

1) 10 hus, 3 av dem har problem

$$f = 3$$

$$n = 10$$

$$\boxed{\frac{3}{10}}$$

relativ frekvens

$$p = .3$$

$$P[x_1 = s, \text{ och } x_2 = s]$$

2) $p = .5$ två söner födda ↓

Alla möjligheter $S = \{ ff, ss, fs, sf \}$

$$n(A) = 1$$

$$\frac{1}{4} = .25$$

klassiska

$$n(S) = 4$$

$$P[A_1 \cap A_2] = P[A_1]P[A_2]$$

om oberoende!

not: X = antalet barn m. hemofili

hur många på två försök

Binom ($n=2, p=.5$)

$$P[X=2] = f(2) = \binom{2}{2} 0.5^2 (0.5)^0 = 0.5^2 = 0.25$$

$$3) \quad 9! = 9 \cdot 8 \cdot 7 \cdot 6 \cdot 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1 = 362\,880$$

$$6! = 6 \cdot 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1 = 720$$

$$7P_3 = \frac{7!}{(7-3)!} = \frac{7!}{4!} = 7 \cdot 6 \cdot 5 = 210$$

$$6P_2 = \frac{6!}{6-2!} = 6 \cdot 5 = 30$$

$$5P_5 = \frac{5!}{(5-5)!} = \frac{5!}{0!} = 5! = 120$$

$$6P_6 = \frac{6!}{(6-6)!} = 6! = 720$$

$$9C_4 = \frac{9!}{4!(9-4)!} = \frac{9!}{4!5!} = \frac{9 \cdot 8 \cdot 7 \cdot 6}{4 \cdot 3 \cdot 2} = 9 \cdot 2 \cdot 7 = 126$$

$${}^8C_3 = \frac{8!}{3!(8-3)!} = \frac{8 \cdot 7 \cdot 6}{3 \cdot 2} = 56$$

$$\binom{8}{5} = {}^8C_5 = \frac{8!}{5!3!} = \frac{8 \cdot 7 \cdot 6}{3 \cdot 2} = 56$$

$$\binom{8}{5} = \binom{8}{3} = 56$$

$$\binom{8}{0} = 1, \quad \binom{8}{8} = 1$$

$$\binom{8}{7} = 8 = \binom{8}{1}$$

4, Programmers: $\begin{pmatrix} 10 \\ 3 \end{pmatrix}$

SAs: $\begin{pmatrix} 8 \\ 2 \end{pmatrix}$

ce $\begin{pmatrix} 4 \\ 2 \end{pmatrix}$

stat $\begin{pmatrix} 3 \\ 1 \end{pmatrix}$

$$a) \begin{pmatrix} 10 \\ 3 \end{pmatrix} \begin{pmatrix} 8 \\ 2 \end{pmatrix} \begin{pmatrix} 4 \\ 2 \end{pmatrix} \begin{pmatrix} 3 \\ 1 \end{pmatrix} = 60480$$

$$b) \begin{pmatrix} 10 \\ 3 \end{pmatrix} \begin{pmatrix} 8 \\ 2 \end{pmatrix} \begin{pmatrix} 3 \\ 1 \end{pmatrix} \begin{pmatrix} 3 \\ 1 \end{pmatrix} = 30240$$

5, Alphabet has 26 letters (for this example)
There are 10 digits.

$$a) 26^5 \cdot 10 = \underline{118\,813\,760}$$

$$b) \binom{5}{3} = \frac{5!}{3!2!} = \frac{5 \cdot 4}{2} = 10$$

$$5 \text{ even digits: } 10 \cdot 5 = \underline{50 \text{ passwords}}$$

$$c) \boxed{1/50}$$