

Chapter 0

Introduction

1. We are trying to understand Mizar. So I am transcribing the source code into a literate program, following the order of compilation. Perhaps this “goes against the spirit” of literate programming, but it makes the most sense to understand what is going on for programmers.

We will begin with the `esmprocessor.pas` file, and all the dependencies needed to compile it. For clarity (or at least ease of reference) each “section” appearing in the table of contents corresponds to a different file.

This discusses Mizar’s source code as of Git commit `9e814a9568cfb44253d677e5209c360390fe6437` (dated 2023 October 11).

2. **Files are chapters.** We will organize the text by compiler dependencies. It makes sense to treat each file as a separate “chapter”. With the exception of this introductory chapter (“chapter 0”), all future chapters are called “File n ”.

Just as Knuth’s *T_EX: The Program* (Addison–Wesley, 1986) was organized into modules which are presented “bottom-up”, each module is discussed and programmed “top-down”, we shall try to do likewise. File $n + 1$ can only depend on code appearing in Files 1 through File n .

There are natural ways to “cluster” the discussion in each File, which motivates the “section” and “subsections”. Each section (*but not subsections!*) starts on a new page, written in sans serif bold prefixed with explicit an “Section”. Subsections are written in sans serif bold prefixed with an explicit “Subsection”, with vertical whitespace separating it. This chapter has two sections (one discussing the flow of Mizar, and the other enumerating observations and “to do” items).

3. Each chapter is written using numbered paragraphs, since we are using Donald Knuth’s **WEB** to write a literate program. References will be made to the paragraphs. Index entries give the paragraph numbers associated with each entry. And even though I just used the term “paragraph number”, they really group several paragraphs into a unit of writing.

Numbers are paragraphed *independently* of chapter, section, subsection. This is a quirk of **WEB**. This was how Mathematicians wrote texts back in Euler’s day. We will refer to a paragraph by writing (§ n) to refer to paragraph n . Again, this was the conventions used by Euler.

Each paragraph consists of three parts: the “text part” (informal prose written in English), the “macros part” (which introduces macros written in the **WEB** language), and the “code part” (which contains a pretty-printed snippet of PASCAL code). A paragraph may omit any of these parts. Thus far, all our numbered paragraphs have consisted of “text parts” only. The “code part” can have a name in angled brackets. If the name is missing, then it continues the previous chunk of code from the previous numbered paragraph.

4. The Mizar program is released under the GNU license. So let us place this license in one place early on.

⟨GNU License 4⟩ ≡

{ This file is part of the Mizar system. Copyright (c) Association of Mizar Users. License terms: GNU General Public License Version 3 or any later version. }

This code is used in sections 23, 54, 77, 83, 89, 102, 115, 128, 182, 462, 463, 485, 487, 514, 554, 588, 647, 681, 719, 735, 850, 1193, 1199, and 1492.

5. Aside: Typography of “Modern” Pascal. We will be following the typographical style as found in Niklaus Wirth’s *Algorithms + Data Structures = Programs* (Prentice–Hall, 1975) and Donald Knuth’s *T_EX: The Program* (Addison–Wesley, 1986). But there are a few typographical situations which requires thinking hard about, since “classical” PASCAL does not have *object* or inheritance (or *unit* modules).

First, we need to know that “modern PASCAL” differs from the PASCAL Knuth worked with, in several ways. Mizar uses “units” which are modules. We will need to format them for **WEAVE**. Note that §42 of **WEAVE** introduces the “ilk” of various syntactic classes (array-like, case-like, for-like, etc.) and §64 of **WEAVE** explicitly initializes all the reserved words for PASCAL.

The reserved words which **WEAVE** highlights and/or pretty prints: **and**, **array**, **begin**, **case**, **const**, **div**, **do**, **downto**, **else**, **end**, **file**, **for**, **function**, **goto**, **if**, **in**, **label**, **mod**, **nil**, **not**, **of**, **or**, **packed**, **procedure**, **program**, **record**, **repeat**, **set**, **then**, **to**, **type**, **until**, **var**, **while**, **with**, **xclause**. These are then grouped into 20 “ilk” classes (see §42 of **WEAVE**).

Documentation and tutorials frequently compare **unit** to **program**, so we should probably typeset it as such. The big question is whether the **interface**, **implementation**, and **uses** keywords are **var**-like or **const**-like. I ultimately decided for the latter.

We will treat **implementation** typographically *as if* it were a **const** because the **end** will not be indented properly otherwise.

```
format unit ≡ program
format interface ≡ const
format implementation ≡ const
format uses ≡ const
```

6. Objects appear in Free PASCAL, and they behave like records. There are also **constructor** and **destructor** functions.

```
format object ≡ record
format constructor ≡ function
format destructor ≡ function
```

7. Primitive functions. We have several primitive functions which should be formatted especially. For example, **shr** is an infix operator like **mod** or **div**. It corresponds to bitwise shifting right.

```
format shr ≡ div
```

8. Cases. Following Knuth’s “T_EX: The Program” (§4), we will use **endcases** to pair with **case**. The “default case” will be **othercases** (because **else** gets too confusing).

```
define othercases ≡ others: { default for cases not listed explicitly }
define endcases ≡ end { follows the default case in an extended case statement }
format othercases ≡ else
format endcases ≡ end
```

9. Debugging. There are conditional compiler directives for debugging purposes. Importantly, these *must* be printed to the source code when we invoke **TANGLE**.

```
define mdebug ≡ @{@&$IFDEF MDEBUG@}
define end_mdebug ≡ @{@&$ENDIF@}
format mdebug ≡ begin
format end_mdebug ≡ end
```

10. Actually, it may be useful just to have helper macros.

```

define if_def(#) ≡ @{@&$IFDEF#@}
define if_not_def(#) ≡ @{@&$IFNDEF#@}
define else_if_def(#) ≡ @{@&$ELSEIF DEFINED(#}@}
define else_def ≡ @{@&$ELSE@}
define endif ≡ @{@&$ENDIF@}
define end_if ≡ endif
format if_def ≡ if
format if_not_def ≡ if
format else_if_def ≡ else
format else_def ≡ else
format endif ≡ end
format end_if ≡ end

```

11. **Toggling IO Checking.** Another compiler directive enables and disables IO checking

```

define disable_io_checking ≡ @{@&$I-@}
define enable_io_checking ≡ @{@&$I+@}
define without_io_checking(#) ≡ disable_io_checking; #; enable_io_checking

```

12. **References.** I have inline citations to the literature, but there’s some references worth explicitly drawing the reader’s attention to (which may or may not make it to an inline citation):

- (1) Andrzej Trybulec, “Some Features of the Mizar Language”, ESPRIT Workshop, Torino, 1993.
Eprint: mizar.uwb.edu.pl/project/trybulec93.pdf — §4 discusses grammatical aspects of Mizar
- (2) Freek Wiedijk, “Mizar’s Soft Type System”. In K. Schneider and J. Brandt, eds., *Theorem Proving in Higher Order Logics. TPHOLs 2007*, Springer, doi:10.1007/978-3-540-74591-4_28 (Eprint pdf).
- (3) Adam Grabowski, Artur Kornilowicz, and Adam Naumowicz’s “Mizar in a Nutshell”
(doi:10.6092/issn.1972-5787/1980)
- (4) Artur Kornilowicz’s “Registrations vs Redefinitions in Mizar” (in A. Kohlhase, P. Libbrecht, BR. Miller, A. Naumowicz, W. Neuper, P. Quaresma, F. Wm. Tompa, M. Suda (eds) *Joint Proc. FMM, MathUI, and ThEdu*, 2016, pp.17–20, ceur-ws.org/Vol-1785/F5.pdf)
- (5) Artur Kornilowicz’s “On rewriting rules in Mizar” (*J. Autom. Reason.* 50 no.2 (2013) 203–210, doi:10.1007/s10817-012-9261-6)
- (6) Mario Carneiro, “Reimplementing Mizar in Rust”. Eprint [arXiv:2304.08391](https://arxiv.org/abs/2304.08391), see especially the first two sections for an overview of Mizar’s workflow. (The code is available at github.com/digama0/mizar-rs.)

I should also credit Wayne Sewell’s *Weaving a Program: Literate Programming in Web* (Van Nostrand Reinhold Computer, 1989) for discussing how to take a pre-existing PASCAL program and turn it into a WEB. Or, depending on the quality of writing in this literate program, it’s all his fault.

Section 0.1. MIZAR'S WORKFLOW

13. This section will give a brief overview of what Mizar “does” when we run it. The analogy to bear in mind is with a batch compiler: there’s parsing, some intermediate steps, then emits some output.

Just to give some rough estimates of where Mizar spends most of its time, there are four phases Mizar reports when checking an article:

- (1) Parser (transforms input into an abstract syntax tree, writes it to an XML file);
- (2) MSM (transforms the abstract syntax tree into an explicitly typed intermediate representation) — `base/first_identification.pas`, the *MSMAnalyzer* procedure; this will require transcribing `kernel/limits.pas` (which is mostly just a bunch of constant parameters);
- (3) Analyzer (performs type checking, tracks the goals, and other miscellaneous jobs) — the *Analyze* procedure in `kernel/analyzer.pas`; this requires transcribing kernel code (`lexicon.pas`, `inout.pas`, `iocorrel.pas`, `correl.pas`, `generato.pas`, `builtin.pas`, `justhan.pas`, `enums.pas`, `formats.pas`, `identify.pas`) and base code (`xmldict.pas`), approximately 19590 lines (16764 lines of code, the rest is whitespace and comments)
- (4) Checker (performs the proof checking for validity) — the *InferenceChecker* procedure in `kernel/checker.pas`. This requires transcribing kernel files (`checker.pas` `prechecker.pas` `equalizer.pas` `unifier.pas` `justhan.pas`), approximately 8191 lines of code.

Using numbers Mario Carneiro reported in his github repository, roughly 14/15 of Mizar’s runtime (as measured in CPU time) is spent on the Analyzer and Checker phases (among which, Mizar spends about 5 times longer in the Checker phase than the Analyzer phase). Parsing and MSM transforms the input into an intermediate representation used in the latter two phases. Mizar spends about 1/15 of its time here.

14. Accommodator. This will produce, among other outputs, the “.dct” file (and its XML counterpart, the “.dcx” file). The “.dct” file contains all the identifiers imported from other articles and reserved keywords for Mizar. The Tokeniser needs it to properly tokenise an article.

15. Parsing phase. We can look at `kernel/verfinit.pas` to find the parsing phase of the Mizar program is handled by the following lines of code:

```
InitPass(`ParserUU`); FileExam(EnvFileName + `.dct`);
InitScanning(MizFileName + ArticleExt, EnvFileName); InitWSMizarArticle; Parse;
gFormatsColl.StoreFormats(EnvFileName + `.frx`); gFormatsColl.Done; FinishScanning;
Write_WSMizArticle(gWSTextProper, EnvFileName + `.wsx`);
```

Our goal is to examine these functions, and understand what is going on. We know *Parse* is defined in `base/parse.pas`, it populates the *gWSTextProper* global variable using `base/parseraddition.pas`, and *Write_WSMizArticle* is defined in `base/wsmarticle.pas`. The *Parse* function continuously invokes *ReadToken* (§726).

This phase will be responsible for generating a “.frx” (formats XML) and a “.wsx” (weakly strict Mizar XML) file.

Section 0.2. LOG OF TODOS, BUGS, IMPROVEMENTS

16. I have a number of observations from transcribing Mizar into WEB. They're the last thing I have included in the introductory chapter.

17. Possible improvements.

- (1) In quicksort, picking the pivot is done by $P \leftarrow (Low + High)/2$, but it should be done by $P \leftarrow Low + ((High - Low)/2)$ to avoid overflow.
- (2) Actually, quicksort should delegate work to a different sorting algorithm when there is less than 10 items in the list. Sedgewick pointed this out in his PhD thesis. (If quicksort *were* a culprit for slowness, we could even hardcode sort networks for small lists.)
- (3) We should also determine the pivot by looking at the median value of $P = (3 * Low + High)/4$, $P2 \leftarrow (Low + High)/2$, $P3 \leftarrow (Low + 3 * High)/4$. This will improve the performance of quicksort.
- (4) In §152, *GCD* could be optimized to avoid calculating $Mul(i, i)$ in every loop iteration.
- (5) In §326, *MStringList.ObjectOf* has duplicate code.
- (6) It seems that parsing Mizar text, emitting XML, and parsing XML seem to contain a lot of code which could be autogenerated from a grammar (a hypothetical “.ebnf” file). This would avoid duplicate work.

18. Possible bugs. I have been working through the source code with the mindset of, “How can I possibly break this?” This has led me to identify a number of situations where things can “go badly”. But they are not all bugs (some are impossible to occur).

- (1) In §168, *RationalGT* is either misnamed (should be *RationalGEQ*) or implemented incorrectly (we should have $RationalGT(a, b) = RationalLT(b, a)$ but do not)
- (2) In §171 *IsRationalGT* is misnamed (should be *IsRationalGEQ*)
- (3) In §272, *MSortedExtList.FindInterval* appears to assume that *MSortedExtList.Find* returns the left-most index.
- (4) In §293, *MSortedCollection.Search* may not return the correct index when there are duplicates. This is not terrible, since *IndexOf* corrects for this possibility.
- (5) In §527, I think *TXTStreamObj.Done* needs to close the associated file.
- (6) In §563, *TSymbol.Init* expects an *fInfinite* argument, but does not use it — shouldn’t it initialize $Infinite \leftarrow fInfinite$?
- (7) In §501, escaped quotation marks are not properly handled.
- (8) For *StreamObj* (§520), the constructors and destructors are not virtual which would impact *XMLOutStreamObj* (§533) — well, we just do duplicate work in *XMLOutStreamObj*’s constructors and destructors.
- (9) Shouldn’t *TokensCollection.InitTokens* (§594) invoke the inherited constructor?
- (10) Shouldn’t *MTokenObj.Init* (§602) invoke inherited constructors? At least to insulate itself from changes to any of its parent (or grandparent) classes?
- (11) The constructor *OutWSMizFileObj.OpenFileWithXSL* (§1015) expects the XML-stylesheet located at `"file:///'+$MIZFILES+'wsmiz.xml"`, but that file is not present in Mizar.
- (12) In *extItemObj.FinishFunctorPattern* (§1323), the default case does not add a new format to the *gFormatsColl* dictionary.
- (13) In *CreateArgs* (§1393) in `parseraddition.pas`, when $aBase \leq 0$, this will set *TermNbr* to a negative number.
- (14) In the *Subexpression* class, there is duplicate code (§1397) — the *CompleteAttributeArguments* and *FinishAttributeArguments* are identical, but only the latter is consistent with the naming conventions for the parser. Or (probably more likely) I am misunderstanding the naming conventions?
- (15) In *CompleteArgument* (§1518), we should also test that *fParenthCnt* is positive, shouldn’t we?
- (16) The *CreateSubexpression* method (§1491), for extended expression objects, may result in a memory leak when *gSubexpPtr* $\neq \mathbf{nil}$ — that is to say, if *KillSubexpression* has not been invoked prior to *CreateSubexpression*.
- (17) Misnamed variable: *gIdentifyEqLociList* should be *gIdentifyEqLociList* (i.e., “identify” should be “identify” — with a ‘t’). (This typo has been corrected in the literate presentation of the code.)
- (18) As discussed in (§1286), there is a mismatch between the documentation and the parser when it comes to parsing loci declarations in a definition block. The `syntax.txt` file is more restrictive than the parser, and should be updated to reflect the parser.
- (19) The *gSuchThat* global variable is never used anywhere (§1292)

19. To do list. There are some things I should revisit, revise, and edit — specifically about this running commentary (*not* the Mizar source code).

- (1) [Missing transcription] I skipped over transcribing the *ItemName* and other constants from `wsmarticle.pas`, which I should probably include.
- (2) [Revise] The XML schema should use the `doc/mizar/xml/Mizar.rnc` schema snippets.
- (3) [Revise] Make an introduction to dynamic arrays as a data structure, just to standardize the terminology used. (Make sure I stick to the standardized terminology!) Including pictures may help...
- (4) [Revise] Review quicksort. I should prove that it works, too. (Has this been done in Mizar? `exchsort` seems to be the closest match.)
- (5) [Improve] Give a “big picture” summary of the architecture. For example, the most interesting routine in parsing Mizar, well, it’s all handled in *MTokenizer.SliceIt* (§612).
- (6) [Linting] Standardize the names of basic data types. PASCAL accepts *integer* as synonymous with *Integer*, but they give different index entries.
- (7) [Cosmetics] Check the typography is correct for the code
- (8) [Cosmetics] Create more `WEB` macros for conditional compilation
- (9) [Cosmetics] Would it help to include more UML class diagrams?
- (10) [Improve] It may be useful to use UML State diagrams to explain the parser — or it may be a huge distraction?

20. Formatting types. This is still a finicky aspect of `WEB`. Strings are a type in Free PASCAL, like *Boolean*.

Looking at Wirth’s book, he typesets a type in *italics* and lowercase — so we have *boolean* and not **boolean** or *Boolean* (or **Boolean** or **boolean** or...). Knuth’s “`TEX`: the program” follows this convention (using *integer*, *boolean*, *char*, etc.).

21. Using Twill (or not). Knuth invented Twill as a “hack” atop `WEAVE` to include “mini-indices” every couple pages. The problem I have with Twill is that it does not adequately index local variables (in the sense that: Knuth’s `TEX` is a giant monolithic program, and any **var** appearing in it is almost certainly a global variable — hence it makes sense to index *all* variables, since they are almost certainly global).

I *want* to use Twill, but it is designed specifically *for* Knuth. Consequently it is not terribly useful for our purposes. We would have to tailor it quite heavily, and I don’t have the energy or patience to do so.

22. Caution: Knuth takes advantage of `WEB` to use `snake_case` when naming things instead of Pascal’s idiomatic `PascalCase`. This probably greatly improves the readability of the code. We should probably think hard about using it.

When `WEAVE` extracts the PASCAL code, it will remove all underscores from the identifiers and capitalize all letters. So instead of “*screaming_run_on_case*” (which appears in the PDF), we will instead obtain “`SCREAMINGRUNONCASE`”, which... yeah, that’s a hot mess.

File 1

Mizar environment

23. We will need some basic library of functions. For example, trimming whitespace from a String.

```

< mizenv.pas 23 > ≡
  < GNU License 4 >
unit mizenv;
  interface
    < interface for mizenv.pas 24 >
  implementation
    < Modules used by mizenv.pas 25 >
    < implementation of mizenv.pas 26 >
end .

```

24. The interface contains all the variables for the unit, and the public facing functions and procedures.

```

< interface for mizenv.pas 24 > ≡
var MizFileName, EnvFileName, ArticleName, ArticleID, ArticleExt: String;
procedure SetStringLength(var aString : String; aLength : integer);

```

See also sections 27, 30, and 34.

This code is used in section 23.

25. The implementation begins with various “uses”.

```

< Modules used by mizenv.pas 25 > ≡
uses { compiler dependent imports }
  if_def (DELPHI) IOUtils, SysUtils, windows, endif
  if_def (FPC) dos, SysUtils, endif
  mconsole; { the only Mizar module mizenv.pas uses }

```

This code is used in section 23.

26. As far as setting the String length, this is a straightforward implementation. When the desired *aLength* is less than the actual length of *aString*, simply delete all characters after *aLength*.

Otherwise, *aString* has fewer characters than desired, so we pad it on the right with however many spaces until the String is as long as *aLength*.

```

< implementation of mizenv.pas 26 > ≡
procedure SetStringLength(var aString : String; aLength : integer);
  var I, L: integer;
  begin L ← length(aString);
  if aLength ≤ L then Delete(aString, aLength + 1, L - aLength)
  else for I ← 1 to aLength - L do aString ← aString + '␣';
  end;

```

See also sections 28, 31, 35, and 46.

This code is used in section 23.

27. We have publicly available functions trimming whitespace from functions.

```

⟨ interface for mizenv.pas 24 ⟩ +≡
function TrimStringLeft(aString : String): String;
function TrimStringRight(aString : String): String;
function TrimString(const aString: String): String;

```

28. Trimming the left String will repeatedly delete any leading whitespace, until the String is empty or has no leading whitespace.

Similarly, trimming the right String will repeatedly delete the *last* character until it is no longer whitespace (or until the String becomes empty).

```

⟨ implementation of mizenv.pas 26 ⟩ +≡
function TrimStringLeft(aString : String): String;
  begin while (length(aString) > 0) ∧ (aString[1] = '␣') do Delete(aString, 1, 1);
  TrimStringLeft ← aString;
end;

function TrimStringRight(aString : String): String;
  begin while (length(aString) > 0) ∧ (aString[length(aString)] = '␣') do
    Delete(aString, length(aString), 1);
  TrimStringRight ← aString;
end;

```

29. Trimming a String amounts to trimming it on the left and right.

```

function TrimString(const aString: String): String;
  begin TrimString ← TrimStringRight(TrimStringLeft(aString));
end;

```

30. We have a few more String manipulation functions for changing case, and turning an integer into a String.

```

⟨ interface for mizenv.pas 24 ⟩ +≡
function UpperCase(const aStr: String): String;
function MizLoCase(aChar : char): char;
function LowerCase(const aStr: String): String;
function IntToStr(aInt : integer): String;

```

31. Now, uppercase letters.

```

⟨ implementation of mizenv.pas 26 ⟩ +≡
function UpperCase(const aStr: String): String;
  var k: integer; { index ranging over aStr }
  lStr: String; { the uppercased String being built and returned }
  begin lStr ← aStr;
  for k ← 1 to length(aStr) do lStr[k] ← UpCase(aStr[k]);
  UpperCase ← lStr;
end;

```

32. Lowercasing a String can be done by iteratively replacing each character with its lowercase version. This “lowercase a single character” function is precisely *MizLoCase*.

```
function MizLoCase(aChar : char): char;
  begin if aChar ∈ [‘A’ .. ‘Z’] then MizLoCase ← Chr(Ord(‘a’) + Ord(aChar) − Ord(‘A’))
  else MizLoCase ← aChar;
  end;

function LowerCase(const aStr: String): String;
  var i: integer; { index ranging over aStr’s length }
      lStr: String; { result being built up }
  begin lStr ← aStr;
  for i ← 1 to length(aStr) do lStr[i] ← MizLoCase(aStr[i]);
  LowerCase ← lStr;
  end;
```

33. We also want to convert an integer to a String.

```
function IntToStr(aInt : integer): String;
  var lStr: String;
  begin Str(aInt, lStr); IntToStr ← lStr;
  end;
```

34. File name manipulation. We will want to test if a file exists, or split a path (represented as a String) into a directory and a filename.

```
{ interface for mizenv.pas 24 } +≡
function MFileExists(const aFileName: String): boolean;
procedure EraseFile(const aFileName: String);
procedure RenameFile(const aName1, aName2: String);
function GetFileTime(aFileName : String): Longint;
procedure SplitFileName ( const aFileName: String;
                          var aDir, aName, aExt: String );
function TruncDir(const aFileName: String): String;
function TruncExt(const aFileName: String): String;
function ExtractFileDir(const aFileName: String): String;
function ExtractFileName(const aFileName: String): String;
function ExtractFileExt(const aFileName: String): String;
function ChangeFileExt(const aFileName, aFileExt: String): String;
```

35. Testing if a file exists uses the Free Pascal’s primitive *FileExists* function.

Similarly, *EraseFile* is just relying on Free Pascal’s *SysUtils.DeleteFile* function.

```
{ implementation of mizenv.pas 26 } +≡
function MFileExists(const aFileName: String): boolean;
  begin MFileExists ← FileExists(aFileName); end;
procedure EraseFile(const aFileName: String);
  begin SysUtils.DeleteFile(aFileName); end;
```

36. We will destructively rename a file. If a file with the name already exists, we delete it.

```
procedure RenameFile(const aName1, aName2: String);
  begin if MFileExists(aName1) then EraseFile(aName2);
  SysUtils.RenameFile(aName1, aName2);
  end;
```

37. Again, relying on Free Pascal's *FileAge* function.

```
function GetFileTime(aFileName : String): Longint;
begin GetFileTime  $\leftarrow$  FileAge(aFileName); end;
```

38. Split a file name into components, namely (1) the directory, (2) the file name, (3) its extension. For example, */path/to/my/file.exe* will be split into */path/to/my/*, *file*, and *exe*.

This implementation depends on the compiler used (Delphi or Free Pascal).

```
procedure SplitFileName ( const aFileName: String; { input }
                        var aDir, aName, aExt: String ); { output }

begin
if_def (FPC)
aDir  $\leftarrow$  SysUtils.ExtractFilePath(aFileName);
aName  $\leftarrow$  SysUtils.ExtractFileName(aFileName);
aExt  $\leftarrow$  SysUtils.ExtractFileExt(aFileName);
endif
if_def (DELPHI)
aDir  $\leftarrow$  TPath.GetDirectoryName(aFileName);
aName  $\leftarrow$  TPath.GetFileName(aFileName);
aExt  $\leftarrow$  TPath.GetExtension(aFileName);
endif
end ;
```

39. “Truncating a directory” means “throw away the directory part of the path” so we end up with just a filename and the file extension.

```
function TruncDir(const aFileName: String): String;
var Dir, lName, Ext: String;
begin SplitFileName(aFileName, Dir, lName, Ext); TruncDir  $\leftarrow$  lName + Ext;
end;
```

40. “Truncating the extension” means throwing away the extension part of a path.

```
function TruncExt(const aFileName: String): String;
var Dir, lName, Ext: String;
begin SplitFileName(aFileName, Dir, lName, Ext); TruncExt  $\leftarrow$  Dir + lName;
end;
```

41. Extracting the file directory will return *just* the directory part of a path.

```
function ExtractFileDir(const aFileName: String): String;
var Dir, lName, Ext: String;
begin SplitFileName(aFileName, Dir, lName, Ext); ExtractFileDir  $\leftarrow$  Dir;
end;
```

42. Extracting the file name will throw away both the directory and extension.

```
function ExtractFileName(const aFileName: String): String;
var Dir, lName, Ext: String;
begin SplitFileName(aFileName, Dir, lName, Ext); ExtractFileName  $\leftarrow$  lName;
end;
```

```
function ExtractFileExt(const aFileName: String): String;
var Dir, lName, Ext: String;
begin SplitFileName(aFileName, Dir, lName, Ext); ExtractFileExt  $\leftarrow$  Ext;
end;
```

43. Changing a file name's extension. See:

<https://www.freepascal.org/docs-html/rtl/sysutils/changefileext.html>

```
function ChangeFileExt(const aFileName, aFileExt: String): String;
begin ChangeFileExt  $\leftarrow$  SysUtils.ChangeFileExt(aFileName, aFileExt); end;
```

44. Getting an environmental variable.

```
function GetEnvStr(aEnvName : String): String;
if_def (FPC)
  begin GetEnvStr  $\leftarrow$  GetEnv(aEnvname); end;
endif
if_def (DELPHI)  $\langle$  Get environment variable, Delphi-compatible mode 45  $\rangle$ 
endif
```

45. The Delphi-compatible version of obtaining an environment variable is rather involved, so let us study it in silent meditation.

\langle Get environment variable, Delphi-compatible mode 45 $\rangle \equiv$

```
const cchBuffer = 255;
var lName, lpszTempPath: array [0 .. cchBuffer] of char;
  i: integer; lStr: String;
begin lStr  $\leftarrow$  '';
for i  $\leftarrow$  1 to length(aEnvname) do lName[i - 1]  $\leftarrow$  aEnvname[i];
lName[length(aEnvname)]  $\leftarrow$  #0;
if GetEnvironmentVariable(lName, lpszTempPath, cchBuffer) > 0 then
  begin for i  $\leftarrow$  0 to cchBuffer do
    begin if lpszTempPath[i] = #0 then break;
    lStr  $\leftarrow$  lStr + lpszTempPath[i];
    end;
  end;
GetEnvStr  $\leftarrow$  lStr;
end;
{ restored for DELPHI4 compatibility ;-( begin GetEnvStr:=GetEnvironmentVariable(aEnvname);
```

end; }

This code is used in section 44.

46. The *DrawMessage* and *DrawIOResult* are procedures in *mconsole.pas* (see §74, and §75).

\langle implementation of *mizenv.pas* 26 $\rangle + \equiv$

```
procedure FileExam(const aFileName: String);
var
  Source: file ;
  I: byte;
begin if aFileName = '' then
  begin DrawMessage('Can't open _miz_', ''); halt(1);
  end;
  FileMode  $\leftarrow$  0; Assign(Source, aFileName); without_io_checking(Reset(Source)); I  $\leftarrow$  ioresult;
if I  $\neq$  0 then DrawIOResult(aFileName, I);
  close(Source); FileMode  $\leftarrow$  2;
end;
```

47. We test if a file exists with the *EnvFileExam* procedure. It will notify the user if the file does not exist, otherwise it is silent.

Again, *DrawMessage* comes from `mconsole.pas` (§74).

```
procedure EnvFileExam(const aFileExt: String);
begin if  $\neg$ MFileExists(EnvFileName + aFileExt) then
  begin DrawMessage('Can't open' + EnvFileName + aFileExt + ' '); Halt(1);
  end;
end;
```

48. The *ParamCount* is PASCAL's way of counting the command-line parameters passed to the program.

```
procedure GetFileName(ParamNr : byte; DefaultExt : String; var aFileName : String);
var lFileExt: String;
begin if ParamNr  $\leq$  ParamCount then
  begin aFileName  $\leftarrow$  ParamStr(ParamNr); lFileExt  $\leftarrow$  ExtractFileExt(aFileName);
  if lFileExt = '' then aFileName  $\leftarrow$  ChangeFileExt(aFileName, DefaultExt);
  exit;
  end;
aFileName  $\leftarrow$  '';
end;
```

49. This procedure will take the *Nr* command line argument. If it lacks a file extension, then it will append the *DefaultExt* to it. At the end, this will populate *aFileName* and *aFileExt* based on the command line.

The *ParamStr*(*Nr*) returns the *Nr*th parameter as a *String* (it's a PASCAL primitive).

```
procedure GetFileExtName(Nr : byte; DefaultExt : String; var aFileName : String; var aFileExt : String);
begin if Nr  $\leq$  ParamCount then
  begin aFileName  $\leftarrow$  ParamStr(Nr); aFileExt  $\leftarrow$  ExtractFileExt(aFileName);
  if aFileExt = '' then aFileExt  $\leftarrow$  DefaultExt
  else aFileName  $\leftarrow$  ChangeFileExt(aFileName, '');
  exit;
  end;
aFileName  $\leftarrow$  ''; aFileExt  $\leftarrow$  '';
end;
```

50. We need to find the first command-line argument which resembles a Mizar article name. Note that Mizar articles have several files associated with it (the article's contents in a `.miz` file, the vocabulary in a `.voc` file, and XML related intermediate representation in `.xml` files, as well as `.evl` files).

Command line flags prefixed with a dash ("-") will not be interpreted as the name of a Mizar article.

```
procedure GetMizFileName(aFileExt : String);
var i: integer;
begin MizFileName  $\leftarrow$  ''; ArticleName  $\leftarrow$  ''; ArticleExt  $\leftarrow$  ''; EnvFileName  $\leftarrow$  '';
for i  $\leftarrow$  1 to ParamCount do
  if ParamStr(i)[1]  $\neq$  '-' then
    begin MizFileName  $\leftarrow$  ParamStr(i); GetFileExtName(i, aFileExt, MizFileName, ArticleExt);
    ArticleName  $\leftarrow$  ExtractFileName(MizFileName); ArticleID  $\leftarrow$  UpperCase(ArticleName);
    if  $\neg$ IsMMLIdentifier(ArticleName) then
      begin DrawMessage('Only letters, numbers and _ allowed in Mizar file names', '');
      halt(1);
      end;
    EnvFileName  $\leftarrow$  MizFileName; exit;
    end;
  end;
end;
```

```

procedure GetArticleName;
begin GetMizFileName('.miz');
end;

```

```

procedure GetEnvironName;
  var i, c: integer;
  begin if MizFileName = `` then GetArticleName;
    EnvFileName  $\leftarrow$  MizFileName; c  $\leftarrow$  0;
  for i  $\leftarrow$  1 to ParamCount do
    if (ParamStr(i)[1]  $\neq$  '-') then
      begin inc(c);
        if c = 2 then EnvFileName  $\leftarrow$  ParamStr(i);
      end;
    end;
  end;

```

[illegible]

File 2

Mizar Console

54. The Mizar Console unit is used for interacting with the command line.

```

< mconsole.pas 54 > ≡
  < GNU License 4 >
unit mconsole;
  interface < Interface for mconsole.pas 56 >
  implementation
    < Import units for mconsole.pas 55 >
    < Implementation for mconsole.pas 65 >
  end

```

55. We import two modules, *pcmizver* (which we have yet to see), and *mizenv* (which we have already introduced).

```

< Import units for mconsole.pas 55 > ≡
uses pcmizver, mizenv;

```

This code is used in section 54.

56. The interface contains the publicly available functions, as well as some specific variables for the state of the analyzer, etc.

```

< Interface for mconsole.pas 56 > ≡
  < Report results to command line 57 >
  < Constants for common error messages reported to console 60 >
  < Interface for accommodator command line options 61 >
  < Interface for MakeEnv command line options 62 >
  < Interface for transfer-specific command line options 63 >
  < Interface for other command line options 64 >

```

This code is used in section 54.

```

57. < Report results to command line 57 > ≡
procedure InitDisplayLine(const aComment: String);
procedure NoDisplayLine(fLine, fErrNbr : integer);
  < DisplayLine global constant 58 >
procedure DrawMizarScreen(const aApplicationName: String);
procedure DrawArticleName(const fName: String);
procedure DrawStr(const aStr: String);
procedure FinishDrawing;

```

See also section 59.

This code is used in section 56.

```

58. < DisplayLine global constant 58 > ≡
const DisplayLine: procedure (fLine, fErrNbr : integer) = NoDisplayLine;

```

This code is used in section 57.

59. Common routines for “drawing” output to the console.

```

⟨Report results to command line 57⟩ +≡
procedure EmptyParameterList;
procedure Noise;
procedure DrawPass(const aName: String);
procedure DrawTime(const aTime: String);
procedure DrawVerifierExit(const aTime: String);
procedure DrawMessage(const Msg1, Msg2: String);
procedure BugInProcessor;
procedure DrawIOResult(const FileName: String; I: byte);
procedure DrawErrorsMsg(aErrorNbr : integer);
procedure DisplayLineInCurPos(fLine, fErrNbr : integer);

```

60. We also have a constant for error messages commonly encountered.

```

⟨Constants for common error messages reported to console 60⟩ ≡
const ErrMsg: array [1..6] of String[20] =
  (‘’,
   ‘File_not_found’,
   ‘Path_not_found’,
   ‘Too_many_open_files’,
   ‘Disk_read_error’,
   ‘Disk_write_error’);

```

This code is used in section 56.

61. Now, we have accommodator specific options.

```

⟨Interface for accommodator command line options 61⟩ ≡
  { Accommodator specific options: }
var InsertHiddenFiles, VocabulariesProcessing, FormatsProcessing, NotationsProcessing, SignatureProcessing,
    ConstructorsProcessing, ClustersProcessing, IdentifyProcessing, ReductionProcessing,
    PropertiesProcessing, DefinitionsProcessing, EqualitiesProcessing, ExpansionsProcessing,
    TheoremsProcessing, SchemesProcessing, TheoremListsProcessing, SchemeListsProcessing: boolean;
procedure InitAccOptions;
procedure GetAccOptions;

```

This code is used in section 56.

```

62. ⟨Interface for MakeEnv command line options 62⟩ ≡
  { MakeEnv specific options: }
var Acomodation: boolean = false; NewAccom: boolean = false;
procedure GetMEOptions;

```

This code is used in section 56.

```

63. ⟨Interface for transfer-specific command line options 63⟩ ≡
  { Transfer specific options: }
var PublicLibr: boolean;
procedure GetTransfOptions;

```

This code is used in section 56.

64. \langle Interface for other command line options 64 $\rangle \equiv$
 $\{$ Other options: $\}$

```
var CtrlCPressed: boolean = false; LongLines: boolean = false; QuietMode: boolean = false;
  StopOnError: boolean = false; FinishingPass: boolean = false; ParserOnly: boolean = false;
  AnalyzerOnly: boolean = false; CheckerOnly: boolean = false; SwitchOffUnifier: boolean = false;
  AxiomsAllowed: boolean = false;
procedure GetOptions;
```

This code is used in section 56.

65. The implementation begins by initializing the Accommodator specific options.

\langle Implementation for mconsole.pas 65 $\rangle \equiv$

```
procedure InitAccOptions;
begin InsertHiddenFiles  $\leftarrow$  true; VocabulariesProcessing  $\leftarrow$  true; FormatsProcessing  $\leftarrow$  true;
  NotationsProcessing  $\leftarrow$  true; SignatureProcessing  $\leftarrow$  true; ConstructorsProcessing  $\leftarrow$  true;
  ClustersProcessing  $\leftarrow$  true; IdentifyProcessing  $\leftarrow$  true; ReductionProcessing  $\leftarrow$  true;
  PropertiesProcessing  $\leftarrow$  true; DefinitionsProcessing  $\leftarrow$  true; EqualitiesProcessing  $\leftarrow$  true;
  ExpansionsProcessing  $\leftarrow$  true; TheoremsProcessing  $\leftarrow$  true; SchemesProcessing  $\leftarrow$  true;
  TheoremListsProcessing  $\leftarrow$  false; SchemeListsProcessing  $\leftarrow$  false;
end;
```

This code is used in section 54.

66. Similarly, we want to be able to *reset* the configuration for the accommodator to the default (initial) values.

```
procedure ResetAccOptions;
begin InsertHiddenFiles  $\leftarrow$  true; VocabulariesProcessing  $\leftarrow$  false; FormatsProcessing  $\leftarrow$  false;
  NotationsProcessing  $\leftarrow$  false; SignatureProcessing  $\leftarrow$  false; ConstructorsProcessing  $\leftarrow$  false;
  ClustersProcessing  $\leftarrow$  false; IdentifyProcessing  $\leftarrow$  false; ReductionProcessing  $\leftarrow$  false;
  PropertiesProcessing  $\leftarrow$  false; DefinitionsProcessing  $\leftarrow$  false; EqualitiesProcessing  $\leftarrow$  false;
  ExpansionsProcessing  $\leftarrow$  false; TheoremsProcessing  $\leftarrow$  false; SchemesProcessing  $\leftarrow$  false;
  TheoremListsProcessing  $\leftarrow$  false; SchemeListsProcessing  $\leftarrow$  false;
end;
```

67. Accommodator options. We will get options for the accommodator passed in from the command line. Broadly, these are:

- **-v** resets the accommodator options, and then toggles *VocabulariesProcessing* to true
- **-f**, **-p** resets the accommodator options, and then toggles *VocabulariesProcessing* to true (so far like **-v**), and then toggles *FormatsProcessing* to true.
- **-P** resets the accommodator options, and then toggles *VocabulariesProcessing* to true (so far like **-v**), and then toggles *FormatsProcessing* to true (so far like **-f** and **-p**), then toggles *TheoremListsProcessing* and *SchemeListsProcessing* to both be true.
- **-e** will do everything **-f** does, and then toggles *ConstructorsProcessing*, *SignatureProcessing*, *ClustersProcessing*, and *NotationsProcessing* to all be true.
- **-h** will set *InsertHiddenFalse* to false (presumably preventing Mizar from loading the “hidden” article, i.e., the primitive notions of **object**, **set**, **in**, **=**, and inequality will not be loaded).
- **-l** will toggle *LongLines* to true (allowing lines with more than 80 characters)
- **-q** will toggle *QuietMode* to true
- **-s** will toggle *StopOnError* to true

Note this processes *all* command line options *in order*. So **-e -v** will produce the same results as **-v** alone.

```

procedure GetAccOptions;
  var i, j: integer;
  begin InitAccOptions;
  for j  $\leftarrow$  1 to ParamCount do
    if ParamStr(j)[1] = '-' then
      for i  $\leftarrow$  2 to length(ParamStr(j)) do
        case ParamStr(j)[i] of
          'v': begin ResetAccOptions; VocabulariesProcessing  $\leftarrow$  true
            end;
          'f', 'p': begin ResetAccOptions; VocabulariesProcessing  $\leftarrow$  true; FormatsProcessing  $\leftarrow$  true;
            end;
          'P': begin ResetAccOptions; VocabulariesProcessing  $\leftarrow$  true; FormatsProcessing  $\leftarrow$  true;
            TheoremListsProcessing  $\leftarrow$  true; SchemeListsProcessing  $\leftarrow$  true;
            end;
          'e': begin ResetAccOptions; VocabulariesProcessing  $\leftarrow$  true; FormatsProcessing  $\leftarrow$  true;
            ConstructorsProcessing  $\leftarrow$  true; SignatureProcessing  $\leftarrow$  true; ClustersProcessing  $\leftarrow$  true;
            NotationsProcessing  $\leftarrow$  true;
            end;
          'h': begin InsertHiddenFiles  $\leftarrow$  false; end;
          'l': LongLines  $\leftarrow$  true;
          'q': QuietMode  $\leftarrow$  true;
          's': StopOnError  $\leftarrow$  true;
        endcases;
      end;
    end;
  end;

```

68. Similarly, we have *MakeEnv* specific options parsed from the command line flags.

```

procedure GetMEOptions;
  var i, j: integer;
  begin for j  $\leftarrow$  1 to ParamCount do
    if ParamStr(j)[1] = '-' then
      for i  $\leftarrow$  2 to length(ParamStr(j)) do
        case ParamStr(j)[i] of
          'n': NewAccom  $\leftarrow$  true;
          'a': Accomodation  $\leftarrow$  true;
          'l': LongLines  $\leftarrow$  true;
          'q': QuietMode  $\leftarrow$  true;
          's': StopOnError  $\leftarrow$  true;
        endcases;
      end;

```

69. The “other” options.

Notably, there is a feature to allow axioms, which is completely undocumented (and probably for good reason!). The axioms must appear in “.axm” files.

```

procedure GetOptions;
  var i, j: integer;
  begin for j  $\leftarrow$  1 to ParamCount do
    if ParamStr(j)[1] = '-' then
      for i  $\leftarrow$  2 to length(ParamStr(j)) do
        case ParamStr(j)[i] of
          'q': QuietMode  $\leftarrow$  true;
          'p': ParserOnly  $\leftarrow$  true;
          'a': AnalyzerOnly  $\leftarrow$  true;
          'c': CheckerOnly  $\leftarrow$  true;
          'l': LongLines  $\leftarrow$  true;
          's': StopOnError  $\leftarrow$  true;
          'u': SwitchOffUnifier  $\leftarrow$  true;
          'x': AxiomsAllowed  $\leftarrow$  true;
        othercases break;
        endcases;
      if ArticleExt = '.axm' then AxiomsAllowed  $\leftarrow$  true;
    end;

```

70. Transfer specific options.

```

procedure GetTransfOptions;
  var lOption: String;
  begin PublicLibr  $\leftarrow$  false;
  if ParamCount  $\geq$  2 then
    begin lOption  $\leftarrow$  ParamStr(2);
    if (length(lOption) = 2)  $\wedge$  (lOption[1]  $\in$  ['/ ', '-']) then PublicLibr  $\leftarrow$  UpCase(lOption[2]) = 'P';
    end
  end;

```

71. We have a number of functions useful for “drawing”, i.e., reporting progress and results (and so on).

```

var gComment: String = ``;
  disable_io_checking;
procedure NoDisplayLine(fLine, fErrNbr : integer);
  begin end;
procedure InitDisplayLine(const aComment: String);
  begin gComment ← aComment; WriteLn; write(aComment); DisplayLine ← DisplayLineInCurPos
  end;
procedure DrawStr(const aStr: String);
  begin write(aStr) end;
procedure FinishDrawing;
  begin WriteLn;
  end;
procedure DrawTPass(const fPassName: String);
  begin write(fPassName) end;
procedure DrawMizarScreen(const aApplicationName: String);
  begin WriteLn(aApplicationName, `,`, PCMizarVersionStr, `,`, PlatformNameStr, ``);
  WriteLn(Copyright);
  end;
procedure Noise;
  begin
  if_not_def ( WIN32)write(↑G↑G↑G);
  endif ;
  end ;
procedure EmptyParameterList;
  begin Noise; WriteLn; WriteLn(`****_Empty_Parameter_List?****`); halt(2);
  end;

```

72. More such procedures, reporting the article processed, the time, etc.

```

procedure DrawArticleName(const fName: String);
  begin WriteLn(`Processing:`, fName); end;
procedure DrawPass(const aName: String);
  begin WriteLn; write(aName); end;
procedure DrawTime(const aTime: String);
  begin write(aTime); end;
procedure DrawVerifierExit(const aTime: String);
  begin WriteLn; WriteLn(`Time_of_mizar:`, aTime);
  end;

```

73.

```

procedure DisplayLineInCurPos(fLine, fErrNbr : integer);
  begin if ( $\neg$ CtrlCPressed)  $\wedge$  ( $\neg$ QuietMode) then
    begin write( $\uparrow M + gComment + \text{'\_'}[$ , fLine : 4);
    if fErrNbr > 0 then write( $\text{'\_'}*$ , fErrNbr);
    write( $\text{'\_'}]$ );
    end;
  if FinishingPass then
    begin write( $\text{'\_'}[$ , fLine : 4);
    if fErrNbr > 0 then write( $\text{'\_'}*$ , fErrNbr);
    write( $\text{'\_'}]$ );
    end;
  end;

```

74.

```

procedure DrawMessage(const Msg1, Msg2 : String);
  var Lh : byte;
  begin Noise; WriteLn; write( $\text{'****\_'}[$ , Msg1); Lh  $\leftarrow$  length(Msg1);
  if length(Msg2) > Lh then Lh  $\leftarrow$  length(Msg2);
  if Lh > length(Msg1) then write( $\text{'\_'} :$  Lh - length(Msg1));
  WriteLn( $\text{'\_'}****]$ );
  if Msg2  $\neq$   $\text{''}$  then
    begin write( $\text{'****\_'}[$ , Msg2);
    if Lh > length(Msg2) then write( $\text{'\_'} :$  Lh - length(Msg2));
    WriteLn( $\text{'\_'}****]$ );
    end;
  end;

```

75.

```

procedure BugInProcessor;
  begin DrawMessage( $\text{'Internal\_Error'}$ ,  $\text{''}$ ); end;
procedure DrawIOResult(const FileName : String;
  I : byte);
  begin if I  $\in$  [2 .. 6, 12, 100] then
    begin if I = 12 then I  $\leftarrow$  7
    else if I = 100 then I  $\leftarrow$  8;
    DrawMessage(ErrMsg[I],  $\text{'Can't\_open\_'}[$  FileName +  $\text{'\_'}]$ );
    end
  else DrawMessage( $\text{'Can't\_open\_'}[$  FileName +  $\text{'\_'}]$ ,  $\text{''}$ );
  halt(1);
  end;

```

76.

```

procedure DrawErrorsMSg(aErrorNbr : integer);
  begin if aErrorNbr > 0 then
    begin WriteLn;
    if aErrorNbr = 1 then WriteLn( $\text{'****\_1\_error\_detected'}$ )
    else WriteLn( $\text{'****\_'}[$ , aErrorNbr,  $\text{'\_errors\_detected'}$ );
    end;
  end;

```

File 3

PC Mizar Version

77. This is used to track the version of Mizar.

```

⟨pcmizver.pas 77⟩ ≡
  ⟨GNU License 4⟩
unit pcmizver;
interface
  const PCMizarReleaseNbr = 8;
    PCMizarVersionNbr = 1;
    PCMizarVariantNbr = 14;
    CurrentYear = 2025;
    @{@&$IFDEF WIN32@}DirSeparator = `\\`;
    @{@&$ELSE@}DirSeparator = `/`;
    @{@&$ENDIF@}

```

78. There are only four functions provided by this module.

```

function PCMizarVersionStr: String;
function VersionStr: String;
function PlatformNameStr: String;
function Copyright: String;

```

79. Their implementation is relatively straightforward: just print the appropriate constants to the screen.

implementation

```

function Copyright: String;
  var s: String;
  begin Str(CurrentYear, s);
  Copyright ← `Copyright_␣(c)␣1990-` + s + `␣Association_␣of_␣Mizar_␣Users`;
  end;

```

80.

```

function VersionStr: String;
  var lRel, lVer, lVar: String[2]; lStr: String;
  begin Str(PCMizarReleaseNbr, lRel); Str(PCMizarVersionNbr, lVer); Str(PCMizarVariantNbr, lVar);
  if length(lVar) = 1 then lVar ← `0` + lVar;
  @{@&$IFDEF VERALPHA@}lStr ← `-alpha`;
  @{@&$ELSE@}lStr ← ``;
  @{@&$ENDIF@}
  VersionStr ← lRel + `.` + lVer + `.` + lVar + lStr;
  end;

```

81. There are a number of platforms supported, a surprisingly large number. If we were to support more platforms (other BSDs, BeOS, GNU Hurd, etc.), then we would need to update this function. To see what platforms are predefined for FreePascal, consult:

- https://wiki.freepascal.org/Platform_defines

Ostensibly, we could extend the platform name string to display “generic UNIX” (and even “generic BSD”), as well as “generic Windows”.

```
function PlatformNameStr: String;
var lStr: String;
begin lStr ← ``;
  if_def (WIN32)lStr ← lStr + `Win32`; end_if
  if_def (LINUX)lStr ← lStr + `Linux`; end_if
  if_def (SOLARIS)lStr ← lStr + `Solaris`; end_if
  if_def (FREEBSD)lStr ← lStr + `FreeBSD`; end_if
  if_def (DARWIN)lStr ← lStr + `Darwin`; end_if
  if_def (FPC)lStr ← lStr + `/FPC`; end_if
  if_def (DELPHI)lStr ← lStr + `/Delphi`; end_if
  PlatformNameStr ← lStr;
end ;
```

82. The last function in the `pcmizver.pas` file provides a String for the Mizar version.

```
function PCMizarVersionStr: String;
  begin PCMizarVersionStr ← `Mizar_` + VersionStr;
  end;
end .
```

File 4

Mizar internal state

83. As far as *processing* an article, Mizar works like a “batch compiler” and works in multiple “passes”.

```

⟨ mstate.pas 83 ⟩ ≡
  ⟨ GNU License 4 ⟩
unit mstate;
  interface
    ⟨ Interface for mstate.pas 84 ⟩
  implementation
    uses mizenv, pcmizver, monitor, errhan, mconsole, mtime
    mdebug , info end_mdebug ;
    var PassTime: longint;
    ⟨ Implementation for mstate.pas 85 ⟩
  end

```

84. ⟨ Interface for mstate.pas 84 ⟩ ≡

```

procedure InitPass(const aPassName: String);
procedure FinishPass;
procedure InitProcessing(const aProgName, aExt: String);
procedure ProcessingEnding;

```

This code is used in section 83.

85. The implementation amounts to, well, these four functions. We have a couple “private” functions to help us: *MError* and *MizarExitProc*.

```

⟨ Implementation for mstate.pas 85 ⟩ ≡
procedure InitPass(const aPassName: String);
  begin CurPos.Line ← 1; CurPos.Col ← 1; InitDisplayLine(aPassName); TimeMark(PassTime);
  end;
procedure FinishPass;
  begin FinishingPass ← true;
  if QuietMode then DisplayLine(CurPos.Line, ErrorNbr);
  FinishingPass ← false; DrawTime(⌈⌋ + ReportTime(PassTime));
  end;
procedure MError(Pos : Position; ErrNr : integer);
  begin WriteError(Pos, ErrNr); DisplayLine(CurPos.Line, ErrorNbr);
  end;

```

This code is used in section 83.

86. We also have *MizarExitProc* as a private “helper” function.

```

var _ExitProc: pointer;
procedure MizarExitProc;
  begin ExitProc  $\leftarrow$  _ExitProc;
    disable_io_checking;
    if IOResult  $\neq$  0 then ;
    if  $\neg$ StopOnError then DisplayLine(CurPos.Line, ErrorNbr);
      PutError  $\leftarrow$  WriteError; DrawVerifierExit(ReportTime(gStartTime)); { Halt(ErrorCode); }
    enable_io_checking;
  end;

```

87.

```

procedure InitProcessing(const aProgName, aExt: String);
  begin DrawMizarScreen(aProgName);
    if ParamCount < 1 then EmptyParameterList;
      GetArticleName; GetEnvironName; DrawArticleName(MizFileName + aExt); GetOptions;
      InitExitProc; FileExam(MizFileName + aExt); _ExitProc  $\leftarrow$  ExitProc; ExitProc  $\leftarrow$  @MizarExitProc;
      PutError  $\leftarrow$  MError; OpenErrors(MizFileName);
    mdebug OpenInfoFile; end_mdebug
  end;

```

88. At the end, we should report the number of errors (if any were encountered).

```

procedure ProcessingEnding;
  begin if ErrorNbr > 0 then
    begin DrawErrorsMsg(ErrorNbr); FinishDrawing;
    end;
  end;

```

File 5

Monitor**89.**

```

⟨ monitor.pas 89 ⟩ ≡
  ⟨ GNU License 4 ⟩
unit monitor;
interface
procedure InitExitProc;
implementation
uses
  @{@&$IFDEF FPC@}
    @{@&$IFDEF WIN32@}
      baseunix,
    @{@&$ENDIF@}
  @{@&$ENDIF@}
  mizenv, errhan, mconsole
  @{@&$IFDEF WIN32@} , windows@{@&$ENDIF@}
  mdebug , info end_mdebug
;
var _ExitProc: pointer; _IOResult: integer;
  ⟨ Implementation for monitor.pas 90 ⟩
end

```

90. There are a few private helper functions in this module.

\langle Implementation for `monitor.pas` 90 $\rangle \equiv$

```

procedure _Halt_(ErrorCode : word);
begin _IOResult  $\leftarrow$  _IOResult; _ErrorAddr  $\leftarrow$  nil;
if ErrorCode > 1 then
  case ErrorCode of
    2 .. 4: begin ErrImm(1000 + ErrorCode); DrawMessage('I/O_error', ErrMsg[ErrorCode]) end;
    5 .. 6: begin ErrImm(1000 + ErrorCode); BugInProcessor end;
    12: begin ErrImm(1000 + ErrorCode); BugInProcessor end;
    97, 98, 99: begin ErrImm(RTErrCode);  $\langle$ Handle runtime error cases for monitor.pas 91 $\rangle$ 
      end;
    100 .. 101: begin ErrImm(1000 + ErrorCode); DrawMessage('I/O_error', ErrMsg[ErrorCode - 95]);
      end;
    102 .. 106: begin ErrImm(1000 + ErrorCode); BugInProcessor end;
    150 .. 162: begin ErrImm(1000 + ErrorCode);
      DrawMessage('I/O_error', 'Critical_disk_error');
      end;
    200 .. 201: begin ErrImm(1000 + ErrorCode); BugInProcessor end;
    202: begin ErrImm(1000 + ErrorCode); DrawMessage('Stack_overflow_error', '') end;
    203, 204: begin ErrImm(1000 + ErrorCode); DrawMessage('Heap_overflow_error', '') end;
    208: begin ErrImm(1000 + ErrorCode); DrawMessage('Overlay_manager_not_installed', '') end;
    209: begin ErrImm(1000 + ErrorCode); DrawMessage('Overlay_file_read_error', '') end;
    210 .. 212: begin ErrImm(1000 + ErrorCode); BugInProcessor end;
    213: begin ErrImm(1000 + ErrorCode); DrawMessage('Collection_Index_out_of_range', '') end;
    214: begin ErrImm(1000 + ErrorCode); DrawMessage('Collection_overflow_error', '') end;
    215: begin ErrImm(1000 + ErrorCode); DrawMessage('Arithmetic_overflow_error', '') end;
    216: begin ErrImm(1000 + ErrorCode); DrawMessage('General_Protection_fault', '') end;
    217: begin ErrImm(1000 + ErrorCode); DrawMessage('Segmentation_fault', '') end;
    218 .. 254: begin ErrImm(1000 + ErrorCode); BugInProcessor end;
    255: ErrImm(1000 + ErrorCode);
  othercases begin ErrImm(ErrorCode);
    if OverflowError then DrawMessage('Mizar_parameter_overflow_error', '')
    else BugInProcessor
    end;
  endcases;
  CloseErrors; ExitProc  $\leftarrow$  _ExitProc;
if (ErrorCode = 0)  $\wedge$  (ErrorNbr  $\neq$  0) then Halt(1)
else Halt(ErrorCode);
end;

```

See also section 92.

This code is used in section 89.

91. \langle Handle runtime error cases for `monitor.pas` 91 $\rangle \equiv$

```

case RTErrorCode of
800,804: DrawMessage('Library_Corrupted', ``);
857: DrawMessage('Connection_Fault', ``);
      { 900..999: DrawMessage('Mizar parameter overflow: '+IntToStr(RTErrorCode), ""); }
1255: DrawMessage('User_break', ``);
othercases if OverflowError then
      DrawMessage('Mizar_parameter_overflow:_' + IntToStr(RTErrorCode), ``)
else BugInProcessor
endcases;

```

This code is used in section 90.

92. The *MizExitProc* is a private “bail out” function.

\langle Implementation for `monitor.pas` 90 $\rangle \equiv$

```

procedure MizExitProc;
begin
  @{@&$IFDEF IODEBUG@} ExitProc  $\leftarrow$  _ExitProc;
  @{@&$ELSE@} _Halt_(ExitCode);
  @{@&$ENDIF@}
end;

```

93. We use the *MizExitProc* to initialize the *ExitProc* pointer.

```

procedure InitExitProc;
begin ExitProc  $\leftarrow$  @MizExitProc
end;

```

94. **Initializing Control.** This is a *heavily* system dependent piece of code. There are two ways to implement it (one way for Windows, another way for everyone else). Once we’re done, we have to initialize the *_ExitProc* and invoke *InitCtrl*.

\langle Non-windows FreePascal implemenation for *InitCtrl* 95 \rangle

\langle Windows implemenation for *InitCtrl* 96 \rangle

```

begin _ExitProc  $\leftarrow$  ExitProc; InitCtrl;
end.

```

95. \langle Non-windows FreePascal implemenation for *InitCtrl* 95 $\rangle \equiv$

```

@{@&$IFDEF FPC@}  @{@&$IFNDEF WIN32@}
procedure CatchSignal(aSig : integer); cdecl;
begin
  case aSig of
    SIGINT, SIGQUIT, SIGTERM: begin CtrlCPressed  $\leftarrow$  true; RunTimeError(1255); end;
  endcases;
end;
var NewSignal, OldSigInt: SignalHandler;
procedure InitCtrl;
begin NewSignal  $\leftarrow$  SignalHandler(@CatchSignal); OldSigInt  $\leftarrow$  fpSignal(SIGINT, NewSignal);
  OldSigInt  $\leftarrow$  fpSignal(SIGQUIT, NewSignal); OldSigInt  $\leftarrow$  fpSignal(SIGTERM, NewSignal);
end;
  @{@&$ENDIF@}@{@&$ENDIF@}

```

This code is used in section 94.

96. Microsoft breaks everything. This is a mess because of them.

```

⟨ Windows implemenation for InitCtrl 96 ⟩ ≡
  @{$IFDEF WIN32@}
    ⟨ Windows implemenation for CtrlSignal 99 ⟩
    @{$IFDEF FPC@}
      ⟨ FreePascal implemenation of InitCtrl for Windows 97 ⟩
    @{$ENDIF@}
    @{$IFDEF DELPHI@}
      ⟨ Delphi implemenation of InitCtrl for Windows 98 ⟩
    @{$ENDIF@}
  @{$ENDIF@}

```

This code is used in section 94.

97. The FreePascal implementation is pretty succinct thanks to the libraries they provide.

```

⟨ FreePascal implemenation of InitCtrl for Windows 97 ⟩ ≡
procedure InitCtrl;
begin SetConsoleCtrlHandler(CtrlSignal, TRUE); end;

```

This code is used in section 96.

```

98. ⟨ Delphi implemenation of InitCtrl for Windows 98 ⟩ ≡
procedure InitCtrl;
var ConsoleMode, lConsoleMode: DWORD;
begin if GetConsoleMode(GetStdHandle(STD_INPUT_HANDLE), ConsoleMode) then
  begin lConsoleMode ← ConsoleMode ∨ ENABLE_PROCESSED_INPUT;
    { Treat Ctrl+C as a signal }
  if SetConsoleMode(GetStdHandle(STD_INPUT_HANDLE), lConsoleMode) then
    begin SetConsoleCtrlHandler(@CtrlSignal, TRUE);
      end;
    end;
  end;
end;

```

This code is used in section 96.

99. Windows requires a helper function *CtrlSignal* for this Microsoft mania.

```

⟨ Windows implemenation for CtrlSignal 99 ⟩ ≡
  ⟨ FreePascal declaration of CtrlSignal for Windows 100 ⟩
  ⟨ Delphi declaration of CtrlSignal for Windows 101 ⟩
begin { TRUE: do not call next handler in the queue, FALSE: call it }
  CtrlCPressed ← true; RunTimeError(1255); CtrlSignal ← true; { ExitProcess(1); }
end;

```

This code is used in section 96.

```

100. ⟨ FreePascal declaration of CtrlSignal for Windows 100 ⟩ ≡
  @{$IFDEF FPC@}
function CtrlSignal(aSignal : DWORD): WINBOOL; stdcall;
  @{$ENDIF@}

```

This code is used in section 99.

```

101. ⟨ Delphi declaration of CtrlSignal for Windows 101 ⟩ ≡
  @{$IFDEF DELPHI@}
function CtrlSignal(aSignal : DWORD): BOOL; cdecl;
  @{$ENDIF@}

```

This code is used in section 99.

File 6

Error handling

102.

```

⟨errhan.pas 102⟩ ≡
  ⟨GNU License 4⟩
unit errhan;
  interface
    ⟨Interface for errhan.pas 103⟩
  implementation
    uses mconsole, mizenv;
    ⟨Implementation for errhan.pas 106⟩
  end ;

```

103. We have a few custom types and internal variables describing the state of the Mizar error handler.

```

⟨Interface for errhan.pas 103⟩ ≡
type Position = ⟨Declare Position as record 104⟩;
  ErrorReport = procedure (Pos : Position; ErrNr : integer);
const ZeroPos: Position = (Line : 0; Col : 0);
var CurPos: Position; { current position }
  ErrorNbr: integer; { current error number }
  PutError: ErrorReport = nil; { reporter for errors }
  RTErrorCode: integer = 0; { runtime error code }
  OverflowError: boolean = false; { overflow error? They're horrible, treat accordingly }

```

See also section 105.

This code is used in section 102.

104. *Position* is just a pair of integers recording the line and offset (“column”).

```

⟨Declare Position as record 104⟩ ≡
  record Line, Col: integer
  end

```

This code is used in section 103.

105. And we just provide the public-facing functions and procedures.

```

<Interface for errhan.pas 103> +≡
procedure Error(Pos : Position; ErrNr : integer);
procedure ErrImm(ErrNr : integer);
procedure WriteError(Pos : Position; ErrNr : integer);
procedure OpenErrors(FileName : String);
procedure AppendErrors(FileName : String);
procedure EraseErrors;
procedure CloseErrors;
procedure OverflowError(ErrorCode : word);
procedure Mizassert(ErrorCode : word; Cond : boolean);
procedure RunTimeError(ErrorCode : word);

```

106. The implementation begins as we would expect/hope. If we have a *preferred* error reporter already present in *PutError*, then we just use it. If we have toggled *StopOnError* to true, then we should end the program here (with a message).

If we want to report an error at the *CurrPos* (current position), then we have a helper function do that for us.

```

<Implementation for errhan.pas 106> ≡
procedure Error(Pos : Position; ErrNr : integer);
  begin inc(ErrorNbr);
  if @PutError ≠ nil then PutError(Pos, ErrNr);
  if StopOnError then
    begin DrawMessage(‘Stopped on first error’, ‘’); Halt(1); end;
  end;
procedure ErrImm(ErrNr : integer);
  begin Error(CurPos, ErrNr);
  end;

```

This code is used in section 102.

107. We also can write errors to a file. This requires keeping track of the file (dubbed *Errors*) and whether it has been opened or not (in the Boolean condition *OpenedErrors*).

Note this takes advantage of **with** to destructure *Pos* into a *Line* and *Col* for us.

```

var Errors: text; { file name for errors file }
    OpenedErrors: boolean = false; { have we opened it yet? }
procedure WriteError(Pos : Position; ErrNr : integer);
  begin if ¬OpenedErrors then RunTimeError(2001);
  with Pos do WriteLn(Errors, Line, ‘_’, Col, ‘_’, ErrNr);
  end;

```

108. Opening an errors file. We can open an errors file, which will reset the *ErrorNbr* counter to zero and re-initialize *CurPos* to line 1 and column 1.

When *PutError* is *nil*, we initialize it to be *WriteError*.

```

procedure OpenErrors(FileName : String);
  begin if ExtractFileExt(FileName) = `` then FileName ← FileName + ``.err`;
  Assign(Errors, FileName); without_io_checking(Rewrite(Errors));
  if IOResult ≠ 0 then
    begin DrawMessage(`Can't open errors file` + FileName + ``for writing`, ``); halt(1);
    end;
  OpenedErrors ← true; ErrorNbr ← 0;
  with CurPos do
    begin Line ← 1; Col ← 1
    end;
  if @PutError = nil then PutError ← WriteError;
end;

```

109. Appending errors to the errors file.

```

procedure AppendErrors(FileName : String);
  begin OpenedErrors ← true;
  if ExtractFileExt(FileName) = `` then FileName ← FileName + ``.err`;
  Assign(Errors, FileName); ErrorNbr ← 0;
  with CurPos do
    begin Line ← 1; Col ← 1
    end;
  without_io_checking(append(Errors));
  if ioresult ≠ 0 then Rewrite(Errors);
end;

```

110. We can also close the errors file and unset the *Errors* variable, “forgetting” where we logged the errors.

```

procedure EraseErrors;
  begin if OpenedErrors then
    begin OpenedErrors ← false; close(Errors); erase(Errors);
    end;
  end;

```

111. We can also just close the errors file.

```

procedure CloseErrors;
  begin if OpenedErrors then
    begin OpenedErrors ← false; close(Errors);
    end;
  end;

```

112. Like I said, overflow errors are especially problematic. If/when they occur, we should just bail out immediately.

```

procedure OverflowError(ErrorCode : word);
  begin RTErrCode ← ErrorCode; OverflowError ← true; RunError(97);
end;

```


113. We have an assertion utility to check if a *Cond* is *true*. When it is *false*, we should report a runtime error.

```
procedure MizAssert(ErrorCode : word; Cond : boolean);  
  begin if  $\neg$ Cond then  
    begin RTErrorCode  $\leftarrow$  ErrorCode; RunError(98);  
    end;  
  end;
```

114. Last, we have a catchall for runtime errors encountered.

```
procedure RunTimeError(ErrorCode : word);  
  begin RTErrorCode  $\leftarrow$  ErrorCode; RunError(99);  
  end;
```

File 7

Time utilities

115. This is another heavily “system dependent” library.

```

<mtime.pas 115> ≡
  <GNU License 4>
unit mtime;
  interface
    <Interface for mtime.pas 116>
  implementation
    <Implementation for mtime.pas 118>
  end ;

```

```

116. <Interface for mtime.pas 116> ≡
procedure TimeMark(var W : longint);
function ElapsedTime(W : longint): longint;
procedure MUnpackTime(W : longint; var H, M, S, F : word);
function ReportTime(W : longint): String;

```

This code is used in section 115.

117. We also have one global variable tracking the start time.

```

var gStartTime: longint;

```

118. The implementation begins with a rather *thorny* digression depending on which compiler we’re using.

```

<Implementation for mtime.pas 118> ≡
  <Timing utilities uses for Delphi 119>
  <Timing utilities uses for FreePascal 120>

```

See also section 121.

This code is used in section 115.

119. Delphi simply requires us to introduce a constant for milliseconds.

```

<Timing utilities uses for Delphi 119> ≡
  @{@&$IFDEF DELPHI@}
  uses windows;
const cmSecs = 1000;
  @{@&$ENDIF@}

```

This code is used in section 118.

120. FreePascal requires a bit more work, alas.

```

⟨Timing utilities uses for FreePascal 120⟩ ≡
  @{&&$IFDEF FPC@}
    uses dos;
const cmSecs = 100;
type TSystemTime =
  record wHour: word;
    wMinute: word;
    wSecond: word;
    wMilliseconds: word;
  end;
procedure GetLocalTime(var aTime : TSystemTime);
  begin with aTime do GetTime(wHour, wMinute, wSecond, wMilliseconds);
  end;
  @{&&$ENDIF@}

```

This code is used in section 118.

121. Now we can happily plug along implementing the functions we need.

```

⟨Implementation for mtime.pas 118⟩ +≡
function SystemTimeToMiliSec(const fTime: TSystemTime): longint;
  begin SystemTimeToMiliSec ← fTime.wHour * (3600 * cmSecs) + fTime.wMinute * longint(60 *
    cmSecs) + fTime.wSecond * cmSecs + fTime.wMilliseconds;
  end;

```

122. We “start the clock”.

```

procedure TimeMark(var W : longint);
  var SystemTime: TSystemTime;
  begin GetLocalTime(SystemTime); W ← SystemTimeToMiliSec(SystemTime);
  end;

```

123. We measure the time lapse since we “started the clock”.

```

function ElapsedTime(W : longint): longint;
  var T: longint; SystemTime: TSystemTime;
  begin GetLocalTime(SystemTime); T ← SystemTimeToMiliSec(SystemTime) − W;
  if T < 0 then T ← 86400 * cmSecs + T;
  ElapsedTime ← T;
  end;

```

124. We can transform an interval of time (in milliseconds) into hours, minutes, seconds, a fractional amount of time.

```

procedure MUnpackTime(W : longint; var H, M, S, F : word);
  begin H ← W div (3600 * cmSecs); M ← (W − H * 3600 * cmSecs) div (60 * cmSecs);
  S ← (W − H * 3600 * cmSecs − M * 60 * cmSecs) div cmSecs;
  F ← W − H * 3600 * cmSecs − M * 60 * cmSecs − S * cmSecs;
  end;

```

125. When reporting time, we want to pad the time by a zero. This is standard conventional stuff (e.g., I have an appointment at 11:01 AM, not 11:1 AM).

```
function LeadingZero(w : word): String;
  var lStr: String;
  begin Str(w : 0, lStr);
  if length(lStr) = 1 then lStr  $\leftarrow$  '0' + lStr;
  LeadingZero  $\leftarrow$  lStr;
end;
```

126. Reporting time transforms a time interval (measured in milliseconds) into a human readable String.

```
function ReportTime(W : longint): String;
  var H, M, S, F: word; lTimeStr: String;
  begin MUnpackTime(ElapsedTime(W), H, M, S, F);
  if F  $\geq$  (cmSecs div 2) then inc(S);
  if H  $\neq$  0 then
    begin Str(H, lTimeStr); lTimeStr  $\leftarrow$  lTimeStr + ':' + LeadingZero(M)
    end
  else Str(M : 2, lTimeStr);
  ReportTime  $\leftarrow$  lTimeStr + ':' + LeadingZero(S);
end;
```

127. When we run the program, we should mark the time.

```
begin TimeMark(gStartTime);
end.
```

File 8

Arbitrary precision arithmetic

128. Specifically, arbitrary precision arithmetic on *integers* and *rational complex* numbers. integers are represented as Strings of digits.

Note:

- (1) The naming convention dictates all functions suffixed with *_XXX* presuppose the arguments are positive.
- (2) Also there are *no checks* whether the parameters contain only digits (and an optional sign “-”).
- (3) Further, *DEBUGNUM* is a conditional variable that can be used (with *DEBUG*) for testing.

⟨ numbers.pas 128 ⟩ ≡

⟨ GNU License 4 ⟩

unit *numbers*;

interface

⟨ Basic arithmetic operations declarations 129 ⟩

⟨ Types for arbitrary-precision arithmetic 130 ⟩

⟨ Zero and units for arbitrary-precision 131 ⟩

⟨ Rational arithmetic declarations 132 ⟩

⟨ Predicate declarations for arbitrary-precision arithmetic 133 ⟩

⟨ Declare public complex-valued arbitrary precision arithmetic 134 ⟩

⟨ Declare public comparison operators for arbitrary-precision numbers 135 ⟩

implementation

uses *mizenv*

@{ @&\$IFDEF CH_REPORT@ } , req_info, prephan, builtin@{ @&\$ENDIF@ }

mdebug , info end_mdebug;

⟨ Trim leading zeros from arbitrary-precision integers 136 ⟩

⟨ Check if arbitrary-precision integers are zero 137 ⟩

⟨ Absolute value for an arbitrary-precision number 138 ⟩

⟨ Test if one arbitrary-precision number is less than or equal to another 139 ⟩

⟨ Arithmetic for arbitrary-precision integers 143 ⟩

⟨ Arbitrary-precision rational arithmetic 160 ⟩

⟨ Complex-rational arbitrary-precision arithmetic 169 ⟩

129. \langle Basic arithmetic operations declarations 129 $\rangle \equiv$

```

function Add(a, b : String): String;
function Sub(a, b : String): String;
function Mul(a, b : String): String;
function Diva(a, b : String): String;
    { *Note: divides absolute values and preserves the sign of the division }
function _Div(a, b : String): String;
function _Mod(a, b : String): String;
function GCD(a, b : String): String;    { *Note: always returns a positive value }
function LCM(a, b : String): String;    { *Note: always returns a positive value }
function Abs(a : String): String;
function IsPrime(a : String): boolean;
function Divides(a, b : String): boolean;

```

This code is used in section 128.

130. Rational numbers are a pair of arbitrary precision integers (represented as a String).

Rational complex numbers are represented by a pair of rational numbers in Cartesian form $z = p + iq$.

\langle Types for arbitrary-precision arithmetic 130 $\rangle \equiv$

```

type Rational = record Num, Den: String
    end;
    RComplex = record Re, Im: Rational
    end;

```

This code is used in section 128.

131. \langle Zero and units for arbitrary-precision 131 $\rangle \equiv$

```

const RZero: Rational = (Num : ^0^; Den : ^1^);
ROne: Rational = (Num : ^1^; Den : ^1^);
CZero: RComplex = (Re : (Num : ^0^; Den : ^1^); Im : (Num : ^0^; Den : ^1^));
COne: RComplex = (Re : (Num : ^1^; Den : ^1^); Im : (Num : ^0^; Den : ^1^));
CMinusOne: RComplex = (Re : (Num : ^-1^; Den : ^1^); Im : (Num : ^0^; Den : ^1^));
CImUnit: RComplex = (Re : (Num : ^0^; Den : ^1^); Im : (Num : ^1^; Den : ^1^));

```

This code is used in section 128.

132. \langle Rational arithmetic declarations 132 $\rangle \equiv$

```

procedure RationalReduce(var r : Rational);
function RationalAdd(const r1, r2 : Rational): Rational;
function RationalSub(const r1, r2 : Rational): Rational;
function RationalNeg(const r1 : Rational): Rational;
function RationalMult(const r1, r2 : Rational): Rational;
function RationalInv(const r : Rational): Rational;
function RationalDiv(const r1, r2 : Rational): Rational;
function RationalEq(const r1, r2 : Rational): boolean;
function RationalLE(const r1, r2 : Rational): boolean;
function RationalGT(const r1, r2 : Rational): boolean;

```

This code is used in section 128.

133. \langle Predicate declarations for arbitrary-precision arithmetic 133 $\rangle \equiv$

```

function IsintegerNumber(const z: RComplex): boolean;
function IsNaturalNumber(const z: RComplex): boolean;
function IsPrimeNumber(const z: RComplex): boolean;
function AreEqComplex(const z1, z2: RComplex): boolean;
function IsEqWithInt(const z: RComplex;
                    n: longint): boolean;
function IsRationalLE(const z1, z2: RComplex): boolean;
function IsRationalGT(const z1, z2: RComplex): boolean;

```

This code is used in section 128.

134. \langle Declare public complex-valued arbitrary precision arithmetic 134 $\rangle \equiv$

```

function IntToComplex(x: integer): RComplex;
function ComplexAdd(const z1, z2: RComplex): RComplex;
function ComplexSub(const z1, z2: RComplex): RComplex;
function ComplexNeg(const z: RComplex): RComplex;
function ComplexMult(const z1, z2: RComplex): RComplex;
function ComplexInv(const z: RComplex): RComplex;
function ComplexDiv(const z1, z2: RComplex): RComplex;
function ComplexNorm(const z: RComplex): Rational;

```

This code is used in section 128.

135. \langle Declare public comparison operators for arbitrary-precision numbers 135 $\rangle \equiv$

```

function CompareInt(X1, X2: Longint): integer;
function CompareIntStr(X1, X2: String): integer;
function CompareComplex(const z1, z2: RComplex): integer;

```

This code is used in section 128.

136. If we are given single character String consisting of zero or the empty String, then we are done.

If we are given anything else, we find the first index (from the left) of a nonzero character. Then we create a copy of the subString starting from the first nonzero digit to the rest of the String.

\langle Trim leading zeros from arbitrary-precision integers 136 $\rangle \equiv$

```

function trimlz(a: String): String;
  var i: integer;
  begin if (a = '0')  $\vee$  (a = '') then trimlz  $\leftarrow$  a
  else begin i  $\leftarrow$  0;
    repeat i  $\leftarrow$  i + 1;
      if a[i]  $\neq$  '0' then break;
    until i = length(a);
    trimlz  $\leftarrow$  copy(a, i, length(a));
  end;
end;

```

This code is used in section 128.

137. First, we check if a starts with “-0”. If so, replace a with 0. Then we do the same thing with b .

We invoke *trimlz* on a and store the result in $a1$. If $a1 \neq a$, then we update $a \leftarrow a1$.

Then we do likewise on b .

⟨ Check if arbitrary-precision integers are zero 137 ⟩ \equiv

```
procedure checkzero(var  $a, b : String$ );
  var  $a1, b1 : String$ ;
  begin if copy( $a, 1, 2$ ) =  $\text{'-0'}$  then
    begin
      @{@&$IFDEF DEBUGNUM@} WriteLn(infofile,  $\text{'a=-0'}$ );
      @{@&$ENDIF@}  $a \leftarrow \text{'0'}$ ;
    end;
  if copy( $b, 1, 2$ ) =  $\text{'-0'}$  then
    begin
      @{@&$IFDEF DEBUGNUM@} WriteLn(infofile,  $\text{'b=-0'}$ );
      @{@&$ENDIF@}
       $b \leftarrow \text{'0'}$ ;
    end;
   $a1 \leftarrow \text{trimlz}(a)$ ;
  if  $a1 \neq a$  then
    begin
      @{@&$IFDEF DEBUGNUM@} WriteLn(infofile,  $\text{'ZEROS1:'}$ ,  $a$ );
      @{@&$ENDIF@}  $a \leftarrow a1$ ;
    end;
   $b1 \leftarrow \text{trimlz}(b)$ ;
  if  $b1 \neq b$  then
    begin
      @{@&$IFDEF DEBUGNUM@} WriteLn(infofile,  $\text{'ZEROS2:'}$ ,  $b$ );
      @{@&$ENDIF@}  $b \leftarrow b1$ ;
    end;
  end;
```

This code is used in section 128.

138. Since arbitrary precision numbers (as Strings) are negative if they begin with a leading “-” character, it is easy to obtain the absolute value (just delete the minus sign).

⟨ Absolute value for an arbitrary-precision number 138 ⟩ \equiv

```
function Abs( $a : String$ ): String;
  begin if length( $a$ ) > 0 then
    if  $a[1] = \text{'-'}$  then delete( $a, 1, 1$ );
   $Abs \leftarrow a$ ;
  end;
```

This code is used in section 128.

139. When checking $a \leq b$ for two non-negative integers, written as Strings (without leading zeros) you can check if the length of a is less than the length of b .

If the length of b is less than the length of a , then $b < a$.

When the length of the two Strings are equal, use lexicographic ordering to determine which is less.

⟨ Test if one arbitrary-precision number is less than or equal to another 139 ⟩ \equiv

```
function _leq(a, b : String): boolean;
  var i, x, y, z: integer;
  begin @{{IFDEF DEBUGNUM@}} WriteLn(Infofile, ' _leq(' , a, ', ' , b, ') ');
  @{{ENDIF@}} checkzero(a, b);
  if length(a) < length(b) then _leq ← true
  else if length(a) > length(b) then _leq ← false
  else begin for i ← 1 to length(a) do
    begin val(a[i], x, z); val(b[i], y, z);
    if x > y then
      begin _leq ← false; exit;
    end;
    if x < y then
      begin _leq ← true; exit;
    end;
    end;
  _leq ← true;
  end;
end;
```

This code is used in section 128.

140. Now the *general* case is when a and b are arbitrary-precision *integers*. If a starts with a minus sign and b starts with a minus sign, then test if $a \geq b$.

When a does not start with a minus sign, but b *does* start with a minus sign, then we're done: $b < a$.

When neither a nor b starts with a minus sign, then we use $_leq(a, b)$ to determine the result.

```
function leq(a, b : String): boolean;
  begin @{{IFDEF DEBUGNUM@}} WriteLn(Infofile, ' leq(' , a, ', ' , b, ') ');
  @{{ENDIF@}} checkzero(a, b);
  if a = b then leq ← true
  else begin if (a[1] = '-' ) ∧ (b[1] ≠ '-' ) then leq ← true;
    if (a[1] = '-' ) ∧ (b[1] = '-' ) then leq ← ¬_leq(abs(a), abs(b));
    if (a[1] ≠ '-' ) ∧ (b[1] = '-' ) then leq ← false;
    if (a[1] ≠ '-' ) ∧ (b[1] ≠ '-' ) then leq ← _leq(a, b);
    end;
  end;
end;
```

141. Testing if $a \geq b$ is simply testing if $b \leq a$ after normalizing the Strings.

```
function geq(a, b : String): boolean;
  begin @{{IFDEF DEBUGNUM@}} WriteLn(Infofile, ' geq(' , a, ', ' , b, ') ');
  @{{ENDIF@}} checkzero(a, b);
  geq ← (¬_leq(a, b)) ∨ (a = b);
  end;
```

142. Similarly, we may check if $a < b$ by testing $a \neq b$ and $a \leq b$.

```

function le( $a, b : String$ ): boolean;
  begin @{@&$IFDEF DEBUGNUM@} WriteLn(infofile, 'le(' ,  $a$ , ', ' ,  $b$ , ') ');
  @{@&$ENDIF@} checkzero( $a, b$ );  $le \leftarrow (a \neq b) \wedge (leq(a, b))$ ;
  end;

function gt( $a, b : String$ ): boolean;
  begin @{@&$IFDEF DEBUGNUM@} WriteLn(infofile, 'gt(' ,  $a$ , ', ' ,  $b$ , ') ');
  @{@&$ENDIF@} checkzero( $a, b$ );  $gt \leftarrow \neg leq(a, b)$ ;
  end;

```

143. Arithmetic operations. Now we get to some interesting bits.

We have `_Add` for the addition of two non-negative integers. The basic strategy is to go digit-by-digit, use the PASCAL-provided integer arithmetic, manually “carrying” 1 if necessary.

The basic strategy is to initialize `a1` to be the larger of the two numbers, and `b1` to the smaller of the two numbers. Then generically we will have

$$\begin{array}{r} a_n \dots a_{m+1} \ a_m \ a_{m-1} \dots a_1 \\ + \quad \quad \quad b_m \ b_{m-1} \dots b_1 \\ \hline \end{array} \quad (143.1)$$

We will separate this out into two sums. First we compute

$$\begin{array}{r} a_m \ a_{m-1} \dots a_1 \\ + \ b_m \ b_{m-1} \dots b_1 \\ \hline c_{m+1} \ r_m \ r_{m-1} \dots r_1 \end{array} \quad (143.2)$$

Then we will compute

$$\begin{array}{r} a_n \dots a_{m+1} \\ + \quad \quad \quad c_{m+1} \\ \hline r_{n+1} \ r_n \dots r_{m+1} \end{array} \quad (143.3)$$

The result is assembled from the digits $r_{n+1}r_n \dots r_1$.

(Arithmetic for arbitrary-precision integers 143) \equiv

```
function _Add(a,b : String): String;
  var c,x,y,z,v: integer; i: integer; a1,b1,s,r: String;
  begin a1 ← a; b1 ← b;
  @{$IFDEF DEBUGNUM@} WriteLn(infofile, ‘_Add(‘, a1, ‘, ‘, b1, ‘)’);
  @{$ENDIF@} checkzero(a1, b1);
  if length(a1) < length(b1) then
    begin s ← b1; b1 ← a1; a1 ← s; end;
  r ← ‘’; c ← 0;
  begin for i ← 0 to length(b1) - 1 do { step 1, Eq (143.2) }
    begin val(a1[length(a1) - i], x, z); val(b1[length(b1) - i], y, z);
    if x + y + c > 9 then
      begin v ← (x + y + c) - 10; c ← 1;
      end
    else begin v ← x + y + c; c ← 0;
      end;
    Str(v, s); r ← s + r;
    end;
  for i ← length(b1) to length(a1) - 1 do { step 2, Eq (143.3) }
    begin val(a1[length(a1) - i], x, z);
    if x + c > 9 then
      begin v ← (x + c) - 10; c ← 1;
      end
    else begin v ← x + c; c ← 0;
      end;
    Str(v, s); r ← s + r;
    end;
  if c = 1 then r ← ‘1’ + r;
  end;
  _Add ← trimlz(r);
end;
```

See also sections 146 and 151.

This code is used in section 128.

144. Subtraction is a bit trickier, because of the “borrowing” operation.

Also note that $_Sub(a, b)$ will start by computing $a_1 \leftarrow \max(a, b)$ and $b_1 \leftarrow \min(a, b)$, then return $a_1 - b_1$.

```

function  $\_Sub(a, b : String) : String$ ;
  var  $x, y, z, v : integer$ ;  $i : integer$ ;  $a1, b1, s, r : String$ ;
   $\langle$  Borrow 1 for  $\_Sub$  145  $\rangle$ 
  begin  $a1 \leftarrow a$ ;  $b1 \leftarrow b$ ;
   $\{ \&\$IFDEF DEBUGNUM \}$   $WriteLn(infofile, \_Sub( \_ , a1, \_ , \_ , b1, \_ ) \_ );$ 
   $\{ \&\$ENDIF \}$   $checkzero(a1, b1)$ ;
  if  $\neg leq(b1, a1)$  then begin  $s \leftarrow b1$ ;  $b1 \leftarrow a1$ ;  $a1 \leftarrow s$ ; end;
   $r \leftarrow \_$ ;
  begin
    for  $i \leftarrow 0$  to  $length(b1) - 1$  do
      begin  $val(a1[length(a1) - i], x, z)$ ;  $val(b1[length(b1) - i], y, z)$ ;
      if  $x < y$  then
        begin  $borrow(length(a1) - i)$ ;  $x \leftarrow x + 10$ ; end;
       $v \leftarrow x - y$ ;  $Str(v, s)$ ;  $r \leftarrow s + r$ ;
      end;
    for  $i \leftarrow length(a1) - length(b1)$  downto 1 do
      begin  $r \leftarrow a1[i] + r$ ; end;
  end;
   $\_Sub \leftarrow trimlz(r)$ ;
end ;

```

145. This is a private “helper function” for subtraction.

```

 $\langle$  Borrow 1 for  $\_Sub$  145  $\rangle \equiv$ 
procedure  $Borrow(k : integer)$ ;
  var  $xx, zz : integer$ ;  $sx : String$ ;
  begin  $val(a1[k - 1], xx, zz)$ ;
  if  $xx \geq 1$  then
    begin  $xx \leftarrow xx - 1$ ;  $Str(xx, sx)$ ;  $a1[k - 1] \leftarrow sx[1]$ ;
    end
  else begin  $a1[k - 1] \leftarrow \_9\_$ ;  $borrow(k - 1)$ ;
    end;
  end;

```

This code is used in section 144.

146. Multiplication. Multiplication of a by b works digit-by-digit, in the sense that for each digit b_i of b , we need to multiply a by b_i . The function `_Mul1` does this.

(Arithmetic for arbitrary-precision integers 143) +≡

```
function _Mul1( $a$  : String;  $y$  : integer): String;
var  $c, x, z, v$ : integer;  $i$ : integer;  $s, r$ : String;
begin
  @{{@&$IFDEF DEBUGNUM@}} WriteLn(infile, '_Mul1(' ,  $a$  , ' ,  $y$  , ' ) ');
  @{{@&$ENDIF@}}  $r \leftarrow ''$ ;  $c \leftarrow 0$ ;
  begin
    for  $i \leftarrow 0$  to length( $a$ ) - 1 do
      begin val( $a$ [length( $a$ ) -  $i$ ],  $x, z$ );
        if  $x * y + c > 9$  then
          begin  $v \leftarrow (x * y + c) \bmod 10$ ;  $c \leftarrow (x * y + c) \div 10$ ; end
        else begin  $v \leftarrow x * y + c$ ;  $c \leftarrow 0$ ; end;
        Str( $v, s$ );  $r \leftarrow s + r$ ;
        end;
      if  $c \neq 0$  then
        begin Str( $c, s$ );  $r \leftarrow s + r$ ; end;

    end;
    _mul1  $\leftarrow$  trimlz( $r$ );
  end;
```

147. Then multiplication proper amounts to decomposing b into its decimal expansion $\sum_k b_k 10^k$ and computing $(a \times b_k) 10^k$.

```
function _Mul( $a, b$  : String): String;
var  $y, z$ : integer;  $i, j$ : integer;  $a1, b1, s, r$ : String;
begin
   $a1 \leftarrow a$ ;  $b1 \leftarrow b$ ;
  @{{@&$IFDEF DEBUGNUM@}} WriteLn(infile, '_Mul(' ,  $a1$  , ' ,  $b1$  , ' ) ');
  @{{@&$ENDIF@}} checkzero( $a1, b1$ );
  if length( $a1$ ) < length( $b1$ ) then
    begin  $s \leftarrow b1$ ;  $b1 \leftarrow a1$ ;  $a1 \leftarrow s$ ; end;
   $r \leftarrow '0'$ ;
  for  $i \leftarrow 0$  to length( $b1$ ) - 1 do
    begin val( $b1$ [length( $b1$ ) -  $i$ ],  $y, z$ );  $s \leftarrow$  _mul1( $a1, y$ );
      for  $j \leftarrow 0$  to  $i - 1$  do  $s \leftarrow s + '0'$ ;
       $r \leftarrow$  _Add( $r, s$ );
    end;
  _Mul  $\leftarrow$  trimlz( $r$ );
end;
```

148. Division. The basic design is similar to multiplication. We will try to divide a by $b \times 10^k$ (which is zero whenever $b \times 10^k > a$).

```
function _Div1(a, b : String): String;
  var i: integer; r: String;
  begin
    @{{IFDEF DEBUGNUM@}} WriteLn(Infofile, ' _Div1(' , a, ' , ' , b, ' ) ');
    @{{ENDIF@}} checkzero(a, b);
    if ¬_leq(b, a) then _div1 ← '0'
    else for i ← 9 downto 1 do
      begin Str(i, r);
        if _leq(_mul(b, r), a) then
          begin _div1 ← trimlz(r); exit; end;
        end;
      end;
    end;
```

149.

```
function _Div(a, b : String): String;
  var z, c, i: integer; s, r, rs: String; b_GPC: boolean;
  ⟨ Get the next digit for dividing arbitrary-precision integers 150 ⟩
  begin
    @{{IFDEF DEBUGNUM@}} WriteLn(Infofile, ' _Div(' , a, ' , ' , b, ' ) ');
    @{{ENDIF@}} checkzero(a, b);
    if a = b then _div ← '1'
    else if ¬_leq(b, a) then _div ← '0'
    else begin s ← ''; r ← ''; z ← 1;
      for i ← 1 to length(b) do s ← s + a[i];
        if ¬_leq(b, s) then
          begin s ← s + a[length(b) + 1]; z ← length(b) + 1; end
        else begin z ← length(b); end;
      repeat rs ← _div1(s, b); r ← r + rs; gets; b_GPC ← _leq(b, s);
      until ¬b_GPC;
      _div ← trimlz(r);
    end;
  end;
```

150. \langle Get the next digit for dividing arbitrary-precision integers 150 $\rangle \equiv$

```

procedure gets;
  var j: integer;
  begin c  $\leftarrow$  1; s  $\leftarrow$  _Sub(s, _mul(rs, b));
  if (s = '0')  $\wedge$  (trimlz(copy(a, z + c, length(a))) = '0') then
    begin @{{IFDEF DEBUGNUM@}} WriteLn(infile, 'Rewriting zeros: ', copy(a, z + c, length(a)));
    @{{ENDIF@}} r  $\leftarrow$  r + copy(a, z + c, length(a)); exit;
    end;
  if z + 1  $\leq$  length(a) then
    begin s  $\leftarrow$  s + a[z + 1]; inc(c);
    if ( $\neg$ _leq(b, s)) then r  $\leftarrow$  r + '0';
    end;
  while ( $\neg$ _leq(b, s))  $\wedge$  (z + c  $\leq$  length(a)) do
    begin s  $\leftarrow$  s + a[z + c]; inc(c);
    if ( $\neg$ _leq(b, s)) then r  $\leftarrow$  r + '0';
    end;
  z  $\leftarrow$  z + c - 1;
  end; { gets }

```

This code is used in section 149.

151. Modulo. We can compute $a \bmod b$ by observing if $a < b$ then we should obtain a . Otherwise, we should compute $r \leftarrow a \div b$, then $a - rb$ is $a \bmod b$.

\langle Arithmetic for arbitrary-precision integers 143 $\rangle + \equiv$

```

function _Mod(a, b : String): String;
  var r: String;
  begin @{{IFDEF DEBUGNUM@}} WriteLn(infile, ' _Mod(' , a, ', ', b, ') ');
  @{{ENDIF@}} checkzero(a, b);
  if le(a, b) then r  $\leftarrow$  a
  else r  $\leftarrow$  _Sub(a, _mul(b, _div(a, b)));
  _Mod  $\leftarrow$  trimlz(r);
  @{{IFDEF DEBUGNUM@}} WriteLn(infile, ' End _Mod: ', r);
  @{{ENDIF@}}
  end;

```

152. Greatest common divisor. We can compute $\gcd(a, b)$ first by setting $a_1 \leftarrow |a|$ and $b_1 \leftarrow |b|$ (since $\gcd(a, b) = \gcd(|a|, |b|)$). Then we handle the special cases:

- (1) $a_1 = 1$ or $b_1 = 1$, then $\gcd(a_1, b_1) = 1$
- (2) $a_1 = 0$ and $b_1 \neq 0$, then $\gcd(a_1, b_1) = b_1$
- (3) $a_1 \neq 0$ and $b_1 = 0$, then $\gcd(a_1, b_1) = a_1$
- (4) $a_1 = b_1$, then $\gcd(a_1, b_1) = a_1$

Otherwise, we end up in the default case, which is handled by the **while** loop.

```
function GCD(a, b : String): String;
  label ex;
  var a1, b1, p, r: String;
  begin a1 ← a; b1 ← b;
  @{$IFDEF DEBUGNUM@} WriteLn(Infofile, 'GCD(' , a1 , ', ' , b1 , ') ');
  @{$ENDIF@} checkzero(a1, b1); a1 ← abs(a1); b1 ← abs(b1);
  if (a1 = '1') ∨ (b1 = '1') then
    begin r ← '1'; goto ex; end;
  if (a1 = '0') ∧ (b1 ≠ '0') then
    begin r ← b1; goto ex; end;
  if (b1 = '0') ∧ (a1 ≠ '0') then
    begin r ← a1; goto ex; end;
  if a1 = b1 then
    begin GCD ← a1; r ← a1; goto ex; end;
  while gt(b1, '0') do
    begin p ← b1; b1 ← _mod(a1, b1); a1 ← p end;
  r ← a1;
ex: GCD ← r;
  @{$IFDEF DEBUGNUM@} WriteLn(Infofile, 'End_GCD: ' , r);
  @{$ENDIF@}
end;
```

153. Least common multiple. We recall $\text{lcm}(a, b) = |ab| / \gcd(|a|, |b|)$.

```
function LCM(a, b : String): String;
  var a1, b1, r: String;
  begin a1 ← a; b1 ← b;
  @{$IFDEF DEBUGNUM@} WriteLn(Infofile, 'LCM(' , a1 , ', ' , b1 , ') ');
  @{$ENDIF@} checkzero(a1, b1); a1 ← abs(a1); b1 ← abs(b1);
  r ← Diva(Mul(a1, b1), GCD(a1, b1)); LCM ← r;
  @{$IFDEF DEBUGNUM@} WriteLn(Infofile, 'End_LCM: ' , r);
  @{$ENDIF@}
end;
```


154. Addition. This is a bit obfuscated with the reliance of **goto** *ex*, but the basic idea is (recalling that $_Sub(a, b)$ calculates $\max(a, b) - \min(a, b)$ for $a \geq 0$ and $b \geq 0$):

- (1) If $a < 0$ and $b < 0$, then $a + b = -(|a| + |b|)$
- (2) Else if $a \geq 0$ and $b \geq 0$, then $a + b$ is computed using $_Add$
- (3) Else if $a < 0$ and $b \geq 0$, then we have two cases
 - (i) If $|a| \geq b$, compute $a + b = -(|a| - b)$
 - (ii) Otherwise, $a + b = b - |a|$
- (4) Else if $a \geq 0$ and $b < 0$, then $a + b = a - |b|$
- (5) Otherwise, when $a \geq 0$ and $b \geq 0$, $a + b$ is computed using $_Add$.

```

function Add(a, b : String) : String;
  label ex;
  var r : String;
  begin @{{IFDEF DEBUGNUM@} WriteLn(infile, 'Add(' , a, ' , ' , b, ' ) ');
```

@{{ENDIF@} checkzero(*a, b*);

```

  if (a[1] = '-' )  $\wedge$  (b[1] = '-' ) then
    begin r  $\leftarrow$  '-' +  $\_Add(abs(a), abs(b))$ ;
    if r = '-0' then r  $\leftarrow$  '0';
    goto ex;
    end;
  if (a[1]  $\neq$  '-' )  $\wedge$  (b[1]  $\neq$  '-' ) then
    begin r  $\leftarrow$   $\_Add(a, b)$ ; goto ex; end;
  if (a[1] = '-' )  $\wedge$  (b[1]  $\neq$  '-' ) then
    if gt(abs(a), b) then
      begin r  $\leftarrow$  '-' +  $\_Sub(abs(a), b)$ ;
      if r = '-0' then r  $\leftarrow$  '0';
      goto ex;
      end
    else begin r  $\leftarrow$   $\_Sub(abs(a), b)$ ; goto ex; end;
  if (a[1]  $\neq$  '-' )  $\wedge$  (b[1] = '-' ) then
    if gt(abs(b), a) then
      begin r  $\leftarrow$  '-' +  $\_Sub(abs(b), a)$ ;
      if r = '-0' then r  $\leftarrow$  '0';
      goto ex;
      end
    else begin r  $\leftarrow$   $\_Sub(abs(b), a)$ ; goto ex; end;
  ex: Add  $\leftarrow$  r;
  @{{IFDEF DEBUGNUM@} WriteLn(infile, 'End_Add: ' , r);
  @{{ENDIF@}
  end;

```

155. Subtraction. Now, given two arbitrary precision integers, we can compute their difference. Again, **goto** *ex* obfuscates the flow here, but the basic logic is:

- (1) If $a < 0$ and $b \geq 0$, then $a - b = -(|a| + b)$
- (2) Else if $a \geq 0$ and $b < 0$, then $a - b = a + |b|$
- (3) Else if $a < 0$ and $b < 0$, then we have two cases
 - (i) If $|a| > |b|$, then $a - b = -(|a| - |b|)$
 - (ii) Otherwise $|a| \leq |b|$, so $a - b = |a| - |b|$
- (4) Else if $a \geq 0$ and $b \geq 0$, then we have two cases
 - (i) If $b > a$, then $a - b = -(b - a)$
 - (ii) Otherwise compute $a - b$ using $_Sub(a, b)$

Testing if $x < 0$ is done by checking $\text{sgn}(x) = -1$, and $x \geq 0$ tests if $\text{sgn}(x) \neq -1$.

```

function Sub(a, b : String): String;
  label ex;
  var r: String;
  begin @{$$IFDEF DEBUGNUM@} WriteLn(infofile, 'Sub(' , a, ', ' , b, ') ');
  @{$$ENDIF@} checkzero(a, b);
  if (a[1] = '-' )  $\wedge$  (b[1]  $\neq$  '-') then
    begin r  $\leftarrow$  '-' + Add(abs(a), b);
    if r = '-0' then r  $\leftarrow$  '0';
    goto ex;
    end;
  if (a[1]  $\neq$  '-')  $\wedge$  (b[1] = '-') then
    begin r  $\leftarrow$  Add(a, abs(b)); goto ex; end;
  if (a[1] = '-')  $\wedge$  (b[1] = '-') then
    if gt(abs(a), abs(b)) then
      begin r  $\leftarrow$  '-' + Sub(abs(a), abs(b));
      if r = '-0' then r  $\leftarrow$  '0';
      goto ex;
      end
    else begin r  $\leftarrow$  Sub(abs(a), abs(b)); goto ex; end;
  if (a[1]  $\neq$  '-')  $\wedge$  (b[1]  $\neq$  '-') then
    if gt(b, a) then
      begin r  $\leftarrow$  '-' + Sub(b, a);
      if r = '-0' then r  $\leftarrow$  '0';
      goto ex;
      end
    else begin r  $\leftarrow$  Sub(a, b); goto ex; end;
  ex: Sub  $\leftarrow$  r;
  @{$$IFDEF DEBUGNUM@} WriteLn(infofile, 'End_Sub: ' , r);
  @{$$ENDIF@}
  end;

```

156. Multiplication of arbitrary-precision integers. We calculate the product of a with b by handling the case where $\text{sgn}(a) \neq \text{sgn}(b)$ as $ab = -|a| \cdot |b|$. Otherwise we can just rely on the $_Mul(a, b)$ to do our work.

```

function  $Mul(a, b : String)$ :  $String$ ;
  label  $ex$ ;
  var  $r$ :  $String$ ;
  begin @&&$IFDEF DEBUGNUM@ WriteLn( $infile$ , 'Mul(' ,  $a$ , ' , ' ,  $b$ , ') ');
  @&&$ENDIF@ checkzero( $a, b$ );
  if (( $a[1] = '-'$ )  $\wedge$  ( $b[1] \neq '-'$ ))  $\vee$  (( $a[1] \neq '-'$ )  $\wedge$  ( $b[1] = '-'$ )) then
    begin  $r \leftarrow '-' + \_Mul(abs(a), abs(b))$ ;
    if  $r = '-0'$  then  $r \leftarrow '0'$ ;
    end
  else  $r \leftarrow \_Mul(abs(a), abs(b))$ ;
 $ex$ :  $Mul \leftarrow r$ ;
  @&&$IFDEF DEBUGNUM@ WriteLn( $infile$ , 'End_Mul: ' ,  $r$ );
  @&&$ENDIF@
end;

```

157. DivA. This is the division for arbitrary-precision integers. Like multiplication, we handle the case $\text{sgn}(a) \neq \text{sgn}(b)$ by computing $a/b = -|a|/|b|$.

```

function  $DivA(a, b : String)$ :  $String$ ;
  label  $ex$ ;
  var  $r$ :  $String$ ;
  begin @&&$IFDEF DEBUGNUM@ WriteLn( $infile$ , 'DivA(' ,  $a$ , ' , ' ,  $b$ , ') ');
  @&&$ENDIF@ checkzero( $a, b$ );
  if (( $a[1] = '-'$ )  $\wedge$  ( $b[1] \neq '-'$ ))  $\vee$  (( $a[1] \neq '-'$ )  $\wedge$  ( $b[1] = '-'$ )) then
    begin  $r \leftarrow '-' + \_Div(abs(a), abs(b))$ ;
    if  $r = '-0'$  then  $r \leftarrow '0'$ ;
    end
  else  $r \leftarrow \_Div(abs(a), abs(b))$ ;
 $ex$ :  $DivA \leftarrow r$ ;
  @&&$IFDEF DEBUGNUM@ WriteLn( $infile$ , 'End_DivA: ' ,  $r$ );
  @&&$ENDIF@
end;

```

158. Testing for primality. We can test if a given arbitrary-precision integer is prime or not. Specifically, we restrict attention to *positive* integers.

The **while** loop calculates $Mul(i, i)$ because Fermat observed we only need to check numbers *up to* $\lceil \sqrt{x} \rceil$ as prime factors of x . But this calculation is a bit costly. This could be approximated by taking the length of the underlying String $n = |s|$ and looking at the leading $\lceil n/2 \rceil$ digits s_{lead} . It's not hard to see that the number x_{lead} described by s_{lead} satisfies $x_{lead}^2 \geq x$.

```
function IsPrime(a : String): boolean;
  var i: String; r: boolean;
  begin if leq(`2`, a) then
    begin r ← true; i ← `2`;
    while leq(Mul(i, i), a) do
      begin if GCD(a, i) = i then
        begin r ← false; break; end;
        i ← Add(i, `1`);
      end;
    end
  else r ← false;
  IsPrime ← r;
end;
```

159. Divides relation. We can check if “ x divides y ” by testing if $\gcd(x, y) = |x|$.

```
function Divides(a, b : String): boolean;
  var r: boolean;
  begin r ← GCD(a, b) = abs(a); Divides ← r;
end;
```

160. Rational arithmetic. Now we begin the rational arithmetic “in earnest”. The first thing to do is provide a way to compute the reduced form for a fraction, i.e.,

$$\frac{n}{d} = \frac{n/\gcd(n, d)}{d/\gcd(n, d)}$$

⟨ Arbitrary-precision rational arithmetic 160 ⟩ ≡

```
procedure RationalReduce(var r : Rational);
  var lGcd: String;
  begin lGcd ← gcd(r.Num, r.Den); r.Num ← diva(r.Num, lGcd); r.Den ← diva(r.Den, lGcd);
end;
```

This code is used in section 128.

161. Rational addition. We recall

$$\frac{a}{b} + \frac{c}{d} = \frac{ad + bc}{bd}$$

```
function RationalAdd(const r1, r2: Rational): Rational;
  var lRes: Rational;
  begin lRes.Num ← Add(Mul(r1.Num, r2.Den), Mul(r1.Den, r2.Num));
  lRes.Den ← Mul(r1.Den, r2.Den); RationalReduce(lRes); RationalAdd ← lRes;
end;
```

162. Rational subtraction. Similar to addition, but the numerator is $ad - bc$.

```
function RationalSub(const r1, r2: Rational): Rational;
  var lRes: Rational;
  begin lRes.Num ← Sub(Mul(r1.Num, r2.Den), Mul(r1.Den, r2.Num));
  lRes.Den ← Mul(r1.Den, r2.Den); RationalReduce(lRes); RationalSub ← lRes;
end;
```

163. Negating a rational number amounts to multiplying the numerator by -1 .

```
function RationalNeg(const r1: Rational): Rational;
  var lRes: Rational;
  begin lRes.Num ← Mul(ˆ-1ˆ, r1.Num); lRes.Den ← r1.Den; RationalNeg ← lRes;
end;
```

164. Multiplying rational numbers. This uses the school-book formula

$$\frac{a}{b} \times \frac{c}{d} = \frac{ac}{bd}$$

```
function RationalMult(const r1, r2: Rational): Rational;
  var lRes: Rational;
  begin lRes.Num ← Mul(r1.Num, r2.Num); lRes.Den ← Mul(r1.Den, r2.Den); RationalReduce(lRes);
  RationalMult ← lRes;
end;
```

165. Inverting a rational number. This is easy, provided the numerator is nonzero. The convention is to make the numerator carry the sign of the number (so n/d has $n \in \mathbf{Z}$ while $d \in \mathbf{N}$).

When the rational number *is* zero, we simply take $0^{-1} = 0$ (as is conventional among proof assistants).

```
function RationalInv(const r: Rational): Rational;
  var lRes: Rational;
  begin if r.Num ≠ ˆ0ˆ then
    begin if le(r.Num, ˆ0ˆ) then lRes.Num ← Mul(ˆ-1ˆ, r.Den)
    else lRes.Num ← r.Den;
    lRes.Den ← Abs(r.Num);
    end
  else lRes ← RZero;
  RationalInv ← lRes;
end;
```

166. Dividing rational numbers. We see that $r_1/r_2 = r_1 \times (r_2^{-1})$. That's the trick.

```
function RationalDiv(const r1, r2: Rational): Rational;
  begin RationalDiv ← RationalMult(r1, RationalInv(r2));
end;
```

167. Equality of rational numbers. Two rational numbers n_1/d_1 and n_2/d_2 are equal if $n_1 = n_2$ and $d_1 = d_2$. This assumes that both rational numbers are in reduced form.

```
function RationalEq(const r1, r2: Rational): boolean;
  begin RationalEq ← (r1.Num = r2.Num) ∧ (r1.Den = r2.Den);
end;
```

168. Testing inequality of rational numbers. We have $n_1/d_1 < n_2/d_2$ if $n_1d_2 < n_2d_1$.

Similarly, we have $n_1/d_1 \geq n_2/d_2$ is just the negation of $n_1/d_1 < n_2/d_2$. **But:** this is misleadingly called *RationalGT* instead of *RationalGEQ*.

```
function RationalLE(const r1, r2: Rational): boolean;
begin RationalLE ← leq(Mul(r1.Num, r2.Den), Mul(r1.Den, r2.Num));
end;
function RationalGT(const r1, r2: Rational): boolean;
begin RationalGT ← ¬RationalLE(r1, r2);
end;
```

169. Rational complex arbitrary-precision arithmetic. We now begin with $\mathbf{Q} + i\mathbf{Q} \subseteq \mathbf{C}$, the subset of complex-numbers where the real and imaginary parts are rational numbers.

We want to know when these numbers describe integers (i.e., the imaginary part is zero and the denominator of the real part is 1) and natural numbers (i.e., when furthermore the numerator of the real part is non-negative).

```
(Complex-rational arbitrary-precision arithmetic 169) ≡
function IsIntegerNumber(const z: RComplex): boolean;
begin IsIntegerNumber ← (z.Im.Num = '0') ∧ (z.Re.Den = '1'); end;
function IsNaturalNumber(const z: RComplex): boolean;
begin IsNaturalNumber ← (z.Im.Num = '0') ∧ (z.Re.Den = '1') ∧ (geq(z.Re.Num, '0')); end;
function IsPrimeNumber(const z: RComplex): boolean;
begin if IsNaturalNumber(z) ∧ IsPrime(z.Re.Num) then IsPrimeNumber ← true
else IsPrimeNumber ← false;
end;
```

This code is used in section 128.

170. Equality of complex numbers. This amounts to checking if the real and imaginary parts are equal to each other as rational numbers.

```
function AreEqComplex(const z1, z2: RComplex): boolean;
begin AreEqComplex ← RationalEq(z1.Re, z2.Re) ∧ RationalEq(z1.Im, z2.Im); end;
function IsEqWithInt(const z: RComplex;
                    n: longint): boolean;
var s: String;
begin Str(n, s); IsEqWithInt ← (z.Im.Num = '0') ∧ (z.Re.Num = s) ∧ (z.Re.Den = '1'); end;
```

171. “Inequalities”. We “induce” the binary relations $<$ and \geq on the subset $\{q + i0 \mid q \in \mathbf{Q}\} \subseteq \mathbf{C}$. Again, what we said earlier about *RationalGT* being badly named holds for *IsRationalGT* being badly named as well.

```
function IsRationalLE(const z1, z2: RComplex): boolean;
begin IsRationalLE ← (z1.Im.Num = '0') ∧ (z2.Im.Num = '0') ∧ RationalLE(z1.Re, z2.Re); end;
function IsRationalGT(const z1, z2: RComplex): boolean;
begin IsRationalGT ← (z1.Im.Num = '0') ∧ (z2.Im.Num = '0') ∧ RationalGT(z1.Re, z2.Re); end;
```

172. Converting integers to complex numbers. We have a function to convert an integer $x \in \mathbf{Z}$ to be the complex number $(x/1) + i(0/1) \in \mathbf{C}$.

```
function IntToComplex(x: integer): RComplex;
var lRes: RComplex;
begin lRes ← COne; lRes.Re.Num ← IntToStr(x); IntToComplex ← lRes;
end;
```

173. Adding complex numbers. We compute the sum of $(x_1 + iy_1)$ and $x_2 + iy_2$ to be $(x_1 + x_2) + i(y_1 + y_2)$.

```
function ComplexAdd(const z1, z2: RComplex): RComplex;
  var lRes: RComplex;
  begin lRes.Re ← RationalAdd(z1.Re, z2.Re); lRes.Im ← RationalAdd(z1.Im, z2.Im);
  @{$IFDEF CH_REPORT@}CHReport.Out_NumReq3(rqRealAdd, z1, z2, lRes);
  @{$ENDIF@}ComplexAdd ← lRes;
end;
```

174. Subtracting complex numbers. We find the difference of complex numbers componentwise.

```
function ComplexSub(const z1, z2: RComplex): RComplex;
  var lRes: RComplex;
  begin lRes.Re ← RationalSub(z1.Re, z2.Re); lRes.Im ← RationalSub(z1.Im, z2.Im);
  @{$IFDEF CH_REPORT@}CHReport.Out_NumReq3(rqRealDiff, z1, z2, lRes);
  @{$ENDIF@}ComplexSub ← lRes;
end;
```

175. Negating complex numbers. We negate a complex number $-z$ by negating its real and imaginary parts.

```
function ComplexNeg(const z: RComplex): RComplex;
  var lRes: RComplex;
  begin lRes.Re ← RationalNeg(z.Re); lRes.Im ← RationalNeg(z.Im);
  @{$IFDEF CH_REPORT@}CHReport.Out_NumReq2(rqRealNeg, z, lRes);
  @{$ENDIF@}ComplexNeg ← lRes;
end;
```

176. Multiplying complex numbers. We use the usual formula

$$(x_1 + iy_1)(x_2 + iy_2) = (x_1x_2 - y_1y_2) + i(x_1y_2 + y_1x_2).$$

```
function ComplexMult(const z1, z2: RComplex): RComplex;
  var lRes: RComplex;
  begin if IsEqWithInt(z1, -1) then ComplexMult ← ComplexNeg(z2)
  else if IsEqWithInt(z2, -1) then ComplexMult ← ComplexNeg(z1)
  else begin lRes.Re ← RationalSub(RationalMult(z1.Re, z2.Re), RationalMult(z1.Im, z2.Im));
    lRes.Im ← RationalAdd(RationalMult(z1.Re, z2.Im), RationalMult(z1.Im, z2.Re));
    ComplexMult ← lRes;
    @{$IFDEF CH_REPORT@}CHReport.Out_NumReq3(rqRealMult, z1, z2, lRes);
    @{$ENDIF@}
  end;
end;
```

177. Dividing complex numbers. We recall

$$\frac{x_1 + iy_1}{x_2 + iy_2} = \frac{(x_1 + iy_1)(x_2 - iy_2)}{x_2^2 + y_2^2}$$

This is the case for nonzero $z_2 \neq 0$. When we try to divide $z_1/0$, we return 0.

```

function ComplexDiv(const z1, z2: RComplex): RComplex;
  var lDenom: Rational; lRes: RComplex;
  begin lRes ← CZero;
  with z2 do lDenom ← RationalAdd(RationalMult(Re, Re), RationalMult(Im, Im));
  if lDenom.Num ≠ '0' then
    begin
      lRes.Re ← RationalDiv(RationalAdd(RationalMult(z1.Re, z2.Re), RationalMult(z1.Im, z2.Im)),
        lDenom);
      lRes.Im ← RationalDiv(RationalSub(RationalMult(z1.Im, z2.Re), RationalMult(z1.Re, z2.Im)),
        lDenom);
      @{@&$IFDEF CH_REPORT@}CHReport.Out_NumReq3(rqRealDiv, z1, z2, lRes);
      @{@&$ENDIF@}
    end;
    ComplexDiv ← lRes;
  end;

```

178. Inverting complex numbers. We can now calculate z^{-1} as just $1/z$.

```

function ComplexInv(const z: RComplex): RComplex;
  begin ComplexInv ← ComplexDiv(COne, z); end;

```

179. Norm of complex numbers. The “norm” or *modulus* for a complex number is just the sum of the square of its components (well, the squareroot of this sum).

```

function ComplexNorm(const z: RComplex): Rational;
  begin ComplexNorm ← RationalAdd(RationalMult(Z.Re, Z.Re), RationalMult(Z.Im, Z.Im)); end;

```

180. Comparison functions. The remainder of `numbers.pas` defines functions which compares numbers. These must return a value in the set $\{-1, 0, +1\}$ as a PASCAL *integer*.

```

function CompareInt(X1, X2: Longint): integer;
  begin if X1 = X2 then CompareInt ← 0
  else if X1 > X2 then CompareInt ← 1
  else CompareInt ← -1;
  end;

function CompareIntStr(X1, X2: String): integer;
  begin if X1 = X2 then CompareIntStr ← 0
  else if gt(X1, X2) then CompareIntStr ← 1
  else CompareIntStr ← -1;
  end;

```


181. There is also a function to “compare” complex numbers. This treats a complex number

$$z = \frac{n_1}{d_1} + i \frac{n_2}{d_2}$$

as a tuple (n_1, d_1, n_2, d_2) then uses lexicographic ordering based on the components.

```
function CompareComplex(const z1, z2: RComplex): integer;
  var Unt: integer;
  begin Unt ← CompareIntStr(z1.Re.Num, z2.Re.Num);
  if Unt ≠ 0 then
    begin CompareComplex ← Unt; exit end;
  Unt ← CompareIntStr(z1.Re.Den, z2.Re.Den);
  if Unt ≠ 0 then
    begin CompareComplex ← Unt; exit end;
  Unt ← CompareIntStr(z1.Im.Num, z2.Im.Num);
  if Unt ≠ 0 then
    begin CompareComplex ← Unt; exit end;
  CompareComplex ← CompareIntStr(z1.Im.Den, z2.Im.Den);
end;
```

File 9

Mizar Objects and Data Structures

182. This is one of the largest files in Mizar (it clocks in at 6594 lines of code). Its interface consists of 552 lines alone (roughly 1/13 of the file).

```

⟨ mobjects.pas 182 ⟩ ≡
  ⟨ GNU License 4 ⟩
unit mobjects;
  interface
    uses numbers;
    ⟨ Public interface for mobjects.pas 184 ⟩
  implementation
    mdebug uses info;
  end_mdebug
  ⟨ Implementation for mobjects.pas 183 ⟩
end ;

```

183. We have an error method for situations when a method is not implemented, for example when there is no ordering operator when the user invokes *MSortedCollection.Compare* (§288).

```

⟨ Implementation for mobjects.pas 183 ⟩ ≡
procedure Abstract1;
  begin RunError(211);
  end;
  ⟨ MObject implementation 187 ⟩
  ⟨ MStrObj implementation 192 ⟩
  ⟨ MList implementation 196 ⟩
  ⟨ MCollection implementation 220 ⟩
  ⟨ MExtList implementation 236 ⟩
  ⟨ MSortedList implementation 251 ⟩
  ⟨ MSortedExtList implementation 268 ⟩
  ⟨ MSortedStrList implementation 282 ⟩
  ⟨ MSortedCollection implementation 287 ⟩
  ⟨ String collection implementation 296 ⟩
  ⟨ MIntCollection implementation 300 ⟩
  ⟨ Stacked object implementation 308 ⟩
  ⟨ String list implementation 310 ⟩
  ⟨ Int relation implementation 351 ⟩
  ⟨ Partial integer function implementation 360 ⟩
  ⟨ NatFunc implementation 380 ⟩
  ⟨ NatSeq implementation 398 ⟩
  ⟨ IntSequence implementation 403 ⟩
  ⟨ IntSet Implementation 419 ⟩
  ⟨ Partial Binary integer Functions 430 ⟩
  ⟨ Partial integers to Pair of integers Functions 448 ⟩

```

This code is used in section 182.

184. Constant parameters.

(Public interface for `mobjects.pas` 184) \equiv
const { Maximum MCollection size }
MaxSize = 2000000;
MaxCollectionSize = *MaxSize* **div** *SizeOf(Pointer)*;
 { Maximum MStringList size }
MaxListSize = *MaxSize* **div** (*SizeOf(Pointer)* * 2);
 { Maximum IntegerList size }
MaxIntegerListSize = *MaxSize* **div** (*SizeOf(integer)*);
 { MCollection error codes }
coIndexError = -1; { Index out of range }
coOverflow = -2; { Overflow }
coConsistentError = -3;
coDuplicate = -5; { Duplicate }
coSortedListError = -6;
coIndexExtError = -7;

See also sections 185, 186, 191, 194, 195, 219, 235, 250, 267, 281, 286, 295, 299, 307, 309, 340, 341, 350, 359, 379, 397, 402, 418, 429, 447, and 461.

This code is used in section 182.

185. Type aliases.

(Public interface for `mobjects.pas` 184) $+ \equiv$
type { String pointers }
PString = \uparrow *ShortString*;
 { Character set type }
PCharSet = \uparrow *TCharSet*;
TCharSet = **set of** *char*;
 { General arrays }
PByteArray = \uparrow *TByteArray*;
TByteArray = **array** [0 .. 32767] **of** *byte*; { $32767 = 2^{15} - 1$ }
PWordArray = \uparrow *TWordArray*;
TWordArray = **array** [0 .. 16383] **of** *word*; { $16383 = 2^{14} - 1$ }

Section 9.1. BASE OBJECT

186. Object-oriented PASCAL is a bit crufty (like all Object-oriented ALGOL-descended languages).

The base *MObject* “class” has a constructor, destructor, a clone function named *CopyObject*, and a “move” function called *MCopy*.

```

⟨Public interface for mobjects.pas 184⟩ +≡
  { MObject base object }
  PObject = ↑MObject;
  ObjectPtr = PObject;
  MObject = object
    constructor Init;
    procedure Free;
    destructor Done; virtual;
    function CopyObject: PObject;
    function MCopy: PObject; virtual;
  end ;

```

187. Note that the *VER70* conditional compilation only plays a role here, in *MObject.Init*.

The constructor will initialize the memory allocated for the *MObject* to be zero.

```

⟨ MObject implementation 187 ⟩ ≡
  { MObject }
constructor MObject.Init;
  @{@&$IFDEF VER70@}
  type Image = record Link: word;
    Data: record
      end;
    end;
  @{@&$ENDIF@}
  begin
    @{@&$IFDEF VER70@} FillChar(Image(Self).Data, SizeOf(Self) - SizeOf(MObject), 0);
    @{@&$ENDIF@}
  end;

```

This code is used in section 183.

188. Destructor. The *MObject.Free* procedure frees all the memory allocated to the caller.

The destructor is, well, what C++ programmers would call an “abstract method”.

```

procedure MObject.Free;
  begin Dispose(PObject(@Self), Done); end;
destructor MObject.Done;
  begin end;

```

189. Copying an object allocates new memory using the Free PASCAL *GetMem* function, then *moves* the contents of the caller to the new region. It **does not** “copy” the contents of the caller to the new region. If we wanted to copy the contents of the caller, we should call something like *Fillchar* or *Fillword*.

It then returns a pointer to the newly allocated object.

```

function MObject.CopyObject: PObject;
  var lObject: PObject;
  begin GetMem(lObject, SizeOf(Self)); Move(Self, lObject↑, SizeOf(Self)); CopyObject ← lObject;
  end;

```

190. The virtual method for copying Mizar objects can be overridden by subclasses. But the default method is just *CopyObject*.

```
function MObject.MCopy: PObject;  
  begin MCopy  $\leftarrow$  CopyObject; end;
```

Section 9.2. MIZAR STRING OBJECT

191. Strings in Mizar amount to a wrapper around the underlying string data type.

```

⟨ Public interface for mobjects.pas 184 ⟩ +≡
  { Specyfif objects based on MObjects for collections }
  PStr = ↑MStrObj;
  MStrPtr = PStr;
  MStrObj = object (MObject)
    fStr: String;
    constructor Init(const aStr: String);
  end ;

```

192. Constructor. The constructor for a string object expects a string, and simply initializes its contents to the given string.

```

⟨ MStrObj implementation 192 ⟩ ≡
  { Specyfif objects based on MObjects for collections }
constructor MStrObj.Init(const aStr: String);
  begin fStr ← aStr; end;

```

This code is used in section 183.

Section 9.3. MIZAR LIST

193. A *MList* is a dynamic array data structure, which represents a list using an array. We reserve an array whose length is referred to as its “**Capacity**” in the literature.

Not all of the underlying array is used by the user. The number of entries which are used by the dynamic array contents is referred to as its “**Logical Size**” (or just its *Size*) in the literature.

When the dynamic array is filled, it “grows”; i.e., it allocates a new array that’s larger, and copies over the contents of its old array, then frees the old array. The growth factor is controlled by the *GrowLimit*(*oldSize*) value.

194. Review of pointers in Pascal. We have a few parameters needed for collections. Remember, if T is a type, then $\uparrow T$ is the type of pointers to T objects. If we want to have a pointer without referring to the *type* of the object referenced, we can use *Pointer*.

The @ operator is the “address of” operator. When setting a pointer p to point to something Foo , we have $p \leftarrow @Foo$.

The \uparrow operator is the “dereferencing” operator which is appended to a pointer identifier. When we want to update the object referenced by a pointer p , we have $p\uparrow \leftarrow newValue$.

```

⟨Public interface for mobjects.pas 184⟩ +≡
  { MCollection types }
  PItemList =  $\uparrow$ MItemList;
  MItemList = array [0 .. MaxCollectionSize - 1] of Pointer;

```

195. A *MList* object is known as a dynamic array. Java programmers would know that as an *ArrayList*.

```

⟨Public interface for mobjects.pas 184⟩ +≡
  { MList object }
  PList = ↑MList;
  MListPtr = PList;
  MList = object (MObject)
    Items: PItemList; { Contents of dynamic array }
    Count: integer; { Logical size of dynamic array }
    Limit: integer; { Capacity of dynamic array }
    constructor Init(ALimit : integer);
    constructor MoveList(var aAnother : MList);
    constructor CopyList(var aAnother : MList);
    destructor Done; virtual;
    function MCopy: PObject; virtual;
    procedure ListError(aCode, aInfo : integer); virtual;
    function At(Index : integer): Pointer;
    function Last: Pointer;
    procedure Insert(aItem : Pointer); virtual;
    procedure AtInsert(aIndex : integer; aItem : Pointer); virtual;
    procedure InsertList(var aAnother : MList); virtual;
    function GetObject(aIndex : integer): Pointer; virtual;
    function IndexOf(aItem : Pointer): integer; virtual;
    procedure DeleteAll; virtual;
    procedure FreeItem(Item : Pointer); virtual;
    procedure FreeAll; virtual;
    procedure FreeItemsFrom(aIndex : integer); virtual;
    procedure Pack; virtual;
    procedure SetLimit(ALimit : integer); virtual;
    procedure AppendTo(var fAnother : MList); virtual;
    procedure TransferItems(var fAnother : MList); virtual;
    procedure CopyItems(var fOrigin : MList); virtual;
end ;

```


196. Growth factor. How quickly an Dynamic Array grows is a subject of debate. Just for a table of the growth factors:

Implementation	Growth Factor
Java's ArrayList	$3/2 = 1.5$
Microsoft's Visual C++	$3/2 = 1.5$
Facebook folly/FBVector	$3/2 = 1.5$
Unreal Engine's TArray	$n + ((3n) \gg 3) \sim 1.375$
Python PyListObject	$n + (n \gg 3) \sim 1.125$
Go slices	between 1.25 and 2
Gnu C++	2
Clang	2
Rust's Vec	2
Nim sequences	2
SBCL vectors	2
C#	2

The *MList* uses a staggered growth factor, specifically something like $s(n) \leftarrow s(n) + \text{GrowLimit}(s(n))$. The sequence of Dynamic Array size would be:

$$s(n) = (0, 4, 8, 12, 28, 44, 60, 76, \dots)$$

followed by $s(n+1) \leftarrow (5/4)s(n)$. I am not sure this is optimal, but I have no better solution.

CAUTION: If the memory allocator uses a first-fit allocation, then growth factors like $\alpha \geq 2$ can cause dynamic array expansion to run out of memory even though a significant amount of memory may still be available. For a discussion about this point, see:

- <http://www.gahcep.com/cpp-internals-stl-vector-part-1/>

It seems that a growth factor $\alpha \leq \varphi = (1 + \sqrt{5})/2$ must be not bigger than the golden ratio. To see this, we need a dyanmic array of size S to have its first growth to allocate αS , then frees up the S bytes from the pre-growth allocation. The second allocation needs $\alpha^2 S$ bytes. Observe the first two allocations requires $S + \alpha S$ bytes available. Now suppose we want this to be able to fit into the newly freed space,

$$\alpha^2 S \leq S + \alpha S$$

which means

$$\alpha^2 - \alpha + 1 \leq 0$$

or (requiring $\alpha > 0$)

$$\alpha \leq \varphi = \frac{1 + \sqrt{5}}{2}.$$

When this fails to hold, a first-fit allocation could run out of memory.

$\langle \textit{MList}$ implementation 196 $\rangle \equiv$

{ Simple Collection }

function *GrowLimit*(*aLimit* : integer): integer;

begin *GrowLimit* \leftarrow 4;

if *aLimit* > 64 **then** *GrowLimit* \leftarrow *aLimit* **div** 4

else if *aLimit* > 8 **then** *GrowLimit* \leftarrow 16;

end;

This code is used in section 183.

197. Constructor. The constructor creates an empty list.

constructor *MList.Init*(*aLimit* : integer);

begin *MObject.Init*; *Items* \leftarrow nil; *Count* \leftarrow 0; *Limit* \leftarrow 0; *SetLimit*(*aLimit*); **end**;

198. Moving a list into the caller.

```
constructor MList.MoveList(var aAnother : MList);
  begin MObject.Init;
    Count  $\leftarrow$  aAnother.Count; Limit  $\leftarrow$  aAnother.Limit; Items  $\leftarrow$  aAnother.Items; { move }
    aAnother.DeleteAll; aAnother.Limit  $\leftarrow$  0; aAnother.Items  $\leftarrow$  nil; { delete aAnother }
  end;
```

199. Copying the contents of *aAnother* list into the current list will essentially reinitialize the current list, the insert all items from the other list into the current list.

```
constructor MList.CopyList(var aAnother : MList);
  begin MObject.Init; Items  $\leftarrow$  nil; Count  $\leftarrow$  0; Limit  $\leftarrow$  0; { initialize }
    SetLimit(aAnother.Limit); InsertList(aAnother);
  end;
```

200. A list is “done” frees all items in the list, sets the limit to zero, and then invokes the superclass’s *Done* method.

```
destructor MList.Done;
  begin FreeAll; SetLimit(0); inherited Done; end;
```

201. We override the *MObject.MCopy* method (§190). This will copy the base object using *CopyObject* (§189), allocate a new array of pointers, copy over the contents of the caller, and then returns the new list.

```
function MList.MCopy: PObject;
  var lList: PObject; i: integer;
  begin lList  $\leftarrow$  CopyObject; GetMem(PList(lList) $\uparrow$ .Items, Self.Limit * SizeOf(Pointer));
  for i  $\leftarrow$  0 to Self.Count - 1 do PList(lList) $\uparrow$ .Items $\uparrow$ [i]  $\leftarrow$  PObject(Self.Items $\uparrow$ [i]) $\uparrow$ .MCopy;
  MCopy  $\leftarrow$  lList;
  end;
```

202. This is the same as *MList.GetObject* (§207), and I am not sure why we have two versions of the same function.

```
function MList.At(Index : integer): Pointer;
  begin if (Index < 0)  $\vee$  (Index  $\geq$  Count) then
    begin ListError(coIndexError, 0); At  $\leftarrow$  nil; end
  else At  $\leftarrow$  Items $\uparrow$ [Index];
  end;
```

203. The *MList.Count* tracks the number of allocated items. So the last item would be located at *MList.Count* - 1 (since we count with zero offset).

```
function MList.Last: Pointer;
  begin Last  $\leftarrow$  At(Count - 1); end;
```

204. Inserting an item into a list requires checking there’s enough free space to the list, then sets the first spot to the item.

```
procedure MList.Insert(aItem : Pointer);
  begin if Limit = Count then SetLimit(Limit + GrowLimit(Limit));
  Items $\uparrow$ [Count]  $\leftarrow$  aItem; inc(Count);
  end;
```

205. If we want to insert a pointer *at a specific index*, then we proceed as follows:

- (1) Check if the index is negative. If so, then we should flag an error using *ListError*, and exit.
- (2) Check if the index is larger than the logical size of the dynamic array; if so, then we grow the dynamic array using *SetLimit*

```

procedure MList.AtInsert(aIndex : integer; aItem : Pointer);
  var i, lLimit: integer;
  begin if aIndex < 0 then
    begin ListError(coIndexError, 0); exit;
    end;
  if (aIndex ≥ Limit) ∨ ((aIndex = Count) ∧ (Limit = Count)) then { ensure capacity }
    begin lLimit ← Limit + GrowLimit(Limit);
    while aIndex + 1 > lLimit do lLimit ← lLimit + GrowLimit(lLimit);
    SetLimit(lLimit); { Copy contents }
    end;
  for i ← Count to aIndex − 1 do Items↑[i] ← nil; { fill new entries as nil }
  Items↑[aIndex] ← aItem; { set the entry at aIndex to the pointer }
  if aIndex ≥ Count then Count ← aIndex + 1; { update logical size, if necessary }
  end;

```

206. When we insert *aAnother* list into the current list, we simply iterate through all the other list's items, and insert (a copy of the pointer to) each one into the current list. This should leave *aAnother* list unmodified.

```

procedure MList.InsertList(var aAnother : MList);
  var i: integer;
  begin for i ← 0 to pred(aAnother.Count) do Insert(PObject(aAnother.Items↑[i])↑.MCopy);
  end;

```

207. Given an index, find the item located there. Well, the pointer to the object. When the index is illegal (out of bounds or negative), then flag an error and return nil. Otherwise return the pointer located at the index.

```

function MList.GetObject(aIndex : integer): Pointer;
  begin if (aIndex < 0) ∨ (aIndex ≥ Count) then
    begin ListError(coIndexError, 0); GetObject ← nil; end
  else GetObject ← Items↑[aIndex];
  end;

```

208. We have a default error code for lists.

```

procedure MList.ListError(aCode, aInfo : integer);
  begin RunError(212 − aCode); end;

```

209. Looking for the index of an item requires iterating through each item of the list, until we find the needle in the haystack. Once found, we return the index for the needle.

If the needle is not in the haystack, return −1.

```

function MList.IndexOf(aItem : Pointer): integer;
  var i: integer;
  begin IndexOf ← −1;
  for i ← 0 to pred(Count) do
    if aItem = Items↑[i] then
      begin IndexOf ← i; break end
  end;

```

210. Deleting all items from a list simply updates the list's logical size (i.e., *Count*) to zero. This will not alter the underlying array allocated for the dynamic array.

```
procedure MList.DeleteAll;  
  begin Count  $\leftarrow$  0; end;
```

211. Freeing a single item will invoke PASCAL's primitive *Dispose* function (which frees up the memory in heap). This is a helper function to avoid accidentally invoking *Dispose*(*PObject*(**nil**), *Done*) which would throw errors.

```
procedure MList.FreeItem(Item : Pointer);  
  begin if Item  $\neq$  nil then Dispose(PObject(Item), Done);  
  end;
```

212. We delegate all the heavy work of *FreeAll* to *FreeItemsFrom*.

```
procedure MList.FreeAll;  
  begin FreeItemsFrom(0); end;
```

213. We can iterate through a list from a start index, freeing the rest of the list starting from *aIndex*. Remember, the data structure for *MList* consists of an *MObject* extended with its capacity, logical size, and a *pointer* to the array on the heap. When freeing an item from the array, we dereference the pointer to look up item *I* in the array.

```
procedure MList.FreeItemsFrom(aIndex : integer);  
  var I: integer;  
  begin for I  $\leftarrow$  Count - 1 downto aIndex do FreeItem(Items $\uparrow$ [I]);  
  Count  $\leftarrow$  aIndex;  
  end;
```

214. If an item has become **nil** in the list, we should shift the rest of the list down. Basically, in Lisp, if null (cadr 1), then setf 1 (cdr 1).

Care must be taken to iterate over the items in the list. Shifting items down by one item requires iterating over *k* from *i* to *Count* - 2 (because the maximum index is *Count* - 1 due to zero offset indexing).

Once we have shifted everything down, we decrement the logical size of the dynamic array.

```
procedure MList.Pack;  
  var i, k: integer;  
  begin for i  $\leftarrow$  Count - 1 downto 0 do  
    if Items $\uparrow$ [i] = nil then  
      begin for k  $\leftarrow$  i to Count - 2 do Items $\uparrow$ [k]  $\leftarrow$  Items $\uparrow$ [k + 1];  
      dec(Count);  
      end;  
    end;  
  end;
```

215. Growing a list handles a few edgecases:

- (1) If the new limit is *smaller* than the existing limit, then just set the new limit equal to the existing limit.
- (2) If the new limit is *larger* than the maximum limit, then just set the new limit equal to the maximum limit.
- (3) If the new limit is not equal to the existing limit, then we have the “standard situation”.
 - (i) When the new limit is zero, simply set the pointer to the item list to **nil**
 - (ii) Otherwise (for a new limit which is a nonzero number), allocate a new chunk of memory for the number of pointers needed, then move them. Be sure to free up the pointers, and update the variables.

```

procedure MList.SetLimit(ALimit : integer);
  var UItems: PItemList;
  begin if ALimit < Count then ALimit ← Count;
  if ALimit > MaxCollectionSize then ALimit ← MaxCollectionSize;
  if ALimit ≠ Limit then
    begin if ALimit = 0 then UItems ← nil
    else begin GetMem(UItems, ALimit * SizeOf(Pointer));
      if ((Count) ≠ 0) ∧ (Items ≠ nil) then Move(Items↑, UItems↑, Count * SizeOf(Pointer));
      end;
      if Limit ≠ 0 then FreeMem(Items, Limit * SizeOf(Pointer));
      Items ← UItems; Limit ← ALimit;
    end;
  end;

```

216. Appending another list to the current list will expand the current list to support the new items, insert the other list’s items at the end of the current list, and then free the other list from memory.

```

procedure MList.AppendTo(var fAnother : MList);
  var k: integer;
  begin SetLimit(Count + fAnother.Count);
  for k ← 0 to fAnother.Count − 1 do Insert(fAnother.Items↑[k]);
  fAnother.DeleteAll; fAnother.Done;
  end;

```

217. There is a comment in Polish at the beginning of this function stating “Przeznaczeniem tej procedury jest uzycie jej w konstruktorach Move, ktore wykonuja jakgdyby pelna instrukcje przypisania (razem z VMTP)” which Google translates as “The purpose of this procedure is to be used in Move constructors, which execute a full assignment statement (including VMTP).”

There is also another comment in Polish, “Nie wolno uzyc SetLimit, bo rozdysponuje Items” which I translated into English and kept inline (“You cannot use SetLimit because it will distribute the Items”).

The semantics of *Object* ← *Object* will *copy* the right-hand side to the left-hand side.

```

procedure MList.TransferItems(var fAnother : MList);
  begin Self ← fAnother; { copy contents of fAnother over to Self }
  fAnother.DeleteAll; fAnother.Limit ← 0; fAnother.Items ← nil;
  { You cannot use SetLimit because it will distribute the Items. }
  end;

```

218. Copying items from a list simply loops through the original list, inserting them into the caller.

```

procedure MList.CopyItems(var fOrigin : MList);
  var i: integer;
  begin for i ← 0 to fOrigin.Count − 1 do Insert(PObject(fOrigin.Items↑[i]↑.CopyObject);
  end;

```

Section 9.4. MIZAR COLLECTION CLASS

219. Curiously, the “Collection” class extends the “List” class, which surprises me. This will change the growth rate from $s(n+1) = s(n) + \text{GrowLimit}(s(n))$ to be

$$s(n+1) = s(n) + \text{GrowLimit}(\Delta + s(n))$$

where $\Delta \geq 0$ is a field of the Collection object. When we move an *MList* into an *MCollection*, we have $\Delta \leftarrow 2$ be the default value.

```

⟨Public interface for mobjects.pas 184⟩ +=
  { MCollection object }
  PCollection = ↑MCollection;
  MCollection = object (MList)
    Delta: integer;
    constructor Init(ALimit, ADelta : integer);
    destructor Done; virtual;
    procedure AtDelete(Index : integer);
    procedure AtFree(Index : integer);
    procedure AtInsert(Index : integer; Item : Pointer); virtual;
    procedure AtPut(Index : integer; Item : Pointer);
    procedure Delete(Item : Pointer);
    procedure Free(Item : Pointer);
    procedure Insert(aItem : Pointer); virtual;
    procedure Pack; virtual;
    constructor MoveCollection(var fAnother : MCollection);
    constructor MoveList(var aAnother : MList);
    constructor CopyList(var aAnother : MList);
    constructor CopyCollection(var AAnother : MCollection);
    constructor Singleton(fSing : PObject; fDelta : integer);
    procedure Prune; virtual;
  end ;

```

220. Constructor. When constructing a new Collection, we allocate an array of the desired limit (using the *SetLimit* (§215) to handle this allocation).

```

⟨MCollection implementation 220⟩ ≡
  { MCollection }
constructor MCollection.Init(ALimit, ADelta : integer);
  begin MObject.Init; Items ← nil; Count ← 0; Limit ← 0; Delta ← ADelta; SetLimit(ALimit);
  end;
destructor MCollection.Done;
  begin FreeAll; SetLimit(0);
  end;

```

This code is used in section 183.

221. When trying to delete an element at *Index*, we first check if the *Index* is within the bounds of the collection. If it's out of bounds, we invoke *ListError* and exit the function.

Otherwise, we shift everything in the collection down by one position.

```
procedure MCollection.AtDelete(Index : integer);
  var i: integer;
  begin if (Index < 0)  $\vee$  (Index  $\geq$  Count) then
    begin ListError(coIndexError, 0); exit; end;
  if Index < pred(Count) then
    for i  $\leftarrow$  Index to Count - 2 do Items $\uparrow$ [i]  $\leftarrow$  Items $\uparrow$ [i + 1];
  Dec(Count);
  end;
```

222. If we want to also *free* an object in a collection, we store it in a temporary variable, then invoke *AtDelete*(*Index*) to update the collection, and finally *Free* the item.

```
procedure MCollection.AtFree(Index : integer);
  var Item: Pointer;
  begin Item  $\leftarrow$  At(Index); AtDelete(Index); FreeItem(Item); end;
```

223. Inserting an item at an *Index*, we first need to check if the position is within the bounds of the collection. If it's out of bounds, then flag a *ListError* and exit the function.

Otherwise, we check if the collection is at capacity (*Limit* = *Count*). If so, we try to expand the collection by *Delta* items. When *Delta* is zero, then raise an error and exit.

Now we are at the “default” case. Simply shift items starting at *Index* up by one. Then set the item at *Index* to be the new *Item*, and increment the count of the collection.

```
procedure MCollection.AtInsert(Index : integer; Item : Pointer);
  begin if (Index < 0)  $\vee$  (Index > Count) then
    begin ListError(coIndexError, 0); exit; end;
  if Limit = Count then
    begin if Delta = 0 then
      begin ListError(coOverflow, 0); exit; end;
      SetLimit(Limit + Delta);
    end;
  if Index  $\neq$  Count then Move(Items $\uparrow$ [Index], Items $\uparrow$ [Index + 1], (Count - Index) * SizeOf(pointer));
  Items $\uparrow$ [Index]  $\leftarrow$  Item; inc(Count);
  end;
```

224. Overwrite contents at index. We can insert a new item at a given index without shifting the collection.

```
procedure MCollection.AtPut(Index : integer; Item : Pointer);
  begin if (Index < 0)  $\vee$  (Index  $\geq$  Count) then ListError(coIndexError, 0)
  else Items $\uparrow$ [Index]  $\leftarrow$  Item;
  end;
```

225. Deleting an item finds the index of the item, then invokes *AtDelete* on that index.

```
procedure MCollection.Delete(Item : Pointer);
  begin AtDelete(IndexOf(Item)); end;
```

226. Similarly, freeing an item is just *Delete*-ing the item, then calling *FreeItem* on the pointer.

```
procedure MCollection.Free(Item : Pointer);
  begin Delete(Item); FreeItem(Item); end;
```

227. Inserting an item at the end of the collection.

```
procedure MCollection.Insert(aItem : Pointer);  
  begin AtInsert(Count, aItem); end;
```

228. We can also “fit” the collection by deleting all **nil** elements.

```
procedure MCollection.Pack;  
  var i: integer;  
  begin for i  $\leftarrow$  pred(Count) downto 0 do  
    if Items $\uparrow$ [i] = nil then AtDelete(i);  
  end;
```

229. Move semantics for creating a new collection.

```
constructor MCollection.MoveCollection(var fAnother : MCollection);  
  begin Init(0, fAnother.Delta); TransferItems(fAnother) end;
```

230. Cloning a collection will simply create an empty collection, the loop through *AAnother* inserting each item from the original collection into the newly minted collection.

```
constructor MCollection.CopyCollection(var AAnother : MCollection);  
  var i: integer;  
  begin Init(AAnother.Limit, AAnother.Delta);  
  for i  $\leftarrow$  0 to AAnother.Count - 1 do Insert(aAnother.Items $\uparrow$ [i]);  
  end;
```

231. A singleton allocates as little as possible.

```
constructor MCollection.Singleton(fSing : PObject; fDelta : integer);  
  begin Init(2, fDelta); Insert(fSing) end;
```

232. Pruning a collection merely sets its limits to zero. It does not free the contents of the collection.

```
procedure MCollection.Prune;  
  begin SetLimit(0) end;
```

233. Moving an *MList* uses PASCAL’s inheritance semantics to invoke *MList.MoveList* and then sets the *Delta* to 2.

```
constructor MCollection.MoveList(var aAnother : MList);  
  begin inherited MoveList(aAnother); Delta  $\leftarrow$  2;  
  end;
```

234. Copying a list invokes *MList.CopyList* on the collection, then sets *Delta* \leftarrow 2.

```
constructor MCollection.CopyList(var aAnother : MList);  
  begin inherited CopyList(aAnother); Delta  $\leftarrow$  2; end;
```


Section 9.5. SIMPLE STACKED (EXTENDIBLE) LISTS

235. This is used to track newly registered clusters in Mizar.

The basic idea is that we partition the array into the first N entries, then the remaining k entries. The last k entries are the “extendible” entries.

We will eventually “digest” the extendible entries (by incrementing $N \leftarrow N+1$ and decrementing $k \leftarrow k-1$ until $k = 0$).

```

⟨ Public interface for mobjects.pas 184 ⟩ +=
  { MExtList object }
  MExtListPtr = ↑MExtList;
  MExtList = object (MList)
    fExtCount: integer;
    constructor Init(aLimit : integer);
    destructor Done; virtual;
    procedure Insert(aItem : Pointer); virtual;
    procedure Mark(var aIndex : integer); virtual;
    procedure FreeItemsFrom(aIndex : integer); virtual;
    procedure DeleteAll; virtual;
    procedure FreeAll; virtual;
    procedure Pack; virtual;
    procedure InsertExt(AItem : Pointer); virtual;
    procedure SetLimit(ALimit : integer); virtual;
    procedure AddExtObject; virtual;
    procedure AddExtItems; virtual;
    procedure DeleteExtItems;
    procedure FreeExtItems;
  end ;

```

236. Simple Stacked (Extendable) Collection.

```

⟨ MExtList implementation 236 ⟩ ≡
constructor MExtList.Init(ALimit : integer);
  begin MObject.Init;
  Items ← nil;
  Count ← 0; Limit ← 0;
  SetLimit(ALimit); fExtCount ← 0;
end;

```

This code is used in section 183.

237. Destructor for MExtList. The destructor for *MExtList* invokes *self.FreeExtItems* and then calls the inherited destructor from the superclass.

```

destructor MExtList.Done;
  begin FreeExtItems; inherited Done; end;

```

238. Inserting an item. The *fExtCounter* field is unclear to me. But if it's nonzero, then an error has occurred and we bail out.

Otherwise, we possibly grow the extendible list, and we insert at the end the given pointer and increment the *Count* of items allocated.

```

procedure MExtList.Insert(aItem : Pointer);
  begin if fExtCount  $\neq$  0 then
    begin ListError(coIndexExtError, 0); exit; end;
  if Limit = Count then SetLimit(Limit + GrowLimit(Limit));
  Items $\uparrow$ [Count]  $\leftarrow$  aItem; { Append the item to the list }
  inc(Count);
end;

```

239. Deleting all entries. We can only call this when the extendible entries have been “digested” into the underlying array (i.e., when *fExtCount* = 0). Otherwise we need to flag an error. Otherwise, when all the extendible entries have been “digested”, we call the parent’s *DeleteAll* method.

```

procedure MExtList.DeleteAll;
  begin if fExtCount  $\neq$  0 then
    begin ListError(coIndexExtError, 0); exit;
    end;
  inherited DeleteAll;
end;

```

240. Free all entries. Like deleting all the entries, we need to fully digest all the extendible entries before invoking the parent class’s *FreeAll* method. If there are extendible entries not fully digested, then we get indigestion (i.e., a list error).

```

procedure MExtList.FreeAll;
  begin if fExtCount  $\neq$  0 then
    begin ListError(coIndexExtError, 0); exit;
    end;
  inherited FreeAll;
end;

```

241. Packing. When packing an extendible list, we assert the extendible items have been digested fully. If not, raise an error. If fully digested, then invoke the parent class’s *Pack* method.

```

procedure MExtList.Pack;
  begin if fExtCount  $\neq$  0 then
    begin ListError(coIndexExtError, 0); exit;
    end;
  inherited Pack;
end;

```

242. Insert extendible items. We can add an extendible item by first growing the list (if necessary), then adding an item at index $N + k$. Then increment the number of extendible items $k \leftarrow k + 1$.

```

procedure MExtList.InsertExt(AItem : Pointer);
  begin if Limit = Count + fExtCount then SetLimit(Limit + GrowLimit(Limit));
  Items $\uparrow$ [Count + fExtCount]  $\leftarrow$  AItem; inc(fExtCount);
end;

```

243. Ensure capacity of extendible list.

- (1) When the new limit is less than the logical size N and the extendible size k , we just set the capacity to $N + k$.
- (2) Else if the new limit is larger than $MaxCollectionSize$, then just use the maximum collection size as the capacity.
- (3) Else if the new limit is different than the existing capacity, then we have to check if the new limit is zero. When it is, just set the capacity to zero and the list of items to **nil**. Otherwise, allocate space for a new array, and move over the contents from the existing array (and then free the existing array). Update the capacity and pointer to the items.

```

procedure MExtList.SetLimit(ALimit : integer);
  var UItems: PItemList;
  begin if ALimit < Count + fExtCount then ALimit ← Count + fExtCount;
  if ALimit > MaxCollectionSize then ALimit ← MaxCollectionSize;
  if ALimit ≠ Limit then
    begin if ALimit = 0 then UItems ← nil
    else begin GetMem(UItems, ALimit * SizeOf(Pointer));
      if ((Count + fExtCount) ≠ 0) ∧ (Items ≠ nil) then
        Move(Items↑, UItems↑, (Count + fExtCount) * SizeOf(Pointer));
      end;
    if Limit ≠ 0 then FreeMem(Items, Limit * SizeOf(Pointer));
    Items ← UItems; Limit ← ALimit;
  end;
end;

```

244. “Marking” an extendible list amounts to setting the procedure’s variable to the capacity of the extendible list.

```

procedure MExtList.Mark(var aIndex : integer);
  begin aIndex ← Count;
  end;

```

245. Freeing items starting at a given index requires the extendible items to be fully digested (if not, raise an error). Then simply free each object using the virtual destructor *MObject.Done*.

```

procedure MExtList.FreeItemsFrom(aIndex : integer);
  var I: integer;
  begin if fExtCount ≠ 0 then
    begin ListError(coIndexExtError, 0); exit;
    end;
  for I ← Count - 1 downto aIndex do
    if Items↑[I] ≠ nil then Dispose(PObject(Items↑[I]), Done);
  Count ← aIndex;
end;

```

246. Digesting one extendible item. We can instruct the extendible list to digest exactly one extendible item. This requires the number of extendible items to be positive $k > 0$. If not, raise an error. Otherwise increment the logical capacity $N \leftarrow N + 1$ and decrement the number of extendible items $k \leftarrow k - 1$.

```

procedure MExtList.AddExtObject;
  begin if fExtCount ≤ 0 then
    begin ListError(coIndexExtError, 0); exit;
    end;
  inc(Count); dec(fExtCount);
end;

```

247. Digest all extendible items. This simply updates capacity to be incremented by the number of extendible items. Then the number of extendible items is set to zero. No error is raised if there are no extendible items (unlike digesting one single extendible item).

```
procedure MExtList.AddExtItems;  
  begin  $Count \leftarrow Count + fExtCount$ ;  $fExtCount \leftarrow 0$ ;  
  end;
```

248. Deleting all extendible items simply sets the *number* of extendible items to zero. This is a “soft delete” which does not affect anything else on the heap.

```
procedure MExtList.DeleteExtItems;  
  begin  $fExtCount \leftarrow 0$ ;  
  end;
```

249. Freeing all the extendible items will “hard delete” each extendible item, removing them from the heap.

```
procedure MExtList.FreeExtItems;  
  var  $I$ : integer;  
  begin for  $I \leftarrow 0$  to  $fExtCount - 1$  do  
    if  $Items \uparrow [Count + I] \neq \text{nil}$  then  $Dispose(PObject(Items \uparrow [Count + I]), Done)$ ;  
   $fExtCount \leftarrow 0$ ;  
  end;
```

Section 9.6. SORTED LISTS

250. These are used in the equalizer and in the correlator, specifically for keeping a collection of identifiers.

A sorted list uses an array of indices (called *fIndex*). The array of indices are sorted according to a comparison of values.

Invariant: $Length(fIndex) = Length(Items)$

Invariant (sorted): for each $i = 0, \dots, Length(Items) - 2$, we have $Items \uparrow [fIndex \uparrow [i]] \leq Items \uparrow [fIndex \uparrow [i + 1]]$.

Also, we are taking the convention that $fCompare(x, y)$ returns -1 when $x < y$; returns 0 when $x = y$; returns $+1$ when $x > y$.

```

⟨ Public interface for mobjects.pas 184 ⟩ +≡
  { MSortedList Object }
  IndexListPtr = ↑ MIndexList;
  MIndexList = array [0 .. MaxCollectionSize - 1] of integer;
  CompareProc = function (aItem1, aItem2 : Pointer): integer;
  MSortedList = object (MList)
    fIndex: IndexListPtr;
    fCompare: CompareProc;
    constructor Init(aLimit : integer);
    constructor InitSorted(aLimit : integer; aCompare : CompareProc);
    constructor MoveList(var aAnother : MList);
    constructor CopyList(const aAnother: MList);
    procedure AtInsert(aIndex : integer; aItem : Pointer); virtual;
    procedure Insert(aItem : Pointer); virtual;
    function IndexOf(aItem : Pointer): integer; virtual;
    procedure Sort(aCompare : CompareProc);
    procedure SetLimit(ALimit : integer); virtual;
    function Find(aKey : Pointer; var aIndex : integer): boolean; virtual;
    function Search(aKey : Pointer; var aIndex : integer): boolean; virtual;
    procedure Pack; virtual;
    procedure FreeItemsFrom(aIndex : integer); virtual;
  end ;

```

251. Constructors. There are four constructors:

- (1) *Init* simply creates an empty list with a given capacity.
- (2) *InitSorted* is like *Init*, but expects an ordering operator.
- (3) *MoveList* moves all the items from another list into the caller, sorting as needed. This will also empty the other list.
- (4) *CopyList* is like *MoveList* but leaves the other list untouched.

```

⟨ MSortedList implementation 251 ⟩ ≡
  { MSortedList object }
  constructor MSortedList.Init(aLimit : integer);
  begin MObject.Init; Items ← nil; Count ← 0; Limit ← 0; fIndex ← nil; fCompare ← nil;
  SetLimit(ALimit);
  end;
  constructor MSortedList.InitSorted(aLimit : integer; aCompare : CompareProc);
  begin MObject.Init; Items ← nil; Count ← 0; Limit ← 0; fIndex ← nil; fCompare ← aCompare;
  SetLimit(ALimit);
  end;

```

See also section 263.

This code is used in section 183.

252. Move constructor. When we move items from an *MList* into the caller, we also sort as we insert.

```

constructor MSortedList.MoveList(var aAnother : MList);
  var I: integer;
  begin Items  $\leftarrow$  aAnother.Items; Count  $\leftarrow$  aAnother.Count; Limit  $\leftarrow$  aAnother.Limit;
    GetMem(fIndex, Limit * SizeOf(integer)); fCompare  $\leftarrow$  nil;
    for I  $\leftarrow$  0 to pred(aAnother.Count) do fIndex $\uparrow$ [I]  $\leftarrow$  I;
      { Empty out the other list }
    aAnother.DeleteAll; aAnother.Limit  $\leftarrow$  0; aAnother.Items  $\leftarrow$  nil;
  end;

```

253. The *CopyList* constructor is like the *MoveList* **except** that the other list is not modified.

```

constructor MSortedList.CopyList(const aAnother: MList);
  var i: integer;
  begin MObject.Init; Items  $\leftarrow$  nil; Count  $\leftarrow$  0; Limit  $\leftarrow$  0; fIndex  $\leftarrow$  nil; fCompare  $\leftarrow$  nil;
    SetLimit(aAnother.Limit); Count  $\leftarrow$  aAnother.Count;
    for i  $\leftarrow$  0 to Count - 1 do
      begin Items $\uparrow$ [i]  $\leftarrow$  PObject(aAnother.Items $\uparrow$ [i]) $\uparrow$ .MCopy; fIndex $\uparrow$ [i]  $\leftarrow$  i;
      end;
    end;

```

254. Insert element at an index. We can insert (potentially overwriting an existing entry) at a given index.

```

  { used in CollectCluster not to repeat the search, should be used only when @fCompare  $\neq$  nil }
procedure MSortedList.AtInsert(aIndex : integer; aItem : Pointer);
  begin if Limit = Count then SetLimit(Limit + GrowLimit(Limit)); { Ensure capacity }
  if aIndex  $\neq$  Count then
    Move(fIndex $\uparrow$ [aIndex], fIndex $\uparrow$ [aIndex + 1], (Count - aIndex) * SizeOf(integer));
    Items $\uparrow$ [Count]  $\leftarrow$  aItem; fIndex $\uparrow$ [aIndex]  $\leftarrow$  Count; inc(Count);
  end;

```

255. Inserting an item. Inserting an item into a sorted list boils down to two cases:

- (1) If there is an ordering operator, we check if the item is in the underlying array using *Find* (§260), which will mutate the *lIndex* to be where it should be located. When the item is missing, simply insert it at *lIndex*. When the item is present, then we do nothing.
- (2) If there is no ordering operator, then check if the item already is present in the sorted list. If so, then don't do anything. Otherwise, insert the item at the start of the list.

```

procedure MSortedList.Insert(aItem : Pointer);
  var lIndex: integer;
  begin if @fCompare = nil then
    begin if Limit = Count then SetLimit(Limit + GrowLimit(Limit));
      Items $\uparrow$ [Count]  $\leftarrow$  aItem; fIndex $\uparrow$ [Count]  $\leftarrow$  Count; inc(Count); exit;
    end;
  if  $\neg$ Find(aItem, lIndex) then AtInsert(lIndex, aItem);
  end;

```

256. Resizing a sorted list. The invariant is that the list is sorted when it has an ordering operator (and so restricting to $aLimit$ preserves the list being sorted), and it is a “set” when it does not have an ordering (and so restricting to $aLimit$ preserves this property of being a finite set without duplicate entries).

```

procedure MSortedList.SetLimit( $aLimit$  : integer);
  var lItems: PItemList; lIndex: IndexListPtr;
  begin if  $aLimit < Count$  then  $aLimit \leftarrow Count$ ;
  if  $aLimit > MaxCollectionSize$  then  $aLimit \leftarrow MaxCollectionSize$ ;
  if  $aLimit \neq Limit$  then
    begin if  $aLimit = 0$  then
      begin lItems  $\leftarrow$  nil; lIndex  $\leftarrow$  nil; end
    else begin GetMem(lItems,  $aLimit * SizeOf(Pointer)$ ); GetMem(lIndex,  $aLimit * SizeOf(integer)$ );
      if  $Count \neq 0$  then
        begin if Items  $\neq$  nil then
          begin Move(Items $\uparrow$ , lItems $\uparrow$ ,  $Count * SizeOf(Pointer)$ );
            Move(fIndex $\uparrow$ , lIndex $\uparrow$ ,  $Count * SizeOf(integer)$ );
          end;
        end;
      end;
    end;
  if  $Limit \neq 0$  then
    begin FreeMem(Items,  $Limit * SizeOf(Pointer)$ ); FreeMem(fIndex,  $Limit * SizeOf(integer)$ );
    end;
  Items  $\leftarrow$  lItems; fIndex  $\leftarrow$  lIndex; Limit  $\leftarrow$  aLimit;
  end;
end;

```

257. Quick sort an array. We have a private helper function for quicksorting an *IndexListPtr* (§250). Initially $L \leftarrow 0$ and $R \leftarrow \text{length}(aList) - 1$. It may be instructive to compare this to Algorithm Q in *The Art of Computer Programming*, third ed., volume 3, §5.2.2. Specifically Mizar appears to use Hoare partitioning. We can summarize its algorithm thus:

Algorithm S (*Quicksort*). This uses Hoare partition. We assume that $L \leq R$, and that *aCompare* is a total order (it's transitive and the law of trichotomy holds on all pairs of elements). Steps S1 through S4 are better known as the “partition” procedure.

- S0.** [Initialize] Set $I \leftarrow L$, $J \leftarrow R$, and the pivot index $P_{idx} \leftarrow (L + R) \text{ shr } 1$, and the pivot value $P \leftarrow aList \uparrow [aIndex \uparrow [(L + R) \text{ shr } 1]]$. Observe $I \leq P_{idx} \leq J$ at this point.
- S1.** [Move *I* right] While $aList[I] < P$, we increment $I \leftarrow I + 1$. This is guaranteed to terminate since $I \leq P_{idx}$, so eventually we will get to $aList[i] = P$.
- S2.** [Move *J* left] While $P < aList[J]$, we decrement $J \leftarrow J - 1$. This is guaranteed to terminate since $P_{idx} \leq J$, so eventually we will get to $aList[J] = P$.
- S3.** [Keep going?] If $I > J$, then we're done “partitioning” (so everything to the left of the pivot is not greater than the pivot value, and everything to the right of the pivot is not lesser than the pivot value), and we go to step S5; otherwise go to the next step.
- S4.** [Swap entries *I* and *J*] We swap the entries located at *I* and *J*, then set $I \leftarrow I + 1$, and $J \leftarrow J - 1$. If $I \leq J$, then return to step S1.
- S5.** [Recur on left half] If $L < J$, then recursively call quicksort on the left half of the index (entries between $L \dots J - 1$).
- S6.** [Sort the right half] If $I \geq R$, then terminate. Otherwise, set $L \leftarrow I$ and return to step S0. ■

For readability, we also introduce a **WEB** macro for swapping the indices.

```

define steal_from(#)  $\equiv aIndex \uparrow [\#]$ ;  $aIndex \uparrow [\#] \leftarrow T$ ;
define swap_indices(#)  $\equiv T \leftarrow aIndex \uparrow [\#]$ ;  $aIndex \uparrow [\#] \leftarrow steal\_from$ 
procedure ListQuickSort(aList : PItemList; aIndex : IndexListPtr; L, R : integer;
    aCompare : CompareProc);
var I, J, T: integer; P: Pointer;
begin repeat  $I \leftarrow L$ ;  $J \leftarrow R$ ;  $P \leftarrow aList \uparrow [aIndex \uparrow [(L + R) \text{ shr } 1]]$ ;
repeat
    {  $I \leq (L + R) \text{ shr } 1 \leq J$  }
    while  $aCompare(aList \uparrow [aIndex \uparrow [I]], P) < 0$  do inc(I);
    {  $P \leq aList \uparrow [aIndex \uparrow [I]]$  }
    while  $aCompare(aList \uparrow [aIndex \uparrow [J]], P) > 0$  do Dec(J);
    {  $aList \uparrow [aIndex \uparrow [J]] \leq P$  }
    {  $I \leq (L + R) \text{ shr } 1 \leq J$  }
    if  $I \leq J$  then
        begin
            {  $aList \uparrow [aIndex \uparrow [J]] < P < aList \uparrow [aIndex \uparrow [I]]$  }
            swap_indices(I)(J);
            {  $aList \uparrow [aIndex \uparrow [I]] < P < aList \uparrow [aIndex \uparrow [J]]$  }
            {  $I < J$  implies  $inc(I) \leq dec(J)$  }
            {  $I = J$  implies  $inc(I) > dec(J)$  }
            inc(I); Dec(J);
        end;
    until  $I > J$ ;
    {  $J \leq (L + R) \text{ shr } 2 \leq I$  and  $J < I$  }
    if  $L < J$  then ListQuickSort(aList, aIndex, L, J, aCompare); { quicksort left half }
     $L \leftarrow I$ ; { recursively quicksort the right half of the array }
until  $I \geq R$ ;
end;

```


258. Remarks.

- (1) It is unclear to me whether we must have $aCompare$ be a linear order, and not a total pre-order. The difference is: do we really need $a \leq b \wedge b \leq a \implies a = b$ (i.e., a total order) or not (i.e., a total pre-order)?
- (2) PRECONDITION: We need to prove the *compare* operators are total orders for quicksort to work as expected.
- (3) ASSERT: Upon arriving to step Q5, the entries in $L \dots J - 1$ are partitioned (i.e., less than the pivot value) as is the entries in $I \dots R$. In particular, the maximal element in $L \dots J - 1$ is located at $J - 1$ while the minimal element in $I \dots R$ is located at I .
- (4) Robert Sedgewick's *Quicksort* (1980) is literally *the* book on the subject. An abbreviated reference may be found in Sedgewick's "The Analysis of Quicksort Programs" (*Acta Inform.* **7** (1977) 327–355, [eprint](#))
- (5) IMPROVEMENT: This can be improved when recursively sorting the left half of the arrays by first checking if $J - L \leq 9$ then use insertion sort otherwise recursively quicksort the left half. (Similarly, instead of iterating the outermost while-loop, we should test if $R - I \leq 9$ then invoking insertion on the subarray indexed by $I \dots R$.)
- (6) IMPROVEMENT: The pivot index P_{ind} is selected as $P_{ind} \leftarrow (L + R)/2$, which can lead to overflow. A safer way to compute this would be $P_{ind} \leftarrow L + ((R - L)/2)$.

According to the paper by Sedgewick we cited, when quicksorting a list of size less than M with a different sorting algorithm, the optimal choice of M (the cutoff for delegating to another sort algorithm) contributes to the runtime of quicksort,

$$f(M) = \frac{1}{6} \left(8M + 71 - 70H_{M+2} + \frac{270}{M+2} + \frac{54}{2M+3} - 36\frac{H_{M+1}}{M+2} \right).$$

We can use the approximation for Harmonic numbers

$$H_n = \ln(n) + \gamma + \frac{1}{2n} + O(n^{-2})$$

where $\gamma \approx 0.57721$ is Euler-Mascheroni constant. Using this replacement, we have

$$f'(M) \approx \frac{4}{3} + \frac{3}{(1+m)^2} - \frac{6}{1+m} + \frac{36\gamma - 253}{6(2+m)^2} - \frac{17}{3(2+m)} - \frac{18}{(3+2m)^2} + \frac{6\ln(1+m)}{(2+m)^2}.$$

We can numerically find the root for this to be $m_0 \approx 8.9888$ which gives a global minimum of $f(9) \approx -8.47671$.

This analysis is sketched out in Knuth's *The Art of Computer Programming*, volume III, but it may be worth sitting down and working this analysis out more fully.

259. Sorting a sorted list. We can update a sorted list to sort according to a new ordering operator, and also update the data structure to record this new ordering operator. This relies on *ListQuickSort* (§257) to do the actual sorting.

```

procedure MSortedList.Sort( $aCompare$  : CompareProc);
  var  $I$ : integer;
  begin  $fCompare \leftarrow aCompare$ ;
  for  $I \leftarrow 0$  to  $Count - 1$  do  $fIndex \uparrow [I] \leftarrow I$ ;
  if ( $Count > 0$ ) then ListQuickSort( $Items, fIndex, 0, Count - 1, aCompare$ );
  end;

```

260. Find item. Finding an item in a sorted list boils down to two cases: do we have *fCompare* populated or not? If so, then use a binary search. If not, then just iterate item-by-item testing if *aKey* is in the underlying array.

CAUTION: The “find” function returns the index for the *fIndex* field, **NOT** the index for the underlying array of values (inherited from the *MList* class).

```

function MSortedList.Find(aKey : Pointer; var aIndex : integer): boolean;
  var L, H, I, C: integer;
  begin Find  $\leftarrow$  False;
  if @fCompare = nil then  $\langle$ Find needle in MSortedList by brute force 262 $\rangle$ ;
   $\langle$ Find needle in MSortedList by binary search 261 $\rangle$ 
  end;

```

261. Binary search is a little clever. We have *L* be the lower bounds index, and *H* the upper bounds index. The midpoint is obtained by taking their sum $L + H$ and shifting to the right by 1 bit (which corresponds to dividing by 2, truncating the result).

We compare the item located at the midpoint to the given *aKey*, and store the result of this comparison in the variable *C*. If $C < 0$, then *aKey* is located to the right of the midpoint (so set $L \leftarrow I + 1$).

On the other hand, if $C \geq 0$, update $H \leftarrow I - 1$. When $C = 0$ (i.e., the midpoint *is equal to aKey*), then we set $L \leftarrow I + 1$ so we have $H < L$ to terminate the loop. We set the return value to *True* when $C = 0$, and we mutate the *aIndex* to the index where we found the needle in the haystack.

```

 $\langle$ Find needle in MSortedList by binary search 261 $\rangle \equiv$ 
  L  $\leftarrow$  0; H  $\leftarrow$  Count - 1;
  while  $L \leq H$  do
    begin I  $\leftarrow$  (L + H) shr 1; C  $\leftarrow$  fCompare(Items $\uparrow$ [fIndex $\uparrow$ [I]], aKey);
    if  $C < 0$  then L  $\leftarrow$  I + 1
    else begin H  $\leftarrow$  I - 1;
      if  $C = 0$  then
        begin Find  $\leftarrow$  True; L  $\leftarrow$  I; end;
      end;
    end;
  aIndex  $\leftarrow$  L;

```

This code is used in section 260.

262. We can simply iterate through the underlying array, testing item-by-item if each entry is equal to the needle or not.

```

 $\langle$ Find needle in MSortedList by brute force 262 $\rangle \equiv$ 
  begin aIndex  $\leftarrow$  Count;
  for I  $\leftarrow$  0 to Count - 1 do
    if aKey = Items $\uparrow$ [I] then
      begin Find  $\leftarrow$  True; aIndex  $\leftarrow$  I; break end;
  exit;
  end

```

This code is used in section 260.

263. Search. We recall that *Find* returns the index of the *fIndex* field matching the needle. Usually, we want to know the index of the value itself. This is what *Search* performs.

$\langle \text{MSortedList implementation } 251 \rangle + \equiv$
function *MSortedList.Search*(*aKey* : *Pointer*; **var** *aIndex* : *integer*): *boolean*;
 var *I*: *integer*;
 begin *aIndex* \leftarrow *Count*; *Search* \leftarrow *false*;
 if *Find*(*aKey*, *I*) **then**
 begin *Search* \leftarrow *true*; *aIndex* \leftarrow *fIndex* \uparrow [*I*];
 end;
 end;

264. Index of a needle. Given a “needle”, where in the haystack is it? Well, we require the ordering operator be non-nil for the sorted list — otherwise raise an error. Then using *Find* (§260), check if the entry is present. If it is, then return the index for the underlying array of values.

If the needle is not in the haystack, return -1 .

function *MSortedList.IndexOf*(*aItem* : *Pointer*): *integer*;
 var *I*: *integer*;
 begin **if** @*fCompare* = **nil** **then**
 begin *ListError*(*coSortedListError*, 0); *exit*;
 end;
 IndexOf \leftarrow -1 ;
 if *Find*(*aItem*, *I*) **then**
 begin { *if I < fCount then* }
 IndexOf \leftarrow *fIndex* \uparrow [*I*];
 end;
 end;

265. Packing a sorted list. Use the superclass’s *Pack* method. Then, when there is an ordering operator present, sort the list.

procedure *MSortedList.Pack*;
 var *lCount*: *integer*;
 begin *lCount* \leftarrow *Count*; *inherited Pack*;
 if (@*fCompare* \neq **nil**) \wedge (*lCount* > *Count*) **then** *Sort*(*fCompare*);
 end;

266. Free items starting at an index. When we want to remove all items starting at index a , we simply iterate through the array of indices starting at entry $i = a$ and delete the value associated with $Items[i]$ when it is non-**nil**.

This will also keep the indices for the non-deleted entries.

```

procedure MSortedList.FreeItemsFrom(aIndex : integer);
  var I, k: integer;
  begin if aIndex = Count then exit;
  { Delete entries from the array of values }
  for I  $\leftarrow$  aIndex to Count - 1 do
    if Items $\uparrow$ [I]  $\neq$  nil then Dispose(PObject(Items $\uparrow$ [I]), Done);
  { Update the array of indices }
  k  $\leftarrow$  0;
  for I  $\leftarrow$  0 to Count - 1 do
    begin if fIndex $\uparrow$ [I] < aIndex then
      begin fIndex $\uparrow$ [k]  $\leftarrow$  fIndex $\uparrow$ [I]; inc(k); end;
    end;
  if k  $\neq$  aIndex then ListError(coSortedListError, 0);
  Count  $\leftarrow$  aIndex;
end;

```

Section 9.7. SORTED EXTENDIBLE LISTS

267. We want to handle a sorted (§250) version of extendible lists — an *MSortedExtList*. It's used in the correlator for functorial registrations and inferred definition constants.

Like *MSortedList*, we add a field *fIndex* for the indices of the entries. This will track the *digested* items, not the extendible items.

An important invariant: the ordering operator (*fCompare*) must be non-**nil**.

⟨Public interface for `mobjects.pas` 184⟩ +≡

```
MSortedExtList = object (MExtList)
  fIndex: IndexListPtr;
  fCompare: CompareProc;
  constructor Init(ALimit : integer);
  constructor InitSorted(aLimit : integer; aCompare : CompareProc);
  destructor Done; virtual;
  function Find(aKey : Pointer; var aIndex : integer): boolean; virtual;
  function FindRight(aKey : Pointer; var aIndex : integer): boolean; virtual;
  function FindInterval(aKey : Pointer; var aLeft, aRight : integer): boolean; virtual;
  function AtIndex(aIndex : integer): Pointer; virtual;
  procedure Insert(aItem : Pointer); virtual;
  procedure Pack; virtual;
  procedure InsertExt(AItem : Pointer); virtual;
  procedure SetLimit(ALimit : integer); virtual;
  procedure FreeItemsFrom(aIndex : integer); virtual;
  procedure AddExtObject; virtual;
  procedure AddExtItems; virtual;
end ;
```

268. Constructors. The *Init* constructor should not be used, and should raise an error if anyone tries to use it.

Instead, the *InitSorted* should be used to construct a new [empty] sorted extendible list with a given ordering operator.

⟨*MSortedExtList* implementation 268⟩ ≡

```
{ MSortedExtList always with possible duplicate keys, always sorted }
constructor MSortedExtList.Init(ALimit : integer);
  begin ListError(coIndexExtError, 0); end;
constructor MSortedExtList.InitSorted(aLimit : integer; aCompare : CompareProc);
  begin inherited Init(aLimit); fCompare ← aCompare;
  end;
```

This code is used in section 183.

269. destructor The destructor for sorted extendible lists is just the inherited destructor from extendible lists.

```
destructor MSortedExtList.Done;
  begin inherited Done; end;
```

270. Finding a needle in the haystack. We require *fCompare* to be non-**nil** and enforce that invariant by raising an error when it is **nil**.

Then we just use bisection search to find the needle in the haystack. Once found, we mutate *aIndex* to the index *L* of the *fIndex* array which indexes the needle.

{ find the left-most if duplicates }

```

function MSortedExtList.Find(aKey : Pointer; var aIndex : integer): boolean;
  var L, H, I, C: integer;
  begin if  $\neg$ Assigned(fCompare) then ListError(coIndexExtError, 0);
  Find  $\leftarrow$  False; L  $\leftarrow$  0; H  $\leftarrow$  Count - 1;
  while L  $\leq$  H do
    begin I  $\leftarrow$  (L + H) shr 1; C  $\leftarrow$  fCompare(Items $\uparrow$ [fIndex $\uparrow$ [I]], aKey);
    if C < 0 then L  $\leftarrow$  I + 1
    else begin H  $\leftarrow$  I - 1;
      if C = 0 then Find  $\leftarrow$  True;
    end;
  end;
  aIndex  $\leftarrow$  L;
end;

```

271. Find the rightmost index for a needle in the haystack. Since the underlying array is sorted, we check to see if the needle is in the haystack. If it is, we keep incrementing *aIndex* until it is no longer indexing the needle.

So upon return, if it returns *True*, then the *aIndex* parameter is mutated to equal the rightmost index for the needle's appearance in the haystack.

{ find the left-most with higher aKey, this is where we can insert }

```

function MSortedExtList.FindRight(aKey : Pointer; var aIndex : integer): boolean;
  begin if Find(aKey, aIndex) then
    begin while (aIndex < Count)  $\wedge$  (0 = fCompare(Items $\uparrow$ [fIndex $\uparrow$ [aIndex]], aKey)) do inc(aIndex);
    FindRight  $\leftarrow$  true;
  end
  else FindRight  $\leftarrow$  false;
end;

```

272. Since we allow duplicate values in a sorted extendible list, we will sometimes wish to know the “interval” of entries equal to a needle. This will mutate *aLeft* and *aRight* to point to the beginning and end of the interval.

When the needle is not in the haystack, the function will mutate the variables to ensure *aRight* < *aLeft* to stress the point.

Possible bug: This assumes the *MSortedExtList.Find* returns the left-most index where the needle appears in the haystack.

{ find the interval of equal guys }

```

function MSortedExtList.FindInterval(aKey : Pointer; var aLeft, aRight : integer): boolean;
  begin if Find(aKey, aLeft) then
    begin aRight  $\leftarrow$  aLeft + 1;
    while (aRight < Count)  $\wedge$  (0 = fCompare(Items $\uparrow$ [fIndex $\uparrow$ [aRight]], aKey)) do inc(aRight);
    dec(aRight); FindInterval  $\leftarrow$  true;
  end
  else begin aRight  $\leftarrow$  aLeft - 1; FindInterval  $\leftarrow$  false;
  end;
end;

```

273. Get value at index. We check if the index i is within bounds of the sorted extendible list. If not, then we raise an error.

Otherwise, the default course of action, we simply lookup the entry $fIndex[i]$ and then lookup the entry in the array of values located with that index.

```
function MSortedExtList.AtIndex(aIndex : integer): Pointer;
  begin if (aIndex < 0)  $\vee$  (aIndex  $\geq$  Count) then ListError(coIndexExtError, 0);
  AtIndex  $\leftarrow$  Items $\uparrow$ [fIndex $\uparrow$ [aIndex]];
end;
```

274. Inserting items. We can only insert an item into an extendible list when it has fully digested all its extendible items. This requirement carries over to sorted extendible lists.

When there are no extendible items, we delegate the work to *InsertExt*.

```
procedure MSortedExtList.Insert(aItem : Pointer);
  begin if fExtCount  $\neq$  0 then ListError(coIndexExtError, 0);
  InsertExt(aItem); AddExtObject;
end;
```

275. Packing a sorted extendible list is unsupported, so just raise an error if anyone tries to use it.

```
procedure MSortedExtList.Pack;
  begin ListError(coIndexExtError, 0);
end;
```

276. Adding an extendible item. We ensure there is sufficient capacity in the underlying array of items, then add *AItem* at the position located by the logical size of the array of items. We also increment the number of extendible items.

```
procedure MSortedExtList.InsertExt(AItem : Pointer);
  begin if Limit = Count + fExtCount then SetLimit(Limit + GrowLimit(Limit));
  Items $\uparrow$ [Count + fExtCount]  $\leftarrow$  AItem; inc(fExtCount);
end;
```

277. Ensure capacity. We can ensure the capacity of a sorted extendible list to be at least as large as $ALimit$.

When $ALimit$ is smaller than the current capacity of the sorted extendible list, we allocate new arrays and copy over the old data. More importantly: we keep the last $fExtCount$ items as (“undigested”) extendible items.

```

procedure MSortedExtList.SetLimit( $ALimit$  : integer);
  var lItems: PItemList; lIndex: IndexListPtr;
  begin Count  $\leftarrow$  Count + fExtCount;
  if aLimit < Count then aLimit  $\leftarrow$  Count;
  if aLimit > MaxCollectionSize then aLimit  $\leftarrow$  MaxCollectionSize;
  if aLimit  $\neq$  Limit then
    begin if aLimit = 0 then
      begin lItems  $\leftarrow$  nil; lIndex  $\leftarrow$  nil;
      end
    else begin { Allocate new arrays for indices and items }
      GetMem(lItems, aLimit * SizeOf(Pointer)); GetMem(lIndex, aLimit * SizeOf(integer));
      if Count  $\neq$  0 then { Copy items and indices from old arrays to new ones }
        begin if Items  $\neq$  nil then
          begin Move(Items $\uparrow$ , lItems $\uparrow$ , Count * SizeOf(Pointer));
            Move(fIndex $\uparrow$ , lIndex $\uparrow$ , Count * SizeOf(integer));
          end;
        end;
      end;
    if Limit  $\neq$  0 then { Free old arrays }
      begin FreeMem(Items, Limit * SizeOf(Pointer)); FreeMem(fIndex, Limit * SizeOf(integer));
      end;
    Items  $\leftarrow$  lItems; fIndex  $\leftarrow$  lIndex; Limit  $\leftarrow$  aLimit; { Update the caller to use new arrays }
    end;
  Count  $\leftarrow$  Count - fExtCount;
end;

```


278. Freeing items starting at an index. We have two exceptional situations:

- (1) The $fExtCount$ must be zero, and if it is nonzero, then an error is raised; and
- (2) If the index given is equal to the logical size of the sorted extendible list, then we terminate early (since there is nothing to do).

```

procedure MSortedExtList.FreeItemsFrom(aIndex : integer);
  var I, k: integer;
  begin if  $fExtCount \neq 0$  then ListError(coIndexExtError, 0);
  if  $aIndex = Count$  then exit;
  { Free items indexed by  $I \geq aIndex$  }
  for  $I \leftarrow aIndex$  to  $Count - 1$  do
    if  $Items \uparrow [I] \neq \text{nil}$  then Dispose(PObject( $Items \uparrow [I]$ ), Done);
  { Sort  $fIndex$  for entries less than  $aIndex$  }
   $k \leftarrow 0$ ;
  for  $I \leftarrow 0$  to  $Count - 1$  do
    begin if  $fIndex \uparrow [I] < aIndex$  then
      begin  $fIndex \uparrow [k] \leftarrow fIndex \uparrow [I]$ ; inc( $k$ );
      end;
    end;
  if  $k \neq aIndex$  then ListError(coSortedListError, 0);
   $Count \leftarrow aIndex$ ;
end;

```

279. Digest an extendible object. When there are extendible objects left to digest among the values (i.e., when $fExtCount > 0$), When $fExtCount \leq 0$, then raise an error (there's nothing left to digest).

The first extendible item left to be digested is located at $Count$ in the array of items. Then we find the right most index for the same extendible item. We digest all of them at once, shifting the $fIndex$ as needed.

Note that the need to shift $fIndex$ down by 1 is needed to keep the array of items sorted.

```

procedure MSortedExtList.AddExtObject;
  var UIndex: integer;
  begin if  $fExtCount \leq 0$  then ListError(coIndexExtError, 0);
  FindRight( $Items \uparrow [Count]$ , UIndex);
  if  $UIndex \neq Count$  then { shift  $fIndex$  to right by 1 }
    Move( $fIndex \uparrow [UIndex]$ ,  $fIndex \uparrow [UIndex + 1]$ ,  $(Count - UIndex) * SizeOf(integer)$ );
   $fIndex \uparrow [UIndex] \leftarrow Count$ ; { extendible item's index }
  inc( $Count$ ); Dec( $fExtCount$ );
end;

```

280. Digest all extendible items. We can simply iterate through all the extendible items, digesting them one-by-one.

```

procedure MSortedExtList.AddExtItems;
  begin while  $fExtCount > 0$  do AddExtObject;
end;

```

Section 9.8. SORTED LIST OF STRINGS

281. This is used in the kernel to track directives, as well as `makenv` and `accdict` needs it.

```

⟨Public interface for mobjects.pas 184⟩ +≡
  MSortedStrList = object (MSortedList)
    constructor Init(ALimit : integer);
    function IndexOfStr(const aStr: String): integer; virtual;
    function ObjectOf(const aStr: String): PObject; virtual;
  end ;

```

282. Pointer comparison. For strings, it is faster to use pointer comparison than lexicographic ordering. Although pointer comparison is a total linear order, it may not produce intuitive comparisons.

```

⟨MSortedStrList implementation 282⟩ ≡
  {MSortedStrList}
function CompareStringPtr(aKey1, aKey2 : Pointer): integer;
begin if PStr(aKey1)↑.fStr < PStr(aKey2)↑.fStr then CompareStringPtr ← -1
else if PStr(aKey1)↑.fStr = PStr(aKey2)↑.fStr then CompareStringPtr ← 0
else CompareStringPtr ← 1;
end;

```

This code is used in section 183.

283. Constructor. We just defer to the *InitSorted* constructor for sorted lists (§251).

As an invariant, the *fCompare* ordering operator is *always* assumed to be set to the *CompareStringPtr*. There is no other way to construct a sorted string list besides this constructor, which enforces this invariant.

```

constructor MSortedStrList.Init(ALimit : integer);
begin InitSorted(ALimit, CompareStringPtr);
end;

```

284. We can locate a string by *Find*-ing its entry in the *fIndex* array.

```

function MSortedStrList.IndexOfStr(const aStr: string): integer;
var I: integer; lStringObj: MStrObj;
begin IndexOfStr ← -1;
if @fCompare = nil then {Invariant violation}
begin ListError(coSortedListError, 0); exit;
end;
lStringObj.Init(aStr);
if Find(@lStringObj, I) then
begin if I < Count then IndexOfStr ← fIndex↑[I];
end;
end;

```

285. We also can return the pointer to the object, if it is present in the sorted string list.

```

function MSortedStrList.ObjectOf(const aStr: string): PObject;
var I: integer;
begin ObjectOf ← nil; I ← IndexOfStr(aStr);
if I ≥ 0 then ObjectOf ← Items↑[I];
end;

```

Section 9.9. SORTED COLLECTIONS

286.

```

⟨Public interface for mobjects.pas 184⟩ +≡
  { MSortedCollection object }
  PSortedCollection = ↑MSortedCollection;
  MSortedCollection = object (MCollection)
    Duplicates: boolean;
    fCompare: CompareProc;
    constructor Init(ALimit, ADelta : integer);
    constructor InitSorted(ALimit, ADelta : integer; aCompare : CompareProc);
    function Compare(Key1, Key2 : Pointer): integer; virtual;
    function IndexOf(aItem : Pointer): integer; virtual;
    procedure Insert(aItem : Pointer); virtual;
    procedure InsertD(Item : Pointer); virtual;
    function KeyOf(Item : Pointer): Pointer; virtual;
    function Search(Key : Pointer; var Index : integer): boolean; virtual;
  end ;

```

287. Constructors. We can construct a sorted collection without an ordering operator, and we can construct one with an ordering operator.

```

⟨MSortedCollection implementation 287⟩ ≡
  { MSortedCollection }
constructor MSortedCollection.Init(aLimit, aDelta : integer);
  begin inherited Init(ALimit, ADelta); Duplicates ← False; fCompare ← nil;
  end;
constructor MSortedCollection.InitSorted(aLimit, aDelta : integer; aCompare : CompareProc);
  begin inherited Init(ALimit, ADelta); Duplicates ← False; fCompare ← aCompare;
  end;

```

This code is used in section 183.

288. Comparing entries. This will invoke *Abstract1* (§183) when there is no ordering operator, which itself raises an error 211.

Otherwise, this just invokes *fCompare* on the two entries.

```

function MSortedCollection.Compare(Key1, Key2 : Pointer): integer;
  begin if @fCompare = nil then Abstract1;
  Compare ← fCompare(Key1, Key2);
  end;

```

289. Find the right-most index for an item in the collection. Searching (§293) for the *KeyOf* (§292). This function corrects for the possible bug in *Search* (§293) which will return the index *just to the left* of an item.

```

function MSortedCollection.IndexOf(aItem : Pointer): integer;
  var I: integer;
  begin IndexOf ← -1;
  if Search(KeyOf(aItem), I) then
    begin if Duplicates then
      while (I < Count) ∧ (aItem ≠ Items↑[I]) do inc(I);
    if I < Count then IndexOf ← I;
    end;
  end;

```

290. Insert the item when it is not in the collection (or if duplicates are allowed). Otherwise do not mutate the caller.

```
procedure MSortedCollection.Insert(aItem : Pointer);
  var I: integer;
  begin if  $\neg$ Search(KeyOf(aItem), I)  $\vee$  Duplicates then AtInsert(I, aItem);
  end;
```

291. Insert an item if it's not in the collection (or if there are duplicates allowed in the collection). Otherwise, delete the item and do not mutate the caller.

```
procedure MSortedCollection.InsertD(Item : Pointer);
  var I: integer;
  begin if  $\neg$ Search(KeyOf(Item), I)  $\vee$  Duplicates then AtInsert(I, Item)
  else Dispose(PObject(Item), Done);
  end;
```

292. We treat the item itself as the key, so return the item. That is to say, this is the identity function. It does not mutate the caller.

```
function MSortedCollection.KeyOf(Item : Pointer): Pointer;
  begin KeyOf  $\leftarrow$  Item;
  end;
```

293. Binary search. This is binary search through a sorted collection. If there are duplicates, this will return the left-most index.

```
function MSortedCollection.Search(Key : Pointer; var Index : integer): boolean;
  var L, H, I, C: integer;
  begin Search  $\leftarrow$  False; L  $\leftarrow$  0; H  $\leftarrow$  Count - 1;
  while L  $\leq$  H do
    begin I  $\leftarrow$  (L + H) shr 1; C  $\leftarrow$  Compare(KeyOf(Items↑[I]), Key);
    if C < 0 then L  $\leftarrow$  I + 1
    else begin H  $\leftarrow$  I - 1;
      if C = 0 then
        begin Search  $\leftarrow$  True;
        if  $\neg$ Duplicates then L  $\leftarrow$  I;
        end;
      end;
    end;
  Index  $\leftarrow$  L;
  end;
```

294. Perform the lexicographic ordering of (x_1, y_1) against (x_2, y_2) .

```
function CompareIntPairs(X1, Y1, X2, Y2 : Longint): integer;
  var lRes: integer;
  begin lRes  $\leftarrow$  CompareInt(X1, X2);
  if lRes = 0 then lRes  $\leftarrow$  CompareInt(Y1, Y2);
  CompareIntPairs  $\leftarrow$  lRes;
  end;
```

Section 9.10. STRING COLLECTION

295.

```

⟨Public interface for mobjects.pas 184⟩ +≡
  { MStringCollection object }
  PStringCollection = ↑MStringCollection;
  MStringCollection = object (MSortedCollection)
    function Compare(Key1, Key2 : Pointer): integer; virtual;
    procedure FreeItem(Item : Pointer); virtual;
  end ;
  { UnsortedStringCollection }
  PUnsortedStringCollection = ↑StringColl;
  StringColl = object (MCollection)
    procedure FreeItem(Item : pointer); virtual;
  end ;

```

296. String ordering operator. We have the usual lexicograph ordering as an operator ordering.

```

⟨String collection implementation 296⟩ ≡
  { MStringCollection }
function CompareStr(aStr1, aStr2 : string): integer;
  begin if aStr1 < aStr2 then CompareStr ← -1
  else if aStr1 = aStr2 then CompareStr ← 0
  else CompareStr ← 1;
  end;

```

This code is used in section 183.

297. We then have a convenience function to handle pointer dereferencing.

```

function MStringCollection.Compare(Key1, Key2 : Pointer): integer;
  begin Compare ← CompareStr(PString(Key1)↑, PString(Key2)↑);
  end;

```

298. Freeing items. We can free an item by simply freeing the string. This is the same for unsorted string collections, too.

```

procedure MStringCollection.FreeItem(Item : Pointer);
  begin DisposeStr(Item);
  end;
{ UnsortedStringCollection }
procedure StringColl.FreeItem(Item : pointer);
  begin DisposeStr(Item);
  end;

```

Section 9.11. INT COLLECTIONS

299. The *TIntItem* is needed for the unifier and equalizer.

```

⟨ Public interface for mobjects.pas 184 ⟩ +≡
  { MIntCollection object }
  IntPair = record X, Y: integer;
    end;
  IntPairItemPtr = ↑IntPairItem;
  IntPairItem = object (MObject)
    fKey: IntPair;
    constructor Init(X, Y : integer);
  end ;
  IntPtr = ↑integer;
  PIntItem = ↑TIntItem;
  TIntItem = object (MObject)
    IntKey: integer;
    constructor Init(fInt : integer);
  end ;
  PIntKeyCollection = ↑TIntKeyCollection;
  TIntKeyCollection = object (MSortedCollection)
    function KeyOf(Item : pointer): pointer; virtual;
    function Compare(Key1, Key2 : pointer): integer; virtual;
  end ;
  IntPairKeyCollectionPtr = ↑IntPairKeyCollection;
  IntPairKeyCollection = object (MSortedCollection)
    function Compare(Key1, Key2 : pointer): integer; virtual;
    function ObjectOf(X, Y : integer): IntPairItemPtr; virtual;
    function FirstThat(X : integer): IntPairItemPtr; virtual;
  end ;

```

300. TIntItem constructor. This just copies the given integer over to the newly allocated *TIntItem* object.

```

⟨ MIntCollection implementation 300 ⟩ ≡
  { MIntCollection }
  constructor TIntItem.Init(fInt : integer);
  begin IntKey ← fInt;
  end;

```

This code is used in section 183.

301. We use *TIntItems* as keys in a *TIntKeyCollection*.

```

function TIntKeyCollection.KeyOf(Item : pointer): pointer;
begin KeyOf ← addr(PIntItem(Item)↑.IntKey);
end;

```

302. Comparing items just looks at the integers referred by the pointers.

```
function TIntKeyCollection.Compare(Key1, Key2 : pointer): integer;
  begin Compare  $\leftarrow$  1;
  if IntPtr(Key1) $\uparrow$  < IntPtr(Key2) $\uparrow$  then
    begin Compare  $\leftarrow$  -1; exit
    end;
  if IntPtr(Key1) $\uparrow$  = IntPtr(Key2) $\uparrow$  then Compare  $\leftarrow$  0;
  end;
```

303. Constructor for pairs of integers.

```
constructor IntPairItem.Init(X, Y : integer);
  begin fKey.X  $\leftarrow$  X; fKey.Y  $\leftarrow$  Y;
  end;
```

304. Comparing two keys in a collection indexed by *IntPairs* is done “in the obvious way”.

```
function IntPairKeyCollection.Compare(Key1, Key2 : pointer): integer;
  begin Compare  $\leftarrow$  CompareIntPairs(IntPairItemPtr(Key1) $\uparrow$ .fKey.X, IntPairItemPtr(Key1) $\uparrow$ .fKey.Y,
    IntPairItemPtr(Key2) $\uparrow$ .fKey.X, IntPairItemPtr(Key2) $\uparrow$ .fKey.Y);
  end;
```

305. We can lookup the value associated to the key (*X*, *Y*) leveraging the *MSortedCollection.Search* function.

```
function IntPairKeyCollection.ObjectOf(X, Y : integer): IntPairItemPtr;
  var lPairItem: IntPairItem; I: integer;
  begin ObjectOf  $\leftarrow$  nil; lPairItem.Init(X, Y);
  if Search(addr(lPairItem), I) then ObjectOf  $\leftarrow$  Items $\uparrow$ [I];
  end;
```

306. This is used in *justhan.pas* and *mizprep.pas*.

```
function IntPairKeyCollection.FirstThat(X : integer): IntPairItemPtr;
  var I: integer;
  begin FirstThat  $\leftarrow$  nil;
  for i  $\leftarrow$  0 to Count - 1 do
    if IntPairItemPtr(Items $\uparrow$ [I]) $\uparrow$ .fKey.X = X then
      begin FirstThat  $\leftarrow$  Items $\uparrow$ [I]; exit
      end;
  end;
```

Section 9.12. STACKED LIST OF OBJECTS

307. “Stacked” lists are really linked lists.

```

⟨ Public interface for mobjects.pas 184 ⟩ +≡
  { Stacked Object (List of objects) }
  StackedPtr = ↑StackedObj;
  StackedObj = object (MObject)
    Previous: StackedPtr;
    constructor Init;
    destructor Done; virtual;
  end ;

```

308. The constructors and destructors are not implemented, so if you try to use them, just raise an error.

```

⟨ Stacked object implementation 308 ⟩ ≡
  { Stacked Object (List of objects) }
constructor StackedObj.Init;
  begin Abstract1;
  end;
destructor StackedObj.Done;
  begin Abstract1;
  end;

```

This code is used in section 183.

Section 9.13. STRING LIST

309.

```

⟨ Public interface for mobjects.pas 184 ⟩ +≡
  { MStringList object }
  MDuplicates = (dupIgnore, dupAccept, dupError);
  PStringItem = ↑MStringItem;
  MStringItem = record fString: PString;
    fObject: PObject;
  end;
  PStringItemList = ↑MStringItemList;
  MStringItemList = array [0 .. MaxListSize] of MStringItem;
  PStringList = ↑MStringList;
  MStringList = object (MObject)
    fList: PStringItemList;
    fCount: integer;
    fCapacity: integer;
    fSorted: boolean;
    fDuplicate: MDuplicates;
    constructor Init(aCapacity : integer);
    constructor MoveStringList(var aAnother : MStringList);
    { – Internal methods- do not use them directly – }
    procedure StringListError(Code, Info : integer); virtual;
    procedure Grow;
    procedure QuickSort(L, R : integer);
    procedure ExchangeItems(Index1, Index2 : integer);
    procedure InsertItem(aIndex : integer;
      const aStr: String); { – – }
    procedure SetSorted(aValue : boolean);
    procedure Sort; virtual;
    function GetString(aIndex : integer): String; virtual;
    function GetObject(aIndex : integer): PObject; virtual;
    procedure PutString(aIndex : integer;
      const aStr: String); virtual;
    procedure PutObject(aIndex : integer; aObject : PObject); virtual;
    procedure SetCapacity(aCapacity : integer); virtual;
    destructor Done; virtual;
    function AddString(const aStr: String): integer; virtual;
    function AddObject(const aStr: String;
      aObject: PObject): integer; virtual;
    procedure AddStrings(var aStrings : MStringList); virtual;
    procedure Clear; virtual;
    procedure Delete(aIndex : integer); virtual;
    procedure Exchange(Index1, Index2 : integer); virtual;
    procedure MoveObject(CurIndex, NewIndex : integer); virtual;
    function Find (
      const aStr: String;
      var aIndex: integer ) : boolean; virtual;
    function IndexOf(const aStr: String): integer; virtual;
    function ObjectOf(const aStr: String): PObject; virtual;
    function IndexOfObject(aObject : PObject): integer;
    procedure Insert(aIndex : integer;
      const aStr: String); virtual;
    procedure InsertObject(aIndex : integer;

```

```

    const aStr: String;
    aObject: PObject);
end ;

```

310. Constructors. We can construct an empty string collection using *Init*. We can also move the contents of *aAnother* string collection into the caller using *MoveStringList*.

```

⟨String list implementation 310⟩ ≡
    {————— MStringList —————}
constructor MStringList.Init(aCapacity : integer);
    begin MObject.Init; fList ← nil; fCount ← 0; fCapacity ← 0; fSorted ← false;
    fDuplicate ← dupError; SetCapacity(aCapacity);
    end;
constructor MStringList.MoveStringList(var aAnother : MStringList);
    begin MObject.Init; fCount ← aAnother.fCount; fCapacity ← aAnother.fCapacity;
    fSorted ← aAnother.fSorted; fList ← aAnother.fList; fDuplicate ← aAnother.fDuplicate;
    { Empty out the other list }
    aAnother.fCount ← 0; aAnother.fCapacity ← 0; aAnother.fList ← nil;
    end;

```

See also section 315.

This code is used in section 183.

311. Destructor. Since a *MStringItem* is a pointer to a string and a pointer to an *MObject*, freeing an *MStringItem* should free both of these (when they are present).

```

destructor MStringList.Done;
    var I: integer;
    begin inherited Done;
    for I ← 0 to fCount - 1 do
        with fList↑[I] do { free fList↑[I] }
            begin DisposeStr(fString);
            if fObject ≠ nil then Dispose(fObject, Done);
            end;
        fCount ← 0; SetCapacity(0);
    end;

```

312. Adding a string. This boils down to determining the position where we will insert the new string, then inserting the string into that location, and finally returning the index to the user.

```

function MStringList.AddString(const aStr: string): integer;
    var lResult: integer;
    begin ⟨Set lResult to the index of the newly inserted string 313⟩;
    InsertItem(lResult, aStr); AddString ← lResult;
    end;

```

313. Determining the index for the string boils down to whether the collection is sorted or not. If it is unsorted, then just append the string at the end of the collection.

For sorted collections, find the location for the string. We need to give particular care when adding the new string would create a duplicate entry in the string list.

```

⟨Set lResult to the index of the newly inserted string 313⟩ ≡
  if ¬fSorted then lResult ← fCount
  else if Find(aStr, lResult) then
    begin AddString ← lResult; ⟨De-duplicate a string list 314⟩;
    end

```

This code is used in section 312.

314. When we ignore duplicates (i.e., the *fDuplicate* flag is equal to *dupIgnore*), we can just terminate adding a string to the collection here.

But when we want to flag an error upon inserting a duplicate entry, then we should raise an error.

All other situations “fall through”.

```

⟨De-duplicate a string list 314⟩ ≡
  case fDuplicate of
    dupIgnore: Exit;
    dupError: StringListError(coDuplicate, 0);
  endcases

```

This code is used in section 313.

315. Inserting an object. We can treat a string list as a dictionary whose keys are strings. This is because the entries are string-(pointer to object) pairs.

```

⟨String list implementation 310⟩ +≡
function MStringList.AddObject(const aStr: string; aObject: PObject): integer;
  var lResult: integer;
  begin lResult ← AddString(aStr); { Insert key }
        PutObject(lResult, aObject); { Insert value }
        AddObject ← lResult; { Return index }
  end;

```

316. Appending a string list. We can add all the entries from another *MStringList* to the caller, which is what we do in the *AddStrings* function. It does not mutate *aStrings*.

```

procedure MStringList.AddStrings(var aStrings : MStringList);
  var I, r: integer;
  begin for I ← 0 to aStrings.fCount − 1 do
    r ← AddObject(aStrings.fList↑[I].fString↑, aStrings.fList↑[I].fObject);
  end;

```

317. Clear a string list. We can delete all the strings from a string list. This *will not* free the “values” in each key-value pair.

```

procedure MStringList.Clear;
  var I: integer;
  begin if fCount ≠ 0 then
    begin for I ← 0 to fCount − 1 do DisposeStr(fList↑[I].fString);
    fCount ← 0; SetCapacity(0);
    end;
  end;

```

318. Deleting an entry by index. When given an index which is within the bounds of the caller, we free the string located at that index, decrement the size, and then shift all entries after it down by one.

```

procedure MStringList.Delete(aIndex : integer);
  begin if (aIndex < 0)  $\vee$  (aIndex  $\geq$  fCount) then StringListError(coIndexError, aIndex);
    DisposeStr(fList↑[aIndex].fString); Dec(fCount);
  if aIndex < fCount then
    Move(fList↑[aIndex + 1], fList↑[aIndex], (fCount - aIndex) * SizeOf(MStringItem));
  end;

```

319. Exchanging items. We have *Exchange* check if the indices are within the bounds of the string list, then *ExchangeItems* swaps the items around.

```

procedure MStringList.Exchange(Index1, Index2 : integer);
  begin if (Index1 < 0)  $\vee$  (Index1  $\geq$  fCount) then StringListError(coIndexError, Index1);
  if (Index2 < 0)  $\vee$  (Index2  $\geq$  fCount) then StringListError(coIndexError, Index2);
    ExchangeItems(Index1, Index2);
  end;

procedure MStringList.ExchangeItems(Index1, Index2 : integer);
  var Temp: MStringItem;
  begin Temp  $\leftarrow$  fList↑[Index1]; fList↑[Index1]  $\leftarrow$  fList↑[Index2]; fList↑[Index2]  $\leftarrow$  Temp;
  end;

```

320. Find an entry by bisection search. We can use bisection search to find the needle in the haystack.

```

function MStringList.Find ( const aStr: string; var aIndex: integer ) : boolean;
  var L, H, I, C: integer; lResult: boolean;
  begin lResult  $\leftarrow$  False; L  $\leftarrow$  0; H  $\leftarrow$  fCount - 1;
  while L  $\leq$  H do
    begin I  $\leftarrow$  (L + H) shr 1; C  $\leftarrow$  CompareStr(fList↑[I].fString↑, aStr);
    if C < 0 then L  $\leftarrow$  I + 1
    else begin H  $\leftarrow$  I - 1;
      if C = 0 then
        begin lResult  $\leftarrow$  True;
        if fDuplicate  $\neq$  dupAccept then L  $\leftarrow$  I;
        end;
      end;
    end;
  end;
  aIndex  $\leftarrow$  L; Find  $\leftarrow$  lResult;
end;

```

321. Reporting errors. We can propagate errors, adjusting the error code as needed. The comment here is in Polish “poprawic bledy” (which Google translates to “correct the errors”)

```

procedure MStringList.StringListError(Code, Info : integer);
  begin RunError(212 - Code); {! poprawic bledy}
  end;

```

322. Getting the string at an index. When given an index within bounds, we try to get the string located there. If there is no string located at that entry, return the empty string.

```

function MStringList.GetString(aIndex : integer): string;
  begin if (aIndex < 0)  $\vee$  (aIndex  $\geq$  fCount) then StringListError(coIndexError, aIndex);
    GetString  $\leftarrow$  ``;
  if fList↑[aIndex].fString  $\neq$  nil then GetString  $\leftarrow$  fList↑[aIndex].fString↑;
  end;

```

323. Get object at index. We can get the object at an index, provided it is within bounds.

```
function MStringList.GetObject(aIndex : integer): PObject;
  begin if (aIndex < 0)  $\vee$  (aIndex  $\geq$  fCount) then StringListError(coIndexError, aIndex);
    GetObject  $\leftarrow$  fList $\uparrow$ [aIndex].fObject;
  end;
```

324. Ensure capacity for string lists. The growth rate for string lists differs from the earlier discussion on the growth rate for dynamic arrays. Well, actually, recalling our discussion (§196), we find this is identical to the previous growth rate. So I am not sure why this code is duplicated.

```
procedure MStringList.Grow;
  var Delta: integer;
  begin if fCapacity > 64 then Delta  $\leftarrow$  fCapacity div 4
    else if fCapacity > 8 then Delta  $\leftarrow$  16
      else Delta  $\leftarrow$  4;
    SetCapacity(fCapacity + Delta);
  end;
```

325. Index of a string. There are two branches to this function: one for unsorted string lists, the second for sorted string lists.

```
function MStringList.IndexOf(const aStr: string): integer;
  var lResult: integer;
  begin if  $\neg$ fSorted then
    begin for lResult  $\leftarrow$  0 to fCount - 1 do
      if CompareStr(fList $\uparrow$ [lResult].fString $\uparrow$ , aStr) = 0 then
        begin IndexOf  $\leftarrow$  lResult; Exit; end;
      lResult  $\leftarrow$  -1;
    end
    else if  $\neg$ Find(aStr, lResult) then lResult  $\leftarrow$  -1;
    { Assert: lResult = -1 if aStr is not in the caller }
    IndexOf  $\leftarrow$  lResult;
  end;
```

326. Value for a key. This appears to duplicate code from *GetObject* (§323).

```
function MStringList.ObjectOf(const aStr: string): PObject;
  var I: integer;
  begin ObjectOf  $\leftarrow$  nil; I  $\leftarrow$  IndexOf(aStr);
  if I  $\geq$  0 then ObjectOf  $\leftarrow$  fList $\uparrow$ [I].fObject;
  end;
```

327. Insert a string at an index. This seems to involve duplicate code as *AddString* (§312), but allows duplicate entries (which might violate the invariants of a string list).

```
procedure MStringList.Insert(aIndex : integer;
  const aStr: string);
  begin if fSorted then StringListError(coSortedListError, 0);
  if (aIndex < 0)  $\vee$  (aIndex > fCount) then StringListError(coIndexError, aIndex);
  InsertItem(aIndex, aStr);
  end;
```

328. Inserting an item at an index. We ensure the capacity of the string list. Then we shift the entries to the right by 1, if needed. We insert the string associated with no object. Then increment the logical size of the dynamic array.

```

procedure MStringList.InsertItem(aIndex : integer;
  const aStr: string);
  begin if fCount = fCapacity then Grow;
  { Shift existing entries to right by 1 }
  if aIndex < fCount then
    Move(fList↑[aIndex], fList↑[aIndex + 1], (fCount - aIndex) * SizeOf(MStringItem));
  with fList↑[aIndex] do
    begin fObject ← nil; fString ← NewStr(aStr); end;
  inc(fCount);
end;

```

329. Find the index for an object. Find the first instance of a key-value entry whose value is equal to the given object. If the given object is absent from the string list, return -1 .

```

function MStringList.IndexOfObject(aObject : PObject): integer;
  var lResult: integer;
  begin for lResult ← 0 to fCount - 1 do
    if GetObject(lResult) = aObject then
      begin IndexOfObject ← lResult; Exit; end;
  IndexOfObject ← -1;
end;

```

330. Inserting an object associated with a string.

```

procedure MStringList.InsertObject(aIndex : integer;
  const aStr: string;
  aObject: PObject);
  begin Insert(aIndex, aStr); PutObject(aIndex, aObject);
end;

```

331. Moving a key-value entry around. We can take the key-value entry at *CurIndex*, remove it from the string list, then insert it at *NewIndex*. It is important to note: the *NewIndex* is the index *after* the delete operation has occurred.

```

procedure MStringList.MoveObject(CurIndex, NewIndex : integer);
  var TempObject: PObject; TempString: string;
  begin if CurIndex ≠ NewIndex then
    begin TempString ← GetString(CurIndex); TempObject ← GetObject(CurIndex);
    Delete(CurIndex); InsertObject(NewIndex, TempString, TempObject);
    end;
  end;

```

332. Inserting a string at an index. Well, if this is a sorted collection, then raise an error: you can't insert strings willy-nilly!

Then check the index is within bounds, raise an error for out-of-bounds indices.

Then mutate the entry at $aIndex$ to have its string be equal to $NewStr(aStr)$.

This will always mutate the caller, even when the string located at the entry indexed by $aIndex$ is identical to $aStr$.

```

procedure MStringList.PutString( $aIndex$  : integer;
    const  $aStr$ : string);
begin if  $fSorted$  then StringListError( $coSortedListError$ , 0);
if ( $aIndex < 0$ )  $\vee$  ( $aIndex \geq fCount$ ) then StringListError( $coIndexError$ ,  $aIndex$ );
 $fList \uparrow [aIndex].fString \leftarrow NewStr(aStr)$ ;
end;

```

333. Inserting an object at an index. When given an index within bounds of the caller's underlying array, mutate its object to be the given $aObject$. Again, this *always* mutates the caller.

```

procedure MStringList.PutObject( $aIndex$  : integer;  $aObject$  : PObject);
begin if ( $aIndex < 0$ )  $\vee$  ( $aIndex \geq fCount$ ) then StringListError( $coIndexError$ ,  $aIndex$ );
 $fList \uparrow [aIndex].fObject \leftarrow aObject$ ;
end;

```

334. Quicksorting a string list. See also §257 and §403.

```

procedure MStringList.QuickSort( $L, R$  : integer);
var  $I, J$ : integer;  $P$ : string;
begin repeat  $I \leftarrow L$ ;  $J \leftarrow R$ ;  $P \leftarrow fList \uparrow [(L + R) \text{ shr } 1].fString$ ;
    repeat while CompareStr( $fList \uparrow [I].fString$ ,  $P$ )  $< 0$  do  $inc(I)$ ;
        while CompareStr( $fList \uparrow [J].fString$ ,  $P$ )  $> 0$  do  $Dec(J)$ ;
        if  $I \leq J$  then
            begin ExchangeItems( $I, J$ );  $inc(I)$ ;  $Dec(J)$ ; end;
        until  $I > J$ ;
        if  $L < J$  then QuickSort( $L, J$ );
         $L \leftarrow I$ ;
until  $I \geq R$ ;
end;

```

335. Changing the capacity of a string list. Of particular note here, changing the capacity of a string list *does not* delete anything. That work must be delegated elsewhere when $aCapacity < Self.fCapacity$ (if that case ever occurs).

```

procedure MStringList.SetCapacity( $aCapacity$  : integer);
var  $lList$ : PStringItemList;
begin if  $aCapacity < fCount$  then  $aCapacity \leftarrow fCount$ ;
if  $aCapacity > MaxListSize$  then  $aCapacity \leftarrow MaxListSize$ ;
if  $aCapacity \neq fCapacity$  then
    begin if  $aCapacity = 0$  then  $lList \leftarrow nil$ 
    else begin GetMem( $lList$ ,  $aCapacity * SizeOf(MStringItem)$ );
        if ( $fCount \neq 0$ )  $\wedge$  ( $fList \neq nil$ ) then Move( $fList \uparrow$ ,  $lList \uparrow$ ,  $fCount * SizeOf(MStringItem)$ );
        end;
    if  $fCapacity \neq 0$  then FreeMem( $fList$ ,  $fCapacity * SizeOf(MStringItem)$ );
     $fList \leftarrow lList$ ;  $fCapacity \leftarrow aCapacity$ ;
    end; { ReallocMem( $fList$ ,  $NewCapacity * SizeOf(MStringItem)$ );  $fCapacity := NewCapacity$ ; }
end;

```


336. Toggle ‘sorted’ flag. Allow the user to toggle the “sorted” flag. When toggled to *True*, be sure to sort the string list.

```

procedure MStringList.SetSorted(aValue : boolean);
  begin if fSorted  $\neq$  aValue then
    begin if aValue then Sort;
    fSorted  $\leftarrow$  aValue;
    end;
  end;

```

337. Sorting. This is a wrapper around the quicksort function (§334), invoked when the *fSorted* flag is false.

This appears to be used in the *SetSorted* procedure, but that is not used anywhere.

```

procedure MStringList.Sort;
  begin if  $\neg$ fSorted  $\wedge$  (fCount > 1) then
    begin fSorted  $\leftarrow$  true; QuickSort(0, fCount - 1);
    end;
  end;

```

338. Allocating a new string. Allocating a new *PString* from a string. When the empty string is given, return **nil**. Otherwise allocate a new block of memory in the Heap, then set its contents equal to *S*.

{ Dynamic string handling routines }

```

function NewStr(const S: String): PString;
  var P: PString;
  begin if S = '' then P  $\leftarrow$  nil
  else begin GetMem(P, length(S) + 1); P $\uparrow$   $\leftarrow$  S;
  end;
  NewStr  $\leftarrow$  P;
end;

```

339. Deleting a string. A convenience function to avoid accidentally freeing a **nil** string pointer.

```

procedure DisposeStr(P : PString);
  begin if P  $\neq$  nil then FreeMem(P, length(P $\uparrow$ ) + 1);
  end;

```

Section 9.14. TUPLES OF INTEGERS**340.**

```

⟨Public interface for mobjects.pas 184⟩ +≡
  { Partial integers Functions }
  IntTriplet = record X1, X2, Y: integer;
  end;
const MaxIntPairSize = MaxSize div SizeOf(IntPair);
  MaxIntTripletSize = MaxSize div SizeOf(IntTriplet);

```

341. Now, this is the remainder of the interface

```

⟨Public interface for mobjects.pas 184⟩ +≡
type IntPairListPtr = ↑IntPairList; IntPairList = array [0 .. MaxIntPairSize - 1] of IntPair;
  IntPairSeqPtr = ↑BinIntFunc; IntPairSeq = object (MObject)
    Items: IntPairListPtr;
    Count: integer;
    Limit: integer;
    constructor Init(aLimit : integer);
    procedure NatSetError(Code, Info : integer); virtual;
    destructor Done; virtual;
    procedure SetLimit(aLimit : integer); virtual;
    procedure Insert(const aItem: IntPair); virtual;
    procedure AtDelete(aIndex : integer);
    procedure DeleteAll;
    procedure AssignPair(X, Y : integer); virtual;
  end ;

```

342. First, we have a helper function for flagging errors.

```

⟨Tuples of integers 342⟩ ≡
  { Pairs of an integers }
procedure IntPairSeq.NatSetError(Code, Info : integer);
  begin RunError(212 - Code); end;

```

343. Constructor.

```

constructor IntPairSeq.Init(aLimit : integer);
  begin MObject.Init; Items ← nil; Count ← 0; Limit ← 0; SetLimit(aLimit);
  end;

```

344. Destructor.

```

destructor IntPairSeq.Done;
  begin Count ← 0; SetLimit(0);
  end;

```

345. Insert an element.

```

procedure IntPairSeq.Insert(const aItem: IntPair);
  begin if Count ≥ MaxIntPairSize then NatSetError(coOverflow, 0);
  if Limit = Count then SetLimit(Limit + GrowLimit(Limit));
  Items↑[Count] ← aItem; inc(Count);
  end;

```

346. Delete an element at an index.

```

procedure IntPairSeq.AtDelete(aIndex : integer);
  var i: integer;
  begin if (aIndex < 0)  $\vee$  (aIndex  $\geq$  Count) then
    begin NatSetError(coIndexError, 0); exit; end;
  if aIndex < Count - 1 then
    for i  $\leftarrow$  aIndex to Count - 2 do Items $\uparrow$ [i]  $\leftarrow$  Items $\uparrow$ [i + 1];
  Dec(Count);
  end;

```

347. Resizing an IntPair sequence.

```

procedure IntPairSeq.SetLimit(aLimit : integer);
  var aItems: IntPairListPtr;
  begin if aLimit < Count then aLimit  $\leftarrow$  Count;
  if aLimit > MaxIntPairSize then ALimit  $\leftarrow$  MaxIntPairSize;
  if aLimit  $\neq$  Limit then
    begin if ALimit = 0 then ALimit  $\leftarrow$  nil
    else begin GetMem(ALimit, ALimit * SizeOf(IntPair));
      if (Count  $\neq$  0)  $\wedge$  (Items  $\neq$  nil) then Move(Items $\uparrow$ , aItems $\uparrow$ , Count * SizeOf(IntPair));
      end;
    if Limit  $\neq$  0 then FreeMem(Items, Limit * SizeOf(IntPair));
    Items  $\leftarrow$  aItems; Limit  $\leftarrow$  aLimit;
    end;
  end;

```

348. Deleting all entries. We just set the logical size to zero. It leaves everything else untouched.

```

procedure IntPairSeq.DeleteAll;
  begin Count  $\leftarrow$  0; end;

```

349. Append a pair of integers. We create a new *IntPair* using *X* and *Y*, then append it to the caller.

```

procedure IntPairSeq.AssignPair(X, Y : integer);
  var UntPair: IntPair;
  begin UntPair.X  $\leftarrow$  X; UntPair.Y  $\leftarrow$  Y; Insert(UntPair);
  end;

```

Section 9.15. INT REL

350. This is used in the `iocorrel.pas`, `identify.pas`, `equalizer.pas`, the analyzer, and a polynomial library.

```

⟨Public interface for mobjects.pas 184⟩ +≡
  IntRelPtr = ↑IntRel;
  IntRel = object (IntPairSeq)
    constructor Init(aLimit : integer);
    procedure Insert(const aItem: IntPair); virtual;
    procedure AtInsert(aIndex : integer;
      const aItem: IntPair); virtual;
    function Search(X, Y : integer; var aIndex : integer): boolean; virtual;
    function IndexOf(X, Y : integer): integer;
    constructor CopyIntRel(var aFunc : IntRel);
    function IsMember(X, Y : integer): boolean; virtual;
    procedure AssignPair(X, Y : integer); virtual;
  end ;

```

351. Constructor. This is just the inherited constructor.

```

⟨Int relation implementation 351⟩ ≡
{ IntRel }
constructor IntRel.Init(aLimit : integer);
  begin inherited Init(aLimit);
  end;

```

This code is used in section 183.

352. Inserting an entry.

```

procedure IntRel.Insert(const aItem: IntPair);
  var I: integer;
  begin if ¬Search(aItem.X, aItem.Y, I) then
    begin if (I < 0) ∨ (I > Count) then
      begin NatSetError(coIndexError, 0); exit; end;
    if Count ≥ MaxIntPairSize then NatSetError(coOverflow, 0);
      { Finished with the possible errors }
    if Limit = Count then SetLimit(Limit + GrowLimit(Limit));
    if I ≠ Count then Move(Items↑[I], Items↑[I + 1], (Count - I) * SizeOf(IntPair));
    Items↑[I] ← aItem; inc(Count);
  end;
end;

```

353. Insert at a specific index.

```

procedure IntRel.AtInsert(aIndex : integer;
  const aItem: IntPair);
  begin if (aIndex < 0)  $\vee$  (aIndex > Count) then NatSetError(coIndexError, aIndex);
  if Count = Limit then SetLimit(Limit + GrowLimit(Limit));
    { Shift everything to the right by 1 }
  if aIndex < Limit then Move(Items $\uparrow$ [aIndex], Items $\uparrow$ [aIndex + 1], (Count - aIndex) * SizeOf(IntPair));
    { Update the items, increment the logical size }
  Items $\uparrow$ [aIndex]  $\leftarrow$  aItem; inc(Count);
end;

```

354. Bisection search for a relation. Search through *IntRel* for a relation $X = Y$. Note that this is not symmetric, i.e., if we have $Y = X$ in the *IntRel*, then it will not match.

Mutates the *aIndex*. If the relation is missing, *aIndex* will return where it *should* be.

```

function IntRel.Search(X, Y : integer; var aIndex : integer): boolean;
  var L, H, I, C: integer;
  begin Search  $\leftarrow$  False; L  $\leftarrow$  0; H  $\leftarrow$  Count - 1;
  while L  $\leq$  H do
    begin I  $\leftarrow$  (L + H) shr 1; C  $\leftarrow$  CompareIntPairs(Items $\uparrow$ [I].X, Items $\uparrow$ [I].Y, X, Y);
    if C < 0 then L  $\leftarrow$  I + 1
    else begin H  $\leftarrow$  I - 1;
      if C = 0 then
        begin Search  $\leftarrow$  True; L  $\leftarrow$  I; end;
      end;
    end;
  aIndex  $\leftarrow$  L;
end;

```

355. Copy constructor. This moves the contents of *aFunc* into the caller. It will mutate the caller *but not* the argument supplied. The *Move* function copies the contents of one region of memory to another.

```

constructor IntRel.CopyIntRel(var aFunc : IntRel);
  begin Init(aFunc.Limit); Move(aFunc.Items $\uparrow$ , Items $\uparrow$ , aFunc.Limit * SizeOf(IntPair));
  Count  $\leftarrow$  aFunc.Count;
end;

```

356. Index of a relation. This will return the index of the $X = Y$ entry. If it is absent from the caller, then return -1.

```

function IntRel.IndexOf(X, Y : integer): integer;
  var I: integer;
  begin IndexOf  $\leftarrow$  -1;
  if Search(X, Y, I) then IndexOf  $\leftarrow$  I;
end;

```

357. Test for membership. This just tests if $X = Y$ is contained in the caller.

```

function IntRel.IsMember(X, Y : integer): boolean;
  var I: integer;
  begin IsMember  $\leftarrow$  Search(X, Y, I); end;

```

358.

```
procedure IntRel.AssignPair(X, Y : integer);  
  begin if IsMember(X, Y) then exit;  
    inherited AssignPair(X, Y);  
  end;
```

Section 9.16. PARTIAL INTEGERS FUNCTIONS

359.

```

⟨Public interface for mobjects.pas 184⟩ +≡
  NatSetPtr = ↑NatSet;
  NatSet = object (IntRel)
    Delta: integer;
    Duplicates: boolean;
    constructor Init(aLimit, aDelta : integer);
    constructor InitWithElement(X : integer);
    destructor Done; virtual;
    procedure Insert(const aItem: IntPair); virtual;
    function SearchPair(X : integer; var Index : integer): boolean; virtual;
    function ElemNr(X : integer): integer;
    { ***** }
    constructor CopyNatSet(const fFunc: NatSet);
    procedure InsertElem(X : integer); virtual;
    procedure DeleteElem(fElem : integer); virtual;
    procedure EnlargeBy(const fAnother: NatSet); { ? virtual? }

    procedure ComplementOf(const fAnother: NatSet);
    procedure IntersectWith(const fAnother: NatSet);
    { ***** }
    function HasInDom(fElem : integer): boolean; virtual;
    function IsEqualTo(const fFunc: NatSet): boolean;
    function IsSubsetOf(const fFunc: NatSet): boolean;
    function IsSupersetOf(const fFunc: NatSet): boolean;
    function Misses(const fFunc: NatSet): boolean;
    constructor MoveNatSet(var fFunc : NatSet);
  end ;

```

360. Constructor. The empty *NatSet* can be constructed with the usual initialization.

```

⟨Partial integer function implementation 360⟩ ≡
  { Partial integers Functions }
constructor NatSet.Init(aLimit, aDelta : integer);
  begin MObject.Init; Items ← nil; Count ← 0; Limit ← 0; Delta ← ADelta; SetLimit(ALimit);
  Duplicates ← False;
end;

```

This code is used in section 183.

361. Singleton constructor. This initializes the *Delta* set to 4, and the *aLimit* set to 0. Then insert the given integer.

```

constructor NatSet.InitWithElement(X : integer);
  begin Init(0, 4); InsertElem(X);
end;

```

362. Destructor. This delegates the heavy work to *SetLimit*(0).

```

destructor NatSet.Done;
  begin Count ← 0; SetLimit(0);
end;

```

363. Inserting a pair of integers. Using *Search* to find where to insert $X = Y$, possibly growing the underlying array if needed.

```

procedure NatSet.Insert(const aItem: IntPair);
  var I: integer;
  begin if  $\neg \text{SearchPair}(aItem.X, I) \vee \text{Duplicates}$  then
    begin if  $(I < 0) \vee (I > \text{Count})$  then { Out of bounds, raise an error }
      begin NatSetError(coIndexError, 0); exit; end;
    if Limit = Count then { Grow the capacity, if possible }
      begin if Delta = 0 then
        begin NatSetError(coOverflow, 0); exit; end;
        SetLimit(Limit + Delta);
      end;
    if  $I \neq \text{Count}$  then Move(Items $\uparrow$ [I], Items $\uparrow$ [I + 1], (Count - I) * SizeOf(IntPair));
    Items $\uparrow$ [I]  $\leftarrow$  aItem; inc(Count);
  end;
end;

```

364. Equality of IntPair objects. This just tests the componentwise equality of two *IntPair* objects.

```

function Equals(Key1, Key2 : IntPair): boolean;
  begin Equals  $\leftarrow$  (Key1.X = Key2.X)  $\wedge$  (Key1.Y = Key2.Y);
end;

```

365. Search. This is a bisection search for any relation of the form $X = Y$ for some Y .

```

function NatSet.SearchPair(X : integer; var Index : integer): boolean;
  var L, H, I, C: integer;
  begin SearchPair  $\leftarrow$  False; L  $\leftarrow$  0; H  $\leftarrow$  Count - 1;
  while  $L \leq H$  do
    begin I  $\leftarrow$   $(L + H) \text{ shr } 1$ ; C  $\leftarrow$  CompareInt(Items $\uparrow$ [I].X, X);
    if  $C < 0$  then L  $\leftarrow$  I + 1
    else begin H  $\leftarrow$  I - 1;
      if  $C = 0$  then
        begin SearchPair  $\leftarrow$  True;
        if  $\neg \text{Duplicates}$  then L  $\leftarrow$  I;
        end;
      end;
    end;
  end;
  Index  $\leftarrow$  L;
end;

```

366. Copy constructor. We can copy the contents of another *NatSet* into the caller. This mutates the caller, but leaves the given *NatSet* unchanged.

```

constructor NatSet.CopyNatSet(const fFunc: NatSet);
  begin Init(fFunc.Limit, fFunc.Delta); Move(fFunc.Items $\uparrow$ , Items $\uparrow$ , fFunc.Limit * SizeOf(IntPair));
  Count  $\leftarrow$  fFunc.Count;
end;

```


367. Move constructor. We can also *move* the contents of another *NatSet* into the caller. This will mutate the other *NatSet* to have **nil** items and 0 capacity.

```

constructor NatSet.MoveNatSet(var fFunc : NatSet);
  begin Init(fFunc.Limit, fFunc.Delta); Self  $\leftarrow$  fFunc; fFunc.DeleteAll; fFunc.Limit  $\leftarrow$  0;
  fFunc.Items  $\leftarrow$  nil;
end;

```

368. Union operation. We can merge another *NatSet* into the caller.

```

procedure NatSet.EnlargeBy(const fAnother : NatSet);
  var I : integer;
  begin for I  $\leftarrow$  0 to fAnother.Count - 1 do InsertElem(fAnother.Items $\uparrow$ [i].X);
end;

```

369. Set complement. We can destructively remove from the caller all elements appearing in *fAnother* nat set.

```

procedure NatSet.ComplementOf(const fAnother : NatSet);
  var I : integer;
  begin for I  $\leftarrow$  0 to fAnother.Count - 1 do DeleteElem(fAnother.Items $\uparrow$ [i].X);
end;

```

370. Take intersection. This computes $Self \leftarrow Self \cap Other$

```

procedure NatSet.IntersectWith(const fAnother : NatSet);
  var k : integer;
  begin k  $\leftarrow$  0;
  while k < Count do
    if  $\neg$ fAnother.HasInDom(Items $\uparrow$ [k].X) then AtDelete(k)
    else inc(k);
  end;

```

371. Insert an element. We can insert $X = 0$ into the caller.

```

procedure NatSet.InsertElem(X : integer);
  var UntPair : IntPair;
  begin UntPair.X  $\leftarrow$  X; UntPair.Y  $\leftarrow$  0; Insert(UntPair);
end;

```

372. Deleting an element. Similarly, we can delete the first element of the form $X = Y$ for some Y .

```

procedure NatSet.DeleteElem(fElem : integer);
  var I : integer;
  begin if SearchPair(fElem, I) then AtDelete(I);
end;

```

373. We can test if an element X is in the domain of the caller.

```

function NatSet.HasInDom(fElem : integer): boolean;
  var I : integer;
  begin HasInDom  $\leftarrow$  SearchPair(fElem, I);
end;

```

374. Set equality predicate. This assumes that there are no duplicate entries in a *NatSet* data structure.

```
function NatSet.IsEqualTo(const fFunc: NatSet): boolean;
  var I: integer;
  begin IsEqualTo ← false;
  if Count ≠ fFunc.Count then exit;
  for I ← 0 to Count - 1 do
    if ¬Equals(Items↑[I], fFunc.Items↑[I]) then exit;
  IsEqualTo ← true;
end;
```

375. Subset predicate. The comment is Polish for (according to Google translate): “If we’re checking if a small function is contained within a large one, commenting it out might be better.” There is a commented out function which I removed.

```
function NatSet.IsSubsetOf(const fFunc: NatSet): boolean;
  var i, j, k, c: integer; { Jezeli sprawdzamy, czy mala funkcja jest zawarta w duzej, to to wykomentowane
                             moze byc lepsze }
  begin IsSubsetOf ← false; c ← fFunc.Count;
  if c < Count then exit;
  j ← 0;
  for i ← 0 to Count - 1 do
    begin k ← Items↑[i].X;
    while (j < c) ∧ (fFunc.Items↑[j].X < k) do inc(j);
    if (j = c) ∨ ¬Equals(fFunc.Items↑[j], Items↑[i]) then exit;
    end;
  IsSubsetOf ← true;
end;
```

376. Superset predicate. This just takes advantage of the fact that $Y \supseteq X$ is the same as $X \subseteq Y$, then use the subset predicate.

```
function NatSet.IsSupersetOf(const fFunc: NatSet): boolean;
  begin IsSupersetOf ← fFunc.IsSubsetOf(Self);
end;
```

377. Test if two sets are disjoint. This iterates over the smaller of the two sets, checking if every element in the smaller set *does not* appear in the larger set.

```
function NatSet.Misses(const fFunc: NatSet): boolean;
  var I, k: integer;
  begin if Count > fFunc.Count then
    begin for k ← 0 to fFunc.Count - 1 do
      if SearchPair(fFunc.Items↑[k].X, I) then
        begin Misses ← false; exit end
      end
    else begin for k ← 0 to Count - 1 do
      if fFunc.SearchPair(Items↑[k].X, I) then
        begin Misses ← false; exit end;
      end;
    Misses ← true;
  end;
```

378. Index for an element. This searches for the index associated with relations of the form $X = Y$. If any such relation appears, return its index. Otherwise, return -1 .

It leaves the caller unmodified, so it is a pure function.

```
function NatSet.ElemNr( $X : integer$ ): integer;  
  var  $I : integer$ ;  
  begin  $ElemNr \leftarrow -1$ ;  
  if SearchPair( $X, I$ ) then  $ElemNr \leftarrow I$ ;  
  end;
```

Section 9.17. FUNCTION OF NATURAL NUMBERS

379. The *NatFunc* is used in the analyzer, equalizer, unifier, and elsewhere. Its destructor is the only place where $nConsistent \leftarrow false$.

```

⟨ Public interface for mobjects.pas 184 ⟩ +≡
  NatFuncPtr = ↑NatFunc;
  NatFunc = object (NatSet)
    nConsistent: boolean;
    constructor InitNatFunc(ALimit, ADelta : integer);
    constructor CopyNatFunc(const fFunc: NatFunc);
    constructor MoveNatFunc(var fFunc : NatFunc);
    constructor LCM(const aFunc1, aFunc2: NatFunc);
    procedure Assign(X, Y : integer); virtual;
    procedure Up(X : integer); virtual;
    procedure Down(X : integer); virtual;
    function Value(fElem : integer): integer; virtual;
    procedure Join(const fFunc: NatFunc);
    destructor Refuted; virtual;
    procedure EnlargeBy(fAnother : NatFuncPtr); { ? virtual;? }

    function JoinAtom(fLatAtom : NatFuncPtr): NatFuncPtr;
    function CompareWith(const fNatFunc: NatFunc): integer;
    function WeakerThan(const fNatFunc: NatFunc): boolean;
    function IsMultipleOf(const fNatFunc: NatFunc): boolean;
    procedure Add(const aFunc: NatFunc);
    function CountAll: integer; virtual;
  end ;

```

380. Constructors. We have the basic constructors for an empty *NatFunc*, a copy constructor, and a move constructor. The move constructor is destructive on the supplied argument.

```

⟨ NatFunc implementation 380 ⟩ ≡
  constructor NatFunc.InitNatFunc(ALimit, ADelta : integer);
    begin inherited Init(ALimit, ADelta); nConsistent ← true;
    end;

  constructor NatFunc.CopyNatFunc(const fFunc: NatFunc);
    begin Init(fFunc.Limit, fFunc.Delta); Move(fFunc.Items↑, Items↑, fFunc.Limit * SizeOf(IntPair));
    Count ← fFunc.Count; nConsistent ← fFunc.nConsistent;
    end;

  constructor NatFunc.MoveNatFunc(var fFunc : NatFunc);
    begin Init(fFunc.Limit, fFunc.Delta); Self ← fFunc; fFunc.DeleteAll; fFunc.Limit ← 0;
    fFunc.Items ← nil;
    end;

```

See also section 396.

This code is used in section 183.

381. Constructor (LCM). The least common multiple between two *NatFunc* objects is another way to construct a *NatFunc* instance. This seems to be the LCM in the sense of commutative rings (if x and y are elements of a commutative ring R , then $\text{lcm}(x, y)$ is such that x divides $\text{lcm}(x, y)$ and y divides $\text{lcm}(x, y)$ — moreover, $\text{lcm}(x, y)$ is the smallest such quantity, in the sense that $\text{lcm}(x, y)$ divides any other such quantity).

For the ring (or ringoid) $\mathbf{N}^{\mathbf{N}}$, this amounts to

$$\text{lcm}(f, g) = \{ (x, y) \mid \exists y_1, y_2, (x, y_1) \in f, (x, y_2) \in g, y = \text{lcm}(y_1, y_2) \},$$

with the condition that when $y_1 = 0$, $y = y_2$ (and similarly $y_2 = 0$ implies $y = y_1$).

```

constructor NatFunc.LCM (const aFunc1, aFunc2: NatFunc);
  var i, j, m: integer;
  begin m  $\leftarrow$  aFunc2.Delta;
  if aFunc1.Delta > m then m  $\leftarrow$  aFunc1.Delta;
  InitNatFunc(aFunc1.Limit + aFunc2.Limit, m); i  $\leftarrow$  0; j  $\leftarrow$  0;
  while (i < aFunc1.Count)  $\wedge$  (j < aFunc2.Count) do
    case CompareInt(aFunc1.Items $\uparrow$ [i].X, aFunc2.Items $\uparrow$ [j].X) of
      -1: begin Insert(aFunc1.Items $\uparrow$ [i]); inc(i) end;
      0: begin { m = max(f(i), g(i) }
          m  $\leftarrow$  aFunc1.Items $\uparrow$ [i].Y;
          if aFunc2.Items $\uparrow$ [j].Y > m then m  $\leftarrow$  aFunc2.Items $\uparrow$ [j].Y;
          Assign(aFunc1.Items $\uparrow$ [i].X, m); { destructively set f(i)  $\leftarrow$  m }
          inc(i); inc(j);
          end;
      1: begin Insert(aFunc2.Items $\uparrow$ [j]); inc(j) end;
    endcases;
  if i  $\geq$  aFunc1.Count then
    for j  $\leftarrow$  j to aFunc2.Count - 1 do Insert(aFunc2.Items $\uparrow$ [j])
  else for i  $\leftarrow$  i to aFunc1.Count - 1 do Insert(aFunc1.Items $\uparrow$ [i]);
  end;

```

382. Extend a natural function. We can extend a natural function to assign a value y to a place where it is not yet defined $x \notin \text{dom}(f)$.

We should recall *HasInDom* (§373) which depends on *SearchPair* (§365) is relevant. When trying to assign a different value y to an already defined $f(x) \neq y$, then we have refuted something.

```

procedure NatFunc.Assign(X, Y: integer);
  var UntPair: IntPair;
  begin if nConsistent then
    begin if HasInDom(X)  $\wedge$  (Value(X)  $\neq$  Y) then
      begin Refuted; exit end;
      UntPair.X  $\leftarrow$  X; UntPair.Y  $\leftarrow$  Y; Insert(UntPair);
    end;
  end;

```

383. Increment $f(x)$. Given a *NatFunc* object f , and an integer x , $f.Up(x)$ will

- (1) If $x \in \text{dom}(f)$, then update the value $f(x) \geq f(x) + 1$
- (2) Otherwise, $x \notin \text{dom}(f)$, so this corresponds to $f(x) = 0$, then we mutate $f(x) \leftarrow 1$.

```

procedure NatFunc.Up( $X : \text{integer}$ );
  var  $I : \text{integer}$ ;  $\text{IntPair} : \text{IntPair}$ ;
  begin if  $n\text{Consistent}$  then
    begin if  $\text{SearchPair}(X, I)$  then  $\text{inc}(\text{Items}\uparrow[I].Y)$ 
    else begin  $\text{IntPair}.X \leftarrow X$ ;  $\text{IntPair}.Y \leftarrow 1$ ;  $\text{Insert}(\text{IntPair})$ ;
      end;
    end;
  end;

```

384. Decrement $f(x)$. Given a *NatFunc* object f , and an integer x , $f.Down(x)$ will

- (1) If $x \in \text{dom}(f)$, then update the value $f(x) \geq f(x) - 1$ and if this is then zero, remove it from the function.
- (2) Otherwise, $x \notin \text{dom}(f)$, so this corresponds to $f(x) = 0$, and we cannot mutate $f(x) \leftarrow -1$ without making it no longer natural-valued. So we raise an error.

```

procedure NatFunc.Down( $X : \text{integer}$ );
  var  $I : \text{integer}$ ;
  begin if  $n\text{Consistent}$  then
    begin if  $\text{SearchPair}(X, I)$  then
      begin  $\text{dec}(\text{Items}\uparrow[I].Y)$ ;
        if  $\text{Items}\uparrow[I].Y = 0$  then  $\text{AtDelete}(I)$ ;
        end
      else  $\text{NatSetError}(\text{coConsistentError}, 0)$ ;
    end;
  end;

```

385. Getting the value of $f(x)$ when $x \in \text{dom}(f)$. When $x \notin \text{dom}(f)$, raise an error.

```

function NatFunc.Value( $f\text{Elem} : \text{integer}$ ):  $\text{integer}$ ;
  var  $I : \text{integer}$ ;
  begin if  $\text{SearchPair}(f\text{Elem}, I)$  then  $\text{Value} \leftarrow \text{Items}\uparrow[I].Y$ 
  else  $\text{NatSetError}(\text{coDuplicate}, 0)$ ;
  end;

```

386. Destructor. We usually try to extend partial functions on \mathbf{N} , but if we end up trying to extend where it is already defined to a different value, then we arrive at an inconsistent extension. It is referred to as a “refuted” situation.

```

destructor NatFunc.Refuted;
  begin  $\text{inherited Done}$ ;  $n\text{Consistent} \leftarrow \text{false}$ 
  end;

```

387. Join. For two partial functions $f: \mathbf{N} \rightarrow \mathbf{N}$ and $g: \mathbf{N} \rightarrow \mathbf{N}$, we form $f \cup g$ provided

$$f \cap g = f|_{\text{dom}(f \cap g)} = g|_{\text{dom}(f \cap g)}.$$

That is to say, for all $x \in \text{dom}(f) \cap \text{dom}(g)$, we have $f(x) = g(x)$.

The comment is in Polish, which Google translates as: “It seems that the *Join* and *EnlargeBy* procedures below do the same thing. *EnlargeBy* should be faster for small collections. If not, it’s not worth the code waste and can be discarded. On the other hand, these procedures are primarily intended for (very) small collections.”

Also worth observing, this tests for consistency in the other *NatFunc*.

```
{ Wyglada na to, ze ponizej podane procedury "Join" i "EnlargeBy" robia to samo, "EnlargeBy"
  powinna byc szybsza dla malych kolekcji. Jezeli tak nie jest nie warto tracic kodu i mozna ja
  wyrzucic. Z drugiej strony procedury te maja byc glownie stosowane do (bardzo) malych kolekcji. }
procedure NatFunc.Join(const fFunc: NatFunc);
var I, k: integer;
begin if nConsistent then
  begin if  $\neg fFunc.nConsistent$  then
    begin Refuted; exit end;
  for  $k \leftarrow 0$  to fFunc.Count  $- 1$  do
    if SearchPair(fFunc.Items $\uparrow[k]$ .X, I) then
      begin if  $\neg Equals(Items\uparrow[I], fFunc.Items\uparrow[k])$  then
        begin Refuted; exit end;
      end
    else Insert(fFunc.Items $\uparrow[k]$ );
  end;
end;
```

388. This function performs the same task as the previous one (i.e., it merges another partial function into the caller, provided it is consistent on overlap).

```
procedure NatFunc.EnlargeBy(fAnother : NatFuncPtr); { ? virtual;? }
var i, j, lCount, lLimit: integer; lItems: IntPairListPtr;
begin if nConsistent then
  begin if  $\neg fAnother\uparrow.nConsistent$  then
    begin Refuted; exit end;
  if fAnother $\uparrow.Count = 0$  then exit;
  lCount  $\leftarrow Count$ ; lItems  $\leftarrow Items$ ; lLimit  $\leftarrow Limit$ ; Limit  $\leftarrow 0$ ; Count  $\leftarrow 0$ ;
  SetLimit(lCount + fAnother $\uparrow.Count$ ); i  $\leftarrow 0$ ; j  $\leftarrow 0$ ;
  while ( $i < lCount$ )  $\wedge$  ( $j < fAnother\uparrow.Count$ ) do
    case CompareInt(lItems $\uparrow[i]$ .X, fAnother $\uparrow.Items$  $\uparrow[j]$ .X) of
       $-1$ : begin Insert(lItems $\uparrow[i]$ ); inc(i) end;
       $0$ : begin if Equals(lItems $\uparrow[i]$ , fAnother $\uparrow.Items$  $\uparrow[j]$ ) then Insert(lItems $\uparrow[i]$ )
        else begin Refuted; FreeMem(lItems, lLimit * SizeOf(IntPair)); exit end;
        inc(i); inc(j);
      end;
       $1$ : begin Insert(fAnother $\uparrow.Items$  $\uparrow[j]$ ); inc(j) end;
    endcases;
  if  $i \geq lCount$  then
    for  $j \leftarrow j$  to fAnother $\uparrow.Count - 1$  do Insert(fAnother $\uparrow.Items$  $\uparrow[j]$ )
  else for  $i \leftarrow i$  to lCount - 1 do Insert(lItems $\uparrow[i]$ );
  SetLimit( $0$ ); FreeMem(lItems, lLimit * SizeOf(IntPair));
  end;
end;
```

389. We want to join two partial functions $f: \mathbf{N} \rightarrow \mathbf{N}$ and $g: \mathbf{N} \rightarrow \mathbf{N}$ without accidentally mutating either f or g to be refuted. To do this, we copy the caller, then enlarge it with the other partial function. If the result is consistent, then return it. Otherwise, return **nil**.

This leaves both the caller and $fLatAtom$ unchanged, so it's a pure function.

```
function NatFunc.JoinAtom(fLatAtom : NatFuncPtr): NatFuncPtr;
var lEval: NatFunc;
begin JoinAtom  $\leftarrow$  nil; lEval.CopyNatFunc(Self); lEval.EnlargeBy(fLatAtom);
if lEval.nConsistent then JoinAtom  $\leftarrow$  NatFuncPtr(lEval.CopyObject);
end;
```

390. Comparing partial functions. Given two partial functions, $f: \mathbf{N} \rightarrow \mathbf{N}$ and $g: \mathbf{N} \rightarrow \mathbf{N}$, we want to compare them. We first start with comparing $\|f\|$ against $\|g\|$. If they are not equal, then this is the result.

When $\|f\| = \|g\|$, iterate through each $x \in \text{dom}(f)$, and then compare $f(x)$ against $g(x)$. If $f(x) < g(x)$, then return -1 . If $f(x) > g(x)$, then return $+1$. Otherwise keep iterating until we have examined all of $\text{dom}(f)$, and then we return 0 .

```
function CompareNatFunc(aKey1, aKey2 : Pointer): integer;
var i, lnt: integer;
begin with NatFuncPtr(aKey1) $\uparrow$  do
  begin lnt  $\leftarrow$  CompareInt(Count, NatFuncPtr(aKey2) $\uparrow$ .Count);
  if lnt  $\neq$   $0$  then
    begin CompareNatFunc  $\leftarrow$  lnt; exit end;
  for i  $\leftarrow$   $0$  to Count  $- 1$  do
    begin lnt  $\leftarrow$  CompareInt(Items $\uparrow$ [i].X, NatFuncPtr(aKey2) $\uparrow$ .Items $\uparrow$ [i].X);
    if lnt  $\neq$   $0$  then
      begin CompareNatFunc  $\leftarrow$  lnt; exit end;
      lnt  $\leftarrow$  CompareInt(Items $\uparrow$ [i].Y, NatFuncPtr(aKey2) $\uparrow$ .Items $\uparrow$ [i].Y);
      if lnt  $\neq$   $0$  then
        begin CompareNatFunc  $\leftarrow$  lnt; exit end;
      end;
    end;
  CompareNatFunc  $\leftarrow$   $0$ ;
end;
```

391. Let $f: \mathbf{N} \rightarrow \mathbf{N}$ and $g: \mathbf{N} \rightarrow \mathbf{N}$ be partial functions. We say that f is “weaker” than g when $\|f\| \leq \|g\|$ and for each $x \in \text{dom}(f)$ we have $f(x) = g(x)$. If there is some $x \in \text{dom}(f)$ such that $x \notin \text{dom}(g)$, then f is not weaker than g .

If there is some $x \in \text{dom}(f)$ such that $x \in \text{dom}(g)$ and $f(x) \neq g(x)$, then f is not weaker than g .

```
function NatFunc.WeakerThan(const fNatFunc: NatFunc): boolean;
var i, k: integer;
begin WeakerThan  $\leftarrow$  false;
if Count  $\leq$  fNatFunc.Count then
  begin for k  $\leftarrow$   $0$  to Count  $- 1$  do
    begin i  $\leftarrow$  Items $\uparrow$ [k].X;
    if  $\neg$ fNatFunc.HasInDom(i) then exit;
    if Items $\uparrow$ [k].Y  $\neq$  fNatFunc.Value(i) then exit;
    end;
  WeakerThan  $\leftarrow$  true;
end;
end;
```


392. Let $f: \mathbf{N} \rightarrow \mathbf{N}$ and $g: \mathbf{N} \rightarrow \mathbf{N}$ be partial functions. We will say that f is a “multiple” of g if $\|g\| \leq \|f\|$ and for each $x \in \text{dom}(g)$ we have $x \in \text{dom}(f)$ and $g(x) \leq f(x)$.

There was some commented code for this function, which I removed.

```
function NatFunc.IsMultipleOf(const fNatFunc: NatFunc): boolean;
var k, l: integer;
begin IsMultipleOf  $\leftarrow$  false;
if fNatFunc.Count  $\leq$  Count then
  begin for k  $\leftarrow$  0 to fNatFunc.Count - 1 do
    if  $\neg$ HasInDom(fNatFunc.Items $\uparrow$ [k].X) then exit
    else if Value(fNatFunc.Items $\uparrow$ [k].X) < fNatFunc.Items $\uparrow$ [k].Y then exit;
  IsMultipleOf  $\leftarrow$  true;
end;
end;
```

393. Comparing partial functions. Let $f: \mathbf{N} \rightarrow \mathbf{N}$ and $g: \mathbf{N} \rightarrow \mathbf{N}$ be partial functions.

If $\|f\| \leq \|g\|$, for each $x \in \text{dom}(f)$ if $x \notin \text{dom}(g)$, then return 0. If $f(x) \neq g(x)$, then return 0. Otherwise return -1.

Else if $\|g\| \leq \|f\|$, for each $x \in \text{dom}(g)$ if $x \notin \text{dom}(f)$, then return 0. If $f(x) \neq g(x)$, then return 0. Otherwise return +1.

This is difficult for me to grasp. It does not seem to adequately satisfy $\text{compare}(f, g) = -\text{compare}(g, f)$, which is catastrophic. It is also unclear to me that this is transitive or reflexive. So it seems like it has no desirable properties.

I am confused why there is this function and also another similarly named function (§390).

The comment in Polish translates as, “Using *WeakerThan* you can shorten *CompareWith*!!!” At least, according to Google, that’s the translation.

{ Uzywajac *WeakerThan* mozna skrociac *CompareWith* !!! }

```
function NatFunc.CompareWith(const fNatFunc: NatFunc): integer;
var i, k: integer;
begin CompareWith  $\leftarrow$  0;
if Count  $\leq$  fNatFunc.Count then
  begin for k  $\leftarrow$  0 to Count - 1 do
    begin i  $\leftarrow$  Items $\uparrow$ [k].X;
    if  $\neg$ fNatFunc.HasInDom(i) then exit;
    if Items $\uparrow$ [k].Y  $\neq$  fNatFunc.Value(i) then exit;
    end;
  CompareWith  $\leftarrow$  -1; exit;
end;
if fNatFunc.Count  $\leq$  Count then
  begin for k  $\leftarrow$  0 to fNatFunc.Count - 1 do
    begin i  $\leftarrow$  fNatFunc.Items $\uparrow$ [k].X;
    if  $\neg$ HasInDom(i) then exit;
    if fNatFunc.Items $\uparrow$ [k].Y  $\neq$  Value(i) then exit;
    end;
  CompareWith  $\leftarrow$  1; exit;
end;
end;
```

394. Let $f: \mathbf{N} \rightarrow \mathbf{N}$ and $g: \mathbf{N} \rightarrow \mathbf{N}$ be partial functions. Then we define $f + g: \mathbf{N} \rightarrow \mathbf{N}$ to be the partial function defined on $\text{dom}(f + g) = \text{dom}(f) \cup \text{dom}(g)$ such that for each $x \in \text{dom}(f \cap g)$ we have $(f + g)(x) = f(x) + g(x)$, and for each $x \in \text{dom}(f) \setminus \text{dom}(g)$ we have $(f + g)(x) = f(x)$, and for each $x \in \text{dom}(g) \setminus \text{dom}(f)$ we have $(f + g)(x) = g(x)$.

There is some subtlety in the implementation because we have to check for overflows, i.e., when

$$g(x) \geq \text{High}(\text{integer}) - f(x)$$

for each $x \in \text{dom}(f) \cap \text{dom}(g)$.

```
procedure NatFunc.Add(const aFunc: NatFunc);
  var k, l: integer;
  begin l  $\leftarrow$  0;
  for k  $\leftarrow$  0 to aFunc.Count - 1 do
    begin while (l < Count)  $\wedge$  (Items $\uparrow$ [l].X < aFunc.Items $\uparrow$ [k].X) do inc(l);
    if (l < Count)  $\wedge$  (Items $\uparrow$ [l].X = aFunc.Items $\uparrow$ [k].X) then
      begin if  $\langle$  Has overflow occurred in NatFunc.Add? 395  $\rangle$  then RunError(215);
      inc(Items $\uparrow$ [l].Y, aFunc.Items $\uparrow$ [k].Y);
      end
    else AtInsert(l, aFunc.Items $\uparrow$ [k]);
    end;
  end;
```

395. An overflow occurs if $f(x) + g(x)$ is greater than $\text{High}(\text{integer})$ (the maximum value for an integer).

\langle Has overflow occurred in *NatFunc.Add*? 395 $\rangle \equiv$
 $\text{Items}\uparrow[l].Y > (\text{High}(\text{integer}) - \text{aFunc.Items}\uparrow[k].Y)$

This code is used in section 394.

396. Sum values of partial function. For a partial function $f: \mathbf{N} \rightarrow \mathbf{N}$, we have

$$\text{CountAll}(f) = \sum_{n \in \text{dom}(f)} f(n).$$

\langle *NatFunc* implementation 380 $\rangle + \equiv$

```
function NatFunc.CountAll: integer;
  var k, l: integer;
  begin l  $\leftarrow$  0;
  for k  $\leftarrow$  0 to Count - 1 do inc(l, Items $\uparrow$ [k].Y);
  CountAll  $\leftarrow$  l;
  end;
```

Section 9.18. SEQUENCES OF NATURAL NUMBERS**397.**

⟨Public interface for `mobjects.pas` 184⟩ $\vdash \equiv$

```

NatSeq = object (NatFunc)
  constructor InitNatSeq(ALimit, ADelta : integer);
  procedure InsertElem(X : integer); virtual;
  function Value(fElem : integer): integer; virtual;
  function IndexOf(Y : integer): integer;
end ;

```

398. Constructor.

⟨NatSeq implementation 398⟩ \equiv

```

constructor NatSeq.InitNatSeq(ALimit, ADelta : integer);
begin inherited Init(ALimit, ADelta); nConsistent ← true;
end;

```

This code is used in section 183.

399. If we have a finite sequence (a_0, \dots, a_{n-1}) , then inserting an element x into it will yield the finite sequence (a_0, \dots, a_{n-1}, x) .

```

procedure NatSeq.InsertElem(X : integer);
var lPair: IntPair;
begin lPair.X ← Count; lPair.Y ← X; inherited Insert(lPair);
end;

```

400. The value for the k^{th} element in a sequence (a_0, \dots, a_{n-1}) is a_k when $0 \leq k < n$, and we take it to be 0 otherwise.

```

function NatSeq.Value(fElem : integer): integer;
begin
  if { (0 ≤ ind) and }
    (fElem < count) then Value ← Items↑[fElem].Y
  else Value ← 0;
end ;

```

401. The index for a_i in the sequence (a_0, \dots, a_{n-1}) is i when a_i is in the sequence. Otherwise, we return -1 .

```

function NatSeq.IndexOf(Y : integer): integer;
var lResult: integer;
begin for lResult ← Count - 1 downto 0 do
  if Items↑[lResult].Y = Y then
    begin IndexOf ← lResult; exit
  end;
IndexOf ← -1;
end;

```

Section 9.19. INTEGER SEQUENCES**402.**

(Public interface for `mobjects.pas` 184) $\vdash \equiv$
IntegerListPtr = \uparrow *IntegerList*;
IntegerList = **array** [0 .. *MaxIntegerListSize* - 1] **of** *integer*;
PIntSequence = \uparrow *IntSequence*;
IntSequencePtr = *PIntSequence*;
IntSequence = **object** (*MObject*)
 fList: *IntegerListPtr*;
 fCount: *integer*;
 fCapacity: *integer*;
 constructor *Init*(*aCapacity* : *integer*);
 constructor *CopySequence*(**const** *aSeq*: *IntSequence*);
 constructor *MoveSequence*(**var** *aSeq* : *IntSequence*);
 destructor *Done*; *virtual*;
 procedure *IntListError*(*Code*, *Info* : *integer*); *virtual*;
 procedure *SetCapacity*(*aCapacity* : *integer*); *virtual*;
 procedure *Clear*; *virtual*;
 function *Insert*(*aInt* : *integer*): *integer*; *virtual*;
 procedure *AddSequence*(**const** *aSeq*: *IntSequence*); *virtual*;
 function *IndexOf*(*aInt* : *integer*): *integer*; *virtual*;
 procedure *AtDelete*(*aIndex* : *integer*); *virtual*;
 function *Value*(*aIndex* : *integer*): *integer*; *virtual*;
 procedure *AtInsert*(*aIndex*, *aInt* : *integer*); *virtual*;
 procedure *AtPut*(*aIndex*, *aInt* : *integer*); *virtual*;
end ;

403. We will need to quicksort lists of integers. This will mutate the *aList* argument, making it sorted. See also §257 and §334.

This procedure does not appear to be used anywhere in Mizar.

(*IntSequence* implementation 403) \equiv
 { *integer* Sequences & Sets }
procedure *IntQuickSort*(*aList* : *IntegerListPtr*; *L*, *R* : *integer*);
 var *I*, *J*, *P*, *lTemp*: *integer*;
 begin repeat *I* \leftarrow *L*; *J* \leftarrow *R*; *P* \leftarrow *aList* \uparrow [(*L* + *R*) shr 1];
 repeat while *CompareInt*(*aList* \uparrow [*I*], *P*) < 0 **do** *inc*(*I*);
 while *CompareInt*(*aList* \uparrow [*J*], *P*) > 0 **do** *Dec*(*J*);
 if *I* \leq *J* **then**
 begin *lTemp* \leftarrow *aList* \uparrow [*I*]; *aList* \uparrow [*I*] \leftarrow *aList* \uparrow [*J*]; *aList* \uparrow [*J*] \leftarrow *lTemp*; *inc*(*I*); *Dec*(*J*);
 end;
 until *I* > *J*;
 if *L* < *J* **then** *IntQuickSort*(*aList*, *L*, *J*);
 L \leftarrow *I*;
 until *I* \geq *R*;
 end;

This code is used in section 183.

404. Constructor. We can create an empty sequence of integers, with a given capacity.

```
constructor IntSequence.Init(aCapacity : integer);
  begin inherited Init; fList  $\leftarrow$  nil; fCount  $\leftarrow$  0; fCapacity  $\leftarrow$  0; SetCapacity(aCapacity);
end;
```

405. Copy constructor. We can copy an existing sequence.

```
constructor IntSequence.CopySequence(const aSeq : IntSequence);
  begin Init(aSeq.fCapacity); AddSequence(aSeq);
end;
```

406. Move constructor. We can create a new array in heap, and move all the elements from a given sequence over, then free up the given sequence.

```
constructor IntSequence.MoveSequence(var aSeq : IntSequence);
  begin inherited Init; fCount  $\leftarrow$  aSeq.fCount; fCapacity  $\leftarrow$  aSeq.fCapacity; fList  $\leftarrow$  aSeq.fList;
  aSeq.fCount  $\leftarrow$  0; aSeq.fCapacity  $\leftarrow$  0; aSeq.fList  $\leftarrow$  nil;
end;
```

407. Destructor.

```
destructor IntSequence.Done;
  begin inherited Done; fCount  $\leftarrow$  0; SetCapacity(0);
end;
```

408. Appending an element. Given a finite sequence of integers (a_0, \dots, a_{n-1}) , we can append a value x to produce the finite sequence (a_0, \dots, a_{n-1}, x) . This will mutate the caller.

```
function IntSequence.Insert(aInt : integer): integer;
  begin if fCount = fCapacity then SetCapacity(fCapacity + GrowLimit(fCapacity));
  fList $\uparrow$ [fCount]  $\leftarrow$  aInt; Insert  $\leftarrow$  fCount; inc(fCount);
end;
```

409. Appending a sequence. This takes a finite sequence (a_0, \dots, a_{n-1}) and another finite sequence (b_0, \dots, b_{m-1}) , then forms a new finite sequence $(a_0, \dots, a_{n-1}, b_0, \dots, b_{m-1})$. It mutates the caller.

```
procedure IntSequence.AddSequence(const aSeq : IntSequence);
  var I, r : integer;
  begin for I  $\leftarrow$  0 to aSeq.fCount - 1 do r  $\leftarrow$  Insert(aSeq.fList $\uparrow$ [I]);
end;
```

410. Clearing a sequence.

```
procedure IntSequence.Clear;
  begin if fCount  $\neq$  0 then
    begin fCount  $\leftarrow$  0; SetCapacity(0);
    end;
end;
```

411. Delete entry in sequence. Removing the i^{th} entry in the sequence $(a_0, \dots, a_{i-1}, a_i, a_{i+1}, \dots, a_{n-1})$ yields the finite sequence $(a_0, \dots, a_{i-1}, a_{i+1}, \dots, a_{n-1})$. If $i < 0$ or $n - 1 < i$, then we raise an error.

```
procedure IntSequence.AtDelete(aIndex : integer);
  begin if (aIndex < 0)  $\vee$  (aIndex  $\geq$  fCount) then IntListError(coIndexError, aIndex);
  Dec(fCount);
  if aIndex < fCount then Move(fList $\uparrow$ [aIndex + 1], fList $\uparrow$ [aIndex], (fCount - aIndex) * SizeOf(integer));
end;
```

412. We report errors using this helper function.

```
procedure IntSequence.IntListError(Code, Info : integer);
  begin RunError(212 - Code);  {! poprawic bledy }
  end;
```

413. Let (a_0, \dots, a_{n-1}) be a finite sequence. The value at index i is a_i when $0 \leq i \leq n-1$, otherwise it raises an error.

```
function IntSequence.Value(aIndex : integer): integer;
  begin if (aIndex < 0)  $\vee$  (aIndex  $\geq$  fCount) then IntListError(coIndexError, aIndex);
    Value  $\leftarrow$  fList $\uparrow$ [aIndex];
  end;
```

414. For a finite sequence (a_0, \dots, a_{n-1}) and a value x , if there is some entry $a_i = x$ with $a_j \neq x$ for $j < i$, then return i . Otherwise return -1 .

```
function IntSequence.IndexOf(aInt : integer): integer;
  var lResult: integer;
  begin for lResult  $\leftarrow$  fCount - 1 downto 0 do
    if fList $\uparrow$ [lResult] = aInt then
      begin IndexOf  $\leftarrow$  lResult; exit
      end;
  IndexOf  $\leftarrow$  -1;
end;
```

415. Given a finite sequence (a_0, \dots, a_{n-1}) , an index i , and a value x :

- (1) If $i < 0$ or i is too big, raise an error.
- (2) If the logical size of the sequence equals its capacity, then grow the underlying array.
- (3) If i is less than the logical size $i < n-1$, then shift all the entries to the right by 1 so we have $(a_0, \dots, a_{i-1}, 0, a_i, \dots, a_{n-1})$
- (4) Set the i^{th} entry to x , so we end up with the caller becoming $(a_0, \dots, a_{i-1}, x, a_i, \dots, a_{n-1})$.

```
procedure IntSequence.AtInsert(aIndex, aInt : integer);
  begin if (aIndex < 0)  $\vee$  (aIndex > fCount) then IntListError(coIndexError, aIndex);
  if fCount = fCapacity then SetCapacity(fCapacity + GrowLimit(fCapacity));
  if aIndex < fCount then Move(fList $\uparrow$ [aIndex], fList $\uparrow$ [aIndex + 1], (fCount - aIndex) * SizeOf(integer));
  fList $\uparrow$ [aIndex]  $\leftarrow$  aInt; inc(fCount);
  end;
```

416. Update entry of sequence. For a sequence (a_0, \dots, a_{n-1}) , an index i , and a new value x , if $0 \leq i \leq n-1$ then we set $a_i \leftarrow x$. Otherwise we have the index be out of bounds ($0 < i$ or $n-1 < i$), and we should raise an error.

```
procedure IntSequence.AtPut(aIndex, aInt : integer);
  begin if (aIndex < 0)  $\vee$  (aIndex  $\geq$  fCount) then IntListError(coIndexError, aIndex);
  fList $\uparrow$ [aIndex]  $\leftarrow$  aInt;
  end;
```

417. Grow the underlying array. When we want to increase (or decrease) the capacity of the underlying array, we invoke this function. It will copy over the relevant contents.

```

procedure IntSequence.SetCapacity(aCapacity : integer);
  var lList: IntegerListPtr;
  begin if aCapacity < fCount then aCapacity  $\leftarrow$  fCount;
  if aCapacity > MaxListSize then aCapacity  $\leftarrow$  MaxListSize;
  if aCapacity  $\neq$  fCapacity then
    begin if aCapacity = 0 then lList  $\leftarrow$  nil
    else begin GetMem(lList, aCapacity * SizeOf(integer));
      if (fCount  $\neq$  0)  $\wedge$  (fList  $\neq$  nil) then Move(fList $\uparrow$ , lList $\uparrow$ , fCount * SizeOf(integer));
      end;
    if fCapacity  $\neq$  0 then FreeMem(fList, fCapacity * SizeOf(integer));
    fList  $\leftarrow$  lList; fCapacity  $\leftarrow$  aCapacity;
    end;
  end;

```

Section 9.20. INTEGER SETS

418.

⟨Public interface for `mobjects.pas` 184⟩ +≡

```

PIntSet = ↑IntSet;
IntSetPtr = pIntSet;
IntSet = object (IntSequence)
  function Insert(aInt : integer): integer; virtual;
  function DeleteInt(aInt : integer): integer; virtual;
  function Find(aInt : integer; var aIndex : integer): boolean; virtual;
  function IndexOf(aInt : integer): integer; virtual;
  procedure AtInsert(aIndex, aInt : integer): virtual;
  function IsInSet(aInt : integer): boolean; virtual;
  function IsEqualTo(const aSet: IntSet): boolean; virtual;
  function IsSubsetOf(const aSet: IntSet): boolean; virtual;
  function IsSupersetOf(var aSet : IntSet): boolean; virtual;
  function Misses(var aSet : IntSet): boolean; virtual;
end ;

```

419. When inserting an element x into a set A , we check if $x \in A$ is already a member. If so, then we're done.

Otherwise, we ensure the capacity of the set can handle adding another element. Then we shift all elements greater than x over to the right by 1. We finally insert x into the underlying array.

⟨*IntSet* Implementation 419⟩ ≡

```

function IntSet.Insert(aInt : integer): integer;
  var lIndex: integer;
  begin if Find(aInt, lIndex) then { already contains the element? }
    begin Insert ← lIndex; exit end;
  if fCount = fCapacity then SetCapacity(fCapacity + GrowLimit(fCapacity));
  if lIndex < fCount then Move(fList↑[lIndex], fList↑[lIndex + 1], (fCount - lIndex) * SizeOf(integer));
  fList↑[lIndex] ← aInt; inc(fCount); Insert ← lIndex;
  end;

```

This code is used in section 183.

420. Removing an element from a set. This will return the former index of the element in the underlying array.

```

function IntSet.DeleteInt(aInt : integer): integer;
  var lIndex: integer;
  begin DeleteInt ← -1;
  if Find(aInt, lIndex) then
    begin DeleteInt ← lIndex; AtDelete(lIndex) end
  end;

```


421. We can use bisection search to find an element $aInt$ in the underlying array. It will mutate $aIndex$ to be where the entry should be, and return *true* if the element is a member of the set (and *false* otherwise).

```
function IntSet.Find(aInt : integer; var aIndex : integer): boolean;
  var L, H, I, C: integer;
  begin Find  $\leftarrow$  False; L  $\leftarrow$  0; H  $\leftarrow$  fCount - 1;
  while L  $\leq$  H do
    begin I  $\leftarrow$  (L + H) shr 1; C  $\leftarrow$  CompareInt(fList $\uparrow$ [I], aInt);
    if C < 0 then L  $\leftarrow$  I + 1
    else begin H  $\leftarrow$  I - 1;
      if C = 0 then
        begin Find  $\leftarrow$  True; L  $\leftarrow$  I; end;
      end;
    end;
  aIndex  $\leftarrow$  L;
end;
```

422. We can find the index of an element (if it is present) by using bisection search.

```
function IntSet.IndexOf(aInt : integer): integer;
  var lResult: integer;
  begin if  $\neg$ Find(aInt, lResult) then lResult  $\leftarrow$  -1;
  IndexOf  $\leftarrow$  lResult;
end;
```

423. The *AtInsert* method is “grandfathered in”, but not supported, so we raise an error if anyone tries using it.

```
procedure IntSet.AtInsert(aIndex, aInt : integer);
  begin IntListError(coSortedListError, 0);
end;
```

424. We can test if an integer is an element of the set, again just piggy-backing off bisection search.

```
function IntSet.IsInSet(aInt : integer): boolean;
  var I: integer;
  begin IsInSet  $\leftarrow$  Find(aInt, I);
end;
```

425. Testing if two finite sets A and B of integers are equal requires $|A| = |B|$ and for each $x \in A$ we have $x \in B$. If these conditions are not both met, then $A \neq B$.

```
function IntSet.IsEqualTo(const aSet: IntSet): boolean;
  var I: integer;
  begin IsEqualTo  $\leftarrow$  false;
  if fCount  $\neq$  aSet.fCount then exit;
  for I  $\leftarrow$  0 to fCount - 1 do
    if fList $\uparrow$ [I]  $\neq$  aSet.fList $\uparrow$ [I] then exit;
  IsEqualTo  $\leftarrow$  true;
end;
```

426. Subset predicate. We can test $A \subseteq B$ by $|A| \leq |B|$ and for each $a \in A$ we have $a \in B$.

```

function IntSet.IsSubsetOf(const aSet: IntSet): boolean;
  var i, j, lnt: integer;
  begin IsSubsetOf  $\leftarrow$  false;
  if aSet.fCount < fCount then exit;
  j  $\leftarrow$  0; { index of B }
  for i  $\leftarrow$  0 to fCount - 1 do { loop over  $a \in A$  }
    begin lnt  $\leftarrow$  fList $\uparrow$ [i];
    while (j < aSet.fCount)  $\wedge$  (aSet.fList $\uparrow$ [j] < lnt) do inc(j);
    if (j = aSet.fCount)  $\vee$  (aSet.fList $\uparrow$ [j]  $\neq$  fList $\uparrow$ [i]) then exit;
    end;
  IsSubsetOf  $\leftarrow$  true;
end;

```

427. Superset predicate. We have $A \supset B$ if $B \subseteq A$.

```

function IntSet.IsSupersetOf(var aSet : IntSet): boolean;
  begin IsSupersetOf  $\leftarrow$  aSet.IsSubsetOf(Self);
end;

```

428. Test for disjointness. We have $A \cap B = \emptyset$ if every $a \in A$ is such that $a \notin B$.

```

function IntSet.Misses(var aSet : IntSet): boolean;
  var k: integer;
  begin if fCount > aSet.fCount then
    begin for k  $\leftarrow$  0 to aSet.fCount - 1 do
      if IsInSet(aSet.fList $\uparrow$ [k]) then
        begin Misses  $\leftarrow$  false; exit end
      end
    else begin for k  $\leftarrow$  0 to fCount - 1 do
      if aSet.IsInSet(fList $\uparrow$ [k]) then
        begin Misses  $\leftarrow$  false; exit end;
      end;
    Misses  $\leftarrow$  true;
  end;

```

Section 9.21. PARTIAL BINARY INTEGER FUNCTIONS

429. We want to describe partial functions like $f: \mathbf{Z} \times \mathbf{Z} \rightarrow \mathbf{Z}$. These are encoded as finite sets of triples $\{(x, y, f(x, y)) \in \mathbf{Z} \times \mathbf{Z} \times \mathbf{Z}\}$. So we need to introduce triples of integers.

```

⟨Public interface for mobjects.pas 184⟩ +≡
  IntTripletListPtr = ↑IntTripletList;
  IntTripletList = array [0 .. MaxIntTripletSize - 1] of IntTriplet;
  BinIntFuncPtr = ↑BinIntFunc;
  BinIntFunc = object (MObject)
    fList: IntTripletListPtr;
    fCount: integer;
    fCapacity: integer;
    constructor Init(aLimit : integer);
    procedure BinIntFuncError(aCode, aInfo : integer); virtual;
    destructor Done; virtual;

    procedure Insert(const aItem: IntTriplet); virtual;
    procedure AtDelete(aIndex : integer);
    procedure SetCapacity(aLimit : integer); virtual;
    procedure DeleteAll;
    function Search(X1, X2 : integer; var aIndex : integer): boolean; virtual;
    function IndexOf(X1, X2 : integer): integer;
    constructor CopyBinIntFunc(var aFunc : BinIntFunc);
    function HasInDom(X1, X2 : integer): boolean; virtual;
    procedure Assign(X1, X2, Y : integer); virtual;
    procedure Up(X1, X2 : integer); virtual;
    procedure Down(X1, X2 : integer); virtual;
    function Value(X1, X2 : integer): integer; virtual;
    procedure Add(const aFunc: BinIntFunc); virtual;
    function CountAll: integer; virtual;
  end ;

```

430. We have a convenience function for reporting errors.

```

⟨Partial Binary integer Functions 430⟩ ≡
procedure BinIntFunc.BinIntFuncError(aCode, aInfo : integer);
  begin RunError(212 - aCode); end;

```

This code is used in section 183.

431. Constructor. We initialize the empty partial function.

```

constructor BinIntFunc.Init(aLimit : integer);
  begin MObject.Init; fList ← nil; fCount ← 0; fCapacity ← 0; SetCapacity(aLimit);
  end;

```

432. Destructor.

```

destructor BinIntFunc.Done;
  begin fCount ← 0; SetCapacity(0);
  end;

```

433. If we have a partial function $f: \mathbf{Z} \times \mathbf{Z} \rightarrow \mathbf{Z}$ and a triple (x, y, z) , then check if $(x, y) \in \text{dom}(f)$. If so, we're done.

Otherwise we add $f(x, y) = z$ to the partial function.

```

procedure BinIntFunc.Insert(const aItem: IntTriplet);
  var I: integer;
  begin if  $\neg \text{Search}(aItem.X1, aItem.X2, I)$  then
    begin if  $(I < 0) \vee (I > fCount)$  then
      begin BinIntFuncError(coIndexError, 0); exit; end;
    if  $fCapacity = fCount$  then SetCapacity( $fCapacity + \text{GrowLimit}(fCapacity)$ );
    if  $I \neq fCount$  then Move( $fList \uparrow [I]$ ,  $fList \uparrow [I + 1]$ ,  $(fCount - I) * \text{SizeOf}(\text{IntTriplet})$ );
     $fList \uparrow [I] \leftarrow aItem$ ; inc( $fCount$ );
    end;
  end;

```

434. Given $f: \mathbf{Z} \times \mathbf{Z} \rightarrow \mathbf{Z}$, we represent it as an array of $\mathbf{Z} \times \mathbf{Z} \times \mathbf{Z}$. So we can remove the entry at index i when $0 \leq i < \|f\|$. Otherwise when $i < 0$ or $\|f\| \leq i$, raise an error.

```

procedure BinIntFunc.AtDelete(aIndex : integer);
  var i: integer;
  begin if  $(aIndex < 0) \vee (aIndex \geq fCount)$  then
    begin BinIntFuncError(coIndexError, 0); exit; end;
  if  $aIndex < fCount - 1$  then
    for  $i \leftarrow aIndex$  to  $fCount - 2$  do  $fList \uparrow [i] \leftarrow fList \uparrow [i + 1]$ ;
  Dec( $fCount$ );
  end;

```

435. Ensure capacity.

```

procedure BinIntFunc.SetCapacity(aLimit : integer);
  var aItems: IntTripletListPtr;
  begin if  $aLimit < fCount$  then  $aLimit \leftarrow fCount$ ;
  if  $aLimit > \text{MaxIntTripletSize}$  then  $ALimit \leftarrow \text{MaxIntTripletSize}$ ;
  if  $aLimit \neq fCapacity$  then
    begin if  $ALimit = 0$  then  $AItems \leftarrow \text{nil}$ 
    else begin GetMem( $AItems$ ,  $ALimit * \text{SizeOf}(\text{IntTriplet})$ );
      if  $(fCount \neq 0) \wedge (fList \neq \text{nil})$  then Move( $fList \uparrow$ ,  $aItems \uparrow$ ,  $fCount * \text{SizeOf}(\text{IntTriplet})$ );
    end;
    if  $fCapacity \neq 0$  then FreeMem( $fList$ ,  $fCapacity * \text{SizeOf}(\text{IntTriplet})$ );
     $fList \leftarrow aItems$ ;  $fCapacity \leftarrow aLimit$ ;
  end;
end;

```

436. Deleting all entries in a partial function $\mathbf{Z} \times \mathbf{Z} \rightarrow \mathbf{Z}$ amounts to setting the logical size of the underlying dynamic array to zero.

```

procedure BinIntFunc.DeleteAll;
  begin  $fCount \leftarrow 0$ ; end;

```

437. We can use bisection search to find an entry (x_1, x_2) such that $(x_1, x_2) \in \text{dom}(f)$.

```
function BinIntFunc.Search(X1, X2 : integer; var aIndex : integer): boolean;
  var L, H, I, C: integer;
  begin Search  $\leftarrow$  False; L  $\leftarrow$  0; H  $\leftarrow$  fCount - 1;
  while L  $\leq$  H do
    begin I  $\leftarrow$  (L + H) shr 1; C  $\leftarrow$  CompareIntPairs(fList↑[I].X1, fList↑[I].X2, X1, X2);
    if C < 0 then L  $\leftarrow$  I + 1
    else begin H  $\leftarrow$  I - 1;
      if C = 0 then
        begin Search  $\leftarrow$  True; L  $\leftarrow$  I; end;
      end;
    end;
  aIndex  $\leftarrow$  L;
end;
```

438. Copy constructor. This leaves *aFunc* unchanged, and clones *aFunc*.

```
constructor BinIntFunc.CopyBinIntFunc(var aFunc : BinIntFunc);
  begin Init(aFunc.fCapacity); Move(aFunc.fList↑, fList↑, aFunc.fCapacity * SizeOf(IntTriplet));
  fCount  $\leftarrow$  aFunc.fCount;
end;
```

439. Given $f: \mathbf{Z} \times \mathbf{Z} \rightarrow \mathbf{Z}$ and (x_1, x_2) , find the index for the underlying dynamic array i such that it contains $(x_1, x_2, f(x_1, x_2))$. If there is no such entry, $i = -1$ is returned.

```
function BinIntFunc.IndexOf(X1, X2 : integer): integer;
  var I: integer;
  begin IndexOf  $\leftarrow$  -1;
  if Search(X1, X2, I) then IndexOf  $\leftarrow$  I;
end;
```

440. Test if $(x_1, x_2) \in \text{dom}(f)$.

```
function BinIntFunc.HasInDom(X1, X2 : integer): boolean;
  var I: integer;
  begin HasInDom  $\leftarrow$  Search(X1, X2, I);
end;
```

441. Given $f: \mathbf{Z} \times \mathbf{Z} \rightarrow \mathbf{Z}$, and $(x_1, x_2) \in \mathbf{Z} \times \mathbf{Z}$ and $y \in \mathbf{Z}$, try setting $f(x_1, x_2) = y$ provided $(x_1, x_2) \notin \text{dom}(f)$ or if $(x_1, x_2, y) \in f$ already. If $f(x_1, x_2) \neq y$ already exists, then raise an error.

```
procedure BinIntFunc.Assign(X1, X2, Y : integer);
  var lntTriplet: IntTriplet;
  begin if HasInDom(X1, X2)  $\wedge$  (Value(X1, X2)  $\neq$  Y) then
    begin BinIntFuncError(coDuplicate, 0); exit
    end;
  lntTriplet.X1  $\leftarrow$  X1; lntTriplet.X2  $\leftarrow$  X2; lntTriplet.Y  $\leftarrow$  Y; Insert(lntTriplet);
end;
```

442. Given $f: \mathbf{Z} \times \mathbf{Z} \rightarrow \mathbf{Z}$ and $(x_1, x_2) \in \mathbf{Z} \times \mathbf{Z}$. If $(x_1, x_2) \in \text{dom}(f)$, then set $f(x_1, x_2) \leftarrow f(x_1, x_2) + 1$. Otherwise set $f(x_1, x_2) \leftarrow 1$.

```
procedure BinIntFunc.Up( $X1, X2 : \text{integer}$ );
  var  $I : \text{integer}$ ;  $\text{IntTriplet} : \text{IntTriplet}$ ;
  begin if Search( $X1, X2, I$ ) then inc( $fList \uparrow [I].Y$ )
  else begin  $\text{IntTriplet}.X1 \leftarrow X1$ ;  $\text{IntTriplet}.X2 \leftarrow X2$ ;  $\text{IntTriplet}.Y \leftarrow 1$ ; Insert( $\text{IntTriplet}$ );
    end;
  end;
```

443. Given $f: \mathbf{Z} \times \mathbf{Z} \rightarrow \mathbf{Z}$ and $(x_1, x_2) \in \mathbf{Z} \times \mathbf{Z}$. If $(x_1, x_2) \in \text{dom}(f)$, then set $f(x_1, x_2) \leftarrow f(x_1, x_2) - 1$. Further, if $f(x_1, x_2) = 0$, then remove it from the underlying dynamic array.

Otherwise for $(x_1, x_2) \notin \text{dom}(f)$, raise an error.

```
procedure BinIntFunc.Down( $X1, X2 : \text{integer}$ );
  var  $I : \text{integer}$ ;
  begin if Search( $X1, X2, I$ ) then
    begin dec( $fList \uparrow [I].Y$ );
    if  $fList \uparrow [I].Y = 0$  then AtDelete( $I$ );
    end
  else BinIntFuncError(coConsistentError, 0);
  end;
```

444. Given $f: \mathbf{Z} \times \mathbf{Z} \rightarrow \mathbf{Z}$, and $(x_1, x_2) \in \mathbf{Z} \times \mathbf{Z}$, if $(x_1, x_2) \notin \text{dom}(f)$ then raise an error. Otherwise when $(x_1, x_2) \in \text{dom}(f)$, return $f(x_1, x_2)$.

```
function BinIntFunc.Value( $X1, X2 : \text{integer}$ ): integer;
  var  $I : \text{integer}$ ;
  begin if Search( $X1, X2, I$ ) then  $\text{Value} \leftarrow fList \uparrow [I].Y$ 
  else BinIntFuncError(coDuplicate, 0);
  end;
```

445. Given two partial functions $f, g: \mathbf{Z} \times \mathbf{Z} \rightarrow \mathbf{Z}$, compute $f + g: \mathbf{Z} \times \mathbf{Z} \rightarrow \mathbf{Z}$. This is defines by:

- (1) For $(x_1, x_2) \in \text{dom}(f) \cap \text{dom}(g)$, set $(f + g)(x_1, x_2) = f(x_1, x_2) + g(x_1, x_2)$
- (2) For $(x_1, x_2) \in \text{dom}(f) \setminus \text{dom}(g)$, set $(f + g)(x_1, x_2) = f(x_1, x_2)$
- (3) For $(x_1, x_2) \in \text{dom}(g) \setminus \text{dom}(f)$, set $(f + g)(x_1, x_2) = g(x_1, x_2)$.

{ **TODO:** this is inefficient, since the search is repeated in the *Assign* method; fix this both here and in other similar methods }

```
procedure BinIntFunc.Add(const  $aFunc : \text{BinIntFunc}$ );
  var  $k, l : \text{integer}$ ;
  begin for  $k \leftarrow 0$  to  $aFunc.fCount - 1$  do
    if Search( $aFunc.fList \uparrow [k].X1, aFunc.fList \uparrow [k].X2, l$ ) then inc( $fList \uparrow [l].Y, aFunc.fList \uparrow [k].Y$ )
    else Assign( $aFunc.fList \uparrow [k].X1, aFunc.fList \uparrow [k].X2, aFunc.fList \uparrow [k].Y$ );
  end;
```

446. Sum. For $f: \mathbf{Z} \times \mathbf{Z} \rightarrow \mathbf{Z}$, we compute

$$\text{CountAll}(f) = \sum_{(m,n) \in \text{dom}(f)} f(m, n).$$

```
function BinIntFunc.CountAll: integer;
  var  $k, l : \text{integer}$ ;
  begin  $l \leftarrow 0$ ;
  for  $k \leftarrow 0$  to  $fCount - 1$  do inc( $l, fList \uparrow [k].Y$ );
   $\text{CountAll} \leftarrow l$ ;
  end;
```

Section 9.22. PARTIAL INTEGERS TO PAIR OF INTEGERS FUNCTIONS

447.

```

⟨Public interface for mobjects.pas 184⟩ +≡
  Int2PairOfInt = record X, Y1, Y2: integer;
    end;
  Int2PairOfIntFuncPtr = ↑Int2PairOfIntFunc;
  Int2PairOfIntFunc = object (MObject)
    fList: array of Int2PairOfInt;
    fCount: integer;
    fCapacity: integer;
    constructor Init(aLimit : integer);
    procedure Int2PairOfIntFuncError(aCode, aInfo : integer); virtual;
    destructor Done; virtual;
    procedure Insert(const aItem: Int2PairOfInt); virtual;
    procedure AtDelete(aIndex : integer);
    procedure SetCapacity(aLimit : integer); virtual;
    procedure DeleteAll;
    function Search(X : integer; var aIndex : integer): boolean; virtual;
    function IndexOf(X : integer): integer;
    constructor CopyInt2PairOfIntFunc(var aFunc : Int2PairOfIntFunc);
    function HasInDom(X : integer): boolean; virtual;
    procedure Assign(X, Y1, Y2 : integer); virtual;
    function Value(X : integer): IntPair; virtual;
  end ;

```

448. We have a helper function for raising errors.

```

⟨Partial integers to Pair of integers Functions 448⟩ ≡
  { Partial integers to Pair of integers Functions }
  procedure Int2PairOfIntFunc.Int2PairOfIntFuncError(aCode, aInfo : integer);
  begin RunError(212 - aCode);
  end;

```

This code is used in section 183.

449. Constructor. Creates an empty $f: \mathbf{Z} \rightarrow \mathbf{Z} \times \mathbf{Z}$ with an underlying dynamic array whose capacity is given as the argument $aLimit$.

```

  constructor Int2PairOfIntFunc.Init(aLimit : integer);
  begin MObject.Init; fList ← nil; fCount ← 0; fCapacity ← 0; SetCapacity(aLimit);
  end;

```

450. Destructor.

```

  destructor Int2PairOfIntFunc.Done;
  begin fCount ← 0; SetCapacity(0);
  end;

```

451. Inserting (x, y_1, y_2) into $f: \mathbf{Z} \rightarrow \mathbf{Z} \times \mathbf{Z}$ amounts to checking if $(x, y_1, y_2) \in f$. If not, then insert the entry.

Otherwise, if $(x, y_1, y_2) \notin f$ but $x \in \text{dom}(f)$, then raise an error.

Otherwise do nothing.

```

procedure Int2PairOfIntFunc.Insert(const aItem: Int2PairOfInt);
  var I: integer;
  begin if  $\neg \text{Search}(aItem.X, I)$  then
    begin if  $(I < 0) \vee (I > fCount)$  then
      begin Int2PairOfIntFuncError(coIndexError, 0); exit; end;
    if  $fCapacity = fCount$  then SetCapacity( $fCapacity + \text{GrowLimit}(fCapacity)$ );
    if  $I \neq fCount$  then Move( $fList[I], fList[I + 1], (fCount - I) * \text{SizeOf}(\text{Int2PairOfInt})$ );
     $fList[I] \leftarrow aItem$ ; inc( $fCount$ );
    end
  else if  $(fList[I].Y1 \neq aItem.Y1) \vee (fList[I].Y2 \neq aItem.Y2)$  then
    begin Int2PairOfIntFuncError(coDuplicate, 0); exit; end;
  end;

```

452. Delete an entry from the underlying dynamic array. Raise an error if the index given is out of bounds.

```

procedure Int2PairOfIntFunc.AtDelete(aIndex : integer);
  var i: integer;
  begin if  $(aIndex < 0) \vee (aIndex \geq fCount)$  then
    begin Int2PairOfIntFuncError(coIndexError, 0); exit;
    end;
  if  $aIndex < fCount - 1$  then
    for  $i \leftarrow aIndex$  to  $fCount - 2$  do  $fList[i] \leftarrow fList[i + 1]$ ;
  dec( $fCount$ );
  end;

```

453.

```

procedure Int2PairOfIntFunc.SetCapacity(aLimit : integer);
  begin if  $aLimit < fCount$  then  $aLimit \leftarrow fCount$ ;
  setlength( $fList, aLimit$ );  $fCapacity \leftarrow aLimit$ ;
  end;

```

454. We can “soft delete” all entries in the partial function.

```

procedure Int2PairOfIntFunc.DeleteAll;
  begin  $fCount \leftarrow 0$ ;
  end;

```


455. We can bisection search on the domain.

```

function Int2PairOfIntFunc.Search(X : integer; var aIndex : integer): boolean;
  var L, H, I, C: integer;
  begin Search  $\leftarrow$  False; L  $\leftarrow$  0; H  $\leftarrow$  fCount - 1;
  while L  $\leq$  H do
    begin I  $\leftarrow$  (L + H) shr 1; C  $\leftarrow$  CompareInt(fList[I].X, X);
    if C < 0 then L  $\leftarrow$  I + 1
    else begin H  $\leftarrow$  I - 1;
      if C = 0 then
        begin Search  $\leftarrow$  True; L  $\leftarrow$  I;
        end;
      end;
    end;
  aIndex  $\leftarrow$  L;
end;

```

456. Copy constructor. This leaves the argument *aFunc* unchanged.

```

constructor Int2PairOfIntFunc.CopyInt2PairOfIntFunc(var aFunc : Int2PairOfIntFunc);
  begin Init(aFunc.fCapacity); Move(aFunc.fList[0], fList[0], aFunc.fCapacity * SizeOf(Int2PairOfInt));
  fCount  $\leftarrow$  aFunc.fCount;
end;

```

457. Find the index in the underlying dynamic array for $x \in \text{dom}(f)$. If $x \notin \text{dom}(f)$, then return -1 .

```

function Int2PairOfIntFunc.IndexOf(X : integer): integer;
  var I: integer;
  begin IndexOf  $\leftarrow$  -1;
  if Search(X, I) then IndexOf  $\leftarrow$  I;
end;

```

458. Test if $x \in \text{dom}(f)$.

```

function Int2PairOfIntFunc.HasInDom(X : integer): boolean;
  var I: integer;
  begin HasInDom  $\leftarrow$  Search(X, I);
end;

```

459. Attempt to insert (x, y_1, y_2) into $f: \mathbf{Z} \rightarrow \mathbf{Z} \times \mathbf{Z}$.

```

procedure Int2PairOfIntFunc.Assign(X, Y1, Y2 : integer);
  var lInt2PairOfInt: Int2PairOfInt;
  begin lInt2PairOfInt.X  $\leftarrow$  X; lInt2PairOfInt.Y1  $\leftarrow$  Y1; lInt2PairOfInt.Y2  $\leftarrow$  Y2;
  Insert(lInt2PairOfInt);
end;

```

460. Given $f: \mathbf{Z} \rightarrow \mathbf{Z} \times \mathbf{Z}$ and $x \in \mathbf{Z}$, if $x \in \text{dom}(f)$ return $f(x)$. Otherwise raise an error.

```

function Int2PairOfIntFunc.Value(X : integer): IntPair;
  var I: integer;
  begin if Search(X, I) then
    begin Result.X  $\leftarrow$  fList[I].Y1; Result.Y  $\leftarrow$  fList[I].Y2;
    end
  else Int2PairOfIntFuncError(coDuplicate, 0);
end;

```

461. We have a myriad of random declarations, so we just stick them all here.

```

⟨Public interface for mobjects.pas 184⟩ +≡
  { Comparing Strings wrt MStrObj }
function CompareStringPtr(aKey1, aKey2 : Pointer): integer;
    { Comparing Strings and integers }
function CompareStr(aStr1, aStr2 : String): integer;
function CompareIntPairs(X1, Y1, X2, Y2 : Longint): integer;
    { Dynamic String handling routines }
function NewStr(const S: String): PString;
procedure DisposeStr(P : PString);
function GrowLimit(aLimit : integer): integer;    { Abstract notification procedure }
function CompareNatFunc(aKey1, aKey2 : Pointer): integer;
procedure Abstract1;
var EmptyNatFunc: NatFunc;

```

File 10

XML Dictionary

462. We have several types declared in the `xml_dict.parse` file. These are enumerated types, and string constants for their names.

```

<xml_dict.pas 462> ≡
  <GNU License 4>
unit xml_dict;
interface
uses mobjects;

{ known (and only allowed) XML elements }
type XMLElemKind = (elUnknown, elAdjective, elAdjectiveCluster, elArticleID, elAncestors,
  elArguments, elBlock, elConditions, elCorrectnessConditions, elDefiniens, elDirective, elEnviron,
  elEquality, elFieldSegment, elFormat, elFormats, elIdent, elItem, elIterativeStep, elLabel, elLink,
  elLoci, elLociEquality, elLocus, elNegatedAdjective, elPartialDefiniens, elPriority, elProposition,
  elProvisionalFormulas, elRedefine, elRightCircumflexSymbol, elSchematicVariables, elScheme,
  elSelector, elSetMember, elSkippedProof, elSymbol, elSymbolCount, elSymbols, elSubstitution,
  elTypeSpecification, elTypeList, elVariable, elVariables, elVocabularies, elVocabulary);

{ known XML attributes }
  XMLAttrKind = (atUnknown, atAid, atArgNr, atArticleId, atArticleExt, atCol, atCondition,
  atConstrNr, atIdNr, atInfinitive, atKind, atLabelNr, atLeftArgNr, atLine, atMizfiles, atName,
  atNegated, atNr, atNumber, atOrigin, atPosLine, atPosCol, atPriority, atProperty,
  atRightSymbolNr, atSchNr, atSerialNr, atShape, atSpelling, atSymbolNr, atValue, atVarNr,
  atVarSort, atX, atX1, atX2, atY, atY1, atY2);
const XMLElemName: array [XMLElemKind] of string = ('Unknown', 'Adjective',
  'Adjective-Cluster', 'ArticleID', 'Ancestors', 'Arguments', 'Block', 'Conditions',
  'CorrectnessConditions', 'Definiens', 'Directive', 'Environ', 'Equality',
  'Field-Segment', 'Format', 'Formats', 'Ident', 'Item', 'Iterative-Step', 'Label', 'Link',
  'Loci', 'LociEquality', 'Locus', 'NegatedAdjective', 'Partial-Definiens', 'Priority',
  'Proposition', 'Provisional-Formulas', 'Redefine', 'Right-Circumflex-Symbol',
  'Schematic-Variables', 'Scheme', 'Selector', 'SetMember', 'elSkippedProof', 'Symbol',
  'SymbolCount', 'Symbols', 'Substitution', 'Type-Specification', 'Type-List',
  'Variable', 'Variables', 'Vocabularies', 'Vocabulary');
XMLAttrName: array [XMLAttrKind] of string = ('unknown', 'aid', 'argnr', 'articleid',
  'articleext', 'col', 'condition', 'constrnr', 'idnr', 'infinitive', 'kind', 'labelnr',
  'leftargnr', 'line', 'mizfiles', 'name', 'negated', 'nr', 'number', 'origin', 'posline',
  'poscol', 'priority', 'property', 'rightsymbolnr', 'schnr', 'serialnr', 'shape',
  'spelling', 'symbolnr', 'value', 'varnr', 'varsort', 'x', 'x1', 'x2', 'y', 'y1', 'y2');
implementation
end .

```

File 11

Environment library

463. We have a library to handle accessing the Mizar mathematical library files. This is used in `makeenv.dpr` and using local `prel/` directories.

This will execute *InitLibrEnv* (§482) and *CheckCompatibility* (§479).

```

<librenv.pas 463> ≡
  <GNU License 4>
unit librenv;
interface
uses mobjects;
  <Interface for MIZFILES library 464>
implementation
uses
  @{@&$IFDEF WIN32@}windows,
  @{@&$ENDIF@}mizenv, pcmizver, mconsole;
  <Implementation for librenv.pas 467>
  begin InitLibrEnv; CheckCompatibility;
end.

```

464. <Interface for MIZFILES library 464> ≡

```

const MML = 'mml'; EnvMizFiles = 'MIZFILES';
var MizPath, MizFiles: string;
function LibraryPath(fName, fExt: string): string;
procedure GetSortedNames(fParam: byte; var fList: MStringCollection);
procedure GetNames(fParam: byte; var fList: StringColl);
procedure ReadSortedNames(fName: string; var fList: MStringCollection);
procedure ReadNames(fName: string; var fList: StringColl);

```

See also section 465.

This code is used in section 463.

465. There are two public-facing classes.

```

<Interface for MIZFILES library 464> +≡
type <Declare FileDescr data type 466>
  <Declare FileDescrCollection data type 469>
var LocFilesCollection: FileDescrCollection;

```

466. File descriptors. We use file descriptors for things. These are just “a file name” and “a timestamp”.

```

⟨ Declare FileDescr data type 466 ⟩ ≡
  PFileDescr = ↑FileDescr;
  FileDescr = object (MObject)
    nName: PString;
    Time: LongInt;
    constructor Init(fIdent : string; fTime : LongInt);
    destructor Done; virtual;
  end ;

```

This code is used in section 465.

467. Constructor.

```

⟨ Implementation for librenv.pas 467 ⟩ ≡
constructor FileDescr.Init(fIdent : string; fTime : LongInt);
  begin nName ← NewStr(fIdent); Time ← fTime;
  end;

```

See also sections 470, 479, and 482.

This code is used in section 463.

468. Destructor.

```

destructor FileDescr.Done;
  begin DisposeStr(nName);
  end;

```

469. Collection of file descriptions.

```

⟨ Declare FileDescrCollection data type 469 ⟩ ≡
  PFileDescrCollection = ↑FileDescrCollection;
  FileDescrCollection = object (MSortedCollection)
    function Compare(Key1, Key2 : Pointer): integer; virtual;
    procedure StoreFIL(fName : string);
    constructor LoadFIL(fName : string);
    procedure InsertTimes;
  end ;

```

This code is used in section 465.

470. Comparing two entries in a file descriptor collection amounts to comparing the names for the file descriptors.

```

⟨ Implementation for librenv.pas 467 ⟩ +≡
function FileDescrCollection.Compare(Key1, Key2 : Pointer): integer;
  begin if PFileDescr(Key1)↑.nName↑ < PFileDescr(Key2)↑.nName↑ then Compare ← -1
  else if PFileDescr(Key1)↑.nName↑ = PFileDescr(Key2)↑.nName↑ then Compare ← 0
  else Compare ← 1;
  end;

```

471. Inserting file times into the file descriptors relies upon mizenv.pas’s *GetFileTime* (§37) function.

```

procedure FileDescrCollection.InsertTimes;
  var z: integer;
  begin for z ← 0 to Count - 1 do
    with PFileDescr(Items↑[z])↑ do Time ← GetFileTime(nName↑);
  end;

```

472. Constructor. This leverages a few primitive PASCAL functions: *assign(file, name)* assigns *name* to a file but does not open the file (it is still considered closed). Then *reset(file)* opens the file for reading.

Specifically, this will load a *.fil* file produced by Mizar. These contain $2N$ lines: a file path on line $2n-1$, then a timestamp on line $2n$ for $n = 1, \dots, N$. This appears to be used for local *prel/* files.

```
constructor FileDescrCollection.LoadFIL(fName : string);
  var FIL: text; lName: string; lTime: longint;
  begin Assign(FIL, fName); Reset(FIL); Init(0, 10);
  while  $\neg$ eof(FIL) do
    begin ReadLn(FIL, lName); ReadLn(FIL, lTime); Insert(new(PFileDescr, Init(lName, lTime)));
    end;
  close(FIL);
end;
```

473. Repopulate .fil file. This will erase the file named *fName*, then assign to *FIL* that file, and *rewrite(FIL)* will open it for writing.

This will loop through every item in the caller's underlying collection, writing the file names and times to the *.fil* file.

```
procedure FileDescrCollection.StoreFIL(fName : string);
  var FIL: text; i: integer;
  begin EraseFile(fName); Assign(FIL, fName); Rewrite(FIL); InsertTimes;
  for i  $\leftarrow$  0 to Count - 1 do
    with PFileDescr(Items $\uparrow$ [i]) $\uparrow$  do
      begin WriteLn(FIL, nName $\uparrow$ ); WriteLn(FIL, Time)
      end;
  Close(FIL);
end;
```

474. The library path tries to use the local version of a file, if it exists as tested with *MFileExists* (§35). Otherwise it looks at the Mizar MML version of a file, if it exists.

This returns the path to the file, as a string. If the file cannot be found either in the local *prel* directory or the MML *prel* directory, then it returns the empty string.

```
function LibraryPath(fName, fExt : string): string;
  begin LibraryPath  $\leftarrow$  '';
  if MFileExists('prel' + DirSeparator + fName + fExt) then
    begin LocFilesCollection.Insert(New(PFileDescr, Init('prel' + DirSeparator + fName + fExt, 0)));
    LibraryPath  $\leftarrow$  'prel' + DirSeparator + fName + fExt; exit
    end;
  if MFileExists(MizFiles + 'prel' + DirSeparator + fName[1] + DirSeparator + fName + fExt) then
    LibraryPath  $\leftarrow$  MizFiles + 'prel' + DirSeparator + fName[1] + DirSeparator + fName + fExt;
  end;
```

475. This function actually is not used anywhere, so I am not sure why we have it.

```
procedure ReadSortedNames(fName : string; var fList : MStringCollection);
  var NamesFile: text;
  begin if fName[1] = '@' then
    begin Delete(fName, 1, 1); FileExam(fName); Assign(NamesFile, fName); Reset(NamesFile);
    fList.Init(100, 100);
    while ¬seekEof(NamesFile) do
      begin ReadLn(NamesFile, fName); fList.Insert(NewStr(fName));
      end;
    exit;
  end;
  fList.Init(2, 10); fList.Insert(NewStr(fName));
end;
```

476. Again, this function is not used anywhere, so I am not sure why we have it.

```
procedure ReadNames(fName : string; var fList : StringColl);
  var NamesFile: text;
  begin if fName[1] = '@' then
    begin Delete(fName, 1, 1); FileExam(fName); Assign(NamesFile, fName); Reset(NamesFile);
    fList.Init(10, 10);
    while ¬seekEof(NamesFile) do
      begin ReadLn(NamesFile, fName); fList.Insert(NewStr(fName));
      end;
    exit;
  end;
  fList.Init(2, 10); fList.Insert(NewStr(fName));
end;
```

477. This function is used in `lisvoc.dpr`

```
procedure GetSortedNames(fParam : byte; var fList : MStringCollection);
  var FileName: string; NamesFile: text; i: integer;
  begin if ParamCount < fParam then
    begin fList.Init(0, 0); exit
    end;
  FileName ← ParamStr(fParam);
  if FileName[1] = '@' then
    begin Delete(FileName, 1, 1); FileExam(FileName); Assign(NamesFile, FileName);
    Reset(NamesFile); fList.Init(10, 10);
    while ¬seekEof(NamesFile) do
      begin ReadLn(NamesFile, FileName); fList.Insert(NewStr(TrimString(FileName)));
      end;
    exit;
  end;
  fList.Init(2, 8); fList.Insert(NewStr(FileName));
  for i ← fParam + 1 to ParamCount do
    begin FileName ← ParamStr(i); fList.Insert(NewStr(FileName));
    end;
end;
```

478. Continuing with the “this is not used anywhere” theme, this function is not used anywhere.

```

procedure GetNames(fParam : byte; var fList : StringColl);
  var FileName: string; NamesFile: text; i: integer;
  begin if ParamCount < fParam then
    begin fList.Init(0,0); exit
    end;
  FileName ← ParamStr(fParam);
  if FileName[1] = ‘@’ then
    begin Delete(FileName, 1, 1); FileExam(FileName); Assign(NamesFile, FileName);
    Reset(NamesFile); fList.Init(10, 10);
    while ¬seekEof(NamesFile) do
      begin ReadLn(NamesFile, FileName); fList.Insert(NewStr(TrimString(FileName)));
      end;
    exit;
    end;
  fList.Init(2, 8); fList.Insert(NewStr(FileName));
  for i ← fParam + 1 to ParamCount do
    begin FileName ← ParamStr(i); fList.Insert(NewStr(FileName));
    end;
  end;

```


479. Check compatibility of Mizar with MML. We will load the `mml.ini` file for the MML version number, and we check it against the Mizar version. If they are not compatible, print a message to the screen, and halt as an error has occurred.

The `mml.ini` file looks something like:

```
[Mizar verifier]
MizarReleaseNbr=8
MizarVersionNbr=1
MizarVariantNbr=15
[MML]
NumberOfArticles=1493
MMLVersion=5.94
```

We will read line-by-line the `mml.ini` file to initialize several variables. This motivates the *Try_read_ini_var* macro.

```
define init_val_and_end(#) ≡ val(lLine,#,lCode);
end
define Try_read_ini_var(#) ≡ lPos ← Pos(#,lLine);
if lPos > 0 then
  begin delete(lLine,1,lPos + 15); init_val_and_end
```

⟨Implementation for `librenv.pas` 467⟩ +≡

```
procedure CheckCompatibility;
var lFile: text; lLine,lVer1,lVer2,l: string; lPos,lCode: integer;
  lMizarReleaseNbr, lMizarVersionNbr, lMizarVariantNbr: integer;
begin ⟨Open mml.ini file 480⟩
  lMizarReleaseNbr ← -1; lMizarVersionNbr ← -1; lMizarVariantNbr ← -1;
  while ¬seekEof(lFile) do
    begin ReadLn(lFile,lLine); Try_read_ini_var('MizarReleaseNbr=')(lMizarReleaseNbr);
      Try_read_ini_var('MizarVersionNbr=')(lMizarVersionNbr);
      Try_read_ini_var('MizarVariantNbr=')(lMizarVariantNbr);
    end;
  close(lFile);
  ⟨Assert MML version is compatible with Mizar version 481⟩
end;
```

480. We open the `$MIZFILES/mml.ini` file for reading.

⟨Open `mml.ini` file 480⟩ ≡
FileExam(*MizFiles* + *MML* + ``.ini``); *Assign*(*lFile*, *MizFiles* + *MML* + ``.ini``); *Reset*(*lFile*);

This code is used in section 479.

481. We need to check the MML version is compatible with the Mizar version. If they are not compatible, raise an error, print a warning to the user, and halt here.

⟨Assert MML version is compatible with Mizar version 481⟩ ≡
 if ¬((*lMizarReleaseNbr* = *PCMizarReleaseNbr*) ∧ (*lMizarVersionNbr* = *PCMizarVersionNbr*)) then
 begin *Str*(*PCMizarReleaseNbr*,*l*); *lVer1* ← *l*; *Str*(*PCMizarVersionNbr*,*l*); *lVer1* ← *lVer1* + ``. `` + *l*;
Str(*PCMizarVariantNbr*,*l*); *lVer1* ← *lVer1* + ``. `` + *l*; *Str*(*lMizarReleaseNbr*,*l*); *lVer2* ← *l*;
Str(*lMizarVersionNbr*,*l*); *lVer2* ← *lVer2* + ``. `` + *l*;
Str(*lMizarVariantNbr*,*l*); *lVer2* ← *lVer2* + ``. `` + *l*; *DrawMessage*(`‘Mizar_System_ver. `` + *lVer1* +
 ``is incompatible with the MML version imported `` + *lVer2* + ``’`,
`‘Please check `` + *MizFiles* + `‘mml.ini`’`); *halt*(1);
 end;

This code is used in section 479.

482. Initialize library environment. This will try to initialize the *MizFiles* variable to be equal to the \$MIZFILES environment variable (if that environment variable exists) or the directory of the program being executed. This *MizFiles* will always end in a directory separator.

We also initialize *MizFileName*, *EnvFileName*, *ArticleName*, *ArticleExt* to be empty strings.

```
define append_dir_separator(#)  $\equiv$  if #[length(#)]  $\neq$  DirSeparator then #  $\leftarrow$  # + DirSeparator;
```

\langle Implementation for *librenv.pas* 467 $\rangle + \equiv$

```
procedure InitLibrEnv;
```

```
begin LocFilesCollection.Init(0,20); MizPath  $\leftarrow$  ExtractFileDir(ParamStr(0));  $\langle$  Initialize Mizfiles 483  $\rangle$   

MizFileName  $\leftarrow$  ``; EnvFileName  $\leftarrow$  ``; ArticleName  $\leftarrow$  ``; ArticleExt  $\leftarrow$  ``;  

end;
```

483. Initializing *Mizfiles* requires a bit of work. We first guess it based on environment variables. Then we need to ensure it is a directory path.

\langle Initialize *Mizfiles* 483 $\rangle \equiv$

\langle Guess *MizFiles* from environment variables or executable path 484 \rangle

```
if MizFiles  $\neq$  `` then append_dir_separator(MizFiles);
```

```
if MizFiles = `` then Mizfiles  $\leftarrow$  DirSeparator;
```

This code is used in section 482.

484. When the \$MIZFILES environment variable is set, we just use it. When it is empty or missing, then we guess the path of the executable invoked.

\langle Guess *MizFiles* from environment variables or executable path 484 $\rangle \equiv$

```
MizFiles  $\leftarrow$  GetEnvStr(EnvMizFiles);
```

```
if MizFiles = `` then MizFiles  $\leftarrow$  MizPath;
```

This code is used in section 483.

File 12

Info file handling

485. I don't think this is actually used anywhere, but I am including it for completeness.

```

< info.pas 485 > ≡
  < GNU License 4 >
unit info;
interface uses errhan;
var InfoFile: text;

procedure InfoChar(C : char);
procedure InfoInt(I : integer);
procedure InfoWord(C : char; I : integer);
procedure InfoNewLine;
procedure InfoString(S : string);
procedure InfoPos(Pos : Position);
procedure InfoCurPos;
procedure OpenInfoFile;
procedure CloseInfofile;

implementation
uses mizenv, mconsole;

procedure InfoChar(C : char);
  begin write(InfoFile, C)
  end;

procedure InfoInt(I : integer);
  begin write(InfoFile, I, '␣')
  end;

procedure InfoWord(C : char; I : integer);
  begin write(InfoFile, C, I, '␣')
  end;

procedure InfoNewLine;
  begin WriteLn(InfoFile)
  end;

procedure InfoString(S : string);
  begin write(InfoFile, S)
  end;

procedure InfoPos(Pos : Position);
  begin with Pos do write(InfoFile, Line, '␣', Col, '␣')
  end;

procedure InfoCurPos;
  begin with CurPos do write(InfoFile, Line, '␣', Col, '␣')
  end;

```

486. There are a few helper functions which is more than “Write \langle data type \rangle to info file”.

```

var _InfoExitProc: pointer;
procedure InfoExitProc;
  begin CloseInfoFile; ExitProc  $\leftarrow$  _InfoExitProc;
  end;

procedure OpenInfoFile;
  begin Assign(InfoFile, MizFileName +  $\text{'\texttt{.inf'}}$ ); Rewrite(InfoFile);
  WriteLn(InfoFile,  $\text{'Mizared\_article:\_'\texttt{'}}$ , MizFileName,  $\text{'\texttt{'}}$ ); _InfoExitProc  $\leftarrow$  ExitProc;
  ExitProc  $\leftarrow$  @InfoExitProc;
  end;

procedure CloseInfofile;
  begin close(InfoFile)
  end;
end .

```

File 13

XML Parser

487. The XML parser module is used for extracting information from XML files. It does not “validate” the XML (it’s assumed to already be valid). The scanner chops up the input stream into tokens, then the parser makes this available as tokens for the user.

Just to review some terminology from XML:

- (1) A **“tag”** is a markup construct that begins with a “<” and ends with a “>”. There are three types of tags:
 - (i) Start-tags: like “<foo>”
 - (ii) End-tags: like “</foo>”
 - (iii) Empty-element tags: like “
”
- (2) A **“Element”** is a logical document component that either (a) begins with a start-tag and ends with an end-tag, or (b) consists of an empty-element tag. The characters between the start-tag and end-tag (if any) are called its **“Contents”**, and may contain markup including other elements which are called **“Child Elements”**.
- (3) An **“Attribute”** is a markup construct consisting of a name-value pair which can exist in a start-tag or an empty-element tag. For example “” has two attributes: one named “src” whose value is “madonna.jpg”, and the other named “alt” whose value is “Madonna”.
- (4) XML documents may start with an **“XML declaration”** which looks something like (after some optional whitespace) “<?xml version=“1.0” encoding=“UTF-8”?>”

⟨xml_parser.pas 487⟩ ≡

⟨GNU License 4⟩

unit *xml_parser*;

interface *uses* *mobjects*, *errhan*;

⟨Constants for xml_parser.pas 488⟩

⟨Type declarations for xml_parser.pas 489⟩

procedure *XMLASSERT*(*aCond* : *boolean*);

procedure *UnexpectedXMLElement*(**const** *aElem* : *string*;
 aErr : *integer*);

implementation

mdebug ;

uses *info*;

end_mdebug;

⟨Implementation of XML Parser 491⟩

end .

488. Constant parameters. We have a few constant parameters for the error codes.

```

⟨ Constants for xml_parser.pas 488 ⟩ ≡
const InOutFileBuffSize = $4000;
{ for xml attribute tables }
const errElRedundant = 7500; { End of element expected, but child element found }
const errElMissing = 7501; { Child element expected, but end of element found }
const errMissingXMLAttribute = 7502; { Required XML attribute not found }
const errWrongXMLElement = 7503; { Different XML element expected }
const errBadXMLToken = 7506; { Unexpected XML token }

```

This code is used in section 487.

489. Public type declarations. We will defer the “PASCAL classes” until we start implementing them. Right now, we have syntactic classes for the tokens. Specifically we have the start of an XML declaration “<?”, the end of an XML declaration “>”, the start of a character data section “<!” , the start and end of tags, quotation marks, equalities, entities, identifiers, and end of text.

```

⟨ Type declarations for xml_parser.pas 489 ⟩ ≡
type XMLTokenKind = (Err, { an error symbol }
  BI, { <? }
  EI, { ?> }
  DT, { <! }
  LT, { < }
  GT, { > }
  ET, { </ }
  EE, { /> }
  QT, { " }
  EQ, { = }
  EN, { Entity }
  ID, { Identifier, Name }
  EOTX); { End of text }
TokensSet = set of XMLTokenKind;
⟨ Declare XML Scanner Object type 494 ⟩
TElementState = (eStart, eEnd); { high-level parser states, see procedure NextElementState }
⟨ Declare XML Attribute Object 490 ⟩
⟨ Declare XML Parser object 502 ⟩

```

This code is used in section 487.

490. XML Attribute Object. An XML attribute contains the attribute name and its value. We can represent it as “just” an *MStrObj* (§191) with an additional “value” field.

```

⟨ Declare XML Attribute Object 490 ⟩ ≡
  XMLAttrPtr = ↑XMLAttrObj;
  XMLAttrObj = object (MStrObj)
    nValue: string;
    constructor Init(const aName, aValue: string);
  end ;

```

This code is used in section 489.

491. Constructor. This uses the *MStrObj.Init* constructor to initialize the name, then it sets the value.

⟨Implementation of XML Parser 491⟩ ≡

```
constructor XMLAttrObj.Init(const aName, aValue: string);
  begin inherited Init(aName); nValue ← aValue;
  end;
```

See also sections 492, 493, 495, 497, 498, 501, 503, 508, and 510.

This code is used in section 487.

492. Assertion. We have a helper function for asserting things about XML. This is just a wrapper around *MizAssert* (§113).

⟨Implementation of XML Parser 491⟩ +≡

```
procedure XMLASSERT(aCond : boolean);
  begin MizAssert(errWrongXMLElement, aCond);
  end;
```

493. Unexpected XML Element. Another helper function for checking XML parsing.

⟨Implementation of XML Parser 491⟩ +≡

```
procedure UnexpectedXMLElem(const aElem: string;
  aErr: integer);
  mdebug ;
  var lEl: string;
  end_mdebug ;
  begin
  mdebug ; InfoNewLine; end_mdebug;
  RuntimeError(aErr);
  end;
```

494. XML Scanner Object. The scanner produces a stream of tokens, which is then consumed by the XML parser. Hence, besides the constructor and destructor, there is only one public facing method: get the next token.

⟨Declare XML Scanner Object type 494⟩ ≡

```
XMLScannObj = object (MObject)
  nSourceFile: text;
  nSourceFileBuff: pointer;
  nCurTokenKind: XMLTokenKind;
  nSpelling: string;
  nPos: Position;
  nCurCol: integer;
  nLine: string;
  constructor InitScanning(const aFileName: string);
  destructor Done; virtual;
  procedure GetToken; private
  procedure GetAttrValue;
  end ;
```

This code is used in section 489.

$$\langle \text{Implementation of XML Parser } 491 \rangle + \equiv$$

496. This prepares to read in from an XML file, setting up a text buffer, and opening the file in “read mode”.

```
Assign(nSourceFile, aFileName); GetMem(nSourceFileBuff, InOutFileBuffSize);
SetTextBuf(nSourceFile, nSourceFileBuff + InOutFileBuffSize); Reset(nSourceFile) { open for reading }
```

497. Destructor. We need to close the XML file, as well as free up the input buffer.

```

destructor XMLScannObj.Done;
begin close(nSourceFile); FreeMem(nSourceFileBuff, InOutFileBuffSize);
nLine  $\leftarrow$  ``; nSpelling  $\leftarrow$  ``;
inherited Done;
end;

```

$$\mathbf{define} \text{ } update_lexeme \equiv nSpelling \leftarrow Copy(nLine, nPos.Col, nCurCol - nPos.Col)$$

```
procedure XMLScannObj.GetToken;
```

[illegible]

499. If we're done in the file, then we've arrived at the “end-of-file” — i.e., $\text{eof}(nSourceFile)$ is true. In this case, the token returned should be an **EOTX** (end of text). We also end the function here.

On the other hand, if there is still more left in the file, we should read in a line, increment the line number, reset the column to 1, and skip over any whitespace (specifically, “SP” are skipped over — tabs or newlines are not skipped).

```

⟨ Skip whitespace for XML parser 499 ⟩ ≡
  while  $nCurCol = \text{length}(nLine)$  do
    begin if  $\text{eof}(nSourceFile)$  then
      begin  $nCurTokenKind \leftarrow EOTX$ ;  $nSpelling \leftarrow \text{``}$ ; exit end;
      ReadLn( $nSourceFile, nLine$ );  $inc(nPos.Line)$ ;  $nLine \leftarrow nLine + \text{``}\lfloor\text{``}$ ;  $nCurCol \leftarrow 1$ ;
      while  $(nCurCol < \text{length}(nLine)) \wedge (nLine[nCurCol] = \text{``}\lfloor\text{``})$  do  $inc(nCurCol)$ ;
    end

```

This code is used in section 498.

500. There are several situations when determining tokens. We will often want to keep accumulating alphanumeric characters, so we describe this in the “keep eating alphadigits” macro.

When we encounter a “<” character, this could begin or end a tag, or it could be something special if the next character is “?” or “!”. We determine the type in the “get tag kind” macro.

```

define keep_eating_alphadigits ≡
  begin  $nCurTokenKind \leftarrow ID$ ;
  repeat  $inc(nCurCol)$ 
  until  $\text{CharKind}[nLine[nCurCol]] = 0$ ;
end

define get_tag_kind ≡  $inc(nCurCol)$ ;
  case  $nLine[nCurCol]$  of
     $\text{``}/\text{``}$ : begin  $nCurTokenKind \leftarrow ET$ ;  $inc(nCurCol)$ ; end;
     $\text{``?}\text{``}$ : begin  $nCurTokenKind \leftarrow BI$ ;  $inc(nCurCol)$ ; end;
     $\text{``!}\text{``}$ : begin  $nCurTokenKind \leftarrow DT$ ;  $inc(nCurCol)$ ; end;
    othercases  $nCurTokenKind \leftarrow LT$ ;
  endcases

define keep_getting_until_end_of_tag(#) ≡ begin  $inc(nCurCol)$ ;
  if  $nLine[nCurCol] = \text{``}>\text{``}$  then
    begin  $nCurTokenKind \leftarrow \#$ ;  $inc(nCurCol)$ ; end
  else  $nCurTokenKind \leftarrow Err$ ;
  end;

```

```

⟨ Get token kind based off of leading character 500 ⟩ ≡
  case  $nLine[nCurCol]$  of
     $\text{``a}\text{``} \dots \text{``z}\text{``}$ ,  $\text{``A}\text{``} \dots \text{``Z}\text{``}$ ,  $\text{``0}\text{``} \dots \text{``9}\text{``}$ ,  $\text{``\_}\text{``}$ ,  $\text{``-}\text{``}$ ,  $\text{``\&}\text{``}$ : keep_eating_alphadigits;
     $\text{``"}\text{``}$ : begin  $nCurTokenKind \leftarrow QT$ ;  $inc(nCurCol)$  end;
     $\text{``=}\text{``}$ : begin  $nCurTokenKind \leftarrow EQ$ ;  $inc(nCurCol)$  end;
     $\text{``<}\text{``}$ : begin get_tag_kind; end;
     $\text{``>}\text{``}$ : begin  $nCurTokenKind \leftarrow GT$ ;  $inc(nCurCol)$  end;
     $\text{``/}\text{``}$ : keep_getting_until_end_of_tag( $EE$ );
     $\text{``?}\text{``}$ : keep_getting_until_end_of_tag( $EI$ );
    othercases begin  $nCurTokenKind \leftarrow Err$ ;  $inc(nCurCol)$  end;
  endcases

```

This code is used in section 498.

501. Scanners can obtain attribute values as tokens. This is used by the XML parser (§§506, 508). I think one possible source of bugs is that this does not handle escaped quotes (e.g., “\” is traditionally parsed as a quotation mark character).

This will not include the delimiting quotation marks, and it will also skip all whitespace *after* the attribute.

```
define skip_to_quotes  $\equiv$  while ( $nCurCol < length(nLine)$ )  $\wedge$  ( $nLine[nCurCol] \neq \text{" "}$ ) do inc( $nCurCol$ )
define is_space  $\equiv$  ( $nCurCol < length(nLine)$ )  $\wedge$  ( $nLine[nCurCol] \in [\text{' '}, \text{'\n'}, \text{'\t'}]$ )
define skip_spaces  $\equiv$  while is_space do inc( $nCurCol$ )
```

(Implementation of XML Parser 491) \vdash

```
procedure XMLScannObj.GetAttrValue;
  var lCol: integer;
  begin lCol  $\leftarrow$  nCurCol; skip_to_quotes;
  nSpelling  $\leftarrow$  Copy(nLine, lCol, nCurCol - lCol); { save the lexeme }
  if nLine[nCurCol] = '"' then inc(nCurCol);
  skip_spaces;
  end;
```

502. XML Parser. We recall (§489) the type for element states (it’s an enumerated type with two values, *eStart* and *eEnd*).

(Declare XML Parser object 502) \equiv

```
XMLParserObj = object (XMLScannObj)
  nElName: string; { name of the current element }
  nState: TElementState;
  nAttrVals: MSortedStrList;

  constructor InitParsing(const aFileName: string);
  destructor Done; virtual;
  procedure ErrorRecovery(aErr: integer; aSym: TokensSet);
  procedure NextTag; virtual;
  procedure NextElementState; virtual;
  procedure AcceptEndState; virtual;
  procedure AcceptStartState; virtual;
  procedure OpenStartTag; virtual;
  procedure CloseStartTag; virtual;
  procedure CloseEmptyElementTag; virtual;
  procedure ProcessEndTag; virtual;
  procedure ProcessAttributeName; virtual;
  procedure ProcessAttributeValue; virtual;
  procedure SetAttributeValue(const aVal: string);
  end ;
```

This code is used in section 489.

503. Constructor. The parser expects an XML file to start with “<?xml ...?>” (everything after the “xml” is ignored). If this is not the first non-whitespace entry, an error will be raised.

The constructor will then skip all other “<?...?>” entities.

```

define skip_xml_prolog  $\equiv$  while ( $nCurTokenKind \neq EOTX$ )  $\wedge$  ( $nCurTokenKind \neq EI$ ) do GetToken;
    if  $nCurTokenKind = EI$  then GetToken
define skip_all_other_ids  $\equiv$  while  $nCurTokenKind = BI$  do
    begin GetToken;
    while ( $nCurTokenKind \neq EOTX$ )  $\wedge$  ( $nCurTokenKind \neq EI$ ) do GetToken;
    if  $nCurTokenKind = EI$  then GetToken;
    end

```

(Implementation of XML Parser 491) $\vdash \equiv$

```

constructor XMLParserObj.InitParsing(const aFileName: string);
begin inherited InitScanning(aFileName); nElName  $\leftarrow$  ``; nAttrVals.Init(0);
if  $nCurTokenKind = BI$  then
    begin GetToken;
    if ( $nCurTokenKind = ID$ )  $\wedge$  ( $nSpelling = \text{`xml`}$ ) then GetToken
    else ErrorRecovery(10, [EI, LT]);
    skip_xml_prolog; skip_all_other_ids; { skip all other initial processing instructions }
    end;
end;

```

504. Destructor. We will set the element name to the empty string, and invoke the destructor for the attribute values.

```

destructor XMLParserObj.Done;
begin inherited Done; nAttrVals.Done; nElName  $\leftarrow$  ``;
end;

```

505. Error recovery. We just raise a runtime error. In fact, this is often used in situations like:

```

if  $nCurTokenKind = ID$  then { success }
else ErrorRecovery(5, [LT, ET]);

```

Consequently, it is probably more idiomatic to introduce a macro *xml_match(tokenKind)(aErr, aSym)* to assert the match and raise an error for mismatch. Unfortunately, WEB macros allow for only one argument, so we need two macros.

```

define report_mismatch(#)  $\equiv$  ErrorRecovery(#)
define xml_match(#)  $\equiv$  if  $nCurTokenKind \neq \#$  then report_mismatch
    { ErrorRecovery is no longer allowed for XML, bad XML is just RTE }
procedure XMLParserObj.ErrorRecovery(aErr : integer; aSym : TokensSet);
begin Mizassert(errBadXMLToken, false);
end;

```

506. The parser will the consume the next tag or element. It's useful to recall the token kinds (§489).

Curiously, the attributes are skipped during this parsing function.

This will be using the inherited procedure *GetToken* (§498).

```

    { Parses next part of XML, used for skipping some part of XML }
    { setting the nState to eStart or eEnd. }
    { nElName is set properly }
    { nAttrVals are omitted (skipped). }

```

```

procedure XMLParserObj.NextTag;
begin case nCurTokenKind of
  EOTX: nState  $\leftarrow$  eEnd; { sometimes we need this }
  LT: begin nState  $\leftarrow$  eStart; GetToken; xml_match(ID)(6, [LT, ET]); OpenStartTag; GetToken;
    < Get contents of XML start tag 507 >;
  end;
  EE: begin nState  $\leftarrow$  eEnd; GetToken; end;
  ET: begin nState  $\leftarrow$  eEnd; GetToken; xml_match(ID)(8, [LT, ET]); OpenStartTag; GetToken;
    xml_match(GT)(7, [LT, ET]); GetToken
  end;
othercases ErrorRecovery(9, [LT, ET]);
endcases;
end;

```

507. When getting the contents of an XML start tag (or possibly an element), we keep going until we get to either “\>” (for an element) or “>” (for a tag). This will be using the inherited procedure *GetToken* (§498).

```

define get_attribute  $\equiv$  begin GetToken; xml_match(EQ)(4, [ID, GT, LT, ET]); GetToken;
  xml_match(QT)(3, [ID, GT, LT, ET]); GetAttrValue; GetToken;
end

```

```

< Get contents of XML start tag 507 >  $\equiv$ 
repeat case nCurTokenKind of
  GT: begin GetToken; break end;
  EE: begin break end;
  ID: get_attribute;
  othercases begin ErrorRecovery(5, [GT, LT, ET]); break end;
endcases;
until nCurTokenKind = EOTX

```

This code is used in section 506.

508. For Mizar, *everything* will be encoded as an element or an attribute on an element. So we do not really need to consider the case where we would encounter text in the body of an element.

(Implementation of XML Parser 491) +≡

{ Parses next part of XML, setting the $nState$ to $eStart$ or $eEnd$. If $nState = eStart$, then $nElName$, $nAttrVals$ are set properly. It is possible to go from $nState = eStart$ to $nState = eStart$ (when the element is non empty), and similarly from $eEnd$ to $eEnd$. }

procedure *XMLParserObj.NextElementState*;

begin case $nCurTokenKind$ **of**

EOTX: $nState \leftarrow eEnd$; { sometimes we need this }

LT: { Parse start of XML tag 509 };

EE: **begin** $nState \leftarrow eEnd$; *GetToken*; **end**;

ET: **begin** $nState \leftarrow eEnd$; *GetToken*; $xml_match(ID)(8, [LT, ET])$; *ProcessEndTag*; *GetToken*;
 $xml_match(GT)(7, [LT, ET])$; *GetToken*; **end**;

othercases *ErrorRecovery*(9, [LT, ET]);

endcases;

end;

509. We start parsing a start-tag because we have encountered an LT token. So at this point, the next token should be an identifier of some kind. A start-tag may actually be an empty-element tag, so we need to look out for the *EE* token kind.

Note: the XML parser does not handle comments, otherwise we would need to consider that situation here.

define *end_start_tag* ≡ **begin** *GetToken*; *CloseStartTag*; *break* **end**

define *end_empty_tag* ≡ **begin** *CloseEmptyElementTag*; *break* **end**

(Parse start of XML tag 509) ≡

begin $nState \leftarrow eStart$; *GetToken*; $xml_match(ID)(6, [LT, ET])$; *OpenStartTag*;

{ Start-Tag or Empty-Element-Tag Name = nSpelling }

GetToken;

repeat case $nCurTokenKind$ **of**

GT: *end_start_tag*; { End of a Start-Tag }

EE: *end_empty_tag*; { End of a Empty-Element-Tag }

ID: **begin** *ProcessAttributeName*; *GetToken*; $xml_match(EQ)(4, [ID, GT, LT, ET])$; *GetToken*;
 $xml_match(QT)(3, [ID, GT, LT, ET])$; *GetAttrValue*; *ProcessAttributeValue*; *GetToken*;

end;

othercases begin *ErrorRecovery*(5, [GT, LT, ET]); *break* **end**;

endcases;

until $nCurTokenKind = EOTX$;

end

This code is used in section 508.

510. We will want assertions reflecting the parser is in a “start” state or an “end” state.

(Implementation of XML Parser 491) +≡

procedure *XMLParserObj.AcceptEndState*;

begin *NextElementState*; *MizAssert*(*errElRedundant*, $nState = eEnd$);

end;

procedure *XMLParserObj.AcceptStartState*;

begin *NextElementState*; *MizAssert*(*errElMissing*, $nState = eStart$);

end;

511.

```
procedure XMLParserObj.OpenStartTag;
  begin nElName  $\leftarrow$  nSpelling; nAttrVals.FreeAll;
  end;
```

512. We have a few procedures which are, well, empty. I am not sure why we have them. Regardless, here they are!

```
procedure XMLParserObj.CloseStartTag;
  begin end;
procedure XMLParserObj.CloseEmptyElementTag;
  begin end;
procedure XMLParserObj.ProcessEndTag;
  begin end;
```

513. We have a list of attributes. When the parser *ProcessAttributeName*, it will merely push a new *XMLAttrPtr* to the list with the given name. Then *ProcessAttributeValue* will associate to it the value which has been parsed. We can, of course, *manually* set the value for an attribute using *SetAttributeValue*.

```
procedure XMLParserObj.ProcessAttributeName;
  begin nAttrVals.Insert(new(XMLAttrPtr, Init(nSpelling, ``)));
  end;
procedure XMLParserObj.ProcessAttributeValue;
  begin SetAttributeValue(nSpelling);
  end;
procedure XMLParserObj.SetAttributeValue(const aVal: string);
  begin with nAttrVals do XMLAttrPtr(Items↑[Count - 1])↑.nValue  $\leftarrow$  aVal;
  end;
```

File 14

I/O with XML

514. We will want to print some XML to a buffer or stream.

Note that XML seems to be frozen at version 1.0 (first published in 1998, last revised in its fifth edition released November 26, 2008).

```

⟨xml_inout.pas 514⟩ ≡
  ⟨GNU License 4⟩
unit xml_inout;
  interface
    uses errhan, mobjects, xml_parser;
    ⟨Type declarations for XML I/O 515⟩
    function QuoteStrForXML(const aStr: string): string;
    function XMLToStr(const aXMLStr: string): string;
    function QuoteXMLAttr(aStr : string): string;
    const gXMLHeader = `<?xml version="1.0"?>` + #10;
  implementation
    uses SysUtils, mizenv, pcmizver, librenv, xml_dict
    mdebug , info end_mdebug;
  ⟨Implementation for I/O of XML 516⟩
end .

```

515. There are only 4 types of streams we care about: Streams, Text Streams, XML Input Streams, and XML Output Streams.

```

⟨Type declarations for XML I/O 515⟩ ≡
  ⟨Public interface for XML Input Stream 528⟩;
  ⟨Public declaration for Stream Object 520⟩;
  ⟨Public declaration for Text Stream Object 524⟩;
  ⟨Public declaration for XML Output Stream 533⟩;

```

This code is used in section 514.

516. Escape for quote string. We want to allow only alphanumerics [a-zA-Z0-9] as well as dashes (“-”), spaces (“ ”), commas (“,”), periods (“.”), apostrophes (“’”), forward slashes (“/”), underscores (“_”), brackets (“[” and “]”), exclamation points (“!”), semicolons and colons (“;” and “:”), and equal signs (“=”). Everything else we transform into an XML entity of the form “&xx” where *x* is a hexadecimal digit.

⟨Implementation for I/O of XML 516⟩ ≡

```
function QuoteStrForXML(const aStr: string): string;
  const ValidCharTable = ([ 'a' .. 'z', 'A' .. 'Z', '0' .. '9', '-', ' ', ',', '.', '!', ';', ':', '=', '\', '/', '_', '[', ']',
    '!', ' ', ',', '.', '!', ';', ':', '=', '\', '/', '_', '[', ']' );
  var c: char; i: integer;
  begin Result ← aStr;
  for i ← length(Result) downto 1 do
    begin c ← Result[i];
    if ¬(c ∈ ValidCharTable) then
      begin Result[i] ← '&'; Insert('#x' + IntToHex(Ord(c), 2) + ', ', Result, i + 1);
      end;
    end;
  end;
```

See also sections 519, 521, 525, 529, 534, and 540.

This code is used in section 514.

517. This appears to “undo” the previous function, transforming XML entities of the form “&xx” into characters.

```
function XMLToStr(const aXMLStr: string): string;
  var i, h: integer; lHexNr: string;
  begin Result ← aXMLStr;
  for i ← length(Result) - 5 downto 1 do
    begin ⟨Transform XML entity into character, if encountering an XML entity at i 518⟩;
    end;
  Result ← Trim(Result);
  end;
```

518. Transforming an XML entity into a character. This specifically checks for *hexadecimal* entities of the form “&#xXX” for some hexadecimal digits *X*. Note we must prepend “0x” to a numeric string for PASCAL to parse it as hexadecimal.

Since PASCAL does not have shortcircuiting Boolean operations, we need to make this a nested **if** statement.

⟨Transform XML entity into character, if encountering an XML entity at i 518⟩ ≡

```
if (Result[i] = '&') ∧ (length(Result) ≥ i + 5) then
  begin if (Result[i + 1] = '#') ∧ (Result[i + 2] = 'x') then
    begin lHexNr ← Result[i + 3] + Result[i + 4]; h ← StrToInt('0x' + lHexNr); Delete(Result, i, 5);
    Result[i] ← chr(h);
    end;
  end
```

This code is used in section 517.

519. We can quote an XML attribute, escaping quotes, ampersands, and angled brackets. For non-ASCII characters, we escape it to a hexadecimal XML entity.

(Implementation for I/O of XML 516) \equiv

```
function QuoteXMLAttr(aStr : string): string;
  var i: integer;
  begin Result  $\leftarrow$  ``;
  for i  $\leftarrow$  1 to length(aStr) do
    case aStr[i] of
      ``": Result  $\leftarrow$  Result + `&quot;;`;
      `&`: Result  $\leftarrow$  Result + `&amp;;`;
      `<`: Result  $\leftarrow$  Result + `&lt;;`;
      `>`: Result  $\leftarrow$  Result + `&gt;;`;
    othercases if integer(aStr[i]) > 127 then
      Result  $\leftarrow$  Result + `&#x` + IntToHex(Ord(aStr[i]), 2) + `;`
    else Result  $\leftarrow$  Result + aStr[i];
    endcases;
  end;
```

520. Stream object class. A stream consists of a file, a character buffer, as well as integers tracking the size of the buffer and (I think) the position in the buffer. This is the parent class to XML output buffers.

(Public declaration for Stream Object 520) \equiv

```
StreamObj = object (MObject)
  nFile: File;
  fFileBuff:  $\uparrow$ BuffChar;
  fBuffCount, fBuffInd: longint;
  constructor InitFile(const AFileName: string);
  procedure Error(Code, Info : integer); virtual;
  destructor Done; virtual;
end
```

This code is used in section 515.

521. We will have a wrapper function for conveniently reporting errors.

(Implementation for I/O of XML 516) \equiv

```
procedure StreamObj.Error(Code, Info : integer);
  begin RunError(2000 + Code);
  end;
```

522. Constructor. We begin by *Assign*-ing a name to a file, allocating a file buffer, then initializing the buffer size to zero, and the buffer position to zero. (The buffer position *fBuffInd* is needed only when writing to an output XML stream.)

```
constructor StreamObj.InitFile(const AFileName: string);
  begin Assign(nFile, AFileName); new(fFileBuff); fBuffCount  $\leftarrow$  0; fBuffInd  $\leftarrow$  0;
  end;
```

523. Destructor. We close the file, and free up the file buffer.

```
destructor StreamObj.Done;
  begin Close(nFile); dispose(fFileBuff);
  end;
```

524. Text Stream Object. A text stream is very similar to a Stream Object, except it is specifically for text.

```

⟨Public declaration for Text Stream Object 524⟩ ≡
  TXTStreamObj = object (MObject)
    nFile: text;
    nFileBuff: pointer;
    constructor InitFile(const AFileName: string);
    procedure Error(Code, Info : integer); virtual;
    destructor Done; virtual;
  end

```

This code is used in section 515.

525. We have the convenience function for reporting errors.

```

⟨Implementation for I/O of XML 516⟩ +≡
procedure TXTStreamObj.Error(Code, Info : integer);
  begin RunError(2000 + Code);
  end;

```

526. Constructor. Assign a name to the file, allocate an input buffer, then initialize the buffer.

```

constructor TXTStreamObj.InitFile(const AFileName: string);
  begin Assign(nFile, AFileName); GetMem(nFileBuff, InOutFileBuffSize);
  SetTextBuf(nFile, nFileBuff↑, InOutFileBuffSize);
  end;

```

527. Destructor. Simply free the underlying file buffer.

```

destructor TXTStreamObj.Done;
  begin FreeMem(nFileBuff, InOutFileBuffSize);
  end;

```

528. XML Input Streams. An input stream reads an XML file and produces an abstract syntax tree for its contents. This extends this XML parser class (§502). It may be tempting to draw similarities with, e.g., the StAX library (in Java), but the truth is there's only finitely many ways to parse XML, and some ways are just more natural.

```

⟨Public interface for XML Input Stream 528⟩ ≡
  XMLInStreamPtr = ↑XMLInStreamObj;
  XMLInStreamObj = object (XMLParserObj)
    constructor OpenFile(const AFileName: string);
    function GetOptAttr(const aAttrName: string; var aVal: string) : boolean;
    function GetAttr(const aAttrName: string): string;
    function GetIntAttr(const aAttrName: string): integer;
  end

```

This code is used in section 515.

529. Constructor. The non-debugging code just invokes the XML Parser's constructor (§503).

```

⟨Implementation for I/O of XML 516⟩ +≡
constructor XMLInStreamObj.OpenFile(const AFileName: string);
  begin
    mdebug ; write(InfoFile, AFileName); end_mdebug;
    InitParsing(AFileName);
    mdebug ; WriteLn(InfoFile, 'reset'); end_mdebug;
  end;

```

530. We use the inherited *XMLParserObj*'s *nAttrVals*: *MSortedStrList* to track the XML attributes. If *aAttrName* is stored there, this will mutate *aVal* to store the associated value and the function will return *true*. Otherwise, this will return *false*.

This is useful for getting the value of an *optional* XML attribute.

```
{ get string denoted by optional XML attribute aAttrName }
function XMLInStreamObj.GetOptAttr (const aAttrName: string; var aVal: string) : boolean;
var lAtt: XMLAttrPtr;
begin lAtt ← XMLAttrPtr(nAttrVals.ObjectOf(aAttrName));
if lAtt ≠ nil then
  begin aVal ← lAtt↑.nValue; GetOptAttr ← true; exit;
  end;
  GetOptAttr ← false;
end;
```

531. When we know an XML attribute is *required*, we can just get the associated value directly (and raise an error if it is missing).

```
{ get string denoted by required XML attribute aAttrName }
function XMLInStreamObj.GetAttr(const aAttrName: string): string;
var lAtt: XMLAttrPtr;
begin lAtt ← XMLAttrPtr(nAttrVals.ObjectOf(aAttrName));
if lAtt ≠ nil then
  begin GetAttr ← lAtt↑.nValue; exit;
  end;
  MizAssert(errMissingXMLAttribute, false);
end;
```

532. When the required attribute has an integer value, we should return the integer-value of it. Does this ever happen? Yes! For example, when writing an article named `article.miz`, then we run the verifier on it, we shall obtain `article.xml` which will contain tags of the form “<Adjective nr="5">”.

```
{ get integer denoted by required XML attribute aAttrName }
function XMLInStreamObj.GetIntAttr(const aAttrName: string): integer;
var lInt, ec: integer;
begin val(GetAttr(aAttrName), lInt, ec); GetIntAttr ← lInt;
end;
```

533. XML Output Streams. We will want to write data to an XML file. This gives us an abstraction for doing so.

```

⟨Public declaration for XML Output Stream 533⟩ ≡
  XMLOutputStreamPtr = ↑XMLOutputStreamObj;
  XMLOutputStreamObj = object (StreamObj)
    nIndent: integer; { indenting }
    constructor OpenFile(const AFileName: string);
    constructor OpenFileWithXSL(const AFileName: string);
    destructor EraseFile;
    procedure OutChar(AChar : char);
    procedure OutNewLine;
    procedure OutString(const AString: string);
    procedure OutIndent;
    procedure Out_XElStart(const fEl: string);
    procedure Out_XAttrEnd;
    procedure Out_XElStart0(const fEl: string);
    procedure Out_XElEnd0;
    procedure Out_XEl1(const fEl: string);
    procedure Out_XElEnd(const fEl: string);
    procedure Out_XAttr(const fAt, fVal: string);
    procedure Out_XIntAttr(const fAt: string;
      fVal: integer);
    procedure Out_PosAsAttrs(const fPos: Position);
    procedure Out_XElWithPos(const fEl: string;
      const fPos: Position);
    procedure Out_XQuotedAttr(const fAt, fVal: string);
    destructor Done; virtual;
  end

```

This code is used in section 515.

534. Constructor. We initialize a file, open it for writing, set the initial indentation amount to zero, and then print the XML header declaration.

```

⟨Implementation for I/O of XML 516⟩ +≡
constructor XMLOutputStreamObj.OpenFile(const AFileName: string);
  begin
    mdebug write(InfoFile, MizFileName + `.` + copy(AFileName, length(AFilename) - 2, 3));
    end_mdebug
    InitFile(AFileName); Rewrite(nFile, 1);
    mdebug WriteLn(InfoFile, `rewritten`); end_mdebug
    nIndent ← 0; OutString(gXMLHeader);
  end;

```

535. Constructor. Since XML supports custom style declarations (think of XSLT), we can also support writing an XML file which uses them. This specifically needs to adjust the XML declaration.

```

  { add the stylesheet procesing info }
constructor XMLOutputStreamObj.OpenFileWithXSL(const AFileName: string);
  begin OpenFile(AFileName);
    OutString('<?xml-stylesheet type="text/xml" href="file://' + MizFiles + `miz.xml">' + #10);
  end;

```

536. Destructor. We need to flush the buffer to the file before freeing up the buffer.

```
destructor XMLOutStreamObj.Done;
  begin if (fBuffInd > 0)  $\wedge$  (fBuffInd < InOutFileBuffSize) then
    BlockWrite(nFile, fFileBuff↑, fBuffInd, fBuffCount);
  inherited Done;
end;
```

537. Destructor. Some times we want to further erase the output file (which seems, at first glance, like a really bad idea...).

```
destructor XMLOutStreamObj.EraseFile;
  begin Done; Erase(nFile);
end;
```

538. Writing a character to the buffer. When the buffer is full, we flush it.

```
procedure XMLOutStreamObj.OutChar(aChar : char);
  begin fFileBuff↑[fBuffInd] ← AnsiChar(aChar); inc(fBuffInd); ⟨Flush XML output buffer, if full 539⟩;
end;
```

539. The XML output buffer is full when the logical size (fBuffInd) is equal to the InOutFileBuffSize. When this happens, we should write everything to the file, then reset the logical size parameter to zero.

```
⟨Flush XML output buffer, if full 539⟩ ≡
  if fBuffInd = InOutFileBuffSize then
    begin BlockWrite(nFile, fFileBuff↑, InOutFileBuffSize, fBuffCount); fBuffInd ← 0;
  end
```

This code is used in section 538.

540. Print a newline ("␣") to the XML output stream.

```
⟨Implementation for I/O of XML 516⟩ +≡
procedure XMLOutStreamObj.OutNewLine;
  begin OutChar(#10);
end;
```

541. Printing a string to the output buffer.

```
procedure XMLOutStreamObj.OutString(const aString: string);
  var i: integer;
  begin for i ← 1 to length(aString) do OutChar(aString[i]);
end;
```

542. Printing nIndent spaces ("␣") to the output buffer.

```
{ print nIndent spaces }
procedure XMLOutStreamObj.OutIndent;
  var i: integer;
  begin for i ← 1 to nIndent do OutChar('␣');
end;
```

543. When printing a start-tag to the file, we start by printing the indentation, then we increment the indentation, then we print the “<” followed by the name of the tag.

```
{ print '<' and the representation of fEl with indenting }
procedure XMLOutStreamObj.Out_XElStart(const fEl: string);
  begin OutIndent; inc(nIndent); OutChar('<'); OutString(fEl);
  end;
```

544. When we are done writing the attributes of a tag, we print the “>” to the file, and we also print a newline to the file.

```
{ close the attributes with '>' }
procedure XMLOutStreamObj.Out_XAttrEnd;
  begin OutChar('>'); OutNewLine;
  end;
```

545. When we want to write the tag, but omit the attributes, we can do so.

```
{ no attributes expected }
procedure XMLOutStreamObj.Out_XElStart0(const fEl: string);
  begin Out_XElStart(fEl); Out_XAttrEnd;
  end;
```

546. For empty-element tags, we should close the tag with “/>”, print a new line, then *decrement* the indentation since there are no children to the tag.

```
{ print '/>' with indenting }
procedure XMLOutStreamObj.Out_XElEnd0;
  begin OutString('>'); OutNewLine; dec(nIndent);
  end;
```

547. When printing an empty-element tag without any attributes, we can combine the preceding functions together.

```
{ no attributes and elements expected }
procedure XMLOutStreamObj.Out_XEl1(const fEl: string);
  begin Out_XElStart(fEl); Out_XElEnd0;
  end;
```

548. Printing end-tags should first decrement the indentation *before* printing the indentation to the file (so that the end-tag vertically aligns with the associated start-tag). Then we print “</” followed by the tag name and then “>”. We should print a newline to the file, too.

```
{ close the fEl element using '</' }
procedure XMLOutStreamObj.Out_XElEnd(const fEl: string);
  begin dec(nIndent); OutIndent; OutString('</'); OutString(fEl); OutChar('>'); OutNewLine;
  end;
```

549. When printing one attribute to a tag, we need a whitespace printed (to separate the tag’s name — or preceding attribute — from the current attribute being printed), followed by the attribute’s name printed with an equality symbol, then enquoted the value of the attribute.

```
{ print one attribute key-value pair }
procedure XMLOutStreamObj.Out_XAttr(const fAt, fVal: string);
  begin OutChar(' '); OutString(fAt); OutString('=''); OutString(fVal); OutChar('"');
  end;
```

550. When the value of an attribute is an integer, invoke *IntToStr(fVal)* to pretend it is a string value. Then printing out to a file an attribute with an integer value boils down to printing out the attribute with a string value.

```
{ print one attribute key-value pair, where value is integer }
procedure XMLOutStreamObj.Out_XIntAttr(const fAt: string; fVal: integer);
  begin Out_XAttr(fAt, IntToStr(fVal));
  end;
```

551. We can now just compose writing the start of a tag (§543), followed by its attributes (§552), and then close the empty-element tag (§546).

```
procedure XMLOutStreamObj.Out_XElWithPos(const fEl: string; const fPos: Position);
  begin Out_XElStart(fEl); Out_PosAsAttrs(fPos); Out_XElEnd0;
  end;
```

552. We will want to treat a *position* (i.e., the line and column) as two attributes. We print this out using *Out_PosAsAttrs*. We rely on the *XMLDict*'s *XMLAttrName* for standardizing the name for the line and column.

```
procedure XMLOutStreamObj.Out_PosAsAttrs(const fPos: Position);
  begin Out_XIntAttr(XMLAttrName[atLine], fPos.Line);
  Out_XIntAttr(XMLAttrName[atCol], fPos.Col);
  end;
```

553. We print a quoted attribute, leveraging printing attributes out to the file (§549). We just need to escape the XML string (§516).

```
procedure XMLOutStreamObj.Out_XQuotedAttr(const fAt, fVal: string);
  begin Out_XAttr(fAt, QuoteStrForXML(fVal));
  end;
```

File 15

Vocabulary file dictionaries

554. Mizar works with vocabulary files (suffixed with `.voc`) for introducing new identifiers.

```

⟨dicthan.pas 554⟩ ≡
  ⟨GNU License 4⟩
unit dicthan;
interface
  uses mobjects;
  ⟨Public constants for dicthan.pas 555⟩
  type SymbolCounters = array [^A .. ^Z] of word;
    SymbolIntSeqArr = array [^A .. ^Z] of IntSequence;
  ⟨Class declarations for dicthan.pas 556⟩
  ⟨Public function declarations for dicthan.pas 557⟩
implementation
  uses mizenv, xml_inout, xml_dict;
  ⟨Implementation for dicthan.pas 558⟩
end .

```

555. We recall from Adam Grabowski, Artur Kornilowicz, and Adam Naumowicz’s “Mizar in a Nutshell” (§4.3, [doi:10.6092/issn.1972-5787/1980](https://doi.org/10.6092/issn.1972-5787/1980)), the various prefixes for vocabulary file entries:

- G for structures
- K for left-functor brackets
- L for right-functor brackets
- M for modes
- O for functors
- R for predicates
- U for selectors
- V for attributes

```

⟨Public constants for dicthan.pas 555⟩ ≡
const
  StandardPriority = 64;
  AvailableSymbols = [^G, ^K, ^L, ^M, ^O, ^R, ^U, ^V];

```

This code is used in section 554.

556. There are only three classes in the dictionary handling module. We have an abstraction for a symbol appearing in a vocabulary file, a sort of “checksum” for the counts of symbols appearing in a vocabulary file, and a dictionary associating to each article name (string) a collection of symbols.

```

⟨Class declarations for dicthan.pas 556⟩ ≡
  ⟨Symbol for vocabulary 562⟩;
  ⟨Abstract vocabulary object declaration 571⟩;
  ⟨Vocabulary object declaration 573⟩;

```

This code is used in section 554.

557. \langle Public function declarations for `dicthan.pas` 557 $\rangle \equiv$
function *GetPrivateVoc*(**const** *fName*: *string*): *PVocabulary*;
function *GetPublicVoc* (**const** *fName*: *string*; **var** *fVocFile*: *text*) : *PVocabulary*;
procedure *LoadMmlVcb* (**const** *aFileName*: *string*; **var** *aMmlVcb*: *MStringList*) ;
procedure *StoreMmlVcb*(**const** *aFileName*: *string*; **const** *aMmlVcb*: *MStringList*);
procedure *StoreMmlVcbX*(**const** *aFileName*: *string*; **const** *aMmlVcb*: *MStringList*);

This code is used in section 554.

558. We can test if an entry in the dictionary is valid. Remember, only functor symbols can have a priority associated with it (and a priority is a number between 0 and $2^8 - 1$, inclusive).

Also remember, that a symbol in a dictionary entry **cannot** have whitespaces in it.

define *delete_prefix* \equiv *Delete*(*lLine*, 1, 1)
 \langle Implementation for `dicthan.pas` 558 $\rangle \equiv$
function *IsValidSymbol*(**const** *aLine*: *string*): *boolean*;
var *lLine*: *string*; *lKind*: *char*; *lPriority*, *lPos*, *lCode*: *integer*;
begin *IsValidSymbol* \leftarrow *false*; *lLine* \leftarrow *TrimString*(*aLine*);
 \langle Initialize *lKind*, but exit if dictionary line contains invalid symbol 559 \rangle ;
delete_prefix;
case *lKind* **of**
 'O' : \langle Check if functor symbol is valid 560 \rangle ;
 'R' : \langle Check if predicate symbol is valid 561 \rangle ;
othercases **begin** **if** *Pos*('\u00a0' , *lLine*) > 0 **then** *exit*;
 IsValidSymbol \leftarrow *true*;
end;
endcases;
end;

See also sections 563, 567, 572, 574, 578, 580, and 581.

This code is used in section 554.

559. An “invalid” line in the dictionary file would be empty lines (whose length is less than one), and lines which do not start with a valid prefix. At the end of this chunk, the *lKind* should be initialized to the prefix of the line.

\langle Initialize *lKind*, but exit if dictionary line contains invalid symbol 559 $\rangle \equiv$
if *length*(*lLine*) \leq 1 **then** *exit*;
lKind \leftarrow *lLine*[1];
if \neg (*lKind* \in *AvailableSymbols*) **then** *exit*

This code is used in section 558.

560. Recall the [specification](#) for *Val* sets *lCode* to zero for success, and the nonzero values store the index where the string is not a numeric value.

We copy the identifier (as determined from the start of the line until, but not including, the index of the first space in the line) and throw away everything after the first whitespace.

When the identifier for the functor symbol is not an empty string *and* the priority can be determined unambiguously, then the functor symbol entry is valid. Otherwise it is invalid.

```

⟨ Check if functor symbol is valid 560 ⟩ ≡
  begin IsValidSymbol ← true; lPos ← Pos(‘␣’, lLine);
  if lPos ≠ 0 then
    begin { Parse priority for symbol }
      val (TrimString(Copy(lLine, lPos, length(lLine))), lPriority, lCode);
      lLine ← TrimString(Copy(lLine, 1, lPos - 1)); IsValidSymbol ← (lCode = 0) ∧ (lLine ≠ ‘’);
    end;
  end
end

```

This code is used in section [558](#).

561. A predicate entry in the dictionary file should not include a priority, nor should it include any whitespaces. This is the criteria for a valid predicate symbol entry in the dictionary.

We enforce this by finding the first “␣” character in the line. If there is one, then we trim both sides of the line (removing leading and trailing whitespace). We should have no more spaces in the line. If there is a space, then it is an invalid predicate symbol.

```

⟨ Check if predicate symbol is valid 561 ⟩ ≡
  begin lPos ← Pos(‘␣’, lLine);
  if lPos ≠ 0 then { lLine contains a space }
    begin lLine ← TrimString(Copy(lLine, lPos, length(lLine)));
    if Pos(‘␣’, lLine) > 0 then exit;
    end;
  IsValidSymbol ← true;
  end
end

```

This code is used in section [558](#).

562. TSymbol. These are used in `kernel/accdict.pas`. The *Kind* is its one-letter kind (discussed in [§555](#)), and *Repr* is its lexeme. For functors, its priority is stored as its *Prior*.

The “infinite” appears to be only used for predicates.

```

⟨ Symbol for vocabulary 562 ⟩ ≡
  PSymbol = ↑TSymbol;
  TSymbol = object (MObject)
    Kind: char;
    Repr, Infinitive: string;
    Prior: byte;
    constructor Init(fKind: char; fRepr, fInfinitive: string; fPriority: byte);
    constructor Extract(const aLine: string);
    function SymbolStr: string;
    constructor Load(var aText: text);
    procedure Store(var aText: text);
    destructor Done; virtual;
  end
end

```

This code is used in section [556](#).

563. Constructor. Given the “kind”, its “representation” and “infinitive”, and its priority (as a number between 0 and 255), we can construct a symbol.

⟨Implementation for `dicthan.pas` 558⟩ +≡

```
constructor TSymbol.Init(fKind : char; fRepr, fInfinitive : string; fPriority : byte);
  begin Kind ← fKind; Repr ← fRepr; Prior ← fPriority; Infinitive ← ``;
end;
```

564. Constructor. When we want to extract a symbol from a line in the dictionary file, care must be taken for functors (since they may contain an explicit priority) and for predicates. Predicates have an undocumented feature to allow “infinitives”, so an acceptable predicate line in a dictionary may look like

`Rpredicate infinitive`

Although what Mizar does with infinitives, I do not know...

```
constructor TSymbol.Extract(const aLine : string);
  var lPos, lCode : integer; lRepr : string;
  begin Kind ← aLine[1]; Repr ← TrimString(Copy(aLine, 2, length(aLine))); Prior ← 0;
  Infinitive ← ``;
  case Kind of
    0 : begin lPos ← Pos(`_`, Repr); Prior ← StandardPriority;
      if lPos ≠ 0 then ⟨Initialize explicit priority for functor entry in dictionary 566⟩;
      end;
    R : begin lPos ← Pos(`_`, Repr);
      if lPos ≠ 0 then ⟨Initilize explicit infinitive for a predicate entry in dictionary 565⟩;
      end;
  endcases;
end;
```

565. Predicates can have an optional infinitive, separated from the lexeme by a single whitespace. It remains unclear what Mizar uses predicate infinitives for, but it is a feature. This is written out to the `.vcx` file, according to `xml_dict.pas`.

Note that there are 4 predicates with infinitives in Mizar:

- (1) `jumps_in` (infinitive: `jump_in`) occurs in the article `AMISTD_1`
- (2) `halts_in` (infinitive: `halt_in`) occurs in the article `EXTPRO_1`
- (3) `refers` (infinitive: `refer`) occurs in the article `SCMFSA7B`
- (4) `destroys` (infinitive: `destroy`) occurs in the article `SCMFSA7B`

⟨Initilize explicit infinitive for a predicate entry in dictionary 565⟩ ≡

```
begin lRepr ← Repr; Repr ← ``; Repr ← TrimString(Copy(lRepr, 1, lPos - 1));
  Infinitive ← TrimString(Copy(lRepr, lPos + 1, length(lRepr)));
end
```

This code is used in section 564.

566. Functors with explicit priorities require parsing that priority. It is assumed that a single whitespace separates the lexeme from the priority.

⟨Initialize explicit priority for functor entry in dictionary 566⟩ ≡

```
begin lRepr ← Repr; Repr ← ``;
  val (TrimString(Copy(lRepr, lPos + 1, length(lRepr))), Prior, lCode); { Store the priority }
  Repr ← TrimString(Copy(lRepr, 1, lPos - 1)); { Store the lexeme }
end
```

This code is used in section 564.

567. Serialize symbols. We can serialize a *TSymbol* object, which produces the sort of entry we'd expect to find in a dictionary. So we would have the symbol kind, the lexeme, and optional data (non-default priorities for functors, infinitives for predicates).

⟨Implementation for `dicthan.pas` 558⟩ \equiv

```
function TSymbol.SymbolStr: string;
  var lStr, lntStr: string;
  begin lStr  $\leftarrow$  Kind + Repr;
  case Kind of
    '0': if Prior  $\neq$  StandardPriority then
      begin Str(Prior, lntStr); lStr  $\leftarrow$  lStr + '␣' + lntStr;
      end;
    'R': if Infinitive  $\neq$  '' then lStr  $\leftarrow$  lStr + '␣' + Infinitive;
  endcases;
  SymbolStr  $\leftarrow$  lStr;
end;
```

568. Given a text (usually the contents of a vocabulary file), we read in a line. When the line is a nonempty string, we initialize the lexeme representation, priority, and infinitives. Then, when the dictionary entry describes a valid symbol (§558), we populate the fields of the *TSymbol*.

```
constructor TSymbol.Load(var aText : text);
  var lDictLine: string;
  begin ReadLn(aText, lDictLine); lDictLine  $\leftarrow$  TrimString(lDictLine);
  if length(lDictLine) = 0 then exit;
  Repr  $\leftarrow$  ''; Prior  $\leftarrow$  0; Infinitive  $\leftarrow$  '';
  if IsValidSymbol(lDictLine) then Extract(lDictLine);
end;
```

569. Storing a *TSymbol* in a file amounts to writing its serialization (§567) to the file.

```
procedure TSymbol.Store(var aText : text);
  begin WriteLn(aText, SymbolStr);
end;
```

570. Destructor. We just reset the lexeme and infinitive strings to be empty strings.

```
destructor TSymbol.Done;
  begin Repr  $\leftarrow$  ''; Infinitive  $\leftarrow$  '';
end;
```

571. Abstract vocabulary objects. This is used in `kernel/impobjs.pas`. We recall (§554) that the *SymbolCounters* are just an enumerated type consisting of a single uppercase Latin Letter.

⟨Abstract vocabulary object declaration 571⟩ \equiv

```
AbsVocabularyPtr =  $\uparrow$ AbsVocabularyObj;
AbsVocabularyObj = object (MObject)
  fSymbolCnt: SymbolCounters;
  constructor Init;
  destructor Done; virtual;
end
```

This code is used in section 556.

572. We only have the constructor and destructor for abstract vocabulary objects.

```

⟨Implementation for dicthan.pas 558⟩ +≡
constructor AbsVocabularyObj.Init;
  begin FillChar(fSymbolCnt, SizeOf(fSymbolCnt), 0);
  end;
destructor AbsVocabularyObj.Done;
  begin end;

```

573. Vocabulary objects. A “vocabulary object” is just a collection of *PSymbols* read in from a vocabulary file.

These are also used in `kernel/accdict.pas`.

```

⟨Vocabulary object declaration 573⟩ ≡
PVocabulary = ↑TVocabulary;
TVocabulary = object (AbsVocabularyObj)
  Reprs: MCollection;
  constructor Init;
  constructor ReadPrivateVoc(const aFileName: string);
  constructor LoadVoc(var aText: text);
  procedure StoreVoc (const aFileName: string; var aText: text );
  destructor Done; virtual;
end

```

This code is used in section 556.

574. Constructor (Empty vocabulary). We can construct the empty vocabulary by just initializing the underlying collection.

```

⟨Implementation for dicthan.pas 558⟩ +≡
constructor TVocabulary.Init;
  begin FillChar(fSymbolCnt, SizeOf(fSymbolCnt), 0); Reprs.Init(10, 10);
  end;

```

575. Destructor. We only need to free up the underlying collection.

```

destructor TVocabulary.Done;
  begin Reprs.Done;
  end;

```

576. Constructor. We can read from a private vocabulary file.

```

constructor TVocabulary.ReadPrivateVoc(const aFileName: string);
  var lDict: text; lDictLine: string; lSymbol: PSymbol;
  begin Init; Assign(lDict, aFileName);
  without_io_checking(reset(lDict));
  if ioresult ≠ 0 then exit; { file is not ready to be read, bail out! }
  while ¬seekEOF(lDict) do ⟨Read line into vocabulary from dictionary file 577⟩;
  Close(lDict);
end;

```

577. When reading dictionary lines into a vocabulary file, we skip over blank lines. Further, we only read *valid* entries into the vocabulary.

```

⟨ Read line into vocabulary from dictionary file 577 ⟩ ≡
  begin readln(lDict, lDictLine); lDictLine ← TrimString(lDictLine);
  if length(lDictLine) > 1 then { if dictionary line is not blank }
    begin lSymbol ← new(PSymbol, Extract(lDictLine));
    if IsValidSymbol(lDictLine) then { add the symbol }
      begin inc(fSymbolCnt[lSymbol↑.Kind]); Reprs.Insert(lSymbol); end;
    end;
  end
end

```

This code is used in section 576.

578. Constructor. We can read in the vocabulary from a file. If I am not mistaken, this is usually from `mml.vct`. We have the first line look like “G3 K0 L0 M1 07 R2 U4 V6”, which enumerates the number of different types of definitions appearing in an article.

```

⟨ Implementation for dicthan.pas 558 ⟩ +≡
constructor TVocabulary.LoadVoc(var aText : text);
  var i, lSymbNbr, lNbr: integer; lKind, lDummy, c: Char;
  begin lSymbNbr ← 0; ⟨ Count lNbr the number of dictionary entries for an article 579 ⟩;
  ReadLn(aText); Reprs.Init(10, 10);
  for i ← 1 to lSymbNbr do
    begin Reprs.Insert(new(PSymbol, Load(aText)));
  end;
end;

```

579. Since the first line counts the different sorts of definitions appearing in the article, we can parse the numbers, then add them up. This initializes the *fSymbolCnt* entry for *c*.

```

⟨ Count lNbr the number of dictionary entries for an article 579 ⟩ ≡
  for c ← 'A' to 'Z' do
    if c ∈ AvailableSymbols then
      begin Read(aText, lKind, lNbr, lDummy); fSymbolCnt[c] ← lNbr; Inc(lSymbNbr, fSymbolCnt[c]);
      end
    end
  end

```

This code is used in section 578.

580. Storing a dictionary entry. This appends to a `.vct` file the entries for an article. Specifically, this is just the “#ARTICLE” and then the counts of the different kinds of definitions.

```

⟨ Implementation for dicthan.pas 558 ⟩ +≡
procedure TVocabulary.StoreVoc (const aFileName: string; var aText: text );
  var i: Byte; c: Char;
  begin WriteLn(aText, '#', aFileName);
  for c ← 'A' to 'Z' do
    if c ∈ AvailableSymbols then Write(aText, c, fSymbolCnt[c], ' ');
  WriteLn(aText);
  for i ← 0 to Reprs.Count - 1 do PSymbol(Reprs.Items↑[i])↑.Store(aText);
  end;
end;

```

581. Miscellaneous public-facing functions.

⟨Implementation for `dicthan.pas` 558⟩ $\vdash \equiv$

```
function GetPrivateVoc(const fName: string): PVocabulary;
var lName: string;
begin lName ← fName;
if ExtractFileExt(lName) = '' then lName ← lName + '.voc';
if ¬MFileExists(lName) then
  begin GetPrivateVoc ← nil; exit;
end;
GetPrivateVoc ← new(PVocabulary, ReadPrivateVoc(lName));
end;
```

582. Reading mml.vct entries. The `$MIZFILES/mml.vct` file contains all the vocabularies concatenated together into one giant vocabulary file. It uses lines prefixed with “#” followed by the article name to separate the vocabularies from different files. We search for the given article name (stored in the `fName` argument). When we find it, we construct the Vocabulary object (§578).

```
function GetPublicVoc (const fName: string; var fVocFile: text ) : PVocabulary;
var lLine: string;
begin GetPublicVoc ← nil; reset(fVocFile);
while ¬eof(fVocFile) do
  begin readln(fVocFile, lLine);
  if (length(lLine) > 0) ∧ (lLine[1] = '#') ∧ (copy(lLine, 2, length(lLine)) = fName) then
    begin GetPublicVoc ← new(PVocabulary, LoadVoc(fVocFile)); exit;
    end;
  end;
end;
```

583. Reading from mml.vct. This function is used by `libtools/checkvoc.dpr` and in a couple user tools. In those other functions, they pass `$MIZFILES/mml.vct` as the value for `aFileName`. This procedure will then populate the `aMmlVcb` file associating to each article name its vocabulary.

```
procedure LoadMmlVcb (const aFileName: string; var aMmlVcb: MStringList );
var lFile: text; lDummy: char; lDictName: string; r: Integer;
begin FileExam(aFileName); Assign(lFile, aFileName); Reset(lFile); { initialize file for reading }
aMmlVcb.Init(1000); aMmlVcb.fSorted ← true;
while ¬eof(lFile) do
  begin ReadLn(lFile, lDummy, lDictName);
  r ← aMmlVcb.AddObject(lDictName, new(PVocabulary, LoadVoc(lFile)));
  end;
Close(lFile);
end;
```

584. Storing a vocabulary delegates much work (§580). However, since `fCount` is not initialized, I am uncertain how this works, exactly... Furthermore, this function is not used anywhere in Mizar.

```
procedure StoreMmlVcb(const aFileName: string; const aMmlVcb: MStringList);
var lFile: text; i: Integer;
begin Assign(lFile, aFileName); Rewrite(lFile);
with aMmlVcb do
  for i ← 0 to fCount - 1 do PVocabulary(fList↑[i].fObject)↑.StoreVoc(fList↑[i].fString↑, lFile);
  Close(lFile);
end;
```

585. Like *StoreMmlVcb*, this function is not used anywhere in Mizar. This appears to produce the XML-equivalent to the previous function.

```
procedure StoreMmlVcbX(const aFileName: string; const aMmlVcb: MStringList);
  var i, s: Integer; c: char; VCXfile: XMLOutputStreamPtr;
  begin VCXfile ← new(XMLOutputStreamPtr, OpenFile(aFileName));
    VCXfile.Out_XElStart0(XMLElemName[elVocabularies]);
  with aMmlVcb do
    for i ← 0 to fCount − 1 do
      with PVocabulary(fList↑[i].fObject)↑ do
        begin VCXfile.Out_XElStart(XMLElemName[elVocabulary]);
          VCXfile.Out_XAttr(XMLAttrName[atName], fList↑[i].fString↑); VCXfile.Out_XAttrEnd;
          ⟨ Write vocabulary counts to XML file 586 ⟩;
          ⟨ Write symbols to vocabulary XML file 587 ⟩;
          VCXfile.Out_XElEnd(XMLElemName[elVocabulary]);
        end;
      VCXfile.Out_XElEnd(XMLElemName[elVocabularies]); dispose(VCXfile, Done);
    end;
```

586. We write out the counts of each kind of definition appearing in the article.

```
⟨ Write vocabulary counts to XML file 586 ⟩ ≡
  { Kinds }
  for c ← ‘A’ to ‘Z’ do
    if c ∈ AvailableSymbols then
      begin VCXfile.Out_XElStart(XMLElemName[elSymbolCount]);
        VCXfile.Out_XAttr(XMLAttrName[atKind], c);
        VCXfile.Out_XIntAttr(XMLAttrName[atNr], fSymbolCnt[c]); VCXfile.Out_XElEnd0;
      end
```

This code is used in section 585.

587. We write out each symbol appearing in the article’s vocabulary.

```
⟨ Write symbols to vocabulary XML file 587 ⟩ ≡
  { Symbols }
  VCXfile.Out_XElStart0(XMLElemName[elSymbols]);
  for s ← 0 to Reprs.Count − 1 do
    with PSymbol(Reprs.Items[s])↑ do
      begin VCXfile.Out_XElStart(XMLElemName[elSymbol]);
        VCXfile.Out_XAttr(XMLAttrName[atKind], Kind);
        VCXfile.Out_XAttr(XMLAttrName[atName], QuoteStrForXML(Repr));
        case Kind of
          ‘0’: VCXfile.Out_XIntAttr(XMLAttrName[atPriority], Prior);
          ‘R’: if Infinitive ≠ ‘’ then VCXfile.Out_XAttr(XMLAttrName[atInfinitive], Infinitive);
        end; VCXfile.Out_XElEnd0;
      end;
    VCXfile.Out_XElEnd(XMLElemName[elSymbols])
```

This code is used in section 585.

File 16

Scanner

588. The `scanner.pas` file contains the *MTokeniser* and the *MScanner*.

It is worth noting: if we want to extend Mizar to support Unicode, then we would want to hack this file accordingly. Or create a `utf8scanner` module, whichever. This scanner class is built specifically to work with ASCII characters, specifically accepting printable characters and the space (“ ”) characters as valid input.

```

<scanner.pas 588> ≡
  <GNU License 4>
unit scanner;
  interface ;
  uses errhan, mobjects;
  const MaxLineLength = 80;
    MaxConstInt = 2147483647; { = 231 - 1, maximal signed 32-bit integer }
  <Type declarations for scanner 589>
  implementation
  uses mizenv, librenv, mconsole, xml_dict, xml_inout;
  <Implementation for scanner.pas 590>
  end .

```

See also section 719.

589. Note that a *LexemRec* is really a standardized token. I was always raised to believe that a “lexeme” refers to the literal text underlying a token.

```

<Type declarations for scanner 589> ≡
type ASCIIArr = array [chr(0) .. chr(255)] of byte;
  LexemRec = record Kind: char;
    Nr: integer;
  end;
  <Token object class 591>;
  <Tokens collection class 593>;
  <MToken object class 601>;
  <MTokeniser class 604>;
  <MScanner object class 632>;

```

This code is used in section 588.

590. The “default allowed” characters are the 10 decimal digits, the 26 uppercase Latin letters, the 26 lowercase Latin letters, and the underscore (“_”) character.

⟨Implementation for scanner.pas 590⟩ ≡
var *DefaultAllowed*: *AsciiArr* =
 (0,
 0,
 0, 1, 0, 0, 0, 1,
 { ‘_’ allowed in identifiers by default! }
 0, 1, 0, 0, 0, 0,
 0,
 0,
 0,
 0,
 0, 0);

See also sections 592, 594, 595, 596, 599, 600, 602, 603, 605, 608, 609, 613, 628, 629, 631, 633, 642, 643, 644, 645, and 646.

This code is used in section 588.

591. Tokens object. A token contains a lexeme, but it extends an *MStr* object.

⟨Token object class 591⟩ ≡
TokenPtr = ↑*TokenObj*;
TokenObj = **object** (*MStrObj*)
fLexem: *LexemRec*;
constructor *Init*(*aKind* : *char*; *aNr* : *integer* ; **const** *aSpelling*: *string*);
end

This code is used in section 589.

592. The constructor for a token requires its kind (functor, mode, predicate, etc.), and its internal “number”, as well as its raw lexeme *aSpelling*.

⟨Implementation for scanner.pas 590⟩ +≡
constructor *TokenObj.Init*(*aKind* : *char*; *aNr* : *integer* ; **const** *aSpelling*: *string*);
begin *fLexem.Kind* ← *aKind*; *fLexem.Nr* ← *aNr*; *fStr* ← *aSpelling*;
end;

Section 16.1. COLLECTIONS OF TOKENS

593. We can populate a token collection from a dictionary file, or we can start with an empty collection. We can save our collection to a file. We can also insert (or “collect”) a new token into the collection.

⟨Tokens collection class 593⟩ ≡

```
TokensCollection = object (MSortedStrList)
  fFirstChar: array [chr(30) .. chr(255)] of integer;
  constructor InitTokens;
  constructor LoadDct(const aDctFileName: string);
  procedure SaveDct(const aDctFileName: string);
  procedure SaveXDct(const aDctFileName: string);
  function CollectToken(const aLexem: LexemRec; const aSpelling: string): boolean;
end
```

This code is used in section 589.

594. Construct empty token collection.

⟨Implementation for scanner.pas 590⟩ +≡

```
constructor TokensCollection.InitTokens;
  begin Init(100);
end;
```

595. Insert. If the collection already contains the token described by *aLexem*, then we just free up the memory allocated for the token (avoid duplicates). Otherwise, we insert the token.

⟨Implementation for scanner.pas 590⟩ +≡

```
function TokensCollection.CollectToken(const aLexem: LexemRec; const aSpelling: string): boolean;
  var k: integer; lToken: TokenPtr;
  begin lToken ← new(TokenPtr, Init(aLexem.Kind, aLexem.Nr, aSpelling));
  if Search(lToken, k) then { already contains token? }
    begin CollectToken ← false; dispose(lToken, Done)
    end
  else begin CollectToken ← true; Insert(lToken)
  end
end;
```

596. Load a dictionary. We open the dictionary “.dct” file (expects the file name to be lacking that extension), and construct an empty token collection. Then we iterate through the dictionary, reading each line, forming a new token, then inserting it into the collection.

The “.dct” file contains all the identifiers from articles referenced in the **environ** part of an article, and it will always have the first 148 lines be for reserved keywords. The format for a “.dct” file consists of lines of the form

$$\langle kind \rangle \langle number \rangle \sqcup \langle name \rangle$$

The “kind” is a single byte, the *number* is an integer assigned for the identifier, and *name* is the lexeme (string literal) for the identifier. This also has an XML file for this same information, the “.dcx” file.

⟨Implementation for scanner.pas 590⟩ +≡

```
constructor TokensCollection.LoadDct(const aDctFileName: string);
  var Dct: text; lKind, lDummy: AnsiChar; lNr: integer; lString: string; i: integer; c: char;
  begin assign(Dct, aDctFileName + ‘.dct’); reset(Dct); InitTokens;
  ⟨Load all tokens from the dictionary 597⟩;
  close(Dct); ⟨Index first character appearances among definitions 598⟩;
end;
```

597. We just iterate through the dictionary, constructing a new token for each line we read.

```

⟨Load all tokens from the dictionary 597⟩ ≡
  while ¬seekEof(Dct) do
    begin readln(Dct, lKind, lNr, lDummy, lString);
           Insert(new(TokenPtr, Init(char(lKind), lNr, lString)));
    end

```

This code is used in section 596.

598. We index the first appearance of each leading character in a token.

```

⟨Index first character appearances among definitions 598⟩ ≡
  for c ← chr(30) to chr(255) do fFirstChar[c] ← -1;
  for i ← 0 to Count - 1 do
    begin c ← TokenPtr(Items↑[fIndex↑[i]]↑.fStr[1];
           if fFirstChar[c] = -1 then fFirstChar[c] ← i;
    end

```

This code is used in section 596.

599. We save a token collection to a “.dct” file. This appears to just produce the concatenation of the definition kind, the identifier number, then a whitespace separating it from the lexeme. **Caution:** this is *not* an XML format! For that, see *SaveDctX*.

```

⟨Implementation for scanner.pas 590⟩ +≡
procedure TokensCollection.SaveDct(const aDctFileName: string);
  var i: integer; DctFile: text;
  begin assign(DctFile, aDctFileName + ‘.dct’); rewrite(DctFile);
  for i ← 0 to Count - 1 do
    with TokenPtr(Items↑[i])↑, fLexem do writeln(DctFile, AnsiChar(Kind), Nr, ‘ ’, fStr);
  close(DctFile);
end;

```

600. Save dictionary to XML file. The RNC (compact Relax NG Schema): Local dictionary for an article. The symbol kinds still use very internal notation.

```

elSymbols =
  attribute atAid {xsd:string}?,
  element elSymbols {
    element elSymbol {
      attribute atKind {xsd:string},
      attribute atNr {xsd:integer},
      attribute atName {xsd:integer}
    }*
  }

```

This creates the .dct file for an article.

⟨Implementation for scanner.pas 590⟩ +≡

```

procedure TokensCollection.SaveXDct(const aDctFileName: string);
var lEnvFile: XMLOutStreamObj; i: integer;
begin lEnvFile.OpenFile(aDctFileName);
with lEnvFile do
  begin Out_XElStart(XMLElemName[elSymbols]); Out_XAttr(XMLAttrName[atAid], ArticleID);
    Out_XQuotedAttr(XMLAttrName[atMizfiles], MizFiles);
    Out_XAttrEnd; { print elSymbols start-tag }
  for i ← 0 to Count − 1 do { print children elSymbol elements }
    with TokenPtr(Items↑[i])↑, fLexem do
      begin Out_XElStart(XMLElemName[elSymbol]);
        Out_XQuotedAttr(XMLAttrName[atKind], Kind); Out_XIntAttr(XMLAttrName[atNr], Nr);
        Out_XQuotedAttr(XMLAttrName[atName], fStr); Out_XElEnd0;
      end;
    Out_XElEnd(XMLElemName[elSymbols]); { print elSymbols end-tag }
  end;
lEnvFile.Done;
end;

```

Section 16.2. MIZAR TOKEN OBJECTS

601. This appears to be tokens for a specific file. An MToken extends a Token (§591).

```

⟨ MToken object class 601 ⟩ ≡
  MTokenPtr = ↑ MTokenObj;
  MTokenObj = object (TokenObj)
    fPos: Position;
    constructor Init(aKind : char; aNr : integer ; const aSpelling: string; const aPos: Position);
  end

```

This code is used in section 589.

602. Constructor. Construct a token. This might be a tad confusing, at least for me, because the lexeme is stored in the *fStr* field, whereas the standardized token is stored in the *fLexem* field.

We do not need to invoke the constructor for any ancestor class, because we just construct everything here. This seems like a bug waiting to happen. . .

```

⟨ Implementation for scanner.pas 590 ⟩ +≡
constructor MTokenObj.Init(aKind : char; aNr : integer;
  const aSpelling: string;
  const aPos: Position);
begin fLexem.Kind ← aKind; fLexem.Nr ← aNr; fStr ← aSpelling; fPos ← aPos;
end;

```

603. Token Kind constants. There are four kinds of tokens we want to distinguish: all valid tokens are either (1) numerals, or (2) identifiers. Then we also have (3) error tokens. But last, we have (4) end of text tokens.

These are for identifying everything which is neither an identifier defined in the vocabulary files, nor a reserved keyword.

```

⟨ Implementation for scanner.pas 590 ⟩ +≡
const Numeral = 'N'; Identifier = 'I'; ErrorSymbol = '?'; EOT = '!';

```

Section 16.3. TOKENISER

604. The first step in lexical analysis is to transform a character stream into a token stream. The Tokeniser extends the MToken object (§601), which in turn extends the Token object (§591).

In particular, we should take a moment to observe the new fields. The *fPhrase* field is a segment of the input stream which is expected to start at a non-whitespace character.

The *SliceIt* function populates the *TokensBuf* and the *fIdents* fields from the *fPhrase* field. I cannot find where *fTokens* is populated.

Note that the MTokeniser is not, itself, used anywhere *directly*. It's extended in the *MScannObj* class, which is used in `base/mscanner.pas` (and in `kernel/envhan.pas`).

The contract for *GetPhrase* ensures the *fPhrase* will be populated with a string ending with a space (“ ”) character or it will be the empty string. Any class extending *MTokeniser* must respect this contract.

⟨ MTokeniser class 604 ⟩ ≡

```

MTokeniser = object (MTokenObj)
  fPhrase: string;
  fPhrasePos: Position;
  fTokensBuf: MCollection;
  fTokens, fIdents: TokensCollection;
  constructor Init;
  destructor Done; virtual;
  procedure SliceIt; virtual;
  procedure GetToken; virtual;
  procedure GetPhrase; virtual;
  function EndOfText: boolean; virtual;
  function IsIdentifierLetter(ch : char): boolean; virtual;
  function IsIdentifierFirstLetter(ch : char): boolean; virtual;
  function Spelling(const aToken: LexemRec): string; virtual;
end

```

This code is used in section 589.

605. Spelling boils down to three cases (c.f., types of tokens §603): numerals, identifiers, and everything else. Numerals spell out the base-10 decimal expansion.

The other two cases boil down to finding the first matching token in the caller's collection of tokens with the same lexeme supplied as an argument, provided certain ‘consistency’ checks hold (the lexeme and token have the same *Kind*).

⟨ Implementation for scanner.pas 590 ⟩ +≡

```

function MTokeniser.Spelling(const aToken: LexemRec): string;
  var i: integer; s: string;
  begin Spelling ← ``;
  if aToken.Kind = Numeral then
    begin Str(aToken.Nr, s); Spelling ← s; end
  else if aToken.Kind = Identifier then ⟨ Spell an identifier for the MTokeniser 606 ⟩
    else ⟨ Spell an error or EOF for the MTokeniser 607 ⟩;
  end;

```

606. Spelling an identifier just needs to match the lexeme's number with the token's number. This finds the first matching token in the underlying collection, then terminates the function.

```

⟨ Spell an identifier for the MTokeniser 606 ⟩ ≡
  begin for  $i \leftarrow 0$  to  $fIdents.Count - 1$  do
    with  $TokenPtr(fIdents.Items \uparrow [i]) \uparrow$  do
      if  $fLexem.Nr = aToken.Nr$  then
        begin  $Spelling \leftarrow fStr$ ; exit
        end;
      end
    end
  end

```

This code is used in section 605.

607. Spelling anything else for the tokeniser needs the kind and number of the lexeme to match those of the token. Again, this finds the first matching token in the underlying collection, then terminates the function.

```

⟨ Spell an error or EOF for the MTokeniser 607 ⟩ ≡
  begin for  $i \leftarrow 0$  to  $fTokens.Count - 1$  do
    with  $TokenPtr(fTokens.Items \uparrow [i]) \uparrow$  do
      if  $(fLexem.Kind = aToken.Kind) \wedge (fLexem.Nr = aToken.Nr)$  then
        begin  $Spelling \leftarrow fStr$ ; exit
        end;
      end
    end
  end

```

This code is used in section 605.

608. Constructor. Initialising a tokeniser starts with a blank phrase and kind, with most fields set to zero.

```

⟨ Implementation for scanner.pas 590 ⟩ +≡
constructor MTokeniser.Init;
  begin  $fPos.Line \leftarrow 0$ ;  $fLexem.Kind \leftarrow \text{`_`}$ ;  $fPhrase \leftarrow \text{`_`}$ ;  $fPhrasePos.Line \leftarrow 0$ ;
     $fPhrasePos.Col \leftarrow 0$ ;  $fTokensBuf.Init(80, 8)$ ;  $fTokens.Init(0)$ ;  $fIdents.Init(100)$ ;
  end;

```

609. Destructor. This chains to free up several fields, just invoking their destructors.

```

⟨ Implementation for scanner.pas 590 ⟩ +≡
destructor MTokeniser.Done;
  begin  $fPhrase \leftarrow \text{``}$ ;  $fTokensBuf.Done$ ;  $fTokens.Done$ ;  $fIdents.Done$ ;
  end;

```


610. Aside on ASCII separators. Note: $\text{chr}(30)$ is the record separator in ASCII, and $\text{chr}(31)$ is the unit separator. Within a group (or table), the records are separated with the “RS” ($\text{chr}(30)$). As far as unit separators, Lammer Bies explains (lammertbies.nl/comm/info/ascii-characters):

The smallest data items to be stored in a database are called units in the ASCII definition. We would call them field now. The unit separator separates these fields in a serial data storage environment. Most current database implementations require that fields of most types have a fixed length. Enough space in the record is allocated to store the largest possible member of each field, even if this is not necessary in most cases. This costs a large amount of space in many situations. The US control code allows all fields to have a variable length. If data storage space is limited—as in the sixties—this is a good way to preserve valuable space. On the other hand is serial storage far less efficient than the table driven RAM and disk implementations of modern times. I can’t imagine a situation where modern SQL databases are run with the data stored on paper tape or magnetic reels...

We will introduce macros for the record separator and the unit separator, because Mizar’s front-end uses them specifically for the following purposes:

- (1) lines longer than 80 characters will contain a *record_separator* character (§637);
- (2) all other invalid characters are replaced with the *unit_separator* character (c.f., §638).

define *record_separator* $\equiv \text{chr}(30)$

define *unit_separator* $\equiv \text{chr}(31)$

611. Example of zeroeth step (“getting a phrase”) in tokenising. The *GetPhrase* function is left as an abstract method of the tokeniser, so it is worth discussing “What it is supposed to do” before getting to the tokenisation of strings.

Suppose we have the following snippet of Mizar:

```
begin

theorem
  for x being object
    holds x= x;
```

This is “sliced up” into the following “phrases” (drawn in boxes) which are clustered by lines:

```
begin_
theorem_
  for_ x_ being_ object_
  holds_ x=_ x_;
```

Observe that the “phrases” are demarcated by whitespaces (“_␣”) or linebreaks. This is the coarse “first pass” before we carve a “phrase” up into a token. A phrase contains at least one token, possibly multiple tokens (e.g., the phrase “x=_” contains the two tokens “x” and “=”).

What is the contract for a “phrase”? A phrase is *guaranteed* to either be equal to “_␣”, or it contains at least one token and it is *guaranteed* to end with a space “_␣” character (ASCII code #32). Further, there are no other possible “_␣” characters in a phrase *except* at the very end. A phrase is never an empty string.

The task is then to *slice up* each phrase into tokens.

612. Tokenise a phrase. When a “phrase” has been loaded into the tokeniser (which is an abstract method implemented by its descendent classes), we tokenise it — “slice it up” into tokens, thereby populating the *fTokensBuf* tokens buffer. This is invoked as needed by the *GetToken* method (§629).

This function is superficially complex, but upon closer scrutiny it is fairly straightforward.

Also note, despite being marked as “virtual”, this is not overridden anywhere in the Mizar program.

The contract ensures, barring catastrophe, the *fLexem*, *fStr*, and *fPos* be populated. **Importantly:** The *fLexem*’s token type is one of the four kinds given in the constant section (§603): **Numeral**, **Identifier**, **ErrorSymbol**, or **EOT**. What about the “reserved keywords” of Mizar? They are already present in the “.dct” file, which is loaded into the *fTokens* dictionary. So they will be discovered in step (§619) in this procedure.

```

⟨ Variables for slicing a phrase 612 ⟩ ≡
lCurrChar: integer; { index in fPhrase for current position }
EndOfSymbol: integer;
EndOfIdent: integer; { index in fPhrase for end of identifier }
FoundToken: TokenPtr; { most recently found token temporary variable }
lPos: Position; { position for debugging purposes }

```

See also sections 615, 618, 621, 623, and 625.

This code is used in section 613.

613. ⟨ Implementation for scanner.pas 590 ⟩ +≡

```

procedure MTokeniser.SliceIt;
  var ⟨ Variables for slicing a phrase 612 ⟩
  begin MizAssert(2333, fTokensBuf.Count = 0); { Requires: token buffer is empty }
  lCurrChar ← 1; lPos ← fPhrasePos;
  ⟨ Slice pragmas 614 ⟩;
  while fPhrase[lCurrChar] ≠ ‘␣’ do
    begin ⟨ Determine the ID 616 ⟩;
    ⟨ Try to find a dictionary symbol 619 ⟩;
    if EndOfSymbol < EndOfIdent then ⟨ Check identifier is not a number 622 ⟩;
    if FoundToken ≠ nil then
      with FoundToken↑ do
        begin lPos.Col ← fPhrasePos.Col + EndOfSymbol - 1;
        fTokensBuf.Insert(new(MTokenPtr, Init(fLexem.Kind, fLexem.Nr, fStr, lPos)));
        lCurrChar ← EndOfSymbol + 1; continue;
        end;
      { else FoundToken = nil }
    ⟨ Whoops! We found an unknown token, insert a 203 error token 627 ⟩;
    end;
  end;

```

614. We begin by slicing pragmas. This will insert the pragma into the tokens buffer.

Note that the “\$EOF” pragma indicates that we should treat the file as ending here. So we comply with the request, inserting the *EOT* (end of text) token as the next token to be offered to the user.

```

⟨ Slice pragmas 614 ⟩ ≡
if (lPos.Col = 1) ∧ (Pos(‘:’:$’, fPhrase) = 1) then
  begin fTokensBuf.Insert(new(MTokenPtr, Init(‘␣’, 0, copy(fPhrase, 3, length(fPhrase) - 3), lPos)));
  if copy(fPhrase, 1, 6) = ‘:’:$EOF’ then
    fTokensBuf.Insert(new(MTokenPtr, Init(EOT, 0, fPhrase, lPos)));
  exit
  end

```

This code is used in section 613.

615. We take the longest possible substring consisting of identifier characters as a possible identifier. The phrase is guaranteed to contain at least one token, maybe more, so we just keep going until we have exhausted the phrase or found a non-identifier character.

Note that all invalid characters are transformed into the “unit character” (c.f., §638). We should treat any occurrence of them as an error.

At the end of this stage of our tokenising journey, for valid tokens, we should have *EndOfIdent* and *IdentLength* both initialized here.

⟨ Variables for slicing a phrase 612 ⟩ +≡
IdentLength: *integer*;

616. ⟨ Determine the ID 616 ⟩ ≡
 { 1. attempt to determine the ID }
EndOfIdent ← *lCurrChar*;
if *IsIdentifierFirstLetter*(*fPhrase*[*EndOfIdent*]) **then**
 while (*EndOfIdent* < *length*(*fPhrase*)) ∧ *IsIdentifierLetter*(*fPhrase*[*EndOfIdent*]) **do**
 inc(*EndOfIdent*);
IdentLength ← *EndOfIdent* − *lCurrChar*;
if *fPhrase*[*EndOfIdent*] ≤ *unit_separator* **then**
 ⟨ Whoops! ID turns out to be invalid, insert an error token, then continue 617 ⟩;
 dec(*EndOfIdent*)

This code is used in section 613.

617. Recall (§637), we treat record separators as indicating the line is “too long” (i.e., more than 80 characters long). So we insert a 201 “Too long source line” error. But anything else is treated as an invalid identifier error.

⟨ Whoops! ID turns out to be invalid, insert an error token, then continue 617 ⟩ ≡
begin *lPos.Col* ← *fPhrasePos.Col* + *EndOfIdent* − 1;
if *fPhrase*[*EndOfIdent*] = *record_separator* **then**
 fTokensBuf.Insert(*new*(*MTokenPtr*, *Init*(*ErrorSymbol*, 200, ‘^’, *lPos*)))
else *fTokensBuf.Insert*(*new*(*MTokenPtr*, *Init*(*ErrorSymbol*, 201, ‘^’, *lPos*)));
 lCurrChar ← *EndOfIdent* + 1; *continue*;
end

This code is used in section 616.

618. We look at the current phrase and try to match against tokens found in the underlying dictionary. When we find a match, we check if there are *multiple* matches and return the last one (this reflects Mizar’s “the last version of the notation is preferred”). We implement this matching scheme using an infinite loop. Note that this uses a “**repeat...until false**” loop, which is identical to “**while true do begin ...end**” loop. (I am tempted to introduce a macro just to have this loop “**repeat...until end_of_time**”...)

Recall (§250), sorted lists have a field *fIndex* which is an array of indices (which are sorted while leaving the underlying array *Items* of data untouched).

Also, *lToken*, *lIndex* are used only in this code chunk. Here *lToken* is translated to an index of the underlying dictionary, so for clarity we introduce a macro to refer to the token directly. And *lIndex* is used as “the current character” index to compare the phrase to the token (indexed by *lToken*) as a match or not.

At the end of this chunk, if successful, then *FoundToken* will be set to a valid token pointer. Further, *EndOfPhrase* will be initialized.

A possible bug: what happens if we look through the entire phrase? We can’t “look any farther” down the phrase, so shouldn’t we throw an error? Or lazily read more characters? Or...something?

Never fear: this will never happen with Mizar’s grammar. The “reserved words” are *always* separated from the other stuff by at least one whitespace.

Also we note the list of symbols is sorted lexicographically.

This appears to match the phrase with the longest possible matching entry in the list of symbols (it is “maximal munch”).

```
define the_item(#)  $\equiv$  Items $\uparrow$ [fIndex $\uparrow$ [#]]
define the_token(#)  $\equiv$  TokenPtr(the_item(#)) $\uparrow$ 
```

⟨ Variables for slicing a phrase 612 ⟩ +≡

EndOfPhrase: integer; { index in *fPhrase* for candidate token }

lIndex: integer; { index for *fIndex* entry }

lToken: integer; { index for entries in dictionary starting with the first character of the current token }

619. Reserved keywords and defined terms are loaded into the *fTokens* dictionary.

⟨ Try to find a dictionary symbol 619 ⟩ ≡

```
EndOfPhrase  $\leftarrow$  lCurrChar; FoundToken  $\leftarrow$  nil; EndOfSymbol  $\leftarrow$  EndOfPhrase - 1;
{ initialized for comparison }
```

```
lToken  $\leftarrow$  fTokens.fFirstChar[fPhrase[EndOfPhrase]]; inc(EndOfPhrase);
```

```
if (lToken  $\geq$  0) then
```

```
  with fTokens do
```

```
    begin lIndex  $\leftarrow$  2;
```

```
    repeat { infinite loop }
```

```
      ⟨ If we matched a dictionary entry, then initialize FoundToken 620 ⟩;
```

```
      if fPhrase[EndOfPhrase] = ‘_’ then break; { we are done! }
```

```
      if (lIndex  $\leq$  length(the_token(lToken).fStr))  $\wedge$ 
```

```
        (the_token(lToken).fStr[lIndex] = fPhrase[EndOfPhrase]) then
```

```
        begin inc(lIndex); inc(EndOfPhrase) end { iterate, look at next character }
```

```
      else if (lToken < Count - 1) then { try looking for the last matching item }
```

```
        begin if (copy(the_token(lToken).fStr, 1, lIndex - 1) =
```

```
          copy(the_token(lToken + 1).fStr, 1, lIndex - 1)) then inc(lToken) { iterate }
```

```
        else break; { we are done! }
```

```
        end
```

```
      else break; { we are done! }
```

```
    until false;
```

```
  end
```

This code is used in section 613.

620. If we have *lIndex* (the index of the current phrase) be longer than the lexeme of the current dictionary entry's lexeme, then we should populate *FoundItem*.

```

⟨ If we matched a dictionary entry, then initialize FoundToken 620 ⟩ ≡
  if lIndex > length(the_token(lToken).fStr) then { we matched the token }
    begin FoundToken ← the_item(lToken); EndOfSymbol ← EndOfPhrase − 1;
    end

```

This code is used in section 619.

621. When the identifier is not a number, we insert an “identifier” token into the tokens buffer.

```

⟨ Variables for slicing a phrase 612 ⟩ +≡
lFailed: integer; { index of first non-digit character }
I: integer; { index ranging over the raw lexeme string }
lSpelling: string; { raw lexeme as a string }

```

```

622. ⟨ Check identifier is not a number 622 ⟩ ≡
  begin lSpelling ← copy(fPhrase, lCurrChar, IdentLength);
  lPos.Col ← fPhrasePos.Col + EndOfIdent − 1;
  if (ord(fPhrase[lCurrChar]) > ord(ˆ0ˆ)) ∧ (ord(fPhrase[lCurrChar]) ≤ ord(ˆ9ˆ)) then
    begin lFailed ← 0; { location of non-digit character }
    for I ← 1 to IdentLength − 1 do
      if (ord(fPhrase[lCurrChar + I]) < ord(ˆ0ˆ)) ∨ (ord(fPhrase[lCurrChar + I]) > ord(ˆ9ˆ)) then
        begin lFailed ← I + 1; break;
        end;
      if lFailed = 0 then { if all characters are digits }
        ⟨ Whoops! Identifier turned out to be a number! 626 ⟩;
      end;
    ⟨ Add token to tokens buffer and iterate 624 ⟩;
  end

```

This code is used in section 613.

623. We add an *Identifier* token to the tokens buffer.

```

⟨ Variables for slicing a phrase 612 ⟩ +≡
lIdent: TokenPtr;

```

```

624. ⟨ Add token to tokens buffer and iterate 624 ⟩ ≡
  lIdent ← new(TokenPtr, Init(Identifier, fIdents.Count + 1, lSpelling));
  if fIdents.Search(lIdent, I) then dispose(lIdent, Done)
  else fIdents.Insert(lIdent);
  fTokensBuf.Insert(new(MTokenPtr, Init(Identifier, TokenPtr(fIdents.Items↑[I])↑.fLexem.Nr, lSpelling, lPos)));
  lCurrChar ← EndOfIdent + 1; continue

```

This code is used in section 622.

625. If we goofed and all the characters turned out to be digits (i.e., the identifier *was* a numeral after all), we should clean things up here. Observe we will end up *continue*-ing along the loop.

When the numeral token is larger than $MaxConstInt = 2^{31} - 1$ (the largest 32-bit integer, §588), then we should raise a “Too large numeral” 202 error token. If we wanted to support “arbitrary precision” numbers, then this should be modified.

We can either insert into the tokens buffer an error token (in two possible outcomes) or a numeral token (in the third possible outcome).

⟨ Variables for slicing a phrase 612 ⟩ +≡
lNumber: *longint*;
J: *integer*;

626. ⟨ Whoops! Identifier turned out to be a number! 626 ⟩ ≡
begin if *IdentLength* > *length(IntToStr(MaxConstInt))* **then** { insert error token }
 begin *fTokensBuf.Insert(new(MTokenPtr, Init(ErrorSymbol, 202, lSpelling, lPos)))*;
 lCurrChar ← *EndOfIdent* + 1; *continue*;
 end;
lNumber ← 0; *J* ← 1;
for *I* ← *IdentLength* − 1 **downto** 0 **do**
 begin *lNumber* ← *lNumber* + (*ord(fPhrase[lCurrChar + I])* − *ord('0')*) * *J*; *J* ← *J* * 10;
 end;
if *lNumber* > *MaxConstInt* **then** { insert error token }
 begin *fTokensBuf.Insert(new(MTokenPtr, Init(ErrorSymbol, 202, lSpelling, lPos)))*;
 lCurrChar ← *EndOfIdent* + 1; *continue*;
 end; { insert numeral token }
 fTokensBuf.Insert(new(MTokenPtr, Init(Numeral, lNumber, lSpelling, lPos)));
 lCurrChar ← *EndOfIdent* + 1; *continue*;
end

This code is used in section 622.

627. If we have tokenised the phrase, but the token is not contained in the dictionary, then we should raise a 203 error.

⟨ Whoops! We found an unknown token, insert a 203 error token 627 ⟩ ≡
 lPos.Col ← *fPhrasePos.Col* + *lCurrChar* − 1;
 fTokensBuf.Insert(new(MTokenPtr, Init(ErrorSymbol, 203, fPhrase[lCurrChar], lPos))); *inc(lCurrChar)*

This code is used in section 613.

628. We have purely abstract methods which will invoke *Abstract1* (§183), which raises a runtime error.

⟨ Implementation for scanner.pas 590 ⟩ +≡
procedure *MTokeniser.GetPhrase*;
 begin *Abstract1*;
 end;
function *MTokeniser.EndOfText*: *boolean*;
 begin *Abstract1*; *EndOfText* ← *false*;
 end;
function *MTokeniser.IsIdentifierLetter*(*ch* : *char*): *boolean*;
 begin *Abstract1*; *IsIdentifierLetter* ← *false*;
 end;

629. Get a token. Getting a token from the tokeniser will check if we’ve exhausted the input stream (which tests if the kind of *fLexem* is *EOT*), and exit if we have.

Otherwise, it looks to see if we’ve got tokens left in the buffer. If so, just pop one and exit.

But when the token buffer is empty, we invoke the abstract method *GetPhrase* to read some of the input stream. If it turns out there’s nothing left to read, then update the tokeniser to be in the “end of text” state.

When we have some of the input stream read into the *fPhrase* field, we tokenise it using the *SliceIt* function. Then we pop a token from the buffer of tokens.

This will populate *fLexem*, *fStr*, and *fPos* with the new token, lexeme, and position...but that’s only because *GetPhrase* (§633) and *SliceIt* (§612) do the actual work.

⟨Implementation for scanner.pas 590⟩ +≡

```

procedure MTokeniser.GetToken;
  begin if fLexem.Kind = EOT then exit;
  if fTokensBuf.Count > 0 then
    begin ⟨Pop a token from the underlying tokens stack 630⟩;
    exit;
    end;
  GetPhrase;
  if EndOfText then
    begin fLexem.Kind ← EOT; fStr ← ‘ ’; fPos ← fPhrasePos; inc(fPos.Col);
    exit;
    end;
  SliceIt; ⟨Pop a token from the underlying tokens stack 630⟩;
end;

```

630. Popping a token will update the lexeme, str, and position fields to be populated from the first item in the tokens buffer. Then it will free that item from the tokens buffer, shifting everything down by one.

⟨Pop a token from the underlying tokens stack 630⟩ ≡

```

fLexem ← MTokenPtr(fTokensBuf.Items↑[0])↑.fLexem;
fStr ← MTokenPtr(fTokensBuf.Items↑[0])↑.fStr; fPos ← MTokenPtr(fTokensBuf.Items↑[0])↑.fPos;
fTokensBuf.AtFree(0)

```

This code is used in sections 629 and 629.

631. Testing if the given character is an identifier character or not requires invoking the abstract method *IsIdentifierLetter* (§628).

⟨Implementation for scanner.pas 590⟩ +≡

```

function MTokeniser.IsIdentifierFirstLetter(ch : char): boolean;
  begin IsIdentifierFirstLetter ← IsIdentifierLetter(ch);
  end;

```

Section 16.4. SCANNER OBJECT

632. This extends the Tokeniser class (§604). It is the only class extending the Tokeniser class.

```

⟨ MScanner object class 632 ⟩ ≡
  MScannPtr = ↑MScannObj;
  MScannObj = object (MTokeniser)
    Allowed: ASCIIArr;
    fSourceBuff: pointer;
    fSourceBuffSize: word;
    fSourceFile: text;
    fCurrentLine: string;
    constructor InitScanning(const aFileName, aDctFileName: string);
    destructor Done; virtual;
    procedure GetPhrase; virtual;
    procedure ProcessComment(fLine, fStart : integer; cmt : string); virtual;
    function EndOfText: boolean; virtual;
    function IsIdentifierLetter(ch : char): boolean; virtual;
  end

```

This code is used in section 589.

633. Get a phrase. We search through the lines for the “first phrase” (i.e., first non-whitespace character, which indicates the start of something interesting). Comments are thrown away as are Mizar pragmas.

This will update *fCurrentLine* as needed, setting it to the next line in the input stream buffer. It will assign a *copy* of the phrase to the field *fPhrase*, as well as update the *fPhrasePos*.

There is a comment in Polish, “uzyskanie pierwszego znaczącego znaku”, which Google translates as: “obtaining the first significant sign”. This seemed like a natural “chunk” of code to study in isolation.

The contract for *GetPhrase* ensures the *fPhrase* will be populated with a string ending with a space (“`␣`”) character, or it will be the empty string (when the end of text has been encountered).

```

⟨ Implementation for scanner.pas 590 ⟩ +≡
procedure MScannObj.GetPhrase;
  const Prohibited: ASCIIArr = ⟨ Characters prohibited by MScanner 634 ⟩;
  var i, k: integer;
  begin fPhrasePos.Col ← fPhrasePos.Col + length(fPhrase) - 1;
  ⟨ Find the first significant ‘sign’ 635 ⟩;
  for i ← fPhrasePos.Col to length(fCurrentLine) do
    if fCurrentLine[i] = ‘␣’ then break;
  fPhrase ← Copy(fCurrentLine, fPhrasePos.Col, i - fPhrasePos.Col + 1);
  end;

```


634. The prohibited ASCII characters are everything *NOT* among the follow characters:

```

␣ ! " # $ % & ' ( ) * + , - . / : ; < = > ? @
[ \ ] ^ _ ` { | } ~ 0 1 2 3 4 5 6 7 8 9
A B C D E F G H I J K L M N O P Q R S T U V W X Y Z
a b c d e f g h i j k l m n o p q r s t u v w x y z

```

The reader will observe these are all the “graphic” ASCII characters, plus the space (“␣”) character.

⟨ Characters prohibited by *MScanner* 634 ⟩ ≡

```

(1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1,
1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,
1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,
1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,
1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,
1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1)

```

This code is used in section 633.

635. Note that the *fCurrentLine* will end with a whitespace, when we have not consumed the entire underlying input stream.

⟨ Find the first significant ‘sign’ 635 ⟩ ≡

```

while fCurrentLine[fPhrasePos.Col] = “␣” do
  begin if fPhrasePos.Col ≥ length(fCurrentLine) then ⟨ Populate the current line 636 ⟩;
  inc(fPhrasePos.Col);
end

```

This code is used in section 633.

636. Now, populating the current line requires a bit of work. We ensure the end of the current line will end with a space character (“␣”), which will guarantee the loop iteratively consumes all empty lines in the file.

Once we arrive at a non-space character, we will break the loop containing this chunk of code. If we have exhausted the underlying input stream, then we will have *EndOfText* be true. Should that occur, we exit the function.

⟨ Populate the current line 636 ⟩ ≡

```

begin if EndOfText then exit;
inc(fPos.Line); inc(fPhrasePos.Line); readln(fSourceFile, fCurrentLine);
⟨ Scan for pragmas, and exit if we found one 640 ⟩;
⟨ Skip comments 641 ⟩;
⟨ Trim whitespace from the right of the current line 639 ⟩;
⟨ Replace every invalid character in current line with the unit character 638 ⟩;
fCurrentLine ← fCurrentLine + “␣”;
if ¬LongLines then
  if length(fCurrentLine) > MaxLineLength then ⟨ Replace end of long line with record separator 637 ⟩;
  { Assert: we have fCurrentLine end in “␣” }
  fPhrasePos.Col ← 0; fPos.Col ← 0;
end

```

This code is used in section 635.

637. When we have excessively long lines, and we have not enabled “long line mode”, then we just delete everything after $MaxLineLength + 1$ and set $MaxLineLength - 1$ to the record separator (which is rejected by the Mizar lexer) and the last character in the line to the space character.

⟨ Replace end of long line with record separator 637 ⟩ \equiv
begin *delete*(*fCurrentLine*, $MaxLineLength + 1$, $length(fCurrentLine)$);
fCurrentLine[$MaxLineLength - 1$] \leftarrow *record_separator*;
fCurrentLine[$MaxLineLength$] \leftarrow ‘ \sqcup ’;
end

This code is used in section 636.

638. In particular, if we every encounter an “invalid” character, then we just replace it with the “unit separator” character.

⟨ Replace every invalid character in current line with the unit character 638 ⟩ \equiv
for $k \leftarrow 1$ **to** $length(fCurrentLine) - 1$ **do**
 if *Prohibited*[*fCurrentLine*[k]] > 0 **then** *fCurrentLine*[k] \leftarrow *unit_separator*

This code is used in section 636.

639. We will trim whitespace from the right of the current line at least twice.

⟨ Trim whitespace from the right of the current line 639 ⟩ \equiv
 $k \leftarrow length(fCurrentLine)$;
while ($k > 0$) \wedge (*fCurrentLine*[k] = ‘ \sqcup ’) **do** *dec*(k);
 delete(*fCurrentLine*, $k + 1$, $length(fCurrentLine)$)

This code is used in sections 636 and 640.

640. Pragmas in Mizar are special comments which start a line with “ $::\$$ ”. They are useful for naming theorems (“ $::\$N \langle name \rangle$ ”), or toggling certain phases of the Mizar checker. This will process the comment (§642).

Since pragmas are important, we treat it as a token (and not a comment to be thrown away).

Note: if you try to invoke a pragma, but do not place it at the start of a line, then Mizar will treat it like a comment.

⟨ Scan for pragmas, and exit if we found one 640 ⟩ \equiv
 $k \leftarrow Pos('::\$', fCurrentLine)$; { Preprocessing directive }
if ($k = 1$) **then**
 begin *ProcessComment*(*fPhrasePos.Line*, 1, *copy*(*fCurrentLine*, 1, $length(fCurrentLine)$));
 ⟨ Trim whitespace from the right of the current line 639 ⟩;
 fCurrentLine \leftarrow *fCurrentLine* + ‘ \sqcup ’; *fPhrase* \leftarrow *Copy*(*fCurrentLine*, 1, $length(fCurrentLine)$);
 fPhrasePos.Col \leftarrow 1; *fPos.Col* \leftarrow 0; *exit*
 end

This code is used in section 636.

641. Scanning a comment will effectively replace the start of the comment (“ $::$ ”) up to and including the end of the line, with a single space. This will process the comment (§642).

⟨ Skip comments 641 ⟩ \equiv
 $k \leftarrow Pos('::', fCurrentLine)$; { Comment }
if ($k \neq 0$) **then**
 begin *ProcessComment*(*fPhrasePos.Line*, k , *copy*(*fCurrentLine*, k , $length(fCurrentLine)$));
 delete(*fCurrentLine*, $k + 1$, $length(fCurrentLine)$); *fCurrentLine*[k] \leftarrow ‘ \sqcup ’;
 end

This code is used in section 636.

642. “Processing a comment” really means skipping the comment.

⟨Implementation for scanner.pas 590⟩ +≡

```
procedure MScannObj.ProcessComment(fLine, fStart : integer; cmt : string);
begin end;
```

643. Testing if the scanner has exhausted the input stream amounts to checking the current line has been completely read *and* the current source file has arrived at an *texttfeof* state.

⟨Implementation for scanner.pas 590⟩ +≡

```
function MScannObj.EndOfText: boolean;
begin EndOfText ← (fPhrasePos.Col ≥ length(fCurrentLine)) ∧ eof(fSourceFile);
end;
```

644. Testing if a character is an identifier letter amounts to testing if it is allowed (i.e., not disallowed).

⟨Implementation for scanner.pas 590⟩ +≡

```
function MScannObj.IsIdentifierLetter(ch : char): boolean;
begin IsIdentifierLetter ← Allowed[ch] ≠ 0;
end;
```

645. Constructor. The only way to construct a scanner. This expects an article to be read in *aFileName* and a dictionary to be loaded (*aDctFileName*, loaded with §596). The buffer size for reading *aFileName* is initially #4000.

⟨Implementation for scanner.pas 590⟩ +≡

```
constructor MScannObj.InitScanning(const aFileName, aDctFileName: string);
begin inherited Init; Allowed ← DefaultAllowed; fTokens.LoadDct(aDctFileName);
  assign(fSourceFile, aFileName); fSourceBuffSize ← #4000; getmem(fSourceBuff, fSourceBuffSize);
  settextbuf(fSourceFile, fSourceBuff↑, #4000); reset(fSourceFile); fCurrentLine ← ‘ ’; GetToken;
end;
```

646. Destructor. We must remember to close the source file, free the buffer, close the lights, and lock the doors.

⟨Implementation for scanner.pas 590⟩ +≡

```
destructor MScannObj.Done;
begin close(fSourceFile); FreeMem(fSourceBuff, fSourceBuffSize); fCurrentLine ← ‘ ’; inherited Done;
end;
```

File 17

Format

647. The first step towards disambiguating the meaning of identifiers is to use “formats”. Recall from, e.g., Andrzej Trybulec’s “Some Features of the Mizar Language” (ESPRIT Workshop, Torino, 1993; mizar.uwb.edu.pl/project/t §3) that the “Format” describes with how many arguments a “Constructor Symbol” may be used. The basic formats:

- Predicates $\langle \text{lexeme}, \text{left arguments number}, \text{right arguments number} \rangle$
- Modes $\langle \text{lexeme}, \text{arguments number} \rangle$ for “mode Foo of T_1, \dots, T_n ” where n is the arguments number
- Functors $\langle \text{lexeme}, \text{left arguments number}, \text{right arguments number} \rangle$
- Bracket functors $\langle \text{left bracket lexeme}, \text{arguments number}, \text{right bracket lexeme} \rangle$
- Selector $\langle \text{lexeme}, 1 \rangle$
- Structure $\langle \text{lexeme}, \text{arguments number} \rangle$ for generic structures over $[\text{arguments number}]$ parameters
- Structure $\langle \text{lexeme}, 1 \rangle$ for situations where we write “the [structure] of [term]”

We store these format information in XML files. See also Adam Grabowski, Artur Korniłowicz, and Adam Naumowicz’s “Mizar in a Nutshell” (viz. §2.3, [doi:10.6092/issn.1972-5787/1980](https://doi.org/10.6092/issn.1972-5787/1980)) for a little more discussion about formats.

```

<_format.pas 647> ≡
  <GNU License 4>
unit _formats;
interface
  uses mobjects, scanner, dictan, xml_inout;
  <Declare classes for _formats.pas 649>
  function CompareFormats(aItem1, aItem2 : Pointer): Integer;
  function In_Format(fInFile : XMLInStreamPtr): MFormatPtr;
  <Global variables (_formats.pas) 648>
implementation
  uses errhan, xml_dict, xml_parser
    mdebug, info end mdebug;
  <Implementation for _formats.pas 650>
end .

```

648.

```

<Global variables (_formats.pas) 648> ≡
var gFormatsColl: MFormatsList; gPriority: BinIntFunc; gFormatsBase: integer;

```

This code is used in section 647.

649. Broadly speaking, there are only 3 types of “formats”: prefix formats, infix formats, bracket-like formats. These are viewed as “subclasses” of a base *MFormat* object.

We will want to collect the formats from articles referenced by the environment of an article being verified or parsed. This motivates the *MFormatList* object.

```

⟨ Declare classes for _formats.pas 649 ⟩ ≡
  ⟨ Declare MFormat object 651 ⟩;
  { TODO: add assertions that nr. of all format arguments is equal to the number of visible args
    (Visible) of a pattern }
  ⟨ Declare MPrefixFormat object 653 ⟩;
  ⟨ Declare MInfixFormat object 655 ⟩;
  ⟨ Declare MBracketFormat object 657 ⟩;
  ⟨ Declare MFormatsList object 665 ⟩;

```

This code is used in section 647.

650. The *presentation* of the code is a bit disorganized from the perspective of pedagogy, so I am going to re-organize for the sake of discussing it.

```

⟨ Implementation for _formats.pas 650 ⟩ ≡
  ⟨ Constructors for derived format classes 652 ⟩
  ⟨ Compare formats 659 ⟩
  ⟨ Implementation for MFormatsList 666 ⟩
  ⟨ Read formats from an XML input stream 677 ⟩
  ⟨ Implement MFormatObj 678 ⟩

```

This code is used in section 647.

651. Format base class. All format instances have a lexeme called its *fSymbol*. Recall that *LexemeRec* (§589) is a normalized token using a single character to describe its kind, and an integer to keep track of it (instead of relying on a raw string).

```

⟨ Declare MFormat object 651 ⟩ ≡
  MFormatPtr = ↑MFormatObj;
  MFormatObj = object (MObject)
    fSymbol: LexemeRec;
    constructor Init(aKind : Char; aSymNr : integer);
    procedure Out_Format(var fOutFile : XMLOutputStreamObj; aFormNr : integer);
  end

```

This code is used in section 649.

652. The constructor expects the “kind” of the object and its symbol number.

```

⟨ Constructors for derived format classes 652 ⟩ ≡
constructor MFormatObj.Init(aKind : Char; aSymNr : integer);
  begin fSymbol.Kind ← aKind; fSymbol.Nr ← aSymNr;
  end;

```

See also sections 654, 656, and 658.

This code is used in section 650.

653. Prefix format object.

```

⟨ Declare MPrefixFormat object 653 ⟩ ≡
  MPrefixFormatPtr = ↑MPrefixFormatObj;
  MPrefixFormatObj = object (MFormatObj)
    fRightArgsNbr: byte;
    constructor Init(aKind : Char; aSymNr, aRArgsNbr : integer);
  end

```

This code is used in section 649.

654. Prefix formats track how many arguments are to the right of the prefix symbol.

```

⟨ Constructors for derived format classess 652 ⟩ +≡
constructor MPrefixFormatObj.Init(aKind : Char; aSymNr, aRArgsNbr : integer);
  begin fSymbol.Kind ← aKind; fSymbol.Nr ← aSymNr; fRightArgsNbr ← aRArgsNbr;
  end;

```

655. Infix format object.

```

⟨ Declare MInfixFormat object 655 ⟩ ≡
  MInfixFormatPtr = ↑MInfixFormatObj;
  MInfixFormatObj = object (MPrefixFormatObj)
    fLeftArgsNbr: byte;
    constructor Init(aKind : Char; aSymNr, aLArgsNbr, aRArgsNbr : integer);
  end

```

This code is used in section 649.

656. And just as prefix symbols tracks the number of arguments to the right, infix symbols tracks the number of arguments to both the left and right.

```

⟨ Constructors for derived format classess 652 ⟩ +≡
constructor MInfixFormatObj.Init(aKind : Char; aSymNr, aLArgsNbr, aRArgsNbr : integer);
  begin fSymbol.Kind ← aKind; fSymbol.Nr ← aSymNr; fLeftArgsNbr ← aLArgsNbr;
  fRightArgsNbr ← aRArgsNbr;
  end;

```

657. Bracket format object.

```

⟨ Declare MBracketFormat object 657 ⟩ ≡
  MBracketFormatPtr = ↑MBracketFormatObj;
  MBracketFormatObj = object (MInfixFormatObj)
    fRightSymbolNr: integer;
    fArgsNbr: byte;
    constructor Init(aLSymNr, aRSymNr, aArgsNbr, aLArgsNbr, aRArgsNbr : integer);
  end

```

This code is used in section 649.

```

658.    ⟨ Constructors for derived format classess 652 ⟩ +≡
constructor MBracketFormatObj.Init(aLSymNr, aRSymNr, aArgsNbr, aLArgsNbr, aRArgsNbr : integer);
  begin fSymbol.Kind ← 'K'; fSymbol.Nr ← aLSymNr; fRightSymbolNr ← aRSymNr;
  fArgsNbr ← aArgsNbr; fLeftArgsNbr ← aLArgsNbr; fRightArgsNbr ← aRArgsNbr;
  end;

```

659. Ordering format objects. We need a *Compare* ordering function on formats. This is a lexicographic ordering on the (kind, number of right symbols, number of arguments, number of left symbols), more or less.

```

⟨ Compare formats 659 ⟩ ≡
function CompareFormats(aItem1, aItem2 : Pointer): Integer;
  begin CompareFormats ← 1;
  if MFormatPtr(aItem1)↑.fSymbol.Kind < MFormatPtr(aItem2)↑.fSymbol.Kind then
    CompareFormats ← -1
  else if MFormatPtr(aItem1)↑.fSymbol.Kind = MFormatPtr(aItem2)↑.fSymbol.Kind then
    ⟨ Compare symbols of the same kind 660 ⟩;
  end;

```

This code is used in section 650.

660. We then check the indexing number of the symbol. When they are the same, we look at the next “entry” in the tuple.

```

⟨ Compare symbols of the same kind 660 ⟩ ≡
  if MFormatPtr(aItem1)↑.fSymbol.Nr < MFormatPtr(aItem2)↑.fSymbol.Nr then
    CompareFormats ← -1
  else if MFormatPtr(aItem1)↑.fSymbol.Nr = MFormatPtr(aItem2)↑.fSymbol.Nr then
    ⟨ Compare same kinded symbols with the same number 661 ⟩

```

This code is used in section 659.

661. The next “entry” in the tuple depends on the kind of symbols we are comparing. Selectors (‘U’) are, at this point, identical (so we return zero). Note that ‘J’ is a historic artifact no longer used (in fact, I cannot locate its meaning in the literature I possess).

Structure (‘G’), right functor brackets (‘L’), modes (‘M’), and attributes (‘V’) can be compared as prefix symbols.

Functors (‘O’) and predicates (‘R’) can be compared as infix symbols.

Left functor brackets (‘K’) can be compared first with bracket-specific characteristics, then as infix symbols.

```

⟨ Compare same kinded symbols with the same number 661 ⟩ ≡
  case MFormatPtr(aItem1)↑.fSymbol.Kind of
    ‘J’, ‘U’: CompareFormats ← 0;
    ‘G’, ‘L’, ‘M’, ‘V’: ⟨ Compare prefix symbols 662 ⟩;
    ‘O’, ‘R’: ⟨ Compare infix symbols 664 ⟩;
    ‘K’: ⟨ Compare bracket symbols 663 ⟩;
  endcases

```

This code is used in section 660.

662. Comparing prefixing symbols, at this points, can only compare the number of arguments to the right.

```

⟨ Compare prefix symbols 662 ⟩ ≡
  if MPrefixFormatPtr(aItem1)↑.fRightArgsNbr < MPrefixFormatPtr(aItem2)↑.fRightArgsNbr then
    CompareFormats ← -1
  else if MPrefixFormatPtr(aItem1)↑.fRightArgsNbr = MPrefixFormatPtr(aItem2)↑.fRightArgsNbr then
    CompareFormats ← 0

```

This code is used in section 661.

663. Comparing bracket symbols first tries to compare the number of symbols to its right. If these are equal, then we try to compare the number of arguments. If these are equal, then we compare them “as if” they were infixing symbols.

```

⟨ Compare bracket symbols 663 ⟩ ≡
  if MBracketFormatPtr(aItem1)↑.fRightSymbolNr < MBracketFormatPtr(aItem2)↑.fRightSymbolNr
    then CompareFormats ← -1
  else if MBracketFormatPtr(aItem1)↑.fRightSymbolNr = MBracketFormatPtr(aItem2)↑.fRightSymbolNr
    then
      if MBracketFormatPtr(aItem1)↑.fArgsNbr < MBracketFormatPtr(aItem2)↑.fArgsNbr then
        CompareFormats ← -1
      else if MBracketFormatPtr(aItem1)↑.fArgsNbr = MBracketFormatPtr(aItem2)↑.fArgsNbr then
        ⟨ Compare infix symbols 664 ⟩

```

This code is used in section 661.

664. Comparing infixing symbols compares the number of arguments to the left. If these are equal, then we try to compare the number of arguments to the right. If these are equal, then we return 0.

```

⟨ Compare infix symbols 664 ⟩ ≡
  if MInfixFormatPtr(aItem1)↑.fLeftArgsNbr < MInfixFormatPtr(aItem2)↑.fLeftArgsNbr then
    CompareFormats ← -1
  else if MInfixFormatPtr(aItem1)↑.fLeftArgsNbr = MInfixFormatPtr(aItem2)↑.fLeftArgsNbr then
    if MInfixFormatPtr(aItem1)↑.fRightArgsNbr < MInfixFormatPtr(aItem2)↑.fRightArgsNbr then
      CompareFormats ← -1
    else if MInfixFormatPtr(aItem1)↑.fRightArgsNbr = MInfixFormatPtr(aItem2)↑.fRightArgsNbr
      then CompareFormats ← 0

```

This code is used in sections 661 and 663.

Section 17.1. LIST OF FORMATS

665. We have a collection of format objects managed by a *MFormatsList* object. There are two groups of public functions: “Lookup” functions (to find the format matching certain parameters), and “Collect” functions (to insert a new format).

```

⟨ Declare MFormatsList object 665 ⟩ ≡
  MFormatsListPtr = ↑MFormatsList;
  MFormatsList = object (MSortedList)
    constructor Init (ALimit : Integer);
    constructor LoadFormats (fName : string);
    procedure StoreFormats (fName : string);
    function Lookup_PrefixFormat (aKind : char; aSymNr, aArgsNbr : integer): integer;
    function Lookup_FuncFormat (aSymNr, aLArgsNbr, aRArgsNbr : integer): integer;
    function Lookup_BracketFormat (aLSymNr, aRSymNr, aArgsNbr, aLArgsNbr, aRArgsNbr : integer):
      integer;
    function Lookup_PredFormat (aSymNr, aLArgsNbr, aRArgsNbr : integer): integer;
    function CollectFormat (aFormat : MFormatPtr): integer;
    function CollectPrefixForm (aKind : char; aSymNr, aArgsNbr : integer): integer;
    function CollectFuncForm (aSymNr, aLArgsNbr, aRArgsNbr : integer): integer;
    function CollectBracketForm (aLSymNr, aRSymNr, aArgsNbr, aLArgsNbr, aRArgsNbr : integer):
      integer;
    function CollectPredForm (aSymNr, aLArgsNbr, aRArgsNbr : integer): integer;
  end

```

This code is used in section 649.

666. We prefix format objects specified by its kind, its symbol number, and the number of arguments it expects.

When the format object is not found, then 0 will be returned. This is a standard convention in these functions to indicate the thing is missing.

```

⟨ Implementation for MFormatsList 666 ⟩ ≡
const PrefixFormatChars = [‘M’, ‘V’, ‘U’, ‘J’, ‘L’, ‘G’];
function MFormatsList.LookUp_PrefixFormat (aKind : char; aSymNr, aArgsNbr : integer): integer;
  var lFormat: MPrefixFormatObj; i: integer;
  begin MizAssert (3300, aKind ∈ PrefixFormatChars);
  lFormat.Init (aKind, aSymNr, aArgsNbr);
  if Find (@lFormat, i) then LookUp_PrefixFormat ← fIndex↑i + 1
  else LookUp_PrefixFormat ← 0;
  end;

```

This code is used in section 650.

667. Looking up an infix functor format (§655). This returns the *index* for the entry.

The contract here is rather confusing. What *should* occur is: if there is a functor symbol with the given left and right number of arguments, then return the index for the entry. Otherwise (when there is no functor symbol) return -1 .

What happens instead is these values are incremented, so if the functor symbol with the given number of left and right arguments is contained in position k , then $k + 1$ will be returned. If there is no such functor symbol, then 0 will be returned.

```
function MFormatsList.LookUp_FuncFormat(aSymNr, aLArgsNbr, aRArgsNbr : integer): integer;
  var lFormat: MInfixFormatObj; i: integer;
  begin lFormat.Init(␣␣, aSymNr, aLArgsNbr, aRArgsNbr);
  if Find(@lFormat, i) then LookUp_FuncFormat  $\leftarrow$  fIndex↑[i] + 1
  else LookUp_FuncFormat  $\leftarrow$  0;
  end;
```

668. Looking up a bracket.

```
function MFormatsList.LookUp_BracketFormat(aLSymNr, aRSymNr, aArgsNbr, aLArgsNbr,
  aRArgsNbr : integer): integer;
  var lFormat: MBracketFormatObj; i: integer;
  begin lFormat.Init(aLSymNr, aRSymNr, aArgsNbr, aLArgsNbr, aRArgsNbr);
  if Find(@lFormat, i) then LookUp_BracketFormat  $\leftarrow$  fIndex↑[i] + 1
  else LookUp_BracketFormat  $\leftarrow$  0;
  end;
```

669. Looking up a predicate.

```
function MFormatsList.LookUp_PredFormat(aSymNr, aLArgsNbr, aRArgsNbr : integer): integer;
  var lFormat: MInfixFormatObj; i: integer;
  begin lFormat.Init(␣␣, aSymNr, aLArgsNbr, aRArgsNbr);
  if Find(@lFormat, i) then LookUp_PredFormat  $\leftarrow$  fIndex↑[i] + 1
  else LookUp_PredFormat  $\leftarrow$  0;
  end;
```

670. Insert a format, if it's missing.

```
function MFormatsList.CollectFormat(aFormat : MFormatPtr): integer;
  var lFormatNr, i: integer;
  begin lFormatNr  $\leftarrow$  0;
  if ¬Find(aFormat, i) then
    begin lFormatNr  $\leftarrow$  Count + 1; Insert(aFormat);
    end;
  CollectFormat  $\leftarrow$  lFormatNr;
  end;
```

671. Inserting a bracket, if it is missing. Returns the format number for the format, whether it is missing or not.

```
function MFormatsList.CollectBracketForm(aLSymNr, aRSymNr, aArgsNbr, aLArgsNbr,
    aRArgsNbr : integer): integer;
var lFormatNr: integer;
begin lFormatNr  $\leftarrow$  LookUp_BracketFormat(aLSymNr, aRSymNr, aArgsNbr, aLArgsNbr, aRArgsNbr);
if lFormatNr = 0 then
    begin lFormatNr  $\leftarrow$  Count + 1;
        Insert(new(MBracketFormatPtr, Init(aLSymNr, aRSymNr, aArgsNbr, aLArgsNbr, aRArgsNbr)));
    end;
    CollectBracketForm  $\leftarrow$  lFormatNr;
end;
```

672. Inserting a functor format, if it is missing. This returns the format number for the functor (whether it is missing or not).

```
function MFormatsList.CollectFuncForm(aSymNr, aLArgsNbr, aRArgsNbr : integer): integer;
var lFormatNr: integer;
begin lFormatNr  $\leftarrow$  LookUp_FuncFormat(aSymNr, aLArgsNbr, aRArgsNbr);
if lFormatNr = 0 then
    begin lFormatNr  $\leftarrow$  Count + 1;
        Insert(new(MInfixFormatPtr, Init(^0^, aSymNr, aLArgsNbr, aRArgsNbr)));
    end;
    CollectFuncForm  $\leftarrow$  lFormatNr;
end;
```

673. Insert a prefix format if it is missing. Then return the format number for the prefix format, missing or not.

```
function MFormatsList.CollectPrefixForm(aKind : char; aSymNr, aArgsNbr : integer): integer;
var lFormatNr: integer;
begin lFormatNr  $\leftarrow$  LookUp_PrefixFormat(aKind, aSymNr, aArgsNbr);
if lFormatNr = 0 then
    begin lFormatNr  $\leftarrow$  Count + 1; Insert(new(MPrefixFormatPtr, Init(aKind, aSymNr, aArgsNbr)));
    end;
    CollectPrefixForm  $\leftarrow$  lFormatNr;
end;
```

674. Insert a predicate format, if it is missing. Then return the format number, whether the predicate format is missing or not.

```
function MFormatsList.CollectPredForm(aSymNr, aLArgsNbr, aRArgsNbr : integer): integer;
var lFormatNr: integer;
begin lFormatNr  $\leftarrow$  LookUp_PredFormat(aSymNr, aLArgsNbr, aRArgsNbr);
if lFormatNr = 0 then
    begin lFormatNr  $\leftarrow$  Count + 1;
        Insert(new(MInfixFormatPtr, Init(^R^, aSymNr, aLArgsNbr, aRArgsNbr)));
    end;
    CollectPredForm  $\leftarrow$  lFormatNr;
end;
```

675. Constructor. Construct the empty list of formats.

```
constructor MFormatsList.Init(ALimit : Integer);
  begin InitSorted(ALimit, CompareFormats);
end;
```

676. Constructor. Parse an XML file for formats, and populate a format list object with the file's contents.

```
constructor MFormatsList.LoadFormats(fName : string);
  var lEnvFile: XMLInStreamPtr; lValue: integer; lLex: LexemRec;
  begin InitSorted(100, CompareFormats); lEnvFile  $\leftarrow$  new(XMLInStreamPtr, OpenFile(fName));
  with lEnvFile  $\uparrow$  do
    begin NextElementState; XMLASSERT(nElName = XMLElemName[elFormats]);
    NextElementState;
    while  $\neg$ (nState = eEnd)  $\wedge$  (nElName = XMLElemName[elFormat]) do Insert(In_Format(lEnvFile));
    gPriority.Init(10);
    while  $\neg$ (nState = eEnd) do
      begin XMLASSERT(nElName = XMLElemName[elPriority]);
      lLex.Kind  $\leftarrow$  GetAttr(XMLAttrName[atKind])[1];
      lLex.Nr  $\leftarrow$  GetIntAttr(XMLAttrName[atSymbolNr]); MizAssert(3300, lLex.Kind  $\in$  [ $\text{'0'}$ ,  $\text{'L'}$ ,  $\text{'K'}$ ]);
      lValue  $\leftarrow$  GetIntAttr(XMLAttrName[atValue]); gPriority.Assign(ord(lLex.Kind), lLex.Nr, lValue);
      AcceptEndState; NextElementState;
      end;
    end;
  dispose(lEnvFile, Done);
end;
```

677. We can read exactly one format from an XML input stream.

\langle Read formats from an XML input stream 677 $\rangle \equiv$

```
function In_Format(fInFile : XMLInStreamPtr): MFormatPtr;
  var lLex: LexemRec; lArgsNbr, lLeftArgsNbr, lRightSymNr: integer;
  begin with fInFile  $\uparrow$  do
    begin lLex.Kind  $\leftarrow$  GetAttr(XMLAttrName[atKind])[1];
    lLex.Nr  $\leftarrow$  GetIntAttr(XMLAttrName[atSymbolNr]);
    lArgsNbr  $\leftarrow$  GetIntAttr(XMLAttrName[atArgNr]);
    case lLex.Kind of
       $\text{'0'}$ ,  $\text{'R'}$ : begin lLeftArgsNbr  $\leftarrow$  GetIntAttr(XMLAttrName[atLeftArgNr]);
        In_Format  $\leftarrow$  new(MInfixFormatPtr, Init(lLex.Kind, lLex.Nr, lLeftArgsNbr,
          lArgsNbr - lLeftArgsNbr));
        end;
       $\text{'J'}$ ,  $\text{'U'}$ ,  $\text{'V'}$ ,  $\text{'G'}$ ,  $\text{'L'}$ ,  $\text{'M'}$ : In_Format  $\leftarrow$  new(MPrefixFormatPtr, Init(lLex.Kind, lLex.Nr, lArgsNbr));
       $\text{'K'}$ : begin lRightSymNr  $\leftarrow$  GetIntAttr(XMLAttrName[atRightSymbolNr]);
        In_Format  $\leftarrow$  new(MBracketFormatPtr, Init(lLex.Nr, lRightSymNr, lArgsNbr, 0, 0));
        end;
    othercases RunTimeError(2019);
    endcases;
    AcceptEndState; NextElementState;
  end;
end;
```

This code is used in section 650.

678. Conversely, we can print to an output stream an XML representation for a format object.

⟨Implement *MFormatObj* 678⟩ ≡

```
procedure MFormatObj.Out_Format(var fOutFile : XMLOutStreamObj; aFormNr : integer);
begin with fOutFile do
  begin Out_XElStart(XMLElemName[elFormat]); Out_XAttr(XMLAttrName[atKind], fSymbol.Kind);
  if aFormNr > 0 then Out_XIntAttr(XMLAttrName[atNr], aFormNr);
  Out_XIntAttr(XMLAttrName[atSymbolNr], fSymbol.Nr);
  case fSymbol.Kind of
    'J', 'U', 'V', 'G', 'L', 'M':
      Out_XIntAttr(XMLAttrName[atArgNr], MPrefixFormatPtr(@Self)↑.fRightArgsNbr);
    'O', 'R': with MInfixFormatPtr(@Self)↑ do
      begin Out_XIntAttr(XMLAttrName[atArgNr], fLeftArgsNbr + fRightArgsNbr);
      Out_XIntAttr(XMLAttrName[atLeftArgNr], fLeftArgsNbr);
      end;
    'K': with MBracketFormatPtr(@Self)↑ do
      begin Out_XIntAttr(XMLAttrName[atArgNr], fArgsNbr);
      Out_XIntAttr(XMLAttrName[atRightSymbolNr], fRightSymbolNr);
      end;
  othercases RuntimeError(3300);
endcases;
  Out_XElEnd0;
end;
end;
```

This code is used in section 650.

679. Given a list of formats, we can store them to an XML file using the previous function.

```
procedure MFormatsList.StoreFormats(fName : string);
var lEnvFile : XMLOutStreamObj; z : integer;
begin lEnvFile.OpenFile(fName);
with lEnvFile do
  begin Out_XElStart0(XMLElemName[elFormats]);
  for z ← 0 to Count − 1 do MFormatPtr(Items↑[z])↑.Out_Format(lEnvFile, z + 1);
  with gPriority do
    for z ← 0 to fCount − 1 do
      begin Out_XElStart(XMLElemName[elPriority]);
      Out_XAttr(XMLAttrName[atKind], chr(fList↑[z].X1));
      Out_XIntAttr(XMLAttrName[atSymbolNr], fList↑[z].X2);
      Out_XIntAttr(XMLAttrName[atValue], fList↑[z].Y); Out_XElEnd0;
      end;
    Out_XElEnd(XMLElemName[elFormats]);
  end;
lEnvFile.Done;
end;
```

680. We clean up the formats collection and the priority. The *gPriority* is initialized and populated in other functions. The *gFormatsColl* is used heavily in *parseraddition.pas* and a few other places.

```
procedure DisposeFormats;
begin gFormatsColl.Done; gPriority.Done;
end;
```

File 18

Syntax

681. This describes the syntax for the Mizar language, using expressions, subexpressions, blocks, and “items” (statements).

We will need to recall *StackedObj* from `mobjects.pas` (§307).

```

<syntax.pas 681> ≡
  <GNU License 4>
unit syntax;
  interface
    uses mobjects, errhan; <Interface for syntax.pas 688>
  implementation
    uses mconsole
      mdebug , info end_mdebug;
      <Implementation for syntax.pas 683>
  end .

```

682. The maximum number of “visible” arguments to an expression is set here, at 10.

```

<Public constants for syntax.pas 682> ≡
const MaxVisArgNbr = 10;

```

This code is used in section 688.

683. The implementation for the abstract syntax of Mizar is rather uninteresting, since most of the methods are abstract.

```

<Implementation for syntax.pas 683> ≡
  <Subexpression constructor 714>
  <Subexpression destructor 715>
  <Expression constructor 711>
  <Subexpression procedures 718>
  <Create a subexpression for an expression 712>
  <Item object implementation 704>
  <Block object implementation 694>
  <Public procedures implementation for syntax.pas 684>

```

This code is used in section 681.

684. Destructor wrappers. We have a few public-facing procedures to free the global subexpression, expression, etc., variables describing the state of the parser.

```

<Public procedures implementation for syntax.pas 684> ≡
procedure KillSubexpression;
  begin if gSubexpPtr = nil then RunTimeError(2144)
  else dispose(gSubexpPtr, Done);
  end;

```

See also sections 685, 686, and 687.

This code is used in section 683.

685.

```

⟨Public procedures implementation for syntax.pas 684⟩ +≡
procedure KillExpression;
  begin if gExpPtr = nil then RunTimeError(2143)
  else dispose(gExpPtr, Done);
  end;

```

686. This method will not be used until we get to the parser, sadly. I am not sure why there are calls to *DisplayLine* in *KillItem* and *KillBlock*, though.

The *KillItem* is called in exactly two places: (1) *Semicolon* in *parser.pas*, (2) *SchemeBlock*, also in the parser. (And *KillBlock* is called only in the parser, as well.)

```

⟨Public procedures implementation for syntax.pas 684⟩ +≡
procedure KillItem;
  begin if gItemPtr = nil then RunTimeError(2142)
  else begin gItemPtr↑.Pop; dispose(gItemPtr, Done); end;
  DisplayLine(CurPos.Line, ErrorNbr);
  end;

```

687.

```

⟨Public procedures implementation for syntax.pas 684⟩ +≡
procedure KillBlock;
  begin if gBlockPtr = nil then RunTimeError(2141)
  else begin gBlockPtr↑.Pop; dispose(gBlockPtr, Done);
  end;
  DisplayLine(CurPos.Line, ErrorNbr);
  end;

```

688.

```

⟨Interface for syntax.pas 688⟩ ≡
  ⟨Public constants for syntax.pas 682⟩
type ⟨BlockKinds (syntax.pas) 692⟩
  ⟨ItemKinds (syntax.pas) 702⟩
  ⟨ExpKinds (syntax.pas) 709⟩
  ⟨Block object interface 693⟩;
  ⟨Class declaration for Item object 703⟩;
  ⟨Subexpression object class 713⟩;
  ⟨Expression class declaration 710⟩;
  ⟨Public procedures for syntax.pas 689⟩
  ⟨Public variables for syntax.pas 690⟩

```

This code is used in section 681.

```

689.  ⟨Public procedures for syntax.pas 689⟩ ≡
procedure KillBlock;
procedure KillItem;
procedure KillExpression;
procedure KillSubexpression;

```

This code is used in section 688.

690. These global public variables for syntax will be manipulated by the parser.

⟨ Public variables for `syntax.pas` 690 ⟩ ≡

```
var gBlockPtr: BlockPtr = nil; gItemPtr: ItemPtr = nil; gExpPtr: ExpressionPtr = nil;  
    gSubexpPtr: SubexpPtr = nil;
```

This code is used in section 688.

Section 18.1. BLOCK OBJECT

691. The Mizar language is block-structured, so we have a Block represent a sequence of statements contained within a block.

This is extended in `parseraddition.pas`.



Fig. 1. UML class diagram for Block object class.

692. There are about a dozen different kinds of blocks.

$\langle \text{BlockKinds (syntax.pas 692)} \rangle \equiv$
BlockKind = (*blMain*, *blDiffuse*, *blHereby*, *blProof*, *blDefinition*, *blNotation*, *blRegistration*, *blCase*,
blSuppose, *blPublicScheme*);

This code is used in section 688.

693. $\langle \text{Block object interface 693} \rangle \equiv$
BlockPtr = $\uparrow \text{BlockObj}$;
ItemPtr = $\uparrow \text{ItemObj}$;
BlockObj = **object** (*StackedObj*)
nBlockKind: *BlockKind*;
constructor *Init*(*fBlockKind* : *BlockKind*);
procedure *Pop*; *virtual*; { inheritance }
destructor *Done*; *virtual*;
procedure *StartProperText*; *virtual*;
procedure *ProcessLink*; *virtual*;
procedure *ProcessRedefine*; *virtual*;
procedure *ProcessBegin*; *virtual*;
procedure *ProcessPragma*; *virtual*;
procedure *StartAtSignProof*; *virtual*;
procedure *FinishAtSignProof*; *virtual*;
procedure *FinishDefinition*; *virtual*;
procedure *CreateItem*(*fItemKind* : *ItemKind*); *virtual*;
procedure *CreateBlock*(*fBlockKind* : *BlockKind*); *virtual*;
procedure *StartSchemeDemonstration*; *virtual*;
procedure *FinishSchemeDemonstration*; *virtual*;
end

This code is used in section 688.

694. The constructor for a Block will initialize its *Previous* pointer to point at the global *gBlockPtr* instance.

$\langle \text{Block object implementation 694} \rangle \equiv$
constructor *BlockObj.Init*(*fBlockKind* : *BlockKind*);
 begin *nBlockKind* \leftarrow *fBlockKind*; *Previous* \leftarrow *gBlockPtr*;
 end;

See also sections 695, 696, 697, 698, 699, and 700.

This code is used in section 683.

695. Note that popping a block object is left for subclasses to handle.

```
⟨Block object implementation 694⟩ +≡
procedure BlockObj.Pop;
  begin end;
```

```
696. ⟨Block object implementation 694⟩ +≡
destructor BlockObj.Done;
  begin gBlockPtr ← BlockPtr(Previous);
  end;
```

697. Abstract methods.

```
⟨Block object implementation 694⟩ +≡
procedure BlockObj.StartProperText;
  begin end;
procedure BlockObj.ProcessRedefine;
  begin end;
procedure BlockObj.ProcessLink;
  begin end;
procedure BlockObj.ProcessBegin;
  begin end;
procedure BlockObj.ProcessPragma;
  begin end;
procedure BlockObj.StartAtSignProof;
  begin end;
procedure BlockObj.FinishAtSignProof;
  begin end;
procedure BlockObj.FinishDefinition;
  begin end;
```

```
698. ⟨Block object implementation 694⟩ +≡
procedure BlockObj.CreateItem(fItemKind : ItemKind);
  begin gItemPtr ← new(ItemPtr, Init(fItemKind));
  end;
```

```
699. ⟨Block object implementation 694⟩ +≡
procedure BlockObj.CreateBlock(fBlockKind : BlockKind);
  begin gBlockPtr ← new(BlockPtr, Init(fBlockKind));
  end;
```

700. More abstract methods.

```
⟨Block object implementation 694⟩ +≡
procedure BlockObj.StartSchemeDemonstration;
  begin end;
procedure BlockObj.FinishSchemeDemonstration;
  begin end;
```

Section 18.2. ITEM OBJECTS

701. The class declaration for an *Item* object is depressingly long, with most of its virtual methods not used. The class diagram is worth drawing out.



Fig. 2. UML class diagram for Item object class.

702. Items are a tagged union, tagged by the “kind” of item.

⟨ItemKinds (syntax.pas) 702⟩ ≡

```

ItemKind = (itIncorrItem, itDefinition, itSchemeBlock, itSchemeHead, itTheorem, itAxiom,
itReservation, itCanceled, itSection, itRegularStatement, itChoice, itReconsider, itPrivFuncDefinition,
itPrivPredDefinition, itConstantDefinition, itGeneralization, itLocDeclaration,
itExistentialAssumption, itExemplification, itPerCases, itConclusion, itCaseBlock, itCaseHead,
itSupposeHead, itAssumption, itCorrCond, itCorrectness, itProperty, itDefPred, itDefFunc,
itDefMode, itDefAttr, itDefStruct, itPredSynonym, itPredAntonym, itFuncNotation, itModeNotation,
itAttrSynonym, itAttrAntonym, itCluster, itIdentify, itReduction, itPropertyRegistration, itPragma);

```

This code is used in section 688.

703. ⟨Class declaration for Item object 703⟩ ≡

```

ItemObj = object (StackedObj)
  nItemKind: ItemKind;
  constructor Init(fItemKind : ItemKind);
  procedure Pop; virtual;
  destructor Done; virtual;
  ⟨Method declarations for Item object 707⟩
end

```

This code is used in section 688.

704. It is particularly important to note, when constructing an *Item* object, the previous item will *automatically* be set to point to the global *gItem* variable.

⟨Item object implementation 704⟩ ≡

```

constructor ItemObj.Init(fItemKind : ItemKind);
  begin nItemKind ← fItemKind; Previous ← gItemPtr;
  end;
procedure ItemObj.Pop;
  begin DisplayLine(CurPos.Line, ErrorNbr);
  end;
destructor ItemObj.Done;
  begin DisplayLine(CurPos.Line, ErrorNbr); gItemPtr ← ItemPtr(Previous);
  end;

```

See also sections 705 and 708.

This code is used in section 683.

705. Creating an expression in an item is handled with this method.

⟨Item object implementation 704⟩ +≡

```
procedure ItemObj.CreateExpression(fExpKind : ExpKind);
  begin gExpPtr ← new(ExpressionPtr, Init(fExpKind));
  end;
```

706. Abstract methods. The methods of the *Item* class can be partitioned into two groups: those which will be implemented by a subclass, and those which will remain “empty” (i.e., whose body is just **begin end**).

⟨Methods overridden by extended Item class 706⟩ ≡

```

procedure StartSentence; virtual;
procedure StartAttributes; virtual;
procedure FinishAntecedent; virtual;
procedure FinishConsequent; virtual;
procedure FinishClusterTerm; virtual;
procedure StartFuncIdentify; virtual;
procedure ProcessFuncIdentify; virtual;
procedure CompleteFuncIdentify; virtual;
procedure ProcessLeftLocus; virtual;
procedure ProcessRightLocus; virtual;
procedure StartFuncReduction; virtual;
procedure ProcessFuncReduction; virtual;
procedure FinishPrivateConstant; virtual;
procedure StartFixedVariables; virtual;
procedure ProcessFixedVariable; virtual;
procedure ProcessBeing; virtual;
procedure StartFixedSegment; virtual;
procedure FinishFixedSegment; virtual;
procedure FinishFixedVariables; virtual;
procedure StartAssumption; virtual;
procedure StartCollectiveAssumption; virtual;
procedure ProcessMeans; virtual;
procedure FinishOtherwise; virtual;
procedure StartDefiniens; virtual;
procedure FinishDefiniens; virtual;
procedure StartGuard; virtual;
procedure FinishGuard; virtual;
procedure ProcessEquals; virtual;
procedure StartExpansion; virtual;
procedure FinishSpecification; virtual;
procedure StartConstructionType; virtual;
procedure FinishConstructionType; virtual;
procedure StartAttributePattern; virtual;
procedure FinishAttributePattern; virtual;
procedure FinishSethoodProperties; virtual;
procedure StartModePattern; virtual;
procedure FinishModePattern; virtual;
procedure StartPredicatePattern; virtual;
procedure ProcessPredicateSymbol; virtual;
procedure FinishPredicatePattern; virtual;
procedure StartFunctorPattern; virtual;
procedure ProcessFunctorSymbol; virtual;
procedure FinishFunctorPattern; virtual;
procedure ProcessAttrAntonym; virtual;
procedure ProcessAttrSynonym; virtual;
procedure ProcessPredAntonym; virtual;
procedure ProcessPredSynonym; virtual;

```

```

procedure ProcessFuncSynonym; virtual;
procedure ProcessModeSynonym; virtual;
procedure StartVisible; virtual;
procedure ProcessVisible; virtual;
procedure FinishPrefix; virtual;
procedure ProcessStructureSymbol; virtual;
procedure StartFields; virtual;
procedure FinishFields; virtual;
procedure StartAggrPattSegment; virtual;
procedure ProcessField; virtual;
procedure FinishAggrPattSegment; virtual;
procedure ProcessSchemeName; virtual;
procedure StartSchemeSegment; virtual;
procedure StartSchemeQualification; virtual;
procedure FinishSchemeQualification; virtual;
procedure ProcessSchemeVariable; virtual;
procedure FinishSchemeSegment; virtual;
procedure FinishSchemeThesis; virtual;
procedure FinishSchemePremise; virtual;

procedure StartReservationSegment; virtual;
procedure ProcessReservedIdentifier; virtual;
procedure FinishReservationSegment; virtual;
procedure StartPrivateDefiniendum; virtual;
procedure FinishLocusType; virtual;

procedure CreateExpression(fExpKind : ExpKind); virtual;

procedure StartPrivateConstant; virtual;
procedure StartPrivateDefiniens; virtual;
procedure FinishPrivateFuncDefinienition; virtual;
procedure FinishPrivatePredDefinienition; virtual;
procedure ProcessReconsideredVariable; virtual;
procedure FinishReconsideredTerm; virtual;
procedure FinishDefaultTerm; virtual;
procedure FinishCondition; virtual;
procedure FinishHypothesis; virtual;
procedure ProcessExemplifyingVariable; virtual;
procedure FinishExemplifyingVariable; virtual;
procedure StartExemplifyingTerm; virtual;
procedure FinishExemplifyingTerm; virtual;
procedure ProcessCorrectness; virtual;
procedure ProcessLabel; virtual;
procedure StartRegularStatement; virtual;
procedure ProcessDefiniensLabel; virtual;
procedure FinishCompactStatement; virtual;
procedure StartIterativeStep; virtual;
procedure FinishIterativeStep; virtual;

    { Justification }
procedure ProcessSchemeReference; virtual;
procedure ProcessPrivateReference; virtual;
procedure StartLibraryReferences; virtual;
procedure StartSchemeLibraryReference; virtual;
procedure ProcessDef; virtual;

```

```
procedure ProcessTheoremNumber; virtual;  
procedure ProcessSchemeNumber; virtual;  
procedure StartJustification; virtual;  
procedure StartSimpleJustification; virtual;  
procedure FinishSimpleJustification; virtual;
```

See also section [1224](#).

This code is used in sections [707](#) and [1225](#).

707. \langle Method declarations for Item object 707 $\rangle \equiv$
 \langle Methods overridden by extended Item class 706 \rangle

```

procedure FinishClusterType; virtual;
procedure FinishSentence; virtual;
procedure FinishReconsidering; virtual;
procedure StartNewType; virtual;
procedure StartCondition; virtual;
procedure FinishChoice; virtual;
procedure FinishAssumption; virtual;

procedure StartEquals; virtual;
procedure StartOtherwise; virtual;
procedure StartSpecification; virtual;
procedure ProcessAttributePattern; virtual;
procedure StartDefPredicate; virtual;

procedure CompletePredAntonymByAttr; virtual;
procedure CompletePredSynonymByAttr; virtual;

procedure StartPredIdentify; virtual;
procedure ProcessPredIdentify; virtual;
procedure CompleteAttrIdentify; virtual;
procedure StartAttrIdentify; virtual;
procedure ProcessAttrIdentify; virtual;
procedure CompletePredIdentify; virtual;

procedure FinishFuncReduction; virtual;
procedure StartSethoodProperties; virtual;
procedure ProcessModePattern; virtual;
procedure StartPrefix; virtual;
procedure FinishVisible; virtual;
procedure FinishSchemeHeading; virtual;
procedure FinishSchemeDeclaration; virtual;
procedure StartSchemePremise; virtual;
procedure StartTheoremBody; virtual;
procedure FinishTheoremBody; virtual;
procedure FinishTheorem; virtual;
procedure FinishReservation; virtual;
procedure ProcessIterativeStep; virtual;

  { Justification }
procedure StartSchemeReference; virtual;
procedure StartReferences; virtual;
procedure ProcessSch; virtual;
procedure FinishTheLibraryReferences; virtual;
procedure FinishSchLibraryReferences; virtual;
procedure FinishReferences; virtual;
procedure FinishSchemeReference; virtual;
procedure FinishJustification; virtual;

```

This code is used in section 703.

708. \langle Item object implementation 704 $\rangle + \equiv$

```

procedure ItemObj.StartAttributes;
  begin end;
procedure ItemObj.FinishAntecedent;
  begin end;
procedure ItemObj.FinishConsequent;
  begin end;
procedure ItemObj.FinishClusterTerm;
  begin end;
procedure ItemObj.FinishClusterType;
  begin end;
procedure ItemObj.StartSentence;
  begin end;
procedure ItemObj.FinishSentence;
  begin end;
procedure ItemObj.FinishPrivateConstant;
  begin end;
procedure ItemObj.StartPrivateConstant;
  begin end;
procedure ItemObj.ProcessReconsideredVariable;
  begin end;
procedure ItemObj.FinishReconsidering;
  begin end;
procedure ItemObj.FinishReconsideredTerm;
  begin end;
procedure ItemObj.FinishDefaultTerm;
  begin end;
procedure ItemObj.StartNewType;
  begin end;
procedure ItemObj.StartCondition;
  begin end;
procedure ItemObj.FinishCondition;
  begin end;
procedure ItemObj.FinishChoice;
  begin end;
procedure ItemObj.StartFixedVariables;
  begin end;
procedure ItemObj.StartFixedSegment;
  begin end;
procedure ItemObj.ProcessFixedVariable;
  begin end;
procedure ItemObj.ProcessBeing;
  begin end;
procedure ItemObj.FinishFixedSegment;
  begin end;
procedure ItemObj.FinishFixedVariables;
  begin end;
procedure ItemObj.StartAssumption;
  begin end;
procedure ItemObj.StartCollectiveAssumption;
  begin end;
procedure ItemObj.FinishHypothesis;

```

```

    begin end;
  procedure ItemObj.FinishAssumption;
    begin end;
  procedure ItemObj.ProcessExemplifyingVariable;
    begin end;
  procedure ItemObj.FinishExemplifyingVariable;
    begin end;
  procedure ItemObj.StartExemplifyingTerm;
    begin end;
  procedure ItemObj.FinishExemplifyingTerm;
    begin end;
  procedure ItemObj.ProcessMeans;
    begin end;
  procedure ItemObj.FinishOtherwise;
    begin end;
  procedure ItemObj.StartDefiniens;
    begin end;
  procedure ItemObj.FinishDefiniens;
    begin end;
  procedure ItemObj.StartGuard;
    begin end;
  procedure ItemObj.FinishGuard;
    begin end;
  procedure ItemObj.StartOtherwise;
    begin end;
  procedure ItemObj.ProcessEquals;
    begin end;
  procedure ItemObj.StartEquals;
    begin end;
  procedure ItemObj.ProcessCorrectness;
    begin end;
  procedure ItemObj.FinishSpecification;
    begin end;
  procedure ItemObj.FinishConstructionType;
    begin end;
  procedure ItemObj.StartSpecification;
    begin end;
  procedure ItemObj.StartExpansion;
    begin end;
  procedure ItemObj.StartConstructionType;
    begin end;
  procedure ItemObj.StartPredicatePattern;
    begin end;
  procedure ItemObj.ProcessPredicateSymbol;
    begin end;
  procedure ItemObj.FinishPredicatePattern;
    begin end;
  procedure ItemObj.StartFunctorPattern;
    begin end;
  procedure ItemObj.ProcessFunctorSymbol;
    begin end;
  procedure ItemObj.FinishFunctorPattern;

```

```

    begin end;
procedure ItemObj.ProcessAttrAntonym;
    begin end;
procedure ItemObj.ProcessAttrSynonym;
    begin end;
procedure ItemObj.ProcessPredAntonym;
    begin end;
procedure ItemObj.ProcessPredSynonym;
    begin end;
procedure ItemObj.ProcessFuncSynonym;
    begin end;
procedure ItemObj.CompletePredSynonymByAttr;
    begin end;
procedure ItemObj.CompletePredAntonymByAttr;
    begin end;
procedure ItemObj.ProcessModeSynonym;
    begin end;
procedure ItemObj.StartFuncIdentify;
    begin end;
procedure ItemObj.ProcessFuncIdentify;
    begin end;
procedure ItemObj.CompleteFuncIdentify;
    begin end;
procedure ItemObj.StartPredIdentify;
    begin end;
procedure ItemObj.ProcessPredIdentify;
    begin end;
procedure ItemObj.CompletePredIdentify;
    begin end;
procedure ItemObj.StartAttrIdentify;
    begin end;
procedure ItemObj.ProcessAttrIdentify;
    begin end;
procedure ItemObj.CompleteAttrIdentify;
    begin end;
procedure ItemObj.ProcessLeftLocus;
    begin end;
procedure ItemObj.ProcessRightLocus;
    begin end;
procedure ItemObj.StartFuncReduction;
    begin end;
procedure ItemObj.ProcessFuncReduction;
    begin end;
procedure ItemObj.FinishFuncReduction;
    begin end;
procedure ItemObj.StartSethoodProperties;
    begin end;
procedure ItemObj.FinishSethoodProperties;
    begin end;
procedure ItemObj.StartModePattern;
    begin end;
procedure ItemObj.ProcessModePattern;

```

```

    begin end;
  procedure ItemObj.FinishModePattern;
    begin end;
  procedure ItemObj.StartAttributePattern;
    begin end;
  procedure ItemObj.ProcessAttributePattern;
    begin end;
  procedure ItemObj.FinishAttributePattern;
    begin end;
  procedure ItemObj.StartDefPredicate;
    begin end;
  procedure ItemObj.StartVisible;
    begin end;
  procedure ItemObj.ProcessVisible;
    begin end;
  procedure ItemObj.FinishVisible;
    begin end;
  procedure ItemObj.StartPrefix;
    begin end;
  procedure ItemObj.FinishPrefix;
    begin end;
  procedure ItemObj.ProcessStructureSymbol;
    begin end;
  procedure ItemObj.StartFields;
    begin end;
  procedure ItemObj.FinishFields;
    begin end;
  procedure ItemObj.StartAggrPattSegment;
    begin end;
  procedure ItemObj.ProcessField;
    begin end;
  procedure ItemObj.FinishAggrPattSegment;
    begin end;
  procedure ItemObj.ProcessSchemeName;
    begin end;
  procedure ItemObj.StartSchemeSegment;
    begin end;
  procedure ItemObj.ProcessSchemeVariable;
    begin end;
  procedure ItemObj.StartSchemeQualification;
    begin end;
  procedure ItemObj.FinishSchemeQualification;
    begin end;
  procedure ItemObj.FinishSchemeSegment;
    begin end;
  procedure ItemObj.FinishSchemeHeading;
    begin end;
  procedure ItemObj.FinishSchemeDeclaration;
    begin end;
  procedure ItemObj.FinishSchemeThesis;
    begin end;
  procedure ItemObj.StartSchemePremise;

```

```

    begin end;
  procedure ItemObj.FinishSchemePremise;
    begin end;
  procedure ItemObj.StartTheoremBody;
    begin end;
  procedure ItemObj.FinishTheoremBody;
    begin end;
  procedure ItemObj.FinishTheorem;
    begin end;
  procedure ItemObj.StartReservationSegment;
    begin end;
  procedure ItemObj.ProcessReservedIdentifier;
    begin end;
  procedure ItemObj.FinishReservationSegment;
    begin end;
  procedure ItemObj.FinishReservation;
    begin end;
  procedure ItemObj.StartPrivateDefiniendum;
    begin end;
  procedure ItemObj.FinishLocusType;
    begin end;
  procedure ItemObj.StartPrivateDefiniens;
    begin end;
  procedure ItemObj.FinishPrivateFuncDefinienition;
    begin end;
  procedure ItemObj.FinishPrivatePredDefinienition;
    begin end;
  procedure ItemObj.ProcessLabel;
    begin end;
  procedure ItemObj.StartRegularStatement;
    begin end;
  procedure ItemObj.ProcessDefiniensLabel;
    begin end;
  procedure ItemObj.ProcessSchemeReference;
    begin end;
  procedure ItemObj.StartSchemeReference;
    begin end;
  procedure ItemObj.StartReferences;
    begin end;
  procedure ItemObj.ProcessPrivateReference;
    begin end;
  procedure ItemObj.StartLibraryReferences;
    begin end;
  procedure ItemObj.StartSchemeLibraryReference;
    begin end;
  procedure ItemObj.ProcessDef;
    begin end;
  procedure ItemObj.ProcessSch;
    begin end;
  procedure ItemObj.ProcessTheoremNumber;
    begin end;
  procedure ItemObj.ProcessSchemeNumber;

```

```

    begin end;
  procedure ItemObj.FinishTheLibraryReferences;
    begin end;
  procedure ItemObj.FinishSchLibraryReferences;
    begin end;
  procedure ItemObj.FinishReferences;
    begin end;
  procedure ItemObj.FinishSchemeReference;
    begin end;
  procedure ItemObj.StartJustification;
    begin end;
  procedure ItemObj.FinishJustification;
    begin end;
  procedure ItemObj.StartSimpleJustification;
    begin end;
  procedure ItemObj.FinishSimpleJustification;
    begin end;
  procedure ItemObj.FinishCompactStatement;
    begin end;
  procedure ItemObj.StartIterativeStep;
    begin end;
  procedure ItemObj.ProcessIterativeStep;
    begin end;
  procedure ItemObj.FinishIterativeStep;
    begin end;

```

Section 18.3. EXPRESSIONS**709.**

⟨ExpKinds (syntax.pas) 709⟩ ≡
ExpKind = (*exNull*, *exType*, *exTerm*, *exFormula*, *exResType*, *exAdjectiveCluster*);
 This code is used in section 688.

710. ⟨Expression class declaration 710⟩ ≡

```

ExpressionPtr = ↑ExpressionObj;
ExpressionObj = object (MObject)
  nExpKind: ExpKind;
  constructor Init(fExpKind : ExpKind);
  procedure CreateSubexpression; virtual;
end

```

This code is used in section 688.

711. Constructor.

⟨Expression constructor 711⟩ ≡
constructor *ExpressionObj.Init*(*fExpKind* : *ExpKind*);
begin *nExpKind* ← *fExpKind*;
end;

This code is used in section 683.

712. Observe that creating a subexpression (1) allocates a new *SubexpPtr* on the heap, and (2) mutates the *gSubexpPtr* global variable.

⟨Create a subexpression for an expression 712⟩ ≡
procedure *ExpressionObj.CreateSubexpression*;
begin *gSubexpPtr* ← *new*(*SubexpPtr*, *Init*);
end;

This code is used in section 683.

Section 18.4. SUBEXPRESSIONS**713.**

```

⟨Subexpression object class 713⟩ ≡
  SubexpPtr = ↑SubexpObj;
  SubexpObj = object (StackedObj)
    constructor Init;
    destructor Done; virtual;
    ⟨Empty method declarations for SubexpObj 717⟩
end

```

This code is used in section 688.

714. Constructor. Importantly, constructing a new *Subexp* object will initialize its *Previous* field to point to the global *gSubexpPtr* object.

```

⟨Subexpression constructor 714⟩ ≡
constructor SubexpObj.Init;
  begin Previous ← gSubexpPtr;
end;

```

This code is used in section 683.

715. Destructor.

```

⟨Subexpression destructor 715⟩ ≡
destructor SubexpObj.Done;
  begin gSubexpPtr ← SubexpPtr(Previous);
end;

```

This code is used in section 683.

716. The remaining methods for subexpression objects are empty.

⟨Methods implemented by subclasses of *SubexpObj* 716⟩ ≡

```

procedure ProcessSimpleTerm; virtual;
procedure StartFraenkelTerm; virtual;
procedure StartPostqualification; virtual;
procedure StartPostqualifyingSegment; virtual;
procedure ProcessPostqualifiedVariable; virtual;
procedure StartPostqualificationSpecyfication; virtual;
procedure FinishPostqualifyingSegment; virtual;
procedure FinishFraenkelTerm; virtual;
procedure StartSimpleFraenkelTerm; virtual;
procedure FinishSimpleFraenkelTerm; virtual;
procedure ProcessThesis; virtual;
procedure StartPrivateTerm; virtual;
procedure FinishPrivateTerm; virtual;
procedure StartBracketedTerm; virtual;
procedure FinishBracketedTerm; virtual;
procedure StartAggregateTerm; virtual;
procedure FinishAggregateTerm; virtual;
procedure StartSelectorTerm; virtual;
procedure FinishSelectorTerm; virtual;
procedure StartForgetfulTerm; virtual;
procedure FinishForgetfulTerm; virtual;
procedure StartChoiceTerm; virtual;
procedure FinishChoiceTerm; virtual;
procedure ProcessNumeralTerm; virtual;
procedure ProcessItTerm; virtual;
procedure ProcessLocusTerm; virtual;
procedure ProcessQua; virtual;
procedure FinishQualifiedTerm; virtual;
procedure ProcessExactly; virtual;
procedure StartLongTerm; virtual;
procedure ProcessFunctorSymbol; virtual;
procedure FinishArgList; virtual;
procedure FinishLongTerm; virtual;
procedure FinishArgument; virtual;
procedure FinishTerm; virtual;
procedure StartType; virtual;
procedure ProcessModeSymbol; virtual;
procedure FinishType; virtual;
procedure CompleteType; virtual; { + }
procedure ProcessAtomicFormula; virtual;
procedure ProcessPredicateSymbol; virtual;
procedure ProcessRightSideOfPredicateSymbol; virtual;
procedure FinishPredicativeFormula; virtual;
procedure FinishRightSideOfPredicativeFormula; virtual;
procedure StartMultiPredicativeFormula; virtual;
procedure FinishMultiPredicativeFormula; virtual;
procedure StartPrivateFormula; virtual; { + }
procedure FinishPrivateFormula; virtual;
procedure ProcessContradiction; virtual;
procedure ProcessNegative; virtual;

```

{ This is a temporary solution, the generation of ExpNodes is such that it is not possible to handle negation uniformly. }

{ Jest to tymczasowe rozwiązanie, generowanie ExpNode'ów jest takie, że nie ma możliwości obsługi jednolitej negacji. }

```

procedure ProcessNegation; virtual;
procedure FinishQualifyingFormula; virtual;
procedure FinishAttributiveFormula; virtual;
procedure ProcessBinaryConnective; virtual;    { + }
procedure ProcessFlexDisjunction; virtual;
procedure ProcessFlexConjunction; virtual;
procedure StartRestriction; virtual;
procedure FinishRestriction; virtual;
procedure FinishBinaryFormula; virtual;
procedure FinishFlexDisjunction; virtual;
procedure FinishFlexConjunction; virtual;
procedure StartExistential; virtual;
procedure FinishExistential; virtual;
procedure StartUniversal; virtual;
procedure FinishUniversal; virtual;    { + }
procedure StartQualifiedSegment; virtual;
procedure StartQualifyingType; virtual;
procedure FinishQualifiedSegment; virtual;
procedure ProcessVariable; virtual;
procedure StartAttributes; virtual;

procedure ProcessNon; virtual;    { + }
procedure ProcessAttribute; virtual;    { + }
procedure StartAttributeArguments; virtual;    { + }
procedure CompleteAttributeArguments; virtual;    { + }
procedure FinishAttributeArguments; virtual;    { + }
procedure CompleteAdjectiveCluster; virtual;    { + }
procedure CompleteClusterTerm; virtual;

  { Errors Recovery }
procedure InsertIncorrTerm; virtual;
procedure InsertIncorrType; virtual;
procedure InsertIncorrBasic; virtual;
procedure InsertIncorrFormula; virtual;

```

See also section [1387](#).

This code is used in sections [717](#) and [1388](#).

717. \langle Empty method declarations for *SubexpObj* 717 $\rangle \equiv$
 \langle Methods implemented by subclasses of *SubexpObj* 716 \rangle

```

procedure FinishSample; virtual;
procedure ProcessThe; virtual;
procedure StartArgument; virtual;
procedure ProcessLeftParenthesis; virtual;
procedure ProcessRightParenthesis; virtual;
procedure StartAtomicFormula; virtual;

procedure ProcessHolds; virtual;
procedure FinishQuantified; virtual;
procedure ProcessNot; virtual;
procedure ProcessDoesNot; virtual;

procedure StartAdjectiveCluster; virtual;
procedure FinishAdjectiveCluster; virtual;

procedure FinishAttributes; virtual;
procedure CompleteAttributes; virtual;
procedure CompleteClusterType; virtual;
procedure FinishEquality; virtual;

```

This code is used in section 713.

718.

(Subexpression procedures 718) \equiv
procedure *SubexpObj.StartAttributes*;
 begin end;
procedure *SubexpObj.StartAdjectiveCluster*;
 begin end;
procedure *SubexpObj.FinishAdjectiveCluster*;
 begin end;
procedure *SubexpObj.ProcessNon*;
 begin end;
procedure *SubexpObj.ProcessAttribute*;
 begin end;
procedure *SubexpObj.FinishAttributes*;
 begin end;
procedure *SubexpObj.CompleteAttributes*;
 begin end;
procedure *SubexpObj.StartAttributeArguments*;
 begin end;
procedure *SubexpObj.CompleteAttributeArguments*;
 begin end;
procedure *SubexpObj.FinishAttributeArguments*;
 begin end;
procedure *SubexpObj.CompleteAdjectiveCluster*;
 begin end;
procedure *SubexpObj.CompleteClusterTerm*;
 begin end;
procedure *SubexpObj.CompleteClusterType*;
 begin end;
procedure *SubexpObj.ProcessSimpleTerm*;
 begin end;
procedure *SubexpObj.ProcessQua*;
 begin end;
procedure *SubexpObj.FinishQualifiedTerm*;
 begin end;
procedure *SubexpObj.ProcessExactly*;
 begin end;
procedure *SubexpObj.StartArgument*;
 begin end;
procedure *SubexpObj.FinishArgument*;
 begin end;
procedure *SubexpObj.FinishTerm*;
 begin end;
procedure *SubexpObj.StartType*;
 begin end;
procedure *SubexpObj.ProcessModeSymbol*;
 begin end;
procedure *SubexpObj.FinishType*;
 begin end;
procedure *SubexpObj.CompleteType*;
 begin end;
procedure *SubexpObj.StartLongTerm*;
 begin end;

```

procedure SubexpObj.FinishLongTerm;
  begin end;
procedure SubexpObj.FinishArgList;
  begin end;
procedure SubexpObj.ProcessFunctorSymbol;
  begin end;
procedure SubexpObj.StartFraenkelTerm;
  begin end;
procedure SubexpObj.FinishSample;
  begin end;
procedure SubexpObj.StartPostqualification;
  begin end;
procedure SubexpObj.StartPostqualificationSpecyfication;
  begin end;
procedure SubexpObj.StartPostqualifyingSegment;
  begin end;
procedure SubexpObj.ProcessPostqualifiedVariable;
  begin end;
procedure SubexpObj.FinishPostqualifyingSegment;
  begin end;
procedure SubexpObj.FinishFraenkelTerm;
  begin end;
procedure SubexpObj.StartSimpleFraenkelTerm;
  begin end;
procedure SubexpObj.FinishSimpleFraenkelTerm;
  begin end;
procedure SubexpObj.StartPrivateTerm;
  begin end;
procedure SubexpObj.FinishPrivateTerm;
  begin end;
procedure SubexpObj.StartBracketedTerm;
  begin end;
procedure SubexpObj.FinishBracketedTerm;
  begin end;
procedure SubexpObj.StartAggregateTerm;
  begin end;
procedure SubexpObj.FinishAggregateTerm;
  begin end;
procedure SubexpObj.ProcessThe;
  begin end;
procedure SubexpObj.StartSelectorTerm;
  begin end;
procedure SubexpObj.FinishSelectorTerm;
  begin end;
procedure SubexpObj.StartForgetfulTerm;
  begin end;
procedure SubexpObj.FinishForgetfulTerm;
  begin end;
procedure SubexpObj.StartChoiceTerm;
  begin end;
procedure SubexpObj.FinishChoiceTerm;
  begin end;

```

```

procedure SubexpObj.ProcessNumeralTerm;
  begin end;
procedure SubexpObj.ProcessItTerm;
  begin end;
procedure SubexpObj.ProcessLocusTerm;
  begin end;
procedure SubexpObj.ProcessThesis;
  begin end;
procedure SubexpObj.StartAtomicFormula;
  begin end;
procedure SubexpObj.ProcessAtomicFormula;
  begin end;
procedure SubexpObj.ProcessPredicateSymbol;
  begin end;
procedure SubexpObj.ProcessRightSideOfPredicateSymbol;
  begin end;
procedure SubexpObj.FinishPredicativeFormula;
  begin end;
procedure SubexpObj.FinishRightSideOfPredicativeFormula;
  begin end;
procedure SubexpObj.StartMultiPredicativeFormula;
  begin end;
procedure SubexpObj.FinishMultiPredicativeFormula;
  begin end;
procedure SubexpObj.FinishQualifyingFormula;
  begin end;
procedure SubexpObj.FinishAttributiveFormula;
  begin end;
procedure SubexpObj.StartPrivateFormula;
  begin end;
procedure SubexpObj.FinishPrivateFormula;
  begin end;
procedure SubexpObj.ProcessContradiction;
  begin end;
procedure SubexpObj.ProcessNot;
  begin end;
procedure SubexpObj.ProcessDoesNot;
  begin end;
procedure SubexpObj.ProcessNegative;
  begin end;
procedure SubexpObj.ProcessNegation;
  begin end;
procedure SubexpObj.StartRestriction;
  begin end;
procedure SubexpObj.FinishRestriction;
  begin end;
procedure SubexpObj.ProcessHolds;
  begin end;
procedure SubexpObj.ProcessBinaryConnective;
  begin end;
procedure SubexpObj.FinishBinaryFormula;
  begin end;

```

```

procedure SubexpObj.ProcessFlexDisjunction;
  begin end;
procedure SubexpObj.ProcessFlexConjunction;
  begin end;
procedure SubexpObj.FinishFlexDisjunction;
  begin end;
procedure SubexpObj.FinishFlexConjunction;
  begin end;
procedure SubexpObj.StartQualifiedSegment;
  begin end;
procedure SubexpObj.StartQualifyingType;
  begin end;
procedure SubexpObj.FinishQualifiedSegment;
  begin end;
procedure SubexpObj.FinishQuantified;
  begin end;
procedure SubexpObj.ProcessVariable;
  begin end;
procedure SubexpObj.StartExistential;
  begin end;
procedure SubexpObj.FinishExistential;
  begin end;
procedure SubexpObj.StartUniversal;
  begin end;
procedure SubexpObj.FinishUniversal;
  begin end;
procedure SubexpObj.ProcessLeftParenthesis;
  begin end;
procedure SubexpObj.ProcessRightParenthesis;
  begin end;
procedure SubexpObj.InsertIncorrType;
  begin end;
procedure SubexpObj.InsertIncorrTerm;
  begin end;
procedure SubexpObj.InsertIncorrBasic;
  begin end;
procedure SubexpObj.InsertIncorrFormula;
  begin end;
procedure SubexpObj.FinishEquality;
  begin end;

```

This code is used in section [683](#).

File 19

MScanner

719. We have the MScanner module transform an article (an input file) into a stream of tokens.

```

< scanner.pas 588 > +≡
  < GNU License 4 >
unit mscanner;
interface
  uses errhan, mobjects, scanner;
  < Public interface for MScanner 720 >
implementation
  uses mizenv;
  < Implementation for MScanner 726 >;

end .

```

720. Public types. We have enumerated types for each construction we'll encounter in Mizar.

```

< Public interface for MScanner 720 > ≡
type < Token kinds for MScanner 724 >;
  CorrectnessKind = (syCorrectness, syCoherence, syCompatibility, syConsistency, syExistence,
    syUniqueness, syReducibility);
  PropertyKind = (sErrProperty, sySymmetry, syReflexivity, syIrreflexivity, syAssociativity, syTransitivity,
    syCommutativity, syConnectedness, syAsymmetry, syIdempotence, syInvolutiveness, syProjectivity,
    sySethood, syAbstractness);
  LibraryReferenceKind = (syThe, syDef, sySch);
  DirectiveKind = (syVocabularies, syNotations, syDefinitions, syTheorems, sySchemes, syRegistrations,
    syConstructors, syRequirements, syEqualities, syExpansions);
  < Token type for MScanner 721 >;

```

See also sections 722 and 723.

This code is used in section 719.

721. Token type for MScanner.

```

< Token type for MScanner 721 > ≡
  Token = record Kind: TokenKind;
    Nr: integer;
    Spelling: string;
  end

```

This code is used in section 720.

722. Constants for MScanner

```

⟨Public interface for MScanner 720⟩ +≡
const { Homonymic and special symbols in buildin vocabulary }
    { Homonymic Selector Symbol }
    StrictSym = 1; { “strict” }
    { Homonymic Mode Symbol }
    SetSym = 1; { ‘set’ }
    { Homonymic Predicate Symbol }
    EqualitySym = 1; { ‘=’ }
    { Homonymic Circumfix Symbols }
    SquareBracket = 1; { ‘[’ ‘]’ }
    CurlyBracket = 2; { “_” “”” }
    RoundedBracket = 3; { “(” “)” }
    scTooLongLineErrorNr = 200; { Error number: Too long line }
⟨Token names for MScanner 725⟩;
CorrectnessName: array [CorrectnessKind] of string = (‘correctness’, ‘coherence’,
    ‘compatibility’, ‘consistency’, ‘existence’, ‘uniqueness’, ‘reducibility’);
PropertyName: array [PropertyKind] of string = (‘’, ‘symmetry’, ‘reflexivity’, ‘irreflexivity’,
    ‘associativity’, ‘transitivity’, ‘commutativity’, ‘connectedness’, ‘asymmetry’,
    ‘idempotence’, ‘involutiveness’, ‘projectivity’, ‘sethood’, ‘abstractness’);
LibraryReferenceName: array [LibraryReferenceKind] of string = (‘the’, ‘def’, ‘sch’);
DirectiveName: array [DirectiveKind] of
    string = (‘vocabularies’, ‘notations’, ‘definitions’, ‘theorems’, ‘schemes’, ‘registrations’,
    ‘constructors’, ‘requirements’, ‘equalities’, ‘expansions’);
PlaceHolderName: array [1 .. 10] of
    string = (‘$1’, ‘$2’, ‘$3’, ‘$4’, ‘$5’, ‘$6’, ‘$7’, ‘$8’, ‘$9’, ‘$10’);
Unexpected = sErrProperty;

```

723. Public facing procedures and global variables. Of particular importance, the global variable *gScanner* is declared here.

```

⟨Public interface for MScanner 720⟩ +≡
var PrevWord, CurWord, AheadWord: Token;
    PrevPos, AheadPos: Position;
procedure ReadToken;
procedure LoadPrf(const aPrfFileName: string);
procedure DisposePrf;
procedure StartScanner;
procedure InitSourceFile(const aFileName, aDctFileName: string);
procedure CloseSourceFile;
procedure InitScanning(const aFileName, aDctFileName: string);
procedure FinishScanning;
var gScanner: MScannPtr = nil; { This is important }
    ModeMaxArgs, StructModeMaxArgs, PredMaxArgs: IntSequence;

```

724. Token kinds. If I were cleverer, I would have some WEB macros to make this readable.

⟨Token kinds for MScanner 724⟩ ≡

```

TokenKind = (syT0, { #0 }
  syT1, { #1 }
  syT2, { #2 }
  syT3, { #3 }
  syT4, { #4 }
  syT5, { #5 }
  syT6, { #6 }
  syT7, { #7 }
  syT8, { #8 }
  syT9, { #9 }
  syT10, { #10 }
  syT11, { #11 }
  syT12, { #12 }
  syT13, { #13 }
  syT14, { #14 }
  syT15, { #15 }
  syT16, { #16 }
  syT17, { #17 }
  syT18, { #18 }
  syT19, { #19 }
  syT20, { #20 }
  syT21, { #21 }
  syT22, { #22 }
  syT23, { #23 }
  syT24, { #24 }
  syT25, { #25 }
  syT26, { #26 }
  syT27, { #27 }
  syT28, { #28 }
  syT29, { #29 }
  syT30, { #30 }
  syT31, { #31 }
  Pragma, { #32 }
  EOT = 33, { ! #33 }
  sy_from, { " #34 }
  sy_identify, { # #35 }
  sy_thesis, { $ #36 }
  sy_contradiction, { % #37 }
  sy_Ampersand, { & #38 }
  sy_by, { ' #39 }
  sy_LeftParanthesis, { ( #40 }
  sy_RightParanthesis, { ) #41 }
  sy_registration, { * #42 }
  sy_definition, { + #43 }
  sy_Comma, { , #44 }
  sy_notation, { - #45 }
  sy_Ellipsis, { . #46 }
  sy_proof, { / #47 }
  syT48, { 0 #48 }
  syT49, { 1 #49 }

```

```

syT50, { 2 #50 }
syT51, { 3 #51 }
syT52, { 4 #52 }
syT53, { 5 #53 }
syT54, { 6 #54 }
syT55, { 7 #55 }
syT56, { 8 #56 }
syT57, { 9 #57 }
sy_Colon, { : #58 }
sy_Semicolon, { ; #59 }
sy_now, { < #60 }
sy_Equal, { = #61 }
sy_end, { > #62 }
sy_Error, { ? #63 }
syT64, { @ #64 }
MMLIdentifier, { A #65 }
syT66, { B #66 }
syT67, { C #67 }
sy_LibraryDirective, { D #68 } { see DirectiveKind }
syT69, { E #69 }
syT70, { F #70 }
StructureSymbol, { G #71 }
syT72, { H #72 }
Identifier, { I #73 }
ForgetfulFunctor, { J #74 }
LeftCircumfixSymbol, { K #75 }
RightCircumfixSymbol, { L #76 }
ModeSymbol, { M #77 }
Numeral, { N #78 }
InfixOperatorSymbol, { O #79 }
syT80, { P #80 }
ReferenceSort, { Q #81 }
PredicateSymbol, { R #82 }
syT83, { S #83 }
syT84, { T #84 }
SelectorSymbol, { U #85 }
AttributeSymbol, { V #86 }
syT87, { W #87 }
sy_Property, { X #88 } { see PropertyKind }
sy_CorrectnessCondition, { Y #89 } { see CorrectnessKind }
sy_Dolar, { Z #90 } { $1 $2 $3 $4 $5 $6 $7 $8 $9 $10 }
sy_LeftSquareBracket, { [ #91 }
syT92, { #92 }
sy_RightSquareBracket, { ] #93 }
syT94, { ^ #94 }
syT95, { _ #95 }
syT96, { ' #96 }
sy_according, { a #97 }
syT98, { b #98 }
sy_reduce, { c #99 }
syT100, { d #100 }
sy_equals, { e #101 }

```

```

syT102, { f #102 }
syT103, { g #103 }
sy_with, { h #104 }
syT105, { i #105 }
syT106, { j #106 }
syT107, { k #107 }
syT108, { l #108 }
syT109, { m #109 }
syT110, { n #110 }
syT111, { o #111 }
syT112, { p #112 }
syT113, { q #113 }
sy_wrt = 114, { r #114 }
syT115, { s #115 }
sy_to, { t #116 }
syT117, { u #117 }
syT118, { v #118 }
sy_when, { w #119 }
sy_axiom, { x #120 }
syT121, { y #121 }
syT122, { z #122 }
sy_LeftCurlyBracket, { #123 }
syT124, { | #124 }
sy_RightCurlyBracket, { #125 }
syT126, { ~ #126 }
syT127, { #127 }
syT128, { #128 }
syT129, { #129 }
syT130, { #130 }
syT131, { #131 }
syT132, { #132 }
syT133, { #133 }
syT134, { #134 }
sy_correctness = 135, { #135 }
syT136, { #136 }
syT137, { #137 }
syT138, { #138 }
syT139, { #139 }
sy_if = 140, { #140 }
syT141, { #141 }
syT142, { #142 }
syT143, { #143 }
sy_is = 144, { #144 }
sy_are, { #145 }
syT146, { #146 }
sy_otherwise, { #147 }
syT148, { #148 }
syT149, { #149 }
syT150, { #150 }
syT151, { #151 }
syT152, { #152 }
syT153, { #153 }

```

```

syT154, { #154 }
syT155, { #155 }
sy-ex = 156, { #156 }
sy-for, { #157 }
syT158, { #158 }
sy-define, { #159 }
syT160, { #160 }
sy-being, { #161 }
sy-over, { #162 }
syT163, { #163 }
sy-canceled, { #164 }
sy-do, { #165 }
sy-does, { #166 }
sy-or, { #167 }
sy-where, { #168 }
sy-non, { #169 }
sy-not, { #170 }
sy-cluster, { #171 }
sy-attr, { #172 }
syT173, { #173 }
sy-StructLeftBracket, { #174 }
sy-StructRightBracket, { #175 }
sy-environ, { #176 }
syT177, { #177 }
sy-begin, { #178 }
syT179, { #179 }
syT180, { #180 }
syT181, { #181 }
syT182, { #182 }
syT183, { #183 }
syT184, { #184 }
sy-hence, { #185 }
syT186, { #186 }
syT187, { #187 }
sy-hereby, { #188 }
syT189, { #189 }
syT190, { #190 }
syT191, { #191 }
sy-then, { #192 }
sy-DotEquals, { #193 }
syT194, { #194 }
syT195, { #195 }
sy-synonym, { #196 }
sy-antonym, { #197 }
syT198, { #198 }
syT199, { #199 }
sy-let, { #200 }
sy-take, { #201 }
sy-assume, { #202 }
sy-thus, { #203 }
sy-given, { #204 }
sy-suppose, { #205 }

```

```

sy_consider, { #206 }
syT207, { #207 }
syT208, { #208 }
syT209, { #209 }
syT210, { #210 }
sy_Arrow, { #211 }
sy_as, { #212 }
sy_qua, { #213 }
sy_be, { #214 }
sy_reserve, { #215 }
syT216, { #216 }
syT217, { #217 }
syT218, { #218 }
syT219, { #219 }
syT220, { #220 }
syT221, { #221 }
syT222, { #222 }
syT223, { #223 }
sy_set, { #224 }
sy_selector, { #225 }
sy_cases, { #226 }
sy_per, { #227 }
sy_scheme, { #228 }
sy_redefine, { #229 }
sy_reconsider, { #230 }
sy_case, { #231 }
sy_prefix, { #232 }
sy_the, { #233 }
sy_it, { #234 }
sy_all, { #235 }
sy_theorem, { #236 }
sy_struct, { #237 }
sy_exactly, { #238 }
sy_mode, { #239 }
sy_iff, { #240 }
sy_func, { #241 }
sy_pred, { #242 }
sy_implies, { #243 }
sy_st, { #244 }
sy_holds, { #245 }
sy_provided, { #246 }
sy_means, { #247 }
sy_of, { #248 }
sy_defpred, { #249 }
sy_deffunc, { #250 }
sy_such, { #251 }
sy_that, { #252 }
sy_aggregate, { #253 }
sy_and { #254 });

```

This code is used in section [720](#).

725. We have string representation for each of the token kinds, which is useful for debugging purposes.

⟨Token names for MScanner 725⟩ ≡

TokenName: **array** [*TokenKind*] **of** *string* = (`` , { #0 }

```

`` , { #1 }
`` , { #2 }
`` , { #3 }
`` , { #4 }
`` , { #5 }
`` , { #6 }
`` , { #7 }
`` , { #8 }
`` , { #9 }
`` , { #10 }
`` , { #11 }
`` , { #12 }
`` , { #13 }
`` , { #14 }
`` , { #15 }
`` , { #16 }
`` , { #17 }
`` , { #18 }
`` , { #19 }
`` , { #20 }
`` , { #21 }
`` , { #22 }
`` , { #23 }
`` , { #24 }
`` , { #25 }
`` , { #26 }
`` , { #27 }
`` , { #28 }
`` , { #29 }
`` , { #30 }
`` , { #31 }
`` , { #32 }
`` , { ! #33 }
`from`, { " #34 }
`identify`, { # #35 }
`thesis`, { $ #36 }
`contradiction`, { % #37 }
`&`, { & #38 }
`by`, { ' #39 }
`(`, { ( #40 }
`)`, { ) #41 }
`registration`, { * #42 }
`definition`, { + #43 }
`,` , { , #44 }
`notation`, { - #45 }
`...`, { . #46 }
`proof`, { / #47 }
`` , { 0 #48 }
`` , { 1 #49 }

```

```

--, { 2 #50 }
--, { 3 #51 }
--, { 4 #52 }
--, { 5 #53 }
--, { 6 #54 }
--, { 7 #55 }
--, { 8 #56 }
--, { 9 #57 }
--, { : #58 }
--, { ; #59 }
now, { < #60 }
=, { = #61 }
end, { > #62 }
--, { ? #63 }
--, { @ #64 }
--, { A #65 }
--, { B #66 }
--, { C #67 }
vocabularies, { D #68 }
--, { E #69 }
--, { F #70 }
--, { G #71 }
--, { H #72 }
--, { I #73 }
--, { J #74 }
--, { K #75 }
--, { L #76 }
--, { M #77 }
--, { N #78 }
--, { O #79 }
--, { P #80 }
def, { Q #81 }
--, { R #82 }
--, { S #83 }
--, { T #84 }
--, { U #85 }
--, { V #86 }
--, { W #87 }
symmetry, { X #88 }
coherence, { Y #89 }
$1, { Z #90 }
[, { [ #91 }
--, { ' #92 }
], { ] #93 }
--, { ^ #94 }
--, { - #95 }
--, { ' #96 }
according, { a #97 }
--, { b #98 }
reduce, { c #99 }
--, { d #100 }
equals, { e #101 }

```



```

^^, {f #102}
^^, {g #103}
`with`, {h #104}
^^, {i #105}
^^, {j #106}
^^, {k #107}
^^, {l #108}
^^, {m #109}
^^, {n #110}
^^, {o #111}
^^, {p #112}
^^, {q #113}
`wrt`, {r #114}
^^, {s #115}
`to`, {t #116}
^^, {u #117}
^^, {v #118}
`when`, {w #119}
`axiom`, {x #120}
^^, {y #121}
^^, {z #122}
`{`, { #123}
^^, {| #124}
`}`, { #125}
^^, {~ #126}
`T127`, {#127}
^^, {#128}
`T129`, {#129}
^^, {#130}
`T131`, {#131}
^^, {#132}
^^, {#133}
^^, {#134}
`correctness`, {#135}
`T136`, {#136}
^^, {#137}
^^, {#138}
^^, {#139}
`if`, {#140}
^^, {#141}
^^, {#142}
^^, {#143}
`is`, {#144}
`are`, {#145}
^^, {#146}
`otherwise`, {#147}
^^, {#148}
^^, {#149}
^^, {#150}
^^, {#151}
`T152`, {#152}
^^, {#153}

```

```

`', {#154}
`', {#155}
`ex`, {#156}
`for`, {#157}
`', {#158}
`define`, {#159}
`', {#160}
`being`, {#161}
`over`, {#162}
`', {#163}
`canceled`, {#164}
`do`, {#165}
`does`, {#166}
`or`, {#167}
`where`, {#168}
`non`, {#169}
`not`, {#170}
`cluster`, {#171}
`attr`, {#172}
`', {#173}
`(\#`, {#174}
`\#)`, {#175}
`environ`, {#176}
`', {#177}
`begin`, {#178}
`', {#179}
`', {#180}
`', {#181}
`', {#182}
`', {#183}
`', {#184}
`hence`, {#185}
`', {#186}
`', {#187}
`hereby`, {#188}
`', {#189}
`', {#190}
`', {#191}
`then`, {#192}
`.=`, {#193}
`', {#194}
`', {#195}
`synonym`, {#196}
`antonym`, {#197}
`', {#198}
`', {#199}
`let`, {#200}
`take`, {#201}
`assume`, {#202}
`thus`, {#203}
`given`, {#204}
`suppose`, {#205}

```

```

`consider`, {#206}
``, {#207}
``, {#208}
``, {#209}
``, {#210}
`->`, {#211}
`as`, {#212}
`qua`, {#213}
`be`, {#214}
`reserve`, {#215}
``, {#216}
``, {#217}
``, {#218}
``, {#219}
``, {#220}
``, {#221}
``, {#222}
``, {#223}
`set`, {#224}
`selector`, {#225}
`cases`, {#226}
`per`, {#227}
`scheme`, {#228}
`redefine`, {#229}
`reconsider`, {#230}
`case`, {#231}
`prefix`, {#232}
`the`, {#233}
`it`, {#234}
`all`, {#235}
`theorem`, {#236}
`struct`, {#237}
`exactly`, {#238}
`mode`, {#239}
`iff`, {#240}
`func`, {#241}
`pred`, {#242}
`implies`, {#243}
`st`, {#244}
`holds`, {#245}
`provided`, {#246}
`means`, {#247}
`of`, {#248}
`defpred`, {#249}
`deffunc`, {#250}
`such`, {#251}
`that`, {#252}
`aggregate`, {#253}
`and` {#254})

```

This code is used in section [722](#).

726. Reading a token. This tokenizes a Mizar article, using the scanner's *GetToken* method. We can trace this *GetToken* back to its implementation (§629). This, in turn, depends on the *SliceIt* method (§612).

This method is used to determine the next token in `parser.pas`'s *Parse* function.

This assumes that *StartScanner* (§729) has been invoked already, which initializes the *CurWord* token and other variables.

Also important to observe: the *Kind* of the token is populated here.

⟨Implementation for MScanner 726⟩ ≡

```
procedure ReadToken;
  begin PrevWord ← CurWord; PrevPos ← CurPos; CurWord ← AheadWord; CurPos ← AheadPos;
    { ' ' is not allowed in an identifiers in the text proper }
  if (CurWord.Kind = sy_Begin) then gScanner↑.Allowed[' ' ] ← 0;
  if (CurWord.Kind = sy_Error) ∧ (CurWord.Nr = scTooLongLineErrorNr) then
    ErrImm(CurWord.Nr);
  gScanner↑.GetToken;
  AheadWord.Kind ← TokenKind(gScanner↑.fLexem.Kind); AheadWord.Nr ← gScanner↑.fLexem.Nr;
  AheadWord.Spelling ← gScanner↑.fStr; AheadPos ← gScanner↑.fPos;
end;
```

See also sections 727, 728, 729, 730, 731, 732, and 733.

This code is used in section 719.

727. Loading a proof file. The `.prf` file is a file containing numerals, and its usage eludes me. The format consists of multiple lines:

Line 1: Three non-negative integers are on the first line “*M S P*”

Line 2: Contains *M* non-negative integers separated by a single whitespace

Line 3: Contains *S* non-negative integers separated by a single whitespace

Line 4: Contains *P* non-negative integers separated by a single whitespace.

This function loads the contents of the `.prf` file. This initializes the global variables *ModeMaxArgs*, *StructureModeMaxArgs*, *PredMaxArgs*, then populates them.

⟨Implementation for MScanner 726⟩ +≡

```
procedure LoadPrf(const aPrfFileName: string);
  var lPrf: text; lModeMaxArgsSize, lStructModeMaxArgsSize, lPredMaxArgsSize, i, lInt, r: integer;
  begin assign(lPrf, aPrfFileName + '.prf'); reset(lPrf);
  Read(lPrf, lModeMaxArgsSize, lStructModeMaxArgsSize, lPredMaxArgsSize);
  ModeMaxArgs.Init(lModeMaxArgsSize + 1); r ← ModeMaxArgs.Insert(0);
  StructModeMaxArgs.Init(lStructModeMaxArgsSize + 1); r ← StructModeMaxArgs.Insert(0);
  PredMaxArgs.Init(lPredMaxArgsSize + 1); r ← PredMaxArgs.Insert(0);
  for i ← 1 to lModeMaxArgsSize do
    begin Read(lPrf, lInt); r ← ModeMaxArgs.Insert(lInt);
    end;
  for i ← 1 to lStructModeMaxArgsSize do
    begin Read(lPrf, lInt); r ← StructModeMaxArgs.Insert(lInt);
    end;
  for i ← 1 to lPredMaxArgsSize do
    begin Read(lPrf, lInt); r ← PredMaxArgs.Insert(lInt);
    end;
  close(lPrf);
end;
```

728. We cleanup after using the `.prf` file.

⟨Implementation for MScanner 726⟩ +≡

```
procedure DisposePrf;
  begin ModeMaxArgs.Done; PredMaxArgs.Done; StructModeMaxArgs.Done;
  end;
```

729. We construct an MScann object to scan a file.

⟨Implementation for MScanner 726⟩ +≡

```
procedure StartScanner;
  begin CurPos.Line ← 1; CurPos.Col ← 0; AheadWord.Kind ← TokenKind(gScanner↑.fLexem.Kind);
  AheadWord.Nr ← gScanner↑.fLexem.Nr; AheadWord.Spelling ← gScanner↑.fStr;
  AheadPos ← gScanner↑.fPos;
  end;
```

730. We initialize a scanner for a file.

⟨Implementation for MScanner 726⟩ +≡

```
procedure InitSourceFile(const aFileName, aDctFileName: string);
  begin new(gScanner, InitScanning(aFileName, aDctFileName)); StartScanner;
  end;
```

731. When we're done with a scanner, we call the destructor for the MScanner.

⟨Implementation for MScanner 726⟩ +≡

```
procedure CloseSourceFile;
  begin dispose(gScanner, Done);
  end;
```

732. We can combine the previous functions together to initialize a scanner for a file (an article) and its dictionary file.

⟨Implementation for MScanner 726⟩ +≡

```
procedure InitScanning(const aFileName, aDctFileName: string);
  begin gScanner ← new(MScannPtr, InitScanning(aFileName, aDctFileName)); StartScanner;
  LoadPrf(aDctFileName);
  end;
```

733. We cleanup after scanning, saving a dictionary XML file to an “`.idx`” file. This uses the global variable *EnvFileName* declared in `mizenv.pas` (§24).

⟨Implementation for MScanner 726⟩ +≡

```
procedure FinishScanning;
  begin gScanner↑.fIdents.SaveXDct(EnvFileName + ‘.idx’); CloseSourceFile; DisposePrf;
  end;
```

File 20

Abstract Syntax

734. A crucial step in any interpreter, compiler, or proof assistant is to transform the concrete syntax into an abstract syntax tree. This module provides all the classes for the abstract syntax tree *of expressions, types, and formulas* in Mizar. The abstract syntax tree for “statements” will be found in the “Weakly Strict Text Proper” module.

This is a bit, well, “Java-esque”, in the sense that each different kind of node in the abstract syntax tree is represented by a different class. If you don’t know abstract syntax trees, I can heartily recommend Bob Nystrom’s *Crafting Interpreters* ([Ch. 5: Representing Code](#)) for an overview.

I’ll be quoting from the grammar for Mizar as we go along, since the class hierarchy names their classes after the nonterminal symbols in the grammar. (It’s what anyone would do.) You can find a local copy of the grammar on most UNIX machines with Mizar installed located at `/usr/local/doc/Mizar/syntax.txt`, which you can study at your leisure.

735. Warning: There is a lot of boiler plate code in the constructors and destructors. I am going to pass over them without much comment, because they are monotonous and uninteresting. The more interesting part will be discussed with the class declarations for each kind of node. I will simply entitle the paragraphs “Constructor” to indicate I am recognizing their existence and moving on.

```

<abstract_syntax.pas 735> ≡
  <GNU License 4>
unit abstract_syntax;
  interface uses errhan, mobjects, syntax;
    <Interface for abstract syntax 737>
  implementation
    <Implementation of abstract syntax 736>
  end .

```

736. The implementation requires discussing a few “special cases” (variables, qualified segments, adjectives) before getting to the usual syntactic classes (terms, types, formulas).

```

<Implementation of abstract syntax 736> ≡
  <Variable AST constructor 739>
  <Qualified segment AST constructor 742>
  <Adjective expression AST constructor 748>
  <Adjective AST constructor 752>
  <Negated adjective AST constructor 750>
  <Implementing term AST 757>
  <Implementing type AST 799>
  <Implementing formula AST 811>
  <Within expression AST implementation 1609>

```

This code is used in section [735](#).

737. The interface consists mostly of classes, as well as a few enumerated types. The gambit resembles what we would do if we were programming in C: define an `enum TermSort`, then introduce a `struct TermAstNode` {`enum TermSort sort;`} to act as an abstract base class for terms (and do likewise for formulas, types, etc.). This allows us to use “struct inheritance” in C, as Bob Nystrom’s *Crafting Interpreters* (Ch. 19) calls it.

```

⟨Interface for abstract syntax 737⟩ ≡
type ⟨Abstract base class for types 797⟩;
  ⟨Abstract base class for terms 753⟩;
  ⟨Abstract base class for formulas 808⟩;
  ⟨Adjective expression (abstract syntax tree) 747⟩;
  ⟨Negated adjective expression (abstract syntax tree) 749⟩;
  ⟨Adjective (abstract syntax tree) 751⟩;
  { Auxiliary structures }
  ⟨Variable (abstract syntax tree) 738⟩;
  ⟨Qualified segment (abstract syntax tree) 741⟩;
  ⟨Classes for terms (abstract syntax tree) 755⟩
  ⟨Classes for type (abstract syntax tree) 798⟩
  ⟨Classes for formula (abstract syntax tree) 810⟩
  { _____ }
  ⟨Class for Within expression 1608⟩;

```

This code is used in section 735.

738. Variable. A variable in the abstract syntax tree is basically a de Bruijn index, in the sense that it is represented by an integer in the metalanguage (PASCAL).

Logicians may feel uncomfortable at variables being outside the term syntax tree. But what logicians think of as “variables” in first-order logic, Mizar calls them “Simple Terms” (§756).

```

⟨Variable (abstract syntax tree) 738⟩ ≡
  VariablePtr = ↑VariableObj;
  VariableObj = object (MObject)
    nIdent: integer; { identifier number }
    nVarPos: Position;
    constructor Init(const aPos: Position; aIdentNr: integer);
end

```

This code is used in section 737.

739. Constructor.

```

⟨Variable AST constructor 739⟩ ≡
constructor VariableObj.Init(const aPos: Position; aIdentNr: integer);
  begin nIdent ← aIdentNr; nVarPos ← aPos;
end;

```

This code is used in section 736.

740. Qualified segment. A qualified segment refers to situations in, e.g., “**consider** $\langle \text{qualified-segment} \rangle^+$ **such that** ...”. This also happens in quantifiers where the Working Mathematician writes $\forall \vec{x}. P[\vec{x}]$, for example (that quantifier prefix “ $\forall \vec{x}$ ” uses the qualifying segment \vec{x}).

The Mizar grammar for qualified segments looks like:

```
Qualified-Variables = Implicitly-Qualified-Variables
                    | Explicitly-Qualified-Variables
                    | Explicitly-Qualified-Variables "," Implicitly-Qualified-Variables .
Implicitly-Qualified-Variables = Variables .
Explicitly-Qualified-Variables = Qualified-Segment {"," Qualified-Segment }.
Qualified-Segment = Variables Qualification .
Variables = Variable-Identifier {"," Variable-Identifier }.
Qualification = ( "being" | "be" ) Type-Expression .
```

We will implement `Qualified-Variables` as an array of pointers to *QualifiedSegment* objects, each one being either implicit or explicit.

741. Abstract base class for qualified segments. We have *implicitly* qualified segments and *explicitly* qualified segments, which are “both” qualified segments. Object-oriented yoga teaches us to describe this situation using a “qualified segment” abstract base class, and then extend it with two subclasses.

```
< Qualified segment (abstract syntax tree 741) > ≡
SegmentKind = (ikImplQualifiedSegm, ikExplQualifiedSegm);
QualifiedSegmentPtr = ↑QualifiedSegmentObj;
QualifiedSegmentObj = object (MObject)
  nSegmPos: Position;
  nSegmentSort: SegmentKind;
  constructor Init(const aPos: Position; aSort: SegmentKind);
end
```

See also sections 743 and 745.

This code is used in section 737.

742. Constructor.

```
< Qualified segment AST constructor 742 > ≡
constructor QualifiedSegmentObj.Init(const aPos: Position; aSort: SegmentKind);
  begin nSegmPos ← aPos; nSegmentSort ← aSort;
  end;
```

See also sections 744 and 746.

This code is used in section 736.

743. Implicitly qualified segments. When we use “reserved variables” in the qualifying segment, we can suppress the type ascription (i.e., the “**being** $\langle \text{Type} \rangle$ ”). This makes the typing *implicit*. Hence the name *implicitly* qualified segments (the types are implicitly given).

```
< Qualified segment (abstract syntax tree 741) > +≡
ImplicitlyQualifiedSegmentPtr = ↑ImplicitlyQualifiedSegmentObj;
ImplicitlyQualifiedSegmentObj = object (QualifiedSegmentObj)
  nIdentifier: VariablePtr;
  constructor Init(const aPos: Position; aIdentifier: VariablePtr);
  destructor Done; virtual;
end ;
```


744. Constructor. The constructors and destructors for implicitly qualified segments are straightforward.

```

< Qualified segment AST constructor 742 > +≡
constructor ImplicitlyQualifiedSegmentObj.Init(const aPos: Position; aIdentifier: VariablePtr);
  begin inherited Init(aPos, ikImplQualifiedSegm); nIdentifier ← aIdentifier;
  end;
destructor ImplicitlyQualifiedSegmentObj.Done;
  begin dispose(nIdentifier, Done);
  end;

```

745. Explicitly qualified segment. The other possibility in Mizar is that we will have “explicitly typed variables” in the qualifying segment. The idea is that, in Mizar, we can permit the following situation:

consider *x, y, z* being set such that ...

This means the three variables *x*, *y*, *z* are explicitly qualified variables with the type “set”. We represent this using one *ExplicitlyQualifiedSegment* object, a vector for the identifiers (*x*, *y*, *z*) and a pointer to their type (set).

```

< Qualified segment (abstract syntax tree) 741 > +≡
  ExplicitlyQualifiedSegmentPtr = ↑ExplicitlyQualifiedSegmentObj;
  ExplicitlyQualifiedSegmentObj = object (QualifiedSegmentObj)
    nIdentifiers: PList; { of identifier numbers }
    nType: TypePtr;
    constructor Init(const aPos: Position; aIdentifiers: PList; aType: TypePtr);
    destructor Done; virtual;
  end

```

746. The constructors and destructors for explicitly qualified segments are straightforward.

```

< Qualified segment AST constructor 742 > +≡
constructor ExplicitlyQualifiedSegmentObj.Init(const aPos: Position;
  aIdentifiers: PList;
  aType: TypePtr);
  begin inherited Init(aPos, ikExplQualifiedSegm); nIdentifiers ← aIdentifiers; nType ← aType;
  end;
destructor ExplicitlyQualifiedSegmentObj.Done;
  begin dispose(nIdentifiers, Done); dispose(nType, Done);
  end;

```

747. Attributes. Attributes can have arguments *preceding* it. The relevant part of the Mizar grammar, I think, is:

```

  Adjective-Cluster = { Adjective } .
  Adjective = [ "non" ] [ Adjective-Arguments ] Attribute-Symbol .

```

```

< Adjective expression (abstract syntax tree) 747 > ≡
  AdjectiveSort = (wsNegatedAdjective, wsAdjective);
  AdjectiveExpressionPtr = ↑AdjectiveExpressionObj;
  AdjectiveExpressionObj = object (MObject)
    nAdjectivePos: Position;
    nAdjectiveSort: AdjectiveSort;
    constructor Init(const aPos: Position; aSort: AdjectiveSort);
    destructor Done; virtual;
  end

```

This code is used in section 737.

748. \langle Adjective expression AST constructor 748 $\rangle \equiv$
constructor *AdjectiveExpressionObj.Init*(**const** *aPos*: *Position*; *aSort*: *AdjectiveSort*);
 begin *nAdjectivePos* \leftarrow *aPos*; *nAdjectiveSort* \leftarrow *aSort*;
 end;
destructor *AdjectiveExpressionObj.Done*;
 begin end;

This code is used in section 736.

749. Negated adjective. We represent an adjective using the EBNF grammar (c.f., the WSM article-related function *InWSMizFileObj.Read_Adjective:AdjectiveExpressionPtr*):

Negated-Adjective ::= "non" *Adjective-Expr*;
Positive-Adjective ::= [*Adjective-Arguments*] *Attribute-Symbol*;
Adjective-Expr ::= *Negated-Adjective* | *Positive-Adjective*;

Hence we only really need a pointer to the “adjective being negated”.

\langle Negated adjective expression (abstract syntax tree) 749 $\rangle \equiv$
NegatedAdjectivePtr = \uparrow *NegatedAdjectiveObj*;
NegatedAdjectiveObj = **object** (*AdjectiveExpressionObj*)
 nArg: *AdjectiveExpressionPtr*; { of *TermPtr*, visible arguments }
 constructor *Init*(**const** *aPos*: *Position*; *aArg*: *AdjectiveExpressionPtr*);
 destructor *Done*; *virtual*;
 end

This code is used in section 737.

750. Constructor.

\langle Negated adjective AST constructor 750 $\rangle \equiv$
constructor *NegatedAdjectiveObj.Init*(**const** *aPos*: *Position*; *aArg*: *AdjectiveExpressionPtr*);
 begin *inherited Init*(*aPos*, *wsNegatedAdjective*); *nArg* \leftarrow *aArg*;
 end;
destructor *NegatedAdjectiveObj.Done*;
 begin *dispose*(*nArg*, *Done*);
 end;

This code is used in section 736.

751. Adjective objects. [[This is the preferred node for later intermediate representations for attributes, since *nNegated* is a field in the class.]]

\langle Adjective (abstract syntax tree) 751 $\rangle \equiv$
AdjectivePtr = \uparrow *AdjectiveObj*;
AdjectiveObj = **object** (*AdjectiveExpressionObj*)
 nAdjectiveSymbol: *integer*;
 nNegated: *boolean*;
 nArgs: *PList*; { of *TermPtr*, visible arguments }
 constructor *Init*(**const** *aPos*: *Position*; *aAdjectiveNr*: *integer* ; *aArgs*: *PList*);
 destructor *Done*; *virtual*;
 end

This code is used in section 737.

752. Constructor.

\langle Adjective AST constructor 752 $\rangle \equiv$

```
constructor AdjectiveObj.Init(const aPos: Position; aAdjectiveNr: integer; aArgs: PList);
  begin inherited Init(aPos, wsAdjective); nAdjectiveSymbol  $\leftarrow$  aAdjectiveNr; nArgs  $\leftarrow$  aArgs;
  end;
destructor AdjectiveObj.Done;
  begin dispose(nArgs, Done);
  end;
```

This code is used in section 736.

Section 20.1. TERMS (ABSTRACT SYNTAX TREE)

753. We have an abstract base class for terms, along with the “sorts” (syntactic subclasses) allowed. This allows, e.g., formulas, to refer to terms without knowing the sort of term involved. The UML class diagram for term:

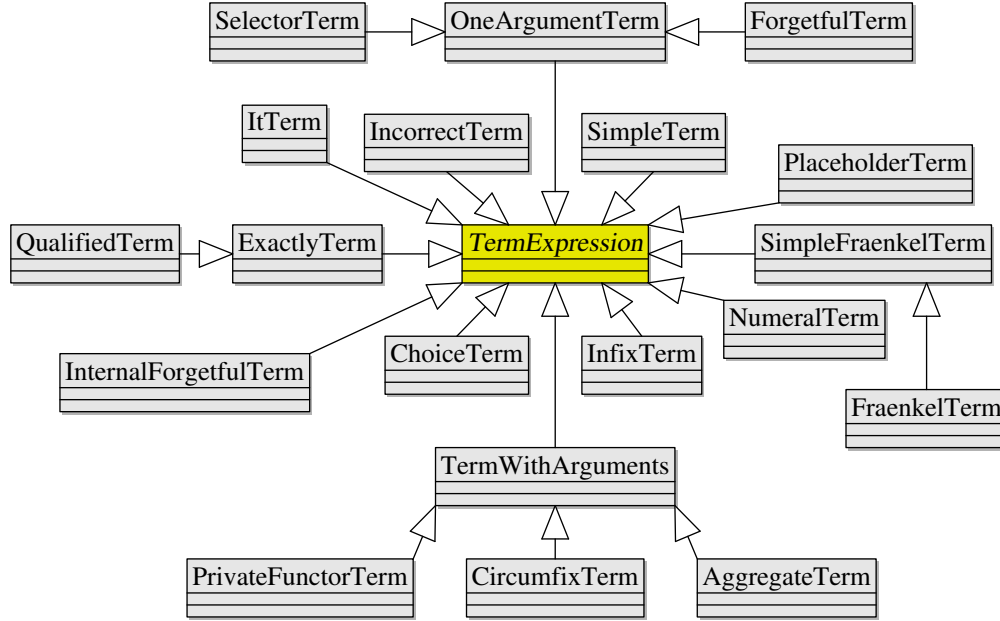


Fig. 3. UML class diagram for abstract syntax tree for terms.

The arrows indicate inheritance, pointing from the subclass to the parent superclass. The abstract base class *TermExpression* is italicized, but it is so difficult to distinguish we have colored it yellow.

NOTE: the class UML diagram may be missing a few descendents of *TermExpression*, but it contains the important subclasses which I could fit into it.

⟨ Abstract base class for terms 753 ⟩ ≡

```

TermSort = (wsErrorTerm, wsPlaceholderTerm, wsNumeralTerm, wsSimpleTerm,
            wsPrivateFunctorTerm, wsInfixTerm, wsCircumfixTerm, wsAggregateTerm, wsForgetfulFunctorTerm,
            wsInternalForgetfulFunctorTerm, wsSelectorTerm, wsInternalSelectorTerm, wsQualificationTerm,
            wsGlobalChoiceTerm, wsSimpleFraenkelTerm, wsFraenkelTerm, wsItTerm, wsExactlyTerm);
TermPtr = ↑TermExpressionObj;
TermExpressionObj = object (MObject)
  nTermSort: TermSort;
  nTermPos: Position;
end

```

This code is used in section 737.

754. The grammar for term expressions in Mizar as stated in `syntax.txt`:

```
Term-Expression = "(" Term-Expression ")"
| [ Arguments ] Functor-Symbol [ Arguments ]
| Left-Functor-Bracket Term-Expression-List Right-Functor-Bracket
| Functor-Identifier "(" [ Term-Expression-List ] ")"
| Structure-Symbol "(#" Term-Expression-List "#)"
| "the" Structure-Symbol "of" Term-Expression
| Variable-Identifier
| "{" Term-Expression { Postqualification } ":" Sentence "}"
| "the" "set" "of" "all" Term-Expression { Postqualification }
| Numeral
| Term-Expression "qua" Type-Expression
| "the" Selector-Symbol "of" Term-Expression
| "the" Selector-Symbol
| "the" Type-Expression
| Private-Definition-Parameter
| "it" .
```

But I think it might be clearer if we view it using the equivalent grammar:

```
Term-Expression = "(" Term-Expression ")"
| [ Arguments ] Functor-Symbol [ Arguments ]
| Left-Functor-Bracket Term-Expression-List Right-Functor-Bracket
| Functor-Identifier "(" [ Term-Expression-List ] ")"
| Aggregate-Term
| Forgetful-Functor-Term
| Variable-Identifier
| Fraenkel-Term
| Numeral
| Qualified-Term
| Selector-Functor
| Internal-Selector-Functor
| Choice-Term
| Private-Definition-Parameter
| "it" .

Aggregate-Term = Structure-Symbol "(#" Term-Expression-List "#)" .
Choice-Term = "the" Type-Expression.
Forgetful-Functor-Term = "the" Structure-Symbol "of" Term-Expression.
Fraenkel-Term = "{" Term-Expression {Postqualification} ":" Sentence "}"
| "the" "set" "of" "all" Term-Expression { Postqualification }.
Internal-Selector-Functor = "the" Selector-Symbol.
Selector-Functor = "the" Selector-Symbol "of" Term-Expression.
Qualified-Term = Term-Expression "qua" Type-Expression.
```

755. Class structure for this syntax tree.

```

⟨Classes for terms (abstract syntax tree) 755⟩ ≡
  { Terms }
  ⟨Simple term (abstract syntax tree) 756⟩;
  ⟨Placeholder term (abstract syntax tree) 758⟩;
  ⟨Numeral term (abstract syntax tree) 760⟩;
  ⟨Infix term (abstract syntax tree) 762⟩;
  ⟨Terms with arguments (abstract syntax tree) 764⟩;
  ⟨Circumfix term (abstract syntax tree) 766⟩;
  ⟨Private functor term (abstract syntax tree) 768⟩;
  ⟨One-argument term (abstract syntax tree) 770⟩;
  ⟨Selector term (abstract syntax tree) 772⟩;
  ⟨Internal selector term (abstract syntax tree) 774⟩;
  ⟨Aggregate term (abstract syntax tree) 776⟩;
  ⟨Forgetful functor (abstract syntax tree) 778⟩;
  ⟨Internal forgetful functors (abstract syntax tree) 780⟩;
  ⟨Fraenkel terms (abstract syntax tree) 782⟩;
  ⟨Exactly term (abstract syntax tree) 788⟩;
  ⟨Qualified term (abstract syntax tree) 786⟩;
  ⟨Choice term (abstract syntax tree) 790⟩;
  ⟨“It” term (abstract syntax tree) 792⟩;
  ⟨Incorrect term (abstract syntax tree) 794⟩;

```

This code is used in section 737.

756. Simple terms. Mizar describes variables *as terms* as a *SimpleTerm*.

```

⟨Simple term (abstract syntax tree) 756⟩ ≡
  SimpleTermPtr = ↑SimpleTermObj;
  SimpleTermObj = object (TermExpressionObj)
    nIdent: integer; { identifier number }
    constructor Init(const aPos: Position; aIdentNr: integer);
  end

```

This code is used in section 755.

757. Constructors.

```

⟨Implementing term AST 757⟩ ≡
constructor SimpleTermObj.Init(const aPos: Position; aIdentNr: integer);
  begin nTermPos ← aPos; nTermSort ← wsSimpleTerm; nIdent ← aIdentNr;
  end;

```

See also sections 759, 761, 763, 765, 767, 769, 771, 773, 775, 777, 779, 781, 783, 785, 787, 789, 791, 793, and 795.

This code is used in section 736.

758. Placeholder terms. These are the parameters “\$1”, “\$2”, etc., which appear in a private functor “`deffunc Foo(object) = ...`”.

```

⟨Placeholder term (abstract syntax tree) 758⟩ ≡
  PlaceholderTermPtr = ↑PlaceholderTermObj; { placeholder }
  PlaceholderTermObj = object (TermExpressionObj)
    nLocusNr: integer; { $1, ... }
    constructor Init(const aPos: Position; aLocusNr: integer);
  end

```

This code is used in section 755.

759. Constructor.

⟨Implementing term AST 757⟩ +≡

```
constructor PlaceholderTermObj.Init(const aPos: Position; aLocusNr: integer);
  begin nTermPos ← aPos; nTermSort ← wsPlaceholderTerm; nLocusNr ← aLocusNr;
  end;
```

760. Numeral terms. Mizar can handle 32-bit integers. If we wanted to extend this to, say, arbitrary precision arithmetic, then we would want to modify this class (and a few other places).

⟨Numeral term (abstract syntax tree) 760⟩ ≡

```
NumeralTermPtr = ↑NumeralTermObj;
NumeralTermObj = object (TermExpressionObj)
  nValue: integer;
  constructor Init(const aPos: Position; aValue: integer);
  end
```

This code is used in section 755.

761. Constructor.

⟨Implementing term AST 757⟩ +≡

```
constructor NumeralTermObj.Init(const aPos: Position; aValue: integer);
  begin nTermPos ← aPos; nTermSort ← wsNumeralTerm; nValue ← aValue;
  end;
```

762. Infix terms. When we have infix binary operators, they are terms with arguments on both sides of it. For example $x + 2$ will have “+” be an infix term with arguments $(x, 2)$.

We *could* permit multiple arguments on the left-hand side (and on the right-hand side), but they are comma-separated in Mizar. This could happen in finite group theory, for example, “p -signalizer over H, G” has two arguments on the right but only one argument on the left.

⟨Infix term (abstract syntax tree) 762⟩ ≡

```
InfixTermPtr = ↑InfixTermObj;
InfixTermObj = object (TermExpressionObj)
  nFunctorSymbol: integer;
  nLeftArgs, nRightArgs: PList;
  constructor Init(const aPos: Position; aFunctorNr: integer; aLeftArgs, aRightArgs: PList);
  destructor Done; virtual;
  end
```

This code is used in section 755.

763. Constructor.

⟨Implementing term AST 757⟩ +≡

```
constructor InfixTermObj.Init(const aPos: Position;
  aFunctorNr: integer;
  aLeftArgs, aRightArgs: PList);
  begin nTermPos ← aPos; nTermSort ← wsInfixTerm; nFunctorSymbol ← aFunctorNr;
  nLeftArgs ← aLeftArgs; nRightArgs ← aRightArgs;
  end;
destructor InfixTermObj.Done;
  begin dispose(nLeftArgs, Done); dispose(nRightArgs, Done);
  end;
```

764. Terms with arguments. This class seems to be used only internally to the `abstract_syntax.pas` module. Recalling the UML class diagram (§753), we remember there are three subclasses to this: private functor terms (which appear in Mizar when we use “`defunc F(...) = ...`”), circumfix (“bracketed”) terms, and aggregate terms (when we construct an instance of a structure).

```

⟨Terms with arguments (abstract syntax tree) 764⟩ ≡
  TermWithArgumentsPtr = ↑TermWithArgumentsObj;
  TermWithArgumentsObj = object (TermExpressionObj)
    nArgs: PList;
    constructor Init(const aPos: Position; aKind: TermSort; aArgs: PList);
    destructor Done; virtual;
  end

```

This code is used in section 755.

765. Constructor.

```

⟨Implementing term AST 757⟩ +≡
constructor TermWithArgumentsObj.Init(const aPos: Position; aKind: TermSort; aArgs: PList);
  begin nTermPos ← aPos; nTermSort ← aKind; nArgs ← aArgs;
  end;
destructor TermWithArgumentsObj.Done;
  begin dispose(nArgs, Done);
  end;

```

766. Circumfix terms. We can introduce different types of brackets in Mizar. For example, for groups, we have the commutator of group elements `[.x,y.]`. These “bracketed terms” are referred to as circumfix terms.

```

⟨Circumfix term (abstract syntax tree) 766⟩ ≡
  CircumfixTermPtr = ↑CircumfixTermObj;
  CircumfixTermObj = object (TermWithArgumentsObj)
    nLeftBracketSymbol, nRightBracketSymbol: integer;
    constructor Init(const aPos: Position; aLeftBracketNr, aRightBracketNr: integer; aArgs: PList);
    destructor Done; virtual;
  end

```

This code is used in section 755.

767. Constructor.

```

⟨Implementing term AST 757⟩ +≡
constructor CircumfixTermObj.Init(const aPos: Position;
                                aLeftBracketNr, aRightBracketNr: integer;
                                aArgs: PList);
  begin inherited Init(aPos, wsCircumfixTerm, aArgs); nLeftBracketSymbol ← aLeftBracketNr;
  nRightBracketSymbol ← aRightBracketNr;
  end;
destructor CircumfixTermObj.Done;
  begin dispose(nArgs, Done);
  end;

```


768. Private functor terms. We introduce private functor terms in Mizar when we have “**defpred** $F(\dots) = \dots$ ”.

```

⟨Private functor term (abstract syntax tree) 768⟩ ≡
  PrivateFunctorTermPtr = ↑PrivateFunctorTermObj;
  PrivateFunctorTermObj = object (TermWithArgumentsObj)
    nFunctorIdent: integer;
    constructor Init(const aPos: Position; aFunctorIdNr: integer; aArgs: PList);
    destructor Done; virtual;
  end

```

This code is used in section 755.

769. Constructor.

```

⟨Implementing term AST 757⟩ +≡
constructor PrivateFunctorTermObj.Init(const aPos: Position; aFunctorIdNr: integer; aArgs: PList);
  begin inherited Init(aPos, wsPrivateFunctorTerm, aArgs); nFunctorIdent ← aFunctorIdNr;
  end;
destructor PrivateFunctorTermObj.Done;
  begin dispose(nArgs, Done);
  end;

```

770. One-argument terms. Recalling the UML class diagram for terms (§753), we remember the class for *OneArgument* terms are either selector terms (“**the** ⟨field⟩ **of** ⟨aggregate⟩”) or forgetful functors (“**the** ⟨structure⟩ **of** ⟨aggregate⟩”).

```

⟨One-argument term (abstract syntax tree) 770⟩ ≡
  OneArgumentTermPtr = ↑OneArgumentTermObj;
  OneArgumentTermObj = object (TermExpressionObj)
    nArg: TermPtr;
    constructor Init(const aPos: Position; aKind: TermSort; aArg: TermPtr);
    destructor Done; virtual;
  end

```

This code is used in section 755.

771. Constructor.

```

⟨Implementing term AST 757⟩ +≡
constructor OneArgumentTermObj.Init(const aPos: Position; aKind: TermSort; aArg: TermPtr);
  begin nTermPos ← aPos; nTermSort ← aKind; nArg ← aArg;
  end;
destructor OneArgumentTermObj.Done;
  begin dispose(nArg, Done);
  end;

```

772. Selector terms. When we have an aggregate term (i.e., an instance of a structure), we want to refer to fields of the structure. This is done with selector terms. [[The selector number refers to the position in the underlying tuple of the structure instance.]]

```

⟨ Selector term (abstract syntax tree) 772 ⟩ ≡
  SelectorTermPtr = ↑SelectorTermObj;
  SelectorTermObj = object (OneArgumentTermObj)
    nSelectorSymbol: integer;
    constructor Init(const aPos: Position; aSelectorNr: integer; aArg: TermPtr);
    destructor Done; virtual;
  end

```

This code is used in section 755.

773. Constructor.

```

⟨ Implementing term AST 757 ⟩ +=
constructor SelectorTermObj.Init(const aPos: Position; aSelectorNr: integer; aArg: TermPtr);
  begin inherited Init(Apos, wsSelectorTerm, aArg); nSelectorSymbol ← aSelectorNr;
  end;
destructor SelectorTermObj.Done;
  begin dispose(nArg, Done);
  end;

```

774. Internal selector terms. An “internal selector” term refers to the case where we have in Mizar “the *⟨selector⟩*” treated as a term.

```

⟨ Internal selector term (abstract syntax tree) 774 ⟩ ≡
  InternalSelectorTermPtr = ↑InternalSelectorTermObj;
  InternalSelectorTermObj = object (TermExpressionObj)
    nSelectorSymbol: integer;
    constructor Init(const aPos: Position; aSelectorNr: integer);
  end

```

This code is used in section 755.

775. Constructor.

```

⟨ Implementing term AST 757 ⟩ +=
constructor InternalSelectorTermObj.Init(const aPos: Position; aSelectorNr: integer);
  begin nTermPos ← aPos; nTermSort ← wsInternalSelectorTerm; nSelectorSymbol ← aSelectorNr;
  end;

```

776. Aggregate terms. When we construct a new instance of a structure, well, that’s a term. Such terms are called “aggregate terms” in Mizar.

```

⟨ Aggregate term (abstract syntax tree) 776 ⟩ ≡
  AggregateTermPtr = ↑AggregateTermObj;
  AggregateTermObj = object (TermWithArgumentsObj)
    nStructSymbol: integer;
    constructor Init(const aPos: Position; aStructSymbol: integer; aArgs: PList);
    destructor Done; virtual;
  end

```

This code is used in section 755.

777. Constructor.

⟨Implementing term AST 757⟩ +≡

```
constructor AggregateTermObj.Init(const aPos: Position; aStructSymbol: integer; aArgs: PList);
  begin inherited Init(aPos, wsAggregateTerm, aArgs); nStructSymbol ← aStructSymbol;
  end;

destructor AggregateTermObj.Done;
  begin dispose(nArgs, Done);
  end;
```

778. Forgetful functors. When we have structure inheritance in Mizar, say structure B extends structure A , and we have b being an instance of B , then we can obtain “the A -object underlying b ” by writing “**the A of b**”. This is an example of what Mizar calls a “forgetful functor” (which is quite the pun).

⟨Forgetful functor (abstract syntax tree) 778⟩ ≡

```
ForgetfulFunctorTermPtr = ↑ForgetfulFunctorTermObj;
ForgetfulFunctorTermObj = object (OneArgumentTermObj)
  nStructSymbol: integer;
  constructor Init(const aPos: Position; aStructSymbol: integer; aArg: TermPtr);
  destructor Done; virtual;
end
```

This code is used in section 755.

779. Constructor.

⟨Implementing term AST 757⟩ +≡

```
constructor ForgetfulFunctorTermObj.Init(const aPos: Position; aStructSymbol: integer;
  aArg: TermPtr);
  begin inherited Init(aPos, wsForgetfulFunctorTerm, aArg); nStructSymbol ← aStructSymbol;
  end;

destructor ForgetfulFunctorTermObj.Done;
  begin dispose(nArg, Done);
  end;
```

780. Internal forgetful functors. When we omit the “structure instance” b in a forgetful functor term — e.g., when we have “**the A**” — then we have an “internal forgetful functor” (named analogous to internal selectors).

⟨Internal forgetful functors (abstract syntax tree) 780⟩ ≡

```
InternalForgetfulFunctorTermPtr = ↑InternalForgetfulFunctorTermObj;
InternalForgetfulFunctorTermObj = object (TermExpressionObj)
  nStructSymbol: integer;
  constructor Init(const aPos: Position; aStructSymbol: integer);
end
```

This code is used in section 755.

781. Constructor.

⟨Implementing term AST 757⟩ +≡

```
constructor InternalForgetfulFunctorTermObj.Init(const aPos: Position; aStructSymbol: integer);
  begin nTermPos ← aPos; nTermSort ← wsInternalForgetfulFunctorTerm;
  nStructSymbol ← aStructSymbol;
  end;
```

782. Simple Fraenkel terms. Fraenkel terms are set-builder notation in Mizar. But “simple” Fraenkel terms occurs when we have “the set of all $\langle termexpr \rangle$ ”.

```

⟨ Fraenkel terms (abstract syntax tree) 782 ⟩ ≡
  SimpleFraenkelTermPtr = ↑SimpleFraenkelTermObj;
  SimpleFraenkelTermObj = object (TermExpressionObj)
    nPostqualification: PList; { of segments }
    nSample: TermPtr;
    constructor Init(const aPos: Position; aPostqual: PList; aSample: TermPtr);
    destructor Done; virtual;
  end ;

```

See also section 784.

This code is used in section 755.

783. Constructor.

```

⟨ Implementing term AST 757 ⟩ +≡
constructor SimpleFraenkelTermObj.Init(const aPos: Position; aPostqual: PList; aSample: TermPtr);
  begin nTermPos ← aPos; nTermSort ← wsSimpleFraenkelTerm; nPostqualification ← aPostqual;
  nSample ← aSample;
  end;
destructor SimpleFraenkelTermObj.Done;
  begin dispose(nSample, Done);
  end;

```

784. Fraenkel terms. Fraenkel terms are sets given by set-builder notation, usually they look like

$$\{f(\vec{t}) \text{ where } \vec{t} \text{ being } \vec{T} : P[\vec{t}]\}$$

This is technically a higher-order object (look, it takes a functor f and a predicate P).

```

⟨ Fraenkel terms (abstract syntax tree) 782 ⟩ +≡
  FraenkelTermPtr = ↑FraenkelTermObj;
  FraenkelTermObj = object (SimpleFraenkelTermObj)
    nFormula: FormulaPtr;
    constructor Init(const aPos: Position; aPostqual: PList; aSample: TermPtr; aFormula:
      FormulaPtr);
    destructor Done; virtual;
  end

```

785. Constructor.

```

⟨ Implementing term AST 757 ⟩ +≡
constructor FraenkelTermObj.Init(const aPos: Position;
  aPostqual: PList;
  aSample: TermPtr;
  aFormula: FormulaPtr);
  begin nTermPos ← aPos; nTermSort ← wsFraenkelTerm; nPostqualification ← aPostqual;
  nSample ← aSample; nFormula ← aFormula;
  end;
destructor FraenkelTermObj.Done;
  begin dispose(nSample, Done); dispose(nPostqualification, Done); dispose(nFormula, Done);
  end;

```

786. Qualified terms. We may wish to explicitly type cast a term (e.g., “`term qua newType`”), which is what Mizar calls a “qualified term”.

```

⟨ Qualified term (abstract syntax tree) 786 ⟩ ≡
  QualifiedTermPtr = ↑QualifiedTermObj;
  QualifiedTermObj = object (ExactlyTermObj)
    nQualification: TypePtr;
    constructor Init(const aPos: Position; aSubject: TermPtr; aType: TypePtr);
    destructor Done; virtual;
  end

```

This code is used in section 755.

787. Constructor.

```

⟨ Implementing term AST 757 ⟩ +≡
constructor QualifiedTermObj.Init(const aPos: Position; aSubject: TermPtr; aType: TypePtr);
  begin nTermPos ← aPos; nTermSort ← wsQualificationTerm; nSubject ← aSubject;
  nQualification ← aType;
  end;
destructor QualifiedTermObj.Done;
  begin dispose(nSubject, Done); dispose(nQualification, Done);
  end;

```

788. Exactly terms. This is the base class for qualified terms. It does not appear to be used anywhere outside the abstract syntax module.

```

⟨ Exactly term (abstract syntax tree) 788 ⟩ ≡
  ExactlyTermPtr = ↑ExactlyTermObj;
  ExactlyTermObj = object (TermExpressionObj)
    nSubject: TermPtr;
    constructor Init(const aPos: Position; aSubject: TermPtr);
    destructor Done; virtual;
  end

```

This code is used in section 755.

789. Constructor.

```

⟨ Implementing term AST 757 ⟩ +≡
constructor ExactlyTermObj.Init(const aPos: Position; aSubject: TermPtr);
  begin nTermPos ← aPos; nTermSort ← wsExactlyTerm; nSubject ← aSubject;
  end;
destructor ExactlyTermObj.Done;
  begin dispose(nSubject, Done);
  end;

```

790. Choice terms. This refers to “the $\langle type \rangle$ ” terms. It is a “global choice term” of sorts, except it “operates” on soft types instead of arbitrary predicates.

```

< Choice term (abstract syntax tree) 790 > ≡
  ChoiceTermPtr = ↑ChoiceTermObj;
  ChoiceTermObj = object (TermExpressionObj)
    nChoiceType: TypePtr;
    constructor Init(const aPos: Position; aType: TypePtr);
    destructor Done; virtual;
end

```

This code is used in section 755.

791. Constructor.

```

< Implementing term AST 757 > +≡
constructor ChoiceTermObj.Init(const aPos: Position; aType: TypePtr);
  begin nTermPos ← aPos; nTermSort ← wsGlobalChoiceTerm; nChoiceType ← aType;
  end;
destructor ChoiceTermObj.Done;
  begin dispose(nChoiceType, Done);
  end;

```

792. It terms. When we define a new mode [type] or functors [terms], Mizar introduces an anaphoric keyword “it” referring to an example of the mode (resp., to the term being defined). Here I borrow the scary phrase “anaphoric” from Lisp macros, so blame Paul Graham for this pretentiousness.

```

< “It” term (abstract syntax tree) 792 > ≡
  ItTermPtr = ↑ItTermObj;
  ItTermObj = object (TermExpressionObj)
    constructor Init(const aPos: Position);
end

```

This code is used in section 755.

793. Constructor.

```

< Implementing term AST 757 > +≡
constructor ItTermObj.Init(const aPos: Position);
  begin nTermPos ← aPos; nTermSort ← wsItTerm;
  end;

```

794. Incorrect terms. Generically, when we run into an error of some kind, we represent the term with an *Incorrect* term instance. This will allow Mizar to continue working when the user goofed.

```

< Incorrect term (abstract syntax tree) 794 > ≡
  IncorrectTermPtr = ↑IncorrectTermObj;
  IncorrectTermObj = object (TermExpressionObj)
    constructor Init(const aPos: Position);
end

```

This code is used in section 755.

795. Constructor.

```

< Implementing term AST 757 > +≡
constructor IncorrectTermObj.Init(const aPos: Position);
  begin nTermPos ← aPos; nTermSort ← wsErrorTerm;
  end;

```

Section 20.2. TYPES (ABSTRACT SYNTAX TREE)

796. The grammar for Mizar types looks like:

```

Type-Expression = "(" Radix-Type ")"
| Adjective-Cluster Type-Expression
| Radix-Type .
Structure-Type-Expression =
  "(" Structure-Symbol ["over" Term-Expression-List] ")"
| Adjective-Cluster Structure-Symbol [ "over" Term-Expression-List ].
Radix-Type = Mode-Symbol [ "of" Term-Expression-List ]
| Structure-Symbol [ "over" Term-Expression-List ] .
Type-Expression-List = Type-Expression { "," Type-Expression } .

```

So there are several main sources of modes [types]: structures, primitive types (like “set” and “object”), and affixing adjectives to types.

For readers who are unfamiliar with types in Mizar, they are “soft types”. What does this mean? Well, we refer the reader to Free Wiedijk’s “Mizar’s Soft Type System” (in K. Schneider and J. Brandt, eds., *Theorem Proving in Higher Order Logics. TPHOLs 2007*, Springer, [doi:10.1007/978-3-540-74591-4_28](https://doi.org/10.1007/978-3-540-74591-4_28)). Essentially, a type ascription in Mizar of the form “for x being Foo st P[x] holds Q[x]”, this is equivalent to Foo being a unary predicate and the formula in first-order logic is “ $\forall x. \text{Foo}[x] \wedge Q[x] \implies P[x]$ ”.

797. We have an abstract base class for types.

```

< Abstract base class for types 797 > ≡
  TypeSort = (wsErrorType, wsStandardType, wsStructureType, wsClusteredType, wsReservedDscrType);
  { Initial structures }
  TypePtr = ↑TypeExpressionObj;
  TypeExpressionObj = object (MObject)
    nTypeSort: TypeSort;
    nTypePos: Position;
  end

```

This code is used in section 737.

798. Radix type. A “radix type” refers to any type of the form “ $\langle \text{RadixType} \rangle$ of T_1, \dots, T_n ”. This usually appears when defining a new expandable mode, where we have:

“mode $\langle \text{Expandable Mode} \rangle$ is $\langle \text{Adjective}_1 \rangle \dots \langle \text{Adjective}_n \rangle \langle \text{Radix Type} \rangle$ ”

This appears to be used only in definitions.

```

< Classes for type (abstract syntax tree) 798 > ≡
  { Types }
  RadixTypePtr = ↑RadixTypeObj;
  RadixTypeObj = object (TypeExpressionObj)
    nArgs: PList; { of }
    constructor Init(const aPos: Position; aKind: TypeSort; aArgs: PList);
    destructor Done; virtual;
  end ;

```

See also sections 800, 802, 804, and 806.

This code is used in section 737.

799. Constructor.

⟨Implementing type AST 799⟩ ≡
constructor *RadixTypeObj.Init*(**const** *aPos*: *Position*; *aKind*: *TypeSort*; *aArgs*: *PList*);
 begin *nTypePos* ← *aPos*; *nTypeSort* ← *aKind*; *nArgs* ← *aArgs*;
 end;
destructor *RadixTypeObj.Done*;
 begin *dispose*(*nArgs*, *Done*);
 end;

See also sections 801, 803, 805, and 807.

This code is used in section 736.

800. Standard type. When we want to refer to an expandable mode in a Mizar formula, then it is represented by a “standard type”. This contrasts it with “clustered types” (i.e., a type stacked with adjectives) and “structure types”.

⟨Classes for type (abstract syntax tree) 798⟩ +≡
 StandardTypePtr = ↑*StandardTypeObj*;
 StandardTypeObj = **object** (*RadixTypeObj*)
 nModeSymbol: *integer*;
 constructor *Init*(**const** *aPos*: *Position*; *aModeSymbol*: *integer*; *aArgs*: *PList*);
 destructor *Done*; *virtual*;
 end ;

801. Constructor.

⟨Implementing type AST 799⟩ +≡
constructor *StandardTypeObj.Init*(**const** *aPos*: *Position*; *aModeSymbol*: *integer*; *aArgs*: *PList*);
 begin *inherited Init*(*aPos*, *wsStandardType*, *aArgs*); *nModeSymbol* ← *aModeSymbol*;
 end;
destructor *StandardTypeObj.Done*;
 begin *inherited Done*;
 end;

802. Structure type. When we define a new structure, we are really introducing a new type. [[The *aArgs* tracks its parent structures and parameter types.]] The structure type extends the *RadixType* class because *RadixType* instances can be “stacked with adjectives”.

⟨Classes for type (abstract syntax tree) 798⟩ +≡
 StructTypePtr = ↑*StructTypeObj*;
 StructTypeObj = **object** (*RadixTypeObj*)
 nStructSymbol: *integer*;
 constructor *Init*(**const** *aPos*: *Position*; *aStructSymbol*: *integer*; *aArgs*: *PList*);
 destructor *Done*; *virtual*;
 end ;

803. Constructor.

⟨Implementing type AST 799⟩ +≡
constructor *StructTypeObj.Init*(**const** *aPos*: *Position*; *aStructSymbol*: *integer*; *aArgs*: *PList*);
 begin *inherited Init*(*aPos*, *wsStructureType*, *aArgs*); *nStructSymbol* ← *aStructSymbol*;
 end;
destructor *StructTypeObj.Done*;
 begin *inherited Done*;
 end;

804. Clustered type. The clustered type describes the situation where we accumulate *aCluster* of adjectives atop *aType*.

```

⟨ Classes for type (abstract syntax tree) 798 ⟩ +≡
  ClusteredTypePtr = ↑ClusteredTypeObj;
  ClusteredTypeObj = object (TypeExpressionObj)
    nAdjectiveCluster: PList;
    nType: TypePtr;
    constructor Init(const aPos: Position; aCluster: PList; aType: TypePtr);
    destructor Done; virtual;
end ;

```

805. Constructor.

```

⟨ Implementing type AST 799 ⟩ +≡
constructor ClusteredTypeObj.Init(const aPos: Position; aCluster: PList; aType: TypePtr);
  begin nTypePos ← aPos; nTypeSort ← wsClusteredType; nAdjectiveCluster ← aCluster;
  nType ← aType;
end;
destructor ClusteredTypeObj.Done;
  begin dispose(nAdjectiveCluster, Done); dispose(nType, Done);
end;

```

806. Incorrect type. We want Mizar to be resilient against typing errors, so we have an *IncorrectType* node for the syntax tree. The alternative would be to crash upon error.

```

⟨ Classes for type (abstract syntax tree) 798 ⟩ +≡
  IncorrectTypePtr = ↑IncorrectTypeObj;
  IncorrectTypeObj = object (TypeExpressionObj)
    constructor Init(const aPos: Position);
end

```

807. Constructor.

```

⟨ Implementing type AST 799 ⟩ +≡
constructor IncorrectTypeObj.Init(const aPos: Position);
  begin nTypePos ← aPos; nTypeSort ← wsErrorType;
end;

```

Section 20.3. FORMULAS (ABSTRACT SYNTAX TREE)

808. We have an abstract base class for formulas.

(Abstract base class for formulas 808) \equiv

```

FormulaSort = (wsErrorFormula, wsThesis, wsContradiction, wsRightSideOfPredicativeFormula,
wsPredicativeFormula, wsMultiPredicativeFormula, wsPrivatePredicateFormula,
wsAttributiveFormula, wsQualifyingFormula, wsUniversalFormula, wsExistentialFormula,
wsNegatedFormula, wsConjunctiveFormula, wsDisjunctiveFormula, wsConditionalFormula,
wsBiconditionalFormula, wsFlexaryConjunctiveFormula, wsFlexaryDisjunctiveFormula);
FormulaPtr =  $\uparrow$ FormulaExpressionObj;
FormulaExpressionObj = object (MObject)
  nFormulaSort: FormulaSort;
  nFormulaPos: Position;
end

```

This code is used in section 737.

809. The syntax for Mizar formulas looks like:

```

Formula-Expression = "(" Formula-Expression ")"
| Atomic-Formula-Expression
| Quantified-Formula-Expression
| Formula-Expression "&" Formula-Expression
| Formula-Expression "&" "." "&" Formula-Expression
| Formula-Expression "or" Formula-Expression
| Formula-Expression "or" "." "or" Formula-Expression
| Formula-Expression "implies" Formula-Expression
| Formula-Expression "iff" Formula-Expression
| "not" Formula-Expression
| "contradiction"
| "thesis" .

Atomic-Formula-Expression =
  [Term-Expression-List] [("does" | "do") "not"] Predicate-Symbol [Term-Expression-List]
  { [("does" | "do") "not"] Predicate-Symbol Term-Expression-List }
| Predicate-Identifier "[" [ Term-Expression-List ] "]"
| Term-Expression "is" Adjective { Adjective }
| Term-Expression "is" Type-Expression .

Quantified-Formula-Expression =
  "for" Qualified-Variables
  [ "st" Formula-Expression ]
  ( "holds" Formula-Expression | Quantified-Formula-Expression )
| "ex" Qualified-Variables "st" Formula-Expression .

```

810. Right-side of predicative formula.

⟨Classes for formula (abstract syntax tree) 810⟩ ≡
 { Formulas }
RightSideOfPredicativeFormulaPtr = \uparrow *RightSideOfPredicativeFormulaObj*;
RightSideOfPredicativeFormulaObj = **object** (*FormulaExpressionObj*)
 nPredNr: integer;
 nRightArgs: PList;
 constructor *Init*(**const** *aPos*: Position; *aPredNr*: integer; *aRightArgs*: PList);
 destructor *Done*; virtual;
end

See also sections 812, 814, 816, 818, 820, 822, 824, 826, 828, 830, 832, 834, 836, 838, 840, 842, 844, 846, and 848.

This code is used in section 737.

811. Constructor.

⟨Implementing formula AST 811⟩ ≡
constructor *RightSideOfPredicativeFormulaObj.Init*(**const** *aPos*: Position;
 aPredNr: integer;
 aRightArgs: PList);
begin *nFormulaPos* \leftarrow *aPos*; *nFormulaSort* \leftarrow *wsRightSideOfPredicativeFormula*;
 nPredNr \leftarrow *aPredNr*; *nRightArgs* \leftarrow *aRightArgs*;
end;
destructor *RightSideOfPredicativeFormulaObj.Done*;
begin *dispose*(*nRightArgs*, *Done*);
end;

See also sections 813, 815, 817, 819, 821, 823, 825, 827, 829, 831, 833, 835, 837, 839, 841, 843, 845, 847, and 849.

This code is used in section 736.

812. Predicative formula. A “predicative” formula refers to a formula involving predicates. A predicate will have a list of terms \vec{t} it expects as arguments, as well as two numbers ℓ, r such that t_1, \dots, t_ℓ are the arguments to its left, and $t_{\ell+1}, \dots, t_{\ell+r}$ are on the right. When $\ell = 0$, all arguments are on the right; and when $r = 0$, all arguments are on the left.

⟨Classes for formula (abstract syntax tree) 810⟩ +≡
PredicativeFormulaPtr = \uparrow *PredicativeFormulaObj*;
PredicativeFormulaObj = **object** (*RightSideOfPredicativeFormulaObj*)
 nLeftArgs: PList;
 constructor *Init*(**const** *aPos*: Position; *aPredNr*: integer; *aLeftArgs*, *aRightArgs*: PList);
 destructor *Done*; virtual;
end

813. Constructor.

⟨Implementing formula AST 811⟩ +≡
constructor *PredicativeFormulaObj.Init*(**const** *aPos*: Position;
 aPredNr: integer;
 aLeftArgs, *aRightArgs*: PList);
begin *nFormulaPos* \leftarrow *aPos*; *nFormulaSort* \leftarrow *wsPredicativeFormula*; *nPredNr* \leftarrow *aPredNr*;
 nLeftArgs \leftarrow *aLeftArgs*; *nRightArgs* \leftarrow *aRightArgs*;
end;
destructor *PredicativeFormulaObj.Done*;
begin *dispose*(*nLeftArgs*, *Done*); *dispose*(*nRightArgs*, *Done*);
end;

814. Multi-predicative formula. The Working Mathematician writes things like “ $1 \leq i \leq \|T\|$ ” and Mizar wants to support this. Multi-predicative formulas are of this form “ $1 \leq i \leq \|T\|$ ”. This occurs in VECTSP13, for example.

```

⟨Classes for formula (abstract syntax tree) 810⟩ +=
  MultiPredicativeFormulaPtr = ↑MultiPredicativeFormulaObj;
  MultiPredicativeFormulaObj = object (FormulaExpressionObj)
    nScraps: PList;
    constructor Init(const aPos: Position; aScraps: PList);
    destructor Done; virtual;
end

```

815. Constructor.

```

⟨Implementing formula AST 811⟩ +=
constructor MultiPredicativeFormulaObj.Init(const aPos: Position; aScraps: PList);
  begin nFormulaPos ← aPos; nFormulaSort ← wsMultiPredicativeFormula; nScraps ← aScraps;
  end;
destructor MultiPredicativeFormulaObj.Done;
  begin dispose(nScraps, Done);
  end;

```

816. Attributive formula. As part of Mizar’s soft type system, we can use attributes (adjectives) to form a formula like “ $\langle term \rangle$ is $\langle adjective \rangle$ ”. We can stack multiple adjectives in an attributive formula.

```

⟨Classes for formula (abstract syntax tree) 810⟩ +=
  AttributiveFormulaPtr = ↑AttributiveFormulaObj;
  AttributiveFormulaObj = object (FormulaExpressionObj)
    nSubject: TermPtr;
    nAdjectives: PList;
    constructor Init(const aPos: Position; aSubject: TermPtr; aAdjectives: PList);
    destructor Done; virtual;
end

```

817. Constructor.

```

⟨Implementing formula AST 811⟩ +=
constructor AttributiveFormulaObj.Init(const aPos: Position; aSubject: TermPtr; aAdjectives: PList);
  begin nFormulaPos ← aPos; nFormulaSort ← wsAttributiveFormula; nSubject ← aSubject;
  nAdjectives ← aAdjectives;
  end;
destructor AttributiveFormulaObj.Done;
  begin dispose(nSubject, Done); dispose(nAdjectives, Done);
  end;

```

818. Private predicative formula. When we have “**defpred** P[...] **means** ...” in Mizar, we refer to “P” as a private predicate. It is represented in the abstract syntax tree as a private predicative formula object.

```

⟨Classes for formula (abstract syntax tree) 810⟩ +≡
  PrivatePredicativeFormulaPtr = ↑PrivatePredicativeFormulaObj;
  PrivatePredicativeFormulaObj = object (FormulaExpressionObj)
    nPredIdNr: integer;
    nArgs: PList;
    constructor Init(const aPos: Position; aPredIdNr: integer; aArgs: PList);
    destructor Done; virtual;
end

```

819. Constructor.

```

⟨Implementing formula AST 811⟩ +≡
constructor PrivatePredicativeFormulaObj.Init(const aPos: Position;
    aPredIdNr: integer;
    aArgs: PList);
  begin nFormulaPos ← aPos; nFormulaSort ← wsPrivatePredicateFormula; nPredIdNr ← aPredIdNr;
  nArgs ← aArgs;
  end;
destructor PrivatePredicativeFormulaObj.Done;
  begin dispose(nArgs, Done);
  end;

```

820. Qualifying formula. Using Mizar’s soft type system, we may have formulas of the form “⟨term⟩ is ⟨type⟩”. These are referred to as “qualifying formulas”, at least when discussing the abstract syntax tree.

```

⟨Classes for formula (abstract syntax tree) 810⟩ +≡
  QualifyingFormulaPtr = ↑QualifyingFormulaObj;
  QualifyingFormulaObj = object (FormulaExpressionObj)
    nSubject: TermPtr;
    nType: TypePtr;
    constructor Init(const aPos: Position; aSubject: TermPtr; aType: TypePtr); y
    destructor Done; virtual;
end

```

821. Constructor.

```

⟨Implementing formula AST 811⟩ +≡
constructor QualifyingFormulaObj.Init(const aPos: Position; aSubject: TermPtr; aType: TypePtr);
  begin nFormulaPos ← aPos; nFormulaSort ← wsQualifyingFormula; nSubject ← aSubject;
  nType ← aType;
  end;
destructor QualifyingFormulaObj.Done;
  begin dispose(nSubject, Done); dispose(nType, Done);
  end;

```

822. Negative formula. Now we can proceed with the familiar formulas in first-order logic. Negative formulas are of the form $\neg\varphi$ for some formula φ .

```

⟨ Classes for formula (abstract syntax tree) 810 ⟩ +=
  NegativeFormulaPtr = ↑NegativeFormulaObj;
  NegativeFormulaObj = object (FormulaExpressionObj)
    nArg: FormulaPtr;
    constructor Init(const aPos: Position; aArg: FormulaPtr);
    destructor Done; virtual;
end

```

823. Constructor.

```

⟨ Implementing formula AST 811 ⟩ +=
constructor NegativeFormulaObj.Init(const aPos: Position; aArg: FormulaPtr);
  begin nFormulaPos ← aPos; nFormulaSort ← wsNegatedFormula; nArg ← aArg;
  end;
destructor NegativeFormulaObj.Done;
  begin dispose(nArg, Done);
  end;

```

824. Binary arguments formula. We have a class describing formulas involving binary logical connectives. We will extend it to describe conjunctive formulas, disjunctive formulas, conditionals, biconditionals, etc.

```

⟨ Classes for formula (abstract syntax tree) 810 ⟩ +=
  BinaryFormulaPtr = ↑BinaryArgumentsFormula;
  BinaryArgumentsFormula = object (FormulaExpressionObj)
    nLeftArg, nRightArg: FormulaPtr;
    constructor Init(const aPos: Position; aLeftArg, aRightArg: FormulaPtr);
    destructor Done; virtual;
end

```

825. Constructor.

```

⟨ Implementing formula AST 811 ⟩ +=
constructor BinaryArgumentsFormula.Init(const aPos: Position; aLeftArg, aRightArg: FormulaPtr);
  begin nFormulaPos ← aPos; nLeftArg ← aLeftArg; nRightArg ← aRightArg;
  end;
destructor BinaryArgumentsFormula.Done;
  begin dispose(nLeftArg, Done); dispose(nRightArg, Done);
  end;

```

826. Conjunctive formula. A conjunctive formula looks like $\varphi \wedge \psi$ where φ and ψ are logical formulas.

```

⟨ Classes for formula (abstract syntax tree) 810 ⟩ +=
  ConjunctiveFormulaPtr = ↑ConjunctiveFormulaObj;
  ConjunctiveFormulaObj = object (BinaryArgumentsFormula)
    constructor Init(const aPos: Position; aLeftArg, aRightArg: FormulaPtr);
end

```

827. Constructor.

⟨Implementing formula AST 811⟩ +≡

```
constructor ConjunctiveFormulaObj.Init(const aPos: Position; aLeftArg, aRightArg: FormulaPtr);
  begin inherited Init(aPos, aLeftArg, aRightArg); nFormulaSort ← wsConjunctiveFormula;
  end;
```

828. Disjunctive formula. Disjunctive formulas look like $\varphi \vee \psi$ where φ and ψ are formulas.

⟨Classes for formula (abstract syntax tree) 810⟩ +≡

```
DisjunctiveFormulaPtr = ↑DisjunctiveFormulaObj;
DisjunctiveFormulaObj = object (BinaryArgumentsFormula)
  constructor Init(const aPos: Position; aLeftArg, aRightArg: FormulaPtr);
  end
```

829. Constructor.

⟨Implementing formula AST 811⟩ +≡

```
constructor DisjunctiveFormulaObj.Init(const aPos: Position;
  aLeftArg, aRightArg: FormulaPtr);
  begin inherited Init(aPos, aLeftArg, aRightArg); nFormulaSort ← wsDisjunctiveFormula;
  end;
```

830. Conditional formula. Conditional formulas look like $\varphi \implies \psi$ where φ and ψ are formulas.

⟨Classes for formula (abstract syntax tree) 810⟩ +≡

```
ConditionalFormulaPtr = ↑ConditionalFormulaObj;
ConditionalFormulaObj = object (BinaryArgumentsFormula)
  constructor Init(const aPos: Position; aLeftArg, aRightArg: FormulaPtr);
  end
```

831. Constructor.

⟨Implementing formula AST 811⟩ +≡

```
constructor ConditionalFormulaObj.Init(const aPos: Position; aLeftArg, aRightArg: FormulaPtr);
  begin inherited Init(aPos, aLeftArg, aRightArg); nFormulaSort ← wsConditionalFormula;
  end;
```

832. Biconditional formula. Biconditional formulas look like $\varphi \iff \psi$ where φ and ψ are formulas.

⟨Classes for formula (abstract syntax tree) 810⟩ +≡

```
BiconditionalFormulaPtr = ↑BiconditionalFormulaObj;
BiconditionalFormulaObj = object (BinaryArgumentsFormula)
  constructor Init(const aPos: Position; aLeftArg, aRightArg: FormulaPtr);
  end
```

833. Constructor.

⟨Implementing formula AST 811⟩ +≡

```
constructor BiconditionalFormulaObj.Init(const aPos: Position; aLeftArg, aRightArg: FormulaPtr);
  begin inherited Init(aPos, aLeftArg, aRightArg); nFormulaSort ← wsBiconditionalFormula;
  end;
```

834. Flexary Conjunctive formula. Flexary conjunctive formulas are unique to Mizar, though the Working Mathematician would recognize them as “just a bunch of conjunctions”. These look like $\varphi[1] \wedge \dots \wedge \varphi[n]$ where $\varphi[i]$ is a formula parametrized by a natural number i .

```

⟨Classes for formula (abstract syntax tree) 810⟩ +=
  FlexaryConjunctiveFormulaPtr = ↑FlexaryConjunctiveFormulaObj;
  FlexaryConjunctiveFormulaObj = object (BinaryArgumentsFormula)
    constructor Init(const aPos: Position; aLeftArg, aRightArg: FormulaPtr);
  end

```

835. Constructor.

```

⟨Implementing formula AST 811⟩ +=
constructor FlexaryConjunctiveFormulaObj.Init(const aPos: Position;
                                              aLeftArg, aRightArg: FormulaPtr);
begin inherited Init(aPos, aLeftArg, aRightArg); nFormulaSort ← wsFlexaryConjunctiveFormula;
end;

```

836. Flexary Disjunctive formula. Flexary disjunctive formulas are unique to Mizar, though the Working Mathematician would recognize them as “just a bunch of disjunctions”. These look like $\varphi[1] \vee \dots \vee \varphi[n]$ where $\varphi[i]$ is a formula parametrized by a natural number i .

```

⟨Classes for formula (abstract syntax tree) 810⟩ +=
  FlexaryDisjunctiveFormulaPtr = ↑FlexaryDisjunctiveFormulaObj;
  FlexaryDisjunctiveFormulaObj = object (BinaryArgumentsFormula)
    constructor Init(const aPos: Position; aLeftArg, aRightArg: FormulaPtr);
  end

```

837. Constructor.

```

⟨Implementing formula AST 811⟩ +=
constructor FlexaryDisjunctiveFormulaObj.Init(const aPos: Position;
                                              aLeftArg, aRightArg: FormulaPtr);
begin inherited Init(aPos, aLeftArg, aRightArg); nFormulaSort ← wsFlexaryDisjunctiveFormula;
end;

```

838. Quantified formula. First-order logic is distinguished by the use of terms and quantifying formulas over terms. We have a base class for quantified formulas. Using the Mizar soft type system, quantified variables are “qualified segments”.

```

⟨Classes for formula (abstract syntax tree) 810⟩ +=
  QuantifiedFormulaPtr = ↑QuantifiedFormulaObj;
  QuantifiedFormulaObj = object (FormulaExpressionObj)
    nSegment: QualifiedSegmentPtr;
    nScope: FormulaPtr;
    constructor Init(const aPos: Position; aSegment: QualifiedSegmentPtr; aScope: FormulaPtr);
    destructor Done; virtual;
  end

```


839. Constructor.

⟨Implementing formula AST 811⟩ +≡

```

constructor QuantifiedFormulaObj.Init(const aPos: Position;
                                         aSegment: QualifiedSegmentPtr;
                                         aScope: FormulaPtr);
    begin nFormulaPos ← aPos; nSegment ← aSegment; nScope ← aScope;
    end;

destructor QuantifiedFormulaObj.Done;
    begin dispose(nSegment, Done); dispose(nScope, Done);
    end;

```

840. Universal formula. When we want to describe a formula of the form “ $\forall x : T. \varphi[x]$ ” where T is a soft type and $\varphi[x]$ is a formula parametrized by x .

⟨Classes for formula (abstract syntax tree) 810⟩ +≡

```

UniversalFormulaPtr = ↑UniversalFormulaObj;
UniversalFormulaObj = object (QuantifiedFormulaObj)
    constructor Init(const aPos: Position; aSegment: QualifiedSegmentPtr; aScope: FormulaPtr);
    end

```

841. Constructor.

⟨Implementing formula AST 811⟩ +≡

```

constructor UniversalFormulaObj.Init(const aPos: Position;
                                         aSegment: QualifiedSegmentPtr;
                                         aScope: FormulaPtr);
    begin inherited Init(aPos, aSegment, aScope); nFormulaSort ← wsUniversalFormula;
    end;

```

842. Existential formula. The other quantified formula are existentially quantified formulas, which resemble “ $\exists x : T. \varphi[x]$ ” where T is a soft type and $\varphi[x]$ is a formula parametrized by x .

⟨Classes for formula (abstract syntax tree) 810⟩ +≡

```

ExistentialFormulaPtr = ↑ExistentialFormulaObj;
ExistentialFormulaObj = object (QuantifiedFormulaObj)
    constructor Init(const aPos: Position; aSegment: QualifiedSegmentPtr; aScope: FormulaPtr);
    end

```

843. Constructor.

⟨Implementing formula AST 811⟩ +≡

```

constructor ExistentialFormulaObj.Init(const aPos: Position;
                                         aSegment: QualifiedSegmentPtr;
                                         aScope: FormulaPtr);
    begin inherited Init(aPos, aSegment, aScope); nFormulaSort ← wsExistentialFormula;
    end;

```

844. Contradiction formula. The canonical contradiction \perp in Mizar is represented by the reserved keyword “contradiction”.

⟨Classes for formula (abstract syntax tree) 810⟩ +≡

```

ContradictionFormulaPtr = ↑ContradictionFormulaObj;
ContradictionFormulaObj = object (FormulaExpressionObj)
    constructor Init(const aPos: Position);
    end

```

845. Constructor.

⟨ Implementing formula AST 811 ⟩ +≡
constructor *ContradictionFormulaObj.Init*(**const** *aPos*: *Position*);
 begin *nFormulaPos* ← *aPos*; *nFormulaSort* ← *wsContradiction*;
 end;

846. Thesis formula. When we are in the middle of a proof, the goal or obligation left to be proven is called the “thesis”.

⟨ Classes for formula (abstract syntax tree) 810 ⟩ +≡
 ThesisFormulaPtr = ↑*ThesisFormulaObj*;
 ThesisFormulaObj = **object** (*FormulaExpressionObj*)
 constructor *Init*(**const** *aPos*: *Position*);
 end

847. Constructor.

⟨ Implementing formula AST 811 ⟩ +≡
constructor *ThesisFormulaObj.Init*(**const** *aPos*: *Position*);
 begin *nFormulaPos* ← *aPos*; *nFormulaSort* ← *wsThesis*;
 end;

848. Incorrect formula. We also have a node in abstract syntax trees for “incorrect” formulas.

⟨ Classes for formula (abstract syntax tree) 810 ⟩ +≡
 IncorrectFormulaPtr = ↑*IncorrectFormula*;
 IncorrectFormula = **object** (*FormulaExpressionObj*)
 constructor *Init*(**const** *aPos*: *Position*);
 end

849. Constructor.

⟨ Implementing formula AST 811 ⟩ +≡
constructor *IncorrectFormula.Init*(**const** *aPos*: *Position*);
 begin *nFormulaPos* ← *aPos*; *nformulaSort* ← *wsErrorFormula*;
 end;

File 21

Weakly strict Mizar article

850. The parser “eats in” a mizar article, then produces a `.wsx` (weakly strict Mizar) XML file containing the abstract syntax tree, and also a `.ftr` article containing the formats for the article.

This strategy should be familiar to anyone who has looked into compilers and interpreters: transform the abstract syntax tree into an intermediate representation, then transform the intermediate representations in various passes.

This module will transform the parse tree to an abstract syntax tree in XML format.

```

< wsmarticle.pas 850 > ≡
  < GNU License 4 >
unit wsmarticle;
interface
uses mobjects, errhan, mscanner, syntax, abstract_syntax, xml_dict, xml_inout;
  < Publicly declared types in wsmarticle.pas 852 >
const
  < Publicly declared constants in wsmarticle.pas 855 >
  < Publicly declared functions in wsmarticle.pas 853 >
  < Global variables publicly declared in wsmarticle.pas 1007 >
implementation
uses mizenv, mconsole, librenv, scanner, xml_parser
      mdebug, info end_mdebug;
  < Implementation for wsmarticle.pas 854 >
end .

```

851. Exercise. We will create a class hierarchy for the abstract syntax trees for Mizar. A lot of this is boiler-plate. The reader is invited to write a couple of programs which will:

- (1) read in an EBNF-like grammar and emit the class hierarchy for its abstract syntax tree.
- (2) read in an EBNF-like grammar, and emit the class hierarchy for generating the XML for it.

After all, if you look at the sheer number of sections in this file, it’s staggeringly huge. But a lot of it is boiler-plate.

852. < Publicly declared types in wsmarticle.pas 852 > ≡

See also sections 856, 862, 864, 867, 868, 870, 871, 875, 877, 879, 881, 884, 886, 888, 890, 893, 895, 897, 900, 906, 909, 911, 913, 915, 916, 924, 926, 928, 930, 946, 948, 950, 952, 954, 956, 958, 960, 962, 964, 966, 968, 970, 972, 974, 976, 978, 980, 982, 984, 987, 989, 991, 993, 995, 997, 999, 1001, 1003, 1014, 1097, and 1148.

This code is used in section 850.

853. < Publicly declared functions in wsmarticle.pas 853 > ≡

This code is used in section 850.

854. \langle Implementation for `wsmarticle.pas` 854 $\rangle \equiv$

See also sections 857, 858, 861, 863, 865, 869, 872, 876, 878, 880, 882, 885, 887, 889, 891, 894, 896, 898, 901, 907, 910, 912, 914, 917, 918, 925, 927, 929, 931, 934, 936, 938, 940, 942, 947, 949, 951, 953, 955, 957, 959, 961, 963, 965, 967, 969, 971, 973, 975, 977, 979, 981, 983, 985, 988, 990, 992, 994, 996, 998, 1000, 1002, 1004, 1005, 1006, 1008, 1013, 1015, 1016, 1017, 1018, 1019, 1020, 1021, 1022, 1023, 1024, 1025, 1026, 1027, 1042, 1043, 1044, 1045, 1058, 1059, 1060, 1061, 1067, 1068, 1069, 1070, 1071, 1072, 1073, 1074, 1075, 1076, 1077, 1078, 1079, 1080, 1095, 1098, 1099, 1100, 1101, 1102, 1103, 1104, 1105, 1106, 1107, 1108, 1109, 1110, 1111, 1112, 1113, 1114, 1115, 1118, 1119, 1120, 1121, 1122, 1123, 1124, 1125, 1126, 1127, 1128, 1129, 1130, 1131, 1132, 1133, 1134, 1135, 1136, 1137, 1138, 1139, 1140, 1141, 1142, 1143, 1144, 1145, 1146, 1147, 1149, 1150, 1151, 1152, 1153, 1154, 1155, 1156, 1157, 1158, 1159, 1160, 1161, 1162, 1163, 1164, 1165, 1166, 1167, 1168, 1169, 1170, 1171, 1172, 1173, 1174, 1175, 1176, 1177, 1178, 1179, 1180, 1181, 1182, 1183, 1184, 1185, 1186, 1187, 1188, 1189, 1190, 1191, and 1192.

This code is used in section 850.

Section 21.1. WEAKLY STRICT TEXT PROPER

855. Mizar provides a grammar for its syntax in the file
It uses a variant of EBNF:

/usr/local/doc/mizar/syntax

- Terminal symbols are written "in quotes"
- Production rules are separated by vertical lines "|"
- Optional symbols are placed in [brackets]
- Repeated items zero or more times are placed in {braces}.
- Rules end in a period "."

We will freely quote from `syntax.txt`, rearranging the rules as needed to discuss the relevant parts of Mizar's grammar. We will write the `syntax.txt` passages in typewriter font.

We should recall the syntax for text items:

```
Text-Propor = Section { Section } .
Section = "begin" { Text-Item } .
Text-Item = Reservation
| Definitional-Item
| Registration-Item
| Notation-Item
| Theorem
| Scheme-Item
| Auxiliary-Item .
Definitional-Item = Definitional-Block ";" .
Registration-Item = Registration-Block ";" .
Theorem = "theorem" Compact-Statement .
Compact-Statement = Proposition Justification ";" .
Justification = Simple-Justification | Proof .
Auxiliary-Item = Statement | Private-Definition .
```

These are the different syntactic classes for "top-level statements" in the text (not the environment header) of a Mizar article. The interested reader can investigate the `syntax.txt` file more fully to get all the block statements in Mizar. We have already made these different kinds of blocks syntactic values of *BlockKind* earlier (§692). Now we want to be able to translate them into English. We will just skip ahead and make these different syntactic classes into values of an enumerated type.

(Publicly declared constants in `wsmarticle.pas` 855) \equiv

```
BlockName: array [BlockKind] of string =
  ( `Text-Propor`, { blMain }
  `Now-Reasoning`, { blDiffuse }
  `Hereby-Reasoning`, { blHereby }
  `Proof`, { blProof }
  `Definitional-Block`, { blDefinition }
  `Notation-Block`, { blNotation }
  `Registration-Block`, { blRegistration }
  `Case`, { blCase }
  `Suppose`, { blSuppose }
  `Scheme-Block` { blPublicScheme } );
```

This code is used in section 850.

856. Class hierarchy for blocks. We can now translate the grammar for blocks into a class hierarchy. The “text proper” extends an abstract “block” statement. We will provide factory methods “*wsTextProper.NewBlock*” and “*NewItem*” for adding a new block (and item) contained within the caller “block”. We will be tracking the “kind” of block (§692), and the text proper will need to track which article it belongs to.

All the various kinds of blocks are handled with this one class: proofs, definitions, notations, registrations, cases, suppose blocks, schemes, hereby statements, and so on. However, some of these blocks have extra content which needs their own nodes in the abstract syntax tree, especially Definitions (§§943 *et seq.*) and Registrations (§§986 *et seq.*).

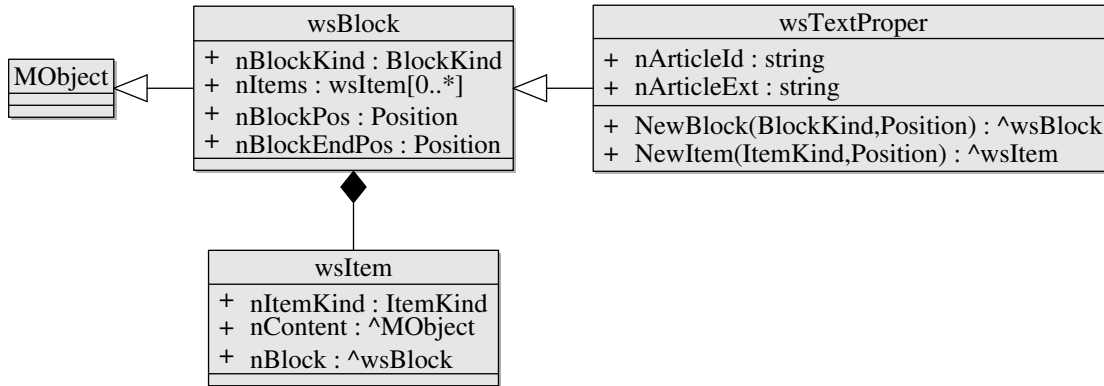


Fig. 4. UML class diagram for *wsBlock* and related classes.

It is important to stress: **wsBlock instances represent all statements which are block statements and all other statements are wsItem instances.** Looking back at the different kinds of blocks, you see that they are “block openers” and will expect to have a matching “end” statement closing it.

```

⟨ Publicly declared types in wsmarticle.pas 852 ⟩ +=
  wsBlockPtr = ↑wsBlock;
  wsBlock = object (MObject)
    nBlockKind: BlockKind;
    nItems: PList; { list of wsItem objects }
    nBlockPos, nBlockEndPos: Position;
    constructor Init(aBlockKind : BlockKind ; const aPos: Position);
    destructor Done; virtual;
  end ;
  ⟨ Weakly strict Item class 860 ⟩;
  wsTextProperPtr = ↑wsTextProper;
  wsTextProper = object (wsBlock)
    nArticleID, nArticleExt: string;
    constructor Init(const aArticleID, aArticleExt: string ; const aPos: Position);
    destructor Done; virtual;
    function NewBlock(aBlockKind : BlockKind ; const aPos: Position): wsBlockPtr;
    function NewItem(aItemKind : ItemKind ; const aPos: Position): wsItemPtr;
  end ;
  
```

857. Constructor. We initialize using the inherited *wsBlock* constructor (§859). The “text proper” refers to a block which is as top-level as possible, so we construct it as a block whose kind is *blMain* located at *aPos*.

```

⟨Implementation for wsmarticle.pas 854⟩ +≡
constructor wsTextProper.Init(const aArticleID, aArticleExt: string; const aPos: Position);
  begin inherited Init(blMain, aPos); nArticleID ← aArticleID; nArticleExt ← aArticleExt;
  end;
destructor wsTextProper.Done;
  begin inherited Done;
  end;

```

858. Adding statements into a block. we will add a block to a “text proper”, which will then construct a block which tracks the caller as its containing block. This requires giving the kind of the newly minted block (§692).

Similarly, when constructing an item which is contained in the block, we need to pass along the item kind (§702).

```

⟨Implementation for wsmarticle.pas 854⟩ +≡
function wsTextProper.NewBlock(aBlockKind : BlockKind ; const aPos: Position): wsBlockPtr;
  begin result ← new(WSBlockPtr, Init(aBlockKind, CurPos));
  end;
function wsTextProper.NewItem(aItemKind : ItemKind ; const aPos: Position): wsItemPtr;
  begin result ← new(wsItemPtr, Init(aItemKind, CurPos));
  end;

```

859. Block Constructor. Curiously, the *MObject* constructor (§187) is not invoked when constructing a *wsBlock*. We will also need the position (§103) of the block in the article. The collection of items in the block is initialized to be empty.

```

constructor wsBlock.Init(aBlokKind : BlockKind ; const aPos: Position);
  begin nBlockKind ← aBlokKind; nBlockPos ← aPos; nBlockEndPos ← aPos;
  nItems ← New(PList, Init(0));
  end;
destructor wsBlock.Done;
  begin dispose(nItems, Done); inherited Done;
  end;

```

860. Text items. An item requires its “kind” (§702) for its syntactic class.

```

⟨Weakly strict Item class 860⟩ ≡
  wsItemPtr = ↑wsItem;
  wsItem = object (MObject)
    nItemKind: ItemKind;
    nItemPos, nItemEndPos: Position;
    nContent: PObject;
    nBlock: wsBlockPtr;
    constructor Init(aItemKind : ItemKind ; const aPos: Position);
    destructor Done; virtual;
  end ;

```

This code is used in section 856.

861. Constructor

⟨Implementation for `wsmarticle.pas 854`⟩ +≡
constructor *wsItem.Init*(*aItemKind* : *ItemKind* ; **const** *aPos*: *Position*);
 begin *nItemKind* ← *aItemKind*; *nItemPos* ← *aPos*; *nItemEndPos* ← *aPos*; *nContent* ← **nil**;
 nBlock ← **nil**;
 end;
destructor *wsItem.Done*;
 begin **if** *nBlock* ≠ **nil** **then** *dispose*(*nBlock*, *Done*);
 inherited Done;
 end;

862. Pragmas. Mizar supports pragmas (analogous to conditional compilation).

⟨Publicly declared types in `wsmarticle.pas 852`⟩ +≡
PragmaPtr = ↑*PragmaObj*;
PragmaObj = **object** (*MObject*)
 nPragmaStr: *string*;
 constructor *Init*(*aStr* : *string*);
end ;

863. Constructor.

⟨Implementation for `wsmarticle.pas 854`⟩ +≡
constructor *PragmaObj.Init*(*aStr* : *string*);
 begin *nPragmaStr* ← *aStr*;
 end;

864. Labels and propositions. A proposition is just a sentence with a label. We will need to represent both of these in our abstract syntax tree.

⟨Publicly declared types in `wsmarticle.pas 852`⟩ +≡
LabelPtr = ↑*LabelObj*;
LabelObj = **object** (*MObject*)
 nLabelIdNr: *integer*;
 nLabelPos: *Position*;
 constructor *Init*(*aLabelId* : *integer* ; **const** *aPos*: *Position*);
end ;
PropositionPtr = ↑*PropositionObj*;
PropositionObj = **object** (*mObject*)
 nLab: *LabelPtr*;
 nSntPos: *Position*;
 nSentence: *FormulaPtr*;
 constructor *Init*(*aLab* : *LabelPtr*; *aSentence* : *FormulaPtr* ; **const** *aSntPos*: *Position*);
 destructor *Done*; *virtual*;
end ;

865. Constructor.

```

⟨Implementation for wsmarticle.pas 854⟩ +≡
constructor LabelObj.Init(aLabelId : integer ; const aPos: Position);
  begin nLabelIdNr ← aLabelId; nLabelPos ← aPos;
  end;
constructor PropositionObj.Init(alab : LabelPtr; aSentence : FormulaPtr ; const aSntPos: Position);
  begin nLab ← aLab; nSntPos ← aSntPos; nSentence ← aSentence;
  end;
destructor PropositionObj.Done;
  begin dispose(nLab, Done); dispose(nSentence, Done);
  end;

```

866. References. References are either local (i.e., from the file being processed) or library (i.e., from the Mizar math library). The grammar for library references is rather generous. The basic rules are that we have theorem references,

$$\langle article \rangle : \langle number \rangle$$

and definition references,

$$\langle article \rangle : \text{def } \langle number \rangle$$

and scheme references,

$$\langle article \rangle : \text{sch } \langle number \rangle$$

What makes it tricky is we also allow multiple references from the same article to just add a comma followed by the theorem number

$$\langle article \rangle : \langle number \rangle \{ , \langle number \rangle \}$$

or a comma followed by definition numbers

$$\langle article \rangle : \text{def } \langle number \rangle \{ , \text{def } \langle number \rangle \}$$

So far, so good, right? Now we can go even further, mixing theorem references and definitions references from the same article.

We recall the grammar for references:

```

Reference = Local-Reference | Library-Reference .
Scheme-Reference = Local-Scheme-Reference
  | Library-Scheme-Reference .
Local-Reference = Label-Identifier .
Local-Scheme-Reference = Scheme-Identifier .
Library-Reference = Article-Name ":" ( Theorem-Number | "def" Definition-Number )
  { ",", ( Theorem-Number | "def" Definition-Number ) } .
Library-Scheme-Reference = Article-Name ":" "sch" Scheme-Number .

```

867. Class structure. We have an abstract “reference” class, which is either a local reference (to a label within the article) or a library reference (to some result in the MML).

```

⟨ Publicly declared types in wsmarticle.pas 852 ⟩ +≡
  ReferenceKind = (LocalReference, TheoremReference, DefinitionReference);
  ⟨ Inference kinds (wsmarticle.pas) 874 ⟩;
  ReferencePtr = ↑ReferenceObj;
  ReferenceObj = object (MObject)
    nRefSort: ReferenceKind;
    nRefPos: Position;
  end;

```

868. Local references.

```

⟨ Publicly declared types in wsmarticle.pas 852 ⟩ +≡
  LocalReferencePtr = ↑LocalReferenceObj;
  LocalReferenceObj = object (ReferenceObj)
    nLabId: integer;
    constructor Init(aLabId : integer ; const aPos: Position);
  end ;

```

869. Constructor. The reference constructors simply populate the appropriate fields in the reference, and the position in the article’s text.

```

⟨ Implementation for wsmarticle.pas 854 ⟩ +≡
constructor LocalReferenceObj.Init(aLabId : integer;
  const aPos: Position);
begin nRefSort ← LocalReference; nLabId ← aLabId; nRefPos ← aPos
end;

```

870. Library references. This is the abstract class representing either theorem or definition references from an article.

```

⟨ Publicly declared types in wsmarticle.pas 852 ⟩ +≡
  LibraryReferencePtr = ↑LibraryReferenceObj;
  LibraryReferenceObj = object (ReferenceObj)
    nArticleNr: integer;
  end;

```

871. Theorem and definition references. I am of a divided mind here. On the one hand, we can see that a *LibraryReference* is a tagged union already, and we do not need separate subclasses for theorem references and definition references. On the other hand, separate subclasses makes things easier when emitting XML for the abstract syntax tree for a Mizar article. Since it is more clear with separate subclasses, and it is better to be clear than clever, I think this design is wiser than the alternatives.

```

⟨ Publicly declared types in wsmarticle.pas 852 ⟩ +≡
  TheoremReferencePtr = ↑TheoremReferenceObj;
  TheoremReferenceObj = object (LibraryReferenceObj)
    nTheoNr: integer;
    constructor Init(aArticleNr, aTheoNr : integer ; const aPos: Position);
end ;
  DefinitionReferencePtr = ↑DefinitionReferenceObj;
  DefinitionReferenceObj = object (LibraryReferenceObj)
    nDefNr: integer;
    constructor Init(aArticleNr, aDefNr : integer ; const aPos: Position);
end ;

```

872. Constructor. The reference constructors simply populate the appropriate fields in the reference, and the position in the article's text.

```

⟨ Implementation for wsmarticle.pas 854 ⟩ +≡
constructor TheoremReferenceObj.Init(aArticleNr, aTheoNr : integer;
  const aPos: Position);
  begin nRefSort ← TheoremReference; nArticleNr ← aArticleNr; nTheoNr ← aTheoNr;
  nRefPos ← aPos
end;
constructor DefinitionReferenceObj.Init(aArticleNr, aDefNr : integer;
  const aPos: Position);
  begin nRefSort ← DefinitionReference; nArticleNr ← aArticleNr; nDefNr ← aDefNr;
  nRefPos ← aPos
end;

```

873. Justifications. The grammar for justifications looks like:

```

Justification = Simple-Justification
  | Proof .
Simple-Justification = Straightforward-Justification
  | Scheme-Justification .
Proof = "proof" Reasoning "end" .
Straightforward-Justification = [ "by" References ] .
Scheme-Justification = "from" Scheme-Reference [ "(" References ")" ] .

```

Proof blocks are already represented as a *Block* object. We just need to represent the other kinds of justifications as nodes in the abstract syntax tree.

874. The different kinds of inference, since a *Justification* is a tagged union of sorts.

```

⟨ Inference kinds (wsmarticle.pas) 874 ⟩ ≡
  InferenceKind = (infError, infStraightforwardJustification, infSchemeJustification, infProof,
    infSkippedProof)

```

This code is used in section 867.

875. Class structure for justifications. The class hierarchy for justifications reflects the grammar we just discussed.

```

⟨ Publicly declared types in wsmarticle.pas 852 ⟩ +≡
  JustificationPtr = ↑JustificationObj;
  JustificationObj = object (MObject)
    nInfSort: InferenceKind;
    nInfPos: Position;
    constructor Init(aInferSort : InferenceKind ; const aPos: Position);
  end ;

```

876. Constructor.

```

⟨ Implementation for wsmarticle.pas 854 ⟩ +≡
constructor JustificationObj.Init(aInferSort : InferenceKind ; const aPos: Position);
  begin nInfSort ← aInferSort; nInfPos ← aPos;
  end;

```

877. Simple justifications. These are either “by” a list of references, or “from” a scheme.

```

⟨ Publicly declared types in wsmarticle.pas 852 ⟩ +≡
  SimpleJustificationPtr = ↑SimpleJustificationObj;
  SimpleJustificationObj = object (JustificationObj)
    nReferences: PList;
    constructor Init(aInferSort : InferenceKind ; const aPos: Position);
    destructor Done; virtual;
  end ;

```

878. Constructor.

```

⟨ Implementation for wsmarticle.pas 854 ⟩ +≡
constructor SimpleJustificationObj.Init(aInferSort : InferenceKind ; const aPos: Position);
  begin inherited Init(aInferSort, aPos); nReferences ← new(PList, Init(0));
  end;
destructor SimpleJustificationObj.Done;
  begin dispose(nReferences, Done); inherited Done;
  end;

```

879. Straightforward justification.

```

⟨ Publicly declared types in wsmarticle.pas 852 ⟩ +≡
  StraightforwardJustificationPtr = ↑StraightforwardJustificationObj;
  StraightforwardJustificationObj = object (SimpleJustificationObj)
    nLinked: boolean;
    nLinkPos: Position;
    constructor Init(const aPos: Position; aLinked: boolean; const aLinkPos: Position);
    destructor Done; virtual;
  end ;

```

880. Constructor.

⟨Implementation for `wsmarticle.pas 854`⟩ +≡
constructor *StraightforwardJustificationObj*.Init(**const** *aPos*: *Position*;
 aLinked: *boolean*;
 const *aLinkPos*: *Position*);
begin *inherited* Init(*infStraightforwardJustification*, *aPos*); *nLinked* ← *aLinked*; *nLinkPos* ← *aLinkPos*;
end;
destructor *StraightforwardJustificationObj*.Done;
begin *inherited* Done;
end;

881. Scheme justification.

⟨Publicly declared types in `wsmarticle.pas 852`⟩ +≡
SchemeJustificationPtr = ↑*SchemeJustificationObj*;
SchemeJustificationObj = **object** (*SimpleJustificationObj*)
 nSchFileNr: *integer*; { 0 for schemes from current article and positive for library references }
 nSchemeIdNr: *integer*; { a number of a scheme for library reference *nSchFileNr* > 0 or a number of
 an identifier name for scheme name from current article }
 nSchemeInfPos: *Position*;
constructor Init(**const** *aPos*: *Position*; *aArticleNr*, *aNr*: *integer*);
destructor Done; *virtual*;
end ;

882. Constructor.

⟨Implementation for `wsmarticle.pas 854`⟩ +≡
constructor *SchemeJustificationObj*.Init(**const** *aPos*: *Position*; *aArticleNr*, *aNr*: *integer*);
begin *inherited* Init(*infSchemeJustification*, *aPos*); *nSchFileNr* ← *aArticleNr*; *nSchemeIdNr* ← *aNr*;
 nSchemeInfPos ← *aPos*;
end;
destructor *SchemeJustificationObj*.Done;
begin *inherited* Done;
end;

Section 21.2. SCHEMES

883. The grammar for schemes looks like:

```

Scheme-Item = Scheme-Block ";" .
Scheme-Block = "scheme" Scheme-Identifier "{" Scheme-Parameters "}" ":"
  Scheme-Conclusion ["provided" Scheme-Premise {"and" Scheme-Premise}]
  ("proof" | ";") Reasoning "end" .
Scheme-Identifier = Identifier .
Scheme-Parameters = Scheme-Segment "," Scheme-Segment .
Scheme-Conclusion = Sentence .
Scheme-Premise = Proposition .
Scheme-Segment = Predicate-Segment | Functor-Segment .
Predicate-Segment =
  Predicate-Identifier {""," Predicate-Identifier} "[" [Type-Expression-List] "]" .
Predicate-Identifier = Identifier .
Functor-Segment =
  Functor-Identifier {""," Functor-Identifier} "(" [Type-Expression-List] ")" Specification .
Functor-Identifier = Identifier .

```

We begin with the abstract syntax for scheme parameters.

884. Class hierarchy for schemes. We need “predicate segments” and “functor segments” for the second-order variable parameters to the scheme.

```

⟨ Publicly declared types in wsmarticle.pas 852 ⟩ +≡
  SchemeSegmentKind = (PredicateSegment, FunctorSegment);
  SchemeSegmentPtr = ↑SchemeSegmentObj;
  SchemeSegmentObj = object (MObject)
    nSegmPos: Position;
    nSegmSort: SchemeSegmentKind;
    nVars: PList;
    nTypeExpList: PList;
    constructor Init(const aPos: Position; aSegmSort: SchemeSegmentKind;
      aVars, aTypeExpList: PList);
    destructor Done; virtual;
  end ;

```

885. Constructor.

```

⟨ Implementation for wsmarticle.pas 854 ⟩ +≡
constructor SchemeSegmentObj.Init(const aPos: Position;
  aSegmSort: SchemeSegmentKind;
  aVars, aTypeExpList: PList);
begin nSegmPos ← aPos; nSegmSort ← aSegmSort; nVars ← aVars; nTypeExpList ← aTypeExpList;
end;
destructor SchemeSegmentObj.Done;
begin dispose(nVars, Done); dispose(nTypeExpList, Done);
end;

```

886. Segment variables for schemes. We need “predicate segments” and “functor segments” for the second-order variable parameters to the scheme.

```

⟨ Publicly declared types in wsmarticle.pas 852 ⟩ +≡
  PredicateSegmentPtr = SchemeSegmentPtr;
  FunctorSegmentPtr = ↑FunctorSegmentObj;
  FunctorSegmentObj = object (SchemeSegmentObj)
    nSpecification: TypePtr;
    constructor Init(const aPos: Position; aVars, aTypeExpList: PList; aSpecification: TypePtr);
    destructor Done; virtual;
  end ;

```

887. Constructor.

```

⟨ Implementation for wsmarticle.pas 854 ⟩ +≡
constructor FunctorSegmentObj.Init(const aPos: Position;
                                   aVars, aTypeExpList: PList;
                                   aSpecification: TypePtr);
begin inherited Init(aPos, FunctorSegment, aVars, aTypeExpList); nSpecification ← aSpecification;
end;
destructor FunctorSegmentObj.Done;
begin dispose(nSpecification, Done); inherited Done;
end;

```

888. Scheme. A *Scheme* object is the parent class of *MSScheme* objects in *first_identification.pas*. But it does not appear to be used anywhere else. This has no place in the abstract syntax tree, for example.

```

⟨ Publicly declared types in wsmarticle.pas 852 ⟩ +≡
  SchemePtr = ↑SchemeObj;
  SchemeObj = object (MObject)
    nSchemeIdNr: integer;
    nSchemePos: Position;
    nSchemeParams: PList;
    nSchemeConclusion: FormulaPtr;
    nSchemePremises: PList;
    constructor Init(aIdNr: integer ; const aPos: Position; aParams: PList; aPrems: PList;
                    aConcl: FormulaPtr);
    destructor Done; virtual;
  end ;

```

889. Constructor.

(Implementation for `wsmarticle.pas` 854) +≡
constructor *SchemeObj.Init*(*aIdNr* : *integer*;
 const *aPos*: *Position*;
 aParams: *PList*;
 aPremis: *PList*;
 aConcl: *FormulaPtr*);
begin *nSchemeIdNr* ← *aIdNr*; *nSchemePos* ← *aPos*; *nSchemeParams* ← *aParams*;
nSchemeConclusion ← *aConcl*; *nSchemePremises* ← *aPremis*;
end;
destructor *SchemeObj.Done*;
begin *dispose*(*nSchemeParams*, *Done*); *dispose*(*nSchemeConclusion*, *Done*);
dispose(*nSchemePremises*, *Done*);
end;

890. Reservations. We can “reserve” an identifier and its type, so we do not need to quantify over it for each theorem. The grammar for it:

Reservation = "reserve" **Reservation-Segment** { ", " **Reservation-Segment** } "; " .
Reservation-Segment = **Reserved-Identifiers** "for" **Type-Expression** .
Reserved-Identifiers = **Identifier** { ", " **Identifier** } .

The data needed for a **reserved** node in the abstract syntax tree amounts to a list of identifiers and a type.

(Publicly declared types in `wsmarticle.pas` 852) +≡
ReservationSegmentPtr = ↑*ReservationSegmentObj*;
ReservationSegmentObj = **object** (*MObject*)
 nIdentifiers: *PList*;
 nResType: *TypePtr*;
 constructor *Init*(*aIdentifiers* : *PList*; *aType* : *TypePtr*);
 destructor *Done*; *virtual*;
end ;

891. Constructor.

(Implementation for `wsmarticle.pas` 854) +≡
constructor *ReservationSegmentObj.Init*(*aIdentifiers* : *PList*; *aType* : *TypePtr*);
begin *nIdentifiers* ← *aIdentifiers*; *nResType* ← *aType*;
end;
destructor *ReservationSegmentObj.Done*;
begin *dispose*(*nIdentifiers*, *Done*); *dispose*(*nResType*, *Done*);
end;

Section 21.3. PRIVATE DEFINITIONS

892. The grammar for “private definitions” (which introduces block-local or article-local terms and predicates) looks like:

```

Private-Definition = Constant-Definition
                   | Private-Function-Definition
                   | Private-Predicate-Definition .
Constant-Definition = "set" Equating-List ";" .
Equating-List = Equating {"", " Equating" }.
Equating = Variable-Identifier "=" Term-Expression .
Private-Function-Definition = "deffunc" Private-Function-Pattern "=" Term-Expression ";" .
Private-Predicate-Definition = "defpred" Private-Predicate-Pattern "means" Sentence ";" .
Private-Function-Pattern = Function-Identifier "(" [ Type-Expression-List ] ")" .
Private-Predicate-Pattern = Predicate-Identifier "[" [Type-Expression-List ] "]" .

```

So we really only need to describe private predicates, private functions, and “constant definitions” (which introduce an abbreviation).

893. Private functions.

```

⟨ Publicly declared types in wsmarticle.pas 852 ⟩ +≡
  PrivateFunctionDefinitionPtr = ↑PrivateFunctionDefinitionObj;
  PrivateFunctionDefinitionObj = object (MObject)
    nFuncId: VariablePtr;
    nTypeExpList: PList;
    nTermExpr: TermPtr;
    constructor Init(aFuncId : VariablePtr; aTypeExpList : Plist; aTerm : TermPtr);
    destructor Done; virtual;
  end ;

```

894. Constructor.

```

⟨ Implementation for wsmarticle.pas 854 ⟩ +≡
constructor PrivateFunctionDefinitionObj.Init(aFuncId : VariablePtr; aTypeExpList : Plist;
  aTerm : TermPtr);
  begin nFuncId ← aFuncId; nTypeExpList ← aTypeExpList; nTermExpr ← aTerm;
  end;
destructor PrivateFunctionDefinitionObj.Done;
  begin dispose(nFuncId, Done); dispose(nTypeExpList, Done); dispose(nTermExpr, Done);
  end;

```

895. Private predicates.

```

⟨ Publicly declared types in wsmarticle.pas 852 ⟩ +≡
  PrivatePredicateDefinitionPtr = ↑PrivatePredicateDefinitionObj;
  PrivatePredicateDefinitionObj = object (MObject)
    nPredId: VariablePtr;
    nTypeExpList: PList;
    nSentence: FormulaPtr;
    constructor Init(aPredId : VariablePtr; aTypeExpList : Plist; aSnt : FormulaPtr);
    destructor Done; virtual;
  end ;

```

896. Constructor.

(Implementation for `wsmarticle.pas 854`) +≡
constructor *PrivatePredicateDefinitionObj*.Init(*aPredId* : *VariablePtr*; *aTypeExpList* : *Plist*;
 aSnt : *FormulaPtr*);
 begin *nPredId* ← *aPredId*; *nTypeExpList* ← *aTypeExpList*; *nSentence* ← *aSnt*;
 end;
destructor *PrivatePredicateDefinitionObj*.Done;
 begin *dispose*(*nPredId*, Done); *dispose*(*nTypeExpList*, Done); *dispose*(*nSentence*, Done);
 end;

897. Constant definitions. These are little more than abbreviations for terms, and their implementations reflects this: they are pointers with delusions of grandeur.

(Publicly declared types in `wsmarticle.pas 852`) +≡
ConstantDefinitionPtr = ↑*ConstantDefinitionObj*;
ConstantDefinitionObj = **object** (*MObject*)
 nVarId: *VariablePtr*;
 nTermExpr: *TermPtr*;
 constructor Init(*aVarId* : *VariablePtr*; *aTerm* : *TermPtr*);
 destructor Done; *virtual*;
 end ;

898. Constructor.

(Implementation for `wsmarticle.pas 854`) +≡
constructor *ConstantDefinitionObj*.Init(*aVarId* : *VariablePtr*; *aTerm* : *TermPtr*);
 begin *nVarId* ← *aVarId*; *nTermExpr* ← *aTerm*;
 end;
destructor *ConstantDefinitionObj*.Done;
 begin *dispose*(*nVarId*, Done); *dispose*(*nTermExpr*, Done);
 end;

Section 21.4. CHANGING TYPES

899. Each term has a soft type associated with it, but we can “reconsider” or change its type. Mizar requires a proof that the term really has the new type. The grammar for this statement:

```
Type-Changing-Statement =
  "reconsider" Type-Change-List "as" Type-ExpressionSimple-Justification ";" .
Type-Change-List =
  (Equating | Variable-Identifier) {"," (Equating | Variable-Identifier)} .
```

This requires a bit of work since we really have *two* types of reconsiderations within a single reconsider statement:

- (1) “reconsider $\langle identifier \rangle$ as $\langle type \rangle$ ”
- (2) “reconsider $\langle identifier \rangle = \langle term \rangle$ as $\langle type \rangle$ ”

The trick is to represent a Type-Change-List as a list of Type-Changes. Then a Type-Change-Statement is just a Type-Change-List and a type.

900. Class hierarchy.

```
<Publicly declared types in wsmarticle.pas 852> +≡
TypeChangeSort = (Equating, VariableIdentifier);
TypeChangePtr = ↑TypeChangeObj;
TypeChangeObj = object (MObject)
  nTypeChangeKind: TypeChangeSort;
  nVar: VariablePtr;
  nTermExpr: TermPtr;
  constructor Init(aKind : TypeChangeSort; aVar : VariablePtr; aTerm : TermPtr);
  destructor Done; virtual;
end ;
<Example classes (wsmarticle.pas) 903>
TypeChangingStatementPtr = ↑TypeChangingStatementObj;
TypeChangingStatementObj = object (MObject)
  nTypeChangeList: PList;
  nTypeExpr: TypePtr;
  nJustification: SimpleJustificationPtr;
  constructor Init(aTypeChangeList : PList; aTypeExpr : TypePtr;
    aJustification : SimpleJustificationPtr);
  destructor Done; virtual;
end ;
```

901. Constructor.

(Implementation for `wsmarticle.pas` 854) $\vdash \equiv$
constructor *TypeChangeObj*.Init(*aKind* : *TypeChangeSort*; *aVar* : *VariablePtr*; *aTerm* : *TermPtr*);
 begin *nTypeChangeKind* \leftarrow *aKind*; *nVar* \leftarrow *aVar*; *nTermExpr* \leftarrow *aTerm*;
 end;
destructor *TypeChangeObj*.Done;
 begin *dispose*(*nVar*, *Done*);
 if *nTermExpr* \neq **nil** **then** *dispose*(*nTermExpr*, *Done*);
 end;
 (Constructors for example statements (`wsmarticle.pas` 904)
constructor *TypeChangingStatementObj*.Init(*aTypeChangeList* : *PList*; *aTypeExpr* : *TypePtr*;
 aJustification : *SimpleJustificationPtr*);
 begin *nTypeChangeList* \leftarrow *aTypeChangeList*; *nTypeExpr* \leftarrow *aTypeExpr*;
 nJustification \leftarrow *aJustification*;
 end;
destructor *TypeChangingStatementObj*.Done;
 begin *dispose*(*nTypeChangeList*, *Done*); *dispose*(*nTypeExpr*, *Done*); *dispose*(*nJustification*, *Done*);
 end;

Section 21.5. PROOF STEPS

902. Most of the proof steps are handled in generic text-item objects. But there are a few which are outside that tagged union. In particular: existential elimination (**consider** $\langle variables \rangle$ **such that** $\langle formula \rangle$), existential introduction (**take** $\langle terms \rangle$), and concluding statements (**thus** $\langle formula \rangle$).

903. Examples, existential introduction. The proof step “take x ” transforms goals of the form $\exists x. P[x]$ into a new goal $P[x]$. The grammar for examples looks like:

Exemplification = "take" Example {"," Example} ";" .

Example = Term-Expression | Variable-Identifier "=" Term-Expression .

```

⟨ Example classes (wsmarticle.pas) 903 ⟩ ≡
  ExamplePtr = ↑ExampleObj;
  ExampleObj = object (MObject)
    nVarId: VariablePtr;
    nTermExpr: TermPtr;
    constructor Init(aVarId : VariablePtr; aTerm : TermPtr);
    destructor Done; virtual;
  end ;

```

This code is used in section 900.

904. Constructor.

```

⟨ Constructors for example statements (wsmarticle.pas) 904 ⟩ ≡
constructor ExampleObj.Init(aVarId : VariablePtr; aTerm : TermPtr);
  begin nVarId ← aVarId; nTermExpr ← aTerm;
  end;
destructor ExampleObj.Done;
  begin if nVarId ≠ nil then dispose(nVarId, Done);
  if nTermExpr ≠ nil then dispose(nTermExpr, Done);
  end;

```

This code is used in section 901.

905. Existential elimination. We continue plugging along with the statements, and existential elimination (or “choice”) statements are the next one.

```

Linkable-Statement = Compact-Statement
  | Choice-Statement
  | Type-Changing-Statement
  | Iterative-Equality .

```

Choice-Statement = "consider" Qualified-Variables "such" ConditionsSimple-Justification ";" .

```

906. ⟨ Publicly declared types in wsmarticle.pas 852 ⟩ +≡
  ChoiceStatementPtr = ↑ChoiceStatementObj;
  ChoiceStatementObj = object (MObject)
    nQualVars: PList;
    nConditions: PList;
    nJustification: SimpleJustificationPtr;
    constructor Init(aQualVars, aConds : PList; aJustification : SimpleJustificationPtr);
    destructor Done; virtual;
  end ;

```

907. Constructor.

```

⟨Implementation for wsmarticle.pas 854⟩ +≡
constructor ChoiceStatementObj.Init(aQualVars : PList; aConds : PList; aJustification : SimpleJustificationPtr);
  begin nQualVars ← aQualVars; nConditions ← aConds; nJustification ← aJustification;
  end;
destructor ChoiceStatementObj.Done;
  begin dispose(nQualVars, Done); dispose(nConditions, Done); dispose(nJustification, Done);
  end;

```

908. Conclusion statements. We recall the grammar for conclusion statements:

```

Conclusion = ( "thus" | "hence" ) ( Compact-Statement | Iterative-Equality )
           | Diffuse-Conclusion .
Diffuse-Conclusion = "thus" Diffuse-Statement | "hereby" Reasoning "end" ";" .
Iterative-Equality =
[ Label-Identifier ":" ] Term-Expression "=" Term-ExpressionSimple-Justification
                        "." Term-Expression Simple-Justification
                        { "." Term-Expression Simple-Justification } ";" .

```

NOTE: the whitespace in the *Iterative-Equality* rule is unimportant, but that is how Mizar users often structure them (to align the equals sign).

909. Abstract base class.

```

⟨Publicly declared types in wsmarticle.pas 852⟩ +≡
  RegularStatementKind = (stDiffuseStatement, stCompactStatement, stIterativeEquality);
  RegularStatementPtr = ↑RegularStatementObj;
  RegularStatementObj = object (MObject)
    nStatementSort: RegularStatementKind;
    nLab: LabelPtr;
    constructor Init(aStatementSort : RegularStatementKind);
    destructor Done; virtual;
  end ;

```

910. Constructor.

```

⟨Implementation for wsmarticle.pas 854⟩ +≡
constructor RegularStatementObj.Init(aStatementSort : RegularStatementKind);
  begin nStatementSort ← aStatementSort;
  end;
destructor RegularStatementObj.Done;
  begin inherited Done;
  end;

```

911. Thus statement. The conclusion of a proof (idiomatically “*thus thesis*”) is always a “*thus*”, which Mizar calls a “diffuse statement”.

```

⟨Publicly declared types in wsmarticle.pas 852⟩ +≡
  DiffuseStatementPtr = ↑DiffuseStatementObj;
  DiffuseStatementObj = object (RegularStatementObj)
    constructor Init(aLab : LabelPtr; aStatementSort : RegularStatementKind);
    destructor Done; virtual;
  end ;

```

912. Constructor.

⟨Implementation for `wsmarticle.pas 854`⟩ +≡
constructor *DiffuseStatementObj.Init*(*aLab* : *LabelPtr*; *aStatementSort* : *RegularStatementKind*);
 begin *inherited Init*(*stDiffuseStatement*); *nLab* ← *aLab*; *nStatementSort* ← *aStatementSort*;
 end;
destructor *DiffuseStatementObj.Done*;
 begin *dispose*(*nLab*, *Done*);
 end;

913. Compact statements. We recall the syntax for a compact statement is:

Compact-Statement = Proposition Justification ";" .

⟨Publicly declared types in `wsmarticle.pas 852`⟩ +≡
CompactStatementPtr = ↑*CompactStatementObj*;
CompactStatementObj = **object** (*RegularStatementObj*)
 nProp: *PropositionPtr*;
 nJustification: *JustificationPtr*;
 constructor *Init*(*aProp* : *PropositionPtr*; *aJustification* : *JustificationPtr*);
 destructor *Done*; *virtual*;
end ;

914. Constructor.

⟨Implementation for `wsmarticle.pas 854`⟩ +≡
constructor *CompactStatementObj.Init*(*aProp* : *PropositionPtr*; *aJustification* : *JustificationPtr*);
 begin *inherited Init*(*stCompactStatement*); *nProp* ← *aProp*; *nJustification* ← *aJustification*;
 end;
destructor *CompactStatementObj.Done*;
 begin if *nJustification* ≠ nil then *dispose*(*nJustification*, *Done*);
 inherited Done;
 end;

915. Iterative equality. Chain of equations, where we keep transforming the right-hand side until we arrive at the desired outcome.

⟨Publicly declared types in `wsmarticle.pas 852`⟩ +≡
IterativeStepPtr = ↑*IterativeStepObj*;
IterativeStepObj = **object** (*MObject*)
 nIterPos: *Position*;
 nTerm: *TermPtr*;
 nJustification: *SimpleJustificationPtr*;
 constructor *Init*(**const** *aPos*: *Position*; *aTerm*: *TermPtr*; *aJustification*: *JustificationPtr*);
 destructor *Done*; *virtual*;
end ;

916. ⟨Publicly declared types in `wsmarticle.pas 852`⟩ +≡

IterativeEqualityPtr = ↑*IterativeEqualityObj*;
IterativeEqualityObj = **object** (*CompactStatementObj*)
 nIterSteps: *PList*;
 constructor *Init*(*aProp* : *PropositionPtr*; *aJustification* : *JustificationPtr*; *aIters* : *PList*);
 destructor *Done*; *virtual*;
end ;

917. Constructor.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```
constructor IterativeStepObj.Init(const aPos: Position; aTerm: TermPtr; aJustification:  
    JustificationPtr);  
    begin nIterPos ← aPos; nTerm ← aTerm; nJustification ← SimpleJustificationPtr(aJustification);  
    end;  
destructor IterativeStepObj.Done;  
    begin dispose(nTerm, Done); dispose(nJustification, Done);  
    end;
```

918. Constructor.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```
constructor IterativeEqualityObj.Init(aProp : PropositionPtr; aJustification : JustificationPtr;  
    aIters : PList);  
    begin inherited Init(aProp, aJustification); nStatementSort ← stIterativeEquality; nIterSteps ← aIters;  
    end;  
destructor IterativeEqualityObj.Done;  
    begin dispose(nIterSteps, Done); inherited Done;  
    end;
```

919. Remaining proof steps? So where are the other proof steps like `let` or `assume`? Well, these are handled as “generic text items” and use the *TextItem* class (§860).

Section 21.6. STRUCTURES

920. Just an aside first on “what is a structure in Mathematics?” Logic textbooks assume an *intuitive* (i.e., not formal) “finitary metatheory” following Hilbert and his famous Programme in the foundations of Mathematics. We will build a “skyscraper” atop this foundation of finitary metatheory. The first thing we do is describe a logic, the first floor in our sky scraper. This “Logic #1” is the metalogic we use to construct an axiomatic set theory, “Set Theory #2”. We use “Set Theory #2” to construct another floor, a “Logic #3”, which then builds another floor “Set Theory #4”, and so on. We can potentially iterate building as many floors as we want, but 4 is sufficient for our purposes.

We **assert** that “Set Theory #2” is the Platonic “mathematical reality”. Then “Logic #3” is the (ambient) logic we use to do Mathematics; it is purely “syntactic”, a language for expressing proofs and definitions. Mizar’s proof steps, formulas, and definitions corresponds to “Logic #3”. With it, we describe an axiomatic “Set Theory #4”, which is Tarski–Grothendieck set theory for Mizar. Sketching this situation out diagrammatically:

Set Theory #4	(Where we work) [syntactic]
Logic #3	“Object logic” (Where we write proofs) [syntactic]
Set Theory #2	“Mathematical Reality” [semantic]
Logic #1	“Metalogic”
Finitary Metatheory	

Fig. 5. Mathematical Platonism as a skyscraper.

Now, “mathematical objects” live in “Set Theory #2”. Model theory studies structures (objects in “Set Theory #2”) of theories (described in “Logic #3”). Since we “believe” that set theory “describes reality”, that means we just need to describe [“syntactic”] theories using “Set Theory #4” and their “real world occurrences” in “Set Theory #2”. (Well, this is a gloss, model theory sets up two additional floors in the skyscraper, and studies “models” of theories described using Logic #5 and Set Theory #6 in Set Theory #4 — and we pretend it describes the relationship between Set Theory #2 and the “syntactic floors” of the Mathematical skyscraper.)

How do we *syntactically* describe these “structures”? Well, we *know* they are not “first-class citizens” in Mizar, in the sense that they are not “just” a tuple. How do we know this? Gilbert Lee and Piotr Rudnicki’s “Alternative Aggregates in Mizar” (in *MKM 2007*, Springer, pp.327–341; [doi:10.1007/978-3-540-73086-6_26](https://doi.org/10.1007/978-3-540-73086-6_26)) discuss how to implement first-class structures in Mizar. This means that *technically* structures live in Logic #3. Field symbols are terms in Logic #3.

921. Why do we need this convoluted skyscraper? Without it, how do we describe a “true” formula? We can only speak of a *provable* formula. Bourbaki’s *Theory of Sets* (I §2.2) confuses “provable” with “true” formulas (they speak of a formula being “false in a theory \mathcal{T} ” as being synonymous with the formula contradicting the axioms for a theory, and true in a theory as being synonymous for being a logical consequence from the axioms for a theory). This only matters for Mathematical Platonists. Formalists (like the author) would find this discussion muddled and nearly metaphysical, generating more heat than light.

922. Aside: finitary metatheory, programming languages, implementing proof assistants.

How does that diagram in Figure 5 of the last section compare to the *actual implementation* of Mizar? Well, a proof assistant replaces the “finitary metatheory” with an actual programming language. Then, since only Mathematical Platonists care about the “Metalogic” and “Mathematical reality”, we jump ahead to implement Logic #3 — this is what happens in Mizar and other proof assistants: we implement a “purely formal” (purely syntactic) logic using a programming language. Curiously, this reflects Bourbaki’s approach to the foundations of Mathematics.

We should note that programming languages are strictly stronger than finitary metatheory, since programming languages are *Turing complete*. This means they support general recursion, whereas finitary metatheory supports only primitive recursive functions. For an example of a “programming language” which is equally as strong as a finitary metatheory, see Albert R. Meyer and Dennis M. Ritchie, “The complexity of loop programs” (*ACM ’67 Proc.*, 1967, [doi:10.1145/800196.806014](https://doi.org/10.1145/800196.806014)).

Is Turing completeness “too much” for a finitary metatheory? The short answer is: yes. Even restricting a Turing complete programming language is “too much” to be finitary. Gödel’s System T was developed to preserve the “constructive character” while jettisoning the “finitary character” of Hilbert’s finitary metatheory, and System T is not even Turing complete. See Kurt Gödel’s *Collected Works* (vol. II, Oxford University Press, [doi:10.1093/oso/9780195147216.001.0001](https://doi.org/10.1093/oso/9780195147216.001.0001), 1989; viz., pp. 245–247) for his discussion of System T. The interested reader should consult David A. Turner’s “Elementary strong functional programming” (in *Int. Symp. on Funct. Program. Lang. in Educ.*, eds P.H. Hartel and R. Plasmeijer, Springer, pages 1–13, [doi:10.1007/3-540-60675-0_35](https://doi.org/10.1007/3-540-60675-0_35)) for how to obtain System T by restricting any statically typed functional programming language.

923. Grammar for structures. We can recall the syntax for structures and fields:

```
Structure-Definition =
  "struct" [ "(" Ancestors ")" ] Structure-Symbol [ "over" Loci ] "(" Fields ")" ";" .
Ancestors = Structure-Type-Expression { "," Structure-Type-Expression } .
Structure-Symbol = Symbol .
Loci = Locus { "," Locus } .
Fields = Field-Segment { "," Field-Segment } .
Locus = Variable-Identifier .
Variable-Identifier = Identifier .
Field-Segment = Selector-Symbol { "," Selector-Symbol } Specification .
Selector-Symbol = Symbol .
```

924. Field symbol. A “field symbol” refers to the identifier used for a field in a structure, but not its type.

```
< Publicly declared types in wsmarticle.pas 852 > +≡
  FieldSymbolPtr = ↑FieldSymbolObj;
  FieldSymbolObj = object (MObject)
    nFieldPos: Position;
    nFieldSymbol: integer;
    constructor Init(const aPos: Position; aFieldSymbNr: integer);
  end ;
```

925. Constructor.

```
< Implementation for wsmarticle.pas 854 > +≡
constructor FieldSymbolObj.Init(const aPos: Position; aFieldSymbNr: integer);
  begin nFieldPos ← aPos; nFieldSymbol ← aFieldSymbNr;
end;
```

926. Field segment. A field segment refers to a list of 1 or more field symbols, and the associated type it has.

```

⟨ Publicly declared types in wsmarticle.pas 852 ⟩ +≡
  FieldSegmentPtr = ↑FieldSegmentObj;
  FieldSegmentObj = object (MObject)
    nFieldSegmPos: Position;
    nFields: PList;
    nSpecification: TypePtr;
    constructor Init(const aPos: Position; aFields: PList; aSpec: TypePtr);
    destructor Done; virtual;
  end ;

```

927. Constructor.

```

⟨ Implementation for wsmarticle.pas 854 ⟩ +≡
constructor FieldSegmentObj.Init(const aPos: Position; aFields: PList; aSpec: TypePtr);
  begin nFieldSegmPos ← aPos; nFields ← aFields; nSpecification ← aSpec;
  end;
destructor FieldSegmentObj.Done;
  begin dispose(nFields, Done); dispose(nSpecification, Done);
  end;

```

928. Locus. A “locus” refers to a term or type parametrizing a definition.

```

⟨ Publicly declared types in wsmarticle.pas 852 ⟩ +≡
  LocusPtr = ↑LocusObj;
  LocusObj = object (MObject)
    nVarId: integer;
    nVarIdPos: Position;
    constructor Init(const aPos: Position; aIdentNr: integer);
  end ;

```

929. Constructor.

```

⟨ Implementation for wsmarticle.pas 854 ⟩ +≡
constructor LocusObj.Init(const aPos: Position; aIdentNr: integer);
  begin nVarId ← aIdentNr; nVarIdPos ← aPos;
  end;

```

930. Structure definition. Finally, structures are finite maps from selectors to terms, with structure inheritance thrown into the mix. They may be defined “**over**” a finite list of types (e.g., a module structure is “**over**” a ring). Note that we need to first introduce “patterns” before describing the structure definition, since “patterns” are needed in definitions.

```

⟨ Publicly declared types in wsmarticle.pas 852 ⟩ +≡
  ⟨ Pattern objects (wsmarticle.pas) 933 ⟩
  StructureDefinitionPtr = ↑StructureDefinitionObj;
  StructureDefinitionObj = object (MObject)
    nStrPos: Position;
    nAncestors: PList;
    nDefStructPattern: ModePatternPtr;
    nSgmFields: PList;
    constructor Init(const aPos: Position; aAncestors: PList; aStructSymb: integer;
      aOverArgs: PList; aFields: PList);
    destructor Done; virtual;
  end ;

```

931. Constructor.

```

⟨ Implementation for wsmarticle.pas 854 ⟩ +≡
constructor StructureDefinitionObj.Init(const aPos: Position; aAncestors: PList;
  aStructSymb: integer; aOverArgs: PList; aFields: PList);
  begin nStrPos ← aPos; nAncestors ← aAncestors;
    nDefStructPattern ← new(ModePatternPtr, Init(aPos, aStructSymb, aOverArgs));
    nDefStructPattern↑.nPatternSort ← itDefStruct; nSgmFields ← aFields;
  end;
destructor StructureDefinitionObj.Done;
  begin dispose(nAncestors, Done); dispose(nDefStructPattern, Done); dispose(nSgmFields, Done);
  end;

```

Section 21.7. PATTERNS

932. A “*Pattern*” in Mizar is a format with the type information for all the arguments around a term. The notion of a “*Pattern*” also refers to the definiendum of a definition. The syntax of patterns

```

Mode-Pattern = Mode-Symbol [ "of" Loci ] .
Attribute-Pattern = Locus "is" [ Attribute-Loci ] Attribute-Symbol .
Attribute-Loci = Loci | "(" Loci ")" .
Predicate-Pattern = [ Loci ] Predicate-Symbol [ Loci ] .
Functor-Pattern = [ Functor-Loci ] Functor-Symbol [ Functor-Loci ]
  | Left-Functor-Bracket Loci Right-Functor-Bracket .
Functor-Loci = Locus | "(" Loci ")" .

```

933. Base class for patterns.

```

⟨Pattern objects (wsmarticle.pas) 933⟩ ≡
  PatternPtr = ↑PatternObj;
  PatternObj = object (mObject)
    nPatternPos: Position;
    nPatternSort: ItemKind;
    constructor Init(const aPos: Position; aSort: ItemKind);
  end ;

```

See also sections 935, 937, 939, and 941.

This code is used in section 930.

934. ⟨Implementation for wsmarticle.pas 854⟩ +≡
constructor PatternObj.Init(const aPos: Position; aSort: ItemKind);
begin nPatternPos ← aPos; nPatternSort ← aSort;
end;

935. Mode patterns. The syntax for “mode patterns” looks like:

```

Mode-Pattern = Mode-Symbol [ "of" Loci ] .
⟨Pattern objects (wsmarticle.pas) 933⟩ +≡
  ModePatternPtr = ↑ModePatternObj;
  ModePatternObj = object (PatternObj)
    nModeSymbol: Integer;
    nArgs: PList;
    constructor Init(const aPos: Position; aSymb: integer; aArgs: PList);
    destructor Done; virtual;
  end ;

```

936. Constructor.

```

⟨Implementation for wsmarticle.pas 854⟩ +≡
constructor ModePatternObj.Init(const aPos: Position; aSymb: integer; aArgs: PList);
  begin inherited Init(aPos, itDefMode); nModeSymbol ← aSymb; nArgs ← aArgs;
end;
destructor ModePatternObj.Done;
  begin dispose(nArgs, Done);
end;

```

937. Attribute patterns. Attributes can have loci prefixing the attribute symbol, but *not* suffixing the attribute symbol.

```
Attribute-Pattern = Locus "is" [ Attribute-Loci ] Attribute-Symbol .
Attribute-Loci = Loci | "(" Loci ")" .
⟨ Pattern objects (wsmarticle.pas 933) +≡
  AttributePatternPtr = ↑AttributePatternObj;
  AttributePatternObj = object (PatternObj)
    nAttrSymbol: Integer;
    nArg: LocusPtr;
    nArgs: PList;
    constructor Init(const aPos: Position; aArg: LocusPtr; aSymb: integer; aArgs: PList);
    destructor Done; virtual;
end ;
```

938. Constructor.

```
⟨ Implementation for wsmarticle.pas 854 +≡
constructor AttributePatternObj.Init(const aPos: Position; aArg: LocusPtr; aSymb: integer; aArgs:
  PList);
  begin inherited Init(aPos, itDefAttr); nAttrSymbol ← aSymb; nArg ← aArg; nArgs ← aArgs;
end;
destructor AttributePatternObj.Done;
  begin dispose(nArg, Done); dispose(nArgs, Done);
end;
```

939. Predicate patterns. Predicates can have loci on either side of the predicate symbol, without requiring parentheses (unlike functors).

```
Predicate-Pattern = [ Loci ] Predicate-Symbol [ Loci ] .
⟨ Pattern objects (wsmarticle.pas 933) +≡
  PredicatePatternPtr = ↑PredicatePatternObj;
  PredicatePatternObj = object (PatternObj)
    nPredSymbol: Integer;
    nLeftArgs, nRightArgs: PList;
    constructor Init(const aPos: Position; aLArgs: PList; aSymb: integer; aRArgs: PList);
    destructor Done; virtual;
end ;
```

940. Constructor.

```
⟨ Implementation for wsmarticle.pas 854 +≡
constructor PredicatePatternObj.Init(const aPos: Position;
  aLArgs: PList; aSymb: integer; aRArgs: PList);
  begin inherited Init(aPos, itDefPred); nPredSymbol ← aSymb; nLeftArgs ← aLArgs;
  nRightArgs ← aRArgs;
end;
destructor PredicatePatternObj.Done;
  begin dispose(nLeftArgs, Done); dispose(nRightArgs, Done);
end;
```

941. Functor pattern. Functors can have loci on either side. If more than one locus is used on one side, then it must be placed in parentheses and comma-separated. The syntax:

```

Functor-Pattern = [ Functor-Loci ] Functor-Symbol [ Functor-Loci ]
                | Left-Functor-Bracket Loci Right-Functor-Bracket .
Functor-Loci = Locus | "(" Loci ")" .
⟨Pattern objects (wsmarticle.pas) 933⟩ +≡
  FunctorSort = (InfixFunctor, CircumfixFunctor);
  FunctorPatternPtr = ↑FunctorPatternObj;
  FunctorPatternObj = object (PatternObj)
    nFunctKind: FunctorSort;
    constructor Init(const aPos: Position; aKind: FunctorSort);
  end ;
  CircumfixFunctorPatternPtr = ↑CircumfixFunctorPatternObj;
  CircumfixFunctorPatternObj = object (FunctorPatternObj)
    nLeftBracketSymb, nRightBracketSymb: integer;
    nArgs: PList;
    constructor Init(const aPos: Position; aLBSymb, aRBSymb: integer; aArgs: PList);
    destructor Done; virtual;
  end ;
  InfixFunctorPatternPtr = ↑InfixFunctorPatternObj;
  InfixFunctorPatternObj = object (FunctorPatternObj)
    nOperSymb: integer;
    nLeftArgs, nRightArgs: PList;
    constructor Init(const aPos: Position; aLArgs: PList; aSymb: integer; aRArgs: PList);
    destructor Done; virtual;
  end ;

```

942. Constructor.

```

⟨Implementation for wsmarticle.pas 854⟩ +≡
constructor FunctorPatternObj.Init(const aPos: Position; aKind: FunctorSort);
  begin inherited Init(aPos, itDefFunc); nFunctKind ← aKind;
  end;
constructor CircumfixFunctorPatternObj.Init(const aPos: Position; aLBSymb, aRBSymb: integer;
  aArgs: PList);
  begin inherited Init(aPos, CircumfixFunctor); nLeftBracketSymb ← aLBSymb;
  nRightBracketSymb ← aRBSymb; nArgs ← aArgs;
  end;
destructor CircumfixFunctorPatternObj.Done;
  begin dispose(nArgs, Done);
  end;
constructor InfixFunctorPatternObj.Init(const aPos: Position; aLArgs: PList; aSymb: integer; aRArgs:
  PList);
  begin inherited Init(aPos, InfixFunctor); nOperSymb ← aSymb; nLeftArgs ← aLArgs;
  nRightArgs ← aRArgs;
  end;
destructor InfixFunctorPatternObj.Done;
  begin dispose(nLeftArgs, Done); dispose(nRightArgs, Done);
  end;

```

Section 21.8. DEFINITIONS

943. In Mizar, we can redefine an existing definition (either changing the type of a term or “the right hand side” of a definition) *or* we can introduce a new definition. There are 5 different things we can introduce: structures, modes [types], functors [terms], predicates, and attributes. Rather than bombard the reader with a long chunk of grammar, let us divide it up into easy-to-digest pieces. The basic block structure of a definition is the same for all these situations, its grammar looks like:

```

Definitional-Item = Definitional-Block ";" .
Definitional-Block = "definition" { Definition-Item | Definition | Redefinition } "end" .
Definition-Item = Loci-Declaration | Permissive-Assumption | Auxiliary-Item .
Loci-Declaration = "let" Qualified-Variables [ "such" Conditions ] ";" .
Permissive-Assumption = Assumption .
Definition = Structure-Definition
| Mode-Definition
| Functor-Definition
| Predicate-Definition
| Attribute-Definition .

```

944. Redefinitions. Redefinitions allow us to alter the type or meaning of a definition. This isn’t willy-nilly, the user still needs to prove the redefined version is logically equivalent to the initial definition.

```

Redefinition =
  "redefine" ( Mode-Definition | Functor-Definition | Predicate-Definition | Attribute-Definition ) .

```

945. Structure definitions. Structures intuitively correspond to new “gadgets” (sets equipped with extra structure), which is often presented in Mathematics as “just another tuple”. Mizar allows structures to inherit other structures, so a topological group extends a topological space structure *and* a magma structure (since a group in Mizar is a magma with some extra properties).

```

Structure-Definition =
  "struct" [ "(" Ancestors ")" ] Structure-Symbol [ "over" Loci ] "(#" Fields "#)" ";" .
Ancestors = Structure-Type-Expression { "," Structure-Type-Expression } .
Structure-Symbol = Symbol .
Loci = Locus { "," Locus } .
Fields = Field-Segment { "," Field-Segment } .
Locus = Variable-Identifier .
Variable-Identifier = Identifier .
Field-Segment = Selector-Symbol { "," Selector-Symbol } Specification .
Selector-Symbol = Symbol .
Specification = "->" Type-Expression .

```

946. Definiens. Recall the grammar for Definiens looks like:

```

Definiens = Simple-Definiens | Conditional-Definiens .
Simple-Definiens = [ ":" Label-Identifier ":" ] ( Sentence | Term-Expression ) .
Label-Identifier = Identifier .
Conditional-Definiens = [ ":" Label-Identifier ":" ] Partial-Definiens-List
  [ "otherwise" ( Sentence | Term-Expression ) ] .
Partial-Definiens-List = Partial-Definiens { "," Partial-Definiens } .
Partial-Definiens = ( Sentence | Term-Expression ) "if" Sentence .

```


We begin with a base class for definiens. This is extended by *SimpleDefiniens* and *ConditionalDefiniens* classes.

```

⟨ Publicly declared types in wsmarticle.pas 852 ⟩ +≡
  HowToDefine = (dfEmpty, dfMeans, dfEquals);
  DefiniensSort = (SimpleDefiniens, ConditionalDefiniens);
  DefiniensPtr = ↑DefiniensObj;
  DefiniensObj = object (MObject)
    nDefSort: DefiniensSort;
    nDefPos: Position;
    nDefLabel: LabelPtr;
    constructor Init(const aPos: Position; aLab: LabelPtr; aKind: DefiniensSort);
    destructor Done; virtual;
  end ;

```

947. Constructor.

```

⟨ Implementation for wsmarticle.pas 854 ⟩ +≡
constructor DefiniensObj.Init(const aPos: Position; aLab: LabelPtr; aKind: DefiniensSort);
  begin nDefSort ← aKind; nDefPos ← aPos; nDefLabel ← aLab;
  end;
destructor DefiniensObj.Done;
  begin if nDefLabel ≠ nil then dispose(nDefLabel, Done);
  end;

```

948. Definiens expression. These nodes in the abstract syntax tree describe “the right hand side” of a definition. A simple definiens is just a pointer to one definiens expression object, for example.

```

⟨ Publicly declared types in wsmarticle.pas 852 ⟩ +≡
  DefExpressionPtr = ↑DefExpressionObj;
  DefExpressionObj = object (MObject)
    nExprKind: ExpKind;
    nExpr: PObject;
    constructor Init(aKind: ExpKind; aExpr: PObject);
    destructor Done; virtual;
  end ;

```

949. Constructor.

```

⟨ Implementation for wsmarticle.pas 854 ⟩ +≡
constructor DefExpressionObj.Init(aKind: ExpKind; aExpr: Pobject);
  begin nExprKind ← aKind; nExpr ← aExpr;
  end;
destructor DefExpressionObj.Done;
  begin dispose(nExpr, Done);
  end;

```

950. Simple definiens. This is the “default” definiens, i.e., the definiens which are not “by cases”.

```

⟨ Publicly declared types in wsmarticle.pas 852 ⟩ +≡
  SimpleDefiniensPtr = ↑SimpleDefiniensObj;
  SimpleDefiniensObj = object (DefiniensObj)
    nExpression: DefExpressionPtr;
    constructor Init(const aPos: Position; aLab: LabelPtr; aDef: DefExpressionPtr);
    destructor Done; virtual;
  end ;

```

951. Constructor.

```

⟨ Implementation for wsmarticle.pas 854 ⟩ +≡
constructor SimpleDefiniensObj.Init(const aPos: Position; aLab: LabelPtr; aDef: DefExpressionPtr);
  begin inherited Init(aPos, aLab, SimpleDefiniens); nExpression ← aDef;
  end;
destructor SimpleDefiniensObj.Done;
  begin dispose(nExpression, Done); inherited Done;
  end;

```

952. Definition for particular case. We have “⟨sentence or term⟩ if ⟨guard condition⟩” represented by a couple of pointers: one to the “sentence or term” definiens, and the second to the “guard” condition.

```

⟨ Publicly declared types in wsmarticle.pas 852 ⟩ +≡
  PartDefPtr = ↑PartDefObj;
  PartDefObj = object (MObject)
    nPartDefiniens: DefExpressionPtr;
    nGuard: FormulaPtr;
    constructor Init(aPartDef: DefExpressionPtr; aGuard: FormulaPtr);
    destructor Done; virtual;
  end ;

```

953. Constructor.

```

⟨ Implementation for wsmarticle.pas 854 ⟩ +≡
constructor PartDefObj.Init(aPartDef: DefExpressionPtr; aGuard: FormulaPtr);
  begin nGuard ← aGuard; nPartDefiniens ← aPartDef;
  end;
destructor PartDefObj.Done;
  begin dispose(nPartDefiniens, Done); dispose(nGuard, Done);
  end;

```

954. Conditional definiens. A conditional definiens consists of a finite list of pointers to *PartDef* objects, and a pointer to the default “otherwise” definien.

```

⟨ Publicly declared types in wsmarticle.pas 852 ⟩ +≡
  ConditionalDefiniensPtr = ↑ConditionalDefiniensObj;
  ConditionalDefiniensObj = object (DefiniensObj)
    nConditionalDefiniensList: PList;
    nOtherwise: DefExpressionPtr;
    constructor Init(const aPos: Position; aLab: LabelPtr; aPartialDefs: PList;
      aOtherwise: DefExpressionPtr);
    destructor Done; virtual;
  end ;

```

955. Constructor.

```

⟨Implementation for wsmarticle.pas 854⟩ +≡
constructor ConditionalDefiniensObj.Init(const aPos: Position;
    aLab: LabelPtr; aPartialDefs: PList; aOtherwise: DefExpressionPtr);
    begin inherited Init(aPos, aLab, ConditionalDefiniens); nConditionalDefiniensList ← aPartialDefs;
    nOtherwise ← aOtherwise;
    end;
destructor ConditionalDefiniensObj.Done;
    begin if nOtherwise ≠ nil then dispose(nOtherwise, Done);
    dispose(nConditionalDefiniensList, Done); inherited Done;
    end;

```

956. Mode definitions. Mizar was heavily inspired by ALGOL, and even borrows ALGOL's terminology for types ("modes"). These are "soft types", which are predicates in the ambient logic.

However, we need to establish the well-definedness of types (i.e., they are inhabited by at least one term), or else we end up in "free logic". For example, if `EmptyType` is a hypothetical empty type, then `for x being EmptyType holds P[x]` is always true, and `ex x being EmptyType st P[x]` is always false. The clever Mizar user can abuse this, and end up compromising the soundness of classical logic. To avert catastrophe, we require proving there exists at least one term of the newly defined type.

```

Mode-Definition = "mode" Mode-Pattern
    ( [ Specification ] [ "means" Definiens ] ";" Correctness-Conditions | "is" Type-Expression ";" )
    { Mode-Property } .
Mode-Pattern = Mode-Symbol [ "of" Loci ] .
Mode-Symbol = Symbol | "set" .
Mode-Synonym = "synonym" Mode-Pattern "for" Mode-Pattern ";" .
Mode-Property = "sethood" Justification ";" .

⟨Publicly declared types in wsmarticle.pas 852⟩ +≡
ModeDefinitionSort = (defExpandableMode, defStandardMode);
ModeDefinitionPtr = ↑ModeDefinitionObj;
ModeDefinitionObj = object (MObject)
    nDefKind: ModeDefinitionSort;
    nDefModePos: Position;
    nDefModePattern: ModePatternPtr;
    nRedefinition: boolean;
    constructor Init(const aPos: Position; aDefKind: ModeDefinitionSort; aRedef: boolean;
        aPattern: ModePatternPtr);
    destructor Done; virtual;
end ;

```

957. Constructor.

```

⟨Implementation for wsmarticle.pas 854⟩ +≡
constructor ModeDefinitionObj.Init(const aPos: Position; aDefKind: ModeDefinitionSort;
    aRedef: boolean; aPattern: ModePatternPtr);
    begin nDefKind ← aDefKind; nDefModePos ← aPos; nRedefinition ← aRedef;
    nDefModePattern ← aPattern;
    end;
destructor ModeDefinitionObj.Done;
    begin dispose(nDefModePattern, Done);
    end;

```

958. Expandable mode definitions. These are simple “abbreviations” of modes which are of the form “mode $\langle type\ name \rangle$ is $\langle adjective_1 \rangle \cdots \langle adjective_n \rangle \langle type \rangle$ ”, i.e., just a stack of adjectives atop a type.

```

< Publicly declared types in wsmarticle.pas 852 > +≡
  ExpandableModeDefinitionPtr = ↑ExpandableModeDefinitionObj;
  ExpandableModeDefinitionObj = object (ModeDefinitionObj)
    nExpansion: TypePtr;
    constructor Init(const aPos: Position; aPattern: ModePatternPtr; aExp: TypePtr);
    destructor Done; virtual;
  end ;

```

959. Constructor.

```

< Implementation for wsmarticle.pas 854 > +≡
constructor ExpandableModeDefinitionObj.Init(const aPos: Position;
  aPattern: ModePatternPtr; aExp: TypePtr);
  begin inherited Init(aPos, defExpandableMode, false, aPattern); nExpansion ← aExp;
  end;
destructor ExpandableModeDefinitionObj.Done;
  begin dispose(nExpansion, Done); inherited Done;
  end;

```

960. Standard mode definitions.

```

< Publicly declared types in wsmarticle.pas 852 > +≡
  StandardModeDefinitionPtr = ↑StandardModeDefinitionObj;
  StandardModeDefinitionObj = object (ModeDefinitionObj)
    nSpecification: TypePtr;
    nDefiniens: DefiniensPtr;
    constructor Init(const aPos: Position; aRedef: boolean; aPattern: ModePatternPtr;
  aSpec: TypePtr; aDef: DefiniensPtr);
    destructor Done; virtual;
  end ;

```

961. Constructor.

```

< Implementation for wsmarticle.pas 854 > +≡
constructor StandardModeDefinitionObj.Init(const aPos: Position;
  aRedef: boolean; aPattern: ModePatternPtr; aSpec: TypePtr; aDef: DefiniensPtr);
  begin inherited Init(aPos, defStandardMode, aRedef, aPattern); nSpecification ← aSpec;
  nDefiniens ← aDef;
  end;
destructor StandardModeDefinitionObj.Done;
  begin dispose(nSpecification, Done); dispose(nDefiniens, Done); inherited Done;
  end;

```

962. Attribute definitions. Attributes, like predicates, do not need to worry about correctness conditions. It's only when we want to use them like adjectives on a type that we need to worry, but that's a registration block concern.

```
Attribute-Definition = "attr" Attribute-Pattern "means" Definiens ";" Correctness-Conditions .
Attribute-Pattern = Locus "is" [ Attribute-Loci ] Attribute-Symbol .

⟨Publicly declared types in wsmarticle.pas 852⟩ +≡
  AttributeDefinitionPtr = ↑AttributeDefinitionObj;
  AttributeDefinitionObj = object (MObject)
    nDefAttrPos: Position;
    nDefAttrPattern: AttributePatternPtr;
    nRedefinition: boolean;
    nDefiniens: DefiniensPtr;
    constructor Init(const aPos: Position; aRedef: boolean; aPattern: AttributePatternPtr;
      aDef: DefiniensPtr);
    destructor Done; virtual;
  end ;
```

963. Constructor.

```
⟨Implementation for wsmarticle.pas 854⟩ +≡
constructor AttributeDefinitionObj.Init(const aPos: Position;
  aRedef: boolean; aPattern: AttributePatternPtr; aDef: DefiniensPtr);
begin nDefAttrPos ← aPos; nRedefinition ← aRedef; nDefAttrPattern ← aPattern;
  nDefiniens ← aDef;
end;

destructor AttributeDefinitionObj.Done;
begin dispose(nDefAttrPattern, Done); dispose(nDefiniens, Done);
end;
```

964. Predicate definitions. Predicates are among the less demanding of the definitions: they are always well-defined, so we do not need to worry about correctness conditions.

```
Predicate-Definition = "pred" Predicate-Pattern [ "means" Definiens ] ";"
Correctness-Conditions { Predicate-Property } .
Predicate-Pattern = [ Loci ] Predicate-Symbol [ Loci ] .
Predicate-Property = ("symmetry" | "asymmetry" | "connectedness" | "reflexivity" | "irreflexivity")
  Justification ";" .
Predicate-Synonym = "synonym" Predicate-Pattern "for" Predicate-Pattern ";" .
Predicate-Antonym = "antonym" Predicate-Pattern "for" Predicate-Pattern ";" .
Predicate-Symbol = Symbol | "=" .

⟨Publicly declared types in wsmarticle.pas 852⟩ +≡
  PredicateDefinitionPtr = ↑PredicateDefinitionObj;
  PredicateDefinitionObj = object (MObject)
    nDefPredPos: Position;
    nDefPredPattern: PredicatePatternPtr;
    nRedefinition: boolean;
    nDefiniens: DefiniensPtr;
    constructor Init(const aPos: Position; aRedef: boolean; aPattern: PredicatePatternPtr;
      aDef: DefiniensPtr);
    destructor Done; virtual;
  end ;
```

965. Constructor.

```

⟨Implementation for wsmarticle.pas 854⟩ +≡
constructor PredicateDefinitionObj.Init(const aPos: Position;
    aRedef: boolean; aPattern: PredicatePatternPtr; aDef: DefiniensPtr);
    begin nDefPredPos ← aPos; nRedefinition ← aRedef; nDefPredPattern ← aPattern;
    nDefiniens ← aDef;
    end;
destructor PredicateDefinitionObj.Done;
    begin dispose(nDefPredPattern, Done); dispose(nDefiniens, Done);
    end;

```

966. Functor definitions. We can also define new terms. Well, they introduce “term constructors” (constructors for terms). Mizar calls these guys “functors”.

Functor definitions need to establish the well-definedness of the new term constructor. What this means depends on whether we define the new term using “means” or “equals”, i.e.,

- (1) “⟨new term⟩ **means** ⟨formula⟩” requires proving the existence and uniqueness of the new term;
- (2) “⟨new term⟩ **equals** ⟨term expression⟩” requires proving the new term has the given type.

Why do we need to prove well-definedness? Well, classical logic requires proving there exists a model for a theory, so our hands are tied. If we removed this restriction, then we’d end up with something called “free logic”, which is... weird.

```

Functor-Definition = "func" Functor-Pattern [ Specification ]
    [ ( "means" | "equals" ) Definiens ] ";"
    Correctness-Conditions { Functor-Property } .
Functor-Pattern = [ Functor-Loci ] Functor-Symbol [ Functor-Loci ]
    | Left-Functor-Bracket Loci Right-Functor-Bracket .
Functor-Property = ( "commutativity" | "idempotence" | "involutiveness" | "projectivity" )
    Justification ";" .
Functor-Synonym = "synonym" Functor-Pattern "for" Functor-Pattern ";" .
Functor-Loci = Locus | "(" Loci ")" .
Functor-Symbol = Symbol .
Left-Functor-Bracket = Symbol | "{" | "[" .
Right-Functor-Bracket = Symbol | "}" | "]" .
⟨Publicly declared types in wsmarticle.pas 852⟩ +≡
    FunctorDefinitionPtr = ↑FunctorDefinitionObj;
    FunctorDefinitionObj = object (MObject)
        nDefFuncPos: Position;
        nDefFuncPattern: FunctorPatternPtr;
        nRedefinition: boolean;
        nSpecification: TypePtr;
        nDefiningWay: HowToDefine;
        nDefiniens: DefiniensPtr;
        constructor Init(const aPos: Position; aRedef: boolean; aPattern: FunctorPatternPtr;
            aSpec: TypePtr; aDefWay: HowToDefine; aDef: DefiniensPtr);
        destructor Done; virtual;
    end ;

```

967. Constructor.

(Implementation for `wsmarticle.pas` 854) +≡
constructor *FunctorDefinitionObj*.Init(**const** *aPos*: *Position*; *aRedef*: *boolean*;
aPattern: *FunctorPatternPtr*; *aSpec*: *TypePtr*; *aDefWay*: *HowToDefine*; *aDef*: *DefiniensPtr*);
begin *nDefFuncPos* ← *aPos*; *nRedefinition* ← *aRedef*; *nDefFuncPattern* ← *aPattern*;
nSpecification ← *aSpec*; *nDefiningWay* ← *aDefWay*; *nDefiniens* ← *aDef*;
end;
destructor *FunctorDefinitionObj*.Done;
begin *dispose*(*nDefFuncPattern*, Done); *dispose*(*nDefiniens*, Done);
end;

968. Notation block. We can recall the syntax for notation blocks.

Notation-Block = "notation" { Loci-Declaration | Notation-Declaration } "end" .

Notation-Declaration = Mode-Synonym
| Functor-Synonym
| Attribute-Synonym | Attribute-Antonym
| Predicate-Synonym | Predicate-Antonym .

Mode-Synonym = "synonym" Mode-Pattern "for" Mode-Pattern ";" .

Functor-Synonym = "synonym" Functor-Pattern "for" Functor-Pattern ";" .

Predicate-Synonym = "synonym" Predicate-Pattern "for" Predicate-Pattern ";" .

Predicate-Antonym = "antonym" Predicate-Pattern "for" Predicate-Pattern ";" .

Attribute-Synonym = "synonym" Attribute-Pattern "for" Attribute-Pattern ";" .

Attribute-Antonym = "antonym" Attribute-Pattern "for" Attribute-Pattern ";" .

The reader will observe all these notation items relate a new pattern which is either a synonym or antonym for an old pattern. That is to say, we only need two patterns to store as data in a notation item node in the abstract syntax tree.

(Publicly declared types in `wsmarticle.pas` 852) +≡
NotationDeclarationPtr = ↑*NotationDeclarationObj*;
NotationDeclarationObj = **object** (*mObject*)
nNotationPos: *Position*;
nNotationSort: *ItemKind*;
nOriginPattern, *nNewPattern*: *PatternPtr*;
constructor *Init*(**const** *aPos*: *Position*; *aNSort*: *ItemKind*; *aNewPatt*, *aOrigPatt*: *PatternPtr*);
destructor *Done*; *virtual*;
end ;

969. Constructor.

(Implementation for `wsmarticle.pas` 854) +≡
constructor *NotationDeclarationObj*.Init(**const** *aPos*: *Position*; *aNSort*: *ItemKind*;
aNewPatt, *aOrigPatt*: *PatternPtr*);
begin *nNotationPos* ← *aPos*; *nNotationSort* ← *aNSort*; *nOriginPattern* ← *aOrigPatt*;
nNewPattern ← *aNewPatt*;
end;
destructor *NotationDeclarationObj*.Done;
begin *dispose*(*nOriginPattern*, Done); *dispose*(*nNewPattern*, Done);
end;

970. Assumptions in a definition block. The syntax for assumptions in a definition block looks like:

```
Assumption = Single-Assumption | Collective-Assumption | Existential-Assumption .
Single-Assumption = "assume" Proposition ";" .
Collective-Assumption = "assume" Conditions ";" .
Existential-Assumption = "given" Qualified-Variables [ "such" Conditions ] ";" .
Conditions = "that" Proposition { "and" Proposition } .
Proposition = [ Label-Identifier ":" ] Sentence .
Sentence = Formula-Expression .
```

```
< Publicly declared types in wsmarticle.pas 852 > +≡
  AssumptionKind = (SingleAssumption, CollectiveAssumption, ExistentialAssumption);
  AssumptionPtr = ↑AssumptionObj;
  AssumptionObj = object (MObject)
    nAssumptionPos: Position;
    nAssumptionSort: AssumptionKind;
    constructor Init(const aPos: Position; aSort: AssumptionKind);
  end ;
```

971. Constructor.

```
< Implementation for wsmarticle.pas 854 > +≡
constructor AssumptionObj.Init(const aPos: Position; aSort: AssumptionKind);
  begin nAssumptionPos ← aPos; nAssumptionSort ← aSort;
end ;
```

972. Single assumption. When a definition has a single assumption, i.e., a single (usually labeled) formula.

```
< Publicly declared types in wsmarticle.pas 852 > +≡
  SingleAssumptionPtr = ↑SingleAssumptionObj;
  SingleAssumptionObj = object (AssumptionObj)
    nProp: PropositionPtr;
    constructor Init(const aPos: Position; aProp: PropositionPtr);
    destructor Done; virtual;
  end ;
```

973. Constructor.

```
< Implementation for wsmarticle.pas 854 > +≡
constructor SingleAssumptionObj.Init(const aPos: Position; aProp: PropositionPtr);
  begin inherited Init(aPos, SingleAssumption); nProp ← aProp;
end ;
destructor SingleAssumptionObj.Done;
  begin dispose(nProp, Done);
end ;
```


974. Collective assumption. This describes the case when the assumption is “assume C_1 and ... and C_n ”.

```

⟨ Publicly declared types in wsmarticle.pas 852 ⟩ +≡
  CollectiveAssumptionPtr = ↑CollectiveAssumptionObj;
  CollectiveAssumptionObj = object (AssumptionObj)
    nConditions: PList;
    constructor Init(const aPos: Position; aProps: PList);
    destructor Done; virtual;
  end ;

```

975. Constructor.

```

⟨ Implementation for wsmarticle.pas 854 ⟩ +≡
constructor CollectiveAssumptionObj.Init(const aPos: Position; aProps: PList);
  begin inherited Init(aPos, CollectiveAssumption); nConditions ← aProps;
  end;
destructor CollectiveAssumptionObj.Done;
  begin dispose(nConditions, Done);
  end;

```

976. Existential assumption. I must confess I am surprised to see an existential assumption node being a subclass of a collective assumption node.

```

⟨ Publicly declared types in wsmarticle.pas 852 ⟩ +≡
  ExistentialAssumptionPtr = ↑ExistentialAssumptionObj;
  ExistentialAssumptionObj = object (CollectiveAssumptionObj)
    nQVars: PList;
    constructor Init(const aPos: Position; aQVars, aProps: PList);
    destructor Done; virtual;
  end ;

```

977. Constructor.

```

⟨ Implementation for wsmarticle.pas 854 ⟩ +≡
constructor ExistentialAssumptionObj.Init(const aPos: Position; aQVars, aProps: PList);
  begin AssumptionObj.Init(aPos, CollectiveAssumption); nConditions ← aProps; nQVars ← aQVars;
  end;
destructor ExistentialAssumptionObj.Done;
  begin dispose(nQVars, Done); inherited Done;
  end;

```

978. Correctness conditions. The syntax for correctness conditions:

```
Correctness-Conditions = {Correctness-Condition} [ "correctness" Justification ";" ] .
Correctness-Condition =
  ( "existence" | "uniqueness" | "coherence" | "compatibility" | "consistency" | "reducibility" )
  Justification ";" .
```

We begin with an abstract base class for correctness conditions.

```
< Publicly declared types in wsmarticle.pas 852 > +≡
  CorrectnessPtr = ↑CorrectnessObj;
  CorrectnessObj = object (MObject)
    nCorrCondPos: Position;
    nJustification: JustificationPtr;
    constructor Init(const aPos: Position; aJustification: JustificationPtr);
    destructor Done; virtual;
  end ;
```

979. Constructor.

```
< Implementation for wsmarticle.pas 854 > +≡
constructor CorrectnessObj.Init(const aPos: Position; aJustification: JustificationPtr);
  begin nCorrCondPos ← aPos; nJustification ← aJustification;
  end;
destructor CorrectnessObj.Done;
  begin dispose(nJustification, Done);
  end;
```

980. Correctness condition. For the correctness condition associated with a definition or registration, we have this *CorrectnessCondition* object. When we need multiple correctness conditions, we extend it with a subclass.

```
< Publicly declared types in wsmarticle.pas 852 > +≡
  CorrectnessConditionPtr = ↑CorrectnessConditionObj;
  CorrectnessConditionObj = object (CorrectnessObj)
    nCorrCondSort: CorrectnessKind;
    constructor Init(const aPos: Position; aSort: CorrectnessKind; aJustification: JustificationPtr);
    destructor Done; virtual;
  end ;
```

981. Constructor.

```
< Implementation for wsmarticle.pas 854 > +≡
constructor CorrectnessConditionObj.Init(const aPos: Position;
  aSort: CorrectnessKind; aJustification: JustificationPtr);
  begin inherited Init(aPos, aJustification); nCorrCondSort ← aSort;
  end;
destructor CorrectnessConditionObj.Done;
  begin inherited Done;
  end;
```

982. Multiple correctness conditions. For, e.g., functors which require proving both “existence” and “uniqueness”, we have a *CorrectnessConditions* class. This extends the [singular] *CorrectnessCondition* class.

```
(Publicly declared types in wsmarticle.pas 852) +≡
  CorrectnessConditionsSet = set of CorrectnessKind;
  CorrectnessConditionsPtr = ↑CorrectnessConditionsObj;
  CorrectnessConditionsObj = object (CorrectnessObj)
    nConditions: CorrectnessConditionsSet;
    constructor Init(const aPos: Position; const aConds: CorrectnessConditionsSet;
      aJustification: JustificationPtr);
    destructor Done; virtual;
  end ;
```

983. Constructor.

```
(Implementation for wsmarticle.pas 854) +≡
constructor CorrectnessConditionsObj.Init(const aPos: Position;
  const aConds: CorrectnessConditionsSet;
  aJustification: JustificationPtr);
begin inherited Init(aPos, aJustification); nConditions ← aConds;
end;
destructor CorrectnessConditionsObj.Done;
begin inherited Done;
end;
```

984. Definition properties. The grammar for properties in a definition looks like:

Mode-Property = "sethood" Justification ";" .

Functor-Property = ("commutativity" | "idempotence" | "involutiveness" | "projectivity")
Justification ";" .

Predicate-Property = ("symmetry" | "asymmetry" | "connectedness" | "reflexivity" | "irreflexivity")
Justification ";" .

We see these are all, more or less, “the same”: we have a “kind” of property and a justification. We recall (§720) that we have already introduced the “kind” of properties. So the class describing a definition property node in the abstract syntax tree is:

```
(Publicly declared types in wsmarticle.pas 852) +≡
  PropertyPtr = ↑PropertyObj;
  PropertyObj = object (MObject)
    nPropertyPos: Position;
    nPropertySort: PropertyKind;
    nJustification: JustificationPtr;
    constructor Init(const aPos: Position; aSort: PropertyKind; aJustification: JustificationPtr);
    destructor Done; virtual;
  end ;
```

985. Constructor.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```
constructor PropertyObj.Init(const aPos: Position; aSort: PropertyKind;
    aJustification: JustificationPtr);
    begin nPropertyPos ← aPos; nPropertySort ← aSort; nJustification ← aJustification;
    end;
destructor PropertyObj.Done;
    begin inherited Done;
    end;
```

Section 21.9. REGISTRATIONS

986. There are three “main” types of registrations, which are “cluster registrations” (because they all involve the “cluster” keyword):

- (1) Existential registrations are of the form “cluster $\langle attribute \rangle$ for $\langle type \rangle$ ” and establishes that a given attribute can act as an adjective for the type.
- (2) Conditional registrations are of the form “cluster $\langle attribute_1 \rangle \rightarrow \langle attribute_2 \rangle$ for $\langle type \rangle$ ” which tells Mizar that when $\langle attribute_1 \rangle$ is established for a term, then Mizar can automatically add $\langle attribute_2 \rangle$ for the term
- (3) Functorial registrations are of the form “cluster $\langle term \rangle \rightarrow \langle attribute \rangle$ [for $\langle type \rangle$]” which will automatically add an attribute to a term.

We also have three lesser registrations which are still important:

- (1) Sethood registrations, establishes a type can be used as a set in a Fraenkel term.
- (2) Reduction registration, which allows Mizar’s term rewriting module to use this rule when reasoning about things.
- (3) Identification registration, which allows Mizar to identify terms of different types.

```
Cluster-Registration = Existential-Registration
```

```
| Conditional-Registration
```

```
| Functorial-Registration .
```

```
Existential-Registration = "cluster" Adjective-Cluster "for" Type-Expression ";"
```

```
Correctness-Conditions .
```

```
Adjective-Cluster = { Adjective } .
```

```
Adjective = [ "non" ] [ Adjective-Arguments ] Attribute-Symbol .
```

```
Conditional-Registration = "cluster" Adjective-Cluster "->" Adjective-Cluster "for" Type-Expression ";"
```

```
Correctness-Conditions .
```

```
Functorial-Registration = "cluster" Term-Expression "->" Adjective-Cluster [ "for" Type-Expression ] ";"
```

```
Correctness-Conditions .
```

```
Identify-Registration = "identify" Functor-Pattern "with" Functor-Pattern
```

```
[ "when" Locus "=" Locus { ", " Locus "=" Locus } ] ";"
```

```
Correctness-Conditions .
```

```
Property-Registration = "sethood" "of" Type-Expression Justification ";" .
```

```
Reduction-Registration = "reduce" Term-Expression "to" Term-Expression ";"
```

```
Correctness-Conditions .
```

987. Cluster registration. We have a base class for the three types of cluster registrations.

(Publicly declared types in `wsmarticle.pas` 852) +≡

```
ClusterRegistrationKind = (ExistentialRegistration, ConditionalRegistration, FunctorialRegistration);
```

```
ClusterPtr = ↑ClusterObj;
```

```
ClusterObj = object (MObject)
```

```
  nClusterPos: Position;
```

```
  nClusterKind: ClusterRegistrationKind;
```

```
  nConsequent: PList;
```

```
  nClusterType: TypePtr;
```

```
  constructor Init(const aPos: Position; aKind: ClusterRegistrationKind; aCons: PList;
```

```
    aTyp: TypePtr);
```

```
  destructor Done; virtual;
```

```
end ;
```

988. Constructor.

```

⟨Implementation for wsmarticle.pas 854⟩ +≡
constructor ClusterObj.Init(const aPos: Position;
    aKind: ClusterRegistrationKind; aCons: PList; aTyp: TypePtr);
    begin nClusterPos ← aPos; nClusterKind ← aKind; nConsequent ← aCons; nClusterType ← aTyp;
    end;
destructor ClusterObj.Done;
    begin dispose(nConsequent, Done);
    end;

```

989. Existential cluster. We register the fact there always exists a term of a given type satisfying an attribute (e.g., “empty” for “set” means there always exists an empty set; registering the existential cluster “non empty” for “set” means there always exists a nonempty set). This means the attribute may henceforth be used as an adjective on the type.

```

⟨Publicly declared types in wsmarticle.pas 852⟩ +≡
EClusterPtr = ↑EClusterObj;
EClusterObj = object (ClusterObj)
    constructor Init(const aPos: Position; aCons: PList; aTyp: TypePtr);
    destructor Done; virtual;
end ;

```

990. Constructor. There are no additional fields to an existential cluster object, so it literally passes the parameters onto the superclass’s constructor.

```

⟨Implementation for wsmarticle.pas 854⟩ +≡
constructor EClusterObj.Init(const aPos: Position; aCons: PList; aTyp: TypePtr);
    begin ClusterObj.Init(aPos, ExistentialRegistration, aCons, aTyp);
    end;
destructor EClusterObj.Done;
    begin if nClusterType ≠ nil then dispose(nClusterType, Done);
    inherited Done;
    end;

```

991. Conditional cluster. For example “empty sets” are always “finite sets”. This requires tracking the antecedent (“empty”), and the superclass tracks the consequents (“finite”).

```

⟨Publicly declared types in wsmarticle.pas 852⟩ +≡
CClusterPtr = ↑CClusterObj;
CClusterObj = object (ClusterObj)
    nAntecedent: PList;
    constructor Init(const aPos: Position; aAntec, aCons: PList; aTyp: TypePtr);
    destructor Done; virtual;
end ;

```

992. Constructor.

```

⟨Implementation for wsmarticle.pas 854⟩ +≡
constructor CClusterObj.Init(const aPos: Position; aAntec, aCons: PList; aTyp: TypePtr);
    begin ClusterObj.Init(aPos, ConditionalRegistration, aCons, aTyp); nAntecedent ← aAntec;
    end;
destructor CClusterObj.Done;
    begin dispose(nAntecedent, Done); inherited Done;
    end;

```

993. Functorial cluster. The generic form a functorial registrations associated to a term some cluster of adjectives. We need to track the term, but the superclass can manage the cluster of adjectives.

```

⟨Publicly declared types in wsmarticle.pas 852⟩ +≡
  FClusterPtr = ↑FClusterObj;
  FClusterObj = object (ClusterObj)
    nClusterTerm: TermPtr;
    constructor Init(const aPos: Position; aTrm: TermPtr; aCons: PList; aTyp: TypePtr);
    destructor Done; virtual;
  end ;

```

994. Constructor.

```

⟨Implementation for wsmarticle.pas 854⟩ +≡
constructor FClusterObj.Init(const aPos: Position;
  aTrm: TermPtr; aCons: PList; aTyp: TypePtr);
  begin ClusterObj.Init(aPos, FunctorialRegistration, aCons, aTyp); nClusterTerm ← aTrm;
  end;
destructor FClusterObj.Done;
  begin if nClusterTerm ≠ nil then Dispose(nClusterTerm, Done);
  if nClusterType ≠ nil then dispose(nClusterType, Done);
  inherited Done;
  end;

```

995. Loci equality. This is used in identification registrations.

```

⟨Publicly declared types in wsmarticle.pas 852⟩ +≡
  LociEqualityPtr = ↑LociEqualityObj;
  LociEqualityObj = object (mObject)
    nEqPos: Position;
    nLeftLocus, nRightLocus: LocusPtr;
    constructor Init(const aPos: Position; aLeftLocus, aRightLocus: LocusPtr);
    destructor Done; virtual;
  end ;

```

996. Constructor.

```

⟨Implementation for wsmarticle.pas 854⟩ +≡
constructor LociEqualityObj.Init(const aPos: Position; aLeftLocus, aRightLocus: LocusPtr);
  begin nEqPos ← aPos; nLeftLocus ← aLeftLocus; nRightLocus ← aRightLocus;
  end;
destructor LociEqualityObj.Done;
  begin Dispose(nLeftLocus, Done); dispose(nRightLocus, Done);
  end;

```

997. Identification registration. Term identification was first introduced in Artur Korniłowicz’s “How to define terms in Mizar effectively” (in A. Grabowski and A. Naumowicz (eds.), *Computer Reconstruction of the Body of Mathematics*, issue of *Studies in Logic, Grammar and Rhetoric* **18** no.31 (2009), pp. 67–77). See also §2.7 of Adam Grabowski, Artur Korniłowicz, and Adam Naumowicz’s “Mizar in a Nutshell” ([doi:10.6092/issn.1972-5787/1980](https://doi.org/10.6092/issn.1972-5787/1980)) for user-oriented details.

```

⟨ Publicly declared types in wsmarticle.pas 852 ⟩ +≡
  IdentifyRegistrationPtr = ↑IdentifyRegistrationObj;
  IdentifyRegistrationObj = object (mObject)
    nIdentifyPos: Position;
    nOriginPattern, nNewPattern: PatternPtr;
    nEqLocList: PList;
    constructor Init(const aPos: Position; aNewPatt, aOrigPatt: PatternPtr; aEqList: PList);
    destructor Done; virtual;
  end ;

```

998. Constructor.

```

⟨ Implementation for wsmarticle.pas 854 ⟩ +≡
constructor IdentifyRegistrationObj.Init(const aPos: Position;
  aNewPatt, aOrigPatt: PatternPtr; aEqList: PList);
  begin nIdentifyPos ← aPos; nOriginPattern ← aOrigPatt; nNewPattern ← aNewPatt;
  nEqLocList ← aEqList;
  end;
destructor IdentifyRegistrationObj.Done;
  begin dispose(nOriginPattern, Done); dispose(nNewPattern, Done);
  if nEqLocList ≠ nil then dispose(nEqLocList, Done);
  end;

```

999. Property registration. These were introduced in Mizar to facilitated registering “sethood” for types. Thus far, only the “sethood” property is handled in this registration.

```

⟨ Publicly declared types in wsmarticle.pas 852 ⟩ +≡
  PropertyRegistrationPtr = ↑PropertyRegistrationObj;
  PropertyRegistrationObj = object (mObject)
    nPropertyPos: Position;
    nPropertySort: PropertyKind;
    constructor Init(const aPos: Position; aKind: PropertyKind);
    destructor Done; virtual;
  end ;

```

1000. Constructor.

```

⟨ Implementation for wsmarticle.pas 854 ⟩ +≡
constructor PropertyRegistrationObj.Init(const aPos: Position; aKind: PropertyKind);
  begin nPropertyPos ← aPos; nPropertySort ← aKind;
  end;
destructor PropertyRegistrationObj.Done;
  begin end;

```


1001. Sethood registration. Artur Kornilowicz’s “Sethood Property in Mizar” (in *Joint Proc. FMM and LML Workshops*, 2019, ceur-ws.org/Vol-2634/FMM3.pdf) introduces this “sethood” property. It’s the first (and, so far, only) property registration in Mizar.

```

⟨ Publicly declared types in wsmarticle.pas 852 ⟩ +≡
  SethoodRegistrationPtr = ↑SethoodRegistrationObj;
  SethoodRegistrationObj = object (PropertyRegistrationObj)
    nSethoodType: TypePtr;
    nJustification: JustificationPtr;
    constructor Init(const aPos: Position; aKind: PropertyKind; aType: TypePtr);
    destructor Done; virtual;
  end ;

```

1002. Constructor.

```

⟨ Implementation for wsmarticle.pas 854 ⟩ +≡
constructor SethoodRegistrationObj.Init(const aPos: Position;
  aKind: PropertyKind; aType: TypePtr);
  begin inherited Init(aPos, aKind); nSethoodType ← aType; nJustification ← nil;
  end;
destructor SethoodRegistrationObj.Done;
  begin dispose(nSethoodType, Done); dispose(nJustification, Done); inherited Done;
  end;

```

1003. Reduce registration. These were introduced, I think, in Artur Kornilowicz’s “On rewriting rules in Mizar” (*J. Autom. Reason.* **50** no.2 (2013) 203–210, [doi:10.1007/s10817-012-9261-6](https://doi.org/10.1007/s10817-012-9261-6)). These extend the checker with new term rewriting rules.

```

⟨ Publicly declared types in wsmarticle.pas 852 ⟩ +≡
  ReduceRegistrationPtr = ↑ReduceRegistrationObj;
  ReduceRegistrationObj = object (MObject)
    nReducePos: Position;
    nOriginTerm, nNewTerm: TermPtr;
    constructor Init(const aPos: Position; aOrigTerm, aNewTerm: TermPtr);
    destructor Done; virtual;
  end ;

```

1004. Constructor.

```

⟨ Implementation for wsmarticle.pas 854 ⟩ +≡
constructor ReduceRegistrationObj.Init(const aPos: Position; aOrigTerm, aNewTerm: TermPtr);
  begin nReducePos ← aPos; nOriginTerm ← aOrigTerm; nNewTerm ← aNewTerm;
  end;
destructor ReduceRegistrationObj.Done;
  begin dispose(nOriginTerm, Done); dispose(nNewTerm, Done);
  end;

```

Section 21.10. HELPER FUNCTIONS

1005. Capitalization checks if the first character c is lowercase. If so, then set the leading character to be $c \leftarrow c - (\text{ord}(\text{'a'}) - \text{ord}(\text{'A'}))$. But it leaves the rest of the string untouched.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```
function CapitalizeName(aName : string): string;
  begin result ← aName;
  if aName[1] ∈ [‘a’ .. ‘z’] then dec(Result[1], ord(‘a’) – ord(‘A’))
  end;
```

1006. Uncapitalizing works in the opposite direction, setting the first letter c of a string to be $c \leftarrow c + (\text{ord}(\text{'a'}) - \text{ord}(\text{'A'}))$. Observe capitalizing and uncapitalizing are “nearly inverses” of each other: $\text{CapitalizeName}(\text{UncapitalizeName}(\text{CapitalizeName}(s))) = \text{CapitalizeName}(s)$, and similarly we find $\text{UncapitalizeName}(\text{CapitalizeName}(\text{UncapitalizeName}(s))) = \text{UncapitalizeName}(s)$.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```
function UncapitalizeName(aName : string): string;
  begin result ← aName;
  if aName[1] ∈ [‘A’ .. ‘Z’] then inc(Result[1], ord(‘a’) – ord(‘A’))
  end;
```

1007. We will be populating global variables tracking names of identifiers, modes, and other syntactic classes.

⟨Global variables publicly declared in `wsmarticle.pas` 1007⟩ ≡

```
var IdentifierName, AttributeName, StructureName, ModeName, PredicateName, FunctorName,
    SelectorName, LeftBracketName, RightBracketName, MMLIdentifierName: array of string;
```

This code is used in section 850.

1008. We will want to initialize these global variables based on previous passes of the scanner.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```
procedure InitScannerNames;
  var i, lCnt, lNr: integer; lDct: text; lInFile: XMLInStreamPtr; lKind, lDummy: AnsiChar;
      lString: string;
  begin ⟨Populate global variables with XML entities 1009⟩;
  ⟨Reset reserved keywords 1011⟩;
  { Identifiers }
  ⟨Initialize identifier names from .idx file 1012⟩;
  end;
```

1009. We need to initialize the length for each of these arrays. Even a crude approximation works, like the total number of lines in the `.dct` file. Then we transform each line of the `lDct` (dictionary file) into appropriate entries of the relevant array.

```

⟨Populate global variables with XML entities 1009⟩ ≡
  assign(lDct, MizFileName + ` .dct `); reset(lDct); lCnt ← 0;
  while ¬seekEof(lDct) do
    begin readln(lDct); inc(lCnt);
    end;
  setlength(AttributeName, lCnt); setlength(StructureName, lCnt); setlength(ModeName, lCnt);
  setlength(PredicateName, lCnt); setlength(FunctorName, lCnt); setlength(SelectorName, lCnt);
  setlength(LeftBracketName, lCnt); setlength(RightBracketName, lCnt);
  setlength(MMLIdentifierName, lCnt); reset(lDct);
  while ¬seekEof(lDct) do
    begin readln(lDct, lKind, lNr, lDummy, lString); ⟨Store XML version of vocabulary word 1010⟩;
    end;
  close(lDct)

```

This code is used in section 1008.

1010. We have read in from the “`.dct`” file one line. The first 148 lines of a “`.dct`” file consists of the reserved keywords for Mizar. A random example of the last few lines of such a file look like:

```

A36 VECTSP_4
A37 ORDINAL1
A38 CARD_FIL
A39 RANKNULL
A40 VECTSP_1
A41 VECTSP_6
A42 VECTSP13
A43 ALGSTR_0
A44 HALLMAR1
A45 MATROIDO

```

So we read the first leading letter of a line into `lKind`, then the number into `lNr`, the space is stuffed into `lDummy`, and the remainder of the line is placed in `lString`.

```

⟨Store XML version of vocabulary word 1010⟩ ≡
  case lKind of
    `A`: MMLIdentifierName[lNr] ← QuoteStrForXML(lString);
    `G`: StructureName[lNr] ← QuoteStrForXML(lString);
    `M`: ModeName[lNr] ← QuoteStrForXML(lString);
    `K`: LeftBracketName[lNr] ← QuoteStrForXML(lString);
    `L`: RightBracketName[lNr] ← QuoteStrForXML(lString);
    `O`: FunctorName[lNr] ← QuoteStrForXML(lString);
    `R`: PredicateName[lNr] ← QuoteStrForXML(lString);
    `U`: SelectorName[lNr] ← QuoteStrForXML(lString);
    `V`: AttributeName[lNr] ← QuoteStrForXML(lString);
  endcases

```

This code is used in section 1009.

1011. Preserve reserved keywords. We want to prevent the user from “overwriting” or “shadowing” the builtin primitive reserved words. This should probably be documented in the user-manual somewhere. The reserved words are: “**strict**”, “**set**”, “**=**”, and the brackets `[]`, braces `{}`, and parentheses `()`. Curiously, “**object**” is not considered a ‘primitive’ worth preserving.

```

⟨ Reset reserved keywords 1011 ⟩ ≡
  AttributeName[StrictSym] ← `strict`; ModeName[SetSym] ← `set`;
  PredicateName[EqualitySym] ← `=`; LeftBracketName[SquareBracket] ← `[`;
  LeftBracketName[CurlyBracket] ← `{`; LeftBracketName[RoundedBracket] ← `(`;
  RightBracketName[SquareBracket] ← `]`; RightBracketName[CurlyBracket] ← `}`;
  RightBracketName[RoundedBracket] ← `)`

```

This code is used in section 1008.

1012. The `.idx` file provides numbers for the local labels and article names referenced in an article.

```

⟨ Initialize identifier names from .idx file 1012 ⟩ ≡
  assign(lDct, MizFileName + `.idx`); reset(lDct); lCnt ← 0;
  while ¬seekEof(lDct) do
    begin readln(lDct); inc(lCnt);
    end;
  close(lDct);
  setlength(IdentifierName, lCnt); IdentifierName[0] ← ``;
  lInFile ← new(XMLInStreamPtr, OpenFile(MizFileName + `.idx`)); lInFile↑.NextElementState;
  lInFile↑.NextElementState;
  while (lInFile.nState = eStart) ∧ (lInFile.nElName = XMLElemName[elSymbol]) do
    begin lNr ← lInFile↑.GetIntAttr(`nr`); lString ← lInFile↑.GetAttr(`name`);
    IdentifierName[lNr] ← lString; lInFile↑.NextElementState; lInFile↑.NextElementState;
    end;
  dispose(lInFile, Done)

```

This code is used in section 1008.

1013. We will want to obtain the name for an article ID number, provided it is a legal number (i.e., less than the dictionary for article ID numbers). This function looks up its entry in the *IdentifierName* array.

```

⟨ Implementation for wsmarticle.pas 854 ⟩ +≡
function IdentRepr(aIdNr : integer): string;
begin mizassert(2000, aIdNr ≤ length(IdentifierName));
if aIdNr > 0 then IdentRepr ← IdentifierName[aIdNr]
else IdentRepr ← ``;
end;

```

Section 21.11. WRITING WSM XML FILES

1014.

```

⟨ Publicly declared types in wsmarticle.pas 852 ⟩ +≡
  OutWSMizFilePtr = ↑ OutWSMizFileObj;
  OutWSMizFileObj = object (XMLOutStreamObj)
    nDisplayInformationOnScreen: boolean;
    nMizarAppearance: boolean;
    constructor OpenFile(const aFileName: string);
    constructor OpenFileWithXSL(const aFileName: string);
    destructor Done; virtual;
    procedure Out_TextProper(aWSTextProper : WSTextProperPtr); virtual;
    procedure Out_Block(aWSBlock : WSBlockPtr); virtual;
    procedure Out_Item(aWSItem : WSItemPtr); virtual;
    procedure Out_ItemContentsAttr(aWSItem : WSItemPtr); virtual;
    procedure Out_ItemContents(aWSItem : WSItemPtr); virtual;
    procedure Out_Variable(aVar : VariablePtr); virtual;
    procedure Out_ReservedVariable(aVar : VariablePtr); virtual;
    procedure Out_TermList(aTrmList : PList); virtual;
    procedure Out_Adjective(aAttr : AdjectiveExpressionPtr); virtual;
    procedure Out_AdjectiveList(aCluster : PList); virtual;
    procedure Out_Type(aTyp : TypePtr); virtual;
    procedure Out_ImplicitlyQualifiedVariable(aSegm : ImplicitlyQualifiedSegmentPtr); virtual;
    procedure Out_VariableSegment(aSegm : QualifiedSegmentPtr); virtual;
    procedure Out_PrivatePredicativeFormula(aFrm : PrivatePredicativeFormulaPtr); virtual;
    procedure Out_Formula(aFrm : FormulaPtr); virtual;
    procedure Out_Term(aTrm : TermPtr); virtual;
    procedure Out_SimpleTerm(aTrm : SimpleTermPtr); virtual;
    procedure Out_PrivateFunctorTerm(aTrm : PrivateFunctorTermPtr); virtual;
    procedure Out_InternalSelectorTerm(aTrm : InternalSelectorTermPtr); virtual;
    procedure Out_TypeList(aTypeList : PList); virtual;
    procedure Out_Locus(aLocus : LocusPtr); virtual;
    procedure Out_Loci(aLoci : PList); virtual;
    procedure Out_Pattern(aPattern : PatternPtr); virtual;
    procedure Out_Label(aLab : LabelPtr); virtual;
    procedure Out_Definiens(aDef : DefiniensPtr); virtual;
    procedure Out_ReservationSegment(aRes : ReservationSegmentPtr); virtual;
    procedure Out_SchemeNameInSchemeHead(aSch : SchemePtr); virtual;
    procedure Out_CompactStatement(aCStm : CompactStatementPtr; aBlock : wsBlockPtr); virtual;
    procedure Out_RegularStatement(aRStm : RegularStatementPtr; aBlock : wsBlockPtr); virtual;
    procedure Out_Proposition(aProp : PropositionPtr); virtual;
    procedure Out_LocalReference(aRef : LocalReferencePtr); virtual;
    procedure Out_References(aRefs : PList); virtual;
    procedure Out_Link(aInf : JustificationPtr); virtual;
    procedure Out_SchemeJustification(aInf : SchemeJustificationPtr); virtual;
    procedure Out_Justification(aInf : JustificationPtr; aBlock : wsBlockPtr); virtual;
  end ;

```

1015. Constructor. The constructor *OutWSMizFileObj.OpenFileWithXSL* is not used anywhere, nor is the associated “*wsmiz.xml*” file present anywhere.

Importantly, the *nMizarAppearance* field controls whether the XML generated includes the raw lexeme string as an attribute in the XML elements or not.

The constructor *OpenFileWithXSL* is never used. The XML stylesheet *wsmiz.xml* does not seem to be present in the Mizar distribution.

⟨Implementation for *wsmarticle.pas* 854⟩ +≡

```

constructor OutWSMizFileObj.OpenFile(const aFileName: string);
  begin inherited OpenFile(aFileName); nMizarAppearance ← false;
  nDisplayInformationOnScreen ← false;
  end;
constructor OutWSMizFileObj.OpenFileWithXSL(const aFileName: string);
  begin inherited OpenFile(aFileName);
  OutString(‘<?xml-stylesheet_type="text/xml" href="file://’ + MizFiles + ‘wsmiz.xml"?>’ + #10);
  nMizarAppearance ← false;
  end;
destructor OutWSMizFileObj.Done;
  begin inherited Done;
  end;

```

1016. We can write the XML for a *wsTextProper* object (§856). This writes out the start tag, the children, and the end-tag for the “text proper” and its contents. The RNG compact schema for this looks like:

```

TextProper = element Text-Propser {
  attribute idnr { xsd:integer },
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Item*
}

```

⟨Implementation for *wsmarticle.pas* 854⟩ +≡

```

procedure OutWSMizFileObj.Out_TextProper(aWSTextProper : WSTextProperPtr);
  var i: integer;
  begin with aWSTextProper↑ do
    begin { Write the start-tag }
    Out_XElStart(BlockName[blMain]); Out_XAttr(XMLAttrName[atArticleId], nArticleId);
    Out_XAttr(XMLAttrName[atArticleExt], nArticleExt); Out_PosAsAttrs(nBlockPos); Out_XAttrEnd;
    for i ← 0 to nItems↑.Count − 1 do Out_Item(nItems.Items↑[i]); { ...then write the children }
    Out_XElEnd(BlockName[blMain]);
  end;
end;

```

1017. Writing a block out as XML works similarly: write the start-tag, then its children elements, then the end-tag.

```
Block = element Block {
  attribute kind { "Text-Propser" | "Now-Reasoning"
    | "Hereby-Reasoning" | "Definitional-Block"
    | "Notation-Block" | "Registration-Block" | "Case"
    | "Suppose" | "Scheme-Block" },
  attribute idnr { xsd:integer },
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Item*
}
```

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```
procedure OutWSMizFileObj.Out_Block(aWSBlock : WSBlockPtr);
var i: integer;
begin with aWSBlock↑ do
  begin { write the start-tag }
    Out_XElStart(XMLElemName[elBlock]);
    Out_XAttr(XMLAttrName[atKind], BlockName[nBlockKind]); CurPos ← nBlockPos;
    Out_PosAsAttrs(nBlockPos); Out_XIntAttr(XMLAttrName[atPosLine], nBlockEndPos.Line);
    Out_XIntAttr(XMLAttrName[atPosCol], nBlockEndPos.Col); Out_XAttrEnd;
    for i ← 0 to nItems↑.Count − 1 do
      begin Out_Item(nItems↑.Items↑[i]); end; { Then write the children }
    Out_XElEnd(XMLElemName[elBlock]);
  end;
end;
```

1018. Writing a term list to XML amounts to just writing the terms as XML elements. They will be contained in a parent element, so there will be no ambiguity in their role.

```
Term-List = ( Term* )
```

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```
procedure OutWSMizFileObj.Out_TermList(aTrmList : PList);
var i: integer;
begin for i ← 0 to aTrmList↑.Count − 1 do Out_Term(aTrmList↑.Items↑[i]);
end;
```

1019. The XML for an adjective boils down to two cases:

Case 1 (negated attribute). Write a `<NegatedAdjective>` tag around the XML produced from case 2 for the positive version of the attribute.

Case 2 (positive attribute). Write the adjective, and its children are the [term] arguments to the adjective (if any — if there are none, then an empty-element will be produced).

```

PositiveAdjective = element Adjective {
  attribute nr { xsd:integer },
  attribute name { text },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer }
  Term*
}
Adjective = PositiveAdjective | element NegatedAdjective {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  PositiveAdjective
}
<Implementation for wsmarticle.pas 854> +≡
procedure OutWSMizFileObj.Out_Adjective(aAttr : AdjectiveExpressionPtr);
begin case aAttr↑.nAdjectiveSort of
  wsAdjective: begin Out_XElStart(XMLElemName[elAdjective]);
    with AdjectivePtr(aAttr)↑ do
      begin Out_XIntAttr(XMLAttrName[atNr], nAdjectiveSymbol);
        if nMizarAppearance then
          Out_XAttr(XMLAttrName[atSpelling], AttributeName[nAdjectiveSymbol]);
          Out_PosAsAttrs(nAdjectivePos);
        if nArgs↑.Count = 0 then Out_XElEnd0
        else begin Out_XAttrEnd; Out_TermList(nArgs); Out_XElEnd(XMLElemName[elAdjective]);
          end;
        end;
      end;
    end;
  wsNegatedAdjective: begin Out_XElStart(XMLElemName[elNegatedAdjective]);
    with NegatedAdjectivePtr(aAttr)↑ do
      begin Out_PosAsAttrs(nAdjectivePos); Out_XAttrEnd; Out_Adjective(nArg);
        end;
      Out_XElEnd(XMLElemName[elNegatedAdjective]);
    end;
  endcases;
end;

```


1020. Writing an adjective list to XML amounts to stuffing all the adjectives into an element. If there are no adjectives, it is the empty-element.

```

Adjective-Cluster = element Adjective-Cluster {
  attribute count { xsd:integer },
  Adjective*
}

```

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

procedure OutWSMizFileObj.Out_AdjectiveList(aCluster : PList);
  var i: integer;
  begin Out_XElStart(XMLElemName[elAdjectiveCluster]);
  if aCluster↑.Count = 0 then
    begin Out_XElEnd0; exit;
    end;
  Out_XAttrEnd;
  with aCluster↑ do
    for i ← 0 to Count − 1 do Out_Adjective(Items↑[i]);
  Out_XElEnd(XMLElemName[elAdjectiveCluster]);
  end;

```

Subsection 21.11.1. Emitting XML for types

1021. Writing the XML for a Mizar type.

```

StandardType = element Standard-Type {
  attribute nr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Term*
}
StructureType = element Structure-Type {
  attribute nr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Term*
}
ClusteredType = element Clustered-Type {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Adjective-Cluster,
  Type,
}
Type = StandardType | StructureType | ClusteredType

define print_arguments(#) ≡
  if nArgs↑.Count = 0 then Out_XElEnd0
  else begin Out_XAttrEnd; Out_TermList(nArgs); Out_XElEnd(TypeName[#]);
  end
end

⟨Implementation for wsmarticle.pas 854⟩ +≡
procedure Out_WSMizFileObj.Out_Type(aTyp : TypePtr);
begin with aTyp↑ do
  case aTyp↑.nTypeSort of
    wsStandardType: with StandardTypePtr(aTyp)↑ do
      begin Out_XElStart(TypeName[wsStandardType]);
      Out_XIntAttr(XMLAttrName[atNr], nModeSymbol);
      if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], ModeName[nModeSymbol]);
      Out_PosAsAttrs(nTypePos); print_arguments(wsStandardType);
      end;
    wsStructureType: with StructTypePtr(aTyp)↑ do
      begin Out_XElStart(TypeName[wsStructureType]);
      Out_XIntAttr(XMLAttrName[atNr], nStructSymbol);
      if nMizarAppearance then
        Out_XAttr(XMLAttrName[atSpelling], StructureName[nStructSymbol]);
      Out_PosAsAttrs(nTypePos); print_arguments(wsStructureType);
      end;
    wsClusteredType: with ClusteredTypePtr(aTyp)↑ do
      begin Out_XElStart(TypeName[wsClusteredType]); Out_PosAsAttrs(nTypePos); Out_XAttrEnd;
      Out_AdjectiveList(nAdjectiveCluster); Out_Type(nType);
      Out_XElEnd(TypeName[wsClusteredType]);
      end;
    wsErrorType: begin Out_XElWithPos(TypeName[wsErrorType], nTypePos);
      end;
  endcases;

```

end;

1022. Printing a variable as an XML element.

```
Variable = element Variable {
  attribute idnr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer }
}

⟨Implementation for wsmarticle.pas 854⟩ +≡
procedure OutWSMizFileObj.Out_Variable(aVar : VariablePtr);
  begin with aVar↑ do
    begin Out_XElStart(XMLElemName[elVariable]); Out_XIntAttr(XMLAttrName[atIdNr], nIdent);
    if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], IdentRepr(nIdent));
    Out_PosAsAttrs(nVarPos); Out_XElEnd0
    end;
  end;
```

1023. Variables introduced using “**reserve**” are just printed out like any other variable.

```
⟨Implementation for wsmarticle.pas 854⟩ +≡
procedure OutWSMizFileObj.Out_ReservedVariable(aVar : VariablePtr);
  begin Out_Variable(aVar);
  end;
```

1024. Implicitly qualified variables (i.e., variables which are **reserved** with a type, then used in, e.g., a quantified formula) are just variables appearing as children of an “implicitly qualified” XML element.

```
VariableSegment |= element Implicitly-Qualified-Segment {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Variable
}

⟨Implementation for wsmarticle.pas 854⟩ +≡
procedure OutWSMizFileObj.Out_ImplicitlyQualifiedVariable(aSegm : ImplicitlyQualifiedSegmentPtr);
  begin Out_XElStart(SegmentKindName[ikImplQualifiedSegm]); Out_PosAsAttrs(aSegm↑.nSegmPos);
  Out_XAttrEnd; Out_Variable(aSegm↑.nIdentifier);
  Out_XElEnd(SegmentKindName[ikImplQualifiedSegm]);
  end;
```

1025. Qualified variable segments are either implicitly qualified (hence we use the previous function) or explicitly qualified (which look like “ $\langle \text{variable list} \rangle$ being $\langle \text{type} \rangle$ ”).

Explicitly qualified segments are an XML element with two children (a “variables” XML element, and a “type” XML element).

```
VariableSegment |= element Explicitly-Qualified-Segment {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  element Variables { Variable* },
  Type
}

⟨Implementation for wsmarticle.pas 854⟩ +≡
procedure OutWSMizFileObj.Out_VariableSegment(aSegm : QualifiedSegmentPtr);
  var i: integer;
  begin case aSegm↑.nSegmentSort of
    ikImplQualifiedSegm: Out_ImplicitlyQualifiedVariable(ImplicitlyQualifiedSegmentPtr(aSegm));
    ikExplQualifiedSegm: with ExplicitlyQualifiedSegmentPtr(aSegm)↑ do
      begin Out_XElStart(SegmentKindName[ikExplQualifiedSegm]); Out_PosAsAttrs(nSegmPos);
        Out_XAttrEnd; Out_XElStart0(XMLElemName[elVariables]);
        for i ← 0 to nIdentifiers↑.Count − 1 do Out_Variable(nIdentifiers↑.Items↑[i]);
        Out_XElEnd(XMLElemName[elVariables]); Out_Type(nType);
        Out_XElEnd(SegmentKindName[ikExplQualifiedSegm]);
      end;
    endcases;
  end;
```

1026. Private predicates have the XML schema

```
Private-Predicate-Formula = element Private-Predicate-Formula {
  attribute idnr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Term-List?
}

⟨Implementation for wsmarticle.pas 854⟩ +≡
procedure OutWSMizFileObj.Out_PrivatePredicativeFormula(aFrm : PrivatePredicativeFormulaPtr);
  begin with PrivatePredicativeFormulaPtr(aFrm)↑ do
    begin Out_XElStart(FormulaName[wsPrivatePredicateFormula]);
      Out_XIntAttr(XMLAttrName[atIdNr], nPredIdNr);
      if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], IdentRepr(nPredIdNr));
      Out_PosAsAttrs(nFormulaPos);
      if nArgs↑.Count = 0 then Out_XElEnd0
      else begin Out_XAttrEnd; Out_TermList(nArgs);
        Out_XElEnd(FormulaName[wsPrivatePredicateFormula]);
      end;
    end;
  end;
```

Subsection 21.11.2. Emitting XML for formulas

1027. The XML schema for formulas looks something like:

```

Formula = NegatedFormula
| ConjunctiveFormula
| DisjunctiveFormula
| ConditionalFormula
| BiconditionalFormula
| FlexaryConjunctiveFormula
| FlexaryDisjunctiveFormula
| Predicative-Formula
| RightSideOf-Predicative-Formula
| Multi-Predicative-Formula
| Attributive-Formula
| Qualifying-Formula
| Universal-Quantifier-Formula
| Existential-Quantifier-Formula
| element Contradiction {
    attribute col { xsd:integer },
    attribute line { xsd:integer } }
| element Thesis {
    attribute col { xsd:integer },
    attribute line { xsd:integer } }
| element Formula-Error {
    attribute col { xsd:integer },
    attribute line { xsd:integer } }

```

(Implementation for `wsmarticle.pas` 854) +≡

```

procedure OutWSMizFileObj.Out_Formula(aFrm : FormulaPtr);
  var i: integer;
  begin case aFrm↑.nFormulaSort of
    wsNegatedFormula: ⟨Emit XML for negated formula (WSM) 1028⟩;
    wsConjunctiveFormula: ⟨Emit XML for conjunction (WSM) 1029⟩;
    wsDisjunctiveFormula: ⟨Emit XML for disjunction (WSM) 1030⟩;
    wsConditionalFormula: ⟨Emit XML for conditional formula (WSM) 1031⟩;
    wsBiconditionalFormula: ⟨Emit XML for biconditional formula (WSM) 1032⟩;
    wsFlexaryConjunctiveFormula: ⟨Emit XML for flexary-conjunction (WSM) 1033⟩;
    wsFlexaryDisjunctiveFormula: ⟨Emit XML for flexary-disjunction (WSM) 1034⟩;
    wsPredicativeFormula: ⟨Emit XML for predicative formula (WSM) 1035⟩;
    wsRightSideOfPredicativeFormula: ⟨Emit XML for right-side of predicative formula (WSM) 1036⟩;
    wsMultiPredicativeFormula: ⟨Emit XML for multi-predicative formula (WSM) 1037⟩;
    wsPrivatePredicateFormula: Out_PrivatePredicativeFormula(PrivatePredicativeFormulaPtr(aFrm));
    wsAttributiveFormula: ⟨Emit XML for attributive formula (WSM) 1038⟩;
    wsQualifyingFormula: ⟨Emit XML for qualifying formula (WSM) 1039⟩;
    wsUniversalFormula: ⟨Emit XML for universal formula (WSM) 1040⟩;
    wsExistentialFormula: ⟨Emit XML for existential formula (WSM) 1041⟩;
    wsContradiction: begin Out_XElWithPos(FormulaName[wsContradiction], aFrm↑.nFormulaPos);
      end;
    wsThesis: begin Out_XElWithPos(FormulaName[wsThesis], aFrm↑.nFormulaPos);
      end;
    wsErrorFormula: begin Out_XElWithPos(FormulaName[wsErrorFormula], aFrm↑.nFormulaPos);
      end;
  endcases;
end;

```

1028.

```

NegatedFormula = element Negated-Formula {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Formula
}

```

$\langle \text{Emit XML for negated formula (WSM) 1028} \rangle \equiv$
begin *Out_XElStart*(*FormulaName*[*wsNegatedFormula*]); *Out_PosAsAttrs*(*aFrm*↑.*nFormulaPos*);
Out_XAttrEnd; *Out_Formula*(*NegativeFormulaPtr*(*aFrm*↑.*nArg*));
Out_XElEnd(*FormulaName*[*wsNegatedFormula*]);
end

This code is used in section 1027.

1029.

```

ConjunctiveFormula = element Conjunctive-Formula {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Formula,
  Formula
}

```

$\langle \text{Emit XML for conjunction (WSM) 1029} \rangle \equiv$
begin *Out_XElStart*(*FormulaName*[*wsConjunctiveFormula*]); *Out_PosAsAttrs*(*aFrm*↑.*nFormulaPos*);
Out_XAttrEnd; *Out_Formula*(*BinaryFormulaPtr*(*aFrm*↑.*nLeftArg*));
Out_Formula(*BinaryFormulaPtr*(*aFrm*↑.*nRightArg*));
Out_XElEnd(*FormulaName*[*wsConjunctiveFormula*]);
end

This code is used in section 1027.

1030.

```

DisjunctiveFormula = element Disjunctive-Formula {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Formula,
  Formula
}

```

$\langle \text{Emit XML for disjunction (WSM) 1030} \rangle \equiv$
begin *Out_XElStart*(*FormulaName*[*wsDisjunctiveFormula*]); *Out_PosAsAttrs*(*aFrm*↑.*nFormulaPos*);
Out_XAttrEnd; *Out_Formula*(*BinaryFormulaPtr*(*aFrm*↑.*nLeftArg*));
Out_Formula(*BinaryFormulaPtr*(*aFrm*↑.*nRightArg*));
Out_XElEnd(*FormulaName*[*wsDisjunctiveFormula*]);
end

This code is used in section 1027.

1031.

```
ConditionalFormula = element Conditional-Formula {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Formula,
  Formula
}
```

⟨Emit XML for conditional formula (WSM) 1031⟩ ≡
begin *Out_XElStart*(*FormulaName*[*wsConditionalFormula*]); *Out_PosAsAttrs*(*aFrm*↑.*nFormulaPos*);
Out_XAttrEnd; *Out_Formula*(*BinaryFormulaPtr*(*aFrm*↑.*nLeftArg*);
Out_Formula(*BinaryFormulaPtr*(*aFrm*↑.*nRightArg*);
Out_XElEnd(*FormulaName*[*wsConditionalFormula*]);
end

This code is used in section 1027.

1032.

```
BiconditionalFormula = element Biconditional-Formula {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Formula,
  Formula
}
```

⟨Emit XML for biconditional formula (WSM) 1032⟩ ≡
begin *Out_XElStart*(*FormulaName*[*wsBiconditionalFormula*]); *Out_PosAsAttrs*(*aFrm*↑.*nFormulaPos*);
Out_XAttrEnd; *Out_Formula*(*BinaryFormulaPtr*(*aFrm*↑.*nLeftArg*);
Out_Formula(*BinaryFormulaPtr*(*aFrm*↑.*nRightArg*);
Out_XElEnd(*FormulaName*[*wsBiconditionalFormula*]);
end

This code is used in section 1027.

1033.

```
FlexaryConjunctiveFormula = element FlexaryConjunctive-Formula {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Formula,
  Formula
}
```

⟨Emit XML for flexary-conjunction (WSM) 1033⟩ ≡
begin *Out_XElStart*(*FormulaName*[*wsFlexaryConjunctiveFormula*]);
Out_PosAsAttrs(*aFrm*↑.*nFormulaPos*); *Out_XAttrEnd*;
Out_Formula(*BinaryFormulaPtr*(*aFrm*↑.*nLeftArg*);
Out_Formula(*BinaryFormulaPtr*(*aFrm*↑.*nRightArg*);
Out_XElEnd(*FormulaName*[*wsFlexaryConjunctiveFormula*]);
end

This code is used in section 1027.

1034.

```

FlexaryDisjunctiveFormula = element FlexaryDisjunctive-Formula {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Formula,
  Formula
}

```

```

⟨ Emit XML for flexary-disjunction (WSM) 1034 ⟩ ≡
  begin Out_XElStart (FormulaName[wsFlexaryDisjunctiveFormula]);
    Out_PosAsAttrs (aFrm↑.nFormulaPos); Out_XAttrEnd;
    Out_Formula (BinaryFormulaPtr (aFrm↑.nLeftArg);
    Out_Formula (BinaryFormulaPtr (aFrm↑.nRightArg);
    Out_XElEnd (FormulaName[wsFlexaryDisjunctiveFormula]);
  end

```

This code is used in section 1027.

1035.

```

Predicative-Formula = element Predicative-Formula {
  attribute nr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  element Arguments { Term-List? },
  element Arguments { Term-List? }
}

```

```

⟨ Emit XML for predicative formula (WSM) 1035 ⟩ ≡
  with PredicativeFormulaPtr (aFrm)↑ do
    begin Out_XElStart (FormulaName[wsPredicativeFormula]);
      Out_XIntAttr (XMLAttrName[atNr], nPredNr);
      if nMizarAppearance then Out_XAttr (XMLAttrName[atSpelling], PredicateName[nPredNr]);
      Out_PosAsAttrs (nFormulaPos); Out_XAttrEnd;
      if nLeftArgs↑.Count = 0 then Out_XEl1 (XMLElemName[elArguments])
      else begin Out_XElStart0 (XMLElemName[elArguments]); Out_TermList (nLeftArgs);
        Out_XElEnd (XMLElemName[elArguments]);
        end;
      if nRightArgs↑.Count = 0 then Out_XEl1 (XMLElemName[elArguments])
      else begin Out_XElStart0 (XMLElemName[elArguments]); Out_TermList (nRightArgs);
        Out_XElEnd (XMLElemName[elArguments]);
        end;
      Out_XElEnd (FormulaName[wsPredicativeFormula]);
    end
  end

```

This code is used in section 1027.

1036.

```

RightSideOf-Predicative-Formula = element RightSideOf-Predicative-Formula {
  attribute nr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  element Arguments { Term-List? }
}

⟨Emit XML for right-side of predicative formula (WSM) 1036⟩ ≡
  with RightSideOfPredicativeFormulaPtr(aFrm)↑ do
    begin Out_XElStart(FormulaName[wsRightSideOfPredicativeFormula]);
      Out_XIntAttr(XMLAttrName[atNr], nPredNr);
      if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], PredicateName[nPredNr]);
        Out_PosAsAttrs(nFormulaPos); Out_XAttrEnd;
      if nRightArgs↑.Count = 0 then Out_XEl1(XMLElemName[elArguments])
      else begin Out_XElStart0(XMLElemName[elArguments]); Out_TermList(nRightArgs);
        Out_XElEnd(XMLElemName[elArguments]);
      end;
      Out_XElEnd(FormulaName[wsRightSideOfPredicativeFormula])
    end
  end

```

This code is used in section 1027.

1037.

```

Multi-Predicative-Formula = element Multi-Predicative-Formula {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Formula*
}

⟨Emit XML for multi-predicative formula (WSM) 1037⟩ ≡
  with MultiPredicativeFormulaPtr(aFrm)↑ do
    begin Out_XElStart(FormulaName[wsMultiPredicativeFormula]);
      Out_PosAsAttrs(aFrm↑.nFormulaPos); Out_XAttrEnd;
      for i ← 0 to nScraps.Count - 1 do Out_Formula(nScraps↑.Items↑[i]);
        Out_XElEnd(FormulaName[wsMultiPredicativeFormula])
      end
    end
  end

```

This code is used in section 1027.

1038.

```

Attributive-Formula = element Attributive-Formula {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Term,
  Adjective-Cluster.element
}

```

```

⟨Emit XML for attributive formula (WSM) 1038⟩ ≡
  with AttributiveFormulaPtr(aFrm)↑ do
    begin Out_XElStart(FormulaName[wsAttributiveFormula]); Out_PosAsAttrs(nFormulaPos);
      Out_XAttrEnd; Out_Term(nSubject); Out_AdjectiveList(nAdjectives);
      Out_XElEnd(FormulaName[wsAttributiveFormula]);
    end

```

This code is used in section 1027.

1039.

```

Qualifying-Formula = element Qualifying-Formula {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Term,
  Type,
  Formula
}

```

```

⟨Emit XML for qualifying formula (WSM) 1039⟩ ≡
  with QualifyingFormulaPtr(aFrm)↑ do
    begin Out_XElStart(FormulaName[wsQualifyingFormula]); Out_PosAsAttrs(nFormulaPos);
      Out_XAttrEnd; Out_Term(nSubject); Out_Type(nType);
      Out_XElEnd(FormulaName[wsQualifyingFormula]);
    end

```

This code is used in section 1027.

1040.

```

Universal-Quantifier-Formula = element Universal-Quantifier-Formula {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Variable-Segment,
  Formula
}

```

```

⟨Emit XML for universal formula (WSM) 1040⟩ ≡
  with QuantifiedFormulaPtr(aFrm)↑ do
    begin Out_XElStart(FormulaName[wsUniversalFormula]); Out_PosAsAttrs(nFormulaPos);
      Out_XAttrEnd; Out_VariableSegment(QuantifiedFormulaPtr(aFrm)↑.nSegment);
      Out_Formula(QuantifiedFormulaPtr(aFrm)↑.nScope);
      Out_XElEnd(FormulaName[wsUniversalFormula]);
    end

```

This code is used in section 1027.

1041.

```

Existential-Quantifier-Formula = element Existential-Quantifier-Formula {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Variable-Segment,
  Formula
}

```

< Emit XML for existential formula (WSM) 1041 > \equiv
 with *QuantifiedFormulaPtr*(*aFrm*) \uparrow do
 begin *Out_XElStart*(*FormulaName*[*wsExistentialFormula*]); *Out_PosAsAttrs*(*nFormulaPos*);
 Out_XAttrEnd; *Out_VariableSegment*(*QuantifiedFormulaPtr*(*aFrm*) \uparrow .*nSegment*);
 Out_Formula(*QuantifiedFormulaPtr*(*aFrm*) \uparrow .*nScope*);
 Out_XElEnd(*FormulaName*[*wsExistentialFormula*]);
 end

This code is used in section 1027.

Subsection 21.11.3. Emitting XML for Terms

1042. We begin with simple terms.

```

Term |= element Simple-Term {
  attribute idnr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer }
}

```

< Implementation for *wsmarticle.pas* 854 > + \equiv
procedure *Out_WSMizFileObj.Out_SimpleTerm*(*aTrm* : *SimpleTermPtr*);
 begin *Out_XElStart*(*TermName*[*wsSimpleTerm*]);
 Out_XIntAttr(*XMLAttrName*[*atIdNr*], *aTrm* \uparrow .*nIdent*);
 if *nMizarAppearance* **then** *Out_XAttr*(*XMLAttrName*[*atSpelling*], *IdentRepr*(*aTrm* \uparrow .*nIdent*));
 Out_PosAsAttrs(*aTrm* \uparrow .*nTermPos*); *Out_XElEnd0*;
 end;

1043. Terms: Private functors.

```

Term |= element Private-Function-Term {
  attribute idnr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  element Arguments { Term-List }?
}

```

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

procedure OutWSMizFileObj.Out_PrivateFunctionTerm(aTrm : PrivateFunctionTermPtr);
begin with PrivateFunctionTermPtr(aTrm)↑ do
  begin Out_XElStart(TermName[wsPrivateFunctionTerm]);
    Out_XIntAttr(XMLAttrName[atIdNr], nFunctionIdent);
    if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], IdentRepr(nFunctionIdent));
    Out_PosAsAttrs(nTermPos);
    if nArgs↑.Count = 0 then Out_XElEnd0
    else begin Out_XAttrEnd; Out_TermList(nArgs); Out_XElEnd(TermName[wsPrivateFunctionTerm]);
      end;
    end;
  end;
end;

```

1044. Terms: internal selectors.

```

Term |= element Internal-Selector-Term {
  attribute nr { text },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer }
}

```

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

procedure OutWSMizFileObj.Out_InternalSelectorTerm(aTrm : InternalSelectorTermPtr);
begin with aTrm↑ do
  begin Out_XElStart(TermName[wsInternalSelectorTerm]);
    Out_XIntAttr(XMLAttrName[atNr], nSelectorSymbol);
    if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], SelectorName[nSelectorSymbol]);
    Out_PosAsAttrs(nTermPos); Out_XElEnd0;
  end;
end;

```

1045. Terms: numerals, anaphoric “it”, error.

```
Term |= element Numeral {
  attribute number { xsd:int },
  attribute col { xsd:integer },
  attribute line { xsd:integer }
}
```

```
Term |= element It-Term {
  attribute col { xsd:integer },
  attribute line { xsd:integer }
}
```

```
Term |= element Error-Term { }
```

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```
procedure OutWSMizFileObj.Out_Term(aTrm : TermPtr);
  var i: integer;
  begin case aTrm↑.nTermSort of
    wsPlaceholderTerm: ⟨Emit XML for placeholder (WSM) 1046⟩;
    wsSimpleTerm: Out_SimpleTerm(SimpleTermPtr(aTrm));
    wsNumeralTerm: begin ; Out_XElStart(TermName[wsNumeralTerm]);
      Out_XIntAttr(XMLAttrName[atNumber], NumeralTermPtr(aTrm)↑.nValue);
      Out_PosAsAttrs(aTrm↑.nTermPos); Out_XElEnd0;
    end;
    wsInfixTerm: ⟨Emit XML for infix term (WSM) 1047⟩;
    wsCircumfixTerm: ⟨Emit XML for circumfix term (WSM) 1048⟩;
    wsPrivateFunctorTerm: Out_PrivateFunctorTerm(PrivateFunctorTermPtr(aTrm));
    wsAggregateTerm: ⟨Emit XML for aggregate term (WSM) 1049⟩;
    wsSelectorTerm: ⟨Emit XML for selector term (WSM) 1050⟩;
    wsInternalSelectorTerm: Out_InternalSelectorTerm(InternalSelectorTermPtr(aTrm));
    wsForgetfulFunctorTerm: ⟨Emit XML for forgetful functor (WSM) 1051⟩;
    wsInternalForgetfulFunctorTerm: ⟨Emit XML for internal forgetful functor (WSM) 1052⟩;
    wsFraenkelTerm: ⟨Emit XML for Fraenkel term (WSM) 1053⟩;
    wsSimpleFraenkelTerm: ⟨Emit XML for simple Fraenkel term (WSM) 1054⟩;
    wsQualificationTerm: ⟨Emit XML for qualification term (WSM) 1055⟩;
    wsExactlyTerm: ⟨Emit XML for exactly qualification term (WSM) 1056⟩;
    wsGlobalChoiceTerm: ⟨Emit XML for global choice term (WSM) 1057⟩;
    wsItTerm: Out_XElWithPos(TermName[wsItTerm], aTrm↑.nTermPos);
    wsErrorTerm: Out_XEl1(TermName[wsErrorTerm]);
  endcases;
end;
```

1046. Terms: placeholders.

```

Term |= element Placeholder-Term {
  attribute nr { text },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer }
}

⟨Emit XML for placeholder (WSM) 1046⟩ ≡
  begin Out_XElStart( TermName[wsPlaceholderTerm]);
    Out_XIntAttr( XMLAttrName[atNr], PlaceholderTermPtr(aTrm)↑.nLocusNr);
    if nMizarAppearance then Out_XAttr( XMLAttrName[atSpelling],
      QuoteStrForXML(PlaceHolderName[PlaceholderTermPtr(aTrm)↑.nLocusNr]));
    Out_PosAsAttrs(aTrm↑.nTermPos); Out_XElEnd0;
  end

```

This code is used in section 1045.

1047. Terms: infix.

```

Term |= element Infix-Term {
  attribute nr { text },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  element Arguments { Term-List? },
  element Arguments { Term-List? }
}

⟨Emit XML for infix term (WSM) 1047⟩ ≡
  with InfixTermPtr(aTrm)↑ do
    begin Out_XElStart( TermName[wsInfixTerm]);
      Out_XIntAttr( XMLAttrName[atNr], nFunctorSymbol);
      if nMizarAppearance then Out_XAttr( XMLAttrName[atSpelling], FunctorName[nFunctorSymbol]);
      Out_PosAsAttrs(nTermPos); Out_XAttrEnd;
      if nLeftArgs↑.Count = 0 then Out_XEl1( XMLElemName[elArguments])
      else begin Out_XElStart0( XMLElemName[elArguments]); Out_TermList(nLeftArgs);
        Out_XElEnd( XMLElemName[elArguments]);
        end;
      if nRightArgs↑.Count = 0 then Out_XEl1( XMLElemName[elArguments])
      else begin Out_XElStart0( XMLElemName[elArguments]); Out_TermList(nRightArgs);
        Out_XElEnd( XMLElemName[elArguments]);
        end;
      Out_XElEnd( TermName[wsInfixTerm]);
    end
  end

```

This code is used in section 1045.

1048. Terms: brackets.

```

Term |= element Circumfix-Term {
  attribute nr { text },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  element Right-Circumflex-Symbol {
    attribute nr { text },
    attribute spelling { text }?,
    attribute col { xsd:integer },
    attribute line { xsd:integer }
  },
  element Arguments { Term-List? }
}

```

⟨Emit XML for circumfix term (WSM) 1048⟩ ≡

```

with CircumfixTermPtr(aTrm)↑ do
  begin Out_XElStart(TermName[wsCircumfixTerm]);
    Out_XIntAttr(XMLAttrName[atNr], nLeftBracketSymbol);
    if nMizarAppearance then
      Out_XAttr(XMLAttrName[atSpelling], LeftBracketName[nLeftBracketSymbol]);
      Out_PosAsAttrs(nTermPos); Out_XAttrEnd;
      Out_XElStart(XMLElemName[elRightCircumflexSymbol]);
      Out_XIntAttr(XMLAttrName[atNr], nRightBracketSymbol);
      if nMizarAppearance then
        Out_XAttr(XMLAttrName[atSpelling], RightBracketName[nRightBracketSymbol]);
        Out_PosAsAttrs(nTermPos); Out_XElEnd0; Out_TermList(nArgs);
        Out_XElEnd(TermName[wsCircumfixTerm]);
      end
    end
  end

```

This code is used in section 1045.

1049. Terms: structure instances.

```

Term |= element Aggregate-Term {
  attribute nr { text },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  element Arguments { Term-List }?
}

```

⟨Emit XML for aggregate term (WSM) 1049⟩ ≡

```

with AggregateTermPtr(aTrm)↑ do
  begin Out_XElStart(TermName[wsAggregateTerm]);
    Out_XIntAttr(XMLAttrName[atNr], nStructSymbol);
    if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], StructureName[nStructSymbol]);
    Out_PosAsAttrs(nTermPos);
    if nArgs↑.Count = 0 then Out_XElEnd0
    else begin Out_XAttrEnd; Out_TermList(nArgs); Out_XElEnd(TermName[wsAggregateTerm]);
      end;
    end
  end

```

This code is used in section 1045.

1050. Terms: selectors.


```

Term |= element Selector-Term {
  attribute nr { text },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Term
}

```

⟨Emit XML for selector term (WSM) 1050⟩ ≡

```

with SelectorTermPtr(aTrm)↑ do
  begin Out_XElStart( TermName[wsSelectorTerm]);
    Out_XIntAttr(XMLAttrName[atNr], nSelectorSymbol);
    if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], SelectorName[nSelectorSymbol]);
      Out_PosAsAttrs(nTermPos); Out_XAttrEnd; Out_Term(nArg);
    Out_XElEnd( TermName[wsSelectorTerm]);
  end

```

This code is used in section 1045.

1051. Terms: forgetful functors.

```

Term |= element Forgetful-Function-Term {
  attribute nr { text },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Term
}

```

⟨Emit XML for forgetful functor (WSM) 1051⟩ ≡

```

with ForgetfulFunctionTermPtr(aTrm)↑ do
  begin Out_XElStart( TermName[wsForgetfulFunctionTerm]);
    Out_XIntAttr(XMLAttrName[atNr], nStructSymbol);
    if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], StructureName[nStructSymbol]);
      Out_PosAsAttrs(nTermPos); Out_XAttrEnd; Out_Term(nArg);
    Out_XElEnd( TermName[wsForgetfulFunctionTerm]);
  end

```

This code is used in section 1045.

1052. Terms: internal forgetful functors.

```

Term |= element Internal-Forgetful-Function-Term {
  attribute nr { text },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
}

```

⟨Emit XML for internal forgetful functor (WSM) 1052⟩ ≡

```

with InternalForgetfulFunctionTermPtr(aTrm)↑ do
  begin Out_XElStart( TermName[wsInternalForgetfulFunctionTerm]);
    Out_XIntAttr(XMLAttrName[atNr], nStructSymbol); Out_PosAsAttrs(nTermPos); Out_XElEnd0;
  end

```

This code is used in section 1045.

1053. Terms: Fraenkel operators.

```

Term |= element Fraenkel-Term {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Variable-Segment*,
  Term,
  Formula
}

```

⟨Emit XML for Fraenkel term (WSM) 1053⟩ ≡

```

with FraenkelTermPtr(aTrm)↑ do
  begin Out_XElStart(TermName[wsFraenkelTerm]); Out_PosAsAttrs(nTermPos); Out_XAttrEnd;
  for i ← 0 to nPostqualification↑.Count - 1 do Out_VariableSegment(nPostqualification↑.Items↑[i]);
  Out_Term(nSample); Out_Formula(nFormula); Out_XElEnd(TermName[wsFraenkelTerm]);
  end

```

This code is used in section 1045.

1054. Terms: Simple Fraenkel expressions.

```

Term |= element Simple-Fraenkel-Term {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Variable-Segment*,
  Term
}

```

⟨Emit XML for simple Fraenkel term (WSM) 1054⟩ ≡

```

with SimpleFraenkelTermPtr(aTrm)↑ do
  begin Out_XElStart(TermName[wsSimpleFraenkelTerm]); Out_PosAsAttrs(nTermPos);
  Out_XAttrEnd;
  for i ← 0 to nPostqualification↑.Count - 1 do Out_VariableSegment(nPostqualification↑.Items↑[i]);
  Out_Term(nSample); Out_XElEnd(TermName[wsSimpleFraenkelTerm]);
  end

```

This code is used in section 1045.

1055. Terms: qualification.

```

Term |= element Qualification-Term {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Term,
  Type
}

```

⟨Emit XML for qualification term (WSM) 1055⟩ ≡

```

with QualifiedTermPtr(aTrm)↑ do
  begin Out_XElStart(TermName[wsQualificationTerm]); Out_PosAsAttrs(nTermPos); Out_XAttrEnd;
  Out_Term(nSubject); Out_Type(nQualification); Out_XElEnd(TermName[wsQualificationTerm]);
  end

```

This code is used in section 1045.

1056. Terms: exactly qualified.

```
Term |= element Exactly-Qualification-Term {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Term
}
```

⟨Emit XML for exactly qualification term (WSM) 1056⟩ ≡

```
with ExactlyTermPtr(aTrm)↑ do
  begin Out_XElStart(TermName[wsQualificationTerm]); Out_PosAsAttrs(nTermPos);
    Out_XAttrEnd; Out_Term(nSubject); Out_XElEnd(TermName[wsQualificationTerm]);
  end
```

This code is used in section 1045.

1057. Terms: global choice expressions.

```
Term |= element Global-Choice-Term {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Type
}
```

⟨Emit XML for global choice term (WSM) 1057⟩ ≡

```
begin Out_XElStart(TermName[wsGlobalChoiceTerm]); Out_PosAsAttrs(aTrm↑.nTermPos);
  Out_XAttrEnd; Out_Type(ChoiceTermPtr(aTrm)↑.nChoiceType);
  Out_XElEnd(TermName[wsGlobalChoiceTerm]);
end
```

This code is used in section 1045.

Subsection 21.11.4. Emitting XML for text items

1058. Type-lists are needed for text items.

```
Type-List = element Type-List {
  Type*
}
```

⟨Implementation for wsmarticle.pas 854⟩ +≡

```
procedure OutWSMizFileObj.Out_TypeList(aTypeList : PList);
  var i: integer;
  begin Out_XElStart0(XMLElemName[elTypeList]);
    for i ← 0 to aTypeList↑.Count - 1 do Out_Type(aTypeList↑.Items↑[i]);
      Out_XElEnd(XMLElemName[elTypeList]);
    end;
```

1059. Locus.

```

Locus = element Locus {
  attribute idnr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer }
}

⟨Implementation for wsmarticle.pas 854⟩ +≡
procedure OutWSMizFileObj.Out_Locus(aLocus : LocusPtr);
  begin with aLocus↑ do
    begin Out_XElStart(XMLElemName[elLocus]); Out_XIntAttr(XMLAttrName[atIdNr], nVarId);
    if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], IdentRepr(nVarId));
    Out_PosAsAttrs(nVarIdPos); Out_XElEnd0
    end;
  end;

```

1060.

```

Loci = element Loci { Locus* }

⟨Implementation for wsmarticle.pas 854⟩ +≡
procedure OutWSMizFileObj.Out_Loci(aLoci : PList);
  var i: integer;
  begin if (aLoci = nil) ∨ (aLoci↑.Count = 0) then Out_XEl1(XMLElemName[elLoci])
  else begin Out_XElStart0(XMLElemName[elLoci]);
    for i ← 0 to aLoci↑.Count − 1 do Out_Locus(aLoci↑.Items↑[i]);
    Out_XElEnd(XMLElemName[elLoci]);
  end;
  end;

```

1061. Patterns.

```

⟨Implementation for wsmarticle.pas 854⟩ +≡
procedure OutWSMizFileObj.Out_Pattern(aPattern : PatternPtr);
  begin case aPattern↑.nPatternSort of
    itDefPred: ⟨Emit XML for predicate pattern (WSM) 1062⟩;
    itDefFunc: begin case FunctorPatternPtr(aPattern)↑.nFunctKind of
      InfixFunctor: ⟨Emit XML for infix functor pattern (WSM) 1063⟩;
      CircumfixFunctor: ⟨Emit XML for bracket functor pattern (WSM) 1064⟩;
    endcases;
  end;
  itDefMode: ⟨Emit XML for mode pattern (WSM) 1065⟩;
  end;
  itDefAttr: ⟨Emit XML for attribute pattern (WSM) 1066⟩;
  endcases;
  end ;

```

1062.

```

Predicate-Pattern = element Predicate-Pattern {
  attribute nr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Loci,
  Loci
}

⟨Emit XML for predicate pattern (WSM) 1062⟩ ≡
  with PredicatePatternPtr(aPattern)↑ do
    begin Out_XElStart(DefPatternName[itDefPred]);
      Out_XIntAttr(XMLAttrName[atNr], nPredSymbol);
      if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], PredicateName[nPredSymbol]);
        Out_PosAsAttrs(nPatternPos); Out_XAttrEnd; Out_Loci(nLeftArgs); Out_Loci(nRightArgs);
        Out_XElEnd(DefPatternName[itDefPred]);
      end
  end

```

This code is used in section 1061.

1063.

```

Operation-Functor-Pattern = element Operation-Functor-Pattern {
  attribute nr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Loci,
  Loci
}

⟨Emit XML for infix functor pattern (WSM) 1063⟩ ≡
  with InfixFunctorPatternPtr(aPattern)↑ do
    begin Out_XElStart(FunctorPatternName[InfixFunctor]);
      Out_XIntAttr(XMLAttrName[atNr], nOperSymb);
      if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], FunctorName[nOperSymb]);
        Out_PosAsAttrs(nPatternPos); Out_XAttrEnd; Out_Loci(nLeftArgs); Out_Loci(nRightArgs);
        Out_XElEnd(FunctorPatternName[InfixFunctor]);
      end
  end

```

This code is used in section 1061.

1064.

```

Bracket-Function-Pattern = element Bracket-Function-Pattern {
  attribute nr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  element RightCircumflexSymbol {
    attribute nr { xsd:integer },
    attribute spelling { text }?
  },
  Loci
}

```

⟨Emit XML for bracket functor pattern (WSM) 1064⟩ ≡

```

with CircumfixFunctionPatternPtr(aPattern)↑ do
  begin Out_XElStart(FunctionPatternName[CircumfixFunction]);
  Out_XIntAttr(XMLAttrName[atNr], nLeftBracketSymb);
  if nMizarAppearance then
    Out_XAttr(XMLAttrName[atSpelling], LeftBracketName[nLeftBracketSymb]);
    Out_PosAsAttrs(nPatternPos); Out_XAttrEnd;
    Out_XElStart(XMLElemName[elRightCircumflexSymbol]);
    Out_XIntAttr(XMLAttrName[atNr], nRightBracketSymb);
    if nMizarAppearance then
      Out_XAttr(XMLAttrName[atSpelling], RightBracketName[nRightBracketSymb]);
      Out_XAttrEnd; Out_XElEnd(XMLElemName[elRightCircumflexSymbol]); Out_Loci(nArgs);
      Out_XElEnd(FunctionPatternName[CircumfixFunction]);
    end
  end

```

This code is used in section 1061.

1065.

```

Mode-Pattern = element Mode-Pattern {
  attribute nr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Loci
}

```

⟨Emit XML for mode pattern (WSM) 1065⟩ ≡

```

with ModePatternPtr(aPattern)↑ do
  begin Out_XElStart(DefPatternName[itDefMode]);
  Out_XIntAttr(XMLAttrName[atNr], nModeSymbol);
  if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], ModeName[nModeSymbol]);
  Out_PosAsAttrs(nPatternPos); Out_XAttrEnd; Out_Loci(nArgs);
  Out_XElEnd(DefPatternName[itDefMode])

```

This code is used in section 1061.

1066. I am confused why there is both a locus and loci elements in an attribute pattern.

```
Attribute-Pattern = element Attribute-Pattern {
  attribute nr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Locus,
  Loci
}
```

⟨ Emit XML for attribute pattern (WSM) 1066 ⟩ ≡

```
with AttributePatternPtr(aPattern)↑ do
  begin Out_XElStart(DefPatternName[itDefAttr]); Out_XIntAttr(XMLAttrName[atNr], nAttrSymbol);
  if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], AttributeName[nAttrSymbol]);
  Out_PosAsAttrs(nPatternPos); Out_XAttrEnd; Out_Locus(nArg); Out_Loci(nArgs);
  Out_XElEnd(DefPatternName[itDefAttr]);
end
```

This code is used in section 1061.

1067.

```
Label = element Label {
  attribute idnr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Locus,
  Loci
}
```

⟨ Implementation for wsmarticle.pas 854 ⟩ +≡

```
procedure OutWSMizFileObj.Out_Label(aLab : LabelPtr);
begin
  if (aLab ≠ nil) { ∧(aLab.nLabelIdNr > 0) }
  then
    begin Out_XElStart(XMLElemName[elLabel]);
    Out_XIntAttr(XMLAttrName[atIdNr], aLab↑.nLabelIdNr);
    if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], IdentRepr(aLab↑.nLabelIdNr));
    Out_PosAsAttrs(aLab↑.nLabelPos); Out_XElEnd0
    end;
  end ;
```

1068. Emitting XML for definiens.

```

Definiens = element Definiens {
  attribute kind { "Simple-Definiens" },
  attribute shape { text }?,
  Label,
  (Term | Formula)
} | element Definiens {
  attribute kind { "Conditional-Definiens" },
  attribute shape { text }?,
  Label,
  element Partial-Definiens { (Term | Formula)* },
  (Term | Formula)?
}

⟨Implementation for wsmarticle.pas 854⟩ +≡
procedure OutWSMizFileObj.Out_Definiens(aDef : DefiniensPtr);
var i: integer; lExprKind: ExprKind;
begin if aDef ≠ nil then
  with DefiniensPtr(aDef)↑ do
    begin Out_XElStart(XMLElemName[elDefiniens]); Out_PosAsAttrs(nDefPos);
    case nDefSort of
      SimpleDefiniens: with SimpleDefiniensPtr(aDef)↑, nExpression↑ do
        begin Out_XAttr(XMLAttrName[atKind], DefiniensKindName[SimpleDefiniens]);
          Out_XAttr(XMLAttrName[atShape], ExpName[nExprKind]); Out_XAttrEnd;
          Out_Label(nDefLabel);
        case nExprKind of
          exTerm: Out_Term(TermPtr(nExpr));
          exFormula: Out_Formula(FormulaPtr(nExpr));
        endcases;
      end;
      ConditionalDefiniens: with ConditionalDefiniensPtr(aDef)↑ do
        begin Out_XAttr(XMLAttrName[atKind], DefiniensKindName[ConditionalDefiniens]);
          lExprKind ← exFormula;
          if nOtherwise ≠ nil then lExprKind ← nOtherwise↑.nExprKind
          else if nConditionalDefiniensList↑.Count > 0 then lExprKind ←
            PartDefPtr(nConditionalDefiniensList↑.Items↑[0])↑.nPartDefiniens↑.nExprKind;
          Out_XAttr(XMLAttrName[atShape], ExpName[lExprKind]); Out_XAttrEnd;
          Out_Label(nDefLabel);
          for i ← 0 to nConditionalDefiniensList↑.Count - 1 do
            with PartDefPtr(nConditionalDefiniensList↑.Items↑[i])↑ do
              begin Out_XElStart0(XMLElemName[elPartialDefiniens]);
                with nPartDefiniens↑ do
                  case nExprKind of
                    exTerm: Out_Term(TermPtr(nExpr));
                    exFormula: Out_Formula(FormulaPtr(nExpr));
                  endcases;
                Out_Formula(nGuard); Out_XElEnd(XMLElemName[elPartialDefiniens]);
              end;
            if nOtherwise ≠ nil then
              with nOtherwise↑ do
                case nExprKind of
                  exTerm: Out_Term(TermPtr(nExpr));
                  exFormula: Out_Formula(FormulaPtr(nExpr));

```



```

        endcases;
    end;
    endcases; Out_XElEnd(XMLElemName[elDefiniens]);
    end;
end;

```

1069.

```

Proposition = element Proposition {
    Label,
    Formula
}
<Implementation for wsmarticle.pas 854> +≡
procedure Out_WSMizFileObj.Out_Proposition(aProp : PropositionPtr);
    begin Out_XElStart(XMLElemName[elProposition]); Out_XAttrEnd; Out_Label(aProp↑.nLab);
        Out_Formula(aProp↑.nSentence); Out_XElEnd(XMLElemName[elProposition]);
    end;

```

1070.

```

Local-Reference = element Local-Reference {
    attribute col { xsd:integer },
    attribute line { xsd:integer },
    attribute idnr { xsd:integer },
    attribute spelling { text }?
}
<Implementation for wsmarticle.pas 854> +≡
procedure Out_WSMizFileObj.Out_LocalReference(aRef : LocalReferencePtr);
    begin with LocalReferencePtr(aRef)↑ do
        begin Out_XElStart(ReferenceKindName[LocalReference]); Out_PosAsAttrs(nRefPos);
            Out_XIntAttr(XMLAttrName[atIdNr], nLabId);
            if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], IdentRepr(nLabId));
                Out_XElEnd0;
            end;
        end;
    end;

```

1071.

```

References = (Local-Reference
| element Theorem-Reference {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  attribute at { xsd:integer },
  attribute spelling { text }?,
  attribute nr { xsd:integer }
} | element Definition-Reference {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  attribute at { xsd:integer },
  attribute spelling { text }?,
  attribute nr { xsd:integer }
})*

⟨Implementation for wsmarticle.pas 854⟩ +≡
procedure OutWSMizFileObj.Out_References(aRefs : PList);
  var i: integer;
  begin for i ← 0 to aRefs↑.Count − 1 do
    with ReferencePtr(aRefs↑.Items↑[i])↑ do
      case nRefSort of
        LocalReference: Out_LocalReference(aRefs↑.Items↑[i]);
        TheoremReference: begin Out_XElStart(ReferenceKindName[TheoremReference]);
          Out_PosAsAttrs(nRefPos);
          Out_XIntAttr(XMLAttrName[atNr], TheoremReferencePtr(aRefs↑.Items↑[i])↑.nArticleNr);
          if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling],
            MMLIdentifierName[TheoremReferencePtr(aRefs↑.Items↑[i])↑.nArticleNr]);
          Out_XIntAttr(XMLAttrName[atNumber], TheoremReferencePtr(aRefs↑.Items↑[i])↑.nTheoNr);
          Out_XElEnd0;
          end;
        DefinitionReference: begin Out_XElStart(ReferenceKindName[DefinitionReference]);
          Out_PosAsAttrs(nRefPos);
          Out_XIntAttr(XMLAttrName[atNr], DefinitionReferencePtr(aRefs↑.Items↑[i])↑.nArticleNr);
          if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling],
            MMLIdentifierName[TheoremReferencePtr(aRefs↑.Items↑[i])↑.nArticleNr]);
          Out_XIntAttr(XMLAttrName[atNumber], DefinitionReferencePtr(aRefs↑.Items↑[i])↑.nDefNr);
          Out_XElEnd0;
          end;
        endcases;
      end;
    end;
  end;

```

1072.

```

Link = element Link {
  attribute col { xsd:integer },
  attribute line { xsd:integer }
}

⟨Implementation for wsmarticle.pas 854⟩ +≡
procedure OutWSMizFileObj.Out_Link(aInf : JustificationPtr);
  begin with StraightforwardJustificationPtr(aInf)↑ do
    if nLinked then
      begin Out_XElStart(XMLElemName[elLink]); Out_PosAsAttrs(nLinkPos); Out_XElEnd0;
      end;
    end;

```

1073.

```

Scheme-Justification = element Scheme-Justification {
  attribute nr { xsd:integer },
  attribute idnr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  attribute poscol { xsd:integer },
  attribute posline { xsd:integer },
  References
}

⟨Implementation for wsmarticle.pas 854⟩ +≡
procedure OutWSMizFileObj.Out_SchemeJustification(aInf : SchemeJustificationPtr);
  begin with aInf↑ do
    begin Out_XElStart(InferenceName[infSchemeJustification]);
    Out_XIntAttr(XMLAttrName[atNr], nSchFileNr);
    Out_XIntAttr(XMLAttrName[atIdNr], nSchemeIdNr);
    if nMizarAppearance then
      if nSchFileNr > 0 then Out_XAttr(XMLAttrName[atSpelling], MMLIdentifierName[nSchFileNr])
      else if nSchemeIdNr > 0 then Out_XAttr(XMLAttrName[atSpelling], IdentRepr(nSchemeIdNr));
    Out_PosAsAttrs(nInfPos); Out_XIntAttr(XMLAttrName[atPosLine], nSchemeInfPos.Line);
    Out_XIntAttr(XMLAttrName[atPosCol], nSchemeInfPos.Col); Out_XAttrEnd;
    Out_References(nReferences); Out_XElEnd(InferenceName[infSchemeJustification]);
    end;
  end;

```

1074.

```

Justification =
( element Straightforward-Justification {
    attribute col { xsd:integer },
    attribute line { xsd:integer },
    (Link, References)?
  }
| Scheme-Justification
| element Inference-Error {
    attribute col { xsd:integer },
    attribute line { xsd:integer }
  }
| element Skipped-Proof {
    attribute col { xsd:integer },
    attribute line { xsd:integer }
  }
| Block # proof block
)

<Implementation for wsmarticle.pas 854> +≡
procedure OutWSMizFileObj.Out_Justification(aInf : JustificationPtr; aBlock : wsBlockPtr);
begin case aInf↑.nInfSort of
  infStraightforwardJustification: with StraightforwardJustificationPtr(aInf)↑ do
    begin Out_XElStart(InferenceName[infStraightforwardJustification]); Out_PosAsAttrs(nInfPos);
    if ¬nLinked ∧ (nReferences↑.Count = 0) then Out_XElEnd0
    else begin Out_XAttrEnd; Out_Link(aInf); Out_References(nReferences);
      Out_XElEnd(InferenceName[infStraightforwardJustification]);
    end;
    end;
  infSchemeJustification: Out_SchemeJustification(SchemeJustificationPtr(aInf));
  infError: Out_XElWithPos(InferenceName[infError], aInf↑.nInfPos);
  infSkippedProof: Out_XElWithPos(InferenceName[infSkippedProof], aInf↑.nInfPos);
  infProof: Out_Block(aBlock);
endcases;
end;

```

1075.

```

Compact-Statement = (Proposition, Justification)

<Implementation for wsmarticle.pas 854> +≡
procedure OutWSMizFileObj.Out_CompactStatement(aCStm : CompactStatementPtr;
  aBlock : wsBlockPtr);
begin with aCStm↑ do
  begin Out_Proposition(nProp); Out_Justification(nJustification, aBlock);
  end;
end;

```

1076.

```

Regular-Statement =
( (Label, Block)
| Compact-Statement
| (Compact-Statement,
  element Iterative-Step {
    attribute col { xsd:integer },
    attribute line { xsd:integer },
    Term,
    Justification
  })*
)

<Implementation for wsmarticle.pas 854> +≡
procedure OutWSMizFileObj.Out_RegularStatement(aRStm : RegularStatementPtr; aBlock : wsBlockPtr);
var i : integer;
begin case aRStm↑.nStatementSort of
  stDiffuseStatement: begin Out_Label(DiffuseStatementPtr(aRStm↑.nLab); Out_Block(aBlock);
    end;
  stCompactStatement: Out_CompactStatement(CompactStatementPtr(aRStm), aBlock);
  stIterativeEquality: begin Out_CompactStatement(CompactStatementPtr(aRStm), nil);
    with IterativeEqualityPtr(aRStm)↑ do
      for i ← 0 to nIterSteps↑.Count − 1 do
        with IterativeStepPtr(nIterSteps↑.Items↑[i])↑ do
          begin Out_XElStart(XMLElemName[elIterativeStep]); Out_PosAsAttrs(nIterPos);
            Out_XAttrEnd; Out_Term(nTerm); Out_Justification(nJustification, nil);
            Out_XElEnd(XMLElemName[elIterativeStep]);
          end;
        end;
      endcases;
    end;
  end;

```

1077.

```

Variables = element Variables {
  Variable*
}

<Implementation for wsmarticle.pas 854> +≡
procedure OutWSMizFileObj.Out_ReservationSegment(aRes : ReservationSegmentPtr);
var i : integer;
begin with aRes↑ do
  begin Out_XElStart0(XMLElemName[elVariables]);
    for i ← 0 to nIdentifiers↑.Count − 1 do Out_ReservedVariable(nIdentifiers↑.Items↑[i]);
    Out_XElEnd(XMLElemName[elVariables]); Out_Type(nResType);
  end;
end;

```

1078. <Implementation for wsmarticle.pas 854> +≡

```

procedure OutWSMizFileObj.Out_SchemeNameInSchemeHead(aSch : SchemePtr);
begin Out_XIntAttr(XMLAttrName[atIdNr], aSch↑.nSchemeIdNr);
if nMizarAppearance then Out_XAttr(XMLAttrName[atSpelling], IdentRepr(aSch↑.nSchemeIdNr));
end;

```

1079. \langle Implementation for `wsmarticle.pas` 854 $\rangle + \equiv$

```

procedure OutWSMizFileObj.Out_ItemContentsAttr(aWSItem : WSItemPtr);
begin with aWSItem↑ do
  begin CurPos ← nItemPos;
  if nDisplayInformationOnScreen then DisplayLine(CurPos.Line, ErrorNbr);
  case nItemKind of
    itDefinition, itSchemeBlock, itSchemeHead, itTheorem, itAxiom, itReservation: ;
    itSection: ;
    itConclusion, itRegularStatement: case RegularStatementPtr(nContent)↑.nStatementSort of
      stDiffuseStatement:
        Out_XAttr(XMLAttrName[atShape], RegularStatementName[stDiffuseStatement]);
      stCompactStatement:
        Out_XAttr(XMLAttrName[atShape], RegularStatementName[stCompactStatement]);
      stIterativeEquality: Out_XAttr(XMLAttrName[atShape], RegularStatementName[stIterativeEquality]);
    endcases;
    itChoice, itReconsider, itPrivFuncDefinition, itPrivPredDefinition, itConstantDefinition, itGeneralization,
      itLocDeclaration, itExistentialAssumption, itExemplification, itPerCases, itCaseBlock: ;
    itCaseHead, itSupposeHead, itAssumption: ;
    itCorrCond: Out_XAttr(XMLAttrName[atCondition],
      CorrectnessName[CorrectnessConditionPtr(nContent)↑.nCorrCondSort]);
    itCorrectness: Out_XAttr(XMLAttrName[atCondition], CorrectnessName[syCorrectness]);
    itProperty:
      Out_XAttr(XMLAttrName[atProperty], PropertyName[PropertyPtr(nContent)↑.nPropertySort]);
    itDefFunc: Out_XAttr(XMLAttrName[atShape],
      DefiningWayName[FunctorDefinitionPtr(nContent)↑.nDefiningWay]);
    itDefPred, itDefMode, itDefAttr, itDefStruct, itPredSynonym, itPredAntonym, itFuncNotation,
      itModeNotation, itAttrSynonym, itAttrAntonym, itCluster, itIdentify, itReduction: ;
    itPropertyRegistration:
      Out_XAttr(XMLAttrName[atProperty], PropertyName[PropertyPtr(nContent)↑.nPropertySort]);
    itPragma:
      Out_XAttr(XMLAttrName[atSpelling], QuoteStrForXML(PragmaPtr(nContent)↑.nPragmaStr));
  endcases;
end;
end;

```

1080. Emitting XML for item contents. This is used to expedite emitting the XML for a text-item (§1095).

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

procedure OutWSMizFileObj.Out_ItemContents(aWSItem : WSItemPtr);
  var i, j: integer; s: CorrectnessKind;
  begin with aWSItem↑ do
    begin case nItemKind of
      itDefinition: Out_Block(nBlock);
      itSchemeBlock: Out_Block(nBlock);
      itSchemeHead: ⟨Emit XML for schema (WSM) 1081⟩;
      itTheorem: Out_CompactStatement(CompactStatementPtr(nContent), nBlock);
      itAxiom: begin end;
      itReservation: Out_ReservationSegment(ReservationSegmentPtr(nContent));
      itSection: ;
      itConclusion, itRegularStatement: Out_RegularStatement(RegularStatementPtr(nContent), nBlock);
      itChoice: ⟨Emit XML for consider contents (WSM) 1082⟩;
      itReconsider: ⟨Emit XML for reconsider contents (WSM) 1083⟩;
      ⟨Emit XML for definition-related items (WSM) 1084⟩;
      itPredSynonym, itPredAntonym, itFuncNotation, itModeNotation, itAttrSynonym, itAttrAntonym:
        with NotationDeclarationPtr(nContent)↑ do
          begin Out_Pattern(nOriginPattern); Out_Pattern(nNewPattern);
          end;
      ⟨Emit XML for registration-related items (WSM) 1093⟩;
      itPragma: ;
      itIncorrItem: ;
    end;
  endcases;
end;

```

1081.

```

Item-contents |= Scheme-contents
Scheme-contents = element Scheme {
  attribute idnr { xsd:integer },
  attribute spelling { text }?,
  element Schematic-Variables {
    (element Predicate-Segment {
      attribute col { xsd:integer },
      attribute line { xsd:integer },
      element Variables { Variable* },
      Type
    } | element Functor-Segment {
      attribute col { xsd:integer },
      attribute line { xsd:integer },
      element Variables { Variable* },
      Type-List,
      element Type-Specification { Type }
    })*
  },
  Formula,
  element Provisional-Formulas { Proposition* }?
}
⟨Emit XML for schema (WSM) 1081⟩ ≡
  with SchemePtr(nContent)↑ do
    begin Out_XElStart(XMLElemName[elScheme]);
      Out_SchemeNameInSchemeHead(SchemePtr(nContent)); Out_XElEnd0;
      Out_XElStart0(XMLElemName[elSchematicVariables]);
      for j ← 0 to nSchemeParams↑.Count - 1 do
        case SchemeSegmentPtr(nSchemeParams.Items↑[j])↑.nSegmSort of
          PredicateSegment: with PredicateSegmentPtr(nSchemeParams.Items↑[j])↑ do
            begin Out_XElStart(SchemeSegmentName[PredicateSegment]); Out_PosAsAttrs(nSegmPos);
              Out_XAttrEnd; Out_XElStart0(XMLElemName[elVariables]);
              for i ← 0 to nVars↑.Count - 1 do Out_Variable(nVars.Items↑[i]);
                Out_XElEnd(XMLElemName[elVariables]); Out_TypeList(nTypeExpList);
                Out_XElEnd(SchemeSegmentName[PredicateSegment]);
              end;
            FunctorSegment: with FunctorSegmentPtr(nSchemeParams.Items↑[j])↑ do
              begin Out_XElStart(SchemeSegmentName[FunctorSegment]); Out_PosAsAttrs(nSegmPos);
                Out_XAttrEnd; Out_XElStart0(XMLElemName[elVariables]);
                for i ← 0 to nVars↑.Count - 1 do Out_Variable(nVars.Items↑[i]);
                  Out_XElEnd(XMLElemName[elVariables]); Out_TypeList(nTypeExpList);
                  Out_XElStart0(XMLElemName[elTypeSpecification]); Out_Type(nSpecification);
                  Out_XElEnd(XMLElemName[elTypeSpecification]);
                  Out_XElEnd(SchemeSegmentName[FunctorSegment]);
                end;
            endcases;
          Out_XElEnd(XMLElemName[elSchematicVariables]); Out_Formula(nSchemeConclusion);
        if (nSchemePremises ≠ nil) ∧ (nSchemePremises↑.Count > 0) then
          begin Out_XElStart0(XMLElemName[elProvisionalFormulas]);
            for i ← 0 to nSchemePremises↑.Count - 1 do Out_Proposition(nSchemePremises↑.Items↑[i]);
              Out_XElEnd(XMLElemName[elProvisionalFormulas]);
            end;
        end;

```


end

This code is used in section 1080.

1082.

```

Item-contents |= Consider-Statement-contents
Consider-Statement-contents =
( Variable-Segment*,
  element Conditions { Proposition },
  Justification
)
⟨Emit XML for consider contents (WSM) 1082⟩ ≡
  with ChoiceStatementPtr(nContent)↑ do
    begin for i ← 0 to nQualVars↑.Count − 1 do Out_VariableSegment(nQualVars↑.Items↑[i]);
      Out_XElStart0(XMLElemName[elConditions]);
      for i ← 0 to nConditions↑.Count − 1 do Out_Proposition(nConditions↑.Items↑[i]);
        Out_XElEnd(XMLElemName[elConditions]); Out_Justification(nJustification, nil);
      end
    end

```

This code is used in section 1080.

1083.

```

Item-contents |= Type-Changing-Statement-contents
Type-Changing-Statement-contents =
((element Equality {
  Variable,
  Term
} | Variable),
Type)
⟨Emit XML for reconsider contents (WSM) 1083⟩ ≡
  with TypeChangingStatementPtr(nContent)↑ do
    begin for i ← 0 to nTypeChangeList↑.Count − 1 do
      case TypeChangePtr(nTypeChangeList.Items↑[i])↑.nTypeChangeKind of
        Equating: begin Out_XElStart0(XMLElemName[elEquality]);
          Out_Variable(TypeChangePtr(nTypeChangeList.Items↑[i])↑.nVar);
          Out_Term(TypeChangePtr(nTypeChangeList.Items↑[i])↑.nTermExpr);
          Out_XElEnd(XMLElemName[elEquality]);
        end;
        VariableIdentifier: begin Out_Variable(TypeChangePtr(nTypeChangeList.Items↑[i])↑.nVar);
          end;
      endcases;
      Out_Type(nTypeExpr); Out_Justification(nJustification, nil);
    end
  end

```

This code is used in section 1080.

1084. We will need to recall *Out_Variable* (§1022) fr *PrivateFunctorDefinitionObj* (§893).

```

Item-contents |=
  (Variable, Type-List, Term) # private functors and predicates
| (Variable, Term) # constants
| Variable-Segment # loci
⟨Emit XML for definition-related items (WSM) 1084⟩ ≡
itPrivFuncDefinition: with PrivateFunctorDefinitionPtr(nContent)↑ do
  begin Out_Variable(nFuncId); Out_TypeList(nTypeExpList); Out_Term(nTermExpr);
  end;
itPrivPredDefinition: with PrivatePredicateDefinitionPtr(nContent)↑ do
  begin Out_Variable(nPredId); Out_TypeList(nTypeExpList); Out_Formula(nSentence);
  end;
itConstantDefinition: with ConstantDefinitionPtr(nContent)↑ do
  begin Out_Variable(nVarId); Out_Term(nTermExpr);
  end;
itLocDeclaration, itGeneralization: Out_VariableSegment(QualifiedSegmentPtr(nContent));
itCaseHead, itSupposeHead, itAssumption: ⟨Emit XML for assumptions item (WSM) 1092⟩;
See also sections 1085, 1086, 1087, 1088, 1089, 1090, and 1091.
This code is used in section 1080.

```

1085.

```

Item-contents |=
( Variable-Segment*,
  element Conditions { Proposition* } )
⟨Emit XML for definition-related items (WSM) 1084⟩ +≡
itExistentialAssumption: with ExistentialAssumptionPtr(nContent)↑ do
  begin for i ← 0 to nQVars↑.Count - 1 do Out_VariableSegment(nQVars↑.Items↑[i]);
  Out_XElStart0(XMLElemName[elConditions]);
  for i ← 0 to nConditions↑.Count - 1 do Out_Proposition(nConditions↑.Items↑[i]);
  Out_XElEnd(XMLElemName[elConditions]);
  end;

```

1086.

```

Item-contents |= ( Variable?, Term? ) # Exemplification
                  | Justification # percases, correctness-condition
                  | Block # case block
⟨Emit XML for definition-related items (WSM) 1084⟩ +≡
itExemplification: with ExamplePtr(nContent)↑ do
  begin if nVarId ≠ nil then Out_Variable(nVarId);
  if nTermExpr ≠ nil then Out_Term(nTermExpr);
  end;
itPerCases: Out_Justification(JustificationPtr(nContent), nil);
itCaseBlock: Out_Block(nBlock);
itCorrCond: Out_Justification(CorrectnessConditionPtr(nContent)↑.nJustification, nBlock);

```

1087.

```

Item-contents |=
  element CorrectnessConditions { # sic!
    element Correctness { attribute condition { text } }*,
    Justification }
|Justification # Property
⟨Emit XML for definition-related items (WSM) 1084⟩ +≡
itCorrectness: begin Out_XElStart0 (XMLElemName[elCorrectnessConditions]);
  for  $s \in \text{CorrectnessConditionsPtr}(nContent) \uparrow .nConditions$  do
    begin Out_XElStart (ItemName[itCorrectness]);
      Out_XAttr (XMLAttrName[atCondition], CorrectnessName[s]); Out_XElEnd0;
    end;
  Out_XElEnd (XMLElemName[elCorrectnessConditions]);
  Out_Justification (CorrectnessPtr(nContent)↑.nJustification, nBlock);
end;
itProperty: Out_Justification (PropertyPtr(nContent)↑.nJustification, nBlock);

```

1088.

```

Item-contents |=
( element Redefine { }?,
  Pattern,
  element Standard-Mode { Type },
  | element Expandable-Mode {
    element Type-Specification { Type }?,
    Definiens
  })
⟨Emit XML for definition-related items (WSM) 1084⟩ +≡
itDefMode: with ModeDefinitionPtr(nContent)↑ do
  begin if nRedefinition then Out_XEl1 (XMLElemName[elRedefine]);
    Out_Pattern(nDefModePattern);
  case nDefKind of
    defExpandableMode: begin Out_XElStart0 (ModeDefinitionSortName[defExpandableMode]);
      Out_Type (ExpandableModeDefinitionPtr(nContent)↑.nExpansion);
      Out_XElEnd (ModeDefinitionSortName[defExpandableMode]);
    end;
    defStandardMode: with StandardModeDefinitionPtr(nContent)↑ do
      begin Out_XElStart0 (ModeDefinitionSortName[defStandardMode]);
        if nSpecification ≠ nil then
          begin Out_XElStart0 (XMLElemName[elTypeSpecification]); Out_Type(nSpecification);
            Out_XElEnd (XMLElemName[elTypeSpecification]);
          end;
          Out_Definiens(nDefiniens); Out_XElEnd (ModeDefinitionSortName[defStandardMode]);
        end;
      endcases;
    end;

```

1089.

```

Item-contents |=
(element Redefine { }?,
 Pattern,
 Definiens)
⟨Emit XML for definition-related items (WSM) 1084⟩ +≡
itDefAttr: with AttributeDefinitionPtr(nContent)↑ do
    begin if nRedefinition then Out_XEl1(XMLElemName[elRedefine]);
    Out_Pattern(nDefAttrPattern); Out_Definiens(nDefiniens);
    end;
itDefPred: with PredicateDefinitionPtr(nContent)↑ do
    begin if nRedefinition then Out_XEl1(XMLElemName[elRedefine]);
    Out_Pattern(nDefPredPattern); Out_Definiens(nDefiniens);
    end;

```

1090.

```

Item-contents |=
(element Redefine { }?,
 Pattern,
 element Type-Specification { Type }?,
 Definiens)
⟨Emit XML for definition-related items (WSM) 1084⟩ +≡
itDefFunc: with FunctorDefinitionPtr(nContent)↑ do
    begin if nRedefinition then Out_XEl1(XMLElemName[elRedefine]);
    Out_Pattern(nDefFuncPattern);
    if nSpecification ≠ nil then
        begin Out_XElStart0(XMLElemName[elTypeSpecification]); Out_Type(nSpecification);
        Out_XElEnd(XMLElemName[elTypeSpecification]);
        end;
    Out_Definiens(nDefiniens);
    end;

```

1091.

```

Item-contents |=
(element Ancestors { Type* },
  attribute nr { xsd:integer },
  attribute spelling { text }?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Loci,
  (element Field-Segment {
    attribute col { xsd:integer },
    attribute line { xsd:integer },
    (element Selector {
      attribute nr { xsd:integer },
      attribute spelling { text }?,
      attribute col { xsd:integer },
      attribute line { xsd:integer }
    })*,
    Type
  )*
),
{
  (Emit XML for definition-related items (WSM) 1084) +≡
  itDefStruct: with StructureDefinitionPtr(nContent)↑ do
    begin Out_XElStart0(XMLElemName[elAncestors]);
    for i ← 0 to nAncestors↑.Count - 1 do Out_Type(nAncestors↑.Items↑[i]);
    Out_XElEnd(XMLElemName[elAncestors]); Out_XElStart(DefPatternName[itDefStruct]);
    Out_XIntAttr(XMLAttrName[atNr], nDefStructPattern↑.nModeSymbol);
    if nMizarAppearance then
      Out_XAttr(XMLAttrName[atSpelling], StructureName[nDefStructPattern↑.nModeSymbol]);
    Out_PosAsAttrs(nStrPos); Out_XAttrEnd; Out_Loci(nDefStructPattern↑.nArgs);
    for i ← 0 to nSgmFields↑.Count - 1 do
      with FieldSegmentPtr(nSgmFields↑.Items↑[i])↑ do
        begin Out_XElStart(XMLElemName[elFieldSegment]); Out_PosAsAttrs(nFieldSegmPos);
        Out_XAttrEnd;
        for j ← 0 to nFields↑.Count - 1 do
          with FieldSymbolPtr(nFields↑.Items↑[j])↑ do
            begin Out_XElStart(XMLElemName[elSelector]);
            Out_XIntAttr(XMLAttrName[atNr], nFieldSymbol);
            if nMizarAppearance then
              Out_XAttr(XMLAttrName[atSpelling], SelectorName[nFieldSymbol]);
            Out_PosAsAttrs(nFieldPos); Out_XElEnd0
            end;
          Out_Type(nSpecification); Out_XElEnd(XMLElemName[elFieldSegment]);
        end;
      Out_XElEnd(DefPatternName[itDefStruct]);
    end
  end
}

```

1092.

```

Item-contents |= (element Single-Assumption {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Proposition
} | element Collective-Assumption {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  element Conditions { Proposition* }
})

⟨Emit XML for assumptions item (WSM) 1092⟩ ≡
  case AssumptionPtr(nContent)↑.nAssumptionSort of
    SingleAssumption: begin Out_XElStart(AssumptionKindName[SingleAssumption]);
      Out_PosAsAttrs(AssumptionPtr(nContent)↑.nAssumptionPos); Out_XAttrEnd;
      Out_Proposition(SingleAssumptionPtr(nContent)↑.nProp);
      Out_XElEnd(AssumptionKindName[SingleAssumption]);
    end;
    CollectiveAssumption: begin Out_XElStart(AssumptionKindName[CollectiveAssumption]);
      Out_PosAsAttrs(AssumptionPtr(nContent)↑.nAssumptionPos); Out_XAttrEnd;
      Out_XElStart0(XMLElemName[elConditions]);
      with CollectiveAssumptionPtr(nContent)↑ do
        for i ← 0 to nConditions↑.Count - 1 do Out_Proposition(nConditions↑.Items↑[i]);
          Out_XElEnd(XMLElemName[elConditions]);
          Out_XElEnd(AssumptionKindName[CollectiveAssumption]);
        end;
      endcases
  endcases

```

This code is used in section 1084.

1093. We have cluster registrations and non-cluster registrations.

```

Existential-Registration-content = element Existential-Registration {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Adjective-Cluster,
  Type
}
Conditional-Registration-content = element Conditional-Registration {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Adjective-Cluster, Adjective-Cluster,
  Type
}
Functorial-Registration-content = element Functorial-Registration {
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  Term,
  Adjective-Cluster,
  Type?
}
⟨Emit XML for registration-related items (WSM) 1093⟩ ≡
itCluster: case ClusterPtr(nContent)↑.nClusterKind of
  ExistentialRegistration: with EClusterPtr(nContent)↑ do
    begin Out_XElStart(ClusterRegistrationName[ExistentialRegistration]);
    Out_PosAsAttrs(nClusterPos); Out_XAttrEnd; Out_AdjectiveList(nConsequent);
    Out_Type(nClusterType); Out_XElEnd(ClusterRegistrationName[ExistentialRegistration]);
    end;
  ConditionalRegistration: with CClusterPtr(nContent)↑ do
    begin Out_XElStart(ClusterRegistrationName[ConditionalRegistration]);
    Out_PosAsAttrs(nClusterPos); Out_XAttrEnd; Out_AdjectiveList(nAntecedent);
    Out_AdjectiveList(nConsequent); Out_Type(nClusterType);
    Out_XElEnd(ClusterRegistrationName[ConditionalRegistration]);
    end;
  FunctorialRegistration: with FClusterPtr(nContent)↑ do
    begin Out_XElStart(ClusterRegistrationName[FunctorialRegistration]);
    Out_PosAsAttrs(nClusterPos); Out_XAttrEnd; Out_Term(nClusterTerm);
    Out_AdjectiveList(nConsequent);
    if nClusterType ≠ nil then Out_Type(nClusterType);
    Out_XElEnd(ClusterRegistrationName[FunctorialRegistration]);
    end;
endcases;

```

See also section 1094.

This code is used in section 1080.

1094.

```

Identify-Registration-content =
  (Pattern, Pattern,
    element LociEquality {
      attribute col { xsd:integer },
      attribute line { xsd:integer },
      Locus, Locus
    }*
  })
Sethood-Registration-content = (Type, Justification)
Reduction-Registration-content = (Term, Term)
⟨Emit XML for registration-related items (WSM) 1093⟩ +≡
itIdentify: with IdentifyRegistrationPtr(nContent)↑ do
  begin Out_Pattern(nOriginPattern); Out_Pattern(nNewPattern);
  if nEqLociList ≠ nil then
    begin for i ← 0 to nEqLociList↑.Count − 1 do
      with LociEqualityPtr(nEqLociList↑.Items↑[i])↑ do
        begin Out_XElStart(XMLElemName[elLociEquality]); Out_PosAsAttrs(nEqPos);
          Out_XAttrEnd; Out_Locus(nLeftLocus); Out_Locus(nRightLocus);
          Out_XElEnd(XMLElemName[elLociEquality]);
        end;
      end;
    end;
  end;
itPropertyRegistration: case PropertyRegistrationPtr(nContent)↑.nPropertySort of
  sySethood: with SethoodRegistrationPtr(nContent)↑ do
    begin Out_Type(nSethoodType); Out_Justification(nJustification, nBlock);
    end;
  endcases;
itReduction: with ReduceRegistrationPtr(nContent)↑ do
  begin Out_Term(nOriginTerm); Out_Term(nNewTerm);
  end

```


1095. Emitting an item.

```

Item = element Item {
  attribute kind { text },
  Item-contents-attribute?,
  attribute col { xsd:integer },
  attribute line { xsd:integer },
  attribute posline { xsd:integer },
  attribute poscol { xsd:integer },
  (Block | Item-contents)?
}

⟨Implementation for wsmarticle.pas 854⟩ +≡
procedure OutWSMizFileObj.Out_Item(aWSItem : WSItemPtr);
  var i, j: integer;
  begin with aWSItem↑ do
    begin CurPos ← nItemPos; Out_XElStart(XMLElemName[elItem]);
    Out_XAttr(XMLAttrName[atKind], ItemName[nItemKind]);
    if nContent ≠ nil then Out_ItemContentsAttr(aWsItem);
    Out_PosAsAttrs(nItemPos); Out_XIntAttr(XMLAttrName[atPosLine], nItemEndPos.Line);
    Out_XIntAttr(XMLAttrName[atPosCol], nItemEndPos.Col); Out_XAttrEnd;
    if nContent = nil then
      begin if nBlock ≠ nil then Out_Block(nBlock);
      end
    else Out_ItemContents(aWsItem);
    Out_XElEnd(XMLElemName[elItem]);
    end;
  end;

```

1096. Writing out to an XML file.

```

procedure Write_WSMizArticle(aWSTextProper : wsTextProperPtr; aFileName : string);
  var lWSMizOutput: OutWSMizFilePtr;
  begin InitScannerNames; lWSMizOutput ← new(OutWSMizFilePtr, OpenFile(aFileName));
  lWSMizOutput↑.nMizarAppearance ← true; lWSMizOutput↑.Out_TextProper(aWSTextProper);
  dispose(lWSMizOutput, Done);
  end;

```

Section 21.12. READING WSM FILES (DEFERRED)

1097. Reading a WSM file amounts to reading an XML file, which means that the *XMLInStream* class (§528) is a natural parent class. Recall, the state of the *XMLInStream* contains the current start tag and a dictionary for the attributes and their values.

The code is a “mirror image” to writing XML files, and the XML schema guides the implementation.

```
{Publicly declared types in wsmarticle.pas 852} +≡
  InWSMizFilePtr = ↑InWSMizFileObj;
  InWSMizFileObj = object (XMLInStreamObj)
    nDisplayInformationOnScreen: boolean;
    constructor OpenFile(const aFileName: string);
    destructor Done; virtual;
    function GetAttrValue(const aAttrName: string): string;
    function GetAttrPos: Position;
    function Read_TextProper: wsTextProperPtr; virtual;
    function Read_Block: wsBlockPtr; virtual;
    function Read_Item: wsItemPtr; virtual;
    procedure Read_ItemContentsAttr(aItem : wsItemPtr; var aShape : string); virtual;
    procedure Read_ItemContents(aItem : wsItemPtr ; const aShape: string); virtual;
    function Read_TermList: PList; virtual;
    function Read_Adjective: AdjectiveExpressionPtr; virtual;
    function Read_AdjectiveList: PList; virtual;
    function Read_Type: TypePtr; virtual;
    function Read_Variable: VariablePtr; virtual;
    function Read_ImplicitlyQualifiedSegment: ImplicitlyQualifiedSegmentPtr; virtual;
    function Read_VariableSegment: QualifiedSegmentPtr; virtual;
    function Read_PrivatePredicativeFormula: PrivatePredicativeFormulaPtr; virtual;
    function Read_Formula: FormulaPtr; virtual;
    function Read_SimpleTerm: SimpleTermPtr; virtual;
    function Read_PrivateFunctorTerm: PrivateFunctorTermPtr; virtual;
    function Read_InternalSelectorTerm: InternalSelectorTermPtr; virtual;
    function Read_Term: TermPtr; virtual;
    function Read_TypeList: PList; virtual;
    function Read_Locus: LocusPtr; virtual;
    function Read_Loci: PList; virtual;
    function Read_ModePattern: ModePatternPtr; virtual;
    function Read_AttributePattern: AttributePatternPtr; virtual;
    function Read_FunctorPattern: FunctorPatternPtr; virtual;
    function Read_PredicatePattern: PredicatePatternPtr; virtual;
    function Read_Pattern: PatternPtr; virtual;
    function Read_Definiens: DefiniensPtr; virtual;
    function Read_ReservationSegment: ReservationSegmentPtr; virtual;
    function Read_SchemeNameInSchemeHead: SchemePtr; virtual;
    function Read_Label: LabelPtr; virtual;
    function Read_Proposition: PropositionPtr; virtual;
    function Read_CompactStatement: CompactStatementPtr; virtual;
    function Read_LocalReference: LocalReferencePtr; virtual;
    function Read_References: PList; virtual;
    function Read_StraightforwardJustification: StraightforwardJustificationPtr; virtual;
    function Read_SchemeJustification: SchemeJustificationPtr; virtual;
    function Read_Justification: JustificationPtr; virtual;
    function Read_RegularStatement(const aShape: string): RegularStatementPtr; virtual;
  end ;
```

1098. Constructor.

⟨Implementation for `wsmarticle.pas 854`⟩ +≡
constructor *InWSMizFileObj.OpenFile*(**const** *aFileName*: *string*);
 begin *inherited OpenFile(aFileName)*; *nDisplayInformationOnScreen* \leftarrow *false*;
 end;
destructor *InWSMizFileObj.Done*;
 begin *inherited Done*;
 end;

1099. Getting the value for an attribute. Returns **nil** if there is no attribute with the given name. (Recall (§490), an *XMLAttr* is just a wrapper around a string *nValue*.)

⟨Implementation for `wsmarticle.pas 854`⟩ +≡
function *InWSMizFileObj.GetAttrValue*(**const** *aAttrName*: *string*): *string*;
 var *lObj*: *PObject*;
 begin *result* \leftarrow *''*; *lObj* \leftarrow *nAttrVals.ObjectOf(aAttrName)*;
 if *lObj* \neq **nil** **then** *result* \leftarrow *XMLAttrPtr(lObj)* \uparrow .*nValue*;
 end;

1100. We can query for the *position* of the XML attribute.

⟨Implementation for `wsmarticle.pas 854`⟩ +≡
function *InWSMizFileObj.GetAttrPos*: *Position*;
 var *lLine*, *lCol*: *XMLAttrPtr*; *lCode*: *integer*;
 begin *result.Line* \leftarrow 1; *result.Col* \leftarrow 1;
 lLine \leftarrow *XMLAttrPtr(nAttrVals.ObjectOf(XMLAttrName[atLine]))*;
 lCol \leftarrow *XMLAttrPtr(nAttrVals.ObjectOf(XMLAttrName[atCol]))*;
 if (*lLine* \neq **nil**) \wedge (*lCol* \neq **nil**) **then**
 begin *Val(lLine* \uparrow .*nValue*, *result.Line*, *lCode*); *Val(lCol* \uparrow .*nValue*, *result.Col*, *lCode*);
 end;
 end;

1101. The state of the WSM parser may be described with a handful of lookup tables.

(Implementation for `wsmarticle.pas` 854) +≡

```
var ElemLookupTable, AttrLookupTable, BlockLookupTable, ItemLookupTable, FormulaKindLookupTable,
    TermKindLookupTable, PatternKindLookupTable, CorrectnessKindLookupTable,
    PropertyKindLookupTable: MSortedStrList;
```

```
procedure InitWSLookupTables;
```

```
  var e: XMLElemKind; a: XMLAttrKind; b: BlockKind; i: ItemKind; f: FormulaSort; t: TermSort;
      p: PropertyKind; c: CorrectnessKind;
```

```
  begin ElemLookupTable.Init(Ord(High(XMLElemKind)) + 1);
```

```
    AttrLookupTable.Init(Ord(High(XMLAttrKind)) + 1);
```

```
    BlockLookupTable.Init(Ord(High(BlockKind)) + 1); ItemLookupTable.Init(Ord(High(ItemKind)) + 1);
```

```
    FormulaKindLookupTable.Init(Ord(High(FormulaSort)) + 1);
```

```
    TermKindLookupTable.Init(Ord(High(TermSort)) + 1);
```

```
    PatternKindLookupTable.Init(Ord(itDefStruct) - Ord(itDefPred) + 1);
```

```
    CorrectnessKindLookupTable.Init(ord(High(CorrectnessKind)) + 1);
```

```
    PropertyKindLookupTable.Init(ord(High(PropertyKind)) + 1);
```

```
  for e ← Low(XMLElemKind) to High(XMLElemKind) do
    ElemLookupTable.Insert(new(MStrPtr, Init(XMLElemName[e]]));
```

```
  for a ← Low(XMLAttrKind) to High(XMLAttrKind) do
    AttrLookupTable.Insert(new(MStrPtr, Init(XMLAttrName[a]]));
```

```
  for b ← Low(BlockKind) to High(BlockKind) do
    BlockLookupTable.Insert(new(MStrPtr, Init(BlockName[b]]));
```

```
  for i ← Low(ItemKind) to High(ItemKind) do
    ItemLookupTable.Insert(new(MStrPtr, Init(ItemName[i]]));
```

```
  for f ← Low(FormulaSort) to High(FormulaSort) do
    FormulaKindLookupTable.Insert(new(MStrPtr, Init(FormulaName[f]]));
```

```
  for t ← Low(TermSort) to High(TermSort) do
    TermKindLookupTable.Insert(new(MStrPtr, Init(TermName[t]]));
```

```
  for i ← itDefPred to itDefStruct do
    PatternKindLookupTable.Insert(new(MStrPtr, Init(DefPatternName[i]]));
```

```
  for p ← Low(PropertyKind) to High(PropertyKind) do
    PropertyKindLookupTable.Insert(new(MStrPtr, Init(PropertyName[p]]));
```

```
  for c ← Low(CorrectnessKind) to High(CorrectnessKind) do
    CorrectnessKindLookupTable.Insert(new(MStrPtr, Init(CorrectnessName[c]]));
```

```
  end;
```

1102. We also need to free the memory consumed by the lookup tables.

(Implementation for `wsmarticle.pas` 854) +≡

```
procedure DisposeWSLookupTables;
```

```
  begin ElemLookupTable.Done; AttrLookupTable.Done; BlockLookupTable.Done;
```

```
    ItemLookupTable.Done; FormulaKindLookupTable.Done; TermKindLookupTable.Done;
```

```
    CorrectnessKindLookupTable.Done; PropertyKindLookupTable.Done;
```

```
  end;
```

1103. We can recall, from the XML dictionary module (§462), the different kinds of XML elements as specified by an enumerated constant. This converts the “nr” attribute to the human readable equivalents.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```
function Str2XMLElemKind(aStr : string): XMLElemKind;
  var lNr: integer;
  begin lNr ← ElemLookupTable.IndexOfStr(aStr);
  if lNr > -1 then Str2XMLElemKind ← XMLElemKind(lNr)
  else Str2XMLElemKind ← elUnknown;
  end;
```

1104. Like the previous function, this converts the “nr” attribute for a WSM Mizar attribute XML element into a human readable form.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```
function Str2XMLAttrKind(aStr : string): XMLAttrKind;
  var lNr: integer;
  begin lNr ← AttrLookupTable.IndexOfStr(aStr);
  if lNr > -1 then Str2XMLAttrKind ← XMLAttrKind(lNr)
  else Str2XMLAttrKind ← atUnknown;
  end;
```

1105. The “kinds” of different syntactic classes were introduced earlier in `wsmarticle.pas`, now we want to translate them into human readable form.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```
function Str2BlockKind(aStr : string): BlockKind;
  var lNr: integer;
  begin lNr ← BlockLookupTable.IndexOfStr(aStr);
  if lNr > -1 then Str2BlockKind ← BlockKind(lNr)
  else Str2BlockKind ← blMain;
  end;
```

```
function Str2ItemKind(aStr : string): ItemKind;
  var lNr: integer;
  begin lNr ← ItemLookupTable.IndexOfStr(aStr);
  if lNr > -1 then Str2ItemKind ← ItemKind(lNr)
  else Str2ItemKind ← itIncorrItem;
  end;
```

```
function Str2PatterenKind(aStr : string): ItemKind;
  var lNr: integer;
  begin lNr ← PatternKindLookupTable.IndexOfStr(aStr);
  if lNr > -1 then Str2PatterenKind ← ItemKind(Ord(ItDefPred) + lNr)
  else Str2PatterenKind ← itIncorrItem;
  end;
```

```
function Str2FormulaKind(aStr : string): FormulaSort;
  var lNr: integer;
  begin lNr ← FormulaKindLookupTable.IndexOfStr(aStr);
  if lNr > -1 then Str2FormulaKind ← FormulaSort(lNr)
  else Str2FormulaKind ← wsErrorFormula;
  end;
```

1106.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡
function *Str2TermKind*(*aStr* : *string*): *TermSort*;
 var *lNr*: *integer*;
 begin *lNr* ← *TermKindLookupTable.IndexOfStr*(*aStr*);
 if *lNr* > -1 **then** *Str2TermKind* ← *TermSort*(*lNr*)
 else *Str2TermKind* ← *wsErrorTerm*;
 end;
function *Str2PropertyKind*(*aStr* : *string*): *PropertyKind*;
 var *lNr*: *integer*;
 begin *lNr* ← *PropertyKindLookupTable.IndexOfStr*(*aStr*);
 if *lNr* > -1 **then** *Str2PropertyKind* ← *PropertyKind*(*lNr*)
 end;
function *Str2CorrectnessKind*(*aStr* : *string*): *CorrectnessKind*;
 var *lNr*: *integer*;
 begin *lNr* ← *CorrectnessKindLookupTable.IndexOfStr*(*aStr*);
 if *lNr* > -1 **then** *Str2CorrectnessKind* ← *CorrectnessKind*(*lNr*)
 end;

Subsection 21.12.1. Parsing types

1107. Reading a “term list” just iteratively invokes *Read_Term* (§1121) until all the children have been read.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡
function *InWSMizFileObj.Read_TermList*: *PList*;
 begin *result* ← *new*(*PList*, *Init*(0));
 while *nState* ≠ *eEnd* **do** *result*↑.*Insert*(*Read_Term*);
 end;

1108. An adjective is either “positive” (i.e., not negated) or “negative” (i.e., negated). We handle the first case in the “true” branch, and the second case in the “false” branch.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡
function *InWSMizFileObj.Read_Adjective*: *AdjectiveExpressionPtr*;
 var *lAttrNr*: *integer*; *lPos*: *Position*; *lNoneOcc*: *Boolean*;
 begin if *nElName* = *AdjectiveSortName*[*wsAdjective*] **then**
 begin *lPos* ← *GetAttrPos*; *lAttrNr* ← *GetIntAttr*(*XMLAttrName*[*atNr*]); *NextElementState*;
 result ← *new*(*AdjectivePtr*, *Init*(*lPos*, *lAttrNr*, *Read_TermList*)); *NextElementState*;
 end
 else begin *lPos* ← *GetAttrPos*; *NextElementState*;
 result ← *new*(*NegatedAdjectivePtr*, *Init*(*lPos*, *Read_Adjective*)); *NextElementState*;
 end;
 end;

1109. Reading a list of adjectives just iterates over the children of an element.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡
function *InWSMizFileObj.Read_AdjectiveList*: *PList*;
 begin *result* ← *new*(*PList*, *Init*(0)); *NextElementState*;
 while *nState* ≠ *eEnd* **do** *result*↑.*Insert*(*Read_Adjective*);
 NextElementState;
 end;

1110. There are three valid Mizar types: “standard” types, structure types, and expandable modes (i.e., a cluster of adjectives stacked atop a type). If the XML element fails to match these three, then we should produce an “incorrect type”.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡
function *InWSMizFileObj.Read_Type*: *TypePtr*;
 var *lList*: *Plist*; *lPos*: *Position*; *lModeSymbol*: *integer*;
 begin if *nElName* = *TypeName*[*wsStandardType*] **then**
 begin *lPos* ← *GetAttrPos*; *lModeSymbol* ← *GetIntAttr*(*XMLAttrName*[*atNr*]); *NextElementState*;
 result ← *new*(*StandardTypePtr*, *Init*(*lPos*, *lModeSymbol*, *Read_TermList*)); *NextElementState*;
 end
 else if *nElName* = *TypeName*[*wsStructureType*] **then**
 begin *lPos* ← *GetAttrPos*; *lModeSymbol* ← *GetIntAttr*(*XMLAttrName*[*atNr*]); *NextElementState*;
 result ← *new*(*StructTypePtr*, *Init*(*lPos*, *lModeSymbol*, *Read_TermList*)); *NextElementState*;
 end
 else if *nElName* = *TypeName*[*wsClusteredType*] **then**
 begin *lPos* ← *GetAttrPos*; *NextElementState*; *lList* ← *Read_AdjectiveList*;
 result ← *new*(*ClusteredTypePtr*, *Init*(*lPos*, *lList*, *Read_Type*)); *NextElementState*;
 end
 else begin *lPos* ← *GetAttrPos*; *NextElementState*; *result* ← *new*(*IncorrectTypePtr*, *Init*(*lPos*));
 NextElementState;
 end
end;

Subsection 21.12.2. Parsing formulas

1111. Parsing a variable from XML just requires reading the attributes, since it is an empty-element.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡
function *InWSMizFileObj.Read_Variable*: *VariablePtr*;
 var *lPos*: *Position*; *lNr*: *integer*;
 begin *lPos* ← *GetAttrPos*; *lNr* ← *GetIntAttr*(*XMLAttrName*[*atIdNr*]);
 NextElementState; { closes the variable’s tag }
 result ← *new*(*VariablePtr*, *Init*(*lPos*, *lNr*));
 NextElementState; { starts the next tag }
end;

1112. Implicitly qualified variables are just wrappers around a variable.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡
function *InWSMizFileObj.Read_ImplicitlyQualifiedSegment*: *ImplicitlyQualifiedSegmentPtr*;
 var *lPos*: *Position*;
 begin *lPos* ← *GetAttrPos*; *NextElementState*;
 result ← *new*(*ImplicitlyQualifiedSegmentPtr*, *Init*(*lPos*, *Read_Variable*)); *NextElementState*;
end;

1113. Recall (§1025) that a “qualified segment” is either implicit (i.e., a wrapper around a single variable) or explicit (i.e., an element whose children are variables and a type).

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```
function InWSMizFileObj.Read_VariableSegment: QualifiedSegmentPtr;
  var lPos: Position; lVar: VariablePtr; lList: PList;
  begin if nElName = SegmentKindName[ikImplQualifiedSegm] then
    begin result ← Read_ImplicitlyQualifiedSegment;
    end
  else if nElName = SegmentKindName[ikExplQualifiedSegm] then
    begin lPos ← GetAttrPos; NextElementState; lList ← new(PList, Init(0));
    NextElementState; { read the variables }
    while (nState = eStart) ∧ (nElName = XMLElemName[elVariable]) do
      lList↑.Insert(Read_Variable);
    NextElementState; { read the type }
    result ← new(ExplicitlyQualifiedSegmentPtr, Init(lPos, lList, Read_Type));
    NextElementState; { start the next tag }
    end
  end;
```

1114. Private predicates are empty elements, so we only need to read their attributes.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```
function InWSMizFileObj.Read_PrivatePredicativeFormula: PrivatePredicativeFormulaPtr;
  var lPos: Position; lNr: integer;
  begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atIdNr]); NextElementState;
  Result ← new(PrivatePredicativeFormulaPtr, Init(lPos, lNr, Read_TermList)); NextElementState;
  end;
```

1115.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

function InWSMizFileObj.Read_Formula: FormulaPtr;
  var lPos: Position; lNr: integer; lList: PList; lFrm: FormulaPtr; lTrm: TermPtr;
      lSgm: QualifiedSegmentPtr;
  begin case Str2FormulaKind(nElName) of
    wsNegatedFormula: begin lPos ← GetAttrPos; NextElementState;
      result ← new(NegativeFormulaPtr, Init(lPos, Read_Formula)); NextElementState;
    end;
    ⟨Parse XML for formula with binary connective 1116⟩;
    wsFlexaryConjunctiveFormula: begin lPos ← GetAttrPos; NextElementState; lFrm ← Read_Formula;
      result ← new(FlexaryConjunctiveFormulaPtr, Init(lPos, lFrm, Read_Formula)); NextElementState;
    end;
    wsFlexaryDisjunctiveFormula: begin lPos ← GetAttrPos; NextElementState; lFrm ← Read_Formula;
      result ← new(FlexaryDisjunctiveFormulaPtr, Init(lPos, lFrm, Read_Formula)); NextElementState;
    end;
    ⟨Parse XML for predicate-based formula 1117⟩;
    wsAttributiveFormula: begin lPos ← GetAttrPos; NextElementState; lTrm ← Read_Term;
      Result ← new(AttributiveFormulaPtr, Init(lPos, lTrm, Read_AdjectiveList)); NextElementState;
    end;
    wsQualifyingFormula: begin lPos ← GetAttrPos; NextElementState; lTrm ← Read_Term;
      Result ← new(QualifyingFormulaPtr, Init(lPos, lTrm, Read_Type)); NextElementState;
    end;
    wsUniversalFormula: begin lPos ← GetAttrPos; NextElementState; lSgm ← Read_VariableSegment;
      Result ← new(UniversalFormulaPtr, Init(lPos, lSgm, Read_Formula)); NextElementState;
    end;
    wsExistentialFormula: begin lPos ← GetAttrPos; NextElementState; lSgm ← Read_VariableSegment;
      Result ← new(ExistentialFormulaPtr, Init(lPos, lSgm, Read_Formula)); NextElementState;
    end;
    wsContradiction: begin lPos ← GetAttrPos; NextElementState;
      result ← new(ContradictionFormulaPtr, Init(lPos)); NextElementState;
    end;
    wsThesis: begin lPos ← GetAttrPos; NextElementState; result ← new(ThesisFormulaPtr, Init(lPos));
      NextElementState;
    end;
    wsErrorFormula: begin lPos ← GetAttrPos; NextElementState;
      result ← new(IncorrectFormulaPtr, Init(lPos)); NextElementState;
    end;
  endcases;
end;

```

1116. For formulas with binary connectives, we read both arguments.

```

⟨ Parse XML for formula with binary connective 1116 ⟩ ≡
wsConjunctiveFormula: begin lPos ← GetAttrPos; NextElementState; lFrm ← Read_Formula;
    result ← new(ConjunctiveFormulaPtr, Init(lPos, lFrm, Read_Formula)); NextElementState;
end;
wsDisjunctiveFormula: begin lPos ← GetAttrPos; NextElementState; lFrm ← Read_Formula;
    result ← new(DisjunctiveFormulaPtr, Init(lPos, lFrm, Read_Formula)); NextElementState;
end;
wsConditionalFormula: begin lPos ← GetAttrPos; NextElementState; lFrm ← Read_Formula;
    result ← new(ConditionalFormulaPtr, Init(lPos, lFrm, Read_Formula)); NextElementState;
end;
wsBiconditionalFormula: begin lPos ← GetAttrPos; NextElementState; lFrm ← Read_Formula;
    result ← new(BiconditionalFormulaPtr, Init(lPos, lFrm, Read_Formula)); NextElementState;
end

```

This code is used in section 1115.

1117.

```

⟨ Parse XML for predicate-based formula 1117 ⟩ ≡
wsPredicativeFormula: begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]);
    NextElementState; NextElementState; { Arguments }
    lList ← Read_TermList; NextElementState; { Arguments }
    NextElementState; { Arguments }
    Result ← new(PredicativeFormulaPtr, Init(lPos, lNr, lList, Read_TermList)); NextElementState;
    NextElementState;
end;
wsRightSideOfPredicativeFormula: begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]);
    NextElementState; NextElementState; { Arguments }
    Result ← new(RightSideOfPredicativeFormulaPtr, Init(lPos, lNr, Read_TermList)); NextElementState;
    NextElementState;
end;
wsMultiPredicativeFormula: begin lPos ← GetAttrPos; NextElementState; lList ← new(PList, Init(0));
    while nState ≠ eEnd do lList↑.Insert(Read_Formula);
    result ← new(MultiPredicativeFormulaPtr, Init(lPos, lList)); NextElementState;
end;
wsPrivatePredicateFormula: begin Result ← Read_PrivatePredicativeFormula;
end

```

This code is used in section 1115.

Subsection 21.12.3. Parsing terms**1118.**⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

function InWSMizFileObj.Read_SimpleTerm: SimpleTermPtr;
  var lPos: Position; lNr: integer;
  begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atIdNr]); NextElementState;
  result ← new(SimpleTermPtr, Init(lPos, lNr)); NextElementState;
  end;

```

1119.⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

function InWSMizFileObj.Read_PrivateFunctorTerm: PrivateFunctorTermPtr;
  var lPos: Position; lNr: integer;
  begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atIdNr]); NextElementState;
  result ← new(PrivateFunctorTermPtr, Init(lPos, lNr, Read_TermList)); NextElementState;
  end;

```

1120.⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

function InWSMizFileObj.Read_InternalSelectorTerm: InternalSelectorTermPtr;
  var lPos: Position; lNr: integer;
  begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]); NextElementState;
  result ← new(InternalSelectorTermPtr, Init(lPos, lNr)); NextElementState;
  end;

```

1121.

(Implementation for `wsmarticle.pas` 854) +≡

```

function InWSMizFileObj.Read_Term: TermPtr;
  var lPos, lRPos: Position; lNr, lRNR: integer; lList: PList; lTrm: TermPtr;
  begin case Str2TermKind(nElName) of
    wsPlaceholderTerm: begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]);
      NextElementState; result ← new(PlaceholderTermPtr, Init(lPos, lNr)); NextElementState;
    end;
    wsSimpleTerm: begin result ← Read_SimpleTerm;
    end;
    wsNumeralTerm: begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNumber]);
      NextElementState; result ← new(NumeralTermPtr, Init(lPos, lNr)); NextElementState;
    end;
    wsInfixTerm: begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]); NextElementState;
      NextElementState; { Arguments }
      lList ← Read_TermList; NextElementState; { Arguments }
      NextElementState; { Arguments }
      result ← new(InfixTermPtr, Init(lPos, lNr, lList, Read_TermList)); NextElementState;
      NextElementState;
    end;
    wsCircumfixTerm: begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]);
      NextElementState; NextElementState; lRNR ← GetIntAttr(XMLAttrName[atNr]);
      lRPos ← GetAttrPos; NextElementState;
      result ← new(CircumfixTermPtr, Init(lPos, lNr, lRNR, Read_TermList)); NextElementState;
    end;
    wsPrivateFunctorTerm: begin result ← Read_PrivateFunctorTerm;
    end;
    wsAggregateTerm: begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]);
      NextElementState; result ← new(AggregateTermPtr, Init(lPos, lNr, Read_TermList));
      NextElementState;
    end;
    wsSelectorTerm: begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]);
      NextElementState; result ← new(SelectorTermPtr, Init(lPos, lNr, Read_Term)); NextElementState;
    end;
    wsInternalSelectorTerm: result ← Read_InternalSelectorTerm;
    wsForgetfulFunctorTerm: begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]);
      NextElementState; result ← new(ForgetfulFunctorTermPtr, Init(lPos, lNr, Read_Term));
      NextElementState;
    end;
    wsInternalForgetfulFunctorTerm: begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]);
      NextElementState; result ← new(InternalForgetfulFunctorTermPtr, Init(lPos, lNr));
      NextElementState;
    end;
    wsFraenkelTerm: begin lPos ← GetAttrPos; NextElementState; lList ← new(PList, Init(0));
      while (nState = eStart) ∧ ((nElName = SegmentKindName[ikImplQualifiedSegm]) ∨ (nElName =
        SegmentKindName[ikExplQualifiedSegm])) do lList↑.Insert(Read_VariableSegment);
      lTrm ← Read_Term; result ← new(FraenkelTermPtr, Init(lPos, lList, lTrm, Read_Formula));
      NextElementState;
    end;
    wsSimpleFraenkelTerm: begin lPos ← GetAttrPos; NextElementState; lList ← new(PList, Init(0));
      while (nState = eStart) ∧ ((nElName = SegmentKindName[ikImplQualifiedSegm]) ∨ (nElName =
        SegmentKindName[ikExplQualifiedSegm])) do lList↑.Insert(Read_VariableSegment);

```

```

    lTrm ← Read_Term; result ← new(SimpleFraenkelTermPtr, Init(lPos, lList, lTrm));
    NextElementState;
  end;
wsQualificationTerm: begin lPos ← GetAttrPos; NextElementState; lTrm ← Read_Term;
  Result ← new(QualifiedTermPtr, Init(lPos, lTrm, Read_Type)); NextElementState;
  end;
wsExactlyTerm: begin lPos ← GetAttrPos; NextElementState;
  Result ← new(ExactlyTermPtr, Init(lPos, Read_Term)); NextElementState;
  end;
wsGlobalChoiceTerm: begin lPos ← GetAttrPos; NextElementState;
  Result ← new(ChoiceTermPtr, Init(lPos, Read_Type)); NextElementState;
  end;
wsItTerm: begin lPos ← GetAttrPos; NextElementState; Result ← new(ItTermPtr, Init(lPos));
  NextElementState;
  end;
wsErrorTerm: begin lPos ← GetAttrPos; NextElementState;
  Result ← new(IncorrectTermPtr, Init(lPos)); NextElementState;
  end;
endcases;
end;

```

Subsection 21.12.4. Parsing text items

1122.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡
function InWSMizFileObj.Read_TypeList: PList;
begin NextElementState; result ← new(PList, Init(0));
while nState ≠ eEnd **do** result↑.Insert(Read_Type);
 NextElementState;
end;

1123.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡
function InWSMizFileObj.Read_Locus: LocusPtr;
var lPos: Position; lNr: integer;
begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atIdNr]); NextElementState;
 result ← new(LocusPtr, Init(lPos, lNr)); NextElementState;
end;

1124.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡
function InWSMizFileObj.Read_Loci: PList;
begin NextElementState; result ← new(PList, Init(0));
while nState ≠ eEnd **do** result↑.Insert(Read_Locus);
 NextElementState;
end;

1125.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

function InWSMizFileObj.Read_ModePattern: ModePatternPtr;
  var lPos: Position; lNr: integer;
  begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]); NextElementState;
  result ← new(ModePatternPtr, Init(lPos, lNr, Read_Loci)); NextElementState;
  end;

```

1126.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

function InWSMizFileObj.Read_AttributePattern: AttributePatternPtr;
  var lPos: Position; lNr: integer; lArg: LocusPtr;
  begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]); NextElementState;
  lArg ← Read_Locus; result ← new(AttributePatternPtr, Init(lPos, lArg, lNr, Read_Loci));
  NextElementState;
  end;

```

1127.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

function InWSMizFileObj.Read_FunctorPattern: FunctorPatternPtr;
  var lPos, lRPos: Position; lNr, lRNr: integer; lArgs: PList;
  begin if nState = eStart then
    if nElName = FunctorPatternName[InfixFunctor] then
      begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]); NextElementState;
      lArgs ← Read_Loci; result ← new(InfixFunctorPatternPtr, Init(lPos, lArgs, lNr, Read_Loci));
      NextElementState;
      end
    else if nElName = FunctorPatternName[CircumfixFunctor] then
      begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]); NextElementState;
      lRNr ← GetIntAttr(XMLAttrName[atNr]); NextElementState; NextElementState;
      result ← new(CircumfixFunctorPatternPtr, Init(lPos, lNr, lRNr, Read_Loci)); NextElementState;
      end;
    end;
  end;

```

1128.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

function InWSMizFileObj.Read_PredicatePattern: PredicatePatternPtr;
  var lPos, lRPos: Position; lNr, lRNr: integer; lArgs: PList;
  begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]); NextElementState;
  lArgs ← Read_Loci; result ← new(PredicatePatternPtr, Init(lPos, lArgs, lNr, Read_Loci));
  NextElementState;
  end;

```

1129.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

function InWSMizFileObj.Read_Pattern: PatternPtr;
  begin case Str2PatterenKind(nElName) of
    itDefPred: result  $\leftarrow$  Read_PredicatePattern;
    itDefFunc: result  $\leftarrow$  Read_FunctorPattern;
    itDefMode: result  $\leftarrow$  Read_ModePattern;
    itDefAttr: result  $\leftarrow$  Read_AttributePattern;
  othercases if (nElName = FunctorPatternName[InfixFunctor])  $\vee$  (nElName =
    FunctorPatternName[CircumfixFunctor]) then result  $\leftarrow$  Read_FunctorPattern
  else result  $\leftarrow$  nil;
endcases;
end;

```


1130.

(Implementation for `wsmarticle.pas` 854) +≡

```

function InWSMizFileObj.Read_Definiens: DefiniensPtr;
  var lPos: Position; lKind, lShape: string; lLab: LabelPtr; lExpr: PObject; lExpKind: ExpKind;
      lList: PList; lOtherwise: DefExpressionPtr;
begin result ← nil;
if (nState = eStart) ∧ (nElName = XMLElemName[elDefiniens]) then
  begin lPos ← GetAttrPos; lKind ← GetAttr(XMLAttrName[atKind]);
    lShape ← GetAttr(XMLAttrName[atShape]); NextElementState; lLab ← Read_Label;
    if lKind = DefiniensKindName[SimpleDefiniens] then
      begin lExpKind ← exFormula;
        if lShape = ExpName[exTerm] then lExpKind ← exTerm;
        case lExpKind of
          exTerm: lExpr ← Read_Term;
          exFormula: lExpr ← Read_Formula;
        endcases;
        result ← new(SimpleDefiniensPtr, Init(lPos, lLab, new(DefExpressionPtr, Init(lExpKind, lExpr))));
      end
    else begin lList ← new(PList, Init(0));
      while (nState = eStart) ∧ (nElName = XMLElemName[elPartialDefiniens]) do
        begin NextElementState; lExpKind ← exFormula;
          if lShape = ExpName[exTerm] then lExpKind ← exTerm;
          case lExpKind of
            exTerm: lExpr ← Read_Term;
            exFormula: lExpr ← Read_Formula;
          endcases; lList↑.Insert(new(PartDefPtr, Init(new(DefExpressionPtr, Init(lExpKind, lExpr)),
            Read_Formula))); NextElementState;
          end;
        lOtherwise ← nil;
      if nState ≠ eEnd then
        begin lExpKind ← exFormula;
          if lShape = ExpName[exTerm] then lExpKind ← exTerm;
          case lExpKind of
            exTerm: lExpr ← Read_Term;
            exFormula: lExpr ← Read_Formula;
          endcases; lOtherwise ← new(DefExpressionPtr, Init(lExpKind, lExpr));
          end;
        result ← new(ConditionalDefiniensPtr, Init(lPos, lLab, lList, lOtherwise))
      end;
      NextElementState;
    end;
  end;
end;

```

1131.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```
function InWSMizFileObj.Read_Label: LabelPtr;
  var lLabPos: Position; lLabId: Integer;
  begin result ← nil;
  if (nState = eStart) ∧ (nElName = XMLElemName[elLabel]) then
    begin lLabId ← GetIntAttr(XMLAttrName[atIdNr]); lLabPos ← GetAttrPos; NextElementState;
    NextElementState; result ← new(LabelPtr, Init(lLabId, lLabPos));
    end;
  end;
```

1132.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```
function InWSMizFileObj.Read_Proposition: PropositionPtr;
  var lPos: Position; lLab: LabelPtr;
  begin NextElementState; lLab ← Read_label;
  result ← new(PropositionPtr, Init(lLab, Read_Formula, lPos)); NextElementState;
  end;
```

1133.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```
function InWSMizFileObj.Read_LocalReference: LocalReferencePtr;
  var lPos: Position; lNr: integer;
  begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atIdNr]); NextElementState;
  NextElementState; result ← new(LocalReferencePtr, Init(lNr, lPos));
  end;
```

1134.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```
function InWSMizFileObj.Read_References: PList;
  var lPos: Position; lNr, lFileNr: integer;
  begin result ← new(PList, Init(0));
  while nState ≠ eEnd do
    if nElName = ReferenceKindName[LocalReference] then
      begin result↑.Insert(Read_LocalReference)
      end
    else if nElName = ReferenceKindName[TheoremReference] then
      begin lPos ← GetAttrPos; lFileNr ← GetIntAttr(XMLAttrName[atNr]);
      lNr ← GetIntAttr(XMLAttrName[atNumber]); NextElementState; NextElementState;
      result↑.Insert(new(TheoremReferencePtr, Init(lFileNr, lNr, lPos)))
      end
    else if nElName = ReferenceKindName[DefinitionReference] then
      begin lPos ← GetAttrPos; lFileNr ← GetIntAttr(XMLAttrName[atNr]);
      lNr ← GetIntAttr(XMLAttrName[atNumber]); NextElementState; NextElementState;
      result↑.Insert(new(DefinitionReferencePtr, Init(lFileNr, lNr, lPos)))
      end;
  end;
```

1135.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

function InWSMizFileObj.Read_ReservationSegment: ReservationSegmentPtr;
  var lList: PList;
  begin lList ← new(PList, Init(0)); NextElementState; {elVariables}
  while (nState = eStart) ∧ (nElName = XMLElemName[elVariable]) do lList↑.Insert(Read_Variable);
  NextElementState; result ← new(ReservationSegmentPtr, Init(lList, Read_Type));
  end;

```

1136.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

function InWSMizFileObj.Read_SchemeNameInSchemeHead: SchemePtr;
  var lNr: Integer; lPos: Position;
  begin lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atIdNr]);
  result ← new(SchemePtr, Init(lNr, lPos, nil, nil, nil));
  end;

```

1137.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

function InWSMizFileObj.Read_CompactStatement: CompactStatementPtr;
  var lProp: PropositionPtr;
  begin lProp ← Read_Proposition; result ← new(CompactStatementPtr, Init(lProp, Read_Justification));
  end;

```

1138.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

function InWSMizFileObj.Read_StraightforwardJustification: StraightforwardJustificationPtr;
  var lPos, lLinkPos: Position; lLinked: boolean;
  begin lPos ← GetAttrPos; NextElementState; lLinked ← false; lLinkPos ← lPos;
  if nelName = XMLElemName[elLink] then
    begin lLinked ← true; lLinkPos ← GetAttrPos; NextElementState; NextElementState;
    end;
  result ← new(StraightforwardJustificationPtr, Init(lPos, lLinked, lLinkPos));
  StraightforwardJustificationPtr(result)↑.nReferences ← Read_References; NextElementState;
  end;

```

1139.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

function InWSMizFileObj.Read_SchemeJustification: SchemeJustificationPtr;
  var lInfPos, lPos: Position; lNr, lIdNr: integer;
  begin lInfPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]);
  lIdNr ← GetIntAttr(XMLAttrName[atIdNr]); lPos.Line ← GetIntAttr(XMLAttrName[atPosLine]);
  lPos.Col ← GetIntAttr(XMLAttrName[atPosCol]); NextElementState;
  result ← new(SchemeJustificationPtr, Init(lInfPos, lNr, lIdNr));
  SchemeJustificationPtr(result)↑.nSchemeInfPos ← lPos;
  SchemeJustificationPtr(result)↑.nReferences ← Read_References; NextElementState;
  end;

```

1140.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

function InWSMizFileObj.Read_Justification: JustificationPtr;
  var lPos: Position;
  begin if nState = eStart then
    if nElName = InferenceName[infStraightforwardJustification] then
      result ← Read_StraightforwardJustification
    else if nElName = InferenceName[infSchemeJustification] then result ← Read_SchemeJustification
    else if nElName = InferenceName[infError] then
      begin lPos ← GetAttrPos; NextElementState;
      result ← new(JustificationPtr, Init(infError, lPos)); NextElementState;
      end
    else if nElName = InferenceName[infSkippedProof] then
      begin lPos ← GetAttrPos; NextElementState;
      result ← new(JustificationPtr, Init(infSkippedProof, lPos)); NextElementState;
      end
    else result ← new(JustificationPtr, Init(infProof, CurPos));
  end;

```

1141.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

function InWSMizFileObj.Read_RegularStatement(const aShape: string): RegularStatementPtr;
  var lPos: Position; lIdNr: integer; lTrm: TermPtr; lCStm: CompactStatementPtr; lLab: LabelPtr;
  begin if aShape = RegularStatementName[stDiffuseStatement] then
    begin lLab ← Read_Label; result ← new(DiffuseStatementPtr, Init(lLab, stDiffuseStatement));
    end
  else if aShape = RegularStatementName[stCompactStatement] then
    begin result ← Read_CompactStatement;
    end
  else if aShape = RegularStatementName[stIterativeEquality] then
    begin lCStm ← Read_CompactStatement; result ← new(IterativeEqualityPtr,
      Init(lCStm↑.nProp, lCStm↑.nJustification, new(PList, Init(0))));
    while (nState = eStart) ∧ (nElName = XMLElemName[elIterativeStep]) do
      begin lPos ← GetAttrPos; NextElementState; lTrm ← Read_Term;
      IterativeEqualityPtr(result)↑.nIterSteps↑.Insert(new(IterativeStepPtr, Init(lPos, lTrm,
        Read_Justification))); NextElementState;
      end;
    end;
  end;

```

1142.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

procedure *InWSMizFileObj.Read_ItemContentsAttr*(*aItem* : *wsItemPtr*; **var** *aShape* : *string*);

begin *aShape* ← ``;

case *aItem*↑.*nItemKind* **of**

itIncorrItem : ;

itDefinition, *itSchemeBlock*, *itSchemeHead*, *itTheorem*, *itAxiom*, *itReservation* : ;

itSection : ;

itConclusion, *itRegularStatement* : *aShape* ← *GetAttr*(*XMLAttrName*[*atShape*]);

itChoice, *itReconsider*, *itPrivFuncDefinition*, *itPrivPredDefinition*, *itConstantDefinition*, *itGeneralization*,
 itLociDeclaration, *itExistentialAssumption*, *itExemplification*, *itPerCases*, *itCaseBlock* : ;

itCaseHead, *itSupposeHead*, *itAssumption* : ;

itCorrCond : *aItem*↑.*nContent* ← *new*(*CorrectnessConditionPtr*, *Init*(*CurPos*,
 Str2CorrectnessKind(*GetAttr*(*XMLAttrName*[*atCondition*])), **nil**));

itCorrectness : *aItem*↑.*nContent* ← *new*(*CorrectnessConditionsPtr*, *Init*(*CurPos*, [], **nil**));

itProperty : *aShape* ← *GetAttr*(*XMLAttrName*[*atProperty*]);

itDefFunc : *aShape* ← *GetAttr*(*XMLAttrName*[*atShape*]);

itDefPred, *itDefMode*, *itDefAttr*, *itDefStruct*, *itPredSynonym*, *itPredAntonym*, *itFuncNotation*,
 itModeNotation, *itAttrSynonym*, *itAttrAntonym*, *itCluster*, *itIdentify*, *itReduction* : ;

itPropertyRegistration : *aShape* ← *GetAttr*(*XMLAttrName*[*atProperty*]);

itPragma : *aItem*↑.*nContent* ← *new*(*PragmaPtr*, *Init*(*XMLToStr*(*GetAttr*(*XMLAttrName*[*atSpelling*]))));

endcases;

end;

1143.

(Implementation for `wsmarticle.pas` 854) +≡

```

procedure InWSMizFileObj.Read_ItemContents(aItem : wsItemPtr;
  const aShape : string);
var lList, lCons, lConds, lVars, lFields, lTyps, lSels : PList; lType : TypePtr; lNr : Integer;
  lVar : VariablePtr; lLocus : LocusPtr; lTrm : TermPtr; lPos, lFieldSgmPos : Position;
  lRedefinition : boolean; lPattern : PatternPtr; lDef : HowToDefine; lPropertySort : PropertyKind;
begin lPos ← CurPos;
case aItem↑.nItemKind of
  itIncorrItem : ;
  itDefinition : ;
  itSchemeBlock : ;
  itSchemeHead : begin aItem↑.nContent ← Read_SchemeNameInSchemeHead; NextElementState;
    NextElementState; NextElementState; { elSchematicVariables }
    lList ← new(PList, Init(0));
    while (nState = eStart) ∧ ((nElName = SchemeSegmentName[PredicateSegment]) ∨ (nElName =
      SchemeSegmentName[FunctorSegment])) do
      if nElName = SchemeSegmentName[PredicateSegment] then
        begin lPos ← GetAttrPos; NextElementState; lVars ← new(PList, Init(0)); NextElementState;
          { elVariables }
          while (nState = eStart) ∧ (nElName = XMLElemName[elVariable]) do
            lVars↑.Insert(Read_Variable);
            NextElementState;
            lList↑.Insert(new(PredicateSegmentPtr, Init(lPos, PredicateSegment, lVars, Read_TypeList)));
            NextElementState;
          end
        else begin lPos ← GetAttrPos; NextElementState; lVars ← new(PList, Init(0));
          NextElementState; { elVariables }
          while (nState = eStart) ∧ (nElName = XMLElemName[elVariable]) do
            lVars↑.Insert(Read_Variable);
            NextElementState; lTyps ← Read_TypeList; NextElementState;
            lList↑.Insert(new(FunctorSegmentPtr, Init(lPos, lVars, lTyps, Read_Type))); NextElementState;
            NextElementState;
          end;
        SchemePtr(aItem↑.nContent)↑.nSchemeParams ← lList; NextElementState;
          { elSchematicVariables }
        SchemePtr(aItem↑.nContent)↑.nSchemeConclusion ← Read_Formula; lConds ← new(PList, Init(0));
        if (nState = eStart) ∧ (nElName = XMLElemName[elProvisionalFormulas]) then
          begin NextElementState;
            while (nState = eStart) ∧ (nElName = XMLElemName[elProposition]) do
              lConds↑.Insert(Read_Proposition);
              NextElementState;
            end;
            SchemePtr(aItem↑.nContent)↑.nSchemePremises ← lConds;
          end;
        itTheorem : aItem↑.nContent ← Read_CompactStatement;
        itAxiom : begin end;
        itReservation : aItem↑.nContent ← Read_ReservationSegment;
        itSection : ;
        itChoice : begin lList ← new(PList, Init(0));
          while (nState = eStart) ∧ ((nElName = SegmentKindName[ikImplQualifiedSegm]) ∨ (nElName =
            SegmentKindName[ikExplQualifiedSegm])) do lList↑.Insert(Read_VariableSegment);

```

```

    NextElementState; lConds ← nil;
    if nElName = XMLElemName[elProposition] then
        begin lConds ← new(PList, Init(0));
        while (nState = eStart) ∧ (nElName = XMLElemName[elProposition]) do
            lConds↑.Insert(Read_Proposition);
        end;
        NextElementState; aItem↑.nContent ← new(ChoiceStatementPtr, Init(lList, lConds,
            SimpleJustificationPtr(Read_Justification)));
    end;
itReconsider: begin lList ← new(PList, Init(0));
    while (nState = eStart) ∧ ((nElName = XMLElemName[elEquality]) ∨ (nElName =
        XMLElemName[elVariable])) do
        if nElName = XMLElemName[elVariable] then
            lList↑.Insert(new(TypeChangePtr, Init(VariableIdentifier, Read_Variable, nil)))
        else begin NextElementState; lVar ← Read_Variable;
            lList↑.Insert(new(TypeChangePtr, Init(Equating, lVar, Read_Term))); NextElementState;
        end;
        lType ← Read_Type; aItem↑.nContent ← new(TypeChangingStatementPtr, Init(lList, lType,
            SimpleJustificationPtr(Read_Justification)));
    end;
itPrivFuncDefinition: begin lVar ← Read_Variable; lList ← Read_TypeList;
    aItem↑.nContent ← new(PrivateFunctorDefinitionPtr, Init(lVar, lList, Read_Term));
    end;
itPrivPredDefinition: begin lVar ← Read_Variable; lList ← Read_TypeList;
    aItem↑.nContent ← new(PrivatePredicateDefinitionPtr, Init(lVar, lList, Read_Formula));
    end;
itConstantDefinition: begin lVar ← Read_Variable;
    aItem↑.nContent ← new(ConstantDefinitionPtr, Init(lVar, Read_Term));
    end;
itLocDeclaration, itGeneralization: aItem↑.nContent ← Read_VariableSegment;
itPerCases: aItem↑.nContent ← Read_Justification;
itCaseBlock: ;
itCorrCond: begin CorrectnessConditionPtr(aItem↑.nContent)↑.nJustification ← Read_Justification;
    end;
itCorrectness: begin NextElementState;
    while (nState = eStart) ∧ (nElName = ItemName[itCorrectness]) do
        begin NextElementState; include(CorrectnessConditionsPtr(aItem↑.nContent)↑.nConditions,
            Str2CorrectnessKind(GetAttr(XMLAttrName[atCondition]))); NextElementState;
        end;
        NextElementState; CorrectnessConditionPtr(aItem↑.nContent)↑.nJustification ← Read_Justification;
    end;
itProperty:
    aItem↑.nContent ← new(PropertyPtr, Init(lPos, Str2PropertyKind(aShape), Read_Justification));
itConclusion, itRegularStatement: aItem↑.nContent ← Read_RegularStatement(aShape);
itCaseHead, itSupposeHead, itAssumption: if nState = eStart then
    if nElName = AssumptionKindName[SingleAssumption] then
        begin lPos ← GetAttrPos; NextElementState;
        aItem↑.nContent ← new(SingleAssumptionPtr, Init(lPos, Read_Proposition)); NextElementState;
        end
    else if nElName = AssumptionKindName[CollectiveAssumption] then
        begin lPos ← GetAttrPos; NextElementState;
        aItem↑.nContent ← new(CollectiveAssumptionPtr, Init(lPos, new(PList, Init(0))));
    end
end

```

```

    NextElementState;
    while (nState = eStart) ∧ (nElName = XMLElemName[elProposition]) do
        CollectiveAssumptionPtr(aItem↑.nContent)↑.nConditions↑.Insert(Read_Proposition);
        NextElementState; NextElementState;
    end;
itExistentialAssumption: begin aItem↑.nContent ← new(ExistentialAssumptionPtr, Init(lPos,
    new(PList, Init(0)), new(PList, Init(0))));
    while (nState = eStart) ∧ ((nElName = SegmentKindName[ikImplQualifiedSegm]) ∨ (nElName =
        SegmentKindName[ikExplQualifiedSegm])) do
        ExistentialAssumptionPtr(aItem↑.nContent)↑.nQVars↑.Insert(Read_VariableSegment);
        NextElementState;
    while (nState = eStart) ∧ (nElName = XMLElemName[elProposition]) do
        ExistentialAssumptionPtr(aItem↑.nContent)↑.nConditions↑.Insert(Read_Proposition);
        NextElementState;
    end;
itExemplification: begin lVar ← nil;
    if (nState = eStart) ∧ (nElName = XMLElemName[elVariable]) then lVar ← Read_Variable;
    lTrm ← nil;
    if nState ≠ eEnd then lTrm ← Read_Term;
    aItem↑.nContent ← new(ExamplePtr, Init(lVar, lTrm));
    end;
itDefPred: begin lRedefinition ← false;
    if (nState = eStart) ∧ (nElName = XMLElemName[elRedefine]) then
        begin NextElementState; NextElementState; lRedefinition ← true;
        end;
    lPattern ← Read_PredicatePattern; aItem↑.nContent ← new(PredicateDefinitionPtr, Init(lPos,
        lRedefinition, PredicatePatternPtr(lPattern), Read_Definiens));
    end;
itDefFunc: begin lRedefinition ← false;
    if (nState = eStart) ∧ (nElName = XMLElemName[elRedefine]) then
        begin NextElementState; NextElementState; lRedefinition ← true;
        end;
    lPattern ← Read_FunctorPattern; lType ← nil;
    if (nState = eStart) ∧ (nElName = XMLElemName[elTypeSpecification]) then
        begin NextElementState; lType ← Read_Type; NextElementState;
        end;
    if aShape = DefiningWayName[dfMeans] then lDef ← dfMeans
    else if aShape = DefiningWayName[dfEquals] then lDef ← dfEquals
    else lDef ← dfEmpty;
    case lDef of
    dfEquals: aItem↑.nContent ← new(FunctorDefinitionPtr, Init(lPos, lRedefinition,
        FunctorPatternPtr(lPattern), lType, lDef, Read_Definiens));
    dfMeans: aItem↑.nContent ← new(FunctorDefinitionPtr, Init(lPos, lRedefinition,
        FunctorPatternPtr(lPattern), lType, lDef, Read_Definiens));
    dfEmpty: aItem↑.nContent ← new(FunctorDefinitionPtr, Init(lPos, lRedefinition,
        FunctorPatternPtr(lPattern), lType, lDef, nil));
    endcases;
    end;
itDefMode: begin lRedefinition ← false;
    if (nState = eStart) ∧ (nElName = XMLElemName[elRedefine]) then
        begin NextElementState; NextElementState; lRedefinition ← true;
        end;
    end;

```



```

lPattern ← Read_ModePattern;
if (nState = eStart) ∧ (nElName = ModeDefinitionSortName[defExpandableMode]) then
  begin NextElementState; aItem↑.nContent ← new(ExpandableModeDefinitionPtr, Init(CurPos,
    ModePatternPtr(lPattern), Read_Type)); NextElementState;
  end
else if (nState = eStart) ∧ (nElName = ModeDefinitionSortName[defStandardMode]) then
  begin NextElementState; lType ← nil;
  if (nState = eStart) ∧ (nElName = XMLElemName[elTypeSpecification]) then
    begin NextElementState; lType ← Read_Type; NextElementState;
    end;
    aItem↑.nContent ← new(StandardModeDefinitionPtr, Init(CurPos, lRedefinition,
      ModePatternPtr(lPattern), lType, Read_Definiens)); NextElementState;
    end;
  end;
end;
itDefAttr: begin lRedefinition ← false;
  if (nState = eStart) ∧ (nElName = XMLElemName[elRedefine]) then
    begin NextElementState; NextElementState; lRedefinition ← true;
    end;
    lPattern ← Read_AttributePattern; aItem↑.nContent ← new(AttributeDefinitionPtr, Init(CurPos,
      lRedefinition, AttributePatternPtr(lPattern), Read_Definiens));
    end;
itDefStruct: begin NextElementState; lTyps ← new(PList, Init(0));
  while nState ≠ eEnd do lTyps↑.Insert(Read_Type);
  NextElementState; lPos ← GetAttrPos; lNr ← GetIntAttr(XMLAttrName[atNr]);
  NextElementState; lList ← nil;
  if (nState = eStart) ∧ (nElName = XMLElemName[elLoc]) then lList ← Read_Loci;
  lFields ← new(PList, Init(0));
  while (nState = eStart) ∧ (nElName = XMLElemName[elFieldSegment]) do
    begin lFieldSgmPos ← GetAttrPos; NextElementState; lSels ← new(PList, Init(0));
    while (nState = eStart) ∧ (nElName = XMLElemName[elSelector]) do
      begin lSels↑.Insert(new(FieldSymbolPtr, Init(GetAttrPos, GetIntAttr(XMLAttrName[atNr]))));
      NextElementState; NextElementState;
      end;
      lFields↑.Insert(new(FieldSegmentPtr, Init(lFieldSgmPos, lSels, Read_Type))); NextElementState;
    end;
  NextElementState;
  aItem↑.nContent ← new(StructureDefinitionPtr, Init(lPos, lTyps, lNr, lList, lFields));
  end;
itPredSynonym, itPredAntonym, itFuncNotation, itModeNotation, itAttrSynonym, itAttrAntonym: begin
  lPattern ← Read_Pattern; aItem↑.nContent ← new(NotationDeclarationPtr, Init(lPos,
    aItem↑.nItemKind, Read_Pattern, lPattern));
  end;
itCluster: if nState = eStart then
  if nElName = ClusterRegistrationName[ExistentialRegistration] then
    begin lPos ← GetAttrPos; NextElementState; lList ← Read_AdjectiveList;
    aItem↑.nContent ← new(EClusterPtr, Init(lPos, lList, Read_Type)); NextElementState;
    end
  else if nElName = ClusterRegistrationName[ConditionalRegistration] then
    begin lPos ← GetAttrPos; NextElementState; lList ← Read_AdjectiveList;
    lCons ← Read_AdjectiveList;
    aItem↑.nContent ← new(CClusterPtr, Init(lPos, lList, lCons, Read_Type)); NextElementState;
    end
  end

```

```

    else if  $nElName = ClusterRegistrationName[FunctorialRegistration]$  then
      begin  $lPos \leftarrow GetAttrPos$ ;  $NextElementState$ ;  $lTrm \leftarrow Read\_Term$ ;
       $lCons \leftarrow Read\_AdjectiveList$ ;  $lType \leftarrow nil$ ;
      if  $nState \neq eEnd$  then  $lType \leftarrow Read\_Type$ ;
       $aItem \uparrow.nContent \leftarrow new(FClusterPtr, Init(lPos, lTrm, lCons, lType)); NextElementState$ ;
      end;
    itIdentify: begin  $lPattern \leftarrow Read\_Pattern$ ;  $aItem \uparrow.nContent \leftarrow new(IdentifyRegistrationPtr,$ 
       $Init(lPos, Read\_Pattern, lPattern, new(PList, Init(0))))$ ;
    while  $(nState = eStart) \wedge (nElName = XMLElemName[elLocEquality])$  do
      begin  $lPos \leftarrow GetAttrPos$ ;  $NextElementState$ ;  $lLocus \leftarrow Read\_Locus$ ;
       $IdentifyRegistrationPtr(aItem \uparrow.nContent) \uparrow.nEqLocList \uparrow.Insert(new(LocEqualityPtr, Init(lPos,$ 
         $lLocus, Read\_Locus)))$ ;  $NextElementState$ ;
      end;
    end;
  end;
itPropertyRegistration: begin  $lPropertySort \leftarrow Str2PropertyKind(aShape)$ ;
  case  $lPropertySort$  of
    sySethood: begin
       $aItem \uparrow.nContent \leftarrow new(SethoodRegistrationPtr, Init(lPos, lPropertySort, Read\_Type))$ ;
       $SethoodRegistrationPtr(aItem \uparrow.nContent) \uparrow.nJustification \leftarrow Read\_Justification$ ;
      end;
    endcases;
  end;
itReduction: begin  $lTrm \leftarrow Read\_Term$ ;
   $aItem \uparrow.nContent \leftarrow new(ReduceRegistrationPtr, Init(lPos, Read\_Term, lTrm))$ ;
  end;
itPragma: ;
endcases;
end;

```

1144.

(Implementation for `wsmarticle.pas` 854) +≡

```

function InWSMizFileObj.Read_TextProper: wsTextProperPtr;
var  $lPos$ : Position;
begin  $NextElementState$ ;  $lPos.Line \leftarrow GetIntAttr(XMLAttrName[atLine])$ ;
 $lPos.Col \leftarrow GetIntAttr(XMLAttrName[atCol])$ ;  $result \leftarrow new(wsTextProperPtr,$ 
   $Init(GetAttr(XMLAttrName[atArticleID]), GetAttr(XMLAttrName[atArticleExt]), lPos))$ ;
if  $nDisplayInformationOnScreen$  then  $DisplayLine(result \uparrow.nBlockPos.Line, 0)$ ;
 $CurPos \leftarrow result \uparrow.nBlockPos$ ;
if  $(nState = eStart) \wedge (nElName = BlockName[blMain])$  then
  begin  $NextElementState$ ;
  while  $(nState = eStart) \wedge (nElName = XMLElemName[elItem])$  do
     $result \uparrow.nItems \uparrow.Insert(Read\_Item)$ ;
  end;
 $NextElementState$ ;
end;

```

1145.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

function InWSMizFileObj.Read_Block: wsBlockPtr;
  var lPos: Position;
  begin lPos.Line ← GetIntAttr(XMLAttrName[atLine]);
  lPos.Col ← GetIntAttr(XMLAttrName[atCol]);
  result ← new(WSBlockPtr, Init(Str2BlockKind(GetAttr(XMLAttrName[atKind])), lPos));
  if nDisplayInformationOnScreen then DisplayLine(result↑.nBlockPos.Line, 0);
  lPos.Line ← GetIntAttr(XMLAttrName[atPosLine]);
  lPos.Col ← GetIntAttr(XMLAttrName[atPosCol]); result↑.nBlockEndPos ← lPos;
  CurPos ← result↑.nBlockPos; NextElementState;
  while (nState = eStart) ∧ (nElName = XMLElemName[elItem]) do result↑.nItems↑.Insert(Read_Item);
  CurPos ← result↑.nBlockEndPos; NextElementState;
end;

```

1146.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

function InWSMizFileObj.Read_Item: wsItemPtr;
  var lStartTagNbr: integer; lItemKind: ItemKind; lShape: string; lPos: Position;
  begin lItemKind ← Str2ItemKind(GetAttr(XMLAttrName[atKind]));
  lPos.Line ← GetIntAttr(XMLAttrName[atLine]); lPos.Col ← GetIntAttr(XMLAttrName[atCol]);
  CurPos ← lPos;
  if nDisplayInformationOnScreen then DisplayLine(lPos.Line, 0);
  result ← new(WSItemPtr, Init(lItemKind, lPos)); lPos.Line ← GetIntAttr(XMLAttrName[atPosLine]);
  lPos.Col ← GetIntAttr(XMLAttrName[atPosCol]); result↑.nItemEndPos ← lPos;
  result↑.nContent ← nil; Read_ItemContentsAttr(result, lShape); NextElementState; lStartTagNbr ← 0;
  if nState ≠ eEnd then
    begin Read_ItemContents(result, lShape);
    if (nState = eStart) ∧ (nElName = XMLElemName[elBlock]) then result↑.nBlock ← Read_Block
    else if result↑.nContent = nil then
      begin repeat if nState = eStart then inc(lStartTagNbr)
        else dec(lStartTagNbr);
        NextElementState;
      until ((nState = eEnd) ∧ (lStartTagNbr = 0)) ∨ ((nState = eStart) ∧ (nElName =
        XMLElemName[elBlock]));
      if (nState = eStart) ∧ (nElName = XMLElemName[elBlock]) then result↑.nBlock ← Read_Block;
      end;
    end;
  CurPos ← lPos; NextElementState;
end;

```

1147.

⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

function Read_WSMizArticle(aFileName : string): wsTextProperPtr;
  var lInFile: InWSMizFilePtr;
  begin InitWSLookupTables; lInFile ← new(InWSMizFilePtr, OpenFile(aFileName));
  result ← lInFile↑.Read_TextProper; dispose(lInFile, Done); DisposeWSLookupTables;
end;

```

Section 21.13. PRETTYPRINTING WSM FILES (DEFERRED)

1148.

```

{Publicly declared types in wsmarticle.pas 852} +≡
  WSMizarPrinterPtr = ↑WSMizarPrinterObj;
  WSMizarPrinterObj = object (TXTStreamObj)
    nDisplayInformationOnScreen: boolean;
    nIndent: integer; { indenting }
    constructor OpenFile(const aFileName: string);
    destructor Done; virtual;
    procedure Print_Char(AChar : char);
    procedure Print_NewLine;
    procedure Print_Number(const aNumber: integer);
    procedure Print_String(const aString: string);
    procedure Print_Indent;
    procedure Print_TextProper(aWSTextProper : WSTextProperPtr); virtual;
    procedure Print_Item(aWSItem : WSItemPtr); virtual;
    procedure Print_SchemeNameInSchemeHead(aSch : SchemePtr); virtual;
    procedure Print_Block(aWSBlock : WSBlockPtr); virtual;
    procedure Print_Adjective(aAttr : AdjectiveExpressionPtr); virtual;
    procedure Print_AdjectiveList(aCluster : PList); virtual;
    procedure Print_Variable(aVar : VariablePtr); virtual;
    procedure Print_ImplicitlyQualifiedVariable(aSegm : ImplicitlyQualifiedSegmentPtr); virtual;
    procedure Print_VariableSegment(aSegm : QualifiedSegmentPtr); virtual;
    procedure Print_Type(aTyp : TypePtr); virtual;
    procedure Print_BinaryFormula(aFrm : BinaryFormulaPtr); virtual;
    procedure Print_PrivatePredicativeFormula(aFrm : PrivatePredicativeFormulaPtr); virtual;
    procedure Print_Formula(aFrm : FormulaPtr); virtual;
    procedure Print_OpenTermList(aTrmList : PList); virtual;
    procedure Print_TermList(aTrmList : PList); virtual;
    procedure Print_SimpleTermTerm(aTrm : SimpleTermPtr); virtual;
    procedure Print_PrivateFunctorTerm(aTrm : PrivateFunctorTermPtr); virtual;
    procedure Print_Term(aTrm : TermPtr); virtual;
    procedure Print_TypeList(aTypeList : PList); virtual;
    procedure Print_Label(aLab : LabelPtr); virtual;
    procedure Print_Reference(aRef : LocalReferencePtr); virtual;
    procedure Print_References(aRefs : PList); virtual;
    procedure Print_StraightforwardJustification(aInf : StraightforwardJustificationPtr); virtual;
    procedure Print_SchemeNameInJustification(aInf : SchemeJustificationPtr); virtual;
    procedure Print_SchemeJustification(aInf : SchemeJustificationPtr); virtual;
    procedure Print_Justification(aInf : JustificationPtr; aBlock : wsBlockPtr); virtual;
    procedure Print_Linkage; virtual;
    procedure Print_RegularStatement(aRStm : RegularStatementPtr; aBlock : wsBlockPtr); virtual;
    procedure Print_CompactStatement(aCStm : CompactStatementPtr; aBlock : wsBlockPtr); virtual;
    procedure Print_Proposition(aProp : PropositionPtr); virtual;
    procedure Print_Conditions(aCond : PList);
    procedure Print_AssumptionConditions(aCond : AssumptionPtr); virtual;
    procedure Print_Pattern(aPattern : PatternPtr); virtual;
    procedure Print_Locus(aLocus : LocusPtr); virtual;
    procedure Print_Loci(aLoci : PList); virtual;
    procedure Print_Definiens(aDef : DefiniensPtr); virtual;
    procedure Print_ReservedType(aResType : TypePtr); virtual;
  end ;

```

1149. Constructor.

⟨Implementation for `wsmarticle.pas 854`⟩ +≡
constructor *WSMizarPrinterObj.OpenFile*(**const** *aFileName*: *string*);
 begin *inherited InitFile*(*AFileName*); *rewrite*(*nFile*); *nIndent* ← 0;
 nDisplayInformationOnScreen ← *false*;
 end;
destructor *WSMizarPrinterObj.Done*;
 begin *close*(*nFile*); *inherited Done*;
 end;

1150. ⟨Implementation for `wsmarticle.pas 854`⟩ +≡
procedure *WSMizarPrinterObj.Print_Char*(*aChar* : *char*);
 begin *write*(*nFile*, *aChar*);
 end;

1151. ⟨Implementation for `wsmarticle.pas 854`⟩ +≡
procedure *WSMizarPrinterObj.Print_NewLine*;
 begin *writeln*(*nFile*);
 end;

1152. ⟨Implementation for `wsmarticle.pas 854`⟩ +≡
procedure *WSMizarPrinterObj.Print_Number*(**const** *aNumber*: *integer*);
 begin *write*(*nFile*, *aNumber*); *Print_Char*(‘␣’);
 end;

1153. The comment is translated from the Polish comment “?? czy na pewno trzeba robic konwersje”, so I may be mistranslating.

⟨Implementation for `wsmarticle.pas 854`⟩ +≡
procedure *WSMizarPrinterObj.Print_String*(**const** *aString*: *string*);
 var *i*: *integer*;
 begin *write*(*nFile*, *XMLToStr*(*aString*)); { Do you really need to do conversions? }
 Print_Char(‘␣’);
 end;

1154. ⟨Implementation for `wsmarticle.pas 854`⟩ +≡
procedure *WSMizarPrinterObj.Print_Indent*;
 var *i*: *integer*;
 begin for *i* ← 1 **to** *nIndent* **do** *Print_Char*(‘␣’);
 end;

1155. ⟨Implementation for `wsmarticle.pas 854`⟩ +≡
procedure *WSMizarPrinterObj.Print_Adjective*(*aAttr* : *AdjectiveExpressionPtr*);
 begin case *aAttr*↑.*nAdjectiveSort* **of**
 wsAdjective: **with** *AdjectivePtr*(*aAttr*)↑ **do**
 begin if *nArgs*↑.*Count* ≠ 0 **then** *Print_TermList*(*nArgs*);
 Print_String(*AttributeName*[*nAdjectiveSymbol*]);
 end;
 wsNegatedAdjective: **begin** *Print_String*(*TokenName*[*sy_Non*]);
 Print_Adjective(*NegatedAdjectivePtr*(*aAttr*)↑.*nArg*);
 end;
 endcases;
end;

1156. \langle Implementation for `wsmarticle.pas` 854 $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_AdjectiveList(aCluster : PList);
  var i: integer;
  begin with aCluster $\uparrow$  do
    for i  $\leftarrow$  0 to Count - 1 do
      begin Print_Adjective(Items $\uparrow$ [i]);
      end;
    end;

```

1157. \langle Implementation for `wsmarticle.pas` 854 $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_Variable(aVar : VariablePtr);
  begin with aVar $\uparrow$  do
    begin Print_String(IdentRepr(nIdent));
    end;
  end;

```

1158. \langle Implementation for `wsmarticle.pas` 854 $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_ImplicitlyQualifiedVariable(aSegm : ImplicitlyQualifiedSegmentPtr);
  begin Print_Variable(aSegm $\uparrow$ .nIdentifier);
  end;

```

1159. \langle Implementation for `wsmarticle.pas` 854 $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_VariableSegment(aSegm : QualifiedSegmentPtr);
  var i: integer;
  begin case aSegm $\uparrow$ .nSegmentSort of
    ikImplQualifiedSegm: Print_ImplicitlyQualifiedVariable(ImplicitlyQualifiedSegmentPtr(aSegm));
    ikExplQualifiedSegm: with ExplicitlyQualifiedSegmentPtr(aSegm) $\uparrow$  do
      begin Print_Variable(nIdentifiers.Items $\uparrow$ [0]);
      for i  $\leftarrow$  1 to nIdentifiers $\uparrow$ .Count - 1 do
        begin Print_String( $\cdot$ ,  $\cdot$ ); Print_Variable(nIdentifiers $\uparrow$ .Items $\uparrow$ [i]);
        end;
      Print_String(TokenName[sy_Be]); Print_Type(nType);
      end;
    endcases;
  end;

```

1160. \langle Implementation for `wsmarticle.pas` 854 $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_OpenTermList(aTrmList : PList);
  var i: integer;
  begin if aTrmList $\uparrow$ .Count > 0 then
    begin Print_Term(aTrmList $\uparrow$ .Items $\uparrow$ [0]);
    for i  $\leftarrow$  1 to aTrmList $\uparrow$ .Count - 1 do
      begin Print_String( $\cdot$ ,  $\cdot$ ); Print_Term(aTrmList $\uparrow$ .Items $\uparrow$ [i]);
      end;
    end;
  end;

```

1161. ⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

procedure WSMizarPrinterObj.Print_TermList(aTrmList : PList);
  var i: integer;
  begin if aTrmList↑.Count > 0 then
    begin Print_String(' '); Print_Term(aTrmList↑.Items↑[0]);
    for i ← 1 to aTrmList↑.Count - 1 do
      begin Print_String(' '); Print_Term(aTrmList↑.Items↑[i]);
      end;
    Print_String(' ');
  end;
end;

```

1162. ⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

procedure WSMizarPrinterObj.Print_Type(aTyp : TypePtr);
  begin with aTyp↑ do
    begin case aTyp↑.nTypeSort of
      wsStandardType: with StandardTypePtr(aTyp)↑ do
        begin if nArgs↑.Count = 0 then Print_String(ModeName[nModeSymbol])
        else begin Print_String(' '); Print_String(ModeName[nModeSymbol]);
          Print_String(TokenName[sy_Of]); Print_OpenTermList(nArgs); Print_String(' ');
        end;
      end;
      wsStructureType: with StructTypePtr(aTyp)↑ do
        begin if nArgs↑.Count = 0 then Print_String(StructureName[nStructSymbol])
        else begin Print_String(' '); Print_String(StructureName[nStructSymbol]);
          Print_String(TokenName[sy_Over]); Print_OpenTermList(nArgs); Print_String(' ');
        end;
      end;
      wsClusteredType: with ClusteredTypePtr(aTyp)↑ do
        begin Print_AdjectiveList(nAdjectiveCluster); Print_Type(nType);
        end;
      wsErrorType: begin end;
    endcases;
  end;
end;

```

1163. ⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

procedure WSMizarPrinterObj.Print_BinaryFormula(aFrm : BinaryFormulaPtr);
  begin Print_String(' '); Print_Formula(aFrm↑.nLeftArg);
  case aFrm↑.nFormulaSort of
    wsConjunctiveFormula: Print_String(TokenName[sy_Ampersand]);
    wsDisjunctiveFormula: Print_String(TokenName[sy_Or]);
    wsConditionalFormula: Print_String(TokenName[sy_Implies]);
    wsBiconditionalFormula: Print_String(TokenName[sy_Iff]);
    wsFlexaryConjunctiveFormula: begin Print_String(TokenName[sy_Ampersand]);
      Print_String(TokenName[sy_Ellipsis]); Print_String(TokenName[sy_Ampersand]);
    end;
    wsFlexaryDisjunctiveFormula: begin Print_String(TokenName[sy_Or]);
      Print_String(TokenName[sy_Ellipsis]); Print_String(TokenName[sy_Or]);
    end;
  endcases; Print_Formula(aFrm↑.nRightArg); Print_String(' ');
end;

```


1164. \langle Implementation for `wsmarticle.pas` 854 $\rangle + \equiv$

```
procedure WSMizarPrinterObj.Print_PrivatePredicativeFormula(aFrm : PrivatePredicativeFormulaPtr);
begin with PrivatePredicativeFormulaPtr(aFrm) $\uparrow$  do
  begin Print_String(IdentRepr(nPredIdNr)); Print_String('['); Print_OpenTermList(nArgs);
    Print_String(']');
  end;
end;
```

1165. \langle Implementation for `wsmarticle.pas` 854 $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_Formula(aFrm : FormulaPtr);
  var i: Integer; lNeg: boolean; lFrm: FormulaPtr;
  begin case aFrm↑.nFormulaSort of
    wsNegatedFormula: begin Print_String(TokenName[sy_Not]);
      Print_Formula(NegativeFormulaPtr(aFrm)↑.nArg);
    end;
    wsConjunctiveFormula, wsDisjunctiveFormula, wsConditionalFormula,
      wsBiconditionalFormula, wsFlexaryConjunctiveFormula, wsFlexaryDisjunctiveFormula:
      Print_BinaryFormula(BinaryFormulaPtr(aFrm));
    wsPredicativeFormula: with PredicativeFormulaPtr(aFrm)↑ do
      begin Print_String(`(`);
      if nLeftArgs↑.Count  $\neq$  0 then
        begin Print_OpenTermList(nLeftArgs);
        end;
        Print_String(PredicateName[nPredNr]);
      if nRightArgs↑.Count  $\neq$  0 then
        begin Print_OpenTermList(nRightArgs);
        end;
        Print_String(`)`);
      end;
    wsMultiPredicativeFormula: with MultiPredicativeFormulaPtr(aFrm)↑ do
      begin Print_String(`(`); lFrm ← nScraps.Items↑[0];
      lNeg ← lFrm↑.nFormulaSort = wsNegatedFormula;
      if lNeg then lFrm ← NegativeFormulaPtr(lFrm)↑.nArg;
      with PredicativeFormulaPtr(lFrm)↑ do
        begin if nLeftArgs↑.Count  $\neq$  0 then Print_OpenTermList(nLeftArgs);
        if lNeg then
          begin Print_String(TokenName[sy_Does]); Print_String(TokenName[sy_Not]);
          end;
          Print_String(PredicateName[nPredNr]);
        if nRightArgs↑.Count  $\neq$  0 then Print_OpenTermList(nRightArgs);
        end;
        for i ← 1 to nScraps.Count − 1 do
          begin lFrm ← nScraps.Items↑[i]; lNeg ← lFrm↑.nFormulaSort = wsNegatedFormula;
          if lNeg then lFrm ← NegativeFormulaPtr(lFrm)↑.nArg;
          with RightSideOfPredicativeFormulaPtr(lFrm)↑ do
            begin if lNeg then
              begin Print_String(TokenName[sy_Does]); Print_String(TokenName[sy_Not]);
              end;
              Print_String(PredicateName[nPredNr]);
            if nRightArgs↑.Count  $\neq$  0 then Print_OpenTermList(nRightArgs);
            end;
            end;
            Print_String(`)`);
          end;
        end;
      end;
    wsPrivatePredicateFormula: Print_PrivatePredicativeFormula(PrivatePredicativeFormulaPtr(aFrm));
    wsAttributiveFormula: with AttributiveFormulaPtr(aFrm)↑ do
      begin Print_String(`(`); Print_Term(nSubject); Print_String(TokenName[sy_Is]);
      Print_AdjectiveList(nAdjectives); Print_String(`)`);
      end;
    wsQualifyingFormula: with QualifyingFormulaPtr(aFrm)↑ do

```

```

begin Print_String(`(`); Print_Term(nSubject); Print_String(TokenName[sy_Is]);
Print_Type(nType); Print_String(`)`);
end;
wsUniversalFormula: with QuantifiedFormulaPtr(aFrm)↑ do
begin Print_String(`(`); Print_String(TokenName[sy_For]);
Print_VariableSegment(QuantifiedFormulaPtr(aFrm)↑.nSegment);
Print_String(TokenName[sy_Holds]); Print_Formula(QuantifiedFormulaPtr(aFrm)↑.nScope);
Print_String(`)`);
end;
wsExistentialFormula: with QuantifiedFormulaPtr(aFrm)↑ do
begin Print_String(`(`); Print_String(TokenName[sy_Ex]);
Print_VariableSegment(QuantifiedFormulaPtr(aFrm)↑.nSegment); Print_String(TokenName[sy_St]);
Print_Formula(QuantifiedFormulaPtr(aFrm)↑.nScope); Print_String(`)`);
end;
wsContradiction: begin Print_String(TokenName[sy_Contradiction]);
end;
wsThesis: begin Print_String(TokenName[sy_Thesis]);
end;
wsErrorFormula: begin end;
endcases;
end;

```

1166. ⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

procedure WSMizarPrinterObj.Print_SimpleTermTerm(aTrm : SimpleTermPtr);
begin Print_String(IdentRepr(SimpleTermPtr(aTrm)↑.nIdent));
end;

```

1167. ⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

procedure WSMizarPrinterObj.Print_PrivateFunctorTerm(aTrm : PrivateFunctorTermPtr);
begin Print_String(IdentRepr(aTrm↑.nFunctorIdent)); Print_String(`(`);
Print_OpenTermList(aTrm↑.nArgs); Print_String(`)`);
end;

```

1168. \langle Implementation for `wsmarticle.pas` 854 $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_Term(aTrm : TermPtr);
  var i, j: integer; lPrintWhere: boolean;
  begin case aTrm↑.nTermSort of
    wsPlaceholderTerm: begin Print_Char( '$' ); Print_Number( PlaceholderTermPtr(aTrm)↑.nLocusNr );
      end;
    wsSimpleTerm: begin Print_SimpleTermTerm( SimpleTermPtr(aTrm) );
      end;
    wsNumeralTerm: begin Print_Number( NumeralTermPtr(aTrm)↑.nValue );
      end;
    wsInfixTerm: with InfixTermPtr(aTrm)↑ do
      begin Print_String( '(' );
      if nLeftArgs↑.Count  $\neq$  0 then
        begin Print_TermList( nLeftArgs );
        end;
      Print_String( FunctorName[ nFunctorSymbol ] );
      if nRightArgs↑.Count  $\neq$  0 then
        begin Print_TermList( nRightArgs );
        end;
      Print_String( ')' );
      end;
    wsCircumfixTerm: with CircumfixTermPtr(aTrm)↑ do
      begin Print_String( LeftBracketName[ nLeftBracketSymbol ] ); Print_OpenTermList( nArgs );
      Print_String( RightBracketName[ nRightBracketSymbol ] );
      end;
    wsPrivateFunctorTerm: Print_PrivateFunctorTerm( PrivateFunctorTermPtr(aTrm) );
    wsAggregateTerm: with AggregateTermPtr(aTrm)↑ do
      begin Print_String( StructureName[ nStructSymbol ] );
      Print_String( TokenName[ sy_StructLeftBracket ] ); Print_OpenTermList( nArgs );
      Print_String( TokenName[ sy_StructRightBracket ] );
      end;
    wsSelectorTerm: with SelectorTermPtr(aTrm)↑ do
      begin Print_String( '(' ); Print_String( TokenName[ sy_The ] );
      Print_String( SelectorName[ nSelectorSymbol ] ); Print_String( TokenName[ sy_Of ] );
      Print_Term( nArg ); Print_String( ')' );
      end;
    wsInternalSelectorTerm: with InternalSelectorTermPtr(aTrm)↑ do
      begin Print_String( TokenName[ sy_The ] ); Print_String( SelectorName[ nSelectorSymbol ] );
      end;
    wsForgetfulFunctorTerm: with ForgetfulFunctorTermPtr(aTrm)↑ do
      begin Print_String( '(' ); Print_String( TokenName[ sy_The ] );
      Print_String( StructureName[ nStructSymbol ] ); Print_String( TokenName[ sy_Of ] );
      Print_Term( nArg ); Print_String( ')' );
      end;
    wsInternalForgetfulFunctorTerm: with InternalForgetfulFunctorTermPtr(aTrm)↑ do
      begin Print_String( '(' ); Print_String( TokenName[ sy_The ] );
      Print_String( StructureName[ nStructSymbol ] ); Print_String( ')' );
      end;
    wsFraenkelTerm: with FraenkelTermPtr(aTrm)↑ do
      begin Print_String( '{' ); Print_Term( nSample );
      if nPostqualification↑.Count > 0 then
        begin lPrintWhere  $\leftarrow$  true;

```

```

for  $i \leftarrow 0$  to  $nPostqualification \uparrow .Count - 1$  do
  case  $QualifiedSegmentPtr(nPostqualification \uparrow .Items \uparrow [i]) \uparrow .nSegmentSort$  of
     $ikImplQualifiedSegm$ : with  $ImplicitlyQualifiedSegmentPtr(nPostqualification \uparrow .Items \uparrow [i]) \uparrow$  do
      begin  $Print\_String(TokenName[sy\_Where])$ ;  $Print\_Variable(nIdentifier)$ ;
      end;
     $ikExplQualifiedSegm$ : with  $ExplicitlyQualifiedSegmentPtr(nPostqualification \uparrow .Items \uparrow [i]) \uparrow$  do
      begin if  $lPrintWhere$  then
        begin  $Print\_String(TokenName[sy\_Where])$ ;  $lPrintWhere \leftarrow false$ ;
        end;
       $Print\_Variable(nIdentifiers.Items \uparrow [0])$ ;
      for  $j \leftarrow 1$  to  $nIdentifiers \uparrow .Count - 1$  do
        begin  $Print\_String( ', ' )$ ;  $Print\_Variable(nIdentifiers \uparrow .Items \uparrow [j])$ ;
        end;
       $Print\_String(TokenName[sy\_Is])$ ;  $Print\_Type(nType)$ ;
      if  $i < nPostqualification \uparrow .Count - 1$  then  $Print\_String( ', ' )$ ;
      end;
    endcases;
  end;
   $Print\_String( ': ' )$ ;  $Print\_Formula(nFormula)$ ;  $Print\_String( ' } ' )$ ;
end;
 $wsSimpleFraenkelTerm$ : with  $SimpleFraenkelTermPtr(aTrm) \uparrow$  do
  begin  $Print\_String( ' ( ' )$ ;  $Print\_String(TokenName[sy\_The])$ ;  $Print\_String(TokenName[sy\_Set])$ ;
   $Print\_String(TokenName[sy\_Of])$ ;  $Print\_String(TokenName[sy\_All])$ ;  $Print\_Term(nSample)$ ;
  if  $nPostqualification \uparrow .Count > 0$  then
    begin  $lPrintWhere \leftarrow true$ ;
    for  $i \leftarrow 0$  to  $nPostqualification \uparrow .Count - 1$  do
      case  $QualifiedSegmentPtr(nPostqualification \uparrow .Items \uparrow [i]) \uparrow .nSegmentSort$  of
         $ikImplQualifiedSegm$ : with  $ImplicitlyQualifiedSegmentPtr(nPostqualification \uparrow .Items \uparrow [i]) \uparrow$  do
          begin  $Print\_String(TokenName[sy\_Where])$ ;  $Print\_Variable(nIdentifier)$ ;
          end;
         $ikExplQualifiedSegm$ : with  $ExplicitlyQualifiedSegmentPtr(nPostqualification \uparrow .Items \uparrow [i]) \uparrow$  do
          begin if  $lPrintWhere$  then
            begin  $Print\_String(TokenName[sy\_Where])$ ;  $lPrintWhere \leftarrow false$ ;
            end;
           $Print\_Variable(nIdentifiers.Items \uparrow [0])$ ;
          for  $j \leftarrow 1$  to  $nIdentifiers \uparrow .Count - 1$  do
            begin  $Print\_String( ', ' )$ ;  $Print\_Variable(nIdentifiers \uparrow .Items \uparrow [j])$ ;
            end;
           $Print\_String(TokenName[sy\_Is])$ ;  $Print\_Type(nType)$ ;
          if  $i < nPostqualification \uparrow .Count - 1$  then  $Print\_String( ', ' )$ ;
          end;
        endcases;
      end;
     $Print\_String( ' ) ' )$ ;
  end;
 $wsQualificationTerm$ : with  $QualifiedTermPtr(aTrm) \uparrow$  do
  begin  $Print\_String( ' ( ' )$ ;  $Print\_Term(nSubject)$ ;  $Print\_String(TokenName[sy\_Qua])$ ;
   $Print\_Type(nQualification)$ ;  $Print\_String( ' ) ' )$ ;
  end;
 $wsExactlyTerm$ : with  $ExactlyTermPtr(aTrm) \uparrow$  do
  begin  $Print\_Term(nSubject)$ ;  $Print\_String(TokenName[sy\_Exactly])$ ;
  end;

```

```

wsGlobalChoiceTerm: begin Print_String(`(`); Print_String(TokenName[sy_The]);
  Print_Type(ChoiceTermPtr(aTrm)↑.nChoiceType); Print_String(`)`);
end;
wsItTerm: begin Print_String(TokenName[sy_It]);
end;
wsErrorTerm:
endcases;
end;

```

1169. ⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

procedure WSMizarPrinterObj.Print_TypeList(aTypeList : PList);
var i: integer;
begin if aTypeList↑.Count > 0 then
  begin Print_Type(aTypeList↑.Items↑[0]);
  for i ← 1 to aTypeList↑.Count - 1 do
    begin Print_String(`,`); Print_Type(aTypeList↑.Items↑[i]);
    end;
  end;
end;

```

1170. ⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

procedure WSMizarPrinterObj.Print_Label(aLab : LabelPtr);
begin if (aLab ≠ nil) ∧ (aLab.nLabelIdNr > 0) then
  begin Print_String(IdentRepr(aLab↑.nLabelIdNr)); Print_String(`:`);
  end;
end;

```

1171. ⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

procedure WSMizarPrinterObj.Print_Proposition(aProp : PropositionPtr);
begin Print_Label(aProp↑.nLab); Print_Formula(aProp↑.nSentence);
end;

```

1172. ⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

procedure WSMizarPrinterObj.Print_CompactStatement(aCStm : CompactStatementPtr;
  aBlock : wsBlockPtr);
begin with aCStm↑ do
  begin Print_Proposition(nProp); Print_Justification(nJustification, aBlock);
  end;
end;

```

1173. ⟨Implementation for `wsmarticle.pas` 854⟩ +≡

```

procedure WSMizarPrinterObj.Print_Linkage;
begin Print_String(TokenName[sy_Then]);
end;

```

1174. \langle Implementation for `wsmarticle.pas` 854 $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_RegularStatement(aRStm : RegularStatementPtr;
  aBlock : wsBlockPtr);
  var i: integer;
  begin case aRStm↑.nStatementSort of
    stDiffuseStatement: begin Print_Label(DiffuseStatementPtr(aRStm)↑.nLab); Print_Block(aBlock);
      end;
    stCompactStatement: begin
      if (CompactStatementPtr(aRStm)↑.nJustification↑.nInfSort = infStraightforwardJustification) ∧
        StraightforwardJustificationPtr(CompactStatementPtr(aRStm)↑.nJustification)↑.nLinked then
        begin Print_Linkage;
          end;
        Print_CompactStatement(CompactStatementPtr(aRStm), aBlock);
      end;
    stIterativeEquality: begin
      if (CompactStatementPtr(aRStm)↑.nJustification↑.nInfSort = infStraightforwardJustification) ∧
        StraightforwardJustificationPtr(CompactStatementPtr(aRStm)↑.nJustification)↑.nLinked then
        begin Print_Linkage;
          end;
        Print_CompactStatement(CompactStatementPtr(aRStm), nil);
      with IterativeEqualityPtr(aRStm)↑ do
        for i ← 0 to nIterSteps↑.Count − 1 do
          with IterativeStepPtr(nIterSteps↑.Items↑[i])↑ do
            begin Print_NewLine; Print_String(TokenName[sy_DotEquals]); Print_Term(nTerm);
              Print_Justification(nJustification, nil);
            end;
          end;
        endcases;
      end;
  end;

```

1175. \langle Implementation for `wsmarticle.pas` 854 $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_Reference(aRef : LocalReferencePtr);
  begin Print_String(IdentRepr(aRef↑.nLabId));
  end;

```

1176. \langle Implementation for `wsmarticle.pas` 854 $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_References(aRefs : PList);
  var i: integer;
  begin for i  $\leftarrow$  0 to aRefs.Count - 1 do
    with ReferencePtr(aRefs.Items[i]) do
      begin case nRefSort of
        LocalReference: begin Print_Reference(aRefs.Items[i]);
          end;
        TheoremReference: begin
          Print_String(MMLIdentifierName[TheoremReferencePtr(aRefs.Items[i]).nArticleNr]);
          Print_String(':'); Print_Number(TheoremReferencePtr(aRefs.Items[i]).nTheoNr);
          end;
        DefinitionReference: begin
          Print_String(MMLIdentifierName[DefinitionReferencePtr(aRefs.Items[i]).nArticleNr]);
          Print_String(':'); Print_String('def');
          Print_Number(DefinitionReferencePtr(aRefs.Items[i]).nDEfNr);
          end;
      endcases;
      if i < aRefs.Count - 1 then Print_String(' , ');
      end;
    end;

```

1177. \langle Implementation for `wsmarticle.pas` 854 $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_StraightforwardJustification(aInf : StraightforwardJustificationPtr);
  begin with aInf do
    begin if nReferences.Count  $\neq$  0 then
      begin Print_String(TokenName[sy_By]); Print_References(nReferences);
      end;
    end;
  end;

```

1178. \langle Implementation for `wsmarticle.pas` 854 $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_SchemeNameInJustification(aInf : SchemeJustificationPtr);
  begin Print_String(IdentRepr(aInf.nSchemeIdNr));
  end;

```

1179. \langle Implementation for `wsmarticle.pas` 854 $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_SchemeJustification(aInf : SchemeJustificationPtr);
  begin with aInf do
    begin Print_String(TokenName[sy_From]);
    if nSchFileNr > 0 then
      begin Print_String(MMLIdentifierName[nSchFileNr]); Print_String(':'); Print_String('sch');
      Print_Number(nSchemeIdNr);
      end
    else if nSchemeIdNr > 0 then Print_SchemeNameInJustification(aInf);
    if nReferences.Count > 0 then
      begin Print_String('('); Print_References(nReferences); Print_String(')');
      end;
    end;
  end;

```


1180. \langle Implementation for `wsmarticle.pas` 854 $\rangle + \equiv$

```
procedure WSMizarPrinterObj.Print_Justification(aInf : JustificationPtr; aBlock : wsBlockPtr);
  begin case aInf↑.nInfSort of
    infStraightforwardJustification: Print_StraightforwardJustification(StraightforwardJustificationPtr(aInf));
    infSchemeJustification: Print_SchemeJustification(SchemeJustificationPtr(aInf));
    infError, infSkippedProof: begin end;
    infProof: Print_Block(aBlock);
  endcases;
end;
```

1181. \langle Implementation for `wsmarticle.pas` 854 $\rangle + \equiv$

```
procedure WSMizarPrinterObj.Print_Conditions(aCond : PList);
  var i: integer;
  begin Print_String(TokenName[sy_That]); Print_NewLine; Print_Proposition(aCond↑.Items↑[0]);
  for i ← 1 to aCond↑.Count − 1 do
    begin Print_String(TokenName[sy_And]); Print_NewLine; Print_Proposition(aCond↑.Items↑[i]);
    end;
  end;
```

1182. \langle Implementation for `wsmarticle.pas` 854 $\rangle + \equiv$

```
procedure WSMizarPrinterObj.Print_AssumptionConditions(aCond : AssumptionPtr);
  begin case aCond↑.nAssumptionSort of
    SingleAssumption: begin Print_Proposition(SingleAssumptionPtr(aCond)↑.nProp);
    end;
    CollectiveAssumption: begin Print_Conditions(CollectiveAssumptionPtr(aCond)↑.nConditions);
    end;
  endcases;
end;
```

1183. \langle Implementation for `wsmarticle.pas` 854 $\rangle + \equiv$

```
procedure WSMizarPrinterObj.Print_Locus(aLocus : LocusPtr);
  begin with aLocus↑ do
    begin Print_String(IdentRepr(nVarId));
    end;
  end;
```

1184. \langle Implementation for `wsmarticle.pas` 854 $\rangle + \equiv$

```
procedure WSMizarPrinterObj.Print_Loci(aLoci : PList);
  var i: integer;
  begin if (aLoci = nil)  $\vee$  (aLoci↑.Count = 0) then
  else begin Print_Locus(aLoci↑.Items↑[0]);
    for i ← 1 to aLoci↑.Count − 1 do
      begin Print_String(`, `); Print_Locus(aLoci↑.Items↑[i]);
      end;
    end;
  end;
```

```

1185.  ⟨Implementation for wsmarticle.pas 854⟩ +≡
procedure WSMizarPrinterObj.Print_Pattern(aPattern : PatternPtr);
  begin case aPattern↑.nPatternSort of
    itDefPred: with PredicatePatternPtr(aPattern)↑ do
      begin Print_Loci(nLeftArgs); Print_String(PredicateName[nPredSymbol]); Print_Loci(nRightArgs);
      end;
    itDefFunc: begin case FunctorPatternPtr(aPattern)↑.nFuncKind of
      InfixFunctor: with InfixFunctorPatternPtr(aPattern)↑ do
        begin if (nLeftArgs ≠ nil) ∧ (nLeftArgs↑.Count > 1) then Print_String('(');
        Print_Loci(nLeftArgs);
        if (nLeftArgs ≠ nil) ∧ (nLeftArgs↑.Count > 1) then Print_String(' ');
        Print_String(FunctorName[nOperSymb]);
        if (nRightArgs ≠ nil) ∧ (nRightArgs↑.Count > 1) then Print_String('(');
        Print_Loci(nRightArgs);
        if (nRightArgs ≠ nil) ∧ (nRightArgs↑.Count > 1) then Print_String(' ');
        end;
      CircumfixFunctor: with CircumfixFunctorPatternPtr(aPattern)↑ do
        begin Print_String(LeftBracketName[nLeftBracketSymb]); Print_Loci(nArgs);
        Print_String(RightBracketName[nRightBracketSymb]);
        end;
    endcases;
  end;
  itDefMode: with ModePatternPtr(aPattern)↑ do
    begin Print_String(ModeName[nModeSymbol]);
    if (nArgs ≠ nil) ∧ (nArgs↑.Count > 0) then
      begin Print_String(TokenName[sy_Of]); Print_Loci(nArgs);
      end;
    end;
  itDefAttr: with AttributePatternPtr(aPattern)↑ do
    begin Print_Locus(nArg); Print_String(TokenName[sy_Is]); Print_Loci(nArgs);
    Print_String(AttributeName[nAttrSymbol]);
    end;
  endcases;
end;

```

1186. \langle Implementation for `wsmarticle.pas` 854 $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_Definiens(aDef : DefiniensPtr);
  var i: integer;
  begin if aDef  $\neq$  nil then
    with DefiniensPtr(aDef) $\uparrow$  do
      begin case nDefSort of
        SimpleDefiniens: begin if (nDefLabel  $\neq$  nil)  $\wedge$  (nDefLabel $\uparrow$ .nLabelIdNr > 0) then
          begin Print_String(' '); Print_Label(nDefLabel);
          end;
          with SimpleDefiniensPtr(aDef) $\uparrow$ , nExpression $\uparrow$  do
            case nExprKind of
              exTerm: Print_Term(TermPtr(nExpr));
              exFormula: Print_Formula(FormulaPtr(nExpr));
            endcases;
          end;
        ConditionalDefiniens: begin if (nDefLabel  $\neq$  nil)  $\wedge$  (nDefLabel $\uparrow$ .nLabelIdNr > 0) then
          begin Print_String(' '); Print_Label(nDefLabel);
          end;
          with ConditionalDefiniensPtr(aDef) $\uparrow$  do
            begin for i  $\leftarrow$  0 to nConditionalDefiniensList $\uparrow$ .Count - 1 do
              begin with PartDefPtr(nConditionalDefiniensList $\uparrow$ .Items $\uparrow$ [i]) $\uparrow$  do
                begin with nPartDefiniens $\uparrow$  do
                  case nExprKind of
                    exTerm: Print_Term(TermPtr(nExpr));
                    exFormula: Print_Formula(FormulaPtr(nExpr));
                  endcases;
                  Print_String(TokenName[sy_If]); Print_Formula(nGuard);
                end;
              if (i  $\geq$  0)  $\wedge$  (i < nConditionalDefiniensList $\uparrow$ .Count - 1) then
                begin Print_String(' '); Print_NewLine;
                end;
              end;
            if nOtherwise  $\neq$  nil then
              with nOtherwise $\uparrow$  do
                begin Print_String(TokenName[sy_Otherwise]);
                case nExprKind of
                  exTerm: Print_Term(TermPtr(nExpr));
                  exFormula: Print_Formula(FormulaPtr(nExpr));
                endcases;
                end;
              end;
            end;
          end;
        endcases;
      end;
    end;
  end;

```

1187. \langle Implementation for `wsmarticle.pas` 854 $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_Block(aWSBlock : WSBlockPtr);
  var i, lIndent: integer;
  begin with aWSBlock↑ do
    begin lIndent  $\leftarrow$  nIndent; Print_NewLine; Print_Indent;
    case nBlockKind of
      blDiffuse: begin Print_String(TokenName[sy_Now]); Print_NewLine;
        end;
      blHereby: begin Print_String(TokenName[sy_Now]); Print_NewLine;
        end;
      blProof: begin Print_String(TokenName[sy_Proof]); Print_NewLine;
        end;
      blDefinition: begin Print_String(TokenName[sy_Definition]); Print_NewLine;
        end;
      blNotation: begin Print_String(TokenName[sy_Notation]); Print_NewLine;
        end;
      blRegistration: begin Print_String(TokenName[sy_Registration]); Print_NewLine;
        end;
      blCase: Print_String(TokenName[sy_Case]);
      blSuppose: Print_String(TokenName[sy_Suppose]);
      blPublicScheme: ;
    endcases;
    for i  $\leftarrow$  0 to nItems↑.Count - 1 do
      begin Print_Item(nItems↑.Items↑[i]);
      end;
    nIndent  $\leftarrow$  lIndent; Print_Indent; Print_String(TokenName[sy_End]);
    end;
  end;

```

1188. \langle Implementation for `wsmarticle.pas` 854 $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_TextProper(aWSTextProper : WSTextProperPtr);
  var i: integer;
  begin with aWSTextProper↑ do
    begin for i  $\leftarrow$  0 to nItems↑.Count - 1 do Print_Item(nItems↑.Items↑[i]);
    end;
  end;

```

1189. \langle Implementation for `wsmarticle.pas` 854 $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_ReservedType(aResType : TypePtr);
  begin Print_Type(aResType);
  end;

```

1190. \langle Implementation for `wsmarticle.pas` 854 $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_SchemeNameInSchemeHead(aSch : SchemePtr);
  begin Print_String(IdentRepr(aSch↑.nSchemeIdNr));
  end;

```

1191. \langle Implementation for `wsmarticle.pas` 854 $\rangle + \equiv$

```

procedure WSMizarPrinterObj.Print_Item(aWSItem : WSItemPtr);
var i, j, Indent: integer;
begin with aWSItem↑ do
  begin CurPos ← nItemPos;
  if nDisplayInformationOnScreen then DisplayLine(CurPos.Line, ErrorNbr);
  case nItemKind of
    itDefinition: begin Print_Block(nBlock); Print_String(' '); Print_NewLine;
      end;
    itSchemeBlock: begin Print_Block(nBlock); Print_String(' '); Print_NewLine;
      end;
    itSchemeHead: with SchemePtr(nContent)↑ do
      begin Print_String(TokenName[sy_Scheme]);
        Print_SchemeNameInSchemeHead(SchemePtr(nContent)); Print_String('{ ');
        for j ← 0 to nSchemeParams↑.Count − 1 do
          begin case SchemeSegmentPtr(nSchemeParams↑.Items↑[j])↑.nSegmSort of
            PredicateSegment: with PredicateSegmentPtr(nSchemeParams↑.Items↑[j])↑ do
              begin Print_Variable(nVars↑.Items↑[0]);
                for i ← 1 to nVars↑.Count − 1 do
                  begin Print_String(' ', ' '); Print_Variable(nVars↑.Items↑[i]);
                    end;
                  Print_String(' [ '); Print_TypeList(nTypeExpList); Print_String(' ] ');
                    end;
                FunctorSegment: with FunctorSegmentPtr(nSchemeParams↑.Items↑[j])↑ do
                  begin Print_Variable(nVars↑.Items↑[0]);
                    for i ← 1 to nVars.Count − 1 do
                      begin Print_String(' ', ' '); Print_Variable(nVars↑.Items↑[i]);
                        end;
                      Print_String(' ( '); Print_TypeList(nTypeExpList); Print_String(' ) ');
                        Print_String(TokenName[sy_Arrow]); Print_Type(nSpecification);
                          end;
                    endcases;
                    if (j ≥ 0) ∧ (j < nSchemeParams↑.Count − 1) then Print_String(' ', ' ');
                      end;
                    Print_String(' } '); Print_String(' : '); Print_Newline; Print_Formula(nSchemeConclusion);
                      Print_NewLine;
                    if (nSchemePremises ≠ nil) ∧ (nSchemePremises↑.Count > 0) then
                      begin Print_String(TokenName[sy_Provided]);
                        Print_Proposition(nSchemePremises↑.Items↑[0]);
                        for i ← 1 to nSchemePremises↑.Count − 1 do
                          begin Print_String(TokenName[sy_And]); Print_NewLine;
                            Print_Proposition(nSchemePremises↑.Items↑[i]);
                              end;
                          end;
                        Print_String(TokenName[sy_Proof]); Print_NewLine;
                          end;
                      itTheorem: with CompactStatementPtr(nContent)↑ do
                        begin Print_NewLine; nIndent ← 0; Print_String(TokenName[sy_Theorem]);
                          Print_Label(nProp↑.nLab); Print_NewLine; nIndent ← 2; Print_Indent;
                          Print_Formula(nProp↑.nSentence); nIndent ← 0; Print_Justification(nJustification, nBlock);
                          Print_String(' '); Print_NewLine;
                          end;
                        end;
                      end;
                    end;
                  end;
                end;
              end;
            end;
          end;
        end;
      end;
    end;
  end;

```

```

itAxiom: begin end;
itReservation: with ReservationSegmentPtr(nContent)↑ do
  begin Print_NewLine; Print_String(TokenName[sy_reserve]);
  Print_Variable(nIdentifiers.Items↑[0]);
  for i ← 1 to nIdentifiers.Count − 1 do
    begin Print_String(`,`); Print_Variable(nIdentifiers.Items↑[i]);
    end;
  Print_String(TokenName[sy_For]); Print_ReservedType(nResType); Print_String(`,`);
  Print_NewLine;
  end;
itSection: begin Print_NewLine; Print_String(TokenName[sy_Begin]); Print_NewLine;
  end;
itRegularStatement: begin Print_RegularStatement(RegularStatementPtr(nContent), nBlock);
  Print_String(`,`); Print_NewLine;
  end;
itChoice: with ChoiceStatementPtr(nContent)↑ do
  begin if (nJustification↑.nInfSort = infStraightforwardJustification) ∧
    StraightforwardJustificationPtr(nJustification)↑.nLinked then
    begin Print_Linkage;
    end;
    Print_String(TokenName[sy_Consider]); Print_VariableSegment(nQualVars.Items↑[0]);
    for i ← 1 to nQualVars.Count − 1 do
      begin Print_String(`,`); Print_VariableSegment(nQualVars.Items↑[i]);
      end;
    if (nConditions ≠ nil) ∧ (nConditions↑.Count > 0) then
      begin Print_String(TokenName[sy_Such]); Print_Conditions(nConditions);
      end;
      Print_Justification(nJustification, nil); Print_String(`,`); Print_NewLine;
    end;
itReconsider: with TypeChangingStatementPtr(nContent)↑ do
  begin if (nJustification↑.nInfSort = infStraightforwardJustification) ∧
    StraightforwardJustificationPtr(nJustification)↑.nLinked then
    begin Print_Linkage;
    end;
    Print_String(TokenName[sy_Reconsider]);
    for i ← 0 to nTypeChangeList.Count − 1 do
      begin case TypeChangePtr(nTypeChangeList.Items↑[i])↑.nTypeChangeKind of
        Equating: begin Print_Variable(TypeChangePtr(nTypeChangeList.Items↑[i])↑.nVar);
          Print_String(`=); Print_Term(TypeChangePtr(nTypeChangeList.Items↑[i])↑.nTermExpr);
          end;
        VariableIdentifier: begin Print_Variable(TypeChangePtr(nTypeChangeList.Items↑[i])↑.nVar);
          end;
        endcases;
      if (i ≥ 0) ∧ (i < nTypeChangeList.Count − 1) then Print_String(`,`);
      end;
      Print_String(TokenName[sy_As]); Print_Type(nTypeExpr);
      Print_Justification(nJustification, nil); Print_String(`,`); Print_NewLine;
    end;
itPrivFuncDefinition: with PrivateFunctorDefinitionPtr(nContent)↑ do
  begin Print_String(TokenName[sy_DefFunc]); Print_Variable(nFuncId); Print_String(`,`);
  Print_TypeList(nTypeExpList); Print_String(`,`); Print_String(`=); Print_Term(nTermExpr);
  Print_String(`,`); Print_NewLine;

```

```

    end;
itPrivPredDefinition: with PrivatePredicateDefinitionPtr(nContent)↑ do
    begin Print_String(TokenName[sy_DefPred]); Print_Variable(nPredId); Print_String('[');
    Print_TypeList(nTypeExpList); Print_String(']'); Print_String(TokenName[sy_Means]);
    Print_Formula(nSentence); Print_String(';'); Print_NewLine;
    end;
itConstantDefinition: with ConstantDefinitionPtr(nContent)↑ do
    begin Print_String(TokenName[sy_Set]); Print_Variable(nVarId); Print_String('=');
    Print_Term(nTermExpr); Print_String(';'); Print_NewLine;
    end;
itLocDeclaration, itGeneralization: begin Print_String(TokenName[sy_Let]);
    Print_VariableSegment(QualifiedSegmentPtr(nContent)); Print_String(';'); Print_NewLine;
    end;
itAssumption: begin Print_String(TokenName[sy_Assume]);
    Print_AssumptionConditions(AssumptionPtr(nContent)); Print_String(';'); Print_NewLine;
    end;
itExistentialAssumption: with ExistentialAssumptionPtr(nContent)↑ do
    begin Print_String(TokenName[sy_Given]); Print_VariableSegment(nQVars↑.Items↑[0]);
    for i ← 1 to nQVars↑.Count - 1 do
        begin Print_String(','); Print_VariableSegment(nQVars↑.Items↑[i]);
        end;
    Print_String(TokenName[sy_Such]); Print_String(TokenName[sy_That]); Print_NewLine;
    Print_Proposition(nConditions↑.Items↑[0]);
    for i ← 1 to nConditions↑.Count - 1 do
        begin Print_String(TokenName[sy_And]); Print_NewLine;
        Print_Proposition(nConditions↑.Items↑[i]);
        end;
    Print_String(';'); Print_NewLine;
    end;
itExemplification: with ExamplePtr(nContent)↑ do
    begin Print_String(TokenName[sy_Take]);
    if nVarId ≠ nil then
        begin Print_Variable(nVarId);
        if nTermExpr ≠ nil then
            begin Print_String('=');
            end;
        end;
    if nTermExpr ≠ nil then Print_Term(nTermExpr);
    Print_String(';'); Print_NewLine;
    end;
itPerCases: begin if (JustificationPtr(nContent)↑.nInfSort =
    infStraightforwardJustification) ∧ StraightforwardJustificationPtr(nContent)↑.nLinked then
    begin Print_Linkage;
    end;
    Print_String(TokenName[sy_Per]); Print_String(TokenName[sy_Cases]);
    Print_Justification(JustificationPtr(nContent), nil); Print_String(';'); Print_NewLine;
    end;
itConclusion: begin Print_String(TokenName[sy_Thus]);
    Print_RegularStatement(RegularStatementPtr(nContent), nBlock); Print_String(';');
    Print_NewLine;
    end;
itCaseBlock: begin Print_Block(nBlock); Print_String(';'); Print_NewLine;

```

```

    end;
itCaseHead, itSupposeHead: begin Print_AssumptionConditions( AssumptionPtr(nContent));
    Print_String( '~;~'); Print_NewLine;
    end;
itCorrCond: begin
    Print_String( CorrectnessName[ CorrectnessConditionPtr(nContent)↑.nCorrCondSort]);
    Print_Justification( CorrectnessConditionPtr(nContent)↑.nJustification, nBlock); Print_String( '~;~');
    Print_NewLine;
    end;
itCorrectness: begin Print_String( TokenName[sy_Correctness]);
    Print_Justification( CorrectnessPtr(nContent)↑.nJustification, nBlock); Print_String( '~;~');
    Print_NewLine;
    end;
itProperty: begin Print_String( PropertyName[PropertyPtr(nContent)↑.nPropertySort]);
    Print_Justification( PropertyPtr(nContent)↑.nJustification, nBlock); Print_String( '~;~');
    Print_NewLine;
    end;
itDefMode: with ModeDefinitionPtr(nContent)↑ do
    begin if nRedefinition then
        begin Print_String( TokenName[sy_Redefine]);
        end;
        Print_String( TokenName[sy_Mode]); Print_Pattern(nDefModePattern);
    case nDefKind of
        defExpandableMode: begin Print_String( TokenName[sy_Is]);
            Print_Type( ExpandableModeDefinitionPtr(nContent)↑.nExpansion);
            end;
        defStandardMode: with StandardModeDefinitionPtr(nContent)↑ do
            begin if nSpecification ≠ nil then
                begin Print_String( TokenName[sy_Arrow]); Print_Type(nSpecification);
                end;
            if nDefiniens ≠ nil then
                begin Print_String( TokenName[sy_Means]); Print_NewLine; Print_Definiens(nDefiniens);
                end;
            end;
        endcases; Print_String( '~;~'); Print_NewLine;
    end;
itDefAttr: with AttributeDefinitionPtr(nContent)↑ do
    begin if nRedefinition then
        begin Print_String( TokenName[sy_Redefine]);
        end;
        Print_String( TokenName[sy_Attr]); Print_Pattern(nDefAttrPattern);
        Print_String( TokenName[sy_Means]); Print_NewLine; Print_Definiens(nDefiniens);
        Print_String( '~;~'); Print_NewLine;
    end;
itDefPred: with PredicateDefinitionPtr(nContent)↑ do
    begin if nRedefinition then
        begin Print_String( TokenName[sy_Redefine]);
        end;
        Print_String( TokenName[sy_Pred]); Print_Pattern(nDefPredPattern);
    if nDefiniens ≠ nil then
        begin Print_String( TokenName[sy_Means]); Print_NewLine; Print_Definiens(nDefiniens);
        end;

```



```

    Print_String(' '); Print_NewLine;
  end;
itDefFunc: with FunctorDefinitionPtr(nContent)↑ do
  begin if nRedefinition then
    begin Print_String(TokenName[sy_Redefine]);
    end;
    Print_String(TokenName[sy_Func]); Print_Pattern(nDefFuncPattern);
  if nSpecification ≠ nil then
    begin Print_String(TokenName[sy_Arrow]); Print_Type(nSpecification);
    end;
  case nDefiningWay of
    dfEmpty: ;
    dfMeans: begin Print_String(TokenName[sy_Means]); Print_NewLine;
    end;
    dfEquals: begin Print_String(TokenName[sy_Equals]);
    end;
  endcases; Print_Definiens(nDefiniens); Print_String(' '); Print_NewLine;
  end;
itDefStruct: with StructureDefinitionPtr(nContent)↑ do
  begin Print_String(TokenName[sy_Struct]);
  if nAncestors↑.Count > 0 then
    begin Print_String(' ( '); Print_Type(nAncestors↑.Items↑[0]);
    for i ← 1 to nAncestors↑.Count - 1 do
      begin Print_String(' ', ' '); Print_Type(nAncestors↑.Items↑[i]);
      end;
    Print_String(' ');
    end;
    Print_String(StructureName[nDefStructPattern↑.nModeSymbol]);
  if (nDefStructPattern↑.nArgs ≠ nil) ∧ (nDefStructPattern↑.nArgs↑.Count > 0) then
    begin Print_String(TokenName[sy_Over]); Print_Loci(nDefStructPattern↑.nArgs);
    end;
    Print_String(TokenName[sy_StructLeftBracket]);
  for i ← 0 to nSgmFields↑.Count - 1 do
    with FieldSegmentPtr(nSgmFields↑.Items↑[i])↑ do
      begin Print_String(SelectorName[FieldSymbolPtr(nFields↑.Items↑[0])↑.nFieldSymbol]);
      for j ← 1 to nFields↑.Count - 1 do
        with FieldSymbolPtr(nFields↑.Items↑[j])↑ do
          begin Print_String(' ', ' '); Print_String(SelectorName[nFieldSymbol]);
          end;
          Print_String(TokenName[sy_Arrow]); Print_Type(nSpecification);
          if (i ≥ 0) ∧ (i < nSgmFields↑.Count - 1) then Print_String(' ', ' ');
          end;
        end;
      end;
    Print_String(TokenName[sy_StructRightBracket]); Print_String(' '); Print_NewLine;
  end;
itPredSynonym, itFuncNotation, itModeNotation, itAttrSynonym:
  with NotationDeclarationPtr(nContent)↑ do
    begin Print_String(TokenName[sy_Synonym]); Print_Pattern(nNewPattern);
    Print_String(TokenName[sy_For]); Print_Pattern(nOriginPattern); Print_String(' ');
    Print_NewLine;
  end;
itPredAntonym, itAttrAntonym: with NotationDeclarationPtr(nContent)↑ do
  begin Print_String(TokenName[sy_Antonym]); Print_Pattern(nNewPattern);

```

```

    Print_String(TokenName[sy_For]); Print_Pattern(nOriginPattern); Print_String(';');
    Print_NewLine;
  end;
itCluster: begin Print_String(TokenName[sy_Cluster]);
  case ClusterPtr(nContent)↑.nClusterKind of
    ExistentialRegistration: with EClusterPtr(nContent)↑ do
      begin Print_AdjectiveList(nConsequent); Print_String(TokenName[sy_For]);
      Print_Type(nClusterType);
      end;
    ConditionalRegistration: with CClusterPtr(nContent)↑ do
      begin Print_AdjectiveList(nAntecedent); Print_String(TokenName[sy_Arrow]);
      Print_AdjectiveList(nConsequent); Print_String(TokenName[sy_For]);
      Print_Type(nClusterType);
      end;
    FunctorialRegistration: with FClusterPtr(nContent)↑ do
      begin Print_Term(nClusterTerm); Print_String(TokenName[sy_Arrow]);
      Print_AdjectiveList(nConsequent);
      if nClusterType ≠ nil then
        begin Print_String(TokenName[sy_For]); Print_Type(nClusterType);
        end;
      end;
  endcases; Print_String(';'); Print_NewLine;
end;
itIdentify: with IdentifyRegistrationPtr(nContent)↑ do
  begin Print_String(TokenName[sy_Identify]); Print_Pattern(nNewPattern);
  Print_String(TokenName[sy_With]); Print_Pattern(nOriginPattern);
  if (nEqLocList ≠ nil) ∧ (nEqLocList↑.Count > 0) then
    begin Print_String(TokenName[sy_When]);
    for i ← 0 to nEqLocList↑.Count - 1 do
      with LociEqualityPtr(nEqLocList↑.Items↑[i])↑ do
        begin Print_Locus(nLeftLocus); Print_String('='); Print_Locus(nRightLocus);
        if (i ≥ 0) ∧ (i < nEqLocList↑.Count - 1) then Print_String(',');
        end;
      end;
    end;
    Print_String(';'); Print_NewLine;
  end;
itPropertyRegistration: case PropertyRegistrationPtr(nContent)↑.nPropertySort of
  sySethood: with SethoodRegistrationPtr(nContent)↑ do
    begin Print_String(PropertyName[nPropertySort]); Print_String(TokenName[sy_Of]);
    Print_Type(nSethoodType); Print_Justification(nJustification, nBlock); Print_String(';');
    Print_NewLine;
    end;
  endcases;
itReduction: begin with ReduceRegistrationPtr(nContent)↑ do
  begin Print_String(TokenName[sy_Reduce]); Print_Term(nOriginTerm);
  Print_String(TokenName[sy_To]); Print_Term(nNewTerm);
  end;
  Print_String(';'); Print_NewLine;
end;
itPragma: begin Print_NewLine; Print_String('::' + PragmaPtr(nContent)↑.nPragmaStr);
  Print_NewLine;
end;

```

```
    itIncorrItem: ;  
  end;  
endcases;  
end;
```

1192. 〈Implementation for `wsmarticle.pas` 854〉 +≡

```
procedure Print_WSMizArticle(aWSTextProper : wsTextProperPtr; aFileName : string);  
  var lWSMizOutput: WSMizarPrinterPtr;  
  begin InitScannerNames; lWSMizOutput ← new(WSMizarPrinterPtr, OpenFile(aFileName));  
    lWSMizOutput↑.Print_TextProper(aWSTextProper); dispose(lWSMizOutput, Done);  
  end;
```

File 22

Detour: Pragas

1193. This chapter is a “detour” because it is out of order for the compiler, but it is a dependency for the next file (`parseradditions.pas`).

The `base/pragmas.pas` contains the global variables which are toggled by pragmas like “`::$P+`”. This will toggle the *ProofPragma*. In particular, when *ProofPragma* is true, then Mizar will double check the proofs. When *ProofPragma* is false, Mizar will skip the proofs.

```

⟨pragmas.pas 1193⟩ ≡
  ⟨GNU License 4⟩
unit pragmas;
  interface uses mobjects;
  var VerifyPragmaOn, VerifyPragmaOff: NatSet; VerifyPragmaIntervals: NatFunc;
      SchemePragmaOn, SchemePragmaOff: NatSet; SchemePragmaIntervals: NatFunc;
      ProofPragma: Boolean = true; { check the proofs? }

  procedure SetParserPragma(aPrg : string);
  procedure InsertPragma(aLine : integer; aPrg : string);
  procedure CompletePragmas(aLine : integer);
  procedure CanceledPragma ( const aPrg: string; var aKind: char; var aNbr: integer ) ;
implementation
  uses mizenv;

```

1194. Cancelling a definition or theorem is handled with the “`::$C`” pragma, which is administered only by the editors of the MML.

```

procedure CanceledPragma ( const aPrg: string; var aKind: char; var aNbr: integer ) ;
var lStr: string; k, lCod: integer;
  begin aKind ← ‘␣’;
  if (Copy(aPrg, 1, 2) = ‘$C’) then
    begin if (length(aPrg) ≥ 3) ∧ (aPrg[3] ∈ [‘D’, ‘S’, ‘T’]) then
      begin aKind ← aPrg[3]; lStr ← TrimString(Copy(aPrg, 4, length(aPrg) – 3)); aNbr ← 1;
      if length(lStr) > 0 then
        begin k ← 1;
        while (k ≤ length(lStr)) ∧ (lStr[k] ∈ [‘0’ .. ‘9’]) do inc(k);
        delete(lStr, k, length(lStr));
        if length(lStr) > 0 then Val(lStr, aNbr, lCod);
        end;
      end;
    end;
  end;

```

1195. The “`::$P+`” pragma instructs Mizar to start checking the proofs for correctness. The “`::$P-`” pragma instructs Mizar to skip checking proofs.

```
procedure SetParserPragma(aPrg : string);
  begin if copy(aPrg, 1, 3) = ‘$P+’ then
    begin ProofPragma  $\leftarrow$  true;
    end;
  if copy(aPrg, 1, 3) = ‘$P-’ then
    begin ProofPragma  $\leftarrow$  false;
    end;
  end;
```

1196. The “`::$S+`” pragma will tell Mizar to check the scheme references, whereas “`::$S-`” pragma tells Mizar to stop verifying scheme references.

The “`::$V+`” pragma enables the verifier, and the “`::$V-`” pragma disables the verifier (skipping all verification until it is re-enabled).

```
procedure InsertPragma(aLine : integer; aPrg : string);
  begin if copy(aPrg, 1, 3) = ‘$V+’ then
    begin VerifyPragmaOn.InsertElem(aLine); end;
  if copy(aPrg, 1, 3) = ‘$V-’ then
    begin VerifyPragmaOff.InsertElem(aLine); end;
  if copy(aPrg, 1, 3) = ‘$S+’ then
    begin SchemePragmaOn.InsertElem(aLine); end;
  if copy(aPrg, 1, 3) = ‘$S-’ then
    begin SchemePragmaOff.InsertElem(aLine); end;
  end;
```

1197. The *CompletePragmas* function will compute the intervals for which the pragmas are “active”, then check whether the given line number falls within the “active range”.

```
procedure CompletePragmas(aLine : integer);
  var i, j, a, b: integer; f: boolean;
  begin for i  $\leftarrow$  0 to VerifyPragmaOff.Count - 1 do
    begin f  $\leftarrow$  false; a  $\leftarrow$  VerifyPragmaOff.Items $\uparrow$ [i].X;
    for j  $\leftarrow$  0 to VerifyPragmaOn.Count - 1 do
      begin b  $\leftarrow$  VerifyPragmaOn.Items $\uparrow$ [j].X;
      if b  $\geq$  a then
        begin VerifyPragmaIntervals.Assign(a, b); f  $\leftarrow$  true; break; end;
      end;
    if  $\neg$ f then VerifyPragmaIntervals.Assign(a, aLine);
    end;
  for i  $\leftarrow$  0 to SchemePragmaOff.Count - 1 do
    begin f  $\leftarrow$  false; a  $\leftarrow$  SchemePragmaOff.Items $\uparrow$ [i].X;
    for j  $\leftarrow$  0 to SchemePragmaOn.Count - 1 do
      begin b  $\leftarrow$  SchemePragmaOn.Items $\uparrow$ [j].X;
      if b  $\geq$  a then
        begin SchemePragmaIntervals.Assign(a, b); f  $\leftarrow$  true; break; end;
      end;
    if  $\neg$ f then SchemePragmaIntervals.Assign(a, aLine);
    end;
  end;
```

1198. Now we initialize the global variables declared in this module.

```
begin VerifyPragmaOn.Init(10,10); VerifyPragmaOff.Init(10,10);  
      VerifyPragmaIntervals.InitNatFunc(10,10); SchemePragmaOn.Init(10,10);  
      SchemePragmaOff.Init(10,10); SchemePragmaIntervals.InitNatFunc(10,10);  
end.
```

File 23

Detour: Parser additions

1199. This chapter is a “detour” because we are “going out of [compiler] order” to discuss `parseradditions.pas`. Why? Well, because the file provides subclasses to those introduced in the abstract syntax unit, and are necessary for understanding the `parser.pas` unit.

One of the difficulties with this file is that there are 37 global variables declared here, and 46 module-wide variables, declared here. It’s hard to juggle that knowledge! These “global” variables really describe the state of the parser, and do not seem to be used anywhere else.

[[It would probably be wise to refactor the design to isolate these variables inside a `Parser` class, so they are not randomly distributed throughout this part of the program.]]

CONVENTIONS: The classes have methods prefixed by *Start*, *Process*, and *Finish*.

- The *Start* methods reset the state variables needed to parse the syntactic entity.
- The *Process* methods usually update the state variables, either allocating new objects or transferring the current contents of a state variable in a different state variable.
- The *Finish* methods construct a WSM abstract syntax tree for the parsed entity.

⟨`parseraddition.pas` 1199⟩ ≡

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unit *parseraddition*;

interface

uses *syntax*, *errhan*, *mobjects*, *mscanner*, *abstract_syntax*, *wsmarticle*, *xml_inout*;

procedure *InitWsMizarArticle*;

type

⟨Extended block class declaration 1205⟩

⟨Extended item class declaration 1225⟩

⟨Extended subexpression class declaration 1388⟩

⟨Extended expression class declaration 1489⟩

function *GetIdentifier*: *integer*;

function *CreateArgs*(*aBase* : *integer*): *PList*;

var ⟨Global variables introduced in `parseraddition.pas` 1202⟩

implementation

uses *mizenv*, *mconsole*, *parser*, *_formats*, *pragmas*

mdebug , *info* **end_mdebug**;

const *MaxSubTermNbr* = 64;

var ⟨Local variables for parser additions 1209⟩

⟨Implementation of parser additions 1200⟩

end .

1200. \langle Implementation of parser additions 1200 $\rangle \equiv$
 \langle Get the identifier number for current word 1201 \rangle
 \langle Initialize WS Mizar article 1203 \rangle ;
 \langle Extended block implementation 1206 \rangle
 \langle Extended item implementation 1226 \rangle
 \langle Extended subexpression implementation 1390 \rangle
 \langle Extended expression implementation 1490 \rangle

This code is used in section 1199.

1201. When the current token is an identifier, we should obtain its number. If the current token is not an identifier, we should return 0.

\langle Get the identifier number for current word 1201 $\rangle \equiv$
function *GetIdentifier*: *integer*;
 begin *result* \leftarrow 0;
 if *CurWord.Kind* = *Identifier* **then** *result* \leftarrow *CurWord.Nr*
 end;

This code is used in section 1200.

1202. Initializing a weakly-strict Mizar article requires setting the values for some of the global variables. Importantly, this will initialize the *gBlockPtr* in the Parser to be an *extBlockObj* instance. Note that this will create “the” *blMain* block object.

\langle Global variables introduced in *parseraddition.pas* 1202 $\rangle \equiv$
gWSTextProper: *wsTextProperPtr*;
gLastWSBlock: *WSBlockPtr*;
gLastWSItem: *WSItemPtr*;

See also sections 1210, 1212, 1227, 1231, 1234, 1240, 1243, 1247, 1256, 1268, 1273, 1287, 1297, 1308, 1316, 1320, 1328, 1336, 1338, 1340, 1346, 1348, 1367, 1370, 1374, and 1394.

This code is used in section 1199.

1203. \langle Initialize WS Mizar article 1203 $\rangle \equiv$
procedure *InitWsMizarArticle*;
 begin { initialize global variables which were declared in *parseraddition* }
 gWSTextProper \leftarrow *new*(*wsTextProperPtr*, *Init*(*ArticleID*, *ArticleExt*, *CurPos*));
 gLastWSBlock \leftarrow *gWSTextProper*; *gLastWSItem* \leftarrow **nil**;
 gBlockPtr \leftarrow *new*(*extBlockPtr*, *Init*(*blMain*)); { initialize other global variables }
 end;

This code is used in section 1200.

Section 23.1. EXTENDED BLOCK CLASS

1204. We extend the *Block* class (§691) introduced in the `syntax.pas` unit. Also recall the *wsBlock* class (§856) and the *wsItem* class (§860).

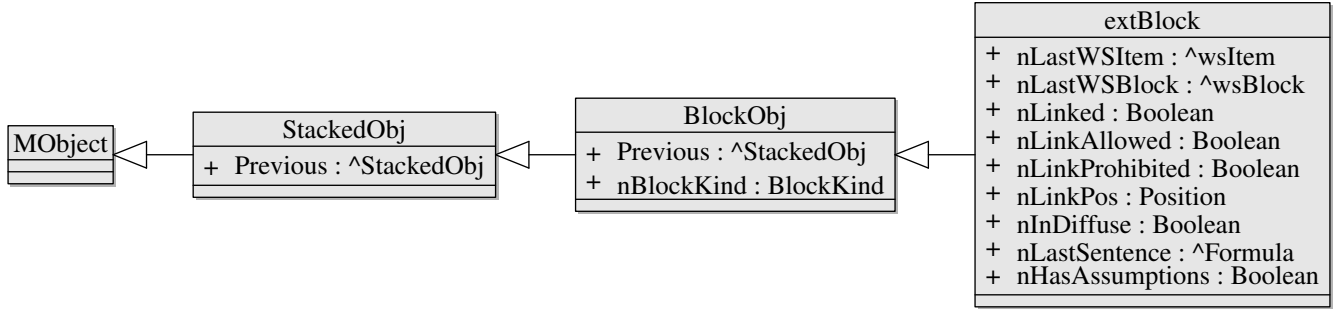


Fig. 6. Class hierarchy for *extBlockObj*, methods omitted.

1205. \langle Extended block class declaration 1205 $\rangle \equiv$

```

extBlockPtr = ↑extBlockObj;
extBlockObj = object (BlockObj)
  nLastWSItem: WSItemPtr;
  nLastWSBlock: WSBlockPtr;
  nLinked: Boolean; { is block prefixed by “then”? }
  nLinkAllowed: Boolean; { isn’t this a duplicate of next field? }
  nLinkProhibited: Boolean; { can statement kind be prefixed by “then”? }
  nLinkPos: Position;
  nInDiffuse: boolean;
  nLastSentence: FormulaPtr;
  nHasAssumptions: Boolean;
constructor Init(fBlockKind : BlockKind);
procedure Pop; virtual;
procedure StartProperText; virtual;
procedure ProcessRedefine; virtual;
procedure ProcessLink; virtual;
procedure ProcessBegin; virtual;
procedure ProcessPragma; virtual;
procedure StartSchemeDemonstration; virtual;
procedure FinishSchemeDemonstration; virtual;
procedure CreateItem(fItemKind : ItemKind); virtual;
procedure CreateBlock(fBlockKind : BlockKind); virtual;
end ;
  
```

This code is used in section 1199.

1206. Constructor. The constructor for an extended block object invokes the parent class’s constructor (§694), initializes the instance variables, then its behaviour depends on whether we are constructing a “main” block or not.

```

⟨Extended block implementation 1206⟩ ≡
constructor extBlockObj.Init(fBlockKind : BlockKind);
  begin inherited Init(fBlockKind);
  ⟨Initialize default values for extBlock instance 1207⟩;
  if nBlockKind = blMain then ⟨Initialize main extBlock instance 1208⟩
  else ⟨Initialize “proper text” extBlock instance 1211⟩;
  end;

```

See also sections 1213, 1214, 1215, 1216, 1217, 1218, 1219, 1221, 1222, and 1223.

This code is used in section 1200.

1207. We have the default values suppose links are prohibited for the block, and there are no assumptions for the block. The last *wsItem* and *wsBlock* pointers are set to the global *gLastWSItem* and *gLastWSBlock* variables, respectively.

```

⟨Initialize default values for extBlock instance 1207⟩ ≡
  nLinked ← false; nLinkPos ← CurPos; nLinkAllowed ← false; nLinkProhibited ← true;
  nHasAssumptions ← false; gRedefinitions ← false;
  nLastWSItem ← gLastWSItem; nLastWSBlock ← gLastWSBlock;

```

This code is used in section 1206.

1208. The “main” block of text needs to load the formats file, and populate the *gFormatsColl* (§648) and the *gFormatsBase* (*ibid.*) global variables. The *parseraddition.pas* unit’s *gProofCnt* global variable is initialized to zero here.

```

⟨Initialize main extBlock instance 1208⟩ ≡
  begin nInDiffuse ← true; gProofCnt ← 0;
  FileExam(EnvFileName + ‘.frm’); gFormatsColl.LoadFormats(EnvFileName + ‘.frm’);
  gFormatsBase ← gFormatsColl.Count; setlength(Term, MaxSubTermNbr);
  end

```

This code is used in section 1206.

1209. ⟨Local variables for parser additions 1209⟩ ≡
Term: **array of** *TermPtr*; { (§753) }

See also sections 1228, 1232, 1238, 1241, 1244, 1245, 1248, 1252, 1258, 1260, 1262, 1269, 1271, 1274, 1278, 1284, 1292, 1298, 1302, 1309, 1317, 1331, 1382, and 1389.

This code is used in section 1199.

1210. ⟨Global variables introduced in *parseraddition.pas* 1202⟩ +≡
gProofCnt: *integer*;

1211. The “proper text” branch updates the *gLastWSBlock* global variable. For most of the kinds of blocks, we will have to toggle *nInDiffuse* to be true or false. For proof blocks, we will need to increment the “depth” counter tracking the proof block “nestedness”.

Only the “**case**” and “**suppose**” blocks, when determining if they are in “diffuse mode” or not, need to confer with the previous block. (Recall (§307), *StackedObj* classes has a *Previous* pointer.)

```

⟨ Initialize “proper text” extBlock instance 1211 ⟩ ≡
  begin gLastWSBlock ← gWsTextProper↑.NewBlock(nBlockKind, CurPos);
  mizassert(2341, gLastWSItem ≠ nil);
  if gLastWSItem↑.nItemKind ∈ [itDefinition, itRegularStatement, itSchemeBlock, itTheorem,
    itConclusion, itCaseBlock, itCorrCond, itCorrectness, itProperty, itPropertyRegistration] then
    wsItemPtr(gLastWSItem).nBlock ← gLastWSBlock;
  case nBlockKind of
    blDefinition: nInDiffuse ← false;
    blNotation: nInDiffuse ← false;
    blDiffuse: nInDiffuse ← true;
    blHereby: nInDiffuse ← true;
    blProof: begin nLastSentence ← gLastFormula; inc(gProofCnt); end;
    blCase: nInDiffuse ← extBlockPtr(Previous)↑.nInDiffuse;
    blSuppose: nInDiffuse ← extBlockPtr(Previous)↑.nInDiffuse;
    blRegistration: nInDiffuse ← false;
    blPublicScheme: nInDiffuse ← false;
  endcases;
end

```

This code is used in section 1206.

1212. Popping a block. When we “pop” a proof block, we need to track the formula that was just proven and store it in the global variable *gLastFormula*.

```

⟨ Global variables introduced in parseraddition.pas 1202 ⟩ +=
gLastFormula: FormulaPtr;

```

1213. This actually implements the *Pop* method for blocks. When a block “closes” (i.e., the corresponding “**end**” statement has been encountered), we restore the global state’s *gLastWSItem* and *gLastWSBlock* pointers. When a proof block closes, we also restore the *gLastFormula* state.

Also note: the parent class’s method (§695) does nothing. This will be invoked in the *KillBlock* (§687).

```

⟨ Extended block implementation 1206 ⟩ +=
procedure extBlockObj.Pop;
  begin gLastWSBlock↑.nBlockEndPos ← CurPos;
  case nBlockKind of
    blProof: begin gLastFormula ← nLastSentence; dec(gProofCnt); end;
  endcases;
  gLastWSItem ← nLastWSItem; gLastWSBlock ← nLastWSBlock; { restore the “last” pointers }
  inherited Pop;
end;

```

1214. Process “begin”. Mizar uses “begin” to start a new “section” at the top-level of an article. Recall the grammar for this bit of Mizar:

```
Text-Propser = Section { Section } .
Section = "begin" { Text-Item } .
```

There are zero or more Text-Items in a section.

We should note that the main text is not organized as a linked list of “main” blocks. Instead, we have a single “main” block, and we just push an *itSection* item to its contents.

⟨Extended block implementation 1206⟩ +≡

```
procedure extBlockObj.ProcessBegin;
begin nLinkAllowed ← false; nLinkProhibited ← true;
      gLastWSItem ← gWsTextPropser↑.NewItem(itSection, CurPos); nLastWSItem ← gLastWSItem;
      gLastWSBlock↑.nItems.Insert(gLastWSItem);
end;
```

1215. This will add a pragma item to the current block. The parser’s *ProcessPragmas* (§1570) invokes this method.

⟨Extended block implementation 1206⟩ +≡

```
procedure extBlockObj.ProcessPragma;
begin nLinkAllowed ← false; nLinkProhibited ← true;
      { Create a new item }
      gLastWSItem ← gWsTextPropser↑.NewItem(itPragma, CurPos);
      gLastWSItem↑.nContent ← new(PpragmaPtr, Init(CurWord.Spelling));
      { Insert the pragma, update last item in block }
      nLastWSItem ← gLastWSItem; gLastWSBlock↑.nItems.Insert(gLastWSItem);
end;
```

1216. Starting the proper text will just update the *nBlockPos* field to whatever the current position is.

⟨Extended block implementation 1206⟩ +≡

```
procedure extBlockObj.StartProperText;
begin gWSTextPropser↑.nBlockPos ← CurPos; end;
```

1217. Processing redefinitions sets the global variable *gRedefinitions* to the result of comparing the current word to the “redefine” keyword.

⟨Extended block implementation 1206⟩ +≡

```
procedure extBlockObj.ProcessRedefine;
begin gRedefinitions ← CurWord.Kind = sy_Redefine; end;
```

1218. When a block statement is linked, but it should not, then we raise a 164 error. Otherwise, be sure to mark the block as linked (i.e., toggle *nLinked* to be true) and assign the *nLinkPos* to be the current position.

⟨Extended block implementation 1206⟩ +≡

```
procedure extBlockObj.ProcessLink;
begin if CurWord.Kind ∈ [sy_Then, sy_Hence] then
      begin if nLinkProhibited then ErrImm(164);
          nLinked ← true; nLinkPos ← CurPos;
        end;
    end;
```

1219. Proof of a scheme. We should increment the proof depth global variable.

Recall that *ProofPragma* means “check the proof is valid?” In other words, when *ProofPragma* is false, we are skipping the proofs.

```

thesis-formula:macro-def
  define thesis_formula ≡ new(ThesisFormulaPtr, Init(CurPos))
  define thesis_prop ≡ new(PropositionPtr, Init(new(LabelPtr, Init(0, CurPos)), thesis_formula, CurPos))
  define skipped_proof_justification ≡ new(JustificationPtr, Init(infSkippedProof, CurPos))
  ⟨Extended block implementation 1206⟩ +≡
procedure extBlockObj.StartSchemeDemonstration;
begin inc(gProofCnt);
if ¬ProofPragma then ⟨Mark schema proof as “skipped” 1220⟩;
end;

```

1220. When we skip the proof (due to pragmas being set), we just add the scheme as a compact statement whose justification is the “skipped proof justification”.

First, we create a new text item for the proper text global variable. Then we set its content to the compact statement with the “skipped” justification. Finally we add this item to the “last” (latest) *wsBlock* global variable.

```

  ⟨Mark schema proof as “skipped” 1220⟩ ≡
    begin gLastWSItem ← gWsTextProper↑.NewItem(itConclusion, CurPos);
    gLastWSItem↑.nContent ← new(CompactStatementPtr, Init(thesis_prop, skipped_proof_justification));
    gLastWSBlock↑.nItems.Insert(gLastWSItem);
    end

```

This code is used in section 1219.

1221. Finishing the proof for a scheme should decrement the global “proof depth” counter.

```

  ⟨Extended block implementation 1206⟩ +≡
procedure extBlockObj.FinishSchemeDemonstration;
  begin dec(gProofCnt); end;

```

1222. The factory method for *extBlock* creating an item will update the global *gItemPtr* variable (§690).

```

  ⟨Extended block implementation 1206⟩ +≡
procedure extBlockObj.CreateItem(fItemKind : ItemKind);
  begin gItemPtr ← new(extItemPtr, Init(fItemKind)); end;

```

1223. The factory method for *extBlock* creating a new block will update the *gBlockPtr* global variable (§690).

```

  ⟨Extended block implementation 1206⟩ +≡
procedure extBlockObj.CreateBlock(fBlockKind : BlockKind);
  begin gBlockPtr ← new(extBlockPtr, Init(fBlockKind)) end;

```

Section 23.2. EXTENDED ITEM CLASS

1224. The class diagram for extended items looks like:

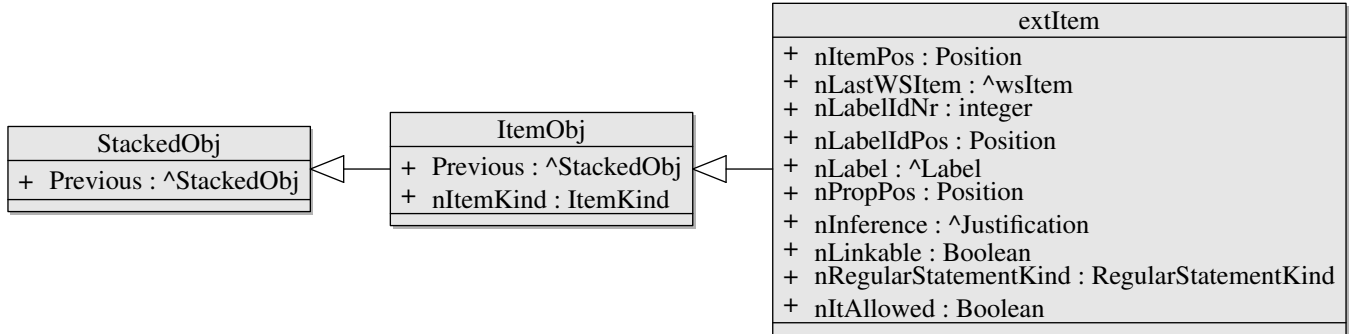


Fig. 7. Class hierarchy for *extItemObj*. The base *MObject* class omitted from the hierarchy.

Recall (§909) the regular statement kind is one of three possibilities: diffuse statement, compact statement, iterative equality.

The “Finish” methods updates the contents of the *extItem* class with a WSM abstract syntax tree for the statement.

Since this is a “stub”, I will just leave the placeholder chunk for the methods overridden by the extended Item class here (remove later).

⟨Methods overridden by extended Item class 706⟩ +≡

1225. ⟨Extended item class declaration 1225⟩ ≡
extItemPtr = ↑*extItemObj*;
extItemObj = **object** (*ItemObj*)
 nItemPos: *Position*;
 nLastWSItem: *WSItemPtr*;
 nLabelIdNr: *integer*;
 nLabelIdPos: *Position*;
 nLabel: *LabelPtr*;
 nPropPos: *Position*;
 nInference: *JustificationPtr*;
 nLinkable: *boolean*;
 nRegularStatementKind: *RegularStatementKind*;
 nItAllowed: *boolean*;
 constructor *Init* (*fKind* : *ItemKind*);
 procedure *Pop*; *virtual*;
 ⟨Methods overridden by extended Item class 706⟩
end ;

This code is used in section 1199.

Subsection 23.2.1. Constructor

1226. There are a number of comments in Polish which I haphazardly translated into English (“Przygotowanie definiensow:” translates as “Preparation of definiens:”; “Ew. zakaz przy obiektach ekspandowanych” translates as “Possible ban on expanded facilities”)

```

⟨ Extended item implementation 1226 ⟩ ≡
constructor extItemObj.Init(fKind : ItemKind);
  begin inherited Init(fKind);
  ⟨ Initialize the fields for newly allocated extItem object 1229 ⟩
  mizassert(2343, gLastWSBlock ≠ nil);
  if ¬(nItemKind ∈ [itReservation, itConstantDefinition, itExemplification, itGeneralization,
    itLocDeclaration]) then
    begin gLastWSItem ← gWsTextProper↑.NewItem(fKind, CurPos); nLastWSItem ← gLastWSItem;
    end;
  case nItemKind of
    ⟨ Initialize extended item by ItemKind 1230 ⟩
  endcases;
  if ¬(nItemKind ∈ [itReservation, itConstantDefinition, itExemplification, itGeneralization,
    itLocDeclaration]) then gLastWSBlock↑.nItems.Insert(gLastWSItem);
  end;

```

See also sections 1249, 1277, 1279, 1280, 1281, 1282, 1283, 1285, 1286, 1288, 1289, 1290, 1291, 1293, 1294, 1295, 1296, 1299, 1300, 1301, 1303, 1304, 1305, 1306, 1307, 1310, 1311, 1312, 1313, 1314, 1315, 1318, 1319, 1321, 1322, 1323, 1324, 1325, 1326, 1327, 1329, 1330, 1332, 1333, 1334, 1335, 1337, 1339, 1341, 1342, 1343, 1344, 1345, 1347, 1349, 1350, 1351, 1352, 1353, 1354, 1355, 1356, 1357, 1358, 1359, 1360, 1361, 1362, 1363, 1364, 1365, 1366, 1368, 1369, 1371, 1372, 1373, 1375, 1376, 1377, 1378, 1379, 1380, 1381, 1383, 1384, and 1385.

This code is used in section 1200.

1227. Initializing the fields. The *it_Allowed* global variable is toggled on and off when the parser encounters “guards” in conditional definitions, whereas the *nItAllowed* fields reflects whether the sort of definition allows “it” in the definiens.

```

⟨ Global variables introduced in parseraddition.pas 1202 ⟩ +≡
dol_Allowed: Boolean;
it_Allowed: Boolean;
in_AggrPattern: Boolean;
gLastType: TypePtr;
gLastTerm: TermPtr;
gDefiningWay: HowToDefine;

```

1228. ⟨ Local variables for parser additions 1209 ⟩ +≡
gClusterSort: *ClusterRegistrationKind*;
gDefiniens: *DefiniensPtr*;
gPartialDefs: *PList*;
nDefiniensProhibited: *boolean*;
gSpecification: *TypePtr*;

1229. \langle Initialize the fields for newly allocated *extItem* object 1229 $\rangle \equiv$
 $nItemPos \leftarrow CurPos$; $gClusterSort \leftarrow ExistentialRegistration$; $nItAllowed \leftarrow false$; $it_Allowed \leftarrow false$;
 { global variable! }
 $in_AggrPattern \leftarrow false$; $dol_Allowed \leftarrow false$; $gSpecification \leftarrow nil$; $gLastType \leftarrow nil$;
 $gLastFormula \leftarrow nil$; $gLastTerm \leftarrow nil$;
 { Preparation of definiens: }
 $nDefiniensProhibited \leftarrow false$;
 { Possible ban on expanded facilities }
 $gDefiningWay \leftarrow dfEmpty$; $gDefiniens \leftarrow nil$; $gPartialDefs \leftarrow nil$; $nLinkable \leftarrow false$;

This code is used in section 1226.

1230. Kind-specific initialization. Each kind of item may need some specific initialization. We work through all the cases. The first two cases considered are generalization (“**let** $\langle Qualified Variables \rangle$ **be** [such $\langle Conditions \rangle$]”) and existential assumptions (“**given** $\langle Qualified Variables \rangle$ **such** $\langle Conditions \rangle$ ”). Existential assumptions need to toggle the “has assumptions” field to true for the global block pointer.

\langle Initialize extended item by *ItemKind* 1230 $\rangle \equiv$
 $itGeneralization$: ; { **let** statements }
 $itExistentialAssumption$: $ExtBlockPtr(gBlockPtr) \uparrow .nHasAssumptions \leftarrow true$;

See also sections 1233, 1235, 1237, 1239, 1242, and 1246.

This code is used in sections 1226 and 1244.

1231. Property initialization. Initializing a property statement *Item* should raise an error when the property does not appear in the correct block.

- Defining a predicate can support the following properties: symmetry, reflectivity, irreflexivity, transitivity, connectedness, asymmetry.
- Functors can support: associativity, commutativity, idempotence, involutiveness, and projectivity properties.
- Modes can support the sethood property.

In all other situations, an error should be flagged (the user is trying to assert an invalid property).

\langle Global variables introduced in *parseraddition.pas* 1202 $\rangle + \equiv$
 $gDefKind$: *ItemKind*;

1232. \langle Local variables for parser additions 1209 $\rangle + \equiv$
 $gExpandable$: *boolean*;
 $gPropertySort$: *PropertyKind*;

1233. \langle Initialize extended item by *ItemKind* 1230 $\rangle + \equiv$
 $itProperty$: **begin** $gPropertySort \leftarrow PropertyKind(CurWord.Nr)$;
case $PropertyKind(CurWord.Nr)$ **of**
 $sySymmetry, syReflexivity, syIrreflexivity, syTransitivity, syConnectedness, syAsymmetry$:
if $gDefKind \neq itDefPred$ **then**
begin $ErrImm(81)$; $gPropertySort \leftarrow sErrProperty$; **end**;
 $syAssociativity, syCommutativity, syIdempotence$: **if** $gDefKind \neq itDefFunc$ **then**
begin $ErrImm(82)$; $gPropertySort \leftarrow sErrProperty$; **end**;
 $syInvolutiveness, syProjectivity$: **if** $gDefKind \neq itDefFunc$ **then**
begin $ErrImm(83)$; $gPropertySort \leftarrow sErrProperty$; **end**;
 $sySethood$: **if** $(gDefKind \neq itDefMode) \vee gExpandable$ **then**
begin $ErrImm(86)$; $gPropertySort \leftarrow sErrProperty$; **end**;
endcases;
end;

1234. Reconsider initialization. We need to allocate a new (empty) list for the list of terms being reconsidered.

⟨Global variables introduced in `parseraddition.pas` 1202⟩ +≡
gReconsiderList: *PList*;

1235. ⟨Initialize extended item by *ItemKind* 1230⟩ +≡
itReconsider: *gReconsiderList* ← *new(PList, Init(0))*;

1236. We can have in Mizar “**suppose that** *<statement>*” (as well as “**case that...**”). But in those cases, the statement cannot be linked to the next statement (i.e., the next statement cannot begin with “**then...**”). Assumptions without “**that**” are always linkable.

Theorems, “regular statements”, and conclusions are always linkable.

1237. ⟨Initialize extended item by *ItemKind* 1230⟩ +≡
itRegularStatement: *nLinkable* ← *true*;
itConclusion: *nLinkable* ← *true*;
itPerCases: ;
itCaseHead: **if** *AheadWord.Kind* ≠ *sy_That* **then** *nLinkable* ← *true*;
itSupposeHead: **if** *AheadWord.Kind* ≠ *sy_That* **then** *nLinkable* ← *true*;
itTheorem: *nLinkable* ← *true*;
itAxiom: **if** ¬*AxiomsAllowed* **then** *ErrImm*(66);
itChoice: ;

1238. Initializing an assumption. Collective assumptions (“**assume that** *<formula>*”) are not linkable, but single assumptions (“**assume** *<Proposition>*”) are linkable. The statement will introduce a list of premises, which will be tracked in the *gPremises* local variable for the module.

⟨Local variables for parser additions 1209⟩ +≡
gPremises: *PList*;

1239. ⟨Initialize extended item by *ItemKind* 1230⟩ +≡
itAssumption: **begin if** *AheadWord.Kind* ≠ *sy_That* **then** *nLinkable* ← *true*;
 gPremises ← *nil*;
end;

1240. Definition items. Definition items need to be initialized with some nuance. Some definitions permit “**it**” to be used in the definiens, but others do not. Mizar toggles the global variables tracking this here. There is a common set of things toggled which we have isolated as the WEB macro *initialize_definition_item* common to initializing all definition items.

The correctness conditions are determined at this point, as well.

define *initialize_definition_item* ≡ *gCorrectnessConditions* ← []; *gDefPos* ← *CurPos*;
 gDefKind ← *nItemKind*

⟨Global variables introduced in `parseraddition.pas` 1202⟩ +≡
gCorrectnessConditions: *CorrectnessConditionsSet*;

1241. ⟨Local variables for parser additions 1209⟩ +≡
gDefPos: *Position*;
gStructPrefixes: *PList*;

1242. \langle Initialize extended item by *ItemKind* 1230 $\rangle + \equiv$

```

itLocDeclaration: ;
itDefMode: begin nItAllowed  $\leftarrow$  true; gExpandable  $\leftarrow$  false; initialize_definition_item end;
itDefAttr: begin initialize_definition_item end;
itAttrSynonym: begin initialize_definition_item end;
itAttrAntonym: begin initialize_definition_item end;
itModeNotation: begin initialize_definition_item end;
itDefFunc: begin nItAllowed  $\leftarrow$  true; initialize_definition_item end;
itFuncNotation: begin initialize_definition_item; end;
itDefPred, itPredSynonym, itCluster, itIdentify, itReduction:
  begin initialize_definition_item; end;
itPropertyRegistration: begin initialize_definition_item; gPropertySort  $\leftarrow$  PropertyKind(CurWord.Nr);
  end;
itDefStruct: begin initialize_definition_item; gStructPrefixes  $\leftarrow$  new(PList, Init(0)); end;
itCanceled: begin ErrImm(88); end;

```

1243. Correctness conditions. Registrations and definitions need correctness conditions to ensure the well-definedness of adjective clusters and terms. The correctness conditions needed for a definition (or registration) are inserted into the *gCorrectnessConditions* variable. When the correctness condition is found, we remove it from the *gCorrectnessConditions* set.

\langle Global variables introduced in *parseraddition.pas* 1202 $\rangle + \equiv$

gRedefinitions: boolean;

1244. \langle Local variables for parser additions 1209 $\rangle + \equiv$

```

gCorrCondSort: CorrectnessKind;
 $\langle$  Initialize extended item by ItemKind 1230  $\rangle =$  itCorrCond:
  if CorrectnessKind(CurWord.Nr)  $\in$  gCorrectnessConditions then
    begin exclude(gCorrectnessConditions, CorrectnessKind(CurWord.Nr));
    gCorrCondSort  $\leftarrow$  CorrectnessKind(CurWord.Nr);
    if (gRedefinitions  $\wedge$  (gCorrCondSort = syCoherence)  $\wedge$  ExtBlockPtr(gBlockPtr) $\uparrow$ .nHasAssumptions)
      then ErrImm(243);
    end
  else begin ErrImm(72); gCorrCondSort  $\leftarrow$  CorrectnessKind(0); end;
itCorrectness: if (gRedefinitions  $\wedge$  ExtBlockPtr(gBlockPtr) $\uparrow$ .nHasAssumptions) then ErrImm(243);

```

1245. The last statement needing attention will be the **scheme** block. Note that *gLocalScheme* is not used anywhere.

\langle Local variables for parser additions 1209 $\rangle + \equiv$

gLocalScheme: boolean;

gSchemePos: Position;

1246. \langle Initialize extended item by *ItemKind* 1230 $\rangle + \equiv$

```

itDefinition, itSchemeHead, itReservation, itPrivFuncDefinition, itPrivPredDefinition, itConstantDefinition,
  itExemplification: ;
itCaseBlock: ;
itSchemeBlock: begin gLocalScheme  $\leftarrow$  CurWord.Kind  $\neq$  sy.Scheme; gSchemePos  $\leftarrow$  CurPos; end;

```

1247. Popping an extended item.

\langle Global variables introduced in *parseraddition.pas* 1202 $\rangle + \equiv$

gSchemeParams: PList;

1248. \langle Local variables for parser additions 1209 $\rangle + \equiv$

```

gPatternPos: Position;
gPattern: PatternPtr;
gNewPatternPos: Position;
gNewPattern: PatternPtr;
gSchemeIdNr: integer;
gSchemeIdPos: Position;
gSchemeConclusion: FormulaPtr;
gSchemePremises: PList;

```

Subsection 23.2.2. Popping

1249. Popping an item is invoked as part of *KillItem*, which occurs whenever (1) a semicolon is encountered, or (2) when starting a proof environment.

The contract for popping an item ensures the *nContent* field shall be populated for valid items.

NOTE: PASCAL has a set operation *include(set, element)* which adjoins an *element* to a *set*.

\langle Extended item implementation 1226 $\rangle + \equiv$

```

procedure extItemObj.Pop;
  var k: integer;
  begin gLastWSItem↑.nItemEndPos ← PrevPos;  $\langle$  Check for errors with definition items 1253  $\rangle$ 
   $\langle$  Update content of nLastWSItem based on type of item popped 1250  $\rangle$ ;
   $\langle$  Check the popped item's linkages are valid 1276  $\rangle$ ;
  if gDefiningWay ≠ dfEmpty then
    begin if gDefiniens↑.nDefSort = ConditionalDefiniens then
      include(gCorrectnessConditions, syConsistency);
    if gRedefinitions then include(gCorrectnessConditions, syCompatibility);
    end;
  inherited Pop; { (§704) }
  end;

```

1250. We will update the caller's *nLastWSItem*'s contents in most cases.

```

⟨ Update content of nLastWSItem based on type of item popped 1250 ⟩ ≡
  case nItemKind of
    itTheorem: nLastWSItem↑.nContent ← new(CompactStatementPtr, Init(new(PropositionPtr,
      Init(nLabel, gLastFormula, nPropPos)), nInference));
    ⟨ Pop a proof step 1254 ⟩
    itConclusion, itRegularStatement: ⟨ Pop a conclusion or regular statement 1261 ⟩
    itGeneralization, itLocDeclaration: ⟨ Pop a “let” statement 1263 ⟩
    ⟨ Pop a definition item 1264 ⟩
    itPredSynonym, itPredAntonym, itFuncNotation, itModeNotation, itAttrSynonym, itAttrAntonym:
      nLastWSItem↑.nContent ← new(NotationDeclarationPtr, Init(gNewPatternPos, nItemKind,
        gNewPattern, gPattern));
    ⟨ Pop a registration item 1272 ⟩
    itCorrCond: nLastWSItem↑.nContent ← new(CorrectnessConditionPtr, Init(nItemPos, gCorrCondSort,
      nInference));
    itCorrectness: nLastWSItem↑.nContent ← new(CorrectnessConditionsPtr, Init(nItemPos,
      gCorrectnessConditions, nInference));
    itProperty: nLastWSItem↑.nContent ← new(PropertyPtr, Init(nItemPos, gPropertySort, nInference));
    itSchemeHead: nLastWSItem↑.nContent ← new(SchemePtr, Init(gSchemeIdNr, gSchemeIdPos,
      gSchemeParams, gSchemePremises, gSchemeConclusion));
    ⟨ Pop skips remaining cases 1251 ⟩
  endcases

```

This code is used in section 1249.

1251. ⟨ Pop skips remaining cases 1251 ⟩ ≡

```

itPrivFuncDefinition, itPrivPredDefinition, itPragma, itDefinition, itSchemeBlock, itReservation,
  itExemplification, itCaseBlock: ;

```

This code is used in section 1250.

1252. Check for errors. We need to flag a 253 or 254 error when the user tries to introduce an axiom (which shouldn't occur much anymore, since axioms are not even documented anywhere).

```

⟨ Local variables for parser additions 1209 ⟩ +≡
  gMeansPos: Position;

```

1253. ⟨ Check for errors with definition items 1253 ⟩ ≡

```

case nItemKind of
  itDefPred, itDefFunc, itDefMode, itDefAttr: begin if gDefiningWay ≠ dfEmpty then
    begin if nDefiniensProhibited ∧ ¬AxiomsAllowed then
      begin Error(gMeansPos, 254); gDefiningWay ← dfEmpty; end;
    end
  else if ¬gRedefinitions ∧ ¬nDefiniensProhibited ∧ ¬AxiomsAllowed then SemErr(253);
  end;
endcases;

```

This code is used in section 1249.

1254. Pop a proof step. Popping a proof step should assign to the contents of the caller's *nLastWsItem* some kind of inference justification, usually in the form of a statement in the WSM syntax tree.

$\langle \text{Pop a proof step } 1254 \rangle \equiv$
itPerCases: *nLastWsItem*↑.*nContent* \leftarrow *nInference*;

See also sections 1255, 1257, and 1259.

This code is used in section 1250.

1255. Popping a reconsideration. We should assign a *TypeChangingStatement* to the content of the caller's last item, using the *nInference* field of the caller as the justification.

$\langle \text{Pop a proof step } 1254 \rangle + \equiv$
itReconsider: *nLastWsItem*↑.*nContent* \leftarrow *new*(*TypeChangingStatementPtr*, *Init*(*gReconsiderList*,
gLastType, *SimpleJustificationPtr*(*nInference*)));

1256. Popping existential elimination and introduction. We assign a *consider* (or *given*) WSM statement to the caller's previous *WSItem*'s contents when popping a choice (resp., existential assumption) item.

We should remind the reader of the grammar here:

$\langle \text{Qualified-Segment} \rangle ::= \langle \text{Variables} \rangle \langle \text{Qualification} \rangle$
 $\langle \text{Variables} \rangle ::= \langle \text{Variable} \rangle \{ \text{"}, \text{"} \langle \text{Variable} \rangle \}$
 $\langle \text{Qualification} \rangle ::= (\text{"being"} \mid \text{"be"}) \langle \text{Type-Expression} \rangle$

And, of course, a qualified-segment list is just a comma-separated list of qualified-segments.

$\langle \text{Global variables introduced in parseraddition.pas } 1202 \rangle + \equiv$
gQualifiedSegmentList: *PList*;

1257. $\langle \text{Pop a proof step } 1254 \rangle + \equiv$
itChoice: **begin** *nLastWsItem*↑.*nContent* \leftarrow *new*(*ChoiceStatementPtr*, *Init*(*gQualifiedSegmentList*,
gPremises, *SimpleJustificationPtr*(*nInference*))); *gPremises* \leftarrow **nil**;
end;
itExistentialAssumption: **begin** *nLastWsItem*↑.*nContent* \leftarrow *new*(*ExistentialAssumptionPtr*,
Init(*nItemPos*, *gQualifiedSegmentList*, *gPremises*)); *gPremises* \leftarrow **nil**;
end;

1258. Popping a stipulation. When we pop a *case*, *suppose*, or *assume* — some kind of “assumption”-like statement — we are assigning either a *CollectiveAssumption* object or a *SingleAssumption* object to the content of the *current WSItem global* variable.

$\langle \text{Local variables for parser additions } 1209 \rangle + \equiv$
gThatPos: *Position*;

1259. $\langle \text{Pop a proof step } 1254 \rangle + \equiv$
itSupposeHead, *itCaseHead*, *itAssumption*: **if** *gPremises* \neq **nil** **then**
begin *gLastWsItem*↑.*nContent* \leftarrow *new*(*CollectiveAssumptionPtr*, *Init*(*gThatPos*, *gPremises*));
gPremises \leftarrow **nil**;
end
else *gLastWsItem*↑.*nContent* \leftarrow *new*(*SingleAssumptionPtr*, *Init*(*nItemPos*, *new*(*PropositionPtr*,
Init(*nLabel*, *gLastFormula*, *nPropPos*))));

1260. Pop a conclusion or regular statement. We assign an appropriate WSM statement node to the previous item's contents.

⟨Local variables for parser additions 1209⟩ +≡
gIterativeSteps: *PList*;
gIterativeLastFormula: *FormulaPtr*;
gInference: *JustificationPtr*;

1261. ⟨Pop a conclusion or regular statement 1261⟩ ≡
case *nRegularStatementKind* **of**
stDiffuseStatement:
 nLastWSItem↑.*nContent* ← *new*(*DiffuseStatementPtr*, *Init*(*nLabel*, *stDiffuseStatement*));
stCompactStatement: *nLastWSItem*↑.*nContent* ← *new*(*CompactStatementPtr*, *Init*(*new*(*PropositionPtr*,
 Init(*nLabel*, *gLastFormula*, *nPropPos*)), *nInference*));
stIterativeEquality: *nLastWSItem*↑.*nContent* ← *new*(*IterativeEqualityPtr*, *Init*(*new*(*PropositionPtr*,
 Init(*nLabel*, *gIterativeLastFormula*, *nPropPos*)), *gInference*, *gIterativeSteps*));
endcases;

This code is used in section 1250.

1262. Pop a ‘let’ statement. For generic let statements of the form

$$\text{let } \vec{x}_1 \text{ be } T_1, \dots, \vec{x}_n \text{ be } T_n$$

we transform it to *n* statements of the form “let \vec{x} be *T*”, then add these to the *gLastWSBlock*’s items. When we have

$$\text{let } \vec{x} \text{ be } T \text{ such that } \Phi$$

we need to add a *CollectiveAssumption* node to the **global** *gLastWSBlock*’s items.

⟨Local variables for parser additions 1209⟩ +≡
gSuchPos: *Position*;

1263. ⟨Pop a “let” statement 1263⟩ ≡
begin for *k* ← 0 **to** *gQualifiedSegmentList*↑.*Count* − 1 **do**
 begin *gLastWSItem* ← *gWsTextProper*↑.*NewItem*(*nItemKind*,
 QualifiedSegmentPtr(*gQualifiedSegmentList*↑.*Items*↑[*k*]↑.*nSegmPos*);
 nLastWSItem ← *gLastWSItem*; *gLastWSItem*↑.*nContent* ← *gQualifiedSegmentList*↑.*Items*↑[*k*];
 if *k* = *gQualifiedSegmentList*↑.*Count* − 1 **then** *gLastWSItem*↑.*nItemEndPos* ← *PrevPos*
 else *gLastWSItem*↑.*nItemEndPos* ← *QualifiedSegmentPtr*(*gQualifiedSegmentList*↑.*Items*↑[*k* +
 1]↑.*nSegmPos*);
 gQualifiedSegmentList↑.*Items*↑[*k*] ← **nil**; *gLastWSBlock*↑.*nItems.Insert*(*gLastWSItem*);
 end;
 dispose(*gQualifiedSegmentList*, *Done*);
 if *gPremises* ≠ **nil** **then**
 begin *gLastWSItem* ← *gWsTextProper*↑.*NewItem*(*itAssumption*, *gSuchPos*);
 gLastWSItem↑.*nContent* ← *new*(*CollectiveAssumptionPtr*, *Init*(*gThatPos*, *gPremises*));
 gPremises ← **nil**; *gLastWSItem*↑.*nItemEndPos* ← *PrevPos*; *nLastWSItem* ← *gLastWSItem*;
 gLastWSBlock↑.*nItems.Insert*(*gLastWSItem*);
 end;
 end;

This code is used in section 1250.

1264. Pop a mode definition. A mode is either expandable (an abbreviation) or nonexpandable. For expandable modes, we just add a new *ExpandableModeDefinition* WSM object to the caller’s *nLastWSItem*’s contents.

On the other hand, non-expandable modes should add to the caller’s *nLastWSItem*’s contents a new *StandardModeDefinition* object. If this is not a redefinition, then we must add the “**existence**” correctness condition to the global variable *gCorrectnessConditions*.

```

⟨Pop a definition item 1264⟩ ≡
itDefMode: begin if gExpandable then nLastWSItem↑.nContent ← new(ExpandableModeDefinitionPtr,
    Init(gPatternPos, ModePatternPtr(gPattern), gLastType))
else begin nLastWSItem↑.nContent ← new(StandardModeDefinitionPtr, Init(gPatternPos,
    gRedefinitions, ModePatternPtr(gPattern), gSpecification, gDefiniens));
    if ¬gRedefinitions then include(gCorrectnessConditions, syExistence);
    end;
end;

```

See also sections 1265, 1266, 1267, and 1270.

This code is used in section 1250.

1265. Pop a functor definition. When popping a functor definition, we just add a *FunctorDefinition* object to the caller’s *nLastWSItem*’s contents.

```

⟨Pop a definition item 1264⟩ +≡
itDefFunc: begin nLastWSItem↑.nContent ← new(FunctorDefinitionPtr, Init(gPatternPos,
    gRedefinitions, FunctorPatternPtr(gPattern), gSpecification, gDefiningWay, gDefiniens));
end;

```

1266. Pop an attribute definition. We just need to add an *AttributeDefinition* object to the caller’s *nLastWSItem*’s contents.

```

⟨Pop a definition item 1264⟩ +≡
itDefAttr: begin nLastWSItem↑.nContent ← new(AttributeDefinitionPtr, Init(gPatternPos,
    gRedefinitions, AttributePatternPtr(gPattern), gDefiniens));
end;

```

1267. Pop a predicate definition. We just need to add a *PredicateDefinition* object to the caller’s *nLastWSItem*’s contents.

```

⟨Pop a definition item 1264⟩ +≡
itDefPred: begin nLastWSItem↑.nContent ← new(PredicateDefinitionPtr, Init(gPatternPos,
    gRedefinitions, PredicatePatternPtr(gPattern), gDefiniens));
end;

```

1268. Popping a structure definition. We just need to add a *StructureDefinition* object to the caller’s *nLastWSItem*’s contents.

```

⟨Global variables introduced in parseraddition.pas 1202⟩ +≡
gConstructorNr: integer;

```

```

1269. ⟨Local variables for parser additions 1209⟩ +≡
gParams: PList;
gStructFields: PList;

```

```

1270. ⟨Pop a definition item 1264⟩ +≡
itDefStruct: begin nLastWSItem↑.nContent ← new(StructureDefinitionPtr, Init(gPatternPos,
    gStructPrefixes, gConstructorNr, gParams, gStructFields));
end;

```

1271. Pop a cluster registration item. A “cluster” registration (i.e., a existential, conditional, or functor registration) adds to the caller’s *nLastWSItem*’s contents a new cluster object (of appropriate kind). The *gClusterSort* is populated when the parser finishes a cluster registration when invoking *extItemObj.FinishAntecedent* (§1281) or similar methods.

The *gClusterTerm* is populated in the *extItemObj.FinishClusterTerm* method (§1282).

⟨Local variables for parser additions 1209⟩ +≡
gAntecedent, *gConsequent*: *PList*;
gClusterTerm: *TermPtr*;

1272. ⟨Pop a registration item 1272⟩ ≡
itCluster: **begin case** *gClusterSort* **of**
 ExistentialRegistration: **begin**
 nLastWSItem↑.*nContent* ← *new*(*EClusterPtr*, *Init*(*nItemPos*, *gConsequent*, *gLastType*));
 include(*gCorrectnessConditions*, *syExistence*)
 end;
 ConditionalRegistration: **begin** *nLastWSItem*↑.*nContent* ← *new*(*CClusterPtr*, *Init*(*nItemPos*,
 gAntecedent, *gConsequent*, *gLastType*)); *include*(*gCorrectnessConditions*, *syCoherence*);
 end;
 FunctorialRegistration: **begin** *nLastWSItem*↑.*nContent* ← *new*(*FClusterPtr*, *Init*(*nItemPos*,
 gClusterTerm, *gConsequent*, *gLastType*)); *include*(*gCorrectnessConditions*, *syCoherence*);
 end;
endcases;
end;

See also section 1275.

This code is used in section 1250.

1273. Pop a registration item. For an *identify* or *reduce* registration, we assign the content of the caller’s *nLastWSItem* a new *IdentifyRegistration* (resp., *ReduceRegistration*) object. Identify registrations use the *gIdentifyEqLocList* local variable, while the reduction registrations use the *gLeftTermInReduction* module-wide variable.

⟨Global variables introduced in *parseraddition.pas* 1202⟩ +≡
gLeftTermInReduction: *TermPtr*;

1274. ⟨Local variables for parser additions 1209⟩ +≡
gIdentifyEqLocList: *PList*;

1275. ⟨Pop a registration item 1272⟩ +≡
itIdentify: **begin** *nLastWSItem*↑.*nContent* ← *new*(*IdentifyRegistrationPtr*, *Init*(*nItemPos*, *gNewPattern*,
 gPattern, *gIdentifyEqLocList*)); *include*(*gCorrectnessConditions*, *syCompatibility*);
end;
itReduction: **begin** *nLastWSItem*↑.*nContent* ← *new*(*ReduceRegistrationPtr*, *Init*(*nItemPos*,
 gLeftTermInReduction, *gLastTerm*)); *include*(*gCorrectnessConditions*, *syReducibility*);
end;
itPropertyRegistration: *SethoodRegistrationPtr*(*nLastWSItem*↑.*nContent*)↑.*nJustification* ← *nInference*;

1276. Check linkages are valid. When popping an item, we should check if the block containing the caller is *nLinked*. If so, flag a “178” error and assign *nLinked* \leftarrow *false*. Update the block’s *nLinkAllowed* depending on the caller’s *nLinkable* field. But if the parser is in panic mode, the containing block’s *nLinkAllowed* and *nLinkProhibited* are both assigned to false. [[This configuration appears to encode a particular state which feels a bit of a “kludge” to me...]]

```

⟨ Check the popped item’s linkages are valid 1276 ⟩ ≡
  with extBlockPtr(gBlockPtr)↑ do
    begin if nLinked then
      begin Error(nLinkPos, 178); nLinked  $\leftarrow$  false end;
      nLinkAllowed  $\leftarrow$  nLinkable; nLinkProhibited  $\leftarrow$  ¬nLinkable;
    if ¬StillCorrect then
      begin nLinkAllowed  $\leftarrow$  false; nLinkProhibited  $\leftarrow$  false end;
    end

```

This code is used in section 1249.

Subsection 23.2.3. Registrations and notations

1277. Processing synonyms. We need to update the *gNewPatternPos* and *gNewPattern* global variables when processing a synonym.

```

  define process_notation_item ≡ gNewPatternPos  $\leftarrow$  gPatternPos; gNewPattern  $\leftarrow$  gPattern
⟨ Extended item implementation 1226 ⟩ +≡
procedure extItemObj.ProcessModeSynonym;
  begin process_notation_item; end;
procedure extItemObj.ProcessAttrSynonym;
  begin process_notation_item; end;
procedure extItemObj.ProcessAttrAntonym;
  begin process_notation_item; end;
procedure extItemObj.ProcessPredSynonym;
  begin process_notation_item; end;
procedure extItemObj.ProcessPredAntonym;
  begin process_notation_item; end;
procedure extItemObj.ProcessFuncSynonym;
  begin process_notation_item; end;

```

1278. Starting attributes. This is used when the parser encounters a cluster registration (§1594). The *gAttrColl* is populated in the *extSubexpObj.CompleteAdjectiveCluster* (§1398) method.

```

⟨ Local variables for parser additions 1209 ⟩ +≡
gAttrColl: PList;

```

```

1279. ⟨ Extended item implementation 1226 ⟩ +≡
procedure extItemObj.StartAttributes;
  begin gAttrColl  $\leftarrow$  new(PList, Init(6));
  end;

```

1280. Starting a sentence. We just need to populate the caller's $nPropPos$, assigning to it the current position of the parser.

⟨Extended item implementation 1226⟩ $\vdash \equiv$
procedure *extItemObj.StartSentence*;
 begin $nPropPos \leftarrow CurPos$;
 end;

1281. Processing conditional registration. This populates the $gClusterSort$ and the related global variables, as the parser finishes parsing the antecedent and consequent to the cluster.

⟨Extended item implementation 1226⟩ $\vdash \equiv$
procedure *extItemObj.FinishAntecedent*;
 begin $gClusterSort \leftarrow ConditionalRegistration$; $gAntecedent \leftarrow gAttrColl$;
 end;
procedure *extItemObj.FinishConsequent*;
 begin $gConsequent \leftarrow gAttrColl$;
 end;

1282. Finishing a cluster. This populates the $gClusterSort$ and the $gClusterTerm$.

⟨Extended item implementation 1226⟩ $\vdash \equiv$
procedure *extItemObj.FinishClusterTerm*;
 begin $gClusterSort \leftarrow FunctorialRegistration$; $gClusterTerm \leftarrow gLastTerm$;
 end;

1283. Identify registration. Schematically, we have the registration statement look like (using global variable names for the subexpressions):

identify $\langle gNewPattern \rangle$ **with** $\langle gPattern \rangle$ [**when** $\langle gIdentifyEqLocList \rangle$];

We store the first pattern in the $gNewPattern$ global variable, then the second pattern in the $gPattern$ global variable. Completing the identify registration will check if the current word is “when” and, if so, start a list of loci equalities.

⟨Extended item implementation 1226⟩ $\vdash \equiv$
procedure *extItemObj.StartFuncIdentify*;
 begin end;
procedure *extItemObj.ProcessFuncIdentify*;
 begin $gNewPatternPos \leftarrow gPatternPos$; $gNewPattern \leftarrow gPattern$;
 end;
procedure *extItemObj.CompleteFuncIdentify*;
 begin $gIdentifyEqLocList \leftarrow \text{nil}$;
 if $CurWord.Kind = sy_When$ **then** $gIdentifyEqLocList \leftarrow new(PList, Init(0))$;
 end;

1284. “Reduces to” registrations. Recall, these schematically look like

reduce $\langle gLeftLocus \rangle$ **to** $\langle Locus \rangle$;

Mizar will populate $gLeftLocus$. The gambit will be to treat this as a functor pattern; i.e., the $gLeftLocus$ will be used to populate $gNewPattern$ in the method *extItemObj.FinishFunctorPattern* (§1323).

⟨Local variables for parser additions 1209⟩ $\vdash \equiv$
 $gLeftLocus: LocusPtr$;

1285. $\langle \text{Extended item implementation 1226} \rangle + \equiv$
procedure *extItemObj.ProcessLeftLocus*;
 begin *gLeftLocus* \leftarrow *new*(*LocusPtr*, *Init*(*CurPos*, *GetIdentifier*));
 end;
procedure *extItemObj.ProcessRightLocus*;
 begin *gIdentifyEqLocList.Insert*(*new*(*LociEqualityPtr*, *Init*(*PrevPos*, *gLeftLocus*, *new*(*LocusPtr*,
 Init(*CurPos*, *GetIdentifier*))));
 end;
procedure *extItemObj.StartFuncReduction*;
 begin end;
procedure *extItemObj.ProcessFuncReduction*;
 begin *gNewPatternPos* \leftarrow *gPatternPos*; *gLeftTermInReduction* \leftarrow *gLastTerm*;
 end;

Subsection 23.2.4. Processing definitions

1286. The terminology used by the parser appears to be (§§1558 *et seq.*):

let $\langle \textit{Fixed Variables} \rangle$;

and

consider $\langle \textit{Fixed Variables} \rangle$ **such that**...

This would mean that we would have “fixed variables” refer to a list of qualified segments. We remind the reader of the grammar

$$\begin{aligned} \langle \textit{Fixed-Variables} \rangle &::= \langle \textit{Implicitly-Qualified-Variables} \rangle \{ \text{"}, \text{"} \langle \textit{Fixed-Variables} \rangle \} \\ &\quad | \langle \textit{Explicitly-Qualified-Variables} \rangle \{ \text{"}, \text{"} \langle \textit{Fixed-Variables} \rangle \} \\ \langle \textit{Implicitly-Qualified-Variables} \rangle &::= \langle \textit{Variables} \rangle \\ \langle \textit{Explicitly-Qualified-Variables} \rangle &::= \langle \textit{Qualified-Segment} \rangle \{ \text{"}, \text{"} \langle \textit{Qualified-Segment} \rangle \} \\ \langle \textit{Qualified-Segment} \rangle &::= \langle \textit{Variables} \rangle \langle \textit{Qualification} \rangle \\ \langle \textit{Variables} \rangle &::= \langle \textit{Variable} \rangle \{ \text{"}, \text{"} \langle \textit{Variable} \rangle \} \\ \langle \textit{Qualification} \rangle &::= (\text{"be"} | \text{"being"}) \langle \textit{Type} \rangle \end{aligned}$$

The “fixed variables” routine in the parser will parse a comma-separated list of qualified variables.

CAUTION: The grammar in the `syntax.txt` file is actually more strict than this, because it actually states the following:

$$\langle \textit{Loci-Declaration} \rangle ::= \text{"let"} \langle \textit{Qualified-Variables} \rangle [\text{"such"} \langle \textit{Conditions} \rangle] ;$$

The grammar for a qualified segment *requires* implicitly qualified variables appear at the very end.

$\langle \text{Extended item implementation 1226} \rangle + \equiv$
procedure *extItemObj.StartFixedVariables*;
 begin *gQualifiedSegmentList* \leftarrow *new*(*PList*, *Init*(0));
 end;

1287. $\langle \text{Global variables introduced in parseraddition.pas 1202} \rangle + \equiv$
gQualifiedSegment: *MList*;
gSegmentPos: *Position*;

1288. Fixed segments. This refers to each “explicitly qualified segment” or “implicitly qualified segment” appearing in the fixed variables portion. The fixed segments are separated by commas.

⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.StartFixedSegment;
  begin gQualifiedSegment.Init(0); gSegmentPos ← CurPos;
  end;
```

1289. When parsing fixed variables, and the parser has just entered the loop to parse fixed variables, this function will be invoked.

⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.ProcessFixedVariable;
  begin gQualifiedSegment.Insert(new(VariablePtr, Init(CurPos, GetIdentifier)));
  end;
```

1290. This “clears the cache” for assigning the type in an explicitly qualified segment (appearing in a fixed variable segment).

⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.ProcessBeing;
  begin gLastType ← nil;
  end;
```

1291. The last statement in the parser loop when parsing “fixed variables” is to push the “fixed segment” onto the *gQualifiedSegmentList* global variable. There are two cases to consider: the implicitly qualified variables and the explicitly qualified variables.

The implicitly qualified case simply *moves* the pointers around “manually”, so we need to update every entry of *gQualifiedSegment.Items* to be **nil**. The explicitly qualified case moves the pointers around using the *MList* constructor, mutating *gQualifiedSegment* into a list of **nil** pointers.

⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.FinishFixedSegment;
  var k: integer;
  begin if gLastType ≠ nil then { explicitly qualified case }
    begin gQualifiedSegmentList↑.Insert(new(ExplicitlyQualifiedSegmentPtr, Init(gSegmentPos,
      new(PList, MoveList(gQualifiedSegment)), gLastType))); gQualifiedSegment.DeleteAll;
    end
  else begin for k ← 0 to gQualifiedSegment.Count − 1 do
    begin gQualifiedSegmentList↑.Insert(new(ImplicitlyQualifiedSegmentPtr,
      Init(VariablePtr(gQualifiedSegment.Items↑[k]↑.nVarPos, gQualifiedSegment.Items↑[k])));
      gQualifiedSegment.Items↑[k] ← nil;
    end;
  end;
  gQualifiedSegment.Done;
  end;
```

1292. When we finish parsing fixed variables, we need to “unset” the *gPremises* global variable. The parser will either be looking at a semicolon token or at “**such** ⟨*Conditions*⟩”. The reader should note that *gSuchThatOcc* is not used in the parser, nor anywhere else in Mizar. But we recall (§1262) the *gSuchPos* is used when popping a **let** statement.

⟨Local variables for parser additions 1209⟩ +≡

```
gSuchThatOcc: boolean; { not used }
```

1293. $\langle \text{Extended item implementation 1226} \rangle + \equiv$

```
procedure extItemObj.FinishFixedVariables;
  begin gSuchThatOcc  $\leftarrow$  CurWord.Kind = sy_Such; gSuchPos  $\leftarrow$  CurPos; gPremises  $\leftarrow$  nil;
  end;
```

1294. When the parser encounters the statement:

let $\langle \textit{Fixed-Variables} \rangle$ **such that** $\langle \textit{Assumption} \rangle$;

The first things it does when encountering the “**such**” token is move to the next token (“**that**”) and then invoke the *StartAssumption* method. We should allocate a fresh list for *gPremises* and mark the position of the “**that**” token.

$\langle \text{Extended item implementation 1226} \rangle + \equiv$

```
procedure extItemObj.StartAssumption;
  begin gPremises  $\leftarrow$  new(PList, Init(0)); gThatPos  $\leftarrow$  CurPos;
  end;
```

1295. Finishing an assumption will update the global variable *gBlockPtr*’s field reflecting it has assumptions.

$\langle \text{Extended item implementation 1226} \rangle + \equiv$

```
procedure extItemObj.FinishAssumption;
  begin ExtBlockPtr(gBlockPtr)↑.nHasAssumptions  $\leftarrow$  true;
  end;
```

1296. When the Mizar parser has encountered

assume that $\langle \textit{Conditions} \rangle$;

we start a collective assumption when the parser has just encountered the “**that**” token. As with the “**let** statement with assumptions”, we need to allocate a new list for *gPremises* and assign the *gThatPos* to the current position.

$\langle \text{Extended item implementation 1226} \rangle + \equiv$

```
procedure extItemObj.StartCollectiveAssumption;
  begin gPremises  $\leftarrow$  new(PList, Init(0)); gThatPos  $\leftarrow$  CurPos;
  end;
```

1297. Processing copula in a definition. When defining a (nonexpandable) mode, a functor, a predicate, or an attribute, we have

$$\langle Pattern \rangle \text{ means } \langle Expression \rangle;$$

or

$$\langle Pattern \rangle \text{ equals } \langle Expression \rangle;$$

The expression may or may not be labeled, we may or may not have the definition-by-cases. Whatever the situation, we should initialize the variables describing the definiens:

- the *gDefLabId* should be reset to zero (and populated in the *ProcessDefLabel* method);
- the *gDefLabPos* should be reset to the current position (and populated in the *ProcessDefLabel* method);
- the *gDefiningWay* should be assigned to *dfMeans* or *dfEquals* depending on the copula used in the definition;
- the *gOtherwise* pointer should be assigned to **nil**;
- the *gMeansPos* position should be assigned to the current position.

Following tradition in logic, we will refer to “means” and “equals” as the “**Copula**” in the definition.

\langle Global variables introduced in [parseraddition.pas 1202](#) $\rangle + \equiv$

gDefLabId: integer;

gDefLabPos: Position;

1298. \langle Local variables for parser additions [1209](#) $\rangle + \equiv$

gOtherwise: PObject;

1299. \langle Extended item implementation [1226](#) $\rangle + \equiv$

procedure *extItemObj.ProcessMeans*;

begin *gDefLabId* \leftarrow 0; *gDefLabPos* \leftarrow *CurPos*; *gDefiningWay* \leftarrow *dfMeans*; *gOtherwise* \leftarrow **nil**;
gMeansPos \leftarrow *CurPos*
end;

procedure *extItemObj.ProcessEquals*;

begin *gDefLabId* \leftarrow 0; *gDefLabPos* \leftarrow *CurPos*; *gDefiningWay* \leftarrow *dfEquals*; *gOtherwise* \leftarrow **nil**;
gMeansPos \leftarrow *CurPos*;
end;

1300. When parsing a definition-by-cases, the cases are terminated with an “otherwise” keyword. Recall the grammar for such definitions looks like:

$$\langle Partial-Definiens-List \rangle \text{ "otherwise" } \langle Expression \rangle;$$

What happens depends on whether the definition uses “means” or “equals”: in the former case, we should update the *gOtherwise* pointer to be the *gLastFormula*; in the latter case, we should update the *gOtherwise* to be the *gLastTerm*.

\langle Extended item implementation [1226](#) $\rangle + \equiv$

procedure *extItemObj.FinishOtherwise*;

begin if *gDefiningWay* = *dfEquals* **then** *gOtherwise* \leftarrow *gLastTerm*
else *gOtherwise* \leftarrow *gLastFormula*;
end;

1301. Starting a definiens should mutate the *it_Allowed* global variable to be equal to the caller's *nItAllowed* field. The *it_Allowed* global variable is toggled on and off when the parser encounters “guards” in conditional definitions, whereas the *nItAllowed* fields reflects whether the sort of definition allows “it” in the definiens.

⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.StartDefiniens;
  begin it_Allowed ← nItAllowed;
  end;
```

1302. “Guards” refers to the conditions in a definition-by-cases. Specifically, we have

$$\langle \textit{Partial-Definiens} \rangle ::= \langle \textit{Expression} \rangle \text{ "if" } \langle \textit{Guard-Formula} \rangle$$

be the grammar for one particular case. We have a comma-separated list of partial definiens, so whenever the parser (a) first encounters the “if” keyword in a definiens, or (b) has already encountered the “if” keyword and now has encountered a comma — these are the two cases to start a new guard.

⟨Local variables for parser additions 1209⟩ +≡

gPartDef: *PObject*;

1303. ⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.StartGuard;
  begin if gPartialDefs = nil then gPartialDefs ← new(PList, Init(0));
  it_Allowed ← false;
  if gDefiningWay = dfMeans then gPartDef ← gLastFormula
  else gPartDef ← gLastTerm;
  end;
```

1304. After parsing a formula, then the parser will invoke *FinishGuard*. This will append to *gPartialDefs* a new partial definiens.

⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.FinishGuard;
  begin it_Allowed ← nItAllowed;
  case gDefiningWay of
    dfMeans: gPartialDefs.Insert(new(PartDefPtr, Init(new(DefExpressionPtr, Init(exFormula, gPartDef)), gLastFormula)));
    dfEquals: gPartialDefs.Insert(new(PartDefPtr, Init(new(DefExpressionPtr, Init(exTerm, gPartDef)), gLastFormula)));
  endcases;
  end;
```

1305. Recall for functor definitions we have something like:

```
func  $\langle Pattern \rangle \rightarrow \langle Type \rangle$  ( means | equals ) ...
```

Similarly, nonexpandable modes look like

```
mode  $\langle Pattern \rangle \rightarrow \langle Type \rangle$  means ...
```

The “ $\rightarrow \langle Type \rangle$ ” is called the [type] *specification* for the definition. We should update the *gSpecification* global variable to point to whatever the last type parsed was — which is stored in the *gLastType* global variable.

```
 $\langle$  Extended item implementation 1226  $\rangle + \equiv$   
procedure extItemObj.FinishSpecification;  
  begin gSpecification  $\leftarrow$  gLastType;  
  end;
```

1306. “Construction type” is the term used by the parser for “nonexpandable modes”. They, too, have a type specification. The *FinishConstructionType* populates the *gSpecification* global variable with this type.

```
 $\langle$  Extended item implementation 1226  $\rangle + \equiv$   
procedure extItemObj.FinishConstructionType;  
  begin gSpecification  $\leftarrow$  gLastType;  
  end;
```

1307. Expandable mode definitions, after encountering the “is” keyword, invokes the *StartExpansion* method. This just ensures there is no definiens, and the *gExpandable* global variable is assigned to “true”.

```
 $\langle$  Extended item implementation 1226  $\rangle + \equiv$   
procedure extItemObj.StartExpansion;  
  begin if gRedefinitions then ErrImm(271);  
    nDefiniensProhibited  $\leftarrow$  true; gExpandable  $\leftarrow$  true;  
  end;
```

1308. The parser, when determining the pattern for an attribute (§1579), resets the state when starting to determine the pattern for the attribute. This is handled by the *StartAttribute* method.

We should remind the reader that attributes can only have arguments *to its left*.

```
 $\langle$  Global variables introduced in parseraddition.pas 1202  $\rangle + \equiv$   
gParamNbr: integer;
```

1309. \langle Local variables for parser additions 1209 $\rangle + \equiv$
gLocus: *LocusPtr*;

```
 $\langle$  Extended item implementation 1226  $\rangle + \equiv$   
procedure extItemObj.StartAttributePattern;  
  begin gParamNbr  $\leftarrow$  0; gParams  $\leftarrow$  nil; gLocus  $\leftarrow$  new(LocusPtr, Init(CurPos, GetIdentifier));  
  end;
```


1311. Since an attribute can only have attributes to its left, it's pretty clear when the attribute pattern has been parsed: the parser has found the attribute being defined. In that case (assuming we're not panicking), we should add the attribute format to the *gFormatsColl* dictionary and update the global variables.

⟨Extended item implementation 1226⟩ +≡

procedure *extItemObj.FinishAttributePattern*;

var *lFormatNr*: integer;

begin *lFormatNr* ← 0;

if (*CurWord.Kind* = *AttributeSymbol*) ∧ *stillcorrect* **then**

lFormatNr ← *gFormatsColl.CollectPrefixForm*(*ˆVˆ*, *CurWord.Nr*, *gParamNbr*);

gPatternPos ← *CurPos*; *gConstructorNr* ← *CurWord.Nr*;

gPattern ← *new*(*AttributePatternPtr*, *Init*(*gPatternPos*, *gLocus*, *gConstructorNr*, *gParams*));

end;

1312. A mode definition may include a “sethood” property. This particular function is used when registering sethood in a registration block.

⟨Extended item implementation 1226⟩ +≡

procedure *extItemObj.FinishSethoodProperties*;

begin

nLastWSItem↑.*nContent* ← *new*(*SethoodRegistrationPtr*, *Init*(*nItemPos*, *gPropertySort*, *gLastType*));

end;

1313. We remind the reader the grammar for a mode pattern

$$\langle \textit{Mode-Pattern} \rangle ::= \langle \textit{Mode-Symbol} \rangle [\textit{"of"} \langle \textit{Loc} \rangle]$$

The loci parameters can only appear *after* the mode symbol (and before the “of” reserved keyword). Starting a mode pattern should reset the relevant global variables.

⟨Extended item implementation 1226⟩ +≡

procedure *extItemObj.StartModePattern*;

begin *gParamNbr* ← 0; *gParams* ← **nil**; *gPatternPos* ← *CurPos*; *gConstructorNr* ← *CurWord.Nr*;

end;

1314. Finishing a mode pattern should build a new *ModePatternObj*, and store it in the *gPattern* global variable. And if we are not panicking, we should add it to the *gFormatsColl* dictionary.

⟨Extended item implementation 1226⟩ +≡

procedure *extItemObj.FinishModePattern*;

var *lFormatNr*: integer;

begin *lFormatNr* ← 0;

if *StillCorrect* **then** *lFormatNr* ← *gFormatsColl.CollectPrefixForm*(*ˆMˆ*, *gConstructorNr*, *gParamNbr*);

gPattern ← *new*(*ModePatternPtr*, *Init*(*gPatternPos*, *gConstructorNr*, *gParams*));

end;

1315. When parser starts parsing a new predicate pattern, we should reset the relevant global variables.

⟨Extended item implementation 1226⟩ +≡

procedure *extItemObj.StartPredicatePattern*;

begin *gParamNbr* ← 0; *gParams* ← **nil**;

end;

1316. When the parser tries to parse a “predicative formula” (i.e., a formula involving a predicate) — including predicate patterns — the first thing it does is invoke this *ProcessPredicateSymbol* method. This resets the global variables needed to populate the arguments to the predicate in the formula.

⟨Global variables introduced in *parseraddition.pas* 1202⟩ +≡

gLeftLocaNbr: integer;

1317. ⟨Local variables for parser additions 1209⟩ +≡

gLeftLoc: *PList*;

1318. ⟨Extended item implementation 1226⟩ +≡

procedure *extItemObj.ProcessPredicateSymbol*;

begin *gPatternPos* ← *CurPos*; *gLeftLocaNbr* ← *gParamNbr*; *gLeftLoc* ← *gParams*; *gParamNbr* ← 0;
gParams ← **nil**; *gConstructorNr* ← *CurWord.Nr*;
end;

1319. Finishing a predicate pattern will create a new *PredicatePattern* object, update the *gPattern* global variable to point to it, and (if the parser is not panicking) add the predicate’s format to the *gFormatsColl* dictionary.

⟨Extended item implementation 1226⟩ +≡

procedure *extItemObj.FinishPredicatePattern*;

var *lFormatNr*: integer;
begin *lFormatNr* ← 0;
if *StillCorrect* **then**
 lFormatNr ← *gFormatsColl.CollectPredForm*(*gConstructorNr*, *gLeftLocaNbr*, *gParamNbr*);
 gPattern ← *new*(*PredicatePatternPtr*, *Init*(*gPatternPos*, *gLeftLoc*, *gConstructorNr*, *gParams*));
end;

1320. Functor patterns a bit trickier. When starting one, what should occur depends on the type of functor being defined. Specifically, we handle brackets differently than other functors, and within the brackets we handle braces (i.e., definitions like $\{x_1, \dots, x_n\}$) differently than square brackets ($[x_1, \dots, x_n]$) differently than everything other functor bracket.

In all cases, even non-bracket functors, we need to reset the *gParamNbr* and *gParams* global variables so they may be populated correctly.

⟨Global variables introduced in *parseraddition.pas* 1202⟩ +≡

gSubItemKind: *TokenKind*;

1321. ⟨Extended item implementation 1226⟩ +≡

procedure *extItemObj.StartFunctorPattern*;

begin *gPatternPos* ← *CurPos*; *gSubItemKind* ← *CurWord.Kind*;
case *CurWord.Kind* **of**
 LeftCircumfixSymbol: *gConstructorNr* ← *CurWord.Nr*;
 sy_LeftSquareBracket: **begin** *gSubItemKind* ← *LeftCircumfixSymbol*; *gConstructorNr* ← *SquareBracket*
 end;
 sy_LeftCurlyBracket: **begin** *gSubItemKind* ← *LeftCircumfixSymbol*; *gConstructorNr* ← *CurlyBracket*
 end;
 othercases *gConstructorNr* ← 0;
endcases; *gParamNbr* ← 0; *gParams* ← **nil**;
end;

1322. For “non-bracket” functors (i.e., infix operators), the functor pattern is processed by (1) getting the left parameters, (2) processing the functor symbol, (3) getting the right parameters. This function is precisely step (2).

⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.ProcessFunctorSymbol;
  begin gPatternPos ← CurPos;
  if CurWord.Kind = InfixOperatorSymbol then
    begin gSubItemKind ← InfixOperatorSymbol; gConstructorNr ← CurWord.Nr;
    gLeftLociNbr ← gParamNbr; gLeftLocs ← gParams; gParamNbr ← 0; gParams ← nil;
    end;
  end;
```

1323. When defining a bracket functor pattern, we add a new bracket format to the *gFormatsColl* dictionary, and then set *gPattern* to a newly allocated Bracket pattern.

When defining an infix functor, we add a new functor format to the *gFormatsColl* dictionary, and then we set the *gPattern* to a newly allocated infix functor pattern.

The “other cases” constructs an infix functor pattern, but does not add the form to the *gFormatsColl* dictionary.

⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.FinishFunctorPattern;
  var lConstructorNr, lFormatNr: integer;
  begin lFormatNr ← 0;
  case gSubItemKind of
    LeftCircumfixSymbol: begin lConstructorNr ← CurWord.Nr;
      if StillCorrect then
        lFormatNr ← gFormatsColl.CollectBracketForm(gConstructorNr, lConstructorNr, gParamNbr, 0, 0);
        gPattern ← new(CircumfixFunctorPatternPtr, Init(gPatternPos, gConstructorNr, lConstructorNr,
          gParams));
        end;
      InfixOperatorSymbol: begin if StillCorrect then
        lFormatNr ← gFormatsColl.CollectFuncForm(gConstructorNr, gLeftLocsNbr, gParamNbr);
        gPattern ← new(InfixFunctorPatternPtr, Init(gPatternPos, gLeftLocs, gConstructorNr, gParams));
        end;
      othercases
        gPattern ← new(InfixFunctorPatternPtr, Init(gPatternPos, gLeftLocs, gConstructorNr, gParams));
      endcases;
  end;
```

1324. The Parser’s *ReadVisible* procedure begins by invoking this *StartVisible* method. The *ReadVisible* procedure occurs when getting most patterns.

⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.StartVisible;
  begin gParams ← new(PList, Init(0));
  end;
```

1325. The parser iteratively calls its *GetVisible* procedure when *ReadVisible* arguments in a pattern. The *GetVisible* procedure in turn invokes this *ProcessVisible*, which increments the number of parameters, and pushes a new *Locus* object onto the *gParams* stack.

⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.ProcessVisible;
begin inc(gParamNbr);
if gParams ≠ nil then gParams↑.Insert(new(LocusPtr, Init(CurPos, GetIdentifier)));
end;
```

1326. Recall a structure definition, when it has ancestors, looks like

struct (⟨*Ancestors*⟩) ⟨*Structure-Symbol*⟩ ...

The ⟨*Ancestors*⟩ field is considered the “prefix” to the structure definition. The Parser parses a type (thereby populating the *gLastType* global variable), then invokes the *FinishPrefix* method, then iterates if it encounters a comma.

The *FinishPrefix* method pushes the *gLastType* global variable to the *gStructPrefixes* state variable.

⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.FinishPrefix;
begin gStructPrefixes.Insert(gLastType);
end;
```

1327. ⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.ProcessStructureSymbol;
var lFormatNr: integer;
begin gConstructorNr ← 0; gPatternPos ← CurPos;
if CurWord.Kind = StructureSymbol then gConstructorNr ← CurWord.Nr;
lFormatNr ← gFormatsColl.CollectPrefixForm(ˆJˆ, gConstructorNr, 1); gParamNbr ← 0;
gParams ← nil;
end;
```

1328. When the Parser has just finished parsing the ancestors to a structure, but has not parsed the visible arguments. Then the Parser prepares for reading the visible arguments and then the fields by invoking this method. This initializes the *gStructFields* state variable as well as the *gFieldsNbr* state variable.

⟨Global variables introduced in *parseraddition.pas* 1202⟩ +≡

gFieldsNbr: *integer*;

1329. ⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.StartFields;
var lFormatNr: integer;
begin lFormatNr ← gFormatsColl.CollectPrefixForm(ˆLˆ, gConstructorNr, gParamNbr);
in_AggrPattern ← true; gStructFields ← new(PList, Init(0)); gFieldsNbr ← 0;
end;
```

1330. The Parser has just encountered the end structure bracket (“#”) token, so we want to add the format to the *gFormatsColl* dictionary.

⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.FinishFields;
var lFormatNr: integer;
begin lFormatNr ← gFormatsColl.CollectPrefixForm(ˆGˆ, gConstructorNr, gFieldsNbr);
end;
```

1331. Recall that each field-segment looks like

$$\langle \textit{Field-Segment} \rangle ::= \langle \textit{Selector-Symbol} \rangle \{ ", " \langle \textit{Selector-Symbol} \rangle \} \langle \textit{Specification} \rangle$$

Before parsing the field-segment, the *StartAggrPattSegment* is invoked.

$\langle \text{Local variables for parser additions 1209} \rangle + \equiv$
gStructFieldsSegment: *PList*;
gSgmPos: *Position*;

1332. $\langle \text{Extended item implementation 1226} \rangle + \equiv$
procedure *extItemObj.StartAggrPattSegment*;
 begin *gStructFieldsSegment* \leftarrow *new(PList, Init(0))*; *gSgmPos* \leftarrow *CurPos*;
 end;

1333. For each selector-symbol the Parser encounters, it invokes the *ProcessField*.

$\langle \text{Extended item implementation 1226} \rangle + \equiv$
procedure *extItemObj.ProcessField*;
 var *lFormatNr*: *integer*;
 begin *lFormatNr* \leftarrow *gFormatsColl.CollectPrefixForm*(`U' , *CurWord.Nr*, 1);
 gStructFieldsSegment \uparrow .*Insert*(*new(FieldSymbolPtr, Init(CurPos, CurWord.Nr))*); *inc(gFieldsNbr)*;
 end;

1334. After each field has been parsed, the Parser invokes this method to update the *gStructFields* will push a new field segment object onto it.

$\langle \text{Extended item implementation 1226} \rangle + \equiv$
procedure *extItemObj.FinishAggrPattSegment*;
 begin *gStructFields.Insert*(*new(FieldSegmentPtr, Init(gSgmPos, gStructFieldsSegment, gLastType))*);
 end;

Subsection 23.2.5. Processing remaining statements

1335. Processing schemes. Most of these methods are used in parsing a scheme block (§1602). It will be useful to examine that function to see where these methods are invoked.

When the Parser starts a new scheme, several state variables need to be reset. The *gSchemeIdNr* is populated by the *GetIdentifier* (§1201) procedure, the *gSchemeIdPos* is assigned the current position, and the *gSchemeParams* should be allocated to an empty list.

$\langle \text{Extended item implementation 1226} \rangle + \equiv$
procedure *extItemObj.ProcessSchemeName*;
 begin *gSchemeIdNr* \leftarrow *GetIdentifier*; *gSchemeIdPos* \leftarrow *CurPos*;
 gSchemeParams \leftarrow *new(PList, Init(0))*;
 end;

1336. A scheme qualification segment looks like, for predicates:

$$\langle \text{Variable} \rangle \{ \text{ " , " } \langle \text{Variable} \rangle \} \text{ " [" } [\langle \text{Type-Expression-List} \rangle] \text{ "] "}$$

And for functors:

$$\langle \text{Variable} \rangle \{ \text{ " , " } \langle \text{Variable} \rangle \} \text{ " (" } [\langle \text{Type-Expression-List} \rangle] \text{ ") "}$$

When the comma-separated list of identifiers have all been read, but before either “(” or “[” has been discerned, the Parser invokes *StartSchemeQualification*.

This will assign the current word kind to *gSubItemKind*, and then initialize the *gTypeList* to 4 items.

\langle Global variables introduced in `parseraddition.pas` 1202 $\rangle + \equiv$
gTypeList: *MList*;

1337. \langle Extended item implementation 1226 $\rangle + \equiv$
procedure *extItemObj.StartSchemeQualification*;
 begin *gSubItemKind* \leftarrow *CurWord.Kind*; *gTypeList.Init*(4);
 end;

1338. After the type-list has been parsed, but before the closing parentheses or bracket has been encountered, the Parser invokes the *FinishSchemeQualification* method. This assigns the current position to the *gSubItemPos*.

\langle Global variables introduced in `parseraddition.pas` 1202 $\rangle + \equiv$
gSubItemPos: *Position*;

1339. \langle Extended item implementation 1226 $\rangle + \equiv$
procedure *extItemObj.FinishSchemeQualification*;
 begin *gSubItemPos* \leftarrow *CurPos*
 end;

1340. Starting a scheme segment describes the situation where we are *just about* to start parsing the comma-separated list of identifiers for the scheme parameters. This just assigns the current position to the *gSubItemPos*, then initializes *gSchVarIds* to 2 spots.

\langle Global variables introduced in `parseraddition.pas` 1202 $\rangle + \equiv$
gSchVarIds: *MList*;

1341. \langle Extended item implementation 1226 $\rangle + \equiv$
procedure *extItemObj.StartSchemeSegment*;
 begin *gSubItemPos* \leftarrow *CurPos*; *gSchVarIds.Init*(2);
 end;

1342. After parsing the identifier for an entry in the comma-separated list of scheme variables, the Parser invokes *ProcessSchemeVariable* to add the recently parsed identifier to the *gSchVarIds* state variable.

\langle Extended item implementation 1226 $\rangle + \equiv$
procedure *extItemObj.ProcessSchemeVariable*;
 begin *gSchVarIds.Insert*(*new*(*VariablePtr*, *Init*(*CurPos*, *GetIdentifier*)));
 end;

1343. Once the list of scheme variables and their type specification has been parsed, then the Parser invokes the *FinishSchemeSegment* method. This just turns the *gSchVarIds* list into a Predicate segment or a Functor segment, using the type list the Parser just finished parsing.

⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.FinishSchemeSegment;
  begin case gSubItemKind of
    sy_LeftParanthesis: begin gSchemeParams.Insert(new(FunctorSegmentPtr, Init(gSubItemPos,
      new(PList, MoveList(gSchVarIds)), new(PList, MoveList(gTypeList)), gLastType)));
    end;
    sy_LeftSquareBracket: begin gSchemeParams.Insert(new(SchemeSegmentPtr, Init(gSubItemPos,
      PredicateSegment, new(PList, MoveList(gSchVarIds)), new(PList, MoveList(gTypeList))));
    end;
  endcases;
end;
```

1344. The “scheme thesis” is the formula statement of the scheme. Informally, a scheme looks like:

scheme {⟨Scheme-Parameters⟩} ⟨Scheme-thesis⟩ **"provided"** ⟨Scheme-premises⟩

This means the *gLastFormula* state variable contains the scheme’s thesis. But the Parser has not yet started the list of premises. This is when the Parser invokes the *FinishSchemeThesis* method, which assigns the *gLastFormula* to *gSchemeConclusion*, then allocates a new empty list for the *gSchemePremises*.

⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.FinishSchemeThesis;
  begin gSchemeConclusion ← gLastFormula; gSchemePremises ← new(Plist, Init(0));
  end;
```

1345. The premises for a scheme consists of finitely many formulas separated by “**and**” keywords. The Parser enters into a loop invoking this method *after* parsing the formula but *before* checking the next word is “**and**” (and iterating loop). We just need to push the formula onto the *gSchemePremises* list.

⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.FinishSchemePremise;
  begin gSchemePremises↑.Insert(new(PropositionPtr, Init(nLabel, gLastFormula, nPropPos)));
  end;
```

1346. Reserved variables. These methods are invoked only when the Parser parses a reservation (§1599). A “reservation segment” refers to the comma-separated list of variables and the type.

Starting a reservation segment allocates a new (empty) list for *gResIdents*, and assigns the *gResPos* to the current position. Each variable encountered in the comma-separated list of variables is appended to the *gResIdents* list using the *ProcessReservedIdentifier* method.

Mizar treats each reservation segment as a separate statement. So there is no difference between:

```
reserve G for Group, x,y,z for Element of G;
...and...
```

```
reserve G for Group;
reserve x,y,z for Element of G;
```

Finishing a reservation mutates both the *gLastWSItem* and *gLastWSBlock* global variables. Specifically, we allocate a new reservation *Item*, then update *gLastWSItem* to point to it. The caller’s *nLastWSItem* is updated to point to it, too. We assign the content of this newly allocated reservation *Item* based on the *gResIdents* list. We insert this *Item* to the end of the *gLastWSBlock*’s items.

⟨Global variables introduced in *parseraddition.pas* 1202⟩ +≡
gResIdents: *PList*;
gResPos: *Position*;

1347. ⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.StartReservationSegment;
begin gResIdents ← new(Plist, Init(0)); gResPos ← CurPos;
end;
```

```
procedure extItemObj.ProcessReservedIdentifier;
begin gResIdents↑.Insert(new(VariablePtr, Init(CurPos, GetIdentifier)));
end;
```

```
procedure extItemObj.FinishReservationSegment;
begin gLastWSItem ← gWsTextProper↑.NewItem(itReservation, gResPos);
nLastWSItem ← gLastWSItem;
gLastWSItem↑.nContent ← new(ReservationSegmentPtr, Init(gResIdents, gLastType));
gLastWSItem↑.nItemEndPos ← PrevPos; gLastWSBlock↑.nItems.Insert(gLastWSItem);
end;
```

1348. Both “defpred” and “deffunc” invokes *StartPrivateDefiniendum* to initialize the *gTypeList*, store the identifier in the *gPrivateId*, and assign the current position to the *gPrivateIdPos*. Further, *dolAllowed* is toggled to *true* — placeholder variables are going to be allowed in the type declarations of the private functor or private predicate (for example “defpred Foo[set, Element of \$1]”).

⟨Global variables introduced in *parseraddition.pas* 1202⟩ +≡
gPrivateId: *Integer*;
gPrivateIdPos: *Position*;

1349. ⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.StartPrivateDefiniendum;
begin gPrivateId ← GetIdentifier; gPrivateIdPos ← CurPos; dolAllowed ← true; gTypeList.Init(4);
end;
```


1350. Reading a “type list” (for scheme parameters or for private definitions) loops over reading a type, then pushing it onto the *gTypeList*. The parser delegates that latter “push work” to the *FinishLocusType* method.

⟨Extended item implementation 1226⟩ +≡
procedure *extItemObj.FinishLocusType*;
 begin *gTypeList.Insert(gLastType)*;
 end;

1351. The life-cycle of expressions is a little convoluted. The *Item* will allocate a new *extExpression* object and assign it to the *gExpPtr*. Later, almost always, the *gExpPtr* will invoke a method to create a subexpression. This subexpression will be populated, then the *gLastTerm* (or *gLastFormula*) will be updated to point to this subexpression object. The expression object will be freed.

⟨Extended item implementation 1226⟩ +≡
procedure *extItemObj.CreateExpression*(*fExpKind* : *ExpKind*);
 begin *gExpPtr* ← *new*(*extExpressionPtr*, *Init*(*fExpKind*));
 end;

1352. Recall the “set” statement is of the form

$$\text{"set" } \langle \text{Variable} \rangle \text{"=" } \langle \text{Term} \rangle \{ \text{"," } \langle \text{Variable} \rangle \text{"=" } \langle \text{Term} \rangle \}$$

The Parser parses this as a loop of assignments of terms to identifiers. Before iterating, the Parser invokes the *FinishPrivateConstant* method. This allocates a new item for the constant definition, then assigns it to the *gLastWSItem* and to the caller’s *nLastWSItem* field. Then the content for the new item is allocated to be a constant definition object using the *VariablePtr* state variable and the *gLastTerm* state variable. The *gLastBlock* global variable pushes the new constant definition item to its contents.

⟨Extended item implementation 1226⟩ +≡
procedure *extItemObj.FinishPrivateConstant*;
 begin *gLastWSItem* ← *gWsTextProper*↑.*NewItem*(*itConstantDefinition*, *nItemPos*);
 nLastWSItem ← *gLastWSItem*; *gLastWSItem*↑.*nContent* ← *new*(*ConstantDefinitionPtr*,
 Init(*new*(*VariablePtr*, *Init*(*gPrivateIdPos*, *gPrivateId*)), *gLastTerm*));
 gLastWSItem↑.*nItemEndPos* ← *PrevPos*; *gLastWSBlock*↑.*nItems.Insert*(*gLastWSItem*);
 nItemPos ← *CurPos*;
 end;

1353. When the Parser is about to start parsing an assignment “⟨*Variable*⟩ = ⟨*Term*⟩” in a “set” statement, the Parser invokes this method. The caller assigns the *gPrivateId* state variable to be the result of *GetIdentifier*, and the *gPrivateIdPos* state variable to be the current position.

⟨Extended item implementation 1226⟩ +≡
procedure *extItemObj.StartPrivateConstant*;
 begin *gPrivateId* ← *GetIdentifier*; *gPrivateIdPos* ← *CurPos*;
 end;

1354. For a “defpred” and a “deffunc”, before parsing the definiens, we need to set the *dol_Allowed* global variable to true (to allow placeholder variables).

⟨Extended item implementation 1226⟩ +≡
procedure *extItemObj.StartPrivateDefiniens*;
 begin *dol_Allowed* ← *true*;
 end;

1355. After parsing the definiendum term for a “**deffunc**”, the Parser invokes this *FinishPrivateFuncDefinienition* method. This assigns the contents of the caller to a WSM private functor definition syntax tree.

⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.FinishPrivateFuncDefinienition;
  begin nLastWSItem↑.nContent ← new(PrivateFunctorDefinitionPtr, Init(new(VariablePtr,
    Init(gPrivateIdPos, gPrivateId)), new(PList, MoveList(gTypeList)), gLastTerm));
  end;
```

1356. When finishing the definiendum formula for a “**defpred**”, the Parser invokes this *FinishPrivatePredDefinienition* method.

⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.FinishPrivatePredDefinienition;
  begin nLastWSItem↑.nContent ← new(PrivatePredicateDefinitionPtr, Init(new(VariablePtr,
    Init(gPrivateIdPos, gPrivateId)), new(PList, MoveList(gTypeList)), gLastFormula));
  end;
```

1357. Reconsider statements.

⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.ProcessReconsideredVariable;
  begin gPrivateId ← GetIdentifier; gPrivateIdPos ← CurPos;
  end;
```

```
procedure extItemObj.FinishReconsideredTerm;
  begin gReconsiderList↑.Insert(new(TypeChangePtr, Init(Equating, new(VariablePtr,
    Init(gPrivateIdPos, gPrivateId)), gLastTerm)));
  end;
```

1358. This is invoked when parsing a private item which is a “**reconsider**” statement.

⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.FinishDefaultTerm;
  begin gReconsiderList↑.Insert(new(TypeChangePtr, Init(VariableIdentifier, new(VariablePtr,
    Init(gPrivateIdPos, gPrivateId)), nil)));
  end;
```

1359. When the Parser finishes parsing a formula in “**consider** ⟨Segment⟩ **such that** ⟨Formula⟩ {**and** ⟨Formula⟩}”, the Parser invokes the *FinishCondition* method. This checks that *gPremises* has been allocated, then pushes a new labeled formula into it.

⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.FinishCondition;
  begin if gPremises = nil then gPremises ← new(PList, Init(0));
  gPremises↑.Insert(new(PropositionPtr, Init(nLabel, gLastFormula, nPropPos)));
  end;
```

1360. In statements of the form

assume $\langle Formula \rangle$;

Or of the form

assume $\langle Formula \rangle$ **and** $\langle Formula \rangle$ **and** ... **and** $\langle Formula \rangle$;

After each formula parsed, the Parser invokes the *FinishHypothesis*. This just inserts a new labeled formula into the *gPremises* state variable, when the *gPremises* state variable is not **nil**.

\langle Extended item implementation 1226 $\rangle + \equiv$

```
procedure extItemObj.FinishHypothesis;
  begin if gPremises  $\neq$  nil then
    gPremises $\uparrow$ .Insert(new(PropositionPtr, Init(nLabel, gLastFormula, nPropPos)));
  end;
```

1361. “Take” statements. For statements of the form

take $\langle Variable \rangle = \langle Term \rangle$;

The Parser invokes the *ProcessExemplifyingVariable* method, then parses the term, and then constructs the AST by invoking *FinishExemplifyingVariable*.

Finishing a “take” statement mutates both the *gLastWSItem* and the *gLastWSBlock* global variables.

\langle Extended item implementation 1226 $\rangle + \equiv$

```
procedure extItemObj.ProcessExemplifyingVariable;
  begin gPrivateId  $\leftarrow$  GetIdentifier; gPrivateIdPos  $\leftarrow$  CurPos;
  end;
```

```
procedure extItemObj.FinishExemplifyingVariable;
  begin gLastWSItem  $\leftarrow$  gWsTextProper $\uparrow$ .NewItem(itExemplification, nItemPos);
  nLastWSItem  $\leftarrow$  gLastWSItem; gLastWSItem $\uparrow$ .nContent  $\leftarrow$  new(ExamplePtr, Init(new(VariablePtr,
    Init(gPrivateIdPos, gPrivateId)), gLastTerm)); gLastWSItem $\uparrow$ .nItemEndPos  $\leftarrow$  PrevPos;
  gLastWSBlock $\uparrow$ .nItems.Insert(gLastWSItem); nItemPos  $\leftarrow$  CurPos;
  end;
```

1362. In statements of the form

take $\langle Term \rangle$;

the Parser begins by invoking *StartExemplifyingTerm*, parses the term, then *FinishExemplifyingTerm*.

\langle Extended item implementation 1226 $\rangle + \equiv$

```
procedure extItemObj.StartExemplifyingTerm;
  begin if (CurWord.Kind = Identifier)  $\wedge$  extBlockPtr(gBlockPtr) $\uparrow$ .nInDiffuse  $\wedge$  ((AheadWord.Kind =
    sy_Comma)  $\vee$  (AheadWord.Kind = sy_Semicolon)) then
    begin gPrivateId  $\leftarrow$  GetIdentifier; gPrivateIdPos  $\leftarrow$  CurPos;
    end
  else gPrivateId  $\leftarrow$  0;
  end;

procedure extItemObj.FinishExemplifyingTerm;
  begin gLastWSItem  $\leftarrow$  gWsTextProper $\uparrow$ .NewItem(itExemplification, nItemPos);
  nLastWSItem  $\leftarrow$  gLastWSItem;
  if gPrivateId  $\neq$  0 then gLastWSItem $\uparrow$ .nContent  $\leftarrow$  new(ExamplePtr, Init(new(VariablePtr,
    Init(gPrivateIdPos, gPrivateId)), nil))
  else gLastWSItem $\uparrow$ .nContent  $\leftarrow$  new(ExamplePtr, Init(nil, gLastTerm));
  gLastWSItem $\uparrow$ .nItemEndPos  $\leftarrow$  PrevPos; gLastWSBlock $\uparrow$ .nItems.Insert(gLastWSItem);
  nItemPos  $\leftarrow$  CurPos;
  end;
```

1363. When the Parser examines the correctness conditions (§1585), it loops over the correctness conditions and justifications. Afterwards, it invokes the *ProcessCorrectness* method, which tests that the parser is not current looking at a correctness keyword. Then it tests if *gCorrectnessConditions* is empty or *AxiomsAllowed* (in which case, correctness has been satisfies, so the Parser moves happily along). But if *gCorrectnessConditions* $\neq \emptyset$ or axioms are not allowed, then a 73 error is raised.

\langle Extended item implementation 1226 $\rangle + \equiv$

```
procedure extItemObj.ProcessCorrectness;
  begin if CurWord.Kind  $\neq$  sy_Correctness then
    if (gCorrectnessConditions  $\neq$  [])  $\wedge$   $\neg$ AxiomsAllowed then Error(gDefPos, 73);
  end;
```

1364. A “construction type” appears in a redefinition where the type is redefined. In such a situation, we need to add “coherence” as a correctness condition. The *StartConstructionType* handles this task.

\langle Extended item implementation 1226 $\rangle + \equiv$

```
procedure extItemObj.StartConstructionType;
  begin if gRedefinitions  $\wedge$  (CurWord.Kind = sy_Arrow) then
    include(gCorrectnessConditions, syCoherence);
  end;
```

1365. This is used in the Parser’s *ProcessLab* procedure. Really, all the work is being done here: the *nLabel* field of the caller is assigned to a newly allocated *Label* object.

\langle Extended item implementation 1226 $\rangle + \equiv$

```
procedure extItemObj.ProcessLabel;
  begin nLabelIdNr  $\leftarrow$  0; nLabelIdPos  $\leftarrow$  CurPos;
  if (CurWord.Kind = Identifier)  $\wedge$  (AheadWord.Kind = sy_Colon) then nLabelIdNr  $\leftarrow$  CurWord.Nr;
  nLabel  $\leftarrow$  new(LabelPtr, Init(nLabelIdNr, nLabelIdPos));
  end;
```

1366. A regular statement is either a “diffuse” statement (which occurs with the “now” keyword) or else it’s a “compact” statement.

⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.StartRegularStatement;
  begin if CurWord.Kind = sy_Now then nRegularStatementKind ← stDiffuseStatement
  else nRegularStatementKind ← stCompactStatement;
  end;
```

1367. If the Parser encounters a colon after the copula, then it invokes this method to construct a label for the Definiens.

⟨Global variables introduced in *parseraddition.pas* 1202⟩ +≡

gDefLabel: *LabelPtr*;

1368. ⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.ProcessDefiniensLabel;
  begin gDefLabId ← 0; gDefLabPos ← CurPos;
  if (CurWord.Kind = Identifier) ∧ (AheadWord.Kind = sy_Colon) then gDefLabId ← CurWord.Nr;
  gDefLabel ← new(LabelPtr, Init(gDefLabId, gDefLabPos));
  end;
```

1369. The Parser, having encountered “from” and a non-MML reference, tries to treat the identifier as the label for a scheme declared in the current article. The *nInference* field would be a *SchemeJustification* object, so we just populate its *nSchemeIdNr* and position fields.

⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.ProcessSchemeReference;
  begin if CurWord.Kind = Identifier then
    begin SchemeJustificationPtr(nInference)↑.nSchemeIdNr ← CurWord.Nr;
    SchemeJustificationPtr(nInference)↑.nSchemeInfPos ← CurPos;
    end;
  end;
```

1370. When a “by” refers to a theorem or definition from an article in the MML, the Parser invokes the *StartLibraryReference* method.

⟨Global variables introduced in *parseraddition.pas* 1202⟩ +≡

gTHEFileNr: *integer*;

1371. ⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.StartLibraryReferences;
  begin gTHEFileNr ← CurWord.Nr;
  end;
```

1372. The Parser has already encountered a “from” and then an MML article identifier. Before continuing to parse the scheme number, the Parser invokes this method to initialize the relevant state variables.

⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.StartSchemeLibraryReference;
  begin gTHEFileNr ← CurWord.Nr;
  end;
```

1373. For references to labels found in the article being processed (“private references”), this method is invoked.

⟨Extended item implementation 1226⟩ +≡
procedure *extItemObj.ProcessPrivateReference*;
 begin *SimpleJustificationPtr*(*nInference*)↑.*nReferences*↑.*Insert*(*new*(*LocalReferencePtr*,
 Init(*GetIdentifier*, *CurPos*)));
 end;

1374. When using a definition from an MML article in a scheme reference (something like “from *MyScheme*(*ARTICLE:def* 5,...)”), well, the Parser stores this fact in a state variable *gDefinitional*. The *ProcessDef* method populates this state variable correctly.

⟨Global variables introduced in *parseraddition.pas* 1202⟩ +≡
gDefinitional: *boolean*;

1375. ⟨Extended item implementation 1226⟩ +≡
procedure *extItemObj.ProcessDef*;
 begin *gDefinitional* ← (*CurWord.Kind* = *ReferenceSort*) ∧ (*CurWord.Nr* = *ord*(*syDef*))
 end;

1376. When accumulating the references in a Scheme-Justification, and a reference is from an MML article, *ProcessTheoremNumber* transforms it into a newly allocated reference object. The caller’s *nInference* then adds the newly allocated object to its *nReferences* collection.

⟨Extended item implementation 1226⟩ +≡
procedure *extItemObj.ProcessTheoremNumber*;
 var *lRefPtr*: *ReferencePtr*;
 begin if *CurWord.Kind* ≠ *Numeral* **then** *exit*;
 if *CurWord.Nr* = 0 **then**
 begin *ErrImm*(146); *exit*
 end;
 if *gDefinitional* **then** *lRefPtr* ← *new*(*DefinitionReferencePtr*, *Init*(*gTHEFileNr*, *CurWord.Nr*, *CurPos*))
 else *lRefPtr* ← *new*(*TheoremReferencePtr*, *Init*(*gTHEFileNr*, *CurWord.Nr*, *CurPos*));
 SimpleJustificationPtr(*nInference*)↑.*nReferences*↑.*Insert*(*lRefPtr*);
 end;

1377. When a Scheme-Justification uses a local reference, the Parser delegates the work to the *Item*’s *ProcessSchemeNumber* method. This updates the caller’s *nInference* field.

⟨Extended item implementation 1226⟩ +≡
procedure *extItemObj.ProcessSchemeNumber*;
 begin if *CurWord.Kind* ≠ *Numeral* **then** *exit*;
 if *CurWord.Nr* = 0 **then**
 begin *ErrImm*(146); *exit*
 end;
 with *SchemeJustificationPtr*(*nInference*)↑ **do**
 begin *nSchFileNr* ← *gTHEFileNr*; *nSchemeIdNr* ← *CurWord.Nr*; *nSchemeInfPos* ← *PrevPos*;
 end;
 end;

1378. This appears when the Parser starts its *Justification* (§1567) procedure, or in the *RegularStatement* (§1574) procedure.

This clears the *nInference*, reassigning it to the **nil** pointer.

For nested “**proof**” blocks, check if the ‘check proofs’ (“**:\$P+**”) pragma has been enabled — if so, just set the caller’s *nInference* to be a new Justification object with a ‘proof’ tag. Otherwise, we’re skipping the proofs, so set *nInference* to be the ‘skipped’ justification.

⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.StartJustification;
  begin nInference ← nil;
  if CurWord.Kind = sy_Proof then
    begin if ProofPragma then nInference ← new(JustificationPtr, Init(infProof, CurPos))
    else nInference ← new(JustificationPtr, Init(infSkippedProof, CurPos))
    end;
  end;
```

1379. A simple justification is either a Scheme-Justification (“**from...**”), a Straightforward-Justification (“**by...**”), or... something else?

⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.StartSimpleJustification;
  begin case CurWord.Kind of
    sy_From: nInference ← new(SchemeJustificationPtr, Init(CurPos, 0, 0));
    sy_By: with extBlockPtr(gBlockPtr)↑ do
      nInference ← new(StraightforwardJustificationPtr, Init(CurPos, nLinked, nLinkPos));
    othercases with extBlockPtr(gBlockPtr)↑ do
      nInference ← new(StraightforwardJustificationPtr, Init(PrevPos, nLinked, nLinkPos));
    endcases;
  end;
```

1380. We should update the *nInference* field’s sort to be *infError* when, well, the inference is an error (e.g., the Parser is in panic mode). We should set the *gBlockPtr*’s *nLinked* field to false when we just added a straightforward justification (or an erroneous justification).

```
define is_inference_error ≡ ¬StillCorrect ∨
  ((CurWord.Kind ≠ sy_Semicolon) ∧ (CurWord.Kind ≠ sy_DotEquals)) ∨
  ((nInference↑.nInfSort = infStraightforwardJustification) ∧ (byte(nLinked) > byte(nLinkAllowed))) ∨
  ((nInference↑.nInfSort = infSchemeJustification) ∧
    (SchemeJustificationPtr(nInference)↑.nSchemeIdNr = 0))
```

⟨Extended item implementation 1226⟩ +≡

```
procedure extItemObj.FinishSimpleJustification;
  begin with extBlockPtr(gBlockPtr)↑ do
    begin if is_inference_error then nInference↑.nInfSort ← infError;
    end;
  if (nInference↑.nInfSort = infStraightforwardJustification) ∨ (nInference↑.nInfSort = infError) then
    extBlockPtr(gBlockPtr)↑.nLinked ← false;
  end;
```

1381. For iterative equalities, we should recall that it looks like

```
LHS = RHS <Justification>
  .= RHS2
  .= ...;
```

This matters because, well, when the Parser has parsed “LHS = RHS <Justification>”, the Parser believes it is a compact statement. Until the Parser looks at the next token, it does not know whether this is a Compact-Statement or an iterated equality. The *FinishCompactMethod* peeks at the token, and when the token is an iterated equality (“.=”) updates the caller’s fields as well as initialize the *gIterativeLastFormula*, *gIterativeSteps*, and *gInference* state variables. The *gBlockPtr* is updated to make its *nLinked* field false.

<Extended item implementation 1226> +≡

procedure *extItemObj.FinishCompactStatement*;

begin if *CurWord.Kind* = *sy.DotEquals* **then**

begin *gIterativeLastFormula* \leftarrow *gLastFormula*; *nRegularStatementKind* \leftarrow *stIterativeEquality*;

extBlockPtr(*gBlockPtr*) \uparrow .*nLinked* \leftarrow false; *gIterativeSteps* \leftarrow *new*(*PList*, *Init*(0));

gInference \leftarrow *nInference*;

end;

end;

1382. Every time the Parser encounters the “.=” token, it immediately invokes the *StartIterativeStep* method. This just updates the *gIterPos* state variable to the current position.

<Local variables for parser additions 1209> +≡

gIterPos: *Position*;

1383. <Extended item implementation 1226> +≡

procedure *extItemObj.StartIterativeStep*;

begin *gIterPos* \leftarrow *CurPos*; **end**;

1384. Right before the Parser iterates the loop checking if “.=” is the next token for an iterative equation, the Parser invokes the *FinishIterativeStep* method. This just adds a new *IterativeStep* object, an AST node representing the preceding “.= RHS by <Justification>”.

<Extended item implementation 1226> +≡

procedure *extItemObj.FinishIterativeStep*;

begin *gIterativeSteps* \uparrow .*Insert*(*new*(*IterativeStepPtr*, *Init*(*gIterPos*, *gLastTerm*, *nInference*)));

end;

1385. In a definition, after the Parser finishes parsing the definiens, we construct the AST node for it with the *FinishDefiniens* method.

For each copula (“means” and “equals”), the algorithm is the same: if we just had a definition-by-cases, then store the “otherwise” clause in *lExp* and assign the *gDefiniens* state variable to a newly allocated conditional definiens object. If the definiens is not a definition-by-cases (i.e., it’s a “simple” definition), then just assign *gDefiniens* a newly allocated *SimpleDefiniens* object.

For functor definitions (not redefinitions), the *gCorrectnessConditions* are assigned here.

⟨Extended item implementation 1226⟩ +=

```

procedure extItemObj.FinishDefiniens;
  var lExp: DefExpressionPtr;
  begin case gDefiningWay of
    dfMeans:
      if gPartialDefs  $\neq$  nil then
        begin lExp  $\leftarrow$  nil;
        if gOtherwise  $\neq$  nil then lExp  $\leftarrow$  new(DefExpressionPtr, Init(exFormula, gOtherwise));
        gDefiniens  $\leftarrow$  new(ConditionalDefiniensPtr, Init(gMeansPos, gDefLabel, gPartialDefs, lExp))
        end
      else gDefiniens  $\leftarrow$  new(SimpleDefiniensPtr, Init(gMeansPos, gDefLabel, new(DefExpressionPtr,
        Init(exFormula, gLastFormula))));
    dfEquals:
      if gPartialDefs  $\neq$  nil then
        begin lExp  $\leftarrow$  nil;
        if gOtherwise  $\neq$  nil then lExp  $\leftarrow$  new(DefExpressionPtr, Init(exTerm, gOtherwise));
        gDefiniens  $\leftarrow$  new(ConditionalDefiniensPtr, Init(gMeansPos, gDefLabel, gPartialDefs, lExp))
        end
      else gDefiniens  $\leftarrow$  new(SimpleDefiniensPtr, Init(gMeansPos, gDefLabel, new(DefExpressionPtr,
        Init(exTerm, gLastTerm))));
  endcases;
  if  $\neg$ gRedefinitions  $\wedge$  (nItemKind = itDefFunc) then
    begin if gDefiningWay = dfMeans then gCorrectnessConditions  $\leftarrow$  [syExistence, syUniqueness]
    else if gDefiningWay = dfEquals then gCorrectnessConditions  $\leftarrow$  [syCoherence];
    end;
  end;

```

Section 23.3. EXTENDED SUBEXPRESSION CLASS

1386. Aside: refactoring. We should probably refactor a private procedure *PushTermStack* to push a new term onto the term stack, and a private function *PopTermStack* to return the top of the term stack (and mutate the term stack), and possibly a *ResetTermStack* procedure (which will clear the term stack and possibly the objects stored in it?).

We see that *TermNbr* is decremented when popping the *Term* stack (via *FinishTerm*); when *FinishQualifyingFormula* is invoked, it decrements the *TermNbr*; when *FinishAttributiveFormula* is invoked, it decrements the *TermNbr*; but these latter two methods can (and should) be refactored to use the *FinishTerm* to pop the term stack and decrement the *TermNbr* state variable.

Assigning the *TermNbr* occurs when *CreateArgs* method is invoked; the *InsertIncorrBasic* method resets the *TermNbr* to the *nTermBase*; the *ProcessAtomicFormula*, when a 157 error is raised, will reset the *TermNbr* to the *nTermBase*; when the constructor for an *extExpression* object is invoked, it resets the *TermNbr* to zero (which happens in the *extItem*’s *CreateExpression* method—which occurs frequently enough to be a worry).

The only time when the *TermNbr* is incremented is when we push a new term onto the *Term* stack.

1387. There is a comment in Polish “teraz jest to kolekcja MultipleTypeExp”, which Google translates to “now it is a MultipleTypeExp collection”. I have made this replacement in the code below, prefixed with a “+” sign (to distinguish it from the other comment already in English).

Also note: the *nRestriction* refers to the subformula in a universally quantified formula

for $\langle \text{Variables} \rangle$ st $\langle \text{Restriction} \rangle$ holds ...

```

define arg_type  $\equiv$  record Start, Length: integer;
    end
define func_type  $\equiv$  record Instance, SymPri: integer;
    FuncPos: Position;
    end

```

\langle Methods implemented by subclasses of *SubexpObj* 716 $\rangle + \equiv$

1388. \langle Extended subexpression class declaration 1388 $\rangle \equiv$
extSubexpPtr = \uparrow *extSubexpObj*;
extSubexpObj = **object** (*SubexpObj*)
 nTermBase, *nRightArgBase*: *integer*;
 nSubexpPos, *nNotPos*, *nRestrPos*: *Position*;
 nQuaPos: *Position*;
 nSpelling: *Integer*;
 nSymbolNr, *nRSymbolNr*: *integer*;
 nConnective, *nNextWord*: *TokenKind*;
 nModeKind: *TokenKind*;
 nModeNr: *integer*;
 nRightSideOfPredPos: *Position*;
 nMultipredicateList: *MList*;
 nSample: *TermPtr*; { for Fraenkel terms }
 nAllPos: *Position*;
 nPostQualList: *MList*; { + now it is a MultipleTypeExp collection }
 nQualifiedSegments: *MList*;
 nSegmentIdentColl: *MList*; { quantified variables, keeps spellings of vars }
 nSegmentPos: *Position*;
 nFirstSententialOperand: *FormulaPtr*;
 nRestriction: *FormulaPtr*;
 nAttrCollection: *MList*;
 nNoneOcc: *boolean*;
 nNonPos: *Position*;
 nPostNegated: *boolean*;
 nArgListNbr: *integer*; { position in a term (§1519) }
 nArgList: **array of** *arg_type*;
 nFunc: **array of** *func_type*;
 constructor *Init*;
 \langle Methods implemented by subclasses of *SubexpObj* 716 \rangle
end ;

This code is used in section 1199.

1389. The *TermNbr* is used to treat a list of terms as a stack data structure. Specifically, the *Term* array is treated as a stack, and the *TermNbr* is the index of the “top” of the stack.

\langle Local variables for parser additions 1209 $\rangle + \equiv$
TermNbr: *integer*;

1390. \langle Extended subexpression implementation 1390 $\rangle \equiv$
 $\{ \textit{Subexpressions handling} \}$

```
constructor extSubexpObj.Init;
  const MaxArgListNbr = 20;
  begin inheritedInit; nRestriction  $\leftarrow$  nil; nTermBase  $\leftarrow$  TermNbr; nArgListNbr  $\leftarrow$  0;
    setlength(nArgList, MaxArgListNbr + 1); setlength(nFunc, MaxArgListNbr + 1);
    nArgList[0].Start  $\leftarrow$  TermNbr + 1;
  end;
```

See also sections 1391, 1392, 1393, 1395, 1396, 1397, 1398, 1399, 1400, 1401, 1402, 1403, 1404, 1405, 1406, 1407, 1408, 1409, 1410, 1411, 1413, 1417, 1429, 1430, 1431, 1432, 1433, 1434, 1435, 1436, 1437, 1438, 1439, 1440, 1441, 1442, 1443, 1444, 1445, 1446, 1447, 1448, 1449, 1450, 1451, 1452, 1453, 1454, 1455, 1456, 1457, 1458, 1459, 1460, 1461, 1462, 1463, 1464, 1465, 1466, 1467, 1468, 1469, 1470, 1471, 1472, 1473, 1474, 1475, 1476, 1477, 1478, 1479, 1480, 1481, 1482, 1483, 1484, 1485, 1486, 1487, and 1488.

This code is used in section 1200.

1391. When the Parser is about to parse a stack of attributes, either in a registration or on a type, we need to initialize the appropriate state variables. We also need the caller's *nAttrCollection* to be initialized with an empty list.

\langle Extended subexpression implementation 1390 $\rangle + \equiv$

```
procedure extSubexpObj.StartAttributes;
  begin nAttrCollection.Init(0); gLastType  $\leftarrow$  nil;
  end;
```

1392. When the Parser expects an adjective, and the caller is used to store the adjective or attribute, we need to check if it is negated. This handles it.

\langle Extended subexpression implementation 1390 $\rangle + \equiv$

```
procedure extSubexpObj.ProcessNon;
  begin nNoneOcc  $\leftarrow$  CurWord.Kind = sy_Non; nNonPos  $\leftarrow$  CurPos;
  end;
```

1393. Pop arguments from term stack. This will take some parameter *aBase* and copy pointers to each element of *Term*[*aBase* .. *TermNbr*] into a new list. Then the *TermNbr* state variable is updated to be *aBase* - 1.

This means that executing "*list1* \leftarrow *CreateArgs*(*aBase*); *list2* \leftarrow *CreateArgs*(*aBase*);" will have *list2* = **nil**.

Bug: when *aBase* \leq 0, this will set *TermNbr* to a negative number.

\langle Extended subexpression implementation 1390 $\rangle + \equiv$

```
function CreateArgs(aBase : integer): PList;
  var k: integer; lList: PList;
  begin lList  $\leftarrow$  new(PList, Init(TermNbr - aBase));
  for k  $\leftarrow$  aBase to TermNbr do lList.Insert(Term[k]);
  TermNbr  $\leftarrow$  aBase - 1; CreateArgs  $\leftarrow$  lList;
  end;
```

1394. The "process (singular) attribute" method is invoked in the "process (plural) attributes" procedure (§1524), and in the *ATTSubexpression* procedure (§1593). This method will be invoked when the Parser is looking at an attribute token.

When there is no format recorded for such an attribute, then a 175 error will be raised.

This will allocate a new Adjective object, store it in the *gLastAdjective* state variable, then append it to the *nAttrCollection* field of the caller.

\langle Global variables introduced in *parseraddition.pas* 1202 $\rangle + \equiv$

```
gLastAdjective: AdjectiveExpressionPtr;
```

1395. \langle Extended subexpression implementation 1390 $\rangle + \equiv$

```

procedure extSubexpObj.ProcessAttribute;
  var lFormatNr: integer;
  begin if CurWord.Kind = AttributeSymbol then
    begin
      lFormatNr  $\leftarrow$  gFormatsColl.LookUp_PrefixFormat(~V, CurWord.Nr, TermNbr - nTermBase + 1);
      if lFormatNr = 0 then { format not found! }
        begin gLastAdjective  $\leftarrow$  new(AdjectivePtr, Init(CurPos, 0, CreateArgs(nTermBase + 1)));
          Error(CurPos, 175)
        end
      else begin
        gLastAdjective  $\leftarrow$  new(AdjectivePtr, Init(CurPos, CurWord.Nr, CreateArgs(nTermBase + 1)));
        if nNoneOcc then gLastAdjective  $\leftarrow$  new(NegatedAdjectivePtr, Init(nNonPos, gLastAdjective));
        end;
      end
    else { needed for ATTSubexpression adjective cluster handling }
      begin gLastAdjective  $\leftarrow$  new(AdjectivePtr, Init(CurPos, 0, CreateArgs(nTermBase + 1)));
        end;
      nAttrCollection.Insert(gLastAdjective);
    end;

```

1396. These next next method is invoked before the Parser parses arguments for an attribute.

\langle Extended subexpression implementation 1390 $\rangle + \equiv$

```

procedure extSubexpObj.StartAttributeArguments;
  begin nTermBase  $\leftarrow$  TermNbr;
  end;

```

1397. The next two methods are invoked after the Parser has finished parsing the arguments for an attribute.

I am confused why there is duplicate code here, and the naming conventions suggest the *FinishAttributeArguments* method should be preferred. ■

\langle Extended subexpression implementation 1390 $\rangle + \equiv$

```

procedure extSubexpObj.CompleteAttributeArguments;
  begin nSubexpPos  $\leftarrow$  CurPos; nRightArgBase  $\leftarrow$  TermNbr;
  end;

procedure extSubexpObj.FinishAttributeArguments;
  begin nSubexpPos  $\leftarrow$  CurPos; nRightArgBase  $\leftarrow$  TermNbr;
  end;

```

1398. This allocates a new list of pointers, moves the caller's *nAttrCollection* into the list, and updates the *gAttrColl* state variable to point at them.

Again, this should be named *FinishedAdjectiveCluster* to be consistent with the naming conventions seemingly adopted.

\langle Extended subexpression implementation 1390 $\rangle + \equiv$

```

procedure extSubexpObj.CompleteAdjectiveCluster;
  begin gAttrColl  $\leftarrow$  new(PList, MoveList(nAttrCollection));
  end;

```

1399. When the Parser works its way through a registration block, check that the *TermNbr* points to not farther ahead than one more token ahead from the caller's *nTermBase* field. Raise an error if that happens.

This method is only invoked in the Parser module's the *RegisterCluster* (§1594) procedure.

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.CompleteClusterTerm;
  begin if TermNbr − nTermBase > 1 then
    begin ErrImm(379); gLastTerm ← new(IncorrectTermPtr, Init(CurPos));
    end;
  end;
```

1400. A “simple term” appears to be a variable. This is used when the Parser parses an identifier as a closed term (§1509). The state variable *gLastTerm* is updated to point to a newly allocated *SimpleTerm* object.

This method should probably be moved closer to the other methods used when parsing terms.

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.ProcessSimpleTerm;
  begin gLastTerm ← new(SimpleTermPtr, Init(CurPos, GetIdentifier));
  end;
```

1401. Qualified terms. The Parser invokes *ProcessQua* when it is looking directly at a “qua” token, specifically in the *AppendQua* (§1504) procedure. The *ProcessQua* method is used nowhere else. It is solely responsible for “marking the current position” of the Parser, and storing that in the caller's *nQuaPos* field.

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.ProcessQua;
  begin nQuaPos ← CurPos
  end;
```

1402. The Parser invokes the *FinishedQualifiedTerm* method after encountering a “qua” and after parsing the type. This method constructs a new *QualifiedTerm* object reflecting the top of the *Term* stack is taken “qua” the *gLastType*, and the mutates the top of the *Term* stack to be this newly allocated *QualifiedTerm* object.

This method does not push anything new to the term stack, but it does mutate the *Term* stack.

This method is used nowhere else other than the Parser's *AppendQua* (§1504) procedure.

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.FinishQualifiedTerm;
  begin Term[TermNbr] ← new(QualifiedTermPtr, Init(nQuaPos, Term[TermNbr], gLastType));
  end;
```

1403. Although the “**exactly**” reserved keyword is not used for anything, the method for *ProcessExactly* marks the current position and stores it in the caller's *nQuaPos*, then *updates* (**not** pushes) to the top of the term stack by turning the top of the stack into an *ExactlyTerm* object.

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.ProcessExactly;
  begin nQuaPos ← CurPos; Term[TermNbr] ← new(ExactlyTermPtr, Init(nQuaPos, Term[TermNbr]));
  end;
```

1404. Arguments to a term. The *CheckTermLimit* procedure is a “private helper function” for the *FinishArgument* method.

⟨Extended subexpression implementation 1390⟩ +≡

```

procedure CheckTermLimit;
  var l: integer;
  begin if TermNbr ≥ length(Term) then
    begin l ← 2 * length(Term); setlength(Term, l);
    end;
  end;

```

1405. Pushing the Term stack. This method pushes the *gLastTerm* state variable’s contents to the *Term* stack, mutating the *TermNbr* and *Term* module-local variables.

⟨Extended subexpression implementation 1390⟩ +≡

```

procedure extSubexpObj.FinishArgument;
  begin CheckTermLimit; inc(TermNbr); Term[TermNbr] ← gLastTerm;
  end;

```

1406. Pop the Term stack. The evil twin to “pushing” an element onto a stack, “popping” a stack removes the top element. We pop the *Term* stack whenever we finish the term.

This is only used in *AppendFunc* (§1519).

This should probably check that the *Term* stack is not empty before being invoked.

⟨Extended subexpression implementation 1390⟩ +≡

```

procedure extSubexpObj.FinishTerm;
  begin gLastTerm ← Term[TermNbr]; dec(TermNbr);
  end;

```

Subsection 23.3.1. Parsing Types

1407. When we start parsing a new type, we make sure the *gLastType* state variable is not caching an old type. We assign it to be the **nil** pointer.

⟨Extended subexpression implementation 1390⟩ +≡

```

procedure extSubexpObj.StartType;
  begin gLastType ← nil;
  end;

```

1408. This is invoked only by the Parser’s *RadixTypeSubexpression* (§1525) procedure. The Parser delegates the work of storing the mode information to this method. In turn, the caller’s *nModeKind* field stores the current word’s token *Kind*, and the caller’s *nModeNr* field stores the current word’s number. The Parser’s current position is marked and stored in the caller’s *nSubexpPos* field.

But no state variables are mutated by this method.

⟨Extended subexpression implementation 1390⟩ +≡

```

procedure extSubexpObj.ProcessModeSymbol;
  begin nModeKind ← CurWord.Kind; nModeNr ← CurWord.Nr;
  if (CurWord.Kind = sy_Set) { ?^(AheadWord.Kind ≠ sy_Of)? }
  then nModeKind ← ModeSymbol; nSubexpPos ← CurPos;
  end ;

```

1409. The Parser has just finished parsing a type and its arguments — “ $\langle Mode \rangle$ of $\langle Term\text{-}list \rangle$ ” or “ $\langle Structure \rangle$ over $\langle Term\text{-}list \rangle$ ”. The data has been accumulated into the caller, which will now be constructed into an AST object. The newly allocated AST node will be stored in the *gLastType* state variable.

If the caller is trying to construct a mode which does not match the format recorded in the *gFormatsColl*, a 151 error will be raised.

Similarly, if the caller is trying to construct a structure which does not match the format recorded in the *gFormatsColl*, a 185 error will be raised.

This is invoked only by the Parser’s *RadixTypeSubexpression* (§1525) procedure.

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.FinishType;
  var lFormatNr: integer;
  begin case nModeKind of
    ModeSymbol: begin
      lFormatNr  $\leftarrow$  gFormatsColl.LookUp_PrefixFormat(‘M’, nModeNr, TermNbr – nTermBase);
      if lFormatNr = 0 then Error(nSubexpPos, 151); { format missing }
      gLastType  $\leftarrow$  new(StandardTypePtr, Init(nSubexpPos, nModeNr, CreateArgs(nTermBase + 1)));
      end;
    StructureSymbol: begin
      lFormatNr  $\leftarrow$  gFormatsColl.LookUp_PrefixFormat(‘L’, nModeNr, TermNbr – nTermBase);
      if lFormatNr = 0 then SemErr(185); { format missing }
      gLastType  $\leftarrow$  new(StructTypePtr, Init(nSubexpPos, nModeNr, CreateArgs(nTermBase + 1)));
      end;
    othercases begin gLastType  $\leftarrow$  new(IncorrectTypePtr, Init(CurPos)); end;
  endcases;
end;
```

1410. If the Parser has the misfortune of trying to make sense of a malformed type expression, then with a heavy heart it invokes this method to update the *gLastType* state variable to be an incorrect type expression at the current position.

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.InsertIncorrType;
  begin gLastType  $\leftarrow$  new(IncorrectTypePtr, Init(CurPos));
  end;
```


1411. When the parser encounters a qualifying formula (“ $\langle Term \rangle$ is $\langle Type \rangle$ ”) or is parsing a type for a cluster (the “**cluster** ... **for** $\langle Type \rangle$ ”), after parsing the type, this method is invoked to **update** the *gLastType* state variable to store the *ClusteredType* AST node (which decorates a type — the contents of *gLastType* at the time of calling — with a bunch of attributes).

The caller’s *nAttrCollection* is transferred to the *gLastType*. At the end of the method, the caller’s *nAttrCollection* (array of pointers) is freed. This does not free the objects referenced by the pointers, however.

If *gLastType* = **nil**, then the Parser has somehow failed to parse the type expression. An error should be raised.

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.CompleteType;
  var j: integer;
  begin mizassert(5433, gLastType ≠ nil);
  if nAttrCollection.Count > 0 then
    begin gLastType ← new(ClusteredTypePtr, Init(gLastType↑.nTypePos, new(PList,
      Init(nAttrCollection.Count)), gLastType));
    for j ← 0 to nAttrCollection.Count − 1 do
      ClusteredTypePtr(gLastType)↑.nAdjectiveCluster↑.Insert(PObject(nAttrCollection.Items↑[j]));
    nAttrCollection.DeleteAll;
  end;
end;
```

Subsection 23.3.2. Parsing operator precedence

1412. Mario Carneiro’s “Mizar in Rust” (§6.2) gives an overview of this parsing routine (see also his `mizar-rs/src/parser/miz.rs` for the Rust version of the same code). It is a constrained optimization problem. We shall take care to dissect this routine. This appears to be where operator precedence, the *gPriority* (§648) global variable, comes into play.

1413. Starting a “long term”.

We can observe that *nTermBase* is initialized upon construction to *TermNbr*; in *ProcessAtomicFormula* and *StartPrivateFormula* it is assigned to *TermNbr*.

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.StartLongTerm;
  begin nArgListNbr ← 0; nArgList[0].Length ← TermNbr − nTermBase;
end;
```

1414. Malformed term errors.

We should remind the reader, errors 165–175 are “unknown functor format”, errors 176 is “unknown attribute format”, and error 177 is “unknown structure format”. Only when such an error occurs, the flow experiences a **goto** *AfterBalance*.

For an example of a 168, 169 error:

```
for x being Nat
holds (id + x +) = x;
```

For an example of a 170, 171 error (the first 0 will be flagged 170, the second 0 will be flagged as 171):

```
for x being Nat
holds 0 0 + x = x;
```

For an example of a 172, 173 error:

```
for x being Nat
holds x + / = x;
```

For an example of a 174, 175 error:

```
for x being Nat
holds x + (1,2) + x = x;
```

1415. We can recall that a “generic” term looks like an infix operator of the form

$$(t_1^{(\ell)}, \dots, t_m^{(\ell)}) t (t_1^{(r)}, \dots, t_n^{(r)})$$

The parentheses are optional. Constants will have $m = n = 0$ and look like $() t ()$. Function-like terms will have $m = 0$ and look like $() t (t_1^{(r)}, \dots, t_n^{(r)})$. The problem statement could be re-phrased as: given several infix terms without parentheses inserted anywhere, determine how to cluster terms together.

1416. The problem statement for constructing the syntax tree for a term is something like the following: we have an expression of the form

$$x_1^{(0)}, \dots, x_{k_0}^{(0)} F_1 x_1^{(1)}, \dots, x_{k_1}^{(1)} F_2 \cdots F_n x_1^{(n)}, \dots, x_{k_n}^{(n)}$$

We want to produce a suitable binary tree with F_i on the internal nodes and the $(x_j^{(i)})_{j \leq k_i}$ on the leafs, respecting precedence such that each F_i is applied to the correct number of arguments.

Mario Carneiro noted ([arXiv:2304.08391](https://arxiv.org/abs/2304.08391), §6.2) the existence of an $O(n^4)$ algorithm using dynamic programming techniques. The trick is to compute the minimal “cost” [number of violations] for each substring of nodes $F_a \cdots F_b$ for each $1 \leq a \leq i \leq b \leq n$ with node F_i being the root of the subtree. There are $O(n^3)$ such subproblems, and they can be calculated from smaller subproblems in $O(n)$. This might seem alarmingly large, but usually the terms in Mizar are sufficiently small.

It is interesting to see how other languages tackle this problem, so I am going to give a haphazard literature review:

- (1) Nils Anders Danielsson and Ulf Norell’s “Parsing Mifix Operators” (in SB. Scholz and O. Chitil (eds.), *Symposium on Implementation and Application of Functional Languages*, Springer 2008, pp. 80–99; [doi:10.1007/978-3-642-24452-0_5](https://doi.org/10.1007/978-3-642-24452-0_5)) discuss how Agda approaches parsing mixfix operators with different precedence.
- (2) The Isabelle proof assistant uses a modified version of Earley parsing of terms, supporting precedence between 0 to 1000.

1417. The only two place where *FinishLongTerm* is invoked is in the *AppendFunc* procedure (§1519) in *parser.pas*.

This relies on *MFormatsList.LookUpFuncFormat* (§667), which attempts to look up an *MinfixFormatObj* (§655) with a given id number as well as number of left and right arguments.

We will need to populate *ArgsLength* and *To_Right* to determine the syntax tree for the term (which is our real goal here). The *ArgsLength* encodes the number of terms are to the left and right of each “internal node”. The *To_Right* controls associativity (which is how Mizar handles operator precedence): if node F_{k+1} is higher precedence than node F_k , then *To_Right*(k) is true.

The *Exchange*(i) procedure will make node i a child of $i-1$ (when node i is a child of $i-1$), and vice-versa. Visually, this means we transform the tree as:

$$(\cdots F_{i-1} x_1, \dots, x_\ell), x_{\ell+1}, \dots, x_n F_i \cdots \longleftrightarrow \cdots F_{i-1} x_1, \dots, x_{\ell-1}, (x_\ell, x_{\ell+1}, \dots, x_n F_i \cdots)$$

Observe that “*Exchange*(i); *Exchange*(i)” is equivalent to doing nothing.

We should recall (§1387) that *nArgList* is an array of “**record** *Instance*, *SymPri*: *integer*; *FuncPos*: *Position*; **end**”.

⟨Extended subexpression implementation 1390⟩ $\vdash \equiv$

procedure *extSubexpObj.FinishLongTerm*;

var *ArgsLength*: **array of record** *l, r*: *integer*;
 end;

To_Right: **array of boolean**;

procedure *Exchange*(i : *integer*);

var l : *integer*;

begin $l \leftarrow \text{ArgsLength}[i].l$; $\text{ArgsLength}[i].l \leftarrow \text{ArgsLength}[i-1].r$; $\text{ArgsLength}[i-1].r \leftarrow l$;

To_Right[$i-1$] $\leftarrow \neg \text{To_Right}[i-1]$;

end;

var Bl, new_Bl : *integer*; { indexes *nFunc*, *ArgsLength* }

i, j, k : *integer*; { various indices }

 ⟨Variables for finishing a long term in a subexpression 1426⟩

label *Corrected*, *AfterBalance*;

begin ⟨Rebalance the long term tree 1418⟩

AfterBalance: ⟨Construct the term’s syntax tree after balancing arguments among subterms 1427⟩

end;

1418. Rebalancing the term tree.

Note that $nArgListNbr$ is mutated only in $extSubexpObj.ProcessFuncSymbol$ (§1429), and in $ProcessAtomicFormula$ (§1459) it is reset to zero.

```

define missing_funcator_format  $\equiv gFormatsColl.LookUp\_FuncFormat(Instance, l, r) = 0$ 
⟨ Rebalance the long term tree 1418 ⟩  $\equiv$ 
  ⟨ Initialize To_Right and ArgsLength arrays 1421 ⟩
  ⟨ Initialize Bl, goto AfterBalance if term has at most one argument 1423 ⟩
    {  $Bl = 1 \vee Bl = 2$  }
  for  $k \leftarrow 2$  to  $nArgListNbr - 1$  do
    with  $nFunc[k], ArgsLength[k]$  do
      begin if missing_funcator_format then ⟨ Guess the  $k^{th}$  funcator format 1424 ⟩
        Corrected: end;
      for  $j \leftarrow nArgListNbr$  downto  $Bl + 1$  do
        with  $nFunc[j], ArgsLength[j]$  do
          begin if  $\neg$ missing_funcator_format then goto AfterBalance;
          Exchange( $j$ ); ⟨ Check for 172/173 error, goto AfterBalance if erred 1419 ⟩
          end;
        ⟨ Check for 174/175 error, goto AfterBalance if erred 1420 ⟩

```

This code is used in section 1417.

```

1419. ⟨ Check for 172/173 error, goto AfterBalance if erred 1419 ⟩  $\equiv$ 
  if missing_funcator_format then
    begin Error(FuncPos, 172); Error( $nFunc[nArgListNbr].FuncPos$ , 173); goto AfterBalance; end;

```

This code is used in section 1418.

```

1420. ⟨ Check for 174/175 error, goto AfterBalance if erred 1420 ⟩  $\equiv$ 
  with  $nFunc[Bl], ArgsLength[Bl]$  do
    if missing_funcator_format then
      begin Error(FuncPos, 174); Error( $nFunc[nArgListNbr].FuncPos$ , 175); goto AfterBalance; end;

```

This code is used in section 1418.

1421. We first allocate the arrays, then we initialize the values.

```

⟨ Initialize To_Right and ArgsLength arrays 1421 ⟩  $\equiv$ 
  setlength(ArgsLength,  $nArgListNbr + 1$ ); setlength(To_Right,  $nArgListNbr + 1$ );
  setlength(Depo,  $nArgListNbr + 1$ );

```

See also section 1422.

This code is used in section 1418.

1422. The initial guess depends on whether F_k has precedence over F_{k+1} or not.

If F_{k+1} has higher precedence than F_k , then the initial guess groups terms as:

$$\cdots F_k ((x_1^{(k)}, \dots, x_{m_k}^{(k)}) F_{k+1}(\cdots)) \cdots, \quad \text{and} \quad To_Right[k] = true.$$

On the other hand, if F_{k+1} *does not* have higher precedence than F_k , then we guess the terms are grouped as

$$\cdots (\cdots F_k(x_1^{(k)}, \dots, x_{m_k}^{(k)}) F_{k+1} \cdots), \quad \text{and} \quad To_Right[k] = false.$$

This is a first stab, but sometimes we get lucky and it's correct.

define *next_term_has_higher_precedence*(#) \equiv
 $gPriority.Value(ord('0'), nFunc[\#].Instance) < gPriority.Value(ord('0'), nFunc[\# + 1].Instance)$

\langle Initialize *To_Right* and *ArgsLength* arrays 1421 $\rangle \equiv$

ArgsLength[1].*l* \leftarrow *nArgList*[0].*Length*; *To_Right*[0] \leftarrow *true*;

for $k \leftarrow 1$ **to** *nArgListNbr* $- 1$ **do**

with *ArgsLength*[k] **do**

if *next_term_has_higher_precedence*(k) **then**

begin $r \leftarrow 1$; *ArgsLength*[$k + 1$].*l* \leftarrow *nArgList*[k].*Length*; *To_Right*[k] \leftarrow *true* **end**

else begin $r \leftarrow$ *nArgList*[k].*Length*; *ArgsLength*[$k + 1$].*l* $\leftarrow 1$; *To_Right*[k] \leftarrow *false* **end**;

ArgsLength[*nArgListNbr*].*r* \leftarrow *nArgList*[*nArgListNbr*].*Length*; *To_Right*[*nArgListNbr*] \leftarrow *false*;

1423. The first situation we encounter is if the user tries to tell Mizar to evaluate something like:

```
for x being Nat
holds x + (1,2) = x;
```

Mizar will not understand “ $x + (1,2)$ ” because it is an invalid functor format — the format would look something like $\langle “+”, \text{left} : 1, \text{right} : 1 \rangle$ but the format of the expression is $\langle \text{left} : 1, \text{right} : 2 \rangle$. The mismatch on the “right” values in the formats will raise a 165 error.

For a 166 error example,

```
for x being Nat
holds + / = x;
```

Mizar will not like the leading “+ /” expression, and flag this with the 166 error.

Mizar will flag “+ 0” as a 165 error.

\langle Initialize *Bl*, **goto** *AfterBalance* if term has at most one argument 1423 $\rangle \equiv$

with *nFunc*[1], *ArgsLength*[1] **do**

begin if *nArgListNbr* = 1 **then**

begin if *missing_functor_format* **then**

begin *Error*(*FuncPos*, 165); **goto** *AfterBalance* **end**;

goto *AfterBalance*;

end;

$Bl \leftarrow 1$;

if *missing_functor_format* **then**

begin *Exchange*(2); $Bl \leftarrow 2$;

if *missing_functor_format* **then**

begin *Error*(*FuncPos*, 166); **goto** *AfterBalance* **end**;

end;

end;

This code is used in section 1418.

1424. \langle Guess the k^{th} functor format [1424](#) $\rangle \equiv$
begin *Exchange*($k + 1$); *new_Bl* \leftarrow *Bl*;
if *missing_functor_format* **then**
 begin if *Bl* = *k* **then**
 begin *Error*(*nFunc*[$k - 1$].*FuncPos*, 168); *Error*(*FuncPos*, 169); **goto** *AfterBalance*; **end**;
 Exchange($k + 1$); *Exchange*(*k*); *new_Bl* \leftarrow *k*;
 if *missing_functor_format* **then**
 begin *Exchange*($k + 1$); *new_Bl* \leftarrow $k + 1$;
 if *missing_functor_format* **then**
 begin *Error*(*FuncPos*, 167); **goto** *AfterBalance* **end**;
 end;
 for *j* \leftarrow $k - 1$ **downto** *Bl* + 1 **do**
 with *nFunc*[*j*], *ArgsLength*[*j*] **do**
 begin if \neg *missing_functor_format* **then** **goto** *Corrected*;
 Exchange(*j*);
 if *missing_functor_format* **then**
 begin *Error*(*FuncPos*, 168); *Error*(*nFunc*[*k*].*FuncPos*, 169); **goto** *AfterBalance*; **end**;
 end;
 \langle Check term *Bl* has valid functor format, **goto** *AfterBalance* if not [1425](#) \rangle
 end;
Bl \leftarrow *new_Bl*;
end;

This code is used in section [1418](#).

1425. \langle Check term *Bl* has valid functor format, **goto** *AfterBalance* if not [1425](#) $\rangle \equiv$
with *nFunc*[*Bl*], *ArgsLength*[*Bl*] **do**
 if *missing_functor_format* **then**
 begin *Error*(*FuncPos*, 170); *Error*(*nFunc*[*k*].*FuncPos*, 171); **goto** *AfterBalance*; **end**;

This code is used in section [1424](#).

1426. Constructing the syntax tree. The second half of finishing a long term constructs the syntax tree for the term.

\langle Variables for finishing a long term in a subexpression [1426](#) $\rangle \equiv$
ak, pl, ll, kn: *integer*;
lTrm: *TermPtr*;
lLeftArgs, lRightArgs: *PList*;
DepoNbr: *integer*;
Depo: **array of record** *FuncInstNr*: *integer*;
 dArgList: *PList*;
end;

This code is used in section [1417](#).

1427. \langle Construct the term's syntax tree after balancing arguments among subterms 1427 $\rangle \equiv$
 \langle Initialize symbol priorities, determine last ll , pl values 1428 \rangle
 $DepoNbr \leftarrow 0$;
for $kn \leftarrow nArgListNbr$ **downto** 2 **do**
 if $To_Right[kn - 1]$ **then** { if kn node is parent of $kn - 1$ node }
 begin with $nFunc[kn]$ **do**
 begin $lRightArgs \leftarrow CreateArgs(nArgList[kn].Start)$; { (§1393) }
 $lLeftArgs \leftarrow CreateArgs(nArgList[kn - 1].Start)$;
 $lTrm \leftarrow new(InfixTermPtr, Init(FuncPos, Instance, lLeftArgs, lRightArgs))$;
 end;
 for $j \leftarrow DepoNbr$ **downto** 1 **do**
 with $Depo[j], nFunc[FuncInstNr]$ **do**
 begin if $symPri \leq nFunc[kn - 1].SymPri$ **then break**;
 $dec(DepoNbr)$; $lLeftArgs \leftarrow new(PList, Init(1))$; $lLeftArgs \uparrow.Insert(lTrm)$;
 $lTrm \leftarrow new(InfixTermPtr, Init(FuncPos, Instance, lLeftArgs, dArgList))$;
 end;
 $gLastTerm \leftarrow lTrm$;
 $gSubexpPtr \uparrow.FinishArgument$;
 end
 else begin $inc(DepoNbr)$;
 with $Depo[DepoNbr]$ **do**
 begin $FuncInstNr \leftarrow kn$; $dArgList \leftarrow CreateArgs(nArgList[kn].Start)$; **end**;
 end;
 with $nFunc[1]$ **do**
 begin $lRightArgs \leftarrow CreateArgs(nArgList[1].Start)$; $lLeftArgs \leftarrow CreateArgs(nArgList[0].Start)$;
 $lTrm \leftarrow new(InfixTermPtr, Init(FuncPos, Instance, lLeftArgs, lRightArgs))$;
 end;
 for $j \leftarrow DepoNbr$ **downto** 1 **do**
 with $Depo[j], nFunc[FuncInstNr]$ **do**
 begin $lLeftArgs \leftarrow new(PList, Init(1))$; $lLeftArgs \uparrow.Insert(lTrm)$;
 $lTrm \leftarrow new(InfixTermPtr, Init(FuncPos, Instance, lLeftArgs, dArgList))$;
 end;
 $gLastTerm \leftarrow lTrm$;

This code is used in section 1417.

1428. \langle Initialize symbol priorities, determine last ll , pl values 1428 $\rangle \equiv$
for $ak \leftarrow 1$ **to** $nArgListNbr$ **do**
 begin $ll \leftarrow 1$; $pl \leftarrow 1$;
 if $To_Right[ak - 1]$ **then** $ll \leftarrow nArgList[ak - 1].Length$;
 if $\neg To_Right[ak]$ **then** $pl \leftarrow nArgList[ak].Length$;
 with $nFunc[ak]$ **do**
 begin $symPri \leftarrow gPriority.Value(ord('0'), Instance)$; **end**;
 end;

This code is used in section 1427.

Subsection 23.3.3. Processing subexpressions

1429. Note that *ProcessFunctorSymbol* is the only place where *nArgListNbr* is incremented. Processing functor symbols occurs in the parser’s *AppendFunc* (§1519) in a loop.

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.ProcessFunctorSymbol;
  var l: integer;
  begin inc(nArgListNbr);
  if nArgListNbr ≥ length(nFunc) then
    begin l ← 2 * length(nFunc) + 1; setlength(nArgList, l); setlength(nFunc, l);
    end;
  nArgList[nArgListNbr].Start ← TermNbr + 1; nFunc[nArgListNbr].FuncPos ← CurPos;
  nFunc[nArgListNbr].Instance ← CurWord.Nr;
  end;
```

1430. The Parser is in the middle of *AppendFunc* and has just finished parsing a term *t* or a tuple of terms (*t*₁, . . . , *t*_{*n*}). Before the Parser checks if it’s looking at an infix functor operator or not, the Parser invokes the *FinishArgList* method. It’s the only time where the *FinishArgList* method is invoked.

This allocates either 1 or *n* to the length of *nArgList*[*nArgListNbr*], to store the information for the term(s).

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.FinishArgList;
  begin nArgList[nArgListNbr].Length ← TermNbr − nArgList[nArgListNbr].Start + 1;
  end;
```

1431. The Parser is looking at “where” or (when the variables are all reserved) a colon “:”, the Parser invokes the *StartFraenkelTerm* which will store the previous term in the *nSample* field — so schematically, the Fraenkel term could look like

$$\{\langle nSample \rangle \textbf{ where } \langle Postqualification \rangle : \langle Formula \rangle\}$$

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.StartFraenkelTerm;
  begin nSample ← gLastTerm;
  end;
```

1432. This is only invoked in the Parser’s *ProcessPostqualification* (§1506) procedure, which is only invoked after the Parser calls the *extSubexp* object’s *StartFraenkelTerm* method.

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.StartPostqualification;
  begin nPostQualList.Init(0);
  end;
```

1433. The parser is looking at the post-qualified segment of a Fraenkel operator. This will be a list of variables “being” a type, we allocate an array for the variables. This is handled by the *StartPostQualifyingSegment* method.

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.StartPostQualifyingSegment;
  begin nSegmentIdentColl.Init(2);
  end;
```


1434. While looping over the comma-separated list of variables in a post-qualified segment (in a Fraenkel term), the Parser invokes the *ProcessPostqualifiedVariable* on each iteration until it has parsed all the variables. This allocates a new *Variable* object, and pushes it onto the *nSegmentIdentColl* “stack”.

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.ProcessPostqualifiedVariable;
  begin nSegmentIdentColl.Insert(new(VariablePtr, Init(CurPos, GetIdentifier)));
  end;
```

1435. The parser is looking at “is” or “are” in a Fraenkel term’s post-qualification segment, but has not yet parsed the type. This method will assign the *nSegmentPos* field to be the current position, and assign the *gLastType* state variable to be the **nil** pointer.

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.StartPostqualificationSpecyfication;
  begin nSegmentPos ← CurPos; gLastType ← nil;
  end;
```

1436. The Parser has just parsed either (1) a comma-separated list of variables, the copula “is” or “are”, and the type; or (2) a comma-separated list of reserved variables (but no copula and no type). We just need to construct an appropriate node for the abstract syntax tree. This method will append a new Segment to the *nPostQualList*.

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.FinishPostQualifyingSegment;
  var k: integer; lSegment: ExplicitlyQualifiedSegmentPtr;
  begin if gLastType ≠ nil then
    begin lSegment ← new(ExplicitlyQualifiedSegmentPtr, Init(nSegmentPos, new(PList, Init(0)),
      gLastType)); nPostQualList.Insert(lSegment);
    for k ← 0 to nSegmentIdentColl.Count − 1 do
      begin ExplicitlyQualifiedSegmentPtr(lSegment)↑.nIdentifiers.Insert(nSegmentIdentColl.Items↑[k]);
      end;
    end
  else begin for k ← 0 to nSegmentIdentColl.Count − 1 do
    begin nPostQualList.Insert(new(ImplicitlyQualifiedSegmentPtr,
      Init(VariablePtr(nSegmentIdentColl.Items↑[k])↑.nVarPos, nSegmentIdentColl.Items↑[k])));
    end;
  end;
  nSegmentIdentColl.DeleteAll; nSegmentIdentColl.Done;
end;
```

1437. The Parser has just finished the formula in a Fraenkel term, and it is staring at the closet “}” bracket. The Parser invokes this method to construct a new *FraenkelTerm* AST node, and updates the *gLastTerm* to point at it.

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.FinishFraenkelTerm;
  begin gLastTerm ← new(FraenkelTermPtr, Init(CurPos, new(PList, MoveList(nPostQualList)),
    nSample, gLastFormula));
  end;
```

1438. The Parser has already encountered “**the set**” and the next token is “**of**”, which means the Parser has encountered a “simple” Fraenkel term of the form “**the set of all** $\langle Term \rangle \dots$ ”. This method will be invoked once the Parser has stumbled across the “**all**”. The caller updates its $nAllPos$ to the Parser’s current position.

\langle Extended subexpression implementation 1390 $\rangle + \equiv$
procedure *extSubexpObj.StartSimpleFraenkelTerm*;
 begin $nAllPos \leftarrow CurPos$;
 end;

1439. The Parser has just finished parsing the post-qualification to the simple Fraenkel term, which means it has finished parsing the simple Fraenkel term. This method allocates a new *SimpleFraenkelTerm* AST node with the accumulated AST nodes, then updates the $gLastTerm$ to point to the allocated *SimpleFraenkelTerm* node.

\langle Extended subexpression implementation 1390 $\rangle + \equiv$
procedure *extSubexpObj.FinishSimpleFraenkelTerm*;
 begin $gLastTerm \leftarrow new(SimpleFraenkelTermPtr, Init(nAllPos, new(PList, MoveList(nPostQualList)), nSample))$;
 end;

1440. The Parser is looking at a closed term of the form “ $\langle Identifier \rangle (\dots$ ”, and so it looks like a private functor. This method updates the caller’s $nSubexpPos$ to the Parser’s current position, and the $nSpelling$ is assigned to the identifier’s number (for the private functor).

\langle Extended subexpression implementation 1390 $\rangle + \equiv$
procedure *extSubexpObj.StartPrivateTerm*;
 begin $nSubexpPos \leftarrow CurPos$; $nSpelling \leftarrow CurWord.Nr$;
 end;

1441. The Parser just finished parsing all the arguments to the private functor, and is looking at the closing parentheses for the private functor. This method allocates a new *PrivateFunctorTerm* object, using the arguments just parsed, and updates the $gLastTerm$ state variable to point to it.

\langle Extended subexpression implementation 1390 $\rangle + \equiv$
procedure *extSubexpObj.FinishPrivateTerm*;
 begin $gLastTerm \leftarrow new(PrivateFunctorTermPtr, Init(nSubexpPos, nSpelling, CreateArgs(nTermBase + 1)))$;
 end;

1442. The Parser has just encountered either a left bracket term or the opening left bracket for a set “{”. The Parser calls this method, which just updates the caller’s $nSymbolNr$ to be whatever the current token’s numeric ID value is.

\langle Extended subexpression implementation 1390 $\rangle + \equiv$
procedure *extSubexpObj.StartBracketedTerm*;
 begin $nSymbolNr \leftarrow CurWord.Nr$;
 end;

1443. If the Parser is in panic mode, this method does nothing.

Either the Parser has finished parsing an enumerated set $\{x_1, \dots, x_n\}$ or a bracketed term. We need to double check the format for the bracket matches what is stored in the *gFormatsColl*, and raise a 152 error if there's a mismatch. Otherwise, allocate a new AST node for the bracketed term, and use *CreateArgs* on the terms contained within the brackets.

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.FinishBracketedTerm;
  var lFormatNr: integer;
  begin if StillCorrect then
    begin nRSymbolNr ← CurWord.Nr; lFormatNr ← gFormatsColl.LookUp_BracketFormat(nSymbolNr,
      nRSymbolNr, TermNbr − nTermBase, 0, 0);
    if lFormatNr = 0 then SemErr(152);
    gLastTerm ← new(CircumfixTermPtr, Init(CurPos, nSymbolNr, nRSymbolNr,
      CreateArgs(nTermBase + 1)));
    end;
  end;
```

1444. Remember that Mizar calls “an instance of structure” an “**Aggregate**”. When the Parser is parsing for a closed subterm and has stumbled across a structure constructor (§1510), it first invokes this method. This stores the ID number for the structure in the caller's *nSymbolNr*.

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.StartAggregateTerm;
  begin nSymbolNr ← CurWord.Nr;
  end;
```

1445. The Parser has just parsed the arguments for the structure constructor, and the Parser is now looking at the “#)” token. This method is invoked.

We should check the format for the structure constructor is stored in the *gFormatsColl*. If not, raise a 176 error. Otherwise, we allocate a new *AggregateTerm* with the parsed arguments, and then update the *gLastTerm* pointer to point at it.

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.FinishAggregateTerm;
  var lFormatNr: integer;
  begin lFormatNr ← gFormatsColl.LookUp_PrefixFormat(‘G’, nSymbolNr, TermNbr − nTermBase);
  if lFormatNr = 0 then Error(CurPos, 176); { missing format error }
  gLastTerm ← new(AggregateTermPtr, Init(CurPos, nSymbolNr, CreateArgs(nTermBase + 1)));
  end;
```

1446. The Parser is parsing for a closed subterm, and has stumbled across “the” and is looking at a selector token (§1515). This method is invoked. We assign the caller's *nSymbolNr* to the ID number for the selector token, assign the caller's *nSubexpPos* to the Parser's current position, and store the next token's kind (i.e., the “of” token's kind) in the *nNextWord* field.

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.StartSelectorTerm;
  begin nSymbolNr ← CurWord.Nr; nSubexpPos ← CurPos; nNextWord ← AheadWord.Kind;
  end;
```

1447. The Parser has just parsed “the $\langle Selector \rangle$ of $\langle Term \rangle$ ”. Now this method is invoked to assemble the parsed data into an AST node.

If there is no selector with this matching format, then a 182 error will be raised.

If the caller’s *nNextWord* is an “of” token’s kind, then we’re describing a selector term. We update the *gLastTerm* state variable to point to a newly allocated *SelectorTerm* object with the appropriate data set.

On the other hand, “**internal selectors**” occur when defining a structure. For example,

```
struct (1-sorted) multMagma (#
  carrier -> set,
  multF -> BinOp of the carrier
#);
```

Observe the *multF* specification is *BinOp of the carrier*. That “the carrier” is an internal selector. In this case, allocate a new *InternalSelectorTerm* object, and update the *gLastTerm* state variable to point to it.

If, for some reason, the Parser is in neither situation, then just *gLastTerm* state variable to be an incorrect term.

\langle Extended subexpression implementation 1390 $\rangle + \equiv$

procedure *extSubexpObj.FinishSelectorTerm*;

var *lFormatNr*: integer;

begin *lFormatNr* \leftarrow *gFormatsColl.LookUp_PrefixFormat*(‘U’, *nSymbolNr*, 1);

if *lFormatNr* = 0 **then** *Error*(*nSubexpPos*, 182); { missing format error }

if *nNextWord* = *sy_Of* **then**

gLastTerm \leftarrow *new*(*SelectorTermPtr*, *Init*(*nSubexpPos*, *nSymbolNr*, *gLastTerm*))

else if *in_AggrPattern* **then**

gLastTerm \leftarrow *new*(*InternalSelectorTermPtr*, *Init*(*nSubexpPos*, *nSymbolNr*))

else begin *gLastTerm* \leftarrow *new*(*IncorrectTermPtr*, *Init*(*nSubexpPos*)); *Error*(*nSubexpPos*, 329)

end;

end;

1448. The Parser is about to start parsing a forgetful functor (§1516) — for example “the *multMagma* of *REAL.TopGroup*”. This method is invoked. The caller’s *nSymbolNr* field is updated to the current token’s ID Number, the *nSubexpPos* field is assigned the Parser’s current position, and the *nNextWord* field is assigned to the token kind of the next token — this is expected to be “of”.

\langle Extended subexpression implementation 1390 $\rangle + \equiv$

procedure *extSubexpObj.StartForgetfulTerm*;

begin *nSymbolNr* \leftarrow *CurWord.Nr*; *nSubexpPos* \leftarrow *CurPos*; *nNextWord* \leftarrow *AheadWord.Kind*;

end;

1449. The Parser just finished parsing a forgetful functor. If the Parser is not panicking, check the format for the forgetful functor matches what is stored in the *gFormatsColl* state variable. If the format is invalid, raise a 184 error.

Whether the Parser is panicking or not, allocate a new *ForgetfulFunctor* term, and update the *gLastTerm* to point to it.

⟨Extended subexpression implementation 1390⟩ +≡

procedure *extSubexpObj.FinishForgetfulTerm*;

var *lFormatNr*: integer;

begin *lFormatNr* ← 0;

if *StillCorrect* **then**

begin *lFormatNr* ← *gFormatsColl.LookUp_PrefixFormat*(*ˆJ*, *nSymbolNr*, 1);

if *lFormatNr* = 0 **then** *Error*(*nSubexpPos*, 184); { missing format }

end;

gLastTerm ← *new*(*ForgetfulFunctorTermPtr*, *Init*(*nSubexpPos*, *nSymbolNr*, *gLastTerm*));

end;

1450. There are several situations where this is invoked:

- (1) The Parser has just parsed “the” but is not looking at a selector symbol (“the multF of...”), nor is the Parser looking at a forgetful functor (“the multMagma of...”). Then this is interpreted as looking at a choice operator (§1515).
- (2) The Parser has just parsed “the” but is not looking at a forgetful functor, so the Parser believes it must be looking at a choice operator (§1516).
- (3) The Parser has just parsed “the” and is now looking at “set” — so this is invoking the axiom of choice to pick “the set” (§1517).

In these three situations, the Parser invokes this method. It just updates the caller’s *nSubexpPos* field to point to the Parser’s current position.

⟨Extended subexpression implementation 1390⟩ +≡

procedure *extSubexpObj.StartChoiceTerm*;

begin *nSubexpPos* ← *CurPos*;

end;

1451. The Parser has just parsed a type, and now believes it has finished parsing a choice expression. Then it invokes this method to construct an appropriate AST node for the term, by specifically allocating a new *ChoiceTerm* for the *gLastType* type. We then update the *gLastTerm* state variable to point to this newly allocated term.

⟨Extended subexpression implementation 1390⟩ +≡

procedure *extSubexpObj.FinishChoiceTerm*;

begin *gLastTerm* ← *new*(*ChoiceTermPtr*, *Init*(*nSubexpPos*, *gLastType*));

end;

1452. When the Parser encounters a numeral while seeking a closed subterm (§1508), it invokes this method to allocate a new *NumeralTerm*. The *gLastTerm* state variable is updated to point to this newly allocated numeral object.

⟨Extended subexpression implementation 1390⟩ +≡

procedure *extSubexpObj.ProcessNumeralTerm*;

begin *gLastTerm* ← *new*(*NumeralTermPtr*, *Init*(*CurPos*, *CurWord.Nr*));

end;

1453. The Parser tries to parse a closed subterm (§1508) and encounters the “it” token. Well, if the *it_Allowed* state variable is true, then we should allocate a new *ItTerm* and update the *gLastTerm* state variable to point to it.

Otherwise, when the *it_Allowed* state variable is false, we should raise a 251 error.

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.ProcessItTerm;
  begin if it_Allowed then gLastTerm ← new(ItTermPtr, Init(CurPos))
  else begin gLastTerm ← new(IncorrectTermPtr, Init(CurPos)); ErrImm(251)
  end;
end;
```

1454. The Parser tries parsing for a closed subterm and has encountered a placeholder term for a private functor (e.g., “\$1”). If the *dol_Allowed* state variable is true, then allocate a new *PlaceholderTerm* object and update the *gLastTerm* state variable to point at it.

If the *dol_Allowed* state variable is false, then we should raise a 181 error.

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.ProcessLocusTerm;
  begin if dol_Allowed then gLastTerm ← new(PlaceholderTermPtr, Init(CurPos, CurWord.Nr))
  else begin gLastTerm ← new(IncorrectTermPtr, Init(CurPos)); ErrImm(181)
  end;
end;
```

1455. Calamity! An incorrect expression has crossed the Parser’s path. Allocate an *IncorrectTerm* object located at the Parser’s current position, then update the *gLastTerm* state variable to point to it.

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.InsertIncorrTerm;
  begin gLastTerm ← new(IncorrectTermPtr, Init(CurPos));
end;
```

Subsection 23.3.4. Parsing formulas

1456. The Parser is trying to parse an atomic formula (§1541), but something has gone awry. Allocate a new *IncorrectFormula* object located at the Parser’s current position, update the *gLastFormula* state variable to point to it, and “reset” the *TermNbr* state variable to point to where the caller’s *nTermBase* is located.

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.InsertIncorrBasic;
  begin gLastFormula ← new(IncorrectFormulaPtr, Init(CurPos)); TermNbr ← nTermBase;
end;
```

1457. While the Parser was trying to parse a formula, it found something which “doesn’t quite fit”. Allocate a new *IncorrectFormula* object, then update the *gLastFormula* state variable to point to it.

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.InsertIncorrFormula;
  begin gLastFormula ← new(IncorrectFormulaPtr, Init(CurPos));
end;
```

1458. If we are in a proof, allocate a new *ThesisFormula* object (recall the **WEB** macro for this §????). Otherwise, raise a 65 error.

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.ProcessThesis;
  begin if gProofCnt > 0 then gLastFormula ← thesis_formula
  else begin ErrImm(65); gLastFormula ← new(IncorrectFormulaPtr, Init(CurPos));
    end;
  end;
```

1459. The Parser has encountered “⟨*Term*⟩ **is**”, or some other generic atomic formula (§1541), this method is invoked.

If more than one term appears before the “**is**” token (i.e., if $TermNbr - nTermBase \neq 1$), then a 157 error is raised. There is a Polish comment here, “Trzeba chyba wstawic recovery dla $TermNbr = nTermBase$ ”, which I translated to English.

This will initialize the fields for the caller in preparation for parsing some atomic formula. In particular, this is the only place where *TermNbr* is initialized to a nonzero value (and isn’t in an incorrect formula).

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.ProcessAtomicFormula;
  const MaxArgListNbr = 20;
  begin nSubexpPos ← CurPos; nSymbolNr ← 0;
  case CurWord.Kind of
    sy_Is: if  $TermNbr - nTermBase \neq 1$  then
      begin ErrImm(157); TermNbr ← nTermBase; InsertIncorrTerm; FinishArgument;
        { I think you need to insert recovery for  $TermNbr = nTermBase$  }
      end;
    endcases;
  nRightArgBase ← TermNbr; nTermBase ← TermNbr; nPostNegated ← false; nArgListNbr ← 0;
  nArgList[0].Start ← TermNbr + 1;
  end;
```

1460. The Parser is either finishing a “predicative formula” (§1540) or it’s parsing a predicate pattern (§1581), it invokes this method to initialize the fields needed when forming an AST node. Specifically, the *nSubexpPos* is assigned to the Parser’s current position, the *nSymbolNr* is updated either to the current token’s ID number (if the current token is “=” or a predicate) or else assigned to be zero. Last, the *nRightArgBase* is assigned to equal the *TermNbr* state variable.

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.ProcessPredicateSymbol;
  begin nSubexpPos ← CurPos;
  case CurWord.Kind of
    sy_Equal, PredicateSymbol: nSymbolNr ← CurWord.Nr;
    othercases nSymbolNr ← 0;
  endcases;
  nRightArgBase ← TermNbr;
  end;
```


1461. The Parser is parsing a “predicate formula” which has arguments on the righthand side of the predicate symbol (§1538).

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.ProcessRightSideOfPredicateSymbol;
  begin nRightSideOfPredPos ← CurPos;
  case CurWord.Kind of
    sy_Equal, PredicateSymbol: nSymbolNr ← CurWord.Nr;
  othercases nSymbolNr ← 0;
  endcases;
  nRightArgBase ← TermNbr;
end;
```

1462. The Parser has just finished a “predicate formula” (§1540), then this method is invoked to construct an AST for the formula. First we check if the format is valid. If the format for the formula is not found in the *gFormatsColl*, then we must raise a 153 error. Otherwise, we construct two lists (one for the left arguments, another for the right arguments), and use them to construct a new *PredicativeFormula* object. We update the *gLastFormula* state variable to point to the newly allocated formula object.

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.FinishPredicativeFormula;
  var lLeftArgs, lRightArgs: PList; lFormatNr: integer;
  begin lFormatNr ← gFormatsColl.LookUp_PredFormat(nSymbolNr, nRightArgBase − nTermBase,
    TermNbr − nRightArgBase);
  if lFormatNr = 0 then Error(nSubexpPos, 153); { missing format }
  lRightArgs ← CreateArgs(nRightArgBase + 1); lLeftArgs ← CreateArgs(nTermBase + 1);
  gLastFormula ← new(PredicativeFormulaPtr, Init(nSubexpPos, nSymbolNr, lLeftArgs, lRightArgs));
end;
```

1463. The Parser tries to construct an AST when finishing up the right-hand side of a predicative formula (§1538), it invokes this method after the *extSubexpObj.FinishPredicativeFormula* has been invoked.

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.FinishRightSideOfPredicativeFormula;
  var lRightArgs: PList; lLeftArgsNbr, lFormatNr: integer; lFrm: FormulaPtr;
  begin lFrm ← gLastFormula;
  if lFrm.nFormulaSort = wsNegatedFormula then lFrm ← NegativeFormulaPtr(lFrm).nArg;
  lLeftArgsNbr ← RightSideOfPredicativeFormulaPtr(lFrm).nRightArgs.Count;
  lFormatNr ← gFormatsColl.LookUp_PredFormat(nSymbolNr, lLeftArgsNbr, TermNbr − nRightArgBase);
  if lFormatNr = 0 then Error(nSubexpPos, 153); { missing format }
  lRightArgs ← CreateArgs(nRightArgBase + 1);
  gLastFormula ← new(RightSideOfPredicativeFormulaPtr, Init(nSubexpPos, nSymbolNr, lRightArgs));
  nMultiPredicateList.Insert(gLastFormula);
end;
```

1464. When the Parser is parsing an atomic formula, when it has parsed a formula and encounters another predicate, it defaults to thinking that it is starting a “multi-predicative formula” (§1539), and it invokes this method. This initializes the *nMultiPredicateList* to an empty list of length 4, and the first entry points to the same formula pointed to by the *gLastFormula* state variable.

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.StartMultiPredicativeFormula;
  begin nMultiPredicateList.Init(4); nMultiPredicateList.Insert(gLastFormula);
end;
```


1465. Finishing a “multi-predicative formula” allocates a new *MultiPredicativeFormula* object, and moves the contents of the caller’s *nMultiPredicateList* to the newly minted formula. The *gLastFormula* state variable is updated to point to this newly allocated formula object.

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.FinishMultiPredicativeFormula;
  begin gLastFormula ← new(MultiPredicativeFormulaPtr, Init(nSubexpPos, new(PList,
    MoveList(nMultiPredicateList))));
  end;
```

1466. The Parser has just parsed “⟨*Term*⟩ is ⟨*Type*⟩”, and now we need to store the accumulated data into a Formula AST. Of course, if the *gLastType* variable is not pointing to a type object, then we should raise an error (clearly something has gone wrong somewhere).

If we have accumulated attributes while parsing, then we should update the *gLastType* to be a clustered type object (and we should move the attributes over).

We should allocate a *QualifiedFormula* object, update the *gLastFormula* state variable to point to it. If the Parser has encountered “⟨*Term*⟩ is not ⟨*Type*⟩”, then it will tell the caller to toggle the *nPostNegated* to be true — and in that case, we should negate the *gLastFormula* state variable.

We mutate the *TermNbr* state variable, decrementing it by one (since we consumed the top of the term stack).

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.FinishQualifyingFormula;
  var j: integer;
  begin mizassert(5430, gLastType ≠ nil);
  if nAttrCollection.Count > 0 then
    begin gLastType ← new(ClusteredTypePtr, Init(gLastType↑.nTypePos, new(PList,
      Init(nAttrCollection.Count), gLastType)));
    for j ← 0 to nAttrCollection.Count − 1 do
      ClusteredTypePtr(gLastType)↑.nAdjectiveCluster↑.Insert(PObject(nAttrCollection.Items↑[j]));
    end;
    gLastFormula ← new(QualifyingFormulaPtr, Init(nSubexpPos, Term[TermNbr], gLastType));
    if nPostNegated then gLastFormula ← new(NegativeFormulaPtr, Init(nNotPos, gLastFormula));
    dec(TermNbr);
  end;
```

1467. The Parser has just finished parsing “⟨*Term*⟩ is ⟨*Attribute*⟩” or “⟨*Term*⟩ is not ⟨*Attribute*⟩”, and so it invokes this method. We allocate a new *AttributiveFormula* object, and negate it if needed. We also decrement the *TermNbr* state variable (since we consumed one element of the term stack).

⟨Extended subexpression implementation 1390⟩ +≡

```
procedure extSubexpObj.FinishAttributiveFormula;
  begin gLastFormula ← new(AttributiveFormulaPtr, Init(nSubExpPos, Term[TermNbr], new(PList,
    MoveList(nAttrCollection))));
  if nPostNegated then gLastFormula ← new(NegativeFormulaPtr, Init(nNotPos, gLastFormula));
  dec(TermNbr);
  end;
```

1468. While the Parser is working its way through a formula, and it is looking at an identifier and the next token is a square bracket “[”, then the Parser invokes this method to initialize the relevant fields to store accumulated data.

⟨Extended subexpression implementation 1390⟩ +≡

procedure *extSubexpObj.StartPrivateFormula*;

begin *nTermBase* \leftarrow *TermNbr*; *nSubexpPos* \leftarrow *CurPos*; *nSpelling* \leftarrow *CurWord.Nr*;
end;

1469. The Parser has just encountered “]” and now we assemble the accumulated data into a formula. This allocates a new *PrivatePredicativeFormula*, moves the arguments encountered since starting the private predicate into a list (§1393) owned by the formula object. The *gLastFormula* is updated to point to the newly allocated formula object.

⟨Extended subexpression implementation 1390⟩ +≡

procedure *extSubexpObj.FinishPrivateFormula*;

begin *gLastFormula* \leftarrow *new(PrivatePredicativeFormulaPtr, Init(nSubexpPos, nSpelling, CreateArgs(nTermBase + 1)))*;
end;

1470. The Parser has encountered the “contradiction” token, so it invokes this method, which allocates a *ContradictionFormula* and updates the *gLastFormula* state variable to point to it.

⟨Extended subexpression implementation 1390⟩ +≡

procedure *extSubexpObj.ProcessContradiction*;

begin *gLastFormula* \leftarrow *new(ContradictionFormulaPtr, Init(CurPos))*;
end;

1471. The Parser routinely allocates a formula object, then realizes later it should negate that formula object. This is handled by storing the formula object in the *gLastFormula* object, then this method allocates a new formula (which is the negation of the *gLastFormula*) and updates the *gLastFormula* to point to the newly allocated negated formula.

⟨Extended subexpression implementation 1390⟩ +≡

procedure *extSubexpObj.ProcessNegation*;

begin *gLastFormula* \leftarrow *new(NegativeFormulaPtr, Init(CurPos, gLastFormula))*;
end;

1472. When the Parser has encountered the “not” reserved keyword, it invokes the *ProcessNegation* method which just toggles the *nPostNegated* field of the caller, and assigns the *nNotPos* field to the Parser’s current position.

⟨Extended subexpression implementation 1390⟩ +≡

procedure *extSubexpObj.ProcessNegation*;

begin *nPostNegated* \leftarrow \neg *nPostNegated*; *nNotPos* \leftarrow *CurPos*;
end;

1473. When the Parser is looking at a binary connective token (e.g., “implies”, “or”, etc.), this method is invoked to store the connective kind as well as the “left-hand side” to the binary connective in the *nFirstSententialOperand* field.

⟨Extended subexpression implementation 1390⟩ +≡

procedure *extSubexpObj.ProcessBinaryConnective*;

begin *nConnective* \leftarrow *CurWord.Kind*; *nFirstSententialOperand* \leftarrow *gLastFormula*;
nSubexpPos \leftarrow *CurPos*;
end;

```

 $\langle \text{Extended subexpression implementation } 1390 \rangle \vdash \equiv$ 
procedure extSubexpObj.ProcessFlexDisjunction;
begin nFirstSententialOperand  $\leftarrow$  gLastFormula;
end;

```

```

⟨Extended subexpression implementation 1390⟩ +≡
procedure extSubexpObj.ProcessFlexConjunction;
begin nFirstSententialOperand ← gLastFormula;
end;

```

```

 $\langle \text{Extended subexpression implementation } 1390 \rangle \equiv$ 
procedure extSubexpObj.StartRestriction;
begin nRestrPos  $\leftarrow$  CurPos;
end;

```

```

 $\langle \text{Extended subexpression implementation } 1390 \rangle + \equiv$ 
procedure extSubexpObj.FinishRestriction;
begin nRestriction  $\leftarrow$  gLastFormula;
end;

```

```

⟨Extended subexpression implementation 1390⟩ +≡
procedure extSubexpObj.FinishBinaryFormula;

```

```

begin case nConnective of
sy_Implies: gLastFormula  $\leftarrow$  new(ConditionalFormulaPtr, Init(nSubExpPos, nFirstSententialOperand,
gLastFormula));
sy_Iff: gLastFormula  $\leftarrow$  new(BiconditionalFormulaPtr, Init(nSubexpPos, nFirstSententialOperand,
gLastFormula));
sy_Or: gLastFormula  $\leftarrow$  new(DisjunctiveFormulaPtr, Init(nSubexpPos, nFirstSententialOperand,
gLastFormula));
sy_Ampersand: gLastFormula  $\leftarrow$  new(ConjunctiveFormulaPtr, Init(nSubexpPos,
nFirstSententialOperand, gLastFormula));
othercases RunTimeError(3124);
endcases;
end;

```

1479. We have parsed “ $\langle Formula \rangle$ or ... or $\langle Formula \rangle$ ”, and the Parser invokes this method to construct an AST for the formula. This method allocates a new *FlexaryDisjunctive* formula object, and updates the *gLastFormula* state variable to point to it.

There is a comment in Polish, “polaczyc z flexConj”, which Google translates to “connect to flexConj”.

\langle Extended subexpression implementation 1390 $\rangle + \equiv$

```
procedure extSubexpObj.FinishFlexDisjunction; { polaczyc z flexConj }
begin gLastFormula  $\leftarrow$  new(FlexaryDisjunctiveFormulaPtr, Init(CurPos, nFirstSententialOperand,
    gLastFormula));
end;
```

1480. We have parsed “ $\langle Formula \rangle$ & ... & $\langle Formula \rangle$ ”, and the Parser invokes this method to construct an AST for the formula. This allocates a new *FlexaryConjunctive* formula object, and updates the *gLastFormula* state variable to point to it.

\langle Extended subexpression implementation 1390 $\rangle + \equiv$

```
procedure extSubexpObj.FinishFlexConjunction;
begin gLastFormula  $\leftarrow$  new(FlexaryConjunctiveFormulaPtr, Init(CurPos, nFirstSententialOperand,
    gLastFormula));
end;
```

1481. The Parser is looking at the “ex” token, then invokes this method to reset the caller’s fields in preparation for accumulating data needed when constructing the formula’s AST.

\langle Extended subexpression implementation 1390 $\rangle + \equiv$

```
procedure extSubexpObj.StartExistential;
begin nQualifiedSegments.Init(0); nSubexpPos  $\leftarrow$  CurPos;
end;
```

1482. The Parser is looking at the “for” token, and it invokes this method to reset the relevant fields in the caller.

\langle Extended subexpression implementation 1390 $\rangle + \equiv$

```
procedure extSubexpObj.StartUniversal;
begin nQualifiedSegments.Init(0); nSubexpPos  $\leftarrow$  CurPos;
end;
```

1483. After the Parser has invoked *StartUniversal* or *StartExistential*, it parses the quantified variables (which begins by invoking this method).

\langle Extended subexpression implementation 1390 $\rangle + \equiv$

```
procedure extSubexpObj.StartQualifiedSegment;
begin nSegmentIdentColl.Init(2); nSegmentPos  $\leftarrow$  CurPos;
end;
```

1484. The Parser has parsed a comma-separated list and is expecting either “be” or “being”, but before parsing for that copula the Parser invokes the *StartQualifyingType* method to update the *gLastType* state variable to point to **nil**.

\langle Extended subexpression implementation 1390 $\rangle + \equiv$

```
procedure extSubexpObj.StartQualifyingType;
begin gLastType  $\leftarrow$  nil;
end;
```

1485. The Parser has just finished parsing quantified variables. There are two possible situations:

- (1) We have just parsed reserved variables, so the types are all known. Then the $gLastType = \mathbf{nil}$.
- (2) We have parsed an explicitly typed list of variables, so the $gLastType \neq \mathbf{nil}$.

In the first case, we should allocate an *ImplicitlyQualifiedSegment* object and move all the segment's identifiers to this object. Then we clean up the caller's *nSegmentIdentColl* field (since it's an array of **nil** pointers).

In the second case, we can just move the identifiers when allocating a new *ExplicitlyQualifiedSegment* object.

In both cases, the new allocated *QuantifiedSegment* object is appended to the caller's *nQualifiedSegments* field.

(Extended subexpression implementation 1390) +≡

procedure *extSubexpObj.FinishQualifiedSegment*;

var *k*: integer;

begin if *gLastType* = **nil** **then**

begin for *k* ← 0 **to** *nSegmentIdentColl.Count* − 1 **do**

begin *nQualifiedSegments.Insert*(*new*(*ImplicitlyQualifiedSegmentPtr*,

Init(*VariablePtr*(*nSegmentIdentColl.Items*↑[*k*])↑.*nVarPos*, *nSegmentIdentColl.Items*↑[*k*]));

nSegmentIdentColl.Items↑[*k*] ← **nil**;

end;

nSegmentIdentColl.Done;

end

else begin *nQualifiedSegments.Insert*(*new*(*ExplicitlyQualifiedSegmentPtr*, *Init*(*nSegmentPos*,
new(*PList*, *MoveList*(*nSegmentIdentColl*)), *gLastType*)));

end;

end;

1486. When the Parser is parsing quantified variables, specifically when it is parsing a comma-separated list of variables, it will invoke this method, then check if the next token is a comma (and if so iterate). This *ProcessVariable* method should accumulate a *Variable* object with the current token's identifier, then insert it into the caller's *nSegmentIdentColl* field.

(Extended subexpression implementation 1390) +≡

procedure *extSubexpObj.ProcessVariable*;

begin *nSegmentIdentColl.Insert*(*new*(*VariablePtr*, *Init*(*CurPos*, *GetIdentifier*)));

end;

1487. The Parser has just finished something like

$$\text{ex } \langle \text{Qualified-Variables} \rangle , \dots , \langle \text{Qualified-Variables} \rangle \text{ st } \langle \text{Formula} \rangle$$

Now we assemble it as

$$\text{ex } \langle \text{Qualified-Variables} \rangle \text{ st } (\text{ex } \dots \text{ st } (\text{ex } \langle \text{Qualified-Variables} \rangle \text{ st } \langle \text{Formula} \rangle))$$

starting with the innermost existentially quantified formula, working our ways outwards.

Importantly, assembling the AST reflects the quantified variables has the grammar

$$\begin{aligned} \langle \text{Qualified-Variables} \rangle &= \langle \text{Implicitly-Qualified-Variables} \rangle \\ &\quad | \langle \text{Explicitly-Qualified-Variables} \rangle \\ &\quad | \langle \text{Explicitly-Qualified-Variables} \rangle " , " \langle \text{Implicitly-Qualified-Variables} \rangle \end{aligned}$$

(Extended subexpression implementation 1390) +≡

procedure *extSubexpObj.FinishExistential*;

var *k*: integer;

begin for *k* ← *nQualifiedSegments.Count* − 1 **downto** 1 **do** { from inside outwards }

begin *gLastFormula* ← new(*ExistentialFormulaPtr*,
Init(*QualifiedSegmentPtr*(*nQualifiedSegments.Items*↑[*k*])↑.*nSegmPos*,
nQualifiedSegments.Items↑[*k*], *gLastFormula*)); *nQualifiedSegments.Items*↑[*k*] ← nil;

end;

if *nQualifiedSegments.Count* > 0 **then**

begin *gLastFormula* ← new(*ExistentialFormulaPtr*, Init(*nSubexpPos*, *nQualifiedSegments.Items*↑[0],
gLastFormula)); *nQualifiedSegments.Items*↑[0] ← nil;

end;

nQualifiedSegments.Done;

end;

1488. Universally quantified formulas first transforms

$$\text{for } \langle \text{Qualified-Variables} \rangle \text{ st } \langle \text{Formula} \rangle_1 \text{ holds } \langle \text{Formula} \rangle_2$$

into

$$\text{for } \langle \text{Qualified-Variables} \rangle \text{ holds } \langle \text{Formula} \rangle_1 \text{ implies } \langle \text{Formula} \rangle_2$$

which is handled immediately.

The remainder of the method iteratively constructs the universally quantified formulas by “unrolling” the qualified segments, just as we did for existentially quantified formulas.

(Extended subexpression implementation 1390) +≡

procedure *extSubexpObj.FinishUniversal*;

var *k*: integer;

begin if *nRestriction* ≠ nil **then** { transform st into implies }

gLastFormula ← new(*ConditionalFormulaPtr*, Init(*nRestrPos*, *nRestriction*, *gLastFormula*));

for *k* ← *nQualifiedSegments.Count* − 1 **downto** 1 **do**

begin *gLastFormula* ← new(*UniversalFormulaPtr*,
Init(*QualifiedSegmentPtr*(*nQualifiedSegments.Items*↑[*k*])↑.*nSegmPos*,
nQualifiedSegments.Items↑[*k*], *gLastFormula*)); *nQualifiedSegments.Items*↑[*k*] ← nil;

end;

if *nQualifiedSegments.Count* > 0 **then**

begin *gLastFormula* ← new(*UniversalFormulaPtr*, Init(*nSubexpPos*, *nQualifiedSegments.Items*↑[0],
gLastFormula)); *nQualifiedSegments.Items*↑[0] ← nil;

end;

end;

Section 23.4. EXTENDED EXPRESSION CLASS

1489. When an expression is needed, the *gExpPtr* state variable is used to build it out of subexpressions. The *gExpPtr* state variable is an instance of the *extExpression* class.

⟨ Extended expression class declaration 1489 ⟩ ≡
extExpressionPtr = ↑*extExpressionObj*;
extExpressionObj = **object** (*ExpressionObj*)
constructor *Init* (*fExpKind* : *ExpKind*);
procedure *CreateSubexpression*; *virtual*;
end ;

This code is used in section 1199.

1490. Constructor. This just invokes the parent class's constructor (§711), then resets the module-wide variable *TermNbr* to zero.

⟨ Extended expression implementation 1490 ⟩ ≡
constructor *extExpressionObj.Init* (*fExpKind* : *ExpKind*);
begin *inherited Init* (*fExpKind*); *TermNbr* ← 0;
end;

See also section 1491.

This code is used in section 1200.

1491. An *extExpression* creating a subexpression *overrides* the parent class's method (§712), and sets the global *gSubexpPtr* to point to a new *extSubexp* object.

⟨ Extended expression implementation 1490 ⟩ +≡
procedure *extExpressionObj.CreateSubexpression*;
begin *gSubexpPtr* ← *new* (*extSubexpPtr*, *Init*)
end;

File 24

Parser

1492. The parser has a “big red button”: a single “obvious” function for the user to, you know, push. Namely, the *Parse* procedure (§§1603 *et seq.*). Everything else is just a helper function.

The design of the parser appears to be a recursive descent parser on statements, with parsing expressions handled specially.

Note that the `base/parser.pas` file appears to be naturally divided up into sections, with comments which appear to use the Germanic “s p a c i n g f o r i t a l i c s” (which I have just replaced with more readable *italicized* versions). I have used these cleavages to organize the discussion of this file.

The *StillCorrect* global variable is *false* when the parser has entered what programmers call “**Panic Mode**”: something has gone awry, and the parser is trying to recover gracefully. For a friendly review of panicking, see Bob Nystrom’s *Crafting Interpreters* (Chapter 6, Section 3).

```

⟨ parser.pas 1492 ⟩ ≡
  ⟨ GNU License 4 ⟩
unit parser;
interface
  uses mscanner;
  var StillCorrect: boolean = true;
  type ReadTokenProcedure = Procedure;
  const ReadTokenProc: ReadTokenProcedure = ReadToken; { from mscanner.pas }
  procedure Parse;
  procedure SemErr(fErrNr : integer);
implementation
  uses syntax, errhan, pragmas
    mdebug , info end_mdebug;
  ⟨ Implementation of parser.pas 1493 ⟩

```

1493. We have a few constants, but the implementation is loosely organized around parsing expressions (terms and formulas), statements, and then blocks.

```

⟨ Implementation of parser.pas 1493 ⟩ ≡
  ⟨ Local constants for parser.pas 1494 ⟩;
  ⟨ Parse expressions (parser.pas) 1502 ⟩
  ⟨ Communicate with items (parser.pas) 1549 ⟩
  ⟨ Process miscellany (parser.pas) 1552 ⟩
  ⟨ Parse simple justifications (parser.pas) 1563 ⟩
  ⟨ Parse statements and reasoning (parser.pas) 1566 ⟩
  ⟨ Parse patterns (parser.pas) 1575 ⟩
  ⟨ Parse definitions (parser.pas) 1584 ⟩
  ⟨ Parse scheme block (parser.pas) 1602 ⟩
  ⟨ Main parse method (parser.pas) 1603 ⟩

```

See also sections 1495, 1496, 1498, 1499, 1500, and 1501.

This code is used in section 1492.

1494. We have error codes for syntactically invalid situations. These are all different ways for panic to occur (hence the “pa-” prefix).

⟨Local constants for parser.pas 1494⟩ ≡

```
const paUnexpOf = 183; paUnexpOver = 184; paUnexpEquals = 186; paUnexpAntonym1 = 198;
  paUnexpAntonym2 = 198; paUnexpSynonym = 199; paUnpairedSymbol = 214; paEndExp = 215;
  paUnexpHereby = 216; paAdjClusterExp = 223; paUnexpReconsider = 228; paPerExp = 231;
  paSupposeOrCaseExp = 232; paOfExp = 256; paUnexpRedef = 273; paAllExp = 275;
  paIdentExp1 = 300; paIdentExp2 = 300; paIdentExp3 = 300; paIdentExp4 = 300; paIdentExp5 = 300;
  paIdentExp6 = 300; paIdentExp7 = 300; paIdentExp8 = 300; paIdentExp9 = 300; paIdentExp10 = 300;
  paIdentExp11 = 300; paIdentExp12 = 300; paIdentExp13 = 300; paWrongPredPattern = 301;
  paFunctExp1 = 302; paFunctExp2 = 302; paFunctExp3 = 302; paFunctExp4 = 302;
  paWrongModePatternBeg = 303; paStructExp1 = 304; paSelectExp1 = 305; paAttrExp1 = 306;
  paAttrExp2 = 306; paAttrExp3 = 306; paNumExp = 307; paWrongReferenceBeg = 308;
  paTypeOrAttrExp = 309; paRightBraExp1 = 310; paRightBraExp2 = 310;
  paWrongRightBracket1 = 311; paWrongRightBracket2 = 311; paDefExp = 312; paSchExp = 313;
  paWrongPattBeg1 = 314; paWrongPattBeg2 = 314; paWrongPattBeg3 = 314;
  paWrongModePatternSet = 315; paWrongAfterThe = 320; paWrongPredSymbol = 321;
  paSemicolonExp = 330; paUnexpConnective = 336; paWrongScopeBeg = 340; paThatExp1 = 350;
  paThatExp2 = 350; paCasesExp = 351; paLeftParenthExp = 360; paLeftSquareExp = 361;
  paLeftCurledExp = 362; paLeftDoubleExp1 = 363; paLeftDoubleExp3 = 363;
  paWrongSchemeVarQual = 364; paRightParenthExp1 = 370; paRightParenthExp2 = 370;
  paRightParenthExp3 = 370; paRightParenthExp4 = 370; paRightParenthExp5 = 370;
  paRightParenthExp6 = 370; paRightParenthExp7 = 370; paRightParenthExp8 = 370;
  paRightParenthExp9 = 370; paRightParenthExp10 = 370; paRightParenthExp11 = 370;
  paRightSquareExp1 = 371; paRightSquareExp2 = 371; paRightSquareExp3 = 371;
  paRightSquareExp4 = 371; paRightSquareExp5 = 371; paRightCurledExp1 = 372;
  paRightCurledExp2 = 372; paRightCurledExp3 = 372; paRightDoubleExp1 = 373;
  paRightDoubleExp2 = 373; paWrongAttrPrefixExpr = 375; paWrongAttrArgumentSuffix = 376;
  paTypeExpInAdjectiveCluster = 377; paEqualityExp1 = 380; paEqualityExp2 = 380; paIfExp = 381;
  paForExp = 382; paIsExp = 383; paColonExp1 = 384; paColonExp2 = 384; paColonExp3 = 384;
  paColonExp4 = 384; paArrowExp1 = 385; paArrowExp2 = 385; paMeansExp = 386; paStExp = 387;
  paAsExp = 388; paProofExp = 389; paWithExp = 390; paWrongItemBeg = 391;
  paUnexpItemBeg = 392; paWrongJustificationBeg = 395; paWrongFormulaBeg = 396;
  paWrongTermBeg = 397; paWrongRadTypeBeg = 398; paWrongFunctorPatternBeg = 399;
  paStillNotImplemented = 400; paNotExpected = 401; paInfinitiveExp = 402; paSuchExp = 403;
  paToExp = 404; paTypeUnexpInClusterRegistration = 405; paForOrArrowExpected = 406;
```

See also section 1497.

This code is used in section 1493.

1495. ⟨Implementation of parser.pas 1493⟩ +≡

```
var gAddSymbolsSet: set of char = []; { not used anywhere }
```

1496. Syntax errors do three things:

- (1) Marks *StillCorrect* to be false (i.e., enters panic mode)
- (2) Reports the error with the *ErrImm* (§106) function.
- (3) Skips ahead until we find a token in the *gMainSet*, then try to proceed like things are still alright (so we “fail gracefully”).

⟨Implementation of parser.pas 1493⟩ +≡

```
procedure SynErr(fPos : Position; fErrNr : integer);
begin if StillCorrect then
  begin StillCorrect  $\leftarrow$  false;
  if CurWord.Kind = sy_Error then
    begin if CurWord.Nr  $\neq$  scTooLongLineErrorNr then ErrImm(CurWord.Nr)
    else Error(fPos, fErrNr);
    end
  else Error(fPos, fErrNr);
  while  $\neg$ (CurWord.Kind  $\in$  gMainSet) do ReadTokenProc;
  end;
end;
```

1497. What constants are good “check-in points” for the parser to recover at? The beginning of blocks, the end of statements (especially semicolons), and the end of text.

⟨Local constants for parser.pas 1494⟩ +≡

```
const gMainSet: set of TokenKind = [sy_Begin, sy_Semicolon, sy_Proof, sy_Now, sy_Hereby,
  sy_Definition, sy_End, sy_Theorem, sy_Reserve, sy_Notation, sy_Registration, sy_Scheme, EOT,
  sy_Deffunc, sy_Defpred, sy_Reconsider, sy_Consider, sy_Then, sy_Per, sy_Case, sy_Suppose];
```

1498. We have a few more methods for *specific* kinds of errors we are likely to encounter.

⟨Implementation of parser.pas 1493⟩ +≡

```
procedure MissingWord(fErrNr : integer);
  var lPos: Position;
  begin lPos  $\leftarrow$  PrevPos; inc(lPos.Col); SynErr(lPos, fErrNr)
  end;

procedure WrongWord(fErrNr : integer);
  begin SynErr(CurPos, fErrNr)
  end;
```

1499. We will want to assert the parser has encountered a specific token (like a semicolon or “**end**”) and raise an error if it has not. This will make for much more readable code later on. We should recall *KillItem* (§686) mutates the global state.

⟨Implementation of parser.pas 1493⟩ +≡

```
procedure Semicolon;
  begin KillItem;
  if CurWord.Kind  $\neq$  sy_Semicolon then MissingWord(paSemicolonExp);
  if CurWord.Kind = sy_Semicolon then ReadTokenProc;
  end;

procedure AcceptEnd(fPos : Position);
  begin if CurWord.Kind = sy_End then ReadTokenProc
  else begin Error(fPos, paEndExp); MissingWord(paUnpairedSymbol)
  end;
end;
```

1500. These previous methods can be generalized to an *Accept* procedure which checks whether a given *TokenKind* has “occurred”. If so, just read the next word. Otherwise, flag an error.

⟨Implementation of parser.pas 1493⟩ +≡

```
procedure ReadWord;
  begin Mizassert(2546, StillCorrect); ReadTokenProc
  end;

function Occurs(fW : TokenKind): boolean;
  begin Occurs ← false;
  if CurWord.Kind = fW then
    begin ReadWord; Occurs ← true
    end
  end;

procedure Accept(fCh : TokenKind; fErrNr : integer);
  begin if ¬Occurs(fCh) then MissingWord(fErrNr)
  end;
```

1501. Flagging a semantic error should first check if we are in “panic mode” or not. If we are already panicking, there’s no reason to heap more panicky error messages onto the screen.

⟨Implementation of parser.pas 1493⟩ +≡

```
procedure SemErr(fErrNr : integer);
  begin if StillCorrect then ErrImm(fErrNr)
  end;
```

Section 24.1. EXPRESSIONS

1502. We have a few token kinds which indicate the start of a term:

- (1) identifiers (for variables and private functors),
- (2) infix operators,
- (3) numerals,
- (4) left and right brackets of all sorts,
- (5) the anaphoric “it” constant used in definitions,
- (6) “the” choice operator,
- (7) placeholder variables appearing in private functors and predicates,
- (8) structure symbols.

⟨ Parse expressions (`parser.pas`) 1502 ⟩ ≡
 { *Expressions* }

const *TermBegSys*: **set of**

TokenKind = [*Identifier*, *InfixOperatorSymbol*, *Numeral*, *LeftCircumfixSymbol*, *sy_LeftParanthesis*,
sy_It, *sy_LeftCurlyBracket*, *sy_LeftSquareBracket*, *sy_The*, *sy_Dolar*, *Structuresymbol*];

See also sections 1503, 1504, 1505, 1506, 1508, 1518, 1519, 1520, 1523, 1525, 1530, 1531, 1533, 1534, 1535, 1536, 1537, 1538, 1539, 1540, 1541, 1542, 1543, 1544, 1545, 1546, 1547, and 1548.

This code is used in section 1493.

Subsection 24.1.1. Terms

1503. We have a few helper function for *Accept*-ing parentheses. This invokes the *ProcessLeftParanthesis* method for the *gSubexpPtr* (§690) global variable which we recall (§718) is an empty virtual method. So the parser just “consumes” a left parentheses, and will continue to read tokens while they are left parentheses. The argument passed in will be mutated to track the number of left parentheses consumed.

Similarly, the *CloseParenth* method will have the compiler consume right parentheses, mutating the argument passed in (to decrement the number of right parentheses consumed). This will let us track mismatched parentheses errors.

⟨ Parse expressions (`parser.pas`) 1502 ⟩ +≡

procedure *OpenParenth*(**var** *fParenthCnt* : *integer*);

begin *fParenthCnt* ← 0;

while *CurWord.Kind* = *sy_LeftParanthesis* **do**

begin *gSubexpPtr*↑.*ProcessLeftParanthesis*; *ReadWord*; *inc*(*fParenthCnt*);

end;

end;

procedure *CloseParenth*(**var** *fParenthCnt* : *integer*);

begin while (*CurWord.Kind* = *sy_RightParanthesis*) ∧ (*fParenthCnt* > 0) **do**

begin *dec*(*fParenthCnt*); *gSubexpPtr*↑.*ProcessRightParanthesis*; *ReadWord*;

end;

end;

1504. Qualified expressions. Parsing qualified expressions includes a control flow for “exactly” qualified expressions.

We should recall from “Mizar in a nutshell” that the “**exactly**” keyword is reserved but not currently used for anything. The global subexpression pointer is invoking empty virtual methods (§718). So what’s going on?

Well, the only work being done here is in the branch handling “qua”, specifically the next word is read, and then control is handed off to *TypeSubexpression*.

⟨ Parse expressions (**parser.pas**) 1502 ⟩ +≡

procedure *TypeSubexpression*; *forward*;

procedure *AppendQua*;

begin while *CurWord.Kind* = *sy_Qua* **do**

begin *gSubexpPtr*↑.*ProcessQua*; *ReadWord*; *TypeSubexpression*; *gSubexpPtr*↑.*FinishQualifiedTerm*;
end;

if *CurWord.Kind* = *sy_Exactly* **then**

begin *gSubexpPtr*↑.*ProcessExactly*; *ReadWord*
end;

end;

1505. Parsing *the contents of* a bracketed term starts a bracketed term (§718), reads the next word after the start of the bracket, then consumes the maximum number of visible arguments (§682).

The contract for this function is that a left bracket token has been encountered, the parser has moved on to the next token, and then invoked this function.

⟨ Parse expressions (**parser.pas**) 1502 ⟩ +≡

procedure *GetArguments*(**const** *fArgsNbr*: *integer*); *forward*;

procedure *BracketedTerm*;

begin *gSubexpPtr*↑.*StartBracketedTerm*; *ReadWord*; *GetArguments*(*MaxVisArgNbr*);
gSubexpPtr↑.*FinishBracketedTerm*;

end;

1506. Parsing post-qualified variables (i.e., variables which appear in a Fraenkel term’s “**where**” clause) which consists of a comma-separated list of post-qualified segments.

⟨ Parse expressions (**parser.pas**) 1502 ⟩ +≡

procedure *TermSubexpression*; *forward*;

procedure *FormulaSubexpression*; *forward*;

procedure *ArgumentsTail*(*fArgsNbr* : *integer*); *forward*;

procedure *ProcessPostqualification*;

begin *gSubexpPtr*↑.*StartPostqualification*;

while *CurWord.Kind* = *sy_Where* **do**

begin repeat ⟨ Process post-qualified segment 1507 ⟩

until *CurWord.Kind* ≠ *sy_Comma*;

end;

end;

1507. Each “segment” in a post-qualification looks like:

$$\langle \text{variable} \rangle \{ ", " \langle \text{variable} \rangle \} ("is" \mid "being") \langle \text{type} \rangle$$

We can process the comma-separated list of variables, then the type ascription term (“is” or “being”), then process the type.

```

define process_postqualified_variables  $\equiv$  repeat gSubexpPtr↑.ProcessPostqualifiedVariable;
    Accept(Identifier, paIdentExp1);
until  $\neg$ Occurs(sy_Comma)
define post_qualified_type  $\equiv$  begin ReadWord; TypeSubexpression; end
 $\langle$  Process post-qualified segment 1507  $\rangle \equiv$ 
    gSubexpPtr↑.StartPostQualifyingSegment; ReadWord;
    process_postqualified_variables;
    gSubexpPtr↑.StartPostqualificationSpecyfication;
    if CurWord.Kind  $\in$  [sy_Is, sy_are] then post_qualified_type;
    gSubexpPtr↑.FinishPostqualifyingSegment;

```

This code is used in section 1506.

1508. Getting a closed subterm is part of the loop for parsing a term. The intricate relationship of mutually recursive function calls looks something like the following (assuming there are no parsing errors):

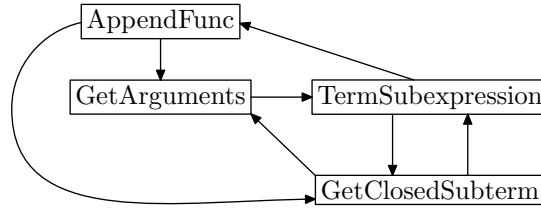


Fig. 8. Control flow when parsing a term.

The *GetArguments* parses a comma-separated list of terms. Since each term in the comma-separated list will be a *subterm* of a larger expression, we parse it with *TermSubexpression* (which invokes *GetClosedSubterm* in a mutually recursive relation). If there is a chain of infix operators (like $x + y - z \times \omega$), then *AppendFunc* is invoked on the infix operators.

```

 $\langle$  Parse expressions (parser.pas) 1502  $\rangle + \equiv$ 
procedure GetClosedSubterm;
    begin case CurWord.Kind of
         $\langle$  Get closed subterm of identifier 1509  $\rangle$ ;
         $\langle$  Get closed subterm of structure 1510  $\rangle$ ;
        Numeral: begin gSubexpPtr↑.ProcessNumeralTerm; ReadWord end;
         $\langle$  Get closed subterm of bracketed expression 1511  $\rangle$ ;
        sy_It: begin gSubexpPtr↑.ProcessItTerm; ReadWord end;
        sy_Dolar: begin gSubexpPtr↑.ProcessLocusTerm; ReadWord end;
         $\langle$  Get closed subterm of Fraenkel operator or enumerated set 1512  $\rangle$ ;
         $\langle$  Get closed subterm of choice operator 1515  $\rangle$ ;
    othercases RunTimeError(2133);
    endcases;
end;

```

1509. If we treat an identifier as a term, then it is either a private functor or it is a variable. How do we tell the difference? A private functor starts with an identifier followed by a left parentheses.

```

⟨ Get closed subterm of identifier 1509 ⟩ ≡
Identifier: if AheadWord.Kind = sy_LeftParanthesis then { treat identifier as private functor }
    begin gSubexpPtr↑.StartPrivateTerm; ReadWord; ReadWord;
    if CurWord.Kind ≠ sy_RightParanthesis then GetArguments(MaxVisArgNbr);
    gSubexpPtr↑.FinishPrivateTerm; Accept(sy_RightParanthesis, paRightParenthExp2);
    end
else { treat identifier as variable }
begin gSubexpPtr↑.ProcessSimpleTerm; ReadWord end

```

This code is used in section 1508.

1510. If the parser stumbles across the name of a structure when expecting a term, then the parser should treat it as constructing a new instance of the structure.

```

⟨ Get closed subterm of structure 1510 ⟩ ≡
StructureSymbol: begin gSubexpPtr↑.StartAggregateTerm; ReadWord;
    Accept(sy_StructLeftBracket, paLeftDoubleExp1); GetArguments(MaxVisArgNbr);
    gSubexpPtr↑.FinishAggregateTerm; Accept(sy_StructRightBracket, paRightDoubleExp1);
end

```

This code is used in section 1508.

1511. Encountering a left bracket of some kind should cause the parser to look for the contents of a bracketed term (§1505), then a right bracket.

```

⟨ Get closed subterm of bracketed expression 1511 ⟩ ≡
LeftCircumfixSymbol, sy_LeftSquareBracket: begin BracketedTerm;
    case Curword.Kind of
    sy_RightSquareBracket, sy_RightCurlyBracket, sy_RightParanthesis: ReadWord;
    othercases Accept(RightCircumfixSymbol, paRightBraExp1);
    endcases;
end

```

This code is used in section 1508.

1512. When the parser runs into a left curly bracket “{”, we either have encountered a Fraenkel operator or we have encountered a finite set.

```

⟨ Get closed subterm of Fraenkel operator or enumerated set 1512 ⟩ ≡
sy_LeftCurlyBracket: begin gSubexpPtr↑.StartBracketedTerm; ReadWord; TermSubexpression;
    if (CurWord.Kind = sy_Colon) ∨ (CurWord.Kind = sy_Where) then ⟨ Parse a Fraenkel operator 1513 ⟩
    else ⟨ Parse an enumerated set 1514 ⟩;
end

```

This code is used in section 1508.

1513. Parsing a Fraenkel operator, well, we recall Fraenkel operators look like

$$\{ \langle term \rangle \langle post-qualified segment \rangle " : " \langle formula \rangle \}$$

```

⟨ Parse a Fraenkel operator 1513 ⟩ ≡
begin gSubexpPtr↑.StartFraenkelTerm; ProcessPostqualification; gSubexpPtr↑.FinishSample;
    Accept(sy_Colon, paColonExp1); FormulaSubexpression; gSubexpPtr↑.FinishFraenkelTerm;
    Accept(sy_RightCurlyBracket, paRightCurledExp1);
end

```

This code is used in section 1512.

1514. We can also run into a finite set $\{x_1, \dots, x_n\}$.

```

⟨ Parse an enumerated set 1514 ⟩ ≡
  begin gSubexpPtr↑.FinishArgument; ArgumentsTail(MaxVisArgNbr − 1);
  gSubexpPtr↑.FinishBracketedTerm;
  case Curword.Kind of
    sy_RightSquareBracket, sy_RightCurlyBracket, sy_RightParanthesis: ReadWord;
  othercases Accept(RightCircumfixSymbol, paRightBraExp1);
  endcases;
  end

```

This code is used in section 1512.

1515. Mizar allows “the” to be used for selector functors, forgetful functors, choice operators, or simple Fraenkel terms.

```

⟨ Get closed subterm of choice operator 1515 ⟩ ≡
sy_The: begin gSubexpPtr↑.ProcessThe; ReadWord;
  case CurWord.Kind of
    SelectorSymbol: begin gSubexpPtr↑.StartSelectorTerm; ReadWord;
      if Occurs(sy_Of) then TermSubexpression;
      gSubexpPtr↑.FinishSelectorTerm;
      end;
    StructureSymbol: ⟨ Parse forgetful functor or choice of structure type 1516 ⟩;
    sy_Set: ⟨ Parse simple Fraenkel expression or “the set” 1517 ⟩;
    ModeSymbol, AttributeSymbol, sy_Non, sy_LeftParanthesis, Identifier, InfixOperatorSymbol, Numeral,
      LeftCircumfixSymbol, sy_It, sy_LeftCurlyBracket, sy_LeftSquareBracket, sy_The, sy_Dolar:
      begin gSubexpPtr↑.StartChoiceTerm; TypeSubexpression; gSubexpPtr↑.FinishChoiceTerm;
      end
    othercases begin gSubexpPtr↑.InsertIncorrTerm; WrongWord(paWrongAfterThe) end;
  endcases;
  end

```

This code is used in section 1508.

1516. A forgetful functor always looks like

"the" ⟨*structure*⟩ "of" ⟨*term*⟩

On the other hand, the choice operator acting on a structure type looks similar. We should distinguish these two by the presence of the keyword "of".

```

⟨ Parse forgetful functor or choice of structure type 1516 ⟩ ≡
  if AheadWord.Kind = sy_Of then { forgetful functor }
    begin gSubexpPtr↑.StartForgetfulTerm; ReadWord; Accept(sy_Of, paOfExp); TermSubexpression;
    gSubexpPtr↑.FinishForgetfulTerm;
    end
  else { choice operator }
    begin gSubexpPtr↑.StartChoiceTerm; TypeSubexpression; gSubexpPtr↑.FinishChoiceTerm;
    end

```

This code is used in section 1515.

1517. Mizar allows “**the set of**” to start a simple Fraenkel expression. But we could also refer to “**the set**” as the set chosen by the axiom of choice.

```

⟨ Parse simple Fraenkel expression or “the set” 1517 ⟩ ≡
  if AheadWord.Kind = sy_Of then { simple Fraenkel expression }
    begin ReadWord; { set }
      ReadWord; { of }
      gSubexpPtr↑.StartSimpleFraenkelTerm; Accept(sy_All, paAllExp); TermSubexpression;
      gSubexpPtr↑.StartFraenkelTerm; ProcessPostqualification; gSubexpPtr↑.FinishSimpleFraenkelTerm;
    end
  else { “the set” }
    begin gSubexpPtr↑.StartChoiceTerm; TypeSubexpression; gSubexpPtr↑.FinishChoiceTerm; end

```

This code is used in section 1515.

1518. Subexpression object’s *FinishArgument* (§1405) is invoked. This will invoke the *AppendQua* (§1504) method and expect a closed parentheses afterwards (§1503).

Possible bug: what should happen when *fParenthCnt* is zero or negative?

```

⟨ Parse expressions (parser.pas) 1502 ⟩ +≡
procedure CompleteArgument(var fParenthCnt : integer);
  begin gSubexpPtr↑.FinishArgument;
  repeat AppendQua; CloseParenth(fParenthCnt);
  until CurWord.Kind ≠ sy_Qua; { ∧(CurWord.Kind ≠ sy_Exactly) }
end;

```

1519. Keep parsing “infix operators”. When the current token is an infix operator, this will consume the arguments to its right, then iterate. It’s also worth remembering that *gExpPtr* (§690) was a global variable declared back in `syntax.pas`, and the *CreateSubexpression* (§1491) mutates the *gSubexpPtr* variable. Now we see it in action.

This invokes the *ProcessLeftParenthesis* method for the *gSubexpPtr* (§690) global variable which we recall (§718) is an empty virtual method. So the parser just “consumes” a left parentheses.

Note that the **case** expression considers the type of *TokenKind* (§724) of the current word. But it is not exhaustive.

There is a comment in Polish, “Chyba po prostu TermSubexpression”, which Google translated into English as “I guess it’s just Term Subexpression”. I swapped this in the code below.

```

⟨Parse expressions (parser.pas) 1502⟩ +≡
procedure AppendFunc(var fParenthCnt : integer);
begin while CurWord.Kind = InfixOperatorSymbol do
  begin gSubexpPtr↑.StartLongTerm; { (§1413) }
  repeat gSubexpPtr↑.ProcessFunctorSymbol; { (§1429) }
    ReadWord;
  case CurWord.Kind of
    sy_LeftParanthesis:
      begin { parenthesised term(s) }
        gSubexpPtr↑.ProcessLeftParenthesis; ReadWord; { consume the left paren }
        GetArguments(MaxVisArgNbr); { (§1534) }
        gSubexpPtr↑.ProcessRightParenthesis; Accept(sy_RightParanthesis, paRightParenthExp3);
          { consume matching right paren }
        end;
      Identifier, Numeral, LeftCircumfixSymbol, sy_It, sy_LeftCurlyBracket, sy_LeftSquareBracket, sy_The,
        sy_Dolar, StructureSymbol: { I guess it’s just Term Subexpression }
      begin gExpPtr↑.CreateSubexpression; { (§1491) }
        GetClosedSubterm; { (§1508) }
        gSubexpPtr↑.FinishArgument; { (§1405) }
        KillSubexpression; { (§684) }
      end;
    endcases;
    gSubexpPtr↑.FinishArgList; { (§1430) }
  until CurWord.Kind ≠ InfixOperatorSymbol;
  gSubexpPtr↑.FinishLongTerm; { (§1417) }
  CompleteArgument(fParenthCnt); { (§1518) }
end;
end;

```

1520. Parse terms with infix operators. Note this appears to parse infix operators as left-associative (e.g., $x + y + z$ is parsed as $(x + y) + z$).

⟨ Parse expressions (`parser.pas`) 1502 ⟩ +≡

```
procedure ProcessArguments;
  var lParenthCnt: integer;
  begin OpenParenth(lParenthCnt);
  case CurWord.Kind of
    Identifier, Numeral, LeftCircumfixSymbol, sy_It, sy_LeftCurlyBracket, sy_LeftSquareBracket, sy_The,
      sy_Dolar, StructureSymbol:
      begin GetClosedSubterm; CompleteArgument(lParenthCnt); end;
    InfixOperatorSymbol: ;
  othercases begin gSubexpPtr↑.InsertIncorrTerm; gSubexpPtr↑.FinishArgument;
    WrongWord(paWrongTermBeg);
  end;
endcases;
  ⟨ Keep parsing as long as there is an infix operator to the right 1521 ⟩;
  ⟨ Check every remaining open (left) parentheses has a corresponding partner 1522 ⟩;
end;
```

1521. ⟨ Keep parsing as long as there is an infix operator to the right 1521 ⟩ ≡

```
repeat AppendFunc(lParenthCnt);
  if CurWord.Kind = sy_Comma then
    begin ArgumentsTail(MaxVisArgNbr − 1);
    if (lParenthCnt > 0) ∧ (CurWord.Kind = sy_RightParanthesis) then
      begin dec(lParenthCnt); gSubexpPtr↑.ProcessRightParanthesis; ReadWord;
      end;
    end;
  until CurWord.Kind ≠ InfixOperatorSymbol
```

This code is used in section 1520.

1522. ⟨ Check every remaining open (left) parentheses has a corresponding partner 1522 ⟩ ≡

```
while lParenthCnt > 0 do
  begin gSubexpPtr↑.ProcessRightParanthesis; Accept(sy_RightParanthesis, paRightParenthExp1);
  dec(lParenthCnt);
  end
```

This code is used in section 1520.

1523. An adjective cluster is just one or more (possibly negated) attribute.

⟨ Parse expressions (`parser.pas`) 1502 ⟩ +≡

⟨ Process attributes (`parser.pas`) 1524 ⟩

```
procedure GetAdjectiveCluster;
  begin gSubexpPtr↑.StartAdjectiveCluster; ProcessAttributes; gSubexpPtr↑.FinishAdjectiveCluster;
  end;
```

1524. Parsing an attribute amounts to:

- (1) handling a leading “non”
- (2) handling attribute arguments (which always occurs *before* the attribute)
- (3) handling the attribute.

define *ahead_is_attribute_argument* \equiv (*CurWord.Kind* \in (*TermBegSys* – [*sy_LeftParanthesis*, *StructureSymbol*])) \vee ((*CurWord.Kind* = *sy_LeftParanthesis*) \wedge \neg (*AheadWord.Kind* \in [*sy_Set*, *ModeSymbol*, *StructureSymbol*])) \vee
 ((*CurWord.Kind* = *StructureSymbol*) \wedge (*AheadWord.Kind* = *sy_StructLeftBracket*))

\langle Process attributes (**parser.pas**) 1524 $\rangle \equiv$

procedure *ProcessAttributes*;

begin while (*CurWord.Kind* \in [*AttributeSymbol*, *sy_Non*]) \vee *ahead_is_attribute_argument* **do**
begin *gSubexpPtr* \uparrow .*ProcessNon*;
if *CurWord.Kind* = *sy_Non* **then** *ReadWord*;
if *ahead_is_attribute_argument* **then**
begin *gSubexpPtr* \uparrow .*StartAttributeArguments*; *ProcessArguments*;
gSubexpPtr \uparrow .*CompleteAttributeArguments*;
end;
if *CurWord.Kind* = *AttributeSymbol* **then**
begin *gSubexpPtr* \uparrow .*ProcessAttribute*; *ReadWord*; **end**
else begin *SynErr*(*CurPos*, *paAttrExp1*) **end**;
end;
end;

This code is used in section 1523.

1525. Parsing a radix type. For Mizar, a Radix type is either a structure type or a mode (or it’s the “set” type).

There is a comment in Polish, “zawieszone na czas zmiany semantyki”, which is translated into English.

\langle Parse expressions (**parser.pas**) 1502 $\rangle + \equiv$

procedure *RadixTypeSubexpression*;

var *lSymbol*, *lParenthCnt*: *integer*;
begin *lParenthCnt* \leftarrow 0; \langle Parse optional left-paren 1528 \rangle ;
gSubexpPtr \uparrow .*ProcessModeSymbol*; { (§1408) }
case *CurWord.Kind* **of**
sy_Set: **begin** *ReadWord*;
{ ? if Occurs(*syOf*) then TypeSubexpression suspended while semantics change }
end;
ModeSymbol: \langle Parse mode as radix type 1526 \rangle ;
StructureSymbol: \langle Parse structure as radix type 1527 \rangle ;
othercases begin *MissingWord*(*paWrongRadTypeBeg*); *gSubexpPtr* \uparrow .*InsertIncorrType* **end**;
endcases;
 \langle Close the parentheses 1529 \rangle ;
gSubexpPtr \uparrow .*FinishType*;
end;

1526. \langle Parse mode as radix type 1526 $\rangle \equiv$

begin *lSymbol* \leftarrow *CurWord.Nr*; *ReadWord*;
if *CurWord.Kind* = *sy_Of* **then**
if *ModeMaxArgs.fList* \uparrow [*lSymbol*] = 0 **then** *WrongWord*(*paUnexpOf*)
else begin *ReadWord*; *GetArguments*(*ModeMaxArgs.fList* \uparrow [*lSymbol*]) **end**;
end

This code is used in section 1525.

1527. $\langle \text{Parse structure as radix type } 1527 \rangle \equiv$
begin $lSymbol \leftarrow CurWord.Nr$; $ReadWord$;
if $CurWord.Kind = sy_Over$ **then**
 if $StructModeMaxArgs.fList[lSymbol] = 0$ **then** $WrongWord(paUnexpOver)$
 else begin $ReadWord$; $GetArguments(StructModeMaxArgs.fList[lSymbol])$ **end**;
end

This code is used in section 1525.

1528. $\langle \text{Parse optional left-paren } 1528 \rangle \equiv$
if $CurWord.Kind = sy_LeftParenthesis$ **then**
 begin $gSubexpPtr \uparrow.ProcessLeftParenthesis$; $ReadWord$; $inc(lParenthCnt)$;
 end

This code is used in section 1525.

1529. $\langle \text{Close the parentheses } 1529 \rangle \equiv$
if $lParenthCnt > 0$ **then**
 begin $gSubexpPtr \uparrow.ProcessRightParenthesis$; $Accept(sy_RightParenthesis, paRightParenthExp1)$;
 end

This code is used in section 1525.

1530. Now we have to parse the type subexpression. We basically get the adjectives with *GetAdjectiveCluster*, then we get the radix type with *RadixTypeSubexpression*.

$\langle \text{Parse expressions (parser.pas) } 1502 \rangle + \equiv$

procedure *TypeSubexpression*;

begin $gExpPtr \uparrow.CreateSubexpression$; $gSubexpPtr \uparrow.StartType$; $gSubexpPtr \uparrow.StartAttributes$;
 $GetAdjectiveCluster$; $RadixTypeSubexpression$;
 $gSubexpPtr \uparrow.CompleteAttributes$; $gSubexpPtr \uparrow.CompleteType$;
 $KillSubexpression$;
end;

1531. We should recall from Figure 8 (§1508) that this is a critical part of parsing terms.

$\langle \text{Parse expressions (parser.pas) } 1502 \rangle + \equiv$

procedure *TermSubexpression*;

var $lParenthCnt$: integer;
begin $gExpPtr \uparrow.CreateSubexpression$; $OpenParenth(lParenthCnt)$; { (§1503) }
case $CurWord.Kind$ **of**
 $Identifier$, $Numeral$, $LeftCircumfixSymbol$, sy_It , $sy_LeftCurlyBracket$, $sy_LeftSquareBracket$, sy_The ,
 sy_Dolar , $StructureSymbol$:
 begin $GetClosedSubterm$; $CompleteArgument(lParenthCnt)$; **end**;
 $InfixOperatorSymbol$: { skip } ;
othercases begin $gSubexpPtr \uparrow.InsertIncorrTerm$; $gSubexpPtr \uparrow.FinishArgument$;
 $WrongWord(paWrongTermBeg)$;
 end;
endcases;
 $AppendFunc(lParenthCnt)$; { (§1519) }
while $lParenthCnt > 0$ **do** $\langle \text{Parse arguments to the right } 1532 \rangle$;
 $gSubexpPtr \uparrow.FinishTerm$; $KillSubexpression$;
end;

1532. $\langle \text{Parse arguments to the right } 1532 \rangle \equiv$
begin *ArgumentsTail*(*MaxVisArgNbr* - 1); *dec*(*lParenthCnt*); *gSubexpPtr*↑.*ProcessRightParenthesis*;
Accept(*sy_RightParanthesis*, *paRightParenthExp10*);
if *CurWord.Kind* \neq *InfixOperatorSymbol* **then** *MissingWord*(*paFuncExp3*);
AppendFunc(*lParenthCnt*);
end

This code is used in section 1531.

1533. This will parse *fArgsNbr* comma separated terms. It's used to parse the arguments "to the right" of a term, for parsing the contents of an enumerated set (e.g., $\{x, y, z, w\}$), among many other places.

We should recall that the *StartArgument* method is empty.

$\langle \text{Parse expressions (parser.pas) } 1502 \rangle + \equiv$
procedure *ArgumentsTail*(*fArgsNbr* : integer);
begin while (*fArgsNbr* > 0) \wedge *Occurs*(*sy_Comma*) **do**
begin *gSubexpPtr*↑.*StartArgument*; *TermSubexpression*; *gSubexpPtr*↑.*FinishArgument*;
dec(*fArgsNbr*);
end;
end;

1534. Attributes, terms, predicates have terms as arguments. This relies upon the *FinishArguments* method (§1405).

$\langle \text{Parse expressions (parser.pas) } 1502 \rangle + \equiv$
procedure *GetArguments*(**const** *fArgsNbr*: integer);
begin if *fArgsNbr* > 0 **then**
begin *TermSubexpression*; *gSubexpPtr*↑.*FinishArgument*; *ArgumentsTail*(*fArgsNbr* - 1);
end;
end;

Subsection 24.1.2. Formulas

1535.

$\langle \text{Parse expressions (parser.pas) } 1502 \rangle + \equiv$
procedure *QuantifiedVariables*;
begin repeat *gSubexpPtr*↑.*StartQualifiedSegment*; *ReadWord*;
repeat *gSubexpPtr*↑.*ProcessVariable*; *Accept*(*Identifier*, *paIdentExp2*);
until \neg *Occurs*(*sy_Comma*);
gSubexpPtr↑.*StartQualifyingType*;
if *Occurs*(*sy_Be*) \vee *Occurs*(*sy_Being*) **then** *TypeSubexpression*;
gSubexpPtr↑.*FinishQualifiedSegment*;
until *CurWord.Kind* \neq *sy_Comma*;
end;

1536.

$\langle \text{Parse expressions (parser.pas) } 1502 \rangle + \equiv$
procedure *ExistentialFormula*;
begin *gSubexpPtr*↑.*StartExistential*; *QuantifiedVariables*; *gSubexpPtr*↑.*FinishQuantified*;
Accept(*sy_St*, *paStExp*); *FormulaSubexpression*; *gSubexpPtr*↑.*FinishExistential*;
end;

1537.

⟨ Parse expressions (parser.pas) 1502 ⟩ +≡

```

procedure UniversalFormula;
  begin gSubexpPtr↑.StartUniversal; QuantifiedVariables; gSubexpPtr↑.FinishQuantified;
  if CurWord.Kind = sy_St then
    begin gSubexpPtr↑.StartRestriction; ReadWord; FormulaSubexpression;
    gSubexpPtr↑.FinishRestriction;
    end;
  case CurWord.Kind of
    sy_Holds: begin gSubexpPtr↑.ProcessHolds; ReadWord
    end;
    sy_For, sy_Ex: ;
    othercases begin gSubexpPtr↑.InsertIncorrFormula; MissingWord(paWrongScopeBeg)
    end;
  endcases; FormulaSubexpression; gSubexpPtr↑.FinishUniversal;
end;

```

1538.

⟨ Parse expressions (parser.pas) 1502 ⟩ +≡

```

procedure ConditionalTail; forward;
procedure CompleteRightSideOfThePredicativeFormula(aPredSymbol : integer);
  begin gSubexpPtr↑.ProcessRightSideOfPredicateSymbol; ReadWord;
  if CurWord.Kind ∈ TermBegSys then GetArguments(PredMaxArgs.fList↑[aPredSymbol]);
  gSubexpPtr↑.FinishRightSideOfPredicativeFormula;
end;

```

1539. Recall a “multi-predicative formula” is something of the form $a \leq x \leq b$.

⟨ Parse expressions (parser.pas) 1502 ⟩ +≡

```

procedure CompleteMultiPredicativeFormula;
  begin gSubexpPtr↑.StartMultiPredicativeFormula;
  repeat case CurWord.Kind of
    sy_Equal, PredicateSymbol: CompleteRightSideOfThePredicativeFormula(CurWord.Nr);
    sy_Does, sy_Do: begin gSubexpPtr↑.ProcessDoesNot; ReadWord; Accept(sy_Not, paNotExpected);
    if CurWord.Kind ∈ [PredicateSymbol, sy_Equal] then
      begin CompleteRightSideOfThePredicativeFormula(CurWord.Nr); gSubexpPtr↑.ProcessNegative;
      end
    else begin gSubExpPtr↑.InsertIncorrFormula; SynErr(CurPos, paInfinitiveExp)
    end;
  end;
  endcases;
  until ¬(CurWord.Kind ∈ [sy_Equal, PredicateSymbol, sy_Does, sy_Do]);
  gSubexpPtr↑.FinishMultiPredicativeFormula;
end;

```

1540.

⟨ Parse expressions (parser.pas) 1502 ⟩ +≡

```

procedure CompletePredicativeFormula(aPredSymbol : integer);
  begin gSubexpPtr↑.ProcessPredicateSymbol; ReadWord;
  if CurWord.Kind ∈ TermBegSys then GetArguments(PredMaxArgs.fList↑[aPredSymbol]);
  gSubexpPtr↑.FinishPredicativeFormula;
end;

```

1541.

```

⟨ Parse expressions (parser.pas) 1502 ⟩ +≡
procedure CompleteAtomicFormula(var aParenthCnt : integer);
  var lPredSymbol: integer;
  label Predicate;
  begin repeat AppendFunc(aParenthCnt);
    if CurWord.Kind = sy_Comma then
      begin ArgumentsTail(MaxVisArgNbr - 1);
      if (aParenthCnt > 0) ∧ (CurWord.Kind = sy_RightParanthesis) then
        begin dec(aParenthCnt); gSubexpPtr↑.ProcessRightParenthesis; ReadWord;
        if CurWord.Kind ≠ InfixOperatorSymbol then MissingWord(paFunctExp1);
        end;
      end;
    until CurWord.Kind ≠ InfixOperatorSymbol;
    case CurWord.Kind of
      sy_Equal, PredicateSymbol: begin CompletePredicativeFormula(CurWord.Nr);
        if CurWord.Kind ∈ [sy_Equal, PredicateSymbol, sy_Does, sy_Do] then
          CompleteMultiPredicativeFormula
        end;
      sy_Does, sy_Do: begin gSubexpPtr↑.ProcessDoesNot; ReadWord; Accept(sy_Not, paNotExpected);
        if CurWord.Kind ∈ [PredicateSymbol, sy_Equal] then
          begin CompletePredicativeFormula(CurWord.Nr); gSubexpPtr↑.ProcessNegative;
          if CurWord.Kind ∈ [sy_Equal, PredicateSymbol, sy_Does, sy_Do] then
            CompleteMultiPredicativeFormula
          end
        else begin gSubExpPtr↑.InsertIncorrFormula; SynErr(CurPos, paInfinitiveExp)
        end;
        end;
      sy_Is: begin gSubexpPtr↑.ProcessAtomicFormula; ReadWord;
        if (CurWord.Kind = sy_Not) ∧ (AheadWord.Kind ∈ TermBegSys + [ModeSymbol, StructureSymbol,
          sy_Set, AttributeSymbol, sy_Non]) ∨ (CurWord.Kind ∈ TermBegSys + [ModeSymbol,
          StructureSymbol, sy_Set, AttributeSymbol, sy_Non]) then
          begin gSubexpPtr↑.StartType; gSubexpPtr↑.StartAttributes;
          if CurWord.Kind = sy_Not then
            begin gSubexpPtr↑.ProcessNegation; ReadWord;
            end;
            GetAdjectiveCluster;
          case CurWord.Kind of
            sy_LeftParanthesis, ModeSymbol, StructureSymbol, sy_Set: begin RadixTypeSubexpression;
              gSubexpPtr↑.CompleteAttributes; gSubexpPtr↑.CompleteType;
              gSubexpPtr↑.FinishQualifyingFormula;
            end;
            othercases begin gSubexpPtr↑.CompleteAttributes; gSubexpPtr↑.FinishAttributiveFormula;
            end;
          endcases;
        end
      else begin gSubExpPtr↑.InsertIncorrFormula; WrongWord(paTypeOrAttrExp);
      end;
    end;
  othercases begin gSubexpPtr↑.ProcessAtomicFormula; MissingWord(paWrongPredSymbol);
    gSubexpPtr↑.InsertIncorrBasic;
  end;

```



```

endcases;
end;

```

1542. There is a comment in Polish, a single word (“Kolejność”) which translates into English as “Order”.

⟨ Parse expressions (parser.pas) 1502 ⟩ +≡

```

procedure ViableFormula;
  var lParenthCnt: integer;
  label NotPrivate;
  begin gExpPtr↑.CreateSubexpression; OpenParenth(lParenthCnt);
  case CurWord.Kind of
    sy_For: UniversalFormula;
    sy_Ex: ExistentialFormula; { !!!!!!!!!!!!!!! Order }
    sy_Contradiction: begin gSubexpPtr↑.ProcessContradiction; ReadWord;
      end;
    sy_Thesis: begin gSubexpPtr↑.ProcessThesis; ReadWord;
      end;
    sy_Not: begin gSubexpPtr↑.ProcessNot; ReadWord; ViableFormula; KillSubexpression;
      gSubexpPtr↑.ProcessNegative;
      end;
  Identifier: if AheadWord.Kind = sy_LeftSquareBracket then
    begin gSubexpPtr↑.StartPrivateFormula; ReadWord; ReadWord;
    if CurWord.Kind ≠ sy_RightSquareBracket then GetArguments(MaxVisArgNbr);
      Accept(sy_RightSquareBracket, paRightSquareExp2); gSubexpPtr↑.FinishPrivateFormula;
    end
    else goto NotPrivate;
  Numeral, LeftCircumfixSymbol, sy_It, sy_LeftCurlyBracket, sy_LeftSquareBracket, sy_The, sy_Dolar,
    StructureSymbol: NotPrivate: begin gSubexpPtr↑.StartAtomicFormula;
    { ??? TermSubexpression }
    GetClosedSubterm; CompleteArgument(lParenthCnt); CompleteAtomicFormula(lParenthCnt);
  end;
  InfixOperatorSymbol, PredicateSymbol, sy_Does, sy_Do, sy_Equal: begin gSubexpPtr↑.StartAtomicFormula;
    CompleteAtomicFormula(lParenthCnt);
  end;
  othercases begin gSubexpPtr↑.InsertIncorrFormula; WrongWord(paWrongFormulaBeg)
  end;
endcases;
while lParenthCnt > 0 do
  begin ConditionalTail; gSubexpPtr↑.ProcessRightParenthesis;
    Accept(sy_RightParanthesis, paRightParenthExp4); dec(lParenthCnt); CloseParenth(lParenthCnt);
  end;
end;

```

1543.

⟨ Parse expressions (parser.pas) 1502 ⟩ +≡

```

procedure ConjunctiveTail;
  begin while (CurWord.Kind = sy_Ampersand) ∧ (AheadWord.Kind ≠ sy_Ellipsis) do
    begin gSubexpPtr↑.ProcessBinaryConnective; ReadWord; ViableFormula; KillSubexpression;
      gSubexpPtr↑.FinishBinaryFormula;
    end;
  end;

```

1544.

⟨ Parse expressions (parser.pas) 1502 ⟩ +≡

procedure *FlexConjunctiveTail*;

begin *ConjunctiveTail*;

if *CurWord.Kind* = *sy_Ampersand* **then**

begin *Assert*(*AheadWord.Kind* = *sy_Ellipsis*); *ReadWord*; *ReadWord*; *Accept*(*sy_Ampersand*, 402);

gSubexpPtr↑. *ProcessFlexConjunction*; *ViableFormula*; *ConjunctiveTail*; *KillSubexpression*;

gSubexpPtr↑. *FinishFlexConjunction*;

end;

end;

1545.

⟨ Parse expressions (parser.pas) 1502 ⟩ +≡

procedure *DisjunctiveTail*;

begin *FlexConjunctiveTail*;

while (*CurWord.Kind* = *sy_Or*) ∧ (*AheadWord.Kind* ≠ *sy_Ellipsis*) **do**

begin *gSubexpPtr*↑. *ProcessBinaryConnective*; *ReadWord*; *ViableFormula*; *FlexConjunctiveTail*;

KillSubexpression; *gSubexpPtr*↑. *FinishBinaryFormula*;

end;

end;

1546.

⟨ Parse expressions (parser.pas) 1502 ⟩ +≡

procedure *FlexDisjunctiveTail*;

begin *DisjunctiveTail*;

if *CurWord.Kind* = *sy_Or* **then**

begin *Assert*(*AheadWord.Kind* = *sy_Ellipsis*); *ReadWord*; *ReadWord*; *Accept*(*sy_Or*, 401);

gSubexpPtr↑. *ProcessFlexDisjunction*; *ViableFormula*; *DisjunctiveTail*; *KillSubexpression*;

gSubexpPtr↑. *FinishFlexDisjunction*;

end;

end;

1547.

⟨ Parse expressions (parser.pas) 1502 ⟩ +≡

procedure *ConditionalTail*;

begin *FlexDisjunctiveTail*;

case *CurWord.Kind* **of**

sy_Implies, *sy_Iff*: **begin** *gSubexpPtr*↑. *ProcessBinaryConnective*; *ReadWord*; *ViableFormula*;

FlexDisjunctiveTail; *KillSubexpression*; *gSubexpPtr*↑. *FinishBinaryFormula*;

case *CurWord.Kind* **of**

sy_Implies, *sy_Iff*: *WrongWord*(*paUnexpConnective*);

endcases;

end;

endcases;

end;

1548.

⟨ Parse expressions (parser.pas) 1502 ⟩ +≡

procedure *FormulaSubexpression*;

begin *ViableFormula*; *ConditionalTail*; *KillSubexpression*;

end;

Section 24.2. COMMUNICATION WITH ITEMS**1549.**

⟨ Communicate with items (`parser.pas`) 1549 ⟩ ≡
 { *Communication with items* }

```
procedure TermExpression;  
    begin gItemPtr↑.CreateExpression(exTerm); TermSubexpression; KillExpression;  
    end;
```

See also sections 1550 and 1551.

This code is used in section 1493.

1550.

⟨ Communicate with items (`parser.pas`) 1549 ⟩ +≡
procedure *TypeExpression*;
 begin *gItemPtr*↑.*CreateExpression*(*exType*); *TypeSubexpression*; *KillExpression*;
 end;

1551.

⟨ Communicate with items (`parser.pas`) 1549 ⟩ +≡
procedure *FormulaExpression*;
 begin *gItemPtr*↑.*CreateExpression*(*exFormula*); *FormulaSubexpression*; *KillExpression*;
 end;

Section 24.3. MISCELLANEOUS**1552.**

$\langle \text{Process miscellany (parser.pas) 1552} \rangle \equiv$
 $\{ \text{Miscellaneous} \}$
procedure *ProcessLab*;
 begin *gItemPtr*↑.*ProcessLabel*;
 if (*CurWord.Kind* = *Identifier*) \wedge (*AheadWord.Kind* = *sy_Colon*) **then**
 begin *ReadWord*; *ReadWord*
 end;
 end;

See also sections 1553, 1554, 1555, 1556, 1557, 1558, 1559, 1560, 1561, and 1562.

This code is used in section 1493.

1553.

$\langle \text{Process miscellany (parser.pas) 1552} \rangle + \equiv$
procedure *ProcessSentence*;
 begin *gItemPtr*↑.*StartSentence*; *FormulaExpression*; *gItemPtr*↑.*FinishSentence*;
 end;

1554.

$\langle \text{Process miscellany (parser.pas) 1552} \rangle + \equiv$
procedure *InCorrSentence*;
 begin *gItemPtr*↑.*StartSentence*; *gItemPtr*↑.*CreateExpression*(*exFormula*);
 gExpPtr↑.*CreateSubexpression*; *gSubexpPtr*↑.*InsertIncorrFormula*; *KillSubexpression*; *KillExpression*;
 gItemPtr↑.*FinishSentence*;
 end;

1555.

$\langle \text{Process miscellany (parser.pas) 1552} \rangle + \equiv$
procedure *InCorrStatement*;
 begin *gItemPtr*↑.*ProcessLabel*; *gItemPtr*↑.*StartRegularStatement*; *InCorrSentence*;
 end;

1556.

$\langle \text{Process miscellany (parser.pas) 1552} \rangle + \equiv$
procedure *ProcessHypotheses*;
 begin repeat *ProcessLab*; *ProcessSentence*; *gItemPtr*↑.*FinishHypothesis*;
 until $\neg \text{Occurs}(\text{sy_And})$
 end;

1557.

〈Process miscellany (parser.pas) 1552〉 +≡

```

procedure Assumption;
  begin if CurWord.Kind = sy_That then
    begin gItemPtr↑.StartCollectiveAssumption; ReadWord; ProcessHypotheses
    end
  else begin ProcessLab; ProcessSentence; gItemPtr↑.FinishHypothesis;
    end;
    gItemPtr↑.FinishAssumption;
  end;

```

1558.

〈Process miscellany (parser.pas) 1552〉 +≡

```

procedure FixedVariables;
  begin gItemPtr↑.StartFixedVariables;
  repeat gItemPtr↑.StartFixedSegment;
    repeat gItemPtr↑.ProcessFixedVariable; Accept(Identifier, paIdentExp4);
    until  $\neg$ Occurs(sy_Comma);
    gItemPtr↑.ProcessBeing;
    if Occurs(sy_Be)  $\vee$  Occurs(sy_Being) then TypeExpression;
    gItemPtr↑.FinishFixedSegment;
  until  $\neg$ Occurs(sy_Comma);
  gItemPtr↑.FinishFixedVariables;
end;

```

1559.

〈Process miscellany (parser.pas) 1552〉 +≡

```

procedure ProcessChoice;
  begin FixedVariables; Accept(sy_Such, paSuchExp); Accept(sy_That, paThatExp2);
  repeat gItemPtr↑.StartCondition; ProcessLab; ProcessSentence; gItemPtr↑.FinishCondition;
  until  $\neg$ Occurs(sy_And);
  gItemPtr↑.FinishChoice;
end;

```

1560.

〈Process miscellany (parser.pas) 1552〉 +≡

```

procedure Generalization;
  begin ReadWord; FixedVariables;
  if Occurs(sy_Such) then
    begin gItemPtr↑.StartAssumption; Accept(sy_That, paThatExp1); ProcessHypotheses;
    gItemPtr↑.FinishAssumption;
    end;
  end;

```

1561.

〈Process miscellany (parser.pas) 1552〉 +≡

```

procedure ExistentialAssumption;
  begin gBlockPtr↑.CreateItem(itExistentialAssumption); ReadWord; ProcessChoice;
end;

```

1562. \langle Process miscellany (**parser.pas**) 1552 $\rangle + \equiv$ **procedure** *Canceled*; **begin** *gBlockPtr*↑.*CreateItem(itCanceled)*; *ReadWord*; **if** *CurWord.Kind* = *Numeral* **then** *ReadWord*; *gItemPtr*↑.*FinishTheorem*; **end**;

Section 24.4. SIMPLE JUSTIFICATIONS**1563.**

⟨ Parse simple justifications (`parser.pas`) 1563 ⟩ ≡
 { *Simple Justifications* }

```

procedure GetReferences;
begin gItemPtr↑.StartReferences;
repeat ReadWord;
  case CurWord.Kind of
    MMLIdentifier: begin gItemPtr↑.StartLibraryReferences; ReadWord;
      if CurWord.Kind = sy_Colon then
        repeat ReadWord; gItemPtr↑.ProcessDef;
          if CurWord.Kind = ReferenceSort then
            begin if CurWord.Nr ≠ ord(syDef) then ErrImm(paDefExp);
              ReadWord;
            end;
            gItemPtr↑.ProcessTheoremNumber; Accept(Numeral, paNumExp);
          until (CurWord.Kind ≠ sy_Comma) ∨ (AheadWord.Kind = Identifier) ∨ (AheadWord.Kind =
            MMLIdentifier)
          else MissingWord(paColonExp4);
          gItemPtr↑.FinishTheLibraryReferences;
        end;
      Identifier: begin gItemPtr↑.ProcessPrivateReference; ReadWord
        end;
      othercases WrongWord(paWrongReferenceBeg);
    endcases;
  until CurWord.Kind ≠ sy_Comma;
  gItemPtr↑.FinishReferences;
end;

```

See also sections 1564 and 1565.

This code is used in section 1493.

1564.

〈 Parse simple justifications (`parser.pas`) 1563 〉 +≡
procedure *GetSchemeReference*;
 begin *gItemPtr*↑.*StartSchemeReference*; *ReadWord*;
 case *CurWord.Kind* **of**
 MMLIdentifier: **begin** *gItemPtr*↑.*StartSchemeLibraryReference*; *ReadWord*;
 if *CurWord.Kind* = *sy_Colon* **then**
 begin *ReadWord*; *gItemPtr*↑.*ProcessSch*;
 if *CurWord.Kind* = *ReferenceSort* **then**
 begin **if** *CurWord.Nr* ≠ *ord(sySch)* **then** *ErrImm(paSchExp)*;
 ReadWord;
 end
 else *ErrImm(paSchExp)*;
 gItemPtr↑.*ProcessSchemeNumber*; *Accept(Numeral, paNumExp)*;
 end
 else *MissingWord(paColonExp4)*;
 gItemPtr↑.*FinishSchLibraryReferences*;
 end;
 Identifier: **begin** *gItemPtr*↑.*ProcessSchemeReference*; *ReadWord*
 end;
 othercases *WrongWord(paWrongReferenceBeg)*;
 endcases;
 if *CurWord.Kind* = *sy_LeftParanthesis* **then**
 begin *GetReferences*; *Accept(sy_RightParanthesis, paRightParenthExp7)*
 end;
 gItemPtr↑.*FinishSchemeReference*;
 end;

1565.

〈 Parse simple justifications (`parser.pas`) 1563 〉 +≡
procedure *SimpleJustification*;
 begin *gItemPtr*↑.*StartSimpleJustification*;
 case *CurWord.Kind* **of**
 sy_By: *GetReferences*;
 sy_Semicolon, *sy_DotEquals*: ;
 sy_From: *GetSchemeReference*;
 othercases *WrongWord(paWrongJustificationBeg)*;
 endcases; *gItemPtr*↑.*FinishSimpleJustification*;
 end;

Section 24.5. STATEMENTS AND REASONINGS**1566.**

\langle Parse statements and reasoning (parser.pas) 1566 $\rangle \equiv$
 $\{ \textit{Statements \& Reasonings} \}$
procedure *Reasoning*; forward;
procedure *IgnoreProof*;
 var *lCounter*: integer; *ReasPos*: Position;
 begin *gBlockPtr*↑.StartAtSignProof; *ReasPos* ← *CurPos*; *ReadTokenProc*; *lCounter* ← 1;
 repeat case *CurWord.Kind* **of**
 sy_Proof, *sy_Now*, *sy_Hereby*, *sy_Case*, *sy_Suppose*: *inc*(*lCounter*);
 sy_End: *dec*(*lCounter*);
 sy_Reserve, *sy_Scheme*, *sy_Theorem*, *sy_Definition*, *sy_Begin*, *sy_Notation*, *sy_Registration*, *EOT*: **begin**
 AcceptEnd(*ReasPos*); *exit*
 end;
 endcases; *ReadTokenProc*;
 until *lCounter* = 0;
 gBlockPtr↑.FinishAtSignProof;
end;

See also sections 1567, 1568, 1569, 1570, 1571, 1572, 1573, and 1574.

This code is used in section 1493.

1567. Parsing either a “by” justification or a nested “proof” block.

\langle Parse statements and reasoning (parser.pas) 1566 $\rangle + \equiv$
procedure *Justification*;
 begin *gItemPtr*↑.StartJustification;
 case *CurWord.Kind* **of**
 sy_Proof: **if** *ProofPragma* **then** *Reasoning*
 else *IgnoreProof*;
 othercases *SimpleJustification*;
 endcases; *gItemPtr*↑.FinishJustification;
end;

1568.

\langle Parse statements and reasoning (parser.pas) 1566 $\rangle + \equiv$
procedure *ReadTypeList*;
 begin case *CurWord.Kind* **of**
 sy_RightSquareBracket, *sy_RightParanthesis*: ;
 othercases repeat *TypeExpression*; *gItemPtr*↑.FinishLocusType
 until \neg *Occurs*(*sy_Comma*);
 endcases;
end;

1569.

⟨ Parse statements and reasoning (`parser.pas`) 1566 ⟩ \vdash

procedure *RegularStatement*; *forward*;

procedure *PrivateItem*;

begin *gBlockPtr*↑.*ProcessLink*;

if *CurWord.Kind* = *sy.Then* **then** *ReadWord*;

case *CurWord.Kind* **of**

sy_Deffunc: **begin** *gBlockPtr*↑.*CreateItem(itPrivFuncDefinition)*; *ReadWord*;

gItemPtr↑.*StartPrivateDefiniendum*; *Accept(Identifier, paIdentExp6)*;

Accept(sy_LeftParanthesis, paLeftParenthExp); *ReadTypeList*;

Accept(sy_RightParanthesis, paRightParenthExp8); *gItemPtr*↑.*StartPrivateDefiniens*;

Accept(sy_Equal, paEqualityExp1); *TermExpression*; *gItemPtr*↑.*FinishPrivateFuncDefinienition*;

end;

sy_Deftpred: **begin** *gBlockPtr*↑.*CreateItem(itPrivPredDefinition)*; *ReadWord*;

gItemPtr↑.*StartPrivateDefiniendum*; *Accept(Identifier, paIdentExp7)*;

Accept(sy_LeftSquareBracket, paLeftSquareExp); *ReadTypeList*;

Accept(sy_RightSquareBracket, paRightSquareExp4); *gItemPtr*↑.*StartPrivateDefiniens*;

Accept(sy_Means, paMeansExp); *FormulaExpression*; *gItemPtr*↑.*FinishPrivatePredDefinienition*;

end;

sy_Set: **begin** *gBlockPtr*↑.*CreateItem(itConstantDefinition)*; *ReadWord*;

repeat *gItemPtr*↑.*StartPrivateConstant*; *Accept(Identifier, paIdentExp8)*;

Accept(sy_Equal, paEqualityExp2); *TermExpression*; *gItemPtr*↑.*FinishPrivateConstant*;

until \neg *Occurs(sy.Comma)*;

end;

sy_Reconsider: **begin** *gBlockPtr*↑.*CreateItem(itReconsider)*; *ReadWord*;

repeat *gItemPtr*↑.*ProcessReconsideredVariable*; *Accept(Identifier, paIdentExp9)*;

case *CurWord.Kind* **of**

sy_Equal: **begin** *ReadWord*; *TermExpression*; *gItemPtr*↑.*FinishReconsideredTerm*;

end;

else *gItemPtr*↑.*FinishDefaultTerm*;

end;

until \neg *Occurs(sy.Comma)*;

gItemPtr↑.*StartNewType*; *Accept(sy_As, paAsExp)*; *TypeExpression*; *gItemPtr*↑.*FinishReconsidering*;
 SimpleJustification;

end;

sy_Consider: **begin** *gBlockPtr*↑.*CreateItem(itChoice)*; *ReadWord*; *ProcessChoice*; *SimpleJustification*;

end;

Identifier, *sy.Now*, *sy_For*, *sy_Ex*, *sy_Not*, *sy_Thesis*, *sy_LeftSquareBracket*, *sy_Contradiction*,

PredicateSymbol, *sy_Does*, *sy_Do*, *sy_Equal*, *InfixOperatorSymbol*, *Numeral*, *LeftCircumfixSymbol*,

sy_LeftParanthesis, *sy_It*, *sy_Dolar*, *StructureSymbol*, *sy_The*, *sy_LeftCurlyBracket*, *sy_Proof*: **begin**

gBlockPtr↑.*CreateItem(itRegularStatement)*; *RegularStatement*;

end;

othercases begin *gBlockPtr*↑.*CreateItem(itIncorrItem)*; *WrongWord(paWrongItemBeg)*; **end**;

endcases;

end;

1570.

⟨ Parse statements and reasoning (parser.pas) 1566 ⟩ +≡

procedure *ProcessPragmas*; **begin while** *CurWord.Kind* = *Pragma* **do** **begin** *SetParserPragma*(*CurWord.Spelling*); *gBlockPtr*↑.*ProcessPragma*; *ReadTokenProc*; **end**; **end**;

1571.

⟨ Parse statements and reasoning (parser.pas) 1566 ⟩ +≡

procedure *LinearReasoning*; **begin while** *CurWord.Kind* ≠ *sy_End* **do** **begin** *StillCorrect* ← *true*; *ProcessPragmas*; **case** *CurWord.Kind* **of** *sy_Let*: **begin** *gBlockPtr*↑.*CreateItem*(*itGeneralization*); *Generalization*; **end**; *sy_Given*: *ExistentialAssumption*; *sy_Assume*: **begin** *gBlockPtr*↑.*CreateItem*(*itAssumption*); *ReadWord*; *Assumption*; **end**; *sy_Take*: **begin** *gBlockPtr*↑.*CreateItem*(*itExemplification*); *ReadWord*; **repeat if** (*CurWord.Kind* = *Identifier*) ∧ (*AheadWord.Kind* = *sy_Equal*) **then** **begin** *gItemPtr*↑.*ProcessExemplifyingVariable*; *ReadWord*; *ReadWord*; *TermExpression*; *gItemPtr*↑.*FinishExemplifyingVariable*; **end** **else begin** *gItemPtr*↑.*StartExemplifyingTerm*; *TermExpression*; *gItemPtr*↑.*FinishExemplifyingTerm*; **end**; **until** ¬*Occurs*(*sy_Comma*); **end**; *sy_Hereby*: **begin** *gBlockPtr*↑.*CreateItem*(*itConclusion*); *Reasoning*; **end**; *sy_Hence*: **begin** *gBlockPtr*↑.*ProcessLink*; *ReadWord*; *gBlockPtr*↑.*CreateItem*(*itConclusion*);
 RegularStatement; **end**; *sy_Thus*: **begin** *ReadWord*; *gBlockPtr*↑.*ProcessLink*; **if** *CurWord.Kind* = *sy_Then* **then** *ReadWord*; *gBlockPtr*↑.*CreateItem*(*itConclusion*); *RegularStatement*; **end**; *sy_Per*: *exit*; *sy_Case*, *sy_Suppose*: *exit*; *sy_Reserve*, *sy_Scheme*, *sy_Theorem*, *sy_Definition*, *sy_Begin*, *sy_Notation*, *sy_Registration*, *EOT*: *exit*; *sy_Then*: **begin if** *AheadWord.Kind* = *sy_Per* **then** **begin** *gBlockPtr*↑.*ProcessLink*; *ReadWord*; *exit*; **end** **else** *PrivateItem*; **end**; **othercases** *PrivateItem*; **endcases**; *Semicolon*; **end**; **end**;

1572.

⟨ Parse statements and reasoning (parser.pas) 1566 ⟩ +≡

procedure *NonBlockReasoning*;

var *CasePos*: *Position*; *lCaseKind*: *TokenKind*;

procedure *ProcessCase*;

begin *Assumption*; *Semicolon*; *LinearReasoning*;

if *CurWord.Kind* = *sy_Per* **then** *NonBlockReasoning*;

KillBlock; *AcceptEnd*(*CasePos*); *Semicolon*;

end;

begin case *CurWord.Kind* **of**

sy_Per, *sy_Case*, *sy_Suppose*: **begin** *gBlockPtr*↑. *CreateItem*(*itPerCases*); *Accept*(*sy_Per*, *paPerExp*);

Accept(*sy_Cases*, *paCasesExp*); *SimpleJustification*; *Semicolon*; *lCaseKind* ← *CurWord.Kind*;

if (*CurWord.Kind* ≠ *sy_Case*) ∧ (*CurWord.Kind* ≠ *sy_Suppose*) **then**

begin *MissingWord*(*paSupposeOrCaseExp*); *lCaseKind* ← *sy_Suppose*;

gBlockPtr↑. *CreateItem*(*itCaseBlock*); *gBlockPtr*↑. *CreateBlock*(*blSuppose*);

gBlockPtr↑. *CreateItem*(*itSupposeHead*); *StillCorrect* ← *true*; *CasePos* ← *CurPos*; *ProcessCase*;

end;

repeat while (*CurWord.Kind* = *sy_Case*) ∨ (*CurWord.Kind* = *sy_Suppose*) **do**

begin *gBlockPtr*↑. *CreateItem*(*itCaseBlock*);

if *lCaseKind* = *sy_Case* **then** *gBlockPtr*↑. *CreateBlock*(*blCase*)

else *gBlockPtr*↑. *CreateBlock*(*blSuppose*);

CasePos ← *CurPos*; *StillCorrect* ← *true*;

if *lCaseKind* = *sy_Case* **then** *gBlockPtr*↑. *CreateItem*(*itCaseHead*)

else *gBlockPtr*↑. *CreateItem*(*itSupposeHead*);

if *CurWord.Kind* ≠ *lCaseKind* **then** *ErrImm*(58);

ReadWord; *ProcessCase*;

end;

case *Curword.Kind* **of**

sy_Reserve, *sy_Scheme*, *sy_Theorem*, *sy_Definition*, *sy_Begin*, *sy_Notation*, *sy_Registration*, *EOT*: *exit*;

sy_End: ;

othercases begin *MissingWord*(*paSupposeOrCaseExp*); *gBlockPtr*↑. *CreateItem*(*itCaseBlock*);

if *lCaseKind* = *sy_Case* **then** *gBlockPtr*↑. *CreateBlock*(*blCase*)

else *gBlockPtr*↑. *CreateBlock*(*blSuppose*);

if *lCaseKind* = *sy_Case* **then** *gBlockPtr*↑. *CreateItem*(*itCaseHead*)

else *gBlockPtr*↑. *CreateItem*(*itSupposeHead*);

StillCorrect ← *true*; *CasePos* ← *CurPos*; *ProcessCase*;

end;

endcases;

until (*Curword.Kind* = *sy_End*);

end;

endcases;

end;

1573.

⟨ Parse statements and reasoning (parser.pas) 1566 ⟩ +≡

```

procedure Reasoning;
  var ReasPos: Position;
  begin ReasPos ← CurPos;
  case CurWord.Kind of
    sy_Proof: begin gBlockPtr↑.CreateBlock(blProof); ReadTokenProc; end;
    sy_Hereby: begin gBlockPtr↑.CreateBlock(blHereby); ReadTokenProc; end;
    sy_Now: begin gBlockPtr↑.CreateBlock(blDiffuse); ReadTokenProc; end;
    othercases begin gBlockPtr↑.CreateBlock(blProof); WrongWord(paProofExp); end;
  endcases;
  LinearReasoning; NonBlockReasoning; KillBlock; AcceptEnd(ReasPos);
end;

```

1574.

⟨ Parse statements and reasoning (parser.pas) 1566 ⟩ +≡

```

procedure RegularStatement;
  begin ProcessLab; gItemPtr↑.StartRegularStatement;
  case CurWord.Kind of
    sy_Now: Reasoning;
    othercases begin ProcessSentence;
      case CurWord.Kind of
        sy_Proof: begin gItemPtr↑.StartJustification;
          if ProofPragma then Reasoning
          else IgnoreProof;
          gItemPtr↑.FinishJustification;
          end;
        othercases begin gItemPtr↑.StartJustification; SimpleJustification; gItemPtr↑.FinishJustification;
          gItemPtr↑.FinishCompactStatement;
          while CurWord.Kind = sy_DotEquals do
            begin gItemPtr↑.StartIterativeStep; ReadWord; TermExpression;
              gItemPtr↑.ProcessIterativeStep; gItemPtr↑.StartJustification; SimpleJustification;
              gItemPtr↑.FinishJustification; gItemPtr↑.FinishIterativeStep;
            end;
          end;
        endcases;
      end;
    endcases;
  end;
endcases;
end;

```

Section 24.6. PATTERNS**1575.**

$\langle \text{Parse patterns (parser.pas) 1575} \rangle \equiv$
 $\{ \text{Patterns} \}$
var *gVisibleNbr*: integer;
procedure *GetVisible*;
 begin *gItemPtr*↑.ProcessVisible; inc(*gVisibleNbr*); Accept(*Identifier*, *paIdentExp3*);
 end;

See also sections 1576, 1577, 1578, 1579, 1580, 1581, 1582, and 1583.

This code is used in section 1493.

1576.

$\langle \text{Parse patterns (parser.pas) 1575} \rangle + \equiv$
procedure *ReadVisible*;
 begin *gItemPtr*↑.StartVisible; *gVisibleNbr* ← 0;
 repeat *GetVisible*;
 until $\neg \text{Occurs}(\text{sy_Comma})$;
 gItemPtr↑.FinishVisible;
 end;

1577.

$\langle \text{Parse patterns (parser.pas) 1575} \rangle + \equiv$
procedure *GetModePattern*;
 var *lModesymbol*: integer;
 begin *gItemPtr*↑.StartModePattern;
 case *CurWord.Kind* **of**
 sy_Set: **begin** **if** *AheadWord.Kind* = *sy_Of* **then** WrongWord(*paWrongModePatternSet*)
 else *ReadWord*;
 end;
 ModeSymbol: **begin** *lModeSymbol* ← *CurWord.Nr*; *gVisibleNbr* ← 0; *ReadWord*;
 gItemPtr↑.ProcessModePattern;
 if *Occurs*(*sy_Of*) **then** *ReadVisible*;
 if (*ModeMaxArgs.fList*↑[*lModeSymbol*] < *gVisibleNbr*) \vee (*ModeMaxArgs.fList*↑[*lModeSymbol*] = \$FF)
 then *ModeMaxArgs.fList*↑[*lModeSymbol*] ← *gVisibleNbr*;
 end
 othercases WrongWord(*paWrongModePatternBeg*);
 endcases; *gItemPtr*↑.FinishModePattern;
 end;

1578.

$\langle \text{Parse patterns (parser.pas) 1575} \rangle + \equiv$
procedure *ReadParams*;
 begin **if** *Occurs*(*sy_LeftParanthesis*) **then**
 begin *ReadVisible*; Accept(*sy_RightParanthesis*, *paRightParenthExp5*)
 end
 else **if** *CurWord.Kind* = *Identifier* **then**
 begin *gItemPtr*↑.StartVisible; *GetVisible*; *gItemPtr*↑.FinishVisible;
 end;
 end;

1579.

⟨ Parse patterns (parser.pas) 1575 ⟩ +≡

```

procedure GetAttrPattern;
  begin gItemPtr↑.StartAttributePattern; gVisibleNbr ← 0; GetVisible;
  gItemPtr↑.ProcessAttributePattern; Accept(sy_Is, paIsExp);
  if Occurs(sy_LeftParanthesis) then
    begin ReadVisible; Accept(sy_RightParanthesis, paRightParenthExp11)
    end
  else if CurWord.Kind = Identifier then ReadVisible;
  gItemPtr↑.FinishAttributePattern; Accept(AttributeSymbol, paAttrExp2);
end;

```

1580.

⟨ Parse patterns (parser.pas) 1575 ⟩ +≡

```

procedure GetFuncPattern;
  begin gItemPtr↑.StartFunctorPattern;
  case CurWord.Kind of
    Identifier, InfixOperatorSymbol, sy_LeftParanthesis: begin ReadParams;
      gItemPtr↑.ProcessFunctorSymbol; { (§1322) }
      Accept(InfixOperatorSymbol, paFunctExp2); ReadParams; gItemPtr↑.FinishFunctorPattern;
    end;
    LeftCircumfixSymbol, sy_LeftSquareBracket, sy_LeftCurlyBracket: begin ReadWord; ReadVisible;
      gItemPtr↑.FinishFunctorPattern;
    case Curword.Kind of
      sy_RightSquareBracket, sy_RightCurlyBracket, sy_RightParanthesis: ReadWord;
    othercases Accept(RightCircumfixSymbol, paRightBraExp2);
    endcases;
  end;
othercases begin WrongWord(paWrongFunctorPatternBeg); gItemPtr↑.FinishFunctorPattern;
end;
endcases;
end;

```

1581.

⟨ Parse patterns (parser.pas) 1575 ⟩ +≡

```

procedure GetPredPattern;
  var lPredSymbol: integer;
  begin gItemPtr↑.StartPredicatePattern;
  if CurWord.Kind = Identifier then ReadVisible;
  gItemPtr↑.ProcessPredicateSymbol;
  case CurWord.Kind of
    sy_Equal, PredicateSymbol: begin lPredSymbol ← CurWord.Nr;
      if CurWord.Kind = sy_Equal then lPredSymbol ← EqualitySym;
      gVisibleNbr ← 0; ReadWord;
      if CurWord.Kind = Identifier then ReadVisible;
      if (PredMaxArgs.fList↑[lPredSymbol] < gVisibleNbr) ∨ (PredMaxArgs.fList↑[lPredSymbol] = $FF)
        then PredMaxArgs.fList↑[lPredSymbol] ← gVisibleNbr;
      end;
    othercases WrongWord(paWrongPredPattern);
  endcases; gItemPtr↑.FinishPredicatePattern;
end;

```

1582.

⟨ Parse patterns (parser.pas) 1575 ⟩ +≡

procedure *Specification*;

begin *gItemPtr*↑.*StartSpecification*; *Accept*(*sy_Arrow*, *paArrowExp1*); *TypeExpression*;
gItemPtr↑.*FinishSpecification*;
end;

1583.

⟨ Parse patterns (parser.pas) 1575 ⟩ +≡

procedure *GetStructPatterns*;

var *lStructureSymbol*: integer;
begin *gBlockPtr*↑.*CreateItem*(*itDefStruct*); *ReadWord*;
if *CurWord*.*Kind* = *sy_LeftParanthesis* **then**
 begin repeat *gItemPtr*↑.*StartPrefix*; *ReadWord*; *TypeExpression*; *gItemPtr*↑.*FinishPrefix*;
 until *CurWord*.*Kind* ≠ *sy_Comma*;
 Accept(*sy_RightParanthesis*, *paRightParenthExp6*);
 end;
 gItemPtr↑.*ProcessStructureSymbol*; *lStructureSymbol* ← \$FF;
 if *CurWord*.*Kind* = *StructureSymbol* **then** *lStructureSymbol* ← *CurWord*.*Nr*;
 Accept(*StructureSymbol*, *paStructExp1*);
 if *Occurs*(*sy_Over*) **then** *ReadVisible*;
 gItemPtr↑.*StartFields*;
 if *lStructureSymbol* ≠ \$FF **then**
 if (*StructModeMaxArgs*.*fList*↑[*lStructureSymbol*] < *gVisibleNbr*) ∨
 (*StructModeMaxArgs*.*fList*↑[*lStructureSymbol*] = \$FF) **then**
 StructModeMaxArgs.*fList*↑[*lStructureSymbol*] ← *gVisibleNbr*;
 Accept(*sy_StructLeftBracket*, *paLeftDoubleExp3*);
 repeat *gItemPtr*↑.*StartAggrPattSegment*;
 repeat *gItemPtr*↑.*ProcessField*; *Accept*(*SelectorSymbol*, *paSelectExp1*);
 until ¬*Occurs*(*sy_Comma*);
 Specification; *gItemPtr*↑.*FinishAggrPattSegment*;
 until ¬*Occurs*(*sy_Comma*);
 gItemPtr↑.*FinishFields*; *Accept*(*sy_StructRightBracket*, *paRightDoubleExp2*);
end;

Section 24.7. DEFINITIONS**1584.**

⟨ Parse definitions (`parser.pas`) 1584 ⟩ ≡
 { *Definitions* }

```
procedure ConstructionType;
begin gItemPtr↑.StartConstructionType;
if CurWord.Kind = sy_Arrow then
  begin ReadWord; TypeExpression
  end;
gItemPtr↑.FinishConstructionType;
end;
```

See also sections 1585, 1586, 1587, 1588, 1589, 1590, 1591, 1592, 1593, 1594, 1595, 1596, 1597, 1598, 1599, 1600, and 1601.

This code is used in section 1493.

1585.

⟨ Parse definitions (`parser.pas`) 1584 ⟩ +≡

```
procedure Correctness;
begin while CurWord.Kind = sy_CorrectnessCondition do
  begin StillCorrect ← true; gBlockPtr↑.CreateItem(itCorrCond); ReadWord; Justification;
  Semicolon;
  end;
gItemPtr↑.ProcessCorrectness; { o jaki tu item chodzi? definitional-item? }
if CurWord.Kind = sy_Correctness then
  begin StillCorrect ← true; gBlockPtr↑.CreateItem(itCorrectness); ReadWord; Justification;
  Semicolon;
  end;
end;
```

1586.

⟨ Parse definitions (parser.pas) 1584 ⟩ +≡

```

procedure Definition;
  var lDefKind: TokenKind; lDefiniensExpected: boolean;
  begin lDefKind ← CurWord.Kind; lDefiniensExpected ← true;
  case CurWord.Kind of
    sy_Mode: begin gBlockPtr↑.CreateItem(itDefMode); ReadWord; GetModePattern;
      case CurWord.Kind of
        sy_Is: begin gItemPtr↑.StartExpansion; ReadWord; TypeExpression; lDefiniensExpected ← false;
          end;
        othercases ConstructionType;
      endcases;
    end;
    sy_Attr: begin gBlockPtr↑.CreateItem(itDefAttr); ReadWord; GetAttrPattern;
      end;
    sy_Struct: begin GetStructPatterns; lDefiniensExpected ← false;
      end;
    sy_Func: begin gBlockPtr↑.CreateItem(itDefFunc); ReadWord; GetFuncPattern; ConstructionType;
      end;
    sy_Pred: begin gBlockPtr↑.CreateItem(itDefPred); ReadWord; gItemPtr↑.StartDefPredicate;
      GetPredPattern;
      end;
  endcases;
  if lDefiniensExpected then
    case CurWord.Kind of
      sy_Means: begin gItemPtr↑.ProcessMeans; ReadWord;
        if Occurs(sy_Colon) then
          begin gItemPtr↑.ProcessDefiniensLabel; Accept(Identifier, paIdentExp10);
            Accept(sy_Colon, paColonExp2);
          end
        else gItemPtr↑.ProcessDefiniensLabel;
          gItemPtr↑.StartDefiniens; FormulaExpression;
          if CurWord.Kind = sy_If then
            begin gItemPtr↑.StartGuard; ReadWord; FormulaExpression; gItemPtr↑.FinishGuard;
              while Occurs(sy_Comma) do
                begin FormulaExpression; gItemPtr↑.StartGuard; Accept(sy_If, paIfExp);
                  FormulaExpression; gItemPtr↑.FinishGuard;
                end;
              if CurWord.Kind = sy_Otherwise then
                begin gItemPtr↑.StartOtherwise; ReadWord; FormulaExpression; gItemPtr↑.FinishOtherwise;
                  end;
                end
              else gItemPtr↑.FinishOtherwise;
                gItemPtr↑.FinishDefiniens;
              end;
            end
          sy_Equals: if lDefKind ≠ sy_Func then
            begin WrongWord(paUnexpEquals);
              end
            else begin gItemPtr↑.ProcessEquals; ReadWord;
              if Occurs(sy_Colon) then
                begin gItemPtr↑.ProcessDefiniensLabel; Accept(Identifier, paIdentExp10);
                  Accept(sy_Colon, paColonExp2);

```

```

    end
  else gItemPtr↑.ProcessDefiniensLabel;
    gItemPtr↑.StartEquals; TermExpression;
  if CurWord.Kind = sy_If then
    begin gItemPtr↑.StartGuard; ReadWord; FormulaExpression; gItemPtr↑.FinishGuard;
    while Occurs(sy_Comma) do
      begin TermExpression; gItemPtr↑.StartGuard; Accept(sy_If, paIfExp); FormulaExpression;
      gItemPtr↑.FinishGuard;
    end;
    if CurWord.Kind = sy_Otherwise then
      begin gItemPtr↑.StartOtherwise; ReadWord; TermExpression; gItemPtr↑.FinishOtherwise;
    end;
  end
  else gItemPtr↑.FinishOtherwise;
    gItemPtr↑.FinishDefiniens;
  end;
endcases;
Semicolon; Correctness;
while (CurWord.Kind = sy_Property) do
  begin gBlockPtr↑.CreateItem(itProperty); StillCorrect ← true; ReadWord; Justification; Semicolon;
  end;
gBlockPtr↑.FinishDefinition;
end;

```

1587.

⟨ Parse definitions (*parser.pas*) 1584 ⟩ +=

```

function CurrPatternKind: TokenKind;
  begin if CurWord.Kind = ModeSymbol then CurrPatternKind ← ModeSymbol
  else if CurWord.Kind = StructureSymbol then CurrPatternKind ← StructureSymbol
  else if (CurWord.Kind = Identifier) ∧ (AheadWord.Kind = sy_Is) then
    CurrPatternKind ← AttributeSymbol
  else if (CurWord.Kind ∈ [LeftCircumfixSymbol, sy_LeftCurlyBracket,
    sy_LeftSquareBracket, sy_LeftParanthesis, InfixOperatorSymbol]) ∨ (CurWord.Kind =
    Identifier) ∧ (AheadWord.Kind = InfixOperatorSymbol) then
    CurrPatternKind ← InfixOperatorSymbol
  else if (CurWord.Kind = PredicateSymbol) ∨ (CurWord.Kind = sy_Equal) ∨ (CurWord.Kind =
    Identifier) ∧ (AheadWord.Kind ∈ [sy_Comma, PredicateSymbol, sy_Equal]) then
    CurrPatternKind ← PredicateSymbol
  else if (CurWord.Kind = sy_The) ∧ (AheadWord.Kind = SelectorSymbol) then
    CurrPatternKind ← SelectorSymbol
  else if (CurWord.Kind = sy_The) ∧ (AheadWord.Kind = StructureSymbol) then
    CurrPatternKind ← ForgetfulFunctor
  else CurrPatternKind ← sy_Error;
end;

```

1588.

⟨ Parse definitions (parser.pas) 1584 ⟩ +≡

```

procedure Synonym;
  begin ReadWord;
  case CurrPatternKind of
    ModeSymbol: begin    { Mode synonym }
      gBlockPtr↑.CreateItem(itModeNotation); GetModePattern; gItemPtr↑.ProcessModeSynonym;
      Accept(sy_For, paForExp); GetModePattern;
    end;
    AttributeSymbol: begin  { Attribute synonym }
      gBlockPtr↑.CreateItem(itAttrSynonym); GetAttrPattern; gItemPtr↑.ProcessAttrSynonym;
      Accept(sy_For, paForExp); GetAttrPattern;
    end;
    InfixOperatorSymbol: begin  { Functor synonym }
      gBlockPtr↑.CreateItem(itFuncNotation); GetFuncPattern; gItemPtr↑.ProcessFuncSynonym;
      Accept(sy_For, paForExp); GetFuncPattern;
    end;
    PredicateSymbol: begin    { Predicate synonym }
      gBlockPtr↑.CreateItem(itPredSynonym); gItemPtr↑.StartDefPredicate; GetPredPattern;
      gItemPtr↑.ProcessPredSynonym; Accept(sy_For, paForExp); GetPredPattern;
    end
    othercases begin gBlockPtr↑.CreateItem(itIncorrItem); ErrImm(paWrongPattBeg1);
    end;
  endcases;
end;

```

1589.

⟨ Parse definitions (parser.pas) 1584 ⟩ +≡

```

procedure Antonym;
  begin ReadWord;
  case CurrPatternKind of
    Attributesymbol: begin  { Attribute antonym }
      gBlockPtr↑.CreateItem(itAttrAntonym); GetAttrPattern; gItemPtr↑.ProcessAttrAntonym;
      Accept(sy_For, paForExp); GetAttrPattern;
    end;
    PredicateSymbol: begin  { Predicate antonym }
      gBlockPtr↑.CreateItem(itPredAntonym); gItemPtr↑.StartDefPredicate; GetPredPattern;
      gItemPtr↑.ProcessPredAntonym; Accept(sy_For, paForExp); GetPredPattern;
    end
    othercases begin gBlockPtr↑.CreateItem(itIncorrItem); ErrImm(paWrongPattBeg2);
    end;
  endcases;
end;

```

1590.

⟨ Parse definitions (parser.pas) 1584 ⟩ +≡

```

procedure UnexpectedItem;
  begin case CurWord.Kind of
    sy_Case, sy_Suppose, sy_Hereby: begin ErrImm(paWrongItemBeg); ReadWord;
      if CurWord.Kind = sy_That then ReadWord;
        PrivateItem;
      end;
    sy_Per: begin gBlockPtr↑.CreateItem(itIncorrItem); ErrImm(paWrongItemBeg); ReadWord;
      if CurWord.Kind = sy_Cases then
        begin ReadWord; InCorrStatement; SimpleJustification;
        end;
      end;
    othercases begin ErrImm(paUnexpItemBeg); StillCorrect ← true; PrivateItem;
    end;
  endcases;
end;

```

1591.

⟨ Parse definitions (parser.pas) 1584 ⟩ +≡

```

procedure DefinitionalBlock;
  var DefPos: Position;
  begin gBlockPtr↑.CreateItem(itDefinition); gBlockPtr↑.CreateBlock(blDefinition); DefPos ← CurPos;
  ReadWord;
  while CurWord.Kind ≠ sy_End do
    begin StillCorrect ← true; gBlockPtr↑.ProcessRedefine;
    if Occurs(sy_Redefine) then
      if ¬(CurWord.Kind ∈ [sy_Mode, sy_Attr, sy_Func, sy_Pred]) then Error(PrevPos, paUnexpRedef);
    case CurWord.Kind of
      sy_Mode, sy_Attr, sy_Struct, sy_Func, sy_Pred: Definition;
      sy_Begin, EOT, sy_Reserve, sy_Scheme, sy_Theorem, sy_Definition, sy_Registration, sy_Notation: break;
      Pragma: ProcessPragmas;
    othercases begin case CurWord.Kind of
      sy_Let: begin gBlockPtr↑.CreateItem(itLocDeclaration); Generalization;
        end;
      sy_Given: ExistentialAssumption;
      sy_Assume: begin gBlockPtr↑.CreateItem(itAssumption); ReadWord; Assumption;
        end;
      sy_Canceled: Canceled;
      sy_Case, sy_Suppose, sy_Per, sy_Hereby: UnexpectedItem;
      othercases PrivateItem;
    endcases; Semicolon;
    end;
  endcases;
  end;
  KillBlock; AcceptEnd(DefPos);
end;

```

1592.

⟨ Parse definitions (`parser.pas`) 1584 ⟩ +≡

procedure *NotationBlock*;

var *DefPos*: *Position*;

begin *gBlockPtr*↑.*CreateItem*(*itDefinition*); *gBlockPtr*↑.*CreateBlock*(*blNotation*); *DefPos* ← *CurPos*;
 ReadWord;

while *CurWord.Kind* ≠ *sy_End* **do**

begin *StillCorrect* ← *true*;

case *CurWord.Kind* **of**

sy_Begin, *EOT*, *sy_Reserved*, *sy_Scheme*, *sy_Theorem*, *sy_Definition*, *sy_Registration*, *sy_Notation*: *break*;

Pragma: *ProcessPragmas*;

othercases begin case *CurWord.Kind* **of**

sy_Synonym: *Synonym*;

sy_Antonym: *Antonym*;

sy_Let: **begin** *gBlockPtr*↑.*CreateItem*(*itLocDeclaration*); *ReadWord*; *FixedVariables*;

end;

othercases *UnexpectedItem*;

endcases; *Semicolon*;

end;

endcases;

end;

KillBlock; *AcceptEnd*(*DefPos*);

end;

1593.

⟨ Parse definitions (`parser.pas`) 1584 ⟩ +≡

```

procedure ATTSubexpression(var aExpKind : ExpKind);
  var lAttrExp: boolean;
  begin aExpKind ← exNull; gSubexpPtr↑.StartAttributes;
  while (CurWord.Kind ∈ [AttributeSymbol,
    sy_Non]) ∨ (CurWord.Kind ∈ (TermBegSys - [sy_LeftParanthesis,
    StructureSymbol])) ∨ ((CurWord.Kind = sy_LeftParanthesis) ∧ ¬(AheadWord.Kind ∈ [sy_Set,
    ModeSymbol, StructureSymbol])) ∨ (CurWord.Kind = StructureSymbol) ∧ (AheadWord.Kind =
    sy_StructLeftBracket) do
    begin gSubexpPtr↑.ProcessNon; lAttrExp ← CurWord.Kind = sy_Non;
    if CurWord.Kind = sy_Non then ReadWord;
    if (CurWord.Kind ∈ (TermBegSys - [StructureSymbol])) ∨ (CurWord.Kind =
      StructureSymbol) ∧ (AheadWord.Kind = sy_StructLeftBracket) then
      begin if aExpKind = exNull then aExpKind ← exTerm;
        gSubexpPtr↑.StartAttributeArguments; ProcessArguments; gSubexpPtr↑.FinishAttributeArguments;
      end;
    if CurWord.Kind = AttributeSymbol then
      begin aExpKind ← exAdjectiveCluster; gSubexpPtr↑.ProcessAttribute; ReadWord;
    end
    else begin if lAttrExp ∨ (aExpKind = exAdjectiveCluster) then
      begin gSubexpPtr↑.ProcessAttribute; SynErr(CurPos, paAttrExp3);
    end;
    break;
    end;
  end;
  gSubexpPtr↑.CompleteAttributes;
end;

```

1594.

⟨ Parse definitions (parser.pas) 1584 ⟩ +≡

```

procedure RegisterCluster;
  var lExpKind: ExpKind;
  begin gBlockPtr↑.CreateItem(itCluster); ReadWord;
  if (CurWord.Kind = Identifier) ∧ (AheadWord.Kind = sy_Arrow) then ErrImm(paFunctExp4);
  gItemPtr↑.StartAttributes; { (§1278) }
  gItemPtr↑.CreateExpression(exAdjectiveCluster); { (§1351) }
  gExpPtr↑.CreateSubexpression; ATTSubexpression(lExpKind);
  case lExpKind of
    exTerm: gSubexpPtr↑.CompleteClusterTerm;
    exNull, exAdjectiveCluster: gSubexpPtr↑.CompleteAdjectiveCluster;
  endcases;
  KillSubexpression; KillExpression;
  case lExpKind of
    exTerm: begin gItemPtr↑.FinishClusterTerm; Accept(sy_Arrow, paArrowExp2);
      gItemPtr↑.CreateExpression(exAdjectiveCluster); gExpPtr↑.CreateSubexpression;
      gSubexpPtr↑.StartAttributes; ATTSubexpression(lExpKind);
      if lExpKind ≠ exAdjectiveCluster then
        begin ErrImm(paAdjClusterExp)
        end;
      gSubexpPtr↑.CompleteAdjectiveCluster; KillSubexpression; KillExpression;
      gItemPtr↑.FinishConsequent;
      if CurWord.Kind = sy_For then
        begin ReadWord; gItemPtr↑.CreateExpression(exType); gExpPtr↑.CreateSubexpression;
          gSubexpPtr↑.StartType; gSubexpPtr↑.StartAttributes; GetAdjectiveCluster;
          RadixTypeSubexpression; gSubexpPtr↑.CompleteAttributes; gSubexpPtr↑.CompleteType;
          gSubexpPtr↑.CompleteClusterType; KillSubexpression; KillExpression;
        end;
      gItemPtr↑.FinishClusterType;
    end;
    exNull, exAdjectiveCluster: case CurWord.Kind of
      sy_Arrow: begin gItemPtr↑.FinishAntecedent; ReadWord;
        gItemPtr↑.CreateExpression(exAdjectiveCluster); gExpPtr↑.CreateSubexpression;
        gSubexpPtr↑.StartAttributes; ATTSubexpression(lExpKind);
        if lExpKind ≠ exAdjectiveCluster then
          begin ErrImm(paAdjClusterExp);
          end;
        gSubexpPtr↑.CompleteAdjectiveCluster; KillSubexpression; KillExpression;
        gItemPtr↑.FinishConsequent; Accept(sy_For, paForExp); gItemPtr↑.CreateExpression(exType);
        gExpPtr↑.CreateSubexpression; gSubexpPtr↑.StartType; gSubexpPtr↑.StartAttributes;
        GetAdjectiveCluster; RadixTypeSubexpression; gSubexpPtr↑.CompleteAttributes;
        gSubexpPtr↑.CompleteType; gSubexpPtr↑.CompleteClusterType; KillSubexpression; KillExpression;
        gItemPtr↑.FinishClusterType;
      end;
      sy_For: begin gItemPtr↑.FinishConsequent; ReadWord; gItemPtr↑.CreateExpression(exType);
        gExpPtr↑.CreateSubexpression; gSubexpPtr↑.StartType; gSubexpPtr↑.StartAttributes;
        GetAdjectiveCluster; RadixTypeSubexpression; gSubexpPtr↑.CompleteAttributes;
        gSubexpPtr↑.CompleteType; gSubexpPtr↑.CompleteClusterType; KillSubexpression; KillExpression;
        gItemPtr↑.FinishClusterType;
      end;
    othercases begin SynErr(CurPos, paForOrArrowExpected); gItemPtr↑.FinishConsequent;

```



```

    gItemPtr↑.CreateExpression(exType); gExpPtr↑.CreateSubexpression; gSubexpPtr↑.StartType;
    gSubexpPtr↑.InsertIncorrType; gSubexpPtr↑.CompleteType; gSubexpPtr↑.CompleteClusterType;
    KillSubexpression; KillExpression; gItemPtr↑.FinishClusterType;
  end;
endcases;
endcases; Semicolon; Correctness;
end;

```

1595.

⟨ Parse definitions (parser.pas) 1584 ⟩ +≡

```

procedure Reduction;
  var lExpKind: ExpKind;
  begin gBlockPtr↑.CreateItem(itReduction); ReadWord;
  if (CurWord.Kind = Identifier) ∧ (AheadWord.Kind = sy_Arrow) then ErrImm(paFuncExp4);
  gItemPtr↑.StartFuncReduction; TermExpression; gItemPtr↑.ProcessFuncReduction;
  Accept(sy_To, paToExp); TermExpression; gItemPtr↑.FinishFuncReduction; Semicolon; Correctness;
  end;

```

1596.

⟨ Parse definitions (parser.pas) 1584 ⟩ +≡

```

procedure Identification;
  begin gBlockPtr↑.CreateItem(itIdentify); ReadWord; { begin }
  gItemPtr↑.StartFuncIdentify; GetFuncPattern; gItemPtr↑.ProcessFuncIdentify;
  Accept(sy_With, paWithExp); GetFuncPattern; gItemPtr↑.CompleteFuncIdentify; { end; }
  if CurWord.Kind = sy_When then
    begin ReadWord;
    repeat gItemPtr↑.ProcessLeftLocus; Accept(Identifier, paIdentExp3);
      Accept(sy_Equal, paEqualityExp1); gItemPtr↑.ProcessRightLocus; Accept(Identifier, paIdentExp3);
    until ¬Occurs(sy_Comma);
    end;
  Semicolon; Correctness;
  end;

```

1597.

⟨ Parse definitions (parser.pas) 1584 ⟩ +≡

```

procedure RegisterProperty;
  begin gBlockPtr↑.CreateItem(itPropertyRegistration);
  case PropertyKind(CurWord.Nr) of
    sySethood: begin ReadWord; Accept(sy_of, paOfExp); gItemPtr↑.StartSethoodProperties;
      TypeExpression; gItemPtr↑.FinishSethoodProperties; Justification;
    end;
  othercases begin SynErr(CurPos, paStillNotImplemented);
  end;
  endcases; Semicolon;
  end;

```

1598.

⟨ Parse definitions (parser.pas) 1584 ⟩ +≡

procedure *RegistrationBlock*;

var *DefPos*: *Position*;

begin *gBlockPtr*↑.*CreateItem*(*itDefinition*); *gBlockPtr*↑.*CreateBlock*(*blRegistration*);

DefPos ← *CurPos*; *ReadWord*;

while *CurWord.Kind* ≠ *sy_End* **do**

begin *StillCorrect* ← *true*;

case *CurWord.Kind* **of**

sy_Cluster: *RegisterCluster*;

sy_Reduce: *Reduction*;

sy_Identify: *Identification*;

sy_Property: *RegisterProperty*;

sy_Begin, *EOT*, *sy_Resume*, *sy_Scheme*, *sy_Theorem*, *sy_Definition*, *sy_Registration*, *sy_Notation*: *break*;

Pragma: *ProcessPragmas*;

othercases begin case *CurWord.Kind* **of**

sy_Let: **begin** *gBlockPtr*↑.*CreateItem*(*itLocDeclaration*); *ReadWord*; *FixedVariables*;

end;

sy_Canceled: *Canceled*;

sy_Case, *sy_Suppose*, *sy_Per*, *sy_Hereby*: *UnexpectedItem*;

othercases *PrivateItem*;

endcases; *Semicolon*;

end;

endcases;

end;

KillBlock; *AcceptEnd*(*DefPos*);

end;

1599.

⟨ Parse definitions (parser.pas) 1584 ⟩ +≡

procedure *Reservation*;

begin *gBlockPtr*↑.*CreateItem*(*itReservation*); *ReadWord*;

repeat *gItemPtr*↑.*StartReservationSegment*;

repeat *gItemPtr*↑.*ProcessReservedIdentifier*; *Accept*(*Identifier*, *paIdentExp11*);

until ¬*Occurs*(*sy_Comma*);

Accept(*sy_For*, *paForExp*); *gItemPtr*↑.*CreateExpression*(*exResType*); *TypeSubexpression*;

KillExpression; *gItemPtr*↑.*FinishReservationSegment*;

until ¬*Occurs*(*sy_Comma*);

gItemPtr↑.*FinishReservation*;

end;

1600.

⟨ Parse definitions (parser.pas) 1584 ⟩ +≡

procedure *Theorem*;

begin *gBlockPtr*↑.*CreateItem*(*itTheorem*); *ReadWord*; *ProcessLab*; *gItemPtr*↑.*StartTheoremBody*;

ProcessSentence; *gItemPtr*↑.*FinishTheoremBody*; *Justification*; *gItemPtr*↑.*FinishTheorem*;

end;

1601. \langle Parse definitions (**parser.pas**) 1584 $\rangle + \equiv$ **procedure** *Axiom*;**begin** *gBlockPtr*↑.*CreateItem(itAxiom)*; *ReadWord*; *ProcessLab*; *gItemPtr*↑.*StartTheoremBody*;
ProcessSentence; *gItemPtr*↑.*FinishTheoremBody*; *gItemPtr*↑.*FinishTheorem*;
end;

Section 24.8. SCHEME BLOCKS

1602.

```

⟨ Parse scheme block (parser.pas) 1602 ⟩ ≡
  { Main (with Schemes) }
procedure SchemeBlock;
  var SchemePos: Position;
  begin gBlockPtr↑.CreateItem(itSchemeBlock); gBlockPtr↑.CreateBlock(blPublicScheme); ReadWord;
  gBlockPtr↑.CreateItem(itSchemeHead); gItemPtr↑.ProcessSchemeName; SchemePos ← PrevPos;
  if CurWord.Kind = Identifier then ReadWord;
  Accept(sy_LeftCurlyBracket, paLeftCurledExp);
  repeat gItemPtr↑.StartSchemeSegment;
    repeat gItemPtr↑.ProcessSchemeVariable; Accept(Identifier, paIdentExp13);
    until ¬Occurs(sy_Comma);
    gItemPtr↑.StartSchemeQualification;
    case CurWord.Kind of
      sy_LeftSquareBracket: begin ReadWord; ReadTypeList; gItemPtr↑.FinishSchemeQualification;
        Accept(sy_RightSquareBracket, paRightSquareExp5);
      end;
      sy_LeftParanthesis: begin ReadWord; ReadTypeList; gItemPtr↑.FinishSchemeQualification;
        Accept(sy_RightParanthesis, paRightParenthExp9); Specification;
      end;
    othercases begin ErrImm(paWrongSchemeVarQual); gItemPtr↑.FinishSchemeQualification;
      Specification;
    end;
    endcases; gItemPtr↑.FinishSchemeSegment;
  until ¬Occurs(sy_Comma);
  Accept(sy_RightCurlyBracket, paRightCurledExp3); gItemPtr↑.FinishSchemeHeading;
  Accept(sy_Colon, paColonExp3); FormulaExpression; gItemPtr↑.FinishSchemeThesis;
  if CurWord.Kind = sy_Provided then
    repeat gItemPtr↑.StartSchemePremise; ReadWord; ProcessLab; ProcessSentence;
      gItemPtr↑.FinishSchemePremise;
    until CurWord.Kind ≠ sy_And;
  gItemPtr↑.FinishSchemeDeclaration;
  if CurWord.Kind = sy_Proof then
    begin KillItem; { only KillItem which is run outside of Semicolon procedure }
    if ¬ProofPragma then
      begin gBlockPtr↑.StartSchemeDemonstration; IgnoreProof;
        gBlockPtr↑.FinishSchemeDemonstration;
      end
    else begin StillCorrect ← true; Accept(sy_Proof, paProofExp);
      gBlockPtr↑.StartSchemeDemonstration; LinearReasoning;
      if CurWord.Kind = sy_Per then NonBlockReasoning;
      AcceptEnd(SchemePos); gBlockPtr↑.FinishSchemeDemonstration;
    end;
    end
  else begin Semicolon;
    if ¬ProofPragma then
      begin gBlockPtr↑.StartSchemeDemonstration; IgnoreProof;
        gBlockPtr↑.FinishSchemeDemonstration;
      end
    else begin StillCorrect ← true;
      if CurWord.Kind = sy_Proof then
        begin WrongWord(paProofExp); StillCorrect ← true; ReadWord;

```

```
    end;  
    gBlockPtr↑.StartSchemeDemonstration; LinearReasoning;  
    if CurWord.Kind = sy_Per then NonBlockReasoning;  
    AcceptEnd(SchemePos); gBlockPtr↑.FinishSchemeDemonstration;  
    end;  
end;  
KillBlock;  
end;
```

This code is used in section [1493](#).

Section 24.9. MAIN PARSE PROCEDURE

1603. The main *Parse* method essentially skips ahead to the first “begin”, then skips ahead to the first top-level block statement.

```

define skip_to_begin  $\equiv$  ReadTokenProc;
      while (CurWord.Kind  $\neq$  sy_Begin)  $\wedge$  (CurWord.Kind  $\neq$  EOT) do ReadTokenProc
 $\langle$  Main parse method (parser.pas) 1603  $\rangle \equiv$ 
procedure Parse;
  begin skip_to_begin; { Skips ahead until EOT or finds ‘begin’ }
  if CurWord.Kind = EOT then ErrImm(213)
  else  $\langle$  Parse proper text 1604  $\rangle$ ; { CurrWord.Kind = sy_Begin }
  KillBlock;
  end;

```

This code is used in section 1493.

1604. Parsing the “text proper” checks that we have encountered a “begin” keyword, then parses the block statements in the article’s contents.

Note that *ProcessBegin* (§1214) and *StartProperText* (§1216) are both implemented in the extended block class.

```

 $\langle$  Parse proper text 1604  $\rangle \equiv$ 
  begin gBlockPtr $\uparrow$ .StartProperText; gBlockPtr $\uparrow$ .ProcessBegin; Accept(sy_Begin, 213);
  while CurWord.Kind  $\neq$  EOT do  $\langle$  Parse next block 1605  $\rangle$ ;
  end

```

This code is used in section 1603.

1605. When parsing the next top-level block in a Mizar article, we tell Mizar’s parser we are not in “panic mode”. Then we test for unexpected “end” tokens. If we can recover a “begin” token, just start the loop over again.

If we encounter an “end of text” token, then we should terminate the loop.

Otherwise, we dispatch the parser’s control depending on the kind of token we encounter.

```

⟨ Parse next block 1605 ⟩ ≡
  begin ⟨ Parse pragmas and begins 1606 ⟩;
  StillCorrect ← true; { we are not in panic mode }
  if CurWord.Kind = sy_End then
    begin ⟨ Skip all end tokens, report errors 1607 ⟩;
    if CurWord.Kind = sy_Begin then continue;
    end;
  if CurWord.Kind = EOT then break;
  case CurWord.Kind of
    sy_Scheme: SchemeBlock;
    sy_Definition: DefinitionalBlock;
    sy_Notation: NotationBlock;
    sy_Registration: RegistrationBlock;
    sy_Reserve: Reservation;
    sy_Theorem: Theorem;
    sy_Axiom: Axiom;
    sy_Canceled: Canceled;
    sy_Case, sy_Suppose, sy_Per, sy_Hereby: UnexpectedItem;
  othercases PrivateItem;
  endcases;
  Semicolon; { block is expected to end in a semicolon }
end

```

This code is used in section 1604.

1606. The *ProcessPragmas* (§1570) consumes a token when the current token is a pragma. So we effectively have a loop where we consume all the pragmas and the “begin” keywords until we find something else.

```

⟨ Parse pragmas and begins 1606 ⟩ ≡
  while CurWord.Kind ∈ [sy_Begin, Pragma] do
    begin ProcessPragmas;
    if CurWord.Kind = sy_Begin then
      begin gBlockPtr↑.ProcessBegin; ReadTokenProc;
      end;
    end
  end

```

This code is used in section 1605.

1607. In the unfortunate event that the parser has stumbled across an “end” token, skip all the “end” and semicolon tokens and report errors.

```

⟨ Skip all end tokens, report errors 1607 ⟩ ≡
  repeat ErrImm(216); ReadTokenProc;
  if CurWord.Kind = sy_Semicolon then ReadTokenProc;
  until CurWord.Kind ≠ sy_End

```

This code is used in section 1605.

1608. Deferred.

This will not be analyzed until `first_identification.pas`

⟨ Class for Within expression 1608 ⟩ ≡

This code is used in section 737.

1609. ⟨ Within expression AST implementation 1609 ⟩ ≡

This code is used in section 736.

1610. Index. Underlined entries in an index item refers to which section defines the identifier. Primitive types (*char*, *Boolean*, *string*, etc.) are omitted from the index.

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