wsItem objects }
    nBlockPos, nBlockEndPos: Position;
    constructor Init(aBlockKind : BlockKind ; const aPos: Position);
    destructor Done; virtual;
  end ;

⟨ Weakly strict Item class 1007 ⟩;
  wsTextProperPtr = ↑wsTextProper;
  wsTextProper = object (wsBlock)
    nArticleID, nArticleExt: string;
    constructor Init(const aArticleID, aArticleExt: string ; const aPos: Position);
    destructor Done; virtual;
    function NewBlock(aBlockKind : BlockKind ; const aPos: Position): wsBlockPtr;
    function NewItem(aItemKind : ItemKind ; const aPos: Position): wsItemPtr;
  end ;
  
```

1004. Constructor. We initialize using the inherited *wsBlock* constructor (§1006). The “text proper” refers to a block which is as top-level as possible, so we construct it as a block whose kind is *blMain* located at *aPos*.

```

⟨Implementation for wsmarticle.pas 1001⟩ +≡
constructor wsTextProper.Init(const aArticleID, aArticleExt: string; const aPos: Position);
  begin inherited Init(blMain, aPos); nArticleID ← aArticleID; nArticleExt ← aArticleExt;
  end;
destructor wsTextProper.Done;
  begin inherited Done;
  end;

```

1005. Adding statements into a block. we will add a block to a “text proper”, which will then construct a block which tracks the caller as its containing block. This requires giving the kind of the newly minted block (§819).

Similarly, when constructing an item which is contained in the block, we need to pass along the item kind (§829).

```

⟨Implementation for wsmarticle.pas 1001⟩ +≡
function wsTextProper.NewBlock(aBlockKind : BlockKind ; const aPos: Position): wsBlockPtr;
  begin result ← new(WSBlockPtr, Init(aBlockKind, CurPos));
  end;
function wsTextProper.NewItem(aItemKind : ItemKind ; const aPos: Position): wsItemPtr;
  begin result ← new(wsItemPtr, Init(aItemKind, CurPos));
  end;

```

1006. Block Constructor. Curiously, the *MObject* constructor (§312) is not invoked when constructing a *wsBlock*. We will also need the position (§127) of the block in the article. The collection of items in the block is initialized to be empty.

```

constructor wsBlock.Init(aBlokKind : BlockKind ; const aPos: Position);
  begin nBlockKind ← aBlokKind; nBlockPos ← aPos; nBlockEndPos ← aPos;
  nItems ← New(PList, Init(0));
  end;
destructor wsBlock.Done;
  begin dispose(nItems, Done); inherited Done;
  end;

```

1007. Text items. An item requires its “kind” (§829) for its syntactic class.

```

⟨Weakly strict Item class 1007⟩ ≡
  wsItemPtr = ↑wsItem;
  wsItem = object (MObject)
    nItemKind: ItemKind;
    nItemPos, nItemEndPos: Position;
    nContent: PObject;
    nBlock: wsBlockPtr;
    constructor Init(aItemKind : ItemKind ; const aPos: Position);
    destructor Done; virtual;
  end ;

```

This code is used in section 1003.

1008. Constructor

⟨Implementation for `wsmarticle.pas 1001`⟩ +≡
constructor *wsItem.Init*(*aItemKind* : *ItemKind* ; **const** *aPos*: *Position*);
 begin *nItemKind* ← *aItemKind*; *nItemPos* ← *aPos*; *nItemEndPos* ← *aPos*; *nContent* ← **nil**;
 nBlock ← **nil**;
 end;
destructor *wsItem.Done*;
 begin **if** *nBlock* ≠ **nil** **then** *dispose*(*nBlock*, *Done*);
 inherited Done;
 end;

1009. Pragmas. Mizar supports pragmas (analogous to conditional compilation).

⟨Publicly declared types in `wsmarticle.pas 999`⟩ +≡
PragmaPtr = ↑*PragmaObj*;
PragmaObj = **object** (*MObject*)
 nPragmaStr: *string*;
 constructor *Init*(*aStr* : *string*);
 end ;

1010. Constructor.

⟨Implementation for `wsmarticle.pas 1001`⟩ +≡
constructor *PragmaObj.Init*(*aStr* : *string*);
 begin *nPragmaStr* ← *aStr*;
 end;

1011. Labels and propositions. A proposition is just a sentence with a label. We will need to represent both of these in our abstract syntax tree.

⟨Publicly declared types in `wsmarticle.pas 999`⟩ +≡
LabelPtr = ↑*LabelObj*;
LabelObj = **object** (*MObject*)
 nLabelIdNr: *integer*;
 nLabelPos: *Position*;
 constructor *Init*(*aLabelId* : *integer* ; **const** *aPos*: *Position*);
 end ;
PropositionPtr = ↑*PropositionObj*;
PropositionObj = **object** (*mObject*)
 nLab: *LabelPtr*;
 nSntPos: *Position*;
 nSentence: *FormulaPtr*;
 constructor *Init*(*aLab* : *LabelPtr*; *aSentence* : *FormulaPtr* ; **const** *aSntPos*: *Position*);
 destructor *Done*; *virtual*;
 end ;

1012. Constructor.

```

⟨Implementation for wsmarticle.pas 1001⟩ +≡
constructor LabelObj.Init(aLabelId : integer ; const aPos: Position);
  begin nLabelIdNr ← aLabelId; nLabelPos ← aPos;
  end;
constructor PropositionObj.Init(alab : LabelPtr; aSentence : FormulaPtr ; const aSntPos: Position);
  begin nLab ← aLab; nSntPos ← aSntPos; nSentence ← aSentence;
  end;
destructor PropositionObj.Done;
  begin dispose(nLab, Done); dispose(nSentence, Done);
  end;

```

1013. References. References are either local (i.e., from the file being processed) or library (i.e., from the Mizar math library). The grammar for library references is rather generous. The basic rules are that we have theorem references,

$$\langle \text{article} \rangle \text{ ":" } \langle \text{number} \rangle$$

and definition references,

$$\langle \text{article} \rangle \text{ ":"def " } \langle \text{number} \rangle$$

and scheme references,

$$\langle \text{article} \rangle \text{ ":"sch " } \langle \text{number} \rangle$$

What makes it tricky is we also allow multiple references from the same article to just add a comma followed by the theorem number

$$\langle \text{article} \rangle \text{ ":" } \langle \text{number} \rangle \{ \text{ "," } \langle \text{number} \rangle \}$$

or a comma followed by definition numbers

$$\langle \text{article} \rangle \text{ ":"def " } \langle \text{number} \rangle \{ \text{ "," "def " } \langle \text{number} \rangle \}$$

So far, so good, right? Now we can go even further, mixing theorem references and definitions references from the same article.

We recall the grammar for references:

```

⟨Reference⟩ ::= ⟨Local-Reference⟩ | ⟨Library-Reference⟩.
⟨Scheme-Reference⟩ ::= ⟨Local-Scheme-Reference⟩ | ⟨Library-Scheme-Reference⟩.
⟨Local-Reference⟩ ::= ⟨Label-Identifier⟩.
⟨Local-Scheme-Reference⟩ ::= ⟨Scheme-Identifier⟩.
⟨Library-Reference⟩ ::= ⟨Article-Name⟩ ":" (⟨Theorem-Number⟩ | "def" ⟨Definition-Number⟩)
  { \text{ "," } (⟨Theorem-Number⟩ | "def" ⟨Definition-Number⟩) } .
⟨Library-Scheme-Reference⟩ ::= ⟨Article-Name⟩ ":" "sch" ⟨Scheme-Number⟩.

```

1014. Class structure. We have an abstract “reference” class, which is either a local reference (to a label within the article) or a library reference (to some result in the MML).

```

⟨Publicly declared types in wsmarticle.pas 999⟩ +≡
ReferenceKind = (LocalReference, TheoremReference, DefinitionReference);
⟨Inference kinds (wsmarticle.pas) 1021⟩;
ReferencePtr = ↑ReferenceObj;
ReferenceObj = object (MObject)
  nRefSort: ReferenceKind;
  nRefPos: Position;
end;

```

1015. Local references.

```

⟨ Publicly declared types in wsmarticle.pas 999 ⟩ +≡
  LocalReferencePtr = ↑LocalReferenceObj;
  LocalReferenceObj = object (ReferenceObj)
    nLabId: integer;
    constructor Init(aLabId : integer ; const aPos: Position);
end ;

```

1016. Constructor. The reference constructors simply populate the appropriate fields in the reference, and the position in the article's text.

```

⟨ Implementation for wsmarticle.pas 1001 ⟩ +≡
constructor LocalReferenceObj.Init(aLabId : integer;
  const aPos: Position);
begin nRefSort ← LocalReference; nLabId ← aLabId; nRefPos ← aPos
end;

```

1017. Library references. This is the abstract class representing either theorem or definition references from an article.

```

⟨ Publicly declared types in wsmarticle.pas 999 ⟩ +≡
  LibraryReferencePtr = ↑LibraryReferenceObj;
  LibraryReferenceObj = object (ReferenceObj)
    nArticleNr: integer;
end;

```

1018. Theorem and definition references. I am of a divided mind here. On the one hand, we can see that a *LibraryReference* is a tagged union already, and we do not need separate subclasses for theorem references and definition references. On the other hand, separate subclasses makes things easier when emitting XML for the abstract syntax tree for a Mizar article. Since it is more clear with separate subclasses, and it is better to be clear than clever, I think this design is wiser than the alternatives.

```

⟨ Publicly declared types in wsmarticle.pas 999 ⟩ +≡
  TheoremReferencePtr = ↑TheoremReferenceObj;
  TheoremReferenceObj = object (LibraryReferenceObj)
    nTheoNr: integer;
    constructor Init(aArticleNr, aTheoNr : integer ; const aPos: Position);
end ;

  DefinitionReferencePtr = ↑DefinitionReferenceObj;
  DefinitionReferenceObj = object (LibraryReferenceObj)
    nDefNr: integer;
    constructor Init(aArticleNr, aDefNr : integer ; const aPos: Position);
end ;

```

1019. Constructor. The reference constructors simply populate the appropriate fields in the reference, and the position in the article's text.

```

⟨Implementation for wsmarticle.pas 1001⟩ +≡
constructor TheoremReferenceObj.Init(aArticleNr, aTheoNr : integer;
  const aPos: Position);
  begin nRefSort ← TheoremReference; nArticleNr ← aArticleNr; nTheoNr ← aTheoNr;
  nRefPos ← aPos
  end;
constructor DefinitionReferenceObj.Init(aArticleNr, aDefNr : integer;
  const aPos: Position);
  begin nRefSort ← DefinitionReference; nArticleNr ← aArticleNr; nDefNr ← aDefNr;
  nRefPos ← aPos
  end;

```

1020. Justifications. The grammar for justifications looks like:

```

Justification = Simple-Justification
  | Proof .
Simple-Justification = Straightforward-Justification
  | Scheme-Justification .
Proof = "proof" Reasoning "end" .
Straightforward-Justification = [ "by" References ] .
Scheme-Justification = "from" Scheme-Reference [ "(" References ")" ] .

```

Proof blocks are already represented as a *Block* object. We just need to represent the other kinds of justifications as nodes in the abstract syntax tree.

1021. The different kinds of inference, since a *Justification* is a tagged union of sorts.

```

⟨Inference kinds (wsmarticle.pas) 1021⟩ ≡
  InferenceKind = (infError, infStraightforwardJustification, infSchemeJustification, infProof,
    infSkippedProof)
This code is used in section 1014.

```

1022. Class structure for justifications. The class hierarchy for justifications reflects the grammar we just discussed.

```

⟨Publicly declared types in wsmarticle.pas 999⟩ +≡
  JustificationPtr = ↑JustificationObj;
  JustificationObj = object (MObject)
    nInfSort: InferenceKind;
    nInfPos: Position;
    constructor Init(aInferSort : InferenceKind ; const aPos: Position);
  end ;

```

1023. Constructor.

```

⟨Implementation for wsmarticle.pas 1001⟩ +≡
constructor JustificationObj.Init(aInferSort : InferenceKind ; const aPos: Position);
  begin nInfSort ← aInferSort; nInfPos ← aPos;
  end;

```

1024. Simple justifications. These are either “by” a list of references, or “from” a scheme.

```
(Publicly declared types in wsmarticle.pas 999) +≡
  SimpleJustificationPtr = ↑SimpleJustificationObj;
  SimpleJustificationObj = object (JustificationObj)
    nReferences: PList;
    constructor Init(aInferSort : InferenceKind ; const aPos: Position);
    destructor Done; virtual;
  end ;
```

1025. Constructor.

```
(Implementation for wsmarticle.pas 1001) +≡
constructor SimpleJustificationObj.Init(aInferSort : InferenceKind ; const aPos: Position);
  begin inherited Init(aInferSort, aPos); nReferences ← new(PList, Init(0));
  end;
destructor SimpleJustificationObj.Done;
  begin dispose(nReferences, Done); inherited Done;
  end;
```

1026. Straightforward justification.

```
(Publicly declared types in wsmarticle.pas 999) +≡
  StraightforwardJustificationPtr = ↑StraightforwardJustificationObj;
  StraightforwardJustificationObj = object (SimpleJustificationObj)
    nLinked: boolean;
    nLinkPos: Position;
    constructor Init(const aPos: Position; aLinked: boolean; const aLinkPos: Position);
    destructor Done; virtual;
  end ;
```

1027. Constructor.

```
(Implementation for wsmarticle.pas 1001) +≡
constructor StraightforwardJustificationObj.Init(const aPos: Position;
  aLinked: boolean;
  const aLinkPos: Position);
  begin inherited Init(infStraightforwardJustification, aPos); nLinked ← aLinked; nLinkPos ← aLinkPos;
  end;
destructor StraightforwardJustificationObj.Done;
  begin inherited Done;
  end;
```

1028. Scheme justification.

```
(Publicly declared types in wsmarticle.pas 999) +≡
  SchemeJustificationPtr = ↑SchemeJustificationObj;
  SchemeJustificationObj = object (SimpleJustificationObj)
    nSchFileNr: integer; { 0 for schemes from current article and positive for library references }
    nSchemeIdNr: integer; { a number of a scheme for library reference nSchFileNr > 0 or a number of
      an identifier name for scheme name from current article }
    nSchemeInfPos: Position;
    constructor Init(const aPos: Position; aArticleNr, aNr: integer);
    destructor Done; virtual;
  end ;
```

1029. Constructor.

⟨Implementation for `wsmarticle.pas` 1001⟩ +≡

```

constructor SchemeJustificationObj.Init(const aPos: Position; aArticleNr, aNr: integer);
  begin inherited Init(infSchemeJustification, aPos); nSchFileNr ← aArticleNr; nSchemeIdNr ← aNr;
    nSchemeInfPos ← aPos;
  end;

destructor SchemeJustificationObj.Done;
  begin inherited Done;
  end;

```


Section 21.2. SCHEMES

1030. The grammar for schemes looks like:

```

Scheme-Item = Scheme-Block ";" .
Scheme-Block = "scheme" Scheme-Identifier "{" Scheme-Parameters "}" ":"
  Scheme-Conclusion ["provided" Scheme-Premise {"and" Scheme-Premise}]
  ("proof" | ";") Reasoning "end" .
Scheme-Identifier = Identifier .
Scheme-Parameters = Scheme-Segment "," Scheme-Segment .
Scheme-Conclusion = Sentence .
Scheme-Premise = Proposition .
Scheme-Segment = Predicate-Segment | Functor-Segment .
Predicate-Segment =
  Predicate-Identifier {""," Predicate-Identifier} "[" [Type-Expression-List] "]" .
Predicate-Identifier = Identifier .
Functor-Segment =
  Functor-Identifier {""," Functor-Identifier} "(" [Type-Expression-List] ")" Specification .
Functor-Identifier = Identifier .

```

We begin with the abstract syntax for scheme parameters.

1031. Class hierarchy for schemes. We need “predicate segments” and “functor segments” for the second-order variable parameters to the scheme.

```

⟨ Publicly declared types in wsmarticle.pas 999 ⟩ +≡
  SchemeSegmentKind = (PredicateSegment, FunctorSegment);
  SchemeSegmentPtr = ↑SchemeSegmentObj;
  SchemeSegmentObj = object (MObject)
    nSegmPos: Position;
    nSegmSort: SchemeSegmentKind;
    nVars: PList;
    nTypeExpList: PList;
    constructor Init(const aPos: Position; aSegmSort: SchemeSegmentKind;
      aVars, aTypeExpList: PList);
    destructor Done; virtual;
  end ;

```

1032. Constructor.

```

⟨ Implementation for wsmarticle.pas 1001 ⟩ +≡
constructor SchemeSegmentObj.Init(const aPos: Position;
  aSegmSort: SchemeSegmentKind;
  aVars, aTypeExpList: PList);
begin nSegmPos ← aPos; nSegmSort ← aSegmSort; nVars ← aVars; nTypeExpList ← aTypeExpList;
end;
destructor SchemeSegmentObj.Done;
begin dispose(nVars, Done); dispose(nTypeExpList, Done);
end;

```

1033. Segment variables for schemes. We need “predicate segments” and “functor segments” for the second-order variable parameters to the scheme.

```

⟨ Publicly declared types in wsmarticle.pas 999 ⟩ +≡
  PredicateSegmentPtr = SchemeSegmentPtr;
  FunctorSegmentPtr = ↑FunctorSegmentObj;
  FunctorSegmentObj = object (SchemeSegmentObj)
    nSpecification: TypePtr;
    constructor Init(const aPos: Position; aVars, aTypeExpList: PList; aSpecification: TypePtr);
    destructor Done; virtual;
  end ;

```

1034. Constructor.

```

⟨ Implementation for wsmarticle.pas 1001 ⟩ +≡
constructor FunctorSegmentObj.Init(const aPos: Position;
                                   aVars, aTypeExpList: PList;
                                   aSpecification: TypePtr);
  begin inherited Init(aPos, FunctorSegment, aVars, aTypeExpList); nSpecification ← aSpecification;
  end;
destructor FunctorSegmentObj.Done;
  begin dispose(nSpecification, Done); inherited Done;
  end;

```

1035. Scheme. A *Scheme* object is the parent class of *MSScheme* objects in *first_identification.pas*. But it does not appear to be used anywhere else. This has no place in the abstract syntax tree, for example.

```

⟨ Publicly declared types in wsmarticle.pas 999 ⟩ +≡
  SchemePtr = ↑SchemeObj;
  SchemeObj = object (MObject)
    nSchemeIdNr: integer;
    nSchemePos: Position;
    nSchemeParams: PList;
    nSchemeConclusion: FormulaPtr;
    nSchemePremises: PList;
    constructor Init(aIdNr: integer ; const aPos: Position; aParams: PList; aPrems: PList;
                    aConcl: FormulaPtr);
    destructor Done; virtual;
  end ;

```

1036. Constructor.

⟨Implementation for `wsmarticle.pas` 1001⟩ +≡

```
constructor SchemeObj.Init(aIdNr : integer;
                           const aPos: Position;
                           aParams: PList;
                           aPremis: PList;
                           aConcl: FormulaPtr);
  begin nSchemeIdNr ← aIdNr; nSchemePos ← aPos; nSchemeParams ← aParams;
        nSchemeConclusion ← aConcl; nSchemePremises ← aPremis;
  end;

destructor SchemeObj.Done;
  begin dispose(nSchemeParams, Done); dispose(nSchemeConclusion, Done);
        dispose(nSchemePremises, Done);
  end;
```

1037. Reservations. We can “reserve” an identifier and its type, so we do not need to quantify over it for each theorem. The grammar for it:

```
Reservation = "reserve" Reservation-Segment { "," Reservation-Segment } ";" .
Reservation-Segment = Reserved-Identifiers "for" Type-Expression .
Reserved-Identifiers = Identifier { "," Identifier } .
```

The data needed for a **reserved** node in the abstract syntax tree amounts to a list of identifiers and a type.

⟨Publicly declared types in `wsmarticle.pas` 999⟩ +≡

```
ReservationSegmentPtr = ↑ReservationSegmentObj;
ReservationSegmentObj = object (MObject)
  nIdentifiers: PList;
  nResType: TypePtr;
  constructor Init(aIdentifiers : PList; aType : TypePtr);
  destructor Done; virtual;
end ;
```

1038. Constructor.

⟨Implementation for `wsmarticle.pas` 1001⟩ +≡

```
constructor ReservationSegmentObj.Init(aIdentifiers : PList; aType : TypePtr);
  begin nIdentifiers ← aIdentifiers; nResType ← aType;
  end;

destructor ReservationSegmentObj.Done;
  begin dispose(nIdentifiers, Done); dispose(nResType, Done);
  end;
```

Section 21.3. PRIVATE DEFINITIONS

1039. The grammar for “private definitions” (which introduces block-local or article-local terms and predicates) looks like:

```

Private-Definition = Constant-Definition
                   | Private-Functor-Definition
                   | Private-Predicate-Definition .
Constant-Definition = "set" Equating-List ";" .
Equating-List = Equating {" ," Equating }.
Equating = Variable-Identifier "=" Term-Expression .
Private-Functor-Definition = "deffunc" Private-Functor-Pattern "=" Term-Expression ";" .
Private-Predicate-Definition = "defpred" Private-Predicate-Pattern "means" Sentence ";" .
Private-Functor-Pattern = Functor-Identifier "(" [ Type-Expression-List ] ")" .
Private-Predicate-Pattern = Predicate-Identifier "[" [Type-Expression-List ] "]" .

```

So we really only need to describe private predicates, private functors, and “constant definitions” (which introduce an abbreviation).

1040. Private functors.

```

⟨ Publicly declared types in wsmarticle.pas 999 ⟩ +≡
  PrivateFunctorDefinitionPtr = ↑PrivateFunctorDefinitionObj;
  PrivateFunctorDefinitionObj = object (MObject)
    nFuncId: VariablePtr;
    nTypeExpList: PList;
    nTermExpr: TermPtr;
    constructor Init(aFuncId : VariablePtr; aTypeExpList : Plist; aTerm : TermPtr);
    destructor Done; virtual;
  end ;

```

1041. Constructor.

```

⟨ Implementation for wsmarticle.pas 1001 ⟩ +≡
constructor PrivateFunctorDefinitionObj.Init(aFuncId : VariablePtr; aTypeExpList : Plist;
  aTerm : TermPtr);
  begin nFuncId ← aFuncId; nTypeExpList ← aTypeExpList; nTermExpr ← aTerm;
  end;
destructor PrivateFunctorDefinitionObj.Done;
  begin dispose(nFuncId, Done); dispose(nTypeExpList, Done); dispose(nTermExpr, Done);
  end;

```

1042. Private predicates.

```

⟨ Publicly declared types in wsmarticle.pas 999 ⟩ +≡
  PrivatePredicateDefinitionPtr = ↑PrivatePredicateDefinitionObj;
  PrivatePredicateDefinitionObj = object (MObject)
    nPredId: VariablePtr;
    nTypeExpList: PList;
    nSentence: FormulaPtr;
    constructor Init(aPredId : VariablePtr; aTypeExpList : Plist; aSnt : FormulaPtr);
    destructor Done; virtual;
  end ;

```

1043. Constructor.

⟨ Implementation for `wsmarticle.pas 1001` ⟩ +≡
constructor *PrivatePredicateDefinitionObj*.Init(*aPredId* : *VariablePtr*; *aTypeExpList* : *Plist*;
aSnt : *FormulaPtr*);
 begin *nPredId* ← *aPredId*; *nTypeExpList* ← *aTypeExpList*; *nSentence* ← *aSnt*;
 end;
destructor *PrivatePredicateDefinitionObj*.Done;
 begin *dispose*(*nPredId*, Done); *dispose*(*nTypeExpList*, Done); *dispose*(*nSentence*, Done);
 end;

1044. Constant definitions. These are little more than abbreviations for terms, and their implementations reflects this: they are pointers with delusions of grandeur.

⟨ Publicly declared types in `wsmarticle.pas 999` ⟩ +≡
ConstantDefinitionPtr = ↑ *ConstantDefinitionObj*;
ConstantDefinitionObj = **object** (*MObject*)
 nVarId: *VariablePtr*;
 nTermExpr: *TermPtr*;
 constructor *Init*(*aVarId* : *VariablePtr*; *aTerm* : *TermPtr*);
 destructor *Done*; *virtual*;
end ;

1045. Constructor.

⟨ Implementation for `wsmarticle.pas 1001` ⟩ +≡
constructor *ConstantDefinitionObj*.Init(*aVarId* : *VariablePtr*; *aTerm* : *TermPtr*);
 begin *nVarId* ← *aVarId*; *nTermExpr* ← *aTerm*;
 end;
destructor *ConstantDefinitionObj*.Done;
 begin *dispose*(*nVarId*, Done); *dispose*(*nTermExpr*, Done);
 end;

Section 21.4. CHANGING TYPES

1046. Each term has a soft type associated with it, but we can “reconsider” or change its type. Mizar requires a proof that the term really has the new type. The grammar for this statement:

```
Type-Changing-Statement =
  "reconsider" Type-Change-List "as" Type-ExpressionSimple-Justification ";" .
Type-Change-List =
  (Equating | Variable-Identifier) {"," (Equating | Variable-Identifier)} .
```

This requires a bit of work since we really have *two* types of reconsiderations within a single reconsider statement:

- (1) “reconsider $\langle identifier \rangle$ as $\langle type \rangle$ ”
- (2) “reconsider $\langle identifier \rangle = \langle term \rangle$ as $\langle type \rangle$ ”

The trick is to represent a **Type-Change-List** as a list of **Type-Changes**. Then a **Type-Change-Statement** is just a **Type-Change-List** and a type.

1047. Class hierarchy.

```
<Publicly declared types in wsmarticle.pas 999> +≡
  TypeChangeSort = (Equating, VariableIdentifier);
  TypeChangePtr = ↑TypeChangeObj;
  TypeChangeObj = object (MObject)
    nTypeChangeKind: TypeChangeSort;
    nVar: VariablePtr;
    nTermExpr: TermPtr;
    constructor Init(aKind : TypeChangeSort; aVar : VariablePtr; aTerm : TermPtr);
    destructor Done; virtual;
  end ;
<Example classes (wsmarticle.pas) 1050>
  TypeChangingStatementPtr = ↑TypeChangingStatementObj;
  TypeChangingStatementObj = object (MObject)
    nTypeChangeList: PList;
    nTypeExpr: TypePtr;
    nJustification: SimpleJustificationPtr;
    constructor Init(aTypeChangeList : PList; aTypeExpr : TypePtr;
      aJustification : SimpleJustificationPtr);
    destructor Done; virtual;
  end ;
```

1048. Constructor.

```

⟨ Implementation for wsmarticle.pas 1001 ⟩ +≡
constructor TypeChangeObj.Init(aKind : TypeChangeSort; aVar : VariablePtr; aTerm : TermPtr);
  begin nTypeChangeKind ← aKind; nVar ← aVar; nTermExpr ← aTerm;
  end;

destructor TypeChangeObj.Done;
  begin dispose(nVar, Done);
  if nTermExpr ≠ nil then dispose(nTermExpr, Done);
  end;

⟨ Constructors for example statements (wsmarticle.pas) 1051 ⟩
constructor TypeChangingStatementObj.Init(aTypeChangeList : PList; aTypeExpr : TypePtr;
  aJustification : SimpleJustificationPtr);
  begin nTypeChangeList ← aTypeChangeList; nTypeExpr ← aTypeExpr;
  nJustification ← aJustification;
  end;

destructor TypeChangingStatementObj.Done;
  begin dispose(nTypeChangeList, Done); dispose(nTypeExpr, Done); dispose(nJustification, Done);
  end;

```

Section 21.5. PROOF STEPS

1049. Most of the proof steps are handled in generic text-item objects. But there are a few which are outside that tagged union. In particular: existential elimination (**consider** $\langle variables \rangle$ **such that** $\langle formula \rangle$), existential introduction (**take** $\langle terms \rangle$), and concluding statements (**thus** $\langle formula \rangle$).

1050. Examples, existential introduction. The proof step “take x ” transforms goals of the form $\exists x. P[x]$ into a new goal $P[x]$. The grammar for examples looks like:

Exemplification = "take" Example {"," Example} ";" .

Example = Term-Expression | Variable-Identifier "=" Term-Expression .

```

<Example classes (wsmarticle.pas) 1050> ≡
  ExamplePtr = ↑ExampleObj;
  ExampleObj = object (MObject)
    nVarId: VariablePtr;
    nTermExpr: TermPtr;
    constructor Init(aVarId : VariablePtr; aTerm : TermPtr);
    destructor Done; virtual;
  end ;

```

This code is used in section 1047.

1051. Constructor.

```

<Constructors for example statements (wsmarticle.pas) 1051> ≡
constructor ExampleObj.Init(aVarId : VariablePtr; aTerm : TermPtr);
  begin nVarId ← aVarId; nTermExpr ← aTerm;
  end;
destructor ExampleObj.Done;
  begin if nVarId ≠ nil then dispose(nVarId, Done);
  if nTermExpr ≠ nil then dispose(nTermExpr, Done);
  end;

```

This code is used in section 1048.

1052. Existential elimination. We continue plugging along with the statements, and existential elimination (or “choice”) statements are the next one.

```

Linkable-Statement = Compact-Statement
  | Choice-Statement
  | Type-Changing-Statement
  | Iterative-Equality .

```

Choice-Statement = "consider" Qualified-Variables "such" ConditionsSimple-Justification ";" .

```

1053. <Publicly declared types in wsmarticle.pas 999> +≡
  ChoiceStatementPtr = ↑ChoiceStatementObj;
  ChoiceStatementObj = object (MObject)
    nQualVars: PList;
    nConditions: PList;
    nJustification: SimpleJustificationPtr;
    constructor Init(aQualVars, aConds : PList; aJustification : SimpleJustificationPtr);
    destructor Done; virtual;
  end ;

```


1054. Constructor.

```

⟨Implementation for wsmarticle.pas 1001⟩ +≡
constructor ChoiceStatementObj.Init(aQualVars, aConds : PList; aJustification : SimpleJustificationPtr);
  begin nQualVars ← aQualVars; nConditions ← aConds; nJustification ← aJustification;
  end;
destructor ChoiceStatementObj.Done;
  begin dispose(nQualVars, Done); dispose(nConditions, Done); dispose(nJustification, Done);
  end;

```

1055. Conclusion statements. We recall the grammar for conclusion statements:

```

Conclusion = ( "thus" | "hence" ) ( Compact-Statement | Iterative-Equality )
           | Diffuse-Conclusion .
Diffuse-Conclusion = "thus" Diffuse-Statement | "hereby" Reasoning "end" ";" .
Iterative-Equality =
[ Label-Identifier ":" ] Term-Expression "=" Term-ExpressionSimple-Justification
                        "." Term-Expression Simple-Justification
                        { "." Term-Expression Simple-Justification } ";" .

```

NOTE: the whitespace in the Iterative-Equality rule is unimportant, but that is how Mizar users often structure them (to align the equals sign).

1056. Abstract base class.

```

⟨Publicly declared types in wsmarticle.pas 999⟩ +≡
RegularStatementKind = (stDiffuseStatement, stCompactStatement, stIterativeEquality);
RegularStatementPtr = ↑RegularStatementObj;
RegularStatementObj = object (MObject)
  nStatementSort: RegularStatementKind;
  nLab: LabelPtr;
  constructor Init(aStatementSort : RegularStatementKind);
  destructor Done; virtual;
end ;

```

1057. Constructor.

```

⟨Implementation for wsmarticle.pas 1001⟩ +≡
constructor RegularStatementObj.Init(aStatementSort : RegularStatementKind);
  begin nStatementSort ← aStatementSort;
  end;
destructor RegularStatementObj.Done;
  begin inherited Done;
  end;

```

1058. Thus statement. The conclusion of a proof (idiomatically “thus thesis”) is always a “thus”, which Mizar calls a “diffuse statement”.

```

⟨Publicly declared types in wsmarticle.pas 999⟩ +≡
DiffuseStatementPtr = ↑DiffuseStatementObj;
DiffuseStatementObj = object (RegularStatementObj)
  constructor Init(aLab : LabelPtr; aStatementSort : RegularStatementKind);
  destructor Done; virtual;
end ;

```

1059. Constructor.

\langle Implementation for `wsmarticle.pas 1001` $\rangle + \equiv$
constructor *DiffuseStatementObj.Init*(*aLab* : *LabelPtr*; *aStatementSort* : *RegularStatementKind*);
 begin *inherited Init*(*stDiffuseStatement*); *nLab* \leftarrow *aLab*; *nStatementSort* \leftarrow *aStatementSort*;
 end;
destructor *DiffuseStatementObj.Done*;
 begin *dispose*(*nLab*, *Done*);
 end;

1060. Compact statements. We recall the syntax for a compact statement is:

Compact-Statement = Proposition Justification ";" .

\langle Publicly declared types in `wsmarticle.pas 999` $\rangle + \equiv$
CompactStatementPtr = \uparrow *CompactStatementObj*;
CompactStatementObj = **object** (*RegularStatementObj*)
 nProp: *PropositionPtr*;
 nJustification: *JustificationPtr*;
 constructor *Init*(*aProp* : *PropositionPtr*; *aJustification* : *JustificationPtr*);
 destructor *Done*; *virtual*;
end ;

1061. Constructor.

\langle Implementation for `wsmarticle.pas 1001` $\rangle + \equiv$
constructor *CompactStatementObj.Init*(*aProp* : *PropositionPtr*; *aJustification* : *JustificationPtr*);
 begin *inherited Init*(*stCompactStatement*); *nProp* \leftarrow *aProp*; *nJustification* \leftarrow *aJustification*;
 end;
destructor *CompactStatementObj.Done*;
 begin if *nJustification* \neq **nil** **then** *dispose*(*nJustification*, *Done*);
 inherited Done;
 end;

1062. Iterative equality. Chain of equations, where we keep transforming the right-hand side until we arrive at the desired outcome.

\langle Publicly declared types in `wsmarticle.pas 999` $\rangle + \equiv$
IterativeStepPtr = \uparrow *IterativeStepObj*;
IterativeStepObj = **object** (*MObject*)
 nIterPos: *Position*;
 nTerm: *TermPtr*;
 nJustification: *SimpleJustificationPtr*;
 constructor *Init*(**const** *aPos*: *Position*; *aTerm*: *TermPtr*; *aJustification*: *JustificationPtr*);
 destructor *Done*; *virtual*;
end ;

1063. \langle Publicly declared types in `wsmarticle.pas 999` $\rangle + \equiv$

IterativeEqualityPtr = \uparrow *IterativeEqualityObj*;
IterativeEqualityObj = **object** (*CompactStatementObj*)
 nIterSteps: *PList*;
 constructor *Init*(*aProp* : *PropositionPtr*; *aJustification* : *JustificationPtr*; *aIters* : *PList*);
 destructor *Done*; *virtual*;
end ;

1064. Constructor.

⟨ Implementation for `wsmarticle.pas` 1001 ⟩ +≡

```
constructor IterativeStepObj.Init(const aPos: Position; aTerm: TermPtr; aJustification:  
    JustificationPtr);  
    begin nIterPos ← aPos; nTerm ← aTerm; nJustification ← SimpleJustificationPtr(aJustification);  
    end;  
destructor IterativeStepObj.Done;  
    begin dispose(nTerm, Done); dispose(nJustification, Done);  
    end;
```

1065. Constructor.

⟨ Implementation for `wsmarticle.pas` 1001 ⟩ +≡

```
constructor IterativeEqualityObj.Init(aProp : PropositionPtr; aJustification : JustificationPtr;  
    aIters : PList);  
    begin inherited Init(aProp, aJustification); nStatementSort ← stIterativeEquality; nIterSteps ← aIters;  
    end;  
destructor IterativeEqualityObj.Done;  
    begin dispose(nIterSteps, Done); inherited Done;  
    end;
```

1066. Remaining proof steps? So where are the other proof steps like `let` or `assume`? Well, these are handled as “generic text items” and use the *TextItem* class (§1007).

Section 21.6. STRUCTURES

1067. Just an aside first on “what is a structure in Mathematics?” Logic textbooks assume an *intuitive* (i.e., not formal) “finitary metatheory” following Hilbert and his famous Programme in the foundations of Mathematics. We will build a “skyscraper” atop this foundation of finitary metatheory. The first thing we do is describe a logic, the first floor in our sky scraper. This “Logic #1” is the metalogic we use to construct an axiomatic set theory, “Set Theory #2”. We use “Set Theory #2” to construct another floor, a “Logic #3”, which then builds another floor “Set Theory #4”, and so on. We can potentially iterate building as many floors as we want, but 4 is sufficient for our purposes.

We **assert** that “Set Theory #2” is the Platonic “mathematical reality”. Then “Logic #3” is the (ambient) logic we use to do Mathematics; it is purely “syntactic”, a language for expressing proofs and definitions. Mizar’s proof steps, formulas, and definitions corresponds to “Logic #3”. With it, we describe an axiomatic “Set Theory #4”, which is Tarski–Grothendieck set theory for Mizar. Sketching this situation out diagrammatically:

Set Theory #4	(Where we work) [syntactic]
Logic #3	“Object logic” (Where we write proofs) [syntactic]
Set Theory #2	“Mathematical Reality” [semantic]
Logic #1	“Metalogic”
Finitary Metatheory	

Fig. 5. Mathematical Platonism as a skyscraper.

Now, “mathematical objects” live in “Set Theory #2”. Model theory studies structures (objects in “Set Theory #2”) of theories (described in “Logic #3”). Since we “believe” that set theory “describes reality”, that means we just need to describe [“syntactic”] theories using “Set Theory #4” and their “real world occurrences” in “Set Theory #2”. (Well, this is a gloss, model theory sets up two additional floors in the skyscraper, and studies “models” of theories described using Logic #5 and Set Theory #6 in Set Theory #4 — and we pretend it describes the relationship between Set Theory #2 and the “syntactic floors” of the Mathematical skyscraper.)

How do we *syntactically* describe these “structures”? Well, we *know* they are not “first-class citizens” in Mizar, in the sense that they are not “just” a tuple. How do we know this? Gilbert Lee and Piotr Rudnicki’s “Alternative Aggregates in Mizar” (in *MKM 2007*, Springer, pp.327–341; [doi:10.1007/978-3-540-73086-6_26](https://doi.org/10.1007/978-3-540-73086-6_26)) discuss how to implement first-class structures in Mizar. This means that *technically* structures live in Logic #3. Field symbols are terms in Logic #3.

1068. Why do we need this convoluted skyscraper? Without it, how do we describe a “true” formula? We can only speak of a *provable* formula. Bourbaki’s *Theory of Sets* (I §2.2) confuses “provable” with “true” formulas (they speak of a formula being “false in a theory \mathcal{T} ” as being synonymous with the formula contradicting the axioms for a theory, and true in a theory as being synonymous for being a logical consequence from the axioms for a theory). This only matters for Mathematical Platonists. Formalists (like the author) would find this discussion muddled and nearly metaphysical, generating more heat than light.

1069. Aside: finitary metatheory, programming languages, implementing proof assistants.

How does that diagram in Figure 5 of the last section compare to the *actual implementation* of Mizar? Well, a proof assistant replaces the “finitary metatheory” with an actual programming language. Then, since only Mathematical Platonists care about the “Metalogic” and “Mathematical reality”, we jump ahead to implement Logic #3 — this is what happens in Mizar and other proof assistants: we implement a “purely formal” (purely syntactic) logic using a programming language. Curiously, this reflects Bourbaki’s approach to the foundations of Mathematics.

We should note that programming languages are strictly stronger than finitary metatheory, since programming languages are *Turing complete*. This means they support general recursion, whereas finitary metatheory supports only primitive recursive functions. For an example of a “programming language” which is equally as strong as a finitary metatheory, see Albert R. Meyer and Dennis M. Ritchie, “The complexity of loop programs” (*ACM ’67 Proc.*, 1967, [doi:10.1145/800196.806014](https://doi.org/10.1145/800196.806014)).

Is Turing completeness “too much” for a finitary metatheory? The short answer is: yes. Even restricting a Turing complete programming language is “too much” to be finitary. Gödel’s System T was developed to preserve the “constructive character” while jettisoning the “finitary character” of Hilbert’s finitary metatheory, and System T is not even Turing complete. See Kurt Gödel’s *Collected Works* (vol. II, Oxford University Press, [doi:10.1093/oso/9780195147216.001.0001](https://doi.org/10.1093/oso/9780195147216.001.0001), 1989; viz., pp. 245–247) for his discussion of System T. The interested reader should consult David A. Turner’s “Elementary strong functional programming” (in *Int. Symp. on Funct. Program. Lang. in Educ.*, eds P.H. Hartel and R. Plasmeijer, Springer, pages 1–13, [doi:10.1007/3-540-60675-0_35](https://doi.org/10.1007/3-540-60675-0_35)) for how to obtain System T by restricting any statically typed functional programming language.

1070. Grammar for structures. We can recall the syntax for structures and fields:

```
Structure-Definition =
  "struct" [ "(" Ancestors ")" ] Structure-Symbol [ "over" Loci ] "(" Fields ")" ";" .
Ancestors = Structure-Type-Expression { "," Structure-Type-Expression } .
Structure-Symbol = Symbol .
Loci = Locus { "," Locus } .
Fields = Field-Segment { "," Field-Segment } .
Locus = Variable-Identifier .
Variable-Identifier = Identifier .
Field-Segment = Selector-Symbol { "," Selector-Symbol } Specification .
Selector-Symbol = Symbol .
```

1071. Field symbol. A “field symbol” refers to the identifier used for a field in a structure, but not its type.

```
< Publicly declared types in wsmarticle.pas 999 > +≡
  FieldSymbolPtr = ↑FieldSymbolObj;
  FieldSymbolObj = object (MObject)
    nFieldPos: Position;
    nFieldSymbol: integer;
    constructor Init(const aPos: Position; aFieldSymbNr: integer);
  end ;
```

1072. Constructor.

```
< Implementation for wsmarticle.pas 1001 > +≡
constructor FieldSymbolObj.Init(const aPos: Position; aFieldSymbNr: integer);
  begin nFieldPos ← aPos; nFieldSymbol ← aFieldSymbNr;
end ;
```

1073. Field segment. A field segment refers to a list of 1 or more field symbols, and the associated type it has.

```

⟨ Publicly declared types in wsmarticle.pas 999 ⟩ +≡
  FieldSegmentPtr = ↑FieldSegmentObj;
  FieldSegmentObj = object (MObject)
    nFieldSegmPos: Position;
    nFields: PList;
    nSpecification: TypePtr;
    constructor Init(const aPos: Position; aFields: PList; aSpec: TypePtr);
    destructor Done; virtual;
  end ;

```

1074. Constructor.

```

⟨ Implementation for wsmarticle.pas 1001 ⟩ +≡
constructor FieldSegmentObj.Init(const aPos: Position; aFields: PList; aSpec: TypePtr);
  begin nFieldSegmPos ← aPos; nFields ← aFields; nSpecification ← aSpec;
  end;
destructor FieldSegmentObj.Done;
  begin dispose(nFields, Done); dispose(nSpecification, Done);
  end;

```

1075. Locus. A “locus” refers to a term or type parametrizing a definition.

```

⟨ Publicly declared types in wsmarticle.pas 999 ⟩ +≡
  LocusPtr = ↑LocusObj;
  LocusObj = object (MObject)
    nVarId: integer;
    nVarIdPos: Position;
    constructor Init(const aPos: Position; aIdentNr: integer);
  end ;

```

1076. Constructor.

```

⟨ Implementation for wsmarticle.pas 1001 ⟩ +≡
constructor LocusObj.Init(const aPos: Position; aIdentNr: integer);
  begin nVarId ← aIdentNr; nVarIdPos ← aPos;
  end;

```

1077. Structure definition. Finally, structures are finite maps from selectors to terms, with structure inheritance thrown into the mix. They may be defined “**over**” a finite list of types (e.g., a module structure is “**over**” a ring). Note that we need to first introduce “patterns” before describing the structure definition, since “patterns” are needed in definitions.

```

⟨ Publicly declared types in wsmarticle.pas 999 ⟩ +≡
  ⟨ Pattern objects (wsmarticle.pas) 1080 ⟩
  StructureDefinitionPtr = ↑StructureDefinitionObj;
  StructureDefinitionObj = object (MObject)
    nStrPos: Position;
    nAncestors: PList;
    nDefStructPattern: ModePatternPtr;
    nSgmFields: PList;
    constructor Init(const aPos: Position; aAncestors: PList; aStructSymb: integer;
      aOverArgs: PList; aFields: PList);
    destructor Done; virtual;
  end ;

```

1078. Constructor.

```

⟨ Implementation for wsmarticle.pas 1001 ⟩ +≡
constructor StructureDefinitionObj.Init(const aPos: Position; aAncestors: PList;
  aStructSymb: integer; aOverArgs: PList; aFields: PList);
  begin nStrPos ← aPos; nAncestors ← aAncestors;
    nDefStructPattern ← new(ModePatternPtr, Init(aPos, aStructSymb, aOverArgs));
    nDefStructPattern.↑.nPatternSort ← itDefStruct; nSgmFields ← aFields;
  end;
destructor StructureDefinitionObj.Done;
  begin dispose(nAncestors, Done); dispose(nDefStructPattern, Done); dispose(nSgmFields, Done);
  end;

```

Section 21.7. PATTERNS

1079. A “*Pattern*” in Mizar is a format with the type information for all the arguments around a term. The notion of a “*Pattern*” also refers to the definiendum of a definition. The syntax of patterns

```
Mode-Pattern = Mode-Symbol [ "of" Loci ] .
Attribute-Pattern = Locus "is" [ Attribute-Loci ] Attribute-Symbol .
Attribute-Loci = Loci | "(" Loci ")" .
Predicate-Pattern = [ Loci ] Predicate-Symbol [ Loci ] .
Functor-Pattern = [ Functor-Loci ] Functor-Symbol [ Functor-Loci ]
  | Left-Functor-Bracket Loci Right-Functor-Bracket .
Functor-Loci = Locus | "(" Loci ")" .
```

1080. Base class for patterns.

```
<Pattern objects (wsmarticle.pas 1080) > ≡
  PatternPtr = ↑PatternObj;
  PatternObj = object (mObject)
    nPatternPos: Position;
    nPatternSort: ItemKind;
    constructor Init(const aPos: Position; aSort: ItemKind);
  end ;
```

See also sections 1082, 1084, 1086, and 1088.

This code is used in section 1077.

```
1081. <Implementation for wsmarticle.pas 1001> +≡
constructor PatternObj.Init(const aPos: Position; aSort: ItemKind);
  begin nPatternPos ← aPos; nPatternSort ← aSort;
end;
```

1082. Mode patterns. The syntax for “mode patterns” looks like:

```
Mode-Pattern = Mode-Symbol [ "of" Loci ] .
<Pattern objects (wsmarticle.pas 1080) +≡
  ModePatternPtr = ↑ModePatternObj;
  ModePatternObj = object (PatternObj)
    nModeSymbol: Integer;
    nArgs: PList;
    constructor Init(const aPos: Position; aSymb: integer; aArgs: PList);
    destructor Done; virtual;
  end ;
```

1083. Constructor.

```
<Implementation for wsmarticle.pas 1001> +≡
constructor ModePatternObj.Init(const aPos: Position; aSymb: integer; aArgs: PList);
  begin inherited Init(aPos, itDefMode); nModeSymbol ← aSymb; nArgs ← aArgs;
end;
destructor ModePatternObj.Done;
  begin dispose(nArgs, Done);
end;
```


1084. Attribute patterns. Attributes can have loci prefixing the attribute symbol, but *not* suffixing the attribute symbol.

```
Attribute-Pattern = Locus "is" [ Attribute-Loci ] Attribute-Symbol .
Attribute-Loci = Loci | "(" Loci ")" .
⟨ Pattern objects (wsmarticle.pas) 1080 ⟩ +≡
  AttributePatternPtr = ↑AttributePatternObj;
  AttributePatternObj = object (PatternObj)
    nAttrSymbol: Integer;
    nArg: LocusPtr;
    nArgs: PList;
    constructor Init(const aPos: Position; aArg: LocusPtr; aSymb: integer; aArgs: PList);
    destructor Done; virtual;
  end ;
```

1085. Constructor.

```
⟨ Implementation for wsmarticle.pas 1001 ⟩ +≡
constructor AttributePatternObj.Init(const aPos: Position; aArg: LocusPtr; aSymb: integer; aArgs:
  PList);
  begin inherited Init(aPos, itDefAttr); nAttrSymbol ← aSymb; nArg ← aArg; nArgs ← aArgs;
  end;
destructor AttributePatternObj.Done;
  begin dispose(nArg, Done); dispose(nArgs, Done);
  end;
```

1086. Predicate patterns. Predicates can have loci on either side of the predicate symbol, without requiring parentheses (unlike functors).

```
Predicate-Pattern = [ Loci ] Predicate-Symbol [ Loci ] .
⟨ Pattern objects (wsmarticle.pas) 1080 ⟩ +≡
  PredicatePatternPtr = ↑PredicatePatternObj;
  PredicatePatternObj = object (PatternObj)
    nPredSymbol: Integer;
    nLeftArgs, nRightArgs: PList;
    constructor Init(const aPos: Position; aLArgs: PList; aSymb: integer; aRArgs: PList);
    destructor Done; virtual;
  end ;
```

1087. Constructor.

```
⟨ Implementation for wsmarticle.pas 1001 ⟩ +≡
constructor PredicatePatternObj.Init(const aPos: Position;
  aLArgs: PList; aSymb: integer; aRArgs: PList);
  begin inherited Init(aPos, itDefPred); nPredSymbol ← aSymb; nLeftArgs ← aLArgs;
  nRightArgs ← aRArgs;
  end;
destructor PredicatePatternObj.Done;
  begin dispose(nLeftArgs, Done); dispose(nRightArgs, Done);
  end;
```

1088. Functor pattern. Functors can have loci on either side. If more than one locus is used on one side, then it must be placed in parentheses and comma-separated. The syntax:

```

Functor-Pattern = [ Functor-Loci ] Functor-Symbol [ Functor-Loci ]
                | Left-Functor-Bracket Loci Right-Functor-Bracket .
Functor-Loci = Locus | "(" Loci ")" .
⟨Pattern objects (wsmarticle.pas 1080) +≡
  FunctorSort = (InfixFunctor, CircumfixFunctor);
  FunctorPatternPtr = ↑FunctorPatternObj;
  FunctorPatternObj = object (PatternObj)
    nFunctKind: FunctorSort;
    constructor Init(const aPos: Position; aKind: FunctorSort);
  end ;
  CircumfixFunctorPatternPtr = ↑CircumfixFunctorPatternObj;
  CircumfixFunctorPatternObj = object (FunctorPatternObj)
    nLeftBracketSymb, nRightBracketSymb: integer;
    nArgs: PList;
    constructor Init(const aPos: Position; aLBSymb, aRBSymb: integer; aArgs: PList);
    destructor Done; virtual;
  end ;
  InfixFunctorPatternPtr = ↑InfixFunctorPatternObj;
  InfixFunctorPatternObj = object (FunctorPatternObj)
    nOperSymb: integer;
    nLeftArgs, nRightArgs: PList;
    constructor Init(const aPos: Position; aLArgs: PList; aSymb: integer; aRArgs: PList);
    destructor Done; virtual;
  end ;

```

1089. Constructor.

```

⟨Implementation for wsmarticle.pas 1001⟩ +≡
constructor FunctorPatternObj.Init(const aPos: Position; aKind: FunctorSort);
  begin inherited Init(aPos, itDefFunc); nFunctKind ← aKind;
  end;
constructor CircumfixFunctorPatternObj.Init(const aPos: Position; aLBSymb, aRBSymb: integer;
  aArgs: PList);
  begin inherited Init(aPos, CircumfixFunctor); nLeftBracketSymb ← aLBSymb;
  nRightBracketSymb ← aRBSymb; nArgs ← aArgs;
  end;
destructor CircumfixFunctorPatternObj.Done;
  begin dispose(nArgs, Done);
  end;
constructor InfixFunctorPatternObj.Init(const aPos: Position; aLArgs: PList; aSymb: integer; aRArgs:
  PList);
  begin inherited Init(aPos, InfixFunctor); nOperSymb ← aSymb; nLeftArgs ← aLArgs;
  nRightArgs ← aRArgs;
  end;
destructor InfixFunctorPatternObj.Done;
  begin dispose(nLeftArgs, Done); dispose(nRightArgs, Done);
  end;

```

Section 21.8. DEFINITIONS

1090. In Mizar, we can redefine an existing definition (either changing the type of a term or “the right hand side” of a definition) *or* we can introduce a new definition. There are 5 different things we can introduce: structures, modes [types], functors [terms], predicates, and attributes. Rather than bombard the reader with a long chunk of grammar, let us divide it up into easy-to-digest pieces. The basic block structure of a definition is the same for all these situations, its grammar looks like:

```

Definitional-Item = Definitional-Block ";" .
Definitional-Block = "definition" { Definition-Item | Definition | Redefinition } "end" .
Definition-Item = Loci-Declaration | Permissive-Assumption | Auxiliary-Item .
Loci-Declaration = "let" Qualified-Variables [ "such" Conditions ] ";" .
Permissive-Assumption = Assumption .
Definition = Structure-Definition
| Mode-Definition
| Functor-Definition
| Predicate-Definition
| Attribute-Definition .

```

1091. Redefinitions. Redefinitions allow us to alter the type or meaning of a definition. This isn't willy-nilly, the user still needs to prove the redefined version is logically equivalent to the initial definition.

```

Redefinition =
  "redefine" ( Mode-Definition | Functor-Definition | Predicate-Definition | Attribute-Definition ) .

```

1092. Structure definitions. Structures intuitively correspond to new “gadgets” (sets equipped with extra structure), which is often presented in Mathematics as “just another tuple”. Mizar allows structures to inherit other structures, so a topological group extends a topological space structure *and* a magma structure (since a group in Mizar is a magma with some extra properties).

```

Structure-Definition =
  "struct" [ "(" Ancestors ")" ] Structure-Symbol [ "over" Loci ] "(#" Fields "#)" ";" .
Ancestors = Structure-Type-Expression { "," Structure-Type-Expression } .
Structure-Symbol = Symbol .
Loci = Locus { "," Locus } .
Fields = Field-Segment { "," Field-Segment } .
Locus = Variable-Identifier .
Variable-Identifier = Identifier .
Field-Segment = Selector-Symbol { "," Selector-Symbol } Specification .
Selector-Symbol = Symbol .
Specification = "->" Type-Expression .

```

1093. Definiens. Recall the grammar for Definiens looks like:

```

Definiens = Simple-Definiens | Conditional-Definiens .
Simple-Definiens = [ ":" Label-Identifier ":" ] ( Sentence | Term-Expression ) .
Label-Identifier = Identifier .
Conditional-Definiens = [ ":" Label-Identifier ":" ] Partial-Definiens-List
  [ "otherwise" ( Sentence | Term-Expression ) ] .
Partial-Definiens-List = Partial-Definiens { "," Partial-Definiens } .
Partial-Definiens = ( Sentence | Term-Expression ) "if" Sentence .

```

We begin with a base class for definiens. This is extended by *SimpleDefiniens* and *ConditionalDefiniens* classes.

```

⟨ Publicly declared types in wsmarticle.pas 999 ⟩ +≡
  HowToDefine = (dfEmpty, dfMeans, dfEquals);
  DefiniensSort = (SimpleDefiniens, ConditionalDefiniens);
  DefiniensPtr = ↑DefiniensObj;
  DefiniensObj = object (MObject)
    nDefSort: DefiniensSort;
    nDefPos: Position;
    nDefLabel: LabelPtr;
    constructor Init(const aPos: Position; aLab: LabelPtr; aKind: DefiniensSort);
    destructor Done; virtual;
  end ;

```

1094. Constructor.

```

⟨ Implementation for wsmarticle.pas 1001 ⟩ +≡
constructor DefiniensObj.Init(const aPos: Position; aLab: LabelPtr; aKind: DefiniensSort);
  begin nDefSort ← aKind; nDefPos ← aPos; nDefLabel ← aLab;
  end;
destructor DefiniensObj.Done;
  begin if nDefLabel ≠ nil then dispose(nDefLabel, Done);
  end;

```

1095. Definiens expression. These nodes in the abstract syntax tree describe “the right hand side” of a definition. A simple definiens is just a pointer to one definiens expression object, for example.

```

⟨ Publicly declared types in wsmarticle.pas 999 ⟩ +≡
  DefExpressionPtr = ↑DefExpressionObj;
  DefExpressionObj = object (MObject)
    nExprKind: ExpKind;
    nExpr: PObject;
    constructor Init(aKind: ExpKind; aExpr: PObject);
    destructor Done; virtual;
  end ;

```

1096. Constructor.

```

⟨ Implementation for wsmarticle.pas 1001 ⟩ +≡
constructor DefExpressionObj.Init(aKind: ExpKind; aExpr: PObject);
  begin nExprKind ← aKind; nExpr ← aExpr;
  end;
destructor DefExpressionObj.Done;
  begin dispose(nExpr, Done);
  end;

```

1097. Simple definiens. This is the “default” definiens, i.e., the definiens which are not “by cases”.

```

⟨ Publicly declared types in wsmarticle.pas 999 ⟩ +≡
  SimpleDefiniensPtr = ↑SimpleDefiniensObj;
  SimpleDefiniensObj = object (DefiniensObj)
    nExpression: DefExpressionPtr;
    constructor Init(const aPos: Position; aLab: LabelPtr; aDef: DefExpressionPtr);
    destructor Done; virtual;
  end ;

```

1098. Constructor.

```

⟨ Implementation for wsmarticle.pas 1001 ⟩ +≡
constructor SimpleDefiniensObj.Init(const aPos: Position; aLab: LabelPtr; aDef: DefExpressionPtr);
  begin inherited Init(aPos, aLab, SimpleDefiniens); nExpression ← aDef;
  end;
destructor SimpleDefiniensObj.Done;
  begin dispose(nExpression, Done); inherited Done;
  end;

```

1099. Definition for particular case. We have “⟨sentence or term⟩ if ⟨guard condition⟩” represented by a couple of pointers: one to the “sentence or term” definiens, and the second to the “guard” condition.

```

⟨ Publicly declared types in wsmarticle.pas 999 ⟩ +≡
  PartDefPtr = ↑PartDefObj;
  PartDefObj = object (MObject)
    nPartDefiniens: DefExpressionPtr;
    nGuard: FormulaPtr;
    constructor Init(aPartDef: DefExpressionPtr; aGuard: FormulaPtr);
    destructor Done; virtual;
  end ;

```

1100. Constructor.

```

⟨ Implementation for wsmarticle.pas 1001 ⟩ +≡
constructor PartDefObj.Init(aPartDef: DefExpressionPtr; aGuard: FormulaPtr);
  begin nGuard ← aGuard; nPartDefiniens ← aPartDef;
  end;
destructor PartDefObj.Done;
  begin dispose(nPartDefiniens, Done); dispose(nGuard, Done);
  end;

```

1101. Conditional definiens. A conditional definiens consists of a finite list of pointers to *PartDef* objects, and a pointer to the default “otherwise” definien.

```

⟨ Publicly declared types in wsmarticle.pas 999 ⟩ +≡
  ConditionalDefiniensPtr = ↑ConditionalDefiniensObj;
  ConditionalDefiniensObj = object (DefiniensObj)
    nConditionalDefiniensList: PList;
    nOtherwise: DefExpressionPtr;
    constructor Init(const aPos: Position; aLab: LabelPtr; aPartialDefs: PList;
      aOtherwise: DefExpressionPtr);
    destructor Done; virtual;
  end ;

```

1102. Constructor.

```

⟨Implementation for wsmarticle.pas 1001⟩ +≡
constructor ConditionalDefiniensObj.Init(const aPos: Position;
    aLab: LabelPtr; aPartialDefs: PList; aOtherwise: DefExpressionPtr);
    begin inherited Init(aPos, aLab, ConditionalDefiniens); nConditionalDefiniensList ← aPartialDefs;
    nOtherwise ← aOtherwise;
    end;
destructor ConditionalDefiniensObj.Done;
    begin if nOtherwise ≠ nil then dispose(nOtherwise, Done);
    dispose(nConditionalDefiniensList, Done); inherited Done;
    end;

```

1103. Mode definitions. Mizar was heavily inspired by ALGOL, and even borrows ALGOL's terminology for types ("modes"). These are "soft types", which are predicates in the ambient logic.

However, we need to establish the well-definedness of types (i.e., they are inhabited by at least one term), or else we end up in "free logic". For example, if `EmptyType` is a hypothetical empty type, then **for** `x` **being** `EmptyType` `holds` `P[x]` is always true, and **ex** `x` **being** `EmptyType` **st** `P[x]` is always false. The clever Mizar user can abuse this, and end up compromising the soundness of classical logic. To avert catastrophe, we require proving there exists at least one term of the newly defined type.

```

Mode-Definition = "mode" Mode-Pattern
    ( [ Specification ] [ "means" Definiens ] ";" Correctness-Conditions | "is" Type-Expression ";" )
    { Mode-Property } .
Mode-Pattern = Mode-Symbol [ "of" Loci ] .
Mode-Symbol = Symbol | "set" .
Mode-Synonym = "synonym" Mode-Pattern "for" Mode-Pattern ";" .
Mode-Property = "sethood" Justification ";" .

⟨Publicly declared types in wsmarticle.pas 999⟩ +≡
ModeDefinitionSort = (defExpandableMode, defStandardMode);
ModeDefinitionPtr = ↑ModeDefinitionObj;
ModeDefinitionObj = object (MObject)
    nDefKind: ModeDefinitionSort;
    nDefModePos: Position;
    nDefModePattern: ModePatternPtr;
    nRedefinition: boolean;
    constructor Init(const aPos: Position; aDefKind: ModeDefinitionSort; aRedef: boolean;
        aPattern: ModePatternPtr);
    destructor Done; virtual;
end ;

```

1104. Constructor.

```

⟨Implementation for wsmarticle.pas 1001⟩ +≡
constructor ModeDefinitionObj.Init(const aPos: Position; aDefKind: ModeDefinitionSort;
    aRedef: boolean; aPattern: ModePatternPtr);
    begin nDefKind ← aDefKind; nDefModePos ← aPos; nRedefinition ← aRedef;
    nDefModePattern ← aPattern;
    end;
destructor ModeDefinitionObj.Done;
    begin dispose(nDefModePattern, Done);
    end;

```

1105. Expandable mode definitions. These are simple “abbreviations” of modes which are of the form “mode $\langle type\ name \rangle$ is $\langle adjective_1 \rangle \cdots \langle adjective_n \rangle \langle type \rangle$ ”, i.e., just a stack of adjectives atop a type.

```

< Publicly declared types in wsmarticle.pas 999 > +≡
  ExpandableModeDefinitionPtr = ↑ExpandableModeDefinitionObj;
  ExpandableModeDefinitionObj = object (ModeDefinitionObj)
    nExpansion: TypePtr;
    constructor Init(const aPos: Position; aPattern: ModePatternPtr; aExp: TypePtr);
    destructor Done; virtual;
  end ;

```

1106. Constructor.

```

< Implementation for wsmarticle.pas 1001 > +≡
constructor ExpandableModeDefinitionObj.Init(const aPos: Position;
  aPattern: ModePatternPtr; aExp: TypePtr);
  begin inherited Init(aPos, defExpandableMode, false, aPattern); nExpansion ← aExp;
  end;
destructor ExpandableModeDefinitionObj.Done;
  begin dispose(nExpansion, Done); inherited Done;
  end;

```

1107. Standard mode definitions.

```

< Publicly declared types in wsmarticle.pas 999 > +≡
  StandardModeDefinitionPtr = ↑StandardModeDefinitionObj;
  StandardModeDefinitionObj = object (ModeDefinitionObj)
    nSpecification: TypePtr;
    nDefiniens: DefiniensPtr;
    constructor Init(const aPos: Position; aRedef: boolean; aPattern: ModePatternPtr;
  aSpec: TypePtr; aDef: DefiniensPtr);
    destructor Done; virtual;
  end ;

```

1108. Constructor.

```

< Implementation for wsmarticle.pas 1001 > +≡
constructor StandardModeDefinitionObj.Init(const aPos: Position;
  aRedef: boolean; aPattern: ModePatternPtr; aSpec: TypePtr; aDef: DefiniensPtr);
  begin inherited Init(aPos, defStandardMode, aRedef, aPattern); nSpecification ← aSpec;
  nDefiniens ← aDef;
  end;
destructor StandardModeDefinitionObj.Done;
  begin dispose(nSpecification, Done); dispose(nDefiniens, Done); inherited Done;
  end;

```

1109. Attribute definitions. Attributes, like predicates, do not need to worry about correctness conditions. It's only when we want to use them like adjectives on a type that we need to worry, but that's a registration block concern.

```
Attribute-Definition = "attr" Attribute-Pattern "means" Definiens ";" Correctness-Conditions .
Attribute-Pattern = Locus "is" [ Attribute-Loci ] Attribute-Symbol .

⟨Publicly declared types in wsmarticle.pas 999⟩ +=
  AttributeDefinitionPtr = ↑AttributeDefinitionObj;
  AttributeDefinitionObj = object (MObject)
    nDefAttrPos: Position;
    nDefAttrPattern: AttributePatternPtr;
    nRedefinition: boolean;
    nDefiniens: DefiniensPtr;
    constructor Init(const aPos: Position; aRedef: boolean; aPattern: AttributePatternPtr;
      aDef: DefiniensPtr);
    destructor Done; virtual;
  end ;
```

1110. Constructor.

```
⟨Implementation for wsmarticle.pas 1001⟩ +=
constructor AttributeDefinitionObj.Init(const aPos: Position;
  aRedef: boolean; aPattern: AttributePatternPtr; aDef: DefiniensPtr);
begin nDefAttrPos ← aPos; nRedefinition ← aRedef; nDefAttrPattern ← aPattern;
  nDefiniens ← aDef;
end;
destructor AttributeDefinitionObj.Done;
begin dispose(nDefAttrPattern, Done); dispose(nDefiniens, Done);
end;
```

1111. Predicate definitions. Predicates are among the less demanding of the definitions: they are always well-defined, so we do not need to worry about correctness conditions.

```
Predicate-Definition = "pred" Predicate-Pattern [ "means" Definiens ] ";"
Correctness-Conditions { Predicate-Property } .
Predicate-Pattern = [ Loci ] Predicate-Symbol [ Loci ] .
Predicate-Property = ("symmetry" | "asymmetry" | "connectedness" | "reflexivity" | "irreflexivity")
  Justification ";" .
Predicate-Synonym = "synonym" Predicate-Pattern "for" Predicate-Pattern ";" .
Predicate-Antonym = "antonym" Predicate-Pattern "for" Predicate-Pattern ";" .
Predicate-Symbol = Symbol | "=" .

⟨Publicly declared types in wsmarticle.pas 999⟩ +=
  PredicateDefinitionPtr = ↑PredicateDefinitionObj;
  PredicateDefinitionObj = object (MObject)
    nDefPredPos: Position;
    nDefPredPattern: PredicatePatternPtr;
    nRedefinition: boolean;
    nDefiniens: DefiniensPtr;
    constructor Init(const aPos: Position; aRedef: boolean; aPattern: PredicatePatternPtr;
      aDef: DefiniensPtr);
    destructor Done; virtual;
  end ;
```


1112. Constructor.

```

⟨Implementation for wsmarticle.pas 1001⟩ +≡
constructor PredicateDefinitionObj.Init(const aPos: Position;
    aRedef: boolean; aPattern: PredicatePatternPtr; aDef: DefiniensPtr);
    begin nDefPredPos ← aPos; nRedefinition ← aRedef; nDefPredPattern ← aPattern;
    nDefiniens ← aDef;
    end;
destructor PredicateDefinitionObj.Done;
    begin dispose(nDefPredPattern, Done); dispose(nDefiniens, Done);
    end;

```

1113. Functor definitions. We can also define new terms. Well, they introduce “term constructors” (constructors for terms). Mizar calls these guys “functors”.

Functor definitions need to establish the well-definedness of the new term constructor. What this means depends on whether we define the new term using “means” or “equals”, i.e.,

- (1) “⟨new term⟩ **means** ⟨formula⟩” requires proving the existence and uniqueness of the new term;
- (2) “⟨new term⟩ **equals** ⟨term expression⟩” requires proving the new term has the given type.

Why do we need to prove well-definedness? Well, classical logic requires proving there exists a model for a theory, so our hands are tied. If we removed this restriction, then we’d end up with something called “free logic”, which is... weird.

```

Functor-Definition = "func" Functor-Pattern [ Specification ]
    [ ( "means" | "equals" ) Definiens ] ";"
    Correctness-Conditions { Functor-Property } .
Functor-Pattern = [ Functor-Loci ] Functor-Symbol [ Functor-Loci ]
    | Left-Functor-Bracket Loci Right-Functor-Bracket .
Functor-Property = ( "commutativity" | "idempotence" | "involutiveness" | "projectivity" )
    Justification ";" .
Functor-Synonym = "synonym" Functor-Pattern "for" Functor-Pattern ";" .
Functor-Loci = Locus | "(" Loci ")" .
Functor-Symbol = Symbol .
Left-Functor-Bracket = Symbol | "{" | "[" .
Right-Functor-Bracket = Symbol | "}" | "]" .
⟨Publicly declared types in wsmarticle.pas 999⟩ +≡
    FunctorDefinitionPtr = ↑FunctorDefinitionObj;
    FunctorDefinitionObj = object (MObject)
        nDefFuncPos: Position;
        nDefFuncPattern: FunctorPatternPtr;
        nRedefinition: boolean;
        nSpecification: TypePtr;
        nDefiningWay: HowToDefine;
        nDefiniens: DefiniensPtr;
        constructor Init(const aPos: Position; aRedef: boolean; aPattern: FunctorPatternPtr;
            aSpec: TypePtr; aDefWay: HowToDefine; aDef: DefiniensPtr);
        destructor Done; virtual;
    end ;

```

1114. Constructor.

(Implementation for `wsmarticle.pas 1001`) +≡
constructor *FunctorDefinitionObj.Init*(**const** *aPos*: *Position*; *aRedef*: *boolean*;
aPattern: *FunctorPatternPtr*; *aSpec*: *TypePtr*; *aDefWay*: *HowToDefine*; *aDef*: *DefiniensPtr*);
begin *nDefFuncPos* ← *aPos*; *nRedefinition* ← *aRedef*; *nDefFuncPattern* ← *aPattern*;
nSpecification ← *aSpec*; *nDefiningWay* ← *aDefWay*; *nDefiniens* ← *aDef*;
end;
destructor *FunctorDefinitionObj.Done*;
begin *dispose*(*nDefFuncPattern*, *Done*); *dispose*(*nDefiniens*, *Done*);
end;

1115. Notation block. We can recall the syntax for notation blocks.

Notation-Block = "notation" { Loci-Declaration | Notation-Declaration } "end" .

Notation-Declaration = Mode-Synonym
| Functor-Synonym
| Attribute-Synonym | Attribute-Antonym
| Predicate-Synonym | Predicate-Antonym .

Mode-Synonym = "synonym" Mode-Pattern "for" Mode-Pattern ";" .

Functor-Synonym = "synonym" Functor-Pattern "for" Functor-Pattern ";" .

Predicate-Synonym = "synonym" Predicate-Pattern "for" Predicate-Pattern ";" .

Predicate-Antonym = "antonym" Predicate-Pattern "for" Predicate-Pattern ";" .

Attribute-Synonym = "synonym" Attribute-Pattern "for" Attribute-Pattern ";" .

Attribute-Antonym = "antonym" Attribute-Pattern "for" Attribute-Pattern ";" .

The reader will observe all these notation items relate a new pattern which is either a synonym or antonym for an old pattern. That is to say, we only need two patterns to store as data in a notation item node in the abstract syntax tree.

(Publicly declared types in `wsmarticle.pas 999`) +≡
NotationDeclarationPtr = ↑*NotationDeclarationObj*;
NotationDeclarationObj = **object** (*mObject*)
nNotationPos: *Position*;
nNotationSort: *ItemKind*;
nOriginPattern, *nNewPattern*: *PatternPtr*;
constructor *Init*(**const** *aPos*: *Position*; *aNSort*: *ItemKind*; *aNewPatt*, *aOrigPatt*: *PatternPtr*);
destructor *Done*; *virtual*;
end ;

1116. Constructor.

(Implementation for `wsmarticle.pas 1001`) +≡
constructor *NotationDeclarationObj.Init*(**const** *aPos*: *Position*; *aNSort*: *ItemKind*;
aNewPatt, *aOrigPatt*: *PatternPtr*);
begin *nNotationPos* ← *aPos*; *nNotationSort* ← *aNSort*; *nOriginPattern* ← *aOrigPatt*;
nNewPattern ← *aNewPatt*;
end;
destructor *NotationDeclarationObj.Done*;
begin *dispose*(*nOriginPattern*, *Done*); *dispose*(*nNewPattern*, *Done*);
end;

1117. Assumptions in a definition block. The syntax for assumptions in a definition block looks like:

```
Assumption = Single-Assumption | Collective-Assumption | Existential-Assumption .
Single-Assumption = "assume" Proposition ";" .
Collective-Assumption = "assume" Conditions ";" .
Existential-Assumption = "given" Qualified-Variables [ "such" Conditions ] ";" .
Conditions = "that" Proposition { "and" Proposition } .
Proposition = [ Label-Identifier ":" ] Sentence .
Sentence = Formula-Expression .
```

```
< Publicly declared types in wsmarticle.pas 999 > +≡
  AssumptionKind = (SingleAssumption, CollectiveAssumption, ExistentialAssumption);
  AssumptionPtr = ↑AssumptionObj;
  AssumptionObj = object (MObject)
    nAssumptionPos: Position;
    nAssumptionSort: AssumptionKind;
    constructor Init(const aPos: Position; aSort: AssumptionKind);
  end ;
```

1118. Constructor.

```
< Implementation for wsmarticle.pas 1001 > +≡
constructor AssumptionObj.Init(const aPos: Position; aSort: AssumptionKind);
  begin nAssumptionPos ← aPos; nAssumptionSort ← aSort;
end ;
```

1119. Single assumption. When a definition has a single assumption, i.e., a single (usually labeled) formula.

```
< Publicly declared types in wsmarticle.pas 999 > +≡
  SingleAssumptionPtr = ↑SingleAssumptionObj;
  SingleAssumptionObj = object (AssumptionObj)
    nProp: PropositionPtr;
    constructor Init(const aPos: Position; aProp: PropositionPtr);
    destructor Done; virtual;
  end ;
```

1120. Constructor.

```
< Implementation for wsmarticle.pas 1001 > +≡
constructor SingleAssumptionObj.Init(const aPos: Position; aProp: PropositionPtr);
  begin inherited Init(aPos, SingleAssumption); nProp ← aProp;
end ;
destructor SingleAssumptionObj.Done;
  begin dispose(nProp, Done);
end ;
```

1121. Collective assumption. This describes the case when the assumption is “assume C_1 and ... and C_n ”.

```

⟨ Publicly declared types in wsmarticle.pas 999 ⟩ +≡
  CollectiveAssumptionPtr = ↑CollectiveAssumptionObj;
  CollectiveAssumptionObj = object (AssumptionObj)
    nConditions: PList;
    constructor Init(const aPos: Position; aProps: PList);
    destructor Done; virtual;
  end ;

```

1122. Constructor.

```

⟨ Implementation for wsmarticle.pas 1001 ⟩ +≡
constructor CollectiveAssumptionObj.Init(const aPos: Position; aProps: PList);
  begin inherited Init(aPos, CollectiveAssumption); nConditions ← aProps;
  end;
destructor CollectiveAssumptionObj.Done;
  begin dispose(nConditions, Done);
  end;

```

1123. Existential assumption. I must confess I am surprised to see an existential assumption node being a subclass of a collective assumption node.

```

⟨ Publicly declared types in wsmarticle.pas 999 ⟩ +≡
  ExistentialAssumptionPtr = ↑ExistentialAssumptionObj;
  ExistentialAssumptionObj = object (CollectiveAssumptionObj)
    nQVars: PList;
    constructor Init(const aPos: Position; aQVars, aProps: PList);
    destructor Done; virtual;
  end ;

```

1124. Constructor.

```

⟨ Implementation for wsmarticle.pas 1001 ⟩ +≡
constructor ExistentialAssumptionObj.Init(const aPos: Position; aQVars, aProps: PList);
  begin AssumptionObj.Init(aPos, CollectiveAssumption); nConditions ← aProps; nQVars ← aQVars;
  end;
destructor ExistentialAssumptionObj.Done;
  begin dispose(nQVars, Done); inherited Done;
  end;

```

1125. Correctness conditions. The syntax for correctness conditions:

```
Correctness-Conditions = {Correctness-Condition} [ "correctness" Justification ";" ] .
Correctness-Condition =
  ( "existence" | "uniqueness" | "coherence" | "compatibility" | "consistency" | "reducibility" )
  Justification ";" .
```

We begin with an abstract base class for correctness conditions.

```
< Publicly declared types in wsmarticle.pas 999 > +≡
  CorrectnessPtr = ↑CorrectnessObj;
  CorrectnessObj = object (MObject)
    nCorrCondPos: Position;
    nJustification: JustificationPtr;
    constructor Init(const aPos: Position; aJustification: JustificationPtr);
    destructor Done; virtual;
  end ;
```

1126. Constructor.

```
< Implementation for wsmarticle.pas 1001 > +≡
constructor CorrectnessObj.Init(const aPos: Position; aJustification: JustificationPtr);
  begin nCorrCondPos ← aPos; nJustification ← aJustification;
  end;
destructor CorrectnessObj.Done;
  begin dispose(nJustification, Done);
  end;
```

1127. Correctness condition. For the correctness condition associated with a definition or registration, we have this *CorrectnessCondition* object. When we need multiple correctness conditions, we extend it with a subclass.

```
< Publicly declared types in wsmarticle.pas 999 > +≡
  CorrectnessConditionPtr = ↑CorrectnessConditionObj;
  CorrectnessConditionObj = object (CorrectnessObj)
    nCorrCondSort: CorrectnessKind;
    constructor Init(const aPos: Position; aSort: CorrectnessKind; aJustification: JustificationPtr);
    destructor Done; virtual;
  end ;
```

1128. Constructor.

```
< Implementation for wsmarticle.pas 1001 > +≡
constructor CorrectnessConditionObj.Init(const aPos: Position;
  aSort: CorrectnessKind; aJustification: JustificationPtr);
  begin inherited Init(aPos, aJustification); nCorrCondSort ← aSort;
  end;
destructor CorrectnessConditionObj.Done;
  begin inherited Done;
  end;
```

1129. Multiple correctness conditions. For, e.g., functors which require proving both “existence” and “uniqueness”, we have a *CorrectnessConditions* class. This extends the [singular] *CorrectnessCondition* class.

```

⟨Publicly declared types in wsmarticle.pas 999⟩ +≡
  CorrectnessConditionsSet = set of CorrectnessKind;
  CorrectnessConditionsPtr = ↑CorrectnessConditionsObj;
  CorrectnessConditionsObj = object (CorrectnessObj)
    nConditions: CorrectnessConditionsSet;
    constructor Init(const aPos: Position; const aConds: CorrectnessConditionsSet;
      aJustification: JustificationPtr);
    destructor Done; virtual;
  end ;

```

1130. Constructor.

```

⟨Implementation for wsmarticle.pas 1001⟩ +≡
constructor CorrectnessConditionsObj.Init(const aPos: Position;
  const aConds: CorrectnessConditionsSet;
  aJustification: JustificationPtr);
begin inherited Init(aPos, aJustification); nConditions ← aConds;
end;
destructor CorrectnessConditionsObj.Done;
begin inherited Done;
end;

```

1131. Definition properties. The grammar for properties in a definition looks like:

Mode-Property = "sethood" Justification ";" .

Functor-Property = ("commutativity" | "idempotence" | "involutiveness" | "projectivity")
Justification ";" .

Predicate-Property = ("symmetry" | "asymmetry" | "connectedness" | "reflexivity" | "irreflexivity")
Justification ";" .

We see these are all, more or less, “the same”: we have a “kind” of property and a justification. We recall (§847) that we have already introduced the “kind” of properties. So the class describing a definition property node in the abstract syntax tree is:

```

⟨Publicly declared types in wsmarticle.pas 999⟩ +≡
  PropertyPtr = ↑PropertyObj;
  PropertyObj = object (MObject)
    nPropertyPos: Position;
    nPropertySort: PropertyKind;
    nJustification: JustificationPtr;
    constructor Init(const aPos: Position; aSort: PropertyKind; aJustification: JustificationPtr);
    destructor Done; virtual;
  end ;

```

1132. Constructor.

⟨Implementation for `wsmarticle.pas` 1001⟩ +≡

```
constructor PropertyObj.Init(const aPos: Position; aSort: PropertyKind;
    aJustification: JustificationPtr);
    begin nPropertyPos ← aPos; nPropertySort ← aSort; nJustification ← aJustification;
    end;
destructor PropertyObj.Done;
    begin inherited Done;
    end;
```

Section 21.9. REGISTRATIONS

1133. There are three “main” types of registrations, which are “cluster registrations” (because they all involve the “cluster” keyword):

- (1) Existential registrations are of the form “cluster $\langle attributes \rangle$ for $\langle type \rangle$ ” and establishes that a given attribute can act as an adjective for the type.
- (2) Conditional registrations are of the form “cluster $\langle attribute_1 \rangle \rightarrow \langle attribute_2 \rangle$ for $\langle type \rangle$ ” which tells Mizar that when $\langle attribute_1 \rangle$ is established for a term, then Mizar can automatically add $\langle attribute_2 \rangle$ for the term
- (3) Functorial registrations are of the form “cluster $\langle term \rangle \rightarrow \langle attribute \rangle$ [for $\langle type \rangle$]” which will automatically add an attribute to a term.

We also have three lesser registrations which are still important:

- (1) Sethood registrations, establishes a type can be used as a set in a Fraenkel term.
- (2) Reduction registration, which allows Mizar’s term rewriting module to use this rule when reasoning about things.
- (3) Identification registration, which allows Mizar to identify terms of different types.

```
Cluster-Registration = Existential-Registration
```

```
| Conditional-Registration
```

```
| Functorial-Registration .
```

```
Existential-Registration = "cluster" Adjective-Cluster "for" Type-Expression ";"
```

```
Correctness-Conditions .
```

```
Adjective-Cluster = { Adjective } .
```

```
Adjective = [ "non" ] [ Adjective-Arguments ] Attribute-Symbol .
```

```
Conditional-Registration = "cluster" Adjective-Cluster "->" Adjective-Cluster "for" Type-Expression ";"
```

```
Correctness-Conditions .
```

```
Functorial-Registration = "cluster" Term-Expression "->" Adjective-Cluster [ "for" Type-Expression ] ";"
```

```
Correctness-Conditions .
```

```
Identify-Registration = "identify" Functor-Pattern "with" Functor-Pattern
```

```
[ "when" Locus "=" Locus { ", " Locus "=" Locus } ] ";"
```

```
Correctness-Conditions .
```

```
Property-Registration = "sethood" "of" Type-Expression Justification ";" .
```

```
Reduction-Registration = "reduce" Term-Expression "to" Term-Expression ";"
```

```
Correctness-Conditions .
```

1134. Cluster registration. We have a base class for the three types of cluster registrations.

(Publicly declared types in `wsmarticle.pas` 999) +≡

```
ClusterRegistrationKind = (ExistentialRegistration, ConditionalRegistration, FunctorialRegistration);
```

```
ClusterPtr = ↑ClusterObj;
```

```
ClusterObj = object (MObject)
```

```
  nClusterPos: Position;
```

```
  nClusterKind: ClusterRegistrationKind;
```

```
  nConsequent: PList;
```

```
  nClusterType: TypePtr;
```

```
  constructor Init(const aPos: Position; aKind: ClusterRegistrationKind; aCons: PList;
```

```
    aTyp: TypePtr);
```

```
  destructor Done; virtual;
```

```
end ;
```


1135. Constructor.

```

⟨Implementation for wsmarticle.pas 1001⟩ +≡
constructor ClusterObj.Init(const aPos: Position;
    aKind: ClusterRegistrationKind; aCons: PList; aTyp: TypePtr);
    begin nClusterPos ← aPos; nClusterKind ← aKind; nConsequent ← aCons; nClusterType ← aTyp;
    end;
destructor ClusterObj.Done;
    begin dispose(nConsequent, Done);
    end;

```

1136. Existential cluster. We register the fact there always exists a term of a given type satisfying an attribute (e.g., “empty” for “set” means there always exists an empty set; registering the existential cluster “non empty” for “set” means there always exists a nonempty set). This means the attribute may henceforth be used as an adjective on the type.

```

⟨Publicly declared types in wsmarticle.pas 999⟩ +≡
EClusterPtr = ↑EClusterObj;
EClusterObj = object (ClusterObj)
    constructor Init(const aPos: Position; aCons: PList; aTyp: TypePtr);
    destructor Done; virtual;
end ;

```

1137. Constructor. There are no additional fields to an existential cluster object, so it literally passes the parameters onto the superclass’s constructor.

```

⟨Implementation for wsmarticle.pas 1001⟩ +≡
constructor EClusterObj.Init(const aPos: Position; aCons: PList; aTyp: TypePtr);
    begin ClusterObj.Init(aPos, ExistentialRegistration, aCons, aTyp);
    end;
destructor EClusterObj.Done;
    begin if nClusterType ≠ nil then dispose(nClusterType, Done);
    inherited Done;
    end;

```

1138. Conditional cluster. For example “empty sets” are always “finite sets”. This requires tracking the antecedent (“empty”), and the superclass tracks the consequents (“finite”).

```

⟨Publicly declared types in wsmarticle.pas 999⟩ +≡
CClusterPtr = ↑CClusterObj;
CClusterObj = object (ClusterObj)
    nAntecedent: PList;
    constructor Init(const aPos: Position; aAntec, aCons: PList; aTyp: TypePtr);
    destructor Done; virtual;
end ;

```

1139. Constructor.

```

⟨Implementation for wsmarticle.pas 1001⟩ +≡
constructor CClusterObj.Init(const aPos: Position; aAntec, aCons: PList; aTyp: TypePtr);
    begin ClusterObj.Init(aPos, ConditionalRegistration, aCons, aTyp); nAntecedent ← aAntec;
    end;
destructor CClusterObj.Done;
    begin dispose(nAntecedent, Done); inherited Done;
    end;

```

1140. Functorial cluster. The generic form a functorial registrations associated to a term some cluster of adjectives. We need to track the term, but the superclass can manage the cluster of adjectives.

```

⟨Publicly declared types in wsmarticle.pas 999⟩ +≡
  FClusterPtr = ↑FClusterObj;
  FClusterObj = object (ClusterObj)
    nClusterTerm: TermPtr;
    constructor Init(const aPos: Position; aTrm: TermPtr; aCons: PList; aTyp: TypePtr);
    destructor Done; virtual;
  end ;

```

1141. Constructor.

```

⟨Implementation for wsmarticle.pas 1001⟩ +≡
constructor FClusterObj.Init(const aPos: Position;
  aTrm: TermPtr; aCons: PList; aTyp: TypePtr);
  begin ClusterObj.Init(aPos, FunctorialRegistration, aCons, aTyp); nClusterTerm ← aTrm;
  end;
destructor FClusterObj.Done;
  begin if nClusterTerm ≠ nil then Dispose(nClusterTerm, Done);
  if nClusterType ≠ nil then dispose(nClusterType, Done);
  inherited Done;
  end;

```

1142. Loci equality. This is used in identification registrations.

```

⟨Publicly declared types in wsmarticle.pas 999⟩ +≡
  LociEqualityPtr = ↑LociEqualityObj;
  LociEqualityObj = object (mObject)
    nEqPos: Position;
    nLeftLocus, nRightLocus: LocusPtr;
    constructor Init(const aPos: Position; aLeftLocus, aRightLocus: LocusPtr);
    destructor Done; virtual;
  end ;

```

1143. Constructor.

```

⟨Implementation for wsmarticle.pas 1001⟩ +≡
constructor LociEqualityObj.Init(const aPos: Position; aLeftLocus, aRightLocus: LocusPtr);
  begin nEqPos ← aPos; nLeftLocus ← aLeftLocus; nRightLocus ← aRightLocus;
  end;
destructor LociEqualityObj.Done;
  begin Dispose(nLeftLocus, Done); dispose(nRightLocus, Done);
  end;

```

1144. Identification registration. Term identification was first introduced in Artur Kornilowicz’s “How to define terms in Mizar effectively” (in A. Grabowski and A. Naumowicz (eds.), *Computer Reconstruction of the Body of Mathematics*, issue of *Studies in Logic, Grammar and Rhetoric* **18** no.31 (2009), pp. 67–77). See also §2.7 of Adam Grabowski, Artur Kornilowicz, and Adam Naumowicz’s “Mizar in a Nutshell” ([doi:10.6092/issn.1972-5787/1980](https://doi.org/10.6092/issn.1972-5787/1980)) for user-oriented details.

```

⟨ Publicly declared types in wsmarticle.pas 999 ⟩ +≡
  IdentifyRegistrationPtr = ↑IdentifyRegistrationObj;
  IdentifyRegistrationObj = object (mObject)
    nIdentifyPos: Position;
    nOriginPattern, nNewPattern: PatternPtr;
    nEqLocList: PList;
    constructor Init(const aPos: Position; aNewPatt, aOrigPatt: PatternPtr; aEqList: PList);
    destructor Done; virtual;
  end ;

```

1145. Constructor.

```

⟨ Implementation for wsmarticle.pas 1001 ⟩ +≡
constructor IdentifyRegistrationObj.Init(const aPos: Position;
  aNewPatt, aOrigPatt: PatternPtr; aEqList: PList);
  begin nIdentifyPos ← aPos; nOriginPattern ← aOrigPatt; nNewPattern ← aNewPatt;
  nEqLocList ← aEqList;
  end;
destructor IdentifyRegistrationObj.Done;
  begin dispose(nOriginPattern, Done); dispose(nNewPattern, Done);
  if nEqLocList ≠ nil then dispose(nEqLocList, Done);
  end;

```

1146. Property registration. These were introduced in Mizar to facilitated registering “sethood” for types. Thus far, only the “sethood” property is handled in this registration.

```

⟨ Publicly declared types in wsmarticle.pas 999 ⟩ +≡
  PropertyRegistrationPtr = ↑PropertyRegistrationObj;
  PropertyRegistrationObj = object (mObject)
    nPropertyPos: Position;
    nPropertySort: PropertyKind;
    constructor Init(const aPos: Position; aKind: PropertyKind);
    destructor Done; virtual;
  end ;

```

1147. Constructor.

```

⟨ Implementation for wsmarticle.pas 1001 ⟩ +≡
constructor PropertyRegistrationObj.Init(const aPos: Position; aKind: PropertyKind);
  begin nPropertyPos ← aPos; nPropertySort ← aKind;
  end;
destructor PropertyRegistrationObj.Done;
  begin end;

```

1148. Sethood registration. Artur Kornilowicz’s “Sethood Property in Mizar” (in *Joint Proc. FMM and LML Workshops*, 2019, ceur-ws.org/Vol-2634/FMM3.pdf) introduces this “sethood” property. It’s the first (and, so far, only) property registration in Mizar.

```

⟨Publicly declared types in wsmarticle.pas 999⟩ +≡
  SethoodRegistrationPtr = ↑SethoodRegistrationObj;
  SethoodRegistrationObj = object (PropertyRegistrationObj)
    nSethoodType: TypePtr;
    nJustification: JustificationPtr;
    constructor Init(const aPos: Position; aKind: PropertyKind; aType: TypePtr);
    destructor Done; virtual;
  end ;

```

1149. Constructor.

```

⟨Implementation for wsmarticle.pas 1001⟩ +≡
constructor SethoodRegistrationObj.Init(const aPos: Position;
  aKind: PropertyKind; aType: TypePtr);
  begin inherited Init(aPos, aKind); nSethoodType ← aType; nJustification ← nil;
  end;
destructor SethoodRegistrationObj.Done;
  begin dispose(nSethoodType, Done); dispose(nJustification, Done); inherited Done;
  end;

```

1150. Reduce registration. These were introduced, I think, in Artur Kornilowicz’s “On rewriting rules in Mizar” (*J. Autom. Reason.* **50** no.2 (2013) 203–210, [doi:10.1007/s10817-012-9261-6](https://doi.org/10.1007/s10817-012-9261-6)). These extend the checker with new term rewriting rules.

```

⟨Publicly declared types in wsmarticle.pas 999⟩ +≡
  ReduceRegistrationPtr = ↑ReduceRegistrationObj;
  ReduceRegistrationObj = object (MObject)
    nReducePos: Position;
    nOriginTerm, nNewTerm: TermPtr;
    constructor Init(const aPos: Position; aOrigTerm, aNewTerm: TermPtr);
    destructor Done; virtual;
  end ;

```

1151. Constructor.

```

⟨Implementation for wsmarticle.pas 1001⟩ +≡
constructor ReduceRegistrationObj.Init(const aPos: Position; aOrigTerm, aNewTerm: TermPtr);
  begin nReducePos ← aPos; nOriginTerm ← aOrigTerm; nNewTerm ← aNewTerm;
  end;
destructor ReduceRegistrationObj.Done;
  begin dispose(nOriginTerm, Done); dispose(nNewTerm, Done);
  end;

```

Section 21.10. HELPER FUNCTIONS

1152. Capitalization checks if the first character c is lowercase. If so, then set the leading character to be $c \leftarrow c - (\text{ord}(\text{'a'}) - \text{ord}(\text{'A'}))$. But it leaves the rest of the string untouched.

⟨Implementation for `wsmarticle.pas 1001`⟩ +≡

```
function CapitalizeName(aName : string): string;
  begin result  $\leftarrow$  aName;
  if aName[1]  $\in$  ['a' .. 'z'] then dec(Result[1],  $\text{ord}(\text{'a'}) - \text{ord}(\text{'A'})$ )
  end;
```

1153. Uncapitalizing works in the opposite direction, setting the first letter c of a string to be $c \leftarrow c + (\text{ord}(\text{'a'}) - \text{ord}(\text{'A'}))$. Observe capitalizing and uncapitalizing are “nearly inverses” of each other: $\text{CapitalizeName}(\text{UncapitalizeName}(\text{CapitalizeName}(s))) = \text{CapitalizeName}(s)$, and similarly we find $\text{UncapitalizeName}(\text{CapitalizeName}(\text{UncapitalizeName}(s))) = \text{UncapitalizeName}(s)$.

⟨Implementation for `wsmarticle.pas 1001`⟩ +≡

```
function UncapitalizeName(aName : string): string;
  begin result  $\leftarrow$  aName;
  if aName[1]  $\in$  ['A' .. 'Z'] then inc(Result[1],  $\text{ord}(\text{'a'}) - \text{ord}(\text{'A'})$ )
  end;
```

1154. We will be populating global variables tracking names of identifiers, modes, and other syntactic classes.

⟨Global variables publicly declared in `wsmarticle.pas 1154`⟩ ≡

```
var IdentifierName, AttributeName, StructureName, ModeName, PredicateName, FunctorName,
    SelectorName, LeftBracketName, RightBracketName, MMLIdentifierName: array of string;
```

This code is used in section 997.

1155. We will want to initialize these global variables based on previous passes of the scanner.

⟨Implementation for `wsmarticle.pas 1001`⟩ +≡

```
procedure InitScannerNames;
  var i, lCnt, lNr: integer; lDct: text; lInFile: XMLInStreamPtr; lKind, lDummy: AnsiChar;
  lString: string;
  begin ⟨Populate global variables with XML entities 1156⟩;
  ⟨Reset reserved keywords 1158⟩;
  { Identifiers }
  ⟨Initialize identifier names from .idx file 1159⟩;
  end;
```

1156. We need to initialize the length for each of these arrays. Even a crude approximation works, like the total number of lines in the `.dct` file. Then we transform each line of the `lDct` (dictionary file) into appropriate entries of the relevant array.

```

⟨Populate global variables with XML entities 1156⟩ ≡
  assign(lDct, MizFileName + ` .dct `); reset(lDct); lCnt ← 0;
  while ¬seekEof(lDct) do
    begin readln(lDct); inc(lCnt);
    end;
  setlength(AttributeName, lCnt); setlength(StructureName, lCnt); setlength(ModeName, lCnt);
  setlength(PredicateName, lCnt); setlength(FunctorName, lCnt); setlength(SelectorName, lCnt);
  setlength(LeftBracketName, lCnt); setlength(RightBracketName, lCnt);
  setlength(MMLIdentifierName, lCnt); reset(lDct);
  while ¬seekEof(lDct) do
    begin readln(lDct, lKind, lNr, lDummy, lString); ⟨Store XML version of vocabulary word 1157⟩;
    end;
  close(lDct)

```

This code is used in section 1155.

1157. We have read in from the “`.dct`” file one line. The first 148 lines of a “`.dct`” file consists of the reserved keywords for Mizar. A random example of the last few lines of such a file look like:

```

A36 VECTSP_4
A37 ORDINAL1
A38 CARD_FIL
A39 RANKNULL
A40 VECTSP_1
A41 VECTSP_6
A42 VECTSP13
A43 ALGSTR_0
A44 HALLMAR1
A45 MATROIDO

```

So we read the first leading letter of a line into `lKind`, then the number into `lNr`, the space is stuffed into `lDummy`, and the remainder of the line is placed in `lString`.

```

⟨Store XML version of vocabulary word 1157⟩ ≡
  case lKind of
    `A`: MMLIdentifierName[lNr] ← QuoteStrForXML(lString);
    `G`: StructureName[lNr] ← QuoteStrForXML(lString);
    `M`: ModeName[lNr] ← QuoteStrForXML(lString);
    `K`: LeftBracketName[lNr] ← QuoteStrForXML(lString);
    `L`: RightBracketName[lNr] ← QuoteStrForXML(lString);
    `O`: FunctorName[lNr] ← QuoteStrForXML(lString);
    `R`: PredicateName[lNr] ← QuoteStrForXML(lString);
    `U`: SelectorName[lNr] ← QuoteStrForXML(lString);
    `V`: AttributeName[lNr] ← QuoteStrForXML(lString);
  endcases

```

This code is used in section 1156.

1158. Preserve reserved keywords. We want to prevent the user from “overwriting” or “shadowing” the builtin primitive reserved words. This should probably be documented in the user-manual somewhere. The reserved words are: “**strict**”, “**set**”, “**=**”, and the brackets `[]`, braces `{}`, and parentheses `()`. Curiously, “**object**” is not considered a ‘primitive’ worth preserving.

```

⟨Reset reserved keywords 1158⟩ ≡
  AttributeName[StrictSym] ← `strict`; ModeName[SetSym] ← `set`;
  PredicateName[EqualitySym] ← `=`; LeftBracketName[SquareBracket] ← `[`;
  LeftBracketName[CurlyBracket] ← `{`; LeftBracketName[RoundedBracket] ← `(`;
  RightBracketName[SquareBracket] ← `]`; RightBracketName[CurlyBracket] ← `}`;
  RightBracketName[RoundedBracket] ← `)`

```

This code is used in section 1155.

1159. The `.idx` file provides numbers for the local labels and article names referenced in an article.

```

⟨Initialize identifier names from .idx file 1159⟩ ≡
  assign(lDct, MizFileName + `.idx`); reset(lDct); lCnt ← 0;
  while ¬seekEof(lDct) do
    begin readln(lDct); inc(lCnt);
    end;
  close(lDct);
  setlength(IdentifierName, lCnt); IdentifierName[0] ← ``;
  lInFile ← new(XMLInStreamPtr, OpenFile(MizFileName + `.idx`)); lInFile↑.NextElementState;
  lInFile↑.NextElementState;
  while (lInFile.nState = eStart) ∧ (lInFile.nElName = XMLElemName[elSymbol]) do
    begin lNr ← lInFile↑.GetIntAttr(`nr`); lString ← lInFile↑.GetAttr(`name`);
    IdentifierName[lNr] ← lString; lInFile↑.NextElementState; lInFile↑.NextElementState;
    end;
  dispose(lInFile, Done)

```

This code is used in section 1155.

1160. We will want to obtain the name for an article ID number, provided it is a legal number (i.e., less than the dictionary for article ID numbers). This function looks up its entry in the *IdentifierName* array.

```

⟨Implementation for wsmarticle.pas 1001⟩ +≡
function IdentRepr(aIdNr : integer): string;
begin mizassert(2000, aIdNr ≤ length(IdentifierName));
  if aIdNr > 0 then IdentRepr ← IdentifierName[aIdNr]
  else IdentRepr ← ``;
end;

```

Section 21.11. WRITING WSM XML FILES

1161.

```

⟨ Publicly declared types in wsmarticle.pas 999 ⟩ +≡
  OutWSMizFilePtr = ↑ OutWSMizFileObj;
  OutWSMizFileObj = object (XMLOutStreamObj)
    nDisplayInformationOnScreen: boolean;
    nMizarAppearance: boolean;
    constructor OpenFile(const aFileName: string);
    constructor OpenFileWithXSL(const aFileName: string);
    destructor Done; virtual;
    procedure Out_TextProper(aWSTextProper : WSTextProperPtr); virtual;
    procedure Out_Block(aWSBlock : WSBlockPtr); virtual;
    procedure Out_Item(aWSItem : WSItemPtr); virtual;
    procedure Out_ItemContentsAttr(aWSItem : WSItemPtr); virtual;
    procedure Out_ItemContents(aWSItem : WSItemPtr); virtual;
    procedure Out_Variable(aVar : VariablePtr); virtual;
    procedure Out_ReservedVariable(aVar : VariablePtr); virtual;
    procedure Out_TermList(aTrmList : PList); virtual;
    procedure Out_Adjective(aAttr : AdjectiveExpressionPtr); virtual;
    procedure Out_AdjectiveList(aCluster : PList); virtual;
    procedure Out_Type(aTyp : TypePtr); virtual;
    procedure Out_ImplicitlyQualifiedVariable(aSegm : ImplicitlyQualifiedSegmentPtr); virtual;
    procedure Out_VariableSegment(aSegm : QualifiedSegmentPtr); virtual;
    procedure Out_PrivatePredicativeFormula(aFrm : PrivatePredicativeFormulaPtr); virtual;
    procedure Out_Formula(aFrm : FormulaPtr); virtual;
    procedure Out_Term(aTrm : TermPtr); virtual;
    procedure Out_SimpleTerm(aTrm : SimpleTermPtr); virtual;
    procedure Out_PrivateFunctorTerm(aTrm : PrivateFunctorTermPtr); virtual;
    procedure Out_InternalSelectorTerm(aTrm : InternalSelectorTermPtr); virtual;
    procedure Out_TypeList(aTypeList : PList); virtual;
    procedure Out_Locus(aLocus : LocusPtr); virtual;
    procedure Out_Loci(aLoci : PList); virtual;
    procedure Out_Pattern(aPattern : PatternPtr); virtual;
    procedure Out_Label(aLab : LabelPtr); virtual;
    procedure Out_Definiens(aDef : DefiniensPtr); virtual;
    procedure Out_ReservationSegment(aRes : ReservationSegmentPtr); virtual;
    procedure Out_SchemeNameInSchemeHead(aSch : SchemePtr); virtual;
    procedure Out_CompactStatement(aCStm : CompactStatementPtr; aBlock : wsBlockPtr); virtual;
    procedure Out_RegularStatement(aRStm : RegularStatementPtr; aBlock : wsBlockPtr); virtual;
    procedure Out_Proposition(aProp : PropositionPtr); virtual;
    procedure Out_LocalReference(aRef : LocalReferencePtr); virtual;
    procedure Out_References(aRefs : PList); virtual;
    procedure Out_Link(aInf : JustificationPtr); virtual;
    procedure Out_SchemeJustification(aInf : SchemeJustificationPtr); virtual;
    procedure Out_Justification(aInf : JustificationPtr; aBlock : wsBlockPtr); virtual;
  end ;

```


1162. Constructor. The constructor *OutWSMizFileObj.OpenFileWithXSL* is not used anywhere, nor is the associated “wsmiz.xml” file present anywhere.

Importantly, the *nMizarAppearance* field controls whether the XML generated includes the raw lexeme string as an attribute in the XML elements or not.

The constructor *OpenFileWithXSL* is never used. The XML stylesheet *wsmiz.xml* does not seem to be present in the Mizar distribution.

```

<Implementation for wsmarticle.pas 1001> +≡
constructor OutWSMizFileObj.OpenFile(const aFileName: string);
  begin inherited OpenFile(aFileName); nMizarAppearance ← false;
  nDisplayInformationOnScreen ← false;
  end;
constructor OutWSMizFileObj.OpenFileWithXSL(const aFileName: string);
  begin inherited OpenFile(aFileName);
  OutString(‘<?xml-stylesheet_type="text/xml" href="file://’ + MizFiles + ‘wsmiz.xml"?>’ + #10);
  nMizarAppearance ← false;
  end;
destructor OutWSMizFileObj.Done;
  begin inherited Done;
  end;

```

1163. We can write the XML for a *wsTextProper* object (§1003). This writes out the start tag, the children, and the end-tag for the “text proper” and its contents. The RNG compact schema for this looks like:

```

TextProper = element Text-Propser {
  attribute idnr { xsd:integer },
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Item*
}
<Implementation for wsmarticle.pas 1001> +≡
procedure OutWSMizFileObj.Out_TextProper(aWSTextProper : WSTextProperPtr);
  var i: integer;
  begin with aWSTextProper↑ do
    begin { Write the start-tag }
    Out_XElStart(BlockName[blMain]); Out_XAttr(XMLAttrName[atArticleId], nArticleId);
    Out_XAttr(XMLAttrName[atArticleExt], nArticleExt); Out_PosAsAttrs(nBlockPos); Out_XAttrEnd;
    for i ← 0 to nItems↑.Count - 1 do Out_Item(nItems.Items↑[i]); { ...then write the children }
    Out_XElEnd(BlockName[blMain]);
  end;
end;

```

1164. Writing a block out as XML works similarly: write the start-tag, then its children elements, then the end-tag.

```

Block = element Block {
  attribute kind { "Text-Propser" | "Now-Reasoning"
    | "Hereby-Reasoning" | "Definitional-Block"
    | "Notation-Block" | "Registration-Block" | "Case"
    | "Suppose" | "Scheme-Block" },
  attribute idnr { xsd:integer },
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Item*
}

```

(Implementation for `wsmarticle.pas 1001`) +≡
procedure *OutWSMizFileObj.Out_Block*(*aWSBlock* : *WSBlockPtr*);
 var *i*: integer;
 begin with *aWSBlock*↑ **do**
 begin { write the start-tag }
 Out_XElStart(*XMLElemName*[*elBlock*]);
 Out_XAttr(*XMLAttrName*[*atKind*], *BlockName*[*nBlockKind*]); *CurPos* ← *nBlockPos*;
 Out_PosAsAttrs(*nBlockPos*); *Out_XIntAttr*(*XMLAttrName*[*atPosLine*], *nBlockEndPos.Line*);
 Out_XIntAttr(*XMLAttrName*[*atPosCol*], *nBlockEndPos.Col*); *Out_XAttrEnd*;
 for *i* ← 0 **to** *nItems*↑.*Count* − 1 **do**
 begin *Out_Item*(*nItems*↑.*Items*↑[*i*]); **end**; { Then write the children }
 Out_XElEnd(*XMLElemName*[*elBlock*]);
 end;
 end;

1165. Writing a term list to XML amounts to just writing the terms as XML elements. They will be contained in a parent element, so there will be no ambiguity in their role.

```

Term-List = ( Term* )

```

(Implementation for `wsmarticle.pas 1001`) +≡
procedure *OutWSMizFileObj.Out_TermList*(*aTrmList* : *PList*);
 var *i*: integer;
 begin for *i* ← 0 **to** *aTrmList*↑.*Count* − 1 **do** *Out_Term*(*aTrmList*↑.*Items*↑[*i*]);
 end;

1166. The XML for an adjective boils down to two cases:

Case 1 (negated attribute). Write a `<NegatedAdjective>` tag around the XML produced from case 2 for the positive version of the attribute.

Case 2 (positive attribute). Write the adjective, and its children are the [term] arguments to the adjective (if any — if there are none, then an empty-element will be produced).

```

PositiveAdjective = element Adjective {
  attribute nr { xsd:integer },
  attribute name { text },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer }
  Term*
}
Adjective = PositiveAdjective | element NegatedAdjective {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  PositiveAdjective
}
<Implementation for wsmarticle.pas 1001> +=
procedure OutWSMizFileObj.Out_Adjective(aAttr : AdjectiveExpressionPtr);
begin case aAttr↑.nAdjectiveSort of
  wsAdjective: begin Out_XElStart(XMLElemName[elAdjective]);
    with AdjectivePtr(aAttr)↑ do
      begin Out_XIntAttr(XMLAttrName[atNr], nAdjectiveSymbol);
      if nMizarAppearance then
        Out_XAttr(XMLAttrName[atSpelling], AttributeName[nAdjectiveSymbol]);
        Out_PosAsAttrs(nAdjectivePos);
      if nArgs↑.Count = 0 then Out_XElEnd0
      else begin Out_XAttrEnd; Out_TermList(nArgs); Out_XElEnd(XMLElemName[elAdjective]);
        end;
      end;
    end;
  wsNegatedAdjective: begin Out_XElStart(XMLElemName[elNegatedAdjective]);
    with NegatedAdjectivePtr(aAttr)↑ do
      begin Out_PosAsAttrs(nAdjectivePos); Out_XAttrEnd; Out_Adjective(nArg);
      end;
      Out_XElEnd(XMLElemName[elNegatedAdjective]);
    end;
  endcases;
end;

```

1167. Writing an adjective list to XML amounts to stuffing all the adjectives into an element. If there are no adjectives, it is the empty-element.

```

Adjective-Cluster = element Adjective-Cluster {
  attribute count { xsd:integer },
  Adjective*
}

⟨Implementation for wsmarticle.pas 1001⟩ +≡
procedure OutWSMizFileObj.Out_AdjectiveList(aCluster : PList);
  var i: integer;
  begin Out_XElStart(XMLElemName[elAdjectiveCluster]);
  if aCluster↑.Count = 0 then
    begin Out_XElEnd0; exit;
    end;
  Out_XAttrEnd;
  with aCluster↑ do
    for i ← 0 to Count − 1 do Out_Adjective(Items↑[i]);
  Out_XElEnd(XMLElemName[elAdjectiveCluster]);
  end;

```

Subsection 21.11.1. Emitting XML for types

1168. Writing the XML for a Mizar type.

```

StandardType = element Standard-Type {
  attribute nr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Term*
}
StructureType = element Structure-Type {
  attribute nr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Term*
}
ClusteredType = element Clustered-Type {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Adjective-Cluster,
  Type,
}
Type = StandardType | StructureType | ClusteredType

define print_arguments(#) ≡
  if nArgs↑.Count = 0 then Out_XElEnd0
  else begin Out_XAttrEnd; Out_TermList(nArgs); Out_XElEnd(TypeName[#]);
  end
end

⟨Implementation for wsmarticle.pas 1001⟩ +≡
procedure Out_WSMizFileObj.Out_Type(aTyp : TypePtr);
begin with aTyp↑ do
  case aTyp↑.nTypeSort of
    wsStandardType: with StandardTypePtr(aTyp)↑ do
      begin Out_XElStart(TypeName[wsStandardType]);
      Out_XIntAttr(XMLAttrName[atNr], nModeSymbol);
      if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], ModeName[nModeSymbol]);
      Out_PosAsAttrs(nTypePos); print_arguments(wsStandardType);
      end;
    wsStructureType: with StructTypePtr(aTyp)↑ do
      begin Out_XElStart(TypeName[wsStructureType]);
      Out_XIntAttr(XMLAttrName[atNr], nStructSymbol);
      if nMizarAppearance then
        Out_XAttr(XMLAttrName[atSpelling], StructureName[nStructSymbol]);
      Out_PosAsAttrs(nTypePos); print_arguments(wsStructureType);
      end;
    wsClusteredType: with ClusteredTypePtr(aTyp)↑ do
      begin Out_XElStart(TypeName[wsClusteredType]); Out_PosAsAttrs(nTypePos); Out_XAttrEnd;
      Out_AdjectiveList(nAdjectiveCluster); Out_Type(nType);
      Out_XElEnd(TypeName[wsClusteredType]);
      end;
    wsErrorType: begin Out_XElWithPos(TypeName[wsErrorType], nTypePos);
      end;
  endcases;

```

end;

1169. Printing a variable as an XML element.

```
Variable = element Variable {
  attribute idnr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer }
}

⟨Implementation for wsmarticle.pas 1001⟩ +≡
procedure OutWSMizFileObj.Out_Variable(aVar : VariablePtr);
  begin with aVar↑ do
    begin Out_XElStart(XMLElemName[elVariable]); Out_XIntAttr(XMLAttrName[atIdNr], nIdent);
    if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], IdentRepr(nIdent));
    Out_PosAsAttrs(nVarPos); Out_XElEnd0
    end;
  end;
```

1170. Variables introduced using “**reserve**” are just printed out like any other variable.

```
⟨Implementation for wsmarticle.pas 1001⟩ +≡
procedure OutWSMizFileObj.Out_ReservedVariable(aVar : VariablePtr);
  begin Out_Variable(aVar);
  end;
```

1171. Implicitly qualified variables (i.e., variables which are **reserved** with a type, then used in, e.g., a quantified formula) are just variables appearing as children of an “implicitly qualified” XML element.

```
VariableSegment |= element Implicitly-Qualified-Segment {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Variable
}

⟨Implementation for wsmarticle.pas 1001⟩ +≡
procedure OutWSMizFileObj.Out_ImplicitlyQualifiedVariable(aSegm : ImplicitlyQualifiedSegmentPtr);
  begin Out_XElStart(SegmentKindName[ikImplQualifiedSegm]); Out_PosAsAttrs(aSegm↑.nSegmPos);
  Out_XAttrEnd; Out_Variable(aSegm↑.nIdentifier);
  Out_XElEnd(SegmentKindName[ikImplQualifiedSegm]);
  end;
```

1172. Qualified variable segments are either implicitly qualified (hence we use the previous function) or explicitly qualified (which look like “*<variable list> being <type>*”).

Explicitly qualified segments are an XML element with two children (a “variables” XML element, and a “type” XML element).

```
VariableSegment |= element Explicitly-Qualified-Segment {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  element Variables { Variable* },
  Type
}

⟨Implementation for wsmarticle.pas 1001⟩ +≡
procedure OutWSMizFileObj.Out_VariableSegment(aSegm : QualifiedSegmentPtr);
  var i: integer;
  begin case aSegm↑.nSegmentSort of
    ikImplQualifiedSegm: Out_ImplicitlyQualifiedVariable(ImplicitlyQualifiedSegmentPtr(aSegm));
    ikExplQualifiedSegm: with ExplicitlyQualifiedSegmentPtr(aSegm)↑ do
      begin Out_XElStart(SegmentKindName[ikExplQualifiedSegm]); Out_PosAsAttrs(nSegmPos);
        Out_XAttrEnd; Out_XElStart0(XMLElemName[elVariables]);
        for i ← 0 to nIdentifiers↑.Count − 1 do Out_Variable(nIdentifiers↑.Items↑[i]);
        Out_XElEnd(XMLElemName[elVariables]); Out_Type(nType);
        Out_XElEnd(SegmentKindName[ikExplQualifiedSegm]);
      end;
    endcases;
  end;
```

1173. Private predicates have the XML schema

```
Private-Predicate-Formula = element Private-Predicate-Formula {
  attribute idnr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Term-List?
}

⟨Implementation for wsmarticle.pas 1001⟩ +≡
procedure OutWSMizFileObj.Out_PrivatePredicativeFormula(aFrm : PrivatePredicativeFormulaPtr);
  begin with PrivatePredicativeFormulaPtr(aFrm)↑ do
    begin Out_XElStart(FormulaName[wsPrivatePredicateFormula]);
      Out_XIntAttr(XMLAttrName[atIdNr], nPredIdNr);
      if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], IdentRepr(nPredIdNr));
      Out_PosAsAttrs(nFormulaPos);
      if nArgs↑.Count = 0 then Out_XElEnd0
    else begin Out_XAttrEnd; Out_TermList(nArgs);
      Out_XElEnd(FormulaName[wsPrivatePredicateFormula]);
    end;
    end;
  end;
```

Subsection 21.11.2. Emitting XML for formulas

1174. The XML schema for formulas looks something like:

```

Formula = NegatedFormula
| ConjunctiveFormula
| DisjunctiveFormula
| ConditionalFormula
| BiconditionalFormula
| FlexaryConjunctiveFormula
| FlexaryDisjunctiveFormula
| Predicative-Formula
| RightSideOf-Predicative-Formula
| Multi-Predicative-Formula
| Attributive-Formula
| Qualifying-Formula
| Universal-Quantifier-Formula
| Existential-Quantifier-Formula
| element Contradiction {
    attribute col { xsd:integer },
    attribute line { xsd:integer } }
| element Thesis {
    attribute col { xsd:integer },
    attribute line { xsd:integer } }
| element Formula-Error {
    attribute col { xsd:integer },
    attribute line { xsd:integer } }

```

(Implementation for `wsmarticle.pas` 1001) +=

```

procedure OutWSMizFileObj.Out_Formula(aFrm : FormulaPtr);
var i: integer;
begin case aFrm↑.nFormulaSort of
  wsNegatedFormula: ⟨Emit XML for negated formula (WSM) 1175⟩;
  wsConjunctiveFormula: ⟨Emit XML for conjunction (WSM) 1176⟩;
  wsDisjunctiveFormula: ⟨Emit XML for disjunction (WSM) 1177⟩;
  wsConditionalFormula: ⟨Emit XML for conditional formula (WSM) 1178⟩;
  wsBiconditionalFormula: ⟨Emit XML for biconditional formula (WSM) 1179⟩;
  wsFlexaryConjunctiveFormula: ⟨Emit XML for flexary-conjunction (WSM) 1180⟩;
  wsFlexaryDisjunctiveFormula: ⟨Emit XML for flexary-disjunction (WSM) 1181⟩;
  wsPredicativeFormula: ⟨Emit XML for predicative formula (WSM) 1182⟩;
  wsRightSideOfPredicativeFormula: ⟨Emit XML for right-side of predicative formula (WSM) 1183⟩;
  wsMultiPredicativeFormula: ⟨Emit XML for multi-predicative formula (WSM) 1184⟩;
  wsPrivatePredicateFormula: Out_PrivatePredicativeFormula(PrivatePredicativeFormulaPtr(aFrm));
  wsAttributiveFormula: ⟨Emit XML for attributive formula (WSM) 1185⟩;
  wsQualifyingFormula: ⟨Emit XML for qualifying formula (WSM) 1186⟩;
  wsUniversalFormula: ⟨Emit XML for universal formula (WSM) 1187⟩;
  wsExistentialFormula: ⟨Emit XML for existential formula (WSM) 1188⟩;
  wsContradiction: begin Out_XElWithPos(FormulaName[wsContradiction], aFrm↑.nFormulaPos);
    end;
  wsThesis: begin Out_XElWithPos(FormulaName[wsThesis], aFrm↑.nFormulaPos);
    end;
  wsErrorFormula: begin Out_XElWithPos(FormulaName[wsErrorFormula], aFrm↑.nFormulaPos);
    end;
endcases;
end;

```

1175.

```

NegatedFormula = element Negated-Formula {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Formula
}
< Emit XML for negated formula (WSM) 1175 > ≡
  begin Out_XElStart(FormulaName[wsNegatedFormula]); Out_PosAsAttrs(aFrm↑.nFormulaPos);
    Out_XAttrEnd; Out_Formula(NegativeFormulaPtr(aFrm)↑.nArg);
    Out_XElEnd(FormulaName[wsNegatedFormula]);
  end

```

This code is used in section 1174.

1176.

```

ConjunctiveFormula = element Conjunctive-Formula {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Formula,
  Formula
}
< Emit XML for conjunction (WSM) 1176 > ≡
  begin Out_XElStart(FormulaName[wsConjunctiveFormula]); Out_PosAsAttrs(aFrm↑.nFormulaPos);
    Out_XAttrEnd; Out_Formula(BinaryFormulaPtr(aFrm)↑.nLeftArg);
    Out_Formula(BinaryFormulaPtr(aFrm)↑.nRightArg);
    Out_XElEnd(FormulaName[wsConjunctiveFormula]);
  end

```

This code is used in section 1174.

1177.

```

DisjunctiveFormula = element Disjunctive-Formula {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Formula,
  Formula
}
< Emit XML for disjunction (WSM) 1177 > ≡
  begin Out_XElStart(FormulaName[wsDisjunctiveFormula]); Out_PosAsAttrs(aFrm↑.nFormulaPos);
    Out_XAttrEnd; Out_Formula(BinaryFormulaPtr(aFrm)↑.nLeftArg);
    Out_Formula(BinaryFormulaPtr(aFrm)↑.nRightArg);
    Out_XElEnd(FormulaName[wsDisjunctiveFormula]);
  end

```

This code is used in section 1174.

1178.

```
ConditionalFormula = element Conditional-Formula {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Formula,
  Formula
}
```

```
<Emit XML for conditional formula (WSM) 1178> ≡
  begin Out_XElStart(FormulaName[wsConditionalFormula]); Out_PosAsAttrs(aFrm↑.nFormulaPos);
    Out_XAttrEnd; Out_Formula(BinaryFormulaPtr(aFrm↑.nLeftArg);
    Out_Formula(BinaryFormulaPtr(aFrm↑.nRightArg);
    Out_XElEnd(FormulaName[wsConditionalFormula]);
  end
```

This code is used in section 1174.

1179.

```
BiconditionalFormula = element Biconditional-Formula {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Formula,
  Formula
}
```

```
<Emit XML for biconditional formula (WSM) 1179> ≡
  begin Out_XElStart(FormulaName[wsBiconditionalFormula]); Out_PosAsAttrs(aFrm↑.nFormulaPos);
    Out_XAttrEnd; Out_Formula(BinaryFormulaPtr(aFrm↑.nLeftArg);
    Out_Formula(BinaryFormulaPtr(aFrm↑.nRightArg);
    Out_XElEnd(FormulaName[wsBiconditionalFormula]);
  end
```

This code is used in section 1174.

1180.

```
FlexaryConjunctiveFormula = element FlexaryConjunctive-Formula {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Formula,
  Formula
}
```

```
<Emit XML for flexary-conjunction (WSM) 1180> ≡
  begin Out_XElStart(FormulaName[wsFlexaryConjunctiveFormula]);
    Out_PosAsAttrs(aFrm↑.nFormulaPos); Out_XAttrEnd;
    Out_Formula(BinaryFormulaPtr(aFrm↑.nLeftArg);
    Out_Formula(BinaryFormulaPtr(aFrm↑.nRightArg);
    Out_XElEnd(FormulaName[wsFlexaryConjunctiveFormula]);
  end
```

This code is used in section 1174.

1181.

```

FlexaryDisjunctiveFormula = element FlexaryDisjunctive-Formula {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Formula,
  Formula
}

```

```

⟨ Emit XML for flexary-disjunction (WSM) 1181 ⟩ ≡
  begin Out_XElStart(FormulaName[wsFlexaryDisjunctiveFormula]);
    Out_PosAsAttrs(aFrm↑.nFormulaPos); Out_XAttrEnd;
    Out_Formula(BinaryFormulaPtr(aFrm↑.nLeftArg);
    Out_Formula(BinaryFormulaPtr(aFrm↑.nRightArg);
    Out_XElEnd(FormulaName[wsFlexaryDisjunctiveFormula]);
  end

```

This code is used in section 1174.

1182.

```

Predicative-Formula = element Predicative-Formula {
  attribute nr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  element Arguments { Term-List? },
  element Arguments { Term-List? }
}

```

```

⟨ Emit XML for predicative formula (WSM) 1182 ⟩ ≡
  with PredicativeFormulaPtr(aFrm)↑ do
    begin Out_XElStart(FormulaName[wsPredicativeFormula]);
      Out_XIntAttr(XMLAttrName[atNr], nPredNr);
      if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], PredicateName[nPredNr]);
      Out_PosAsAttrs(nFormulaPos); Out_XAttrEnd;
      if nLeftArgs↑.Count = 0 then Out_XEl1(XMLElemName[elArguments])
      else begin Out_XElStart0(XMLElemName[elArguments]); Out_TermList(nLeftArgs);
        Out_XElEnd(XMLElemName[elArguments]);
        end;
      if nRightArgs↑.Count = 0 then Out_XEl1(XMLElemName[elArguments])
      else begin Out_XElStart0(XMLElemName[elArguments]); Out_TermList(nRightArgs);
        Out_XElEnd(XMLElemName[elArguments]);
        end;
      Out_XElEnd(FormulaName[wsPredicativeFormula]);
    end
  end

```

This code is used in section 1174.

1183.

```

RightSideOf-Predicative-Formula = element RightSideOf-Predicative-Formula {
  attribute nr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  element Arguments { Term-List? }
}

⟨Emit XML for right-side of predicative formula (WSM) 1183⟩ ≡
  with RightSideOfPredicativeFormulaPtr(aFrm)↑ do
    begin Out_XElStart(FormulaName[wsRightSideOfPredicativeFormula]);
      Out_XIntAttr(XMLAttrName[atNr], nPredNr);
      if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], PredicateName[nPredNr]);
        Out_PosAsAttrs(nFormulaPos); Out_XAttrEnd;
      if nRightArgs↑.Count = 0 then Out_XEl1(XMLElemName[elArguments])
      else begin Out_XElStart0(XMLElemName[elArguments]); Out_TermList(nRightArgs);
        Out_XElEnd(XMLElemName[elArguments]);
      end;
      Out_XElEnd(FormulaName[wsRightSideOfPredicativeFormula])
    end
  end

```

This code is used in section 1174.

1184.

```

Multi-Predicative-Formula = element Multi-Predicative-Formula {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Formula*
}

⟨Emit XML for multi-predicative formula (WSM) 1184⟩ ≡
  with MultiPredicativeFormulaPtr(aFrm)↑ do
    begin Out_XElStart(FormulaName[wsMultiPredicativeFormula]);
      Out_PosAsAttrs(aFrm↑.nFormulaPos); Out_XAttrEnd;
      for i ← 0 to nScraps.Count - 1 do Out_Formula(nScraps↑.Items↑[i]);
        Out_XElEnd(FormulaName[wsMultiPredicativeFormula])
      end
    end
  end

```

This code is used in section 1174.

1185.

```

Attributive-Formula = element Attributive-Formula {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Term,
  Adjective-Cluster.element
}

```

```

⟨Emit XML for attributive formula (WSM) 1185⟩ ≡
  with AttributiveFormulaPtr(aFrm)↑ do
    begin Out_XElStart(FormulaName[wsAttributiveFormula]); Out_PosAsAttrs(nFormulaPos);
      Out_XAttrEnd; Out_Term(nSubject); Out_AdjectiveList(nAdjectives);
      Out_XElEnd(FormulaName[wsAttributiveFormula]);
    end

```

This code is used in section 1174.

1186.

```

Qualifying-Formula = element Qualifying-Formula {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Term,
  Type,
  Formula
}

```

```

⟨Emit XML for qualifying formula (WSM) 1186⟩ ≡
  with QualifyingFormulaPtr(aFrm)↑ do
    begin Out_XElStart(FormulaName[wsQualifyingFormula]); Out_PosAsAttrs(nFormulaPos);
      Out_XAttrEnd; Out_Term(nSubject); Out_Type(nType);
      Out_XElEnd(FormulaName[wsQualifyingFormula]);
    end

```

This code is used in section 1174.

1187.

```

Universal-Quantifier-Formula = element Universal-Quantifier-Formula {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Variable-Segment,
  Formula
}

```

```

⟨Emit XML for universal formula (WSM) 1187⟩ ≡
  with QuantifiedFormulaPtr(aFrm)↑ do
    begin Out_XElStart(FormulaName[wsUniversalFormula]); Out_PosAsAttrs(nFormulaPos);
      Out_XAttrEnd; Out_VariableSegment(QuantifiedFormulaPtr(aFrm)↑.nSegment);
      Out_Formula(QuantifiedFormulaPtr(aFrm)↑.nScope);
      Out_XElEnd(FormulaName[wsUniversalFormula]);
    end

```

This code is used in section 1174.

1188.

```
Existential-Quantifier-Formula = element Existential-Quantifier-Formula {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Variable-Segment,
  Formula
}

⟨Emit XML for existential formula (WSM) 1188⟩ ≡
  with QuantifiedFormulaPtr(aFrm)↑ do
    begin Out_XElStart(FormulaName[wsExistentialFormula]); Out_PosAsAttrs(nFormulaPos);
      Out_XAttrEnd; Out_VariableSegment(QuantifiedFormulaPtr(aFrm)↑.nSegment);
      Out_Formula(QuantifiedFormulaPtr(aFrm)↑.nScope);
      Out_XElEnd(FormulaName[wsExistentialFormula]);
    end
```

This code is used in section 1174.

Subsection 21.11.3. Emitting XML for Terms

1189. We begin with simple terms.

```
Term |= element Simple-Term {
  attribute idnr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer }
}

⟨Implementation for wsmarticle.pas 1001⟩ +≡
  procedure Out_WSMizFileObj.Out_SimpleTerm(aTrm : SimpleTermPtr);
  begin Out_XElStart(TermName[wsSimpleTerm]);
    Out_XIntAttr(XMLAttrName[atIdNr], aTrm↑.nIdent);
    if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], IdentRepr(aTrm↑.nIdent));
      Out_PosAsAttrs(aTrm↑.nTermPos); Out_XElEnd0;
    end;
```

1190. Terms: Private functors.

```

Term |= element Private-Function-Term {
  attribute idnr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  element Arguments { Term-List }?
}

```

⟨Implementation for `wsmarticle.pas` 1001⟩ +≡

```

procedure OutWSMizFileObj.Out_PrivateFunctionTerm(aTrm : PrivateFunctionTermPtr);
begin with PrivateFunctionTermPtr(aTrm)↑ do
  begin Out_XElStart(TermName[wsPrivateFunctionTerm]);
    Out_XIntAttr(XMLAttrName[atIdNr], nFunctionIdent);
    if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], IdentRepr(nFunctionIdent));
    Out_PosAsAttrs(nTermPos);
    if nArgs↑.Count = 0 then Out_XElEnd0
    else begin Out_XAttrEnd; Out_TermList(nArgs); Out_XElEnd(TermName[wsPrivateFunctionTerm]);
      end;
    end;
  end;
end;

```

1191. Terms: internal selectors.

```

Term |= element Internal-Selector-Term {
  attribute nr { text },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer }
}

```

⟨Implementation for `wsmarticle.pas` 1001⟩ +≡

```

procedure OutWSMizFileObj.Out_InternalSelectorTerm(aTrm : InternalSelectorTermPtr);
begin with aTrm↑ do
  begin Out_XElStart(TermName[wsInternalSelectorTerm]);
    Out_XIntAttr(XMLAttrName[atNr], nSelectorSymbol);
    if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], SelectorName[nSelectorSymbol]);
    Out_PosAsAttrs(nTermPos); Out_XElEnd0;
  end;
end;

```


1192. Terms: numerals, anaphoric “it”, error.

```
Term |= element Numeral {
  attribute number { xsd:int },
  attribute col { xsd:integer },
  attribute line { xsd:integer }
}
```

```
Term |= element It-Term {
  attribute col { xsd:integer },
  attribute line { xsd:integer }
}
```

```
Term |= element Error-Term { }
```

⟨Implementation for `wsmarticle.pas` 1001⟩ +≡

```
procedure OutWSMizFileObj.Out_Term(aTrm : TermPtr);
  var i: integer;
  begin case aTrm↑.nTermSort of
    wsPlaceholderTerm: ⟨Emit XML for placeholder (WSM) 1193⟩;
    wsSimpleTerm: Out_SimpleTerm(SimpleTermPtr(aTrm));
    wsNumeralTerm: begin ; Out_XElStart(TermName[wsNumeralTerm]);
      Out_XIntAttr(XMLAttrName[atNumber], NumeralTermPtr(aTrm)↑.nValue);
      Out_PosAsAttrs(aTrm↑.nTermPos); Out_XElEnd0;
    end;
    wsInfixTerm: ⟨Emit XML for infix term (WSM) 1194⟩;
    wsCircumfixTerm: ⟨Emit XML for circumfix term (WSM) 1195⟩;
    wsPrivateFunctorTerm: Out_PrivateFunctorTerm(PrivateFunctorTermPtr(aTrm));
    wsAggregateTerm: ⟨Emit XML for aggregate term (WSM) 1196⟩;
    wsSelectorTerm: ⟨Emit XML for selector term (WSM) 1197⟩;
    wsInternalSelectorTerm: Out_InternalSelectorTerm(InternalSelectorTermPtr(aTrm));
    wsForgetfulFunctorTerm: ⟨Emit XML for forgetful functor (WSM) 1198⟩;
    wsInternalForgetfulFunctorTerm: ⟨Emit XML for internal forgetful functor (WSM) 1199⟩;
    wsFraenkelTerm: ⟨Emit XML for Fraenkel term (WSM) 1200⟩;
    wsSimpleFraenkelTerm: ⟨Emit XML for simple Fraenkel term (WSM) 1201⟩;
    wsQualificationTerm: ⟨Emit XML for qualification term (WSM) 1202⟩;
    wsExactlyTerm: ⟨Emit XML for exactly qualification term (WSM) 1203⟩;
    wsGlobalChoiceTerm: ⟨Emit XML for global choice term (WSM) 1204⟩;
    wsItTerm: Out_XElWithPos(TermName[wsItTerm], aTrm↑.nTermPos);
    wsErrorTerm: Out_XEl1(TermName[wsErrorTerm]);
  endcases;
end;
```

1193. Terms: placeholders.

```

Term |= element Placeholder-Term {
  attribute nr { text },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer }
}

⟨Emit XML for placeholder (WSM) 1193⟩ ≡
  begin Out_XElStart( TermName[wsPlaceholderTerm]);
    Out_XIntAttr(XMLAttrName[atNr], PlaceholderTermPtr(aTrm)↑.nLocusNr);
    if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling],
      QuoteStrForXML(PlaceHolderName[PlaceholderTermPtr(aTrm)↑.nLocusNr]));
    Out_PosAsAttrs(aTrm↑.nTermPos); Out_XElEnd0;
  end

```

This code is used in section 1192.

1194. Terms: infix.

```

Term |= element Infix-Term {
  attribute nr { text },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  element Arguments { Term-List? },
  element Arguments { Term-List? }
}

⟨Emit XML for infix term (WSM) 1194⟩ ≡
  with InfixTermPtr(aTrm)↑ do
    begin Out_XElStart( TermName[wsInfixTerm]);
      Out_XIntAttr(XMLAttrName[atNr], nFunctorSymbol);
      if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], FunctorName[nFunctorSymbol]);
      Out_PosAsAttrs(nTermPos); Out_XAttrEnd;
      if nLeftArgs↑.Count = 0 then Out_XEl1(XMLElemName[elArguments])
      else begin Out_XElStart0(XMLElemName[elArguments]); Out_TermList(nLeftArgs);
        Out_XElEnd(XMLElemName[elArguments]);
        end;
      if nRightArgs↑.Count = 0 then Out_XEl1(XMLElemName[elArguments])
      else begin Out_XElStart0(XMLElemName[elArguments]); Out_TermList(nRightArgs);
        Out_XElEnd(XMLElemName[elArguments]);
        end;
      Out_XElEnd( TermName[wsInfixTerm]);
    end
  end

```

This code is used in section 1192.

1195. Terms: brackets.

```

Term |= element Circumfix-Term {
  attribute nr { text },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  element Right-Circumflex-Symbol {
    attribute nr { text },
    attribute spelling { text }?,
    attribute col { xsd:integer },
    attribute line { xsd:integer }
  },
  element Arguments { Term-List? }
}

```

⟨Emit XML for circumfix term (WSM) 1195⟩ ≡

```

with CircumfixTermPtr(aTrm)↑ do
  begin Out_XElStart(TermName[wsCircumfixTerm]);
    Out_XIntAttr(XMLAttrName[atNr], nLeftBracketSymbol);
    if nMizarAppearance then
      Out_XAttr(XMLAttrName[atSpelling], LeftBracketName[nLeftBracketSymbol]);
      Out_PosAsAttrs(nTermPos); Out_XAttrEnd;
      Out_XElStart(XMLElemName[elRightCircumflexSymbol]);
      Out_XIntAttr(XMLAttrName[atNr], nRightBracketSymbol);
      if nMizarAppearance then
        Out_XAttr(XMLAttrName[atSpelling], RightBracketName[nRightBracketSymbol]);
        Out_PosAsAttrs(nTermPos); Out_XElEnd0; Out_TermList(nArgs);
        Out_XElEnd(TermName[wsCircumfixTerm]);
      end
    end
  end

```

This code is used in section 1192.

1196. Terms: structure instances.

```

Term |= element Aggregate-Term {
  attribute nr { text },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  element Arguments { Term-List }?
}

```

⟨Emit XML for aggregate term (WSM) 1196⟩ ≡

```

with AggregateTermPtr(aTrm)↑ do
  begin Out_XElStart(TermName[wsAggregateTerm]);
    Out_XIntAttr(XMLAttrName[atNr], nStructSymbol);
    if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], StructureName[nStructSymbol]);
    Out_PosAsAttrs(nTermPos);
    if nArgs↑.Count = 0 then Out_XElEnd0
    else begin Out_XAttrEnd; Out_TermList(nArgs); Out_XElEnd(TermName[wsAggregateTerm]);
      end;
    end
  end

```

This code is used in section 1192.

1197. Terms: selectors.

```

Term |= element Selector-Term {
  attribute nr { text },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Term
}

```

⟨Emit XML for selector term (WSM) 1197⟩ ≡

```

with SelectorTermPtr(aTrm)↑ do
  begin Out_XElStart( TermName[wsSelectorTerm]);
    Out_XIntAttr(XMLAttrName[atNr], nSelectorSymbol);
    if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], SelectorName[nSelectorSymbol]);
    Out_PosAsAttrs(nTermPos); Out_XAttrEnd; Out_Term(nArg);
    Out_XElEnd( TermName[wsSelectorTerm]);
  end

```

This code is used in section 1192.

1198. Terms: forgetful functors.

```

Term |= element Forgetful-Function-Term {
  attribute nr { text },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Term
}

```

⟨Emit XML for forgetful functor (WSM) 1198⟩ ≡

```

with ForgetfulFunctionTermPtr(aTrm)↑ do
  begin Out_XElStart( TermName[wsForgetfulFunctionTerm]);
    Out_XIntAttr(XMLAttrName[atNr], nStructSymbol);
    if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], StructureName[nStructSymbol]);
    Out_PosAsAttrs(nTermPos); Out_XAttrEnd; Out_Term(nArg);
    Out_XElEnd( TermName[wsForgetfulFunctionTerm]);
  end

```

This code is used in section 1192.

1199. Terms: internal forgetful functors.

```

Term |= element Internal-Forgetful-Function-Term {
  attribute nr { text },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
}

```

⟨Emit XML for internal forgetful functor (WSM) 1199⟩ ≡

```

with InternalForgetfulFunctionTermPtr(aTrm)↑ do
  begin Out_XElStart( TermName[wsInternalForgetfulFunctionTerm]);
    Out_XIntAttr(XMLAttrName[atNr], nStructSymbol); Out_PosAsAttrs(nTermPos); Out_XElEnd0;
  end

```

This code is used in section 1192.

1200. Terms: Fraenkel operators.

```

Term |= element Fraenkel-Term {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Variable-Segment*,
  Term,
  Formula
}

```

⟨ Emit XML for Fraenkel term (WSM) 1200 ⟩ ≡

```

with FraenkelTermPtr(aTrm)↑ do
  begin Out_XElStart(TermName[wsFraenkelTerm]); Out_PosAsAttrs(nTermPos); Out_XAttrEnd;
  for i ← 0 to nPostqualification↑.Count − 1 do Out_VariableSegment(nPostqualification↑.Items↑[i]);
  Out_Term(nSample); Out_Formula(nFormula); Out_XElEnd(TermName[wsFraenkelTerm]);
  end

```

This code is used in section 1192.

1201. Terms: Simple Fraenkel expressions.

```

Term |= element Simple-Fraenkel-Term {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Variable-Segment*,
  Term
}

```

⟨ Emit XML for simple Fraenkel term (WSM) 1201 ⟩ ≡

```

with SimpleFraenkelTermPtr(aTrm)↑ do
  begin Out_XElStart(TermName[wsSimpleFraenkelTerm]); Out_PosAsAttrs(nTermPos);
  Out_XAttrEnd;
  for i ← 0 to nPostqualification↑.Count − 1 do Out_VariableSegment(nPostqualification↑.Items↑[i]);
  Out_Term(nSample); Out_XElEnd(TermName[wsSimpleFraenkelTerm]);
  end

```

This code is used in section 1192.

1202. Terms: qualification.

```

Term |= element Qualification-Term {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Term,
  Type
}

```

⟨ Emit XML for qualification term (WSM) 1202 ⟩ ≡

```

with QualifiedTermPtr(aTrm)↑ do
  begin Out_XElStart(TermName[wsQualificationTerm]); Out_PosAsAttrs(nTermPos); Out_XAttrEnd;
  Out_Term(nSubject); Out_Type(nQualification); Out_XElEnd(TermName[wsQualificationTerm]);
  end

```

This code is used in section 1192.

1203. Terms: exactly qualified.

```
Term |= element Exactly-Qualification-Term {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Term
}
```

⟨ Emit XML for exactly qualification term (WSM) 1203 ⟩ ≡

```
with ExactlyTermPtr(aTrm)↑ do
  begin Out_XElStart(TermName[wsQualificationTerm]); Out_PosAsAttrs(nTermPos);
    Out_XAttrEnd; Out_Term(nSubject); Out_XElEnd(TermName[wsQualificationTerm]);
  end
```

This code is used in section 1192.

1204. Terms: global choice expressions.

```
Term |= element Global-Choice-Term {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Type
}
```

⟨ Emit XML for global choice term (WSM) 1204 ⟩ ≡

```
begin Out_XElStart(TermName[wsGlobalChoiceTerm]); Out_PosAsAttrs(aTrm↑.nTermPos);
  Out_XAttrEnd; Out_Type(ChoiceTermPtr(aTrm)↑.nChoiceType);
  Out_XElEnd(TermName[wsGlobalChoiceTerm]);
end
```

This code is used in section 1192.

Subsection 21.11.4. Emitting XML for text items

1205. Type-lists are needed for text items.

```
Type-List = element Type-List {
  Type*
}
```

⟨ Implementation for wsmarticle.pas 1001 ⟩ +≡

```
procedure OutWSMizFileObj.Out_TypeList(aTypeList : PList);
  var i: integer;
  begin Out_XElStart0(XMLElemName[elTypeList]);
    for i ← 0 to aTypeList↑.Count - 1 do Out_Type(aTypeList↑.Items↑[i]);
      Out_XElEnd(XMLElemName[elTypeList]);
    end;
```

1206. Locus.

```

Locus = element Locus {
  attribute idnr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer }
}

⟨Implementation for wsmarticle.pas 1001⟩ +=
procedure OutWSMizFileObj.Out_Locus(aLocus : LocusPtr);
  begin with aLocus↑ do
    begin Out_XElStart(XMLElemName[elLocus]); Out_XIntAttr(XMLAttrName[atIdNr], nVarId);
    if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], IdentRepr(nVarId));
    Out_PosAsAttrs(nVarIdPos); Out_XElEnd0
    end;
  end;

```

1207.

```

Loci = element Loci { Locus* }

⟨Implementation for wsmarticle.pas 1001⟩ +=
procedure OutWSMizFileObj.Out_Loci(aLoci : PList);
  var i: integer;
  begin if (aLoci = nil) ∨ (aLoci↑.Count = 0) then Out_XEl1(XMLElemName[elLoci])
  else begin Out_XElStart0(XMLElemName[elLoci]);
    for i ← 0 to aLoci↑.Count − 1 do Out_Locus(aLoci↑.Items↑[i]);
    Out_XElEnd(XMLElemName[elLoci]);
  end;
  end;

```

1208. Patterns.

```

⟨Implementation for wsmarticle.pas 1001⟩ +=
procedure OutWSMizFileObj.Out_Pattern(aPattern : PatternPtr);
  begin case aPattern↑.nPatternSort of
    itDefPred: ⟨Emit XML for predicate pattern (WSM) 1209⟩;
    itDefFunc: begin case FunctorPatternPtr(aPattern)↑.nFunctKind of
      InfixFunctor: ⟨Emit XML for infix functor pattern (WSM) 1210⟩;
      CircumfixFunctor: ⟨Emit XML for bracket functor pattern (WSM) 1211⟩;
    endcases;
  end;
  itDefMode: ⟨Emit XML for mode pattern (WSM) 1212⟩;
  end;
  itDefAttr: ⟨Emit XML for attribute pattern (WSM) 1213⟩;
  endcases;
  end ;

```

1209.

```

Predicate-Pattern = element Predicate-Pattern {
  attribute nr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Loci,
  Loci
}

⟨Emit XML for predicate pattern (WSM) 1209⟩ ≡
  with PredicatePatternPtr(aPattern)↑ do
    begin Out_XElStart(DefPatternName[itDefPred]);
      Out_XIntAttr(XMLAttrName[atNr], nPredSymbol);
      if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], PredicateName[nPredSymbol]);
        Out_PosAsAttrs(nPatternPos); Out_XAttrEnd; Out_Loci(nLeftArgs); Out_Loci(nRightArgs);
        Out_XElEnd(DefPatternName[itDefPred]);
      end
    end

```

This code is used in section 1208.

1210.

```

Operation-Functor-Pattern = element Operation-Functor-Pattern {
  attribute nr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Loci,
  Loci
}

⟨Emit XML for infix functor pattern (WSM) 1210⟩ ≡
  with InfixFunctorPatternPtr(aPattern)↑ do
    begin Out_XElStart(FunctorPatternName[InfixFunctor]);
      Out_XIntAttr(XMLAttrName[atNr], nOperSymb);
      if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], FunctorName[nOperSymb]);
        Out_PosAsAttrs(nPatternPos); Out_XAttrEnd; Out_Loci(nLeftArgs); Out_Loci(nRightArgs);
        Out_XElEnd(FunctorPatternName[InfixFunctor]);
      end
    end

```

This code is used in section 1208.

1211.

```

Bracket-Function-Pattern = element Bracket-Function-Pattern {
  attribute nr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  element RightCircumflexSymbol {
    attribute nr { xsd:integer },
    attribute spelling { text }?
  },
  Loci
}

```

⟨Emit XML for bracket functor pattern (WSM) 1211⟩ ≡

```

with CircumfixFunctionPatternPtr(aPattern)↑ do
  begin Out_XElStart(FunctionPatternName[CircumfixFunction]);
  Out_XIntAttr(XMLAttrName[atNr], nLeftBracketSymb);
  if nMizarAppearance then
    Out_XAttr(XMLAttrName[atSpelling], LeftBracketName[nLeftBracketSymb]);
    Out_PosAsAttrs(nPatternPos); Out_XAttrEnd;
    Out_XElStart(XMLElemName[elRightCircumflexSymbol]);
    Out_XIntAttr(XMLAttrName[atNr], nRightBracketSymb);
    if nMizarAppearance then
      Out_XAttr(XMLAttrName[atSpelling], RightBracketName[nRightBracketSymb]);
      Out_XAttrEnd; Out_XElEnd(XMLElemName[elRightCircumflexSymbol]); Out_Loci(nArgs);
      Out_XElEnd(FunctionPatternName[CircumfixFunction]);
    end
  end

```

This code is used in section 1208.

1212.

```

Mode-Pattern = element Mode-Pattern {
  attribute nr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Loci
}

```

⟨Emit XML for mode pattern (WSM) 1212⟩ ≡

```

with ModePatternPtr(aPattern)↑ do
  begin Out_XElStart(DefPatternName[itDefMode]);
  Out_XIntAttr(XMLAttrName[atNr], nModeSymbol);
  if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], ModeName[nModeSymbol]);
  Out_PosAsAttrs(nPatternPos); Out_XAttrEnd; Out_Loci(nArgs);
  Out_XElEnd(DefPatternName[itDefMode])

```

This code is used in section 1208.

1213. I am confused why there is both a locus and loci elements in an attribute pattern.

```

Attribute-Pattern = element Attribute-Pattern {
  attribute nr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Locus,
  Loci
}

⟨Emit XML for attribute pattern (WSM) 1213⟩ ≡
  with AttributePatternPtr(aPattern)↑ do
    begin Out_XElStart(DefPatternName[itDefAttr]); Out_XIntAttr(XMLAttrName[atNr], nAttrSymbol);
    if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], AttributeName[nAttrSymbol]);
    Out_PosAsAttrs(nPatternPos); Out_XAttrEnd; Out_Locus(nArg); Out_Loci(nArgs);
    Out_XElEnd(DefPatternName[itDefAttr]);
  end

```

This code is used in section 1208.

1214.

```

Label = element Label {
  attribute idnr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Locus,
  Loci
}

⟨Implementation for wsmarticle.pas 1001⟩ +≡
procedure OutWSMizFileObj.Out_Label(aLab : LabelPtr);
begin
  if (aLab ≠ nil) { ∧(aLab.nLabelIdNr > 0) }
  then
    begin Out_XElStart(XMLElemName[elLabel]);
    Out_XIntAttr(XMLAttrName[atIdNr], aLab↑.nLabelIdNr);
    if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], IdentRepr(aLab↑.nLabelIdNr));
    Out_PosAsAttrs(aLab↑.nLabelPos); Out_XElEnd0
    end;
  end ;

```

1215. Emitting XML for definiens.

```

Definiens = element Definiens {
  attribute kind { "Simple-Definiens" },
  attribute shape { text }?,
  Label,
  (Term | Formula)
} | element Definiens {
  attribute kind { "Conditional-Definiens" },
  attribute shape { text }?,
  Label,
  element Partial-Definiens { (Term | Formula)* },
  (Term | Formula)?
}

⟨Implementation for wsmarticle.pas 1001⟩ +≡
procedure OutWSMizFileObj.Out_Definiens(aDef : DefiniensPtr);
var i: integer; lExprKind: ExprKind;
begin if aDef ≠ nil then
  with DefiniensPtr(aDef)↑ do
    begin Out_XElStart(XMLElemName[elDefiniens]); Out_PosAsAttrs(nDefPos);
    case nDefSort of
      SimpleDefiniens: with SimpleDefiniensPtr(aDef)↑, nExpression↑ do
        begin Out_XAttr(XMLAttrName[atKind], DefiniensKindName[SimpleDefiniens]);
        Out_XAttr(XMLAttrName[atShape], ExpName[nExprKind]); Out_XAttrEnd;
        Out_Label(nDefLabel);
        case nExprKind of
          exTerm: Out_Term(TermPtr(nExpr));
          exFormula: Out_Formula(FormulaPtr(nExpr));
        endcases;
        end;
      ConditionalDefiniens: with ConditionalDefiniensPtr(aDef)↑ do
        begin Out_XAttr(XMLAttrName[atKind], DefiniensKindName[ConditionalDefiniens]);
        lExprKind ← exFormula;
        if nOtherwise ≠ nil then lExprKind ← nOtherwise↑.nExprKind
        else if nConditionalDefiniensList↑.Count > 0 then lExprKind ←
          PartDefPtr(nConditionalDefiniensList↑.Items↑[0])↑.nPartDefiniens↑.nExprKind;
        Out_XAttr(XMLAttrName[atShape], ExpName[lExprKind]); Out_XAttrEnd;
        Out_Label(nDefLabel);
        for i ← 0 to nConditionalDefiniensList↑.Count - 1 do
          with PartDefPtr(nConditionalDefiniensList↑.Items↑[i])↑ do
            begin Out_XElStart0(XMLElemName[elPartialDefiniens]);
            with nPartDefiniens↑ do
              case nExprKind of
                exTerm: Out_Term(TermPtr(nExpr));
                exFormula: Out_Formula(FormulaPtr(nExpr));
              endcases;
            Out_Formula(nGuard); Out_XElEnd(XMLElemName[elPartialDefiniens]);
            end;
          if nOtherwise ≠ nil then
            with nOtherwise↑ do
              case nExprKind of
                exTerm: Out_Term(TermPtr(nExpr));
                exFormula: Out_Formula(FormulaPtr(nExpr));

```

```

        endcases;
    end;
    endcases; Out_XElEnd(XMLElemName[elDefiniens]);
    end;
end;

```

1216.

```

Proposition = element Proposition {
    Label,
    Formula
}
<Implementation for wsmarticle.pas 1001> +≡
procedure Out_WSMizFileObj.Out_Proposition(aProp : PropositionPtr);
    begin Out_XElStart(XMLElemName[elProposition]); Out_XAttrEnd; Out_Label(aProp↑.nLab);
        Out_Formula(aProp↑.nSentence); Out_XElEnd(XMLElemName[elProposition]);
    end;

```

1217.

```

Local-Reference = element Local-Reference {
    attribute col { xsd:integer },
    attribute line { xsd:integer },
    attribute idnr { xsd:integer },
    attribute spelling { text }?
}
<Implementation for wsmarticle.pas 1001> +≡
procedure Out_WSMizFileObj.Out_LocalReference(aRef : LocalReferencePtr);
    begin with LocalReferencePtr(aRef)↑ do
        begin Out_XElStart(ReferenceKindName[LocalReference]); Out_PosAsAttrs(nRefPos);
            Out_XIntAttr(XMLAttrName[atIdNr], nLabId);
            if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], IdentRepr(nLabId));
                Out_XElEnd0;
            end;
        end;
    end;

```

1218.

```

References = (Local-Reference
| element Theorem-Reference {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  attribute at { xsd:integer },
  attribute spelling { text }?,
  attribute nr { xsd:integer }
} | element Definition-Reference {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  attribute at { xsd:integer },
  attribute spelling { text }?,
  attribute nr { xsd:integer }
})*

⟨Implementation for wsmarticle.pas 1001⟩ +≡
procedure OutWSMizFileObj.Out_References(aRefs : PList);
var i: integer;
begin for i ← 0 to aRefs↑.Count − 1 do
  with ReferencePtr(aRefs↑.Items↑[i])↑ do
    case nRefSort of
      LocalReference: Out_LocalReference(aRefs↑.Items↑[i]);
      TheoremReference: begin Out_XElStart(ReferenceKindName[TheoremReference]);
        Out_PosAsAttrs(nRefPos);
        Out_XIntAttr(XMLAttrName[atNr], TheoremReferencePtr(aRefs↑.Items↑[i])↑.nArticleNr);
        if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling],
          MMLIdentifierName[TheoremReferencePtr(aRefs↑.Items↑[i])↑.nArticleNr]);
        Out_XIntAttr(XMLAttrName[atNumber], TheoremReferencePtr(aRefs↑.Items↑[i])↑.nTheoNr);
        Out_XElEnd0;
      end;
      DefinitionReference: begin Out_XElStart(ReferenceKindName[DefinitionReference]);
        Out_PosAsAttrs(nRefPos);
        Out_XIntAttr(XMLAttrName[atNr], DefinitionReferencePtr(aRefs↑.Items↑[i])↑.nArticleNr);
        if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling],
          MMLIdentifierName[TheoremReferencePtr(aRefs↑.Items↑[i])↑.nArticleNr]);
        Out_XIntAttr(XMLAttrName[atNumber], DefinitionReferencePtr(aRefs↑.Items↑[i])↑.nDefNr);
        Out_XElEnd0;
      end;
    endcases;
  end;
end;

```

1219.

```

Link = element Link {
  attribute col { xsd:integer },
  attribute line { xsd:integer }
}

⟨Implementation for wsmarticle.pas 1001⟩ +≡
procedure OutWSMizFileObj.Out_Link(aInf : JustificationPtr);
  begin with StraightforwardJustificationPtr(aInf)↑ do
    if nLinked then
      begin Out_XElStart(XMLElemName[elLink]); Out_PosAsAttrs(nLinkPos); Out_XElEnd0;
      end;
    end;

```

1220.

```

Scheme-Justification = element Scheme-Justification {
  attribute nr { xsd:integer },
  attribute idnr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  attribute poscol { xsd:integer },
  attribute posline { xsd:integer },
  References
}

⟨Implementation for wsmarticle.pas 1001⟩ +≡
procedure OutWSMizFileObj.Out_SchemeJustification(aInf : SchemeJustificationPtr);
  begin with aInf↑ do
    begin Out_XElStart(InferenceName[infSchemeJustification]);
    Out_XIntAttr(XMLAttrName[atNr], nSchFileNr);
    Out_XIntAttr(XMLAttrName[atIdNr], nSchemeIdNr);
    if nMizarAppearance then
      if nSchFileNr > 0 then Out_XAttr(XMLAttrName[atSpelling], MMLIdentifierName[nSchFileNr])
      else if nSchemeIdNr > 0 then Out_XAttr(XMLAttrName[atSpelling], IdentRepr(nSchemeIdNr));
    Out_PosAsAttrs(nInfPos); Out_XIntAttr(XMLAttrName[atPosLine], nSchemeInfPos.Line);
    Out_XIntAttr(XMLAttrName[atPosCol], nSchemeInfPos.Col); Out_XAttrEnd;
    Out_References(nReferences); Out_XElEnd(InferenceName[infSchemeJustification]);
    end;
  end;

```

1221.

```

Justification =
( element Straightforward-Justification {
    attribute col { xsd:integer },
    attribute line { xsd:integer },
    (Link, References)?
  }
| Scheme-Justification
| element Inference-Error {
    attribute col { xsd:integer },
    attribute line { xsd:integer }
  }
| element Skipped-Proof {
    attribute col { xsd:integer },
    attribute line { xsd:integer }
  }
| Block # proof block
)

<Implementation for wsmarticle.pas 1001> +≡
procedure OutWSMizFileObj.Out_Justification(aInf : JustificationPtr; aBlock : wsBlockPtr);
begin case aInf↑.nInfSort of
  infStraightforwardJustification: with StraightforwardJustificationPtr(aInf)↑ do
    begin Out_XElStart(InferenceName[infStraightforwardJustification]); Out_PosAsAttrs(nInfPos);
    if ¬nLinked ∧ (nReferences↑.Count = 0) then Out_XElEnd0
    else begin Out_XAttrEnd; Out_Link(aInf); Out_References(nReferences);
      Out_XElEnd(InferenceName[infStraightforwardJustification]);
    end;
    end;
  infSchemeJustification: Out_SchemeJustification(SchemeJustificationPtr(aInf));
  infError: Out_XElWithPos(InferenceName[infError], aInf↑.nInfPos);
  infSkippedProof: Out_XElWithPos(InferenceName[infSkippedProof], aInf↑.nInfPos);
  infProof: Out_Block(aBlock);
endcases;
end;

```

1222.

```

Compact-Statement = (Proposition, Justification)

<Implementation for wsmarticle.pas 1001> +≡
procedure OutWSMizFileObj.Out_CompactStatement(aCStm : CompactStatementPtr;
  aBlock : wsBlockPtr);
begin with aCStm↑ do
  begin Out_Proposition(nProp); Out_Justification(nJustification, aBlock);
  end;
end;

```

1223.

```

Regular-Statement =
( (Label, Block)
| Compact-Statement
| (Compact-Statement,
  element Iterative-Step {
    attribute col { xsd:integer },
    attribute line { xsd:integer },
    Term,
    Justification
  })*
)

⟨Implementation for wsmarticle.pas 1001⟩ +≡
procedure OutWSMizFileObj.Out_RegularStatement(aRStm : RegularStatementPtr; aBlock : wsBlockPtr);
var i : integer;
begin case aRStm↑.nStatementSort of
  stDiffuseStatement: begin Out_Label(DiffuseStatementPtr(aRStm)↑.nLab); Out_Block(aBlock);
    end;
  stCompactStatement: Out_CompactStatement(CompactStatementPtr(aRStm), aBlock);
  stIterativeEquality: begin Out_CompactStatement(CompactStatementPtr(aRStm), nil);
    with IterativeEqualityPtr(aRStm)↑ do
      for i ← 0 to nIterSteps↑.Count − 1 do
        with IterativeStepPtr(nIterSteps↑.Items↑[i])↑ do
          begin Out_XElStart(XMLElemName[elIterativeStep]); Out_PosAsAttrs(nIterPos);
            Out_XAttrEnd; Out_Term(nTerm); Out_Justification(nJustification, nil);
            Out_XElEnd(XMLElemName[elIterativeStep]);
          end;
        end;
      end;
    end;
  endcases;
end;

```

1224.

```

Variables = element Variables {
  Variable*
}

⟨Implementation for wsmarticle.pas 1001⟩ +≡
procedure OutWSMizFileObj.Out_ReservationSegment(aRes : ReservationSegmentPtr);
var i : integer;
begin with aRes↑ do
  begin Out_XElStart0(XMLElemName[elVariables]);
    for i ← 0 to nIdentifiers↑.Count − 1 do Out_ReservedVariable(nIdentifiers↑.Items↑[i]);
    Out_XElEnd(XMLElemName[elVariables]); Out_Type(nResType);
  end;
end;

```

1225. ⟨Implementation for wsmarticle.pas 1001⟩ +≡

```

procedure OutWSMizFileObj.Out_SchemeNameInSchemeHead(aSch : SchemePtr);
begin Out_XIntAttr(XMLAttrName[atIdNr], aSch↑.nSchemeIdNr);
if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], IdentRepr(aSch↑.nSchemeIdNr));
end;

```


1226. \langle Implementation for `wsmarticle.pas` 1001 $\rangle + \equiv$

```

procedure OutWSMizFileObj.Out_ItemContentsAttr(aWSItem : WSItemPtr);
begin with aWSItem  $\uparrow$  do
  begin CurPos  $\leftarrow$  nItemPos;
  if nDisplayInformationOnScreen then DisplayLine(CurPos.Line, ErrorNbr);
  case nItemKind of
    itDefinition, itSchemeBlock, itSchemeHead, itTheorem, itAxiom, itReservation : ;
    itSection : ;
    itConclusion, itRegularStatement : case RegularStatementPtr(nContent) $\uparrow$ .nStatementSort of
      stDiffuseStatement :
        Out_XAttr(XMLAttrName[atShape], RegularStatementName[stDiffuseStatement]);
      stCompactStatement :
        Out_XAttr(XMLAttrName[atShape], RegularStatementName[stCompactStatement]);
      stIterativeEquality : Out_XAttr(XMLAttrName[atShape], RegularStatementName[stIterativeEquality]);
    endcases;
    itChoice, itReconsider, itPrivFuncDefinition, itPrivPredDefinition, itConstantDefinition, itGeneralization,
      itLocDeclaration, itExistentialAssumption, itExemplification, itPerCases, itCaseBlock : ;
    itCaseHead, itSupposeHead, itAssumption : ;
    itCorrCond : Out_XAttr(XMLAttrName[atCondition],
      CorrectnessName[CorrectnessConditionPtr(nContent) $\uparrow$ .nCorrCondSort]);
    itCorrectness : Out_XAttr(XMLAttrName[atCondition], CorrectnessName[syCorrectness]);
    itProperty :
      Out_XAttr(XMLAttrName[atProperty], PropertyName[PropertyPtr(nContent) $\uparrow$ .nPropertySort]);
    itDefFunc : Out_XAttr(XMLAttrName[atShape],
      DefiningWayName[FunctorDefinitionPtr(nContent) $\uparrow$ .nDefiningWay]);
    itDefPred, itDefMode, itDefAttr, itDefStruct, itPredSynonym, itPredAntonym, itFuncNotation,
      itModeNotation, itAttrSynonym, itAttrAntonym, itCluster, itIdentify, itReduction : ;
    itPropertyRegistration :
      Out_XAttr(XMLAttrName[atProperty], PropertyName[PropertyPtr(nContent) $\uparrow$ .nPropertySort]);
    itPragma :
      Out_XAttr(XMLAttrName[atSpelling], QuoteStrForXML(PragmaPtr(nContent) $\uparrow$ .nPragmaStr));
  endcases;
end;
end;

```

1227. Emitting XML for item contents. This is used to expedite emitting the XML for a text-item (§1242).

⟨Implementation for `wsmarticle.pas` 1001⟩ +≡

```

procedure OutWSMizFileObj.Out_ItemContents(aWSItem : WSItemPtr);
  var i, j: integer; s: CorrectnessKind;
  begin with aWSItem↑ do
    begin case nItemKind of
      itDefinition: Out_Block(nBlock);
      itSchemeBlock: Out_Block(nBlock);
      itSchemeHead: ⟨Emit XML for schema (WSM) 1228⟩;
      itTheorem: Out_CompactStatement(CompactStatementPtr(nContent), nBlock);
      itAxiom: begin end;
      itReservation: Out_ReservationSegment(ReservationSegmentPtr(nContent));
      itSection: ;
      itConclusion, itRegularStatement: Out_RegularStatement(RegularStatementPtr(nContent), nBlock);
      itChoice: ⟨Emit XML for consider contents (WSM) 1229⟩;
      itReconsider: ⟨Emit XML for reconsider contents (WSM) 1230⟩;
      ⟨Emit XML for definition-related items (WSM) 1231⟩;
      itPredSynonym, itPredAntonym, itFuncNotation, itModeNotation, itAttrSynonym, itAttrAntonym:
        with NotationDeclarationPtr(nContent)↑ do
          begin Out_Pattern(nOriginPattern); Out_Pattern(nNewPattern);
          end;
      ⟨Emit XML for registration-related items (WSM) 1240⟩;
      itPragma: ;
      itIncorrItem: ;
    end;
  endcases;
end;

```

1228.

```

Item-contents |= Scheme-contents
Scheme-contents = element Scheme {
  attribute idnr { xsd:integer },
  attribute spelling { text }?,
  element Schematic-Variables {
    (element Predicate-Segment {
      attribute col { xsd:integer },
      attribute line { xsd:integer },
      element Variables { Variable* },
      Type
    } | element Functor-Segment {
      attribute col { xsd:integer },
      attribute line { xsd:integer },
      element Variables { Variable* },
      Type-List,
      element Type-Specification { Type }
    })*
  },
  Formula,
  element Provisional-Formulas { Proposition* }?
}

⟨Emit XML for schema (WSM) 1228⟩ ≡
  with SchemePtr(nContent)↑ do
    begin Out_XElStart(XMLElemName[elScheme]);
      Out_SchemeNameInSchemeHead(SchemePtr(nContent)); Out_XElEnd0;
      Out_XElStart0(XMLElemName[elSchematicVariables]);
      for j ← 0 to nSchemeParams↑.Count - 1 do
        case SchemeSegmentPtr(nSchemeParams.Items↑[j])↑.nSegmSort of
          PredicateSegment: with PredicateSegmentPtr(nSchemeParams.Items↑[j])↑ do
            begin Out_XElStart(SchemeSegmentName[PredicateSegment]); Out_PosAsAttrs(nSegmPos);
              Out_XAttrEnd; Out_XElStart0(XMLElemName[elVariables]);
              for i ← 0 to nVars↑.Count - 1 do Out_Variable(nVars.Items↑[i]);
                Out_XElEnd(XMLElemName[elVariables]); Out_TypeList(nTypeExpList);
                Out_XElEnd(SchemeSegmentName[PredicateSegment]);
              end;
            FunctorSegment: with FunctorSegmentPtr(nSchemeParams.Items↑[j])↑ do
              begin Out_XElStart(SchemeSegmentName[FunctorSegment]); Out_PosAsAttrs(nSegmPos);
                Out_XAttrEnd; Out_XElStart0(XMLElemName[elVariables]);
                for i ← 0 to nVars↑.Count - 1 do Out_Variable(nVars.Items↑[i]);
                  Out_XElEnd(XMLElemName[elVariables]); Out_TypeList(nTypeExpList);
                  Out_XElStart0(XMLElemName[elTypeSpecification]); Out_Type(nSpecification);
                  Out_XElEnd(XMLElemName[elTypeSpecification]);
                  Out_XElEnd(SchemeSegmentName[FunctorSegment]);
                end;
            endcases;
          Out_XElEnd(XMLElemName[elSchematicVariables]); Out_Formula(nSchemeConclusion);
        if (nSchemePremises ≠ nil) ∧ (nSchemePremises↑.Count > 0) then
          begin Out_XElStart0(XMLElemName[elProvisionalFormulas]);
            for i ← 0 to nSchemePremises↑.Count - 1 do Out_Proposition(nSchemePremises↑.Items↑[i]);
              Out_XElEnd(XMLElemName[elProvisionalFormulas]);
            end;
        end;

```

end

This code is used in section 1227.

1229.

```

Item-contents |= Consider-Statement-contents
Consider-Statement-contents =
( Variable-Segment*,
  element Conditions { Proposition },
  Justification
)
⟨Emit XML for consider contents (WSM) 1229⟩ ≡
  with ChoiceStatementPtr(nContent)↑ do
    begin for i ← 0 to nQualVars↑.Count − 1 do Out_VariableSegment(nQualVars↑.Items↑[i]);
      Out_XElStart0(XMLElemName[elConditions]);
      for i ← 0 to nConditions↑.Count − 1 do Out_Proposition(nConditions↑.Items↑[i]);
        Out_XElEnd(XMLElemName[elConditions]); Out_Justification(nJustification, nil);
      end
    end
  end

```

This code is used in section 1227.

1230.

```

Item-contents |= Type-Changing-Statement-contents
Type-Changing-Statement-contents =
((element Equality {
  Variable,
  Term
} | Variable),
Type)
⟨Emit XML for reconsider contents (WSM) 1230⟩ ≡
  with TypeChangingStatementPtr(nContent)↑ do
    begin for i ← 0 to nTypeChangeList↑.Count − 1 do
      case TypeChangePtr(nTypeChangeList.Items↑[i])↑.nTypeChangeKind of
        Equating: begin Out_XElStart0(XMLElemName[elEquality]);
          Out_Variable(TypeChangePtr(nTypeChangeList.Items↑[i])↑.nVar);
          Out_Term(TypeChangePtr(nTypeChangeList.Items↑[i])↑.nTermExpr);
          Out_XElEnd(XMLElemName[elEquality]);
        end;
        VariableIdentifier: begin Out_Variable(TypeChangePtr(nTypeChangeList.Items↑[i])↑.nVar);
        end;
      endcases;
      Out_Type(nTypeExpr); Out_Justification(nJustification, nil);
    end
  end

```

This code is used in section 1227.

1231. We will need to recall *Out_Variable* (§1169) fr *PrivateFunctorDefinitionObj* (§1040).

```

Item-contents |=
  (Variable, Type-List, Term) # private functors and predicates
| (Variable, Term) # constants
| Variable-Segment # loci
< Emit XML for definition-related items (WSM) 1231 > ≡
itPrivFuncDefinition: with PrivateFunctorDefinitionPtr(nContent)↑ do
  begin Out_Variable(nFuncId); Out_TypeList(nTypeExpList); Out_Term(nTermExpr);
  end;
itPrivPredDefinition: with PrivatePredicateDefinitionPtr(nContent)↑ do
  begin Out_Variable(nPredId); Out_TypeList(nTypeExpList); Out_Formula(nSentence);
  end;
itConstantDefinition: with ConstantDefinitionPtr(nContent)↑ do
  begin Out_Variable(nVarId); Out_Term(nTermExpr);
  end;
itLocDeclaration, itGeneralization: Out_VariableSegment(QualifiedSegmentPtr(nContent));
itCaseHead, itSupposeHead, itAssumption: < Emit XML for assumptions item (WSM) 1239 >;
See also sections 1232, 1233, 1234, 1235, 1236, 1237, and 1238.
This code is used in section 1227.

```

1232.

```

Item-contents |=
( Variable-Segment*,
  element Conditions { Proposition* } )
< Emit XML for definition-related items (WSM) 1231 > +≡
itExistentialAssumption: with ExistentialAssumptionPtr(nContent)↑ do
  begin for i ← 0 to nQVars↑.Count - 1 do Out_VariableSegment(nQVars↑.Items↑[i]);
  Out_XElStart0(XMLElemName[elConditions]);
  for i ← 0 to nConditions↑.Count - 1 do Out_Proposition(nConditions↑.Items↑[i]);
  Out_XElEnd(XMLElemName[elConditions]);
  end;

```

1233.

```

Item-contents |= ( Variable?, Term? ) # Exemplification
| Justification # percases, correctness-condition
| Block # case block
< Emit XML for definition-related items (WSM) 1231 > +≡
itExemplification: with ExamplePtr(nContent)↑ do
  begin if nVarId ≠ nil then Out_Variable(nVarId);
  if nTermExpr ≠ nil then Out_Term(nTermExpr);
  end;
itPerCases: Out_Justification(JustificationPtr(nContent), nil);
itCaseBlock: Out_Block(nBlock);
itCorrCond: Out_Justification(CorrectnessConditionPtr(nContent)↑.nJustification, nBlock);

```

1234.

```

Item-contents |=
  element CorrectnessConditions { # sic!
    element Correctness { attribute condition { text } }*,
    Justification }
|Justification # Property
⟨Emit XML for definition-related items (WSM) 1231⟩ +≡
itCorrectness: begin Out_XElStart0 (XMLElemName[elCorrectnessConditions]);
  for  $s \in \text{CorrectnessConditionsPtr}(nContent) \uparrow .nConditions$  do
    begin Out_XElStart (ItemName[itCorrectness]);
      Out_XAttr (XMLAttrName[atCondition], CorrectnessName[s]); Out_XElEnd0;
    end;
  Out_XElEnd (XMLElemName[elCorrectnessConditions]);
  Out_Justification (CorrectnessPtr(nContent)↑.nJustification, nBlock);
end;
itProperty: Out_Justification (PropertyPtr(nContent)↑.nJustification, nBlock);

```

1235.

```

Item-contents |=
( element Redefine { }?,
  Pattern,
  element Standard-Mode { Type },
  | element Expandable-Mode {
    element Type-Specification { Type }?,
    Definiens
  })
⟨Emit XML for definition-related items (WSM) 1231⟩ +≡
itDefMode: with ModeDefinitionPtr(nContent)↑ do
  begin if nRedefinition then Out_XEl1 (XMLElemName[elRedefine]);
    Out_Pattern(nDefModePattern);
  case nDefKind of
    defExpandableMode: begin Out_XElStart0 (ModeDefinitionSortName[defExpandableMode]);
      Out_Type (ExpandableModeDefinitionPtr(nContent)↑.nExpansion);
      Out_XElEnd (ModeDefinitionSortName[defExpandableMode]);
    end;
    defStandardMode: with StandardModeDefinitionPtr(nContent)↑ do
      begin Out_XElStart0 (ModeDefinitionSortName[defStandardMode]);
        if nSpecification ≠ nil then
          begin Out_XElStart0 (XMLElemName[elTypeSpecification]); Out_Type (nSpecification);
            Out_XElEnd (XMLElemName[elTypeSpecification]);
          end;
          Out_Definiens(nDefiniens); Out_XElEnd (ModeDefinitionSortName[defStandardMode]);
        end;
      endcases;
    end;

```

1236.

```

Item-contents |=
(element Redefine { }?,
 Pattern,
 Definiens)
⟨Emit XML for definition-related items (WSM) 1231⟩ +≡
itDefAttr: with AttributeDefinitionPtr(nContent)↑ do
    begin if nRedefinition then Out_XEl1(XMLElemName[elRedefine]);
    Out_Pattern(nDefAttrPattern); Out_Definiens(nDefiniens);
    end;
itDefPred: with PredicateDefinitionPtr(nContent)↑ do
    begin if nRedefinition then Out_XEl1(XMLElemName[elRedefine]);
    Out_Pattern(nDefPredPattern); Out_Definiens(nDefiniens);
    end;

```

1237.

```

Item-contents |=
(element Redefine { }?,
 Pattern,
 element Type-Specification { Type }?,
 Definiens)
⟨Emit XML for definition-related items (WSM) 1231⟩ +≡
itDefFunc: with FunctorDefinitionPtr(nContent)↑ do
    begin if nRedefinition then Out_XEl1(XMLElemName[elRedefine]);
    Out_Pattern(nDefFuncPattern);
    if nSpecification ≠ nil then
        begin Out_XElStart0(XMLElemName[elTypeSpecification]); Out_Type(nSpecification);
        Out_XElEnd(XMLElemName[elTypeSpecification]);
        end;
    Out_Definiens(nDefiniens);
    end;

```

1238.

```

Item-contents |=
(element Ancestors { Type* },
  attribute nr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Loci,
  (element Field-Segment {
    attribute col { xsd:integer },
    attribute line { xsd:integer },
    (element Selector {
      attribute nr { xsd:integer },
      attribute spelling { text }?,
      attribute col { xsd:integer },
      attribute line { xsd:integer }
    })*,
    Type
  )*
),
}
< Emit XML for definition-related items (WSM) 1231 > +=
itDefStruct: with StructureDefinitionPtr(nContent)↑ do
  begin Out_XElStart0(XMLElemName[elAncestors]);
  for i ← 0 to nAncestors↑.Count - 1 do Out_Type(nAncestors↑.Items↑[i]);
  Out_XElEnd(XMLElemName[elAncestors]); Out_XElStart(DefPatternName[itDefStruct]);
  Out_XIntAttr(XMLAttrName[atNr], nDefStructPattern↑.nModeSymbol);
  if nMizarAppearance then
    Out_XAttr(XMLAttrName[atSpelling], StructureName[nDefStructPattern↑.nModeSymbol]);
  Out_PosAsAttrs(nStrPos); Out_XAttrEnd; Out_Loci(nDefStructPattern↑.nArgs);
  for i ← 0 to nSgmFields↑.Count - 1 do
    with FieldSegmentPtr(nSgmFields↑.Items↑[i])↑ do
      begin Out_XElStart(XMLElemName[elFieldSegment]); Out_PosAsAttrs(nFieldSegmPos);
      Out_XAttrEnd;
      for j ← 0 to nFields↑.Count - 1 do
        with FieldSymbolPtr(nFields↑.Items↑[j])↑ do
          begin Out_XElStart(XMLElemName[elSelector]);
          Out_XIntAttr(XMLAttrName[atNr], nFieldSymbol);
          if nMizarAppearance then
            Out_XAttr(XMLAttrName[atSpelling], SelectorName[nFieldSymbol]);
          Out_PosAsAttrs(nFieldPos); Out_XElEnd0
          end;
        Out_Type(nSpecification); Out_XElEnd(XMLElemName[elFieldSegment]);
      end;
    Out_XElEnd(DefPatternName[itDefStruct]);
  end
end

```


1239.

```

Item-contents |= (element Single-Assumption {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Proposition
} | element Collective-Assumption {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  element Conditions { Proposition* }
})

⟨Emit XML for assumptions item (WSM) 1239⟩ ≡
  case AssumptionPtr(nContent)↑.nAssumptionSort of
    SingleAssumption: begin Out_XElStart(AssumptionKindName[SingleAssumption]);
      Out_PosAsAttrs(AssumptionPtr(nContent)↑.nAssumptionPos); Out_XAttrEnd;
      Out_Proposition(SingleAssumptionPtr(nContent)↑.nProp);
      Out_XElEnd(AssumptionKindName[SingleAssumption]);
    end;
    CollectiveAssumption: begin Out_XElStart(AssumptionKindName[CollectiveAssumption]);
      Out_PosAsAttrs(AssumptionPtr(nContent)↑.nAssumptionPos); Out_XAttrEnd;
      Out_XElStart0(XMLElemName[elConditions]);
      with CollectiveAssumptionPtr(nContent)↑ do
        for i ← 0 to nConditions↑.Count - 1 do Out_Proposition(nConditions↑.Items↑[i]);
          Out_XElEnd(XMLElemName[elConditions]);
          Out_XElEnd(AssumptionKindName[CollectiveAssumption]);
        end;
      endcases
  endcases

```

This code is used in section 1231.

1240. We have cluster registrations and non-cluster registrations.

```

Existential-Registration-content = element Existential-Registration {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Adjective-Cluster,
  Type
}
Conditional-Registration-content = element Conditional-Registration {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Adjective-Cluster, Adjective-Cluster,
  Type
}
Functorial-Registration-content = element Functorial-Registration {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Term,
  Adjective-Cluster,
  Type?
}
⟨Emit XML for registration-related items (WSM) 1240⟩ ≡
itCluster: case ClusterPtr(nContent)↑.nClusterKind of
  ExistentialRegistration: with EClusterPtr(nContent)↑ do
    begin Out_XElStart(ClusterRegistrationName[ExistentialRegistration]);
    Out_PosAsAttrs(nClusterPos); Out_XAttrEnd; Out_AdjectiveList(nConsequent);
    Out_Type(nClusterType); Out_XElEnd(ClusterRegistrationName[ExistentialRegistration]);
    end;
  ConditionalRegistration: with CClusterPtr(nContent)↑ do
    begin Out_XElStart(ClusterRegistrationName[ConditionalRegistration]);
    Out_PosAsAttrs(nClusterPos); Out_XAttrEnd; Out_AdjectiveList(nAntecedent);
    Out_AdjectiveList(nConsequent); Out_Type(nClusterType);
    Out_XElEnd(ClusterRegistrationName[ConditionalRegistration]);
    end;
  FunctorialRegistration: with FClusterPtr(nContent)↑ do
    begin Out_XElStart(ClusterRegistrationName[FunctorialRegistration]);
    Out_PosAsAttrs(nClusterPos); Out_XAttrEnd; Out_Term(nClusterTerm);
    Out_AdjectiveList(nConsequent);
    if nClusterType ≠ nil then Out_Type(nClusterType);
    Out_XElEnd(ClusterRegistrationName[FunctorialRegistration]);
    end;
endcases;

```

See also section 1241.

This code is used in section 1227.

1241.

```

Identify-Registration-content =
  (Pattern, Pattern,
    element LociEquality {
      attribute col { xsd:integer },
      attribute line { xsd:integer },
      Locus, Locus
    }*
  )
Sethood-Registration-content = (Type, Justification)
Reduction-Registration-content = (Term, Term)
⟨Emit XML for registration-related items (WSM) 1240⟩ +≡
itIdentify: with IdentifyRegistrationPtr(nContent)↑ do
  begin Out_Pattern(nOriginPattern); Out_Pattern(nNewPattern);
  if nEqLociList ≠ nil then
    begin for i ← 0 to nEqLociList↑.Count − 1 do
      with LociEqualityPtr(nEqLociList↑.Items↑[i])↑ do
        begin Out_XElStart(XMLElemName[elLociEquality]); Out_PosAsAttrs(nEqPos);
          Out_XAttrEnd; Out_Locus(nLeftLocus); Out_Locus(nRightLocus);
          Out_XElEnd(XMLElemName[elLociEquality]);
        end;
      end;
    end;
  end;
itPropertyRegistration: case PropertyRegistrationPtr(nContent)↑.nPropertySort of
  sySethood: with SethoodRegistrationPtr(nContent)↑ do
    begin Out_Type(nSethoodType); Out_Justification(nJustification, nBlock);
    end;
  endcases;
itReduction: with ReduceRegistrationPtr(nContent)↑ do
  begin Out_Term(nOriginTerm); Out_Term(nNewTerm);
  end

```

1242. Emitting an item.

```

Item = element Item {
  attribute kind { text },
  Item-contents-attribute?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  attribute posline { xsd:integer },
  attribute poscol { xsd:integer },
  (Block | Item-contents)?
}

⟨Implementation for wsmarticle.pas 1001⟩ +≡
procedure OutWSMizFileObj.Out_Item(aWSItem : WSItemPtr);
  var i, j: integer;
  begin with aWSItem↑ do
    begin CurPos ← nItemPos; Out_XElStart(XMLElemName[elItem]);
    Out_XAttr(XMLAttrName[atKind], ItemName[nItemKind]);
    if nContent ≠ nil then Out_ItemContentsAttr(aWsItem);
    Out_PosAsAttrs(nItemPos); Out_XIntAttr(XMLAttrName[atPosLine], nItemEndPos.Line);
    Out_XIntAttr(XMLAttrName[atPosCol], nItemEndPos.Col); Out_XAttrEnd;
    if nContent = nil then
      begin if nBlock ≠ nil then Out_Block(nBlock);
      end
    else Out_ItemContents(aWsItem);
    Out_XElEnd(XMLElemName[elItem]);
    end;
  end;

```

1243. Writing out to an XML file.

```

procedure Write_WSMizArticle(aWSTextProper : wsTextProperPtr; aFileName : string);
  var lWSMizOutput: OutWSMizFilePtr;
  begin InitScannerNames; lWSMizOutput ← new(OutWSMizFilePtr, OpenFile(aFileName));
  lWSMizOutput↑.nMizarAppearance ← true; lWSMizOutput↑.Out_TextProper(aWSTextProper);
  dispose(lWSMizOutput, Done);
  end;

```

Section 21.12. READING WSM FILES (DEFERRED)

1244. Reading a WSM file amounts to reading an XML file, which means that the *XMLInStream* class (§655) is a natural parent class. Recall, the state of the *XMLInStream* contains the current start tag and a dictionary for the attributes and their values.

The code is a “mirror image” to writing XML files, and the XML schema guides the implementation.

```
(Publicly declared types in wsmarticle.pas 999) +≡
  InWSMizFilePtr = ↑InWSMizFileObj;
  InWSMizFileObj = object (XMLInStreamObj)
    nDisplayInformationOnScreen: boolean;
    constructor OpenFile(const aFileName: string);
    destructor Done; virtual;
    function GetAttrValue(const aAttrName: string): string;
    function GetAttrPos: Position;
    function Read_TextProper: wsTextProperPtr; virtual;
    function Read_Block: wsBlockPtr; virtual;
    function Read_Item: wsItemPtr; virtual;
    procedure Read_ItemContentsAttr(aItem : wsItemPtr; var aShape : string); virtual;
    procedure Read_ItemContents(aItem : wsItemPtr ; const aShape: string); virtual;
    function Read_TermList: PList; virtual;
    function Read_Adjective: AdjectiveExpressionPtr; virtual;
    function Read_AdjectiveList: PList; virtual;
    function Read_Type: TypePtr; virtual;
    function Read_Variable: VariablePtr; virtual;
    function Read_ImplicitlyQualifiedSegment: ImplicitlyQualifiedSegmentPtr; virtual;
    function Read_VariableSegment: QualifiedSegmentPtr; virtual;
    function Read_PrivatePredicativeFormula: PrivatePredicativeFormulaPtr; virtual;
    function Read_Formula: FormulaPtr; virtual;
    function Read_SimpleTerm: SimpleTermPtr; virtual;
    function Read_PrivateFunctorTerm: PrivateFunctorTermPtr; virtual;
    function Read_InternalSelectorTerm: InternalSelectorTermPtr; virtual;
    function Read_Term: TermPtr; virtual;
    function Read_TypeList: PList; virtual;
    function Read_Locus: LocusPtr; virtual;
    function Read_Loci: PList; virtual;
    function Read_ModePattern: ModePatternPtr; virtual;
    function Read_AttributePattern: AttributePatternPtr; virtual;
    function Read_FunctorPattern: FunctorPatternPtr; virtual;
    function Read_PredicatePattern: PredicatePatternPtr; virtual;
    function Read_Pattern: PatternPtr; virtual;
    function Read_Definiens: DefiniensPtr; virtual;
    function Read_ReservationSegment: ReservationSegmentPtr; virtual;
    function Read_SchemeNameInSchemeHead: SchemePtr; virtual;
    function Read_Label: LabelPtr; virtual;
    function Read_Proposition: PropositionPtr; virtual;
    function Read_CompactStatement: CompactStatementPtr; virtual;
    function Read_LocalReference: LocalReferencePtr; virtual;
    function Read_References: PList; virtual;
    function Read_StraightforwardJustification: StraightforwardJustificationPtr; virtual;
    function Read_SchemeJustification: SchemeJustificationPtr; virtual;
    function Read_Justification: JustificationPtr; virtual;
    function Read_RegularStatement(const aShape: string): RegularStatementPtr; virtual;
  end ;
```

1245. Constructor.

(Implementation for `wsmarticle.pas 1001`) \equiv
constructor *InWSMizFileObj.OpenFile*(**const** *aFileName*: *string*);
 begin *inherited OpenFile*(*aFileName*); *nDisplayInformationOnScreen* \leftarrow *false*;
 end;
destructor *InWSMizFileObj.Done*;
 begin *inherited Done*;
 end;

1246. Getting the value for an attribute. Returns **nil** if there is no attribute with the given name. (Recall (§617), an *XMLAttr* is just a wrapper around a string *nValue*.)

(Implementation for `wsmarticle.pas 1001`) \equiv
function *InWSMizFileObj.GetAttrValue*(**const** *aAttrName*: *string*): *string*;
 var *lObj*: *PObject*;
 begin *result* \leftarrow *''*; *lObj* \leftarrow *nAttrVals.ObjectOf*(*aAttrName*);
 if *lObj* \neq **nil** **then** *result* \leftarrow *XMLAttrPtr*(*lObj*) \uparrow .*nValue*;
 end;

1247. We can query for the *position* of the XML attribute.

(Implementation for `wsmarticle.pas 1001`) \equiv
function *InWSMizFileObj.GetAttrPos*: *Position*;
 var *lLine*, *lCol*: *XMLAttrPtr*; *lCode*: *integer*;
 begin *result.Line* \leftarrow 1; *result.Col* \leftarrow 1;
 lLine \leftarrow *XMLAttrPtr*(*nAttrVals.ObjectOf*(*XMLAttrName*[*atLine*]));
 lCol \leftarrow *XMLAttrPtr*(*nAttrVals.ObjectOf*(*XMLAttrName*[*atCol*]));
 if (*lLine* \neq **nil**) \wedge (*lCol* \neq **nil**) **then**
 begin *Val*(*lLine* \uparrow .*nValue*, *result.Line*, *lCode*); *Val*(*lCol* \uparrow .*nValue*, *result.Col*, *lCode*);
 end;
 end;

1248. The state of the WSM parser may be described with a handful of lookup tables.

(Implementation for `wsmarticle.pas` 1001) +≡

```

var ElemLookupTable, AttrLookupTable, BlockLookupTable, ItemLookupTable, FormulaKindLookupTable,
    TermKindLookupTable, PatternKindLookupTable, CorrectnessKindLookupTable,
    PropertyKindLookupTable: MSortedStrList;

procedure InitWSLookupTables;
var e: XMLElemKind; a: XMLAttrKind; b: BlockKind; i: ItemKind; f: FormulaSort; t: TermSort;
    p: PropertyKind; c: CorrectnessKind;
begin ElemLookupTable.Init(Ord(High(XMLElemKind)) + 1);
    AttrLookupTable.Init(Ord(High(XMLAttrKind)) + 1);
    BlockLookupTable.Init(Ord(High(BlockKind)) + 1); ItemLookupTable.Init(Ord(High(ItemKind)) + 1);
    FormulaKindLookupTable.Init(Ord(High(FormulaSort)) + 1);
    TermKindLookupTable.Init(Ord(High(TermSort)) + 1);
    PatternKindLookupTable.Init(Ord(itDefStruct) - Ord(itDefPred) + 1);
    CorrectnessKindLookupTable.Init(ord(High(CorrectnessKind)) + 1);
    PropertyKindLookupTable.Init(ord(High(PropertyKind)) + 1);
for e ← Low(XMLElemKind) to High(XMLElemKind) do
    ElemLookupTable.Insert(new(MStrPtr, Init(XMLElemName[e])));
for a ← Low(XMLAttrKind) to High(XMLAttrKind) do
    AttrLookupTable.Insert(new(MStrPtr, Init(XMLAttrName[a])));
for b ← Low(BlockKind) to High(BlockKind) do
    BlockLookupTable.Insert(new(MStrPtr, Init(BlockName[b])));
for i ← Low(ItemKind) to High(ItemKind) do
    ItemLookupTable.Insert(new(MStrPtr, Init(ItemName[i])));
for f ← Low(FormulaSort) to High(FormulaSort) do
    FormulaKindLookupTable.Insert(new(MStrPtr, Init(FormulaName[f])));
for t ← Low(TermSort) to High(TermSort) do
    TermKindLookupTable.Insert(new(MStrPtr, Init(TermName[t])));
for i ← itDefPred to itDefStruct do
    PatternKindLookupTable.Insert(new(MStrPtr, Init(DefPatternName[i])));
for p ← Low(PropertyKind) to High(PropertyKind) do
    PropertyKindLookupTable.Insert(new(MStrPtr, Init(PropertyName[p])));
for c ← Low(CorrectnessKind) to High(CorrectnessKind) do
    CorrectnessKindLookupTable.Insert(new(MStrPtr, Init(CorrectnessName[c])));
end;

```

1249. We also need to free the memory consumed by the lookup tables.

(Implementation for `wsmarticle.pas` 1001) +≡

```

procedure DisposeWSLookupTables;
begin ElemLookupTable.Done; AttrLookupTable.Done; BlockLookupTable.Done;
    ItemLookupTable.Done; FormulaKindLookupTable.Done; TermKindLookupTable.Done;
    CorrectnessKindLookupTable.Done; PropertyKindLookupTable.Done;
end;

```


1250. We can recall, from the XML dictionary module (§591), the different kinds of XML elements as specified by an enumerated constant. This converts the “nr” attribute to the human readable equivalents.

⟨Implementation for `wsmarticle.pas` 1001⟩ +≡
function *Str2XMLElemKind*(*aStr* : *string*): *XMLElemKind*;
 var *lNr*: *integer*;
 begin *lNr* ← *ElemLookupTable.IndexOfStr*(*aStr*);
 if *lNr* > −1 **then** *Str2XMLElemKind* ← *XMLElemKind*(*lNr*)
 else *Str2XMLElemKind* ← *elUnknown*;
 end;

1251. Like the previous function, this converts the “nr” attribute for a WSM Mizar attribute XML element into a human readable form.

⟨Implementation for `wsmarticle.pas` 1001⟩ +≡
function *Str2XMLAttrKind*(*aStr* : *string*): *XMLAttrKind*;
 var *lNr*: *integer*;
 begin *lNr* ← *AttrLookupTable.IndexOfStr*(*aStr*);
 if *lNr* > −1 **then** *Str2XMLAttrKind* ← *XMLAttrKind*(*lNr*)
 else *Str2XMLAttrKind* ← *atUnknown*;
 end;

1252. The “kinds” of different syntactic classes were introduced earlier in `wsmarticle.pas`, now we want to translate them into human readable form.

⟨Implementation for `wsmarticle.pas` 1001⟩ +≡
function *Str2BlockKind*(*aStr* : *string*): *BlockKind*;
 var *lNr*: *integer*;
 begin *lNr* ← *BlockLookupTable.IndexOfStr*(*aStr*);
 if *lNr* > −1 **then** *Str2BlockKind* ← *BlockKind*(*lNr*)
 else *Str2BlockKind* ← *blMain*;
 end;
function *Str2ItemKind*(*aStr* : *string*): *ItemKind*;
 var *lNr*: *integer*;
 begin *lNr* ← *ItemLookupTable.IndexOfStr*(*aStr*);
 if *lNr* > −1 **then** *Str2ItemKind* ← *ItemKind*(*lNr*)
 else *Str2ItemKind* ← *itIncorrItem*;
 end;
function *Str2PatterenKind*(*aStr* : *string*): *ItemKind*;
 var *lNr*: *integer*;
 begin *lNr* ← *PatternKindLookupTable.IndexOfStr*(*aStr*);
 if *lNr* > −1 **then** *Str2PatterenKind* ← *ItemKind*(*Ord*(*ItDefPred*) + *lNr*)
 else *Str2PatterenKind* ← *itIncorrItem*;
 end;
function *Str2FormulaKind*(*aStr* : *string*): *FormulaSort*;
 var *lNr*: *integer*;
 begin *lNr* ← *FormulaKindLookupTable.IndexOfStr*(*aStr*);
 if *lNr* > −1 **then** *Str2FormulaKind* ← *FormulaSort*(*lNr*)
 else *Str2FormulaKind* ← *wsErrorFormula*;
 end;

1253.

```

⟨Implementation for wsmarticle.pas 1001⟩ +≡
function Str2TermKind(aStr : string): TermSort;
  var lNr: integer;
  begin lNr ← TermKindLookupTable.IndexOfStr(aStr);
  if lNr > -1 then Str2TermKind ← TermSort(lNr)
  else Str2TermKind ← wsErrorTerm;
  end;

function Str2PropertyKind(aStr : string): PropertyKind;
  var lNr: integer;
  begin lNr ← PropertyKindLookupTable.IndexOfStr(aStr);
  if lNr > -1 then Str2PropertyKind ← PropertyKind(lNr)
  end;

function Str2CorrectnessKind(aStr : string): CorrectnessKind;
  var lNr: integer;
  begin lNr ← CorrectnessKindLookupTable.IndexOfStr(aStr);
  if lNr > -1 then Str2CorrectnessKind ← CorrectnessKind(lNr)
  end;

```

Subsection 21.12.1. Parsing types

1254. Reading a “term list” just iteratively invokes *Read_Term* (§1268) until all the children have been read.

```

⟨Implementation for wsmarticle.pas 1001⟩ +≡
function InWSMizFileObj.Read_TermList: PList;
  begin result ← new(PList, Init(0));
  while nState ≠ eEnd do result↑.Insert(Read_Term);
  end;

```

1255. An adjective is either “positive” (i.e., not negated) or “negative” (i.e., negated). We handle the first case in the “true” branch, and the second case in the “false” branch.

```

⟨Implementation for wsmarticle.pas 1001⟩ +≡
function InWSMizFileObj.Read_Adjective: AdjectiveExpressionPtr;
  var lAttrNr: integer; lPos: Position; lNoneOcc: Boolean;
  begin if nElName = AdjectiveSortName[wsAdjective] then
    begin lPos ← GetAttrPos; lAttrNr ← GetIntAttr(XMLAttrName[atNr]); NextElementState;
    result ← new(AdjectivePtr, Init(lPos, lAttrNr, Read_TermList)); NextElementState;
    end
  else begin lPos ← GetAttrPos; NextElementState;
    result ← new(NegatedAdjectivePtr, Init(lPos, Read_Adjective)); NextElementState;
    end;
  end;

```

1256. Reading a list of adjectives just iterates over the children of an element.

```

⟨Implementation for wsmarticle.pas 1001⟩ +≡
function InWSMizFileObj.Read_AdjectiveList: PList;
  begin result ← new(PList, Init(0)); NextElementState;
  while nState ≠ eEnd do result↑.Insert(Read_Adjective);
  NextElementState;
  end;

```

1257. There are three valid Mizar types: “standard” types, structure types, and expandable modes (i.e., a cluster of adjectives stacked atop a type). If the XML element fails to match these three, then we should produce an “incorrect type”.

```

<Implementation for wsmarticle.pas 1001> +≡
function InWSMizFileObj.Read_Type: TypePtr;
  var lList: Plist; lPos: Position; lModeSymbol: integer;
  begin if nElName = TypeName[wsStandardType] then
    begin lPos ← GetAttrPos; lModeSymbol ← GetIntAttr(XMLAttrName[atNr]); NextElementState;
    result ← new(StandardTypePtr, Init(lPos, lModeSymbol, Read_TermList)); NextElementState;
    end
  else if nElName = TypeName[wsStructureType] then
    begin lPos ← GetAttrPos; lModeSymbol ← GetIntAttr(XMLAttrName[atNr]); NextElementState;
    result ← new(StructTypePtr, Init(lPos, lModeSymbol, Read_TermList)); NextElementState;
    end
  else if nElName = TypeName[wsClusteredType] then
    begin lPos ← GetAttrPos; NextElementState; lList ← Read_AdjectiveList;
    result ← new(ClusteredTypePtr, Init(lPos, lList, Read_Type)); NextElementState;
    end
  else begin lPos ← GetAttrPos; NextElementState; result ← new(IncorrectTypePtr, Init(lPos));
    NextElementState;
  end
end;

```

Subsection 21.12.2. Parsing formulas

1258. Parsing a variable from XML just requires reading the attributes, since it is an empty-element.

```

<Implementation for wsmarticle.pas 1001> +≡
function InWSMizFileObj.Read_Variable: VariablePtr;
  var lPos: Position; lNr: integer;
  begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atIdNr]);
  NextElementState; { closes the variable's tag }
  result ← new(VariablePtr, Init(lPos, lNr));
  NextElementState; { starts the next tag }
end;

```

1259. Implicitly qualified variables are just wrappers around a variable.

```

<Implementation for wsmarticle.pas 1001> +≡
function InWSMizFileObj.Read_ImplicitlyQualifiedSegment: ImplicitlyQualifiedSegmentPtr;
  var lPos: Position;
  begin lPos ← GetAttrPos; NextElementState;
  result ← new(ImplicitlyQualifiedSegmentPtr, Init(lPos, Read_Variable)); NextElementState;
end;

```

1260. Recall (§1172) that a “qualified segment” is either implicit (i.e., a wrapper around a single variable) or explicit (i.e., an element whose children are variables and a type).

⟨Implementation for `wsmarticle.pas` 1001⟩ +≡

```
function InWSMizFileObj.Read_VariableSegment: QualifiedSegmentPtr;
  var lPos: Position; lVar: VariablePtr; lList: PList;
  begin if nElName = SegmentKindName[ikImplQualifiedSegm] then
    begin result ← Read_ImplicitlyQualifiedSegment;
    end
  else if nElName = SegmentKindName[ikExplQualifiedSegm] then
    begin lPos ← GetAttrPos; NextElementState; lList ← new(PList, Init(0));
    NextElementState; { read the variables }
    while (nState = eStart) ∧ (nElName = XMLElemName[elVariable]) do
      lList↑.Insert(Read_Variable);
    NextElementState; { read the type }
    result ← new(ExplicitlyQualifiedSegmentPtr, Init(lPos, lList, Read_Type));
    NextElementState; { start the next tag }
    end
  end;
```

1261. Private predicates are empty elements, so we only need to read their attributes.

⟨Implementation for `wsmarticle.pas` 1001⟩ +≡

```
function InWSMizFileObj.Read_PrivatePredicativeFormula: PrivatePredicativeFormulaPtr;
  var lPos: Position; lNr: integer;
  begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atIdNr]); NextElementState;
  result ← new(PrivatePredicativeFormulaPtr, Init(lPos, lNr, Read_TermList)); NextElementState;
  end;
```

1262.

⟨Implementation for `wsmarticle.pas` 1001⟩ +≡

```

function InWSMizFileObj.Read_Formula: FormulaPtr;
  var lPos: Position; lNr: integer; lList: PList; lFrm: FormulaPtr; lTrm: TermPtr;
      lSgm: QualifiedSegmentPtr;
  begin case Str2FormulaKind(nElName) of
    wsNegatedFormula: begin lPos ← GetAttrPos; NextElementState;
      result ← new(NegativeFormulaPtr, Init(lPos, Read_Formula)); NextElementState;
    end;
    ⟨Parse XML for formula with binary connective 1263⟩;
    wsFlexaryConjunctiveFormula: begin lPos ← GetAttrPos; NextElementState; lFrm ← Read_Formula;
      result ← new(FlexaryConjunctiveFormulaPtr, Init(lPos, lFrm, Read_Formula)); NextElementState;
    end;
    wsFlexaryDisjunctiveFormula: begin lPos ← GetAttrPos; NextElementState; lFrm ← Read_Formula;
      result ← new(FlexaryDisjunctiveFormulaPtr, Init(lPos, lFrm, Read_Formula)); NextElementState;
    end;
    ⟨Parse XML for predicate-based formula 1264⟩;
    wsAttributiveFormula: begin lPos ← GetAttrPos; NextElementState; lTrm ← Read_Term;
      result ← new(AttributiveFormulaPtr, Init(lPos, lTrm, Read_AdjectiveList)); NextElementState;
    end;
    wsQualifyingFormula: begin lPos ← GetAttrPos; NextElementState; lTrm ← Read_Term;
      result ← new(QualifyingFormulaPtr, Init(lPos, lTrm, Read_Type)); NextElementState;
    end;
    wsUniversalFormula: begin lPos ← GetAttrPos; NextElementState; lSgm ← Read_VariableSegment;
      result ← new(UniversalFormulaPtr, Init(lPos, lSgm, Read_Formula)); NextElementState;
    end;
    wsExistentialFormula: begin lPos ← GetAttrPos; NextElementState; lSgm ← Read_VariableSegment;
      result ← new(ExistentialFormulaPtr, Init(lPos, lSgm, Read_Formula)); NextElementState;
    end;
    wsContradiction: begin lPos ← GetAttrPos; NextElementState;
      result ← new(ContradictionFormulaPtr, Init(lPos)); NextElementState;
    end;
    wsThesis: begin lPos ← GetAttrPos; NextElementState; result ← new(ThesisFormulaPtr, Init(lPos));
      NextElementState;
    end;
    wsErrorFormula: begin lPos ← GetAttrPos; NextElementState;
      result ← new(IncorrectFormulaPtr, Init(lPos)); NextElementState;
    end;
  endcases;
end;

```

1263. For formulas with binary connectives, we read both arguments.

```

⟨ Parse XML for formula with binary connective 1263 ⟩ ≡
wsConjunctiveFormula: begin lPos ← GetAttrPos; NextElementState; lFrm ← Read_Formula;
    result ← new(ConjunctiveFormulaPtr, Init(lPos, lFrm, Read_Formula)); NextElementState;
end;
wsDisjunctiveFormula: begin lPos ← GetAttrPos; NextElementState; lFrm ← Read_Formula;
    result ← new(DisjunctiveFormulaPtr, Init(lPos, lFrm, Read_Formula)); NextElementState;
end;
wsConditionalFormula: begin lPos ← GetAttrPos; NextElementState; lFrm ← Read_Formula;
    result ← new(ConditionalFormulaPtr, Init(lPos, lFrm, Read_Formula)); NextElementState;
end;
wsBiconditionalFormula: begin lPos ← GetAttrPos; NextElementState; lFrm ← Read_Formula;
    result ← new(BiconditionalFormulaPtr, Init(lPos, lFrm, Read_Formula)); NextElementState;
end

```

This code is used in section 1262.

1264.

```

⟨ Parse XML for predicate-based formula 1264 ⟩ ≡
wsPredicativeFormula: begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]);
    NextElementState; NextElementState; { Arguments }
    lList ← Read_TermList; NextElementState; { Arguments }
    NextElementState; { Arguments }
    result ← new(PredicativeFormulaPtr, Init(lPos, lNr, lList, Read_TermList)); NextElementState;
    NextElementState;
end;
wsRightSideOfPredicativeFormula: begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]);
    NextElementState; NextElementState; { Arguments }
    result ← new(RightSideOfPredicativeFormulaPtr, Init(lPos, lNr, Read_TermList)); NextElementState;
    NextElementState;
end;
wsMultiPredicativeFormula: begin lPos ← GetAttrPos; NextElementState; lList ← new(PList, Init(0));
    while nState ≠ eEnd do lList↑.Insert(Read_Formula);
    result ← new(MultiPredicativeFormulaPtr, Init(lPos, lList)); NextElementState;
end;
wsPrivatePredicateFormula: begin result ← Read_PrivatePredicativeFormula;
end

```

This code is used in section 1262.

Subsection 21.12.3. Parsing terms**1265.**⟨ Implementation for `wsmarticle.pas 1001` ⟩ +≡

```

function InWSMizFileObj.Read_SimpleTerm: SimpleTermPtr;
  var lPos: Position; lNr: integer;
  begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atIdNr]); NextElementState;
  result ← new(SimpleTermPtr, Init(lPos, lNr)); NextElementState;
  end;

```

1266.⟨ Implementation for `wsmarticle.pas 1001` ⟩ +≡

```

function InWSMizFileObj.Read_PrivateFunctorTerm: PrivateFunctorTermPtr;
  var lPos: Position; lNr: integer;
  begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atIdNr]); NextElementState;
  result ← new(PrivateFunctorTermPtr, Init(lPos, lNr, Read_TermList)); NextElementState;
  end;

```

1267.⟨ Implementation for `wsmarticle.pas 1001` ⟩ +≡

```

function InWSMizFileObj.Read_InternalSelectorTerm: InternalSelectorTermPtr;
  var lPos: Position; lNr: integer;
  begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]); NextElementState;
  result ← new(InternalSelectorTermPtr, Init(lPos, lNr)); NextElementState;
  end;

```

1268.

(Implementation for `wsmarticle.pas` 1001) +≡

```

function InWSMizFileObj.Read_Term: TermPtr;
  var lPos, lRPos: Position; lNr, lRNR: integer; lList: PList; lTrm: TermPtr;
  begin case Str2TermKind(nElName) of
    wsPlaceholderTerm: begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]);
      NextElementState; result ← new(PlaceholderTermPtr, Init(lPos, lNr)); NextElementState;
    end;
    wsSimpleTerm: begin result ← Read_SimpleTerm;
    end;
    wsNumeralTerm: begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNumber]);
      NextElementState; result ← new(NumeralTermPtr, Init(lPos, lNr)); NextElementState;
    end;
    wsInfixTerm: begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]); NextElementState;
      NextElementState; { Arguments }
      lList ← Read_TermList; NextElementState; { Arguments }
      NextElementState; { Arguments }
      result ← new(InfixTermPtr, Init(lPos, lNr, lList, Read_TermList)); NextElementState;
      NextElementState;
    end;
    wsCircumfixTerm: begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]);
      NextElementState; NextElementState; lRNR ← GetIntAttr(XMLAttrName[atNr]);
      lRPos ← GetAttrPos; NextElementState;
      result ← new(CircumfixTermPtr, Init(lPos, lNr, lRNR, Read_TermList)); NextElementState;
    end;
    wsPrivateFunctorTerm: begin result ← Read_PrivateFunctorTerm;
    end;
    wsAggregateTerm: begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]);
      NextElementState; result ← new(AggregateTermPtr, Init(lPos, lNr, Read_TermList));
      NextElementState;
    end;
    wsSelectorTerm: begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]);
      NextElementState; result ← new(SelectorTermPtr, Init(lPos, lNr, Read_Term)); NextElementState;
    end;
    wsInternalSelectorTerm: result ← Read_InternalSelectorTerm;
    wsForgetfulFunctorTerm: begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]);
      NextElementState; result ← new(ForgetfulFunctorTermPtr, Init(lPos, lNr, Read_Term));
      NextElementState;
    end;
    wsInternalForgetfulFunctorTerm: begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]);
      NextElementState; result ← new(InternalForgetfulFunctorTermPtr, Init(lPos, lNr));
      NextElementState;
    end;
    wsFraenkelTerm: begin lPos ← GetAttrPos; NextElementState; lList ← new(PList, Init(0));
      while (nState = eStart) ∧ ((nElName = SegmentKindName[ikImplQualifiedSegm]) ∨ (nElName =
        SegmentKindName[ikExplQualifiedSegm])) do lList↑.Insert(Read_VariableSegment);
      lTrm ← Read_Term; result ← new(FraenkelTermPtr, Init(lPos, lList, lTrm, Read_Formula));
      NextElementState;
    end;
    wsSimpleFraenkelTerm: begin lPos ← GetAttrPos; NextElementState; lList ← new(PList, Init(0));
      while (nState = eStart) ∧ ((nElName = SegmentKindName[ikImplQualifiedSegm]) ∨ (nElName =
        SegmentKindName[ikExplQualifiedSegm])) do lList↑.Insert(Read_VariableSegment);

```



```

    lTrm ← Read_Term; result ← new(SimpleFraenkelTermPtr, Init(lPos, lList, lTrm));
    NextElementState;
  end;
wsQualificationTerm: begin lPos ← GetAttrPos; NextElementState; lTrm ← Read_Term;
  result ← new(QualifiedTermPtr, Init(lPos, lTrm, Read_Type)); NextElementState;
  end;
wsExactlyTerm: begin lPos ← GetAttrPos; NextElementState;
  result ← new(ExactlyTermPtr, Init(lPos, Read_Term)); NextElementState;
  end;
wsGlobalChoiceTerm: begin lPos ← GetAttrPos; NextElementState;
  result ← new(ChoiceTermPtr, Init(lPos, Read_Type)); NextElementState;
  end;
wsItTerm: begin lPos ← GetAttrPos; NextElementState; result ← new(ItTermPtr, Init(lPos));
  NextElementState;
  end;
wsErrorTerm: begin lPos ← GetAttrPos; NextElementState;
  result ← new(IncorrectTermPtr, Init(lPos)); NextElementState;
  end;
endcases;
end;

```

Subsection 21.12.4. Parsing text items

1269.

⟨Implementation for `wsmarticle.pas 1001`⟩ +≡
function *InWSMizFileObj.Read_TypeList*: *PList*;
 begin *NextElementState*; result ← new(*PList*, Init(0));
 while *nState* ≠ *eEnd* do result↑.Insert(*Read_Type*);
NextElementState;
 end;

1270.

⟨Implementation for `wsmarticle.pas 1001`⟩ +≡
function *InWSMizFileObj.Read_Locus*: *LocusPtr*;
 var *lPos*: *Position*; *lNr*: *integer*;
 begin *lPos* ← *GetAttrPos*; *lNr* ← *GetIntAttr*(*XMLAttrName*[*atIdNr*]); *NextElementState*;
 result ← new(*LocusPtr*, Init(*lPos*, *lNr*)); *NextElementState*;
 end;

1271.

⟨Implementation for `wsmarticle.pas 1001`⟩ +≡
function *InWSMizFileObj.Read_Loci*: *PList*;
 begin *NextElementState*; result ← new(*PList*, Init(0));
 while *nState* ≠ *eEnd* do result↑.Insert(*Read_Locus*);
NextElementState;
 end;

1272.

⟨Implementation for `wsmarticle.pas` 1001⟩ +≡

```
function InWSMizFileObj.Read_ModePattern: ModePatternPtr;
  var lPos: Position; lNr: integer;
  begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]); NextElementState;
  result ← new(ModePatternPtr, Init(lPos, lNr, Read_Loci)); NextElementState;
end;
```

1273.

⟨Implementation for `wsmarticle.pas` 1001⟩ +≡

```
function InWSMizFileObj.Read_AttributePattern: AttributePatternPtr;
  var lPos: Position; lNr: integer; lArg: LocusPtr;
  begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]); NextElementState;
  lArg ← Read_Locus; result ← new(AttributePatternPtr, Init(lPos, lArg, lNr, Read_Loci));
  NextElementState;
end;
```

1274.

⟨Implementation for `wsmarticle.pas` 1001⟩ +≡

```
function InWSMizFileObj.Read_FunctorPattern: FunctorPatternPtr;
  var lPos, lRPos: Position; lNr, lRNr: integer; lArgs: PList;
  begin if nState = eStart then
    if nElName = FunctorPatternName[InfixFunctor] then
      begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]); NextElementState;
      lArgs ← Read_Loci; result ← new(InfixFunctorPatternPtr, Init(lPos, lArgs, lNr, Read_Loci));
      NextElementState;
      end
    else if nElName = FunctorPatternName[CircumfixFunctor] then
      begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]); NextElementState;
      lRNr ← GetIntAttr(XMLAttrName[atNr]); NextElementState; NextElementState;
      result ← new(CircumfixFunctorPatternPtr, Init(lPos, lNr, lRNr, Read_Loci)); NextElementState;
      end;
  end;
```

1275.

⟨Implementation for `wsmarticle.pas` 1001⟩ +≡

```
function InWSMizFileObj.Read_PredicatePattern: PredicatePatternPtr;
  var lPos, lRPos: Position; lNr, lRNr: integer; lArgs: PList;
  begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]); NextElementState;
  lArgs ← Read_Loci; result ← new(PredicatePatternPtr, Init(lPos, lArgs, lNr, Read_Loci));
  NextElementState;
end;
```

1276.

⟨Implementation for `wsmarticle.pas` 1001⟩ +≡

```

function InWSMizFileObj.Read_Pattern: PatternPtr;
  begin case Str2PatterenKind(nElName) of
    itDefPred: result ← Read_PredicatePattern;
    itDefFunc: result ← Read_FunctorPattern;
    itDefMode: result ← Read_ModePattern;
    itDefAttr: result ← Read_AttributePattern;
  othercases if (nElName = FunctorPatternName[InfixFunctor]) ∨ (nElName =
    FunctorPatternName[CircumfixFunctor]) then result ← Read_FunctorPattern
  else result ← nil;
endcases;
end;

```

1277.

<Implementation for wsmarticle.pas 1001> +≡

```

function InWSMizFileObj.Read_Definiens: DefiniensPtr;
  var lPos: Position; lKind, lShape: string; lLab: LabelPtr; lExpr: PObject; lExpKind: ExpKind;
      lList: PList; lOtherwise: DefExpressionPtr;
begin result ← nil;
if (nState = eStart) ∧ (nElName = XMLElemName[elDefiniens]) then
  begin lPos ← GetAttrPos; lKind ← GetAttr(XMLAttrName[atKind]);
      lShape ← GetAttr(XMLAttrName[atShape]); NextElementState; lLab ← Read_Label;
if lKind = DefiniensKindName[SimpleDefiniens] then
  begin lExpKind ← exFormula;
      if lShape = ExpName[exTerm] then lExpKind ← exTerm;
case lExpKind of
    exTerm: lExpr ← Read_Term;
    exFormula: lExpr ← Read_Formula;
  endcases;
  result ← new(SimpleDefiniensPtr, Init(lPos, lLab, new(DefExpressionPtr, Init(lExpKind, lExpr))));
end
else begin lList ← new(PList, Init(0));
  while (nState = eStart) ∧ (nElName = XMLElemName[elPartialDefiniens]) do
    begin NextElementState; lExpKind ← exFormula;
      if lShape = ExpName[exTerm] then lExpKind ← exTerm;
case lExpKind of
      exTerm: lExpr ← Read_Term;
      exFormula: lExpr ← Read_Formula;
    endcases; lList↑.Insert(new(PartDefPtr, Init(new(DefExpressionPtr, Init(lExpKind, lExpr)),
        Read_Formula))); NextElementState;
    end;
  lOtherwise ← nil;
if nState ≠ eEnd then
    begin lExpKind ← exFormula;
      if lShape = ExpName[exTerm] then lExpKind ← exTerm;
case lExpKind of
      exTerm: lExpr ← Read_Term;
      exFormula: lExpr ← Read_Formula;
    endcases; lOtherwise ← new(DefExpressionPtr, Init(lExpKind, lExpr));
    end;
  result ← new(ConditionalDefiniensPtr, Init(lPos, lLab, lList, lOtherwise))
  end;
  NextElementState;
end;
end;

```

1278.

```

⟨Implementation for wsmarticle.pas 1001⟩ +≡
function InWSMizFileObj.Read_Label: LabelPtr;
  var lLabPos: Position; lLabId: Integer;
  begin result ← nil;
  if (nState = eStart) ∧ (nElName = XMLElemName[elLabel]) then
    begin lLabId ← GetIntAttr(XMLAttrName[atIdNr]); lLabPos ← GetAttrPos; NextElementState;
    NextElementState; result ← new(LabelPtr, Init(lLabId, lLabPos));
    end;
  end;

```

1279.

```

⟨Implementation for wsmarticle.pas 1001⟩ +≡
function InWSMizFileObj.Read_Proposition: PropositionPtr;
  var lPos: Position; lLab: LabelPtr;
  begin NextElementState; lLab ← Read_label;
  result ← new(PropositionPtr, Init(lLab, Read_Formula, lPos)); NextElementState;
  end;

```

1280.

```

⟨Implementation for wsmarticle.pas 1001⟩ +≡
function InWSMizFileObj.Read_LocalReference: LocalReferencePtr;
  var lPos: Position; lNr: integer;
  begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atIdNr]); NextElementState;
  NextElementState; result ← new(LocalReferencePtr, Init(lNr, lPos));
  end;

```

1281.

```

⟨Implementation for wsmarticle.pas 1001⟩ +≡
function InWSMizFileObj.Read_References: PList;
  var lPos: Position; lNr, lFileNr: integer;
  begin result ← new(PList, Init(0));
  while nState ≠ eEnd do
    if nElName = ReferenceKindName[LocalReference] then
      begin result↑.Insert(Read_LocalReference)
      end
    else if nElName = ReferenceKindName[TheoremReference] then
      begin lPos ← GetAttrPos; lFileNr ← GetIntAttr(XMLAttrName[atNr]);
      lNr ← GetIntAttr(XMLAttrName[atNumber]); NextElementState; NextElementState;
      result↑.Insert(new(TheoremReferencePtr, Init(lFileNr, lNr, lPos)))
      end
    else if nElName = ReferenceKindName[DefinitionReference] then
      begin lPos ← GetAttrPos; lFileNr ← GetIntAttr(XMLAttrName[atNr]);
      lNr ← GetIntAttr(XMLAttrName[atNumber]); NextElementState; NextElementState;
      result↑.Insert(new(DefinitionReferencePtr, Init(lFileNr, lNr, lPos)))
      end;
  end;

```

1282.

⟨Implementation for `wsmarticle.pas 1001`⟩ +≡

```
function InWSMizFileObj.Read_ReservationSegment: ReservationSegmentPtr;
  var lList: PList;
  begin lList ← new(PList, Init(0)); NextElementState; {elVariables}
  while (nState = eStart) ∧ (nElName = XMLElemName[elVariable]) do lList↑.Insert(Read_Variable);
  NextElementState; result ← new(ReservationSegmentPtr, Init(lList, Read_Type));
end;
```

1283.

⟨Implementation for `wsmarticle.pas 1001`⟩ +≡

```
function InWSMizFileObj.Read_SchemeNameInSchemeHead: SchemePtr;
  var lNr: Integer; lPos: Position;
  begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atIdNr]);
  result ← new(SchemePtr, Init(lNr, lPos, nil, nil, nil));
end;
```

1284.

⟨Implementation for `wsmarticle.pas 1001`⟩ +≡

```
function InWSMizFileObj.Read_CompactStatement: CompactStatementPtr;
  var lProp: PropositionPtr;
  begin lProp ← Read_Proposition; result ← new(CompactStatementPtr, Init(lProp, Read_Justification));
end;
```

1285.

⟨Implementation for `wsmarticle.pas 1001`⟩ +≡

```
function InWSMizFileObj.Read_StraightforwardJustification: StraightforwardJustificationPtr;
  var lPos, lLinkPos: Position; lLinked: boolean;
  begin lPos ← GetAttrPos; NextElementState; lLinked ← false; lLinkPos ← lPos;
  if nelName = XMLElemName[elLink] then
    begin lLinked ← true; lLinkPos ← GetAttrPos; NextElementState; NextElementState;
    end;
  result ← new(StraightforwardJustificationPtr, Init(lPos, lLinked, lLinkPos));
  StraightforwardJustificationPtr(result)↑.nReferences ← Read_References; NextElementState;
end;
```

1286.

⟨Implementation for `wsmarticle.pas 1001`⟩ +≡

```
function InWSMizFileObj.Read_SchemeJustification: SchemeJustificationPtr;
  var lInfPos, lPos: Position; lNr, lIdNr: integer;
  begin lInfPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]);
  lIdNr ← GetIntAttr(XMLAttrName[atIdNr]); lPos.Line ← GetIntAttr(XMLAttrName[atPosLine]);
  lPos.Col ← GetIntAttr(XMLAttrName[atPosCol]); NextElementState;
  result ← new(SchemeJustificationPtr, Init(lInfPos, lNr, lIdNr));
  SchemeJustificationPtr(result)↑.nSchemeInfPos ← lPos;
  SchemeJustificationPtr(result)↑.nReferences ← Read_References; NextElementState;
end;
```

1287.

⟨Implementation for `wsmarticle.pas` 1001⟩ +≡

```

function InWSMizFileObj.Read_Justification: JustificationPtr;
  var lPos: Position;
  begin if nState = eStart then
    if nElName = InferenceName[infStraightforwardJustification] then
      result ← Read_StraightforwardJustification
    else if nElName = InferenceName[infSchemeJustification] then result ← Read_SchemeJustification
    else if nElName = InferenceName[infError] then
      begin lPos ← GetAttrPos; NextElementState;
      result ← new(JustificationPtr, Init(infError, lPos)); NextElementState;
      end
    else if nElName = InferenceName[infSkippedProof] then
      begin lPos ← GetAttrPos; NextElementState;
      result ← new(JustificationPtr, Init(infSkippedProof, lPos)); NextElementState;
      end
    else result ← new(JustificationPtr, Init(infProof, CurPos));
  end;

```

1288.

⟨Implementation for `wsmarticle.pas` 1001⟩ +≡

```

function InWSMizFileObj.Read_RegularStatement(const aShape: string): RegularStatementPtr;
  var lPos: Position; lIdNr: integer; lTrm: TermPtr; lCStm: CompactStatementPtr; lLab: LabelPtr;
  begin if aShape = RegularStatementName[stDiffuseStatement] then
    begin lLab ← Read_Label; result ← new(DiffuseStatementPtr, Init(lLab, stDiffuseStatement));
    end
  else if aShape = RegularStatementName[stCompactStatement] then
    begin result ← Read_CompactStatement;
    end
  else if aShape = RegularStatementName[stIterativeEquality] then
    begin lCStm ← Read_CompactStatement; result ← new(IterativeEqualityPtr,
      Init(lCStm↑.nProp, lCStm↑.nJustification, new(PList, Init(0))));
    while (nState = eStart) ∧ (nElName = XMLElemName[elIterativeStep]) do
      begin lPos ← GetAttrPos; NextElementState; lTrm ← Read_Term;
      IterativeEqualityPtr(result)↑.nIterSteps↑.Insert(new(IterativeStepPtr, Init(lPos, lTrm,
        Read_Justification))); NextElementState;
      end;
    end;
  end;

```

1289.

⟨Implementation for `wsmarticle.pas` 1001⟩ +≡

```

procedure InWSMizFileObj.Read_ItemContentsAttr(aItem : wsItemPtr; var aShape : string);
begin aShape ← ``;
case aItem↑.nItemKind of
  itIncorrItem : ;
  itDefinition, itSchemeBlock, itSchemeHead, itTheorem, itAxiom, itReservation : ;
  itSection : ;
  itConclusion, itRegularStatement : aShape ← GetAttr(XMLAttrName[atShape]);
  itChoice, itReconsider, itPrivFuncDefinition, itPrivPredDefinition, itConstantDefinition, itGeneralization,
    itLociDeclaration, itExistentialAssumption, itExemplification, itPerCases, itCaseBlock : ;
  itCaseHead, itSupposeHead, itAssumption : ;
  itCorrCond : aItem↑.nContent ← new(CorrectnessConditionPtr, Init(CurPos,
    Str2CorrectnessKind(GetAttr(XMLAttrName[atCondition])), nil));
  itCorrectness : aItem↑.nContent ← new(CorrectnessConditionsPtr, Init(CurPos, [], nil));
  itProperty : aShape ← GetAttr(XMLAttrName[atProperty]);
  itDefFunc : aShape ← GetAttr(XMLAttrName[atShape]);
  itDefPred, itDefMode, itDefAttr, itDefStruct, itPredSynonym, itPredAntonym, itFuncNotation,
    itModeNotation, itAttrSynonym, itAttrAntonym, itCluster, itIdentify, itReduction : ;
  itPropertyRegistration : aShape ← GetAttr(XMLAttrName[atProperty]);
  itPragma : aItem↑.nContent ← new(PragmaPtr, Init(XMLToStr(GetAttr(XMLAttrName[atSpelling]))));
endcases;
end;

```


1290.

(Implementation for `wsmarticle.pas` 1001) +≡

```

procedure InWSMizFileObj.Read_ItemContents(aItem : wsItemPtr;
  const aShape: string);
var lList, lCons, lConds, lVars, lFields, lTyps, lSels: PList; lType: TypePtr; lNr: Integer;
  lVar: VariablePtr; lLocus: LocusPtr; lTrm: TermPtr; lPos, lFieldSgmPos: Position;
  lRedefinition: boolean; lPattern: PatternPtr; lDef: HowToDefine; lPropertySort: PropertyKind;
begin lPos ← CurPos;
case aItem↑.nItemKind of
  itIncorrItem: ;
  itDefinition: ;
  itSchemeBlock: ;
  itSchemeHead: begin aItem↑.nContent ← Read_SchemeNameInSchemeHead; NextElementState;
    NextElementState; NextElementState; { elSchematicVariables }
    lList ← new(PList, Init(0));
    while (nState = eStart) ∧ ((nElName = SchemeSegmentName[PredicateSegment]) ∨ (nElName =
      SchemeSegmentName[FunctorSegment])) do
      if nElName = SchemeSegmentName[PredicateSegment] then
        begin lPos ← GetAttrPos; NextElementState; lVars ← new(PList, Init(0)); NextElementState;
          { elVariables }
          while (nState = eStart) ∧ (nElName = XMLElemName[elVariable]) do
            lVars↑.Insert(Read_Variable);
            NextElementState;
            lList↑.Insert(new(PredicateSegmentPtr, Init(lPos, PredicateSegment, lVars, Read_TypeList)));
            NextElementState;
          end
        else begin lPos ← GetAttrPos; NextElementState; lVars ← new(PList, Init(0));
          NextElementState; { elVariables }
          while (nState = eStart) ∧ (nElName = XMLElemName[elVariable]) do
            lVars↑.Insert(Read_Variable);
            NextElementState; lTyps ← Read_TypeList; NextElementState;
            lList↑.Insert(new(FunctorSegmentPtr, Init(lPos, lVars, lTyps, Read_Type))); NextElementState;
            NextElementState;
          end;
          SchemePtr(aItem↑.nContent)↑.nSchemeParams ← lList; NextElementState;
          { elSchematicVariables }
          SchemePtr(aItem↑.nContent)↑.nSchemeConclusion ← Read_Formula; lConds ← new(PList, Init(0));
          if (nState = eStart) ∧ (nElName = XMLElemName[elProvisionalFormulas]) then
            begin NextElementState;
              while (nState = eStart) ∧ (nElName = XMLElemName[elProposition]) do
                lConds↑.Insert(Read_Proposition);
                NextElementState;
              end;
              SchemePtr(aItem↑.nContent)↑.nSchemePremises ← lConds;
            end;
            itTheorem: aItem↑.nContent ← Read_CompactStatement;
            itAxiom: begin end;
            itReservation: aItem↑.nContent ← Read_ReservationSegment;
            itSection: ;
            itChoice: begin lList ← new(PList, Init(0));
              while (nState = eStart) ∧ ((nElName = SegmentKindName[ikImplQualifiedSegm]) ∨ (nElName =
                SegmentKindName[ikExplQualifiedSegm])) do lList↑.Insert(Read_VariableSegment);

```

```

    NextElementState; lConds ← nil;
    if nElName = XMLElemName[elProposition] then
        begin lConds ← new(PList, Init(0));
        while (nState = eStart) ∧ (nElName = XMLElemName[elProposition]) do
            lConds↑.Insert(Read_Proposition);
        end;
        NextElementState; aItem↑.nContent ← new(ChoiceStatementPtr, Init(lList, lConds,
            SimpleJustificationPtr(Read_Justification)));
    end;
itReconsider: begin lList ← new(PList, Init(0));
    while (nState = eStart) ∧ ((nElName = XMLElemName[elEquality]) ∨ (nElName =
        XMLElemName[elVariable])) do
        if nElName = XMLElemName[elVariable] then
            lList↑.Insert(new(TypeChangePtr, Init(VariableIdentifier, Read_Variable, nil)))
        else begin NextElementState; lVar ← Read_Variable;
            lList↑.Insert(new(TypeChangePtr, Init(Equating, lVar, Read_Term))); NextElementState;
        end;
        lType ← Read_Type; aItem↑.nContent ← new(TypeChangingStatementPtr, Init(lList, lType,
            SimpleJustificationPtr(Read_Justification)));
    end;
itPrivFuncDefinition: begin lVar ← Read_Variable; lList ← Read_TypeList;
    aItem↑.nContent ← new(PrivateFunctorDefinitionPtr, Init(lVar, lList, Read_Term));
    end;
itPrivPredDefinition: begin lVar ← Read_Variable; lList ← Read_TypeList;
    aItem↑.nContent ← new(PrivatePredicateDefinitionPtr, Init(lVar, lList, Read_Formula));
    end;
itConstantDefinition: begin lVar ← Read_Variable;
    aItem↑.nContent ← new(ConstantDefinitionPtr, Init(lVar, Read_Term));
    end;
itLocDeclaration, itGeneralization: aItem↑.nContent ← Read_VariableSegment;
itPerCases: aItem↑.nContent ← Read_Justification;
itCaseBlock: ;
itCorrCond: begin CorrectnessConditionPtr(aItem↑.nContent)↑.nJustification ← Read_Justification;
    end;
itCorrectness: begin NextElementState;
    while (nState = eStart) ∧ (nElName = ItemName[itCorrectness]) do
        begin NextElementState; include(CorrectnessConditionsPtr(aItem↑.nContent)↑.nConditions,
            Str2CorrectnessKind(GetAttr(XMLAttrName[atCondition]))); NextElementState;
        end;
        NextElementState; CorrectnessConditionPtr(aItem↑.nContent)↑.nJustification ← Read_Justification;
    end;
itProperty:
    aItem↑.nContent ← new(PropertyPtr, Init(lPos, Str2PropertyKind(aShape), Read_Justification));
itConclusion, itRegularStatement: aItem↑.nContent ← Read_RegularStatement(aShape);
itCaseHead, itSupposeHead, itAssumption: if nState = eStart then
    if nElName = AssumptionKindName[SingleAssumption] then
        begin lPos ← GetAttrPos; NextElementState;
        aItem↑.nContent ← new(SingleAssumptionPtr, Init(lPos, Read_Proposition)); NextElementState;
        end
    else if nElName = AssumptionKindName[CollectiveAssumption] then
        begin lPos ← GetAttrPos; NextElementState;
        aItem↑.nContent ← new(CollectiveAssumptionPtr, Init(lPos, new(PList, Init(0))));
    end
end

```

```

    NextElementState;
    while (nState = eStart) ∧ (nElName = XMLElemName[elProposition]) do
        CollectiveAssumptionPtr(aItem↑.nContent)↑.nConditions↑.Insert(Read_Proposition);
        NextElementState; NextElementState;
    end;
itExistentialAssumption: begin aItem↑.nContent ← new(ExistentialAssumptionPtr, Init(lPos,
    new(PList, Init(0)), new(PList, Init(0))));
    while (nState = eStart) ∧ ((nElName = SegmentKindName[ikImplQualifiedSegm]) ∨ (nElName =
        SegmentKindName[ikExplQualifiedSegm])) do
        ExistentialAssumptionPtr(aItem↑.nContent)↑.nQVars↑.Insert(Read_VariableSegment);
        NextElementState;
    while (nState = eStart) ∧ (nElName = XMLElemName[elProposition]) do
        ExistentialAssumptionPtr(aItem↑.nContent)↑.nConditions↑.Insert(Read_Proposition);
        NextElementState;
    end;
itExemplification: begin lVar ← nil;
    if (nState = eStart) ∧ (nElName = XMLElemName[elVariable]) then lVar ← Read_Variable;
    lTrm ← nil;
    if nState ≠ eEnd then lTrm ← Read_Term;
    aItem↑.nContent ← new(ExamplePtr, Init(lVar, lTrm));
    end;
itDefPred: begin lRedefinition ← false;
    if (nState = eStart) ∧ (nElName = XMLElemName[elRedefine]) then
        begin NextElementState; NextElementState; lRedefinition ← true;
        end;
    lPattern ← Read_PredicatePattern; aItem↑.nContent ← new(PredicateDefinitionPtr, Init(lPos,
        lRedefinition, PredicatePatternPtr(lPattern), Read_Definiens));
    end;
itDefFunc: begin lRedefinition ← false;
    if (nState = eStart) ∧ (nElName = XMLElemName[elRedefine]) then
        begin NextElementState; NextElementState; lRedefinition ← true;
        end;
    lPattern ← Read_FunctorPattern; lType ← nil;
    if (nState = eStart) ∧ (nElName = XMLElemName[elTypeSpecification]) then
        begin NextElementState; lType ← Read_Type; NextElementState;
        end;
    if aShape = DefiningWayName[dfMeans] then lDef ← dfMeans
    else if aShape = DefiningWayName[dfEquals] then lDef ← dfEquals
    else lDef ← dfEmpty;
    case lDef of
    dfEquals: aItem↑.nContent ← new(FunctorDefinitionPtr, Init(lPos, lRedefinition,
        FunctorPatternPtr(lPattern), lType, lDef, Read_Definiens));
    dfMeans: aItem↑.nContent ← new(FunctorDefinitionPtr, Init(lPos, lRedefinition,
        FunctorPatternPtr(lPattern), lType, lDef, Read_Definiens));
    dfEmpty: aItem↑.nContent ← new(FunctorDefinitionPtr, Init(lPos, lRedefinition,
        FunctorPatternPtr(lPattern), lType, lDef, nil));
    endcases;
    end;
itDefMode: begin lRedefinition ← false;
    if (nState = eStart) ∧ (nElName = XMLElemName[elRedefine]) then
        begin NextElementState; NextElementState; lRedefinition ← true;
        end;
    end;

```

```

lPattern ← Read_ModePattern;
if (nState = eStart) ∧ (nElName = ModeDefinitionSortName[defExpandableMode]) then
  begin NextElementState; aItem↑.nContent ← new(ExpandableModeDefinitionPtr, Init(CurPos,
    ModePatternPtr(lPattern), Read_Type)); NextElementState;
  end
else if (nState = eStart) ∧ (nElName = ModeDefinitionSortName[defStandardMode]) then
  begin NextElementState; lType ← nil;
  if (nState = eStart) ∧ (nElName = XMLElemName[elTypeSpecification]) then
    begin NextElementState; lType ← Read_Type; NextElementState;
    end;
    aItem↑.nContent ← new(StandardModeDefinitionPtr, Init(CurPos, lRedefinition,
      ModePatternPtr(lPattern), lType, Read_Definiens)); NextElementState;
    end;
  end;
end;
itDefAttr: begin lRedefinition ← false;
  if (nState = eStart) ∧ (nElName = XMLElemName[elRedefine]) then
    begin NextElementState; NextElementState; lRedefinition ← true;
    end;
    lPattern ← Read_AttributePattern; aItem↑.nContent ← new(AttributeDefinitionPtr, Init(CurPos,
      lRedefinition, AttributePatternPtr(lPattern), Read_Definiens));
    end;
itDefStruct: begin NextElementState; lTyps ← new(PList, Init(0));
  while nState ≠ eEnd do lTyps↑.Insert(Read_Type);
  NextElementState; lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]);
  NextElementState; lList ← nil;
  if (nState = eStart) ∧ (nElName = XMLElemName[elLocs]) then lList ← Read_Loci;
  lFields ← new(PList, Init(0));
  while (nState = eStart) ∧ (nElName = XMLElemName[elFieldSegment]) do
    begin lFieldSgmPos ← GetAttrPos; NextElementState; lSels ← new(PList, Init(0));
    while (nState = eStart) ∧ (nElName = XMLElemName[elSelector]) do
      begin lSels↑.Insert(new(FieldSymbolPtr, Init(GetAttrPos, GetIntAttr(XMLAttrName[atNr])));
      NextElementState; NextElementState;
      end;
      lFields↑.Insert(new(FieldSegmentPtr, Init(lFieldSgmPos, lSels, Read_Type))); NextElementState;
    end;
  NextElementState;
  aItem↑.nContent ← new(StructureDefinitionPtr, Init(lPos, lTyps, lNr, lList, lFields));
  end;
itPredSynonym, itPredAntonym, itFuncNotation, itModeNotation, itAttrSynonym, itAttrAntonym: begin
  lPattern ← Read_Pattern; aItem↑.nContent ← new(NotationDeclarationPtr, Init(lPos,
    aItem↑.nItemKind, Read_Pattern, lPattern));
  end;
itCluster: if nState = eStart then
  if nElName = ClusterRegistrationName[ExistentialRegistration] then
    begin lPos ← GetAttrPos; NextElementState; lList ← Read_AdjectiveList;
    aItem↑.nContent ← new(EClusterPtr, Init(lPos, lList, Read_Type)); NextElementState;
    end
  else if nElName = ClusterRegistrationName[ConditionalRegistration] then
    begin lPos ← GetAttrPos; NextElementState; lList ← Read_AdjectiveList;
    lCons ← Read_AdjectiveList;
    aItem↑.nContent ← new(CClusterPtr, Init(lPos, lList, lCons, Read_Type)); NextElementState;
    end
  end

```

```

    else if nElName = ClusterRegistrationName[FunctorialRegistration] then
      begin lPos ← GetAttrPos; NextElementState; lTrm ← Read_Term;
      lCons ← Read_AdjectiveList; lType ← nil;
      if nState ≠ eEnd then lType ← Read_Type;
      aItem↑.nContent ← new(FClusterPtr, Init(lPos, lTrm, lCons, lType)); NextElementState;
      end;
itIdentify: begin lPattern ← Read_Pattern; aItem↑.nContent ← new(IdentifyRegistrationPtr,
  Init(lPos, Read_Pattern, lPattern, new(PList, Init(0))));
  while (nState = eStart) ∧ (nElName = XMLElemName[elLocEquality]) do
    begin lPos ← GetAttrPos; NextElementState; lLocus ← Read_Locus;
    IdentifyRegistrationPtr(aItem↑.nContent)↑.nEqLocList↑.Insert(new(LocEqualityPtr, Init(lPos,
      lLocus, Read_Locus))); NextElementState;
    end;
  end;
end;
itPropertyRegistration: begin lPropertySort ← Str2PropertyKind(aShape);
  case lPropertySort of
  sySethood: begin
    aItem↑.nContent ← new(SethoodRegistrationPtr, Init(lPos, lPropertySort, Read_Type));
    SethoodRegistrationPtr(aItem↑.nContent)↑.nJustification ← Read_Justification;
    end;
  endcases;
end;
itReduction: begin lTrm ← Read_Term;
  aItem↑.nContent ← new(ReduceRegistrationPtr, Init(lPos, Read_Term, lTrm));
  end;
itPragma: ;
endcases;
end;

```

1291.

⟨Implementation for wsmarticle.pas 1001⟩ +≡

```

function InWSMizFileObj.Read_TextProper: wsTextProperPtr;
var lPos: Position;
begin NextElementState; lPos.Line ← GetIntAttr(XMLAttrName[atLine]);
lPos.Col ← GetIntAttr(XMLAttrName[atCol]); result ← new(wsTextProperPtr,
  Init(GetAttr(XMLAttrName[atArticleID]), GetAttr(XMLAttrName[atArticleExt]), lPos));
if nDisplayInformationOnScreen then DisplayLine(result↑.nBlockPos.Line, 0);
CurPos ← result↑.nBlockPos;
if (nState = eStart) ∧ (nElName = BlockName[blMain]) then
  begin NextElementState;
  while (nState = eStart) ∧ (nElName = XMLElemName[elItem]) do
    result↑.nItems↑.Insert(Read_Item);
  end;
  NextElementState;
end;

```

1292.

(Implementation for `wsmarticle.pas 1001`) +≡

```
function InWSMizFileObj.Read_Block: wsBlockPtr;
  var lPos: Position;
  begin lPos.Line ← GetIntAttr(XMLAttrName[atLine]);
  lPos.Col ← GetIntAttr(XMLAttrName[atCol]);
  result ← new(WSBlockPtr, Init(Str2BlockKind(GetAttr(XMLAttrName[atKind])), lPos));
  if nDisplayInformationOnScreen then DisplayLine(result↑.nBlockPos.Line, 0);
  lPos.Line ← GetIntAttr(XMLAttrName[atPosLine]);
  lPos.Col ← GetIntAttr(XMLAttrName[atPosCol]); result↑.nBlockEndPos ← lPos;
  CurPos ← result↑.nBlockPos; NextElementState;
  while (nState = eStart) ∧ (nElName = XMLElemName[elItem]) do result↑.nItems↑.Insert(Read_Item);
  CurPos ← result↑.nBlockEndPos; NextElementState;
end;
```

1293.

(Implementation for `wsmarticle.pas 1001`) +≡

```
function InWSMizFileObj.Read_Item: wsItemPtr;
  var lStartTagNbr: integer; lItemKind: ItemKind; lShape: string; lPos: Position;
  begin lItemKind ← Str2ItemKind(GetAttr(XMLAttrName[atKind]));
  lPos.Line ← GetIntAttr(XMLAttrName[atLine]); lPos.Col ← GetIntAttr(XMLAttrName[atCol]);
  CurPos ← lPos;
  if nDisplayInformationOnScreen then DisplayLine(lPos.Line, 0);
  result ← new(WSItemPtr, Init(lItemKind, lPos)); lPos.Line ← GetIntAttr(XMLAttrName[atPosLine]);
  lPos.Col ← GetIntAttr(XMLAttrName[atPosCol]); result↑.nItemEndPos ← lPos;
  result↑.nContent ← nil; Read_ItemContentsAttr(result, lShape); NextElementState; lStartTagNbr ← 0;
  if nState ≠ eEnd then
    begin Read_ItemContents(result, lShape);
    if (nState = eStart) ∧ (nElName = XMLElemName[elBlock]) then result↑.nBlock ← Read_Block
    else if result↑.nContent = nil then
      begin repeat if nState = eStart then inc(lStartTagNbr)
        else dec(lStartTagNbr);
        NextElementState;
      until ((nState = eEnd) ∧ (lStartTagNbr = 0)) ∨ ((nState = eStart) ∧ (nElName =
        XMLElemName[elBlock]));
      if (nState = eStart) ∧ (nElName = XMLElemName[elBlock]) then result↑.nBlock ← Read_Block;
      end;
    end;
  CurPos ← lPos; NextElementState;
end;
```

1294.

(Implementation for `wsmarticle.pas 1001`) +≡

```
function Read_WSMizArticle(aFileName : string): wsTextProperPtr;
  var lInFile: InWSMizFilePtr;
  begin InitWSLookupTables; lInFile ← new(InWSMizFilePtr, OpenFile(aFileName));
  result ← lInFile↑.Read_TextProper; dispose(lInFile, Done); DisposeWSLookupTables;
end;
```

Section 21.13. PRETTYPRINTING WSM FILES (DEFERRED)

1295.

```

{Publicly declared types in wsmarticle.pas 999} +≡
  WSMizarPrinterPtr = ↑WSMizarPrinterObj;
  WSMizarPrinterObj = object (TXTStreamObj)
    nDisplayInformationOnScreen: boolean;
    nIndent: integer; { indenting }
    constructor OpenFile(const aFileName: string);
    destructor Done; virtual;
    procedure Print_Char(AChar : char);
    procedure Print_NewLine;
    procedure Print_Number(const aNumber: integer);
    procedure Print_String(const aString: string);
    procedure Print_Indent;
    procedure Print_TextProper(aWSTextProper : WSTextProperPtr); virtual;
    procedure Print_Item(aWSItem : WSItemPtr); virtual;
    procedure Print_SchemeNameInSchemeHead(aSch : SchemePtr); virtual;
    procedure Print_Block(aWSBlock : WSBlockPtr); virtual;
    procedure Print_Adjective(aAttr : AdjectiveExpressionPtr); virtual;
    procedure Print_AdjectiveList(aCluster : PList); virtual;
    procedure Print_Variable(aVar : VariablePtr); virtual;
    procedure Print_ImplicitlyQualifiedVariable(aSegm : ImplicitlyQualifiedSegmentPtr); virtual;
    procedure Print_VariableSegment(aSegm : QualifiedSegmentPtr); virtual;
    procedure Print_Type(aTyp : TypePtr); virtual;
    procedure Print_BinaryFormula(aFrm : BinaryFormulaPtr); virtual;
    procedure Print_PrivatePredicativeFormula(aFrm : PrivatePredicativeFormulaPtr); virtual;
    procedure Print_Formula(aFrm : FormulaPtr); virtual;
    procedure Print_OpenTermList(aTrmList : PList); virtual;
    procedure Print_TermList(aTrmList : PList); virtual;
    procedure Print_SimpleTermTerm(aTrm : SimpleTermPtr); virtual;
    procedure Print_PrivateFunctorTerm(aTrm : PrivateFunctorTermPtr); virtual;
    procedure Print_Term(aTrm : TermPtr); virtual;
    procedure Print_TypeList(aTypeList : PList); virtual;
    procedure Print_Label(aLab : LabelPtr); virtual;
    procedure Print_Reference(aRef : LocalReferencePtr); virtual;
    procedure Print_References(aRefs : PList); virtual;
    procedure Print_StraightforwardJustification(aInf : StraightforwardJustificationPtr); virtual;
    procedure Print_SchemeNameInJustification(aInf : SchemeJustificationPtr); virtual;
    procedure Print_SchemeJustification(aInf : SchemeJustificationPtr); virtual;
    procedure Print_Justification(aInf : JustificationPtr; aBlock : wsBlockPtr); virtual;
    procedure Print_Linkage; virtual;
    procedure Print_RegularStatement(aRStm : RegularStatementPtr; aBlock : wsBlockPtr); virtual;
    procedure Print_CompactStatement(aCStm : CompactStatementPtr; aBlock : wsBlockPtr); virtual;
    procedure Print_Proposition(aProp : PropositionPtr); virtual;
    procedure Print_Conditions(aCond : PList);
    procedure Print_AssumptionConditions(aCond : AssumptionPtr); virtual;
    procedure Print_Pattern(aPattern : PatternPtr); virtual;
    procedure Print_Locus(aLocus : LocusPtr); virtual;
    procedure Print_Loci(aLoci : PList); virtual;
    procedure Print_Definiens(aDef : DefiniensPtr); virtual;
    procedure Print_ReservedType(aResType : TypePtr); virtual;
  end ;

```


1296. Constructor.

⟨Implementation for `wsmarticle.pas 1001`⟩ +≡
constructor *WSMizarPrinterObj.OpenFile*(**const** *aFileName*: *string*);
 begin *inherited InitFile*(*AFileName*); *rewrite*(*nFile*); *nIndent* ← 0;
 nDisplayInformationOnScreen ← *false*;
 end;
destructor *WSMizarPrinterObj.Done*;
 begin *close*(*nFile*); *inherited Done*;
 end;

1297. ⟨Implementation for `wsmarticle.pas 1001`⟩ +≡
procedure *WSMizarPrinterObj.Print_Char*(*aChar* : *char*);
 begin *write*(*nFile*, *aChar*);
 end;

1298. ⟨Implementation for `wsmarticle.pas 1001`⟩ +≡
procedure *WSMizarPrinterObj.Print_NewLine*;
 begin *writeln*(*nFile*);
 end;

1299. ⟨Implementation for `wsmarticle.pas 1001`⟩ +≡
procedure *WSMizarPrinterObj.Print_Number*(**const** *aNumber*: *integer*);
 begin *write*(*nFile*, *aNumber*); *Print_Char*(`␣`);
 end;

1300. The comment is translated from the Polish comment “?? czy na pewno trzeba robic konwersje”, so I may be mistranslating.

⟨Implementation for `wsmarticle.pas 1001`⟩ +≡
procedure *WSMizarPrinterObj.Print_String*(**const** *aString*: *string*);
 var *i*: *integer*;
 begin *write*(*nFile*, *XMLToStr*(*aString*)); { Do you really need to do conversions? }
 Print_Char(`␣`);
 end;

1301. ⟨Implementation for `wsmarticle.pas 1001`⟩ +≡
procedure *WSMizarPrinterObj.Print_Indent*;
 var *i*: *integer*;
 begin for *i* ← 1 **to** *nIndent* **do** *Print_Char*(`␣`);
 end;

1302. ⟨Implementation for `wsmarticle.pas 1001`⟩ +≡
procedure *WSMizarPrinterObj.Print_Adjective*(*aAttr* : *AdjectiveExpressionPtr*);
 begin case *aAttr*↑.*nAdjectiveSort* **of**
 wsAdjective: **with** *AdjectivePtr*(*aAttr*)↑ **do**
 begin if *nArgs*↑.*Count* ≠ 0 **then** *Print_TermList*(*nArgs*);
 Print_String(*AttributeName*[*nAdjectiveSymbol*]);
 end;
 wsNegatedAdjective: **begin** *Print_String*(*TokenName*[*sy_Non*]);
 Print_Adjective(*NegatedAdjectivePtr*(*aAttr*)↑.*nArg*);
 end;
 endcases;
end;

1303. \langle Implementation for `wsmarticle.pas 1001` $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_AdjectiveList(aCluster : PList);
  var i: integer;
  begin with aCluster $\uparrow$  do
    for i  $\leftarrow$  0 to Count - 1 do
      begin Print_Adjective(Items $\uparrow$ [i]);
      end;
    end;

```

1304. \langle Implementation for `wsmarticle.pas 1001` $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_Variable(aVar : VariablePtr);
  begin with aVar $\uparrow$  do
    begin Print_String(IdentRepr(nIdent));
    end;
  end;

```

1305. \langle Implementation for `wsmarticle.pas 1001` $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_ImplicitlyQualifiedVariable(aSegm : ImplicitlyQualifiedSegmentPtr);
  begin Print_Variable(aSegm $\uparrow$ .nIdentifier);
  end;

```

1306. \langle Implementation for `wsmarticle.pas 1001` $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_VariableSegment(aSegm : QualifiedSegmentPtr);
  var i: integer;
  begin case aSegm $\uparrow$ .nSegmentSort of
    ikImplQualifiedSegm: Print_ImplicitlyQualifiedVariable(ImplicitlyQualifiedSegmentPtr(aSegm));
    ikExplQualifiedSegm: with ExplicitlyQualifiedSegmentPtr(aSegm) $\uparrow$  do
      begin Print_Variable(nIdentifiers.Items $\uparrow$ [0]);
      for i  $\leftarrow$  1 to nIdentifiers $\uparrow$ .Count - 1 do
        begin Print_String( $\cdot$ ,  $\cdot$ ); Print_Variable(nIdentifiers $\uparrow$ .Items $\uparrow$ [i]);
        end;
      Print_String(TokenName[sy_Be]); Print_Type(nType);
      end;
    endcases;
  end;

```

1307. \langle Implementation for `wsmarticle.pas 1001` $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_OpenTermList(aTrmList : PList);
  var i: integer;
  begin if aTrmList $\uparrow$ .Count > 0 then
    begin Print_Term(aTrmList $\uparrow$ .Items $\uparrow$ [0]);
    for i  $\leftarrow$  1 to aTrmList $\uparrow$ .Count - 1 do
      begin Print_String( $\cdot$ ,  $\cdot$ ); Print_Term(aTrmList $\uparrow$ .Items $\uparrow$ [i]);
      end;
    end;
  end;

```

1308. \langle Implementation for `wsmarticle.pas 1001` $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_TermList(aTrmList : PList);
  var i: integer;
  begin if aTrmList↑.Count > 0 then
    begin Print_String(' ( '); Print_Term(aTrmList↑.Items↑[0]);
    for i ← 1 to aTrmList↑.Count − 1 do
      begin Print_String(' , '); Print_Term(aTrmList↑.Items↑[i]);
      end;
    Print_String(' ');
    end;
  end;

```

1309. \langle Implementation for `wsmarticle.pas 1001` $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_Type(aTyp : TypePtr);
  begin with aTyp↑ do
    begin case aTyp↑.nTypeSort of
      wsStandardType: with StandardTypePtr(aTyp)↑ do
        begin if nArgs↑.Count = 0 then Print_String(ModeName[nModeSymbol])
        else begin Print_String(' ( '); Print_String(ModeName[nModeSymbol]);
          Print_String(TokenName[sy_Of]); Print_OpenTermList(nArgs); Print_String(' ');
          end;
        end;
      wsStructureType: with StructTypePtr(aTyp)↑ do
        begin if nArgs↑.Count = 0 then Print_String(StructureName[nStructSymbol])
        else begin Print_String(' ( '); Print_String(StructureName[nStructSymbol]);
          Print_String(TokenName[sy_Over]); Print_OpenTermList(nArgs); Print_String(' ');
          end;
        end;
      wsClusteredType: with ClusteredTypePtr(aTyp)↑ do
        begin Print_AdjectiveList(nAdjectiveCluster); Print_Type(nType);
        end;
      wsErrorType: begin end;
    endcases;
  end;

```

1310. \langle Implementation for `wsmarticle.pas 1001` $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_BinaryFormula(aFrm : BinaryFormulaPtr);
  begin Print_String(' ( '); Print_Formula(aFrm↑.nLeftArg);
  case aFrm↑.nFormulaSort of
    wsConjunctiveFormula: Print_String(TokenName[sy_Ampersand]);
    wsDisjunctiveFormula: Print_String(TokenName[sy_Or]);
    wsConditionalFormula: Print_String(TokenName[sy_Implies]);
    wsBiconditionalFormula: Print_String(TokenName[sy_Iff]);
    wsFlexaryConjunctiveFormula: begin Print_String(TokenName[sy_Ampersand]);
      Print_String(TokenName[sy_Ellipsis]); Print_String(TokenName[sy_Ampersand]);
      end;
    wsFlexaryDisjunctiveFormula: begin Print_String(TokenName[sy_Or]);
      Print_String(TokenName[sy_Ellipsis]); Print_String(TokenName[sy_Or]);
      end;
  endcases; Print_Formula(aFrm↑.nRightArg); Print_String(' ');
  end;

```

1311. \langle Implementation for `wsmarticle.pas` 1001 $\rangle + \equiv$

```
procedure WSMizarPrinterObj.Print_PrivatePredicativeFormula(aFrm : PrivatePredicativeFormulaPtr);
begin with PrivatePredicativeFormulaPtr(aFrm) $\uparrow$  do
  begin Print_String(IdentRepr(nPredIdNr)); Print_String( $\wedge$  [ $\wedge$ ]; Print_OpenTermList(nArgs);
    Print_String( $\wedge$   $\wedge$ );
  end;
end;
```

1312. \langle Implementation for `wsmarticle.pas` 1001 $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_Formula(aFrm : FormulaPtr);
  var i: Integer; lNeg: boolean; lFrm: FormulaPtr;
  begin case aFrm↑.nFormulaSort of
    wsNegatedFormula: begin Print_String(TokenName[sy_Not]);
      Print_Formula(NegativeFormulaPtr(aFrm)↑.nArg);
    end;
    wsConjunctiveFormula, wsDisjunctiveFormula, wsConditionalFormula,
      wsBiconditionalFormula, wsFlexaryConjunctiveFormula, wsFlexaryDisjunctiveFormula:
      Print_BinaryFormula(BinaryFormulaPtr(aFrm));
    wsPredicativeFormula: with PredicativeFormulaPtr(aFrm)↑ do
      begin Print_String(`(`);
      if nLeftArgs↑.Count  $\neq$  0 then
        begin Print_OpenTermList(nLeftArgs);
        end;
        Print_String(PredicateName[nPredNr]);
      if nRightArgs↑.Count  $\neq$  0 then
        begin Print_OpenTermList(nRightArgs);
        end;
        Print_String(`)`);
      end;
    wsMultiPredicativeFormula: with MultiPredicativeFormulaPtr(aFrm)↑ do
      begin Print_String(`(`); lFrm ← nScraps.Items↑[0];
      lNeg ← lFrm↑.nFormulaSort = wsNegatedFormula;
      if lNeg then lFrm ← NegativeFormulaPtr(lFrm)↑.nArg;
      with PredicativeFormulaPtr(lFrm)↑ do
        begin if nLeftArgs↑.Count  $\neq$  0 then Print_OpenTermList(nLeftArgs);
        if lNeg then
          begin Print_String(TokenName[sy_Does]); Print_String(TokenName[sy_Not]);
          end;
          Print_String(PredicateName[nPredNr]);
          if nRightArgs↑.Count  $\neq$  0 then Print_OpenTermList(nRightArgs);
          end;
        for i ← 1 to nScraps.Count − 1 do
          begin lFrm ← nScraps.Items↑[i]; lNeg ← lFrm↑.nFormulaSort = wsNegatedFormula;
          if lNeg then lFrm ← NegativeFormulaPtr(lFrm)↑.nArg;
          with RightSideOfPredicativeFormulaPtr(lFrm)↑ do
            begin if lNeg then
              begin Print_String(TokenName[sy_Does]); Print_String(TokenName[sy_Not]);
              end;
              Print_String(PredicateName[nPredNr]);
              if nRightArgs↑.Count  $\neq$  0 then Print_OpenTermList(nRightArgs);
              end;
            end;
            Print_String(`)`);
          end;
        end;
      end;
    wsPrivatePredicateFormula: Print_PrivatePredicativeFormula(PrivatePredicativeFormulaPtr(aFrm));
    wsAttributiveFormula: with AttributiveFormulaPtr(aFrm)↑ do
      begin Print_String(`(`); Print_Term(nSubject); Print_String(TokenName[sy_Is]);
      Print_AdjectiveList(nAdjectives); Print_String(`)`);
      end;
    wsQualifyingFormula: with QualifyingFormulaPtr(aFrm)↑ do

```

```

begin Print_String(`(`); Print_Term(nSubject); Print_String(TokenName[sy_Is]);
Print_Type(nType); Print_String(`)`);
end;
wsUniversalFormula: with QuantifiedFormulaPtr(aFrm)↑ do
begin Print_String(`(`); Print_String(TokenName[sy_For]);
Print_VariableSegment(QuantifiedFormulaPtr(aFrm)↑.nSegment);
Print_String(TokenName[sy_Holds]); Print_Formula(QuantifiedFormulaPtr(aFrm)↑.nScope);
Print_String(`)`);
end;
wsExistentialFormula: with QuantifiedFormulaPtr(aFrm)↑ do
begin Print_String(`(`); Print_String(TokenName[sy_Ex]);
Print_VariableSegment(QuantifiedFormulaPtr(aFrm)↑.nSegment); Print_String(TokenName[sy_St]);
Print_Formula(QuantifiedFormulaPtr(aFrm)↑.nScope); Print_String(`)`);
end;
wsContradiction: begin Print_String(TokenName[sy_Contradiction]);
end;
wsThesis: begin Print_String(TokenName[sy_Thesis]);
end;
wsErrorFormula: begin end;
endcases;
end;

```

1313. ⟨Implementation for `wsmarticle.pas` 1001⟩ +≡

```

procedure WSMizarPrinterObj.Print_SimpleTermTerm(aTrm : SimpleTermPtr);
begin Print_String(IdentRepr(SimpleTermPtr(aTrm)↑.nIdent));
end;

```

1314. ⟨Implementation for `wsmarticle.pas` 1001⟩ +≡

```

procedure WSMizarPrinterObj.Print_PrivateFunctorTerm(aTrm : PrivateFunctorTermPtr);
begin Print_String(IdentRepr(aTrm↑.nFunctorIdent)); Print_String(`(`);
Print_OpenTermList(aTrm↑.nArgs); Print_String(`)`);
end;

```

```

1315.  ⟨Implementation for wsmarticle.pas 1001⟩ +≡
procedure WSMizarPrinterObj.Print_Term(aTrm : TermPtr);
  var i, j: integer; lPrintWhere: boolean;
  begin case aTrm↑.nTermSort of
    wsPlaceholderTerm: begin Print_Char( '$' ); Print_Number( PlaceholderTermPtr(aTrm)↑.nLocusNr );
      end;
    wsSimpleTerm: begin Print_SimpleTermTerm( SimpleTermPtr(aTrm) );
      end;
    wsNumeralTerm: begin Print_Number( NumeralTermPtr(aTrm)↑.nValue );
      end;
    wsInfixTerm: with InfixTermPtr(aTrm)↑ do
      begin Print_String( '(' );
      if nLeftArgs↑.Count ≠ 0 then
        begin Print_TermList( nLeftArgs );
        end;
      Print_String( FunctorName[ nFunctorSymbol ] );
      if nRightArgs↑.Count ≠ 0 then
        begin Print_TermList( nRightArgs );
        end;
      Print_String( ')' );
      end;
    wsCircumfixTerm: with CircumfixTermPtr(aTrm)↑ do
      begin Print_String( LeftBracketName[ nLeftBracketSymbol ] ); Print_OpenTermList( nArgs );
      Print_String( RightBracketName[ nRightBracketSymbol ] );
      end;
    wsPrivateFunctorTerm: Print_PrivateFunctorTerm( PrivateFunctorTermPtr(aTrm) );
    wsAggregateTerm: with AggregateTermPtr(aTrm)↑ do
      begin Print_String( StructureName[ nStructSymbol ] );
      Print_String( TokenName[ sy_StructLeftBracket ] ); Print_OpenTermList( nArgs );
      Print_String( TokenName[ sy_StructRightBracket ] );
      end;
    wsSelectorTerm: with SelectorTermPtr(aTrm)↑ do
      begin Print_String( '(' ); Print_String( TokenName[ sy_The ] );
      Print_String( SelectorName[ nSelectorSymbol ] ); Print_String( TokenName[ sy_Of ] );
      Print_Term( nArg ); Print_String( ')' );
      end;
    wsInternalSelectorTerm: with InternalSelectorTermPtr(aTrm)↑ do
      begin Print_String( TokenName[ sy_The ] ); Print_String( SelectorName[ nSelectorSymbol ] );
      end;
    wsForgetfulFunctorTerm: with ForgetfulFunctorTermPtr(aTrm)↑ do
      begin Print_String( '(' ); Print_String( TokenName[ sy_The ] );
      Print_String( StructureName[ nStructSymbol ] ); Print_String( TokenName[ sy_Of ] );
      Print_Term( nArg ); Print_String( ')' );
      end;
    wsInternalForgetfulFunctorTerm: with InternalForgetfulFunctorTermPtr(aTrm)↑ do
      begin Print_String( '(' ); Print_String( TokenName[ sy_The ] );
      Print_String( StructureName[ nStructSymbol ] ); Print_String( ')' );
      end;
    wsFraenkelTerm: with FraenkelTermPtr(aTrm)↑ do
      begin Print_String( '{' ); Print_Term( nSample );
      if nPostqualification↑.Count > 0 then
        begin lPrintWhere ← true;

```

```

for  $i \leftarrow 0$  to  $nPostqualification \uparrow .Count - 1$  do
  case  $QualifiedSegmentPtr(nPostqualification \uparrow .Items \uparrow [i]) \uparrow .nSegmentSort$  of
     $ikImplQualifiedSegm$ : with  $ImplicitlyQualifiedSegmentPtr(nPostqualification \uparrow .Items \uparrow [i]) \uparrow$  do
      begin  $Print\_String(TokenName[sy\_Where])$ ;  $Print\_Variable(nIdentifier)$ ;
      end;
     $ikExplQualifiedSegm$ : with  $ExplicitlyQualifiedSegmentPtr(nPostqualification \uparrow .Items \uparrow [i]) \uparrow$  do
      begin if  $lPrintWhere$  then
        begin  $Print\_String(TokenName[sy\_Where])$ ;  $lPrintWhere \leftarrow false$ ;
        end;
       $Print\_Variable(nIdentifiers.Items \uparrow [0])$ ;
      for  $j \leftarrow 1$  to  $nIdentifiers \uparrow .Count - 1$  do
        begin  $Print\_String(' , ')$ ;  $Print\_Variable(nIdentifiers \uparrow .Items \uparrow [j])$ ;
        end;
       $Print\_String(TokenName[sy\_Is])$ ;  $Print\_Type(nType)$ ;
      if  $i < nPostqualification \uparrow .Count - 1$  then  $Print\_String(' , ')$ ;
      end;
    endcases;
  end;
   $Print\_String(' : ')$ ;  $Print\_Formula(nFormula)$ ;  $Print\_String(' } ')$ ;
end;
 $wsSimpleFraenkelTerm$ : with  $SimpleFraenkelTermPtr(aTrm) \uparrow$  do
  begin  $Print\_String(' ( ')$ ;  $Print\_String(TokenName[sy\_The])$ ;  $Print\_String(TokenName[sy\_Set])$ ;
   $Print\_String(TokenName[sy\_Of])$ ;  $Print\_String(TokenName[sy\_All])$ ;  $Print\_Term(nSample)$ ;
  if  $nPostqualification \uparrow .Count > 0$  then
    begin  $lPrintWhere \leftarrow true$ ;
    for  $i \leftarrow 0$  to  $nPostqualification \uparrow .Count - 1$  do
      case  $QualifiedSegmentPtr(nPostqualification \uparrow .Items \uparrow [i]) \uparrow .nSegmentSort$  of
         $ikImplQualifiedSegm$ : with  $ImplicitlyQualifiedSegmentPtr(nPostqualification \uparrow .Items \uparrow [i]) \uparrow$  do
          begin  $Print\_String(TokenName[sy\_Where])$ ;  $Print\_Variable(nIdentifier)$ ;
          end;
         $ikExplQualifiedSegm$ : with  $ExplicitlyQualifiedSegmentPtr(nPostqualification \uparrow .Items \uparrow [i]) \uparrow$  do
          begin if  $lPrintWhere$  then
            begin  $Print\_String(TokenName[sy\_Where])$ ;  $lPrintWhere \leftarrow false$ ;
            end;
           $Print\_Variable(nIdentifiers.Items \uparrow [0])$ ;
          for  $j \leftarrow 1$  to  $nIdentifiers \uparrow .Count - 1$  do
            begin  $Print\_String(' , ')$ ;  $Print\_Variable(nIdentifiers \uparrow .Items \uparrow [j])$ ;
            end;
           $Print\_String(TokenName[sy\_Is])$ ;  $Print\_Type(nType)$ ;
          if  $i < nPostqualification \uparrow .Count - 1$  then  $Print\_String(' , ')$ ;
          end;
        endcases;
      end;
     $Print\_String(' ) ')$ ;
  end;
 $wsQualificationTerm$ : with  $QualifiedTermPtr(aTrm) \uparrow$  do
  begin  $Print\_String(' ( ')$ ;  $Print\_Term(nSubject)$ ;  $Print\_String(TokenName[sy\_Qua])$ ;
   $Print\_Type(nQualification)$ ;  $Print\_String(' ) ')$ ;
  end;
 $wsExactlyTerm$ : with  $ExactlyTermPtr(aTrm) \uparrow$  do
  begin  $Print\_Term(nSubject)$ ;  $Print\_String(TokenName[sy\_Exactly])$ ;
  end;

```



```

wsGlobalChoiceTerm: begin Print_String(` `); Print_String(TokenName[sy_The]);
  Print_Type(ChoiceTermPtr(aTrm)↑.nChoiceType); Print_String(` `);
end;
wsItTerm: begin Print_String(TokenName[sy_It]);
end;
wsErrorTerm:
endcases;
end;

```

1316. ⟨Implementation for `wsmarticle.pas 1001`⟩ +≡
procedure WSMizarPrinterObj.Print_TypeList(aTypeList : PList);
 var i: integer;
begin if aTypeList↑.Count > 0 **then**
 begin Print_Type(aTypeList↑.Items↑[0]);
 for i ← 1 **to** aTypeList↑.Count - 1 **do**
 begin Print_String(` , `); Print_Type(aTypeList↑.Items↑[i]);
 end;
 end;
end;
end;

1317. ⟨Implementation for `wsmarticle.pas 1001`⟩ +≡
procedure WSMizarPrinterObj.Print_Label(aLab : LabelPtr);
begin if (aLab ≠ nil) ∧ (aLab.nLabelIdNr > 0) **then**
 begin Print_String(IdentRepr(aLab↑.nLabelIdNr)); Print_String(` : `);
 end;
end;

1318. ⟨Implementation for `wsmarticle.pas 1001`⟩ +≡
procedure WSMizarPrinterObj.Print_Proposition(aProp : PropositionPtr);
begin Print_Label(aProp↑.nLab); Print_Formula(aProp↑.nSentence);
end;

1319. ⟨Implementation for `wsmarticle.pas 1001`⟩ +≡
procedure WSMizarPrinterObj.Print_CompactStatement(aCStm : CompactStatementPtr;
 aBlock : wsBlockPtr);
begin with aCStm↑ **do**
 begin Print_Proposition(nProp); Print_Justification(nJustification, aBlock);
 end;
end;

1320. ⟨Implementation for `wsmarticle.pas 1001`⟩ +≡
procedure WSMizarPrinterObj.Print_Linkage;
begin Print_String(TokenName[sy_Then]);
end;

1321. \langle Implementation for `wsmarticle.pas 1001` $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_RegularStatement(aRStm : RegularStatementPtr;
  aBlock : wsBlockPtr);
  var i: integer;
  begin case aRStm↑.nStatementSort of
    stDiffuseStatement: begin Print_Label(DiffuseStatementPtr(aRStm)↑.nLab); Print_Block(aBlock);
      end;
    stCompactStatement: begin
      if (CompactStatementPtr(aRStm)↑.nJustification↑.nInfSort = infStraightforwardJustification) ∧
        StraightforwardJustificationPtr(CompactStatementPtr(aRStm)↑.nJustification)↑.nLinked then
        begin Print_Linkage;
          end;
        Print_CompactStatement(CompactStatementPtr(aRStm), aBlock);
      end;
    stIterativeEquality: begin
      if (CompactStatementPtr(aRStm)↑.nJustification↑.nInfSort = infStraightforwardJustification) ∧
        StraightforwardJustificationPtr(CompactStatementPtr(aRStm)↑.nJustification)↑.nLinked then
        begin Print_Linkage;
          end;
        Print_CompactStatement(CompactStatementPtr(aRStm), nil);
      with IterativeEqualityPtr(aRStm)↑ do
        for i ← 0 to nIterSteps↑.Count − 1 do
          with IterativeStepPtr(nIterSteps↑.Items↑[i])↑ do
            begin Print_NewLine; Print_String(TokenName[sy_DotEquals]); Print_Term(nTerm);
              Print_Justification(nJustification, nil);
            end;
          end;
        end;
      endcases;
    end;

```

1322. \langle Implementation for `wsmarticle.pas 1001` $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_Reference(aRef : LocalReferencePtr);
  begin Print_String(IdentRepr(aRef↑.nLabId));
  end;

```

1323. \langle Implementation for `wsmarticle.pas 1001` $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_References(aRefs : PList);
  var i: integer;
  begin for i  $\leftarrow$  0 to aRefs↑.Count - 1 do
    with ReferencePtr(aRefs↑.Items↑[i])↑ do
      begin case nRefSort of
        LocalReference: begin Print_Reference(aRefs↑.Items↑[i]);
          end;
        TheoremReference: begin
          Print_String(MMLIdentifierName[TheoremReferencePtr(aRefs↑.Items↑[i])↑.nArticleNr]);
          Print_String(': '); Print_Number(TheoremReferencePtr(aRefs↑.Items↑[i])↑.nTheoNr);
          end;
        DefinitionReference: begin
          Print_String(MMLIdentifierName[DefinitionReferencePtr(aRefs↑.Items↑[i])↑.nArticleNr]);
          Print_String(': '); Print_String('def ');
          Print_Number(DefinitionReferencePtr(aRefs↑.Items↑[i])↑.nDEfNr);
          end;
        endcases;
        if i < aRefs↑.Count - 1 then Print_String(',');
        end;
      end;
  end;

```

1324. \langle Implementation for `wsmarticle.pas 1001` $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_StraightforwardJustification(aInf : StraightforwardJustificationPtr);
  begin with aInf↑ do
    begin if nReferences↑.Count  $\neq$  0 then
      begin Print_String(TokenName[sy_By]); Print_References(nReferences);
      end;
    end;
  end;

```

1325. \langle Implementation for `wsmarticle.pas 1001` $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_SchemeNameInJustification(aInf : SchemeJustificationPtr);
  begin Print_String(IdentRepr(aInf↑.nSchemeIdNr));
  end;

```

1326. \langle Implementation for `wsmarticle.pas 1001` $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_SchemeJustification(aInf : SchemeJustificationPtr);
  begin with aInf↑ do
    begin Print_String(TokenName[sy_From]);
    if nSchFileNr > 0 then
      begin Print_String(MMLIdentifierName[nSchFileNr]); Print_String(': '); Print_String('sch ');
      Print_Number(nSchemeIdNr);
      end
    else if nSchemeIdNr > 0 then Print_SchemeNameInJustification(aInf);
    if nReferences↑.Count > 0 then
      begin Print_String( '('); Print_References(nReferences); Print_String( ')');
      end;
    end;
  end;

```

1327. \langle Implementation for `wsmarticle.pas 1001` $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_Justification(aInf : JustificationPtr; aBlock : wsBlockPtr);
  begin case aInf↑.nInfSort of
    infStraightforwardJustification: Print_StraightforwardJustification(StraightforwardJustificationPtr(aInf));
    infSchemeJustification: Print_SchemeJustification(SchemeJustificationPtr(aInf));
    infError, infSkippedProof: begin end;
    infProof: Print_Block(aBlock);
  endcases;
end;

```

1328. \langle Implementation for `wsmarticle.pas 1001` $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_Conditions(aCond : PList);
  var i: integer;
  begin Print_String(TokenName[sy_That]); Print_NewLine; Print_Proposition(aCond↑.Items↑[0]);
  for i ← 1 to aCond↑.Count − 1 do
    begin Print_String(TokenName[sy_And]); Print_NewLine; Print_Proposition(aCond↑.Items↑[i]);
    end;
  end;

```

1329. \langle Implementation for `wsmarticle.pas 1001` $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_AssumptionConditions(aCond : AssumptionPtr);
  begin case aCond↑.nAssumptionSort of
    SingleAssumption: begin Print_Proposition(SingleAssumptionPtr(aCond)↑.nProp);
    end;
    CollectiveAssumption: begin Print_Conditions(CollectiveAssumptionPtr(aCond)↑.nConditions);
    end;
  endcases;
end;

```

1330. \langle Implementation for `wsmarticle.pas 1001` $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_Locus(aLocus : LocusPtr);
  begin with aLocus↑ do
    begin Print_String(IdentRepr(nVarId));
    end;
  end;

```

1331. \langle Implementation for `wsmarticle.pas 1001` $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_Loci(aLoci : PList);
  var i: integer;
  begin if (aLoci = nil)  $\vee$  (aLoci↑.Count = 0) then
  else begin Print_Locus(aLoci↑.Items↑[0]);
    for i ← 1 to aLoci↑.Count − 1 do
      begin Print_String(`, `); Print_Locus(aLoci↑.Items↑[i]);
      end;
    end;
  end;

```

1332. \langle Implementation for `wsmarticle.pas` 1001 $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_Pattern(aPattern : PatternPtr);
  begin case aPattern↑.nPatternSort of
    itDefPred: with PredicatePatternPtr(aPattern)↑ do
      begin Print_Loci(nLeftArgs); Print_String(PredicateName[nPredSymbol]); Print_Loci(nRightArgs);
      end;
    itDefFunc: begin case FunctorPatternPtr(aPattern)↑.nFuncKind of
      InfixFunctor: with InfixFunctorPatternPtr(aPattern)↑ do
        begin if (nLeftArgs ≠ nil) ∧ (nLeftArgs↑.Count > 1) then Print_String('(');
        Print_Loci(nLeftArgs);
        if (nLeftArgs ≠ nil) ∧ (nLeftArgs↑.Count > 1) then Print_String(' ');
        Print_String(FunctorName[nOperSymb]);
        if (nRightArgs ≠ nil) ∧ (nRightArgs↑.Count > 1) then Print_String('(');
        Print_Loci(nRightArgs);
        if (nRightArgs ≠ nil) ∧ (nRightArgs↑.Count > 1) then Print_String(' ');
        end;
      CircumfixFunctor: with CircumfixFunctorPatternPtr(aPattern)↑ do
        begin Print_String(LeftBracketName[nLeftBracketSymb]); Print_Loci(nArgs);
        Print_String(RightBracketName[nRightBracketSymb]);
        end;
    endcases;
  end;
  itDefMode: with ModePatternPtr(aPattern)↑ do
    begin Print_String(ModeName[nModeSymbol]);
    if (nArgs ≠ nil) ∧ (nArgs↑.Count > 0) then
      begin Print_String(TokenName[sy_Of]); Print_Loci(nArgs);
      end;
    end;
  itDefAttr: with AttributePatternPtr(aPattern)↑ do
    begin Print_Locus(nArg); Print_String(TokenName[sy_Is]); Print_Loci(nArgs);
    Print_String(AttributeName[nAttrSymbol]);
    end;
  endcases;
end;

```

1333. $\langle \text{Implementation for } \text{wsmarticle.pas } 1001 \rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_Definiens(aDef : DefiniensPtr);
  var i: integer;
  begin if aDef  $\neq$  nil then
    with DefiniensPtr(aDef) $\uparrow$  do
      begin case nDefSort of
        SimpleDefiniens: begin if (nDefLabel  $\neq$  nil)  $\wedge$  (nDefLabel $\uparrow$ .nLabelIdNr > 0) then
          begin Print_String(' '); Print_Label(nDefLabel);
          end;
          with SimpleDefiniensPtr(aDef) $\uparrow$ , nExpression $\uparrow$  do
            case nExprKind of
              exTerm: Print_Term(TermPtr(nExpr));
              exFormula: Print_Formula(FormulaPtr(nExpr));
            endcases;
          end;
        ConditionalDefiniens: begin if (nDefLabel  $\neq$  nil)  $\wedge$  (nDefLabel $\uparrow$ .nLabelIdNr > 0) then
          begin Print_String(' '); Print_Label(nDefLabel);
          end;
          with ConditionalDefiniensPtr(aDef) $\uparrow$  do
            begin for i  $\leftarrow$  0 to nConditionalDefiniensList $\uparrow$ .Count - 1 do
              begin with PartDefPtr(nConditionalDefiniensList $\uparrow$ .Items $\uparrow$ [i]) $\uparrow$  do
                begin with nPartDefiniens $\uparrow$  do
                  case nExprKind of
                    exTerm: Print_Term(TermPtr(nExpr));
                    exFormula: Print_Formula(FormulaPtr(nExpr));
                  endcases;
                  Print_String(TokenName[sy_If]); Print_Formula(nGuard);
                end;
              if (i  $\geq$  0)  $\wedge$  (i < nConditionalDefiniensList $\uparrow$ .Count - 1) then
                begin Print_String(' '); Print_NewLine;
                end;
              end;
            if nOtherwise  $\neq$  nil then
              with nOtherwise $\uparrow$  do
                begin Print_String(TokenName[sy_Otherwise]);
                case nExprKind of
                  exTerm: Print_Term(TermPtr(nExpr));
                  exFormula: Print_Formula(FormulaPtr(nExpr));
                endcases;
              end;
            end;
          end;
        end;
      endcases;
    end;
  end;

```

1334. \langle Implementation for `wsmarticle.pas 1001` $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_Block(aWSBlock : WSBlockPtr);
  var i, lIndent: integer;
  begin with aWSBlock↑ do
    begin lIndent  $\leftarrow$  nIndent; Print_NewLine; Print_Indent;
    case nBlockKind of
      blDiffuse: begin Print_String(TokenName[sy_Now]); Print_NewLine;
        end;
      blHereby: begin Print_String(TokenName[sy_Now]); Print_NewLine;
        end;
      blProof: begin Print_String(TokenName[sy_Proof]); Print_NewLine;
        end;
      blDefinition: begin Print_String(TokenName[sy_Definition]); Print_NewLine;
        end;
      blNotation: begin Print_String(TokenName[sy_Notation]); Print_NewLine;
        end;
      blRegistration: begin Print_String(TokenName[sy_Registration]); Print_NewLine;
        end;
      blCase: Print_String(TokenName[sy_Case]);
      blSuppose: Print_String(TokenName[sy_Suppose]);
      blPublicScheme: ;
    endcases;
    for i  $\leftarrow$  0 to nItems↑.Count - 1 do
      begin Print_Item(nItems↑.Items↑[i]);
      end;
    nIndent  $\leftarrow$  lIndent; Print_Indent; Print_String(TokenName[sy_End]);
    end;
  end;

```

1335. \langle Implementation for `wsmarticle.pas 1001` $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_TextProper(aWSTextProper : WSTextProperPtr);
  var i: integer;
  begin with aWSTextProper↑ do
    begin for i  $\leftarrow$  0 to nItems↑.Count - 1 do Print_Item(nItems↑.Items↑[i]);
    end;
  end;

```

1336. \langle Implementation for `wsmarticle.pas 1001` $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_ReservedType(aResType : TypePtr);
  begin Print_Type(aResType);
  end;

```

1337. \langle Implementation for `wsmarticle.pas 1001` $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_SchemeNameInSchemeHead(aSch : SchemePtr);
  begin Print_String(IdentRepr(aSch↑.nSchemeIdNr));
  end;

```

```

1338. ⟨Implementation for wsmarticle.pas 1001⟩ +≡
procedure WSMizarPrinterObj.Print_Item(aWSItem : WSItemPtr);
  var i, j, lindent: integer;
begin with aWSItem↑ do
  begin CurPos ← nItemPos;
  if nDisplayInformationOnScreen then DisplayLine(CurPos.Line, ErrorNbr);
  case nItemKind of
  itDefinition: begin Print_Block(nBlock); Print_String(' '); Print_NewLine;
    end;
  itSchemeBlock: begin Print_Block(nBlock); Print_String(' '); Print_NewLine;
    end;
  itSchemeHead: with SchemePtr(nContent)↑ do
    begin Print_String(TokenName[sy_Scheme]);
    Print_SchemeNameInSchemeHead(SchemePtr(nContent)); Print_String('{ ');
    for j ← 0 to nSchemeParams↑.Count - 1 do
      begin case SchemeSegmentPtr(nSchemeParams↑.Items↑[j])↑.nSegmSort of
      PredicateSegment: with PredicateSegmentPtr(nSchemeParams↑.Items↑[j])↑ do
        begin Print_Variable(nVars↑.Items↑[0]);
        for i ← 1 to nVars↑.Count - 1 do
          begin Print_String(' '); Print_Variable(nVars↑.Items↑[i]);
            end;
        Print_String(' [ '); Print_TypeList(nTypeExpList); Print_String(' ] ');
        end;
      FunctorSegment: with FunctorSegmentPtr(nSchemeParams↑.Items↑[j])↑ do
        begin Print_Variable(nVars↑.Items↑[0]);
        for i ← 1 to nVars.Count - 1 do
          begin Print_String(' '); Print_Variable(nVars↑.Items↑[i]);
            end;
        Print_String(' ( '); Print_TypeList(nTypeExpList); Print_String(' ) ');
        Print_String(TokenName[sy_Arrow]); Print_Type(nSpecification);
        end;
      endcases;
    if (j ≥ 0) ∧ (j < nSchemeParams↑.Count - 1) then Print_String(' ');
    end;
    Print_String(' } '); Print_String(': '); Print_Newline; Print_Formula(nSchemeConclusion);
    Print_NewLine;
  if (nSchemePremises ≠ nil) ∧ (nSchemePremises↑.Count > 0) then
    begin Print_String(TokenName[sy_Provided]);
    Print_Proposition(nSchemePremises↑.Items↑[0]);
    for i ← 1 to nSchemePremises↑.Count - 1 do
      begin Print_String(TokenName[sy_And]); Print_NewLine;
      Print_Proposition(nSchemePremises↑.Items↑[i]);
      end;
    end;
    Print_String(TokenName[sy_Proof]); Print_NewLine;
  end;
  itTheorem: with CompactStatementPtr(nContent)↑ do
    begin Print_NewLine; nIndent ← 0; Print_String(TokenName[sy_Theorem]);
    Print_Label(nProp↑.nLab); Print_NewLine; nIndent ← 2; Print_Indent;
    Print_Formula(nProp↑.nSentence); nIndent ← 0; Print_Justification(nJustification, nBlock);
    Print_String(' '); Print_NewLine;
  end;

```



```

itAxiom: begin end;
itReservation: with ReservationSegmentPtr(nContent)↑ do
  begin Print_NewLine; Print_String(TokenName[sy_reserve]);
  Print_Variable(nIdentifiers.Items↑[0]);
  for i ← 1 to nIdentifiers.Count − 1 do
    begin Print_String(' '); Print_Variable(nIdentifiers.Items↑[i]);
    end;
  Print_String(TokenName[sy_For]); Print_ReservedType(nResType); Print_String('; ');
  Print_NewLine;
  end;
itSection: begin Print_NewLine; Print_String(TokenName[sy_Begin]); Print_NewLine;
end;
itRegularStatement: begin Print_RegularStatement(RegularStatementPtr(nContent), nBlock);
  Print_String('; '); Print_NewLine;
end;
itChoice: with ChoiceStatementPtr(nContent)↑ do
  begin if (nJustification↑.nInfSort = infStraightforwardJustification) ∧
    StraightforwardJustificationPtr(nJustification)↑.nLinked then
    begin Print_Linkage;
    end;
  Print_String(TokenName[sy_Consider]); Print_VariableSegment(nQualVars.Items↑[0]);
  for i ← 1 to nQualVars.Count − 1 do
    begin Print_String(' '); Print_VariableSegment(nQualVars.Items↑[i]);
    end;
  if (nConditions ≠ nil) ∧ (nConditions↑.Count > 0) then
    begin Print_String(TokenName[sy_Such]); Print_Conditions(nConditions);
    end;
  Print_Justification(nJustification, nil); Print_String('; '); Print_NewLine;
  end;
itReconsider: with TypeChangingStatementPtr(nContent)↑ do
  begin if (nJustification↑.nInfSort = infStraightforwardJustification) ∧
    StraightforwardJustificationPtr(nJustification)↑.nLinked then
    begin Print_Linkage;
    end;
  Print_String(TokenName[sy_Reconsider]);
  for i ← 0 to nTypeChangeList.Count − 1 do
    begin case TypeChangePtr(nTypeChangeList.Items↑[i])↑.nTypeChangeKind of
      Equating: begin Print_Variable(TypeChangePtr(nTypeChangeList.Items↑[i])↑.nVar);
        Print_String('='); Print_Term(TypeChangePtr(nTypeChangeList.Items↑[i])↑.nTermExpr);
        end;
      VariableIdentifier: begin Print_Variable(TypeChangePtr(nTypeChangeList.Items↑[i])↑.nVar);
        end;
    endcases;
    if (i ≥ 0) ∧ (i < nTypeChangeList.Count − 1) then Print_String(' ');
    end;
  Print_String(TokenName[sy_As]); Print_Type(nTypeExpr);
  Print_Justification(nJustification, nil); Print_String('; '); Print_NewLine;
  end;
itPrivFuncDefinition: with PrivateFunctorDefinitionPtr(nContent)↑ do
  begin Print_String(TokenName[sy_DefFunc]); Print_Variable(nFuncId); Print_String('(');
  Print_TypeList(nTypeExpList); Print_String(' '); Print_String('='); Print_Term(nTermExpr);
  Print_String('; '); Print_NewLine;

```

```

    end;
itPrivPredDefinition: with PrivatePredicateDefinitionPtr(nContent)↑ do
    begin Print_String(TokenName[sy_DefPred]); Print_Variable(nPredId); Print_String('[');
    Print_TypeList(nTypeExpList); Print_String(']'); Print_String(TokenName[sy_Means]);
    Print_Formula(nSentence); Print_String(';'); Print_NewLine;
    end;
itConstantDefinition: with ConstantDefinitionPtr(nContent)↑ do
    begin Print_String(TokenName[sy_Set]); Print_Variable(nVarId); Print_String('=');
    Print_Term(nTermExpr); Print_String(';'); Print_NewLine;
    end;
itLocDeclaration, itGeneralization: begin Print_String(TokenName[sy_Let]);
    Print_VariableSegment(QualifiedSegmentPtr(nContent)); Print_String(';'); Print_NewLine;
    end;
itAssumption: begin Print_String(TokenName[sy_Assume]);
    Print_AssumptionConditions(AssumptionPtr(nContent)); Print_String(';'); Print_NewLine;
    end;
itExistentialAssumption: with ExistentialAssumptionPtr(nContent)↑ do
    begin Print_String(TokenName[sy_Given]); Print_VariableSegment(nQVars↑.Items↑[0]);
    for i ← 1 to nQVars↑.Count - 1 do
        begin Print_String(','); Print_VariableSegment(nQVars↑.Items↑[i]);
        end;
    Print_String(TokenName[sy_Such]); Print_String(TokenName[sy_That]); Print_NewLine;
    Print_Proposition(nConditions↑.Items↑[0]);
    for i ← 1 to nConditions↑.Count - 1 do
        begin Print_String(TokenName[sy_And]); Print_NewLine;
        Print_Proposition(nConditions↑.Items↑[i]);
        end;
    Print_String(';'); Print_NewLine;
    end;
itExemplification: with ExamplePtr(nContent)↑ do
    begin Print_String(TokenName[sy_Take]);
    if nVarId ≠ nil then
        begin Print_Variable(nVarId);
        if nTermExpr ≠ nil then
            begin Print_String('=');
            end;
        end;
    if nTermExpr ≠ nil then Print_Term(nTermExpr);
    Print_String(';'); Print_NewLine;
    end;
itPerCases: begin if (JustificationPtr(nContent)↑.nInfSort =
    infStraightforwardJustification) ∧ StraightforwardJustificationPtr(nContent)↑.nLinked then
    begin Print_Linkage;
    end;
    Print_String(TokenName[sy_Per]); Print_String(TokenName[sy_Cases]);
    Print_Justification(JustificationPtr(nContent), nil); Print_String(';'); Print_NewLine;
    end;
itConclusion: begin Print_String(TokenName[sy_Thus]);
    Print_RegularStatement(RegularStatementPtr(nContent), nBlock); Print_String(';');
    Print_NewLine;
    end;
itCaseBlock: begin Print_Block(nBlock); Print_String(';'); Print_NewLine;

```

```

    end;
itCaseHead, itSupposeHead: begin Print_AssumptionConditions( AssumptionPtr(nContent));
    Print_String(‘;’); Print_NewLine;
    end;
itCorrCond: begin
    Print_String( CorrectnessName[CorrectnessConditionPtr(nContent)↑.nCorrCondSort]);
    Print_Justification( CorrectnessConditionPtr(nContent)↑.nJustification, nBlock); Print_String(‘;’);
    Print_NewLine;
    end;
itCorrectness: begin Print_String( TokenName[sy_Correctness]);
    Print_Justification( CorrectnessPtr(nContent)↑.nJustification, nBlock); Print_String(‘;’);
    Print_NewLine;
    end;
itProperty: begin Print_String( PropertyName[PropertyPtr(nContent)↑.nPropertySort]);
    Print_Justification( PropertyPtr(nContent)↑.nJustification, nBlock); Print_String(‘;’);
    Print_NewLine;
    end;
itDefMode: with ModeDefinitionPtr(nContent)↑ do
    begin if nRedefinition then
        begin Print_String( TokenName[sy_Redefine]);
        end;
        Print_String( TokenName[sy_Mode]); Print_Pattern(nDefModePattern);
    case nDefKind of
        defExpandableMode: begin Print_String( TokenName[sy_Is]);
            Print_Type( ExpandableModeDefinitionPtr(nContent)↑.nExpansion);
            end;
        defStandardMode: with StandardModeDefinitionPtr(nContent)↑ do
            begin if nSpecification ≠ nil then
                begin Print_String( TokenName[sy_Arrow]); Print_Type(nSpecification);
                end;
            if nDefiniens ≠ nil then
                begin Print_String( TokenName[sy_Means]); Print_NewLine; Print_Definiens(nDefiniens);
                end;
            end;
        endcases; Print_String(‘;’); Print_NewLine;
    end;
itDefAttr: with AttributeDefinitionPtr(nContent)↑ do
    begin if nRedefinition then
        begin Print_String( TokenName[sy_Redefine]);
        end;
        Print_String( TokenName[sy_Attr]); Print_Pattern(nDefAttrPattern);
        Print_String( TokenName[sy_Means]); Print_NewLine; Print_Definiens(nDefiniens);
        Print_String(‘;’); Print_NewLine;
    end;
itDefPred: with PredicateDefinitionPtr(nContent)↑ do
    begin if nRedefinition then
        begin Print_String( TokenName[sy_Redefine]);
        end;
        Print_String( TokenName[sy_Pred]); Print_Pattern(nDefPredPattern);
    if nDefiniens ≠ nil then
        begin Print_String( TokenName[sy_Means]); Print_NewLine; Print_Definiens(nDefiniens);
        end;

```

```

    Print_String(' '); Print_NewLine;
  end;
itDefFunc: with FunctorDefinitionPtr(nContent)↑ do
  begin if nRedefinition then
    begin Print_String(TokenName[sy_Redefine]);
    end;
    Print_String(TokenName[sy_Func]); Print_Pattern(nDefFuncPattern);
  if nSpecification ≠ nil then
    begin Print_String(TokenName[sy_Arrow]); Print_Type(nSpecification);
    end;
  case nDefiningWay of
    dfEmpty: ;
    dfMeans: begin Print_String(TokenName[sy_Means]); Print_NewLine;
    end;
    dfEquals: begin Print_String(TokenName[sy_Equals]);
    end;
  endcases; Print_Definiens(nDefiniens); Print_String(' '); Print_NewLine;
  end;
itDefStruct: with StructureDefinitionPtr(nContent)↑ do
  begin Print_String(TokenName[sy_Struct]);
  if nAncestors↑.Count > 0 then
    begin Print_String(' ( '); Print_Type(nAncestors↑.Items↑[0]);
    for i ← 1 to nAncestors↑.Count - 1 do
      begin Print_String(' '); Print_Type(nAncestors↑.Items↑[i]);
      end;
    Print_String(' ');
    end;
    Print_String(StructureName[nDefStructPattern↑.nModeSymbol]);
  if (nDefStructPattern↑.nArgs ≠ nil) ∧ (nDefStructPattern↑.nArgs↑.Count > 0) then
    begin Print_String(TokenName[sy_Over]); Print_Loci(nDefStructPattern↑.nArgs);
    end;
    Print_String(TokenName[sy_StructLeftBracket]);
  for i ← 0 to nSgmFields↑.Count - 1 do
    with FieldSegmentPtr(nSgmFields↑.Items↑[i])↑ do
      begin Print_String(SelectorName[FieldSymbolPtr(nFields↑.Items↑[0])↑.nFieldSymbol]);
      for j ← 1 to nFields↑.Count - 1 do
        with FieldSymbolPtr(nFields↑.Items↑[j])↑ do
          begin Print_String(' '); Print_String(SelectorName[nFieldSymbol]);
          end;
          Print_String(TokenName[sy_Arrow]); Print_Type(nSpecification);
          if (i ≥ 0) ∧ (i < nSgmFields↑.Count - 1) then Print_String(' ');
          end;
        end;
      end;
    Print_String(TokenName[sy_StructRightBracket]); Print_String(' '); Print_NewLine;
  end;
itPredSynonym, itFuncNotation, itModeNotation, itAttrSynonym:
  with NotationDeclarationPtr(nContent)↑ do
    begin Print_String(TokenName[sy_Synonym]); Print_Pattern(nNewPattern);
    Print_String(TokenName[sy_For]); Print_Pattern(nOriginPattern); Print_String(' ');
    Print_NewLine;
  end;
itPredAntonym, itAttrAntonym: with NotationDeclarationPtr(nContent)↑ do
  begin Print_String(TokenName[sy_Antonym]); Print_Pattern(nNewPattern);

```

```

    Print_String(TokenName[sy_For]); Print_Pattern(nOriginPattern); Print_String(';');
    Print_NewLine;
  end;
itCluster: begin Print_String(TokenName[sy_Cluster]);
  case ClusterPtr(nContent)↑.nClusterKind of
    ExistentialRegistration: with EClusterPtr(nContent)↑ do
      begin Print_AdjectiveList(nConsequent); Print_String(TokenName[sy_For]);
      Print_Type(nClusterType);
      end;
    ConditionalRegistration: with CClusterPtr(nContent)↑ do
      begin Print_AdjectiveList(nAntecedent); Print_String(TokenName[sy_Arrow]);
      Print_AdjectiveList(nConsequent); Print_String(TokenName[sy_For]);
      Print_Type(nClusterType);
      end;
    FunctorialRegistration: with FClusterPtr(nContent)↑ do
      begin Print_Term(nClusterTerm); Print_String(TokenName[sy_Arrow]);
      Print_AdjectiveList(nConsequent);
      if nClusterType ≠ nil then
        begin Print_String(TokenName[sy_For]); Print_Type(nClusterType);
        end;
      end;
  endcases; Print_String(';'); Print_NewLine;
end;
itIdentify: with IdentifyRegistrationPtr(nContent)↑ do
  begin Print_String(TokenName[sy_Identify]); Print_Pattern(nNewPattern);
  Print_String(TokenName[sy_With]); Print_Pattern(nOriginPattern);
  if (nEqLocList ≠ nil) ∧ (nEqLocList↑.Count > 0) then
    begin Print_String(TokenName[sy_When]);
    for i ← 0 to nEqLocList↑.Count - 1 do
      with LociEqualityPtr(nEqLocList↑.Items↑[i])↑ do
        begin Print_Locus(nLeftLocus); Print_String('='); Print_Locus(nRightLocus);
        if (i ≥ 0) ∧ (i < nEqLocList↑.Count - 1) then Print_String(',');
        end;
      end;
    end;
    Print_String(';'); Print_NewLine;
  end;
itPropertyRegistration: case PropertyRegistrationPtr(nContent)↑.nPropertySort of
  sySethood: with SethoodRegistrationPtr(nContent)↑ do
    begin Print_String(PropertyName[nPropertySort]); Print_String(TokenName[sy_Of]);
    Print_Type(nSethoodType); Print_Justification(nJustification, nBlock); Print_String(';');
    Print_NewLine;
    end;
  endcases;
itReduction: begin with ReduceRegistrationPtr(nContent)↑ do
  begin Print_String(TokenName[sy_Reduce]); Print_Term(nOriginTerm);
  Print_String(TokenName[sy_To]); Print_Term(nNewTerm);
  end;
  Print_String(';'); Print_NewLine;
end;
itPragma: begin Print_NewLine; Print_String('::' + PragmaPtr(nContent)↑.nPragmaStr);
  Print_NewLine;
end;

```

```
    itIncorrItem: ;  
  end;  
endcases;  
end;
```

1339. 〈Implementation for `wsmarticle.pas` 1001〉 +≡

```
procedure Print_WSMizArticle(aWSTextProper : wsTextProperPtr; aFileName : string);  
  var lWSMizOutput: WSMizarPrinterPtr;  
  begin InitScannerNames; lWSMizOutput ← new(WSMizarPrinterPtr, OpenFile(aFileName));  
    lWSMizOutput↑.Print_TextProper(aWSTextProper); dispose(lWSMizOutput, Done);  
  end;
```

File 22

Detour: Pragmas

1340. This chapter is a “detour” because it is out of order for the compiler, but it is a dependency for the next file (`parseradditions.pas`).

The `base/pragmas.pas` contains the global variables which are toggled by pragmas like “`::$P+`”. This will toggle the *ProofPragma*. In particular, when *ProofPragma* is true, then Mizar will double check the proofs. When *ProofPragma* is false, Mizar will skip the proofs.

```

⟨pragmas.pas 1340⟩ ≡
  ⟨GNU License 4⟩
unit pragmas;
interface uses mobjects;
var VerifyPragmaOn, VerifyPragmaOff: NatSet; VerifyPragmaIntervals: NatFunc;
    SchemePragmaOn, SchemePragmaOff: NatSet; SchemePragmaIntervals: NatFunc;
    ProofPragma: Boolean = true; { check the proofs? }

procedure SetParserPragma(aPrg : string);
procedure InsertPragma(aLine : integer; aPrg : string);
procedure CompletePragmas(aLine : integer);
procedure CanceledPragma ( const aPrg: string; var aKind: char; var aNbr: integer ) ;
implementation
uses mizenv;

```

1341. Cancelling a definition or theorem is handled with the “`::$C`” pragma, which is administered only by the editors of the MML. For example “`::$CD`” will cancel a definition, “`CT`” will cancel a theorem, and “`CS`” cancels a scheme.

```

procedure CanceledPragma ( const aPrg: string; var aKind: char; var aNbr: integer ) ;
var lStr: string; k, lCod: integer;
begin aKind ← ‘_’;
if (Copy(aPrg, 1, 2) = ‘$C’) then
  begin if (length(aPrg) ≥ 3) ∧ (aPrg[3] ∈ [‘D’, ‘S’, ‘T’]) then
    begin aKind ← aPrg[3]; lStr ← TrimString(Copy(aPrg, 4, length(aPrg) – 3)); aNbr ← 1;
    if length(lStr) > 0 then
      begin k ← 1;
      while (k ≤ length(lStr)) ∧ (lStr[k] ∈ [‘0’ .. ‘9’]) do inc(k);
      delete(lStr, k, length(lStr));
      if length(lStr) > 0 then Val(lStr, aNbr, lCod);
      end;
    end;
  end;
end;
end;

```

1342. The “`::$P+`” pragma instructs Mizar to start checking the proofs for correctness. The “`::$P-`” pragma instructs Mizar to skip checking proofs.

```
procedure SetParserPragma(aPrg : string);
  begin if copy(aPrg, 1, 3) = ‘$P+’ then
    begin ProofPragma  $\leftarrow$  true;
    end;
  if copy(aPrg, 1, 3) = ‘$P-’ then
    begin ProofPragma  $\leftarrow$  false;
    end;
  end;
```

1343. The “`::$S+`” pragma will tell Mizar to check the scheme references, whereas “`::$S-`” pragma tells Mizar to stop verifying scheme references.

The “`::$V+`” pragma enables the verifier, and the “`::$V-`” pragma disables the verifier (skipping all verification until it is re-enabled).

```
procedure InsertPragma(aLine : integer; aPrg : string);
  begin if copy(aPrg, 1, 3) = ‘$V+’ then
    begin VerifyPragmaOn.InsertElem(aLine); end;
  if copy(aPrg, 1, 3) = ‘$V-’ then
    begin VerifyPragmaOff.InsertElem(aLine); end;
  if copy(aPrg, 1, 3) = ‘$S+’ then
    begin SchemePragmaOn.InsertElem(aLine); end;
  if copy(aPrg, 1, 3) = ‘$S-’ then
    begin SchemePragmaOff.InsertElem(aLine); end;
  end;
```

1344. The *CompletePragmas* function will compute the intervals for which the pragmas are “active”, then check whether the given line number falls within the “active range”.

```
procedure CompletePragmas(aLine : integer);
  var i, j, a, b: integer; f: boolean;
  begin for i  $\leftarrow$  0 to VerifyPragmaOff.Count - 1 do
    begin f  $\leftarrow$  false; a  $\leftarrow$  VerifyPragmaOff.Items $\uparrow$ [i].X;
    for j  $\leftarrow$  0 to VerifyPragmaOn.Count - 1 do
      begin b  $\leftarrow$  VerifyPragmaOn.Items $\uparrow$ [j].X;
      if b  $\geq$  a then
        begin VerifyPragmaIntervals.Assign(a, b); f  $\leftarrow$  true; break; end;
      end;
    if  $\neg$ f then VerifyPragmaIntervals.Assign(a, aLine);
    end;
  for i  $\leftarrow$  0 to SchemePragmaOff.Count - 1 do
    begin f  $\leftarrow$  false; a  $\leftarrow$  SchemePragmaOff.Items $\uparrow$ [i].X;
    for j  $\leftarrow$  0 to SchemePragmaOn.Count - 1 do
      begin b  $\leftarrow$  SchemePragmaOn.Items $\uparrow$ [j].X;
      if b  $\geq$  a then
        begin SchemePragmaIntervals.Assign(a, b); f  $\leftarrow$  true; break; end;
      end;
    if  $\neg$ f then SchemePragmaIntervals.Assign(a, aLine);
    end;
  end;
```


1345. Now we initialize the global variables declared in this module.

```
begin VerifyPragmaOn.Init(10,10); VerifyPragmaOff.Init(10,10);  
      VerifyPragmaIntervals.InitNatFunc(10,10); SchemePragmaOn.Init(10,10);  
      SchemePragmaOff.Init(10,10); SchemePragmaIntervals.InitNatFunc(10,10);  
end.
```

File 23

Detour: Parser additions

1346. This chapter is a “detour” because we are “going out of [compiler] order” to discuss `parseradditions.pas`. Why? Well, because the file provides subclasses to those introduced in the abstract syntax unit, and are necessary for understanding the `parser.pas` unit.

One of the difficulties with this file is that there are 37 global variables declared here, and 46 module-wide variables, declared here. It’s hard to juggle that knowledge! These “global” variables really describe the state of the Parser, and do not seem to be used anywhere else.

For what it’s worth, this appears to be conventional among compilers in the 1990s to use global variables to control the state of the compiler. For example David Hanson and Christopher Fraser’s *A Retargetable C Compiler: Design and Implementation* (Addison-Wesley, 1995) has quite a few global variables. If we were starting from scratch, it would be more idiomatic to put the state in a *Parser* class instance, and we could then use this to unit test the parser. This would become conventional more than a decade after Hanson and Fraser’s book was published.

[[It would probably be wise to refactor the design to isolate these variables inside a `Parser` class, so they are not randomly distributed throughout this part of the program.]]

CONVENTIONS: The classes have methods prefixed by *Start*, *Process*, and *Finish*.

- The *Start* methods reset the state variables needed to parse the syntactic entity.
- The *Process* methods usually update the state variables, either allocating new objects or transferring the current contents of a state variable in a different state variable.
- The *Finish* methods construct a WSM abstract syntax tree for the parsed entity.

⟨`parseraddition.pas` 1346⟩ ≡

⟨GNU License 4⟩

unit *parseraddition*;

interface

uses *syntax*, *errhan*, *mobjects*, *mscanner*, *abstract_syntax*, *wsmarticle*, *xml_inout*;

procedure *InitWsMizarArticle*;

type

⟨Extended block class declaration 1352⟩

⟨Extended item class declaration 1372⟩

⟨Extended subexpression class declaration 1535⟩

⟨Extended expression class declaration 1636⟩

function *GetIdentifier*: *integer*;

function *CreateArgs*(*aBase* : *integer*): *PList*;

var ⟨Global variables introduced in `parseraddition.pas` 1349⟩

implementation

uses *mizenv*, *mconsole*, *parser*, *_formats*, *pragmas*

mdebug , *info* **end_mdebug**;

const *MaxSubTermNbr* = 64;

var ⟨Local variables for parser additions 1356⟩

⟨Implementation of parser additions 1347⟩

end .

1347. \langle Implementation of parser additions 1347 $\rangle \equiv$
 \langle Get the identifier number for current word 1348 \rangle
 \langle Initialize WS Mizar article 1350 \rangle ;
 \langle Extended block implementation 1353 \rangle
 \langle Extended item implementation 1373 \rangle
 \langle Extended subexpression implementation 1537 \rangle
 \langle Extended expression implementation 1637 \rangle

This code is used in section 1346.

1348. When the current token is an identifier, we should obtain its number. If the current token is not an identifier, we should return 0. Since the ID numbers for variables (and types and...) are nonzero, returning 0 indicates the current token is not an identifier.

\langle Get the identifier number for current word 1348 $\rangle \equiv$
function *GetIdentifier*: *integer*;
 begin *result* \leftarrow 0;
 if *CurWord.Kind* = *Identifier* **then** *result* \leftarrow *CurWord.Nr*
 end;

This code is used in section 1347.

1349. Initializing a weakly-strict Mizar article requires setting the values for some of the global variables. Importantly, this will initialize the *gBlockPtr* in the Parser to be an *extBlockObj* instance. Note that this will create “the” *blMain* block object.

The *gLastWSItem* state variable tracks the last *statement item*.

\langle Global variables introduced in *parseraddition.pas* 1349 $\rangle \equiv$
gWSTextProper: *wsTextProperPtr*; { article’s text body AST }
gLastWSBlock: *WSBlockPtr*; { block statement AST }
gLastWSItem: *WSItemPtr*; { statement AST }

See also sections 1357, 1359, 1374, 1378, 1381, 1387, 1390, 1394, 1403, 1415, 1420, 1434, 1444, 1455, 1463, 1467, 1475, 1483, 1485, 1487, 1493, 1495, 1514, 1517, 1521, and 1541.

This code is used in section 1346.

1350. \langle Initialize WS Mizar article 1350 $\rangle \equiv$
procedure *InitWsMizarArticle*;
 begin { initialize global variables which were declared in *parseraddition* }
 gWSTextProper \leftarrow *new*(*wsTextProperPtr*, *Init*(*ArticleID*, *ArticleExt*, *CurPos*));
 gLastWSBlock \leftarrow *gWSTextProper*; *gLastWSItem* \leftarrow **nil**;
 gBlockPtr \leftarrow *new*(*extBlockPtr*, *Init*(*blMain*)); { initialize other global variables }
 end;

This code is used in section 1347.

Section 23.1. EXTENDED BLOCK CLASS

1351. We extend the *Block* class (§818) introduced in the `syntax.pas` unit. Also recall the *wsBlock* class (§1003) and the *wsItem* class (§1007).

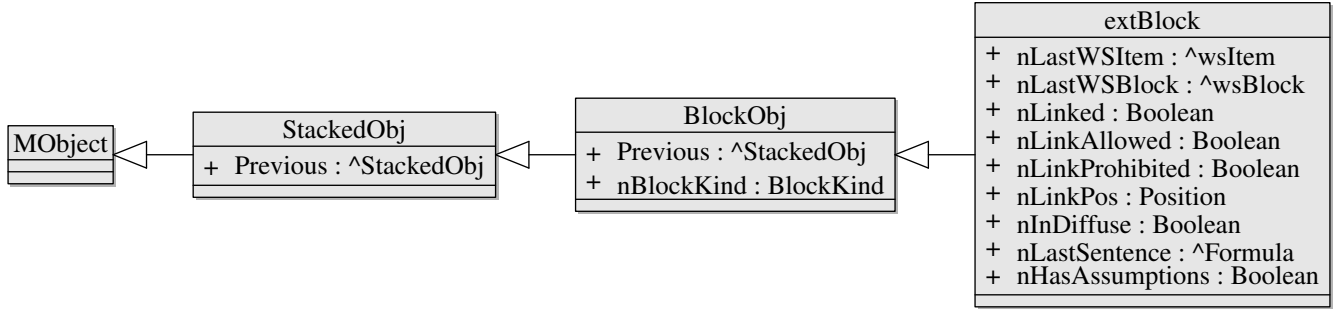


Fig. 6. Class hierarchy for *extBlockObj*, methods omitted.

1352. \langle Extended block class declaration 1352 $\rangle \equiv$

```

extBlockPtr =  $\uparrow$ extBlockObj;
extBlockObj = object (BlockObj)
  nLastWSItem: WSItemPtr;
  nLastWSBlock: WSBlockPtr;
  nLinked: Boolean; { is block prefixed by "then"? }
  nLinkAllowed: Boolean; { isn't this a duplicate of next field? }
  nLinkProhibited: Boolean; { can statement kind be prefixed by "then"? }
  nLinkPos: Position;
  nInDiffuse: boolean;
  nLastSentence: FormulaPtr;
  nHasAssumptions: Boolean;
constructor Init(fBlockKind : BlockKind);
procedure Pop; virtual;
procedure StartProperText; virtual;
procedure ProcessRedefine; virtual;
procedure ProcessLink; virtual;
procedure ProcessBegin; virtual;
procedure ProcessPragma; virtual;
procedure StartSchemeDemonstration; virtual;
procedure FinishSchemeDemonstration; virtual;
procedure CreateItem(fItemKind : ItemKind); virtual;
procedure CreateBlock(fBlockKind : BlockKind); virtual;
end ;
  
```

This code is used in section 1346.

1353. Constructor. The constructor for an extended block object invokes the parent class’s constructor (§821), initializes the instance variables, then its behaviour depends on whether we are constructing a “main” block or not.

```

⟨Extended block implementation 1353⟩ ≡
constructor extBlockObj.Init(fBlockKind : BlockKind);
  begin inherited Init(fBlockKind);
  ⟨Initialize default values for extBlock instance 1354⟩;
  if nBlockKind = blMain then ⟨Initialize main extBlock instance 1355⟩
  else ⟨Initialize “proper text” extBlock instance 1358⟩;
  end;

```

See also sections 1360, 1361, 1362, 1363, 1364, 1365, 1366, 1368, 1369, and 1370.

This code is used in section 1347.

1354. We have the default values suppose links are prohibited for the block, and there are no assumptions for the block. The last *wsItem* and *wsBlock* pointers are set to the global *gLastWSItem* and *gLastWSBlock* variables, respectively.

```

⟨Initialize default values for extBlock instance 1354⟩ ≡
  nLinked ← false; nLinkPos ← CurPos; nLinkAllowed ← false; nLinkProhibited ← true;
  nHasAssumptions ← false; gRedefinitions ← false;
  nLastWSItem ← gLastWSItem; nLastWSBlock ← gLastWSBlock;

```

This code is used in section 1353.

1355. The “main” block of text needs to load the formats file, and populate the *gFormatsColl* (§775) and the *gFormatsBase* (*ibid.*) global variables. The *parseraddition.pas* unit’s *gProofCnt* global variable is initialized to zero here.

```

⟨Initialize main extBlock instance 1355⟩ ≡
  begin nInDiffuse ← true; gProofCnt ← 0;
  FileExam(EnvFileName + ‘.frm’); gFormatsColl.LoadFormats(EnvFileName + ‘.frm’);
  gFormatsBase ← gFormatsColl.Count; setlength(Term, MaxSubTermNbr);
  end

```

This code is used in section 1353.

1356. ⟨Local variables for parser additions 1356⟩ ≡
Term: **array of** *TermPtr*; { (§880) }

See also sections 1375, 1379, 1385, 1388, 1391, 1392, 1395, 1399, 1405, 1407, 1409, 1416, 1418, 1421, 1425, 1431, 1439, 1445, 1449, 1456, 1464, 1478, 1529, and 1536.

This code is used in section 1346.

1357. ⟨Global variables introduced in *parseraddition.pas* 1349⟩ +≡
gProofCnt: *integer*;

1358. The “proper text” branch updates the *gLastWSBlock* global variable. For most of the kinds of blocks, we will have to toggle *nInDiffuse* to be true or false. For proof blocks, we will need to increment the “depth” counter tracking the proof block “nestedness”.

Only the “**case**” and “**suppose**” blocks, when determining if they are in “diffuse mode” or not, need to confer with the previous block. (Recall (§436), *StackedObj* classes has a *Previous* pointer.)

```

⟨ Initialize “proper text” extBlock instance 1358 ⟩ ≡
  begin gLastWSBlock ← gWsTextProper↑.NewBlock(nBlockKind, CurPos);
  mizassert(2341, gLastWSItem ≠ nil);
  if gLastWSItem↑.nItemKind ∈ [itDefinition, itRegularStatement, itSchemeBlock, itTheorem,
    itConclusion, itCaseBlock, itCorrCond, itCorrectness, itProperty, itPropertyRegistration] then
    wsItemPtr(gLastWSItem).nBlock ← gLastWSBlock;
  case nBlockKind of
    blDefinition: nInDiffuse ← false;
    blNotation: nInDiffuse ← false;
    blDiffuse: nInDiffuse ← true;
    blHereby: nInDiffuse ← true;
    blProof: begin nLastSentence ← gLastFormula; inc(gProofCnt); end;
    blCase: nInDiffuse ← extBlockPtr(Previous)↑.nInDiffuse;
    blSuppose: nInDiffuse ← extBlockPtr(Previous)↑.nInDiffuse;
    blRegistration: nInDiffuse ← false;
    blPublicScheme: nInDiffuse ← false;
  endcases;
end

```

This code is used in section 1353.

1359. Popping a block. When we “pop” a proof block, we need to track the formula that was just proven and store it in the global variable *gLastFormula*.

```

⟨ Global variables introduced in parseraddition.pas 1349 ⟩ +≡
gLastFormula: FormulaPtr;

```

1360. This actually implements the *Pop* method for blocks. When a block “closes” (i.e., the corresponding “**end**” statement has been encountered), we restore the global state’s *gLastWSItem* and *gLastWSBlock* pointers. When a proof block closes, we also restore the *gLastFormula* state.

Also note: the parent class’s method (§822) does nothing. This will be invoked in the *KillBlock* (§814).

```

⟨ Extended block implementation 1353 ⟩ +≡
procedure extBlockObj.Pop;
  begin gLastWSBlock↑.nBlockEndPos ← CurPos;
  case nBlockKind of
    blProof: begin gLastFormula ← nLastSentence; dec(gProofCnt); end;
  endcases;
  gLastWSItem ← nLastWSItem; gLastWSBlock ← nLastWSBlock; { restore the “last” pointers }
  inherited Pop;
end;

```

1361. Process “begin”. Mizar uses “begin” to start a new “section” at the top-level of an article. Recall the grammar for this bit of Mizar:

$$\begin{aligned}\langle \textit{Text-Propser} \rangle &::= \langle \textit{Section} \rangle \{ \langle \textit{Section} \rangle \} . \\ \langle \textit{Section} \rangle &::= \textbf{“begin”} \{ \langle \textit{Text-Item} \rangle \} .\end{aligned}$$

There are zero or more Text-Items in a section.

We should note that the main text is not organized as a linked list of “main” blocks. Instead, we have a single “main” block, and we just push an *itSection* item to its contents.

⟨Extended block implementation 1353⟩ +≡

```
procedure extBlockObj.ProcessBegin;
  begin nLinkAllowed  $\leftarrow$  false; nLinkProhibited  $\leftarrow$  true;
  gLastWSItem  $\leftarrow$  gWsTextPropser↑.NewItem(itSection, CurPos); nLastWSItem  $\leftarrow$  gLastWSItem;
  gLastWSBlock↑.nItems.Insert(gLastWSItem);
end;
```

1362. This will add a pragma item to the current block. The Parser’s *ProcessPragmas* (§1782) invokes this method.

⟨Extended block implementation 1353⟩ +≡

```
procedure extBlockObj.ProcessPragma;
  begin nLinkAllowed  $\leftarrow$  false; nLinkProhibited  $\leftarrow$  true;
    { Create a new item }
  gLastWSItem  $\leftarrow$  gWsTextPropser↑.NewItem(itPragma, CurPos);
  gLastWSItem↑.nContent  $\leftarrow$  new(PragmaPtr, Init(CurWord.Spelling));
    { Insert the pragma, update last item in block }
  nLastWSItem  $\leftarrow$  gLastWSItem; gLastWSBlock↑.nItems.Insert(gLastWSItem);
end;
```

1363. Starting the proper text will just update the *nBlockPos* field to whatever the current position is.

⟨Extended block implementation 1353⟩ +≡

```
procedure extBlockObj.StartProperText;
  begin gWSTextPropser↑.nBlockPos  $\leftarrow$  CurPos; end;
```

1364. Processing redefinitions sets the global variable *gRedefinitions* to the result of comparing the current word to the “redefine” keyword.

⟨Extended block implementation 1353⟩ +≡

```
procedure extBlockObj.ProcessRedefine;
  begin gRedefinitions  $\leftarrow$  CurWord.Kind = sy_Redefine; end;
```

1365. When a block statement is linked, but it should not, then we raise a 164 error. Otherwise, be sure to mark the block as linked (i.e., toggle *nLinked* to be true) and assign the *nLinkPos* to be the current position.

⟨Extended block implementation 1353⟩ +≡

```
procedure extBlockObj.ProcessLink;
  begin if CurWord.Kind  $\in$  [sy_Then, sy_Hence] then
    begin if nLinkProhibited then ErrImm(164);
      nLinked  $\leftarrow$  true; nLinkPos  $\leftarrow$  CurPos;
    end;
  end;
```

1366. Proof of a scheme. We should increment the proof depth global variable.

Recall that *ProofPragma* means “check the proof is valid?” In other words, when *ProofPragma* is false, we are skipping the proofs.

```

define thesis_formula  $\equiv$  new(ThesisFormulaPtr, Init(CurPos))
define thesis_prop  $\equiv$  new(PropositionPtr, Init(new(LabelPtr, Init(0, CurPos)), thesis_formula, CurPos))
define skipped_proof_justification  $\equiv$  new(JustificationPtr, Init(infSkippedProof, CurPos))
⟨Extended block implementation 1353⟩ +≡
procedure extBlockObj.StartSchemeDemonstration;
begin inc(gProofCnt);
if  $\neg$ ProofPragma then ⟨Mark schema proof as “skipped” 1367⟩;
end;

```

1367. When we skip the proof (due to pragmas being set), we just add the scheme as a compact statement whose justification is the “skipped proof justification”.

First, we create a new text item for the proper text global variable. Then we set its content to the compact statement with the “skipped” justification. Finally we add this item to the “last” (latest) *wsBlock* global variable.

```

⟨Mark schema proof as “skipped” 1367⟩  $\equiv$ 
begin gLastWSItem  $\leftarrow$  gWsTextProper $\uparrow$ .NewItem(itConclusion, CurPos);
gLastWSItem $\uparrow$ .nContent  $\leftarrow$  new(CompactStatementPtr, Init(thesis_prop, skipped_proof_justification));
gLastWSBlock $\uparrow$ .nItems.Insert(gLastWSItem);
end

```

This code is used in section 1366.

1368. Finishing the proof for a scheme should decrement the global “proof depth” counter.

```

⟨Extended block implementation 1353⟩ +≡
procedure extBlockObj.FinishSchemeDemonstration;
begin dec(gProofCnt); end;

```

1369. The factory method for *extBlock* creating an item will update the global *gItemPtr* variable (§817).

```

⟨Extended block implementation 1353⟩ +≡
procedure extBlockObj.CreateItem(fItemKind : ItemKind);
begin gItemPtr  $\leftarrow$  new(extItemPtr, Init(fItemKind)); end;

```

1370. The factory method for *extBlock* creating a new block will update the *gBlockPtr* global variable (§817).

```

⟨Extended block implementation 1353⟩ +≡
procedure extBlockObj.CreateBlock(fBlockKind : BlockKind);
begin gBlockPtr  $\leftarrow$  new(extBlockPtr, Init(fBlockKind)) end;

```


Section 23.2. EXTENDED ITEM CLASS

1371. The class diagram for extended items looks like:

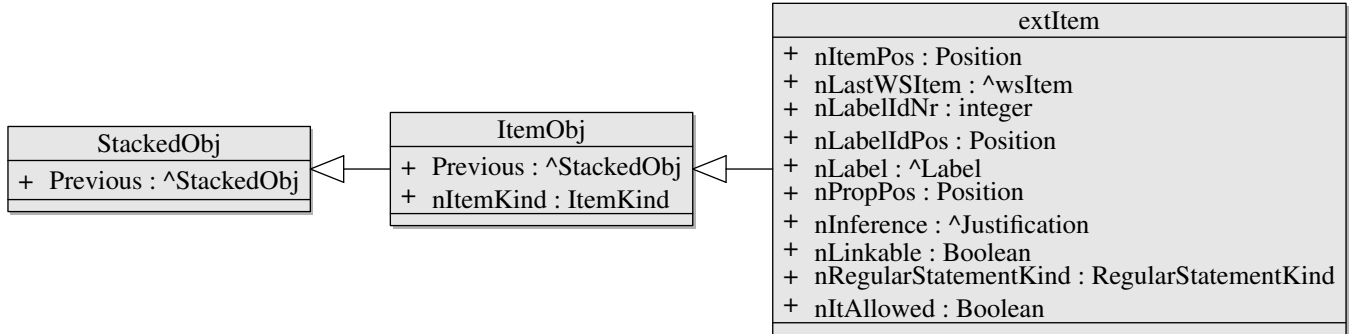


Fig. 7. Class hierarchy for *extItemObj*. The base *MObject* class omitted from the hierarchy.

Recall (§1056) the regular statement kind is one of three possibilities: diffuse statement, compact statement, iterative equality.

The “Finish” methods updates the contents of the *extItem* class with a WSM abstract syntax tree for the statement.

Since this is a “stub”, I will just leave the placeholder chunk for the methods overridden by the extended Item class here (remove later).

⟨Methods overridden by extended Item class 833⟩ +≡

1372. ⟨Extended item class declaration 1372⟩ ≡
extItemPtr = ↑*extItemObj*;
extItemObj = **object** (*ItemObj*)
 nItemPos: *Position*;
 nLastWSItem: *WSItemPtr*;
 nLabelIdNr: *integer*;
 nLabelIdPos: *Position*;
 nLabel: *LabelPtr*;
 nPropPos: *Position*;
 nInference: *JustificationPtr*;
 nLinkable: *boolean*;
 nRegularStatementKind: *RegularStatementKind*;
 nItAllowed: *boolean*;
 constructor *Init*(*fKind* : *ItemKind*);
 procedure *Pop*; *virtual*;
 ⟨Methods overridden by extended Item class 833⟩
end ;

This code is used in section 1346.

Subsection 23.2.1. Constructor

1373. There are a number of comments in Polish which I haphazardly translated into English (“Przygotowanie definiensow:” translates as “Preparation of definiens:”; “Ew. zakaz przy obiektach ekspandowanych” translates as “Possible ban on expanded facilities”)

```

⟨ Extended item implementation 1373 ⟩ ≡
constructor extItemObj.Init(fKind : ItemKind);
  begin inherited Init(fKind);
  ⟨ Initialize the fields for newly allocated extItem object 1376 ⟩
  mizassert(2343, gLastWSBlock ≠ nil);
  if ¬(nItemKind ∈ [itReservation, itConstantDefinition, itExemplification, itGeneralization,
    itLocDeclaration]) then
    begin gLastWSItem ← gWsTextProper↑.NewItem(fKind, CurPos); nLastWSItem ← gLastWSItem;
    end;
  case nItemKind of
    ⟨ Initialize extended item by ItemKind 1377 ⟩
  endcases;
  if ¬(nItemKind ∈ [itReservation, itConstantDefinition, itExemplification, itGeneralization,
    itLocDeclaration]) then gLastWSBlock↑.nItems.Insert(gLastWSItem);
  end;

```

See also sections 1396, 1424, 1426, 1427, 1428, 1429, 1430, 1432, 1433, 1435, 1436, 1437, 1438, 1440, 1441, 1442, 1443, 1446, 1447, 1448, 1450, 1451, 1452, 1453, 1454, 1457, 1458, 1459, 1460, 1461, 1462, 1465, 1466, 1468, 1469, 1470, 1471, 1472, 1473, 1474, 1476, 1477, 1479, 1480, 1481, 1482, 1484, 1486, 1488, 1489, 1490, 1491, 1492, 1494, 1496, 1497, 1498, 1499, 1500, 1501, 1502, 1503, 1504, 1505, 1506, 1507, 1508, 1509, 1510, 1511, 1512, 1513, 1515, 1516, 1518, 1519, 1520, 1522, 1523, 1524, 1525, 1526, 1527, 1528, 1530, 1531, and 1532.

This code is used in section 1347.

1374. Initializing the fields. The *it_Allowed* global variable is toggled on and off when the Parser encounters “guards” in conditional definitions, whereas the *nItAllowed* fields reflects whether the sort of definition allows “it” in the definiens.

```

⟨ Global variables introduced in parseraddition.pas 1349 ⟩ +≡
dol_Allowed: Boolean;
it_Allowed: Boolean;
in_AggrPattern: Boolean;
gLastType: TypePtr;
gLastTerm: TermPtr;
gDefiningWay: HowToDefine;

```

1375. ⟨ Local variables for parser additions 1356 ⟩ +≡
gClusterSort: *ClusterRegistrationKind*;
gDefiniens: *DefiniensPtr*;
gPartialDefs: *PList*;
nDefiniensProhibited: *boolean*;
gSpecification: *TypePtr*;

1376. \langle Initialize the fields for newly allocated *extItem* object 1376 $\rangle \equiv$
 $nItemPos \leftarrow CurPos$; $gClusterSort \leftarrow ExistentialRegistration$; $nItAllowed \leftarrow false$; $it_Allowed \leftarrow false$;
 { global variable! }
 $in_AggrPattern \leftarrow false$; $dol_Allowed \leftarrow false$; $gSpecification \leftarrow nil$; $gLastType \leftarrow nil$;
 $gLastFormula \leftarrow nil$; $gLastTerm \leftarrow nil$;
 { Preparation of definiens: }
 $nDefiniensProhibited \leftarrow false$;
 { Possible ban on expanded facilities }
 $gDefiningWay \leftarrow dfEmpty$; $gDefiniens \leftarrow nil$; $gPartialDefs \leftarrow nil$; $nLinkable \leftarrow false$;

This code is used in section 1373.

1377. Kind-specific initialization. Each kind of item may need some specific initialization. We work through all the cases. The first two cases considered are generalization (“**let** $\langle Qualified Variables \rangle$ **be** [such $\langle Conditions \rangle$]”) and existential assumptions (“**given** $\langle Qualified Variables \rangle$ **such** $\langle Conditions \rangle$ ”). Existential assumptions need to toggle the “has assumptions” field to true for the global block pointer.

\langle Initialize extended item by *ItemKind* 1377 $\rangle \equiv$
 $itGeneralization$: ; { **let** statements }
 $itExistentialAssumption$: $ExtBlockPtr(gBlockPtr) \uparrow .nHasAssumptions \leftarrow true$;

See also sections 1380, 1382, 1384, 1386, 1389, and 1393.

This code is used in sections 1373 and 1391.

1378. Property initialization. Initializing a property statement *Item* should raise an error when the property does not appear in the correct block.

- Defining a predicate can support the following properties: symmetry, reflectivity, irreflexivity, transitivity, connectedness, asymmetry.
- Functors can support: associativity, commutativity, idempotence, involutiveness, and projectivity properties.
- Modes can support the sethood property.

In all other situations, an error should be flagged (the user is trying to assert an invalid property).

\langle Global variables introduced in *parseraddition.pas* 1349 $\rangle + \equiv$
 $gDefKind$: *ItemKind*;

1379. \langle Local variables for parser additions 1356 $\rangle + \equiv$
 $gExpandable$: *boolean*;
 $gPropertySort$: *PropertyKind*;

1380. \langle Initialize extended item by *ItemKind* 1377 $\rangle + \equiv$
 $itProperty$: **begin** $gPropertySort \leftarrow PropertyKind(CurWord.Nr)$;
case $PropertyKind(CurWord.Nr)$ **of**
 $sySymmetry, syReflexivity, syIrreflexivity, syTransitivity, syConnectedness, syAsymmetry$:
if $gDefKind \neq itDefPred$ **then**
begin $ErrImm(81)$; $gPropertySort \leftarrow sErrProperty$; **end**;
 $syAssociativity, syCommutativity, syIdempotence$: **if** $gDefKind \neq itDefFunc$ **then**
begin $ErrImm(82)$; $gPropertySort \leftarrow sErrProperty$; **end**;
 $syInvolutiveness, syProjectivity$: **if** $gDefKind \neq itDefFunc$ **then**
begin $ErrImm(83)$; $gPropertySort \leftarrow sErrProperty$; **end**;
 $sySethood$: **if** $(gDefKind \neq itDefMode) \vee gExpandable$ **then**
begin $ErrImm(86)$; $gPropertySort \leftarrow sErrProperty$; **end**;
endcases;
end;

1381. Reconsider initialization. We need to allocate a new (empty) list for the list of terms being reconsidered.

⟨Global variables introduced in `parseraddition.pas` 1349⟩ +≡
gReconsiderList: *PList*;

1382. ⟨Initialize extended item by *ItemKind* 1377⟩ +≡
itReconsider: *gReconsiderList* ← *new(PList, Init(0))*;

1383. We can have in Mizar “**suppose that** ⟨*statement*⟩” (as well as “**case that...**”). But in those cases, the statement cannot be linked to the next statement (i.e., the next statement cannot begin with “**then...**”). Assumptions without “**that**” are always linkable.

Theorems, “regular statements”, and conclusions are always linkable.

1384. ⟨Initialize extended item by *ItemKind* 1377⟩ +≡
itRegularStatement: *nLinkable* ← *true*;
itConclusion: *nLinkable* ← *true*;
itPerCases: ;
itCaseHead: **if** *AheadWord.Kind* ≠ *sy_That* **then** *nLinkable* ← *true*;
itSupposeHead: **if** *AheadWord.Kind* ≠ *sy_That* **then** *nLinkable* ← *true*;
itTheorem: *nLinkable* ← *true*;
itAxiom: **if** ¬*AxiomsAllowed* **then** *ErrImm*(66);
itChoice: ;

1385. Initializing an assumption. Collective assumptions (“**assume that** ⟨*formula*⟩”) are not linkable, but single assumptions (“**assume** ⟨*Proposition*⟩”) are linkable. The statement will introduce a list of premises, which will be tracked in the *gPremises* local variable for the module.

⟨Local variables for parser additions 1356⟩ +≡
gPremises: *PList*;

1386. ⟨Initialize extended item by *ItemKind* 1377⟩ +≡
itAssumption: **begin if** *AheadWord.Kind* ≠ *sy_That* **then** *nLinkable* ← *true*;
 gPremises ← *nil*;
end;

1387. Definition items. Definition items need to be initialized with some nuance. Some definitions permit “**it**” to be used in the definiens, but others do not. Mizar toggles the global variables tracking this here. There is a common set of things toggled which we have isolated as the WEB macro *initialize_definition_item* common to initializing all definition items.

The correctness conditions are determined at this point, as well.

define *initialize_definition_item* ≡ *gCorrectnessConditions* ← []; *gDefPos* ← *CurPos*;
 gDefKind ← *nItemKind*

⟨Global variables introduced in `parseraddition.pas` 1349⟩ +≡
gCorrectnessConditions: *CorrectnessConditionsSet*;

1388. ⟨Local variables for parser additions 1356⟩ +≡
gDefPos: *Position*;
gStructPrefixes: *PList*;

1389. \langle Initialize extended item by *ItemKind* 1377 $\rangle + \equiv$
itLocDeclaration: ;
itDefMode: **begin** *nItAllowed* \leftarrow true; *gExpandable* \leftarrow false; *initialize_definition_item* **end**;
itDefAttr: **begin** *initialize_definition_item* **end**;
itAttrSynonym: **begin** *initialize_definition_item* **end**;
itAttrAntonym: **begin** *initialize_definition_item* **end**;
itModeNotation: **begin** *initialize_definition_item* **end**;
itDefFunc: **begin** *nItAllowed* \leftarrow true; *initialize_definition_item* **end**;
itFuncNotation: **begin** *initialize_definition_item*; **end**;
itDefPred, *itPredSynonym*, *itCluster*, *itIdentify*, *itReduction*:
begin *initialize_definition_item*; **end**;
itPropertyRegistration: **begin** *initialize_definition_item*; *gPropertySort* \leftarrow *PropertyKind*(*CurWord.Nr*);
end;
itDefStruct: **begin** *initialize_definition_item*; *gStructPrefixes* \leftarrow *new*(*PList*, *Init*(0)); **end**;
itCanceled: **begin** *ErrImm*(88); **end**;

1390. Correctness conditions. Registrations and definitions need correctness conditions to ensure the well-definedness of adjective clusters and terms. The correctness conditions needed for a definition (or registration) are inserted into the *gCorrectnessConditions* variable. When the correctness condition is found, we remove it from the *gCorrectnessConditions* set.

\langle Global variables introduced in *parseraddition.pas* 1349 $\rangle + \equiv$
gRedefinitions: *boolean*;

1391. \langle Local variables for parser additions 1356 $\rangle + \equiv$
gCorrCondSort: *CorrectnessKind*;
 \langle Initialize extended item by *ItemKind* 1377 $\rangle =$ *itCorrCond*:
if *CorrectnessKind*(*CurWord.Nr*) \in *gCorrectnessConditions* **then**
begin *exclude*(*gCorrectnessConditions*, *CorrectnessKind*(*CurWord.Nr*));
gCorrCondSort \leftarrow *CorrectnessKind*(*CurWord.Nr*);
if (*gRedefinitions* \wedge (*gCorrCondSort* = *syCoherence*) \wedge *ExtBlockPtr*(*gBlockPtr*) \uparrow .*nHasAssumptions*)
then *ErrImm*(243);
end
else begin *ErrImm*(72); *gCorrCondSort* \leftarrow *CorrectnessKind*(0); **end**;
itCorrectness: **if** (*gRedefinitions* \wedge *ExtBlockPtr*(*gBlockPtr*) \uparrow .*nHasAssumptions*) **then** *ErrImm*(243);

1392. The last statement needing attention will be the **scheme** block. Note that *gLocalScheme* is not used anywhere.

\langle Local variables for parser additions 1356 $\rangle + \equiv$
gLocalScheme: *boolean*;
gSchemePos: *Position*;

1393. \langle Initialize extended item by *ItemKind* 1377 $\rangle + \equiv$
itDefinition, *itSchemeHead*, *itReservation*, *itPrivFuncDefinition*, *itPrivPredDefinition*, *itConstantDefinition*,
itExemplification: ;
itCaseBlock: ;
itSchemeBlock: **begin** *gLocalScheme* \leftarrow *CurWord.Kind* \neq *sy.Scheme*; *gSchemePos* \leftarrow *CurPos*; **end**;

1394. Popping an extended item.

\langle Global variables introduced in *parseraddition.pas* 1349 $\rangle + \equiv$
gSchemeParams: *PList*;

1395. \langle Local variables for parser additions 1356 $\rangle + \equiv$

```

gPatternPos: Position;
gPattern: PatternPtr;
gNewPatternPos: Position;
gNewPattern: PatternPtr;
gSchemeIdNr: integer;
gSchemeIdPos: Position;
gSchemeConclusion: FormulaPtr;
gSchemePremises: PList;

```

Subsection 23.2.2. Popping

1396. Popping an item is invoked as part of *KillItem*, which occurs whenever (1) a semicolon is encountered, or (2) when starting a proof environment.

The contract for popping an item ensures the *nContent* field shall be populated for valid items.

NOTE: PASCAL has a set operation *include(set, element)* which adjoins an *element* to a *set*.

\langle Extended item implementation 1373 $\rangle + \equiv$

```

procedure extItemObj.Pop;
  var k: integer;
  begin gLastWSItem↑.nItemEndPos ← PrevPos;  $\langle$  Check for errors with definition items 1400  $\rangle$ 
   $\langle$  Update content of nLastWSItem based on type of item popped 1397  $\rangle$ ;
   $\langle$  Check the popped item's linkages are valid 1423  $\rangle$ ;
  if gDefiningWay ≠ dfEmpty then
    begin if gDefiniens↑.nDefSort = ConditionalDefiniens then
      include(gCorrectnessConditions, syConsistency);
    if gRedefinitions then include(gCorrectnessConditions, syCompatibility);
    end;
  inherited Pop; { (§831) }
  end;

```

1397. We will update the caller's *nLastWSItem*'s contents in most cases.

```

⟨ Update content of nLastWSItem based on type of item popped 1397 ⟩ ≡
  case nItemKind of
    itTheorem: nLastWSItem↑.nContent ← new(CompactStatementPtr, Init(new(PropositionPtr,
      Init(nLabel, gLastFormula, nPropPos)), nInference));
    ⟨ Pop a proof step 1401 ⟩
    itConclusion, itRegularStatement: ⟨ Pop a conclusion or regular statement 1408 ⟩
    itGeneralization, itLocDeclaration: ⟨ Pop a “let” statement 1410 ⟩
    ⟨ Pop a definition item 1411 ⟩
    itPredSynonym, itPredAntonym, itFuncNotation, itModeNotation, itAttrSynonym, itAttrAntonym:
      nLastWSItem↑.nContent ← new(NotationDeclarationPtr, Init(gNewPatternPos, nItemKind,
        gNewPattern, gPattern));
    ⟨ Pop a registration item 1419 ⟩
    itCorrCond: nLastWSItem↑.nContent ← new(CorrectnessConditionPtr, Init(nItemPos, gCorrCondSort,
      nInference));
    itCorrectness: nLastWSItem↑.nContent ← new(CorrectnessConditionsPtr, Init(nItemPos,
      gCorrectnessConditions, nInference));
    itProperty: nLastWSItem↑.nContent ← new(PropertyPtr, Init(nItemPos, gPropertySort, nInference));
    itSchemeHead: nLastWSItem↑.nContent ← new(SchemePtr, Init(gSchemeIdNr, gSchemeIdPos,
      gSchemeParams, gSchemePremises, gSchemeConclusion));
    ⟨ Pop skips remaining cases 1398 ⟩
  endcases

```

This code is used in section 1396.

1398. ⟨ Pop skips remaining cases 1398 ⟩ ≡

```

itPrivFuncDefinition, itPrivPredDefinition, itPragma, itDefinition, itSchemeBlock, itReservation,
  itExemplification, itCaseBlock: ;

```

This code is used in section 1397.

1399. Check for errors. We need to flag a 253 or 254 error when the user tries to introduce an axiom (which shouldn't occur much anymore, since axioms are not even documented anywhere).

```

⟨ Local variables for parser additions 1356 ⟩ +≡
  gMeansPos: Position;

```

1400. ⟨ Check for errors with definition items 1400 ⟩ ≡

```

case nItemKind of
  itDefPred, itDefFunc, itDefMode, itDefAttr: begin if gDefiningWay ≠ dfEmpty then
    begin if nDefiniensProhibited ∧ ¬AxiomsAllowed then
      begin Error(gMeansPos, 254); gDefiningWay ← dfEmpty; end;
    end
  else if ¬gRedefinitions ∧ ¬nDefiniensProhibited ∧ ¬AxiomsAllowed then SemErr(253);
  end;
endcases;

```

This code is used in section 1396.

1401. Pop a proof step. Popping a proof step should assign to the contents of the caller's *nLastWsItem* some kind of inference justification, usually in the form of a statement in the WSM syntax tree.

$\langle \text{Pop a proof step } 1401 \rangle \equiv$
itPerCases: *nLastWsItem*↑.*nContent* \leftarrow *nInference*;

See also sections 1402, 1404, and 1406.

This code is used in section 1397.

1402. Popping a reconsideration. We should assign a *TypeChangingStatement* to the content of the caller's last item, using the *nInference* field of the caller as the justification.

$\langle \text{Pop a proof step } 1401 \rangle + \equiv$
itReconsider: *nLastWsItem*↑.*nContent* \leftarrow *new*(*TypeChangingStatementPtr*, *Init*(*gReconsiderList*,
gLastType, *SimpleJustificationPtr*(*nInference*)));

1403. Popping existential elimination and introduction. We assign a *consider* (or *given*) WSM statement to the caller's previous *WSItem*'s contents when popping a choice (resp., existential assumption) item.

We should remind the reader of the grammar here:

$\langle \text{Qualified-Segment} \rangle ::= \langle \text{Variables} \rangle \langle \text{Qualification} \rangle$
 $\langle \text{Variables} \rangle ::= \langle \text{Variable} \rangle \{ \text{"}, \text{"} \langle \text{Variable} \rangle \}$
 $\langle \text{Qualification} \rangle ::= (\text{"being"} \mid \text{"be"}) \langle \text{Type-Expression} \rangle$

And, of course, a qualified-segment list is just a comma-separated list of qualified-segments.

$\langle \text{Global variables introduced in parseraddition.pas } 1349 \rangle + \equiv$
gQualifiedSegmentList: *PList*;

1404. $\langle \text{Pop a proof step } 1401 \rangle + \equiv$
itChoice: **begin** *nLastWsItem*↑.*nContent* \leftarrow *new*(*ChoiceStatementPtr*, *Init*(*gQualifiedSegmentList*,
gPremises, *SimpleJustificationPtr*(*nInference*))); *gPremises* \leftarrow **nil**;
end;
itExistentialAssumption: **begin** *nLastWsItem*↑.*nContent* \leftarrow *new*(*ExistentialAssumptionPtr*,
Init(*nItemPos*, *gQualifiedSegmentList*, *gPremises*)); *gPremises* \leftarrow **nil**;
end;

1405. Popping a stipulation. When we pop a *case*, *suppose*, or *assume* — some kind of “assumption”-like statement — we are assigning either a *CollectiveAssumption* object or a *SingleAssumption* object to the content of the *current WSItem global* variable.

$\langle \text{Local variables for parser additions } 1356 \rangle + \equiv$
gThatPos: *Position*;

1406. $\langle \text{Pop a proof step } 1401 \rangle + \equiv$
itSupposeHead, *itCaseHead*, *itAssumption*: **if** *gPremises* \neq **nil** **then**
begin *gLastWsItem*↑.*nContent* \leftarrow *new*(*CollectiveAssumptionPtr*, *Init*(*gThatPos*, *gPremises*));
gPremises \leftarrow **nil**;
end
else *gLastWsItem*↑.*nContent* \leftarrow *new*(*SingleAssumptionPtr*, *Init*(*nItemPos*, *new*(*PropositionPtr*,
Init(*nLabel*, *gLastFormula*, *nPropPos*))));

1407. Pop a conclusion or regular statement. We assign an appropriate WSM statement node to the previous item's contents.

⟨Local variables for parser additions 1356⟩ +≡
gIterativeSteps: *PList*;
gIterativeLastFormula: *FormulaPtr*;
gInference: *JustificationPtr*;

1408. ⟨Pop a conclusion or regular statement 1408⟩ ≡
case *nRegularStatementKind* **of**
stDiffuseStatement:
 nLastWSItem↑.*nContent* ← *new*(*DiffuseStatementPtr*, *Init*(*nLabel*, *stDiffuseStatement*));
stCompactStatement: *nLastWSItem*↑.*nContent* ← *new*(*CompactStatementPtr*, *Init*(*new*(*PropositionPtr*,
 Init(*nLabel*, *gLastFormula*, *nPropPos*)), *nInference*));
stIterativeEquality: *nLastWSItem*↑.*nContent* ← *new*(*IterativeEqualityPtr*, *Init*(*new*(*PropositionPtr*,
 Init(*nLabel*, *gIterativeLastFormula*, *nPropPos*)), *gInference*, *gIterativeSteps*));
endcases;

This code is used in section 1397.

1409. Pop a ‘let’ statement. For generic let statements of the form

$$\text{let } \vec{x}_1 \text{ be } T_1, \dots, \vec{x}_n \text{ be } T_n$$

we transform it to *n* statements of the form “let \vec{x} be *T*”, then add these to the *gLastWSBlock*’s items. When we have

$$\text{let } \vec{x} \text{ be } T \text{ such that } \Phi$$

we need to add a *CollectiveAssumption* node to the **global** *gLastWSBlock*’s items.

⟨Local variables for parser additions 1356⟩ +≡
gSuchPos: *Position*;

1410. ⟨Pop a “let” statement 1410⟩ ≡
begin for *k* ← 0 **to** *gQualifiedSegmentList*↑.*Count* − 1 **do**
 begin *gLastWSItem* ← *gWsTextProper*↑.*NewItem*(*nItemKind*,
 QualifiedSegmentPtr(*gQualifiedSegmentList*↑.*Items*↑[*k*]↑.*nSegmPos*);
 nLastWSItem ← *gLastWSItem*; *gLastWSItem*↑.*nContent* ← *gQualifiedSegmentList*↑.*Items*↑[*k*];
 if *k* = *gQualifiedSegmentList*↑.*Count* − 1 **then** *gLastWSItem*↑.*nItemEndPos* ← *PrevPos*
 else *gLastWSItem*↑.*nItemEndPos* ← *QualifiedSegmentPtr*(*gQualifiedSegmentList*↑.*Items*↑[*k* +
 1]↑.*nSegmPos*);
 gQualifiedSegmentList↑.*Items*↑[*k*] ← **nil**; *gLastWSBlock*↑.*nItems.Insert*(*gLastWSItem*);
 end;
 dispose(*gQualifiedSegmentList*, *Done*);
 if *gPremises* ≠ **nil** **then**
 begin *gLastWSItem* ← *gWsTextProper*↑.*NewItem*(*itAssumption*, *gSuchPos*);
 gLastWSItem↑.*nContent* ← *new*(*CollectiveAssumptionPtr*, *Init*(*gThatPos*, *gPremises*));
 gPremises ← **nil**; *gLastWSItem*↑.*nItemEndPos* ← *PrevPos*; *nLastWSItem* ← *gLastWSItem*;
 gLastWSBlock↑.*nItems.Insert*(*gLastWSItem*);
 end;
 end;

This code is used in section 1397.

1411. Pop a mode definition. A mode is either expandable (an abbreviation) or nonexpandable. For expandable modes, we just add a new *ExpandableModeDefinition* WSM object to the caller's *nLastWSItem*'s contents.

On the other hand, non-expandable modes should add to the caller's *nLastWSItem*'s contents a new *StandardModeDefinition* object. If this is not a redefinition, then we must add the “**existence**” correctness condition to the global variable *gCorrectnessConditions*.

```

⟨Pop a definition item 1411⟩ ≡
itDefMode: begin if gExpandable then nLastWSItem↑.nContent ← new(ExpandableModeDefinitionPtr,
    Init(gPatternPos, ModePatternPtr(gPattern), gLastType))
else begin nLastWSItem↑.nContent ← new(StandardModeDefinitionPtr, Init(gPatternPos,
    gRedefinitions, ModePatternPtr(gPattern), gSpecification, gDefiniens));
    if ¬gRedefinitions then include(gCorrectnessConditions, syExistence);
    end;
end;

```

See also sections 1412, 1413, 1414, and 1417.

This code is used in section 1397.

1412. Pop a functor definition. When popping a functor definition, we just add a *FunctorDefinition* object to the caller's *nLastWSItem*'s contents.

```

⟨Pop a definition item 1411⟩ +≡
itDefFunc: begin nLastWSItem↑.nContent ← new(FunctorDefinitionPtr, Init(gPatternPos,
    gRedefinitions, FunctorPatternPtr(gPattern), gSpecification, gDefiningWay, gDefiniens));
end;

```

1413. Pop an attribute definition. We just need to add an *AttributeDefinition* object to the caller's *nLastWSItem*'s contents.

```

⟨Pop a definition item 1411⟩ +≡
itDefAttr: begin nLastWSItem↑.nContent ← new(AttributeDefinitionPtr, Init(gPatternPos,
    gRedefinitions, AttributePatternPtr(gPattern), gDefiniens));
end;

```

1414. Pop a predicate definition. We just need to add a *PredicateDefinition* object to the caller's *nLastWSItem*'s contents.

```

⟨Pop a definition item 1411⟩ +≡
itDefPred: begin nLastWSItem↑.nContent ← new(PredicateDefinitionPtr, Init(gPatternPos,
    gRedefinitions, PredicatePatternPtr(gPattern), gDefiniens));
end;

```

1415. Popping a structure definition. We just need to add a *StructureDefinition* object to the caller's *nLastWSItem*'s contents.

```

⟨Global variables introduced in parseraddition.pas 1349⟩ +≡
gConstructorNr: integer;

```

```

1416. ⟨Local variables for parser additions 1356⟩ +≡
gParams: PList;
gStructFields: PList;

```

```

1417. ⟨Pop a definition item 1411⟩ +≡
itDefStruct: begin nLastWSItem↑.nContent ← new(StructureDefinitionPtr, Init(gPatternPos,
    gStructPrefixes, gConstructorNr, gParams, gStructFields));
end;

```

1418. Pop a cluster registration item. A “cluster” registration (i.e., a existential, conditional, or functor registration) adds to the caller’s *nLastWSItem*’s contents a new cluster object (of appropriate kind). The *gClusterSort* is populated when the Parser finishes a cluster registration when invoking *extItemObj.FinishAntecedent* (§1428) or similar methods.

The *gClusterTerm* is populated in the *extItemObj.FinishClusterTerm* method (§1429).

⟨Local variables for parser additions 1356⟩ +≡
gAntecedent, *gConsequent*: *PList*;
gClusterTerm: *TermPtr*;

1419. ⟨Pop a registration item 1419⟩ ≡
itCluster: **begin case** *gClusterSort* **of**
 ExistentialRegistration: **begin**
 nLastWSItem↑.*nContent* ← *new*(*EClusterPtr*, *Init*(*nItemPos*, *gConsequent*, *gLastType*));
 include(*gCorrectnessConditions*, *syExistence*)
 end;
 ConditionalRegistration: **begin** *nLastWSItem*↑.*nContent* ← *new*(*CClusterPtr*, *Init*(*nItemPos*,
 gAntecedent, *gConsequent*, *gLastType*)); *include*(*gCorrectnessConditions*, *syCoherence*);
 end;
 FunctorialRegistration: **begin** *nLastWSItem*↑.*nContent* ← *new*(*FClusterPtr*, *Init*(*nItemPos*,
 gClusterTerm, *gConsequent*, *gLastType*)); *include*(*gCorrectnessConditions*, *syCoherence*);
 end;
endcases;
end;

See also section 1422.

This code is used in section 1397.

1420. Pop a registration item. For an *identify* or *reduce* registration, we assign the content of the caller’s *nLastWSItem* a new *IdentifyRegistration* (resp., *ReduceRegistration*) object. Identify registrations use the *gIdentifyEqLocList* local variable, while the reduction registrations use the *gLeftTermInReduction* module-wide variable.

⟨Global variables introduced in *parseraddition.pas* 1349⟩ +≡
gLeftTermInReduction: *TermPtr*;

1421. ⟨Local variables for parser additions 1356⟩ +≡
gIdentifyEqLocList: *PList*;

1422. ⟨Pop a registration item 1419⟩ +≡
itIdentify: **begin** *nLastWSItem*↑.*nContent* ← *new*(*IdentifyRegistrationPtr*, *Init*(*nItemPos*, *gNewPattern*,
 gPattern, *gIdentifyEqLocList*)); *include*(*gCorrectnessConditions*, *syCompatibility*);
end;
itReduction: **begin** *nLastWSItem*↑.*nContent* ← *new*(*ReduceRegistrationPtr*, *Init*(*nItemPos*,
 gLeftTermInReduction, *gLastTerm*)); *include*(*gCorrectnessConditions*, *syReducibility*);
end;
itPropertyRegistration: *SethoodRegistrationPtr*(*nLastWSItem*↑.*nContent*)↑.*nJustification* ← *nInference*;

1423. Check linkages are valid. When popping an item, we should check if the block containing the caller is *nLinked*. If so, flag a “178” error and assign *nLinked* \leftarrow *false*. Update the block’s *nLinkAllowed* depending on the caller’s *nLinkable* field. But if the Parser is in panic mode, the containing block’s *nLinkAllowed* and *nLinkProhibited* are both assigned to false. [[This configuration appears to encode a particular state which feels a bit of a “kludge” to me...]]

```

⟨ Check the popped item’s linkages are valid 1423 ⟩ ≡
  with extBlockPtr(gBlockPtr)↑ do
    begin if nLinked then
      begin Error(nLinkPos, 178); nLinked  $\leftarrow$  false end;
      nLinkAllowed  $\leftarrow$  nLinkable; nLinkProhibited  $\leftarrow$  ¬nLinkable;
    if ¬StillCorrect then
      begin nLinkAllowed  $\leftarrow$  false; nLinkProhibited  $\leftarrow$  false end;
    end

```

This code is used in section 1396.

Subsection 23.2.3. Registrations and notations

1424. Processing synonyms. We need to update the *gNewPatternPos* and *gNewPattern* global variables when processing a synonym.

```

  define process_notation_item ≡ gNewPatternPos  $\leftarrow$  gPatternPos; gNewPattern  $\leftarrow$  gPattern
⟨ Extended item implementation 1373 ⟩ +=
procedure extItemObj.ProcessModeSynonym;
  begin process_notation_item; end;
procedure extItemObj.ProcessAttrSynonym;
  begin process_notation_item; end;
procedure extItemObj.ProcessAttrAntonym;
  begin process_notation_item; end;
procedure extItemObj.ProcessPredSynonym;
  begin process_notation_item; end;
procedure extItemObj.ProcessPredAntonym;
  begin process_notation_item; end;
procedure extItemObj.ProcessFuncSynonym;
  begin process_notation_item; end;

```

1425. Starting attributes. This is used when the Parser encounters a cluster registration (§1865). The *gAttrColl* is populated in the *extSubexpObj.CompleteAdjectiveCluster* (§1545) method.

```

⟨ Local variables for parser additions 1356 ⟩ +=
gAttrColl: PList;

```

```

1426. ⟨ Extended item implementation 1373 ⟩ +=
procedure extItemObj.StartAttributes;
  begin gAttrColl  $\leftarrow$  new(PList, Init(6));
  end;

```

1427. Starting a sentence. We just need to populate the caller’s $nPropPos$, assigning to it the current position of the Parser.

⟨Extended item implementation 1373⟩ $\vdash \equiv$
procedure *extItemObj.StartSentence*;
 begin $nPropPos \leftarrow CurPos$;
 end;

1428. Processing conditional registration. This populates the $gClusterSort$ and the related global variables, as the Parser finishes parsing the antecedent and consequent to the cluster.

⟨Extended item implementation 1373⟩ $\vdash \equiv$
procedure *extItemObj.FinishAntecedent*;
 begin $gClusterSort \leftarrow ConditionalRegistration$; $gAntecedent \leftarrow gAttrColl$;
 end;
procedure *extItemObj.FinishConsequent*;
 begin $gConsequent \leftarrow gAttrColl$;
 end;

1429. Finishing a cluster. This populates the $gClusterSort$ and the $gClusterTerm$.

⟨Extended item implementation 1373⟩ $\vdash \equiv$
procedure *extItemObj.FinishClusterTerm*;
 begin $gClusterSort \leftarrow FunctorialRegistration$; $gClusterTerm \leftarrow gLastTerm$;
 end;

1430. Identify registration. Schematically, we have the registration statement look like (using global variable names for the subexpressions):

identify $\langle gNewPattern \rangle$ **with** $\langle gPattern \rangle$ [**when** $\langle gIdentifyEqLocList \rangle$];

We store the first pattern in the $gNewPattern$ global variable, then the second pattern in the $gPattern$ global variable. Completing the identify registration will check if the current word is “when” and, if so, start a list of loci equalities.

⟨Extended item implementation 1373⟩ $\vdash \equiv$
procedure *extItemObj.StartFuncIdentify*;
 begin end;
procedure *extItemObj.ProcessFuncIdentify*;
 begin $gNewPatternPos \leftarrow gPatternPos$; $gNewPattern \leftarrow gPattern$;
 end;
procedure *extItemObj.CompleteFuncIdentify*;
 begin $gIdentifyEqLocList \leftarrow \text{nil}$;
 if $CurWord.Kind = sy_When$ **then** $gIdentifyEqLocList \leftarrow new(PList, Init(0))$;
 end;

1431. “Reduces to” registrations. Recall, these schematically look like

reduce $\langle gLeftLocus \rangle$ **to** $\langle Locus \rangle$;

Mizar will populate $gLeftLocus$. The gambit will be to treat this as a functor pattern; i.e., the $gLeftLocus$ will be used to populate $gNewPattern$ in the method *extItemObj.FinishFunctorPattern* (§1470).

⟨Local variables for parser additions 1356⟩ $\vdash \equiv$
 $gLeftLocus: LocusPtr$;

1432. $\langle \text{Extended item implementation } 1373 \rangle + \equiv$
procedure *extItemObj.ProcessLeftLocus*;
 begin *gLeftLocus* \leftarrow *new*(*LocusPtr*, *Init*(*CurPos*, *GetIdentifier*));
 end;
procedure *extItemObj.ProcessRightLocus*;
 begin *gIdentifyEqLociList.Insert*(*new*(*LociEqualityPtr*, *Init*(*PrevPos*, *gLeftLocus*, *new*(*LocusPtr*,
 Init(*CurPos*, *GetIdentifier*))));
 end;
procedure *extItemObj.StartFuncReduction*;
 begin end;
procedure *extItemObj.ProcessFuncReduction*;
 begin *gNewPatternPos* \leftarrow *gPatternPos*; *gLeftTermInReduction* \leftarrow *gLastTerm*;
 end;

Subsection 23.2.4. Processing definitions

1433. The terminology used by the Parser appears to be (§§1749 *et seq.*):

let $\langle \text{Fixed Variables} \rangle$;

and

consider $\langle \text{Fixed Variables} \rangle$ **such that**...

This would mean that we would have “fixed variables” refer to a list of qualified segments. We remind the reader of the grammar

$$\begin{aligned} \langle \text{Fixed-Variables} \rangle &::= \langle \text{Implicitly-Qualified-Variables} \rangle \{ ", " \langle \text{Fixed-Variables} \rangle \} \\ &\quad | \langle \text{Explicitly-Qualified-Variables} \rangle \{ ", " \langle \text{Fixed-Variables} \rangle \} \\ \langle \text{Implicitly-Qualified-Variables} \rangle &::= \langle \text{Variables} \rangle \\ \langle \text{Explicitly-Qualified-Variables} \rangle &::= \langle \text{Qualified-Segment} \rangle \{ ", " \langle \text{Qualified-Segment} \rangle \} \\ \langle \text{Qualified-Segment} \rangle &::= \langle \text{Variables} \rangle \langle \text{Qualification} \rangle \\ \langle \text{Variables} \rangle &::= \langle \text{Variable} \rangle \{ ", " \langle \text{Variable} \rangle \} \\ \langle \text{Qualification} \rangle &::= ("be" | "being") \langle \text{Type} \rangle \end{aligned}$$

The “fixed variables” routine in the Parser will parse a comma-separated list of qualified variables.

CAUTION: The grammar in the `syntax.txt` file is actually more strict than this, because it actually states the following:

$$\langle \text{Loci-Declaration} \rangle ::= \text{"let"} \langle \text{Qualified-Variables} \rangle [\text{"such"} \langle \text{Conditions} \rangle] ;$$

The grammar for a qualified segment *requires* implicitly qualified variables appear at the very end.

$\langle \text{Extended item implementation } 1373 \rangle + \equiv$
procedure *extItemObj.StartFixedVariables*;
 begin *gQualifiedSegmentList* \leftarrow *new*(*PList*, *Init*(0));
 end;

1434. $\langle \text{Global variables introduced in parseraddition.pas } 1349 \rangle + \equiv$
gQualifiedSegment: *MList*;
gSegmentPos: *Position*;

1435. Fixed segments. This refers to each “explicitly qualified segment” or “implicitly qualified segment” appearing in the fixed variables portion. The fixed segments are separated by commas.

⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.StartFixedSegment;
  begin gQualifiedSegment.Init(0); gSegmentPos ← CurPos;
  end;
```

1436. When parsing fixed variables, and the Parser has just entered the loop to parse fixed variables, this function will be invoked.

⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.ProcessFixedVariable;
  begin gQualifiedSegment.Insert(new(VariablePtr, Init(CurPos, GetIdentifier)));
  end;
```

1437. This “clears the cache” for assigning the type in an explicitly qualified segment (appearing in a fixed variable segment).

⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.ProcessBeing;
  begin gLastType ← nil;
  end;
```

1438. The last statement in the Parser loop when parsing “fixed variables” is to push the “fixed segment” onto the *gQualifiedSegmentList* global variable. There are two cases to consider: the implicitly qualified variables and the explicitly qualified variables.

The implicitly qualified case simply *moves* the pointers around “manually”, so we need to update every entry of *gQualifiedSegment.Items* to be **nil**. The explicitly qualified case moves the pointers around using the *MList* constructor, mutating *gQualifiedSegment* into a list of **nil** pointers.

⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.FinishFixedSegment;
  var k: integer;
  begin if gLastType ≠ nil then { explicitly qualified case }
    begin gQualifiedSegmentList↑.Insert(new(ExplicitlyQualifiedSegmentPtr, Init(gSegmentPos,
      new(PList, MoveList(gQualifiedSegment)), gLastType))); gQualifiedSegment.DeleteAll;
    end
  else begin for k ← 0 to gQualifiedSegment.Count − 1 do
    begin gQualifiedSegmentList↑.Insert(new(ImplicitlyQualifiedSegmentPtr,
      Init(VariablePtr(gQualifiedSegment.Items↑[k]↑.nVarPos, gQualifiedSegment.Items↑[k])));
      gQualifiedSegment.Items↑[k] ← nil;
    end;
  end;
  gQualifiedSegment.Done;
  end;
```

1439. When we finish parsing fixed variables, we need to “unset” the *gPremises* global variable. The Parser will either be looking at a semicolon token or at “**such** ⟨*Conditions*⟩”. The reader should note that *gSuchThatOcc* is not used in the Parser, nor anywhere else in Mizar. But we recall (§1409) the *gSuchPos* is used when popping a **let** statement.

⟨Local variables for parser additions 1356⟩ +≡

```
gSuchThatOcc: boolean; { not used }
```

1440. $\langle \text{Extended item implementation 1373} \rangle + \equiv$

```
procedure extItemObj.FinishFixedVariables;
  begin gSuchThatOcc  $\leftarrow$  CurWord.Kind = sy_Such; gSuchPos  $\leftarrow$  CurPos; gPremises  $\leftarrow$  nil;
  end;
```

1441. When the Parser encounters the statement:

let $\langle \textit{Fixed-Variables} \rangle$ **such that** $\langle \textit{Assumption} \rangle$;

The first things it does when encountering the “**such**” token is move to the next token (“**that**”) and then invoke the *StartAssumption* method. We should allocate a fresh list for *gPremises* and mark the position of the “**that**” token.

$\langle \text{Extended item implementation 1373} \rangle + \equiv$

```
procedure extItemObj.StartAssumption;
  begin gPremises  $\leftarrow$  new(PList, Init(0)); gThatPos  $\leftarrow$  CurPos;
  end;
```

1442. Finishing an assumption will update the global variable *gBlockPtr*’s field reflecting it has assumptions.

$\langle \text{Extended item implementation 1373} \rangle + \equiv$

```
procedure extItemObj.FinishAssumption;
  begin ExtBlockPtr(gBlockPtr).nHasAssumptions  $\leftarrow$  true;
  end;
```

1443. When the Mizar Parser has encountered

assume that $\langle \textit{Conditions} \rangle$;

we start a collective assumption when the Parser has just encountered the “**that**” token. As with the “**let** statement with assumptions”, we need to allocate a new list for *gPremises* and assign the *gThatPos* to the current position.

$\langle \text{Extended item implementation 1373} \rangle + \equiv$

```
procedure extItemObj.StartCollectiveAssumption;
  begin gPremises  $\leftarrow$  new(PList, Init(0)); gThatPos  $\leftarrow$  CurPos;
  end;
```


1444. Processing copula in a definition. When defining a (nonexpandable) mode, a functor, a predicate, or an attribute, we have

$$\langle Pattern \rangle \text{ means } \langle Expression \rangle;$$

or

$$\langle Pattern \rangle \text{ equals } \langle Expression \rangle;$$

The expression may or may not be labeled, we may or may not have the definition-by-cases. Whatever the situation, we should initialize the variables describing the definiens:

- the *gDefLabId* should be reset to zero (and populated in the *ProcessDefLabel* method);
- the *gDefLabPos* should be reset to the current position (and populated in the *ProcessDefLabel* method);
- the *gDefiningWay* should be assigned to *dfMeans* or *dfEquals* depending on the copula used in the definition;
- the *gOtherwise* pointer should be assigned to **nil**;
- the *gMeansPos* position should be assigned to the current position.

Following tradition in logic, we will refer to “means” and “equals” as the “**Copula**” in the definition.

\langle Global variables introduced in *parseraddition.pas* 1349 $\rangle + \equiv$
gDefLabId: integer;
gDefLabPos: Position;

1445. \langle Local variables for parser additions 1356 $\rangle + \equiv$
gOtherwise: PObject;

1446. \langle Extended item implementation 1373 $\rangle + \equiv$
procedure *extItemObj.ProcessMeans*;
 begin *gDefLabId* \leftarrow 0; *gDefLabPos* \leftarrow *CurPos*; *gDefiningWay* \leftarrow *dfMeans*; *gOtherwise* \leftarrow **nil**;
 gMeansPos \leftarrow *CurPos*
 end;
procedure *extItemObj.ProcessEquals*;
 begin *gDefLabId* \leftarrow 0; *gDefLabPos* \leftarrow *CurPos*; *gDefiningWay* \leftarrow *dfEquals*; *gOtherwise* \leftarrow **nil**;
 gMeansPos \leftarrow *CurPos*;
 end;

1447. When parsing a definition-by-cases, the cases are terminated with an “otherwise” keyword. Recall the grammar for such definitions looks like:

$$\langle Partial-Definiens-List \rangle \text{ "otherwise" } \langle Expression \rangle;$$

What happens depends on whether the definition uses “means” or “equals”: in the former case, we should update the *gOtherwise* pointer to be the *gLastFormula*; in the latter case, we should update the *gOtherwise* to be the *gLastTerm*.

\langle Extended item implementation 1373 $\rangle + \equiv$
procedure *extItemObj.FinishOtherwise*;
 begin if *gDefiningWay* = *dfEquals* **then** *gOtherwise* \leftarrow *gLastTerm*
 else *gOtherwise* \leftarrow *gLastFormula*;
 end;

1448. Starting a definiens should mutate the *it_Allowed* global variable to be equal to the caller's *nItAllowed* field. The *it_Allowed* global variable is toggled on and off when the Parser encounters “guards” in conditional definitions, whereas the *nItAllowed* fields reflects whether the sort of definition allows “it” in the definiens.

⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.StartDefiniens;
  begin it_Allowed ← nItAllowed;
  end;
```

1449. “Guards” refers to the conditions in a definition-by-cases. Specifically, we have

$$\langle \textit{Partial-Definiens} \rangle ::= \langle \textit{Expression} \rangle \text{ "if" } \langle \textit{Guard-Formula} \rangle$$

be the grammar for one particular case. We have a comma-separated list of partial definiens, so whenever the Parser (a) first encounters the “if” keyword in a definiens, or (b) has already encountered the “if” keyword and now has encountered a comma — these are the two cases to start a new guard.

⟨Local variables for parser additions 1356⟩ +≡

gPartDef: *PObject*;

1450. ⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.StartGuard;
  begin if gPartialDefs = nil then gPartialDefs ← new(PList, Init(0));
  it_Allowed ← false;
  if gDefiningWay = dfMeans then gPartDef ← gLastFormula
  else gPartDef ← gLastTerm;
  end;
```

1451. After parsing a formula, then the Parser will invoke *FinishGuard*. This will append to *gPartialDefs* a new partial definiens.

⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.FinishGuard;
  begin it_Allowed ← nItAllowed;
  case gDefiningWay of
    dfMeans: gPartialDefs.Insert(new(PartDefPtr, Init(new(DefExpressionPtr, Init(exFormula, gPartDef)), gLastFormula)));
    dfEquals: gPartialDefs.Insert(new(PartDefPtr, Init(new(DefExpressionPtr, Init(exTerm, gPartDef)), gLastFormula)));
  endcases;
  end;
```

1452. Recall for functor definitions we have something like:

```
func ⟨Pattern⟩ -> ⟨Type⟩ ( means | equals ) ...
```

Similarly, nonexpandable modes look like

```
mode ⟨Pattern⟩ -> ⟨Type⟩ means ...
```

The “-> ⟨Type⟩” is called the [type] *specification* for the definition. We should update the *gSpecification* global variable to point to whatever the last type parsed was — which is stored in the *gLastType* global variable.

```
⟨Extended item implementation 1373⟩ +≡
procedure extItemObj.FinishSpecification;
  begin gSpecification ← gLastType;
  end;
```

1453. “Construction type” is the term used by the Parser for “nonexpandable modes”. They, too, have a type specification. The *FinishConstructionType* populates the *gSpecification* global variable with this type.

```
⟨Extended item implementation 1373⟩ +≡
procedure extItemObj.FinishConstructionType;
  begin gSpecification ← gLastType;
  end;
```

1454. Expandable mode definitions, after encountering the “is” keyword, invokes the *StartExpansion* method. This just ensures there is no definiens, and the *gExpandable* global variable is assigned to “true”.

```
⟨Extended item implementation 1373⟩ +≡
procedure extItemObj.StartExpansion;
  begin if gRedefinitions then ErrImm(271);
  nDefiniensProhibited ← true; gExpandable ← true;
  end;
```

1455. The Parser, when determining the pattern for an attribute (§1812), resets the state when starting to determine the pattern for the attribute. This is handled by the *StartAttribute* method.

We should remind the reader that attributes can only have arguments *to its left*.

```
⟨Global variables introduced in parseraddition.pas 1349⟩ +≡
gParamNbr: integer;
```

1456. ⟨Local variables for parser additions 1356⟩ +≡
gLocus: LocusPtr;

```
1457. ⟨Extended item implementation 1373⟩ +≡
procedure extItemObj.StartAttributePattern;
  begin gParamNbr ← 0; gParams ← nil; gLocus ← new(LocusPtr, Init(CurPos, GetIdentifier));
  end;
```

1458. Since an attribute can only have attributes to its left, it's pretty clear when the attribute pattern has been parsed: the Parser has found the attribute being defined. In that case (assuming we're not panicking), we should add the attribute format to the *gFormatsColl* dictionary and update the global variables.

⟨Extended item implementation 1373⟩ +≡

procedure *extItemObj.FinishAttributePattern*;

var *lFormatNr*: integer;

begin *lFormatNr* ← 0;

if (*CurWord.Kind* = *AttributeSymbol*) ∧ *stillcorrect* **then**

lFormatNr ← *gFormatsColl.CollectPrefixForm*(*ˆVˆ*, *CurWord.Nr*, *gParamNbr*);

gPatternPos ← *CurPos*; *gConstructorNr* ← *CurWord.Nr*;

gPattern ← *new*(*AttributePatternPtr*, *Init*(*gPatternPos*, *gLocus*, *gConstructorNr*, *gParams*));

end;

1459. A mode definition may include a “sethood” property. This particular function is used when registering sethood in a registration block.

⟨Extended item implementation 1373⟩ +≡

procedure *extItemObj.FinishSethoodProperties*;

begin

nLastWSItem↑.*nContent* ← *new*(*SethoodRegistrationPtr*, *Init*(*nItemPos*, *gPropertySort*, *gLastType*));

end;

1460. We remind the reader the grammar for a mode pattern

$$\langle \text{Mode-Pattern} \rangle ::= \langle \text{Mode-Symbol} \rangle [\text{"of"} \langle \text{Loc} \rangle]$$

The loci parameters can only appear *after* the mode symbol (and before the “of” reserved keyword). Starting a mode pattern should reset the relevant global variables.

⟨Extended item implementation 1373⟩ +≡

procedure *extItemObj.StartModePattern*;

begin *gParamNbr* ← 0; *gParams* ← **nil**; *gPatternPos* ← *CurPos*; *gConstructorNr* ← *CurWord.Nr*;

end;

1461. Finishing a mode pattern should build a new *ModePatternObj*, and store it in the *gPattern* global variable. And if we are not panicking, we should add it to the *gFormatsColl* dictionary.

⟨Extended item implementation 1373⟩ +≡

procedure *extItemObj.FinishModePattern*;

var *lFormatNr*: integer;

begin *lFormatNr* ← 0;

if *StillCorrect* **then** *lFormatNr* ← *gFormatsColl.CollectPrefixForm*(*ˆMˆ*, *gConstructorNr*, *gParamNbr*);

gPattern ← *new*(*ModePatternPtr*, *Init*(*gPatternPos*, *gConstructorNr*, *gParams*));

end;

1462. When Parser starts parsing a new predicate pattern, we should reset the relevant global variables.

⟨Extended item implementation 1373⟩ +≡

procedure *extItemObj.StartPredicatePattern*;

begin *gParamNbr* ← 0; *gParams* ← **nil**;

end;

1463. When the Parser tries to parse a “predicative formula” (i.e., a formula involving a predicate) — including predicate patterns — the first thing it does is invoke this *ProcessPredicateSymbol* method. This resets the global variables needed to populate the arguments to the predicate in the formula.

⟨Global variables introduced in *parseraddition.pas* 1349⟩ +≡
gLeftLocINbr: *integer*;

1464. ⟨Local variables for parser additions 1356⟩ +≡
gLeftLocI: *PList*;

1465. ⟨Extended item implementation 1373⟩ +≡
procedure *extItemObj.ProcessPredicateSymbol*;
 begin *gPatternPos* ← *CurPos*; *gLeftLocINbr* ← *gParamNbr*; *gLeftLocI* ← *gParams*; *gParamNbr* ← 0;
 gParams ← **nil**; *gConstructorNr* ← *CurWord.Nr*;
 end;

1466. Finishing a predicate pattern will create a new *PredicatePattern* object, update the *gPattern* global variable to point to it, and (if the Parser is not panicking) add the predicate’s format to the *gFormatsColl* dictionary.

⟨Extended item implementation 1373⟩ +≡
procedure *extItemObj.FinishPredicatePattern*;
 var *lFormatNr*: *integer*;
 begin *lFormatNr* ← 0;
 if *StillCorrect* **then**
 lFormatNr ← *gFormatsColl.CollectPredForm*(*gConstructorNr*, *gLeftLocINbr*, *gParamNbr*);
 gPattern ← *new*(*PredicatePatternPtr*, *Init*(*gPatternPos*, *gLeftLocI*, *gConstructorNr*, *gParams*));
 end;

1467. Functor patterns a bit trickier. When starting one, what should occur depends on the type of functor being defined. Specifically, we handle brackets differently than other functors, and within the brackets we handle braces (i.e., definitions like $\{x_1, \dots, x_n\}$) differently than square brackets ($[x_1, \dots, x_n]$) differently than everything other functor bracket.

In all cases, even non-bracket functors, we need to reset the *gParamNbr* and *gParams* global variables so they may be populated correctly.

⟨Global variables introduced in *parseraddition.pas* 1349⟩ +≡
gSubItemKind: *TokenKind*;

1468. ⟨Extended item implementation 1373⟩ +≡
procedure *extItemObj.StartFunctorPattern*;
 begin *gPatternPos* ← *CurPos*; *gSubItemKind* ← *CurWord.Kind*;
 case *CurWord.Kind* **of**
 LeftCircumfixSymbol: *gConstructorNr* ← *CurWord.Nr*;
 sy_LeftSquareBracket: **begin** *gSubItemKind* ← *LeftCircumfixSymbol*; *gConstructorNr* ← *SquareBracket*
 end;
 sy_LeftCurlyBracket: **begin** *gSubItemKind* ← *LeftCircumfixSymbol*; *gConstructorNr* ← *CurlyBracket*
 end;
 othercases *gConstructorNr* ← 0;
 endcases; *gParamNbr* ← 0; *gParams* ← **nil**;
 end;

1469. For “non-bracket” functors (i.e., infix operators), the functor pattern is processed by (1) getting the left parameters, (2) processing the functor symbol, (3) getting the right parameters. This function is precisely step (2).

⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.ProcessFunctorSymbol;
  begin gPatternPos ← CurPos;
  if CurWord.Kind = InfixOperatorSymbol then
    begin gSubItemKind ← InfixOperatorSymbol; gConstructorNr ← CurWord.Nr;
    gLeftLociNbr ← gParamNbr; gLeftLocs ← gParams; gParamNbr ← 0; gParams ← nil;
    end;
  end;
```

1470. When defining a bracket functor pattern, we add a new bracket format to the *gFormatsColl* dictionary, and then set *gPattern* to a newly allocated Bracket pattern.

When defining an infix functor, we add a new functor format to the *gFormatsColl* dictionary, and then we set the *gPattern* to a newly allocated infix functor pattern.

The “other cases” constructs an infix functor pattern, but does not add the form to the *gFormatsColl* dictionary.

⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.FinishFunctorPattern;
  var lConstructorNr, lFormatNr: integer;
  begin lFormatNr ← 0;
  case gSubItemKind of
    LeftCircumfixSymbol: begin lConstructorNr ← CurWord.Nr;
      if StillCorrect then
        lFormatNr ← gFormatsColl.CollectBracketForm(gConstructorNr, lConstructorNr, gParamNbr, 0, 0);
        gPattern ← new(CircumfixFunctorPatternPtr, Init(gPatternPos, gConstructorNr, lConstructorNr,
          gParams));
        end;
      InfixOperatorSymbol: begin if StillCorrect then
        lFormatNr ← gFormatsColl.CollectFuncForm(gConstructorNr, gLeftLocsNbr, gParamNbr);
        gPattern ← new(InfixFunctorPatternPtr, Init(gPatternPos, gLeftLocs, gConstructorNr, gParams));
        end;
      othercases
        gPattern ← new(InfixFunctorPatternPtr, Init(gPatternPos, gLeftLocs, gConstructorNr, gParams));
      endcases;
  end;
```

1471. The Parser’s *ReadVisible* procedure begins by invoking this *StartVisible* method. The *ReadVisible* procedure occurs when getting most patterns.

⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.StartVisible;
  begin gParams ← new(PList, Init(0));
  end;
```

1472. The Parser iteratively calls its *GetVisible* (§1802) procedure when *ReadVisible* arguments in a pattern. The *GetVisible* procedure in turn invokes this *ProcessVisible*, which increments the number of parameters, and pushes a new *Locus* object onto the *gParams* stack.

⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.ProcessVisible;
begin inc(gParamNbr);
if gParams ≠ nil then gParams↑.Insert(new(LocusPtr, Init(CurPos, GetIdentifier)));
end;
```

1473. Recall a structure definition, when it has ancestors, looks like

struct (⟨*Ancestors*⟩) ⟨*Structure-Symbol*⟩ ...

The ⟨*Ancestors*⟩ field is considered the “prefix” to the structure definition. The Parser parses a type (thereby populating the *gLastType* global variable), then invokes the *FinishPrefix* method, then iterates if it encounters a comma.

The *FinishPrefix* method pushes the *gLastType* global variable to the *gStructPrefixes* state variable.

⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.FinishPrefix;
begin gStructPrefixes.Insert(gLastType);
end;
```

1474. ⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.ProcessStructureSymbol;
var lFormatNr: integer;
begin gConstructorNr ← 0; gPatternPos ← CurPos;
if CurWord.Kind = StructureSymbol then gConstructorNr ← CurWord.Nr;
lFormatNr ← gFormatsColl.CollectPrefixForm(^J^, gConstructorNr, 1); gParamNbr ← 0;
gParams ← nil;
end;
```

1475. When the Parser has just finished parsing the ancestors to a structure, but has not parsed the visible arguments. Then the Parser prepares for reading the visible arguments and then the fields by invoking this method. This initializes the *gStructFields* state variable as well as the *gFieldsNbr* state variable.

⟨Global variables introduced in *parseraddition.pas* 1349⟩ +≡

gFieldsNbr: *integer*;

1476. ⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.StartFields;
var lFormatNr: integer;
begin lFormatNr ← gFormatsColl.CollectPrefixForm(^L^, gConstructorNr, gParamNbr);
in_AggrPattern ← true; gStructFields ← new(PList, Init(0)); gFieldsNbr ← 0;
end;
```

1477. The Parser has just encountered the end structure bracket (“#”) token, so we want to add the format to the *gFormatsColl* dictionary.

⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.FinishFields;
var lFormatNr: integer;
begin lFormatNr ← gFormatsColl.CollectPrefixForm(^G^, gConstructorNr, gFieldsNbr);
end;
```

1478. Recall that each field-segment looks like

$$\langle \textit{Field-Segment} \rangle ::= \langle \textit{Selector-Symbol} \rangle \{ ", " \langle \textit{Selector-Symbol} \rangle \} \langle \textit{Specification} \rangle$$

Before parsing the field-segment, the *StartAggrPattSegment* is invoked.

$\langle \text{Local variables for parser additions 1356} \rangle + \equiv$
gStructFieldsSegment: *PList*;
gSgmPos: *Position*;

1479. $\langle \text{Extended item implementation 1373} \rangle + \equiv$
procedure *extItemObj.StartAggrPattSegment*;
 begin *gStructFieldsSegment* \leftarrow *new(Plist, Init(0))*; *gSgmPos* \leftarrow *CurPos*;
 end;

1480. For each selector-symbol the Parser encounters, it invokes the *ProcessField*.

$\langle \text{Extended item implementation 1373} \rangle + \equiv$
procedure *extItemObj.ProcessField*;
 var *lFormatNr*: *integer*;
 begin *lFormatNr* \leftarrow *gFormatsColl.CollectPrefixForm*(`U' , *CurWord.Nr*, 1);
 gStructFieldsSegment.*Insert*(*new(FieldSymbolPtr, Init(CurPos, CurWord.Nr))*); *inc(gFieldsNbr)*;
 end;

1481. After each field has been parsed, the Parser invokes this method to update the *gStructFields* will push a new field segment object onto it.

$\langle \text{Extended item implementation 1373} \rangle + \equiv$
procedure *extItemObj.FinishAggrPattSegment*;
 begin *gStructFields.Insert*(*new(FieldSegmentPtr, Init(gSgmPos, gStructFieldsSegment, gLastType))*);
 end;

Subsection 23.2.5. Processing remaining statements

1482. Processing schemes. Most of these methods are used in parsing a scheme block (§1882). It will be useful to examine that function to see where these methods are invoked.

When the Parser starts a new scheme, several state variables need to be reset. The *gSchemeIdNr* is populated by the *GetIdentifier* (§1348) procedure, the *gSchemeIdPos* is assigned the current position, and the *gSchemeParams* should be allocated to an empty list.

$\langle \text{Extended item implementation 1373} \rangle + \equiv$
procedure *extItemObj.ProcessSchemeName*;
 begin *gSchemeIdNr* \leftarrow *GetIdentifier*; *gSchemeIdPos* \leftarrow *CurPos*;
 gSchemeParams \leftarrow *new(PList, Init(0))*;
 end;

1483. A scheme qualification segment looks like, for predicates:

$$\langle \text{Variable} \rangle \{ \text{ " , " } \langle \text{Variable} \rangle \} \text{ " [" } [\langle \text{Type-Expression-List} \rangle] \text{ "] "}$$

And for functors:

$$\langle \text{Variable} \rangle \{ \text{ " , " } \langle \text{Variable} \rangle \} \text{ " (" } [\langle \text{Type-Expression-List} \rangle] \text{ ") "}$$

When the comma-separated list of identifiers have all been read, but before either “(” or “[” has been discerned, the Parser invokes *StartSchemeQualification*.

This will assign the current word kind to *gSubItemKind*, and then initialize the *gTypeList* to 4 items.

\langle Global variables introduced in `parseraddition.pas` 1349 $\rangle + \equiv$
gTypeList: *MList*;

1484. \langle Extended item implementation 1373 $\rangle + \equiv$
procedure *extItemObj.StartSchemeQualification*;
 begin *gSubItemKind* \leftarrow *CurWord.Kind*; *gTypeList.Init*(4);
 end;

1485. After the type-list has been parsed, but before the closing parentheses or bracket has been encountered, the Parser invokes the *FinishSchemeQualification* method. This assigns the current position to the *gSubItemPos*.

\langle Global variables introduced in `parseraddition.pas` 1349 $\rangle + \equiv$
gSubItemPos: *Position*;

1486. \langle Extended item implementation 1373 $\rangle + \equiv$
procedure *extItemObj.FinishSchemeQualification*;
 begin *gSubItemPos* \leftarrow *CurPos*
 end;

1487. Starting a scheme segment describes the situation where we are *just about* to start parsing the comma-separated list of identifiers for the scheme parameters. This just assigns the current position to the *gSubItemPos*, then initializes *gSchVarIds* to 2 spots.

\langle Global variables introduced in `parseraddition.pas` 1349 $\rangle + \equiv$
gSchVarIds: *MList*;

1488. \langle Extended item implementation 1373 $\rangle + \equiv$
procedure *extItemObj.StartSchemeSegment*;
 begin *gSubItemPos* \leftarrow *CurPos*; *gSchVarIds.Init*(2);
 end;

1489. After parsing the identifier for an entry in the comma-separated list of scheme variables, the Parser invokes *ProcessSchemeVariable* to add the recently parsed identifier to the *gSchVarIds* state variable.

\langle Extended item implementation 1373 $\rangle + \equiv$
procedure *extItemObj.ProcessSchemeVariable*;
 begin *gSchVarIds.Insert*(*new*(*VariablePtr*, *Init*(*CurPos*, *GetIdentifier*)));
 end;

1490. Once the list of scheme variables and their type specification has been parsed, then the Parser invokes the *FinishSchemeSegment* method. This just turns the *gSchVarIds* list into a Predicate segment or a Functor segment, using the type list the Parser just finished parsing.

⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.FinishSchemeSegment;
  begin case gSubItemKind of
    sy_LeftParanthesis: begin gSchemeParams.Insert(new(FunctorSegmentPtr, Init(gSubItemPos,
      new(PList, MoveList(gSchVarIds)), new(PList, MoveList(gTypeList)), gLastType)));
    end;
    sy_LeftSquareBracket: begin gSchemeParams.Insert(new(SchemeSegmentPtr, Init(gSubItemPos,
      PredicateSegment, new(PList, MoveList(gSchVarIds)), new(PList, MoveList(gTypeList))));
    end;
  endcases;
end;
```

1491. The “scheme thesis” is the formula statement of the scheme. Informally, a scheme looks like:

scheme {⟨Scheme-Parameters⟩} ⟨Scheme-thesis⟩ **"provided"** ⟨Scheme-premises⟩

This means the *gLastFormula* state variable contains the scheme’s thesis. But the Parser has not yet started the list of premises. This is when the Parser invokes the *FinishSchemeThesis* method, which assigns the *gLastFormula* to *gSchemeConclusion*, then allocates a new empty list for the *gSchemePremises*.

⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.FinishSchemeThesis;
  begin gSchemeConclusion ← gLastFormula; gSchemePremises ← new(Plist, Init(0));
  end;
```

1492. The premises for a scheme consists of finitely many formulas separated by “**and**” keywords. The Parser enters into a loop invoking this method *after* parsing the formula but *before* checking the next word is “**and**” (and iterating loop). We just need to push the formula onto the *gSchemePremises* list.

⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.FinishSchemePremise;
  begin gSchemePremises↑.Insert(new(PropositionPtr, Init(nLabel, gLastFormula, nPropPos)));
  end;
```

1493. Reserved variables. These methods are invoked only when the Parser parses a reservation (§1878). A “reservation segment” refers to the comma-separated list of variables and the type.

Starting a reservation segment allocates a new (empty) list for *gResIdents*, and assigns the *gResPos* to the current position. Each variable encountered in the comma-separated list of variables is appended to the *gResIdents* list using the *ProcessReservedIdentifier* method.

Mizar treats each reservation segment as a separate statement. So there is no difference between:

```
reserve G for Group, x,y,z for Element of G;
...and...
```

```
reserve G for Group;
reserve x,y,z for Element of G;
```

Finishing a reservation mutates both the *gLastWSItem* and *gLastWSBlock* global variables. Specifically, we allocate a new reservation *Item*, then update *gLastWSItem* to point to it. The caller’s *nLastWSItem* is updated to point to it, too. We assign the content of this newly allocated reservation *Item* based on the *gResIdents* list. We insert this *Item* to the end of the *gLastWSBlock*’s items.

⟨Global variables introduced in *parseraddition.pas* 1349⟩ +≡
gResIdents: *PList*;
gResPos: *Position*;

1494. ⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.StartReservationSegment;
begin gResIdents ← new(Plist, Init(0)); gResPos ← CurPos;
end;
```

```
procedure extItemObj.ProcessReservedIdentifier;
begin gResIdents↑.Insert(new(VariablePtr, Init(CurPos, GetIdentifier)));
end;
```

```
procedure extItemObj.FinishReservationSegment;
begin gLastWSItem ← gWsTextProper↑.NewItem(itReservation, gResPos);
nLastWSItem ← gLastWSItem;
gLastWSItem↑.nContent ← new(ReservationSegmentPtr, Init(gResIdents, gLastType));
gLastWSItem↑.nItemEndPos ← PrevPos; gLastWSBlock↑.nItems.Insert(gLastWSItem);
end;
```

1495. Both “defpred” and “deffunc” invokes *StartPrivateDefiniendum* to initialize the *gTypeList*, store the identifier in the *gPrivateId*, and assign the current position to the *gPrivateIdPos*. Further, *dolAllowed* is toggled to *true* — placeholder variables are going to be allowed in the type declarations of the private functor or private predicate (for example “defpred Foo[set, Element of \$1]”).

⟨Global variables introduced in *parseraddition.pas* 1349⟩ +≡
gPrivateId: *Integer*;
gPrivateIdPos: *Position*;

1496. ⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.StartPrivateDefiniendum;
begin gPrivateId ← GetIdentifier; gPrivateIdPos ← CurPos; dolAllowed ← true; gTypeList.Init(4);
end;
```

1497. Reading a “type list” (for scheme parameters or for private definitions) loops over reading a type, then pushing it onto the *gTypeList*. The parser delegates that latter “push work” to the *FinishLocusType* method.

⟨Extended item implementation 1373⟩ +≡
procedure *extItemObj.FinishLocusType*;
 begin *gTypeList.Insert(gLastType)*;
 end;

1498. The life-cycle of expressions is a little convoluted. The *Item* will allocate a new *extExpression* object and assign it to the *gExpPtr*. Later, almost always, the *gExpPtr* will invoke a method to create a subexpression. This subexpression will be populated, then the *gLastTerm* (or *gLastFormula*) will be updated to point to this subexpression object. The expression object will be freed.

⟨Extended item implementation 1373⟩ +≡
procedure *extItemObj.CreateExpression*(*fExpKind* : *ExpKind*);
 begin *gExpPtr* ← *new(extExpressionPtr, Init(fExpKind))*;
 end;

1499. Recall the “set” statement is of the form

$$\text{"set" } \langle \text{Variable} \rangle \text{"=" } \langle \text{Term} \rangle \{ \text{"," } \langle \text{Variable} \rangle \text{"=" } \langle \text{Term} \rangle \}$$

The Parser parses this as a loop of assignments of terms to identifiers. Before iterating, the Parser invokes the *FinishPrivateConstant* method. This allocates a new item for the constant definition, then assigns it to the *gLastWSItem* and to the caller’s *nLastWSItem* field. Then the content for the new item is allocated to be a constant definition object using the *VariablePtr* state variable and the *gLastTerm* state variable. The *gLastBlock* global variable pushes the new constant definition item to its contents.

⟨Extended item implementation 1373⟩ +≡
procedure *extItemObj.FinishPrivateConstant*;
 begin *gLastWSItem* ← *gWsTextProper*↑.*NewItem(itConstantDefinition, nItemPos)*;
 nLastWSItem ← *gLastWSItem*; *gLastWSItem*↑.*nContent* ← *new(ConstantDefinitionPtr,*
 Init(new(VariablePtr, Init(gPrivateIdPos, gPrivateId)), gLastTerm));
 gLastWSItem↑.*nItemEndPos* ← *PrevPos*; *gLastWSBlock*↑.*nItems.Insert(gLastWSItem)*;
 nItemPos ← *CurPos*;
 end;

1500. When the Parser is about to start parsing an assignment “⟨*Variable*⟩ = ⟨*Term*⟩” in a “set” statement, the Parser invokes this method. The caller assigns the *gPrivateId* state variable to be the result of *GetIdentifier*, and the *gPrivateIdPos* state variable to be the current position.

⟨Extended item implementation 1373⟩ +≡
procedure *extItemObj.StartPrivateConstant*;
 begin *gPrivateId* ← *GetIdentifier*; *gPrivateIdPos* ← *CurPos*;
 end;

1501. For a “defpred” and a “deffunc”, before parsing the definiens, we need to set the *dol_Allowed* global variable to true (to allow placeholder variables).

⟨Extended item implementation 1373⟩ +≡
procedure *extItemObj.StartPrivateDefiniens*;
 begin *dol_Allowed* ← *true*;
 end;

1502. After parsing the definiendum term for a “**deffunc**”, the Parser invokes this *FinishPrivateFuncDefinienition* method. This assigns the contents of the caller to a WSM private functor definition syntax tree.

⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.FinishPrivateFuncDefinienition;
  begin nLastWSItem↑.nContent ← new(PrivateFunctorDefinitionPtr, Init(new(VariablePtr,
    Init(gPrivateIdPos, gPrivateId)), new(PList, MoveList(gTypeList)), gLastTerm));
  end;
```

1503. When finishing the definiendum formula for a “**defpred**”, the Parser invokes this *FinishPrivatePredDefinienition* method.

⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.FinishPrivatePredDefinienition;
  begin nLastWSItem↑.nContent ← new(PrivatePredicateDefinitionPtr, Init(new(VariablePtr,
    Init(gPrivateIdPos, gPrivateId)), new(PList, MoveList(gTypeList)), gLastFormula));
  end;
```

1504. Reconsider statements.

⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.ProcessReconsideredVariable;
  begin gPrivateId ← GetIdentifier; gPrivateIdPos ← CurPos;
  end;
```

```
procedure extItemObj.FinishReconsideredTerm;
  begin gReconsiderList↑.Insert(new(TypeChangePtr, Init(Equating, new(VariablePtr,
    Init(gPrivateIdPos, gPrivateId)), gLastTerm)));
  end;
```

1505. This is invoked when parsing a private item which is a “**reconsider**” statement.

⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.FinishDefaultTerm;
  begin gReconsiderList↑.Insert(new(TypeChangePtr, Init(VariableIdentifier, new(VariablePtr,
    Init(gPrivateIdPos, gPrivateId)), nil)));
  end;
```

1506. When the Parser finishes parsing a formula in “**consider** ⟨Segment⟩ **such that** ⟨Formula⟩ {**and** ⟨Formula⟩}”, the Parser invokes the *FinishCondition* method. This checks that *gPremises* has been allocated, then pushes a new labeled formula into it.

⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.FinishCondition;
  begin if gPremises = nil then gPremises ← new(PList, Init(0));
  gPremises↑.Insert(new(PropositionPtr, Init(nLabel, gLastFormula, nPropPos)));
  end;
```

1507. In statements of the form

assume $\langle \text{Formula} \rangle$;

Or of the form

assume $\langle \text{Formula} \rangle$ **and** $\langle \text{Formula} \rangle$ **and** ... **and** $\langle \text{Formula} \rangle$;

After each formula parsed, the Parser invokes the *FinishHypothesis*. This just inserts a new labeled formula into the *gPremises* state variable, when the *gPremises* state variable is not **nil**.

$\langle \text{Extended item implementation 1373} \rangle + \equiv$

```
procedure extItemObj.FinishHypothesis;
  begin if gPremises  $\neq$  nil then
    gPremises $\uparrow$ .Insert(new(PropositionPtr, Init(nLabel, gLastFormula, nPropPos)));
  end;
```

1508. “Take” statements. For statements of the form

take $\langle \text{Variable} \rangle = \langle \text{Term} \rangle$;

The Parser invokes the *ProcessExemplifyingVariable* method, then parses the term, and then constructs the AST by invoking *FinishExemplifyingVariable*.

Finishing a “take” statement mutates both the *gLastWSItem* and the *gLastWSBlock* global variables.

$\langle \text{Extended item implementation 1373} \rangle + \equiv$

```
procedure extItemObj.ProcessExemplifyingVariable;
  begin gPrivateId  $\leftarrow$  GetIdentifier; gPrivateIdPos  $\leftarrow$  CurPos;
  end;
```

```
procedure extItemObj.FinishExemplifyingVariable;
  begin gLastWSItem  $\leftarrow$  gWsTextProper $\uparrow$ .NewItem(itExemplification, nItemPos);
  nLastWSItem  $\leftarrow$  gLastWSItem; gLastWSItem $\uparrow$ .nContent  $\leftarrow$  new(ExamplePtr, Init(new(VariablePtr,
    Init(gPrivateIdPos, gPrivateId)), gLastTerm)); gLastWSItem $\uparrow$ .nItemEndPos  $\leftarrow$  PrevPos;
  gLastWSBlock $\uparrow$ .nItems.Insert(gLastWSItem); nItemPos  $\leftarrow$  CurPos;
  end;
```

1509. In statements of the form

take $\langle Term \rangle$;

the Parser begins by invoking *StartExemplifyingTerm*, parses the term, then *FinishExemplifyingTerm*.

\langle Extended item implementation 1373 $\rangle + \equiv$

```
procedure extItemObj.StartExemplifyingTerm;
  begin if (CurWord.Kind = Identifier)  $\wedge$  extBlockPtr(gBlockPtr) $\uparrow$ .nInDiffuse  $\wedge$  ((AheadWord.Kind =
    sy_Comma)  $\vee$  (AheadWord.Kind = sy_Semicolon)) then
    begin gPrivateId  $\leftarrow$  GetIdentifier; gPrivateIdPos  $\leftarrow$  CurPos;
    end
  else gPrivateId  $\leftarrow$  0;
  end;

procedure extItemObj.FinishExemplifyingTerm;
  begin gLastWSItem  $\leftarrow$  gWsTextProper $\uparrow$ .NewItem(itExemplification, nItemPos);
  nLastWSItem  $\leftarrow$  gLastWSItem;
  if gPrivateId  $\neq$  0 then gLastWSItem $\uparrow$ .nContent  $\leftarrow$  new(ExamplePtr, Init(new(VariablePtr,
    Init(gPrivateIdPos, gPrivateId)), nil))
  else gLastWSItem $\uparrow$ .nContent  $\leftarrow$  new(ExamplePtr, Init(nil, gLastTerm));
  gLastWSItem $\uparrow$ .nItemEndPos  $\leftarrow$  PrevPos; gLastWSBlock $\uparrow$ .nItems.Insert(gLastWSItem);
  nItemPos  $\leftarrow$  CurPos;
  end;
```

1510. When the Parser examines the correctness conditions (§1836), it loops over the correctness conditions and justifications. Afterwards, it invokes the *ProcessCorrectness* method, which tests that the Parser is not current looking at a correctness keyword. Then it tests if *gCorrectnessConditions* is empty or *AxiomsAllowed* (in which case, correctness has been satisfies, so the Parser moves happily along). But if *gCorrectnessConditions* $\neq \emptyset$ or axioms are not allowed, then a 73 error is raised.

\langle Extended item implementation 1373 $\rangle + \equiv$

```
procedure extItemObj.ProcessCorrectness;
  begin if CurWord.Kind  $\neq$  sy_Correctness then
    if (gCorrectnessConditions  $\neq$  [])  $\wedge$   $\neg$ AxiomsAllowed then Error(gDefPos, 73);
  end;
```

1511. A “construction type” appears in a redefinition where the type is redefined. In such a situation, we need to add “coherence” as a correctness condition. The *StartConstructionType* handles this task.

\langle Extended item implementation 1373 $\rangle + \equiv$

```
procedure extItemObj.StartConstructionType;
  begin if gRedefinitions  $\wedge$  (CurWord.Kind = sy_Arrow) then
    include(gCorrectnessConditions, syCoherence);
  end;
```

1512. This is used in the Parser’s *ProcessLab* procedure. Really, all the work is being done here: the *nLabel* field of the caller is assigned to a newly allocated *Label* object.

\langle Extended item implementation 1373 $\rangle + \equiv$

```
procedure extItemObj.ProcessLabel;
  begin nLabelIdNr  $\leftarrow$  0; nLabelIdPos  $\leftarrow$  CurPos;
  if (CurWord.Kind = Identifier)  $\wedge$  (AheadWord.Kind = sy_Colon) then nLabelIdNr  $\leftarrow$  CurWord.Nr;
  nLabel  $\leftarrow$  new(LabelPtr, Init(nLabelIdNr, nLabelIdPos));
  end;
```

1513. A regular statement is either a “diffuse” statement (which occurs with the “now” keyword) or else it’s a “compact” statement.

⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.StartRegularStatement;
  begin if CurWord.Kind = sy_Now then nRegularStatementKind ← stDiffuseStatement
  else nRegularStatementKind ← stCompactStatement;
  end;
```

1514. If the Parser encounters a colon after the copula, then it invokes this method to construct a label for the Definiens.

⟨Global variables introduced in *parseraddition.pas* 1349⟩ +≡

gDefLabel: *LabelPtr*;

1515. ⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.ProcessDefiniensLabel;
  begin gDefLabId ← 0; gDefLabPos ← CurPos;
  if (CurWord.Kind = Identifier) ∧ (AheadWord.Kind = sy_Colon) then gDefLabId ← CurWord.Nr;
  gDefLabel ← new(LabelPtr, Init(gDefLabId, gDefLabPos));
  end;
```

1516. The Parser, having encountered “from” and a non-MML reference, tries to treat the identifier as the label for a scheme declared in the current article. The *nInference* field would be a *SchemeJustification* object, so we just populate its *nSchemeIdNr* and position fields.

⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.ProcessSchemeReference;
  begin if CurWord.Kind = Identifier then
    begin SchemeJustificationPtr(nInference)↑.nSchemeIdNr ← CurWord.Nr;
    SchemeJustificationPtr(nInference)↑.nSchemeInfPos ← CurPos;
    end;
  end;
```

1517. When a “by” refers to a theorem or definition from an article in the MML, the Parser invokes the *StartLibraryReference* method.

⟨Global variables introduced in *parseraddition.pas* 1349⟩ +≡

gTHEFileNr: *integer*;

1518. ⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.StartLibraryReferences;
  begin gTHEFileNr ← CurWord.Nr;
  end;
```

1519. The Parser has already encountered a “from” and then an MML article identifier. Before continuing to parse the scheme number, the Parser invokes this method to initialize the relevant state variables.

⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.StartSchemeLibraryReference;
  begin gTHEFileNr ← CurWord.Nr;
  end;
```


1520. For references to labels found in the article being processed (“private references”), this method is invoked.

⟨Extended item implementation 1373⟩ +≡
procedure *extItemObj.ProcessPrivateReference*;
 begin *SimpleJustificationPtr*(*nInference*)↑.*nReferences*↑.*Insert*(*new*(*LocalReferencePtr*,
 Init(*GetIdentifier*, *CurPos*)));
 end;

1521. When using a definition from an MML article in a scheme reference (something like “from *MyScheme*(*ARTICLE:def* 5,...)”), well, the Parser stores this fact in a state variable *gDefinitional*. The *ProcessDef* method populates this state variable correctly.

⟨Global variables introduced in *parseraddition.pas* 1349⟩ +≡
gDefinitional: *boolean*;

1522. ⟨Extended item implementation 1373⟩ +≡
procedure *extItemObj.ProcessDef*;
 begin *gDefinitional* ← (*CurWord.Kind* = *ReferenceSort*) ∧ (*CurWord.Nr* = *ord*(*syDef*))
 end;

1523. When accumulating the references in a Scheme-Justification, and a reference is from an MML article, *ProcessTheoremNumber* transforms it into a newly allocated reference object. The caller’s *nInference* then adds the newly allocated object to its *nReferences* collection.

⟨Extended item implementation 1373⟩ +≡
procedure *extItemObj.ProcessTheoremNumber*;
 var *lRefPtr*: *ReferencePtr*;
 begin if *CurWord.Kind* ≠ *Numeral* **then** *exit*;
 if *CurWord.Nr* = 0 **then**
 begin *ErrImm*(146); *exit*
 end;
 if *gDefinitional* **then** *lRefPtr* ← *new*(*DefinitionReferencePtr*, *Init*(*gTHEFileNr*, *CurWord.Nr*, *CurPos*))
 else *lRefPtr* ← *new*(*TheoremReferencePtr*, *Init*(*gTHEFileNr*, *CurWord.Nr*, *CurPos*));
 SimpleJustificationPtr(*nInference*)↑.*nReferences*↑.*Insert*(*lRefPtr*);
 end;

1524. When a Scheme-Justification uses a local reference, the Parser delegates the work to the *Item*’s *ProcessSchemeNumber* method. This updates the caller’s *nInference* field.

⟨Extended item implementation 1373⟩ +≡
procedure *extItemObj.ProcessSchemeNumber*;
 begin if *CurWord.Kind* ≠ *Numeral* **then** *exit*;
 if *CurWord.Nr* = 0 **then**
 begin *ErrImm*(146); *exit*
 end;
 with *SchemeJustificationPtr*(*nInference*)↑ **do**
 begin *nSchFileNr* ← *gTHEFileNr*; *nSchemeIdNr* ← *CurWord.Nr*; *nSchemeInfPos* ← *PrevPos*;
 end;
 end;

1525. This appears when the Parser starts its *Justification* (§1770) procedure, or in the *RegularStatement* (§1799) procedure.

This clears the *nInference*, reassigning it to the **nil** pointer.

For nested “**proof**” blocks, check if the ‘check proofs’ (“**::\$P+**”) pragma has been enabled — if so, just set the caller’s *nInference* to be a new Justification object with a ‘proof’ tag. Otherwise, we’re skipping the proofs, so set *nInference* to be the ‘skipped’ justification.

⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.StartJustification;
  begin nInference ← nil;
  if CurWord.Kind = sy_Proof then
    begin if ProofPragma then nInference ← new(JustificationPtr, Init(infProof, CurPos))
    else nInference ← new(JustificationPtr, Init(infSkippedProof, CurPos))
    end;
  end;
```

1526. A simple justification is either a Scheme-Justification (“**from...**”), a Straightforward-Justification (“**by...**”), or...somethign else?

⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.StartSimpleJustification;
  begin case CurWord.Kind of
    sy_From: nInference ← new(SchemeJustificationPtr, Init(CurPos, 0, 0));
    sy_By: with extBlockPtr(gBlockPtr)↑ do
      nInference ← new(StraightforwardJustificationPtr, Init(CurPos, nLinked, nLinkPos));
    othercases with extBlockPtr(gBlockPtr)↑ do
      nInference ← new(StraightforwardJustificationPtr, Init(PrevPos, nLinked, nLinkPos));
    endcases;
  end;
```

1527. We should update the *nInference* field’s sort to be *infError* when, well, the inference is an error (e.g., the Parser is in panic mode). We should set the *gBlockPtr*’s *nLinked* field to false when we just added a straightforward justification (or an erroneous justification).

```
define is_inference_error ≡ ¬StillCorrect ∨
  ((CurWord.Kind ≠ sy_Semicolon) ∧ (CurWord.Kind ≠ sy_DotEquals)) ∨
  ((nInference↑.nInfSort = infStraightforwardJustification) ∧ (byte(nLinked) >
    byte(nLinkAllowed))) ∨ ((nInference↑.nInfSort = infSchemeJustification) ∧
    (SchemeJustificationPtr(nInference)↑.nSchemeIdNr = 0))
```

⟨Extended item implementation 1373⟩ +≡

```
procedure extItemObj.FinishSimpleJustification;
  begin with extBlockPtr(gBlockPtr)↑ do
    begin if is_inference_error then nInference↑.nInfSort ← infError;
    end;
  if (nInference↑.nInfSort = infStraightforwardJustification) ∨ (nInference↑.nInfSort = infError) then
    extBlockPtr(gBlockPtr)↑.nLinked ← false;
  end;
```

1528. For iterative equalities, we should recall that it looks like

```
LHS = RHS <Justification>
  .= RHS2
  .= ...;
```

This matters because, well, when the Parser has parsed “LHS = RHS <Justification>”, the Parser believes it is a compact statement. Until the Parser looks at the next token, it does not know whether this is a Compact-Statement or an iterated equality. The *FinishCompactMethod* peeks at the token, and when the token is an iterated equality (“.”) updates the caller’s fields as well as initialize the *gIterativeLastFormula*, *gIterativeSteps*, and *gInference* state variables. The *gBlockPtr* is updated to make its *nLinked* field false.

<Extended item implementation 1373> +≡

procedure *extItemObj.FinishCompactStatement*;

begin if *CurWord.Kind* = *sy.DotEquals* **then**

begin *gIterativeLastFormula* ← *gLastFormula*; *nRegularStatementKind* ← *stIterativeEquality*;

extBlockPtr(gBlockPtr)↑.nLinked ← *false*; *gIterativeSteps* ← *new(PList, Init(0))*;

gInference ← *nInference*;

end;

end;

1529. Every time the Parser encounters the “.” token, it immediately invokes the *StartIterativeStep* method. This just updates the *gIterPos* state variable to the current position.

<Local variables for parser additions 1356> +≡

gIterPos: *Position*;

1530. <Extended item implementation 1373> +≡

procedure *extItemObj.StartIterativeStep*;

begin *gIterPos* ← *CurPos*; **end**;

1531. Right before the Parser iterates the loop checking if “.” is the next token for an iterative equation, the Parser invokes the *FinishIterativeStep* method. This just adds a new *IterativeStep* object, an AST node representing the preceding “.= RHS by <Justification>”.

<Extended item implementation 1373> +≡

procedure *extItemObj.FinishIterativeStep*;

begin *gIterativeSteps↑.Insert(new(IterativeStepPtr, Init(gIterPos, gLastTerm, nInference)))*;

end;

1532. In a definition, after the Parser finishes parsing the definiens, we construct the AST node for it with the *FinishDefiniens* method.

For each copula (“means” and “equals”), the algorithm is the same: if we just had a definition-by-cases, then store the “otherwise” clause in *lExp* and assign the *gDefiniens* state variable to a newly allocated conditional definiens object. If the definiens is not a definition-by-cases (i.e., it’s a “simple” definition), then just assign *gDefiniens* a newly allocated *SimpleDefiniens* object.

For functor definitions (not redefinitions), the *gCorrectnessConditions* are assigned here.

⟨Extended item implementation 1373⟩ +=

```

procedure extItemObj.FinishDefiniens;
  var lExp: DefExpressionPtr;
  begin case gDefiningWay of
    dfMeans:
      if gPartialDefs  $\neq$  nil then
        begin lExp  $\leftarrow$  nil;
        if gOtherwise  $\neq$  nil then lExp  $\leftarrow$  new(DefExpressionPtr, Init(exFormula, gOtherwise));
        gDefiniens  $\leftarrow$  new(ConditionalDefiniensPtr, Init(gMeansPos, gDefLabel, gPartialDefs, lExp))
        end
      else gDefiniens  $\leftarrow$  new(SimpleDefiniensPtr, Init(gMeansPos, gDefLabel, new(DefExpressionPtr,
        Init(exFormula, gLastFormula))));
    dfEquals:
      if gPartialDefs  $\neq$  nil then
        begin lExp  $\leftarrow$  nil;
        if gOtherwise  $\neq$  nil then lExp  $\leftarrow$  new(DefExpressionPtr, Init(exTerm, gOtherwise));
        gDefiniens  $\leftarrow$  new(ConditionalDefiniensPtr, Init(gMeansPos, gDefLabel, gPartialDefs, lExp))
        end
      else gDefiniens  $\leftarrow$  new(SimpleDefiniensPtr, Init(gMeansPos, gDefLabel, new(DefExpressionPtr,
        Init(exTerm, gLastTerm))));
  endcases;
  if  $\neg$ gRedefinitions  $\wedge$  (nItemKind = itDefFunc) then
    begin if gDefiningWay = dfMeans then gCorrectnessConditions  $\leftarrow$  [syExistence, syUniqueness]
    else if gDefiningWay = dfEquals then gCorrectnessConditions  $\leftarrow$  [syCoherence];
    end;
  end;

```

Section 23.3. EXTENDED SUBEXPRESSION CLASS

1533. Aside: refactoring. We should probably refactor a private procedure *PushTermStack* to push a new term onto the term stack, and a private function *PopTermStack* to return the top of the term stack (and mutate the term stack), and possibly a *ResetTermStack* procedure (which will clear the term stack and possibly the objects stored in it?).

We see that *TermNbr* is decremented when popping the *Term* stack (via *FinishTerm*); when *FinishQualifyingFormula* is invoked, it decrements the *TermNbr*; when *FinishAttributiveFormula* is invoked, it decrements the *TermNbr*; but these latter two methods can (and should) be refactored to use the *FinishTerm* to pop the term stack and decrement the *TermNbr* state variable.

Assigning the *TermNbr* occurs when *CreateArgs* method is invoked; the *InsertIncorrBasic* method resets the *TermNbr* to the *nTermBase*; the *ProcessAtomicFormula*, when a 157 error is raised, will reset the *TermNbr* to the *nTermBase*; when the constructor for an *extExpression* object is invoked, it resets the *TermNbr* to zero (which happens in the *extItem*’s *CreateExpression* method—which occurs frequently enough to be a worry).

The only time when the *TermNbr* is incremented is when we push a new term onto the *Term* stack.

1534. There is a comment in Polish “teraz jest to kolekcja MultipleTypeExp”, which Google translates to “now it is a MultipleTypeExp collection”. I have made this replacement in the code below, prefixed with a “+” sign (to distinguish it from the other comment already in English).

Also note: the *nRestriction* refers to the subformula in a universally quantified formula

for $\langle Variables \rangle$ **st** $\langle Restriction \rangle$ **holds** ...

```
define arg_type  $\equiv$  record Start, Length: integer;
  end
define func_type  $\equiv$  record Instance, SymPri: integer;
  FuncPos: Position;
  end
```

\langle Methods implemented by subclasses of *SubexpObj* 843 $\rangle + \equiv$

1535. \langle Extended subexpression class declaration 1535 $\rangle \equiv$
 $extSubexpPtr = \uparrow extSubexpObj;$
 $extSubexpObj = \mathbf{object} (SubexpObj)$
 $nTermBase, nRightArgBase: integer;$
 $nSubexpPos, nNotPos, nRestrPos: Position;$
 $nQuaPos: Position;$
 $nSpelling: Integer;$
 $nSymbolNr, nRSymbolNr: integer;$
 $nConnective, nNextWord: TokenKind;$
 $nModeKind: TokenKind;$
 $nModeNr: integer;$
 $nRightSideOfPredPos: Position;$
 $nMultipredicateList: MList;$
 $nSample: TermPtr; \{ \text{for Fraenkel terms} \}$
 $nAllPos: Position;$
 $nPostQualList: MList; \{ + \text{ now it is a MultipleTypeExp collection} \}$
 $nQualifiedSegments: MList;$
 $nSegmentIdentColl: MList; \{ \text{quantified variables, keeps spellings of vars} \}$
 $nSegmentPos: Position;$
 $nFirstSententialOperand: FormulaPtr;$
 $nRestriction: FormulaPtr;$
 $nAttrCollection: MList;$
 $nNoneOcc: boolean;$
 $nNonPos: Position;$
 $nPostNegated: boolean;$
 $nArgListNbr: integer; \{ \text{position in a term (\S1681)} \}$
 $nArgList: \mathbf{array\ of\ } arg_type;$
 $nFunc: \mathbf{array\ of\ } func_type;$
 $\mathbf{constructor\ } Init;$
 \langle Methods implemented by subclasses of $SubexpObj$ 843 \rangle
 $\mathbf{end\ ;}$

This code is used in section 1346.

1536. The $TermNbr$ is used to treat a list of terms as a stack data structure. Specifically, the $Term$ array is treated as a stack, and the $TermNbr$ is the index of the “top” of the stack.

\langle Local variables for parser additions 1356 $\rangle + \equiv$
 $TermNbr: integer;$

1537. \langle Extended subexpression implementation 1537 $\rangle \equiv$
 $\{ \textit{Subexpressions handling} \}$

constructor *extSubexpObj.Init*;
const *MaxArgListNbr* = 20;
begin *inheritedInit*; *nRestriction* \leftarrow **nil**; *nTermBase* \leftarrow *TermNbr*; *nArgListNbr* \leftarrow 0;
setlength(*nArgList*, *MaxArgListNbr* + 1); *setlength*(*nFunc*, *MaxArgListNbr* + 1);
nArgList[0].*Start* \leftarrow *TermNbr* + 1;
end;

See also sections 1538, 1539, 1540, 1542, 1543, 1544, 1545, 1546, 1547, 1548, 1549, 1550, 1551, 1552, 1553, 1554, 1555, 1556, 1557, 1558, 1560, 1564, 1576, 1577, 1578, 1579, 1580, 1581, 1582, 1583, 1584, 1585, 1586, 1587, 1588, 1589, 1590, 1591, 1592, 1593, 1594, 1595, 1596, 1597, 1598, 1599, 1600, 1601, 1602, 1603, 1604, 1605, 1606, 1607, 1608, 1609, 1610, 1611, 1612, 1613, 1614, 1615, 1616, 1617, 1618, 1619, 1620, 1621, 1622, 1623, 1624, 1625, 1626, 1627, 1628, 1629, 1630, 1631, 1632, 1633, 1634, and 1635.

This code is used in section 1347.

1538. When the Parser is about to parse a stack of attributes, either in a registration or on a type, we need to initialize the appropriate state variables. We also need the caller's *nAttrCollection* to be initialized with an empty list.

\langle Extended subexpression implementation 1537 $\rangle + \equiv$
procedure *extSubexpObj.StartAttributes*;
begin *nAttrCollection.Init*(0); *gLastType* \leftarrow **nil**;
end;

1539. When the Parser expects an adjective, and the caller is used to store the adjective or attribute, we need to check if it is negated. This handles it.

\langle Extended subexpression implementation 1537 $\rangle + \equiv$
procedure *extSubexpObj.ProcessNon*;
begin *nNoneOcc* \leftarrow *CurWord.Kind* = *sy_Non*; *nNonPos* \leftarrow *CurPos*;
end;

1540. Pop arguments from term stack. This will take some parameter *aBase* and copy pointers to each element of *Term*[*aBase* .. *TermNbr*] into a new list. Then the *TermNbr* state variable is updated to be *aBase* - 1.

This means that executing "*list1* \leftarrow *CreateArgs*(*aBase*); *list2* \leftarrow *CreateArgs*(*aBase*);" will have *list2* = **nil**.

Bug: when *aBase* \leq 0, this will set *TermNbr* to a negative number.

\langle Extended subexpression implementation 1537 $\rangle + \equiv$
function *CreateArgs*(*aBase* : *integer*): *PList*;
var *k*: *integer*; *lList*: *PList*;
begin *lList* \leftarrow *new*(*PList*, *Init*(*TermNbr* - *aBase*));
for *k* \leftarrow *aBase* **to** *TermNbr* **do** *lList.Insert*(*Term*[*k*]);
TermNbr \leftarrow *aBase* - 1; *CreateArgs* \leftarrow *lList*;
end;

1541. The "process (singular) attribute" method is invoked in the "process (plural) attributes" procedure (§1692), and in the *ATTSubexpression* procedure (§1862). This method will be invoked when the Parser is looking at an attribute token.

When there is no format recorded for such an attribute, then a 175 error will be raised.

This will allocate a new Adjective object, store it in the *gLastAdjective* state variable, then append it to the *nAttrCollection* field of the caller.

\langle Global variables introduced in *parseraddition.pas* 1349 $\rangle + \equiv$
gLastAdjective: *AdjectiveExpressionPtr*;

1542. \langle Extended subexpression implementation 1537 $\rangle + \equiv$

```

procedure extSubexpObj.ProcessAttribute;
  var lFormatNr: integer;
  begin if CurWord.Kind = AttributeSymbol then
    begin
      lFormatNr  $\leftarrow$  gFormatsColl.LookUp_PrefixFormat(~V, CurWord.Nr, TermNbr - nTermBase + 1);
      if lFormatNr = 0 then { format not found! }
        begin gLastAdjective  $\leftarrow$  new(AdjectivePtr, Init(CurPos, 0, CreateArgs(nTermBase + 1)));
          Error(CurPos, 175)
        end
      else begin
        gLastAdjective  $\leftarrow$  new(AdjectivePtr, Init(CurPos, CurWord.Nr, CreateArgs(nTermBase + 1)));
        if nNoneOcc then gLastAdjective  $\leftarrow$  new(NegatedAdjectivePtr, Init(nNonPos, gLastAdjective));
        end;
      end
    else { needed for ATTSubexpression adjective cluster handling }
      begin gLastAdjective  $\leftarrow$  new(AdjectivePtr, Init(CurPos, 0, CreateArgs(nTermBase + 1)));
        end;
      nAttrCollection.Insert(gLastAdjective);
    end;

```

1543. These next next method is invoked before the Parser parses arguments for an attribute.

\langle Extended subexpression implementation 1537 $\rangle + \equiv$

```

procedure extSubexpObj.StartAttributeArguments;
  begin nTermBase  $\leftarrow$  TermNbr;
  end;

```

1544. The next two methods are invoked after the Parser has finished parsing the arguments for an attribute.

I am confused why there is duplicate code here, and the naming conventions suggest the *FinishAttributeArguments* method should be preferred. ■

\langle Extended subexpression implementation 1537 $\rangle + \equiv$

```

procedure extSubexpObj.CompleteAttributeArguments;
  begin nSubexpPos  $\leftarrow$  CurPos; nRightArgBase  $\leftarrow$  TermNbr;
  end;

procedure extSubexpObj.FinishAttributeArguments;
  begin nSubexpPos  $\leftarrow$  CurPos; nRightArgBase  $\leftarrow$  TermNbr;
  end;

```

1545. This allocates a new list of pointers, moves the caller's *nAttrCollection* into the list, and updates the *gAttrColl* state variable to point at them.

Again, this should be named *FinishedAdjectiveCluster* to be consistent with the naming conventions seemingly adopted.

\langle Extended subexpression implementation 1537 $\rangle + \equiv$

```

procedure extSubexpObj.CompleteAdjectiveCluster;
  begin gAttrColl  $\leftarrow$  new(PList, MoveList(nAttrCollection));
  end;

```


1546. When the Parser works its way through a registration block, check that the *TermNbr* points to not farther ahead than one more token ahead from the caller's *nTermBase* field. Raise an error if that happens.

This method is only invoked in the Parser module's the *RegisterCluster* (§1865) procedure.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.CompleteClusterTerm;
  begin if TermNbr − nTermBase > 1 then
    begin ErrImm(379); gLastTerm ← new(IncorrectTermPtr, Init(CurPos));
    end;
  end;
```

1547. A “simple term” appears to be a variable. This is used when the Parser parses an identifier as a closed term (§1663). The state variable *gLastTerm* is updated to point to a newly allocated *SimpleTerm* AST node (§883).

This method should probably be moved closer to the other methods used when parsing terms.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.ProcessSimpleTerm;
  begin gLastTerm ← new(SimpleTermPtr, Init(CurPos, GetIdentifier));
  end;
```

1548. Qualified terms. The Parser invokes *ProcessQua* when it is looking directly at a “qua” token, specifically in the *AppendQua* (§1656) procedure. The *ProcessQua* method is used nowhere else. It is solely responsible for “marking the current position” of the Parser, and storing that in the caller's *nQuaPos* field.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.ProcessQua;
  begin nQuaPos ← CurPos
  end;
```

1549. The Parser invokes the *FinishedQualifiedTerm* method after encountering a “qua” and after parsing the type. This method constructs a new *QualifiedTerm* object reflecting the top of the *Term* stack is taken “qua” the *gLastType*, and the mutates the top of the *Term* stack to be this newly allocated *QualifiedTerm* object.

This method does not push anything new to the term stack, but it does mutate the *Term* stack.

This method is used nowhere else other than the Parser's *AppendQua* (§1656) procedure.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.FinishQualifiedTerm;
  begin Term[TermNbr] ← new(QualifiedTermPtr, Init(nQuaPos, Term[TermNbr], gLastType));
  end;
```

1550. Although the “**exactly**” reserved keyword is not used for anything, the method for *ProcessExactly* marks the current position and stores it in the caller's *nQuaPos*, then *updates* (**not** pushes) to the top of the term stack by turning the top of the stack into an *ExactlyTerm* object.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.ProcessExactly;
  begin nQuaPos ← CurPos; Term[TermNbr] ← new(ExactlyTermPtr, Init(nQuaPos, Term[TermNbr]));
  end;
```

1551. Arguments to a term. The *CheckTermLimit* procedure is a “private helper function” for the *FinishArgument* method.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure CheckTermLimit;
  var l: integer;
  begin if TermNbr ≥ length(Term) then
    begin l ← 2 * length(Term); setlength(Term, l);
    end;
  end;
```

1552. Pushing the Term stack. This method pushes the *gLastTerm* state variable’s contents to the *Term* stack, mutating the *TermNbr* and *Term* module-local variables.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.FinishArgument;
  begin CheckTermLimit; inc(TermNbr); Term[TermNbr] ← gLastTerm;
  end;
```

1553. Pop the Term stack. The evil twin to “pushing” an element onto a stack, “popping” a stack removes the top element. We pop the *Term* stack whenever we finish the term.

This is only used in *AppendFunc* (§1681).

This should probably check that the *Term* stack is not empty before being invoked.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.FinishTerm;
  begin gLastTerm ← Term[TermNbr]; dec(TermNbr);
  end;
```

Subsection 23.3.1. Parsing Types

1554. When we start parsing a new type, we make sure the *gLastType* state variable is not caching an old type. We assign it to be the **nil** pointer.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.StartType;
  begin gLastType ← nil;
  end;
```

1555. This is invoked only by the Parser’s *RadixTypeSubexpression* (§1694) procedure. The Parser delegates the work of storing the mode information to this method. In turn, the caller’s *nModeKind* field stores the current word’s token *Kind*, and the caller’s *nModeNr* field stores the current word’s number. The Parser’s current position is marked and stored in the caller’s *nSubexpPos* field.

But no state variables are mutated by this method.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.ProcessModeSymbol;
  begin nModeKind ← CurWord.Kind; nModeNr ← CurWord.Nr;
  if (CurWord.Kind = sy_Set) { ?^(AheadWord.Kind ≠ sy_Of)? }
  then nModeKind ← ModeSymbol; nSubexpPos ← CurPos;
  end ;
```

1556. The Parser has just finished parsing a type and its arguments — “ $\langle Mode \rangle$ of $\langle Term\text{-}list \rangle$ ” or “ $\langle Structure \rangle$ over $\langle Term\text{-}list \rangle$ ”. The data has been accumulated into the caller, which will now be constructed into an AST object. The newly allocated AST node will be stored in the *gLastType* state variable.

If the caller is trying to construct a mode which does not match the format recorded in the *gFormatsColl*, a 151 error will be raised.

Similarly, if the caller is trying to construct a structure which does not match the format recorded in the *gFormatsColl*, a 185 error will be raised.

This is invoked only by the Parser’s *RadixTypeSubexpression* (§1694) procedure.

⟨Extended subexpression implementation 1537⟩ +≡

procedure *extSubexpObj.FinishType*;

var *lFormatNr*: integer;

begin case *nModeKind* **of**

ModeSymbol: **begin**

lFormatNr \leftarrow *gFormatsColl.LookUp_PrefixFormat*(‘M’, *nModeNr*, *TermNbr* – *nTermBase*);

if *lFormatNr* = 0 **then** *Error*(*nSubexpPos*, 151); {format missing}

gLastType \leftarrow *new*(*StandardTypePtr*, *Init*(*nSubexpPos*, *nModeNr*, *CreateArgs*(*nTermBase* + 1)));

end;

StructureSymbol: **begin**

lFormatNr \leftarrow *gFormatsColl.LookUp_PrefixFormat*(‘L’, *nModeNr*, *TermNbr* – *nTermBase*);

if *lFormatNr* = 0 **then** *SemErr*(185); {format missing}

gLastType \leftarrow *new*(*StructTypePtr*, *Init*(*nSubexpPos*, *nModeNr*, *CreateArgs*(*nTermBase* + 1)));

end;

othercases begin *gLastType* \leftarrow *new*(*IncorrectTypePtr*, *Init*(*CurPos*)); **end**;

endcases;

end;

1557. If the Parser has the misfortune of trying to make sense of a malformed type expression, then with a heavy heart it invokes this method to update the *gLastType* state variable to be an incorrect type expression at the current position.

⟨Extended subexpression implementation 1537⟩ +≡

procedure *extSubexpObj.InsertIncorrType*;

begin *gLastType* \leftarrow *new*(*IncorrectTypePtr*, *Init*(*CurPos*));

end;

1558. When the Parser encounters a qualifying formula (“ $\langle Term \rangle$ is $\langle Type \rangle$ ”) or is parsing a type for a cluster (the “**cluster** ... **for** $\langle Type \rangle$ ”), after parsing the type, this method is invoked to **update** the *gLastType* state variable to store the *ClusteredType* AST node (which decorates a type — the contents of *gLastType* at the time of calling — with a bunch of attributes).

The caller’s *nAttrCollection* is transferred to the *gLastType*. At the end of the method, the caller’s *nAttrCollection* (array of pointers) is freed. This does not free the objects referenced by the pointers, however.

If *gLastType* = **nil**, then the Parser has somehow failed to parse the type expression. An error should be raised.

⟨Extended subexpression implementation 1537⟩ +≡

procedure *extSubexpObj.CompleteType*;

var *j*: integer;

begin mizassert(5433, *gLastType* ≠ **nil**);

if *nAttrCollection.Count* > 0 **then**

begin *gLastType* ← new(*ClusteredTypePtr*, Init(*gLastType*↑.*nTypePos*, new(*PList*,
 Init(*nAttrCollection.Count*)), *gLastType*));

for *j* ← 0 **to** *nAttrCollection.Count* − 1 **do**

ClusteredTypePtr(*gLastType*↑.*nAdjectiveCluster*↑.Insert(*PObject*(*nAttrCollection.Items*↑[*j*]));

nAttrCollection.DeleteAll;

end;

end;

Subsection 23.3.2. Parsing operator precedence

1559. Mario Carneiro’s “Mizar in Rust” (§6.2) gives an overview of this parsing routine (see also his `mizar-rs/src/parser/miz.rs` for the Rust version of the same code). It is a constrained optimization problem. We shall take care to dissect this routine. This appears to be where operator precedence, the *gPriority* (§775) global variable, comes into play.

1560. Starting a “long term”.

We can observe that *nTermBase* is initialized upon construction to *TermNbr*; in *ProcessAtomicFormula* and *StartPrivateFormula* it is assigned to *TermNbr*.

⟨Extended subexpression implementation 1537⟩ +≡

procedure *extSubexpObj.StartLongTerm*;

begin *nArgListNbr* ← 0; *nArgList*[0].Length ← *TermNbr* − *nTermBase*;

end;

1561. Malformed term errors.

We should remind the reader, errors 165–175 are “unknown functor format”, errors 176 is “unknown attribute format”, and error 177 is “unknown structure format”. Only when such an error occurs, the flow experiences a **goto** *AfterBalance*.

For an example of a 168, 169 error:

```
for x being Nat
holds (id + x +) = x;
```

For an example of a 170, 171 error (the first 0 will be flagged 170, the second 0 will be flagged as 171):

```
for x being Nat
holds 0 0 + x = x;
```

For an example of a 172, 173 error:

```
for x being Nat
holds x + / = x;
```

For an example of a 174, 175 error:

```
for x being Nat
holds x + (1,2) + x = x;
```

1562. We can recall that a “generic” term looks like an infix operator of the form

$$(t_1^{(\ell)}, \dots, t_m^{(\ell)}) t (t_1^{(r)}, \dots, t_n^{(r)})$$

The parentheses are optional. Constants will have $m = n = 0$ and look like $() t ()$. Function-like terms will have $m = 0$ and look like $() t (t_1^{(r)}, \dots, t_n^{(r)})$. The problem statement could be re-phrased as: given several infix terms without parentheses inserted anywhere, determine how to cluster terms together.

1563. The problem statement for constructing the syntax tree for a term is something like the following: we have an expression of the form

$$x_1^{(0)}, \dots, x_{k_0}^{(0)} F_1 x_1^{(1)}, \dots, x_{k_1}^{(1)} F_2 \cdots F_n x_1^{(n)}, \dots, x_{k_n}^{(n)}$$

We want to produce a suitable binary tree with F_i on the internal nodes and the $(x_j^{(i)})_{j \leq k_i}$ on the leafs, respecting precedence such that each F_i is applied to the correct number of arguments.

Mario Carneiro noted ([arXiv:2304.08391](https://arxiv.org/abs/2304.08391), §6.2) the existence of an $O(n^4)$ algorithm using dynamic programming techniques. The trick is to compute the minimal “cost” [number of violations] for each substring of nodes $F_a \cdots F_b$ for each $1 \leq a \leq i \leq b \leq n$ with node F_i being the root of the subtree. There are $O(n^3)$ such subproblems, and they can be calculated from smaller subproblems in $O(n)$. This might seem alarmingly large, but usually the terms in Mizar are sufficiently small.

It is interesting to see how other languages tackle this problem, so I am going to give a haphazard literature review:

- (1) Nils Anders Danielsson and Ulf Norell’s “Parsing Mixfix Operators” (in SB. Scholz and O. Chitil (eds.), *Symposium on Implementation and Application of Functional Languages*, Springer 2008, pp. 80–99; [doi:10.1007/978-3-642-24452-0_5](https://doi.org/10.1007/978-3-642-24452-0_5)) discuss how Agda approaches parsing mixfix operators with different precedence.
- (2) The Isabelle proof assistant uses a modified version of Earley parsing of terms, supporting precedence between 0 to 1000.

1564. The only two place where *FinishLongTerm* is invoked is in the *AppendFunc* procedure (§1681) in *parser.pas*.

This relies on *MFormatsList.LookUpFuncFormat* (§794), which attempts to look up an *MinfixFormatObj* (§782) with a given id number as well as number of left and right arguments.

We will need to populate *ArgsLength* and *To_Right* to determine the syntax tree for the term (which is our real goal here). The *ArgsLength* encodes the number of terms are to the left and right of each “internal node”. The *To_Right* controls associativity (which is how Mizar handles operator precedence): if node F_{k+1} is higher precedence than node F_k , then *To_Right*(k) is true.

The *Exchange*(i) procedure will make node i a child of $i-1$ (when node i is a child of $i-1$), and vice-versa. Visually, this means we transform the tree as:

$$(\cdots F_{i-1} x_1, \dots, x_\ell), x_{\ell+1}, \dots, x_n F_i \cdots \longleftrightarrow \cdots F_{i-1} x_1, \dots, x_{\ell-1}, (x_\ell, x_{\ell+1}, \dots, x_n F_i \cdots)$$

Observe that “*Exchange*(i); *Exchange*(i)” is equivalent to doing nothing.

We should recall (§1534) that *nArgList* is an array of “**record** *Instance*, *SymPri*: *integer*; *FuncPos*: *Position*; **end**”.

⟨Extended subexpression implementation 1537⟩ $\vdash \equiv$

procedure *extSubexpObj.FinishLongTerm*;

var *ArgsLength*: **array of record** *l, r*: *integer*;
 end;

To_Right: **array of boolean**;

procedure *Exchange*(i : *integer*);

var l : *integer*;

begin $l \leftarrow \text{ArgsLength}[i].l$; $\text{ArgsLength}[i].l \leftarrow \text{ArgsLength}[i-1].r$; $\text{ArgsLength}[i-1].r \leftarrow l$;

To_Right[$i-1$] $\leftarrow \neg \text{To_Right}[i-1]$;

end;

var Bl, new_Bl : *integer*; { indexes *nFunc*, *ArgsLength* }

i, j, k : *integer*; { various indices }

 ⟨Variables for finishing a long term in a subexpression 1573⟩

label *Corrected*, *AfterBalance*;

begin ⟨Rebalance the long term tree 1565⟩

AfterBalance: ⟨Construct the term’s syntax tree after balancing arguments among subterms 1574⟩

end;

1565. Rebalancing the term tree.

Note that $nArgListNbr$ is mutated only in $extSubexpObj.ProcessFuncSymbol$ (§1576), and in $ProcessAtomicFormula$ (§1606) it is reset to zero.

```

define missing_funcator_format  $\equiv gFormatsColl.LookUp\_FuncFormat(Instance, l, r) = 0$ 
⟨ Rebalance the long term tree 1565 ⟩  $\equiv$ 
  ⟨ Initialize To_Right and ArgsLength arrays 1568 ⟩
  ⟨ Initialize Bl, goto AfterBalance if term has at most one argument 1570 ⟩
    {  $Bl = 1 \vee Bl = 2$  }
  for  $k \leftarrow 2$  to  $nArgListNbr - 1$  do
    with  $nFunc[k], ArgsLength[k]$  do
      begin if missing_funcator_format then ⟨ Guess the  $k^{th}$  funcator format 1571 ⟩
        Corrected: end;
      for  $j \leftarrow nArgListNbr$  downto  $Bl + 1$  do
        with  $nFunc[j], ArgsLength[j]$  do
          begin if  $\neg$ missing_funcator_format then goto AfterBalance;
          Exchange( $j$ ); ⟨ Check for 172/173 error, goto AfterBalance if erred 1566 ⟩
          end;
        ⟨ Check for 174/175 error, goto AfterBalance if erred 1567 ⟩

```

This code is used in section 1564.

```

1566. ⟨ Check for 172/173 error, goto AfterBalance if erred 1566 ⟩  $\equiv$ 
  if missing_funcator_format then
    begin Error(FuncPos, 172); Error( $nFunc[nArgListNbr].FuncPos$ , 173); goto AfterBalance; end;

```

This code is used in section 1565.

```

1567. ⟨ Check for 174/175 error, goto AfterBalance if erred 1567 ⟩  $\equiv$ 
  with  $nFunc[Bl], ArgsLength[Bl]$  do
    if missing_funcator_format then
      begin Error(FuncPos, 174); Error( $nFunc[nArgListNbr].FuncPos$ , 175); goto AfterBalance; end;

```

This code is used in section 1565.

1568. We first allocate the arrays, then we initialize the values.

```

⟨ Initialize To_Right and ArgsLength arrays 1568 ⟩  $\equiv$ 
  setlength(ArgsLength,  $nArgListNbr + 1$ ); setlength(To_Right,  $nArgListNbr + 1$ );
  setlength(Depo,  $nArgListNbr + 1$ );

```

See also section 1569.

This code is used in section 1565.

1569. The initial guess depends on whether F_k has precedence over F_{k+1} or not.

If F_{k+1} has higher precedence than F_k , then the initial guess groups terms as:

$$\cdots F_k ((x_1^{(k)}, \dots, x_{m_k}^{(k)}) F_{k+1}(\cdots)) \cdots, \quad \text{and} \quad To_Right[k] = true.$$

On the other hand, if F_{k+1} *does not* have higher precedence than F_k , then we guess the terms are grouped as

$$\cdots (\cdots F_k(x_1^{(k)}, \dots, x_{m_k}^{(k)}) F_{k+1} \cdots), \quad \text{and} \quad To_Right[k] = false.$$

This is a first stab, but sometimes we get lucky and it's correct.

```
define next_term_has_higher_precedence(#)  $\equiv$ 
  gPriority.Value(ord(“0”), nFunc[#].Instance) < gPriority.Value(ord(“0”), nFunc[# + 1].Instance)
< Initialize To_Right and ArgsLength arrays 1568 >  $\equiv$ 
  ArgsLength[1].l  $\leftarrow$  nArgList[0].Length; To_Right[0]  $\leftarrow$  true;
for k  $\leftarrow$  1 to nArgListNbr - 1 do
  with ArgsLength[k] do
    if next_term_has_higher_precedence(k) then
      begin r  $\leftarrow$  1; ArgsLength[k + 1].l  $\leftarrow$  nArgList[k].Length; To_Right[k]  $\leftarrow$  true end
    else begin r  $\leftarrow$  nArgList[k].Length; ArgsLength[k + 1].l  $\leftarrow$  1; To_Right[k]  $\leftarrow$  false end;
  ArgsLength[nArgListNbr].r  $\leftarrow$  nArgList[nArgListNbr].Length; To_Right[nArgListNbr]  $\leftarrow$  false;
```

1570. The first situation we encounter is if the user tries to tell Mizar to evaluate something like:

```
for x being Nat
holds x + (1,2) = x;
```

Mizar will not understand “x + (1,2)” because it is an invalid functor format — the format would look something like $\langle +, \text{left} : 1, \text{right} : 1 \rangle$ but the format of the expression is $\langle \text{left} : 1, \text{right} : 2 \rangle$. The mismatch on the “right” values in the formats will raise a 165 error.

For a 166 error example,

```
for x being Nat
holds + / = x;
```

Mizar will not like the leading “+ /” expression, and flag this with the 166 error.

Mizar will flag “+ 0” as a 165 error.

```
< Initialize Bl, goto AfterBalance if term has at most one argument 1570 >  $\equiv$ 
with nFunc[1], ArgsLength[1] do
  begin if nArgListNbr = 1 then
    begin if missing_functor_format then
      begin Error(FuncPos, 165); goto AfterBalance end;
    goto AfterBalance;
  end;
  Bl  $\leftarrow$  1;
if missing_functor_format then
  begin Exchange(2); Bl  $\leftarrow$  2;
  if missing_functor_format then
    begin Error(FuncPos, 166); goto AfterBalance end;
  end;
end;
```

This code is used in section 1565.

1571. \langle Guess the k^{th} functor format [1571](#) $\rangle \equiv$
begin *Exchange*($k + 1$); *new_Bl* \leftarrow *Bl*;
if *missing_functor_format* **then**
 begin if *Bl* = *k* **then**
 begin *Error*(*nFunc*[$k - 1$].*FuncPos*, 168); *Error*(*FuncPos*, 169); **goto** *AfterBalance*; **end**;
 Exchange($k + 1$); *Exchange*(*k*); *new_Bl* \leftarrow *k*;
 if *missing_functor_format* **then**
 begin *Exchange*($k + 1$); *new_Bl* \leftarrow $k + 1$;
 if *missing_functor_format* **then**
 begin *Error*(*FuncPos*, 167); **goto** *AfterBalance* **end**;
 end;
 for $j \leftarrow k - 1$ **downto** *Bl* + 1 **do**
 with *nFunc*[*j*], *ArgsLength*[*j*] **do**
 begin if \neg *missing_functor_format* **then** **goto** *Corrected*;
 Exchange(*j*);
 if *missing_functor_format* **then**
 begin *Error*(*FuncPos*, 168); *Error*(*nFunc*[*k*].*FuncPos*, 169); **goto** *AfterBalance*; **end**;
 end;
 \langle Check term *Bl* has valid functor format, **goto** *AfterBalance* if not [1572](#) \rangle
 end;
Bl \leftarrow *new_Bl*;
end;

This code is used in section [1565](#).

1572. \langle Check term *Bl* has valid functor format, **goto** *AfterBalance* if not [1572](#) $\rangle \equiv$
with *nFunc*[*Bl*], *ArgsLength*[*Bl*] **do**
 if *missing_functor_format* **then**
 begin *Error*(*FuncPos*, 170); *Error*(*nFunc*[*k*].*FuncPos*, 171); **goto** *AfterBalance*; **end**;

This code is used in section [1571](#).

1573. Constructing the syntax tree. The second half of finishing a long term constructs the syntax tree for the term.

\langle Variables for finishing a long term in a subexpression [1573](#) $\rangle \equiv$
ak, pl, ll, kn: *integer*;
lTrm: *TermPtr*;
lLeftArgs, lRightArgs: *PList*;
DepoNbr: *integer*;
Depo: **array of record** *FuncInstNr*: *integer*;
 dArgList: *PList*;
end;

This code is used in section [1564](#).

1574. \langle Construct the term's syntax tree after balancing arguments among subterms 1574 \equiv
 \langle Initialize symbol priorities, determine last ll , pl values 1575 \rangle
 $DepoNbr \leftarrow 0$;
for $kn \leftarrow nArgListNbr$ **downto** 2 **do**
 if $To_Right[kn - 1]$ **then** { if kn node is parent of $kn - 1$ node }
 begin with $nFunc[kn]$ **do**
 begin $lRightArgs \leftarrow CreateArgs(nArgList[kn].Start)$; { (§1540) }
 $lLeftArgs \leftarrow CreateArgs(nArgList[kn - 1].Start)$;
 $lTrm \leftarrow new(InfixTermPtr, Init(FuncPos, Instance, lLeftArgs, lRightArgs))$;
 end;
 for $j \leftarrow DepoNbr$ **downto** 1 **do**
 with $Depo[j], nFunc[FuncInstNr]$ **do**
 begin if $symPri \leq nFunc[kn - 1].SymPri$ **then break**;
 $dec(DepoNbr)$; $lLeftArgs \leftarrow new(PList, Init(1))$; $lLeftArgs \uparrow.Insert(lTrm)$;
 $lTrm \leftarrow new(InfixTermPtr, Init(FuncPos, Instance, lLeftArgs, dArgList))$;
 end;
 $gLastTerm \leftarrow lTrm$;
 $gSubexpPtr \uparrow.FinishArgument$;
 end
 else begin $inc(DepoNbr)$;
 with $Depo[DepoNbr]$ **do**
 begin $FuncInstNr \leftarrow kn$; $dArgList \leftarrow CreateArgs(nArgList[kn].Start)$; **end**;
 end;
 with $nFunc[1]$ **do**
 begin $lRightArgs \leftarrow CreateArgs(nArgList[1].Start)$; $lLeftArgs \leftarrow CreateArgs(nArgList[0].Start)$;
 $lTrm \leftarrow new(InfixTermPtr, Init(FuncPos, Instance, lLeftArgs, lRightArgs))$;
 end;
 for $j \leftarrow DepoNbr$ **downto** 1 **do**
 with $Depo[j], nFunc[FuncInstNr]$ **do**
 begin $lLeftArgs \leftarrow new(PList, Init(1))$; $lLeftArgs \uparrow.Insert(lTrm)$;
 $lTrm \leftarrow new(InfixTermPtr, Init(FuncPos, Instance, lLeftArgs, dArgList))$;
 end;
 $gLastTerm \leftarrow lTrm$;

This code is used in section 1564.

1575. \langle Initialize symbol priorities, determine last ll , pl values 1575 \equiv
for $ak \leftarrow 1$ **to** $nArgListNbr$ **do**
 begin $ll \leftarrow 1$; $pl \leftarrow 1$;
 if $To_Right[ak - 1]$ **then** $ll \leftarrow nArgList[ak - 1].Length$;
 if $\neg To_Right[ak]$ **then** $pl \leftarrow nArgList[ak].Length$;
 with $nFunc[ak]$ **do**
 begin $symPri \leftarrow gPriority.Value(ord('0'), Instance)$; **end**;
 end;

This code is used in section 1574.

Subsection 23.3.3. Processing subexpressions

1576. Note that *ProcessFunctorSymbol* is the only place where *nArgListNbr* is incremented. Processing functor symbols occurs in the Parser’s *AppendFunc* (§1681) in a loop.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.ProcessFunctorSymbol;
  var l: integer;
  begin inc(nArgListNbr);
  if nArgListNbr ≥ length(nFunc) then
    begin l ← 2 * length(nFunc) + 1; setlength(nArgList, l); setlength(nFunc, l);
    end;
  nArgList[nArgListNbr].Start ← TermNbr + 1; nFunc[nArgListNbr].FuncPos ← CurPos;
  nFunc[nArgListNbr].Instance ← CurWord.Nr;
  end;
```

1577. The Parser is in the middle of *AppendFunc* and has just finished parsing a term *t* or a tuple of terms (*t*₁, . . . , *t*_{*n*}). Before the Parser checks if it’s looking at an infix functor operator or not, the Parser invokes the *FinishArgList* method. It’s the only time where the *FinishArgList* method is invoked.

This allocates either 1 or *n* to the length of *nArgList*[*nArgListNbr*], to store the information for the term(s).

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.FinishArgList;
  begin nArgList[nArgListNbr].Length ← TermNbr − nArgList[nArgListNbr].Start + 1;
  end;
```

1578. The Parser is looking at “where” or (when the variables are all reserved) a colon “:”, the Parser invokes the *StartFraenkelTerm* which will store the previous term in the *nSample* field — so schematically, the Fraenkel term could look like

$$\{\langle nSample \rangle \text{ where } \langle Postqualification \rangle : \langle Formula \rangle\}$$

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.StartFraenkelTerm;
  begin nSample ← gLastTerm;
  end;
```

1579. This is only invoked in the Parser’s *ProcessPostqualification* (§1658) procedure, which is only invoked after the Parser calls the *extSubexp* object’s *StartFraenkelTerm* method.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.StartPostqualification;
  begin nPostQualList.Init(0);
  end;
```

1580. The Parser is looking at the post-qualified segment of a Fraenkel operator. This will be a list of variables “being” a type, we allocate an array for the variables. This is handled by the *StartPostQualifyingSegment* method.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.StartPostQualifyingSegment;
  begin nSegmentIdentColl.Init(2);
  end;
```

1581. While looping over the comma-separated list of variables in a post-qualified segment (in a Fraenkel term), the Parser invokes the *ProcessPostqualifiedVariable* on each iteration until it has parsed all the variables. This allocates a new *Variable* object, and pushes it onto the *nSegmentIdentColl* “stack”.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.ProcessPostqualifiedVariable;
  begin nSegmentIdentColl.Insert(new(VariablePtr, Init(CurPos, GetIdentifier)));
end;
```

1582. The Parser is looking at “is” or “are” in a Fraenkel term’s post-qualification segment, but has not yet parsed the type. This method will assign the *nSegmentPos* field to be the current position, and assign the *gLastType* state variable to be the **nil** pointer.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.StartPostqualificationSpecyfication;
  begin nSegmentPos ← CurPos; gLastType ← nil;
end;
```

1583. The Parser has just parsed either (1) a comma-separated list of variables, the copula “is” or “are”, and the type; or (2) a comma-separated list of reserved variables (but no copula and no type). We just need to construct an appropriate node for the abstract syntax tree. This method will append a new Segment to the *nPostQualList*.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.FinishPostQualifyingSegment;
  var k: integer; lSegment: ExplicitlyQualifiedSegmentPtr;
  begin if gLastType ≠ nil then
    begin lSegment ← new(ExplicitlyQualifiedSegmentPtr, Init(nSegmentPos, new(PList, Init(0)),
      gLastType)); nPostQualList.Insert(lSegment);
    for k ← 0 to nSegmentIdentColl.Count − 1 do
      begin ExplicitlyQualifiedSegmentPtr(lSegment)↑.nIdentifiers.Insert(nSegmentIdentColl.Items↑[k]);
      end;
    end
  else begin for k ← 0 to nSegmentIdentColl.Count − 1 do
    begin nPostQualList.Insert(new(ImplicitlyQualifiedSegmentPtr,
      Init(VariablePtr(nSegmentIdentColl.Items↑[k])↑.nVarPos, nSegmentIdentColl.Items↑[k])));
    end;
  end;
  nSegmentIdentColl.DeleteAll; nSegmentIdentColl.Done;
end;
```

1584. The Parser has just finished the formula in a Fraenkel term, and it is staring at the closet “}” bracket. The Parser invokes this method to construct a new *FraenkelTerm* AST node, and updates the *gLastTerm* to point at it.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.FinishFraenkelTerm;
  begin gLastTerm ← new(FraenkelTermPtr, Init(CurPos, new(PList, MoveList(nPostQualList)),
    nSample, gLastFormula));
end;
```

1585. The Parser has already encountered “**the set**” and the next token is “**of**”, which means the Parser has encountered a “simple” Fraenkel term of the form “**the set of all** $\langle Term \rangle \dots$ ”. This method will be invoked once the Parser has stumbled across the “**all**”. The caller updates its $nAllPos$ to the Parser’s current position.

\langle Extended subexpression implementation 1537 $\rangle + \equiv$
procedure *extSubexpObj.StartSimpleFraenkelTerm*;
 begin $nAllPos \leftarrow CurPos$;
 end;

1586. The Parser has just finished parsing the post-qualification to the simple Fraenkel term, which means it has finished parsing the simple Fraenkel term. This method allocates a new *SimpleFraenkelTerm* AST node with the accumulated AST nodes, then updates the $gLastTerm$ to point to the allocated *SimpleFraenkelTerm* node.

\langle Extended subexpression implementation 1537 $\rangle + \equiv$
procedure *extSubexpObj.FinishSimpleFraenkelTerm*;
 begin $gLastTerm \leftarrow new(SimpleFraenkelTermPtr, Init(nAllPos, new(PList, MoveList(nPostQualList)), nSample))$;
 end;

1587. The Parser is looking at a closed term of the form “ $\langle Identifier \rangle (\dots$ ”, and so it looks like a private functor. This method updates the caller’s $nSubexpPos$ to the Parser’s current position, and the $nSpelling$ is assigned to the identifier’s number (for the private functor).

\langle Extended subexpression implementation 1537 $\rangle + \equiv$
procedure *extSubexpObj.StartPrivateTerm*;
 begin $nSubexpPos \leftarrow CurPos$; $nSpelling \leftarrow CurWord.Nr$;
 end;

1588. The Parser just finished parsing all the arguments to the private functor, and is looking at the closing parentheses for the private functor. This method allocates a new *PrivateFunctorTerm* object, using the arguments just parsed, and updates the $gLastTerm$ state variable to point to it.

\langle Extended subexpression implementation 1537 $\rangle + \equiv$
procedure *extSubexpObj.FinishPrivateTerm*;
 begin $gLastTerm \leftarrow new(PrivateFunctorTermPtr, Init(nSubexpPos, nSpelling, CreateArgs(nTermBase + 1)))$;
 end;

1589. The Parser has just encountered either a left bracket term or the opening left bracket for a set “{”. The Parser calls this method, which just updates the caller’s $nSymbolNr$ to be whatever the current token’s numeric ID value is.

\langle Extended subexpression implementation 1537 $\rangle + \equiv$
procedure *extSubexpObj.StartBracketedTerm*;
 begin $nSymbolNr \leftarrow CurWord.Nr$;
 end;

1590. If the Parser is in panic mode, this method does nothing.

Either the Parser has finished parsing an enumerated set $\{x_1, \dots, x_n\}$ or a bracketed term. We need to double check the format for the bracket matches what is stored in the *gFormatsColl*, and raise a 152 error if there's a mismatch. Otherwise, allocate a new AST node for the bracketed term, and use *CreateArgs* on the terms contained within the brackets.

⟨Extended subexpression implementation 1537⟩ +≡

procedure *extSubexpObj.FinishBracketedTerm*;

var *lFormatNr*: integer;

begin if *StillCorrect* **then**

begin *nRSymbolNr* \leftarrow *CurWord.Nr*; *lFormatNr* \leftarrow *gFormatsColl.LookUp_BracketFormat*(*nSymbolNr*,
nRSymbolNr, *TermNbr* - *nTermBase*, 0, 0);

if *lFormatNr* = 0 **then** *SemErr*(152);

gLastTerm \leftarrow *new*(*CircumfixTermPtr*, *Init*(*CurPos*, *nSymbolNr*, *nRSymbolNr*,
CreateArgs(*nTermBase* + 1)));

end;

end;

1591. Remember that Mizar calls “an instance of structure” an “**Aggregate**”. When the Parser is parsing for a closed subterm and has stumbled across a structure constructor (§1665), it first invokes this method. This stores the ID number for the structure in the caller's *nSymbolNr*.

⟨Extended subexpression implementation 1537⟩ +≡

procedure *extSubexpObj.StartAggregateTerm*;

begin *nSymbolNr* \leftarrow *CurWord.Nr*;

end;

1592. The Parser has just parsed the arguments for the structure constructor, and the Parser is now looking at the “#” token. This method is invoked.

We should check the format for the structure constructor is stored in the *gFormatsColl*. If not, raise a 176 error. Otherwise, we allocate a new *AggregateTerm* with the parsed arguments, and then update the *gLastTerm* pointer to point at it.

⟨Extended subexpression implementation 1537⟩ +≡

procedure *extSubexpObj.FinishAggregateTerm*;

var *lFormatNr*: integer;

begin *lFormatNr* \leftarrow *gFormatsColl.LookUp_PrefixFormat*(‘G’, *nSymbolNr*, *TermNbr* - *nTermBase*);

if *lFormatNr* = 0 **then** *Error*(*CurPos*, 176); { missing format error }

gLastTerm \leftarrow *new*(*AggregateTermPtr*, *Init*(*CurPos*, *nSymbolNr*, *CreateArgs*(*nTermBase* + 1)));

end;

1593. The Parser is parsing for a closed subterm, and has stumbled across “the” and is looking at a selector token (§1673). This method is invoked. We assign the caller's *nSymbolNr* to the ID number for the selector token, assign the caller's *nSubexpPos* to the Parser's current position, and store the next token's kind (i.e., the “of” token's kind) in the *nNextWord* field.

⟨Extended subexpression implementation 1537⟩ +≡

procedure *extSubexpObj.StartSelectorTerm*;

begin *nSymbolNr* \leftarrow *CurWord.Nr*; *nSubexpPos* \leftarrow *CurPos*; *nNextWord* \leftarrow *AheadWord.Kind*;

end;

1594. The Parser has just parsed “**the** $\langle Selector \rangle$ **of** $\langle Term \rangle$ ”. Now this method is invoked to assemble the parsed data into an AST node.

If there is no selector with this matching format, then a 182 error will be raised.

If the caller’s *nNextWord* is an “of” token’s kind, then we’re describing a selector term. We update the *gLastTerm* state variable to point to a newly allocated *SelectorTerm* object with the appropriate data set.

On the other hand, “**internal selectors**” occur when defining a structure. For example,

```
struct (1-sorted) multMagma (#
  carrier -> set,
  multF -> BinOp of the carrier
#);
```

Observe the *multF* specification is *BinOp of the carrier*. That “**the carrier**” is an internal selector. In this case, allocate a new *InternalSelectorTerm* object, and update the *gLastTerm* state variable to point to it.

If, for some reason, the Parser is in neither situation, then just *gLastTerm* state variable to be an incorrect term.

\langle Extended subexpression implementation 1537 $\rangle + \equiv$

procedure *extSubexpObj.FinishSelectorTerm*;

var *lFormatNr*: integer;

begin *lFormatNr* \leftarrow *gFormatsColl.LookUp_PrefixFormat*(‘U’, *nSymbolNr*, 1);

if *lFormatNr* = 0 **then** *Error*(*nSubexpPos*, 182); { missing format error }

if *nNextWord* = *sy_Of* **then**

gLastTerm \leftarrow *new*(*SelectorTermPtr*, *Init*(*nSubexpPos*, *nSymbolNr*, *gLastTerm*))

else if *in_AggrPattern* **then**

gLastTerm \leftarrow *new*(*InternalSelectorTermPtr*, *Init*(*nSubexpPos*, *nSymbolNr*))

else begin *gLastTerm* \leftarrow *new*(*IncorrectTermPtr*, *Init*(*nSubexpPos*)); *Error*(*nSubexpPos*, 329)

end;

end;

1595. The Parser is about to start parsing a forgetful functor (§1676) — for example “**the multMagma of REAL.TopGroup**”. This method is invoked. The caller’s *nSymbolNr* field is updated to the current token’s ID Number, the *nSubexpPos* field is assigned the Parser’s current position, and the *nNextWord* field is assigned to the token kind of the next token — this is expected to be “of”.

\langle Extended subexpression implementation 1537 $\rangle + \equiv$

procedure *extSubexpObj.StartForgetfulTerm*;

begin *nSymbolNr* \leftarrow *CurWord.Nr*; *nSubexpPos* \leftarrow *CurPos*; *nNextWord* \leftarrow *AheadWord.Kind*;

end;

1596. The Parser just finished parsing a forgetful functor. If the Parser is not panicking, check the format for the forgetful functor matches what is stored in the *gFormatsColl* state variable. If the format is invalid, raise a 184 error.

Whether the Parser is panicking or not, allocate a new *ForgetfulFunctor* term, and update the *gLastTerm* to point to it.

⟨Extended subexpression implementation 1537⟩ +≡

procedure *extSubexpObj.FinishForgetfulTerm*;

var *lFormatNr*: integer;

begin *lFormatNr* ← 0;

if *StillCorrect* **then**

begin *lFormatNr* ← *gFormatsColl.LookUp_PrefixFormat*(*ˆJ*, *nSymbolNr*, 1);

if *lFormatNr* = 0 **then** *Error*(*nSubexpPos*, 184); { missing format }

end;

gLastTerm ← *new*(*ForgetfulFunctorTermPtr*, *Init*(*nSubexpPos*, *nSymbolNr*, *gLastTerm*));

end;

1597. There are several situations where this is invoked:

- (1) The Parser has just parsed “the” but is not looking at a selector symbol (“the multF of...”), nor is the Parser looking at a forgetful functor (“the multMagma of...”). Then this is interpreted as looking at a choice operator (§1673).
- (2) The Parser has just parsed “the” but is not looking at a forgetful functor, so the Parser believes it must be looking at a choice operator (§1676).
- (3) The Parser has just parsed “the” and is now looking at “set” — so this is invoking the axiom of choice to pick “the set” (§1678).

In these three situations, the Parser invokes this method. It just updates the caller’s *nSubexpPos* field to point to the Parser’s current position.

⟨Extended subexpression implementation 1537⟩ +≡

procedure *extSubexpObj.StartChoiceTerm*;

begin *nSubexpPos* ← *CurPos*;

end;

1598. The Parser has just parsed a type, and now believes it has finished parsing a choice expression. Then it invokes this method to construct an appropriate AST node for the term, by specifically allocating a new *ChoiceTerm* for the *gLastType* type. We then update the *gLastTerm* state variable to point to this newly allocated term.

⟨Extended subexpression implementation 1537⟩ +≡

procedure *extSubexpObj.FinishChoiceTerm*;

begin *gLastTerm* ← *new*(*ChoiceTermPtr*, *Init*(*nSubexpPos*, *gLastType*));

end;

1599. When the Parser encounters a numeral while seeking a closed subterm (§1662), it invokes this method to allocate a new *NumeralTerm*. The *gLastTerm* state variable is updated to point to this newly allocated numeral object.

⟨Extended subexpression implementation 1537⟩ +≡

procedure *extSubexpObj.ProcessNumeralTerm*;

begin *gLastTerm* ← *new*(*NumeralTermPtr*, *Init*(*CurPos*, *CurWord.Nr*));

end;

1600. The Parser tries to parse a closed subterm (§1662) and encounters the “it” token. Well, if the *it_Allowed* state variable is true, then we should allocate a new *ItTerm* and update the *gLastTerm* state variable to point to it.

Otherwise, when the *it_Allowed* state variable is false, we should raise a 251 error.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.ProcessItTerm;
  begin if it_Allowed then gLastTerm ← new(ItTermPtr, Init(CurPos))
  else begin gLastTerm ← new(IncorrectTermPtr, Init(CurPos)); ErrImm(251)
  end;
end;
```

1601. The Parser tries parsing for a closed subterm and has encountered a placeholder term for a private functor (e.g., “\$1”). If the *dol_Allowed* state variable is true, then allocate a new *PlaceholderTerm* object and update the *gLastTerm* state variable to point at it.

If the *dol_Allowed* state variable is false, then we should raise a 181 error.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.ProcessLocusTerm;
  begin if dol_Allowed then gLastTerm ← new(PlaceholderTermPtr, Init(CurPos, CurWord.Nr))
  else begin gLastTerm ← new(IncorrectTermPtr, Init(CurPos)); ErrImm(181)
  end;
end;
```

1602. Calamity! An incorrect expression has crossed the Parser’s path. Allocate an *IncorrectTerm* object located at the Parser’s current position, then update the *gLastTerm* state variable to point to it.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.InsertIncorrTerm;
  begin gLastTerm ← new(IncorrectTermPtr, Init(CurPos));
end;
```

Subsection 23.3.4. Parsing formulas

1603. The Parser is trying to parse an atomic formula (§1719), but something has gone awry. Allocate a new *IncorrectFormula* object located at the Parser’s current position, update the *gLastFormula* state variable to point to it, and “reset” the *TermNbr* state variable to point to where the caller’s *nTermBase* is located.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.InsertIncorrBasic;
  begin gLastFormula ← new(IncorrectFormulaPtr, Init(CurPos)); TermNbr ← nTermBase;
end;
```

1604. While the Parser was trying to parse a formula, it found something which “doesn’t quite fit”. Allocate a new *IncorrectFormula* object, then update the *gLastFormula* state variable to point to it.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.InsertIncorrFormula;
  begin gLastFormula ← new(IncorrectFormulaPtr, Init(CurPos));
end;
```

1605. If we are in a proof, allocate a new *ThesisFormula* object (recall the `WEB` macro for this §1366). Otherwise, raise a 65 error.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.ProcessThesis;
  begin if gProofCnt > 0 then gLastFormula ← thesis_formula
  else begin ErrImm(65); gLastFormula ← new(IncorrectFormulaPtr, Init(CurPos));
    end;
  end;
```

1606. The Parser has encountered “⟨*Term*⟩ *is*”, or some other generic atomic formula (§1719), this method is invoked.

If more than one term appears before the “*is*” token (i.e., if $TermNbr - nTermBase \neq 1$), then a 157 error is raised. There is a Polish comment here, “Trzeba chyba wstawic recovery dla $TermNbr = nTermBase$ ”, which I translated to English.

This will initialize the fields for the caller in preparation for parsing some atomic formula. In particular, this is the only place where *TermNbr* is initialized to a nonzero value (and isn’t in an incorrect formula).

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.ProcessAtomicFormula;
  const MaxArgListNbr = 20;
  begin nSubexpPos ← CurPos; nSymbolNr ← 0;
  case CurWord.Kind of
    sy_Is: if  $TermNbr - nTermBase \neq 1$  then
      begin ErrImm(157); TermNbr ← nTermBase; InsertIncorrTerm; FinishArgument;
        { I think you need to insert recovery for  $TermNbr = nTermBase$  }
      end;
    endcases;
  nRightArgBase ← TermNbr; nTermBase ← TermNbr; nPostNegated ← false; nArgListNbr ← 0;
  nArgList[0].Start ← TermNbr + 1;
  end;
```

1607. The Parser is either finishing a “predicative formula” (§1718) or it’s parsing a predicate pattern (§1820), it invokes this method to initialize the fields needed when forming an AST node. Specifically, the *nSubexpPos* is assigned to the Parser’s current position, the *nSymbolNr* is updated either to the current token’s ID number (if the current token is “=” or a predicate) or else assigned to be zero. Last, the *nRightArgBase* is assigned to equal the *TermNbr* state variable.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.ProcessPredicateSymbol;
  begin nSubexpPos ← CurPos;
  case CurWord.Kind of
    sy_Equal, PredicateSymbol: nSymbolNr ← CurWord.Nr;
  othercases nSymbolNr ← 0;
  endcases;
  nRightArgBase ← TermNbr;
  end;
```

1608. The Parser is parsing a “predicate formula” which has arguments on the righthand side of the predicate symbol (§1713).

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.ProcessRightSideOfPredicateSymbol;
  begin nRightSideOfPredPos ← CurPos;
  case CurWord.Kind of
    sy_Equal, PredicateSymbol: nSymbolNr ← CurWord.Nr;
  othercases nSymbolNr ← 0;
  endcases;
  nRightArgBase ← TermNbr;
end;
```

1609. The Parser has just finished a “predicate formula” (§1718), then this method is invoked to construct an AST for the formula. First we check if the format is valid. If the format for the formula is not found in the *gFormatsColl*, then we must raise a 153 error. Otherwise, we construct two lists (one for the left arguments, another for the right arguments), and use them to construct a new *PredicativeFormula* object. We update the *gLastFormula* state variable to point to the newly allocated formula object.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.FinishPredicativeFormula;
  var lLeftArgs, lRightArgs: PList; lFormatNr: integer;
  begin lFormatNr ← gFormatsColl.LookUp_PredFormat(nSymbolNr, nRightArgBase − nTermBase,
    TermNbr − nRightArgBase);
  if lFormatNr = 0 then Error(nSubexpPos, 153); { missing format }
  lRightArgs ← CreateArgs(nRightArgBase + 1); lLeftArgs ← CreateArgs(nTermBase + 1);
  gLastFormula ← new(PredicativeFormulaPtr, Init(nSubexpPos, nSymbolNr, lLeftArgs, lRightArgs));
end;
```

1610. The Parser tries to construct an AST when finishing up the right-hand side of a predicative formula (§1713), it invokes this method after the *extSubexpObj.FinishPredicativeFormula* has been invoked.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.FinishRightSideOfPredicativeFormula;
  var lRightArgs: PList; lLeftArgsNbr, lFormatNr: integer; lFrm: FormulaPtr;
  begin lFrm ← gLastFormula;
  if lFrm↑.nFormulaSort = wsNegatedFormula then lFrm ← NegativeFormulaPtr(lFrm)↑.nArg;
  lLeftArgsNbr ← RightSideOfPredicativeFormulaPtr(lFrm)↑.nRightArgs↑.Count;
  lFormatNr ← gFormatsColl.LookUp_PredFormat(nSymbolNr, lLeftArgsNbr, TermNbr − nRightArgBase);
  if lFormatNr = 0 then Error(nSubexpPos, 153); { missing format }
  lRightArgs ← CreateArgs(nRightArgBase + 1);
  gLastFormula ← new(RightSideOfPredicativeFormulaPtr, Init(nSubexpPos, nSymbolNr, lRightArgs));
  nMultiPredicateList.Insert(gLastFormula);
end;
```

1611. When the Parser is parsing an atomic formula, when it has parsed a formula and encounters another predicate, it defaults to thinking that it is starting a “multi-predicative formula” (§1714), and it invokes this method. This initializes the *nMultiPredicateList* to an empty list of length 4, and the first entry points to the same formula pointed to by the *gLastFormula* state variable.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.StartMultiPredicativeFormula;
  begin nMultiPredicateList.Init(4); nMultiPredicateList.Insert(gLastFormula);
end;
```

1612. Finishing a “multi-predicative formula” allocates a new *MultiPredicativeFormula* object, and moves the contents of the caller’s *nMultiPredicateList* to the newly minted formula. The *gLastFormula* state variable is updated to point to this newly allocated formula object.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.FinishMultiPredicativeFormula;
  begin gLastFormula  $\leftarrow$  new(MultiPredicativeFormulaPtr, Init(nSubexpPos, new(PList,
    MoveList(nMultiPredicateList))));
  end;
```

1613. The Parser has just parsed “⟨*Term*⟩ is ⟨*Type*⟩”, and now we need to store the accumulated data into a Formula AST. Of course, if the *gLastType* variable is not pointing to a type object, then we should raise an error (clearly something has gone wrong somewhere).

If we have accumulated attributes while parsing, then we should update the *gLastType* to be a clustered type object (and we should move the attributes over).

We should allocate a *QualifiedFormula* object, update the *gLastFormula* state variable to point to it. If the Parser has encountered “⟨*Term*⟩ is not ⟨*Type*⟩”, then it will tell the caller to toggle the *nPostNegated* to be true — and in that case, we should negate the *gLastFormula* state variable.

We mutate the *TermNbr* state variable, decrementing it by one (since we consumed the top of the term stack).

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.FinishQualifyingFormula;
  var j: integer;
  begin mizassert(5430, gLastType  $\neq$  nil);
  if nAttrCollection.Count > 0 then
    begin gLastType  $\leftarrow$  new(ClusteredTypePtr, Init(gLastType↑.nTypePos, new(PList,
      Init(nAttrCollection.Count), gLastType)));
    for j  $\leftarrow$  0 to nAttrCollection.Count − 1 do
      ClusteredTypePtr(gLastType↑).nAdjectiveCluster↑.Insert(PObject(nAttrCollection.Items↑[j]));
    end;
    gLastFormula  $\leftarrow$  new(QualifyingFormulaPtr, Init(nSubexpPos, Term[TermNbr], gLastType));
    if nPostNegated then gLastFormula  $\leftarrow$  new(NegativeFormulaPtr, Init(nNotPos, gLastFormula));
    dec(TermNbr);
  end;
```

1614. The Parser has just finished parsing “⟨*Term*⟩ is ⟨*Attribute*⟩” or “⟨*Term*⟩ is not ⟨*Attribute*⟩”, and so it invokes this method. We allocate a new *AttributiveFormula* object, and negate it if needed. We also decrement the *TermNbr* state variable (since we consumed one element of the term stack).

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.FinishAttributiveFormula;
  begin gLastFormula  $\leftarrow$  new(AttributiveFormulaPtr, Init(nSubExpPos, Term[TermNbr], new(PList,
    MoveList(nAttrCollection))));
  if nPostNegated then gLastFormula  $\leftarrow$  new(NegativeFormulaPtr, Init(nNotPos, gLastFormula));
  dec(TermNbr);
  end;
```

1615. While the Parser is working its way through a formula, and it is looking at an identifier and the next token is a square bracket “[”, then the Parser invokes this method to initialize the relevant fields to store accumulated data.

⟨Extended subexpression implementation 1537⟩ +≡

procedure *extSubexpObj.StartPrivateFormula*;

begin *nTermBase* \leftarrow *TermNbr*; *nSubexpPos* \leftarrow *CurPos*; *nSpelling* \leftarrow *CurWord.Nr*;
 end;

1616. The Parser has just encountered “]” and now we assemble the accumulated data into a formula. This allocates a new *PrivatePredicativeFormula*, moves the arguments encountered since starting the private predicate into a list (§1540) owned by the formula object. The *gLastFormula* is updated to point to the newly allocated formula object.

⟨Extended subexpression implementation 1537⟩ +≡

procedure *extSubexpObj.FinishPrivateFormula*;

begin *gLastFormula* \leftarrow *new(PrivatePredicativeFormulaPtr, Init(nSubexpPos, nSpelling,*
 CreateArgs(nTermBase + 1)));
 end;

1617. The Parser has encountered the “contradiction” token, so it invokes this method, which allocates a *ContradictionFormula* and updates the *gLastFormula* state variable to point to it.

⟨Extended subexpression implementation 1537⟩ +≡

procedure *extSubexpObj.ProcessContradiction*;

begin *gLastFormula* \leftarrow *new(ContradictionFormulaPtr, Init(CurPos))*;
 end;

1618. The Parser routinely allocates a formula object, then realizes later it should negate that formula object. This is handled by storing the formula object in the *gLastFormula* object, then this method allocates a new formula (which is the negation of the *gLastFormula*) and updates the *gLastFormula* to point to the newly allocated negated formula.

⟨Extended subexpression implementation 1537⟩ +≡

procedure *extSubexpObj.ProcessNegation*;

begin *gLastFormula* \leftarrow *new(NegativeFormulaPtr, Init(CurPos, gLastFormula))*;
 end;

1619. When the Parser has encountered the “not” reserved keyword, it invokes the *ProcessNegation* method which just toggles the *nPostNegated* field of the caller, and assigns the *nNotPos* field to the Parser’s current position.

⟨Extended subexpression implementation 1537⟩ +≡

procedure *extSubexpObj.ProcessNegation*;

begin *nPostNegated* \leftarrow \neg *nPostNegated*; *nNotPos* \leftarrow *CurPos*;
 end;

1620. When the Parser is looking at a binary connective token (e.g., “implies”, “or”, etc.), this method is invoked to store the connective kind as well as the “left-hand side” to the binary connective in the *nFirstSententialOperand* field.

⟨Extended subexpression implementation 1537⟩ +≡

procedure *extSubexpObj.ProcessBinaryConnective*;

begin *nConnective* \leftarrow *CurWord.Kind*; *nFirstSententialOperand* \leftarrow *gLastFormula*;
 nSubexpPos \leftarrow *CurPos*;
 end;

```

 $\langle \text{Extended subexpression implementation } 1537 \rangle \equiv$ 
procedure extSubexpObj.ProcessFlexDisjunction;
begin nFirstSententialOperand  $\leftarrow$  gLastFormula;
end;

```

```

 $\langle \text{Extended subexpression implementation } 1537 \rangle \equiv$ 
procedure extSubexpObj.ProcessFlexConjunction;
begin nFirstSententialOperand  $\leftarrow$  gLastFormula;
end;

```

```

 $\langle \text{Extended subexpression implementation } 1537 \rangle + \equiv$ 
procedure extSubexpObj.StartRestriction;
begin nRestrPos  $\leftarrow$  CurPos;
end;

```

```

 $\langle \text{Extended subexpression implementation } 1537 \rangle + \equiv$ 
procedure extSubexpObj.FinishRestriction;
begin nRestriction  $\leftarrow$  gLastFormula;
end;

```

```

⟨Extended subexpression implementation 1537⟩ +≡
procedure extSubexpObj.FinishBinaryFormula;

```

```

begin case nConnective of
sy_Implies: gLastFormula  $\leftarrow$  new(ConditionalFormulaPtr, Init(nSubExpPos, nFirstSententialOperand,
gLastFormula));
sy_Iff: gLastFormula  $\leftarrow$  new(BiconditionalFormulaPtr, Init(nSubexpPos, nFirstSententialOperand,
gLastFormula));
sy_Or: gLastFormula  $\leftarrow$  new(DisjunctiveFormulaPtr, Init(nSubexpPos, nFirstSententialOperand,
gLastFormula));
sy_Ampersand: gLastFormula  $\leftarrow$  new(ConjunctiveFormulaPtr, Init(nSubexpPos,
nFirstSententialOperand, gLastFormula));
othercases RunTimeError(3124);
endcases;
end;

```

1626. We have parsed “ $\langle Formula \rangle$ or ... or $\langle Formula \rangle$ ”, and the Parser invokes this method to construct an AST for the formula. This method allocates a new *FlexaryDisjunctive* formula object, and updates the *gLastFormula* state variable to point to it.

There is a comment in Polish, “polaczyc z flexConj”, which Google translates to “connect to flexConj”.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.FinishFlexDisjunction; { polaczyc z flexConj }
begin gLastFormula ← new(FlexaryDisjunctiveFormulaPtr, Init(CurPos, nFirstSententialOperand,
    gLastFormula));
end;
```

1627. We have parsed “ $\langle Formula \rangle$ & ... & $\langle Formula \rangle$ ”, and the Parser invokes this method to construct an AST for the formula. This allocates a new *FlexaryConjunctive* formula object, and updates the *gLastFormula* state variable to point to it.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.FinishFlexConjunction;
begin gLastFormula ← new(FlexaryConjunctiveFormulaPtr, Init(CurPos, nFirstSententialOperand,
    gLastFormula));
end;
```

1628. The Parser is looking at the “ex” token, then invokes this method to reset the caller’s fields in preparation for accumulating data needed when constructing the formula’s AST.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.StartExistential;
begin nQualifiedSegments.Init(0); nSubexpPos ← CurPos;
end;
```

1629. The Parser is looking at the “for” token, and it invokes this method to reset the relevant fields in the caller.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.StartUniversal;
begin nQualifiedSegments.Init(0); nSubexpPos ← CurPos;
end;
```

1630. After the Parser has invoked *StartUniversal* or *StartExistential*, it parses the quantified variables (which begins by invoking this method).

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.StartQualifiedSegment;
begin nSegmentIdentColl.Init(2); nSegmentPos ← CurPos;
end;
```

1631. The Parser has parsed a comma-separated list and is expecting either “be” or “being”, but before parsing for that copula the Parser invokes the *StartQualifyingType* method to update the *gLastType* state variable to point to *nil*.

⟨Extended subexpression implementation 1537⟩ +≡

```
procedure extSubexpObj.StartQualifyingType;
begin gLastType ← nil;
end;
```


1632. The Parser has just finished parsing quantified variables. There are two possible situations:

- (1) We have just parsed reserved variables, so the types are all known. Then the $gLastType = \mathbf{nil}$.
- (2) We have parsed an explicitly typed list of variables, so the $gLastType \neq \mathbf{nil}$.

In the first case, we should allocate an *ImplicitlyQualifiedSegment* object and move all the segment's identifiers to this object. Then we clean up the caller's $nSegmentIdentColl$ field (since it's an array of \mathbf{nil} pointers).

In the second case, we can just move the identifiers when allocating a new *ExplicitlyQualifiedSegment* object.

In both cases, the new allocated *QuantifiedSegment* object is appended to the caller's $nQualifiedSegments$ field.

⟨Extended subexpression implementation 1537⟩ +≡

procedure *extSubexpObj.FinishQualifiedSegment*;

var k : integer;

begin if $gLastType = \mathbf{nil}$ **then**

begin for $k \leftarrow 0$ **to** $nSegmentIdentColl.Count - 1$ **do**

begin $nQualifiedSegments.Insert(new(ImplicitlyQualifiedSegmentPtr,$

$Init(VariablePtr(nSegmentIdentColl.Items \uparrow [k]) \uparrow .nVarPos, nSegmentIdentColl.Items \uparrow [k]))$;

$nSegmentIdentColl.Items \uparrow [k] \leftarrow \mathbf{nil}$;

end;

$nSegmentIdentColl.Done$;

end

else begin $nQualifiedSegments.Insert(new(ExplicitlyQualifiedSegmentPtr, Init(nSegmentPos,$
 $new(PList, MoveList(nSegmentIdentColl)), gLastType)))$;

end;

end;

1633. When the Parser is parsing quantified variables, specifically when it is parsing a comma-separated list of variables, it will invoke this method, then check if the next token is a comma (and if so iterate). This *ProcessVariable* method should accumulate a *Variable* object with the current token's identifier, then insert it into the caller's $nSegmentIdentColl$ field.

⟨Extended subexpression implementation 1537⟩ +≡

procedure *extSubexpObj.ProcessVariable*;

begin $nSegmentIdentColl.Insert(new(VariablePtr, Init(CurPos, GetIdentifier)))$;

end;

1634. The Parser has just finished something like

$$\text{ex } \langle \text{Qualified-Variables} \rangle , \dots , \langle \text{Qualified-Variables} \rangle \text{ st } \langle \text{Formula} \rangle$$

Now we assemble it as

$$\text{ex } \langle \text{Qualified-Variables} \rangle \text{ st } (\text{ex } \dots \text{ st } (\text{ex } \langle \text{Qualified-Variables} \rangle \text{ st } \langle \text{Formula} \rangle))$$

starting with the innermost existentially quantified formula, working our ways outwards.

Importantly, assembling the AST reflects the quantified variables has the grammar

$$\begin{aligned} \langle \text{Qualified-Variables} \rangle &= \langle \text{Implicitly-Qualified-Variables} \rangle \\ &\quad | \langle \text{Explicitly-Qualified-Variables} \rangle \\ &\quad | \langle \text{Explicitly-Qualified-Variables} \rangle ", " \langle \text{Implicitly-Qualified-Variables} \rangle \end{aligned}$$

(Extended subexpression implementation 1537) +≡

procedure *extSubexpObj.FinishExistential*;

var *k*: integer;

begin for *k* ← *nQualifiedSegments.Count* − 1 **downto** 1 **do** { from inside outwards }

begin *gLastFormula* ← *new*(*ExistentialFormulaPtr*,
Init(*QualifiedSegmentPtr*(*nQualifiedSegments.Items*↑[*k*])↑.*nSegmPos*,
nQualifiedSegments.Items↑[*k*], *gLastFormula*)); *nQualifiedSegments.Items*↑[*k*] ← **nil**;

end;

if *nQualifiedSegments.Count* > 0 **then**

begin *gLastFormula* ← *new*(*ExistentialFormulaPtr*, Init(*nSubexpPos*, *nQualifiedSegments.Items*↑[0],
gLastFormula)); *nQualifiedSegments.Items*↑[0] ← **nil**;

end;

nQualifiedSegments.Done;

end;

1635. Universally quantified formulas first transforms

$$\text{for } \langle \text{Qualified-Variables} \rangle \text{ st } \langle \text{Formula} \rangle_1 \text{ holds } \langle \text{Formula} \rangle_2$$

into

$$\text{for } \langle \text{Qualified-Variables} \rangle \text{ holds } \langle \text{Formula} \rangle_1 \text{ implies } \langle \text{Formula} \rangle_2$$

which is handled immediately.

The remainder of the method iteratively constructs the universally quantified formulas by “unrolling” the qualified segments, just as we did for existentially quantified formulas.

(Extended subexpression implementation 1537) +≡

procedure *extSubexpObj.FinishUniversal*;

var *k*: integer;

begin if *nRestriction* ≠ **nil** **then** { transform st into implies }

gLastFormula ← *new*(*ConditionalFormulaPtr*, Init(*nRestrPos*, *nRestriction*, *gLastFormula*));

for *k* ← *nQualifiedSegments.Count* − 1 **downto** 1 **do**

begin *gLastFormula* ← *new*(*UniversalFormulaPtr*,
Init(*QualifiedSegmentPtr*(*nQualifiedSegments.Items*↑[*k*])↑.*nSegmPos*,
nQualifiedSegments.Items↑[*k*], *gLastFormula*)); *nQualifiedSegments.Items*↑[*k*] ← **nil**;

end;

if *nQualifiedSegments.Count* > 0 **then**

begin *gLastFormula* ← *new*(*UniversalFormulaPtr*, Init(*nSubexpPos*, *nQualifiedSegments.Items*↑[0],
gLastFormula)); *nQualifiedSegments.Items*↑[0] ← **nil**;

end;

end;

Section 23.4. EXTENDED EXPRESSION CLASS

1636. When an expression is needed, the *gExpPtr* state variable is used to build it out of subexpressions. The *gExpPtr* state variable is an instance of the *extExpression* class.

⟨ Extended expression class declaration 1636 ⟩ ≡
extExpressionPtr = ↑*extExpressionObj*;
extExpressionObj = **object** (*ExpressionObj*)
 constructor *Init* (*fExpKind* : *ExpKind*);
 procedure *CreateSubexpression*; *virtual*;
end ;

This code is used in section 1346.

1637. Constructor. This just invokes the parent class's constructor (§838), then resets the module-wide variable *TermNbr* to zero.

⟨ Extended expression implementation 1637 ⟩ ≡
constructor *extExpressionObj.Init* (*fExpKind* : *ExpKind*);
 begin *inherited Init* (*fExpKind*); *TermNbr* ← 0;
 end;

See also section 1638.

This code is used in section 1347.

1638. An *extExpression* creating a subexpression *overrides* the parent class's method (§839), and sets the global *gSubexpPtr* to point to a new *extSubexp* object.

⟨ Extended expression implementation 1637 ⟩ +≡
procedure *extExpressionObj.CreateSubexpression*;
 begin *gSubexpPtr* ← *new* (*extSubexpPtr*, *Init*)
 end;

File 24

Parser

1639. The Parser has a “big red button”: a single “obvious” function for the user to, you know, push. Namely, the *Parse* procedure (§§1888 *et seq.*). Everything else is just a helper function.

The design of the Parser appears to be a recursive descent Parser on statements, with parsing expressions handled specially.

Note that the `base/parser.pas` file appears to be naturally divided up into sections, with comments which appear to use the Germanic “s p a c i n g f o r i t a l i c s” (which I have just replaced with more readable *italicized* versions). I have used these cleavages to organize the discussion of this file.

The *StillCorrect* global variable is *false* when the Parser has entered what programmers call “**Panic Mode**”: something has gone awry, and the Parser is trying to recover gracefully. For a friendly review of panicking, see Bob Nystrom’s *Crafting Interpreters* ([Chaper 6](#), Section 3).

```

⟨ parser.pas 1639 ⟩ ≡
  ⟨ GNU License 4 ⟩
unit parser;
interface
  uses mscanner;
  var StillCorrect: boolean = true;
  type ReadTokenProcedure = Procedure;
  const ReadTokenProc: ReadTokenProcedure = ReadToken; { from mscanner.pas }
  procedure Parse;
  procedure SemErr(fErrNr : integer);
implementation
  uses syntax, errhan, pragmas
      mdebug , info end_mdebug;
  ⟨ Implementation of parser.pas 1640 ⟩

```

1640. We have a few constants, but the implementation is loosely organized around parsing expressions (terms and formulas), statements, and then blocks.

```

⟨ Implementation of parser.pas 1640 ⟩ ≡
  ⟨ Local constants for parser.pas 1641 ⟩;
  ⟨ Parse expressions (parser.pas) 1654 ⟩
  ⟨ Communicate with items (parser.pas) 1740 ⟩
  ⟨ Process miscellany (parser.pas) 1741 ⟩
  ⟨ Parse simple justifications (parser.pas) 1758 ⟩
  ⟨ Parse statements and reasoning (parser.pas) 1769 ⟩
  ⟨ Parse patterns (parser.pas) 1802 ⟩
  ⟨ Parse definitions (parser.pas) 1835 ⟩
  ⟨ Parse scheme block (parser.pas) 1882 ⟩
  ⟨ Main parse method (parser.pas) 1888 ⟩

```

See also sections 1643, 1644, 1646, 1647, 1649, 1650, and 1651.

This code is used in section 1639.

1641. We have error codes for syntactically invalid situations. These are all different ways for panic to occur (hence the “pa-” prefix). We will introduce the error codes when they are first used. The unused error codes are listed below.

⟨Local constants for parser.pas 1641⟩ ≡
const ⟨Error codes for parser 1642⟩

See also section 1645.

This code is used in section 1640.

1642. ⟨Error codes for parser 1642⟩ ≡
paUnexpAntonym1 = 198; *paUnexpAntonym2* = 198; *paUnexpSynonym* = 199; *paUnexpHereby* = 216;
paUnexpReconsider = 228; *paIdentExp5* = 300; *paIdentExp12* = 300; *paWrongRightBracket1* = 311;
paWrongRightBracket2 = 311; *paWrongPattBeg3* = 314; *paRightSquareExp1* = 371;
paRightSquareExp3 = 371; *paRightCurledExp2* = 372; *paWrongAttrPrefixExpr* = 375;
paWrongAttrArgumentSuffix = 376; *paTypeExpInAdjectiveCluster* = 377;
paTypeUnexpInClusterRegistration = 405;

See also sections 1648, 1661, 1664, 1666, 1668, 1671, 1674, 1677, 1679, 1682, 1684, 1690, 1693, 1695, 1697, 1699, 1708, 1710, 1712, 1717, 1720, 1722, 1726, 1728, 1730, 1732, 1738, 1751, 1753, 1755, 1760, 1762, 1764, 1766, 1768, 1773, 1775, 1777, 1779, 1781, 1791, 1793, 1798, 1803, 1806, 1808, 1811, 1813, 1815, 1817, 1819, 1821, 1824, 1827, 1829, 1832, 1834, 1841, 1843, 1845, 1849, 1851, 1853, 1857, 1863, 1866, 1868, 1872, 1874, 1876, 1879, 1883, and 1885.

This code is used in section 1641.

1643. ⟨Implementation of parser.pas 1640⟩ +≡
var *gAddSymbolsSet*: **set of** *char* = []; { not used anywhere }

1644. Syntax errors do three things:

- (1) Marks *StillCorrect* to be false (i.e., enters panic mode)
- (2) Reports the error with the *ErrImm* (§129) function.
- (3) Skips ahead until we find a token in the *gMainSet*, then try to proceed like things are still alright (so we “fail gracefully”).

⟨Implementation of parser.pas 1640⟩ +≡
procedure *SynErr*(*fPos* : *Position*; *fErrNr* : *integer*);
begin if *StillCorrect* **then**
 begin *StillCorrect* ← *false*;
 if *CurWord.Kind* = *sy_Error* **then**
 begin if *CurWord.Nr* ≠ *scTooLongLineErrorNr* **then** *ErrImm*(*CurWord.Nr*)
 else *Error*(*fPos*, *fErrNr*);
 end
 else *Error*(*fPos*, *fErrNr*);
 while ¬(*CurWord.Kind* ∈ *gMainSet*) **do** *ReadTokenProc*;
 end;
end;

1645. What constants are good “check-in points” for the Parser to recover at? The beginning of blocks, the end of statements (especially semicolons), and the end of text.

Note: *gMainSet* is only used in the *SynErr* procedure, and nowhere else in Mizar.

⟨Local constants for parser.pas 1641⟩ +≡
const *gMainSet*: **set of** *TokenKind* = [*sy_Begin*, *sy_Semicolon*, *sy_Proof*, *sy_Now*, *sy_Hereby*,
sy_Definition, *sy_End*, *sy_Theorem*, *sy_Reserve*, *sy_Notation*, *sy_Registration*, *sy_Scheme*, *EOT*,
sy_Deffunc, *sy_Defpred*, *sy_Reconsider*, *sy_Consider*, *sy_Then*, *sy_Per*, *sy_Case*, *sy_Suppose*];

1646. We have a few more methods for *specific situations* where errors are likely to occur.

⟨Implementation of parser.pas 1640⟩ +≡

```
procedure MissingWord(fErrNr : integer);
  var lPos: Position;
  begin lPos ← PrevPos; inc(lPos.Col); SynErr(lPos,fErrNr)
  end;

procedure WrongWord(fErrNr : integer);
  begin SynErr(CurPos,fErrNr)
  end;
```

1647. We will want to assert the Parser has encountered a specific token (like a semicolon or “end”) and raise an error if it has not. This will make for much more readable code later on. We should recall *KillItem* (§813) mutates the global state.

[[The *Semicolon* procedure should probably match the *AcceptEnd* procedure — i.e., it should be of the form “**if** ⟨*Current token is semicolon*⟩ **then** *ReadTokenProc* **else** ⟨*Flag error*⟩”.]]

⟨Implementation of parser.pas 1640⟩ +≡

```
procedure Semicolon;
  begin KillItem;
  if CurWord.Kind ≠ sy.Semicolon then MissingWord(paSemicolonExp);
  if CurWord.Kind = sy.Semicolon then ReadTokenProc;
  end;

procedure AcceptEnd(fPos : Position);
  begin if CurWord.Kind = sy.End then ReadTokenProc
  else begin Error(fPos,paEndExp); MissingWord(paUnpairedSymbol)
  end;
  end;
```

1648. ⟨Error codes for parser 1642⟩ +≡

paUnpairedSymbol = 214; *paEndExp* = 215; *paSemicolonExp* = 330;

1649. Due to the structure of PASCAL, the Parser will frequently be in situations where we consider the **case** of the current kind of token, and for “valid” branches we will want the Parser to consume the current token and move on. For example, if the Parser is looking at an open bracket.

But if the Parser is a panicking mess, then we should raise an error to alert the user.

[[Either some explanation should be offered for the magic number 2546 = #9f2, or it should be stored in a constant (or a WEB macro).]]

⟨Implementation of parser.pas 1640⟩ +≡

```
procedure ReadWord;
  begin Mizassert(2546,StillCorrect); ReadTokenProc
  end;
```

1650. These previous methods can be generalized to an *Accept* procedure which checks whether a given *TokenKind* has “occurred”. If so, just read the next word. Otherwise, flag an error.

When will an error be flagged? If the Parser is panicking, or if the current token does not match the expected token.

⟨Implementation of parser.pas 1640⟩ +≡

```
function Occurs(fW : TokenKind): boolean;
  begin Occurs ← false;
  if CurWord.Kind = fW then
    begin ReadWord; Occurs ← true end
  end;

procedure Accept(fCh : TokenKind; fErrNr : integer);
  begin if ¬Occurs(fCh) then MissingWord(fErrNr)
  end;
```

1651. Flagging a semantic error should first check if we are in “panic mode” or not. If we are already panicking, there’s no reason to heap more panicky error messages onto the screen.

⟨Implementation of parser.pas 1640⟩ +≡

```
procedure SemErr(fErrNr : integer);
  begin if StillCorrect then ErrImm(fErrNr)
  end;
```

1652. Exercise: For each procedure and function we are about to define in the rest of the Parser, when will an error be raised and by which of these functions?

Section 24.1. EXPRESSIONS

1653. The syntactic classes we're interested in (terms, types, formulas) almost always appear as subexpressions in a formula or some other expression. The Parser works with various procedures to parse these guys as subexpressions: *TermSubexpression* (§1687), *TypeSubexpression* (§1702), *FormulaSubexpression* (§1739). When we need a term (or type or formula) as an expression, as we will in the next section, we use these procedures to construct the abstract syntax tree.

Subsection 24.1.1. Terms

1654. We have a few token kinds which indicate the start of a term:

- (1) identifiers (for variables and private functors),
- (2) infix operators,
- (3) numerals,
- (4) left and right brackets of all sorts,
- (5) the anaphoric “it” constant used in definitions,
- (6) “the” choice operator,
- (7) placeholder variables appearing in private functors and predicates,
- (8) structure symbols.

⟨ Parse expressions (`parser.pas`) 1654 ⟩ ≡
 { *Expressions* }

const *TermBegSys*: **set of**

TokenKind = [*Identifier*, *InfixOperatorSymbol*, *Numeral*, *LeftCircumfixSymbol*, *sy_LeftParanthesis*,
sy_It, *sy_LeftCurlyBracket*, *sy_LeftSquareBracket*, *sy_The*, *sy_Dolar*, *Structuresymbol*];

See also sections 1655, 1656, 1657, 1658, 1662, 1680, 1681, 1683, 1691, 1694, 1702, 1703, 1704, 1705, 1706, 1709, 1711, 1713, 1714, 1718, 1719, 1727, 1733, 1734, 1735, 1736, 1737, and 1739.

This code is used in section 1640.

1655. We have a few helper function for *Accept*-ing parentheses. This invokes the *ProcessLeftParanthesis* method for the *gSubexpPtr* (§817) global variable which we recall (§845) is an empty virtual method. So the Parser just “consumes” a left parentheses, and will continue to read tokens while they are left parentheses. The argument passed in will be mutated to track the number of left parentheses consumed.

Similarly, the *CloseParenth* method will have the compiler consume right parentheses, mutating the argument passed in (to decrement the number of right parentheses consumed). This will let us track mismatched parentheses errors.

[[The *ClosedParenth* method should raise an error when the user passes a negative value for *fParenthCnt*, but that may be “too defensive”.]]

⟨ Parse expressions (`parser.pas`) 1654 ⟩ +≡

procedure *OpenParenth*(**var** *fParenthCnt* : *integer*);

begin *fParenthCnt* ← 0;

while *CurWord.Kind* = *sy_LeftParanthesis* **do**

begin *gSubexpPtr*↑.*ProcessLeftParanthesis*; *ReadWord*; *inc*(*fParenthCnt*);

end; { *fParenthCnt* ≥ 0 }

end;

procedure *CloseParenth*(**var** *fParenthCnt* : *integer*);

begin while (*CurWord.Kind* = *sy_RightParanthesis*) ∧ (*fParenthCnt* > 0) **do**

begin *dec*(*fParenthCnt*); *gSubexpPtr*↑.*ProcessRightParanthesis*; *ReadWord*;

end; { *old*(*fParenthCnt*) ≥ 0 implies *fParenthCnt* ≥ 0 }

end;

1656. Qualified expressions. Parsing qualified expressions includes a control flow for “exactly” qualified expressions.

We should recall from “Mizar in a nutshell” that the “**exactly**” keyword is reserved but not currently used for anything. The global subexpression pointer is invoking empty virtual methods (§845). So what’s going on?

Well, the only work being done here is in the branch handling “qua”, specifically the *gSubexpPtr* state variable marks the “qua” position (§1548), the next word is read, and then control is handed off to the Parser’s *TypeSubexpression* procedure. The AST is assembled with the *FinishQualifiedTerm* (§1549) method.

⟨ Parse expressions (**parser.pas**) 1654 ⟩ +≡

procedure *TypeSubexpression*; *forward*;

procedure *AppendQua*;

begin while *CurWord.Kind* = *sy_Qua* **do**

begin *gSubexpPtr*↑.*ProcessQua*; *ReadWord*; *TypeSubexpression*; *gSubexpPtr*↑.*FinishQualifiedTerm*;
end;

if *CurWord.Kind* = *sy_Exactly* **then**

begin *gSubexpPtr*↑.*ProcessExactly*; *ReadWord*
end;

end;

1657. Parsing *the contents of* a bracketed term starts a bracketed term (§1589), reads the next word after the start of the bracket, then consumes the maximum number of visible arguments (§809). The *gSubexpPtr* constructs the AST for the bracketed term and its contents (§1590).

The contract for this function is that a left bracket token has been encountered, the Parser has moved on to the next token, and then invoked this function.

⟨ Parse expressions (**parser.pas**) 1654 ⟩ +≡

procedure *GetArguments*(**const** *fArgsNbr*: *integer*); *forward*;

procedure *BracketedTerm*;

begin *gSubexpPtr*↑.*StartBracketedTerm*; *ReadWord*; *GetArguments*(*MaxVisArgNbr*);
gSubexpPtr↑.*FinishBracketedTerm*;

end;

1658. Parsing post-qualified variables (i.e., variables which appear in a Fraenkel term’s “**where**” clause) which consists of a comma-separated list of post-qualified segments.

⟨ Parse expressions (**parser.pas**) 1654 ⟩ +≡

procedure *TermSubexpression*; *forward*;

procedure *FormulaSubexpression*; *forward*;

procedure *ArgumentsTail*(*fArgsNbr* : *integer*); *forward*;

procedure *ProcessPostqualification*;

begin *gSubexpPtr*↑.*StartPostqualification*; { (§1579) }

while *CurWord.Kind* = *sy_Where* **do**

begin repeat ⟨ Process post-qualified segment 1659 ⟩

until *CurWord.Kind* ≠ *sy_Comma*;

end;

end;

1659. Each “segment” in a post-qualification looks like:

$$\langle \text{variable} \rangle \{ ", " \langle \text{variable} \rangle \} ("is" | "being") \langle \text{type} \rangle$$

We can process the comma-separated list of variables, then the type ascription term (“is” or “being”), then process the type.

```

define parse_post_qualified_type  $\equiv$  begin ReadWord; TypeSubexpression; end
 $\langle$  Process post-qualified segment 1659  $\rangle \equiv$ 
  gSubexpPtr $\uparrow$ .StartPostQualifyingSegment; { (§1580) } ReadWord;
 $\langle$  Parse post-qualified comma-separated list of variables 1660  $\rangle$ ;
  gSubexpPtr $\uparrow$ .StartPostqualificationSpecyfication; { (§1582) }
  if CurWord.Kind  $\in$  [sy_Is, sy_are] then parse_post_qualified_type;
  gSubexpPtr $\uparrow$ .FinishPostqualifyingSegment; { (§1583) }

```

This code is used in section 1658.

1660. \langle Parse post-qualified comma-separated list of variables 1660 $\rangle \equiv$
repeat gSubexpPtr \uparrow .ProcessPostqualifiedVariable; { (§1581) } Accept(Identifier, paIdentExp1);
until \neg Occurs(sy_Comma)

This code is used in section 1659.

1661. \langle Error codes for parser 1642 $\rangle + \equiv$
 paIdentExp1 = 300; paRightParenthExp1 = 370;

1662. Getting a closed subterm is part of the loop for parsing a term. The intricate relationship of mutually recursive function calls looks something like the following (assuming there are no parsing errors):

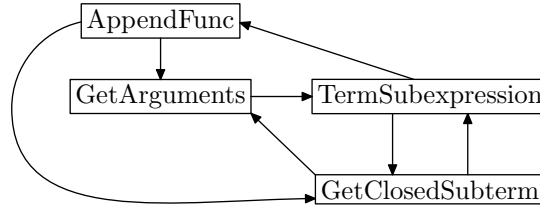


Fig. 8. Control flow when parsing a term.

The *GetArguments* parses a comma-separated list of terms. Since each term in the comma-separated list will be a *subterm* of a larger expression, we parse it with *TermSubexpression* (which invokes *GetClosedSubterm* in a mutually recursive relation). If there is a chain of infix operators (like $x + y - z \times \omega$), then *AppendFunc* is invoked on the infix operators.

```

 $\langle$  Parse expressions (parser.pas) 1654  $\rangle + \equiv$ 
procedure GetClosedSubterm;
  begin case CurWord.Kind of
     $\langle$  Get closed subterm of identifier 1663  $\rangle$ ;
     $\langle$  Get closed subterm of structure 1665  $\rangle$ ;
  Numeral: begin gSubexpPtr $\uparrow$ .ProcessNumeralTerm; ReadWord end;
     $\langle$  Get closed subterm of bracketed expression 1667  $\rangle$ ;
  sy_It: begin gSubexpPtr $\uparrow$ .ProcessItTerm; ReadWord end;
  sy_Dolar: begin gSubexpPtr $\uparrow$ .ProcessLocusTerm; ReadWord end;
     $\langle$  Get closed subterm of Fraenkel operator or enumerated set 1669  $\rangle$ ;
     $\langle$  Get closed subterm of choice operator 1673  $\rangle$ ;
  othercases RunTimeError(2133);
  endcases;
end;

```

1663. If we treat an identifier as a term, then it is either a private functor or it is a variable. How do we tell the difference? A private functor starts with an identifier followed by a left parentheses.

Remember, private functors which omit the closing right parentheses should be flagged with a 370 error.

```

⟨ Get closed subterm of identifier 1663 ⟩ ≡
Identifier: if AheadWord.Kind = sy_LeftParanthesis then { treat identifier as private functor }
  begin gSubexpPtr↑.StartPrivateTerm; ReadWord; ReadWord;
  if CurWord.Kind ≠ sy_RightParanthesis then GetArguments(MaxVisArgNbr);
  gSubexpPtr↑.FinishPrivateTerm; Accept(sy_RightParanthesis, paRightParenthExp2);
  end
else { treat identifier as variable }
  begin gSubexpPtr↑.ProcessSimpleTerm; { (§1547) } ReadWord
  end

```

This code is used in section 1662.

1664. ⟨ Error codes for parser 1642 ⟩ +≡
 paRightParenthExp2 = 370;

1665. If the Parser stumbles across the name of a structure when expecting a term, then the Parser should treat it as constructing a new instance of the structure. A 363 error will be raised if the “(” is missing, and a 373 error will be raised if the “)” structure bracket is missing.

```

⟨ Get closed subterm of structure 1665 ⟩ ≡
StructureSymbol: begin gSubexpPtr↑.StartAggregateTerm; ReadWord;
  Accept(sy_StructLeftBracket, paLeftDoubleExp1); GetArguments(MaxVisArgNbr);
  gSubexpPtr↑.FinishAggregateTerm; { (§1592) } Accept(sy_StructRightBracket, paRightDoubleExp1);
  end

```

This code is used in section 1662.

1666. ⟨ Error codes for parser 1642 ⟩ +≡
 paLeftDoubleExp1 = 363; paRightDoubleExp1 = 373;

1667. Encountering a left bracket of some kind — specifically a user-defined left bracket or a “[” — should cause the Parser to look for the contents of a bracketed term (§1657), then a right bracket.

```

⟨ Get closed subterm of bracketed expression 1667 ⟩ ≡
LeftCircumfixSymbol, sy_LeftSquareBracket: begin BracketedTerm;
  case Curword.Kind of
    sy_RightSquareBracket, sy_RightCurlyBracket, sy_RightParanthesis: ReadWord;
  othercases Accept(RightCircumfixSymbol, paRightBraExp1);
  endcases;
  end

```

This code is used in section 1662.

1668. ⟨ Error codes for parser 1642 ⟩ +≡
 paRightBraExp1 = 310;

1669. When the Parser runs into a left curly bracket “{”, we either have encountered a Fraenkel operator or we have encountered a finite set.

⟨Get closed subterm of Fraenkel operator or enumerated set 1669⟩ ≡
sy_LeftCurlyBracket: **begin** *gSubexpPtr*↑.*StartBracketedTerm*; { (§1589) }
 ReadWord; *TermSubexpression*; { (§1687) }
 if (*CurWord.Kind* = *sy_Colon*) ∨ (*CurWord.Kind* = *sy_Where*) **then** ⟨Parse a Fraenkel operator 1670⟩
 else ⟨Parse an enumerated set 1672⟩;
 end

This code is used in section 1662.

1670. Parsing a Fraenkel operator, well, we recall Fraenkel operators look like

$$\{\langle term \rangle \langle post-qualified segment \rangle " : " \langle formula \rangle\}$$

⟨Parse a Fraenkel operator 1670⟩ ≡
begin *gSubexpPtr*↑.*StartFraenkelTerm*; *ProcessPostqualification*; *gSubexpPtr*↑.*FinishSample*;
 Accept(*sy_Colon*, *paColonExp1*); *FormulaSubexpression*; *gSubexpPtr*↑.*FinishFraenkelTerm*;
 Accept(*sy_RightCurlyBracket*, *paRightCurledExp1*);
end

This code is used in section 1669.

1671. ⟨Error codes for parser 1642⟩ +≡
 paRightCurledExp1 = 372; *paColonExp1* = 384;

1672. The Parser can also run into a finite set $\{x_1, \dots, x_n\}$. The braces are treated like any other functor bracket, in the sense that if the right brace } is missing, then a 310 error will be raised.

⟨Parse an enumerated set 1672⟩ ≡
begin *gSubexpPtr*↑.*FinishArgument*; *ArgumentsTail*(*MaxVisArgNbr* − 1);
 gSubexpPtr↑.*FinishBracketedTerm*;
 case *Curword.Kind* **of**
 sy_RightSquareBracket, *sy_RightCurlyBracket*, *sy_RightParanthesis*: *ReadWord*;
 othercases *Accept*(*RightCircumfixSymbol*, *paRightBraExp1*);
 endcases;
end

This code is used in section 1669.

1673. Mizar allows “**the**” to be used for selector functors, forgetful functors, choice operators, or simple Fraenkel terms.

Note we are generous *here* with what situations leads to treating “**the**” as a choice operator, because in other parsing procedures any mistakes will be caught there.

```
define choice_operator_cases  $\equiv$  ModeSymbol, AttributeSymbol, sy_Non, sy_LeftParanthesis, Identifier,
    InfixOperatorSymbol, Numeral, LeftCircumfixSymbol, sy_It, sy_LeftCurlyBracket,
    sy_LeftSquareBracket, sy_The, sy_Dolar
 $\langle$  Get closed subterm of choice operator 1673  $\rangle \equiv$ 
sy_The: begin gSubexpPtr $\uparrow$ .ProcessThe; ReadWord;
case CurWord.Kind of
  SelectorSymbol:  $\langle$  Parse selector functor 1675  $\rangle$ ;
  StructureSymbol:  $\langle$  Parse forgetful functor or choice of structure type 1676  $\rangle$ ;
  sy_Set:  $\langle$  Parse simple Fraenkel expression or “the set” 1678  $\rangle$ ;
  choice_operator_cases: begin gSubexpPtr $\uparrow$ .StartChoiceTerm; TypeSubexpression;
    gSubexpPtr $\uparrow$ .FinishChoiceTerm;
  end
othercases begin gSubexpPtr $\uparrow$ .InsertIncorrTerm; WrongWord(paWrongAfterThe)
end;
endcases;
end
```

This code is used in section 1662.

1674. \langle Error codes for parser 1642 $\rangle + \equiv$
 paWrongAfterThe = 320;

1675. \langle Parse selector functor 1675 $\rangle \equiv$
begin gSubexpPtr \uparrow .StartSelectorTerm; ReadWord; { parses “**the** \langle selector \rangle ” }
if Occurs(sy_Of) **then** TermSubexpression; { parses “**of** \langle Term \rangle ” }
 gSubexpPtr \uparrow .FinishSelectorTerm; { builds AST subtree }
end

This code is used in section 1673.

1676. A forgetful functor always looks like

“**the**” \langle structure \rangle “**of**” \langle term \rangle

On the other hand, the choice operator acting on a structure type looks similar. We should distinguish these two by the presence of the keyword “**of**”.

```
 $\langle$  Parse forgetful functor or choice of structure type 1676  $\rangle \equiv$ 
if AheadWord.Kind = sy_Of then { forgetful functor }
  begin gSubexpPtr $\uparrow$ .StartForgetfulTerm; ReadWord; Accept(sy_Of, paOfExp); TermSubexpression;
    gSubexpPtr $\uparrow$ .FinishForgetfulTerm;
  end
else { choice operator, e.g., “the multMagma” }
  begin gSubexpPtr $\uparrow$ .StartChoiceTerm; TypeSubexpression; gSubexpPtr $\uparrow$ .FinishChoiceTerm;
  end
```

This code is used in section 1673.

1677. \langle Error codes for parser 1642 $\rangle + \equiv$
 paOfExp = 256;

1678. Mizar allows “the set of” to start a simple Fraenkel expression. But we could also refer to “the set” as the set chosen by the axiom of choice.

```

⟨ Parse simple Fraenkel expression or “the set” 1678 ⟩ ≡
  if AheadWord.Kind = sy_Of then { simple Fraenkel expression }
    begin ReadWord; { set }
      ReadWord; { of }
      gSubexpPtr↑.StartSimpleFraenkelTerm; Accept(sy_All, paAllExp); TermSubexpression;
      gSubexpPtr↑.StartFraenkelTerm; ProcessPostqualification; gSubexpPtr↑.FinishSimpleFraenkelTerm;
    end
  else { “the set” }
    begin gSubexpPtr↑.StartChoiceTerm; TypeSubexpression; gSubexpPtr↑.FinishChoiceTerm; end

```

This code is used in section 1673.

1679. ⟨ Error codes for parser 1642 ⟩ +≡
paAllExp = 275;

1680. Subexpression object’s *FinishArgument* (§1552) is invoked, which pushes a term onto the *Term* stack. This will invoke the *AppendQua* (§1656) method and expect a closed parentheses afterwards (§1655).

Possible bug: what should happen when *fParenthCnt* is zero or negative?

```

⟨ Parse expressions (parser.pas) 1654 ⟩ +≡
procedure CompleteArgument(var fParenthCnt : integer);
  begin gSubexpPtr↑.FinishArgument;
  repeat AppendQua; CloseParenth(fParenthCnt);
  until CurWord.Kind ≠ sy_Qua; { ∧(CurWord.Kind ≠ sy_Exactly) }
end;

```

1681. Keep parsing “infix operators”. When the current token is an infix operator, this will consume the arguments to its right, then iterate. It’s also worth remembering that *gExpPtr* (§817) was a global variable declared back in `syntax.pas`, and the *CreateSubexpression* (§1638) mutates the *gSubexpPtr* variable. Now we see it in action.

This invokes the *ProcessLeftParenthesis* method for the *gSubexpPtr* (§817) global variable which we recall (§845) is an empty virtual method. So the Parser just “consumes” a left parentheses.

Note that the **case** expression considers the type of *TokenKind* (§851) of the current word. But it is not exhaustive.

There is a comment in Polish, “Chyba po prostu TermSubexpression”, which Google translated into English as “I guess it’s just Term Subexpression”. I swapped this in the code below.

```

⟨Parse expressions (parser.pas) 1654⟩ +≡
procedure AppendFunc(var fParenthCnt : integer);
begin while CurWord.Kind = InfixOperatorSymbol do
  begin gSubexpPtr↑.StartLongTerm; { (§1560) }
  repeat gSubexpPtr↑.ProcessFunctorSymbol; { (§1576) }
    ReadWord;
  case CurWord.Kind of
    sy_LeftParanthesis:
      begin { parenthesised term(s) }
        gSubexpPtr↑.ProcessLeftParenthesis; ReadWord; { consume the left paren }
        GetArguments(MaxVisArgNbr); { (§1705) }
        gSubexpPtr↑.ProcessRightParenthesis; Accept(sy_RightParanthesis, paRightParenthExp3);
          { consume matching right paren }
        end;
      Identifier, Numeral, LeftCircumfixSymbol, sy_It, sy_LeftCurlyBracket, sy_LeftSquareBracket, sy_The,
        sy_Dolar, StructureSymbol: { I guess it’s just Term Subexpression }
      begin gExpPtr↑.CreateSubexpression; { (§1638) }
        GetClosedSubterm; { (§1662) }
        gSubexpPtr↑.FinishArgument; { (§1552) }
        KillSubexpression; { (§811) }
      end;
    endcases;
    gSubexpPtr↑.FinishArgList; { (§1577) }
  until CurWord.Kind ≠ InfixOperatorSymbol;
  gSubexpPtr↑.FinishLongTerm; { (§1564) }
  CompleteArgument(fParenthCnt); { (§1680) }
end;
end;

```

1682. ⟨Error codes for parser 1642⟩ +≡
 paRightParenthExp3 = 370;

1683. Parse terms with infix operators. Note this appears to parse infix operators as left-associative (e.g., $x + y + z$ is parsed as $(x + y) + z$).

⟨ Parse expressions (`parser.pas`) 1654 ⟩ +≡

```

procedure ProcessArguments;
  var lParenthCnt: integer;
  begin OpenParenth(lParenthCnt);
  case CurWord.Kind of
    Identifier, Numeral, LeftCircumfixSymbol, sy_It, sy_LeftCurlyBracket, sy_LeftSquareBracket, sy_The,
      sy_Dolar, StructureSymbol:
      begin GetClosedSubterm; CompleteArgument(lParenthCnt); end;
    InfixOperatorSymbol: ;
  othercases begin gSubexpPtr↑.InsertIncorrTerm; gSubexpPtr↑.FinishArgument;
    WrongWord(paWrongTermBeg);
  end;
endcases;
  ⟨ Keep parsing as long as there is an infix operator to the right 1685 ⟩;
  ⟨ Check every remaining open (left) parentheses has a corresponding partner 1686 ⟩;
end;

```

1684. ⟨ Error codes for parser 1642 ⟩ +≡
 paWrongTermBeg = 397;

1685. ⟨ Keep parsing as long as there is an infix operator to the right 1685 ⟩ ≡

```

repeat AppendFunc(lParenthCnt);
  if CurWord.Kind = sy_Comma then
    begin ArgumentsTail(MaxVisArgNbr - 1);
    if (lParenthCnt > 0) ∧ (CurWord.Kind = sy_RightParanthesis) then
      begin dec(lParenthCnt); gSubexpPtr↑.ProcessRightParanthesis; ReadWord;
      end;
    end;
  until CurWord.Kind ≠ InfixOperatorSymbol

```

This code is used in section 1683.

1686. ⟨ Check every remaining open (left) parentheses has a corresponding partner 1686 ⟩ ≡

```

while lParenthCnt > 0 do
  begin gSubexpPtr↑.ProcessRightParanthesis; Accept(sy_RightParanthesis, paRightParenthExp1);
  dec(lParenthCnt);
  end

```

This code is used in section 1683.

1687. Term subexpressions. The Parser wants a term as a subexpression in a formula or attribute cluster or some similar situation. The term specifically is just a *component* of the expression. We should recall from Figure 8 (§1662) that this is a critical part of parsing terms.

```

⟨Parse term subexpressions (parser.pas) 1687⟩ ≡
procedure TermSubexpression;
  var lParenthCnt: integer;
  begin gExpPtr↑.CreateSubexpression; OpenParenth(lParenthCnt); { (§1655) }
  case CurWord.Kind of
    Identifier, Numeral, LeftCircumfixSymbol, sy_It, sy_LeftCurlyBracket, sy_LeftSquareBracket, sy_The,
      sy_Dolar, StructureSymbol:
      begin GetClosedSubterm; CompleteArgument(lParenthCnt); { (§1680) }
      end;
    InfixOperatorSymbol: { skip } ;
  othercases ⟨Raise error over invalid term subexpression 1688⟩;
  endcases;
  AppendFunc(lParenthCnt); { (§1681) }
  while lParenthCnt > 0 do ⟨Parse arguments to the right 1689⟩;
  gSubexpPtr↑.FinishTerm; KillSubexpression;
  end;

```

This code is used in section 1703.

```

1688. ⟨Raise error over invalid term subexpression 1688⟩ ≡
  begin gSubexpPtr↑.InsertIncorrTerm; gSubexpPtr↑.FinishArgument; WrongWord(paWrongTermBeg);
  end

```

This code is used in section 1687.

```

1689. ⟨Parse arguments to the right 1689⟩ ≡
  begin ArgumentsTail(MaxVisArgNbr - 1); dec(lParenthCnt); gSubexpPtr↑.ProcessRightParenthesis;
  Accept(sy_RightParanthesis, paRightParenthExp10);
  if CurWord.Kind ≠ InfixOperatorSymbol then MissingWord(paFuncExp3);
  AppendFunc(lParenthCnt);
  end

```

This code is used in section 1687.

```

1690. ⟨Error codes for parser 1642⟩ +≡
  paFuncExp3 = 302; paRightParenthExp10 = 370;

```

Subsection 24.1.2. Types and Attributes

1691. Types and attributes are closely related, when it comes to parsing Mizar. After all, we can add an adjective to a type and we expect it to be “a type”.

An adjective cluster is just one or more (possibly negated) attribute.

```

⟨Parse expressions (parser.pas) 1654⟩ +≡
  ⟨Process attributes (parser.pas) 1692⟩
procedure GetAdjectiveCluster;
  begin gSubexpPtr↑.StartAdjectiveCluster; ProcessAttributes; gSubexpPtr↑.FinishAdjectiveCluster;
  end;

```


1692. Parsing an attribute amounts to:

- (1) handling a leading “non”
- (2) handling attribute arguments (which always occurs *before* the attribute)
- (3) handling the attribute.

define *kind_is_radix_type*(#) \equiv (# \in [*sy_Set*, *ModeSymbol*, *StructureSymbol*])

define *ahead_is_attribute_argument* \equiv

(*CurWord.Kind* \in (*TermBegSys* – [*sy_LeftParanthesis*, *StructureSymbol*])) \vee
 ((*CurWord.Kind* = *sy_LeftParanthesis*) \wedge \neg (*kind_is_radix_type*(*AheadWord.Kind*))) \vee
 ((*CurWord.Kind* = *StructureSymbol*) \wedge (*AheadWord.Kind* = *sy_StructLeftBracket*))

\langle Process attributes (**parser.pas**) 1692 $\rangle \equiv$

procedure *ProcessAttributes*;

begin while (*CurWord.Kind* \in [*AttributeSymbol*, *sy_Non*]) \vee *ahead_is_attribute_argument* **do**

begin *gSubexpPtr*↑.*ProcessNon*;

if *CurWord.Kind* = *sy_Non* **then** *ReadWord*;

if *ahead_is_attribute_argument* **then**

begin *gSubexpPtr*↑.*StartAttributeArguments*; *ProcessArguments*;

gSubexpPtr↑.*CompleteAttributeArguments*;

end;

if *CurWord.Kind* = *AttributeSymbol* **then**

begin *gSubexpPtr*↑.*ProcessAttribute*; *ReadWord*; **end**

else begin *SynErr*(*CurPos*, *paAttrExp1*)

end;

end;

end;

This code is used in section 1691.

1693. \langle Error codes for parser 1642 $\rangle + \equiv$

paAttrExp1 = 306;

1694. Parsing a radix type. For Mizar, a Radix type is either a structure type or a mode (or it’s the “set” type).

There is a comment in Polish, “zawieszone na czas zmiany semantyki”, which is translated into English.

\langle Parse expressions (**parser.pas**) 1654 $\rangle + \equiv$

procedure *RadixTypeSubexpression*;

var *lSymbol*, *lParenthCnt*: *integer*;

begin *lParenthCnt* \leftarrow 0; \langle Parse optional left-paren 1700 \rangle ;

gSubexpPtr↑.*ProcessModeSymbol*; { (§1555) }

case *CurWord.Kind* **of**

sy_Set: **begin** *ReadWord*;

{ ? if Occurs(*syOf*) then TypeSubexpression suspended while semantics change }

end;

ModeSymbol: \langle Parse mode as radix type 1696 \rangle ;

StructureSymbol: \langle Parse structure as radix type 1698 \rangle ;

othercases begin *MissingWord*(*paWrongRadTypeBeg*); *gSubexpPtr*↑.*InsertIncorrType* **end**;

endcases;

\langle Close the parentheses 1701 \rangle ;

gSubexpPtr↑.*FinishType*;

end;

1695. \langle Error codes for parser 1642 $\rangle + \equiv$

paWrongRadTypeBeg = 398;

1696. $\langle \text{Parse mode as radix type } 1696 \rangle \equiv$
begin $lSymbol \leftarrow CurWord.Nr$; $ReadWord$;
if $CurWord.Kind = sy_Of$ **then**
 if $ModeMaxArgs.fList \uparrow [lSymbol] = 0$ **then** $WrongWord(paUnexpOf)$
 else begin $ReadWord$; $GetArguments(ModeMaxArgs.fList \uparrow [lSymbol])$ **end**;
end

This code is used in section 1694.

1697. $\langle \text{Error codes for parser } 1642 \rangle + \equiv$
 $paUnexpOf = 183$;

1698. $\langle \text{Parse structure as radix type } 1698 \rangle \equiv$
begin $lSymbol \leftarrow CurWord.Nr$; $ReadWord$;
if $CurWord.Kind = sy_Over$ **then**
 if $StructModeMaxArgs.fList \uparrow [lSymbol] = 0$ **then** $WrongWord(paUnexpOver)$
 else begin $ReadWord$; $GetArguments(StructModeMaxArgs.fList \uparrow [lSymbol])$ **end**;
end

This code is used in section 1694.

1699. $\langle \text{Error codes for parser } 1642 \rangle + \equiv$
 $paUnexpOver = 184$;

1700. $\langle \text{Parse optional left-paren } 1700 \rangle \equiv$
if $CurWord.Kind = sy_LeftParanthesis$ **then**
 begin $gSubexpPtr \uparrow .ProcessLeftParanthesis$; $ReadWord$; $inc(lParenthCnt)$;
 end

This code is used in section 1694.

1701. $\langle \text{Close the parentheses } 1701 \rangle \equiv$
if $lParenthCnt > 0$ **then**
 begin $gSubexpPtr \uparrow .ProcessRightParanthesis$; $Accept(sy_RightParanthesis, paRightParenthExp1)$;
 end

This code is used in section 1694.

1702. Type subexpressions. Now the Parser needs a type as a subexpression in a larger expression (e.g., the specification for a definition, or in a formula of the form “ $\langle Term \rangle$ is $\langle Type \rangle$ ”). We basically get the adjectives with $GetAdjectiveCluster$, then we get the radix type with $RadixTypeSubexpression$.

$\langle \text{Parse expressions (parser.pas) } 1654 \rangle + \equiv$

procedure $TypeSubexpression$;

begin $gExpPtr \uparrow .CreateSubexpression$; $gSubexpPtr \uparrow .StartType$; $gSubexpPtr \uparrow .StartAttributes$;
 $GetAdjectiveCluster$; $RadixTypeSubexpression$;
 $gSubexpPtr \uparrow .CompleteAttributes$; $gSubexpPtr \uparrow .CompleteType$;
 $KillSubexpression$;
 end;

1703. Aside: parsing term subexpressions. The code for parsing term subexpressions (§1687) appears here in the code for the Parser, but it felt out of place. I thought it best to place it at the end of the subsection on parsing Term expressions (as it is the pinnacle of Term parsing), rather than leave it here.

$\langle \text{Parse expressions (parser.pas) } 1654 \rangle + \equiv$

$\langle \text{Parse term subexpressions (parser.pas) } 1687 \rangle$

1704. This will parse *fArgsNbr* comma separated terms. It's used to parse the arguments "to the right" of a term, for parsing the contents of an enumerated set (e.g., $\{x, y, z, w\}$), among many other places.

We should recall that the *StartArgument* method is empty.

```

⟨ Parse expressions (parser.pas) 1654 ⟩ +≡
procedure ArgumentsTail(fArgsNbr : integer);
  begin while (fArgsNbr > 0) ∧ Occurs(sy_Comma) do
    begin gSubexpPtr↑.StartArgument; TermSubexpression; gSubexpPtr↑.FinishArgument;
      dec(fArgsNbr);
    end;
  end;

```

1705. Attributes, terms, predicates have terms as arguments. This relies upon the *FinishArguments* method (§1552).

```

⟨ Parse expressions (parser.pas) 1654 ⟩ +≡
procedure GetArguments(const fArgsNbr: integer);
  begin if fArgsNbr > 0 then
    begin TermSubexpression; gSubexpPtr↑.FinishArgument; ArgumentsTail(fArgsNbr − 1);
    end;
  end;

```

Subsection 24.1.3. Formulas

1706. Quantified variables looks like

$$\langle \textit{Variable} \rangle \{ \text{ " , " } \langle \textit{Variable} \rangle \} [(\text{ " be " | " being " }) \langle \textit{Type} \rangle]$$

The parsing routine follows the grammar fairly faithfully.

```

⟨ Parse expressions (parser.pas) 1654 ⟩ +≡
procedure QuantifiedVariables;
  begin repeat gSubexpPtr↑.StartQualifiedSegment; ReadWord;
    ⟨ Parse comma-separated variables for quantified variables 1707 ⟩;
    gSubexpPtr↑.StartQualifyingType;
    if Occurs(sy_Be) ∨ Occurs(sy_Being) then TypeSubexpression;
    gSubexpPtr↑.FinishQualifiedSegment;
  until CurWord.Kind ≠ sy_Comma;
  end;

```

1707. ⟨ Parse comma-separated variables for quantified variables 1707 ⟩ ≡
repeat *gSubexpPtr*↑.*ProcessVariable*; *Accept*(*Identifier*, *paIdentExp2*);
until ¬*Occurs*(*sy_Comma*)

This code is used in section 1706.

1708. ⟨ Error codes for parser 1642 ⟩ +≡
paIdentExp2 = 300;

1709. The existential formula looks like

$$\text{ex } \langle \text{Quantified-Variables} \rangle \text{ st } \langle \text{Formula} \rangle$$

The Parser implements it quite faithfully.

⟨ Parse expressions (parser.pas) 1654 ⟩ +≡

procedure *ExistentialFormula*;

begin *gSubexpPtr*↑.*StartExistential*; *QuantifiedVariables*;

gSubexpPtr↑.*FinishQuantified*; *Accept*(*sy_St*, *paStExp*); *FormulaSubexpression*;

gSubexpPtr↑.*FinishExistential*;

end;

1710. ⟨ Error codes for parser 1642 ⟩ +≡

paStExp = 387;

1711. Universally quantified formulas are tricky because both

$$\text{for } \langle \text{Quantified-Variables} \rangle \text{ holds } \langle \text{Formula} \rangle$$

and

$$\text{for } \langle \text{Quantified-Variables} \rangle \text{ st } \langle \text{Formula} \rangle \text{ holds } \langle \text{Formula} \rangle$$

are acceptable. Furthermore, we may include multiple “for $\langle \text{Quantified-Variables} \rangle$ ” (possibly with “st $\langle \text{Formula} \rangle$ ” restrictions) before arriving at the single “holds $\langle \text{Formula} \rangle$ ”. The trick is to parse this as

$$\text{for } \langle \text{Quantified-Variables} \rangle [\text{st } \langle \text{Formula} \rangle] [\text{holds}] \langle \text{Formula} \rangle$$

so the recursive call to parse the final formula enables us to parse another quantified formula.

⟨ Parse expressions (parser.pas) 1654 ⟩ +≡

procedure *UniversalFormula*;

begin *gSubexpPtr*↑.*StartUniversal*; *QuantifiedVariables*; *gSubexpPtr*↑.*FinishQuantified*;

if *CurWord.Kind* = *sy_St* **then**

begin *gSubexpPtr*↑.*StartRestriction*; *ReadWord*; *FormulaSubexpression*;

gSubexpPtr↑.*FinishRestriction*;

end;

case *CurWord.Kind* **of**

sy_Holds: **begin** *gSubexpPtr*↑.*ProcessHolds*; *ReadWord* **end**;

sy_For, *sy_Ex*: ; { fallthrough }

othercases begin *gSubexpPtr*↑.*InsertIncorrFormula*; *MissingWord*(*paWrongScopeBeg*)

end;

endcases;

FormulaSubexpression; *gSubexpPtr*↑.*FinishUniversal*;

end;

1712. ⟨ Error codes for parser 1642 ⟩ +≡

paWrongScopeBeg = 340;

1713. The Parser’s current token is either “=” or a predicate symbol. Then we should parse “the right-hand side” of the equation (or formula). The current token’s Symbol number is passed as the argument to this procedure.

It’s worth recalling the definition of *TermBegSys* (§1654) which is all the token kinds for starting a term. If the next token is a term, then *GetArguments* is invoked to parse them.

⟨Parse expressions (parser.pas) 1654⟩ +≡

procedure *ConditionalTail*; *forward*;

procedure *CompleteRightSideOfThePredicativeFormula*(*aPredSymbol* : integer);

begin *gSubexpPtr*↑.*ProcessRightSideOfPredicateSymbol*; *ReadWord*;

if *CurWord.Kind* ∈ *TermBegSys* **then** *GetArguments*(*PredMaxArgs.fList*↑[*aPredSymbol*]);

gSubexpPtr↑.*FinishRightSideOfPredicativeFormula*;

end;

1714. Recall a “multi-predicative formula” is something of the form $a \leq x \leq b$. More generally, we could imagine the grammar for such a formula resembles:

$$\langle \text{Formula} \rangle \{ \langle \text{Multi-Predicate} \rangle \langle \text{Term-List} \rangle \}$$

The Parser’s current token is *⟨Multi-Predicate⟩*, and we want to keep parsing until the entire multi-predicative formula has been parsed.

We should mention (because I have not seen it discussed anywhere) Mizar allows “does not” and “do not” in formulas (for example, “Y does not overlap X ∧ Z”), but Mizar **does not** support “does” (or “do”) without the “not”. A 401 error would be raised.

Grammatically, this is known as “do-support”, and Mizar uses it for negating predicates. The verb following the “do” is a “bare infinitive” (which is why Mizar allows an “infinitive” for predicates). This makes sense when the predicate uses a “finite verb”. For “non-finite verb forms”, it is idiomatic English to just negate the verb (as in “Not knowing what that means, I just smile and nod” and “It would be a crime not to learn grammar”).

⟨Parse expressions (parser.pas) 1654⟩ +≡

procedure *CompleteMultiPredicativeFormula*;

begin *gSubexpPtr*↑.*StartMultiPredicativeFormula*;

repeat case *CurWord.Kind* **of**

sy_Equal, *PredicateSymbol*: *CompleteRightSideOfThePredicativeFormula*(*CurWord.Nr*);

sy_Does, *sy_Do*: ⟨Parse multi-predicate with “does” or “do” in copula 1715⟩;

endcases;

until ¬(*CurWord.Kind* ∈ [*sy_Equal*, *PredicateSymbol*, *sy_Does*, *sy_Do*]);

gSubexpPtr↑.*FinishMultiPredicativeFormula*;

end;

1715. ⟨Parse multi-predicate with “does” or “do” in copula 1715⟩ ≡

begin ⟨Consume “does not” or “do not”, raise error otherwise 1716⟩;

if *CurWord.Kind* ∈ [*PredicateSymbol*, *sy_Equal*] **then**

begin *CompleteRightSideOfThePredicativeFormula*(*CurWord.Nr*); *gSubexpPtr*↑.*ProcessNegative*; **end**

else begin *gSubExpPtr*↑.*InsertIncorrFormula*; *SynErr*(*CurPos*, *paInfinitiveExp*)

end;

end

This code is used in section 1714.

1716. ⟨Consume “does not” or “do not”, raise error otherwise 1716⟩ ≡

gSubexpPtr↑.*ProcessDoesNot*; *ReadWord*; *Accept*(*sy_Not*, *paNotExpected*)

This code is used in section 1715.

1717. $\langle \text{Error codes for parser 1642} \rangle + \equiv$
 $paNotExpected = 401; paInfinitiveExp = 402;$

1718. The Parser is trying to parse a predicate and has just parsed a comma-separated list of terms. Now, the Parser's is either (1) looking at a predicate or equality, or (2) has matched “does not” or “do not” and is now looking at a predicate or equality. In both cases, the Parser tries to complete the formula with the *CompletePredicativeFormula* procedure.

$\langle \text{Parse expressions (parser.pas) 1654} \rangle + \equiv$
procedure *CompletePredicativeFormula*(*aPredSymbol* : integer);
 begin *gSubexpPtr*↑.*ProcessPredicateSymbol*; { (§1607) }
 ReadWord;
 if *CurWord.Kind* ∈ *TermBegSys* **then** *GetArguments*(*PredMaxArgs.fList*↑[*aPredSymbol*]);
 gSubexpPtr↑.*FinishPredicativeFormula*;
 end;

1719.

$\langle \text{Parse expressions (parser.pas) 1654} \rangle + \equiv$
procedure *CompleteAtomicFormula*(**var** *aParenthCnt* : integer);
 var *lPredSymbol*: integer;
 label *Predicate*; { not actually used }
 begin $\langle \text{Parse left arguments in a formula 1721} \rangle$;
 case *CurWord.Kind* **of**
 sy_Equal, *PredicateSymbol*: $\langle \text{Parse equation or (possibly infix) predicate 1723} \rangle$;
 sy_Does, *sy_Do*: $\langle \text{Parse formula with “does not” or “do not” 1724} \rangle$;
 sy_Is: $\langle \text{Parse formula with “is not” or “is not” 1725} \rangle$;
 othercases begin *gSubexpPtr*↑.*ProcessAtomicFormula*; *MissingWord*(*paWrongPredSymbol*);
 gSubexpPtr↑.*InsertIncorrBasic*;
 end;
 endcases;
 end;

1720. $\langle \text{Error codes for parser 1642} \rangle + \equiv$
 $paWrongPredSymbol = 321;$

1721. $\langle \text{Parse left arguments in a formula 1721} \rangle \equiv$
 repeat *AppendFunc*(*aParenthCnt*);
 if *CurWord.Kind* = *sy_Comma* **then**
 begin *ArgumentsTail*(*MaxVisArgNbr* − 1);
 if (*aParenthCnt* > 0) ∧ (*CurWord.Kind* = *sy_RightParanthesis*) **then**
 begin *dec*(*aParenthCnt*); *gSubexpPtr*↑.*ProcessRightParenthesis*; *ReadWord*;
 if *CurWord.Kind* ≠ *InfixOperatorSymbol* **then** *MissingWord*(*paFuncExp1*);
 end;
 end;
 until *CurWord.Kind* ≠ *InfixOperatorSymbol*

This code is used in section 1719.

1722. $\langle \text{Error codes for parser 1642} \rangle + \equiv$
 $paFuncExp1 = 302;$

1723. \langle Parse equation or (possibly infix) predicate 1723 $\rangle \equiv$
begin *CompletePredicativeFormula*(*CurWord.Nr*);
if *CurWord.Kind* \in [*sy_Equal*, *PredicateSymbol*, *sy_Does*, *sy_Do*] **then** *CompleteMultiPredicativeFormula*
end

This code is used in section 1719.

1724. \langle Parse formula with “does not” or “do not” 1724 $\rangle \equiv$
begin *gSubexpPtr* \uparrow .*ProcessDoesNot*; *ReadWord*; *Accept*(*sy_Not*, *paNotExpected*);
if *CurWord.Kind* \in [*PredicateSymbol*, *sy_Equal*] **then**
begin *CompletePredicativeFormula*(*CurWord.Nr*); *gSubexpPtr* \uparrow .*ProcessNegative*;
if *CurWord.Kind* \in [*sy_Equal*, *PredicateSymbol*, *sy_Does*, *sy_Do*] **then**
CompleteMultiPredicativeFormula
end
else begin *gSubExpPtr* \uparrow .*InsertIncorrFormula*; *SynErr*(*CurPos*, *paInfinitiveExp*)
end;
end

This code is used in section 1719.

1725. \langle Parse formula with “is not” or “is not” 1725 $\rangle \equiv$
begin *gSubexpPtr* \uparrow .*ProcessAtomicFormula*; *ReadWord*;
if (*CurWord.Kind* = *sy_Not*) \wedge (*AheadWord.Kind* \in *TermBegSys* + [*ModeSymbol*, *StructureSymbol*,
sy_Set, *AttributeSymbol*, *sy_Non*]) \vee (*CurWord.Kind* \in *TermBegSys* + [*ModeSymbol*,
StructureSymbol, *sy_Set*, *AttributeSymbol*, *sy_Non*]) **then**
begin *gSubexpPtr* \uparrow .*StartType*; *gSubexpPtr* \uparrow .*StartAttributes*;
if *CurWord.Kind* = *sy_Not* **then**
begin *gSubexpPtr* \uparrow .*ProcessNegation*; *ReadWord*; **end**;
GetAdjectiveCluster;
case *CurWord.Kind* **of**
sy_LeftParanthesis, *ModeSymbol*, *StructureSymbol*, *sy_Set*: **begin** *RadixTypeSubexpression*;
gSubexpPtr \uparrow .*CompleteAttributes*; *gSubexpPtr* \uparrow .*CompleteType*;
gSubexpPtr \uparrow .*FinishQualifyingFormula*;
end;
othercases begin *gSubexpPtr* \uparrow .*CompleteAttributes*; *gSubexpPtr* \uparrow .*FinishAttributiveFormula*; **end**;
endcases;
end
else begin *gSubExpPtr* \uparrow .*InsertIncorrFormula*; *WrongWord*(*paTypeOrAttrExp*);
end;
end

This code is used in section 1719.

1726. \langle Error codes for parser 1642 $\rangle + \equiv$
paTypeOrAttrExp = 309;

1727. There is a comment in Polish, a single word (“Kolejność”) which translates into English as “Order”.

define *starts_with_term_token* \equiv *Numeral*, *LeftCircumfixSymbol*, *sy_It*, *sy_LeftCurlyBracket*,
sy_LeftSquareBracket, *sy_The*, *sy_Dolar*, *StructureSymbol*

\langle Parse expressions (*parser.pas*) 1654 $\rangle + \equiv$

procedure *ViableFormula*;

var *lParenthCnt*: *integer*;

label *NotPrivate*;

begin *gSubexpPtr* \uparrow .*CreateSubexpression*; *OpenParenth*(*lParenthCnt*);

case *CurWord.Kind* **of**

sy_For: *UniversalFormula*;

sy_Ex: *ExistentialFormula*; { !!!!!!!!!!!!!!! Order }

sy_Contradiction: **begin** *gSubexpPtr* \uparrow .*ProcessContradiction*; *ReadWord*; **end**;

sy_Thesis: **begin** *gSubexpPtr* \uparrow .*ProcessThesis*; *ReadWord*; **end**;

sy_Not: **begin** *gSubexpPtr* \uparrow .*ProcessNot*; *ReadWord*; *ViableFormula*; *KillSubexpression*;
gSubexpPtr \uparrow .*ProcessNegative*;

end;

Identifier: **if** *AheadWord.Kind* = *sy_LeftSquareBracket* **then** \langle Parse private formula 1729 \rangle

else goto *NotPrivate*;

starts_with_term_token:

NotPrivate: **begin** *gSubexpPtr* \uparrow .*StartAtomicFormula*; { ??? TermSubexpression }

GetClosedSubterm; *CompleteArgument*(*lParenthCnt*); *CompleteAtomicFormula*(*lParenthCnt*);

end;

InfixOperatorSymbol, *PredicateSymbol*, *sy_Does*, *sy_Do*, *sy_Equal*: **begin** *gSubexpPtr* \uparrow .*StartAtomicFormula*;
CompleteAtomicFormula(*lParenthCnt*);

end;

othercases begin *gSubexpPtr* \uparrow .*InsertIncorrFormula*; *WrongWord*(*paWrongFormulaBeg*)

end;

endcases; \langle Close parentheses for formula 1731 \rangle ;

end;

1728. \langle Error codes for parser 1642 $\rangle + \equiv$

paWrongFormulaBeg = 396;

1729. \langle Parse private formula 1729 $\rangle \equiv$

begin *gSubexpPtr* \uparrow .*StartPrivateFormula*; *ReadWord*; *ReadWord*;

if *CurWord.Kind* \neq *sy_RightSquareBracket* **then** *GetArguments*(*MaxVisArgNbr*);

Accept(*sy_RightSquareBracket*, *paRightSquareExp2*); *gSubexpPtr* \uparrow .*FinishPrivateFormula*;

end

This code is used in section 1727.

1730. \langle Error codes for parser 1642 $\rangle + \equiv$

paRightSquareExp2 = 371;

1731. \langle Close parentheses for formula 1731 $\rangle \equiv$

while *lParenthCnt* > 0 **do**

begin *ConditionalTail*; *gSubexpPtr* \uparrow .*ProcessRightParenthesis*;

Accept(*sy_RightParanthesis*, *paRightParenthExp4*); *dec*(*lParenthCnt*); *CloseParenth*(*lParenthCnt*);

end

This code is used in section 1727.

1732. \langle Error codes for parser 1642 $\rangle + \equiv$

paRightParenthExp4 = 370;

1733. Precedence for logical connectives. We will now “hardcode” the precedence for logical connectives into the Mizar Parser. Negations (“**not**”) binds tighter than conjunction (“**&**”), which binds tighter than disjunction (“**or**”), which binds tighter than implication (“**implies**” and “**iff**”).

At this point, for the formula “**A & B**”, the Parser has parsed a formula (“**A**”), and we want to parse possible conjunctions. The current token will be “**&**”. If not, then the Parser does nothing: it’s “done”.

We will parse conjunction as left associative — so “**A & B & C**” parses as “(**A & B**) & **C**”.

⟨Parse expressions (parser.pas) 1654⟩ +≡

procedure *ConjunctiveTail*;

```

begin while (CurWord.Kind = sy_Ampersand)  $\wedge$  (AheadWord.Kind  $\neq$  sy_Ellipsis) do
  begin gSubexpPtr↑.ProcessBinaryConnective; ReadWord; ViableFormula; KillSubexpression;
  gSubexpPtr↑.FinishBinaryFormula;
  end;
end;

```

1734. Mizar parses flexary conjunctions (“ $\Phi[0] \& \dots \& \Phi[n]$ ”) as weaker than “ordinary conjunction”. For example “ $\Psi \& \Phi[0] \& \dots \& \Phi[n]$ ” parses as “($\Psi \& \Phi[0]$) & $\dots \& \Phi[n]$ ”.

If the user accidentally forgets the ampersand after the ellipses (“ $\Phi[0] \& \dots \Phi[n]$ ”), a 402 error will be raised.

⟨Parse expressions (parser.pas) 1654⟩ +≡

procedure *FlexConjunctiveTail*;

```

begin ConjunctiveTail;
if CurWord.Kind = sy_Ampersand then
  begin Assert(AheadWord.Kind = sy_Ellipsis); ReadWord; ReadWord; Accept(sy_Ampersand, 402);
  gSubexpPtr↑.ProcessFlexConjunction; ViableFormula; ConjunctiveTail; KillSubexpression;
  gSubexpPtr↑.FinishFlexConjunction;
  end;
end;

```

1735. Disjunction binds weaker than flexary conjunction (which binds weaker than ordinary conjunction).

As for ordinary conjunction, Mizar parses multiple disjunctions as left associative. So “**A or B or C**” parses as “(**A or B**) or **C**”.

⟨Parse expressions (parser.pas) 1654⟩ +≡

procedure *DisjunctiveTail*;

```

begin FlexConjunctiveTail;
while (CurWord.Kind = sy_Or)  $\wedge$  (AheadWord.Kind  $\neq$  sy_Ellipsis) do
  begin gSubexpPtr↑.ProcessBinaryConnective; ReadWord; ViableFormula; FlexConjunctiveTail;
  KillSubexpression; gSubexpPtr↑.FinishBinaryFormula;
  end;
end;

```

1736. Parsing a disjunction will have the Parser’s current token be “or” only if the next token is an ellipsis (“...”), which is precisely the signal for a flexary disjunction. When the current token is not an “or”, then the Parser does nothing (its work is done).

When the user forgets an “or” after ellipsis (e.g., writing “A or ... C”), a 401 error will be raised.

⟨Parse expressions (parser.pas) 1654⟩ +≡

```

procedure FlexDisjunctiveTail;
  begin DisjunctiveTail;
  if CurWord.Kind = sy_Or then
    begin Assert(AheadWord.Kind = sy_Ellipsis); ReadWord; ReadWord; Accept(sy_Or, 401);
    gSubexpPtr↑.ProcessFlexDisjunction; ViableFormula; DisjunctiveTail; KillSubexpression;
    gSubexpPtr↑.FinishFlexDisjunction;
    end;
  end;

```

1737. Mizar parses “implies” and “iff” with lower precedence than “or”, matching common Mathematical practice. Working Mathematicians read “A or B implies C” as “(A or B) implies C”. We impose this precedence with the *FlexDisjunctiveTail* parsing the remaining disjunctions before checking for “iff” or “implies”.

Mizar accepts one “topmost” implication connective. So “A implies B implies C” would be illegal (a 336 error would be raised). You would have to insert parentheses to make this parseable by Mizar (i.e., “A implies (B implies C)”). This makes sense for implication, but there is a compelling argument that “A iff B iff C” could be parsed as “(A iff B) & (B iff C)” — that latter formula *could* be parsed properly by Mizar.

⟨Parse expressions (parser.pas) 1654⟩ +≡

```

procedure ConditionalTail;
  begin FlexDisjunctiveTail;
  case CurWord.Kind of
    sy_Implies, sy_Iff: begin gSubexpPtr↑.ProcessBinaryConnective; ReadWord; ViableFormula;
    FlexDisjunctiveTail; KillSubexpression; gSubexpPtr↑.FinishBinaryFormula;
    case CurWord.Kind of
      sy_Implies, sy_Iff: WrongWord(paUnexpConnective);
    endcases;
    end;
  endcases;
  end;

```

1738. ⟨Error codes for parser 1642⟩ +≡

paUnexpConnective = 336;

1739. Formula subexpressions. When the Parser needs a formula as a subexpression for a larger expression — like when it parses a Fraenkel term (an expression), the Parser will need to parse

$$\{\langle \text{Term} \rangle \langle \text{Qualifying-Segment} \rangle : \langle \text{Formula-Subexpression} \rangle\}$$

This will also serve as the “workhorse” for parsing a formula expression.

⟨Parse expressions (parser.pas) 1654⟩ +≡

```

procedure FormulaSubexpression;
  begin ViableFormula; ConditionalTail; KillSubexpression;
  end;

```

Section 24.2. COMMUNICATION WITH ITEMS

1740. When the Parser constructs the AST for a term, the workflow is as follows:

- (1) Allocate a new *extExpression* object, and update *gExprPtr* to point at it.
- (2) Using the *gExprPtr* to allocate a new *extSubexp* object, and update the *gSubexpPtr* to point at it.
- (3) The Parser will invoke methods for the *gSubexpPtr*'s reference to build the AST. The result will be stored in a state variable (like *gLastTerm* or *gLastType*).
- (4) There will be residual objects allocated, stored in the fields of *gSubexpPtr* and *gExpPtr*. We need to clean those up, freeing them, by invoking *KillExpression* and *KillSubexpression*.

So each of these methods have the following template: allocate a new expression object, update the *gExpPtr* to point to it, parse something, then free the *gExpPtr* using the *KillExpression* procedure.

⟨ Communicate with items (`parser.pas`) 1740 ⟩ \equiv
 { *Communication with items* }

procedure *TermExpression*;

begin *gItemPtr*↑.*CreateExpression*(*exTerm*); *TermSubexpression*; *KillExpression*;
end;

procedure *TypeExpression*;

begin *gItemPtr*↑.*CreateExpression*(*exType*); *TypeSubexpression*; *KillExpression*;
end;

procedure *FormulaExpression*;

begin *gItemPtr*↑.*CreateExpression*(*exFormula*); *FormulaSubexpression*; *KillExpression*;
end;

This code is used in section 1640.

Section 24.3. MISCELLANEOUS

1741. Parsing a label. When the Parser is looking at a label, the *gItemPtr* will construct the label. The Parser still needs to move past the “*<identifier>:*” two tokens.

```

< Process miscellany (parser.pas) 1741 > ≡
  { Miscellaneous }
procedure ProcessLab;
begin gItemPtr↑.ProcessLabel; { (§1512) }
if (CurWord.Kind = Identifier) ∧ (AheadWord.Kind = sy_Colon) then
  begin ReadWord; ReadWord end;
end;

```

See also sections 1742, 1743, 1744, 1745, 1746, 1749, 1752, 1754, 1756, and 1757.

This code is used in section 1640.

1742. Telling the *gItemPtr* state variable we are about to parse a sentence just invokes the *StartSentence* (§1427) method, then the Parser parses the formula, and the *gItemPtr* “finishes” the sentence (which is an empty method).

```

< Process miscellany (parser.pas) 1741 > +≡
procedure ProcessSentence;
begin gItemPtr↑.StartSentence; FormulaExpression; gItemPtr↑.FinishSentence;
end;

```

1743. When the Parser expected a sentence but something unexpected happened, specifically an unexpected statement has cross the Parser’s path. When that statement has encountered an unjustified “per cases”. We just create a new formula expression, and specifically an “incorrect formula”.

```

< Process miscellany (parser.pas) 1741 > +≡
procedure InCorrSentence;
begin gItemPtr↑.StartSentence; gItemPtr↑.CreateExpression(exFormula);
gExpPtr↑.CreateSubexpression; gSubexpPtr↑.InsertIncorrFormula; KillSubexpression; KillExpression;
gItemPtr↑.FinishSentence;
end;

```

1744. The Parser attempts to recover (or at least, report) an unexpected item when expecting a statement. Specifically, a “per cases” appears when it should not.

```

< Process miscellany (parser.pas) 1741 > +≡
procedure InCorrStatement;
begin gItemPtr↑.ProcessLabel; gItemPtr↑.StartRegularStatement; InCorrSentence;
end;

```

1745. The Parser is looking at either

let $\langle Variables \rangle$ **being** $\langle Type \rangle$ **such that** $\langle Hypotheses \rangle$

or

assume that $\langle Hypotheses \rangle$

Specifically, the Parser has arrived at the “ $\langle Hypotheses \rangle$ ” bit and needs to parse it. The $\langle Hypotheses \rangle$ generically looks like

$\langle Hypotheses \rangle = [\langle label \rangle] \langle Formula \rangle \{ \text{and } \langle Hypotheses \rangle \}$

That is to say, a bunch of (possibly labeled) formulas joined together by “and” keywords.

\langle Process miscellany (parser.pas) 1741 $\rangle + \equiv$

procedure *ProcessHypotheses*;

begin repeat *ProcessLab*; *ProcessSentence*; *gItemPtr*↑.*FinishHypothesis*;

until $\neg \text{Occurs}(\text{sy_And})$

end;

1746. An assumption is either collective (using hypotheses) or singular (a single, possibly labeled, formula).

\langle Process miscellany (parser.pas) 1741 $\rangle + \equiv$

procedure *Assumption*;

begin if *CurWord.Kind* = *sy_That* **then** \langle Parse collective assumption 1747 \rangle

else \langle Parse single assumption 1748 \rangle ;

gItemPtr↑.*FinishAssumption*;

end;

1747. \langle Parse collective assumption 1747 $\rangle \equiv$

begin *gItemPtr*↑.*StartCollectiveAssumption*; { (§1443) } *ReadWord*; *ProcessHypotheses*

end

This code is used in section 1746.

1748. \langle Parse single assumption 1748 $\rangle \equiv$

begin *ProcessLab*; *ProcessSentence*; *gItemPtr*↑.*FinishHypothesis*; { (§1507) }

end

This code is used in section 1746.

1749. Fixed variables. Existential elimination in Mizar looks like

consider $\langle Fixed\text{-}variables \rangle$ **such that** $\langle Formula \rangle$

The $\langle Fixed\text{-}variables \rangle$ is just a comma-separated list of segments.

\langle Process miscellany (parser.pas) 1741 $\rangle + \equiv$

procedure *FixedVariables*;

begin *gItemPtr*↑.*StartFixedVariables*;

repeat \langle Parse segment of fixed variables 1750 \rangle ;

until $\neg \text{Occurs}(\text{sy_Comma})$;

gItemPtr↑.*FinishFixedVariables*;

end;

1750. And a “fixed” segment is just a comma-separated list of variables. This is either implicitly qualified (i.e., they are all reserved variables) or explicitly qualified (i.e., there is a “being” or “be”, followed by a type). A 300 error will be raised if the comma-separated list of variables encounters something other than an identifier.

```

⟨ Parse segment of fixed variables 1750 ⟩ ≡
  gItemPtr↑.StartFixedSegment;
  repeat gItemPtr↑.ProcessFixedVariable; Accept(Identifier, paIdentExp4);
  until ¬Occurs(sy_Comma);
  gItemPtr↑.ProcessBeing; { parse the type qualification }
  if Occurs(sy_Be) ∨ Occurs(sy_Being) then TypeExpression;
  gItemPtr↑.FinishFixedSegment

```

This code is used in section 1749.

1751. ⟨ Error codes for parser 1642 ⟩ +≡
 paIdentExp4 = 300;

1752. Parsing ‘consider’ statements. The Parser is trying to parse a “consider” statement or a “given” statement. The Parser will try to parse

$$\langle \textit{Fixed-Variables} \rangle \text{ such that } \langle \textit{Formula} \rangle \{ \text{ and } \langle \textit{Formula} \rangle \}$$

If the user forgot the “such” keyword, a 403 error will be raised. If the user forgot the “that” keyword, a 350 error will be raised.

```

⟨ Process miscellany (parser.pas) 1741 ⟩ +≡
procedure ProcessChoice;
  begin FixedVariables; Accept(sy_Such, paSuchExp); Accept(sy_That, paThatExp2);
  repeat gItemPtr↑.StartCondition; ProcessLab; ProcessSentence; gItemPtr↑.FinishCondition;
  until ¬Occurs(sy_And);
  gItemPtr↑.FinishChoice;
end;

```

1753. ⟨ Error codes for parser 1642 ⟩ +≡
 paThatExp2 = 350; paSuchExp = 403;

1754. Parsing ‘let’ statements. The Parser is looking at the “let” token. There are two possible statements

$$\text{let } \langle \textit{Fixed-variables} \rangle;$$

or possibly with assumptions

$$\text{let } \langle \textit{Fixed-variables} \rangle \text{ such that } \langle \textit{Hypotheses} \rangle;$$

If the user forgot “that” but included a “such” after the fixed-variables, a 350 error is raised.

```

⟨ Process miscellany (parser.pas) 1741 ⟩ +≡
procedure Generalization;
  begin ReadWord; FixedVariables;
  if Occurs(sy_Such) then
    begin gItemPtr↑.StartAssumption; Accept(sy_That, paThatExp1); ProcessHypotheses;
    gItemPtr↑.FinishAssumption;
    end;
  end;

```

1755. \langle Error codes for parser 1642 $\rangle + \equiv$
 $paThatExp1 = 350;$

1756. Parsing ‘given’ statements. The Parser is looking at the “given” token currently. This is the same as “assume ex \vec{x} st $\Phi[\vec{x}]$; then consider \vec{x} such that $\Phi[\vec{x}]$;”.

\langle Process miscellany (parser.pas) 1741 $\rangle + \equiv$

procedure *ExistentialAssumption*;

begin $gBlockPtr \uparrow.CreateItem(itExistentialAssumption); ReadWord; ProcessChoice;$

end;

1757. The Parser is looking at either “canceled;” or “canceled $\langle number \rangle$;”.

\langle Process miscellany (parser.pas) 1741 $\rangle + \equiv$

procedure *Canceled*;

begin $gBlockPtr \uparrow.CreateItem(itCanceled); ReadWord;$

if $CurWord.Kind = Numeral$ **then** $ReadWord;$

$gItemPtr \uparrow.FinishTheorem;$

end;

Section 24.4. SIMPLE JUSTIFICATIONS

1758. The Parser is looking at “by” and now needs to parse the list of references. If the user tries to use something other than a label’s identifier as a reference, then a 308 error will be raised.

```

⟨ Parse simple justifications (parser.pas) 1758 ⟩ ≡
  { Simple Justifications }
procedure GetReferences;
begin gItemPtr↑.StartReferences;
repeat ReadWord; ⟨ Parse single reference 1759 ⟩;
until CurWord.Kind ≠ sy_Comma;
  gItemPtr↑.FinishReferences;
end;

```

See also sections 1763 and 1767.

This code is used in section 1640.

```

1759. ⟨ Parse single reference 1759 ⟩ ≡
  case CurWord.Kind of
    MMLIdentifier: ⟨ Parse library references 1761 ⟩;
    Identifier: begin gItemPtr↑.ProcessPrivateReference; ReadWord end;
    othercases WrongWord(paWrongReferenceBeg);
  endcases

```

This code is used in section 1758.

```

1760. ⟨ Error codes for parser 1642 ⟩ +≡
  paWrongReferenceBeg = 308;

```

1761. Mizar supports multiple references from the same article to “piggyback” off the same article “anchor”. For example, “GROUP_1:13,def 3,17” refers to theorems 13 and 17 and definition 3 from the MML Article GROUP_1.

If the user forgot to include the theorem or definition number — so they just wrote “⟨Article⟩” instead of “⟨Article⟩:⟨Number⟩” or “⟨Article⟩:def ⟨Number⟩” — then Mizar flags this with a 384 error.

```

define no_longer_referencing_article ≡ (CurWord.Kind ≠ sy_Comma) ∨
  (AheadWord.Kind = Identifier) ∨ (AheadWord.Kind = MMLIdentifier)

⟨ Parse library references 1761 ⟩ ≡
  begin gItemPtr↑.StartLibraryReferences; ReadWord;
  if CurWord.Kind = sy_Colon then
    repeat ReadWord; gItemPtr↑.ProcessDef;
      if CurWord.Kind = ReferenceSort then
        begin if CurWord.Nr ≠ ord(syDef) then ErrImm(paDefExp);
          ReadWord;
        end;
        gItemPtr↑.ProcessTheoremNumber; Accept(Numeral, paNumExp);
      until no_longer_referencing_article
    else MissingWord(paColonExp4);
  end
  gItemPtr↑.FinishTheLibraryReferences;
end

```

This code is used in section 1759.

```

1762. ⟨ Error codes for parser 1642 ⟩ +≡
  paNumExp = 307; paDefExp = 312; paColonExp4 = 384;

```


1763. The Parser is currently looking at “**from**”, which means a reference to a scheme identifier will be given next (possibly followed with a comma-separated list of references in parentheses).

If the user tries to give something else (instead of an identifier of a scheme), then a 308 error will be raised. Also, if the user forgot the closing parentheses around the references for the scheme (e.g., “**from** **MyScheme**(**A1**,**A2**)”), then 370 error will be raised.

```

⟨ Parse simple justifications (parser.pas) 1758 ⟩ +≡
procedure GetSchemeReference;
  begin gItemPtr↑.StartSchemeReference; ReadWord;
  case CurWord.Kind of
    MMLIdentifier: ⟨ Parse reference to scheme from MML 1765 ⟩;
    Identifier: begin gItemPtr↑.ProcessSchemeReference; ReadWord end;
    othercases WrongWord(paWrongReferenceBeg);
  endcases;
  if CurWord.Kind = sy_LeftParanthesis then
    begin GetReferences; Accept(sy_RightParanthesis, paRightParenthExp7)
    end;
  gItemPtr↑.FinishSchemeReference;
end;

```

1764. ⟨ Error codes for parser 1642 ⟩ +≡
paRightParenthExp7 = 370;

1765. Mizar expects scheme references to the MML to be of the form “**from** ⟨*Article*⟩:**sch** ⟨*Number*⟩”. If the user forgot the “**sch**” (after the colon), a 313 error will be raised. If the user supplies something other than a *number* for the scheme, a 307 error will be raised.

```

⟨ Parse reference to scheme from MML 1765 ⟩ ≡
  begin gItemPtr↑.StartSchemeLibraryReference; ReadWord;
  if CurWord.Kind = sy_Colon then
    begin ReadWord; gItemPtr↑.ProcessSch;
    if CurWord.Kind = ReferenceSort then
      begin if CurWord.Nr ≠ ord(sy_Sch) then ErrImm(paSchExp);
      ReadWord;
      end
    else ErrImm(paSchExp);
    gItemPtr↑.ProcessSchemeNumber; Accept(Numeral, paNumExp);
    end
  else MissingWord(paColonExp4);
  gItemPtr↑.FinishSchLibraryReferences;
end

```

This code is used in section 1763.

1766. ⟨ Error codes for parser 1642 ⟩ +≡
paSchExp = 313;

1767. The Parser expects a simple justification — i.e., either a “**by**” followed by some references, or “**from**” followed by a scheme reference. For some “obvious” inferences, no justification may be needed.

⟨ Parse simple justifications (**parser.pas**) 1758 ⟩ +≡

```
procedure SimpleJustification;
  begin gItemPtr↑.StartSimpleJustification;
  case CurWord.Kind of
    sy_By: GetReferences;
    sy_Semicolon, sy_DotEquals: ;
    sy_From: GetSchemeReference;
  othercases WrongWord(paWrongJustificationBeg);
  endcases; gItemPtr↑.FinishSimpleJustification;
end;
```

1768. ⟨ Error codes for parser 1642 ⟩ +≡

paWrongJustificationBeg = 395;

Section 24.5. STATEMENTS AND REASONINGS

1769. Pragmas have been enabled which tells Mizar to skip the proof. The Parser simply stores a counter (initialized to 1), and increments it every time a “**proof**” token has been encountered, but decrements it every time an “**end**” token has been encountered. When the counter has reached zero, the proof has ended, and the Parser can stop skipping things.

There are, of course, other blocks which use “**end**” to terminate it. For example, definitions. But if the Parser should encounter such tokens, then things have gone so horribly awry, the Parser should just quit here and now.

```

⟨ Parse statements and reasoning (parser.pas) 1769 ⟩ ≡
  { Statements & Reasonings }
procedure Reasoning; forward;
procedure IgnoreProof;
  var lCounter: integer; ReasPos: Position;
  begin gBlockPtr↑.StartAtSignProof; ReasPos ← CurPos; ReadTokenProc; lCounter ← 1;
  repeat case CurWord.Kind of
    sy_Proof, sy_Now, sy_Hereby, sy_Case, sy_Suppose: inc(lCounter);
    sy_End: dec(lCounter);
    sy_Reserve, sy_Scheme, sy_Theorem, sy_Definition, sy_Begin, sy_Notation, sy_Registration, EOT: begin
      AcceptEnd(ReasPos); exit
    end;
  endcases; ReadTokenProc;
  until lCounter = 0;
  gBlockPtr↑.FinishAtSignProof;
end;

```

See also sections 1770, 1771, 1772, 1782, 1783, 1788, 1797, and 1799.

This code is used in section 1640.

1770. Parsing either a “**by**” justification (or a “**from**” justification) or a nested “**proof**” block. If the Parser is looking at neither situation, the *SimpleJustification* procedure will raise errors.

```

define parse_proof ≡
  if ProofPragma then Reasoning
  else IgnoreProof
  endif
⟨ Parse statements and reasoning (parser.pas) 1769 ⟩ +≡
procedure Justification;
  begin gItemPtr↑.StartJustification;
  case CurWord.Kind of
    sy_Proof: parse_proof;
  othercases SimpleJustification;
  endcases; gItemPtr↑.FinishJustification;
end;

```

1771. For private predicates (“**defpred**”) and private functors (“**deffunc**”), there will be a list of comma-separated types for the arguments of the private definition.

```

define parse_comma_separated_types ≡
  repeat TypeExpression; gItemPtr↑.FinishLocusType
  until ¬Occurs(sy_Comma)
⟨Parse statements and reasoning (parser.pas) 1769⟩ +≡
procedure ReadTypeList;
begin case CurWord.Kind of
  sy_RightSquareBracket, sy_RightParanthesis: ;
othercases parse_comma_separated_types;
endcases;
end;

```

1772. A “**Private Item**” is a statement (“item”) which introduces a new constant local (“private”) to the block or article.

```

define other_regular_statements ≡ Identifier, sy_Now, sy_For, sy_Ex, sy_Not, sy_Thesis,
  sy_LeftSquareBracket, sy_Contradiction, PredicateSymbol, sy_Does, sy_Do, sy_Equal,
  InfixOperatorSymbol, Numeral, LeftCircumfixSymbol, sy_LeftParanthesis, sy_It, sy_Dolar,
  StructureSymbol, sy_The, sy_LeftCurlyBracket, sy_Proof
⟨Parse statements and reasoning (parser.pas) 1769⟩ +≡
procedure RegularStatement; forward; { (§1799) }
procedure PrivateItem;
begin gBlockPtr↑.ProcessLink;
if CurWord.Kind = sy_Then then ReadWord;
case CurWord.Kind of
  sy_Deffunc: ⟨Parse a “deffunc” 1774⟩;
  sy_Defpred: ⟨Parse a “defpred” 1776⟩;
  sy_Set: ⟨Parse a “set” constant definition 1778⟩;
  sy_Reconsider: ⟨Parse a “reconsider” statement 1780⟩;
  sy_Consider: begin gBlockPtr↑.CreateItem(itChoice); ReadWord; ProcessChoice; SimpleJustification;
    end;
  other_regular_statements: begin gBlockPtr↑.CreateItem(itRegularStatement); RegularStatement; end;
othercases begin gBlockPtr↑.CreateItem(itIncorrItem); WrongWord(paWrongItemBeg);
  end;
endcases;
end;

```

1773. ⟨Error codes for parser 1642⟩ +≡
paWrongItemBeg = 391;

1774. ⟨Parse a “**deffunc**” 1774⟩ ≡
begin *gBlockPtr*↑.*CreateItem*(*itPrivFuncDefinition*); *ReadWord*; *gItemPtr*↑.*StartPrivateDefiniendum*;
Accept(*Identifier*, *paIdentExp6*); *Accept*(*sy_LeftParanthesis*, *paLeftParenthExp*); *ReadTypeList*;
Accept(*sy_RightParanthesis*, *paRightParenthExp8*); *gItemPtr*↑.*StartPrivateDefiniens*;
Accept(*sy_Equal*, *paEqualityExp1*); *TermExpression*; *gItemPtr*↑.*FinishPrivateFuncDefinienition*;
end

This code is used in section 1772.

1775. ⟨Error codes for parser 1642⟩ +≡
paIdentExp6 = 300; *paLeftParenthExp* = 360; *paRightParenthExp8* = 370; *paEqualityExp1* = 380;

1776. \langle Parse a “defpred” 1776 $\rangle \equiv$
begin *gBlockPtr*↑.*CreateItem*(*itPrivPredDefinition*); *ReadWord*; *gItemPtr*↑.*StartPrivateDefiniendum*;
Accept(*Identifier*, *paIdentExp7*); *Accept*(*sy_LeftSquareBracket*, *paLeftSquareExp*); *ReadTypeList*;
Accept(*sy_RightSquareBracket*, *paRightSquareExp4*); *gItemPtr*↑.*StartPrivateDefiniens*;
Accept(*sy_Means*, *paMeansExp*); *FormulaExpression*; *gItemPtr*↑.*FinishPrivatePredDefinienition*;
end

This code is used in section 1772.

1777. \langle Error codes for parser 1642 $\rangle + \equiv$
paIdentExp7 = 300; *paLeftSquareExp* = 361; *paRightSquareExp4* = 371; *paMeansExp* = 386;

1778. \langle Parse a “set” constant definition 1778 $\rangle \equiv$
begin *gBlockPtr*↑.*CreateItem*(*itConstantDefinition*); *ReadWord*;
repeat *gItemPtr*↑.*StartPrivateConstant*; *Accept*(*Identifier*, *paIdentExp8*);
Accept(*sy_Equal*, *paEqualityExp2*); *TermExpression*; *gItemPtr*↑.*FinishPrivateConstant*;
until \neg *Occurs*(*sy_Comma*);
end

This code is used in section 1772.

1779. \langle Error codes for parser 1642 $\rangle + \equiv$
paIdentExp8 = 300; *paEqualityExp2* = 380;

1780. \langle Parse a “reconsider” statement 1780 $\rangle \equiv$
begin *gBlockPtr*↑.*CreateItem*(*itReconsider*); *ReadWord*;
repeat *gItemPtr*↑.*ProcessReconsideredVariable*; *Accept*(*Identifier*, *paIdentExp9*);
case *CurWord.Kind* **of**
sy_Equal: **begin** *ReadWord*; *TermExpression*; *gItemPtr*↑.*FinishReconsideredTerm*;
end;
else *gItemPtr*↑.*FinishDefaultTerm*;
end;
until \neg *Occurs*(*sy_Comma*);
gItemPtr↑.*StartNewType*; *Accept*(*sy_As*, *paAsExp*); *TypeExpression*; *gItemPtr*↑.*FinishReconsidering*;
SimpleJustification;
end

This code is used in section 1772.

1781. \langle Error codes for parser 1642 $\rangle + \equiv$
paIdentExp9 = 300; *paAsExp* = 388;

1782. The *SetParserPragma* toggles the state variables for skipping proofs, and storing the pragma in the AST is handled by the *gBlockPtr*’s method call.

\langle Parse statements and reasoning (parser.pas) 1769 $\rangle + \equiv$

procedure *ProcessPragmas*;
begin while *CurWord.Kind* = *Pragma* **do**
begin *SetParserPragma*(*CurWord.Spelling*); { (§1342) }
gBlockPtr↑.*ProcessPragma*; { (§1362) }
ReadTokenProc;
end;
end;

1783. Reasoning items. The “linear reasoning” portion of the Parser corresponds to what “Mizar in a Nutshell” refers to as a sequence of “Reasoning Items”. Basically, everything exception “**per cases**”.

\langle Parse statements and reasoning (`parser.pas`) 1769 $\rangle + \equiv$

procedure *LinearReasoning*;

begin while *CurWord.Kind* \neq *sy_End* **do**

begin *StillCorrect* \leftarrow *true*; *ProcessPragmas*; \langle Parse statement of linear reasoning 1784 \rangle ;
Semicolon;

end;

end;

1784. Most statements are delegated to their own dedicated function.

\langle Parse statement of linear reasoning 1784 $\rangle \equiv$

case *CurWord.Kind* **of**

sy_Let: **begin** *gBlockPtr* \uparrow .*CreateItem(itGeneralization)*; *Generalization*; **end**;

sy_Given: *ExistentialAssumption*;

sy_Assume: **begin** *gBlockPtr* \uparrow .*CreateItem(itAssumption)*; *ReadWord*; *Assumption*; **end**;

sy_Take: \langle Parse “take” statement for linear reasoning 1785 \rangle ;

sy_Hereby: **begin** *gBlockPtr* \uparrow .*CreateItem(itConclusion)*; *Reasoning*; **end**;

\langle Parse “thus” and “hence” for linear reasoning 1786 \rangle ;

sy_Per: *exit*;

sy_Case, *sy_Suppose*: *exit*;

sy_Reserve, *sy_Scheme*, *sy_Theorem*, *sy_Definition*, *sy_Begin*, *sy_Notation*, *sy_Registration*, *EOT*: *exit*;

sy_Then: \langle Parse “then” for linear reasoning 1787 \rangle ;

othercases *PrivateItem*;

endcases

This code is used in section 1783.

1785. Take statements. We recall the syntax for a “take” statement:

$$\text{take } (\langle \text{Term} \rangle \mid \langle \text{Variable} \rangle = \langle \text{Term} \rangle) \{ ", " (\langle \text{Term} \rangle \mid \langle \text{Variable} \rangle = \langle \text{Term} \rangle) \}$$

That is, a comma-separated list of either (1) terms, or (2) a variable equal to a term.

\langle Parse “take” statement for linear reasoning 1785 $\rangle \equiv$

begin *gBlockPtr* \uparrow .*CreateItem(itExemplification)*; *ReadWord*;

repeat if (*CurWord.Kind* = *Identifier*) \wedge (*AheadWord.Kind* = *sy_Equal*) **then**

begin *gItemPtr* \uparrow .*ProcessExemplifyingVariable*; *ReadWord*; *ReadWord*; *TermExpression*;

gItemPtr \uparrow .*FinishExemplifyingVariable*;

end

else begin *gItemPtr* \uparrow .*StartExemplifyingTerm*; *TermExpression*; *gItemPtr* \uparrow .*FinishExemplifyingTerm*;

end;

until \neg *Occurs*(*sy_Comma*);

end

This code is used in section 1784.

1786. Thus statements. Both “**thus**” and “**hence**” (which is syntactic sugar for “**then thus**”) are parsed similarly. So it bears studying them in parallel. The “heavy lifting” is handled by the *RegularStatement* for parsing the formula. But the *gBlockPtr* state variable “primes the pump” by creating a “conclusion” statement.

```

⟨ Parse “thus” and “hence” for linear reasoning 1786 ⟩ ≡
sy_Hence: begin gBlockPtr↑.ProcessLink; ReadWord; gBlockPtr↑.CreateItem(itConclusion);
    RegularStatement;
end;
sy_Thus: begin ReadWord; gBlockPtr↑.ProcessLink;
    if CurWord.Kind = sy_Then then ReadWord;
    gBlockPtr↑.CreateItem(itConclusion); RegularStatement;
end

```

This code is used in section 1784.

1787. Parsing ‘then’ linked statements.

```

⟨ Parse “then” for linear reasoning 1787 ⟩ ≡
begin if AheadWord.Kind = sy_Per then
    begin gBlockPtr↑.ProcessLink; ReadWord; exit; end
else PrivateItem;
end

```

This code is used in section 1784.

1788. Non-block Reasoning. The Parser has just encountered a “**per cases**” statement. Now it must parse “**suppose**” items.

```

⟨ Parse statements and reasoning (parser.pas) 1769 ⟩ +≡
procedure NonBlockReasoning;
    var CasePos: Position; lCaseKind: TokenKind; ⟨ Process “case” (local procedure) 1789 ⟩;
    begin case CurWord.Kind of
        sy_Per, sy_Case, sy_Suppose: begin gBlockPtr↑.CreateItem(itPerCases);
            ⟨ Consume “per cases”, raise an error if they’re missing 1790 ⟩;
            if (CurWord.Kind ≠ sy_Case) ∧ (CurWord.Kind ≠ sy_Suppose) then
                ⟨ Try to synchronize after failing to find initial ‘case’ or ‘suppose’ 1792 ⟩;
            repeat ⟨ Parse “suppose” or “case” block 1794 ⟩;
            until (Curword.Kind = sy_End);
        end;
    endcases;
end;

```

1789. Each “**case**” or “**suppose**” block consists of zero or more linear reasoning items, followed possibly by an optional “non-block reasoning” proof (i.e., another nested “**per cases**” proof by cases).

```

⟨ Process “case” (local procedure) 1789 ⟩ ≡
procedure ProcessCase;
    begin Assumption; Semicolon; LinearReasoning;
    if CurWord.Kind = sy_Per then NonBlockReasoning;
    KillBlock; AcceptEnd(CasePos); Semicolon;
end

```

This code is used in section 1788.

1790. The Parser looks for “**per cases**” tokens, and some simple justification for the statement. If “**per**” is missing, a 231 error is raised. If the “**cases**” is missing, a 351 error is raised. When this code chunk is done, the Parser is looking at either a “**suppose**” token or a “**case**” token.

⟨ Consume “**per cases**”, raise an error if they’re missing 1790 ⟩ ≡
Accept(*sy_Per*, *paPerExp*); *Accept*(*sy_Cases*, *paCasesExp*); *SimpleJustification*; *Semicolon*;
lCaseKind ← *CurWord.Kind*

This code is used in section 1788.

1791. ⟨ Error codes for parser 1642 ⟩ +≡
paPerExp = 231; *paCasesExp* = 351;

1792. The Parser is expecting “**suppose**” or “**case**” after the “**per cases**” statement. But if the Parser fails to find either of these tokens, it *should* enter panic mode.

Like a person falling off a cliff reaches out for something to grab, the Parser in panic mode seeks something to “grab on to” so the Parser can “soldier on”. The technical term for this situation is that the Parser is trying to “synchronize” (usually people just talk about “synchronization”).

Mizar raises a 232 error.

⟨ Try to synchronize after failing to find initial ‘**case**’ or ‘**suppose**’ 1792 ⟩ ≡
begin *MissingWord*(*paSupposeOrCaseExp*); *lCaseKind* ← *sy_Suppose*;
gBlockPtr↑.*CreateItem*(*itCaseBlock*); *gBlockPtr*↑.*CreateBlock*(*blSuppose*);
gBlockPtr↑.*CreateItem*(*itSupposeHead*); *StillCorrect* ← *true*; *CasePos* ← *CurPos*; *ProcessCase*;
end

This code is used in section 1788.

1793. ⟨ Error codes for parser 1642 ⟩ +≡
paSupposeOrCaseExp = 232;

1794. ⟨ Parse “**suppose**” or “**case**” block 1794 ⟩ ≡
while (*CurWord.Kind* = *sy_Case*) ∨ (*CurWord.Kind* = *sy_Suppose*) **do**
 ⟨ Parse contents of “**suppose**” block 1795 ⟩;
case *Curword.Kind* **of**
sy_Reserve, *sy_Scheme*, *sy_Theorem*, *sy_Definition*, *sy_Begin*, *sy_Notation*, *sy_Registration*, *EOT*: *exit*;
sy_End: ;
othercases ⟨ Synchronize after missing ‘**suppose**’ or ‘**case**’ token 1796 ⟩;
endcases

This code is used in section 1788.

1795. Parsing the contents of a “suppose” or “case” block requires creating a new block (for the, you know, block) and creating a new item for the “suppose $\langle Formula \rangle$ ” or “case $\langle Formula \rangle$ ” statement.

If the user tries to “mix and match” the different kind of suppositions (i.e., “case” and “suppose”), then a 58 error should be raised.

```

define create_supposition_block  $\equiv$ 
    if lCaseKind = sy_Case then gBlockPtr↑.CreateBlock(blCase)
    else gBlockPtr↑.CreateBlock(blSuppose)
define create_supposition_head  $\equiv$ 
    if lCaseKind = sy_Case then gBlockPtr↑.CreateItem(itCaseHead)
    else gBlockPtr↑.CreateItem(itSupposeHead)

```

\langle Parse contents of “suppose” block 1795 $\rangle \equiv$

```

begin gBlockPtr↑.CreateItem(itCaseBlock); create_supposition_block; CasePos  $\leftarrow$  CurPos;
    StillCorrect  $\leftarrow$  true; create_supposition_head;
if CurWord.Kind  $\neq$  lCaseKind then ErrImm(58);
    ReadWord; ProcessCase;
end

```

This code is used in section 1794.

1796. \langle Synchronize after missing ‘suppose’ or ‘case’ token 1796 $\rangle \equiv$

```

begin MissingWord(paSupposeOrCaseExp); gBlockPtr↑.CreateItem(itCaseBlock);
    create_supposition_block; create_supposition_head; StillCorrect  $\leftarrow$  true; CasePos  $\leftarrow$  CurPos;
    ProcessCase;
end

```

This code is used in section 1794.

1797. Reasoning. The Parser is looking at “proof”, “hereby”, or “now”. The syntax for Mizar says that we should expect linear reasoning statements, followed by non-block reasoning (i.e., at most one “per cases” statement, and then “suppose” or “case” blocks).

\langle Parse statements and reasoning (*parser.pas*) 1769 $\rangle + \equiv$

```

procedure Reasoning;
    var ReasPos: Position;
    begin ReasPos  $\leftarrow$  CurPos;
    case CurWord.Kind of
        sy_Proof: begin gBlockPtr↑.CreateBlock(blProof); ReadTokenProc; end;
        sy_Hereby: begin gBlockPtr↑.CreateBlock(blHereby); ReadTokenProc; end;
        sy_Now: begin gBlockPtr↑.CreateBlock(blDiffuse); ReadTokenProc; end;
        othercases begin gBlockPtr↑.CreateBlock(blProof); WrongWord(paProofExp);
            end;
    endcases;
    LinearReasoning; NonBlockReasoning; KillBlock; AcceptEnd(ReasPos);
end;

```

1798. \langle Error codes for parser 1642 $\rangle + \equiv$

```

paProofExp = 389;

```

1799. Regular statements. A regular statement is one of the following:

- (1) “**now**” followed by reasoning;
- (2) A sentence (i.e., possibly labeled formula) followed by a “**proof**” block;
- (3) Iterative equalities.

⟨ Parse statements and reasoning (`parser.pas`) 1769 ⟩ +≡

```
procedure RegularStatement;
  begin ProcessLab; gItemPtr↑.StartRegularStatement;
  case CurWord.Kind of
    sy_Now: Reasoning;
  othercases begin ProcessSentence;
    case CurWord.Kind of
      sy_Proof: ⟨ Parse “proof” block 1800 ⟩;
    othercases begin gItemPtr↑.StartJustification; SimpleJustification; gItemPtr↑.FinishJustification;
      gItemPtr↑.FinishCompactStatement;
      while CurWord.Kind = sy_DotEquals do ⟨ Parse iterative equations 1801 ⟩;
      end;
    endcases;
  end;
endcases;
end;
```

1800. ⟨ Parse “proof” block 1800 ⟩ ≡

```
begin gItemPtr↑.StartJustification;
if ProofPragma then Reasoning
else IgnoreProof;
gItemPtr↑.FinishJustification;
end
```

This code is used in section 1799.

1801. ⟨ Parse iterative equations 1801 ⟩ ≡

```
begin gItemPtr↑.StartIterativeStep; ReadWord; TermExpression; gItemPtr↑.ProcessIterativeStep;
gItemPtr↑.StartJustification; SimpleJustification; gItemPtr↑.FinishJustification;
gItemPtr↑.FinishIterativeStep;
end
```

This code is used in section 1799.

Section 24.6. PATTERNS

1802. Visible arguments (compared to “hidden arguments”) appear to the left or right of a functor or predicate (or to the left of an attribute, or to the right of a mode or structure). The *gVisibleNbr* state variable is initialized to zero when the Parser starts parsing visible arguments, and the Parser increments it for each visible argument in the pattern.

If a non-identifier appears in a pattern, Mizar raises a 300 error. So you cannot be clever and try to trick Mizar into thinking “0 + x” is a pattern.

```

⟨ Parse patterns (parser.pas) 1802 ⟩ ≡
  { Patterns }
var gVisibleNbr: integer;
procedure GetVisible;
begin gItemPtr↑.ProcessVisible; { (§1472) }
  inc(gVisibleNbr); Accept(Identifier, paIdentExp3);
end;

```

See also sections 1804, 1805, 1810, 1812, 1814, 1820, 1823, and 1825.

This code is used in section 1640.

1803. ⟨ Error codes for parser 1642 ⟩ +≡
paIdentExp3 = 300;

1804. We will need to Parse a comma-separated list of identifiers when determining a pattern.

```

⟨ Parse patterns (parser.pas) 1802 ⟩ +≡
procedure ReadVisible;
begin gItemPtr↑.StartVisible; gVisibleNbr ← 0;
repeat GetVisible;
until ¬Occurs(sy_Comma);
gItemPtr↑.FinishVisible;
end;

```

1805. There are two cases to consider when determining the pattern for a mode: either the Parser is looking at “set” as a type, or—the more interesting case—the Parser is looking at an identifier which appears in a vocabulary file as a mode symbol.

```

⟨ Parse patterns (parser.pas) 1802 ⟩ +≡
procedure GetModePattern;
var lModesymbol: integer;
begin gItemPtr↑.StartModePattern; { (§1460) }
case CurWord.Kind of
sy_Set: ⟨ Parse pattern for “set” as a mode 1807 ⟩;
ModeSymbol: ⟨ Parse pattern for a mode symbols 1809 ⟩
othercases WrongWord(paWrongModePatternBeg);
endcases;
gItemPtr↑.FinishModePattern; { (§1461) }
end;

```

1806. ⟨ Error codes for parser 1642 ⟩ +≡
paWrongModePatternBeg = 303;

1807. \langle Parse pattern for “set” as a mode 1807 $\rangle \equiv$
begin if *AheadWord.Kind* = *sy_Of* **then** *WrongWord*(*paWrongModePatternSet*)
else *ReadWord*;
end

This code is used in section 1805.

1808. \langle Error codes for parser 1642 $\rangle + \equiv$
paWrongModePatternSet = 315;

1809. The “ \langle Kind \rangle MaxArgs” entry is initialized to \$FF before *ReadVisible* is invoked, which is PASCAL for #FF = 255. So if the *ModeMaxArgs* entry for the mode symbol is (1) less than the number of arguments parsed, or (2) uninitialized; then we should update its entry with the *gVisibleNbr* state variable’s current value.

define *get_index_compare_to_default*(#) \equiv [#] = \$FF
define *entry_is_uninitialized*(#) \equiv #.*fList*↑*get_index_compare_to_default*
 \langle Parse pattern for a mode symbols 1809 $\rangle \equiv$
begin *lModeSymbol* \leftarrow *CurWord.Nr*; *gVisibleNbr* \leftarrow 0; *ReadWord*; *gItemPtr*↑.*ProcessModePattern*;
if *Occurs*(*sy_Of*) **then** *ReadVisible*;
if (*ModeMaxArgs.fList*↑[*lModeSymbol*] < *gVisibleNbr*) \vee
 (*entry_is_uninitialized*(*ModeMaxArgs*)(*lModeSymbol*)) **then**
 ModeMaxArgs.fList↑[*lModeSymbol*] \leftarrow *gVisibleNbr*;
end

This code is used in section 1805.

1810. Parsing the visible arguments for a functor relies on this helper function.

\langle Parse patterns (parser.pas) 1802 $\rangle + \equiv$
procedure *ReadParams*;
begin if *Occurs*(*sy_LeftParanthesis*) **then**
 begin *ReadVisible*; *Accept*(*sy_RightParanthesis*, *paRightParenthExp5*)
 end
else if *CurWord.Kind* = *Identifier* **then**
 begin *gItemPtr*↑.*StartVisible*; *GetVisible*; *gItemPtr*↑.*FinishVisible*; **end**;
end;

1811. \langle Error codes for parser 1642 $\rangle + \equiv$
paRightParenthExp5 = 370;

1812. Attribute patterns allows for arguments *only on the right* of the attribute symbol, i.e., something like

$$\text{attr } \underbrace{\langle \text{Identifier} \rangle \text{ is } \langle \text{Arguments} \rangle \langle \text{Attribute-Name} \rangle}_{\text{pattern}} \text{ means } \dots$$

⟨ Parse patterns (parser.pas) 1802 ⟩ +≡

```

procedure GetAttrPattern;
  begin gItemPtr↑.StartAttributePattern; gVisibleNbr ← 0; GetVisible;
  gItemPtr↑.ProcessAttributePattern; Accept(sy_Is, paIsExp);
  if Occurs(sy_LeftParanthesis) then
    begin ReadVisible; Accept(sy_RightParanthesis, paRightParenthExp11)
    end
  else if CurWord.Kind = Identifier then ReadVisible;
  gItemPtr↑.FinishAttributePattern; Accept(AttributeSymbol, paAttrExp2);
  end;

```

1813. ⟨ Error codes for parser 1642 ⟩ +≡

paAttrExp2 = 306; paRightParenthExp11 = 370; paIsExp = 383;

1814. Functor patterns generically look like:

$$\text{func } \underbrace{\langle \text{Arguments} \rangle \langle \text{Identifier} \rangle \langle \text{Arguments} \rangle}_{\text{pattern}} \rightarrow \dots$$

or

$$\text{func } \underbrace{\langle \text{Left-Bracket} \rangle \langle \text{Arguments} \rangle \langle \text{Right-Bracket} \rangle}_{\text{pattern}} \rightarrow \dots$$

⟨ Parse patterns (parser.pas) 1802 ⟩ +≡

```

procedure GetFuncPattern;
  begin gItemPtr↑.StartFunctorPattern;
  case CurWord.Kind of
    Identifier, InfixOperatorSymbol, sy_LeftParanthesis: ⟨ Parse infix functor pattern 1816 ⟩;
    LeftCircumfixSymbol, sy_LeftSquareBracket, sy_LeftCurlyBracket: ⟨ Parse bracket functor pattern 1818 ⟩;
    othercases begin WrongWord(paWrongFunctorPatternBeg); gItemPtr↑.FinishFunctorPattern; end;
  endcases;
  end;

```

1815. ⟨ Error codes for parser 1642 ⟩ +≡

paWrongFunctorPatternBeg = 399;

1816. ⟨ Parse infix functor pattern 1816 ⟩ ≡

```

begin ReadParams; gItemPtr↑.ProcessFunctorSymbol; { (§1469) }
  Accept(InfixOperatorSymbol, paFuncExp2); ReadParams; gItemPtr↑.FinishFunctorPattern;
end

```

This code is used in section 1814.

1817. ⟨ Error codes for parser 1642 ⟩ +≡

paFuncExp2 = 302;

1818. \langle Parse bracket functor pattern 1818 $\rangle \equiv$
begin *ReadWord*; *ReadVisible*; *gItemPtr*↑.*FinishFunctorPattern*;
case *Curword.Kind* **of**
sy_RightSquareBracket, *sy_RightCurlyBracket*, *sy_RightParanthesis*: *ReadWord*;
othercases *Accept*(*RightCircumfixSymbol*, *paRightBraExp2*);
endcases;
end

This code is used in section 1814.

1819. \langle Error codes for parser 1642 $\rangle + \equiv$
paRightBraExp2 = 310;

1820. Predicate patterns resemble infix functor patterns.

\langle Parse patterns (*parser.pas*) 1802 $\rangle + \equiv$
procedure *GetPredPattern*;
var *lPredSymbol*: *integer*;
begin *gItemPtr*↑.*StartPredicatePattern*;
if *CurWord.Kind* = *Identifier* **then** *ReadVisible*;
gItemPtr↑.*ProcessPredicateSymbol*;
case *CurWord.Kind* **of**
sy_Equal, *PredicateSymbol*: \langle Parse predicate pattern 1822 \rangle ;
othercases *WrongWord*(*paWrongPredPattern*);
endcases; *gItemPtr*↑.*FinishPredicatePattern*;
end;

1821. \langle Error codes for parser 1642 $\rangle + \equiv$
paWrongPredPattern = 301;

1822. \langle Parse predicate pattern 1822 $\rangle \equiv$
begin *lPredSymbol* \leftarrow *CurWord.Nr*;
if *CurWord.Kind* = *sy_Equal* **then** *lPredSymbol* \leftarrow *EqualitySym*;
gVisibleNbr \leftarrow 0; *ReadWord*;
if *CurWord.Kind* = *Identifier* **then** *ReadVisible*;
if (*PredMaxArgs.fList*↑[*lPredSymbol*] < *gVisibleNbr*) \vee (*entry_is_uninitialized*(*PredMaxArgs*)(*lPredSymbol*))
then *PredMaxArgs.fList*↑[*lPredSymbol*] \leftarrow *gVisibleNbr*;
end

This code is used in section 1820.

1823. The “specification” (appearing in a non-expandable mode and functor definitions) refers to the “ \rightarrow *Type*” portion which gives the type for the functor or mode.

\langle Parse patterns (*parser.pas*) 1802 $\rangle + \equiv$
procedure *Specification*;
begin *gItemPtr*↑.*StartSpecification*; *Accept*(*sy_Arrow*, *paArrowExp1*); *TypeExpression*;
gItemPtr↑.*FinishSpecification*;
end;

1824. \langle Error codes for parser 1642 $\rangle + \equiv$
paArrowExp1 = 385;

1825. Parsing a structure pattern is a bit misleading. Unlike the previous procedures, this will actually parse the entirety of a structure definition:

struct $\langle Identifier \rangle$ ($\langle Types \rangle$) (# $\langle Fields \rangle$ #)

\langle Parse patterns (parser.pas) 1802 $\rangle + \equiv$

procedure *GetStructPatterns*;

var *lStructureSymbol*: integer;

begin *gBlockPtr*↑.CreateItem(itDefStruct); ReadWord;

\langle Parse ancestors of structure, if there are any 1826 \rangle ;

\langle Parse “over” and any structure arguments, if any 1828 \rangle ;

gItemPtr↑.StartFields;

\langle Update max arguments for structure symbol, if needed 1830 \rangle ;

\langle Parse the fields of the structure definition 1831 \rangle ;

end;

1826. \langle Parse ancestors of structure, if there are any 1826 $\rangle \equiv$

if *CurWord.Kind* = *sy_LeftParanthesis* **then**

begin repeat *gItemPtr*↑.StartPrefix; ReadWord; TypeExpression; *gItemPtr*↑.FinishPrefix;

until *CurWord.Kind* \neq *sy_Comma*;

 Accept(*sy_RightParanthesis*, *paRightParenthExp6*);

end

This code is used in section 1825.

1827. \langle Error codes for parser 1642 $\rangle + \equiv$

paRightParenthExp6 = 370;

1828. \langle Parse “over” and any structure arguments, if any 1828 $\rangle \equiv$

gItemPtr↑.ProcessStructureSymbol; *lStructureSymbol* \leftarrow \$FF;

if *CurWord.Kind* = *StructureSymbol* **then** *lStructureSymbol* \leftarrow *CurWord.Nr*;

 Accept(*StructureSymbol*, *paStructExp1*);

if Occurs(*sy_Over*) **then** ReadVisible

This code is used in section 1825.

1829. \langle Error codes for parser 1642 $\rangle + \equiv$

paStructExp1 = 304;

1830. \langle Update max arguments for structure symbol, if needed 1830 $\rangle \equiv$

if *lStructureSymbol* \neq \$FF **then**

if (*StructModeMaxArgs.fList*↑[*lStructureSymbol*] < *gVisibleNbr*) \vee

 (*entry_is_uninitialized*(*StructModeMaxArgs*)(*lStructureSymbol*)) **then**

StructModeMaxArgs.fList↑[*lStructureSymbol*] \leftarrow *gVisibleNbr*

This code is used in section 1825.

1831. \langle Parse the fields of the structure definition 1831 $\rangle \equiv$

 Accept(*sy_StructLeftBracket*, *paLeftDoubleExp3*);

repeat \langle Parse field for the structure definition 1833 \rangle ;

until \neg Occurs(*sy_Comma*);

gItemPtr↑.FinishFields; Accept(*sy_StructRightBracket*, *paRightDoubleExp2*)

This code is used in section 1825.

1832. \langle Error codes for parser 1642 $\rangle + \equiv$
paLeftDoubleExp3 = 363; *paRightDoubleExp2* = 373;

1833. \langle Parse field for the structure definition 1833 $\rangle \equiv$
gItemPtr↑.*StartAggrPattSegment*;
repeat *gItemPtr*↑.*ProcessField*; *Accept*(*SelectorSymbol*, *paSelectExp1*);
until \neg *Occurs*(*sy_Comma*);
Specification; *gItemPtr*↑.*FinishAggrPattSegment*

This code is used in section 1831.

1834. \langle Error codes for parser 1642 $\rangle + \equiv$
paSelectExp1 = 305;

Section 24.7. DEFINITIONS

1835. Non-expandable modes, i.e., modes of the form

$$\text{mode } \langle \text{Identifier} \rangle \text{ of } \langle \text{Arguments} \rangle \rightarrow \langle \text{Type} \rangle \text{ means } \langle \text{Formula} \rangle$$

$\langle \text{Parse definitions (parser.pas) 1835} \rangle \equiv$
 $\{ \text{Definitions} \}$

```

procedure ConstructionType;
begin gItemPtr↑.StartConstructionType; { (§1511) }
if CurWord.Kind = sy_Arrow then
  begin ReadWord; TypeExpression end;
  gItemPtr↑.FinishConstructionType; { (§1453) }
end;

```

See also sections 1836, 1837, 1847, 1848, 1850, 1852, 1854, 1859, 1862, 1865, 1871, 1873, 1875, 1877, 1878, 1880, and 1881.

This code is used in section 1640.

1836. Parsing correctness conditions amounts to looping through every “ $\langle \text{Correctness} \rangle \langle \text{Justification} \rangle$,” statement, with a fallback “**correctness** $\langle \text{Justification} \rangle$,” correctness condition.

There is a comment, “o jaki tu item chodzi? definitional-item?”, which Google translates from Polish as, “What item are we talking about here? Definitional-item?” I have swapped this into the code snippet.

$\langle \text{Parse definitions (parser.pas) 1835} \rangle + \equiv$

```

procedure Correctness;
begin while CurWord.Kind = sy_CorrectnessCondition do
  begin StillCorrect ← true; gBlockPtr↑.CreateItem(itCorrCond); ReadWord; Justification;
  Semicolon;
  end;
  gItemPtr↑.ProcessCorrectness; { (§1510) What item are we talking about here? Definitional-item? }
if CurWord.Kind = sy_Correctness then { “correctness” catchall }
  begin StillCorrect ← true; gBlockPtr↑.CreateItem(itCorrectness); ReadWord; Justification;
  Semicolon;
  end;
end;

```

1837.

⟨ Parse definitions (parser.pas) 1835 ⟩ +≡

procedure *Definition*;

var *lDefKind*: *TokenKind*; *lDefiniensExpected*: *boolean*;

begin *lDefKind* ← *CurWord.Kind*; *lDefiniensExpected* ← *true*;

case *CurWord.Kind* **of**

sy_Mode: ⟨ Parse mode definition 1838 ⟩;

sy_Attr: **begin** *gBlockPtr*↑.*CreateItem*(*itDefAttr*); *ReadWord*; *GetAttrPattern*; **end**;

sy_Struct: **begin** *GetStructPatterns*; *lDefiniensExpected* ← *false*; **end**;

sy_Func: **begin** *gBlockPtr*↑.*CreateItem*(*itDefFunc*); *ReadWord*; *GetFuncPattern*; *ConstructionType*;

end;

sy_Pred: **begin** *gBlockPtr*↑.*CreateItem*(*itDefPred*); *ReadWord*; *gItemPtr*↑.*StartDefPredicate*;

GetPredPattern;

end;

endcases;

if *lDefiniensExpected* **then** ⟨ Parse definiens 1839 ⟩;

Semicolon; *Correctness*;

while (*CurWord.Kind* = *sy_Property*) **do**

begin *gBlockPtr*↑.*CreateItem*(*itProperty*); *StillCorrect* ← *true*; *ReadWord*; *Justification*; *Semicolon*;

end;

gBlockPtr↑.*FinishDefinition*;

end;

1838. ⟨ Parse mode definition 1838 ⟩ ≡

begin *gBlockPtr*↑.*CreateItem*(*itDefMode*); *ReadWord*; *GetModePattern*;

case *CurWord.Kind* **of**

sy_Is: **begin** *gItemPtr*↑.*StartExpansion*; *ReadWord*; *TypeExpression*; *lDefiniensExpected* ← *false*;

end;

othercases *ConstructionType*;

endcases;

end

This code is used in section 1837.

1839. ⟨ Parse definiens 1839 ⟩ ≡

case *CurWord.Kind* **of**

sy_Means: ⟨ Parse “means” definiens 1840 ⟩;

sy_Equals: ⟨ Parse “equals” definiens 1844 ⟩;

endcases

This code is used in section 1837.

1840. $\langle \text{Parse “means” definiens 1840} \rangle \equiv$
begin *gItemPtr*↑.*ProcessMeans*; *ReadWord*;
if *Occurs*(*sy_Colon*) **then**
 begin *gItemPtr*↑.*ProcessDefiniensLabel*; *Accept*(*Identifier*, *paIdentExp10*);
 Accept(*sy_Colon*, *paColonExp2*);
 end
else *gItemPtr*↑.*ProcessDefiniensLabel*;
 gItemPtr↑.*StartDefiniens*; *FormulaExpression*;
if *CurWord.Kind* = *sy_If* **then** $\langle \text{Parse “means” definition-by-cases 1842} \rangle$
else *gItemPtr*↑.*FinishOtherwise*;
 gItemPtr↑.*FinishDefiniens*;
end

This code is used in section 1839.

1841. $\langle \text{Error codes for parser 1642} \rangle + \equiv$
 paIdentExp10 = 300; *paColonExp2* = 384;

1842. $\langle \text{Parse “means” definition-by-cases 1842} \rangle \equiv$
begin *gItemPtr*↑.*StartGuard*; *ReadWord*; *FormulaExpression*; *gItemPtr*↑.*FinishGuard*;
while *Occurs*(*sy_Comma*) **do**
 begin *FormulaExpression*; *gItemPtr*↑.*StartGuard*; *Accept*(*sy_If*, *paIfExp*); *FormulaExpression*;
 gItemPtr↑.*FinishGuard*;
 end;
if *CurWord.Kind* = *sy_Otherwise* **then**
 begin *gItemPtr*↑.*StartOtherwise*; *ReadWord*; *FormulaExpression*; *gItemPtr*↑.*FinishOtherwise*; **end**;
end

This code is used in section 1840.

1843. $\langle \text{Error codes for parser 1642} \rangle + \equiv$
 paIfExp = 381;

1844. $\langle \text{Parse “equals” definiens 1844} \rangle \equiv$
if *lDefKind* \neq *sy_Func* **then**
 begin *WrongWord*(*paUnexpEquals*); **end**
else begin *gItemPtr*↑.*ProcessEquals*; *ReadWord*;
 if *Occurs*(*sy_Colon*) **then**
 begin *gItemPtr*↑.*ProcessDefiniensLabel*; *Accept*(*Identifier*, *paIdentExp10*);
 Accept(*sy_Colon*, *paColonExp2*);
 end
 else *gItemPtr*↑.*ProcessDefiniensLabel*;
 gItemPtr↑.*StartEquals*; *TermExpression*;
 if *CurWord.Kind* = *sy_If* **then** $\langle \text{Parse “equals” definition-by-cases 1846} \rangle$
 else *gItemPtr*↑.*FinishOtherwise*;
 gItemPtr↑.*FinishDefiniens*;
 end

This code is used in section 1839.

1845. $\langle \text{Error codes for parser 1642} \rangle + \equiv$
 paUnexpEquals = 186;

1846. $\langle \text{Parse “equals” definition-by-cases } 1846 \rangle \equiv$
begin $gItemPtr \uparrow . \text{StartGuard}$; $ReadWord$; $FormulaExpression$; $gItemPtr \uparrow . \text{FinishGuard}$;
while $Occurs(sy_Comma)$ **do**
 begin $TermExpression$; $gItemPtr \uparrow . \text{StartGuard}$; $Accept(sy_If, paIfExp)$; $FormulaExpression$;
 $gItemPtr \uparrow . \text{FinishGuard}$;
 end;
if $CurWord.Kind = sy_Otherwise$ **then**
 begin $gItemPtr \uparrow . \text{StartOtherwise}$; $ReadWord$; $TermExpression$; $gItemPtr \uparrow . \text{FinishOtherwise}$;
 end;
end

This code is used in section 1844.

1847. When introducing a “synonym” or “antonym”, the Parser needs to determine *what kind of thing* is being introduced as a synonym or antonym.

[[This could probably be turned into an **case** statement, but I am just transcribing the code as faithfully as possible.]]

define $is_attr_pattern \equiv (CurWord.Kind = Identifier) \wedge (AheadWord.Kind = sy_Is)$
define $is_infix_pattern \equiv (CurWord.Kind \in [LeftCircumfixSymbol, sy_LeftCurlyBracket,$
 $sy_LeftSquareBracket, sy_LeftParanthesis, InfixOperatorSymbol]) \vee ((CurWord.Kind =$
 $Identifier) \wedge (AheadWord.Kind = InfixOperatorSymbol))$
define $is_predicate_pattern \equiv (CurWord.Kind = PredicateSymbol) \vee (CurWord.Kind = sy_Equal) \vee$
 $((CurWord.Kind = Identifier) \wedge (AheadWord.Kind \in [sy_Comma, PredicateSymbol, sy_Equal]))$
define $is_selector_pattern \equiv (CurWord.Kind = sy_The) \wedge (AheadWord.Kind = SelectorSymbol)$
define $is_forgetful_functor_pattern \equiv (CurWord.Kind = sy_The) \wedge (AheadWord.Kind = StructureSymbol)$
 $\langle \text{Parse definitions (parser.pas) } 1835 \rangle + \equiv$
function $CurrPatternKind$: $TokenKind$;
 begin **if** $CurWord.Kind = ModeSymbol$ **then** $CurrPatternKind \leftarrow ModeSymbol$
 else **if** $CurWord.Kind = StructureSymbol$ **then** $CurrPatternKind \leftarrow StructureSymbol$
 else **if** $is_attr_pattern$ **then** $CurrPatternKind \leftarrow AttributeSymbol$
 else **if** $is_infix_pattern$ **then** $CurrPatternKind \leftarrow InfixOperatorSymbol$
 else **if** $is_predicate_pattern$ **then** $CurrPatternKind \leftarrow PredicateSymbol$
 else **if** $is_selector_pattern$ **then** $CurrPatternKind \leftarrow SelectorSymbol$
 else **if** $is_forgetful_functor_pattern$ **then** $CurrPatternKind \leftarrow ForgetfulFunctor$
 else $CurrPatternKind \leftarrow sy_Error$;
 end;

1848. The Parser is looking at the “**synonym**” token when this procedure is invoked.

⟨ Parse definitions (parser.pas) 1835 ⟩ +≡

```

procedure Synonym;
  begin ReadWord;
  case CurrPatternKind of
    ModeSymbol: begin { Mode synonym }
      gBlockPtr↑.CreateItem(itModeNotation); GetModePattern; gItemPtr↑.ProcessModeSynonym;
      Accept(sy_For, paForExp); GetModePattern;
    end;
    AttributeSymbol: begin { Attribute synonym }
      gBlockPtr↑.CreateItem(itAttrSynonym); GetAttrPattern; gItemPtr↑.ProcessAttrSynonym;
      Accept(sy_For, paForExp); GetAttrPattern;
    end;
    InfixOperatorSymbol: begin { Functor synonym }
      gBlockPtr↑.CreateItem(itFuncNotation); GetFuncPattern; gItemPtr↑.ProcessFuncSynonym;
      Accept(sy_For, paForExp); GetFuncPattern;
    end;
    PredicateSymbol: begin { Predicate synonym }
      gBlockPtr↑.CreateItem(itPredSynonym); gItemPtr↑.StartDefPredicate; GetPredPattern;
      gItemPtr↑.ProcessPredSynonym; Accept(sy_For, paForExp); GetPredPattern;
    end
  othercases begin gBlockPtr↑.CreateItem(itIncorrItem); ErrImm(paWrongPattBeg1);
  end;
endcases;
end;

```

1849. ⟨ Error codes for parser 1642 ⟩ +≡

paWrongPattBeg1 = 314; *paForExp* = 382;

1850. Antonyms only make sense for attributes and predicates. A 314 error is raised for any other kind of antonym.

⟨ Parse definitions (parser.pas) 1835 ⟩ +≡

```

procedure Antonym;
  begin ReadWord;
  case CurrPatternKind of
    Attributesymbol: begin { Attribute antonym }
      gBlockPtr↑.CreateItem(itAttrAntonym); GetAttrPattern; gItemPtr↑.ProcessAttrAntonym;
      Accept(sy_For, paForExp); GetAttrPattern;
    end;
    PredicateSymbol: begin { Predicate antonym }
      gBlockPtr↑.CreateItem(itPredAntonym); gItemPtr↑.StartDefPredicate; GetPredPattern;
      gItemPtr↑.ProcessPredAntonym; Accept(sy_For, paForExp); GetPredPattern;
    end
  othercases begin gBlockPtr↑.CreateItem(itIncorrItem); ErrImm(paWrongPattBeg2);
  end;
endcases;
end;

```

1851. ⟨ Error codes for parser 1642 ⟩ +≡

paWrongPattBeg2 = 314;

1852.

⟨ Parse definitions (parser.pas) 1835 ⟩ +≡

```

procedure UnexpectedItem;
  begin case CurWord.Kind of
    sy_Case, sy_Suppose, sy_Hereby: begin ErrImm(paWrongItemBeg); ReadWord;
      if CurWord.Kind = sy_That then ReadWord;
        PrivateItem;
      end;
    sy_Per: begin gBlockPtr↑.CreateItem(itIncorrItem); ErrImm(paWrongItemBeg); ReadWord;
      if CurWord.Kind = sy_Cases then
        begin ReadWord; InCorrStatement; SimpleJustification; end;
      end;
    othercases begin ErrImm(paUnexpItemBeg); StillCorrect ← true; PrivateItem; end;
  endcases;
end;

```

1853. ⟨ Error codes for parser 1642 ⟩ +≡

paUnexpItemBeg = 392;

1854. The Parser is currently looking at the “definition” token, so it will construct a definition block AST.

⟨ Parse definitions (parser.pas) 1835 ⟩ +≡

```

procedure DefinitionalBlock;
  var DefPos: Position;
  begin gBlockPtr↑.CreateItem(itDefinition); gBlockPtr↑.CreateBlock(blDefinition); DefPos ← CurPos;
  ReadWord;
  while CurWord.Kind ≠ sy_End do ⟨ Parse item in definition block 1855 ⟩;
  KillBlock; AcceptEnd(DefPos);
end;

```

1855. ⟨ Parse item in definition block 1855 ⟩ ≡

```

begin StillCorrect ← true; gBlockPtr↑.ProcessRedefine;
if Occurs(sy_Redefine) then ⟨ Check we are redefining a mode, attribute, functor, or predicate 1856 ⟩;
case CurWord.Kind of
  sy_Mode, sy_Attr, sy_Struct, sy_Func, sy_Pred: Definition;
  sy_Begin, EOT, sy_Reserve, sy_Scheme, sy_Theorem, sy_Definition, sy_Registration, sy_Notation: break;
  Pragma: ProcessPragmas;
  othercases begin ⟨ Parse loci, assumptions, unexpected items in a definition block 1858 ⟩;
    Semicolon;
  end;
endcases;
end

```

This code is used in section 1854.

1856. ⟨ Check we are redefining a mode, attribute, functor, or predicate 1856 ⟩ ≡

```

if ¬(CurWord.Kind ∈ [sy_Mode, sy_Attr, sy_Func, sy_Pred]) then Error(PrevPos, paUnexpRedef)

```

This code is used in section 1855.

1857. ⟨ Error codes for parser 1642 ⟩ +≡

paUnexpRedef = 273;

1858. $\langle \text{Parse loci, assumptions, unexpected items in a definition block 1858} \rangle \equiv$
case *CurWord.Kind* **of**
sy_Let: **begin** *gBlockPtr*↑.*CreateItem(itLociDeclaration)*; *Generalization*; **end**;
sy_Given: *ExistentialAssumption*;
sy_Assume: **begin** *gBlockPtr*↑.*CreateItem(itAssumption)*; *ReadWord*; *Assumption*; **end**;
sy_Canceled: *Canceled*;
sy_Case, *sy_Suppose*, *sy_Per*, *sy_Hereby*: *UnexpectedItem*;
othercases *PrivateItem*;
endcases

This code is used in section 1855.

1859. The Parser's current token is “**notation**”. Notation blocks are very similar in structure to definition blocks. Unsurprisingly, the Parser's code has a similar structure as parsing a definition block.

$\langle \text{Parse definitions (parser.pas) 1835} \rangle + \equiv$
procedure *NotationBlock*;
var *DefPos*: *Position*;
begin *gBlockPtr*↑.*CreateItem(itDefinition)*; *gBlockPtr*↑.*CreateBlock(blNotation)*; *DefPos* ← *CurPos*;
ReadWord;
while *CurWord.Kind* ≠ *sy_End* **do** $\langle \text{Parse item for notation block 1860} \rangle$;
KillBlock; *AcceptEnd(DefPos)*;
end;

1860. $\langle \text{Parse item for notation block 1860} \rangle \equiv$
begin *StillCorrect* ← *true*;
case *CurWord.Kind* **of**
sy_Begin, *EOT*, *sy_Reserve*, *sy_Scheme*, *sy_Theorem*, *sy_Definition*, *sy_Registration*, *sy_Notation*: *break*;
Pragma: *ProcessPragmas*;
othercases $\langle \text{Parse semicolon-separated items in a notation block 1861} \rangle$;
endcases;
end

This code is used in section 1859.

1861. $\langle \text{Parse semicolon-separated items in a notation block 1861} \rangle \equiv$
begin case *CurWord.Kind* **of**
sy_Synonym: *Synonym*;
sy_Antonym: *Antonym*;
sy_Let: **begin** *gBlockPtr*↑.*CreateItem(itLociDeclaration)*; *ReadWord*; *FixedVariables*; **end**;
othercases *UnexpectedItem*;
endcases;
Semicolon;
end

This code is used in section 1860.

1862.

define *ahead_is_type* \equiv (*AheadWord.Kind* \in [*sy_Set*, *ModeSymbol*, *StructureSymbol*])
define *is_attr_token* \equiv (*CurWord.Kind* \in [*AttributeSymbol*, *sy_Non*]) \vee
 (*CurWord.Kind* \in (*TermBegSys* - [*sy_LeftParanthesis*, *StructureSymbol*])) \vee
 ((*CurWord.Kind* = *sy_LeftParanthesis*) \wedge \neg (*ahead_is_type*)) \vee
 (*CurWord.Kind* = *StructureSymbol*) \wedge (*AheadWord.Kind* = *sy_StructLeftBracket*)

\langle Parse definitions (parser.pas) 1835 $\rangle + \equiv$

procedure *ATTSubexpression*(**var** *aExpKind* : *ExpKind*);
var *lAttrExp*: *boolean*;
begin *aExpKind* \leftarrow *exNull*; *gSubexpPtr* \uparrow .*StartAttributes*;
while *is_attr_token* **do**
begin *gSubexpPtr* \uparrow .*ProcessNon*; *lAttrExp* \leftarrow *CurWord.Kind* = *sy_Non*;
if *CurWord.Kind* = *sy_Non* **then** *ReadWord*;
 \langle Parse arguments for attribute expression 1864 \rangle ;
if *CurWord.Kind* = *AttributeSymbol* **then**
begin *aExpKind* \leftarrow *exAdjectiveCluster*; *gSubexpPtr* \uparrow .*ProcessAttribute*; *ReadWord*; **end**
else begin if *lAttrExp* \vee (*aExpKind* = *exAdjectiveCluster*) **then**
 { *aExpKind* = *exAdjectiveCluster* is never true }
begin *gSubexpPtr* \uparrow .*ProcessAttribute*; *SynErr*(*CurPos*, *paAttrExp3*);
end;
break;
end;
end;
gSubexpPtr \uparrow .*CompleteAttributes*;
end;

1863. \langle Error codes for parser 1642 $\rangle + \equiv$

paAttrExp3 = 306;

1864. \langle Parse arguments for attribute expression 1864 $\rangle \equiv$

if (*CurWord.Kind* \in (*TermBegSys* - [*StructureSymbol*])) \vee
 (*CurWord.Kind* = *StructureSymbol*) \wedge (*AheadWord.Kind* = *sy_StructLeftBracket*) **then**
begin if *aExpKind* = *exNull* **then** *aExpKind* \leftarrow *exTerm*;
gSubexpPtr \uparrow .*StartAttributeArguments*; *ProcessArguments*; *gSubexpPtr* \uparrow .*FinishAttributeArguments*;
end

This code is used in section 1862.

1865. Registration clusters.

⟨ Parse definitions (parser.pas) 1835 ⟩ +≡

```

procedure RegisterCluster;
  var lExpKind: ExpKind;
  begin gBlockPtr↑.CreateItem(itCluster); ReadWord;
  if (CurWord.Kind = Identifier) ∧ (AheadWord.Kind = sy_Arrow) then ErrImm(paFuncExp4);
  gItemPtr↑.StartAttributes; { (§1425) }
  gItemPtr↑.CreateExpression(exAdjectiveCluster); { (§1498) }
  gExpPtr↑.CreateSubexpression; ATTSubexpression(lExpKind);
  case lExpKind of
    exTerm: gSubexpPtr↑.CompleteClusterTerm;
    exNull, exAdjectiveCluster: gSubexpPtr↑.CompleteAdjectiveCluster;
  endcases;
  KillSubexpression; KillExpression;
  case lExpKind of
    exTerm: ⟨ Parse functor registration cluster 1867 ⟩;
    exNull, exAdjectiveCluster: case CurWord.Kind of
      sy_Arrow: ⟨ Parse conditional registration cluster 1869 ⟩;
      sy_For: ⟨ Parse existential registration cluster 1870 ⟩;
    othercases begin SynErr(CurPos, paForOrArrowExpected); gItemPtr↑.FinishConsequent;
      gItemPtr↑.CreateExpression(exType); gExpPtr↑.CreateSubexpression; gSubexpPtr↑.StartType;
      gSubexpPtr↑.InsertIncorrType; gSubexpPtr↑.CompleteType; gSubexpPtr↑.CompleteClusterType;
      KillSubexpression; KillExpression; gItemPtr↑.FinishClusterType;
    end;
  endcases;
endcases; Semicolon; Correctness;
end;

```

1866. ⟨ Error codes for parser 1642 ⟩ +≡

paForOrArrowExpected = 406;

1867. ⟨ Parse functor registration cluster 1867 ⟩ ≡

```

begin gItemPtr↑.FinishClusterTerm; Accept(sy_Arrow, paArrowExp2);
  gItemPtr↑.CreateExpression(exAdjectiveCluster); gExpPtr↑.CreateSubexpression;
  gSubexpPtr↑.StartAttributes; ATTSubexpression(lExpKind);
  if lExpKind ≠ exAdjectiveCluster then
    begin ErrImm(paAdjClusterExp)
    end;
  gSubexpPtr↑.CompleteAdjectiveCluster; KillSubexpression; KillExpression;
  gItemPtr↑.FinishConsequent;
  if CurWord.Kind = sy_For then
    begin ReadWord; gItemPtr↑.CreateExpression(exType); gExpPtr↑.CreateSubexpression;
      gSubexpPtr↑.StartType; gSubexpPtr↑.StartAttributes; GetAdjectiveCluster; RadixTypeSubexpression;
      gSubexpPtr↑.CompleteAttributes; gSubexpPtr↑.CompleteType; gSubexpPtr↑.CompleteClusterType;
      KillSubexpression; KillExpression;
    end;
  gItemPtr↑.FinishClusterType;
end

```

This code is used in section 1865.

1868. ⟨ Error codes for parser 1642 ⟩ +≡

paAdjClusterExp = 223; paArrowExp2 = 385;

1869. $\langle \text{Parse conditional registration cluster } 1869 \rangle \equiv$
begin *gItemPtr*↑.*FinishAntecedent*; *ReadWord*; *gItemPtr*↑.*CreateExpression*(*exAdjectiveCluster*);
gExpPtr↑.*CreateSubexpression*; *gSubexpPtr*↑.*StartAttributes*; *ATTSubexpression*(*lExpKind*);
if *lExpKind* \neq *exAdjectiveCluster* **then**
 begin *ErrImm*(*paAdjClusterExp*);
 end;
gSubexpPtr↑.*CompleteAdjectiveCluster*; *KillSubexpression*; *KillExpression*;
gItemPtr↑.*FinishConsequent*; *Accept*(*sy_For*, *paForExp*); *gItemPtr*↑.*CreateExpression*(*exType*);
gExpPtr↑.*CreateSubexpression*; *gSubexpPtr*↑.*StartType*; *gSubexpPtr*↑.*StartAttributes*;
GetAdjectiveCluster; *RadixTypeSubexpression*; *gSubexpPtr*↑.*CompleteAttributes*;
gSubexpPtr↑.*CompleteType*; *gSubexpPtr*↑.*CompleteClusterType*; *KillSubexpression*; *KillExpression*;
gItemPtr↑.*FinishClusterType*;
end

This code is used in section 1865.

1870. $\langle \text{Parse existential registration cluster } 1870 \rangle \equiv$
begin *gItemPtr*↑.*FinishConsequent*; *ReadWord*; *gItemPtr*↑.*CreateExpression*(*exType*);
gExpPtr↑.*CreateSubexpression*; *gSubexpPtr*↑.*StartType*; *gSubexpPtr*↑.*StartAttributes*;
GetAdjectiveCluster; *RadixTypeSubexpression*; *gSubexpPtr*↑.*CompleteAttributes*;
gSubexpPtr↑.*CompleteType*; *gSubexpPtr*↑.*CompleteClusterType*; *KillSubexpression*; *KillExpression*;
gItemPtr↑.*FinishClusterType*;
end

This code is used in section 1865.

1871. Reduction registration.

$\langle \text{Parse definitions (parser.pas) } 1835 \rangle + \equiv$
procedure *Reduction*;
 var *lExpKind*: *ExpKind*;
 begin *gBlockPtr*↑.*CreateItem*(*itReduction*); *ReadWord*;
 if (*CurWord.Kind* = *Identifier*) \wedge (*AheadWord.Kind* = *sy_Arrow*) **then** *ErrImm*(*paFuncExp4*);
 gItemPtr↑.*StartFuncReduction*; *TermExpression*; *gItemPtr*↑.*ProcessFuncReduction*;
 Accept(*sy_To*, *paToExp*); *TermExpression*; *gItemPtr*↑.*FinishFuncReduction*; *Semicolon*; *Correctness*;
 end;

1872. $\langle \text{Error codes for parser } 1642 \rangle + \equiv$
 paFuncExp4 = 302; *paToExp* = 404;

1873. Identification registration.

$\langle \text{Parse definitions (parser.pas) } 1835 \rangle + \equiv$
procedure *Identification*;
 begin *gBlockPtr*↑.*CreateItem*(*itIdentify*); *ReadWord*; { *begin* }
 gItemPtr↑.*StartFuncIdentify*; *GetFuncPattern*; *gItemPtr*↑.*ProcessFuncIdentify*;
 Accept(*sy_With*, *paWithExp*); *GetFuncPattern*; *gItemPtr*↑.*CompleteFuncIdentify*; { *end*; }
 if *CurWord.Kind* = *sy_When* **then**
 begin *ReadWord*;
 repeat *gItemPtr*↑.*ProcessLeftLocus*; *Accept*(*Identifier*, *paIdentExp3*);
 Accept(*sy_Equal*, *paEqualityExp1*); *gItemPtr*↑.*ProcessRightLocus*; *Accept*(*Identifier*, *paIdentExp3*);
 until \neg *Occurs*(*sy_Comma*);
 end;
 Semicolon; *Correctness*;
end;

1874. \langle Error codes for parser 1642 $\rangle + \equiv$
paWithExp = 390;

1875. Property registration.

\langle Parse definitions (parser.pas) 1835 $\rangle + \equiv$

```
procedure RegisterProperty;
  begin gBlockPtr↑.CreateItem(itPropertyRegistration);
  case PropertyKind(CurWord.Nr) of
    sySethood: begin ReadWord; Accept(sy_of, paOfExp); gItemPtr↑.StartSethoodProperties;
      TypeExpression; gItemPtr↑.FinishSethoodProperties; Justification;
    end;
  othercases begin SynErr(CurPos, paStillNotImplemented);
  end;
endcases;
Semicolon;
end;
```

1876. \langle Error codes for parser 1642 $\rangle + \equiv$
paStillNotImplemented = 400;

1877.

\langle Parse definitions (parser.pas) 1835 $\rangle + \equiv$

```
procedure RegistrationBlock;
  var DefPos: Position;
  begin gBlockPtr↑.CreateItem(itDefinition); gBlockPtr↑.CreateBlock(blRegistration);
  DefPos ← CurPos; ReadWord;
  while CurWord.Kind ≠ sy_End do
    begin StillCorrect ← true;
    case CurWord.Kind of
      sy_Cluster: RegisterCluster;
      sy_Reduce: Reduction;
      sy_Identify: Identification;
      sy_Property: RegisterProperty;
      sy_Begin, EOT, sy_Reserve, sy_Scheme, sy_Theorem, sy_Definition, sy_Registration, sy_Notation: break;
      Pragma: ProcessPragmas;
    othercases begin case CurWord.Kind of
      sy_Let: begin gBlockPtr↑.CreateItem(itLocDeclaration); ReadWord; FixedVariables; end;
      sy_Canceled: Canceled;
      sy_Case, sy_Suppose, sy_Per, sy_Hereby: UnexpectedItem;
    othercases PrivateItem;
    endcases;
    Semicolon;
  end;
endcases;
end;
KillBlock; AcceptEnd(DefPos);
end;
```

1878. Reservation.

⟨ Parse definitions (parser.pas) 1835 ⟩ +≡

```
procedure Reservation;
  begin gBlockPtr↑.CreateItem(itReservation); ReadWord;
  repeat gItemPtr↑.StartReservationSegment;
    repeat gItemPtr↑.ProcessReservedIdentifier; Accept(Identifier, paIdentExp11);
    until ¬Occurs(sy_Comma);
    Accept(sy_For, paForExp); gItemPtr↑.CreateExpression(exResType); TypeSubexpression;
    KillExpression; gItemPtr↑.FinishReservationSegment;
  until ¬Occurs(sy_Comma);
  gItemPtr↑.FinishReservation;
end;
```

1879. ⟨ Error codes for parser 1642 ⟩ +≡

paIdentExp11 = 300;

1880. Theorem.

⟨ Parse definitions (parser.pas) 1835 ⟩ +≡

```
procedure Theorem;
  begin gBlockPtr↑.CreateItem(itTheorem); ReadWord; ProcessLab; gItemPtr↑.StartTheoremBody;
  ProcessSentence; gItemPtr↑.FinishTheoremBody; Justification; gItemPtr↑.FinishTheorem;
end;
```

1881. Axiom.

⟨ Parse definitions (parser.pas) 1835 ⟩ +≡

```
procedure Axiom;
  begin gBlockPtr↑.CreateItem(itAxiom); ReadWord; ProcessLab; gItemPtr↑.StartTheoremBody;
  ProcessSentence; gItemPtr↑.FinishTheoremBody; gItemPtr↑.FinishTheorem;
end;
```

Section 24.8. SCHEME BLOCKS

1882.

⟨ Parse scheme block (parser.pas) 1882 ⟩ ≡
 { Main (with Schemes) }

procedure SchemeBlock;

```

var SchemePos: Position;
begin gBlockPtr↑.CreateItem(itSchemeBlock); gBlockPtr↑.CreateBlock(blPublicScheme); ReadWord;
gBlockPtr↑.CreateItem(itSchemeHead); gItemPtr↑.ProcessSchemeName; SchemePos ← PrevPos;
if CurWord.Kind = Identifier then ReadWord;
⟨ Parse scheme parameters 1884 ⟩;
Accept(sy_RightCurlyBracket, paRightCurledExp3); gItemPtr↑.FinishSchemeHeading;
Accept(sy_Colon, paColonExp3); FormulaExpression; { Scheme-conclusion }
gItemPtr↑.FinishSchemeThesis; ⟨ Parse scheme premises 1886 ⟩;
gItemPtr↑.FinishSchemeDeclaration; ⟨ Parse justification for scheme 1887 ⟩;
KillBlock;
end;
```

This code is used in section 1640.

1883. ⟨ Error codes for parser 1642 ⟩ +≡
 paRightCurledExp3 = 372; paColonExp3 = 384;

1884. ⟨ Parse scheme parameters 1884 ⟩ ≡
 Accept(sy_LeftCurlyBracket, paLeftCurledExp);
repeat gItemPtr↑.StartSchemeSegment;
 repeat gItemPtr↑.ProcessSchemeVariable; Accept(Identifier, paIdentExp13);
 until ¬Occurs(sy_Comma);
 gItemPtr↑.StartSchemeQualification;
 case CurWord.Kind **of**
 sy_LeftSquareBracket: **begin** ReadWord; ReadTypeList; gItemPtr↑.FinishSchemeQualification;
 Accept(sy_RightSquareBracket, paRightSquareExp5);
 end;
 sy_LeftParanthesis: **begin** ReadWord; ReadTypeList; gItemPtr↑.FinishSchemeQualification;
 Accept(sy_RightParanthesis, paRightParenthExp9); Specification;
 end;
 othercases begin ErrImm(paWrongSchemeVarQual); gItemPtr↑.FinishSchemeQualification;
 Specification;
 end;
 endcases; gItemPtr↑.FinishSchemeSegment;
until ¬Occurs(sy_Comma)

This code is used in section 1882.

1885. ⟨ Error codes for parser 1642 ⟩ +≡
 paIdentExp13 = 300; paLeftCurledExp = 362; paWrongSchemeVarQual = 364;
 paRightParenthExp9 = 370; paRightSquareExp5 = 371;

1886. ⟨ Parse scheme premises 1886 ⟩ ≡
if CurWord.Kind = sy_Provided **then**
 repeat gItemPtr↑.StartSchemePremise; ReadWord; ProcessLab; ProcessSentence;
 gItemPtr↑.FinishSchemePremise;
 until CurWord.Kind ≠ sy_And

This code is used in section 1882.

```

1887.  ⟨ Parse justification for scheme 1887 ⟩ ≡
  if CurWord.Kind = sy_Proof then
    begin KillItem; { only KillItem which is run outside of Semicolon procedure }
    if  $\neg$ ProofPragma then
      begin gBlockPtr↑.StartSchemeDemonstration; IgnoreProof;
      gBlockPtr↑.FinishSchemeDemonstration;
      end
    else begin StillCorrect  $\leftarrow$  true; Accept(sy_Proof, paProofExp);
      gBlockPtr↑.StartSchemeDemonstration; LinearReasoning;
      if CurWord.Kind = sy_Per then NonBlockReasoning;
      AcceptEnd(SchemePos); gBlockPtr↑.FinishSchemeDemonstration;
      end;
    end
  else begin Semicolon;
    if  $\neg$ ProofPragma then
      begin gBlockPtr↑.StartSchemeDemonstration; IgnoreProof;
      gBlockPtr↑.FinishSchemeDemonstration;
      end
    else begin StillCorrect  $\leftarrow$  true;
      if CurWord.Kind = sy_Proof then
        begin WrongWord(paProofExp); StillCorrect  $\leftarrow$  true; ReadWord;
        end;
        gBlockPtr↑.StartSchemeDemonstration; LinearReasoning;
        if CurWord.Kind = sy_Per then NonBlockReasoning;
        AcceptEnd(SchemePos); gBlockPtr↑.FinishSchemeDemonstration;
        end;
      end
    end
  end

```

This code is used in section 1882.

Section 24.9. MAIN PARSE PROCEDURE

1888. The main *Parse* method essentially skips ahead to the first “**begin**”, then skips ahead to the first top-level block statement.

```

define skip_to_begin  $\equiv$  ReadTokenProc;
      while (CurWord.Kind  $\neq$  sy_Begin)  $\wedge$  (CurWord.Kind  $\neq$  EOT) do ReadTokenProc
 $\langle$  Main parse method (parser.pas) 1888  $\rangle \equiv$ 
procedure Parse;
  begin skip_to_begin; { Skips ahead until EOT or finds ‘begin’ }
  if CurWord.Kind = EOT then ErrImm(213)
  else  $\langle$  Parse proper text 1889  $\rangle$ ; { CurWord.Kind = sy_Begin }
  KillBlock;
  end;

```

This code is used in section 1640.

1889. Parsing the “text proper” checks that we have encountered a “**begin**” keyword, then parses the block statements in the article’s contents.

Note that *ProcessBegin* (§1361) and *StartProperText* (§1363) are both implemented in the extended block class.

```

[[The 213 magic number should be made a constant, something like paBegExpected?]]
 $\langle$  Parse proper text 1889  $\rangle \equiv$ 
  begin gBlockPtr $\uparrow$ .StartProperText; gBlockPtr $\uparrow$ .ProcessBegin; Accept(sy_Begin, 213);
  while CurWord.Kind  $\neq$  EOT do  $\langle$  Parse next block 1890  $\rangle$ ;
  end

```

This code is used in section 1888.

1890. When parsing the next top-level block in a Mizar article, we tell Mizar’s Parser we are not in “panic mode”. Then we test for unexpected “end” tokens. If we can recover a “begin” token, just start the loop over again.

If we encounter an “end of text” token, then we should terminate the loop.

Otherwise, we dispatch the Parser’s control depending on the kind of token we encounter.

```

⟨ Parse next block 1890 ⟩ ≡
  begin ⟨ Parse pragmas and begins 1891 ⟩;
  StillCorrect ← true; { we are not in panic mode }
  if CurWord.Kind = sy_End then
    begin ⟨ Skip all end tokens, report errors 1892 ⟩;
    if CurWord.Kind = sy_Begin then continue;
    end;
  if CurWord.Kind = EOT then break;
  case CurWord.Kind of
    sy_Scheme: SchemeBlock;
    sy_Definition: DefinitionalBlock;
    sy_Notation: NotationBlock;
    sy_Registration: RegistrationBlock;
    sy_Reserve: Reservation;
    sy_Theorem: Theorem;
    sy_Axiom: Axiom;
    sy_Canceled: Canceled;
    sy_Case, sy_Suppose, sy_Per, sy_Hereby: UnexpectedItem;
  othercases PrivateItem;
  endcases;
  Semicolon; { block is expected to end in a semicolon }
end

```

This code is used in section 1889.

1891. The *ProcessPragmas* (§1782) consumes a token when the current token is a pragma. So we effectively have a loop where we consume all the pragmas and the “begin” keywords until we find something else.

```

⟨ Parse pragmas and begins 1891 ⟩ ≡
  while CurWord.Kind ∈ [sy_Begin, Pragma] do
    begin ProcessPragmas;
    if CurWord.Kind = sy_Begin then
      begin gBlockPtr↑.ProcessBegin; ReadTokenProc;
      end;
    end
  end

```

This code is used in section 1890.

1892. In the unfortunate event that the Parser has stumbled across an “end” token, skip all the “end” and semicolon tokens and report errors.

```

⟨ Skip all end tokens, report errors 1892 ⟩ ≡
  repeat ErrImm(216); ReadTokenProc;
  if CurWord.Kind = sy_Semicolon then ReadTokenProc;
  until CurWord.Kind ≠ sy_End

```

This code is used in section 1890.

1893. Index. Underlined entries in an index item refers to which section defines the identifier. Primitive types (*char*, *Boolean*, *string*, etc.) are omitted from the index.

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Mizar Parser

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