

A Bayesian Growth Mixture Model to Examine Maternal Hypertension and Birth Outcomes

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Gestational Blood Pressure and Birth Outcomes

- Hypertension in pregnancy is associated with a number of adverse birth outcomes, including
 - Preterm birth (PTB)
 - Low birth weight (LBW)
 - Restricted fetal growth

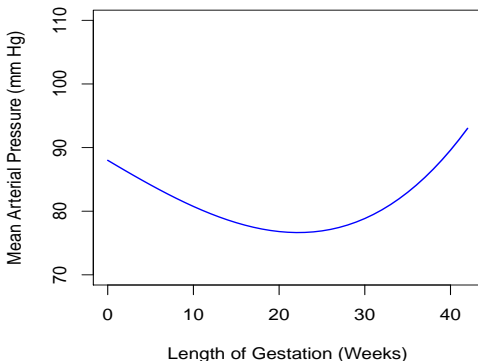
Gestational Blood Pressure

- In healthy pregnant women, blood pressure is U-shaped over the course of pregnancy
 - Declines until mid-gestation, then rises until delivery

Gestational Blood Pressure

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Fig. 1: Typical gestational blood pressure trajectory.



Gestational Blood Pressure and Birth Outcomes

- In contrast, in women who are at increased risk for adverse birth outcomes, blood pressure remains elevated throughout pregnancy
- Elevated blood pressure more likely in
 - Women over age 35
 - Non-Hispanic blacks
 - Primiparous women
- **Clinical relevance:** By monitoring blood pressure during pregnancy, obstetric providers can identify women at risk for adverse outcomes and intervene with appropriate treatments

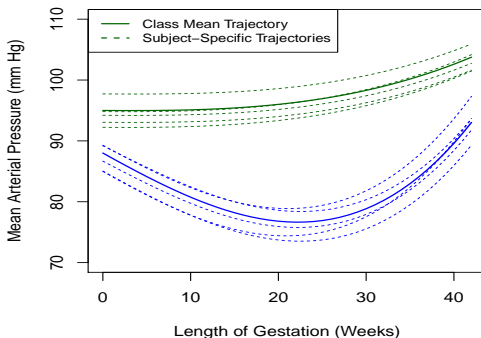
Research Questions

- **Research question 1:** Can we identify distinct patient subpopulations, each characterized by an average blood pressure trajectory over the course of pregnancy?
- **Research question 2:** Are these blood pressure trajectories associated with birth outcomes?

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Fig. 2: Two hypothetical patient subgroups.



Healthy Pregnancy, Healthy Baby (HPHB) Study

- Our analysis is based on data from the Healthy Pregnancy, Healthy Baby (HPHB) Study
 - Prospective cohort study examining how individual, social and environmental factors influence pregnancy outcomes
 - Part of the EPA-funded Southern Center for Environmentally Driven Disparities in Birth Outcomes
 - Enrolls pregnant women from Duke University Obstetrics Clinic and the Durham County Health Department Prenatal Clinic

HPHB Study

- Patient interviews and medical record reviews were used to obtain
 - Demographic information
 - Medical history
 - Blood pressure measurements from routine prenatal visits
- Maternal blood samples collected at 28 weeks to assess environmental exposures
- Birth outcomes recorded at delivery

HPHB Study

- Data analysis limited to:
 - Non-Hispanic white and non-Hispanic black mothers
 - Singleton gestation with delivery between 28–42 weeks
 - No history of chronic hypertension

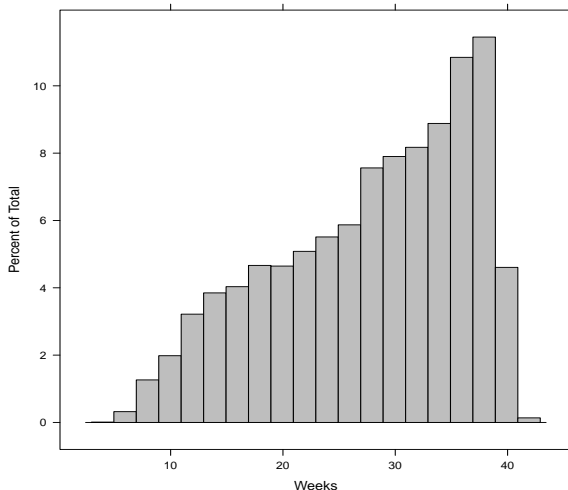
HPHB Patient Characteristics

Table 1: Characteristics of HPHB Study participants ($n = 1027$).

Variable	%
Preterm Birth	13
Low Birth Weight	12
Maternal Race	
Non-Hispanic white	22
Non-Hispanic black	78
Maternal Age	
18–20 years	25
21–34 years	64
≥ 35 years	11
Maternal Education	
> High school	47
\leq High school	53
Parity	
Primiparous	42
Multiparous	58
Insurance Status	
Private	23
Other	77
	Mean (SD)
Serum Cotinine (ng/mL)	19.44 (52.17)
Mean Arterial Pressure (mm Hg)	88.0 (9.13)

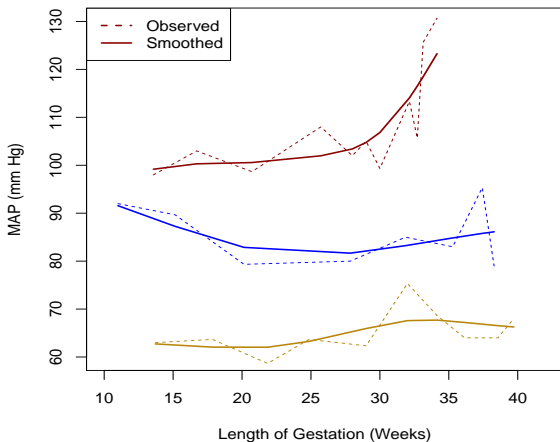
Histogram of Prenatal Visits

Fig. 3: Histogram of Prenatal Visits ($N = 10,290$).



MAP Curves for Three Study Participants

Fig. 4: Raw and smoothed MAP curves for 3 study participants.



Modeling Strategy: Bayesian Growth Mixture Model (GMM)

- **Growth Mixture Model** (Verbeke and Lesaffre, 1996; Muthén and Shedden, 1999)
 - Finite mixture of random effects models
 - Assumes that subjects first fall into one of a small number of latent classes
 - Each class defined by an average trajectory or “growth curve”
 - Around these class means, subjects have their own unique trajectories defined by a set of random effects
- **Resource:** Frühwirth-Schnatter, S. (2006). *Finite Mixture and Markov Switching Models*. Springer: New York.

Model Specification in 4 Steps

Step 1: Specify a growth mixture model for MAP

$$\begin{aligned}f(y_{ij}|\mathbf{b}_i) &= \sum_{k=1}^K \pi_{ik}(\mathbf{w}_i) \mathcal{N}(y_{ij}; \eta_{ijk}, \sigma_k^2) \\&= \sum_{k=1}^K \Pr(C_i = k; \mathbf{w}_i) \mathcal{N}(y_{ij}; \eta_{ijk}, \sigma_k^2); \\ \eta_{ijk} &= \mathbf{t}'_{ij} \boldsymbol{\beta}_k + \mathbf{v}'_{ij} \mathbf{b}_i\end{aligned}$$

where:

- y_{ij} = MAP measurement at the j -th visit for patient i
- $\pi_{ik}(\mathbf{w}_i) = \Pr(\text{patient } i \in \text{class } k)$
- C_i = unobserved class-indicator variable
- $\mathbf{b}_i | C_i = k \sim \mathcal{N}(\mathbf{0}, \boldsymbol{\Sigma}_k)$

Step 2: Link to Birth Outcomes

Step 2: Link MAP trajectories to PTB (z_1) and LBW (z_2)

$$f(y_{ij}, z_{1i}, z_{2i} | \mathbf{b}_i; \mathbf{w}_i, \mathbf{t}_{ij}, \mathbf{v}_{ij}) = \sum_{k=1}^K \pi_{ik}(\mathbf{w}_i) \mathcal{N}(y_{ij}; \eta_{ijk}, \sigma_k^2) \times p(z_{1i}, z_{2i}; \psi_k)$$

- Given $C_i = k$, PTB and LBW are *conditionally independent* of MAP
 - $(z_{1i}, z_{2i}) \perp\!\!\!\perp y_{ij} | C_i \quad \forall i, j$
- However, PTB and LBW are *conditionally correlated* given class membership
- So we allow a “residual” dependence b/w PTB and LBW

Step 3: Bivariate Probit Model for PTB and LBW

Step 3: Specify a bivariate probit model for $p(z_{1i}, z_{2i}; \psi_k)$

- Introduce underlying normal variables, z_{1i}^* and z_{2i}^*
- $z_{1i} = 1$ if $z_{1i}^* > 0$ and $z_{2i} = 1$ if $z_{2i}^* > 0$

$$\begin{pmatrix} z_{1i}^* \\ z_{2i}^* \end{pmatrix} \bigg| C_i = k \sim N_2(\boldsymbol{\mu}_k, \mathbf{R}_k) = N_2 \left[\begin{pmatrix} \mu_{1k} \\ \mu_{2k} \end{pmatrix}, \begin{pmatrix} 1 & \rho_k \\ \rho_k & 1 \end{pmatrix} \right]$$

- Allows us to compute joint probabilities of PTB and LBW for each class
- ρ_k is class-specific correlation between PTB and LBW
- An aside: Could allow $\boldsymbol{\mu}_k$ to be a function of covariates

Final Step: Multinomial Logit Model for Class-Membership Probabilities

Step 4: Link class-membership probabilities to patient covariates (age, race, serum cotinine, etc.) via multinomial logit model:

$$\Pr(C_i = k) = \pi_{ik}(\mathbf{w}_i) = \frac{e^{\mathbf{w}_i' \gamma_k}}{\sum_{h=1}^K e^{\mathbf{w}_i' \gamma_h}}, \text{ with } \gamma_1 = 0.$$

- \mathbf{w}_i = vector of patient-level predictors
- γ = vector of regression parameters
- K = number of blood pressure trajectory classes (≥ 2)

Parameter Estimation

- **Maximum Likelihood Estimation:** EM algorithm (Mplus, R Flexmix)
- **Bayesian Estimation:**
 - Place prior distributions on model parameters
 - Use Markov chain Monte Carlo (MCMC) to draw from joint posterior
- **Priors:**
 - Normal priors for β_k
 - Inverse-gamma/Inverse-Wishart priors for variances
 - Normal priors for μ_k
 - $U(-1,1)$ priors for ρ_k
 - $N(\mathbf{0}, (9/4)\mathbf{I})$ for class-membership parameters, γ_k (Garrett and Zeger, 2000)
 - Centers $\pi_{ik}(\mathbf{w}_i)$'s at $1/K$ and bounds them away from 0 and 1

Posterior Computation

- Data-augmentation approach
 - Draw class-membership parameters, γ_k ($k = 2, \dots, K$)
 - For each subject, compute posterior class-membership probabilities $\Pr(C_i = k | \mathbf{y}_i)$
 - Draw C_i from multinomial logit
 - Using data for subjects assigned to class k , update class- k parameters (β_k , μ_k , etc.)
- In our case, all full conditionals have closed forms **except**:
 - γ_k = Class-membership regression parameters
 - ρ_k = Bivariate probit correlation parameter
 - Used random-walk Metropolis-Hastings

Modeling Selection Strategy

- How many classes?
- Let number of classes K range from $1, 2, \dots, K_{\max}$
- Use **Deviance Information Criterion (DIC)** to choose the optimal model (Spiegelhalter et al., 2002)

$$\text{DIC} = \overline{D} + p_D$$

- Assessment of model fit + penalty for model complexity
 - Smaller values are better
- We use a modified DIC for finite mixture models (Celeux et al., 2006)

Model Selection Results

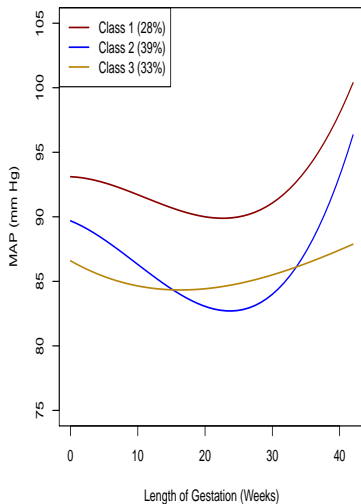
Table 2: Model comparison statistics for HPHB Study.

Number of Classes (K)	Model Description	DIC
1	Cubic Fixed Effects	75743
	Random Intercept	67296
	Random Intercept and Slope	66473
2	Cubic Fixed Effects	71268
	Random Intercept	66912
	Random Intercept and Slope	65942
3	Cubic Fixed Effects	69809
	Random Intercept	66393
	Random Intercept and Slope*	65811
4	Cubic Fixed Effects	69203
	Random Intercept	66715
	Random Intercept and Slope	66047

* **Bold indicates preferred model.**

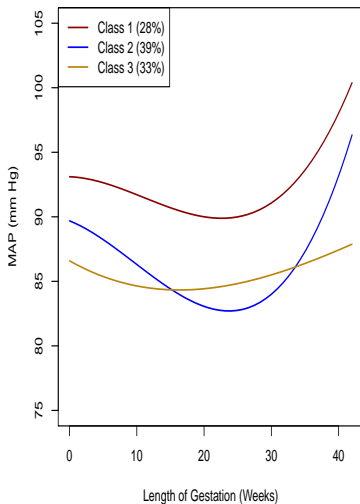
MAP Trajectories

Fig. 5: Posterior MAP trajectories.



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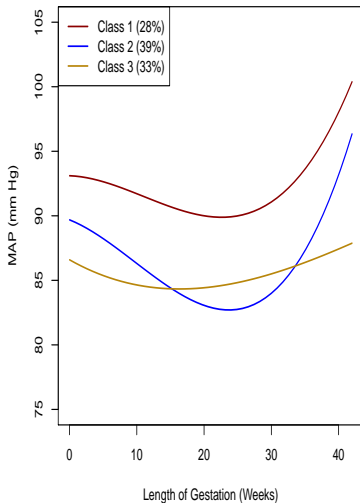


Class 1

LBW	PTB		
	Yes	No	
Yes	0.13	0.05	0.18
No	0.07	0.75	0.82
	0.20	0.80	

MAP Trajectories

Fig. 5: Posterior MAP trajectories.



Class 1

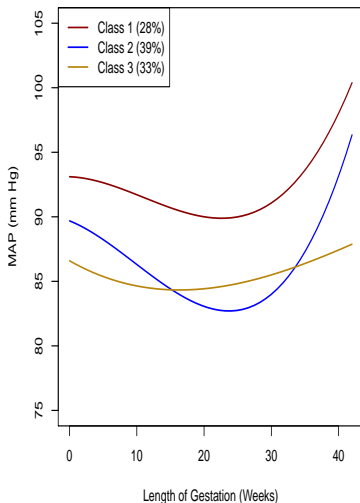
LBW	PTB		
	Yes	No	
Yes	0.13	0.05	0.18
No	0.07	0.75	0.82
	0.20	0.80	

Class 2

LBW	PTB		
	Yes	No	
Yes	0.01	0.08	0.09
No	0.04	0.87	0.91
	0.05	0.95	

MAP Trajectories

Fig. 5: Posterior MAP trajectories.



Class 1

LBW	PTB		
	Yes	No	
Yes	0.13	0.05	0.18
No	0.07	0.75	0.82
	0.20	0.80	

Class 2

LBW	PTB		
	Yes	No	
Yes	0.01	0.08	0.09
No	0.04	0.87	0.91
	0.05	0.95	

Class 3

LBW	PTB		
	Yes	No	
Yes	0.08	0.03	0.11
No	0.07	0.82	0.89
	0.15	0.85	

Class-Membership Probabilities

- Can obtain class-membership probabilities as a function of covariates
- For example:
 - **Reference Group**: Non-Hispanic white, age 21–34 years, multiparous
 - **“High-risk” Group**: Non-Hispanic black, age > 34 , first child

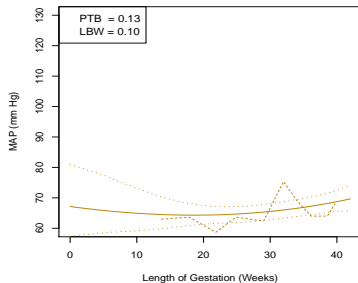
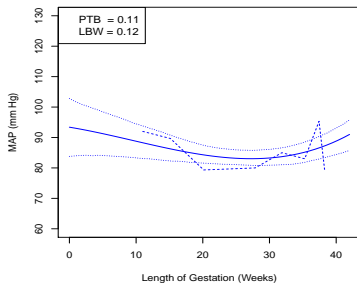
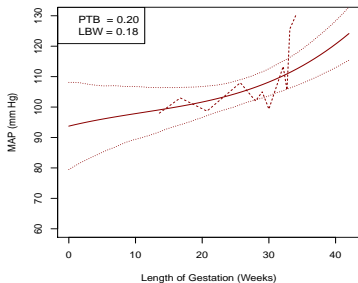
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Table 3: Predicted class-membership probabilities by covariate profile.

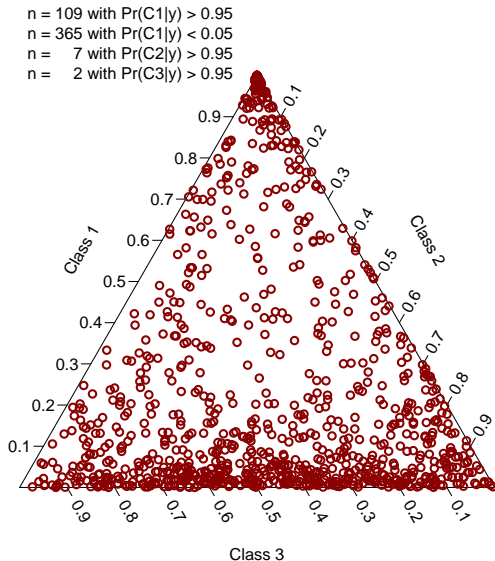
Covariate Profile	Class-Membership Probabilities		
	Class 1	Class 2	Class 3
Reference Group	0.13	0.48	0.39
High-Risk Group	0.39	0.34	0.27

Predicted MAP Curves



Posterior Probability Plot

Triangle Plot of Posterior Class-Membership Probabilities



Recap

- Proposed a growth mixture model to jointly model three outcomes: MAP, PTB and LBW
- The model partitions women into distinct classes characterized by a mean MAP curve and joint probabilities of PTB and LBW
- Bivariate probit used to model PTB and LBW
- Patient covariates influence class-membership probabilities
- Our analysis identified three distinct MAP classes with unique risks of PTB and LBW

Future Directions

- Model could be applied to other settings with a longitudinal biomarker and correlated binary outcomes (e.g., two related diseases)
- More flexible modeling of MAP curves (e.g., via splines)
- Allow probabilities of PTB and LBW to vary by subject, not just class
 - Introduce covariates and random effects into biprobit model for PTB, LBW
- Discrete survival model for gestational length

Thanks

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